

Electroweak Phase Transition at CEPC: A cosmologist's perspective



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WORKSHOP ON CEPC PHYSICS
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Based on

- ... 1608.06619 (PRD) with Peisi Huang & Lian-Tao Wang.
- ... 1708.03061 with Xucheng Gan & Lian-Tao Wang.

- ... see also Barger, Chung, AL, Wang [1112.5460]
 and Chung, AL, Wang [1209.1819].

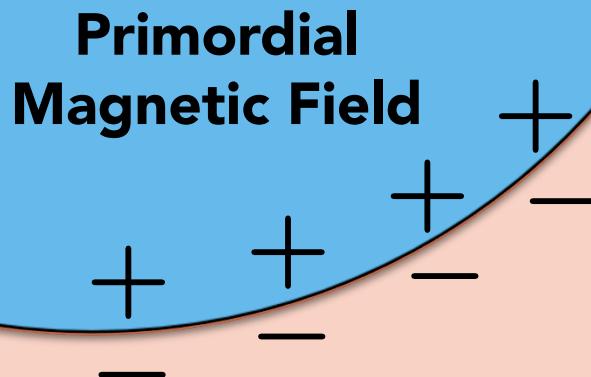
Thought experiment: heating a box of photons



**Does the Higgs (condensate)
melt? Or does it boil?**

(Possible) Cosmological Relics of the EW Epoch

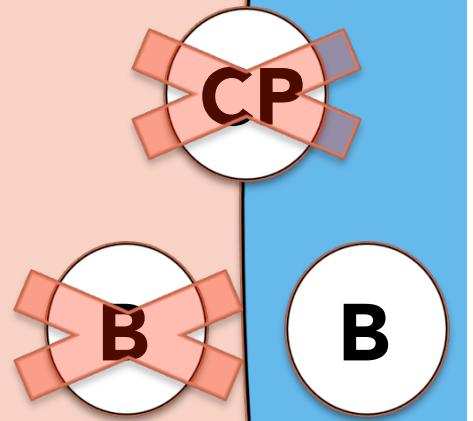
$$\langle \Phi \rangle = v(T) \quad \langle \Phi \rangle = 0$$



Primordial
Gravitational
Waves

Primordial
Black Holes

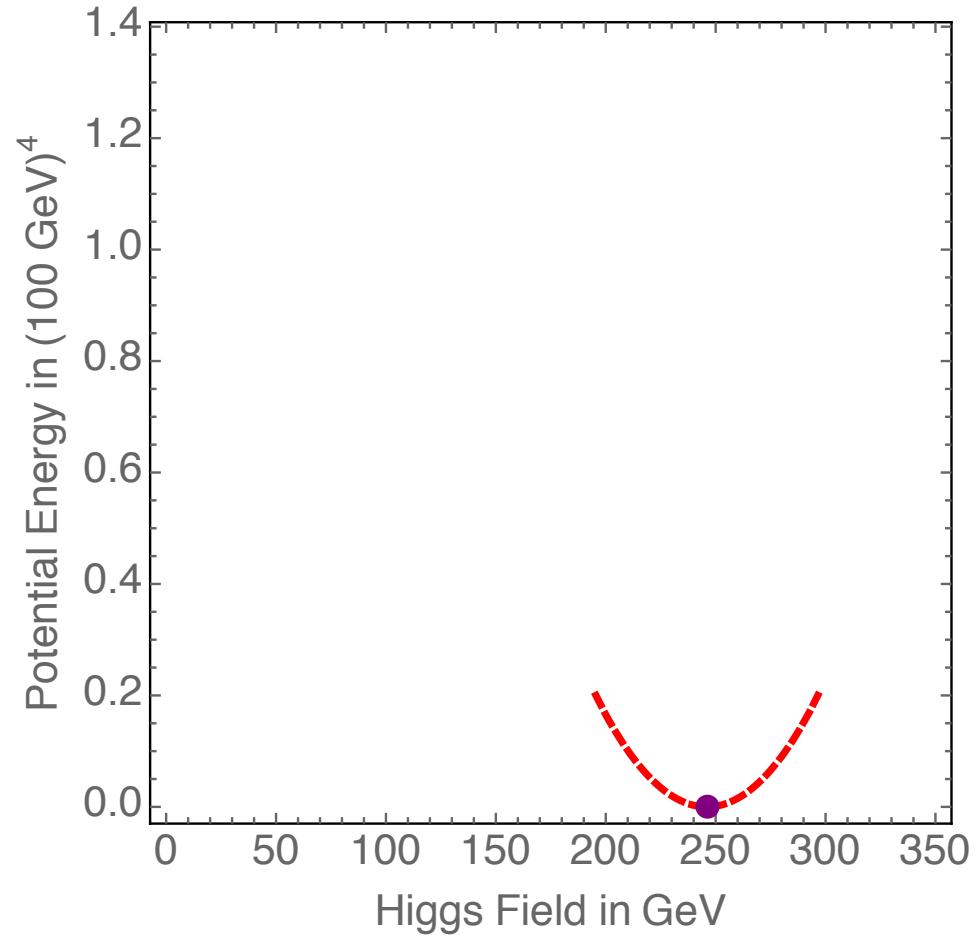
Matter /
Anti-Matter
Asymmetry



We discovered the Higgs!

We know that it's responsible
for EW symmetry breaking!

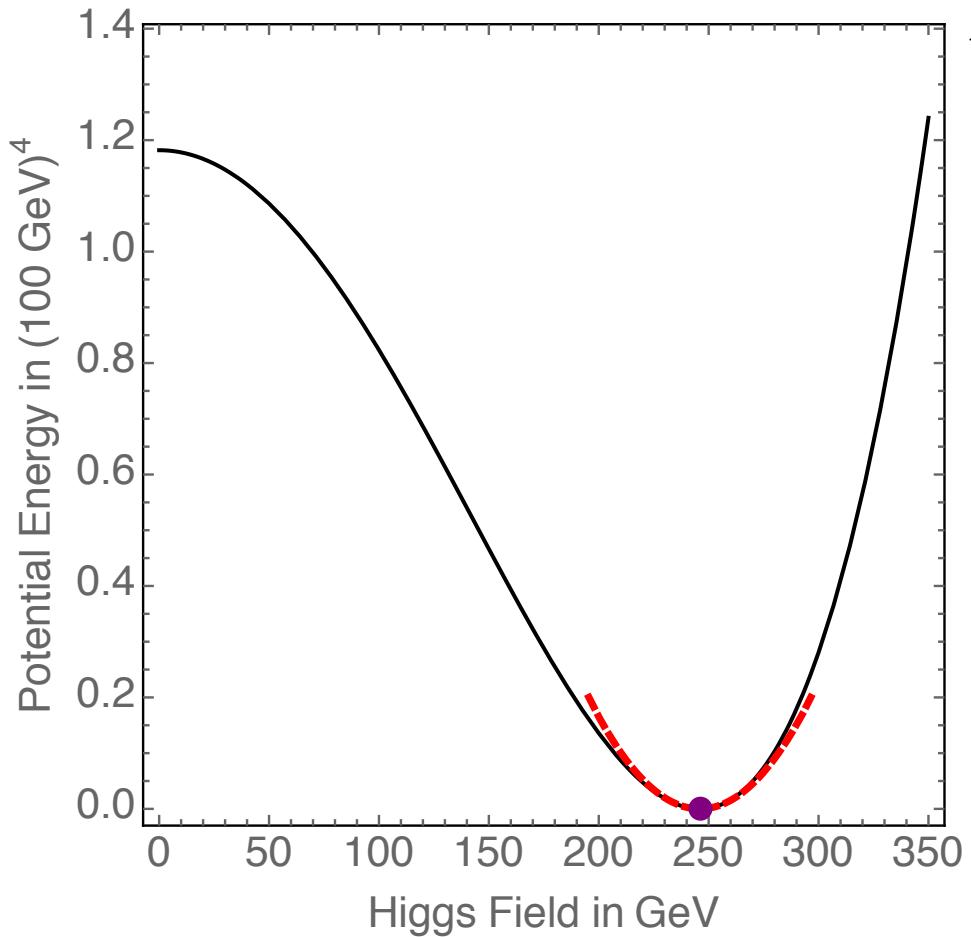
Isn't that enough information
to let us study the EW phase
transition?



Measured Directly:

$$v \simeq 246 \text{ GeV}$$
$$M_h \simeq 125 \text{ GeV}$$

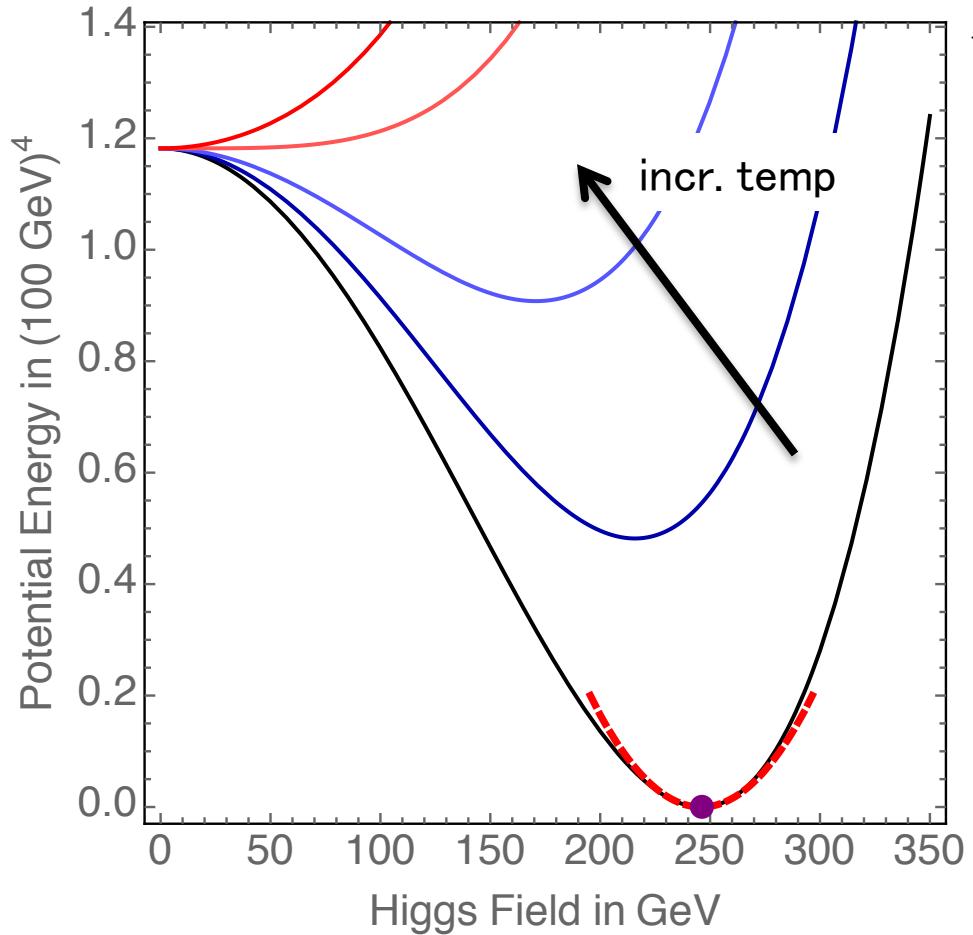
Assuming SM particle content & interactions



$$V = -\mu^2 H^\dagger H + \lambda_h (H^\dagger H)^2$$
$$\begin{cases} \mu^2 = M_h^2/2 \simeq (88 \text{ GeV})^2 \\ \lambda_h = M_h^2/(2v^2) \simeq 0.13 \end{cases}$$

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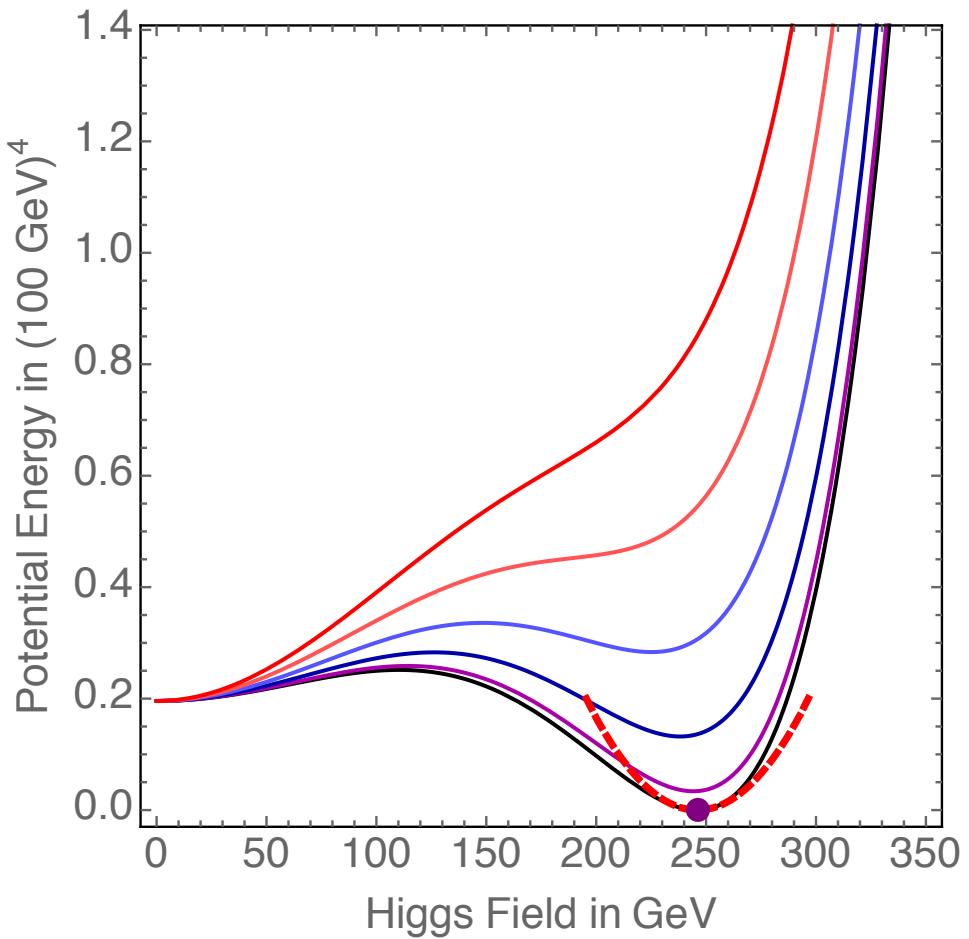
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Thermal support from Higgs interactions with W, Z, t, ...

- EWPT is continuous crossover
- $v(T)$ changes smoothly
- No energy barrier; no bubbles; no cosmological relics

Variant –SM with low cutoff



$$v \simeq 246 \text{ GeV}$$

Measured Directly: $M_h \simeq 125 \text{ GeV}$

Recently studied by

P. Huang, Jokelar, Li, Wagner (2015)

F.P. Huang, Gu, Yin, Yu, Zhang (2015)

F.P. Huang, Wan, Wang, Cai, Zhang (2016)

Cao, F.P. Huang, Xie, & Zhang (2017)

$$\begin{aligned} V = & \mu^2 H^\dagger H - \lambda_h (H^\dagger H)^2 \\ & + \Lambda^{-2} (H^\dagger H)^3 \\ & \left\{ \begin{array}{l} \mu^2 \simeq (44 \text{ GeV})^2 \\ \lambda_h \simeq 0.19 \\ \Lambda \simeq 530 \text{ GeV} \end{array} \right. \end{aligned}$$

Energy barrier may be present already at T=0.

- EWPT is first order
- Possibly interesting cosmological relics!

A short aside on dim-6 ops & EWBG washout

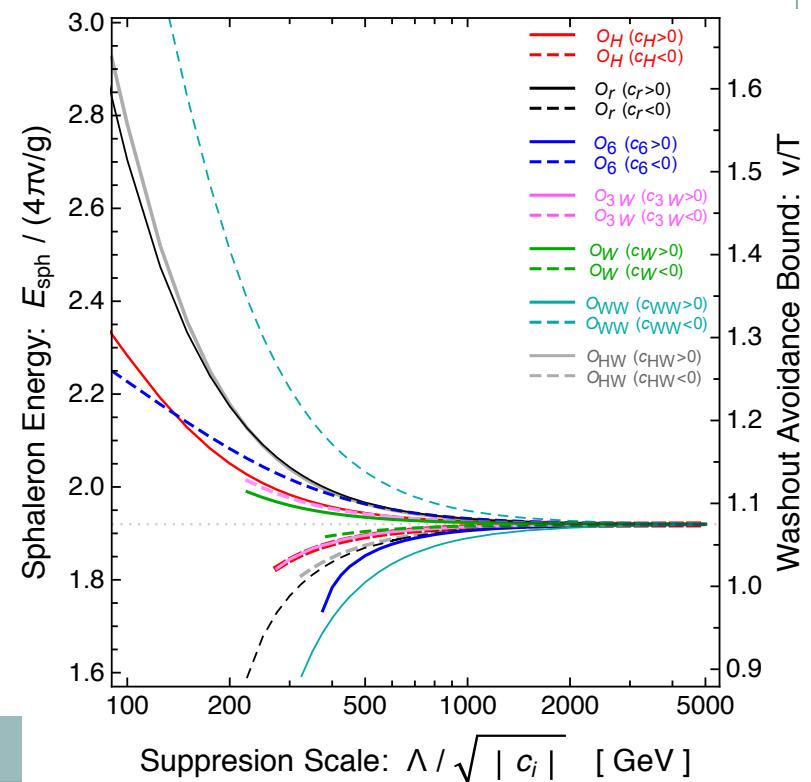
Successful EW baryogenesis requires the sphaleron to be out of equilibrium inside of Higgs-phase bubbles. This implies

$$\frac{v(T)}{T} \gtrsim 1.07$$

The “1” is weakly model-dependent.

In the Higgs-EFT framework, we calculate the new washout criterion for 7 different dimension-6 operators:

Gan, AL, Wang (1708.03061)
see also: Spannowsky & Tamarit (2016)



What can future colliders teach us about the electroweak phase transition?

In models with a first order EW phase transition, there must be new physics coupled to the Higgs.

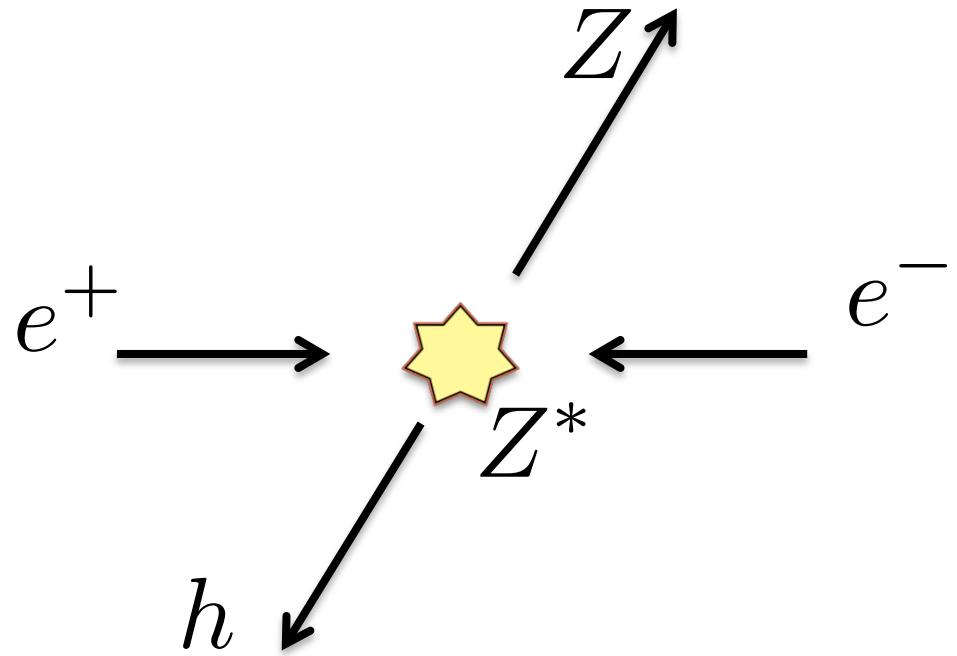
It is reasonable to expect that this NP may also induce deviations in the Higgs couplings with other SM fields.

Precision Measurements w/ Higgs Factories

Lepton colliders provide “clean” environment for studying Higgs physics.

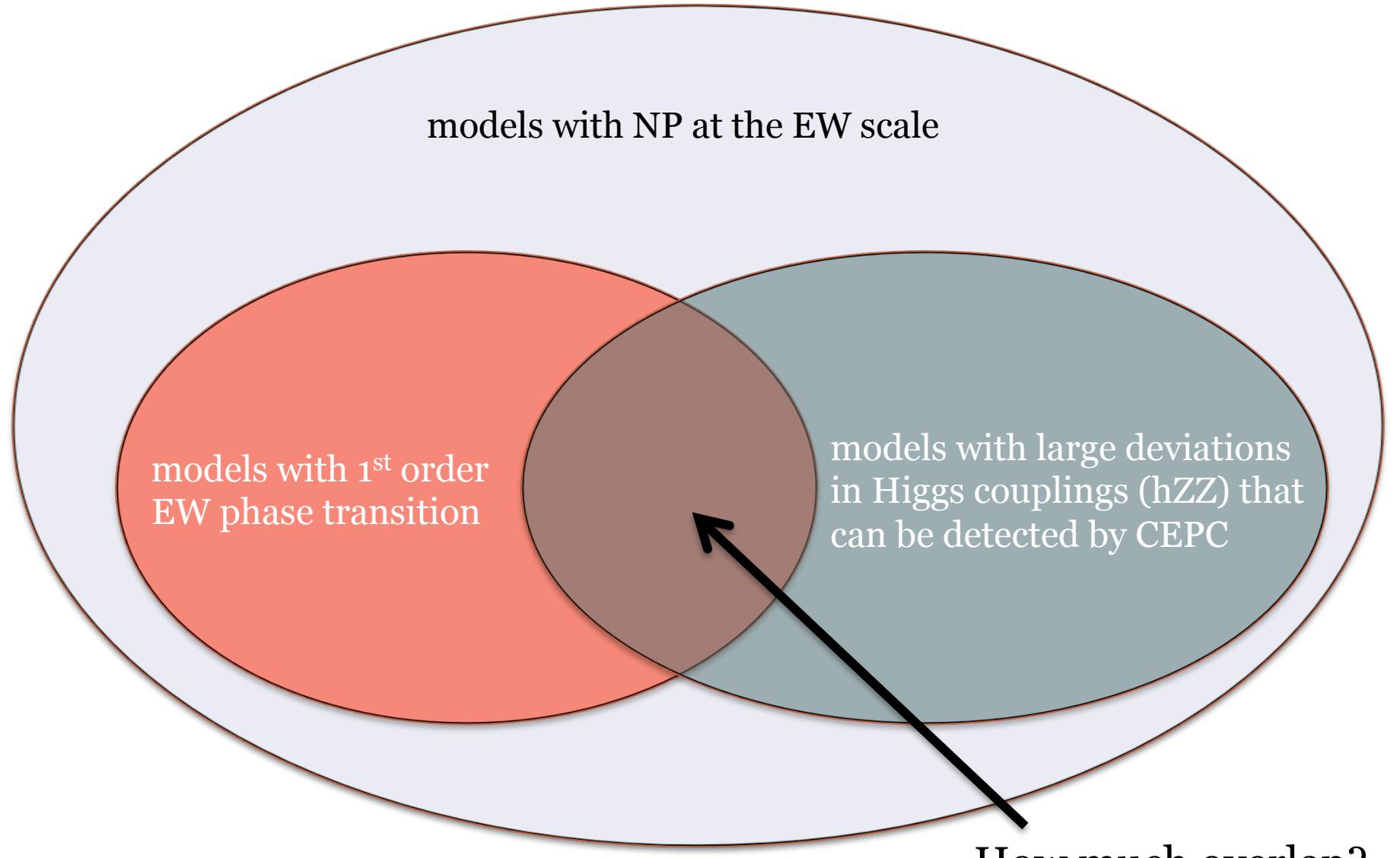
At $E \sim 250$ GeV, the production of Higgs + Z-boson is optimized.

Expect to achieve precision Higgs-Z-Z measurements at the sub-percent level!



Projected Sensitivities to various Higgs couplings at different future colliders:

	current	HL-LHC	CEPC-250	ILC-500	FCC-ee	FCC-hh
hZZ	27%	7%	0.25%	0.25%	0.15%	-
$\Gamma(h \rightarrow \gamma\gamma)$	20%	8%	4%	-	1.5%	-
hhh	N/A	-	-	27%	-	10%



What Kinds of Models?

Model	References
SM + Scalar Singlet	Espinosa & Quiros, 1993; Benson, 1993; Choi & Volkas, 1993; McDonald, 1994; Vergara, 1996; Branco, Delepine, Emmanuel-Costa, & Gonzalez, 1998; Ham, Jeong, & Oh, 2004; Ahriche, 2007; Espinosa & Quiros, 2007; Profumo, Ramsey-Musolf, & Shaughnessy, 2007; Noble & Perelstein, 2007; Espinosa, Konstandin, No, & Quiros, 2008; Ashoorioon & Konstandin, 2009; Das, Fox, Kumar, & Weiner, 2009; Espinosa, Konstandin, & Riva, 2011; Chung & AL, 2011; Wainwright, Profumo, & Ramsey-Musolf, 2012; Barger, Chung, AL, & Wang, 2012; Huang, Shu, Zhang, 2012; Katz & Perelstein, 2014; Jiang, Bian, Huang, Shu, 2015; Huang & Li 2015; Cline, Kainulainen, Tucker-Smith, 2017; Kurup & Perelstein, 2017; Chen, Kozaczuk, & Lewis, 2017
SM + Scalar Doublet	Davies, Froggatt, Jenkins, & Moorhouse, 1994; Huber, 2006; Fromme, Huber, & Seniuch, 2006; Cline, Kainulainen, & Trott, 2011; Kozhushko & Skalozub, 2011;
SM + Scalar Triplet	Patel, Ramsey-Musolf, 2012; Patel, Ramsey-Musolf, Wise, 2013; Huang, Gu, Yin, Yu, Zhang 2016
SM + Chiral Fermions	Carena, Megevand, Quiros, Wagner, 2005
MSSM	Carena, Quiros, & Wagner, 1996; Delepine, Gerard, Gonzales Felipe, & Weyers, 1996; Cline & Kainulainen, 1996; Laine & Rummukainen, 1998; Cohen, Morrissey, & Pierce,; Carena, Nardini, Quiros, & Wagner, 2012;
NMSSM / nMSSM / $\mu\nu$ SSM	Pietroni, 1993; Davies, Froggatt, & Moorhouse, 1995; Huber & Schmidt, 2001; Ham, Oh, Kim, Yoo, & Son, 2004; Menon, Morrissey, & Wagner, 2004; Funakubo, Tao, & Toyoda, 2005; Huber, Kontandin, Prokopec, & Schmidt, 2006; Chung, AL, 2010, Huang, Kang, Shu, Wu, Yang, 2014; Bian, Guo, Shu (2017)
EFT-like Approach (H^6 operator)	Grojean, Servant, Wells, 2005; Huang, Gu, Yin, Yu, Zhang 2015; Huang, Joglekar, Li, Wagner, 2015; Huang, Wan, Wang, Cai, Zhang 2016; Huang, Gu, Yin, Yu, Zhang 2016; Cao, F.P. Huang, Xie, Zhang (2017)

Can we systematize the calculation?



Chung, AL, Wang [1209.1819].

(similar concerns raised in:

Damgaard, Haarr, O'Connell, Tranberg 2015)

There is **no systematic formalism** for studying BSM models that give rise to a first order electroweak phase transition *and* associated collider phenomenology.

Can we use *effective field theory*?

- Not if there are EW-scale particles present in the plasma.
- Not if the particles get their mass from the Higgs (light in symmetric phase).

Can we use *phase transition model classes*? Chung, AL, Wang (2012)

- This framework organizes the PT-side of the calculation, but it is ignorant of the particle physics (phenomenology). E.g., from the PT perspective

$$\text{SM} + 1 \text{ colored scalar} = \text{SM} + 3 \text{ singlet scalars with } \text{SO}(3)$$

Models with very different collider phenomenology can have similar phase transition dynamics.

Models are typically studied on a case-by-case basis.

A Survey of Simplified Models



Model #1 – SM + chiral fermions (like MSSM gauginos)

Model #2 – SM + scalar doublet (like MSSM stops)

Model #3 – SM + real scalar singlet (like NMSSM singlet)

In the simplified / minimal models, the new degrees of freedom are responsible for *both* the 1PT and hZZ

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SM + Scalar Doublet (“stops”)



In the MSSM, the stops play a critical role in making the EWPT first order. Here we considered a simplified version of the SUSY stop sector.

$$\tilde{Q} \sim (\mathbf{1}, \mathbf{2}, 1/3) \times 3 \text{ flavor}$$

$$\tilde{U} \sim (\mathbf{1}, \mathbf{1}, 4/3) \times 3 \text{ flavor}$$

The full Lagrangian is

$$\begin{aligned} \mathcal{L} = & \mathcal{L}_{\text{SM}} + (D_\mu \tilde{Q})^\dagger (D^\mu \tilde{Q}) + (D_\mu \tilde{U})^* (D^\mu \tilde{U}) - [a_{hQU} \tilde{Q} \cdot H \tilde{U}^* + \text{h.c.}] \\ & - m_Q^2 \tilde{Q}^\dagger \tilde{Q} - m_U^2 \tilde{U}^* \tilde{U} - \lambda_Q (\tilde{Q}^\dagger \tilde{Q})^2 - \lambda_U (\tilde{U}^* \tilde{U})^2 \\ & - \lambda_{QU} (\tilde{Q}^\dagger \tilde{Q}) (\tilde{U}^* \tilde{U}) - \lambda_{hU} (H^\dagger H) (\tilde{U}^* \tilde{U}) \\ & - \lambda_{hQ} (H^\dagger H) (\tilde{Q}^\dagger \tilde{Q}) - \lambda'_{hQ} (\tilde{Q} \cdot H)^* (\tilde{Q} \cdot H) - \lambda''_{hQ} (\tilde{Q}^\dagger H)^* (\tilde{Q}^\dagger H) \end{aligned}$$

four model parameters

and for simplicity we focus on

$$\langle \tilde{Q} \rangle = (0, 0) \quad \text{and} \quad \langle \tilde{U} \rangle = 0$$

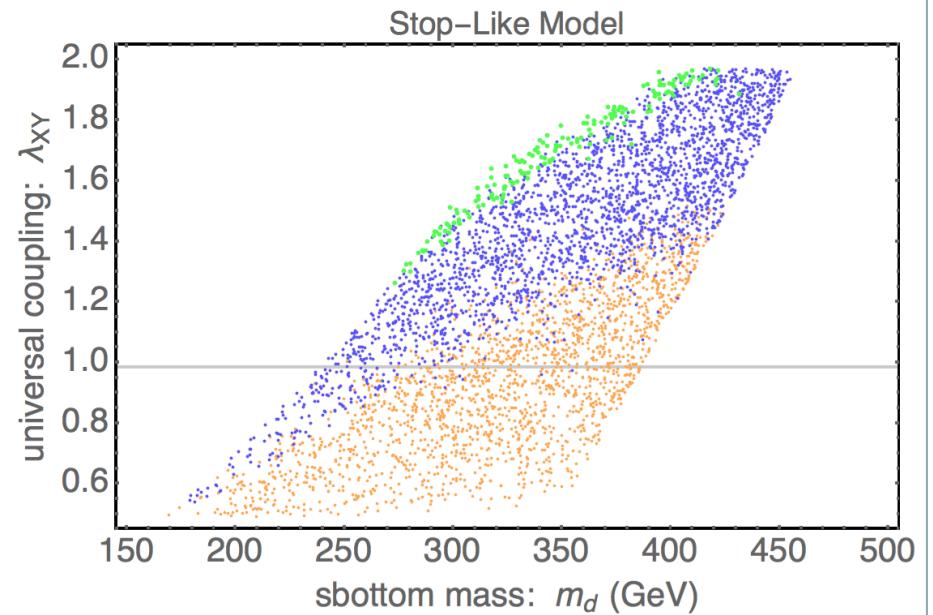
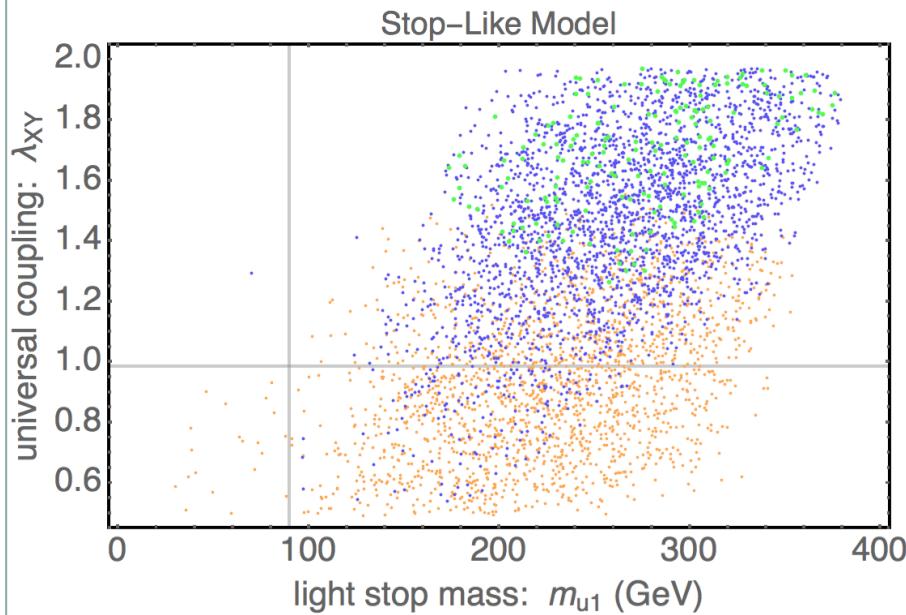
$$\lambda_Q = \lambda_U = \lambda_{QU} = \lambda_{hU} = \lambda_{hQ} = \lambda'_{hQ} = \lambda''_{hQ} \equiv \lambda$$

Spectrum

$$M_{\tilde{t}}^2 = \begin{pmatrix} m_Q^2 + \frac{1}{2}(\lambda_{hQ} + \lambda'_{hQ})v^2 & \frac{a_{hQU}v}{\sqrt{2}} \\ \frac{a_{hQU}v}{\sqrt{2}} & m_U^2 + \frac{1}{2}\lambda_{hU}v^2 \end{pmatrix} \quad \text{2 "stops"}$$

$$\tan 2\theta = \frac{\sqrt{2}a_{hQU}v}{m_Q^2 - m_U^2 + \frac{1}{2}(\lambda_{hQ} + \lambda'_{hQ} - \lambda_{hU})v^2} \quad \text{(mixing)}$$

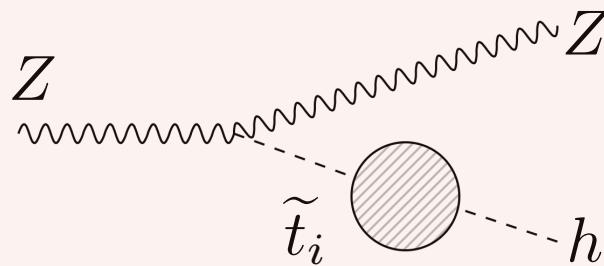
$$M_{\tilde{b}}^2 = m_Q^2 + \frac{1}{2}(\lambda_{hQ} + \lambda''_{hQ})v^2 \quad \text{1 "sbottom"}$$



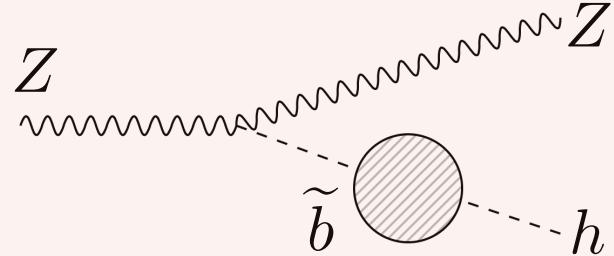
Effective hZZ coupling

(adapted from: Fan, Reece, Wang, 2014)

$$\delta Z_h = -n_f \sum_{i,j=1}^2 \frac{|g_{h\tilde{t}_i\tilde{t}_j}|^2}{32\pi^2} I_B(M_h^2; M_{\tilde{t}_i}^2, M_{\tilde{t}_j}^2)$$



$$- n_f \frac{|g_{h\tilde{b}\tilde{b}}|^2}{32\pi^2} I_B(M_h^2; M_{\tilde{b}}^2, M_{\tilde{b}}^2)$$



+vertex correction (suppressed by g/λ)

$$g_{h\tilde{t}_1\tilde{t}_1} = -\cos^2 \theta (\lambda_{hQ} + \lambda'_{hQ}) v - \sin^2 \theta \lambda_{hU} v + \frac{a_{hQU} \sin 2\theta}{\sqrt{2}}$$

$$g_{h\tilde{t}_2\tilde{t}_2} = -\sin^2 \theta (\lambda_{hQ} + \lambda'_{hQ}) v - \cos^2 \theta \lambda_{hU} v - \frac{a_{hQU} \sin 2\theta}{\sqrt{2}}$$

$$g_{h\tilde{t}_1\tilde{t}_2} = -\frac{\sin 2\theta}{2} (\lambda_{hQ} + \lambda'_{hQ}) v + \frac{\sin 2\theta}{2} \lambda_{hU} v - \frac{a_{hQU} \cos 2\theta}{\sqrt{2}}$$

$$g_{h\tilde{b}\tilde{b}} = -(\lambda_{hQ} + \lambda''_{hQ}) v$$

Higgs di-photon decay width (adapted from: Djouadi, Driesen, Hollik, Illana, 2005)

$$\Gamma_{h \rightarrow \gamma\gamma} = \frac{1}{64\pi} \frac{\alpha^2 M_h^3}{16\pi^2} \left| \bar{A}_W + \bar{A}_t + \bar{A}_{\tilde{t}} + \bar{A}_{\tilde{b}} \right|^2$$

$$\bar{A}_W = \frac{g_{hWW}}{M_W^2} F_1(M_h^2/4M_W^2)$$

$$\bar{A}_t = 2N_c Q_t^2 \frac{g_{htt}}{M_t} F_{1/2}(M_h^2/4M_t^2)$$

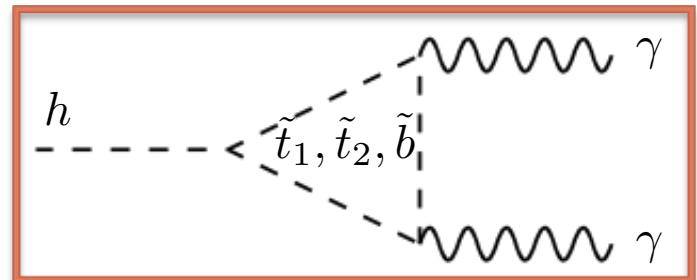
$$\bar{A}_{\tilde{t}} = \sum_{i=1}^2 N_c Q_t^2 \frac{g_{h\tilde{t}_i\tilde{t}_i}}{M_{\tilde{t}_i}^2} F_0(M_h^2/4M_{\tilde{t}_i}^2)$$

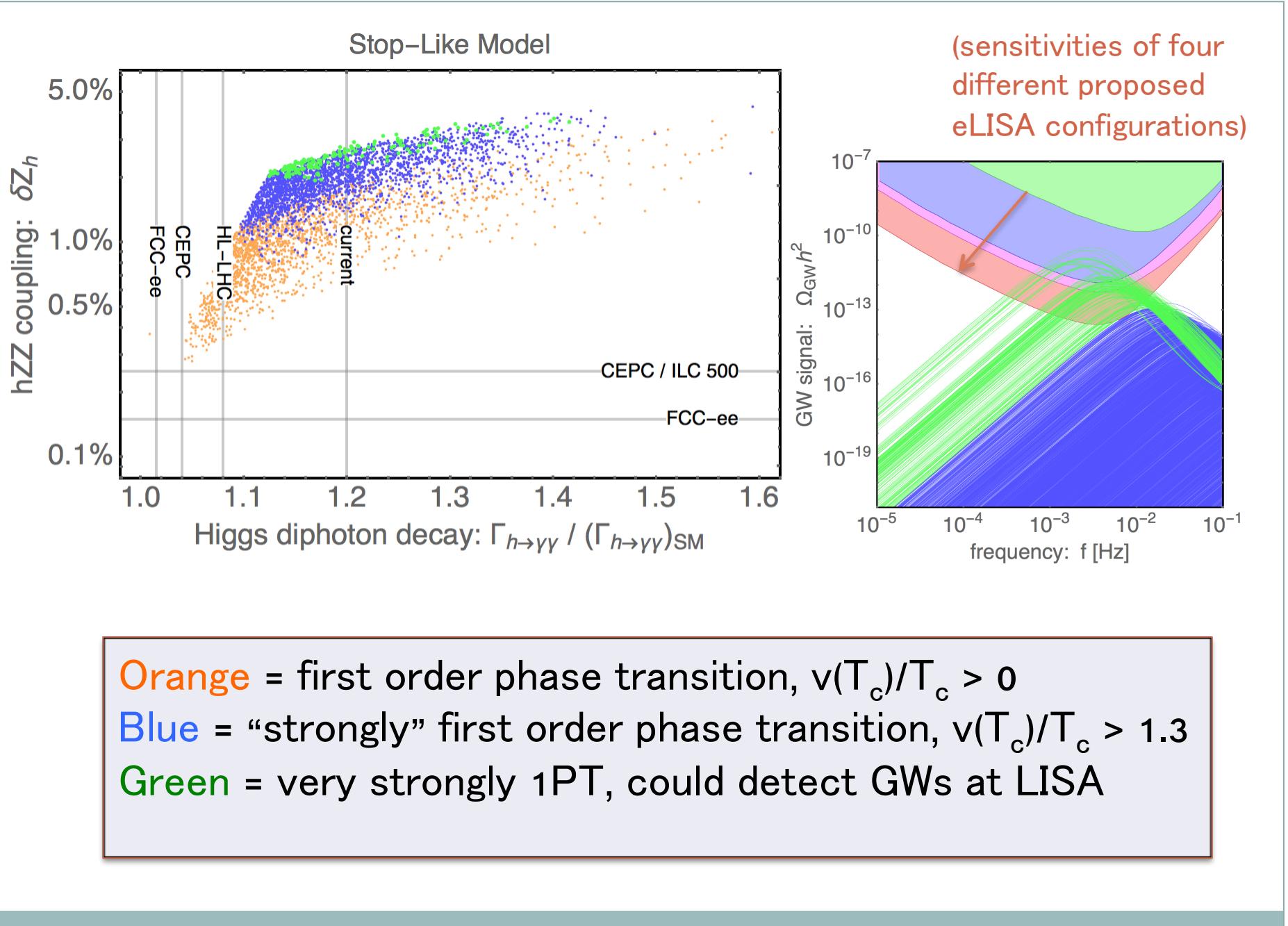
$$\bar{A}_{\tilde{b}} = N_c Q_b^2 \frac{g_{h\tilde{b}\tilde{b}}}{M_{\tilde{b}}^2} F_0(M_h^2/4M_{\tilde{b}}^2)$$

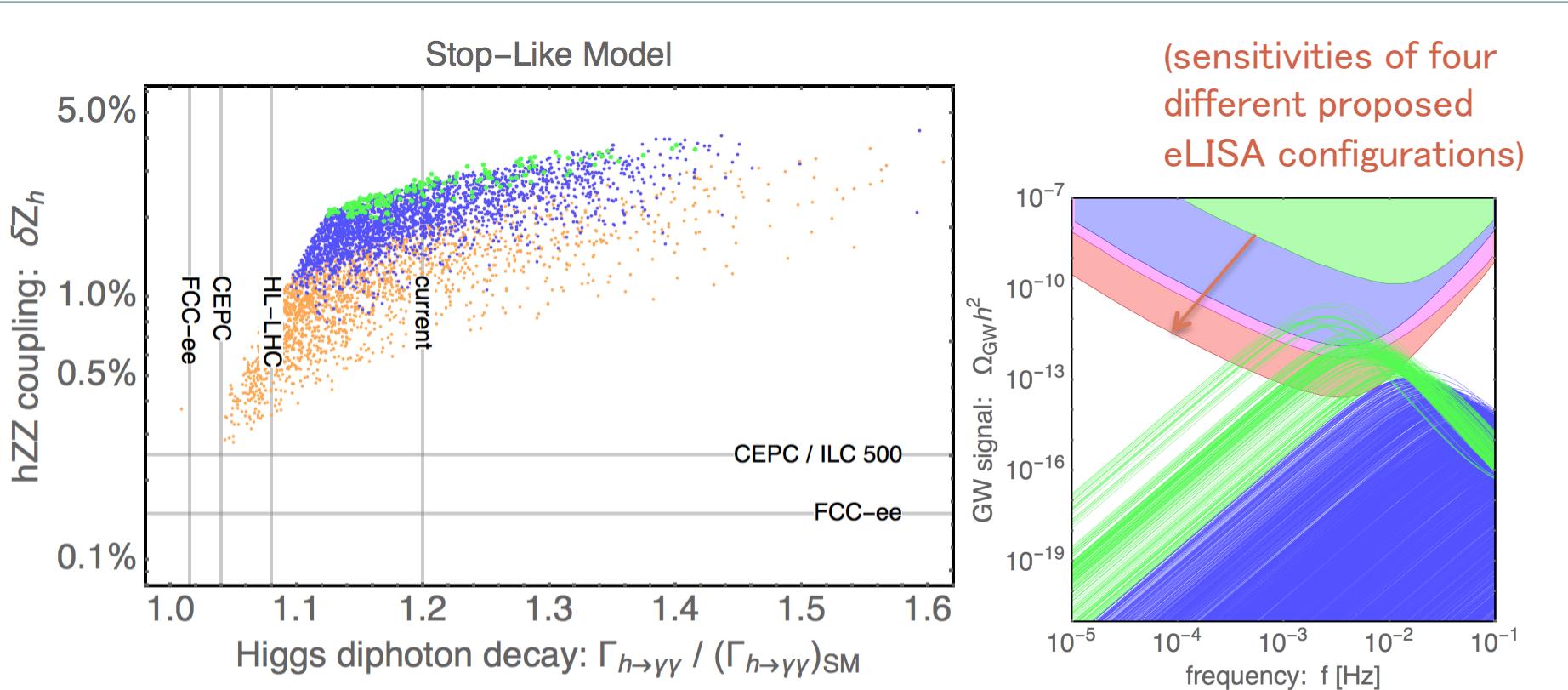
$$F_1(\tau) = \frac{2\tau^2 + 3\tau + 3(2\tau - 1) \arcsin(\tau^{1/2})^2}{\tau^2}$$

$$F_{1/2}(\tau) = -2 \frac{\tau + (\tau - 1) \arcsin(\tau^{1/2})^2}{\tau^2}$$

$$F_0(\tau) = \frac{\tau - \arcsin(\tau^{1/2})^2}{\tau^2}$$







Models with a first order electroweak phase transition (orange, blue, or green) have large **deviation in hZZ** that can be probed by CEPC.

These models also have large enhancement to **Higgs diphoton decay** rate (b/c of charged particles) that can be probed by HL-LHC & CEPC.

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Model #3 – SM + real scalar singlet (like NMSSM singlet)

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SM + Real Scalar Singlet

Consider

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{2} (\partial \phi_s)^2 - \frac{m_s^2}{2} \phi_s^2 - \frac{a_s}{3} \phi_s^3 - \frac{\lambda_s}{4} \phi_s^4 - \underbrace{\lambda_{hs} H^\dagger H \phi_s^2 - 2a_{hs} H^\dagger H \phi_s}_\text{Higgs portal}$$

real scalar singlet Higgs portal

In the vacuum

$$\langle H \rangle = (0, v/\sqrt{2}) \quad \text{and} \quad \langle \phi_s \rangle = v_s$$

$$\sin 2\theta = \frac{4v(a_{hs} + \lambda_{hs}v_s)}{M_h^2 - M_s^2} \quad (\text{mixing})$$

Effective hhh coupling

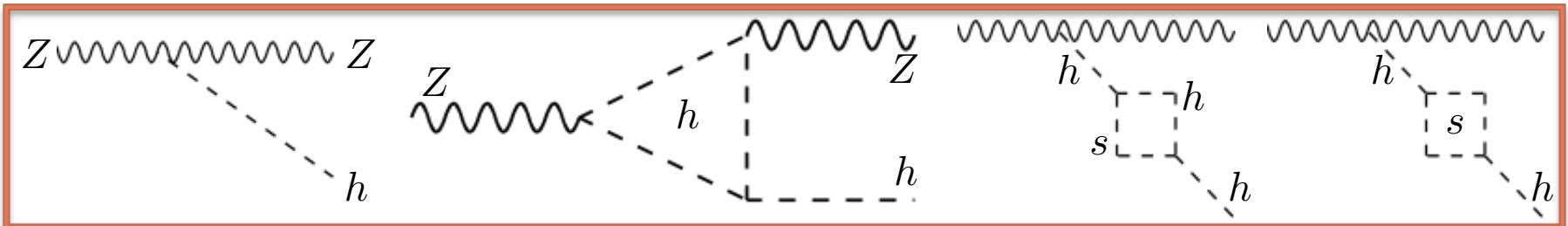
(adapted from: McCullough, 2014; Curtin, Meade, Yu, 2014)

$$\begin{aligned}\lambda_3 = & (6\lambda_h v) \cos^3 \theta + (6a_{hs} + 6\lambda_{hs} v_s) \sin \theta \cos^2 \theta + (6\lambda_{hs} v) \sin^2 \theta \cos \theta \\ & + (2a_s + 6\lambda_s v_s) \sin^3 \theta + 4 \frac{|\lambda_{hs}|^3 v^3}{16\pi^2 M_s^2}\end{aligned}$$

Effective hZZ coupling

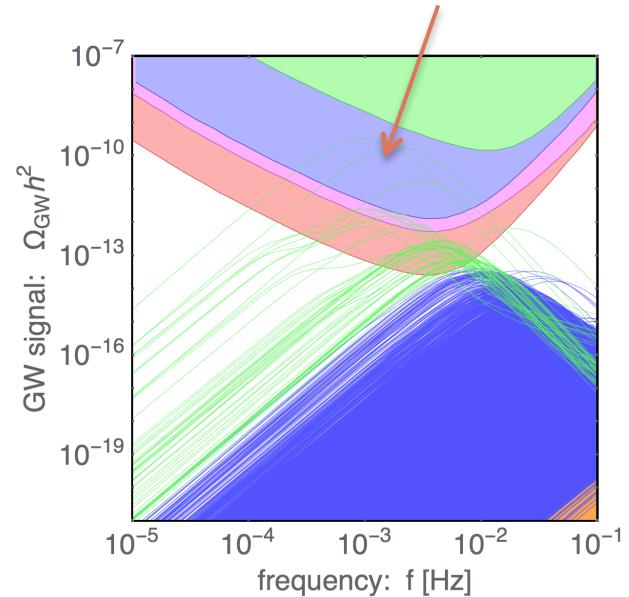
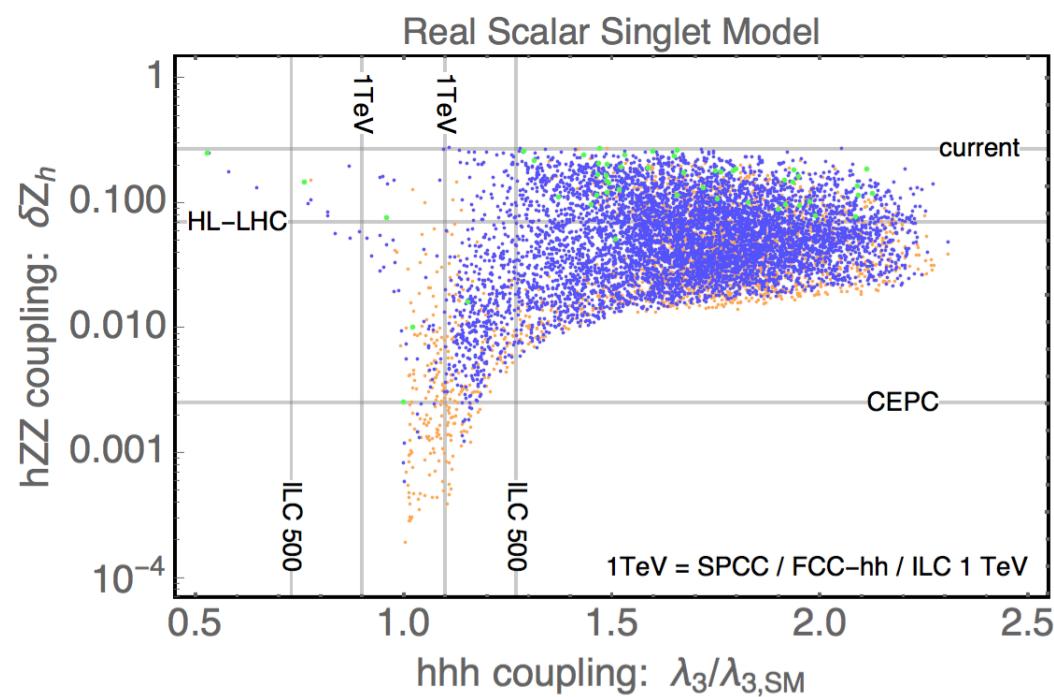
$$\delta Z_h \approx (1 - \cos \theta) - 0.006 \left(\frac{\lambda_3}{\lambda_{3,\text{SM}}} - 1 \right) - \frac{1}{2} \frac{|\lambda_{hs} v_s + a_{hs}|^2}{16\pi^2} I(M_h^2; M_h^2, M_s^2) - \frac{1}{2} \frac{|\lambda_{hs}|^2 v^2}{16\pi^2} I(M_h^2; M_s^2, M_s^2)$$

(leading effect is from mixing)

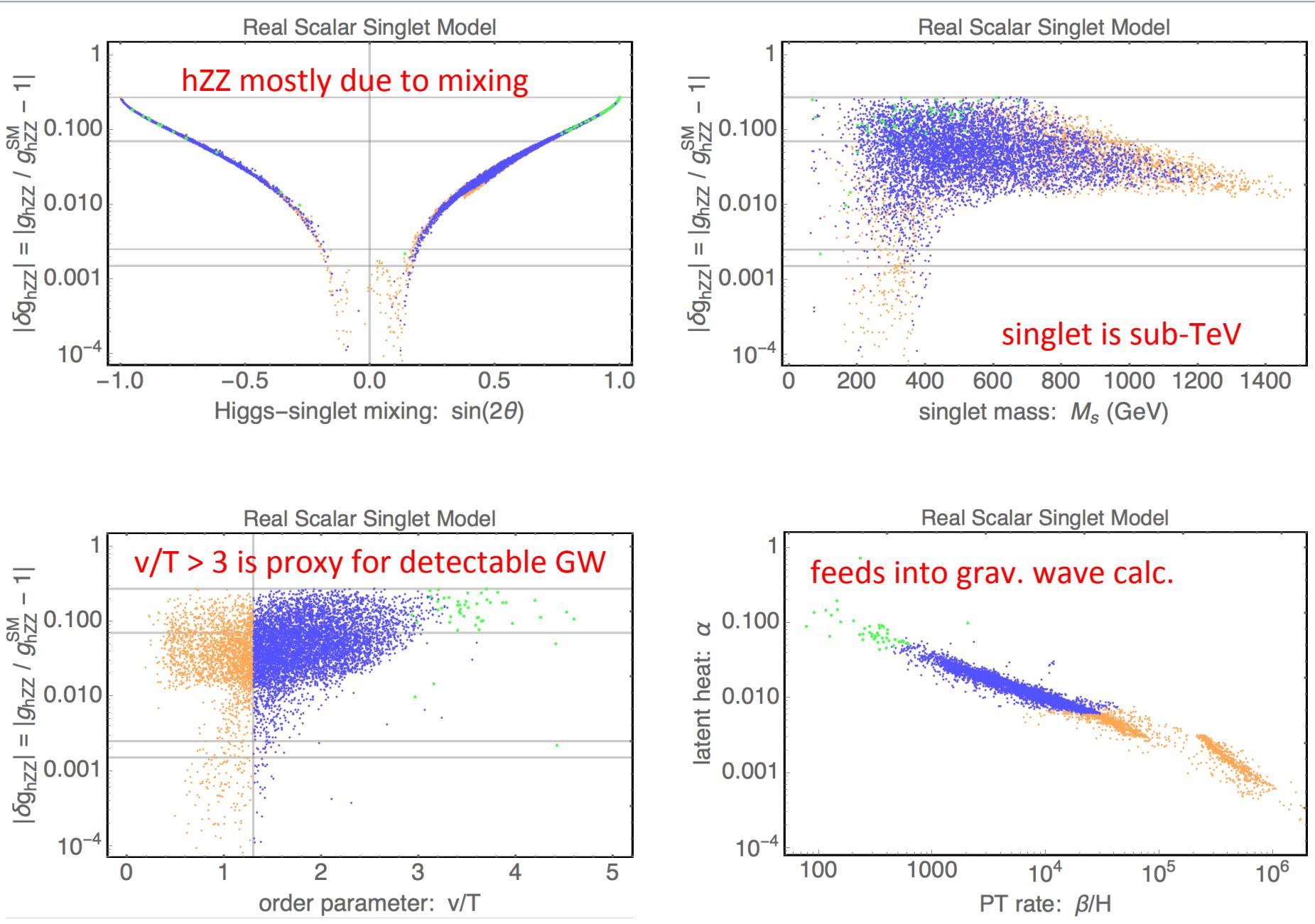


Orange = first order phase transition, $v(T_c)/T_c > 0$
 Blue = “strongly” first order phase transition, $v(T_c)/T_c > 1.3$
 Green = very strongly 1PT, could detect GWs at eLISA

(sensitivities of four different proposed eLISA configurations)



Parameter space with first order electroweak phase transition has large deviation in hZZ, which can be probed by CEPC

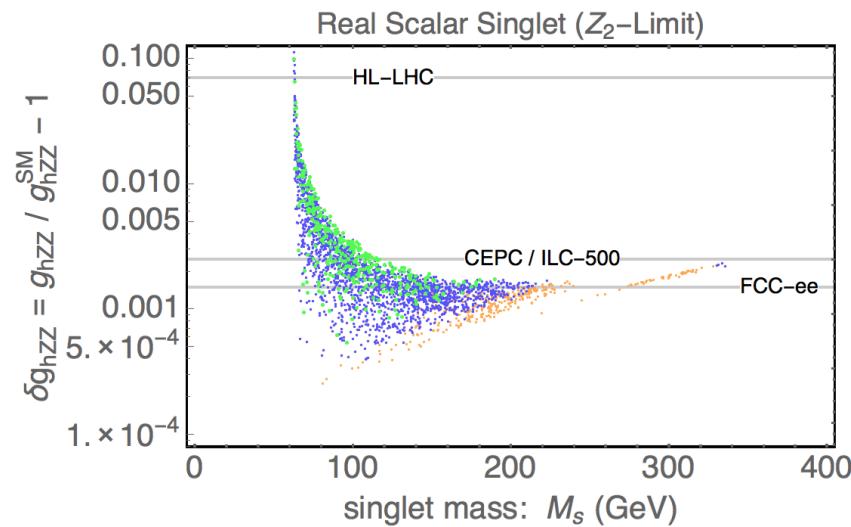


Challenging Limits



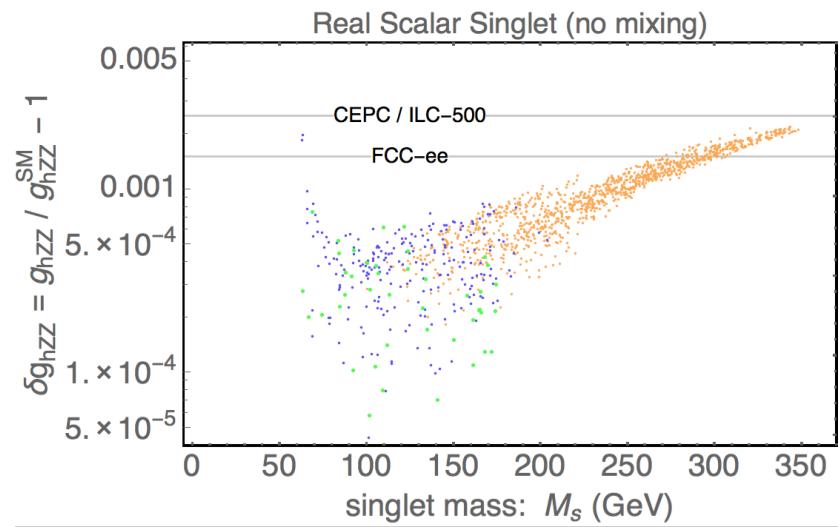
Z₂-Symmetric

$$a_s = a_{hs} = v_s = 0$$



Tuned Zero Mixing

$$a_{hs} + \lambda_{hs}v_s = 0$$



- Dubbed “nightmare scenario” by Curtin, Meade, & Yu (2014).
- No mixing & singlet is stable.

- A new “nightmare scenario” / “blind spot”
- Can be probed by non-resonant pair production $\text{pp} \rightarrow \text{ss}$ and $\text{s} \rightarrow \text{visible}$.
see also : Chen, Kozaczuk, & Lewis (2017)

Summary



The Standard Model predicts a continuous electroweak crossover (no bubbles).

It is easy to extend the SM and find a first order phase transition (bubbles!).

Precision measurements of Higgs couplings may uncover new physics at the EW scale, and thereby indirectly probe the electroweak phase transition.

A large deviation in the hZZ coupling seems to be generic in models with first order EWPT, allowing these models to be tested by Higgs factories.

scalar singlet w/ Z₂ (nightmare scenario)

