

Results on charmonium(-like) states from Belle

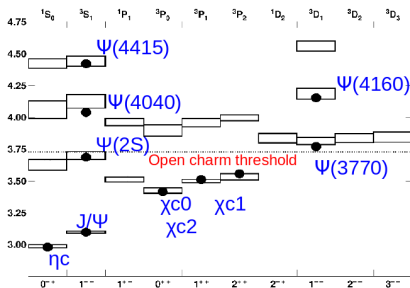
V. Zhukova
Belle Collaboration

“Quarkonium Working Group”, Beijing, 6-10 November 2017

New measurement and angular analysis of the $e^+e^- \rightarrow D^{(*)+}D^{*-}$ process near the open charm threshold with initial state radiation

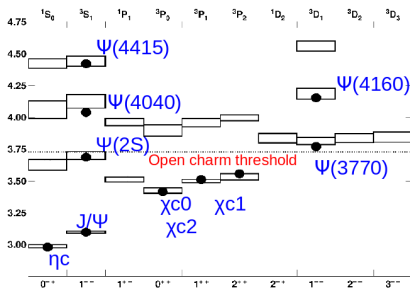
Spectrum of charmonium

- Vector states above open-charm threshold are not fully understood
- Parameters of ψ states obtained from $\sigma_{\text{tot}}(e^+e^- \rightarrow \text{hadrons})$
 - are model-dependent
 - have large uncertainties
- Data collected should allow for coupled-channel analysis



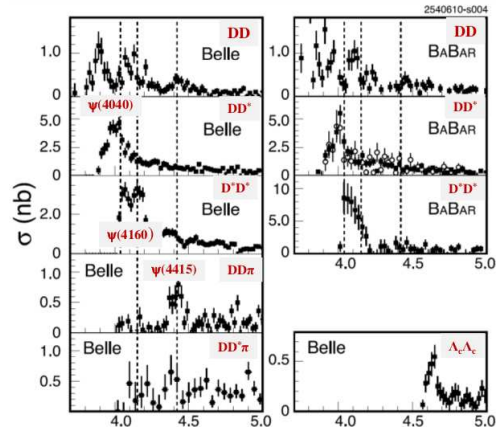
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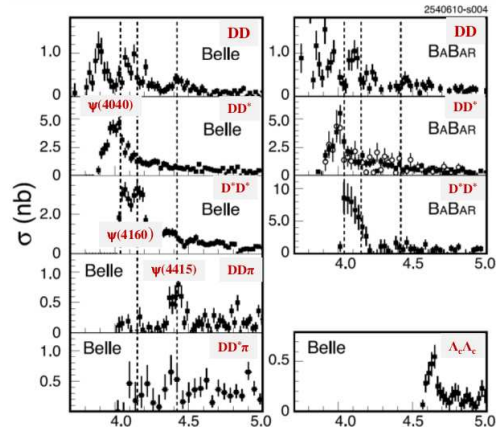
Solution $\implies$ Measure **exclusive** cross sections

Comparison with previous results



- Belle and BaBar results **agree** with each other
- Statistics is **too low** to study the structure of the cross sections
- Sum of **all** measured **exclusive** cross-section to open-charm channels saturates the **total** cross section

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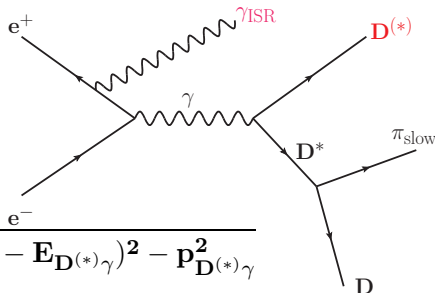
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Goals:

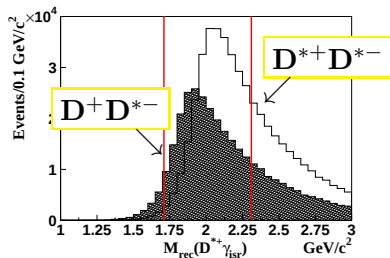
- To improve accuracy of cross section measurements
- To measure separately cross sections for all 3 possible helicity combinations (TT, LT, LL) for the $D^*\bar{D}^*$ final state

Method

- Partial reconstruction
- Reconstruct D^* , γ_{ISR}

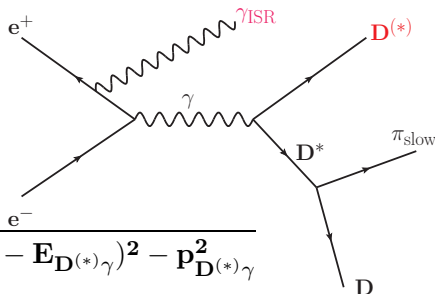


$$M_{\text{recoil}}(D^{(*)}\gamma) = \sqrt{(E_{\text{c.m.}} - E_{D^{(*)}\gamma})^2 - p_{D^{(*)}\gamma}^2}$$

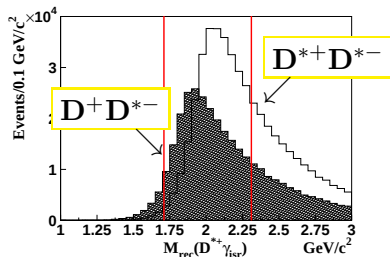


Method

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- Reconstruct D^* , γ_{ISR}



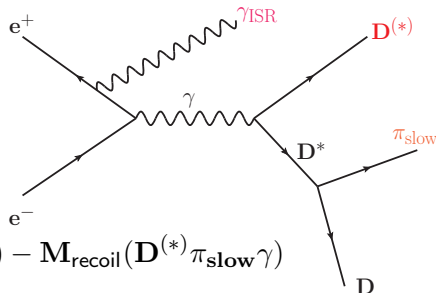
$$M_{recoil}(D^{(*)}\gamma) = \sqrt{(E_{c.m.} - E_{D^{(*)}\gamma})^2 - p_{D^{(*)}\gamma}^2}$$



Problem: Cannot distinguish between D , D^* and D^{**} in the final state

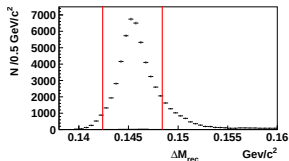
Method

- Partial reconstruction
- Reconstruct D^* , γ_{ISR} and π_{slow}



$$\Delta M_{\text{recoil}} = M_{\text{recoil}}(D^{(*)}\gamma_{\text{ISR}}) - M_{\text{recoil}}(D^{(*)}\pi_{\text{slow}}\gamma)$$

$e^+e^- \rightarrow D^+D^{*-}$



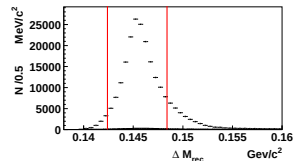
Recoil mass difference

ΔM_{recoil}

cut:

$\pm 3 \text{ MeV}/c^2$

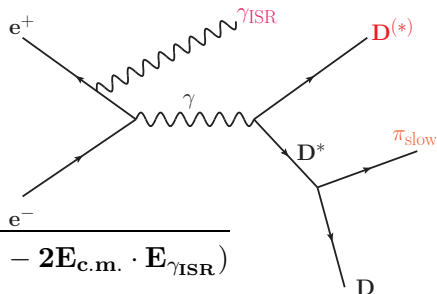
$e^+e^- \rightarrow D^{*+}D^{*-}$



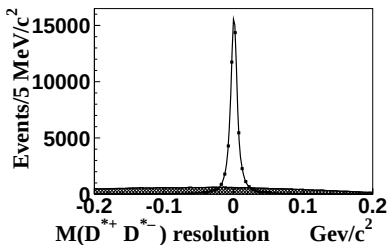
Method

- Partial reconstruction
- Reconstruct D^* , γ_{ISR} and π_{slow}
- $M(D^{(*)} + D^{*-}) \equiv M_{\text{recoil}}(\gamma_{\text{ISR}})$

$$M_{\text{recoil}}(\gamma_{\text{ISR}}) = \sqrt{(\mathbf{E}_{\text{c.m.}}^2 - 2\mathbf{E}_{\text{c.m.}} \cdot \mathbf{E}_{\gamma_{\text{ISR}}})}$$



Refit $M_{\text{recoil}}(D^{(*)}\gamma_{\text{ISR}})$ to D^* mass to **improve** the $M_{\text{recoil}}(\gamma_{\text{ISR}})$ resolution



$M_{\text{recoil}}(\gamma_{\text{ISR}})$ resolution:

Before re-fit — hatched histogram

After re-fit — solid line

Comparison with previous analysis

- Increased data sample: $547 \text{ fb}^{-1} \Rightarrow 951 \text{ fb}^{-1}$
- Additional modes for D reconstruction $\Rightarrow D^0$ decay channels:
- Extended signal region for $M_{\text{recoil}}(D^{(*)}\gamma_{\text{ISR}})$

$$|(M_{\text{recoil}}(D^{(*)+}\gamma_{\text{ISR}}) - M(D^{*-}))| < \overset{300}{200} \text{ MeV}/c^2$$

$$\bullet \sigma[e^+e^- \rightarrow D^{(*)+}D^{*-}] = \frac{dN/dM}{\eta_{\text{tot}}(M) \cdot dL/dM}$$

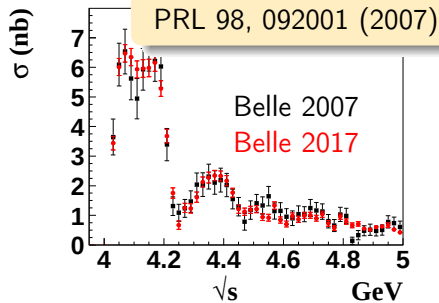
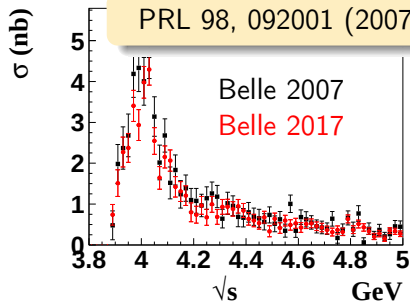
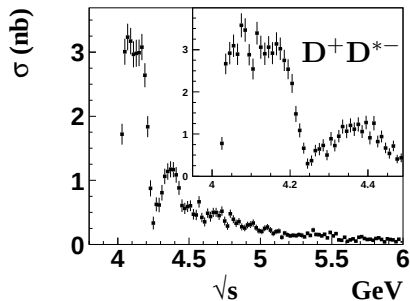
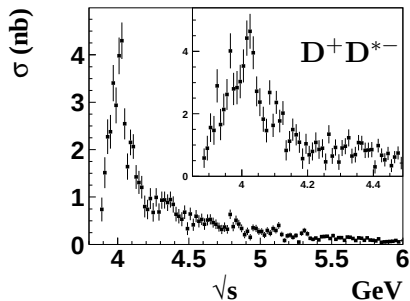
dL/dM up to **second-order** QED corrections
(Kuraev & Fadin (1985))

- ① $K^-\pi^+$
- ② K^-K^+
- ③ $K^-\pi^-\pi^+\pi^+$
- ④ $K_S^0\pi^+\pi^-$
- ⑤ $K^-\pi^+\pi^0$
- ⑥ $K_S^0K^+K^-$
- ⑦ $K_S^0\pi^0$
- ⑧ $K^-K^+\pi^-\pi^+$
- ⑨ $K_S^0\pi^+\pi^-\pi^0$

Backgrounds

- ① **Combinatorial** background under the reconstructed $D^{(*)+}$ peak
- ② Real $D^{(*)+}$ mesons and a **combinatorial** π_{slow}
- ③ **Both** the $D^{(*)+}$ meson and π_{slow} are combinatorial
- ④ **Reflections** from the processes $e^+e^- \rightarrow D^{(*)+}D^{*-}\pi^0\gamma_{\text{ISR}}$ where the π^0 is **lost**
- ⑤ **Contribution** of the $e^+e^- \rightarrow D^{(*)+}D^{*-}\pi_{\text{fast}}^0$ where the hard π_{fast}^0 is **misidentified** as γ_{ISR}

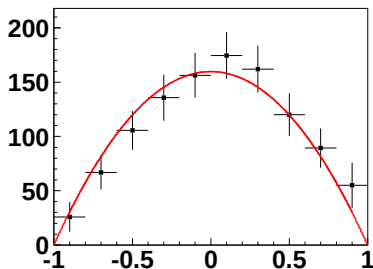
Background contribution estimated from the **data**



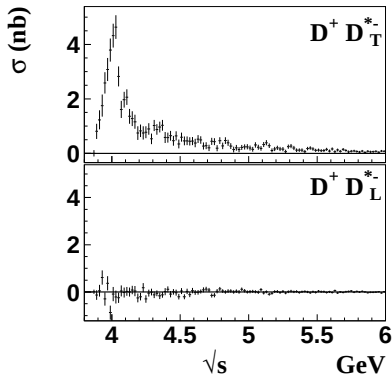
Angular analysis of the process $e^+e^- \rightarrow D^+D^{*-}$

- Study D^* helicity angle distribution in each bin of $M(D^+D^{*-})$
- D^* are transversely polarized $\Rightarrow$ Check method

$$4.05 < M(D^+D^{*-}) < 4.3 \text{ GeV}/c^2$$



$$F(\cos \theta) = \eta(\cos \theta) \cdot dM/dL \cdot (f_L + f_T)$$



$$f_L = \sigma_L \cdot \cos^2 \theta$$

$$f_T = \sigma_T \cdot (1 - \cos^2 \theta)$$

Angular analysis of the process $e^+e^- \rightarrow D^{*+}D^{*-}$

- Study of the D^* helicity angle distribution in each bin of $M(D^{*+}D^{*-})$
- Helicity composition of the $D^{*+}D^{*-}$ final state:

$$D_T^{*+}D_T^{*-}, D_T^{*+}D_L^{*-} \text{ and } D_L^{*+}D_L^{*-}$$

- $D_T^* \equiv$ transversely polarized D^* meson
- $D_L^* \equiv$ longitudinally polarized D^* meson
- Total cross section

$$\sigma = \sigma_{TT} + \sigma_{TL} + \sigma_{LL}$$

$$f = \eta(c_1, c_2) \cdot dL/dM \cdot (f_{LL} + f_{TL} + f_{TT}) + f_{bg}$$

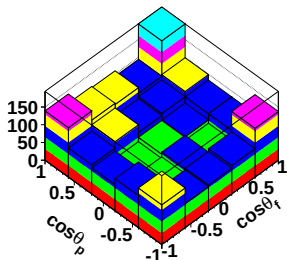
$$c_1 \equiv \cos \theta_f \quad c_2 \equiv \cos \theta_p$$

θ 's are D^* 's helicity angles

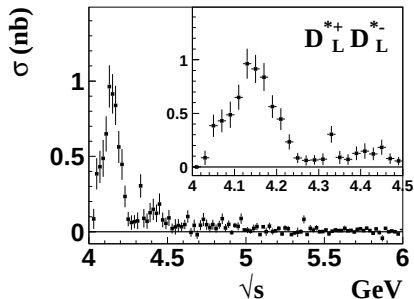
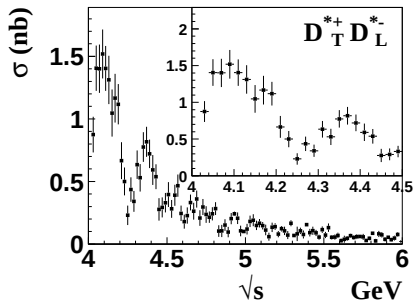
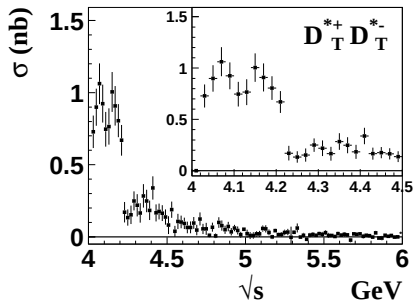
$$f_{TT} = \sigma_{TT} \cdot (1 - c_1^2) \cdot (1 - c_2^2)$$

$$f_{TL} = \sigma_{TL} \cdot ((1 - c_1^2) \cdot c_2^2 + c_1^2 \cdot (1 - c_2^2))$$

$$f_{LL} = \sigma_{LL} \cdot c_1^2 \cdot c_2^2$$



Fit results



Conclusions

- We measured the **exclusive** cross sections of the $e^+e^- \rightarrow D^+D^{*-}$ and $e^+e^- \rightarrow D^{*+}D^{*-}$ processes
- The accuracy of the cross section measurements is **increased**
- The systematic uncertainties are significantly **reduced**
- For the $e^+e^- \rightarrow D^{*+}D^{*-}$ process we measured **separately** the cross sections for all three possible helicity final states (TT, LT and LL)

**Observation of an alternative $\chi_{c0}(2P)$ candidate
in $e^+e^- \rightarrow J/\psi D\bar{D}$**

Motivation

Observed by Belle, confirmed by BaBar in $B \rightarrow (J/\psi \omega) K$

PRL **94**, 182002 (2005), PRD **82**, 011101 (2010)

$X(3915)$

Observed by both Belle and BaBar in $\gamma\gamma \rightarrow J/\psi \omega$

PRL **104**, 092001 (2010), PRD **86**, 072002 (2012)

BaBar: $J^P = 0^+ \implies \chi_{c0}(2P)$ candidate

PRD **86**, 072002(2012)

Difficulties (see, e.g., S. L. Olsen (2015), F.-K. Guo *et al.* (2012)):

- Too narrow: 20 MeV (measured) versus ~ 100 MeV (expected)
- Not seen in $D\bar{D}$ (expected as dominating mode!)
- Unnaturally small 2^3P_2 - 2^3P_1 mass splitting
- Strong OZI violation: large BF in OZI-suppressed $J/\psi \omega$ mode

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Search for alternative $\chi_{c0}(2P)$ candidate in $e^+e^- \rightarrow J/\psi D\bar{D}$ annihilation

Method

$$e^+e^- \rightarrow J/\psi D \bar{D}, \quad D \equiv D^0 \text{ or } D^+$$

$$\mathbf{M}_{\text{rec}}(\mathbf{J}/\psi, \mathbf{D}) = \sqrt{(\mathbf{p}_{e^+e^-} - \mathbf{p}_{J/\psi} - \mathbf{p}_D)^2}$$

- $J/\psi \rightarrow \{e^+e^-, \mu^+\mu^-\}$
- Both D^0 and D^+ used:
 - $D^0 \rightarrow \{K^-\pi^+, K_s^0\pi^+\pi^-, K^-\pi^+\pi^0, K^-\pi^+\pi^+\pi^-\}$ (4 channels)
 - $D^+ \rightarrow \{K_s^0\pi^+, K^-\pi^+\pi^+, K_s^0\pi^+\pi^0, K^-\pi^+\pi^+\pi^0, K_s^0\pi^+\pi^+\pi^-\}$ (5 channels)
- Signal and background **separated** using the MLP **neural network**
- **Global optimization** of the selection requirements: 4 variables per D channel (signal regions in $M_{J/\psi}$, M_D , $M_{\text{rec}}(J/\psi, D)$ and MLP output cutoff value)

Resulting sample: **103** events with **$24.9 \pm 1.1 \pm 1.6$** background events

Signal fit

Amplitude analysis in **6D** phase space: $\{M_{D\bar{D}}, \theta_{\text{prod}}, \theta_{J/\psi}, \theta_{X^*}, \phi_{l-}, \phi_D\}$

$$S(\Phi) = \sum_{\substack{\lambda_{\text{beam}}=-1,1 \\ \lambda_{\ell\ell}=-1,1}} \left| \sum_{X^*} A_{\lambda_{\text{beam}} \lambda_{\ell\ell}}(\Phi) A_{X^*}(M_{D\bar{D}}) \right|^2$$

Resonance: A_{X^*} — relativistic **BW**,

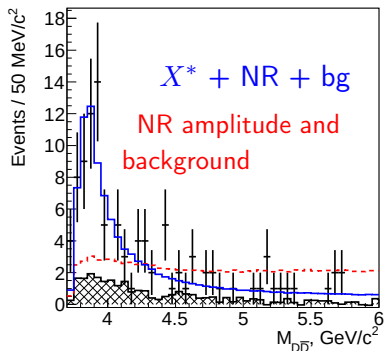
Non-resonant amplitude:

$$A_{X^*} = \sqrt{F_{D\bar{D}}(M_{D\bar{D}})},$$

$F_{D\bar{D}}(M_{D\bar{D}})$ - non-resonant form factor,

default model: $F_{D\bar{D}} = 1$

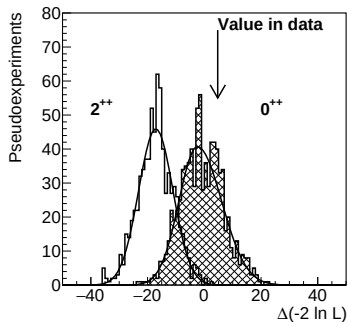
Model: $X^* + \text{non-resonant contribution}$



J^{PC}	Mass, MeV/c ²	Width, MeV	Significance
0 ⁺⁺	3862 ⁺²⁶ ₋₃₂	201 ⁺¹⁵⁴ ₋₆₇	9.1σ
2 ⁺⁺	3879 ⁺²⁰ ₋₁₇	171 ⁺¹²⁹ ₋₆₂	8.0σ
2 ⁺⁺	3879 ⁺¹⁷ ₋₁₇	148 ⁺¹⁰⁸ ₋₅₀	8.0σ
2 ⁺⁺	3883 ⁺²⁶ ₋₂₄	227 ⁺²⁰¹ ₋₁₂₅	8.0σ

$$J^{PC} = 0^{++} \text{ versus } J^{PC} = 2^{++}$$

Approach: Toy MC pseudoexperiments generated in accordance with fit results for $J^{PC} = 0^{++}$ and 2^{++} and fitted for both hypotheses



Result:

- $J^{PC} = 2^{++}$ **excluded** at the level 2.5σ including systematics
- $J^{PC} = 0^{++}$ with **CL=77%** (default model)

$X^*(3860)$ versus $X(3915)$ — the fight for $\chi_{c0}(2P)$

	Theory	$X(3915)$	$X^*(3860)$
J^{PC}	0^{++}	$\pm$	$+$
Mass	3854 MeV/ c^2 (Ebert <i>et al.</i>) 3916 MeV/ c^2 (Godfrey <i>et al.</i>)	$\pm$	$+$
Width	Broad ($\Gamma \sim 100$ MeV)	$-$	$+$
$\frac{m_{\chi_{c2}(2P)} - m_{\chi_{c0}(2P)}}{m_{\chi_{c2}(1P)} - m_{\chi_{c0}(1P)}}$	0.6..0.9	$-$	$+$
BF($D\bar{D}$)	Large	$-$	$+$
BF($J/\psi \omega$)	Small	$-$	$+$

In addition, $X^*(3860)$

- is produced **similarly** to $\chi_{c0}(1P)$ (Belle (2004))
- **agrees** with the peak in $\gamma\gamma$ data with $M = 3837.6 \pm 11.5$ MeV/ c^2 and $\Gamma = 221 \pm 19$ MeV

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	Theory	$X(3915)$	$X^*(3860)$
J^{PC}	0^{++}	$\pm$	$+$
M	$3854 \text{ MeV}/c^2$ (Ebert et al.)	$-$	$-$

Conclusion: $X^*(3860)$ wins!

$\text{BF}(DD)$	Large	$-$	$+$
$\text{BF}(J/\psi \omega)$	Small	$-$	$+$

In addition, $X^*(3860)$

- is produced **similarly** to $\chi_{c0}(1P)$ (Belle (2004))
- **agrees** with the peak in $\gamma\gamma$ data with $M = 3837.6 \pm 11.5 \text{ MeV}/c^2$ and $\Gamma = 221 \pm 19 \text{ MeV}$

Conclusions

- A new charmoniumlike state $X(3860)$ is observed
- $M = 3862_{-32}^{+26} {}_{-13}^{+40} \text{ MeV}/c^2$
- $\Gamma = 201_{-67}^{+154} {}_{-82}^{+88} \text{ MeV}$
- $J^{PC} = 0^{++}$ favoured

$X(3860) \implies$ good $\chi_{c0}(2P)$ candidate

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- $J^{PC} = 0^{++}$ favoured

$X(3860) \implies \text{good } \chi_{c0}(2P) \text{ candidate}$

Thank you for your attention!



Criteria

- $|dr| < 2 \text{ cm}$ and $|dz| < 4 \text{ cm}$
- $\mathcal{P}_{K/\pi} = \mathcal{L}_K / (\mathcal{L}_K + \mathcal{L}_\pi) > 0.6$
- **K_S candidates:**
 - $|M_{inv}(\pi^+\pi^-) - M_{K_S^0}| < 15 \text{ MeV}/c^2$
 - the distance between the two pion tracks $< 1 \text{ cm}$
 - the transverse flight distance from IP $> 0.1 \text{ cm}$
 - the angle between the K_S momentum direction and decay path in $x - y$ plane $< 0.1 \text{ rad}$

π_0 candidates:

- $|M_{inv}(\gamma\gamma) - M_{\pi_0}| < 15 \text{ MeV}/c^2$

D^0 decay channels:

- 1 $K^-\pi^+$
- 2 K^-K^+
- 3 $K^-\pi^-\pi^+\pi^+$
- 4 $K_S^0\pi^+\pi^-$
- 5 $K^-\pi^+\pi^0$
- 6 $K_S^0K^+K^-$
- 7 $K_S^0\pi^0$
- 8 $K^-K^+\pi^-\pi^+$
- 9 $K_S^0\pi^+\pi^-\pi^0$

D^+ decay channels:

- 1 $K^+\pi^-\pi^-$
- 2 $K_S^0\pi^-$
- 3 $K_S^0K^+$

D^* decay channels:

- 1 $D^0\pi^+$

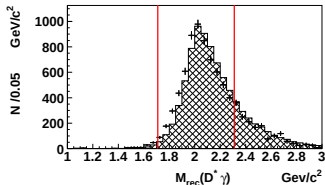
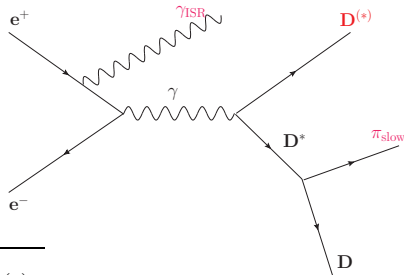
Analysis of the process $e^+e^- \rightarrow D^{(*)}+D^{*-}$

Method:

- partial reconstruction;
- reconstruction D^* , π_{slow} and γ_{ISR} ;

$$M_{\text{recoil}}(D^{(*)}\gamma) = \sqrt{(E_{c.m.} - E_{D^{(*)}\gamma})^2 - p_{D^{(*)}\gamma}^2}$$

$$\Delta M_{\text{recoil}} = M_{\text{recoil}}(D^{(*)}\gamma_{\text{ISR}}) - M_{\text{recoil}}(D^{(*)}\pi_{\text{slow}}\gamma)$$



Spectrum of $M_{\text{recoil}}(D^*\gamma_{\text{ISR}})$

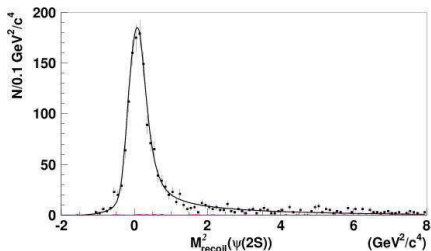
$$M_{\text{recoil}}(D^{(*)}\gamma) = \sqrt{(E_{c.m.} - E_{D^{(*)}\gamma})^2 - p_{D^{(*)}\gamma}^2}$$

Correction of γ_{ISR} energy

reference channel

$$e^+e^- \rightarrow \psi(2S)\gamma_{\text{ISR}}$$

$$\psi(2S) \rightarrow J/\psi \pi^+ \pi^-$$

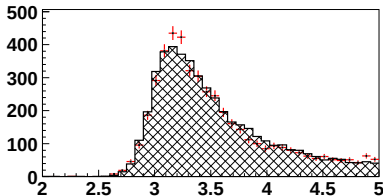
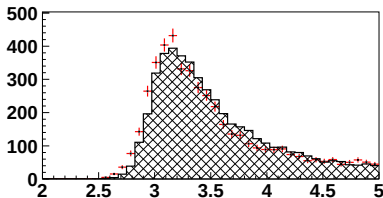


Conclusions:

phokhara generator describes the second radiation correction correctly

The same process on the other side

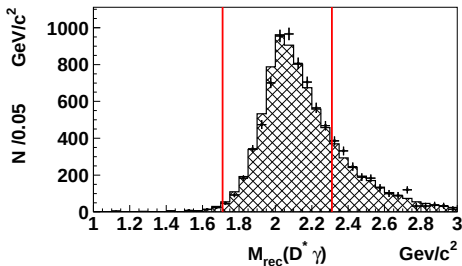
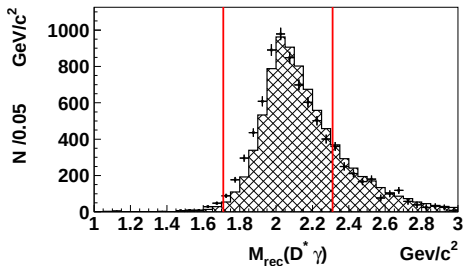
The recoil mass $M_{\text{recoil}}(J/\psi \pi^+ \pi^-)$



The recoil mass $M_{\text{recoil}}(D^* \gamma_{\text{ISR}})$

before correction γ_{ISR} energy

after correction γ_{ISR} energy



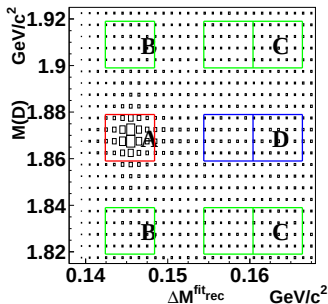
cut:

$$|M_{\text{recoil}}(D^* \gamma_{\text{ISR}}) - M(D^*)| < 300 \text{ MeV}/c^2$$

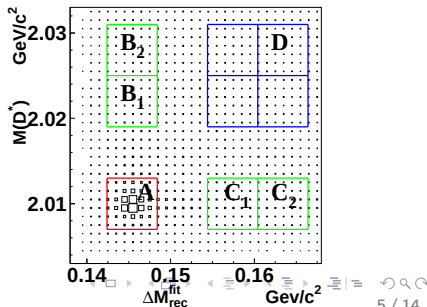
Backgrounds

- 1 **Combinatorial** background under the reconstructed $D^{(*)+}$ peak
- 2 Real $D^{(*)+}$ mesons and a **combinatorial** π_{slow}
- 3 **Both** the $D^{(*)+}$ meson and π_{slow} are combinatorial
- 4 **Reflections** from the processes $e^+e^- \rightarrow D^{(*)+}D^{*-}\pi^0\gamma_{\text{ISR}}$ where the π^0 is **lost**
- 5 **Contribution** of the $e^+e^- \rightarrow D^{(*)+}D^{*-}\pi_{\text{fast}}^0$ where the hard π_{fast}^0 is **misidentified** as γ_{ISR}

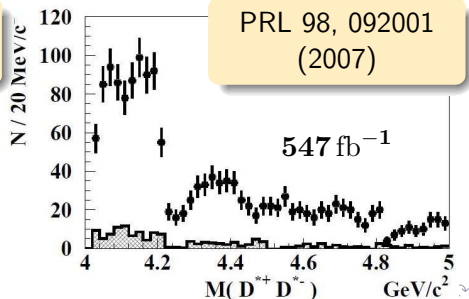
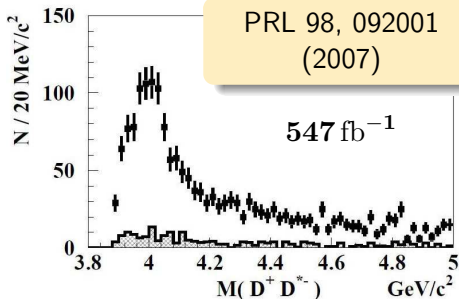
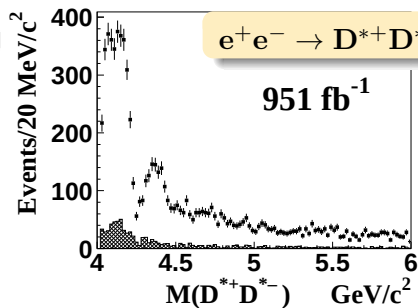
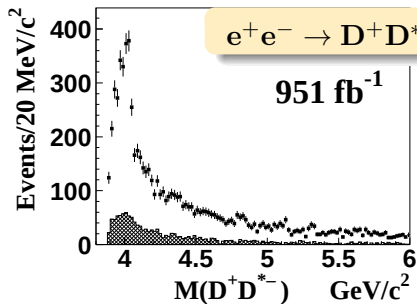
$$e^+e^- \rightarrow D^+D^{*-}$$



$$e^+e^- \rightarrow D^{*+}D^{*-}$$

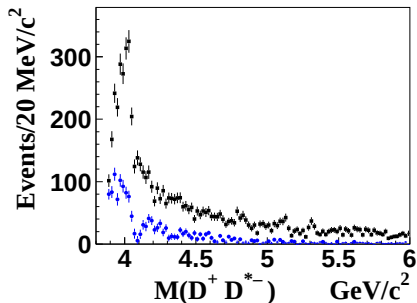


Mass spectra

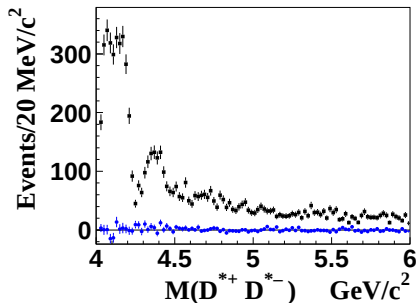


Reflection from the processes $e^+e^- \rightarrow D^{(*)}+D^{*-}\pi^0\gamma_{\text{ISR}}$

$$e^+e^- \rightarrow D^+D^{*-}$$



$$e^+e^- \rightarrow D^{*+}D^{*-}$$



Background (blue points) from

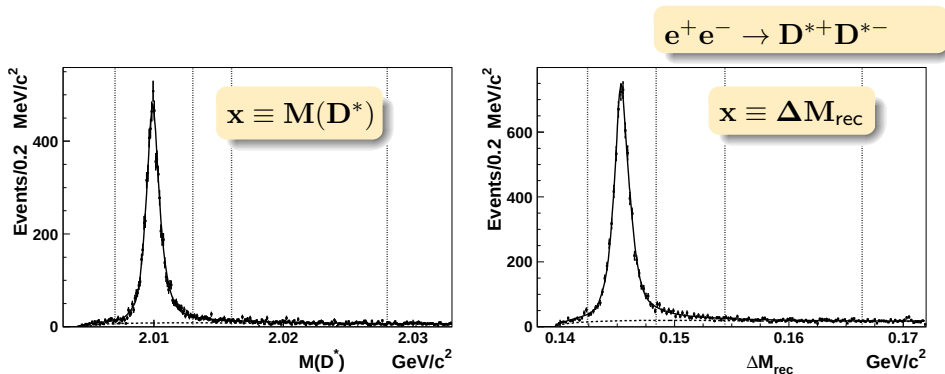
$$e^+e^- \rightarrow D^{(*)}+D^{*-}\pi_{\text{miss}}^0\gamma_{\text{ISR}}$$

is evaluated from the isospin-conjugated process

$$e^+e^- \rightarrow D^{(*)0}D^{*-}\pi_{\text{miss}}^+\gamma_{\text{ISR}}$$

with the reconstruction of $D^{(*)0}$, π_{slow}^- and γ_{ISR}

Backgrounds



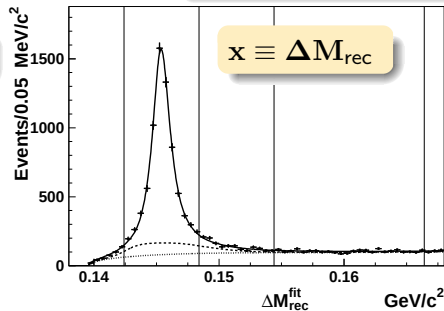
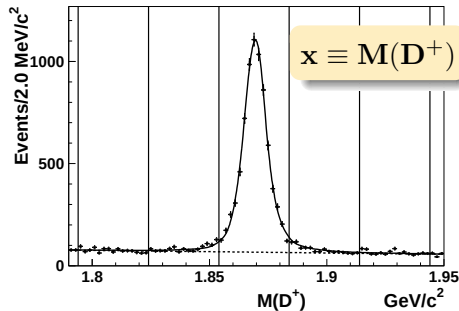
$$f = f_{\text{signal}} + f_{\text{background}}$$

$$f_{\text{background}} = \alpha \cdot \sqrt{x} \cdot (1 + \beta \cdot x + \gamma \cdot x^2)$$

$$M_{\text{bg (1)-(3)}} = 0.58 \cdot M_{\text{sb B}} + 0.53 \cdot M_{\text{sb C}} - 0.307 \cdot M_{\text{sb D}}$$

Backgrounds

$$e^+e^- \rightarrow D^+D^{*-}$$



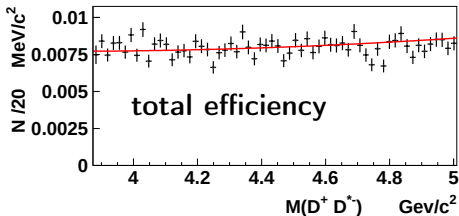
$$f = f_{\text{signal}} + f_{\text{background}}$$

$$f_{\text{background}} = \alpha \cdot \sqrt{x} \cdot (1 + \beta \cdot x + \gamma \cdot x^2)$$

$$M_{\text{bg (1)-(3)}} = 0.5 \cdot M_{\text{sb B}} + 0.5 \cdot M_{\text{sb C}} - 0.25 \cdot M_{\text{sb D}}$$

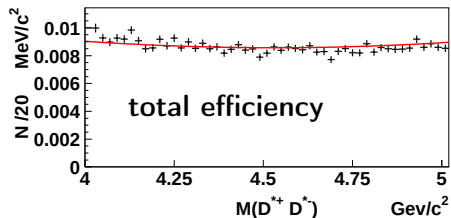
Cross sections calculation

$$e^+e^- \rightarrow D^+D^{*-}$$



$$\sigma_{e^+e^- \rightarrow D^{(*)}+D^{*-}} = \frac{dN/dM}{\eta_{\text{tot}}(M) \cdot dL/dM}$$

$$e^+e^- \rightarrow D^{*+}D^{*-}$$

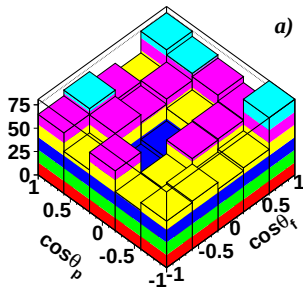


dN/dM - mass spectrum,

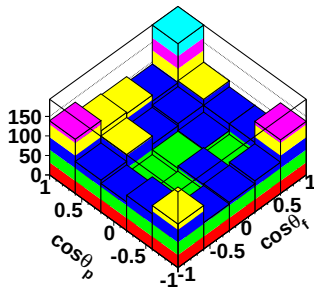
η_{tot} - total efficiency,

dL/dM - differential luminosity;

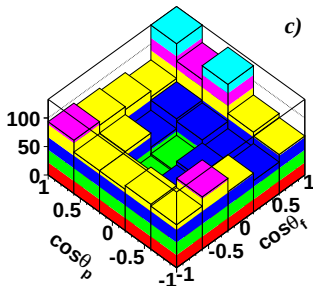
$$4.0 < M(D^{*+}D^{*-}) < 4.1 \text{ GeV}/c^2$$



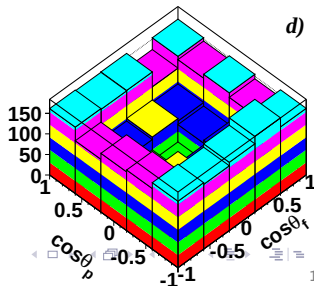
$$4.1 < M(D^{*+}D^{*-}) < 4.25 \text{ GeV}/c^2$$



$$4.25 < M(D^{*+}D^{*-}) < 4.6 \text{ GeV}/c^2$$



$$M(D^{*+}D^{*-}) > 4.6 \text{ GeV}/c^2$$



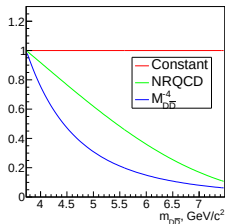
The summary of the systematic errors in the cross section calculation.

Source	$D^+ D^{*-}$	$D^{*+} D^{*-}$
Background subtraction	2%	2%
Reconstruction	3%	4%
Selection	1%	1%
Angular distribution	—	2%
Cross section calculation	1.5%	1.5%
$\mathcal{B}(D^{(*)})$	2%	3%
MC statistics	1%	2%
Total	5%	7%

Signal fit

$$S(\Phi) = \sum_{\substack{\lambda_{\text{beam}}=-1,1 \\ \lambda_{\ell\ell}=-1,1}} \left| \sum_{X^*} A_{\lambda_{\text{beam}} \lambda_{\ell\ell}}(\Phi) A_{X^*}(M_{D\bar{D}}) \right|^2, \quad (1)$$

Here, $A_{\lambda_{\text{beam}} \lambda_{\ell\ell}}(\Phi)$ is the signal amplitude calculated using the helicity formalism (the phase space Φ is 6-dimensional). For resonance, $A_{X^*} =$ relativistic Breit-Wigner. For nonresonant amplitude, $A_{X^*} = \sqrt{F_{D\bar{D}}(M_{D\bar{D}})}$, where $F_{D\bar{D}}(M_{D\bar{D}})$ is the nonresonant amplitude form factor ($F_{D\bar{D}} = 1$ by default). Alternatives: mass dependence of NRQCD prediction for $e^+e^- \rightarrow \psi\chi_c$ [PRD **77**, 014002 (2008)], $F_{D\bar{D}} = M_{D\bar{D}}^{-4}$ [Victor Chernyak, based on PLB **612**, 215 (2005)].



Signal fit results

Fit results in the default model. For the 2^{++} hypothesis, there are three solutions (fit is started 1000 times from random initial values in order to check for that).

J^{PC}	Mass, MeV/c^2	Width, MeV	Significance
0^{++}	3862^{+26}_{-32}	201^{+154}_{-67}	9.1σ
2^{++}	3879^{+20}_{-17}	171^{+129}_{-62}	8.0σ
2^{++}	3879^{+17}_{-17}	148^{+108}_{-50}	8.0σ
2^{++}	3883^{+26}_{-24}	227^{+201}_{-125}	8.0σ

Red dashed line - only background and nonresonant amplitudes, blue solid line - X^* , $J^{PC} = 0^{++}$.

