

# Decays and productions of hadronic molecules

Feng-Kun Guo

Institute of Theoretical Physics, Chinese Academy of Sciences

The 12th International Workshop on Heavy Quarkonium, PKU, Nov. 06–10, 2017

---

For more details and references:

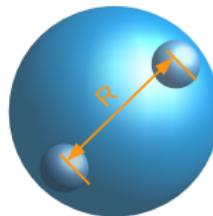
FKG, C. Hanhart, U.-G. Meißner, Q. Wang, Q. Zhao, B.-S. Zou, arXiv:1705.00141

## Hadronic molecules (I)

- Many  $XYZ$  states are candidates of **hadronic molecules** (main component): composite system of hadrons ( $\Rightarrow$  information for hadron-hadron interaction)
- For the constituents to be identified as hadrons, one must have

$$(E_B = m_1 + m_2 - M)$$

size:  $R \sim \frac{1}{\sqrt{2\mu E_B}} \gg r_{\text{hadron}} \sim \frac{1}{\Lambda_{\text{QCD}}}$  (for hadrons containing light quarks)



- ☞ only well defined concept at large distances
- ☞ well-separated scales, can be studied using EFT

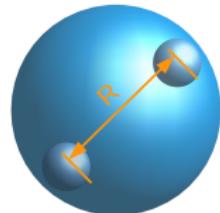
Braaten, Kusunoki, Fleming, Mehen, FKG, Hanhart, Mei $\beta$ nner, Baru, Nefediev, ...

- Only **narrow** hadrons can be considered as components of hadronic molecules,  
 $\Gamma_h \ll 1/r$ ,  $r$ : range of forces

Filin *et al.*, PRL105(2010)019101; FKG, Mei $\beta$ nner, PRD84(2011)014013

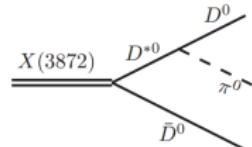
## Hadronic molecules (II)

- Once the same quantum numbers, always mix with other components
- Given a process  $\Rightarrow$  energy/momentum scales
  - to include all relevant d.o.f. at the given scale
  - to study a near-threshold structure, the threshold channel is necessary, unless very weak coupling,  
no matter what model was used as the starting point  
 $\Rightarrow$  for  $X(3872)$  and  $Z_c(3900)$ : has to consider  $D\bar{D}^*$
- Only the quantities at the momentum scale  $\sim 1/R$  measures the hadronic molecular component  
 $\Rightarrow$  not all processes are sensitive to it !
  - long-distance processes
  - short-distance processes



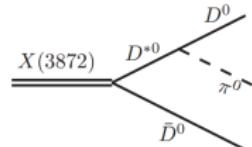
# $X(3872)$ , $Y(4260)$ and $Z_c(3900)$ (I)

- Suppose that the  $X(3872)$ ,  $Y(4260)$  and  $Z_c(3900)$  are hadronic molecules:
  - $\square X(3872): J^{PC} = 1^{++}, D\bar{D}^*$  Törnqvist, PLB590(2004)209; ...
  - $\square Y(4260): J^{PC} = 1^{--}, D_1(2420)\bar{D}$  Wang, Hanhart, Zhao, PRL111(2013)132003
  - $\square Z(3900): J^{PC} = 1^{+-}, D\bar{D}^*$  Wang et al. (2013); FKG et al., PRD88(2013)054007; ...
- Features of hadronic molecules:
  - $\square$  spin partners predictable talk by A. Nefediev
  - $\square$  couple strongly to their components  
⇒ special line shapes talk by C. Hanhart
  - $\square$  can decay through the decays of their components  
examples:  
$$X(3872) \rightarrow D^0 \bar{D}^0 \pi^0, X(3872) \rightarrow D^0 \bar{D}^0 \gamma$$
 Voloshin (2004); ...
  - $\square$  seemingly unrelated processes may be related; ...



# $X(3872)$ , $Y(4260)$ and $Z_c(3900)$ (I)

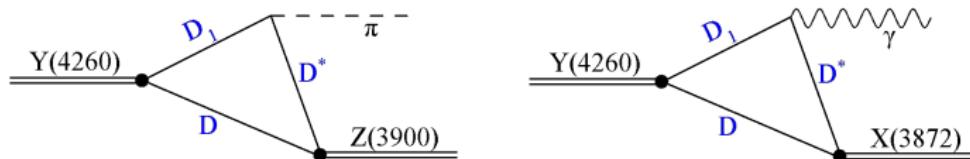
- Suppose that the  $X(3872)$ ,  $Y(4260)$  and  $Z_c(3900)$  are hadronic molecules:
  - $\square X(3872): J^{PC} = 1^{++}, D\bar{D}^*$  Törnqvist, PLB590(2004)209; ...
  - $\square Y(4260): J^{PC} = 1^{--}, D_1(2420)\bar{D}$  Wang, Hanhart, Zhao, PRL111(2013)132003
  - $\square Z(3900): J^{PC} = 1^{+-}, D\bar{D}^*$  Wang et al. (2013); FKG et al., PRD88(2013)054007; ...
- Features of hadronic molecules:
  - $\square$  spin partners predictable talk by A. Nefediev
  - $\square$  couple strongly to their components  
⇒ special line shapes talk by C. Hanhart
  - $\square$  can decay through the decays of their components  
examples:  
$$X(3872) \rightarrow D^0 \bar{D}^0 \pi^0, X(3872) \rightarrow D^0 \bar{D}^0 \gamma$$
  
Voloshin (2004); ...
  - $\square$  seemingly unrelated processes may be related; ...



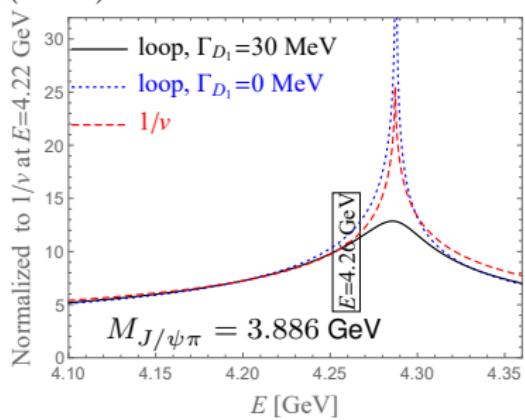
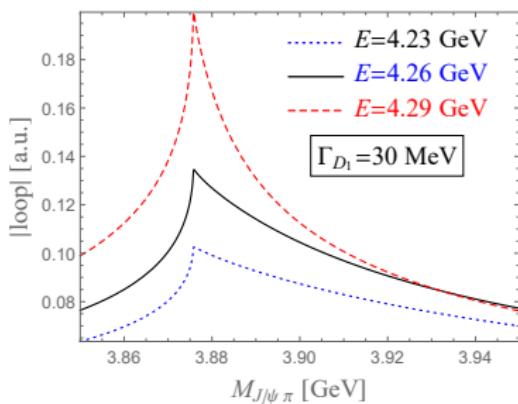
# $X(3872)$ , $Y(4260)$ and $Z_c(3900)$ (II)

Wang et al., PRL111(2013)132003; Cleven et al., PRD90(2014)074039; FKG et al., PLB725(2013)127

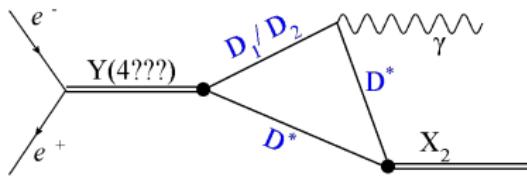
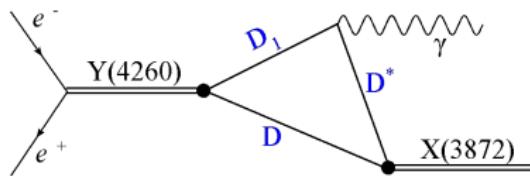
- Production of  $X(3872)$  and  $Z_c(3900)$  in  $Y(4260)$  decays



- Two enhancements: large couplings, triangle diagram  
very sensitive to the cm energy, e.g., for  $Z_c(3900)\pi$



# Production: $e^+e^- \rightarrow \gamma X(3872)$ and $\gamma X_2$



- Predicted production of  $\gamma X(3872)$   
BESIII observed at  $\sqrt{s} = 4.26$  GeV
- Spin partner:  $e^+e^- \rightarrow \gamma X_2$  in energy region  
 $\sqrt{s} \sim 4.26$  GeV +  $(M_{D_1/D_2} + M_{D^*}) - (M_{D_1} + M_D) \sim [4.4, 4.5]$  GeV

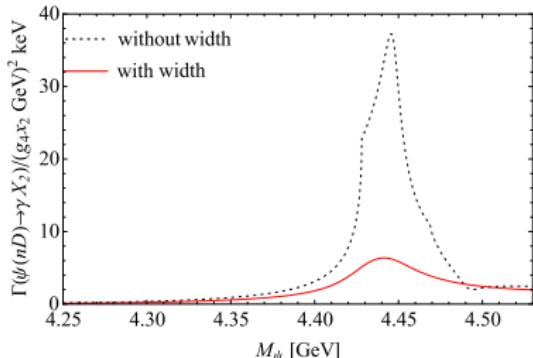
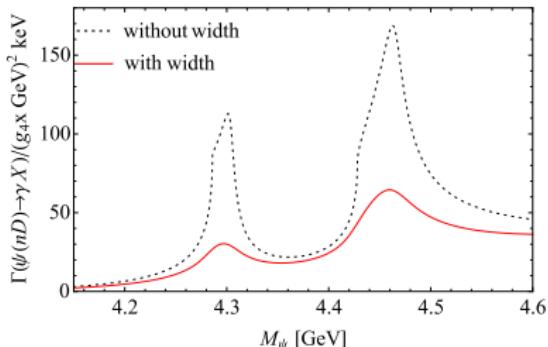
FKG et al., PLB725(2013)127

BESIII, PRL112(2014)092001

FKG, Meißner, Yang, PLB740(2015)42

$$\sqrt{s} \sim 4.26 \text{ GeV} + (M_{D_1/D_2} + M_{D^*}) - (M_{D_1} + M_D) \sim [4.4, 4.5] \text{ GeV}$$

can be facilitated if there is an analogue(s) of  $Y(4260)$ ,  $Y(4360)$  or  $\psi(4415)$ ?



# High energy productions (1)

- Processes driven by **short-distance**  $c\bar{c}$  physics, examples:
  - ↙ production of  $X(3872)$  in  $B$  decays, at hadron colliders with large  $p_T$   
Braaten et al. (2004,2005,2006,2009); Meng, Gao, Chao (2005); Bignamini et al. (2009); Meng, Han, Chao (2017); ...
- Often used to blame the  $D\bar{D}^*$  molecular interpretation ...
- Inequality:

Bignamini et al., PRL103(2009)162001

$$\begin{aligned}\sigma(\bar{p}p \rightarrow X) &\sim \left| \int d^3k \langle X | D^0 \bar{D}^{*0}(k) \rangle \langle D^0 \bar{D}^{*0}(k) | \bar{p}p \rangle \right|^2 \\ &\simeq \left| \int_{\mathcal{R}} d^3k \langle X | D^0 \bar{D}^{*0}(k) \rangle \langle D^0 \bar{D}^{*0}(k) | \bar{p}p \rangle \right|^2 \\ &\leq \int_{\mathcal{R}} d^3k |\Psi(k)|^2 \int_{\mathcal{R}} d^3k |\langle D^0 \bar{D}^{*0}(k) | \bar{p}p \rangle|^2 \\ &\leq \int_{\mathcal{R}} d^3k |\langle D^0 \bar{D}^{*0}(k) | \bar{p}p \rangle|^2\end{aligned}$$

For  $\mathcal{R} \simeq 35$  MeV  $\sim$  binding momentum of  $X(3872)$ ,

$$\Rightarrow \sigma \leq 0.071 \text{ nb} \ll 37 - 115 \text{ nb}$$

CDF, IJMPA20(2005)3765

# High energy productions (1)

- Processes driven by **short-distance**  $c\bar{c}$  physics, examples:
  - ↙ production of  $X(3872)$  in  $B$  decays, at hadron colliders with large  $p_T$   
Braaten et al. (2004,2005,2006,2009); Meng, Gao, Chao (2005); Bignamini et al. (2009); Meng, Han, Chao (2017); ...
- Often used to blame the  $D\bar{D}^*$  molecular interpretation ...
- Inequality: Bignamini et al., PRL103(2009)162001

$$\begin{aligned}\sigma(\bar{p}p \rightarrow X) &\sim \left| \int d^3\mathbf{k} \langle X | D^0 \bar{D}^{*0}(\mathbf{k}) \rangle \langle D^0 \bar{D}^{*0}(\mathbf{k}) | \bar{p}p \rangle \right|^2 \\ &\simeq \left| \int_{\mathcal{R}} d^3\mathbf{k} \langle X | D^0 \bar{D}^{*0}(\mathbf{k}) \rangle \langle D^0 \bar{D}^{*0}(\mathbf{k}) | \bar{p}p \rangle \right|^2 \\ &\leq \int_{\mathcal{R}} d^3\mathbf{k} |\Psi(\mathbf{k})|^2 \int_{\mathcal{R}} d^3\mathbf{k} \left| \langle D^0 \bar{D}^{*0}(\mathbf{k}) | \bar{p}p \rangle \right|^2 \\ &\leq \int_{\mathcal{R}} d^3\mathbf{k} \left| \langle D^0 \bar{D}^{*0}(\mathbf{k}) | \bar{p}p \rangle \right|^2\end{aligned}$$

For  $\mathcal{R} \simeq 35$  MeV  $\sim$  binding momentum of  $X(3872)$ ,

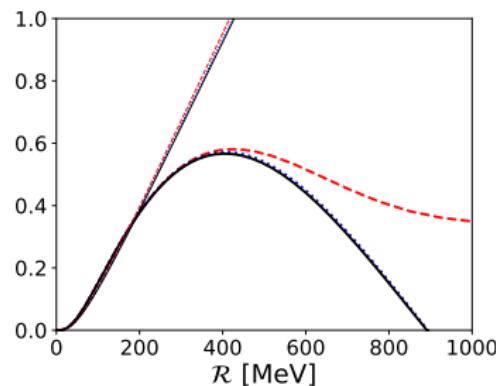
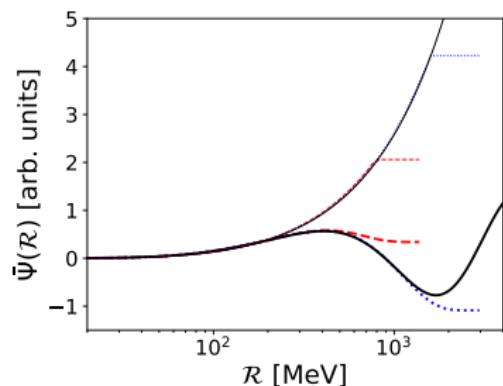
$$\Rightarrow \sigma \leq 0.071 \text{ nb} \ll 37 - 115 \text{ nb}$$

CDF, IJMPA20(2005)3765

## High energy productions (2)

- The deuteron as an example

Albaladejo et al., Chin.Phys.C, in print [arXiv:1709.09101]



- $\mathcal{R}$  must be much larger,  $\mathcal{R} \sim 300$  MeV see also: Artoisenet, Braaten, PRD81(2010)114018

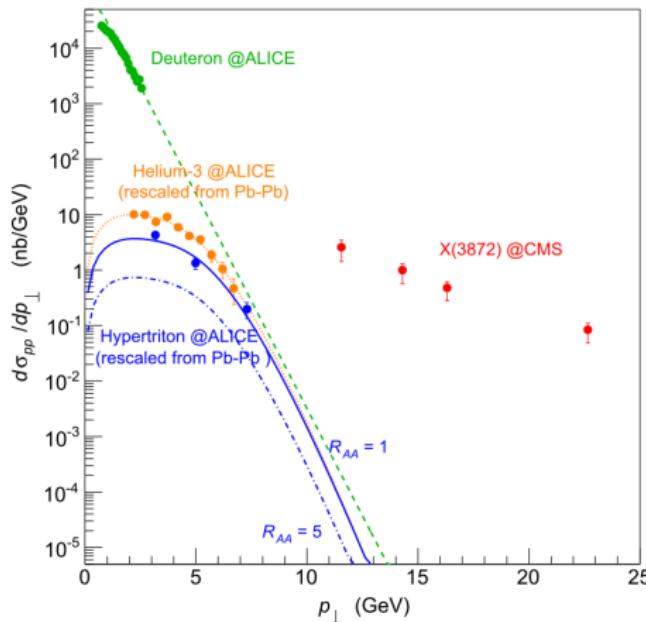
$\sigma(pp/\bar{p} \rightarrow X)$ [nb]	Exp.	$\Lambda=0.1$ GeV	$\Lambda=0.5$ GeV	$\Lambda=1.0$ GeV
CDF [IJMPA20(2005)3765]	37-115	0.07 (0.05)	7 (5)	29 (20)
CMS [JHEP1304(2013)154]	13-39	0.12 (0.04)	13 (4)	55 (15)

here  $\Lambda \simeq 2\sqrt{2/\pi}\mathcal{R} \simeq 1.6\mathcal{R}$

## High energy productions (3)

- A comparison of the production of the light nuclei and  $X(3872)$ , e.g.

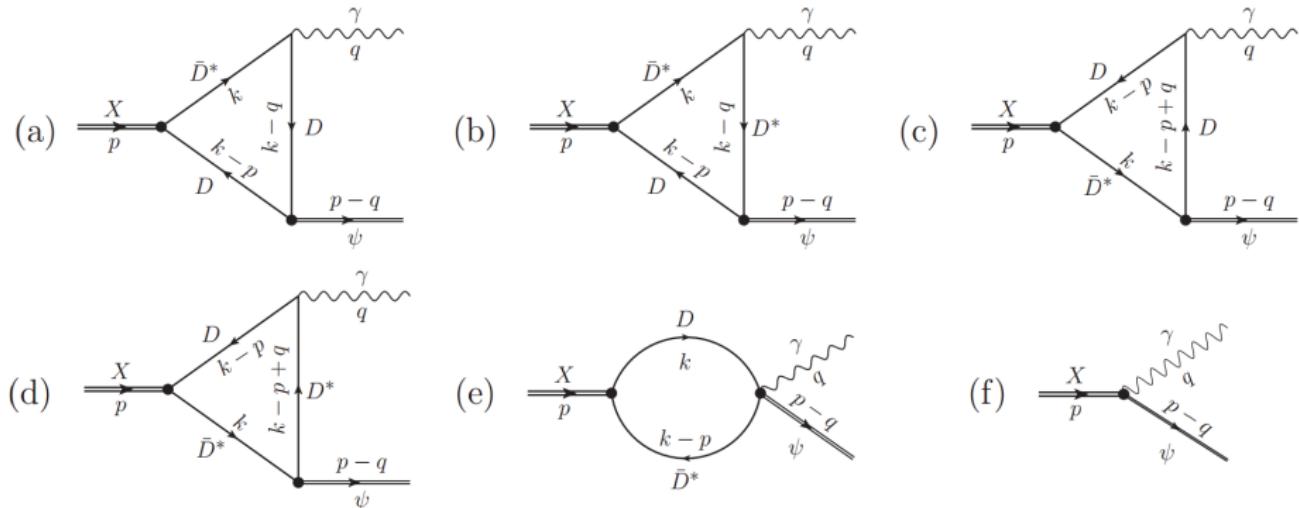
Esposito et al., PRD92(2015)034028 :



- but deutron and  $X$  are very different at short distances:
  - ↳ deutron: 6 quarks
  - ↳  $X$ : dominantly produced by  $c\bar{c}$  at short distances

# $X(3872) \rightarrow \psi\gamma$

FKG, Hanhart, Kalashnikova, Meißner, Nefediev, PLB742(2015)394



The ratio  $\frac{\mathcal{B}(X(3872) \rightarrow \psi'\gamma)}{\mathcal{B}(X(3872) \rightarrow J/\psi\gamma)} = 2.46 \pm 0.64 \pm 0.29$

is **insensitive to the molecular component** of the  $X(3872)$ :

- ☞ loops are sensitive to **unknown** couplings  $g_{\psi' DD}/g_{\psi' \bar{D}\bar{D}}$
- ☞ loops are divergent, needs a counterterm (**short-distance** physics)!

LHCb, NPB886(2014)665

see also Mehen, Springer, PRD83(2011)094009; Molnar et al., arXiv:1601.03366

## Summary

- should go beyond the mass spectrum because coupling strength contains important structure information  $\Rightarrow$  decays and productions
- hadronic molecular component should be detected in processes sensitive to long-distance physics
- high-energy processes:

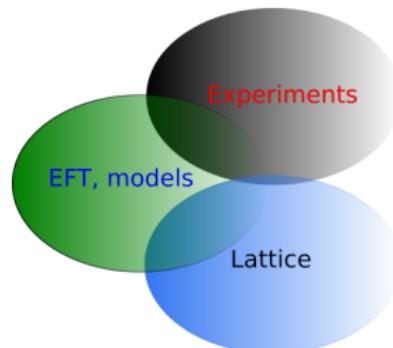
---

short-distance part  $\otimes$  long-distance part

---

cross section	line shapes	see talk by C. Hanhart
insensitive to	sensitive to	the hadronic molecular component

---

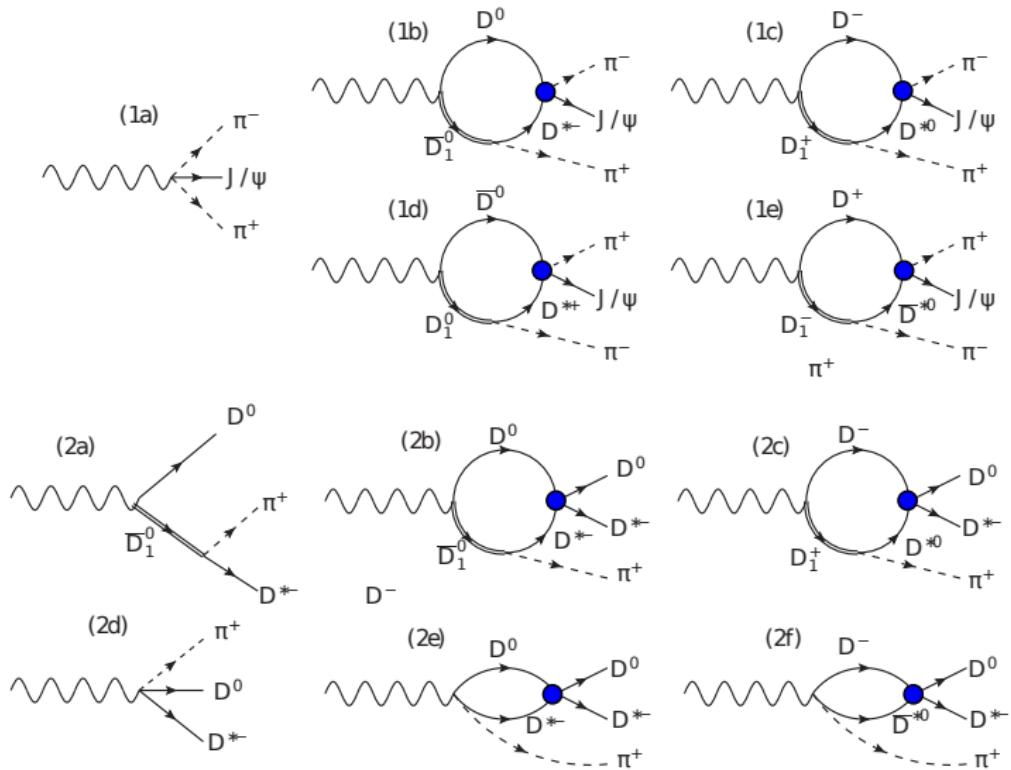


Thank you !

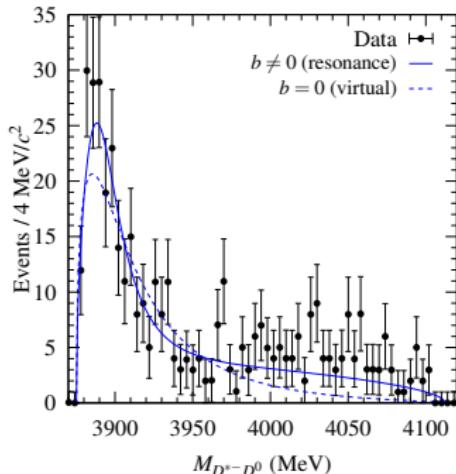
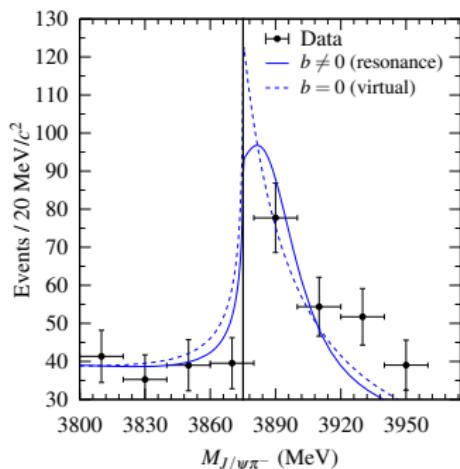
# Backup slides

# More about $Z_c(3900)$

Albaladejo, FKG, Hidalgo-Duque, Nieves, PLB755(2016)337



# More about $Z_c(3900)$



$M_{Z_c}$ (MeV)	$\Gamma_{Z_c}/2$ (MeV)	Ref.	Final state
$3899 \pm 6$	$23 \pm 11$	[1] (BESIII)	$J/\psi \pi$
$3895 \pm 8$	$32 \pm 18$	[2] (Belle)	$J/\psi \pi$
$3886 \pm 5$	$19 \pm 5$	[3] (CLEO-c)	$J/\psi \pi$
$3884 \pm 5$	$12 \pm 6$	[4] (BESIII)	$\bar{D}^* D$
$3882 \pm 3$	$13 \pm 5$	[5] (BESIII)	$\bar{D}^* D$
$3894 \pm 6 \pm 1$	$30 \pm 12 \pm 6$	$\Lambda_2 = 1.0 \text{ GeV}$	$J/\psi \pi, \bar{D}^* D$
$3886 \pm 4 \pm 1$	$22 \pm 6 \pm 4$	$\Lambda_2 = 0.5 \text{ GeV}$	$J/\psi \pi, \bar{D}^* D$
$3831 \pm 26^{+7}_{-28}$	virtual state	$\Lambda_2 = 1.0 \text{ GeV}$	$J/\psi \pi, \bar{D}^* D$
$3844 \pm 19^{+12}_{-21}$	virtual state	$\Lambda_2 = 0.5 \text{ GeV}$	$J/\psi \pi, \bar{D}^* D$

resonance pole

or virtual state

# Decays: $X(3872) \rightarrow D^0 \bar{D}^0 \pi^0$

- A long-distance process, thus can be studied in nonrelativistic EFT
- Already studied by many authors

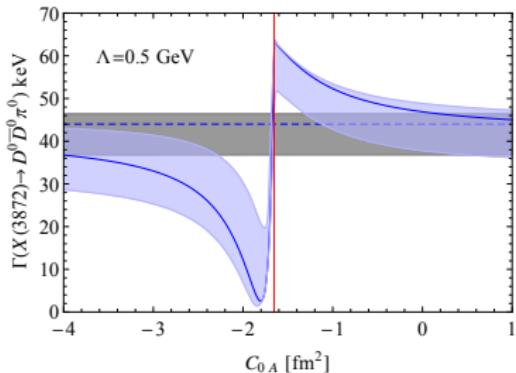
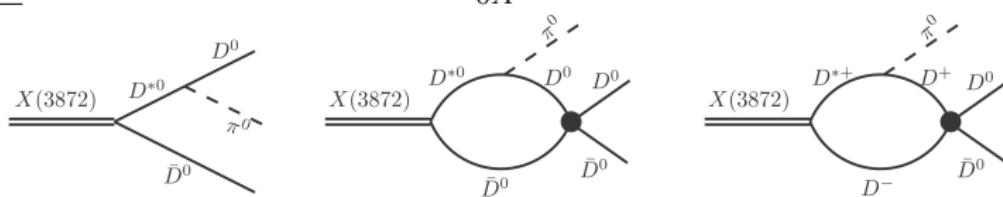
Voloshin (2004); Fleming et al (2007); Braaten, Lu (2007); Hanhart et al (2007); ...

Our new insight:

FKG et al., EPJC74(2014)2885

If there is a **near-threshold**  $D\bar{D}$  hadronic molecule  $\Rightarrow$  a large impact

Problem: one unknown contact term  $C_{0A}$



- ☞ grey band: tree-level result (consistent with Fleming et al., PRD76(2007))
- ☞ vertical line: a  $D\bar{D}$  bound state at threshold