

# $J/\psi + \Upsilon$ production at hadron colliders and double parton scattering

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# Outline

- 1 Introduction
- 2 The frame of Calculation
- 3 Numerical Result
- 4 Summary

Based on HuaSheng Shao, YJZ, PRL 117 (2016) 062001 ( 1605.03061 )

# Introduction

## Quarkonium productions

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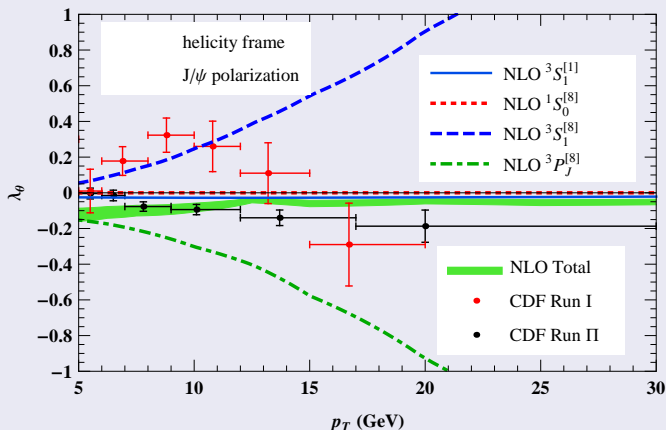
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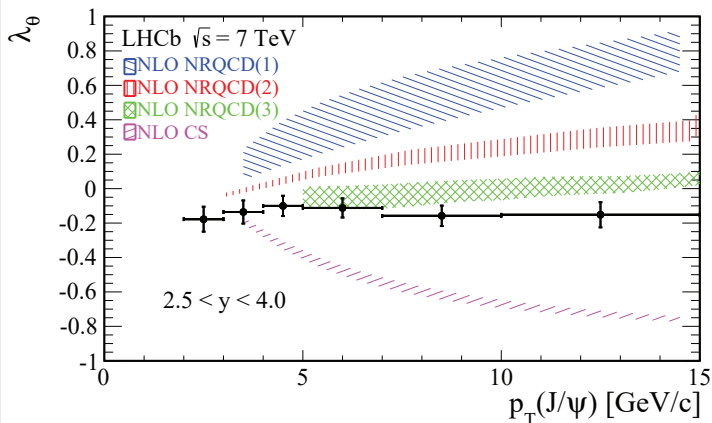
# Quarkonium productions

## NLO $J/\psi$ polarization at CDF, arXiv:1201.2675



# Quarkonium productions

## NLO $J/\psi$ at LHCb, Chao/Wang/Kniehl, 1506.03981



## Quarkonium production and double parton scattering

**Many quarkonium associated production processes seems to be dominant by Double-Parton Scattering (DPS).**

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- 2  $J/\psi + charm$  and  $\Upsilon + charm$  (LHCb, arXiv:1205.0975, 1510.05949)

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- 3  $J/\psi + J/\psi$  (D0, arXiv:1406.2380; CMS, arXiv:1406.0484)

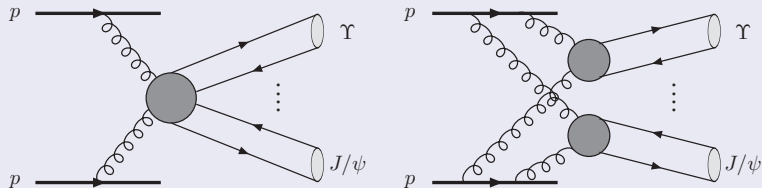
## Quarkonium production and double parton scattering

Many quarkonium associated production processes seems to be dominant by Double-Parton Scattering (DPS).

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- 2  $J/\psi + charm$  and  $\Upsilon + charm$  (LHCb, arXiv:1205.0975, 1510.05949)
- 3  $J/\psi + J/\psi$  (D0, arXiv:1406.2380; CMS, arXiv:1406.0484)
- 4  $\Upsilon + J/\psi$  (D0, arXiv:1511.02428)

## Double parton scattering and Single parton scattering

However, one should keep in mind that before concluding for DPS dominance, one should always carefully examine the Single-Parton Scattering (SPS) contributions.



**Figure:** SPS and DPS of  $pp \rightarrow J/\psi + \Upsilon + X$ .



## Double parton scattering

### Cross section of Double parton scattering

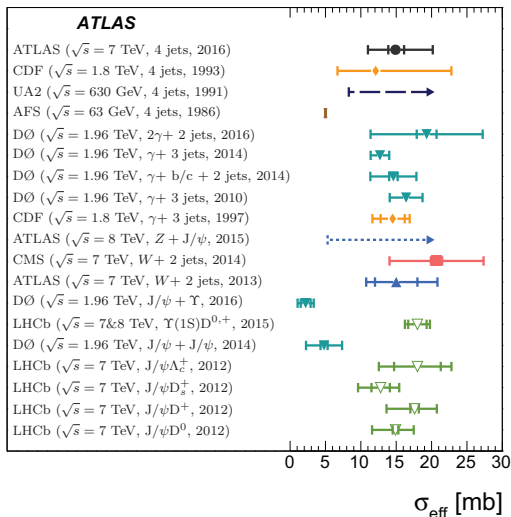
$$\sigma_{DPS}^{AB} = \frac{1}{1 + \delta_{AB}} \frac{\sigma^A \sigma^B}{\sigma_{eff}} \quad (1)$$

### $\sigma_{eff}$ (1306.3763)

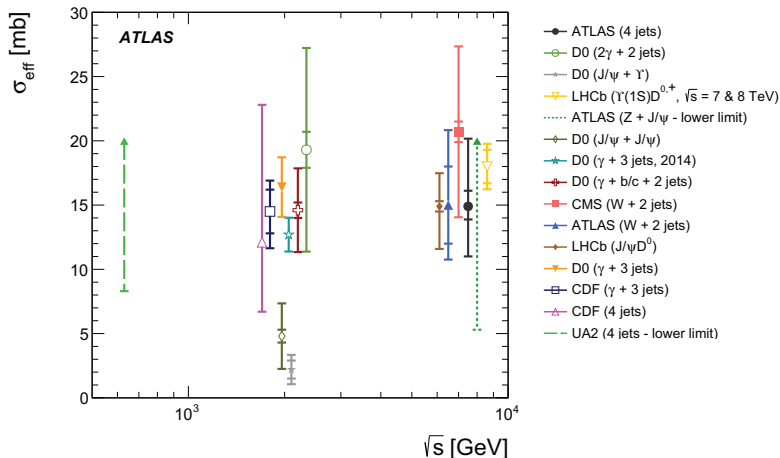
$$\frac{1}{\sigma_{eff}} = \frac{\int \frac{d^2 \vec{\Delta}}{(2\pi)^2} D_{h1}(x_1, x_2, Q_1^2, Q_2^2; \vec{\Delta}) D_{h2}(x_3, x_4, Q_1^2, Q_2^2; -\vec{\Delta})}{D_{h1}(x_1, Q_1^2) D_{h1}(x_2, Q_2^2) D_{h2}(x_3, Q_1^2) D_{h2}(x_4, Q_2^2)} \quad (2)$$

# $\sigma_{\text{eff}}$ (arXiv:1608.01857)

Experiment (energy, final state, year)



# $\sigma_{\text{eff}}$ (arXiv:1608.01857)



## Prompt $J/\psi + \Upsilon$ @ D0

### Prompt $J/\psi + \Upsilon(1S, 2S, 3S)$ @ D0 (arXiv:1511.02428)

$$\sigma_{D0}^{J/\psi+\Upsilon} = 27 \pm 9 \pm 7 \text{ fb} \quad (3)$$

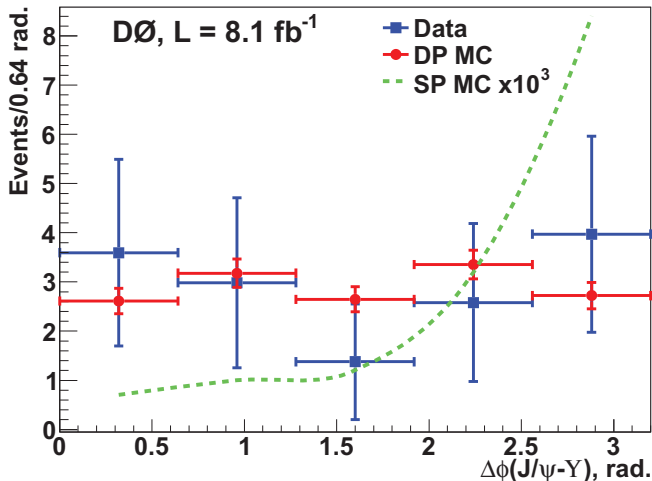
### Ignore the SPS contribution

$$\sigma_{DPS}^{J/\psi+\Upsilon} = \sigma_{D0}^{J/\psi+\Upsilon} = \frac{\sigma^{J/\psi} \sigma^{\Upsilon}}{\sigma_{eff}} \quad (4)$$

$\sigma_{eff}$

$$\sigma_{eff} = 2.2 \pm 0.7 \pm 0.9 \text{ mb} \quad (5)$$

# The distribution of the azimuthal angle between the $J/\psi + \Upsilon$



## Color-Singlet contributions of $J/\psi + \Upsilon$

### Color-Singlet contributions

Unlike  $J/\psi$ -pair or  $\Upsilon$ -pair production, neither  $\mathcal{O}(\alpha_S^4)$  nor  $\mathcal{O}(\alpha_S^5)$  contributions survive in Color-Singlet Model (CSM).

### The approximated Loop-Induced (LI) contribution

The approximated Loop-Induced (LI) contribution in CSM at  $\mathcal{O}(\alpha_S^6)$  was estimated in Ref. (arXiv:1503.00246) with in the specific limit  $\hat{s} \gg |\hat{t}| \gg m_{\psi, \Upsilon}^2$ , where  $\hat{s}$  and  $\hat{t}$  are the Mandelstam variables.

## Color-Octet contributions of $J/\psi + \Upsilon$

### Color-Octet contributions

The process is a golden observable to probe the so-called Color-Octet Mechanism (COM) (arXiv:1007.3095)

### Color-Octet contributions at $\sqrt{s} = 115$ GeV

The Color Octet (CO) contribution were predicted for AFTER@LHC energies  $\sqrt{s} = 115$  GeV (arXiv:1504.06531) with HELAC-Onia (arXiv:1212.5293, 1507.03435).

## Hadroproduction of $\Upsilon + J/\psi$

### SPS contributions were absence

However, the exact calculations of the complete SPS contributions were absence in the literature.

### First complete study of $\Upsilon + J/\psi$

We present the first complete study of the simultaneous production of prompt  $\psi$  and  $\Upsilon$  mesons by including all leading contributions, at order  $\mathcal{O}(\alpha_S^6)$  or equivalent.



# The frame of Calculation

## Cross sections

### Hadron and Parton level cross sections

$$\sigma(h_1 h_2 \rightarrow \mathcal{C} + \mathcal{B} + X) = \sum_{a,b} f_{a/h_1} \otimes f_{b/h_2} \otimes \hat{\sigma}(ab \rightarrow \mathcal{C} + \mathcal{B} + X). \quad (6)$$

### Parton level cross section

$$d\hat{\sigma}(ab \rightarrow \mathcal{C} + \mathcal{B} + X) = \sum_{n_1, n_2} \hat{\sigma}(ab \rightarrow c\bar{c}[n_1] + b\bar{b}[n_2] + X) \langle O^{\mathcal{C}}(n_1) \rangle \langle O^{\mathcal{B}}(n_2) \rangle \quad (7)$$

## Matrix elements

### Fock States Of $J/\psi$

$$\begin{aligned}
 |J/\psi\rangle &= \mathcal{O}(1)|c\bar{c}(^3S_1^{[1]})\rangle + \mathcal{O}(v_c^2)|c\bar{c}(^3S_1^{[8]})gg\rangle \\
 &+ \mathcal{O}(v_c^2)|c\bar{c}(^3P_J^{[1,8]})g\rangle + \mathcal{O}(v_c^2)|c\bar{c}(^1S_0^{[8]})g\rangle + \dots
 \end{aligned}$$

$v^2$

$$v_b^2 \sim v_c^2 \sim 0.1 - 0.3$$

$$\alpha_S \sim 0.2$$

$$\alpha_S \sim v_c^2 \sim v_b^2 \quad (8)$$

## QED

$J^{PC}$  Of  $J/\psi$  or  $\Upsilon$  are  $1^{--}$

QED contributions may be important too.

$\alpha$

$$\alpha \sim 0.008$$

$$\alpha_S \sim \sqrt{\alpha} \quad (9)$$

$$\mathcal{O}(\alpha_S^6)$$

### Color Singlet

The  $\mathcal{O}(\alpha_S^4)$  and  $\mathcal{O}(\alpha_S^5)$  contributions to  $\Upsilon + \psi$  direct production in CSM vanish because of P-parity and C-parity conservation.

### Color Octet

$$\mathcal{O}(\alpha_S^4 v_c^i v_b^j) \leq \mathcal{O}(\alpha_S^6) \text{ with } i + j \geq 4$$

### EW

$$\mathcal{O}(\alpha_S^2 \alpha^2) \leq \mathcal{O}(\alpha_S^6) \text{ with } i + j \geq 4$$

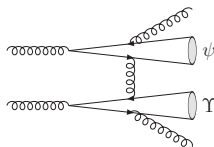
### Feeddown for $\chi_{c,b}$

$$\mathcal{O}(\alpha_S^4 v_c^i v_b^j) \leq \mathcal{O}(\alpha_S^6) \text{ with } i + j \geq 4$$

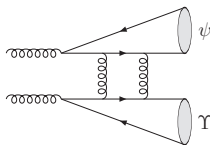
# Order of SPS

Label	HELAC-ONIA 2.0 syntax	First order
DR	<code>g g &gt; cc~(3S11) bb~(3S11) g g</code>	$\mathcal{O}(\alpha_S^6)$
LI	<code>addon 8</code>	$\mathcal{O}(\alpha_S^6)$
EW	<code>p p &gt; cc~(3S11) bb~(3S11)</code>	$\mathcal{O}(\alpha_S^2 \alpha^2)$
INTER	<code>addon 8</code>	$\mathcal{O}(\alpha_S^4 \alpha)$
COM	<code>g g &gt; jpsi y(1s)</code>	$\mathcal{O}(\alpha_S^4 v_c^i v_b^j), i + j \geq 4$

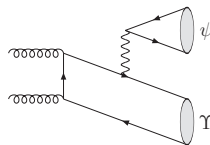
# Feynman Diagram of SPS



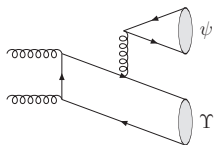
DR



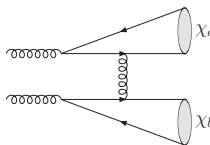
LI



EW



NRQCD



FD

# Numerical Result



# Direct SPS cross sections @ D0 in fb

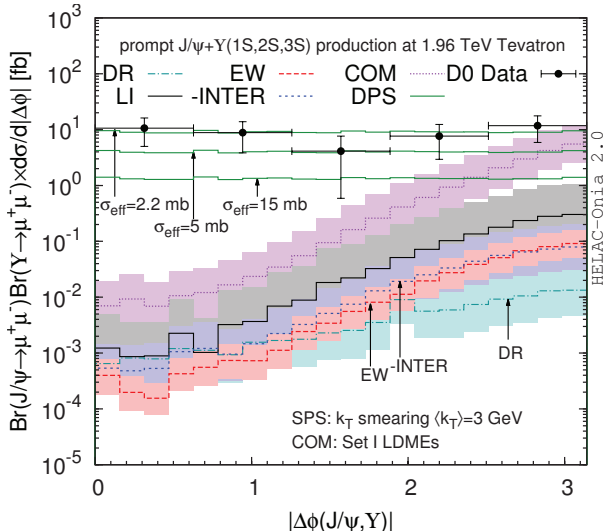
		$J/\psi$	$\psi(2S)$
DR	$\Upsilon(1S)$	$3.58^{+233\%}_{-66.4\%} \pm 4.4\%$	$2.34^{+233\%}_{-66.4\%} \pm 4.4\%$
	$\Upsilon(2S)$	$1.78^{+233\%}_{-66.4\%} \pm 4.4\%$	$1.17^{+233\%}_{-66.4\%} \pm 4.4\%$
	$\Upsilon(3S)$	$1.36^{+233\%}_{-66.4\%} \pm 4.4\%$	$0.894^{+233\%}_{-66.4\%} \pm 4.4\%$
LI	$\Upsilon(1S)$	$56.2^{+264\%}_{-70.2\%} \pm 4.7\%$	$36.8^{+264\%}_{-70.2\%} \pm 4.7\%$
	$\Upsilon(2S)$	$28.0^{+264\%}_{-70.2\%} \pm 4.7\%$	$18.4^{+264\%}_{-70.2\%} \pm 4.7\%$
	$\Upsilon(3S)$	$21.4^{+264\%}_{-70.2\%} \pm 4.7\%$	$14.0^{+264\%}_{-70.2\%} \pm 4.7\%$
EW	$\Upsilon(1S)$	$15.8^{+75.4\%}_{-46.4\%} \pm 4.6\%$	$10.4^{+75.4\%}_{-46.4\%} \pm 4.6\%$
	$\Upsilon(2S)$	$7.90^{+75.4\%}_{-46.4\%} \pm 4.6\%$	$5.18^{+75.4\%}_{-46.4\%} \pm 4.6\%$
	$\Upsilon(3S)$	$6.04^{+75.4\%}_{-46.4\%} \pm 4.6\%$	$3.96^{+75.4\%}_{-46.4\%} \pm 4.6\%$
INTER	$\Upsilon(1S)$	$-16.6^{+162\%}_{-62.0\%} \pm 4.8\%$	$-10.9^{+162\%}_{-62.0\%} \pm 4.8\%$
	$\Upsilon(2S)$	$-8.29^{+162\%}_{-62.0\%} \pm 4.8\%$	$-5.43^{+162\%}_{-62.0\%} \pm 4.8\%$
	$\Upsilon(3S)$	$-6.34^{+162\%}_{-62.0\%} \pm 4.8\%$	$-4.15^{+162\%}_{-62.0\%} \pm 4.8\%$
COM	$\Upsilon(1S)$	$409^{+138\%}_{-56.7\%} \pm 4.4\%$	$174^{+138\%}_{-56.8\%} \pm 4.4\%$
	$\Upsilon(2S)$	$135^{+139\%}_{-57.0\%} \pm 4.4\%$	$57.6^{+139\%}_{-57.1\%} \pm 4.4\%$
	$\Upsilon(3S)$	$197^{+137\%}_{-56.6\%} \pm 4.4\%$	$84.1^{+138\%}_{-56.7\%} \pm 4.4\%$

# SPS cross sections @ D0 & LHCb

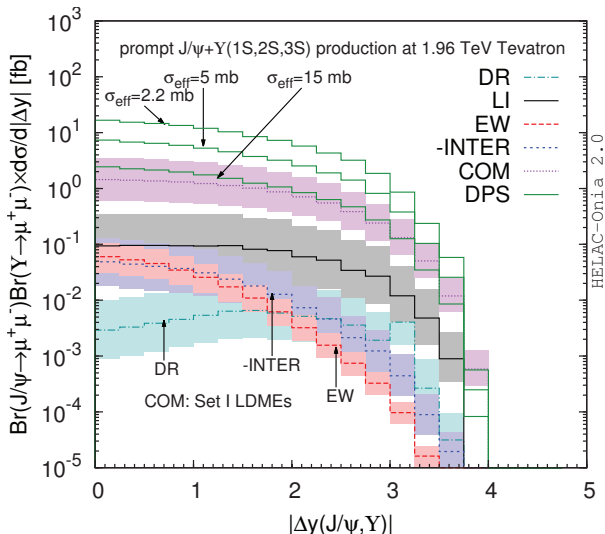
Experiment	CSM				COM			
	DR	LI	EW	INTER	Set I	Set II	Set III	Set IV
D0: $27 \pm 42.2\%$	$0.0146^{+233\%}_{-66.6\%}$	$0.229^{+264\%}_{-70.4\%}$	$0.065^{+75.5\%}_{-46.6\%}$	$-0.068^{+162\%}_{-62.2\%}$	$2.96^{+135\%}_{-56.2\%}$	$1.41^{+160\%}_{-77.6\%}$	$1.80^{+143\%}_{-58.0\%}$	$0.418^{+144\%}_{-58.3\%}$
LHCb	$0.255^{+391\%}_{-79.7\%}$	$6.05^{+436\%}_{-82.2\%}$	$1.71^{+135\%}_{-65.2\%}$	$-3.23^{+262\%}_{-75.9\%}$	$38.8^{+238\%}_{-73.0\%}$	$21.2^{+243\%}_{-73.6\%}$	$28.1^{+243\%}_{-73.8\%}$	$6.57^{+243\%}_{-73.9\%}$

TABLE III: Cross sections  $\sigma(pp(\bar{p}) \rightarrow J/\psi \Upsilon) \times \text{Br}(J/\psi \rightarrow \mu^+ \mu^-) \text{Br}(\Upsilon \rightarrow \mu^+ \mu^-)$  (in units of fb) of prompt  $J/\psi$  and  $\Upsilon(1S, 2S, 3S)$  simultaneous production at the Tevatron in the D0 fiducial region [10] and at  $\sqrt{s} = 13$  TeV LHC in the LHCb acceptance  $2 < y_{J/\psi, \Upsilon} < 4.5$ , where we have also included feeddown contributions from higher-excited quarkonia decay.

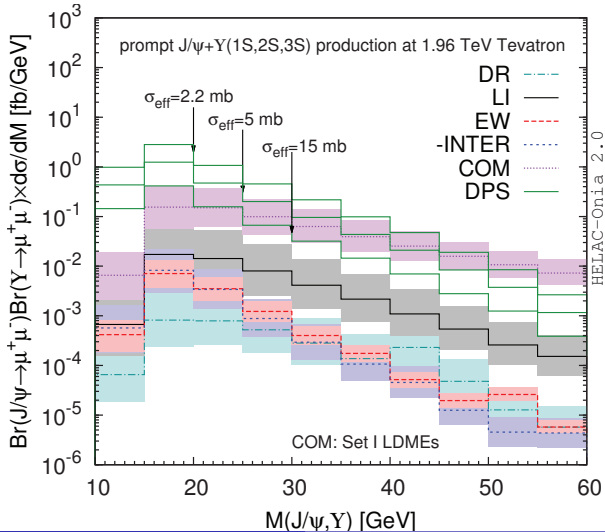
## dphi @ D0



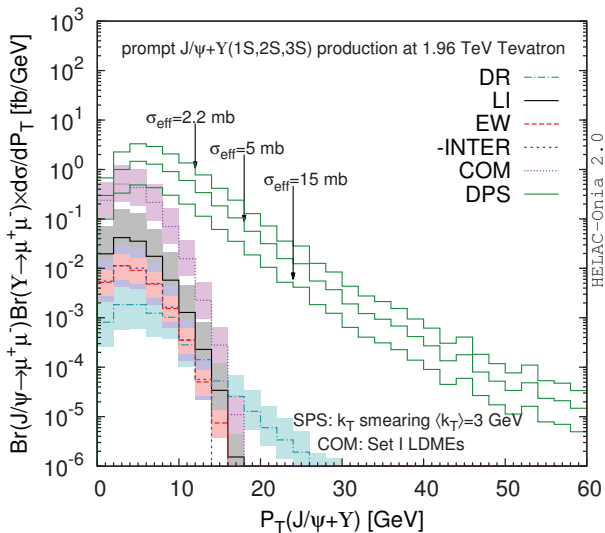
# dy @ D0



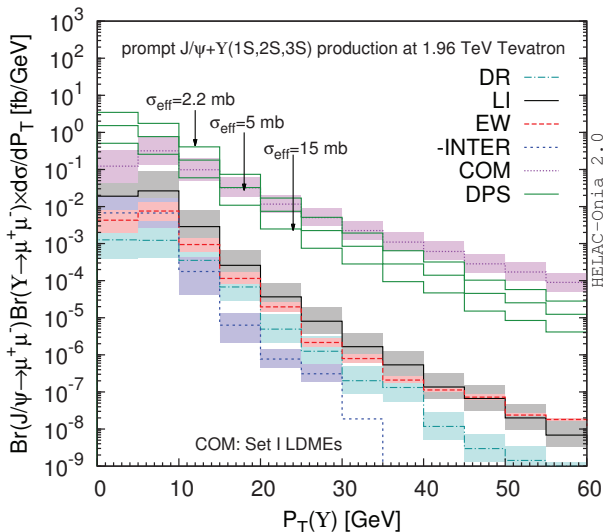
## dM @ D0



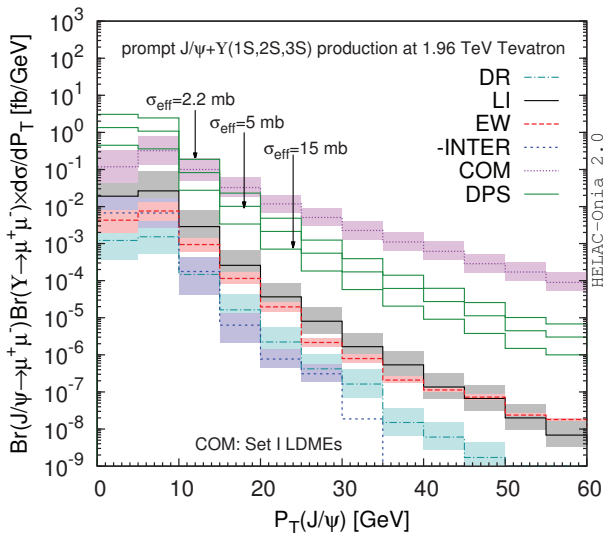
## dPt @ D0



## dptY @ D0

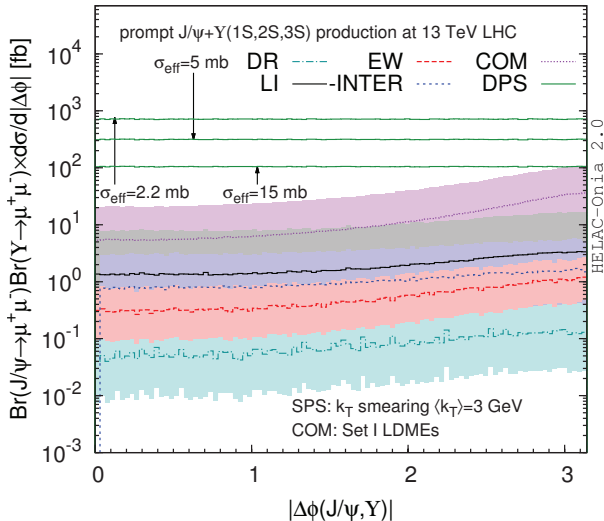


## dptpsi @ D0

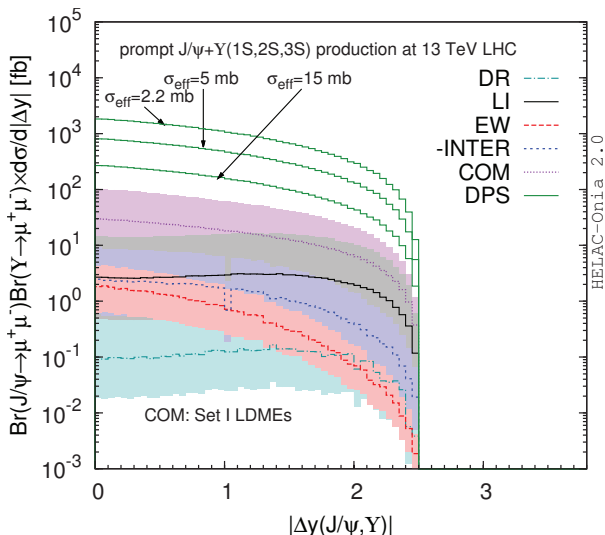




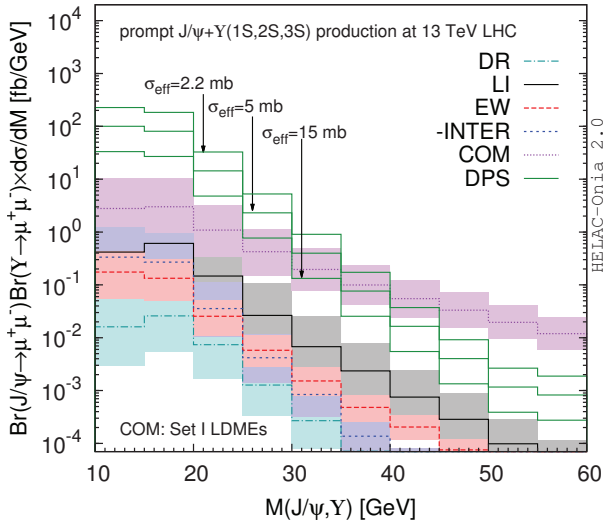
## dphi @ LHCb



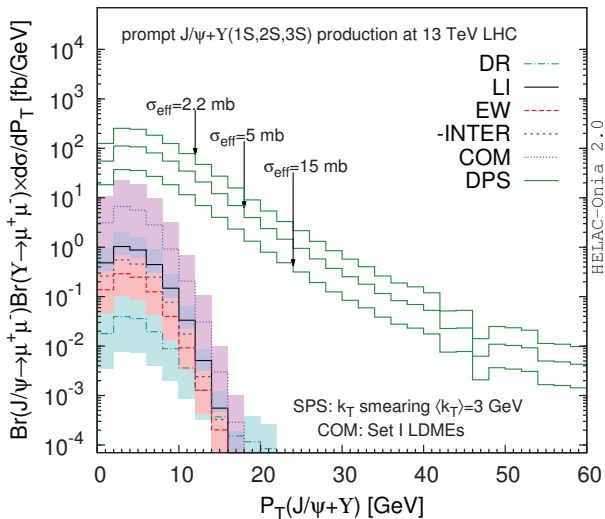
# dy @ LHCb



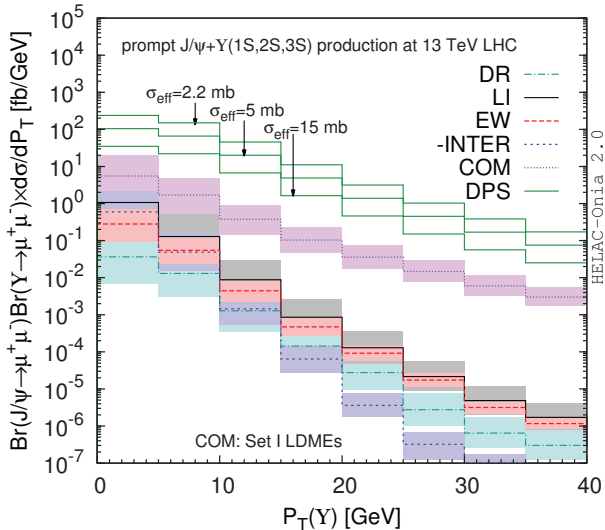
## dM @ LHCb



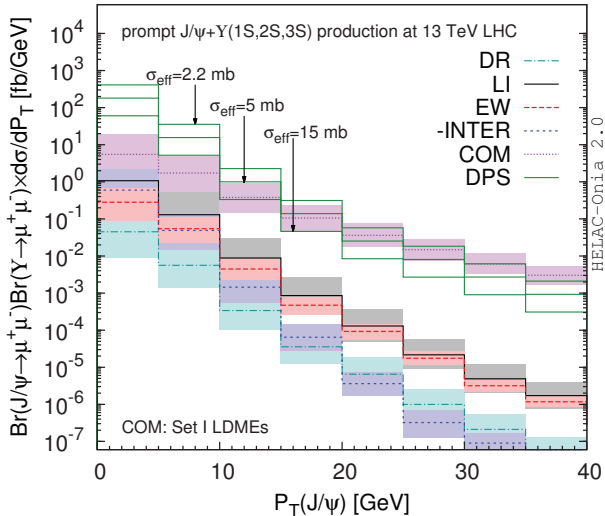
## dPt @ LHCb



## dptY @ LHCb



# dptpsi @ LHCb



## Summary

We have performed the first complete analysis of simultaneous production of prompt  $\psi$  and  $\Upsilon$  mesons including all leading SPS contributions.

Our work shows that it is in fact most probably dominated by DPS contributions for D0 data.

Finally, we also present our predictions of prompt  $J/\psi$  and  $\Upsilon$  production at the LHCb.