

Pinning down the linearly-polarized gluons inside unpolarized protons using J/ψ -pair production at the LHC

Florent SCARPA

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Generalities on gluon TMDs

 $\begin{array}{c} \mathrm{gg} \ \rightarrow \ \mathrm{J}/\psi + \mathrm{J}/\psi \\ \mathrm{0000000} \end{array}$

Summary O

Beyond collinear factorisation

 Observed final-state q_T generated from "intrinsic" k_T from initial partons



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▶ TMD factorisation : collinear partonic scattering amplitude factorised with k_T -dependent correlators in the cross-section for $q_T \ll Q$



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Parametrisation of the TMD correlator for an unpolarised proton :

$$\Phi_{g}^{\mu\nu}(x,\vec{k}_{T}) = -\frac{1}{2x} \left[g_{T}^{\mu\nu} f_{1}^{g}(x,\vec{k}_{T}^{2}) - \left(\frac{k_{T}^{\mu}k_{T}^{\nu}}{M_{H}^{2}} + g_{T}^{\mu\nu} \frac{\vec{k}_{T}^{2}}{2M_{H}^{2}} \right) h_{1}^{\perp g}(x,\vec{k}_{T}^{2}) \right]$$
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 \Rightarrow single helicity flip, $\cos(2\phi_{CS})$ -modulation



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+ $F_4 C[w_4 \times h_1^{\perp g} h_1^{\perp g}] \cos(4\phi_{CS})$

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modulations in $\phi_{CS} = (\vec{P}_{\psi\psi_{T}}, \vec{P}_{\psi_{T}})$

- Non-perturbative interactions of the active quark/gluon with soft spectator partons in the hadron before (Initial-State Interactions) or after (Final-State Interactions) the scattering
- These can make $h_1^{\perp g}$ process dependent and even break factorisation
- ▶ Gluon fusion : ISI can be encapsulated in the TMDs
- ► Colourless final state ⇒ no FSI : leptons/photons/Higgs or Colour-Singlet (CS) hadronisation

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TMD factorisation	$gg \rightarrow J/\psi + J/\psi$	Summary
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> LHCb JHEP 1706 (2017) 047 CMS JHEP 1409 (2014) 094 ATLAS Eur. Phys. J. C (2017) 77:76 D0 PRD 90 (2014) 111101



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- ▶ For $P_{\psi\psi_{\tau}} \leq 6 \text{ GeV}$:
 - LO contributions are dominant
 - O channels are negligible ⇒ FSI don't break TMD factorisation
- For $\Delta y \leq 2$: DPS < SPS



- 2 \rightarrow 2 processes computed in the TMD framework • $gg \rightarrow \gamma\gamma$: J.W Qiu, M. Schlegel, W. Vogelsang, PRL 107, 062001 (2011)
- $gg \rightarrow Q + \gamma$: W. den Dunnen, J.P. Lansberg, C. Pisano, M. Schlegel, PRL 112, 212001 (2014)
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Hard scattering coefficients bound :
$$F_1 \ge F_{2,3,4}$$
 (3)

▶
$$gg \rightarrow J/\psi + J/\psi$$
 limit at $M_{\psi\psi} \gg M_{\psi}$ and $\cos(\theta_{CS}) \rightarrow 0$:

$$F_{1,4} \rightarrow \frac{256\mathcal{N}}{M_{\mathcal{Q}\mathcal{Q}}^4 M_{\mathcal{Q}}^2}, \quad \frac{F_2}{F_1} \rightarrow \frac{81M_{\mathcal{Q}}^4 \cos(\theta_{CS})^2}{2M_{\mathcal{Q}\mathcal{Q}}^4}, \quad \frac{F_3}{F_1} \rightarrow \frac{-24M_{\mathcal{Q}}^2 \cos(\theta_{CS})^2}{M_{\mathcal{Q}\mathcal{Q}}^2} \quad (4)$$

 $F_4=F_1$ at large $M_{\psi\psi}\Rightarrow$ unique feature of di- J/ψ

TMD modelling : f_1^g

$$f_1^g$$
 modelled as a Gaussian in \vec{k}_T : $f_1^g(x, \vec{k}_T^2) = \frac{g(x)}{\pi \langle k_T^2 \rangle} e^{\frac{-k_T}{\langle k_T^2 \rangle}}$ (5)

 $\int d\vec{k}_T f_1^g(x, \vec{k}_T^2) = g(x) \Leftarrow \text{ the usual collinear PDF}$ (6)

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We performed the first determination of the non-perturbative parameter $\langle k_T^2 \rangle$ by fitting the analytical expression of $C[f_1^g f_1^g]$ over latest normalised LHCb's $d\sigma/dP_{\psi\psi\tau}$ data :



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- ► $F_2 \ll F_1 \Rightarrow$ only $C[f_1^g f_1^g]$ contributes to the cross-section
- No evolution so far

TMD modelling : the mysterious $h_1^{\perp g}$

• "Gaussian" $h_1^{\perp g}(x, \vec{k}_T^2) \Rightarrow \text{Model } 1$

Boer, de Dunnen, Pisano, Schlegel, Vogelsang, PRL 108 (2012) 032002

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- ▶ "Gaussian" $h_1^{\perp g}(x, \vec{k}_T^2) \Rightarrow \text{Model 1}$ Boer, de Dunnen, Pisano, Schlegel, Vogelsang, PRL 108 (2012) 032002
- ▶ Positivity bound : $h_1^{\perp g}(x, \vec{k}_T^2) \leq \frac{2M_p^2}{\vec{k}_T^2} f_1^g(x, \vec{k}_T^2) = \text{maximal value}$ (bound saturated) ⇒ Model 2 supported by low-x computations

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> In order to isolate the different ϕ -dependences, one can define :

$$\langle \cos n\phi_{CS} \rangle = \frac{\int_0^{2\pi} d\phi_{CS} \cos n\phi_{CS} d\sigma}{\int_0^{2\pi} d\phi_{CS} d\sigma} \quad n = 0, 2, 4$$
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= relative amplitude of the azimuthal modulations

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▶ $\cos 4\phi$ -modulations up to 50% !

TMD	factoris	sation
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000	00



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тM	D	factorisation	
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- ▶ $\langle \cos 4\phi_{CS} \rangle$ changes sign \Rightarrow one must be careful when integrating over the phase space
- \blacktriangleright Modulations measurable at different energies \Rightarrow possibility to study TMD evolution

- TMD factorisation = systematic method to take into account the TM of partons inside *pp* reactions
- The features of quarkonia make them good probes for the study of gluon TMD-induced effects
- $gg \rightarrow J/\psi + J/\psi$ is a promising channel to investigate :
 - LHC data already available to realise the first extraction of the gluon TMDs
 - Computations show that neither CO nor DPS contributions should complicate the extraction
 - di-J/ ψ prod. is a real gluon TMDs laboratory : magnitude, sign, k_T -dependence and evolution can be studied
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Backup slides

- ► Heavy flavours at the LHC mainly come from gluons ⇒ allows for study of gluon TMDs with low qq̄ contamination
- Their large masses allow to evaluate the partonic scattering process in perturbative QCD
- Interest in producing a pair :
 - Produced J/ψ 's can each have a large $\vec{P}_{\psi\tau}$ adding up to a small $\vec{P}_{\psi\psi\tau}$ for the pair \Rightarrow TMDs relevant for a wide range of final-state momenta
 - Hard scale $Q^2 = M_{OO}^2$ can be tuned to study TMD evolution
- CS vs. CO contributions should be analysed case by case [reactions and kinematics]

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 \blacktriangleright 2 \rightarrow 1 process :

- Resulting particle has to be at small \vec{P}_{Q_T} \Rightarrow likely difficult to measure
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• 2
$$\rightarrow$$
 2 process : $\vec{P}_{Q1_T} \simeq -\vec{P}_{Q2_T}$

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TMD classification

		Parent hadron polarisation			
		Unpolarised	Longitudinal	Transverse	
	U	$f_1(x, \vec{k}_T^2)$ (Number density)		$\begin{array}{c} f_{1T}^{\perp}(x,\vec{k}_{T}^{2}) \\ \text{(Sivers)} \end{array}$	
Parton polarisation	L		$g_1(x, \vec{k}_T^2)$ (Helicity)	$g_{1T}^{\perp}(x,ec{k}_T^2)$	
	Т	$h_1^{\perp}(x, \vec{k}_T^2)$ (Boer-Mulders)	$h_{1L}^{\perp}(x,\vec{k}_T^2)$	$ \begin{array}{c} h_1(x, \vec{k}_T^2) \\ (\text{Transversity}) \\ h_{1T}^{\perp}(x, \vec{k}_T^2) \\ (\text{Pretzelosity}) \end{array} $	

• f_1, g_1, h_1 give the standard PDFs after integration over \vec{k}_T

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Transverse weights

The transverse momentum weights are given by

$$w_{2} \equiv \frac{2(\vec{k}_{1\tau} \cdot \vec{k}_{2\tau})^{2} - \vec{k}_{1\tau}^{2} \vec{k}_{2\tau}^{2}}{4M_{p}^{4}}$$
(8)

$$w_{3} \equiv \frac{q_{\tau}^{2} \vec{k}_{2\tau}^{2} - 2(\vec{q}_{\tau} \cdot \vec{k}_{2\tau})^{2}}{2M_{p}^{2} q_{\tau}^{2}}$$
(9)

$$w_{3}' \equiv \frac{q_{\tau}^{2} \vec{k}_{1\tau}^{2} - 2(\vec{q}_{\tau} \cdot \vec{k}_{1\tau})^{2}}{2M_{p}^{2} q_{\tau}^{2}}$$
(10)

$$w_{4} \equiv 2 \left[\frac{k_{1\tau} \cdot k_{2\tau}}{2M_{p}^{2}} - \frac{(k_{1\tau} \cdot \vec{q_{\tau}})(k_{2\tau} \cdot \vec{q_{\tau}})}{M_{p}^{2}q_{\tau}^{2}} \right] - \frac{k_{1\tau}^{2}k_{2\tau}^{2}}{4M_{p}^{4}}$$
(11)

TMD factorisation	$gg \rightarrow J/\psi + J/\psi$	S
00000	000000	С

Processes of interest : 2 ightarrow 1

 $gg
ightarrow \eta_Q$ and $gg
ightarrow \chi_{Q_{0,2}}$

- Low q_T C-even quarkonium production is a good probe of h₁^{⊥g}
- Very clean action on the low q_T spectra:

$$\frac{1}{\sigma} \frac{d\sigma(\eta_Q)}{d\vec{q}_T^2} \propto 1 - R(\vec{q}_T^2) \& \frac{1}{\sigma} \frac{d\sigma(\chi_{Q,0})}{d\vec{q}_T^2} \propto 1 + R(\vec{q}_T^2)$$

$$\left(R = \frac{\mathcal{C}[w_0^{hh} h_1^{\perp g} h_1^{\perp g}]}{\mathcal{C}[f_1^g f_1^g]}\right)$$

0.8 $\sigma^{-1}d\sigma/dq_T^2$ (GeV⁻²) 0.7 χ₀ 0.6 $(h_1^{\perp g} = 0)$ Xa 0.5 η₀ ----0.4 $\langle p_T^2 \rangle = 1 \text{ GeV}^2$ 0.3 0.2 0.1 0 0 0.5 1 1.5 2 2.5 3 q_T (GeV)

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0.5 1 1.5 2 2.5 3

qT (GeV)

D. Boer, C. Pisano / Physical Review D 86, 094007 (2012)

0.7

0.1

0

 $\sigma^{-1} d\sigma / dq_T^2$ (GeV⁻²)

- Cannot tune $Q \Rightarrow Q \simeq M_Q$
- Low q_T : experimentally very difficult

[Only one η_c production study at collider , for $q_T^{\eta_c} > 6$ GeV LHCb, 1409.3612]

Higgs production

- ► Higgs production : very similar to scalar quarkonium production \Rightarrow same method to add gluon- p_T dependence for $gg \rightarrow H$ cross-section
- $\blacktriangleright \ q \bar{q} \rightarrow \mathcal{Q} \ ({\sf hadronisation}) \Rightarrow {\sf replaced} \ {\sf by} \ {\it Hqq} \ {\sf coupling}$



- Cross-section structure similar to single η_c production
- ▶ The LHC data on Higgs production give access to the value of f_1^g , $h_1^{\perp g}$ for a value of $Q \simeq M_H$

TMD factorisation	$gg \rightarrow J/\psi + J/\psi$
00000	000000

Processes of interest : $2 \rightarrow 2$



J.W Qiu, M. Schlegel, W. Vogelsang, PRL 107, 062001 (2011)

- Beside being the QCD background for H^0 studies in the $\gamma\gamma$ channel, $pp \rightarrow \gamma\gamma X$ is an interesting process to study gluon TMDs
- Only colour-singlet particles in the final state

(also true for *ZZ* and γZ)

• But contaminations from the $q\bar{q}$ channel (particularly at RHIC)





J.W Qiu, M. Schlegel, W. Vogelsang, PRL 107, 062001 (2011)

• At $\sqrt{s} = 500$ GeV, for $p_T^{\gamma} \ge 1$ GeV, $4 \le Q^2 \le 30$ GeV, $0 \le q_T \le 1$ GeV



Only F₄ (*i.e.* the cos(4φ) modulation) is purely gluonic
 Huge background from π⁰ → isolation cuts are needed.



The possibility of isolating the quarkonium eliminates the CO contributions ; the photon is isolated

IMD factorisation	$gg \rightarrow J/\psi + J/\psi$ 0000000		O
$gg ightarrow \mathcal{Q} + \gamma$		dada da	,
			- L-

- The possibility of isolating the quarkonium eliminates the CO contributions ; the photon is isolated
- Good candidate to pin down the gluon TMDs :
 - Gluon sensitive process
 - Colourless final state : TMD factorisation applicable
 - Small sensitivity to QCD corrections (most of them in the TMD evolution)

Expected rates for $\mathcal{Q} + \gamma$

W. den Dunnen, J.P. Lansberg, C. Pisano, M. Schlegel, PRL 112, 212001 (2014)

- *qq̄* contributions negligible
 CO (orange) smaller than CS (blue); isolation not needed for *Υ*
- ► At 14 TeV, $\sigma(J/\psi|\Upsilon+\gamma)|_{Q>20 \text{ GeV}}$ $\simeq 100 \text{ fb}$; about half at 7 TeV



- ▶ With the $L \simeq 20$ fb⁻¹ of *pp* data on tape, one expects up to 2000 events
- ATLAS has looked for $H^0 o J/\psi(\Upsilon) + \gamma$ at $Q\simeq 125\,{
 m GeV}$

Results with UGDs as Ansätze for TMDs

► We define
$$S_{q_{T}}^{(n)} = \frac{A^{(n)}}{A^{f}} \frac{C[w^{(n)} TMD_{1}^{(n)} TMD_{2}^{(n)}]}{\int d^{2}\vec{q}_{T}C[f_{1}^{g}f_{1}^{g}]} \Rightarrow S_{q_{T}}^{(0)}, S_{q_{T}}^{(2)}, S_{q_{T}}^{(4)}$$

S⁽⁰⁾_{q7} 0.10 0.03 0.03 0.03 ()

/ ``

Results with UGDs as Ansätze for TMDs

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S⁽²⁾_{q_T}, S⁽⁴⁾_{q_T} ≠ 0 ⇒ nonzero gluon polarisation in unpolarised protons
 S⁽⁰⁾_{q_T} : f^g₁(x, k_T) from the q_T-dependence of the yield
 ∫ d²q_TS^(2,4)_{q_T} should be measurable (few percent : ok with 2000 events)

S-(4)(GeV-2)

Same at AFTER@LHC AFTER@LHC : a fixed-target experiment using the LHC beams

•
$$\sqrt{2 \times m_N \times E_p} \stackrel{^{7TeV}}{=} 115 \text{ GeV}$$

- ▶ Experimental coverage of ALICE or LHCb is about $y_{cms} \in [-3:0]$
- $\blacktriangleright\,$ For $\psi+\gamma,$ smaller yield (14 TeV \rightarrow 115 GeV) compensated by an access to lower P_T



• At $Y_{
m (cms)}\simeq -2$, $x_2\simeq 10/115 imes e^2\simeq 0.65$. Yet, $g-g>q-ar{q}$!

- ▶ 2 → 2 process \Rightarrow Q^2, q_T tuning possible + presence of ϕ -dependent terms
- Theoretically the simplest, low qq̄ contribution, no reason for significant CO and no final state gluon needed
Summary O

$gg \rightarrow \eta_c + \eta_c$

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	$Q(GeV) \in (6.0, 10.0)$	(10.0, 15.0)	(15.0, 20.0)	(20.0, 40.0)
$\langle 1 \rangle (pb)$	2.3×10^4	$1.7 imes 10^3$	1.8×10^2	1.3×10^2
$ \langle \cos 2\phi \rangle (pb)$	2.4×10^3	$4.6 imes 10^2$	$0.72 imes 10^2$	$0.63 imes 10^2$
$\langle \cos 4\phi \rangle (pb)$	$0.20 imes 10^2$	9.1	2.5	3.3

Guang-Peng Zhang / Phys.Rev. D 90 (2014) 9, 094011. The η_c weighted differential cross-sections obtained from Gaussian model at $\sqrt{s} = 7$ TeV and $\Delta y = 0$ with $\alpha_s = 0.15$ and $M_{\eta_c} = 3.0$ GeV

► At $\sqrt{s} = 14 \text{ TeV}$, cross-sections will increase by a 2 factor ($\langle 1 \rangle \sim \sigma$) $\langle 1, \cos 2\phi \rangle \times Br^2(\eta_c \to p\bar{p}) \simeq 1 - 50 \text{ fb}$ (observable at LHC Run II ?) $\langle \cos 4\phi \rangle$ negligible

▶ However η_c remain hard to see in experiments

Pion and proton TMDs at COMPASS

- ▶ The first evidence for double J/ψ events was reported by NA3 in 1982 in π induced reactions at $p_{\text{lab}} =$ 150(280) GeV, that is $\sqrt{s} = 16.8(22.9)$ GeV NA3 J. Badier et al., PLB 114 (1982) 457.
- The J/ψ were observed in their di-muon decay channel after the absorber, just as COMPASS can look for J/ψ during the Drell-Yan run
- As of the early 80's, theoretical evaluations predicted a slight dominance of qq̄ fusion vs. gg fusion at these energies (because of the presence of a valence antiquark in the π)



R.E. Ecclestone, D.M. Scott ZPC 19 (1983) 29; B. Humpert, P. Mery PLB 124 (1982) 265

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- \blacktriangleright Significant QCD corrections were assumed (K factor \sim 5.4). These theoretical predictions have never been updated with current models and pdfs
- Based on 13 events, NA3 reported $\sigma_{\psi\psi} = 18 \pm 8$ pb at 150 GeV and $\sigma_{\psi\psi} = 30 \pm 10$ pb at 280 GeV and $\frac{\sigma_{\psi\psi}}{\sigma_{\psi}} = (3 \pm 1) \times 10^{-4}$ (no branching)
- Based on robust theoretical considerations, the feed-down from *B* decay was assumed to be negligible
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About the extraction of TMDs

- ▶ If gg fusion from CS is dominant, the results presented above should apply by just replacing the projectile proton TMDs (f_1 and $h_1^{\perp g}$) by those of the π
- ▶ If *qq* fusion dominates, the structure of the azimuthal asymetries needs to be recalculated
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Intrinsic charm coalescence ?

Since most of the events were at large rapidities, it was suggested that they could come from double intrinsic charm coalescence (i.e. not gg or qq fusion)

R. Vogt and S. J. Brodsky, PLB 349 (1995) 569

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Summary O

Gaussian $h_1^{\perp g}$ model from Boer, de Dunnen, Pisano, Schlegel, Vogelsang, PRL 108 (2012) 032002

$$h_1^{\perp g}(x, \vec{k}_T^2) = \frac{2M_p^2}{\langle k_T^2 \rangle} \frac{1-r}{r} \frac{g(x)}{\pi \langle k_T^2 \rangle} e^{1 - \frac{\vec{k}_T^2}{r \langle k_T^2 \rangle}} \quad \text{with} \quad r = 2/3$$
(12)

Gaussian+tail modelisation of TMDs

We do not know the nature of f_1^g or $h_1^{\perp g}$. We can use a Gaussian + tail model to evaluate some observables :

▶ f_1^g is written as the product of the usual integrated PDF $f_1^g(x)$ and a function of \vec{k}_T :

$$f_1^g(x, \vec{k}_T) = \frac{R^2}{2\pi} \frac{1}{1 + \vec{k}_T^2 R^2} f_1^g(x) \quad \text{with } R = 2 \,\text{GeV}^{-1}$$
(13)

▶ $h_1^{\perp g}$ knows a positivity bound : $\frac{\vec{k}_T^2}{2M_\rho^2}|h_1^{\perp g}| \leq f_1^g(x, \vec{k}_T)$. We thus take the positivity bound saturation to get a maximal effect of linearly polarised gluons :

$$|h_1^{\perp g}| \simeq \frac{2M_p^2}{\langle \vec{k}_T^2 \rangle} f_1^g(\mathbf{x}, \vec{k}_T)$$
(14)

Polarised pair production

- $\blacktriangleright~J/\psi=$ massive vector meson \Rightarrow can be longitudinally or transversely polarised
- Measuring polarisation of the produced pair = effect on the TMD extraction ?

 Polarisation is frame/axis-dependent : different frames give different crosssections



Representation of the polarisation axis in the helicity (HX), Gottfried-Jackson (GJ) and Collins-Soper (CS) frames [Faccioli_CERN_3_5_2010]