

# Project A7: Precision Computations in Hadron Physics

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together with Bastian Kubis and Cai-Dian Lü

PKU, Aug. 29th, 2017

# Three Topics

- Bounds on R-parity violating supersymmetry from  $B^0 - \bar{B}^0$  mixing. (H. Dreiner)
- Search for new physics in hadronic  $B$ -decays,  $\Delta S = 2$  transitions. (Cai-Dian Lü)
- Pseudoscalar transition form factors and  $(g - 2)_\mu$  (B. Kubis)

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Detailed talk by Zeren Simon Wang: 31/8

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Detailed talk by Faisal Munir: 30/8

- Pseudoscalar transition form factors and  $(g - 2)_\mu$  (B. Kubis)

# $B^0 - \bar{B}^0$ Mixing and RPV SUSY

## RPV-MSSM superpotential

$$W_{R_p} = \mu_i H_u L_i + \frac{1}{2} \lambda_{ijk} L_i L_j \bar{E}_k + \lambda'_{ijk} L_i Q_j \bar{D}_k + \frac{1}{2} \lambda''_{ijk} \bar{U}_i \bar{D}_j \bar{D}_k \quad (1)$$

- Create effective operators contributing to  $B^0 - \bar{B}^0$  mixing

# $B^0 - \bar{B}^0$ Mixing and RPV SUSY

Effective Lagrangian:

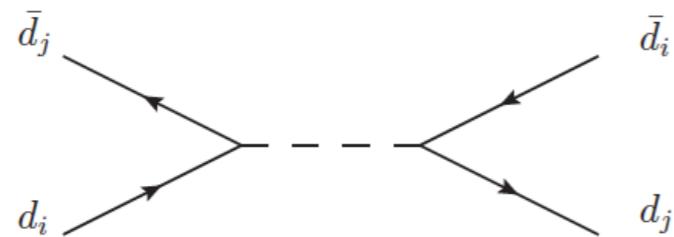
$$\mathcal{L}_{\text{eff}} = \sum_i C_i O_i + h.c.$$

$C_i$ : Wilson coefficients.  $O_i$ : dim-6 operators.

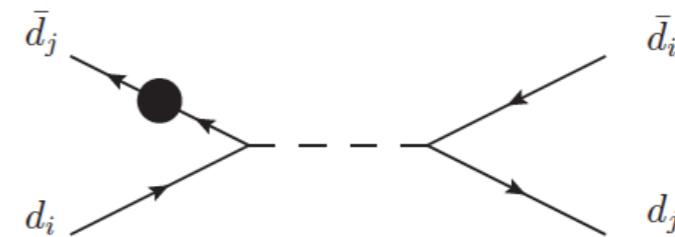
$$\begin{aligned} O_1 &= (\bar{d}_j \gamma^\mu P_L d_i)(\bar{d}_j \gamma_\mu P_L d_i), & \tilde{O}_1 &= (\bar{d}_j \gamma^\mu P_R d_i)(\bar{d}_j \gamma_\mu P_R d_i), \\ O_2 &= (\bar{d}_j P_L d_i)(\bar{d}_j P_L d_i), & \tilde{O}_2 &= (\bar{d}_j P_R d_i)(\bar{d}_j P_R d_i), \\ O_3 &= (\bar{d}_j^a P_L d_i^b)(\bar{d}_j^b P_L d_i^a), & \tilde{O}_3 &= (\bar{d}_j^a P_R d_i^b)(\bar{d}_j^b P_R d_i^a), \\ O_4 &= (\bar{d}_j P_L d_i)(\bar{d}_j P_R d_i), & O_5 &= (\bar{d}_j^a P_L d_i^b)(\bar{d}_j^b P_R d_i^a). \end{aligned}$$

$i, j = d, s, b$  down-type quarks,  $a, b = 1, 2, 3$  three colors.

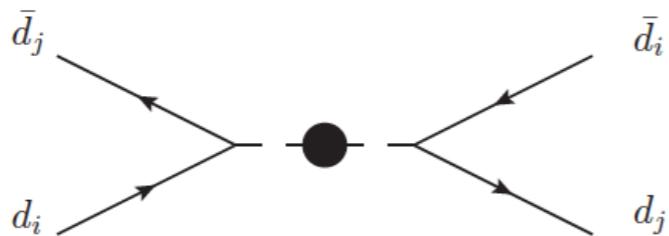
# $B^0 - \bar{B}^0$ Mixing and RPV SUSY



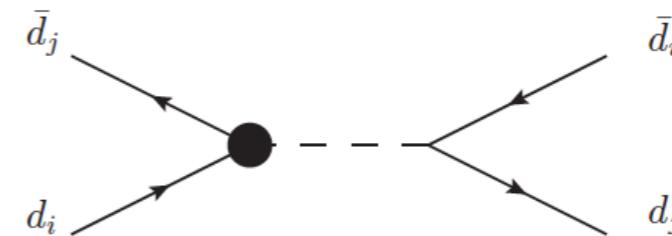
(a) Tree-level Feynman  
diagram



(b) Quark self-energies  
corrections

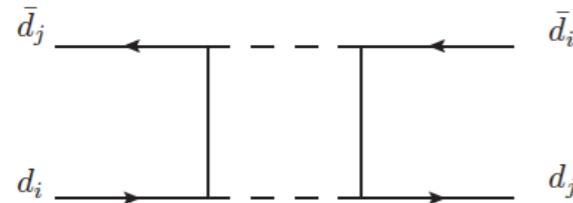


(c) Scalar self-energies

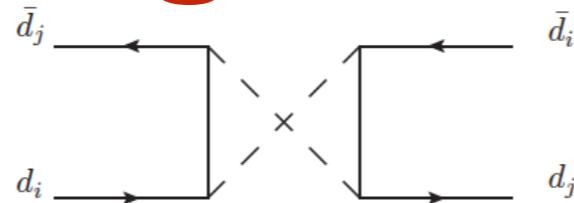


(d) Vertex corrections

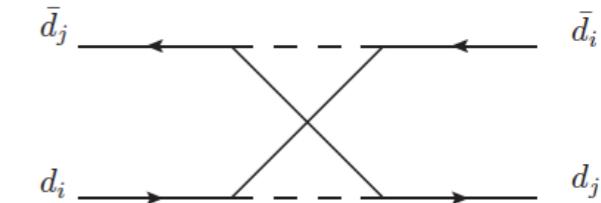
# $B^0 - \bar{B}^0$ Mixing and RPV SUSY



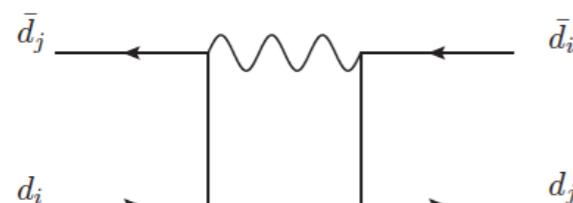
(a) S/F/S/F  
straight box



(b) S/F/S/F  
scalar-cross box



(c) S/F/S/F  
fermion-cross box



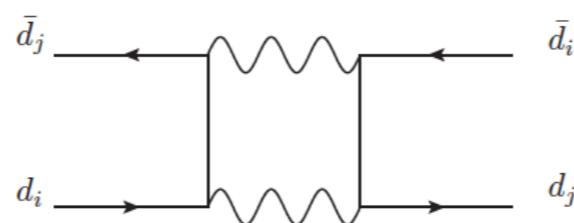
(d) V/F/S/F  
straight box



(e) V/F/S/F  
cross boxes



(f) V/F/S/F  
fermion-cross box



(g) V/F/V/F  
straight box

S: Scalar, F: Fermion, V: Vector



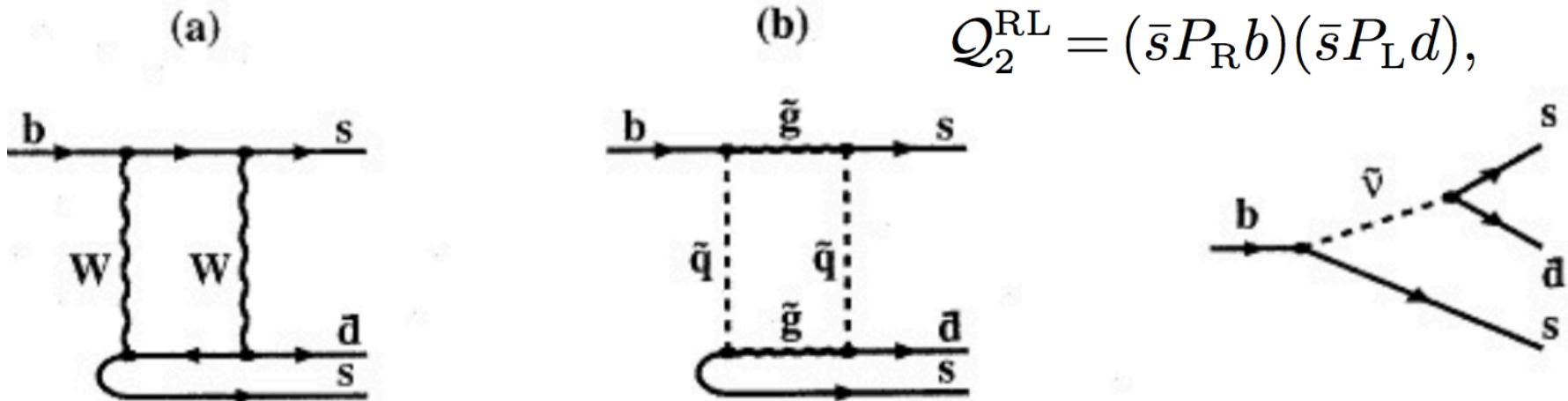
# Search for new physics in hadronic B decays

## - $\Delta S = 2$ transition (talk by F. Munir)

CD Lu, F. Munir, Q. Qin, Chin.  
 Phys. C41 (2017) 053106

**SM BRs:  $\sim 10^{-14}$ ,**  
**New physics can reach  $10^{-6}$**   
**Randall-Sundrum model  $\sim 10^{-10}$**

$$\begin{aligned} \mathcal{Q}_1^{\text{VLL}} &= (\bar{s}\gamma_\mu P_L b)(\bar{s}\gamma^\mu P_L d), \\ \mathcal{Q}_1^{\text{VRR}} &= (\bar{s}\gamma_\mu P_R b)(\bar{s}\gamma^\mu P_R d), \\ \mathcal{Q}_1^{\text{LR}} &= (\bar{s}\gamma_\mu P_L b)(\bar{s}\gamma^\mu P_R d), \\ \mathcal{Q}_2^{\text{LR}} &= (\bar{s}P_L b)(\bar{s}P_R d), \\ \mathcal{Q}_1^{\text{RL}} &= (\bar{s}\gamma_\mu P_R b)(\bar{s}\gamma^\mu P_L d), \\ \mathcal{Q}_2^{\text{RL}} &= (\bar{s}P_R b)(\bar{s}P_L d), \end{aligned}$$



$b \rightarrow ss\bar{d}$  transition (a) SM, (b) MSSM, (c) MSSM with R-parity violating coupling

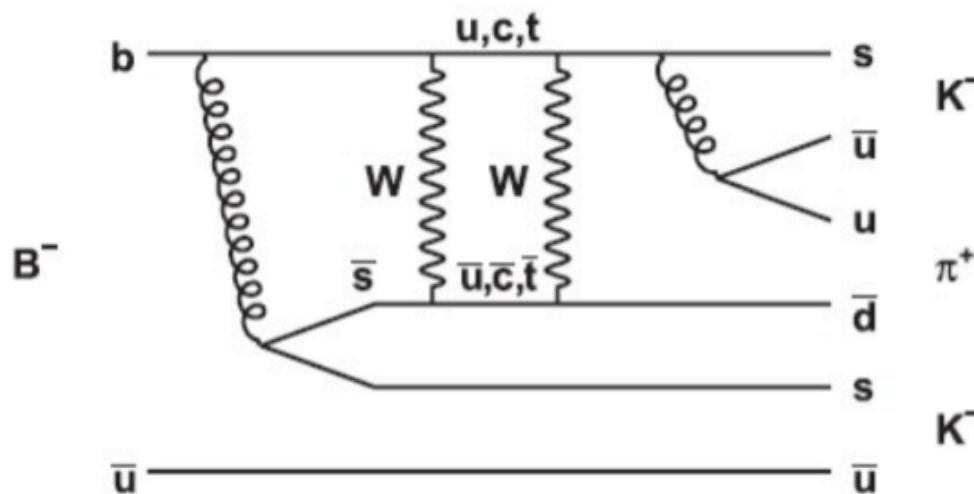


# Experimental search starting from OPAL @ LEP, phys. Lett. B 476 (2000) 233, later searched also by Belle/Babar

BABAR collaboration, Phys. Rev. D 78 (2008) 091102 [arXiv:0808.0900]

A search for the decay  $B^- \rightarrow K^- K^- \pi^+$ , Using a sample of  $(467 \pm 5) \times 10^6 B\bar{B}$  pairs collected with the BABAR detector.

LHCb, Phys.Lett. B765 (2017) 307-316



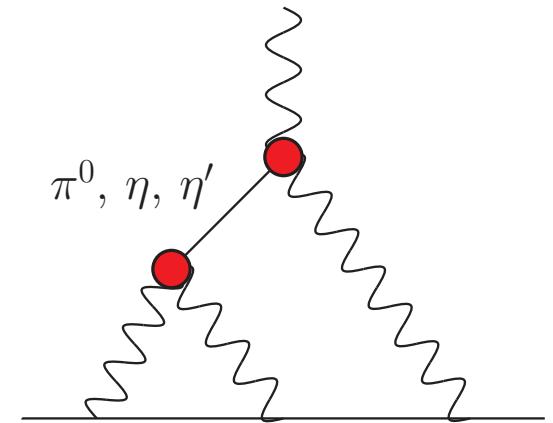
Similar channel  $B^- \rightarrow \pi^- \pi^- K^+$

Result : No evidence for these decays was found and a upper limit was set as

$$\mathcal{B}(B^+ \rightarrow K^+ K^+ \pi^-) < 1.1 \times 10^{-8} \quad \mathcal{B}(B^+ \rightarrow \pi^+ \pi^+ K^-) < 4.6 \times 10^{-8}.$$

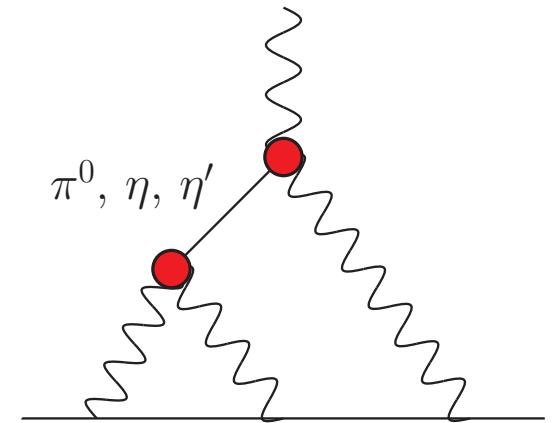
# Pseudoscalar transition form factors and $(g - 2)_\mu$

- largest individual HLbL contribution:  
pseudoscalar pole terms  
singly / doubly virtual form factors  
 $F_{P\gamma\gamma^*}(q^2, 0)$  and  $F_{P\gamma^*\gamma^*}(q_1^2, q_2^2)$



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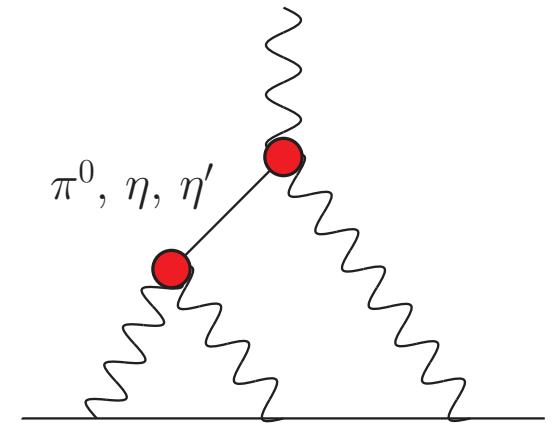
- normalisation fixed by Wess–Zumino–Witten anomaly, e.g.:

$$F_{\pi^0\gamma\gamma}(0, 0) = \frac{e^2}{4\pi^2 F_\pi}$$

$F_\pi$ : pion decay constant → measured at 1.5% level PrimEx 2011

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- $q_i^2$ -dependence: often modelled by vector-meson dominance
  - what can we learn from **analyticity and unitarity constraints?**
  - what **experimental input** sharpens these constraints?

# Dispersive analysis of $\pi^0/\eta^{(\prime)} \rightarrow \gamma^*\gamma^*$

- isospin decomposition:

$$F_{\pi^0\gamma^*\gamma^*}(q_1^2, q_2^2) = F_{\textcolor{red}{v}\textcolor{blue}{s}}(q_1^2, q_2^2) + F_{\textcolor{blue}{v}\textcolor{red}{s}}(q_2^2, q_1^2)$$

$$F_{\eta^{(\prime)}\gamma^*\gamma^*}(q_1^2, q_2^2) = F_{\textcolor{red}{v}v}(q_1^2, q_2^2) + F_{ss}(q_2^2, q_1^2)$$

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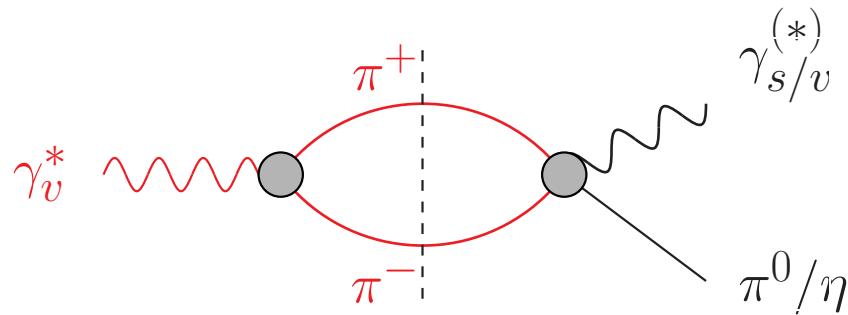
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- analyse the leading hadronic intermediate states:

Hanhart et al. 2013, Hoferichter et al. 2014



▷ isovector photon: 2 pions

$\propto$  pion vector form factor  $\times$   $\gamma^{(*)} \rightarrow 3\pi / \eta^{(\prime)} \rightarrow \pi\pi\gamma^{(*)}$

all determined in terms of pion–pion P-wave phase shift

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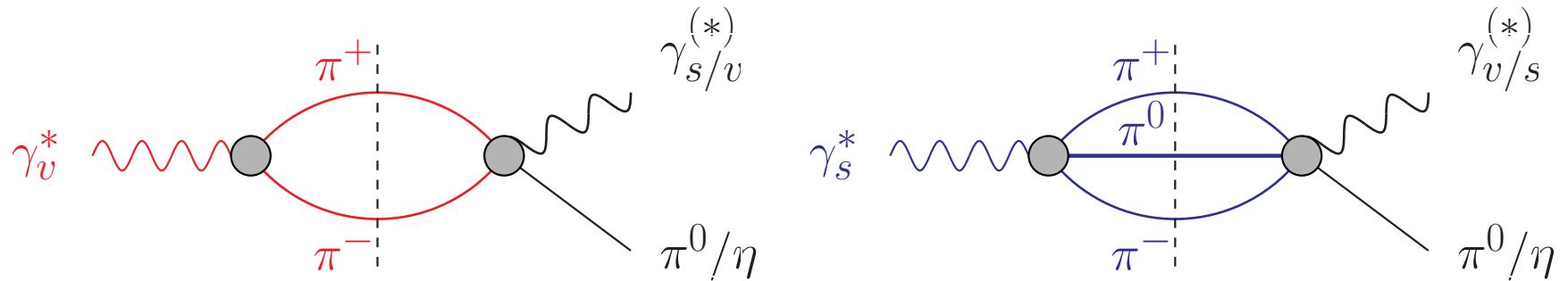
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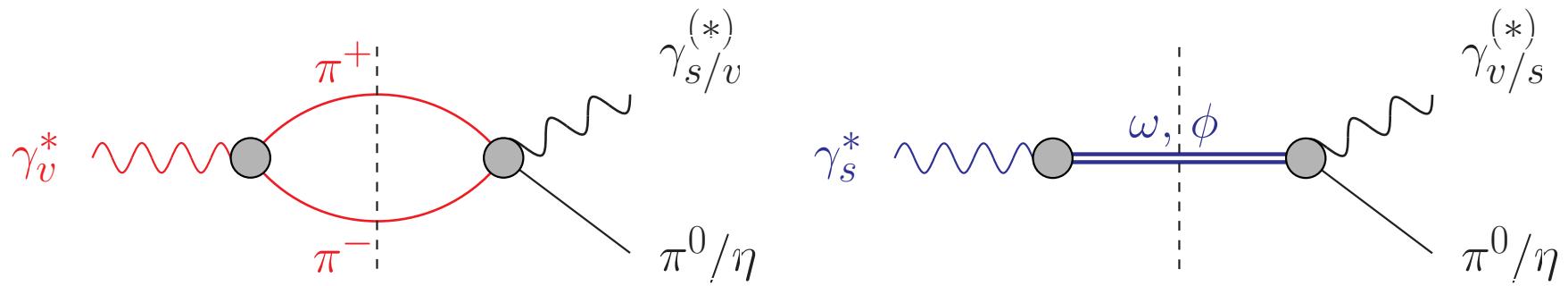
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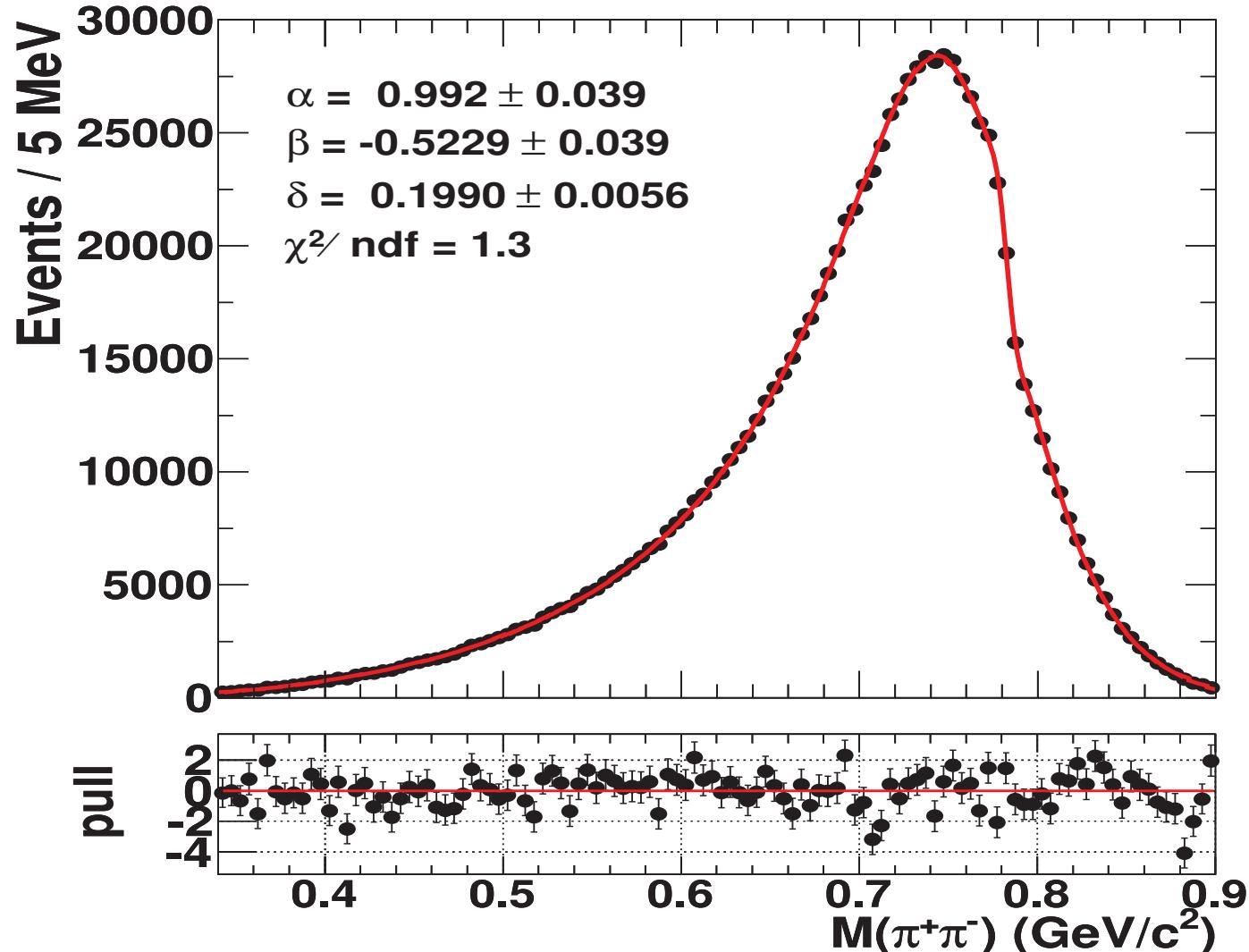
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▷ **isoscalar** photon: 3 pions  $\rightarrow$  dominated by narrow  $\omega, \phi$

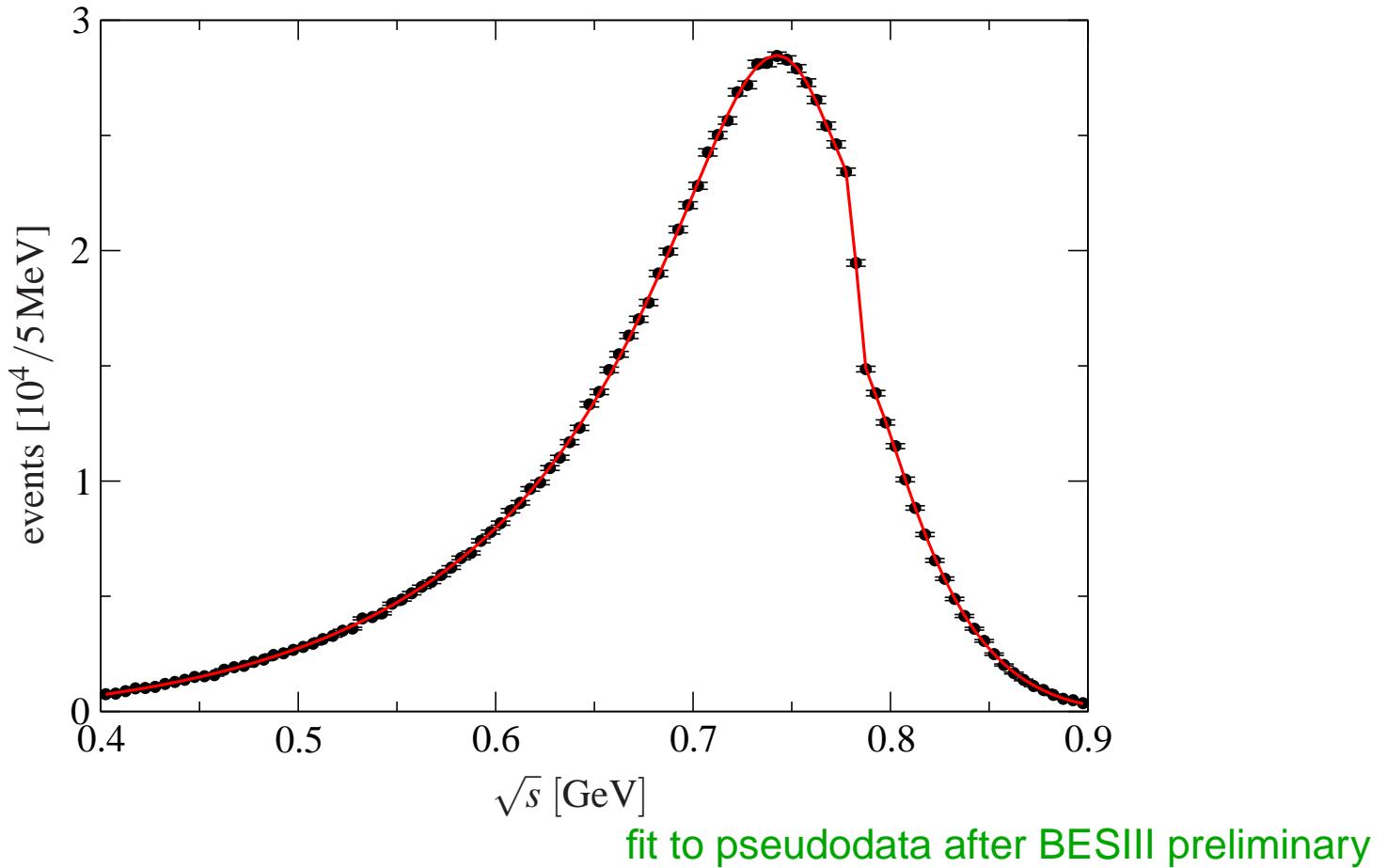
$\leftrightarrow \omega/\phi$  transition form factors; very small for the  $\eta$

# New BESIII data on $\eta' \rightarrow \pi^+ \pi^- \gamma$



BESIII preliminary, Fang 2015

# New BESIII data on $\eta' \rightarrow \pi^+ \pi^- \gamma$



- fit form 
$$\left[ A(1 + \alpha t + \beta t^2) + \frac{\kappa}{m_\omega^2 - t - im_\omega \Gamma_\omega} \right] \times \Omega(t)$$

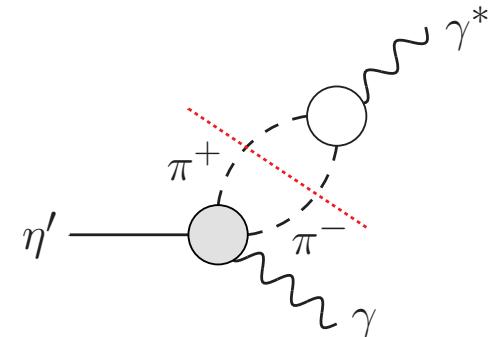
→ curvature  $\propto \beta t^2$  essential

→ even  $\rho-\omega$  mixing clearly visible

Hanhart et al. 2017

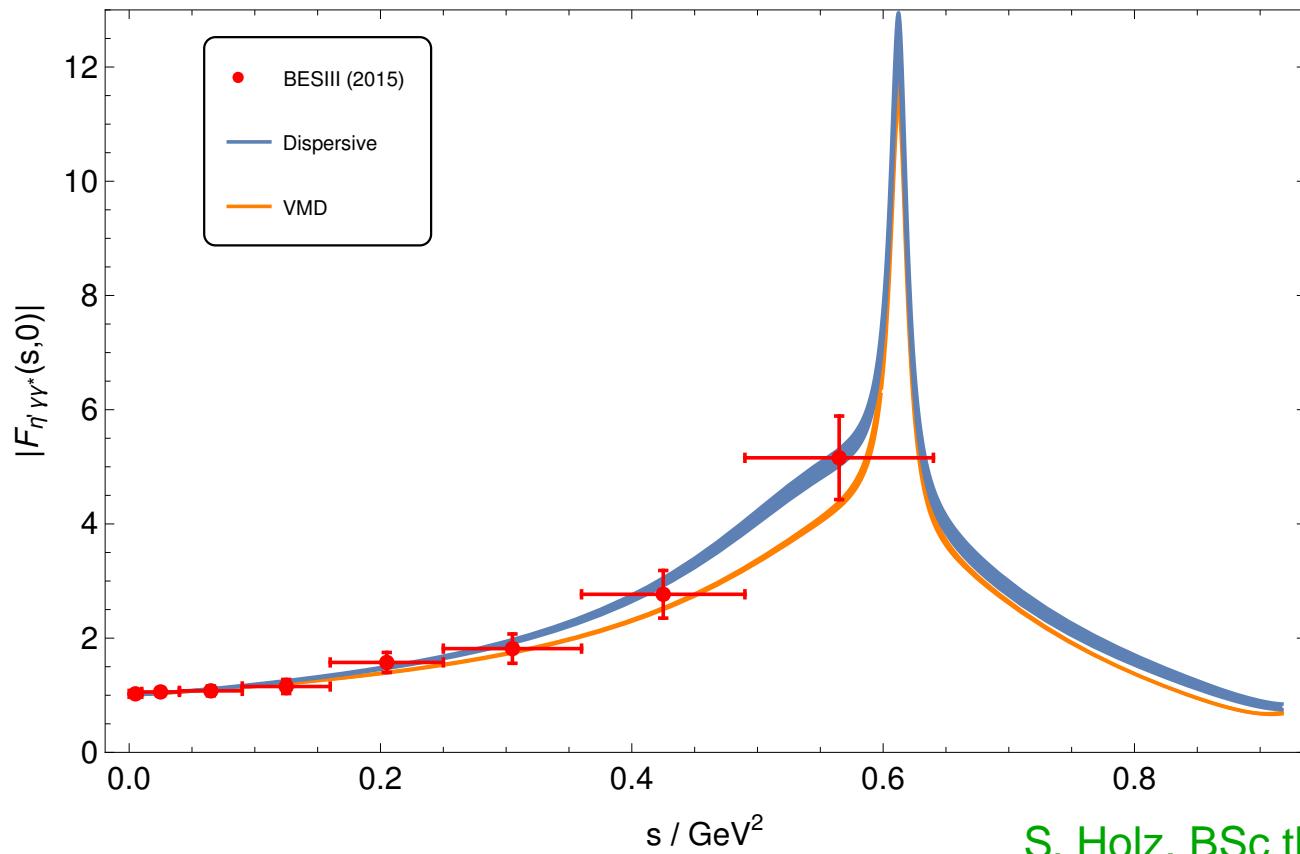
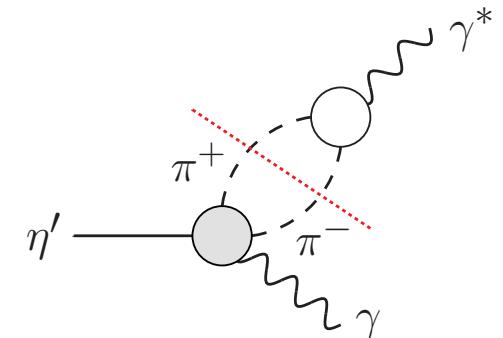
# Prediction for $\eta'$ transition form factor

- **isovector:** combine high-precision data on  $\eta' \rightarrow \pi^+ \pi^- \gamma$  and  $e^+ e^- \rightarrow \pi^+ \pi^-$
- **isoscalar:** VMD, couplings fixed from  $\eta' \rightarrow \omega \gamma$  and  $\phi \rightarrow \eta' \gamma$



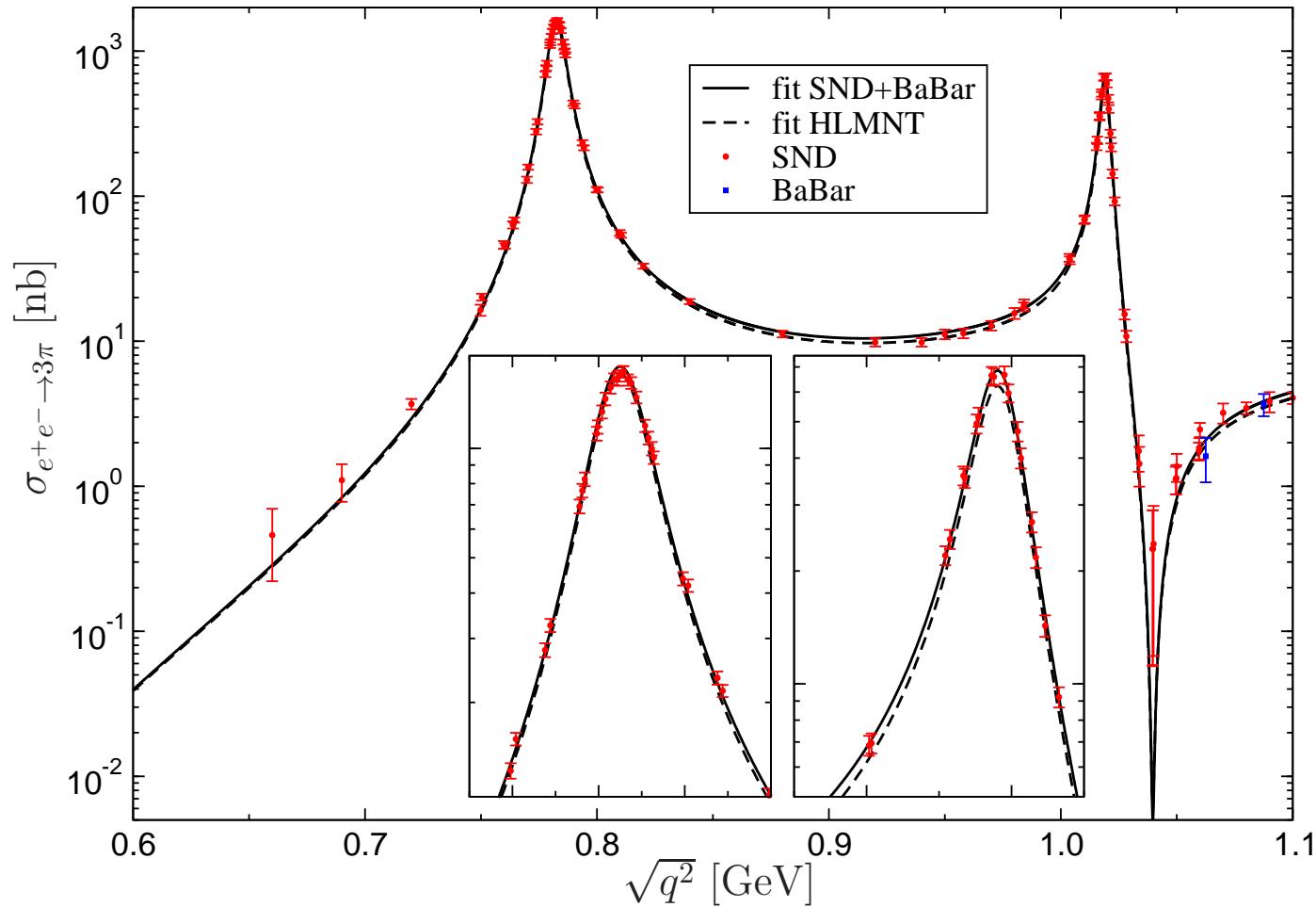
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S. Holz, BSc thesis 2016

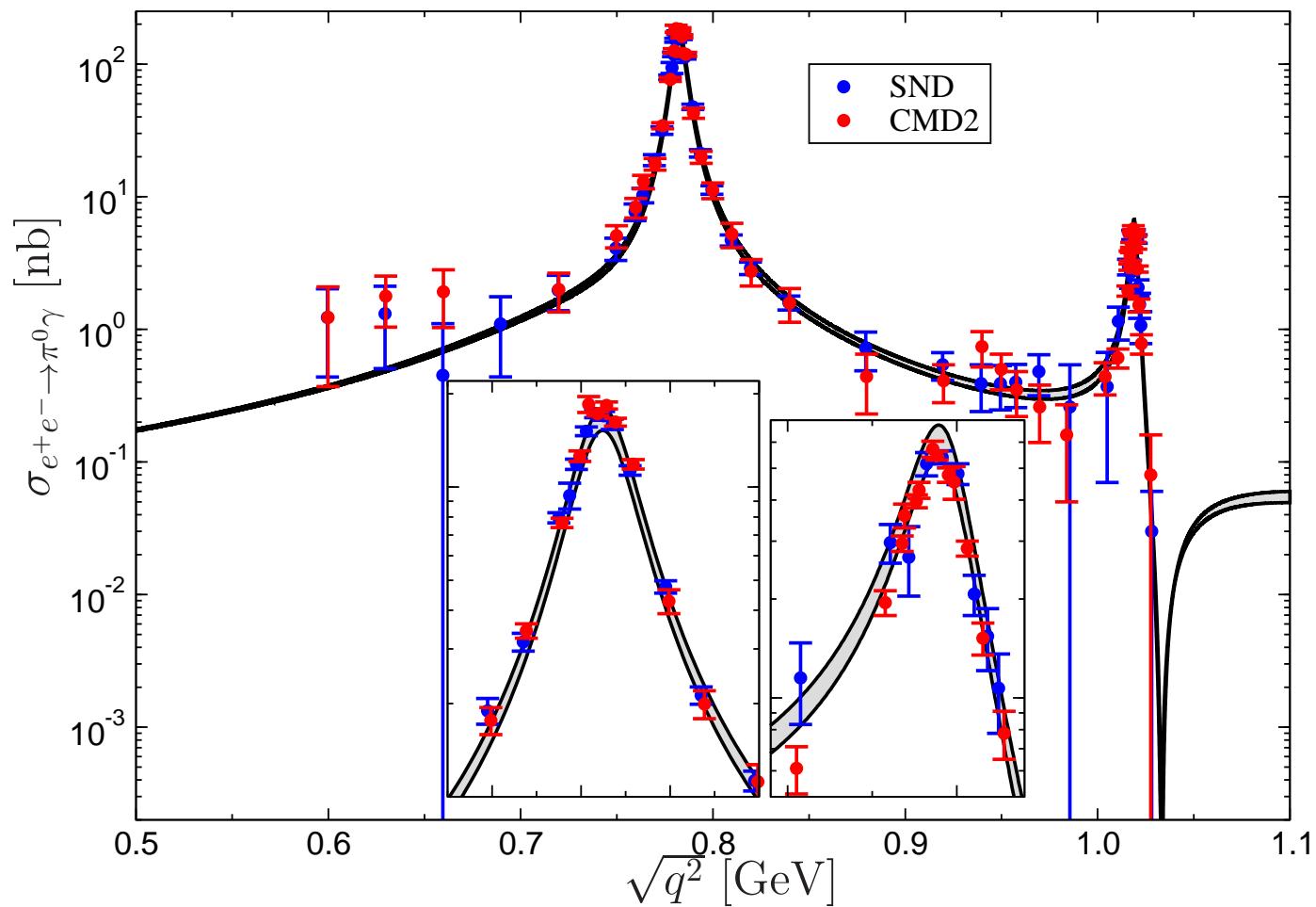
# Fit parametrisation to $e^+e^- \rightarrow 3\pi$ data...



Hoferichter, Kubis, Leupold, Niecknig, Schneider 2014

- one subtraction/normalisation at  $q^2 = 0$  fixed by  $\gamma \rightarrow 3\pi$
- fitted:  $\omega$ ,  $\phi$  residues, linear subtraction  $\beta$

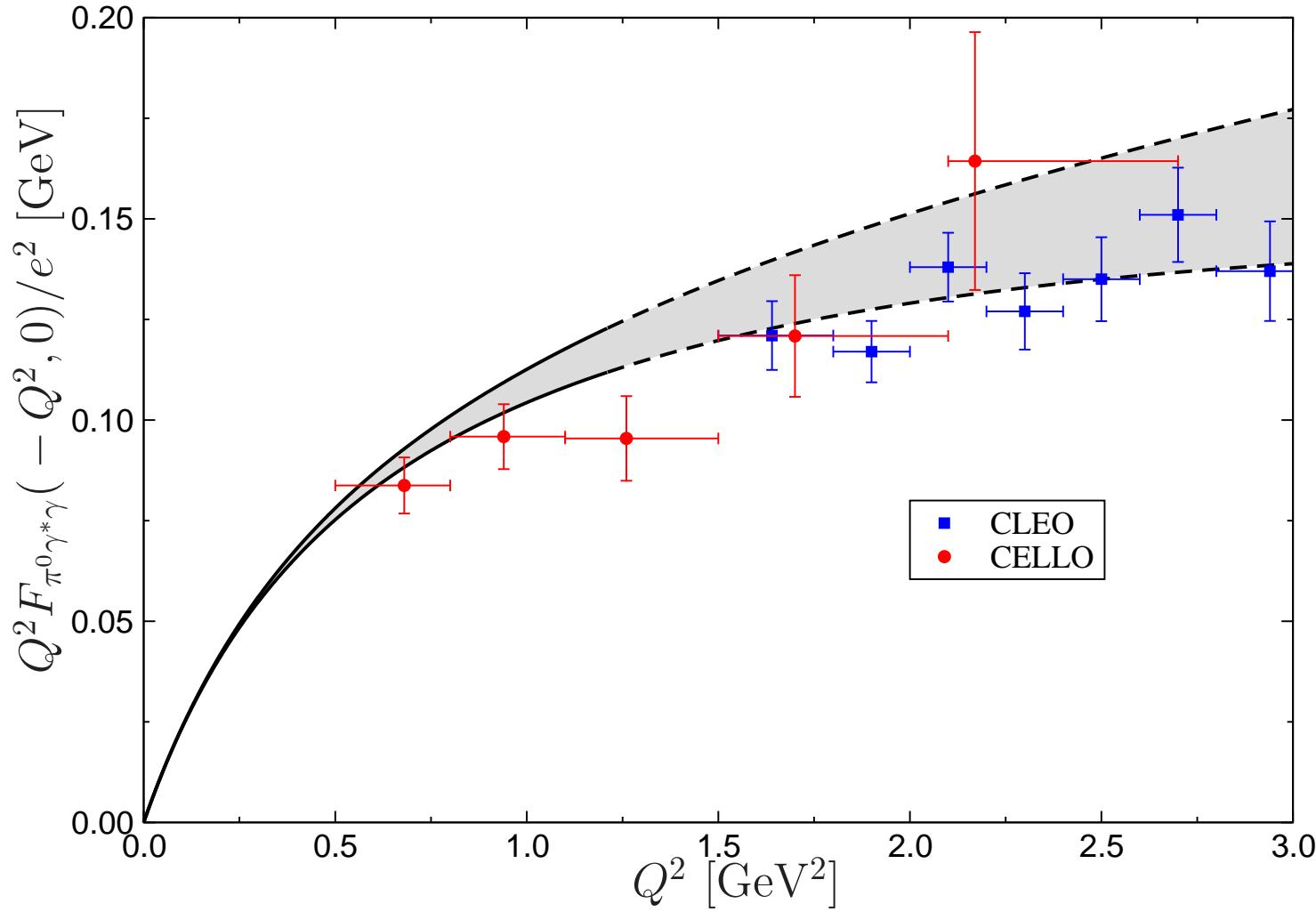
## ... predict/compare to $e^+e^- \rightarrow \pi^0\gamma$ data



Hoferichter, Kubis, Leupold, Niecknig, Schneider 2014

- "prediction"—no further parameters adjusted
- data very well reproduced

# Prediction spacelike form factor



Hoferichter, Kubis, Leupold, Niecknig, Schneider 2014

→ more precise low-energy spacelike data to come

BESIII

# Work in progress: high-energy constraints

- (low-energy) double-spectral-function representation:

$$F_{\pi^0 \gamma^* \gamma^*}(q_1^2, q_2^2) = \frac{1}{\pi^2} \int_{s_{\text{thr}}}^{s_m} dx \int_{4M_\pi^2}^{s_m} dy \left[ \frac{\rho^{\text{disp}}(x, y)}{(x - q_1^2)(y - q_2^2)} + (q_1^2 \leftrightarrow q_2^2) \right]$$

- light-cone pQCD representation in terms of pion wave function:

$$\begin{aligned} F_{\pi^0 \gamma^* \gamma^*}(q_1^2, q_2^2) &= -\frac{2e^2 F_\pi}{3} \int_0^1 dx \frac{\phi_\pi(x)}{x q_1^2 + (1-x) q_2^2} \\ &\longrightarrow \frac{1}{\pi^2} \int_{s_m}^\infty dx \int_{s_m}^\infty dy \frac{\rho^{\text{pQCD}}(x, y)}{(x - q_1^2)(y - q_2^2)} \end{aligned}$$

- the sum  $\rho(x, y) = \rho^{\text{disp}}(x, y) + \rho^{\text{pQCD}}(x, y)$  should reproduce

▷ Brodsky–Lepage limit  $\lim_{Q^2 \rightarrow \infty} F_{\pi^0 \gamma^* \gamma^*}(-Q^2, 0) = \frac{2 e^2 F_\pi}{Q^2}$

▷ OPE limit  $\lim_{Q^2 \rightarrow \infty} F_{\pi^0 \gamma^* \gamma^*}(-Q^2, -Q^2) = \frac{2 e^2 F_\pi}{3 Q^2}$

Long Bai et al., in progress