

# Charm Mixing and $CP$ Violation at B-factories

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# Outline

- *Belle @KEKB and Belle II @SuperKEKB*
  - *Accelerator; detectors; data set etc.*
- *$D^0$ - $\bar{D}^0$  mixing and CP violation*
  - *Formalism and status*
  - *Hadronic WS decay  $D^0 \rightarrow K^+ \pi^-$*
  - *Time-dependent analyses*
- *Time-integrated CP asymmetry*
  - *summary table of measurements*
  - *Search for CPV in  $D^0 \rightarrow K_S K_S$*
  - *CPV in radiative decays  $D^0 \rightarrow \gamma V$*
  - *T-odd asymmetry in  $D^0 \rightarrow K_S \pi \pi \pi^0$*
- *ROE method for  $D^0$  flavor tagging at Belle II*
- *Summary*

# Experimental Charm Data set

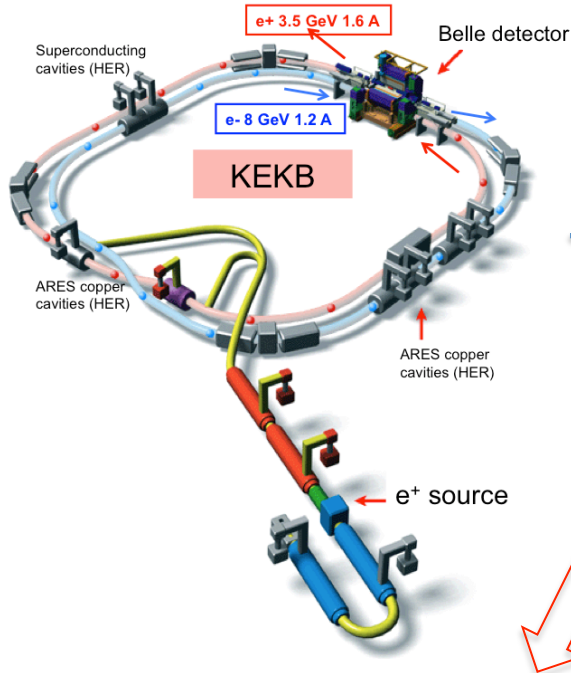
➤ Available data sets from Charm factories, B-factories and hadron colliders

Experiment	Machine	C.M	Lumin.	N(D)	efficiency	😊advantage / 😞disadvantage	
	CESR ( $e^+e^-$ )	3.77 GeV	$0.8 \text{ fb}^{-1}$	$2.9 \times 10^6$ $2.3 \times 10^6 (D^\pm)$	~10-30%	😊 extremely clean enviroment	
		4.17 GeV	$0.6 \text{ fb}^{-1}$	$0.6 \times 10^6$		😊 pure D-beam, almost no bkg	
	BEPC-II ( $e^+e^-$ )	3.77 GeV	$2.92 \text{ fb}^{-1}$	$10.5 \times 10^6$ $8.4 \times 10^6 (D^\pm)$	~10-30%	😊 quantum coherence	
		4.18 GeV	$3 \text{ fb}^{-1}$	$3 \times 10^6$		😞 no CM boost, no T-dep analyses	
						★ ★ ★ ★	
	KEKB ( $e^+e^-$ )	10.58 GeV	$1 \text{ ab}^{-1}$	$1.3 \times 10^9$	~5-10%	😊 clear event environment	
	PEP-II ( $e^+e^-$ )	10.58 GeV	$0.5 \text{ ab}^{-1}$	$6.5 \times 10^8$		😊 high trigger efficiency	
						😊 high-efficiency detection of neutrals	
						😊 many high-statistics control samples	
						😊 time-dependent analysis	
						😞 smaller cross-section than pp colliders	
	Tevatron ( $p\bar{p}$ )	1.96 TeV	$9.6 \text{ fb}^{-1}$	$1.3 \times 10^{11}$	<0.5%	😊 large production cross-section	
	LHC ( $pp$ )	7 TeV	$1.0 \text{ fb}^{-1}$	$5.0 \times 10^{12}$		😊 large boost: excellent time resolution	
		8 TeV	$2.0 \text{ fb}^{-1}$			😞 dedicated trigger required	
						😞 hard to do neutrals and neutrinos	
						★ ★ ★ ★	

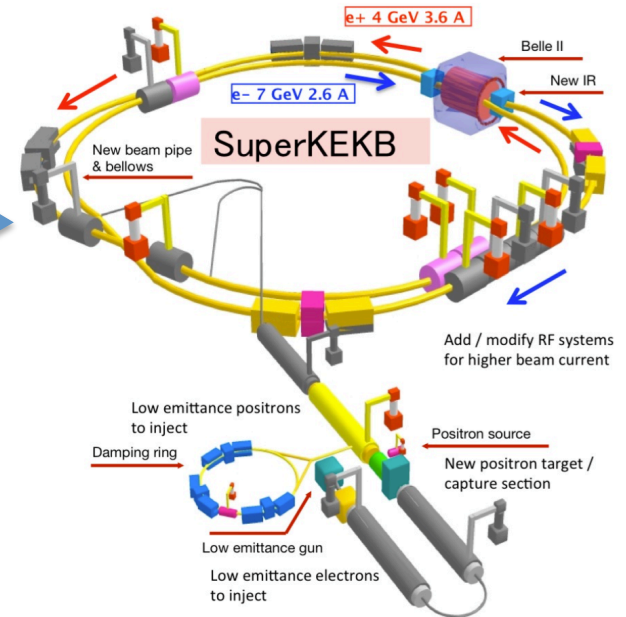
here we used  $\sigma(D^0\bar{D}^0@3.77 \text{ GeV})=3.61 \text{ nb}$ ,  $\sigma(D^+\bar{D}^-@3.77 \text{ GeV})=2.88 \text{ nb}$ ,  $\sigma(D^*\bar{D}_s@4.17 \text{ GeV})=0.967 \text{ nb}$ ,  $\sigma(c\bar{c}@10.58 \text{ GeV})=1.3 \text{ nb}$ ,  $\sigma(D^0@LHCb)=1.661 \text{ nb}$ . This table mainly refers to IJMP A 29 (2014) 24, 14300518 and G. Casarosa's report at SLAC experimental seminar 2016.

# B-factories at KEK

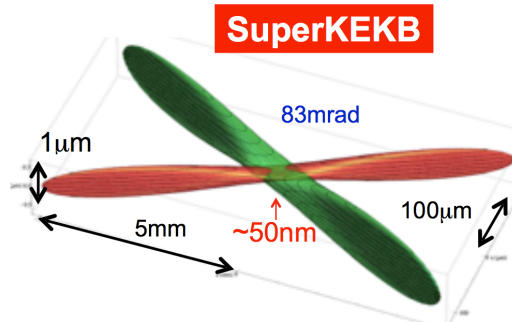
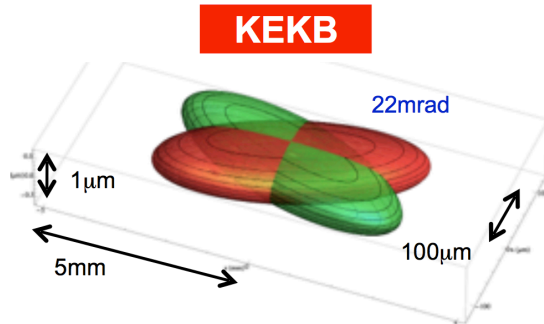
- 1<sup>st</sup> Vs. 2<sup>nd</sup> generation B-factory



**boost:**  
 $\beta\gamma \sim 2/3$   
**Current  $\times 2$**   
**IP impact par.**  
 $\beta_y^* \times 1/20$



- Nano-beam design (by P. Raimondi for SuperB)



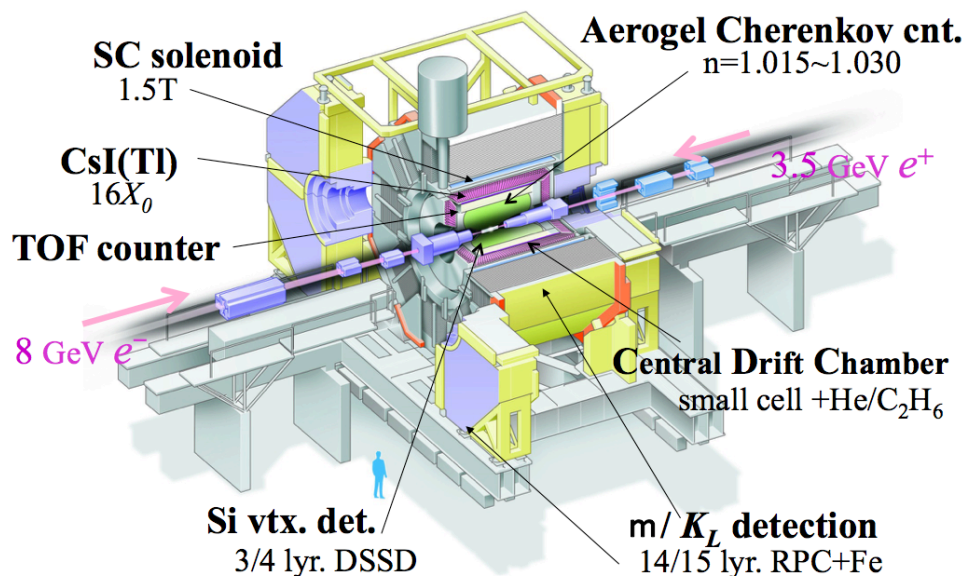
$$\mathcal{L} = \frac{\gamma_{\pm}}{2e r_e} \left( 1 + \frac{\sigma_y^*}{\sigma_x^*} \right) \frac{I_{\pm} \xi_{y\pm}}{\beta_{y\pm}^*} \left( \frac{R_L}{R_{\xi_y}} \right)$$

	Lumin. ( $\text{cm}^{-2} \text{s}^{-1}$ )
KEKB	$2.1 \times 10^{34}$
SuperKEKB	$80 \times 10^{34}$
	$\times 40$

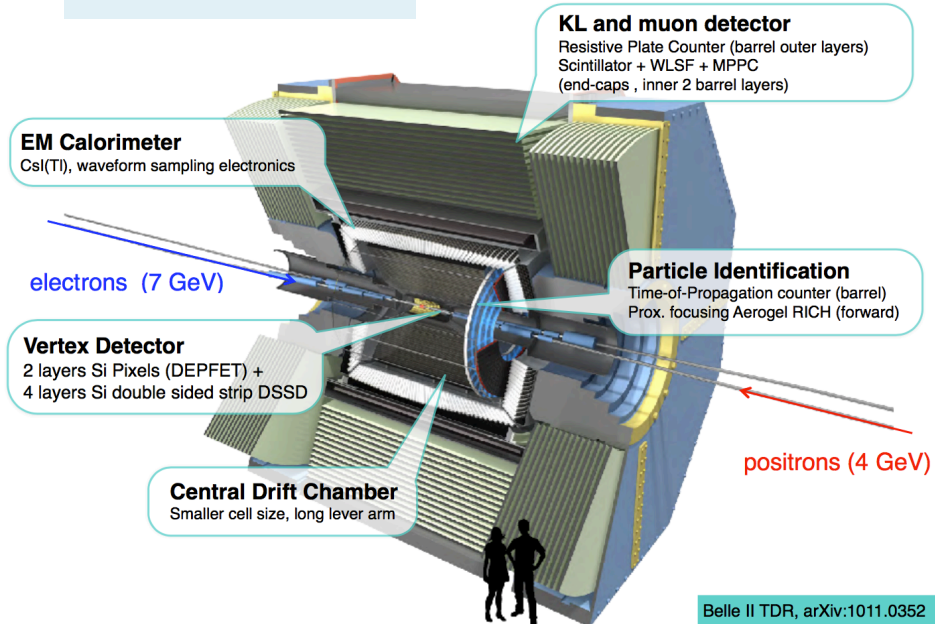


# Detectors at (Super)KEKB

## Belle detector

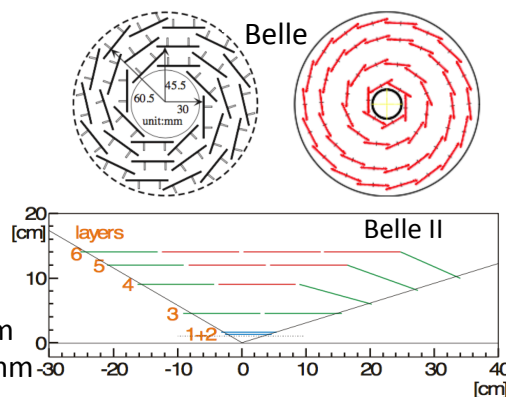


## Belle II detector

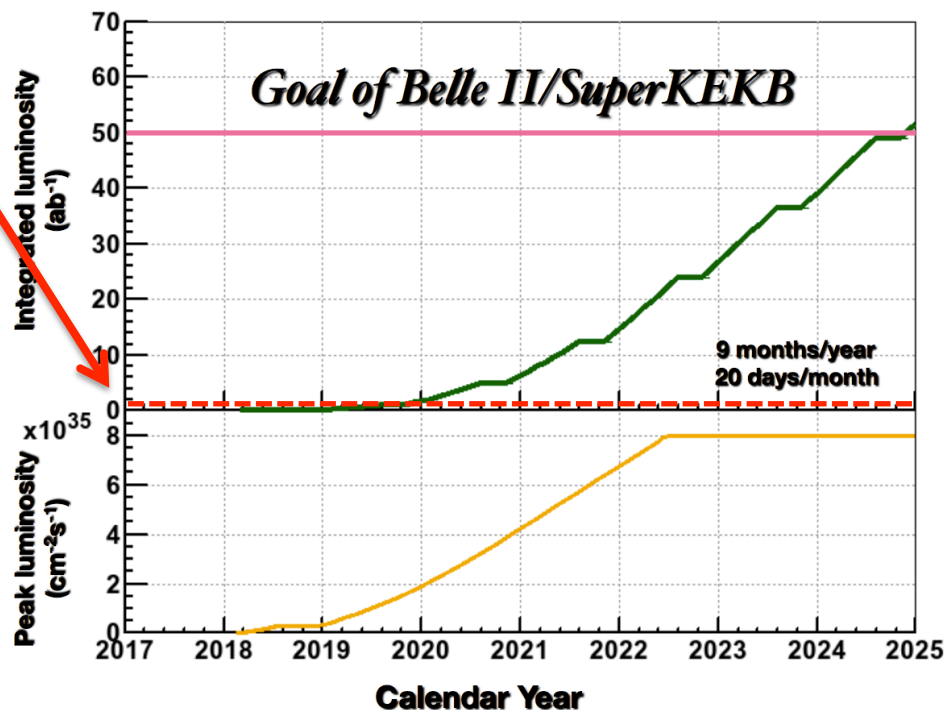
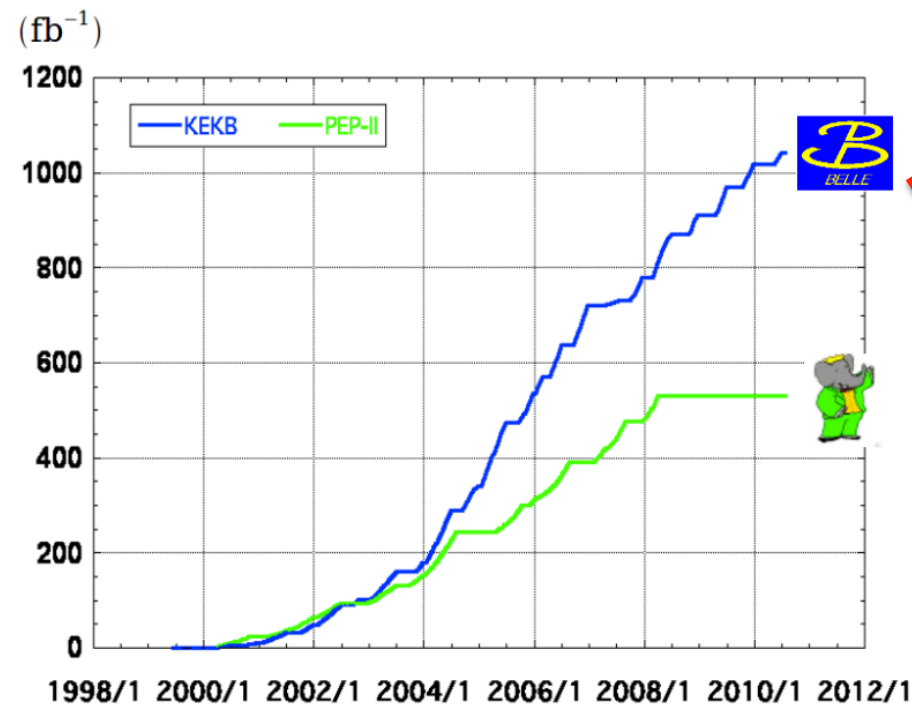


- **SVD:** 4 DSSD lyrs  $\rightarrow$  2 DEPFET lyrs + 4 DSSD lyrs
- **CDC:** *small cell, long lever arm*
- **ACC+TOF**  $\rightarrow$  *imaging "TOP"+Aerogel RICH*
- **ECL:** *waveform sampling*
- **KLM:** *RPC  $\rightarrow$  Scintillator + SiPM (end-caps)*

inner layer:  $r=20\text{ mm} \rightarrow 14\text{ mm}$   
 outer layer:  $r=88\text{ mm} \rightarrow 135\text{ mm}$



# data set at Belle and Belle II



Each 1 ab<sup>-1</sup> experimental data provides

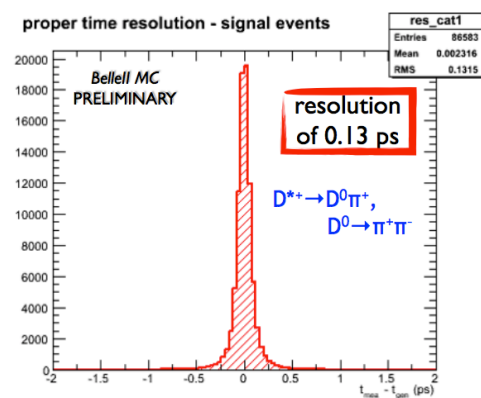
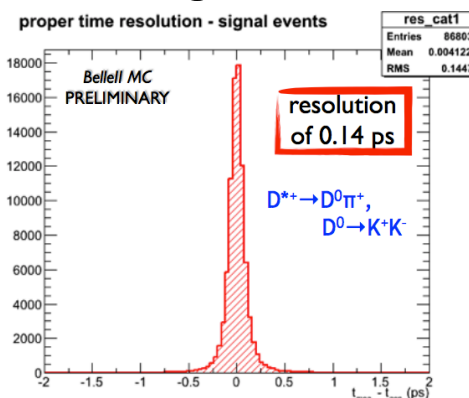
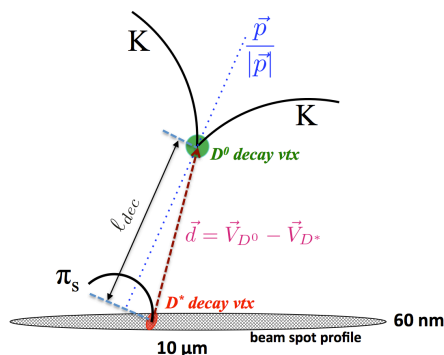
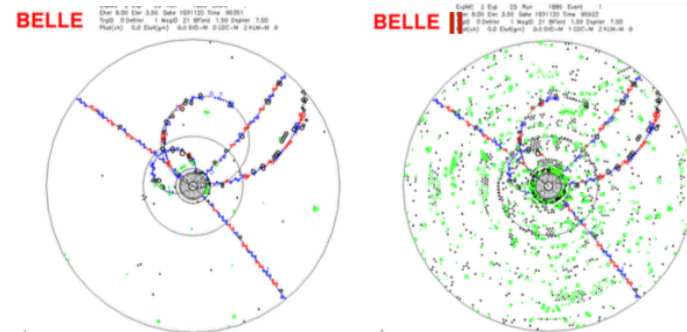
- $\sim 1.1 \times 10^9 B\bar{B} \Rightarrow$  a super **B-factory**;
- $\sim 1.3 \times 10^9 c\bar{c} \Rightarrow$  a super **charm factory**;
- $\sim 0.9 \times 10^9 \tau^+\tau^- \Rightarrow$  a super  **$\tau$  factory**;
- wide effective  $E_{c.m.}=[0.5-10]$  GeV via ISR process.

A rich platform for Charm physics

- ✓ Hadronic Modes
  - ✓ time-dependent CPV & mixing
  - ✓ time-integrated Acp
- ✓ semi-leptonic Modes
- ✓ Leptonic and Radiative Decays
- ✓ More exotic stuff (missing energy...)

# Improved performance

- Higher beam-related and QED background(x20)
- Higher event rate (x10):
  - ✓ L1 trigger: 500Hz(Belle) Vs. 30kHz(Belle II)
- Improved performance:
  - ✓ vertex resolution; tracking;
  - ✓ particle identification;
  - ✓ ...
- Important effects on Charm mixing and CPV



- ▶ Based on MC study, time **resolution = 140 fs**: **2× better** than BaBar (270 fs)
- ▶ Time error  $\sigma_t$ : factor 3 improvement; and **RMS( $\sigma_t$ ): reduced by a factor 2.**
  - $Res = Gauss(\mu, k\sigma_t)$ , so reduced RMS( $\sigma_t$ ) (higher weight in the fit) results in an increased statistics

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# Introduction to $D^0$ - $\bar{D}^0$ mixing and $CP$ violation

- Open-flavor neutral meson transforms to anti-meson:

$$K^0 \Leftrightarrow \bar{K}^0, B_d^0 \Leftrightarrow \bar{B}_d^0, B_s^0 \Leftrightarrow \bar{B}_s^0, D^0 \Leftrightarrow \bar{D}^0$$

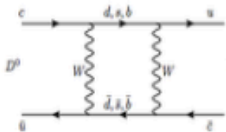
- Flavor eigenstate ( $|D^0\rangle, |\bar{D}^0\rangle$ )  $\neq$  mass eigenstate  $|D_{1,2}\rangle$  with  $M_{1,2}$  and  $\Gamma_{1,2}$

$$|D_{1,2}\rangle \equiv p|D^0\rangle \pm q|\bar{D}^0\rangle \quad (\text{CPT: } p^2 + q^2 = 1)$$

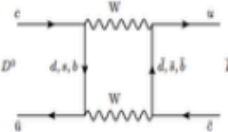
- Mixing parameters:  $\mathbf{x} \equiv 2 \frac{M_1 - M_2}{\Gamma_1 + \Gamma_2}, \quad \mathbf{y} \equiv \frac{\Gamma_1 - \Gamma_2}{\Gamma_1 + \Gamma_2}$

- Unique system: only up-type meson for mixing

- Standard Model(SM) predicts:  $\sim \mathcal{O}(1\%)$



(1) short distance ( $< 0.1\%$ )



(2) long distance ( $\sim 1\%$ )

- Precise measurement of  $x, y$ : effectively limit the New Physics(NP) modes; and search for NP, eg:  $|x| \gg |y|$

- Three types of **C**harged-conjugated-**P**arity combined symmetry **V**iolation (**CPV**):

$$A_{CP}^f = \frac{\Gamma(D \rightarrow f) - \Gamma(\bar{D} \rightarrow \bar{f})}{\Gamma(D \rightarrow f) + \Gamma(\bar{D} \rightarrow \bar{f})} = a_d^f + a_m^f + a_i^f$$

- $a_d^f$ : (direct CPV) CPV in decay  $|\bar{A}_{\bar{f}}/A_f| \neq 1$

$$\left| \begin{array}{c} p^0 \\ \text{---} \end{array} \right. \text{---} \text{---} \left. \begin{array}{c} f \end{array} \right| \neq \left| \begin{array}{c} \bar{p}^0 \\ \text{---} \end{array} \right. \text{---} \text{---} \left. \begin{array}{c} \bar{f} \end{array} \right|$$

- $a_m^f$ : CPV in mixing with  $r_m = |q/p| \neq 1$

$$\left| \begin{array}{c} p^0 \quad \bar{p}^0 \\ \text{---} \end{array} \right. \text{---} \text{---} \left. \begin{array}{c} \bar{f} \end{array} \right| \neq \left| \begin{array}{c} \bar{p}^0 \quad p^0 \\ \text{---} \end{array} \right. \text{---} \text{---} \left. \begin{array}{c} f \end{array} \right|$$







- $a_i^f$ : CPV in interference with  $\arg(q/p) \neq 0$

$$\left| \begin{array}{c} p^0 \\ \text{---} \end{array} \right. \text{---} \text{---} \left. \begin{array}{c} f \end{array} \right| + \left| \begin{array}{c} \bar{p}^0 \\ \text{---} \end{array} \right. \text{---} \text{---} \left. \begin{array}{c} f \end{array} \right| \neq \left| \begin{array}{c} \bar{p}^0 \\ \text{---} \end{array} \right. \text{---} \text{---} \left. \begin{array}{c} f \end{array} \right| + \left| \begin{array}{c} p^0 \\ \text{---} \end{array} \right. \text{---} \text{---} \left. \begin{array}{c} f \end{array} \right|$$

- SM with only a source: the phase in CKM
- in charm sector, it's predicted at  $\sim \mathcal{O}(10^{-3})$
- $\sim 1\%$  exp. sensitivity to observe CPV $\rightarrow$ NP

# measurements of $D^0$ - $\bar{D}^0$ mixing and CPV

➤ summary table Mainly basing on HFLAV group

Decay Type	Final State						
DCS 2-body(WS)	$K^+\pi^-$	★	☆	★ <sup>(a)</sup>	★	✓	✓ <sub><math>\delta K\pi</math></sub>
DCS 3-body(WS)	$K^+\pi^-\pi^0$	○ <sup>(c)</sup>	☆			✓ <sub><math>A_{CP}</math></sub>	○ <sub><math>\delta RS</math></sub>
CP-eigenstate	(even) $h^+h^-$	☆	☆	☆ <sup>(b)</sup> <sub><math>A_{CP}</math></sub>	✓ <sub><math>A_{CP}</math></sub>	✓	
	(odd) $K_S^0\phi$	✓					
Self-conj. 3-body decay	$K_S^0\pi^+\pi^-$	✓	✓	✓	✓ <sub><math>A_{CP}</math></sub>	✓	○ <sub><math>\delta</math></sub>
	$K_S^0K^+K^-$	○	✓	○			○ <sub><math>\delta</math></sub>
	$K_S^0\pi^0\pi^0$					✓ <sub>Dalitz</sub>	○ <sub><math>y_{CP}</math></sub>
Self-conj. SCS 3-body decay	$\pi^+\pi^-\pi^0$	✓ <sub><math>A_{CP}</math></sub>	✓ <sub>mixing</sub> <sub><math>A_{CP}</math></sub>	✓ <sub><math>A_{CP}</math></sub>			○ <sub><math>\delta</math></sub>
	$K^+K^-\pi^0$		✓ <sub><math>A_{CP}</math></sub>				○ <sub><math>\delta</math></sub>
SCS 3-body	$K_S^0K^\pm\pi^\mp$			✓ <sub><math>A_{CP}</math></sub>		✓ <sub><math>\delta</math></sub>	○ <sub><math>\delta</math></sub>
Semileptonic decay	$K^+\ell^-\nu_\ell$	✓	✓			✓	
Multi-body( $n\geq 4$ )	$K^+\pi^-\pi^+\pi^-$	✓ <sub><math>R_{WS}</math></sub>	✓	★			○ <sub><math>\delta RS</math></sub>
	$\pi^+\pi^-\pi^+\pi^-$	○ <sub><math>A_{CP}</math></sub>		✓ <sup>(d)</sup> <sub><math>A_{CP}</math></sub>			
	$K^+K^-\pi^+\pi^-$	○ <sub><math>A_T</math></sub>	✓ <sub><math>A_T</math></sub>	✓ <sup>(e)</sup> <sub><math>A_{CP}</math></sub>		✓ <sub><math>A_{CP}</math></sub>	○
	$K_S^0\pi^+\pi^-\pi^0$	✓ <sub><math>A_T</math></sub>					
$\psi(3770) \rightarrow D^0\bar{D}^0$ via correlations						✓ <sub><math>\delta K\pi</math></sub>	✓ <sub><math>y_{CP}</math></sub>

In  $D^0$ - $\bar{D}^0$  mixing measurements: ★ for observation ( $> 5\sigma$ ); ☆ for evidence ( $> 3\sigma$ ); ✓ for measurement published; ○ for analysis on going.  $A_T$  stands for measuring CP asymmetry using T-odd correlations.

(a) LHCb gave the measurement of charm mixing and CP violation in  $D^0 \rightarrow K^\pm h^\mp$  decay in PRD **95**, 052004 (2017).

(b) LHCb gave the measurements of CP violation in  $D^0 \rightarrow h^- h^+$  decay in PRL **112**, 041801 (2014) and PRL **118**, 261803 (2017).

(c) Belle measured WS-to-RS ratio  $R_{WS}$  and  $A_{CP}$  in  $D^0 \rightarrow K^\mp \pi^\pm \pi^0$  in PRL **95**, 231801 (2005).

(d) LHCb also searched for CP violation in phase space of  $D^0 \rightarrow \pi^+\pi^-\pi^+\pi^-$  decays in PLB **769**(2017) 345.

(e) LHCb also searched for CP violation using T-odd correlations in  $D^0 \rightarrow K^+K^-\pi^+\pi^-$  decays in JHEP **10**(2014)005.

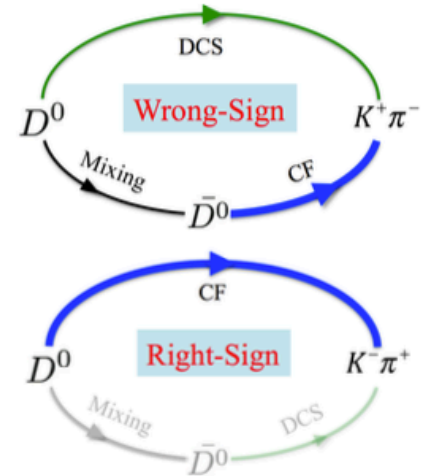
# Hadronic WS decay for mixing & CPV

- Wrong-sign(WS) decay rates with  $D^0$ - $\bar{D}^0$  mixing or CPV-allowed:

$$\frac{N(D^0 \rightarrow f)}{dt} = e^{-\Gamma t} \left[ R_D + \left| \frac{q}{p} \right| \sqrt{R_D} (y' \cos \phi - x' \sin \phi) (\Gamma t) + \left| \frac{q}{p} \right|^2 \frac{(x'^2 + y'^2)}{4} (\Gamma t)^2 \right]$$

$$\frac{N(D^0 \rightarrow f)}{dt} = e^{-\Gamma t} \left[ R_D + \sqrt{R_D} y' (\Gamma t) + \frac{(x'^2 + y'^2)}{4} (\Gamma t)^2 \right] \quad (\text{no CPV})$$

where  $x' = x \cos \delta + y \sin \delta$ ,  $y' = y \cos \delta - x \sin \delta$  with strong phase difference  $\delta$



**first evidence** for  $D^0$ - $\bar{D}^0$  mixing

[B. Aubert et al. PRL 98, 211802 (2007)]



**first observation** in  $e^+e^-$  collisions

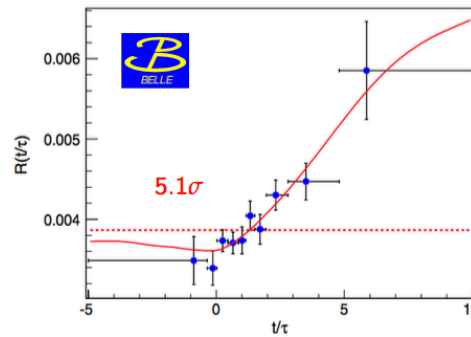
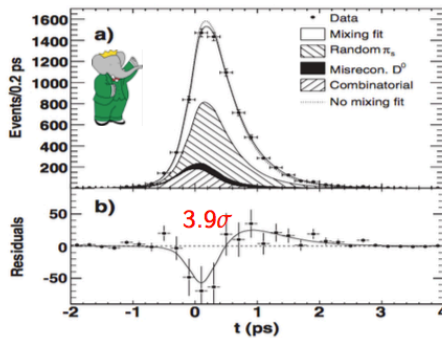
[B.R. Ko et al. PRL 112, 111801 (2014)]

- fitting  $D^0$  proper time distribution of WS sample ( $384 \text{ fb}^{-1}$ )

$$\frac{T_{WS}(t)}{e^{-\Gamma t}} \propto R_D + \sqrt{R_D} y' \Gamma t + \frac{x'^2 + y'^2}{4} (\Gamma t)^2$$

- fitting time-dependent ratio of WS-to-RS decay ( $976 \text{ fb}^{-1}$ )

$$R_{WS}(t) = \frac{\Gamma_{WS}(t)}{\Gamma_{RS}(t)} \approx R_D + \sqrt{R_D} y' \Gamma t + \frac{x'^2 + y'^2}{4} (\Gamma t)^2$$



Parameter		Belle 976 /fb	5 /ab	Belle II 20 /ab	50 /ab
no CPV	$\sigma(x'^2)(10^{-5})$	22	7.5	3.7	2.3
	$\sigma(y')(\%)$	0.34	0.11	0.056	0.035
CPV-allowed	$\sigma(x')(\%)$		0.37	0.23	0.15
	$\sigma(y')(\%)$		0.26	0.17	0.10
	$\sigma( q/p )$		0.197	0.089	0.051
	$\sigma(\phi)(^\circ)$		15.5	9.2	5.7

One order magnitude improvement at Belle II

# Time-dept. analyses for mixing and CPV

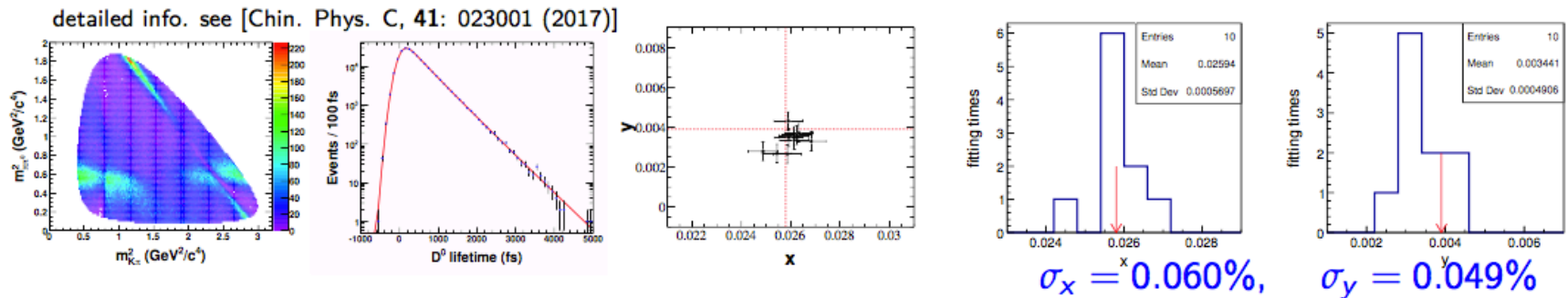
- ▶ Time-dependent Dalitz plot(TDDP) provides an essential tool in studying  $D^0-\bar{D}^0$  mixing.
- ▶ Only method: sensitive to **linear order in both mixing parameters**, especially self-conjugated decays like  $K_S^0 hh$  (not rotated by an unknown  $\delta$ )

- ▶ TDDP fit on  $D^0 \rightarrow K^+ \pi^- \pi^0$  WS decays to extract mixing par.  $(x''/r_0, y''/r_0)$

$$|A_{\bar{f}}|^2 = \left[ |A_{\bar{f}}^{DCS}|^2 e^{-\Gamma t} + \frac{(x'' + y'')^2}{4r_0^2} |\bar{A}_{\bar{f}}^{CF}|^2 (\Gamma t)^2 e^{-\Gamma t} + \left( \frac{y''}{r_0} \text{Re}[\bar{A}_{\bar{f}}^{DCS} \bar{A}_{\bar{f}}^{*CF}] + \frac{x''}{r_0} \text{Im}[\bar{A}_{\bar{f}}^{DCS} \bar{A}_{\bar{f}}^{*CF}] \right) (\Gamma t) e^{-\Gamma t} \right] \otimes_t \text{Res}(t)$$

$$x'' = x \cos \delta_{K\rho} + y \sin \delta_{K\rho}, \quad y'' = y \cos \delta_{K\rho} - x \sin \delta_{K\rho}, \quad r_0 = |A^{CF}|/|A^{DCS}|$$

- ▶ BaBar: the evidence ( $3.2\sigma$ ) with  $384 \text{ fb}^{-1}$ :  $\sigma(x'', y'') = (+0.57, +0.55)_{(-0.68, -0.64)}\%$  [PRL 103, 211801 (2009)]
- ▶ ToyMC: smear lifetime with Gauss( $\sigma=140$  fs); without considering bkg effects.
- ▶ Sensitivity estimation: **one order of magnitude improvement than BaBar**



- ▶ More t-dept. measurements, like  $D^0 \rightarrow K^+ K^-, \pi^+ \pi^-, D^0 \rightarrow K_S^0 \pi^+ \pi^-$  etc. in backup.  
( $y_{CP}, A_{\Gamma}$ ) ( $x, y, |q/p|, \phi$ )



# Time-dept. analyses for mixing and CPV

[L.M. Zhang et al. PRL 99, 131803 \(2007\)](#)

[T. Peng et al. PRD 89, 091103\(R\) \(2014\)](#)

- TDDA in self-conjugated decays:

(1) direct measurement for  $x$  and  $y$ ; (2) search for CPV:  $q/p \neq 1$

- $D^0 \rightarrow K_S^0 \pi^+ \pi^-$  with quasi-two-body decays with difference physics process:

RS:  $\mathcal{A}_f = \langle f | \mathcal{H} | D^0 \rangle$ ;  $\frac{q}{p} \frac{\bar{\mathcal{A}}_f}{\mathcal{A}_f} = \left| \frac{\bar{\mathcal{A}}_f}{\mathcal{A}_f} \right| \frac{1-\epsilon}{1+\epsilon} e^{i(\delta+\phi)}$ ; eg:  $D^0 \rightarrow K^{*-} \pi^+$  etc.

WS:  $\mathcal{A}_{\bar{f}} = \langle \bar{f} | \mathcal{H} | D^0 \rangle$ ;  $\frac{q}{p} \frac{\bar{\mathcal{A}}_{\bar{f}}}{\mathcal{A}_{\bar{f}}} = \left| \frac{\bar{\mathcal{A}}_{\bar{f}}}{\mathcal{A}_{\bar{f}}} \right| \frac{1-\epsilon}{1+\epsilon} e^{-i(\delta-\phi)}$ ; eg:  $D^0 \rightarrow K^{*+} \pi^-$  etc.

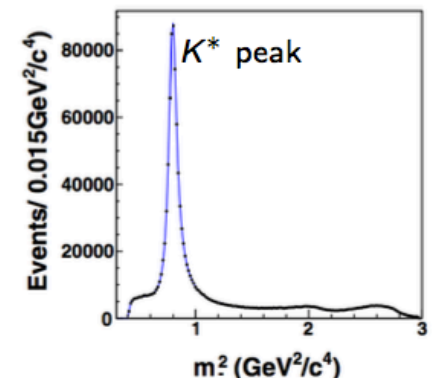
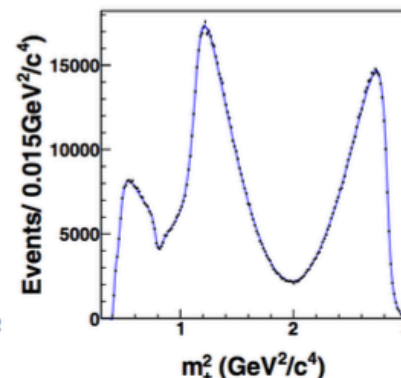
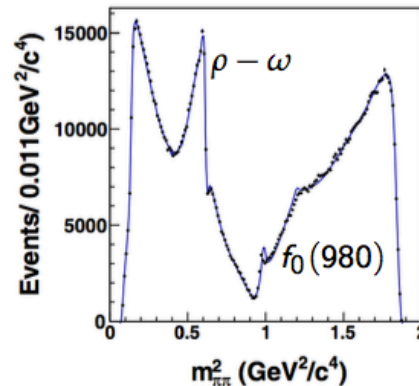
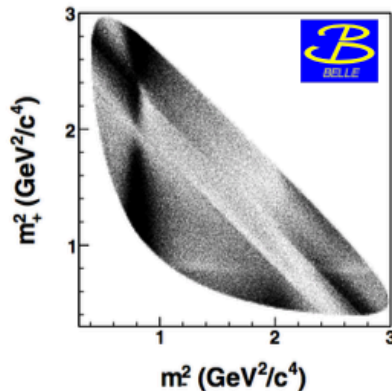
CP:  $\mathcal{A}_+ = \langle + | \mathcal{H} | D^0 \rangle$   $\frac{q}{p} \frac{\bar{\mathcal{A}}_+}{\mathcal{A}_+} = + \frac{1-\epsilon}{1+\epsilon} e^{+i\phi}$ ; eg:  $D^0 \rightarrow K_S^0 f_0$  etc.

CP:  $\mathcal{A}_- = \langle - | \mathcal{H} | D^0 \rangle$   $\frac{q}{p} \frac{\bar{\mathcal{A}}_-}{\mathcal{A}_-} = - \frac{1-\epsilon}{1+\epsilon} e^{-i\phi}$ ; eg:  $D^0 \rightarrow K_S^0 \rho / K_S^0 \omega$  etc.



- DP Model with Isobar: 12 BW+K-matrix( $\pi\pi$  S-wave)+LASS( $K\pi$  S-wave)

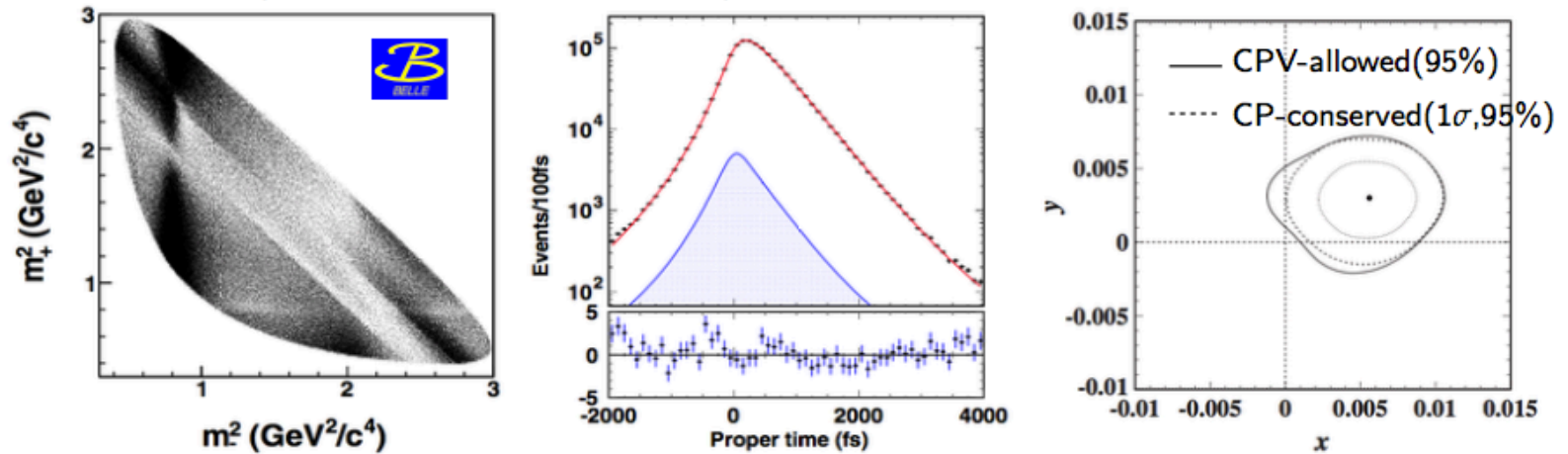
- DP  $m_-^2 = m_{K_S^0 \pi^-}^2$ ,  $m_+^2 = m_{K_S^0 \pi^+}^2$  for  $D^0$ , exchange for  $\bar{D}^0$ .



# Time-dept. analyses for mixing and CPV

- Time-dependent DP fit on  $(m_-^2, m_+^2, t)$  to extract  $(x, y)$  and  $(|q/p|, \arg(q/p))$

$$|\mathcal{M}(f, t)|^2 = \frac{e^{-\Gamma t}}{2} [ (|\mathcal{A}_f|^2 + |\frac{q}{p}|^2 |\mathcal{A}_{\bar{f}}|^2) \cosh(y\Gamma t) + (|\mathcal{A}_f|^2 - |\frac{q}{p}|^2 |\mathcal{A}_{\bar{f}}|^2) \cos(x\Gamma t) \\ + 2 \operatorname{Re}[\frac{q}{p} \mathcal{A}_{\bar{f}} \mathcal{A}_f^*] \sinh(y\Gamma t) + 2 \operatorname{Im}[\frac{q}{p} \mathcal{A}_{\bar{f}} \mathcal{A}_f^*] \sin(x\Gamma t) ]$$



- fit results and prospect estimation:

Fit type	Para.	Belle Fit result	Belle II prospect		model-indept.	LHCb
		921 fb <sup>-1</sup>	5 ab <sup>-1</sup>	50 ab <sup>-1</sup>	100 M signals	50 fb <sup>-1</sup>
No CPV	x(%)	0.56 ± 0.19 <sup>+0.03+0.06</sup> <sub>-0.09-0.09</sub>	±0.08 ± 0.11	±0.03 ± 0.11	±0.017	
	y(%)	0.30 ± 0.15 <sup>+0.04+0.03</sup> <sub>-0.05-0.06</sub>	±0.06 ± 0.05	±0.02 ± 0.04	±0.019	
indirect	x(%)	0.56 ± 0.19 <sup>+0.04+0.06</sup> <sub>-0.08-0.08</sub>	±0.08 ± 0.11	±0.03 ± 0.11		0.04
	y(%)	0.30 ± 0.15 <sup>+0.04+0.03</sup> <sub>-0.05-0.07</sub>	±0.06 ± 0.05	±0.02 ± 0.04		0.004
CPV	q/p	0.90 <sup>+0.16+0.05+0.06</sup> <sub>-0.15-0.04-0.05</sub>	±0.069 ± 0.073	±0.022 ± 0.069		0.04
	arg(q/p)(°)	-6 ± 11 ± 3 <sup>+3</sup> <sub>-4</sub>	±4.7 ± 4.2	±1.5 ± 3.8		3

# Outline

- *Belle @KEKB and Belle II @SuperKEKB*
  - *Accelerator; detectors; dataset etc.*
- *$D^0$ - $\bar{D}^0$  mixing and CP violation*
  - *Formalism and status*
  - *Hadronic WS decay  $D^0 \rightarrow K^+ \pi^-$*
  - *Time-dependent analyses*
- ***Time-integrated CP asymmetry***
  - *summary table of measurements*
  - *Search for CPV in  $D^0 \rightarrow K_S K_S$*
  - *CPV in radiative decays  $D^0 \rightarrow \gamma V$*
  - *T-odd asymmetry in  $D^0 \rightarrow K_S \pi \pi \pi^0$*
- *ROE method for  $D^0$  flavor tagging at Belle II*
- *Summary*

# Time-integrated $CP$ asymmetry measurement

- Time-integrated  $CP$  asymmetries are measured based on partial decay rates:

$$A_{CP}^f = \frac{\Gamma(D \rightarrow f) - \Gamma(\bar{D} \rightarrow \bar{f})}{\Gamma(D \rightarrow f) + \Gamma(\bar{D} \rightarrow \bar{f})} = a_d^f + a_{ind}^f \quad \text{e.g.: in } D^0 \rightarrow K_S^0 h^+, \text{ measured asym.: } A_{raw} = A_{CP} + A_{FB} + A_{\epsilon}^{h^+} + A_{CP}^{K^0}$$

- Several measurements are performed at Belle

Channel	$\mathcal{L}(\text{fb})$	Current measurement value(%)	References	Belle II 50 $\text{ab}^{-1}$ (%)	LHCb 50 $\text{fb}^{-1}$ (%)
$D^0 \rightarrow \pi^+ \pi^-$	976	$+0.55 \pm 0.36 \pm 0.09$	PoS ICHEP2012 (2013) 353	$\pm 0.05$	$\pm 0.03$
$D^0 \rightarrow K^+ K^-$	976	$-0.32 \pm 0.21 \pm 0.09$	PoS ICHEP2012 (2013) 353	$\pm 0.03$	$\pm 0.03$
$D^0 \rightarrow \pi^0 \pi^0$	966	$-0.03 \pm 0.64 \pm 0.10$	PRL 112, 211601 (2014)	$\pm 0.09$	
$D^0 \rightarrow K_S^0 K_S^0$	921	$-0.02 \pm 1.53 \pm 0.17$	PRL 119, 171801 (2017)	$\pm 0.20$	
$D^0 \rightarrow K_S^0 \pi^0$	966	$-0.21 \pm 0.16 \pm 0.07$	PRL 112, 211601 (2014)	$\pm 0.03$	
$D^0 \rightarrow K_S^0 \eta$	791	$+0.54 \pm 0.51 \pm 0.16$	PRL 106, 211801 (2011)	$\pm 0.07$	
$D^0 \rightarrow K_S^0 \eta'$	791	$+0.98 \pm 0.67 \pm 0.14$	PRL 106, 211801 (2011)	$\pm 0.09$	
$D^0 \rightarrow \pi^+ \pi^- \pi^0$	532	$+0.43 \pm 0.41 \pm 1.23$	PLB 662, 102 (2008)	$\pm 0.13$	
$D^0 \rightarrow K^+ \pi^- \pi^0$	281	$-0.60 \pm 5.30$	PRL 95, 231801 (2005)	$\pm 0.40$	
$D^0 \rightarrow K^+ \pi^- \pi^+ \pi^-$	281	$+0.43 \pm 1.30$	PRL 95, 231801 (2005)	$\pm 0.33$	
$D^+ \rightarrow \pi^0 \pi^+$	921	$+2.31 \pm 1.24 \pm 0.23$	Belle Preliminary	$\pm 0.40$	
$D^+ \rightarrow \phi \pi^+$	955	$+0.51 \pm 0.28 \pm 0.05$	PRL 108, 071801 (2012)	$\pm 0.04$	
$D^+ \rightarrow \eta \pi^+$	791	$+1.74 \pm 1.13 \pm 0.19$	PRL 107, 221801 (2011)	$\pm 0.14$	$\pm 0.01$
$D^+ \rightarrow \eta' \pi^+$	791	$-0.12 \pm 1.12 \pm 0.17$	PRL 107, 221801 (2011)	$\pm 0.14$	
$D^+ \rightarrow K_S^0 \pi^+$	977	$-0.363 \pm 0.094 \pm 0.067 (3.2\sigma)$	PRL 109, 021601 (2012)	$\pm 0.03$	$\pm 0.03$
$D^+ \rightarrow K_S^0 K^+$	977	$-0.25 \pm 0.28 \pm 0.14$	JHEP 02 (2013) 098	$\pm 0.05$	
$D_s^+ \rightarrow K_S^0 \pi^+$	673	$+5.45 \pm 2.50 \pm 0.33$	PRL 104, 181602 (2010)	$\pm 0.29$	$\pm 0.03$
$D_s^+ \rightarrow K_S^0 K^+$	673	$+0.12 \pm 0.36 \pm 0.22$	PRL 104, 181602 (2010)	$\pm 0.05$	

- Belle II:** precision of  $\mathcal{O}(0.01\%)$  (down to SM level).  $\sigma_{Belle II} = \sqrt{(\sigma_{stat}^2 + \sigma_{syst}^2) \cdot (\mathcal{L}_{Belle}/50 \text{ ab}^{-1}) + \sigma_{irred}^2}$
- With respect to LHCb, Belle II has advantages of excellent  $\gamma$  and  $\pi^0$  reconstruction.



# Search for CPV in $D^0 \rightarrow K_S^0 K_S^0$

[PRL 119, 171801 \(2017\)](#)

- The measured raw asymmetry:

$$A_{\text{raw}} = \frac{N(D^0) - N(\bar{D}^0)}{N(D^0) + N(\bar{D}^0)} = A_{CP} + A_{FB} + A_{\epsilon}^{\pm} + A_{\epsilon}^K$$

- Choose normalization mode:  $D^0 \rightarrow K_S^0 \pi^0$ :

$$A_{CP}(D^0 \rightarrow K_S^0 K_S^0) = A_{\text{raw}}(D^0 \rightarrow K_S^0 K_S^0) - A_{\text{raw}}(D^0 \rightarrow K_S^0 \pi^0) \\ + A_{CP}(D^0 \rightarrow K_S^0 \pi^0) + A_{\epsilon}^K,$$

$$\frac{\mathcal{B}(D^0 \rightarrow K_S^0 K_S^0)}{\mathcal{B}(D^0 \rightarrow K_S^0 \pi^0)} = \frac{(N/\epsilon)_{D^0 \rightarrow K_S^0 K_S^0}}{(N/\epsilon)_{D^0 \rightarrow K_S^0 \pi^0}}$$

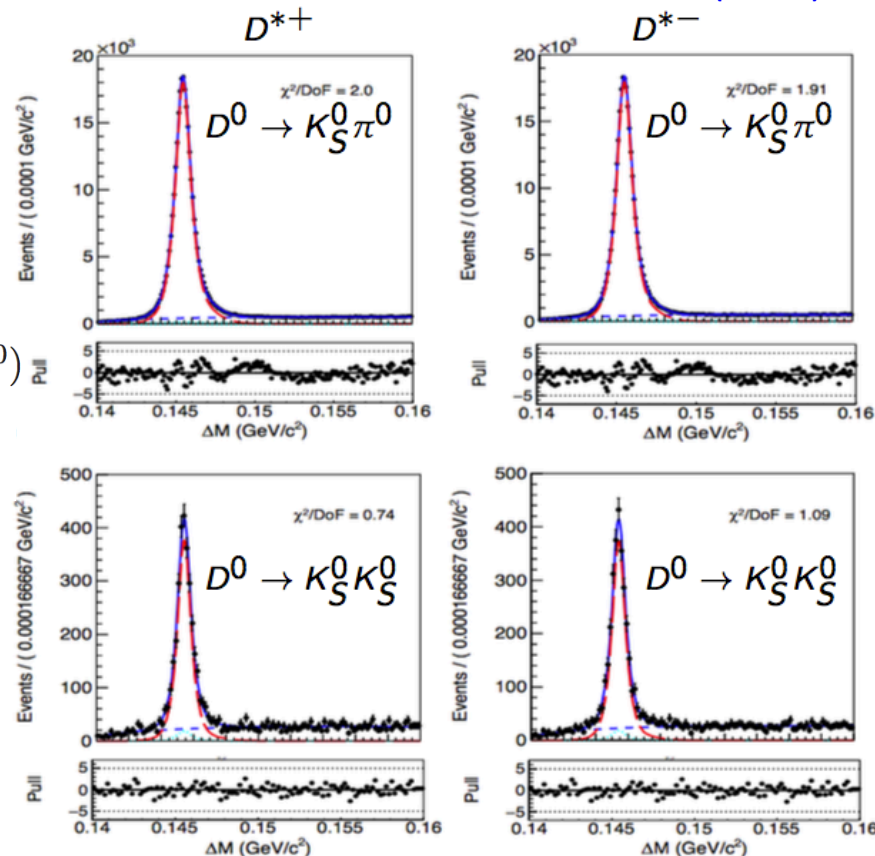
- most precise measurement on both  $A_{CP}$  and BR for  $D^0 \rightarrow K_S K_S$  mode:

$$A_{CP} = (-0.02 \pm 1.53 \pm 0.02 \pm 0.07)\%$$

$$\text{BR} = (1.32 \pm 0.02 \pm 0.04 \pm 0.04) \times 10^{-4}$$

- $A_{CP}$ : consistent with SM expectation (improved to LHCb in 2015:  $(-2.9 \pm 5.2 \pm 2.2)\%$ )
- BR: consistent with PDG:  $(1.8 \pm 0.4) \times 10^{-4}$ , but  $2.3\sigma$  away from BESIII result  $(1.67 \pm 0.11 \pm 0.11) \times 10^{-4}$  [PLB **765** (2017) 231]

- $A_{CP}$  uncertainty dominated by stat. error → Prospect at Belle II: expect a precision of 0.2%

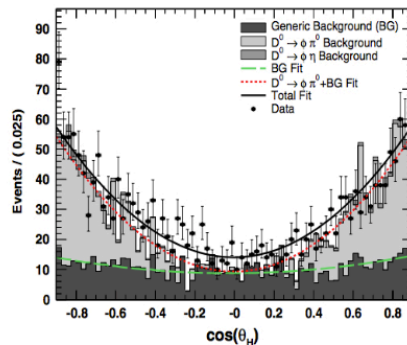
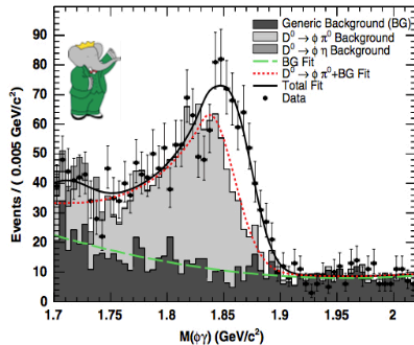


# CPV in $D^0$ radiative decays

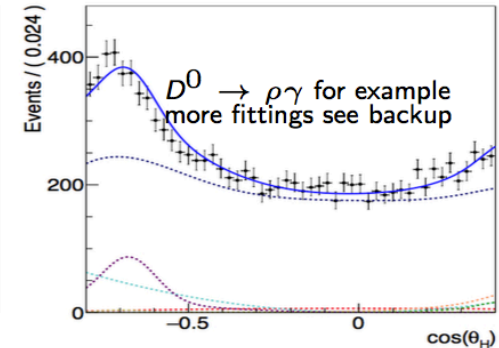
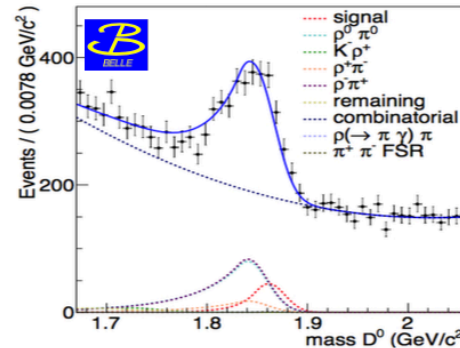
## ➤ branch ratio measurement in $D^0 \rightarrow \gamma V$

- dominated by long-range contribution ( $10^{-5}$ , whereas short-range  $10^{-8}$ )
- Belle gave first observation of  $D^0 \rightarrow \phi \gamma$  with 78.1/fb data [O. Tajima et al. PRL 92,101803 (2004)]
- BABAR give first observation of  $D^0 \rightarrow \bar{K}^{*0} \gamma$  with 387.1/fb data [B. Aubert et al., PRD78,071101(R) (2008)]
- using  $943 \text{ fb}^{-1}$  of data; normalize to  $D^0 \rightarrow K^+ K^- / K^- \pi^+ / \pi^+ \pi^-$  respectively.
- $M_{V\gamma}$  and  $\cos \theta_H$  2-dimension fit

PRD78,071101(R) (2008)



PRL 118, 051801 (2017)



$M_{V\gamma}$  and  $\cos \theta_H$  2-dimension fit:

$$\mathcal{B}(D^0 \rightarrow \phi \gamma) = (2.78 \pm 0.30 \pm 0.27) \times 10^{-5}$$

only  $M_{V\gamma}$  fit, and  $\cos \theta_H$  consistency check:

$$\mathcal{B}(D^0 \rightarrow \bar{K}^{*0} \gamma) = (3.28 \pm 0.20 \pm 0.27) \times 10^{-4}$$

(first observation)

$$\mathcal{B}(D^0 \rightarrow \phi \gamma) = (2.76 \pm 0.20 \pm 0.08) \times 10^{-5}$$

(improved Belle result,  $\simeq$  W.A)

$$\mathcal{B}(D^0 \rightarrow \bar{K}^{*0} \gamma) = (4.66 \pm 0.21 \pm 0.18) \times 10^{-4}$$

( $3.3\sigma$  away from BABAR analysis)

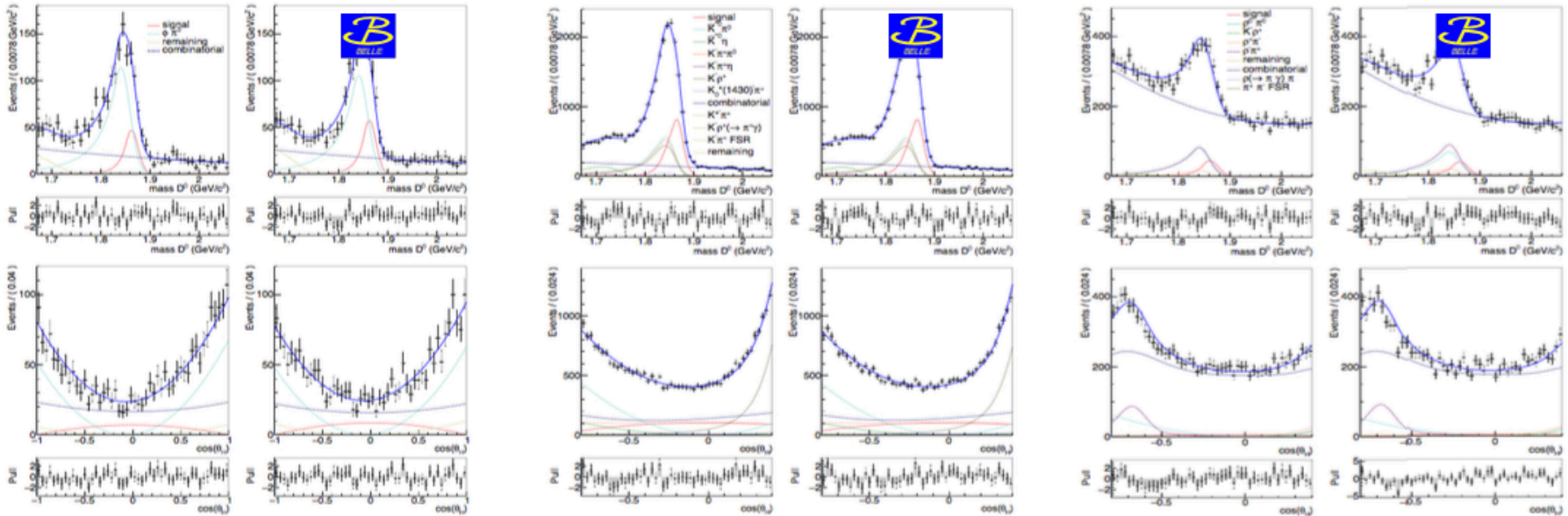
$$\mathcal{B}(D^0 \rightarrow \rho^0 \gamma) = (1.77 \pm 0.30 \pm 0.08) \times 10^{-5}$$

(first observation,  $\simeq$  theoretical predictions)

# CPV in $D^0$ radiative decays

Belle: **First measurement** of  $\mathcal{A}_{CP}$  in  $D^0 \rightarrow V\gamma$  [T. Nanut *et al.*, PRL **118**, 051801 (2017)]

- in radiative charm decays:  $\mathcal{A}_{CP}^{V\gamma} > 3\% \Rightarrow$  signal of NP [RPL109,171801(2012)]
- raw asym.:  $A_{raw} = \frac{N(D^0) - N(\bar{D}^0)}{N(D^0) + N(\bar{D}^0)} = \mathcal{A}_{CP} + A_{FB} + A_{\epsilon}^{\pm}$
- $A_{FB}, A_{\epsilon}^{\pm}$ : eliminated through a relative measurement:  $\mathcal{A}_{CP}^{sig} = A_{raw}^{sig} - A_{raw}^{norm} + \mathcal{A}_{CP}^{norm}$



$$\mathcal{A}_{CP}^{\phi\gamma} = -0.094 \pm 0.066 \pm 0.001$$

$$\mathcal{A}_{CP}^{\bar{K}^{*0}\gamma} = -0.003 \pm 0.020 \pm 0.000$$

$$\mathcal{A}_{CP}^{\rho^0\gamma} = +0.056 \pm 0.151 \pm 0.006$$

Belle II(50 ab<sup>-1</sup>):  $\sigma = \pm 0.01$

$\sigma = \pm 0.003$

$\sigma = \pm 0.02$

# T-odd asymmetry in $D^0 \rightarrow K_S \pi^+ \pi^- \pi^0$

[PRD 95, 091101\(R\) \(2017\)](#)

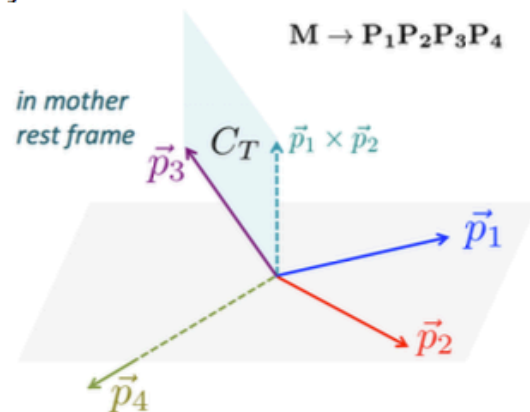
- ▶ T-odd correlations provides a powerful tool to indirectly search for  $CP$  violation:
  - (1) a triple product of momenta;
  - (2) assuming CPT symmetry conservation

- ▶ Parity-odd observable  $C_T = (\vec{p}_1 \times \vec{p}_2) \cdot \vec{p}_3$  and its CP-conjugated observable  $\bar{C}_T$

$$A_T = \frac{\Gamma(C_T > 0) - \Gamma(C_T < 0)}{\Gamma(C_T > 0) + \Gamma(C_T < 0)} \quad \bar{A}_T = \frac{\Gamma(-\bar{C}_T > 0) - \Gamma(-\bar{C}_T < 0)}{\Gamma(-\bar{C}_T > 0) + \Gamma(-\bar{C}_T < 0)}$$

- ▶ T-odd asymmetry: remove strong phase introduced by FSI

$$a_{CP}^{T\text{-odd}} = \frac{1}{2}(A_T - \bar{A}_T)$$



- ▶ Observing a T-odd asymmetry would be a signal for processes beyond the SM.

- ▶ Status of T-odd asymmetries in charmed mesons decay-rates:

$D^0 \rightarrow K_S^0 \pi^+ \pi^- \pi^0$	$a_{CP}^{T\text{-odd}} = (-0.28 \pm 1.38^{+0.23}_{-0.76}) \times 10^{-3}$	Belle <sup>[1]</sup>
$D^0 \rightarrow K^+ K^- \pi^+ \pi^-$	$a_{CP}^{T\text{-odd}} = (+1.7 \pm 2.7) \times 10^{-3}$	LHCb <sup>[2]</sup> , BaBar <sup>[3]</sup> , Focus <sup>[4]</sup>
$D^+ \rightarrow K_S^0 K^+ \pi^+ \pi^-$	$a_{CP}^{T\text{-odd}} = (-1.10 \pm 1.09) \times 10^{-2}$	BaBar <sup>[5]</sup> , Focus <sup>[4]</sup>
$D_s^+ \rightarrow K_S^0 K^+ \pi^+ \pi^-$	$a_{CP}^{T\text{-odd}} = (-1.39 \pm 0.84) \times 10^{-2}$	BaBar <sup>[5]</sup> , Focus <sup>[4]</sup>

[1] K. Prasanth et al.(Belle Collab.), Phys. Rev. D **95**, 091101(R) (2017)

[2] R. Aaij et al.(LHCb Collab.), JHEP **10**, 5 (2014)

[3] P. del Amo Sanchez et al.(BaBar Collab.), Phys. Rev. D **81**, 111103(R) (2010)

[4] J.M. Link et al.(FOCUS Collab.), Phys. Lett. B **622**, 239 (2005)

[5] J.P. Lees et al.(BaBar Collab.), Phys. Rev. D **84**, 031103(R) (2011)

Belle II could improve these results with more precision benefited from the increased dataset.

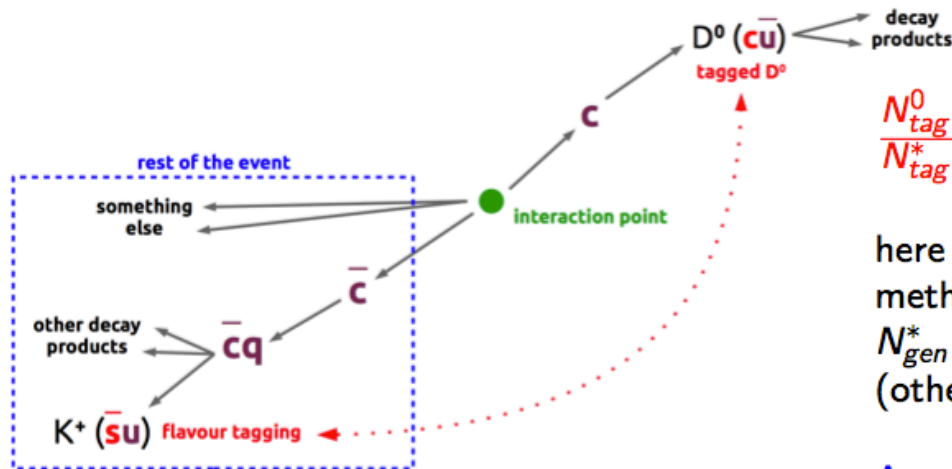
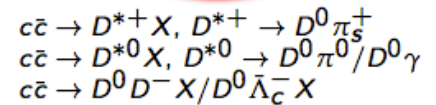
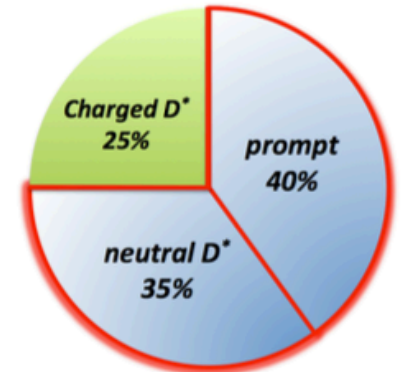


# Outline

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  - *Accelerator; detectors; dataset etc.*
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  - *summary table of measurements*
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  - *T-odd asymmetry in  $D^0 \rightarrow K_S \pi \pi \pi^0$*
- ***ROE method for  $D^0$  flavor tagging at Belle II***
- *Summary*

# ROE method

- To measure CPV, the flavor of  $D^0$  is determined effectively.
- At B-factories, the charge of  $\pi_s$  from  $D^{*+} \rightarrow D^0 \pi_s^+$  is used to tag the flavor of  $D^0$ ; but  $D^0$  mesons from  $B$  decays are excluded.  
 $\Rightarrow$  only  $D^0$  from  $D^{*\pm}$  in  $c\bar{c}$  events (25%) were used.
- ROE** method: select events with only one  $K^\pm$  in the **Rest Of Event**;
- the charge of this  $K^\pm$  in ROE to determine the flavor of  $D^0$ .



$$\frac{N_{tag}^0}{N_{tag}^*} = \frac{\epsilon_{tag}^0}{\epsilon_{tag}^*} \cdot \frac{N_{gen}^0 + (1 - \epsilon_{tag}^*) \cdot N_{gen}^*}{N_{gen}^*} \sim 1$$

here  $\epsilon_{tag}^*$  ( $\epsilon_{tag}^0$ ): tagging efficiency of  $D^*$  (ROE) method with 80% ( $\leq 20\%$ ).

$N_{gen}^*$  ( $N_{gen}^0$ ): number of  $D^0$  produced by a  $D^*$  (other  $c\bar{c}$  event) with  $N_{gen}^0 : N_{gen}^* \simeq 3 : 1$

A reduction of  $\sim 15\%$  of  $\sigma(stat)$  on  $A_{CP}$

An additional  $D^0$  sample from ROE for mixing and CPV measurements.

# Summary

- *Belle at KEKB have proven to be an excellent tool for charm physics*
  - *first (only) observation of  $D^0$ - $\bar{D}^0$  mixing in  $e^+e^-$  collision*
  - *no hints for indirect CPV and no clear evidence for direct CPV*
  - *fruitful results on mixing/CPV measurement, but mostly under statistical limit*
- *Major upgrade at KEKB in 2010-17  $\rightarrow$  SuperKEKB  $\mathcal{L} \times 40 = 50 \text{ ab}^{-1}$  before 2025. Belle II at SuperKEKB will have a rich charm physics program with much improved performance:*
  - *improve precision of mixing and CPV parameters, direct CP asymmetries.*
  - *Many final states studies (e.g. with  $\pi^0/\eta/\eta'$  etc.) complementary to LHCb.*
  - *Some new techniques are developing, like ROE method.*
- *Detector is mostly installed and commissioned, will collect the first data in 2018.*

Let's look forwards to the charming news of charm physic from Belle II (绝世美女二世).

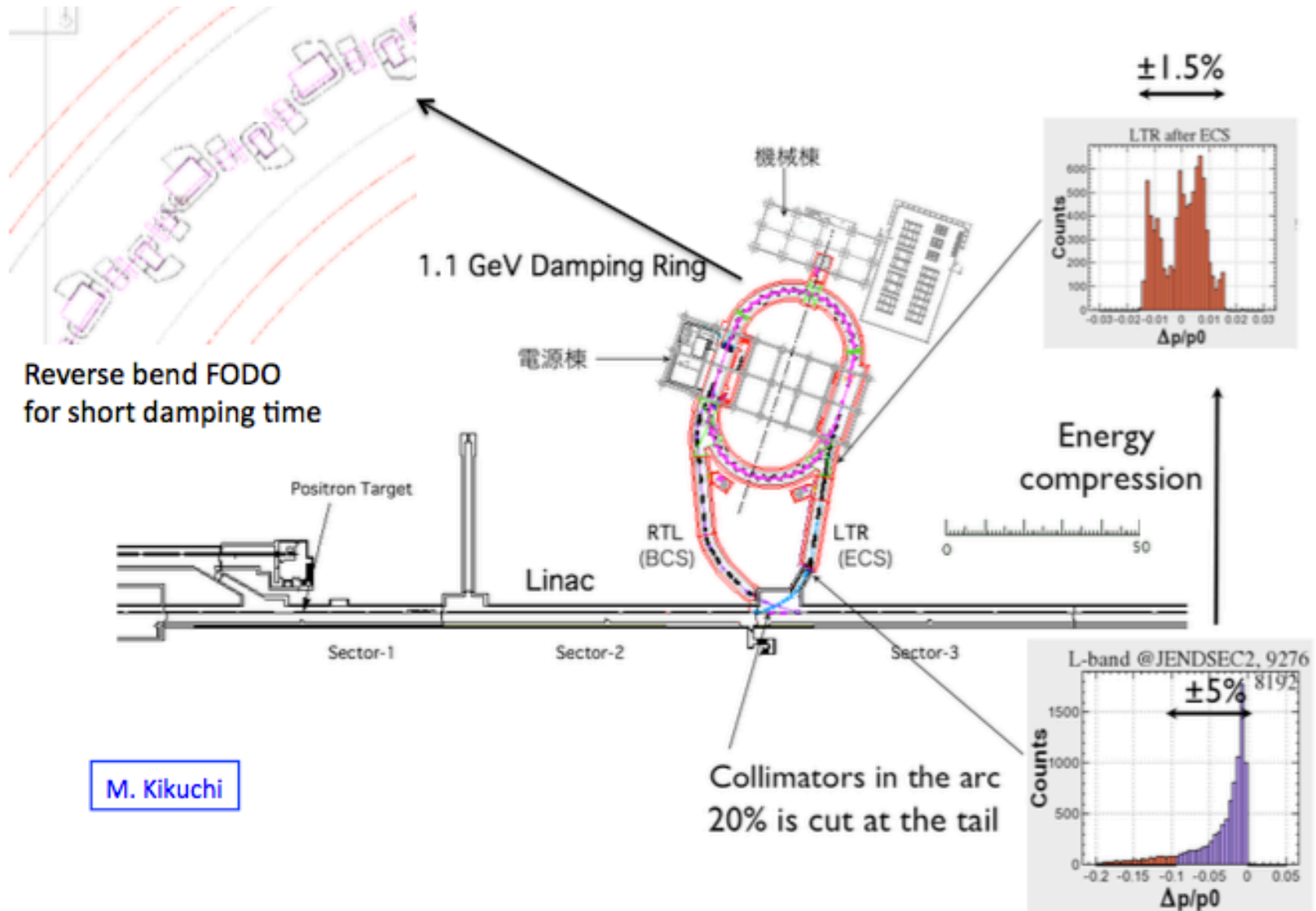
今夕何夕，见此粲者？  
子兮子兮，如此粲者何？  
——《诗经·绸缪》

# backup

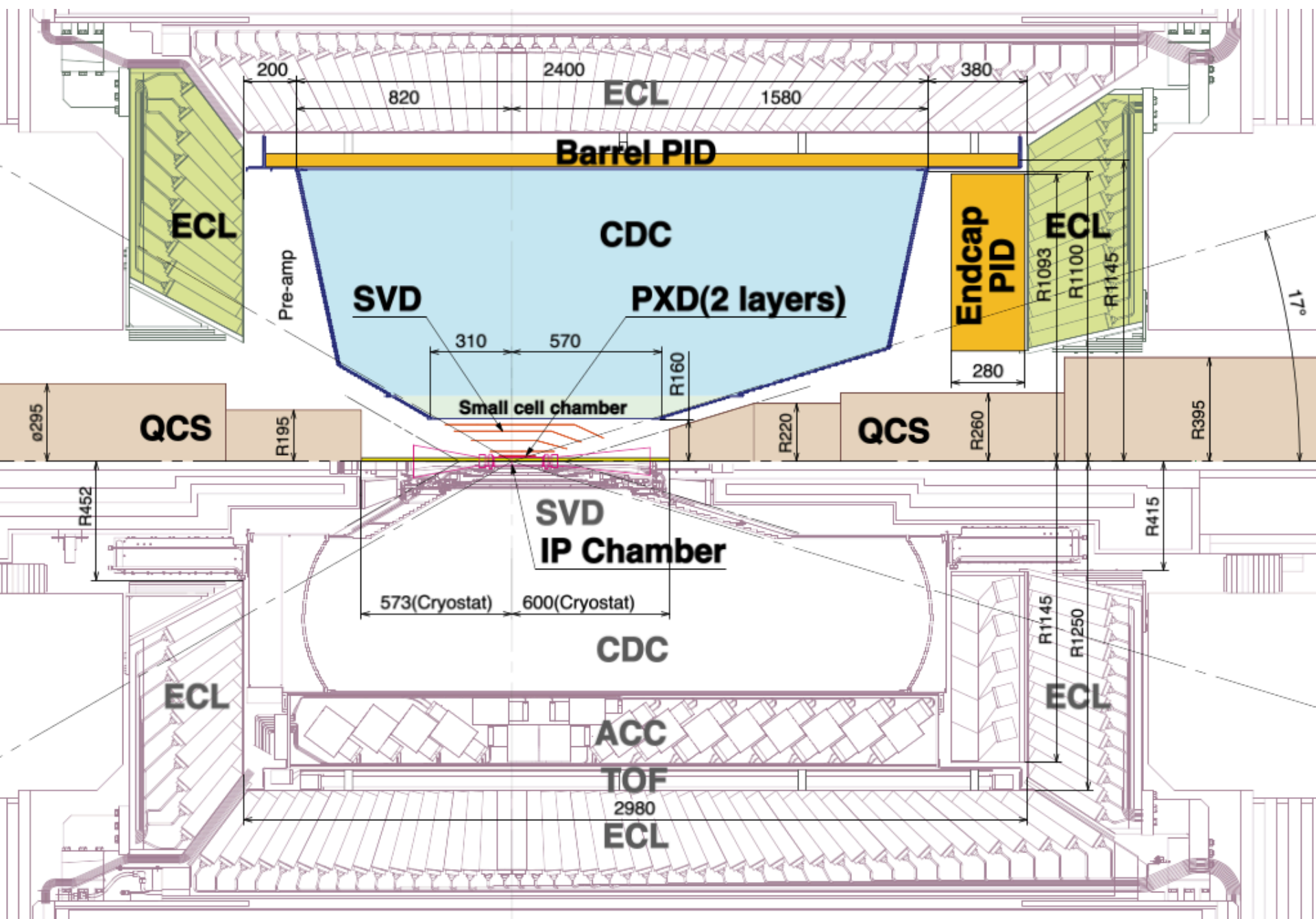


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# Damping Ring

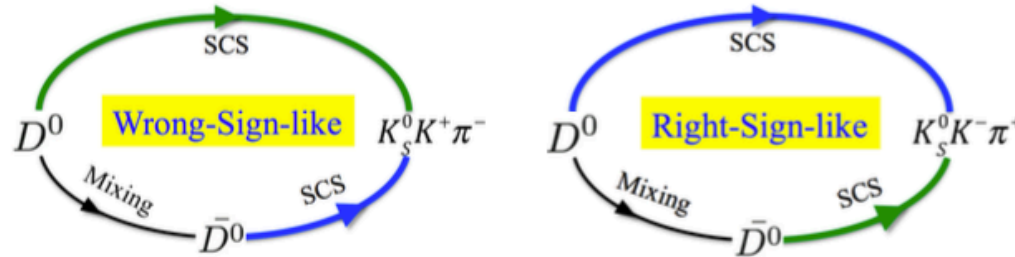






# prospect of mixing in three-body SCS decays

- decay rate of WS-like and RS-like:



- $\Gamma(D^0 \rightarrow K_S^0 K^+ \pi^-) = e^{-\Gamma t} \left[ r_D^2 + r_D R_D y' \Gamma t + \frac{(1-r_D^2)x'^2 + (1+r_D^2)y'^2}{4} (\Gamma t)^2 \right]$

- $\Gamma(D^0 \rightarrow K_S^0 K^- \pi^+) = e^{-\Gamma t} \left[ 1 + r_D R_D y' \Gamma t + \frac{(1+r_D^2)x'^2 - (1-r_D^2)y'^2}{4} (\Gamma t)^2 \right]$

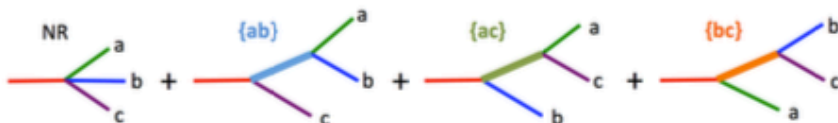
where  $r_D = A_{sup.} / \bar{A}_{fav.}$ ,  $y' = y \cos \delta_D - x \sin \delta_D$ , coherence factor  $R_D$ :  $A_f \bar{A}_f R_D e^{-i\delta_D} = A_f \bar{A}_f^*$

- Comparing with WS decays  $D^0 \rightarrow K^+ \pi^-$ :  $r_D^{K\pi} \ll 1$  Vs.  $r_D^{K_S^0 K \pi} \sim 1$
- $D^0 \rightarrow K_S^0 K \pi$ : effectively sensitive to  $y'$  (large  $R_D$ ); higher purity (large  $r_D$ )
- CLEO gave in  $D^0 \rightarrow K_S^0 K \pi$ ,  $R_D = 0.73 \pm 0.09$  and  $\delta_D = (8.2 \pm 15.2)^\circ$  [PRD 85, 092016(2012)]
- sensitivity estimation of mixing:  $\sigma(y') = 0.55\%$  (80K signals) [PLB 701(2011)353]
- LHCb has performed Dalitz plot fit on these two decays. [PRD 93, 052018 (2016)]
- mixing and CPV measurement in these decays.....

# Time-dependent Dalitz analysis

- DP of 3-body decay described by Isobar model:

Phys. Rev. 123, 333 (1961)

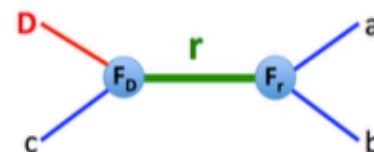


$$\mathcal{M}(m_{ab}^2, m_{bc}^2) = \sum_r a_r e^{i\phi_r} \mathcal{A}_r(m_{ab}^2, m_{bc}^2) + a_{NR} e^{i\phi_{NR}}$$

here  $a_r(\phi_r)$  is magnitude (phase) of resonance  $r$ .

- $\mathcal{A}_r$ : dynamics of  $D \rightarrow (r \rightarrow ab)c$

PRD 63, 092001 (2001)



$$\mathcal{A}_r(m_{ab}^2, m_{bc}^2) = F_D \times F_r \times T_r \times W_r$$

- $T_r$ : resonance lineship

usually use relativistic Breit-Wigner with mass dept. width

For wide width or special resonances:

mass-threshold: Flatté model, eg:  $f_0(980)(KK) / a_0(980)(KK/\eta'\pi)$

$\pi\pi$  S-wave overlapping res.: K-matrix model EPJ A16 (2003) 229-258

$\pi\pi$  P-wave:  $\rho$  with Gounaris-Sakurai (GS) model PRL 24,244(1968)

$K\pi$  S-wave:  $K_0^*(1430)$  with LASS model EPJ C74 (2014): 3026

- $W_r$  angular distribution:

(1) Helicity form [PRD 78, 052001 (2008)]

(2) Zemach covariant tensor form [PR 133, B1201 (1964), PR 140, B109 (1965)]

- $F_r, F_D$  form factor: PR D 63, 092001 (2001)

using Blatt-Weisskopf Barrier form factor, depend on orbital angular momentum  $\ell$  (here  $\ell = J$  (spin of res.)

$$F_{J=0} = 1$$

$$F_{J=1} = \frac{\sqrt{1+z_r}}{\sqrt{1+z_{ab}}}$$

$$F_{J=2} = \frac{\sqrt{(z_r-3)^2+9z_r}}{\sqrt{(z_{ab}-3)^2+9z_{ab}}}$$

$$F_{J=3} = \frac{\sqrt{z_r(z_r-15)^2+9(2z_r-5)}}{\sqrt{z_{ab}(z_{ab}-15)^2+9(2z_{ab}-5)}}$$

$$F_{J=4} = \frac{\sqrt{(z_r^2-45z_r+105)^2+15z_r(21z_r-21)^2}}{\sqrt{(z_{ab}^2-45z_{ab}+105)^2+15z_{ab}(21z_{ab}-21)^2}}$$

here  $z = (R \cdot q)^2$ ,  $R$  is the radius of  $D$  or res.  $r$

# Time-dependent Dalitz analysis

## ► Dalitz plot(DP) fit

### • p.d.f of signal DP:

- (1) efficiency plane  $\epsilon$  correction
- (2) considering mass resolution  $Res(m)$
- (3) normalization

$$p_{\text{sig}}(m_{12,i}^2, m_{23,i}^2) = \frac{|\mathcal{M}(m_{12,i}^2, m_{23,i}^2)|^2 \otimes_m Res(m) \cdot \epsilon(m_{12,i}^2, m_{23,i}^2)}{\iint_{DP} dm_{12}^2 dm_{23}^2 |\mathcal{M}(m_{12}^2, m_{23}^2)|^2 \otimes_m Res(m) \cdot \epsilon(m_{12}^2, m_{23}^2)}$$

### • fit method: unbinned maximum likelihood (UML)

$$2 \ln \mathcal{L} = 2 \sum_{i=1}^n \ln \left[ f_{\text{sig}}^i p_{\text{sig}}(m_{12,i}^2, m_{23,i}^2) + \sum_{X=b\bar{g}} f_X^i p_X(m_{12,i}^2, m_{23,i}^2) \right]$$

signal-to-bkg  $f^i$  determined by kinematic variable fit result, like M-Q.

## ► time-dependent Dalitz plot(TDDP) fit

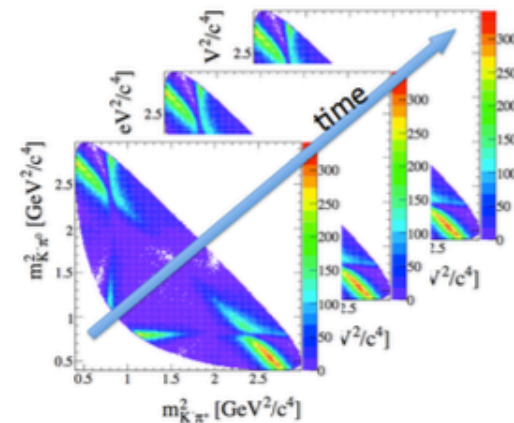
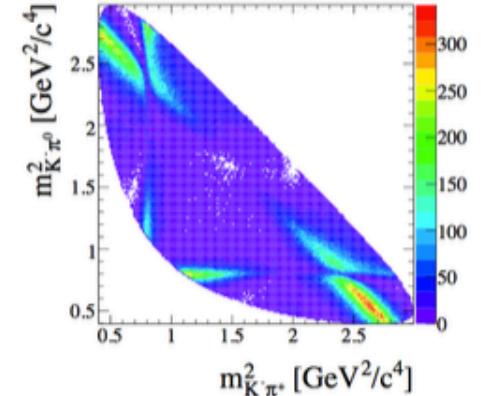
### • p.d.f of signal TDDP with considering time resolution : $R_{\text{sig}}(t)$

$$p_{\text{sig}}(m_{12,i}^2, m_{23,i}^2, t_i, \sigma_t^i) = \frac{\int dt' R_{\text{sig}}(t_i - t', \sigma_t^i) |\mathcal{M}_f(m_{12,i}^2, m_{23,i}^2, t')|^2 \cdot \epsilon(m_{12,i}^2, m_{23,i}^2)}{\int dt \iint_{DP} dm_{12}^2 dm_{23}^2 |\mathcal{M}_f(m_{12}^2, m_{23}^2, t)|^2 \epsilon(m_{12}^2, m_{23}^2)}$$

### • fit method: unbinned maximum likelihood (UML)

$$2 \ln \mathcal{L} = 2 \sum_i \{ \ln(f_{\text{sig}}^i p_{\text{sig}}(m_{12,i}^2, m_{23,i}^2, t_i, \sigma_t^i; \mathbf{x}, \mathbf{y}) p_{\text{sig}}^{nc}(\sigma_t^i)) + \sum_{X=b\bar{g}} f_X^i p_X(m_{12,i}^2, m_{23,i}^2, t_i) p_X^{nc}(\sigma_t^i) \}$$

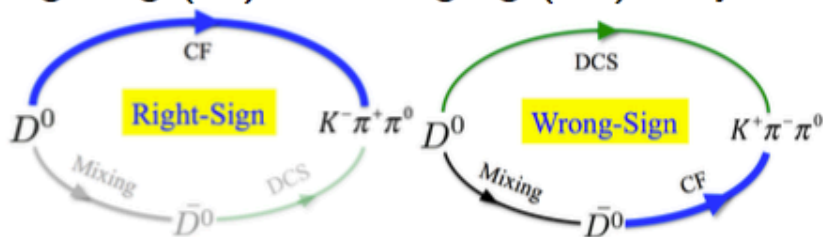
here  $p_X^{nc}(\sigma_t^i)$  is global function for time error, independent on others.





# Time-dependent Dalitz analysis

- Right-Sign(RS) and Wrong-Sign(WS) decays

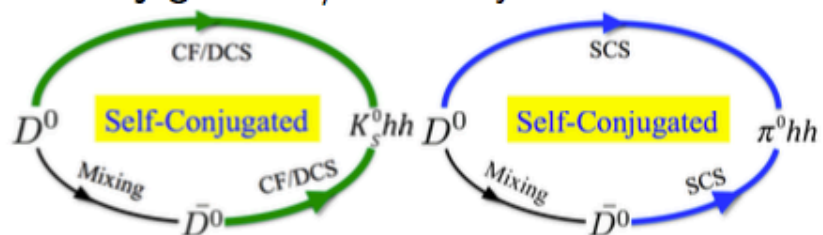


$$|\mathcal{M}_f(RS, t)|^2 = e^{-\Gamma t} |\bar{\mathcal{A}}_f^{CF}|^2$$

$$\mathcal{A}_{\bar{f}} / \bar{\mathcal{A}}_{\bar{f}} = -\sqrt{R_D} e^{-i\delta}; \quad x'' = x \cos \delta + y \sin \delta; \quad y'' = y \cos \delta - x \sin \delta$$

$$|\mathcal{M}_f(WS, t)|^2 = e^{-\Gamma t} \left\{ |\mathcal{A}_f^{DCS}|^2 - \left( \frac{y''}{r_0} \text{Re}[\mathcal{A}_f^{DCS} \bar{\mathcal{A}}_f^{CF*}] + \frac{x''}{r_0} \text{Im}[\mathcal{A}_f^{DCS} \bar{\mathcal{A}}_f^{CF*}] \right) \Gamma t + \frac{x'^2 + y'^2}{4r_0^2} |\mathcal{A}_f^{CF}|^2 (\Gamma t)^2 \right\}$$

- Self-conjugated CF/SCS decays



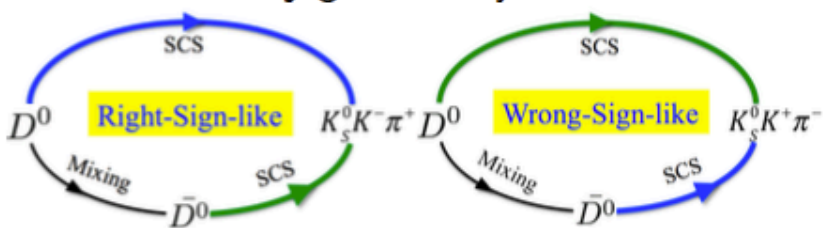
$$RS: \mathcal{A}_f = \langle f | \mathcal{H} | D^0 \rangle; \quad WS: \mathcal{A}_{\bar{f}} = \langle \bar{f} | \mathcal{H} | D^0 \rangle; \quad CP: \mathcal{A}_{\pm} = \langle \pm | \mathcal{H} | D^0 \rangle$$

$$D^0: m_+^2 = m_{K_S^0 h^+}^2; \quad m_-^2 = m_{K_S^0 h^-}^2; \quad \bar{D}^0: m_+^2 = m_{K_S^0 h^+}^2; \quad m_-^2 = m_{K_S^0 h^-}^2$$

$$|\mathcal{M}_f|^2 = \left\{ |A_1|^2 e^{-y\Gamma t} + |A_2|^2 e^{y\Gamma t} + 2 \text{Re}[A_1 A_2^*] \cos(x\Gamma t) + 2 \text{Im}[A_1 A_2^*] \sin(x\Gamma t) \right\} e^{-\Gamma t}$$

$$|\bar{\mathcal{M}}_f|^2 = \left\{ |\bar{A}_1|^2 e^{-y\Gamma t} + |\bar{A}_2|^2 e^{y\Gamma t} + 2 \text{Re}[\bar{A}_1 \bar{A}_2^*] \cos(x\Gamma t) + 2 \text{Im}[\bar{A}_1 \bar{A}_2^*] \sin(x\Gamma t) \right\} e^{-\Gamma t}$$

- SCS non-self-conjugated decays



(very difficult! No one experiment gives time-dept. amplitude analysis to date.)

$$A = \langle K_S^0 K^- \pi^+ | \mathcal{H} | D^0 \rangle = \langle K_S^0 K^+ \pi^- | \mathcal{H} | \bar{D}^0 \rangle; \quad B = \langle K_S^0 K^+ \pi^- | \mathcal{H} | D^0 \rangle = \langle K_S^0 K^- \pi^+ | \mathcal{H} | \bar{D}^0 \rangle$$

$$|\mathcal{M}(RS, t)|^2 = e^{-\Gamma t} \left\{ |A|^2 + \frac{x^2 + y^2}{4} r_D^2 |B|^2 (\Gamma t)^2 + r_D (y' \text{Re}[AB^*] + x' \text{Im}[AB^*]) \Gamma t \right\}$$

$$|\mathcal{M}(WS, t)|^2 = e^{-\Gamma t} \left\{ r_D^2 |B|^2 + \frac{x^2 + y^2}{4} |A|^2 (\Gamma t)^2 + r_D \cdot (y' \text{Re}[BA^*] + x' \text{Im}[BA^*]) \Gamma t \right\}$$



# search for CPV in $D^0 \rightarrow K_S^0 K_S^0$

SM limit 1.1% for direct CPV in  $D^0 \rightarrow K_S^0 K_S^0$

U. Nierste and A. Schacht, PRD 92 (2015) 054036

SCS decays (such as  $D^0 \rightarrow K_S^0 K_S^0$ ) are special interest: possible interference with NP amplitude could lead to larger nonzero CPV

The previous measured  $A_{CP}(D^0 \rightarrow K_S^0 K_S^0)$ :

CLEO  $(-23 \pm 19)\%$   $13.7 \text{ fb}^{-1}$  PRD 63 (2001) 071101

LHCb  $(-2.9 \pm 5.2 \pm 2.2)\%$   $3 \text{ fb}^{-1}$  JHEP 10 (2015) 055

Method:  $A_{CP}(D^0 \rightarrow K_S^0 K_S^0) = (A_{rec}(K_S^0 K_S^0) - A_{rec}(K_S^0 \pi^0)) + A_{CP}(D^0 \rightarrow K_S^0 \pi^0) + A_{K0/K^0}$

$A_{K0/K^0}$ : Asymmetry originating from the different strong interaction of  $K0$  and  $\bar{K}0$  mesons with nucleons of the detector material =  $(-0.11 \pm 0.01)\%$

[B. R. Ko et al., PRD 84 (2011) 111501]

$A_{CP}(D^0 \rightarrow K_S^0 \pi^0) = (-0.20 \pm 0.17)\%$

[PDG]

N. Dash, ICHEP 2016