

Study of double Higgs production at 100 TeV

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on behalf of

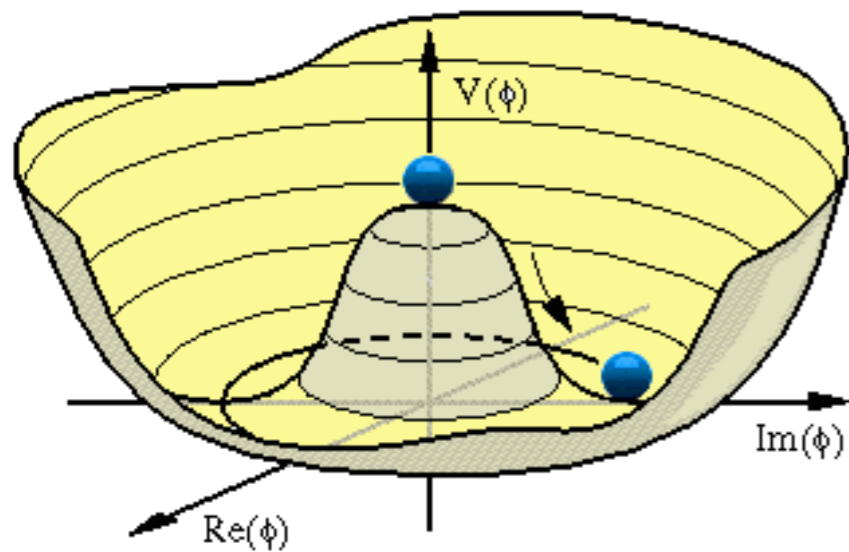
B. Di Micco, S. Braibant, M. Testa, M. Verducci et al.

Simulation and Physics Group Meeting,

August 28

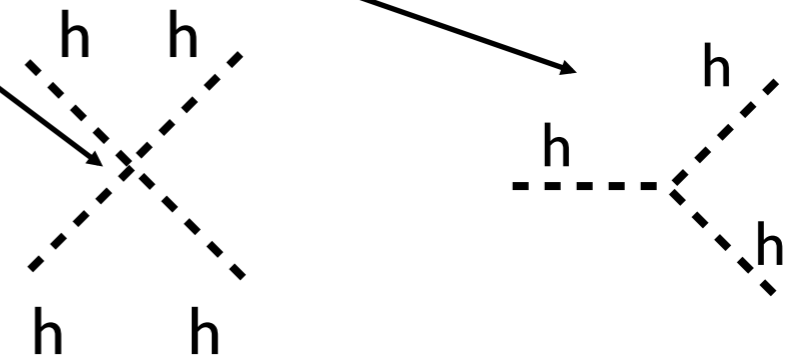
The Higgs potential

$$V(h) = \mu^2 \frac{h^2}{2} + \lambda \frac{h^4}{4}$$



After spontaneous symmetry breaking:

$$\lambda h_0^2 \eta^2 + \frac{\lambda}{4} \eta^4 + \lambda h_0 \eta^3$$
$$m_h^2 = 2\lambda h_0^2$$



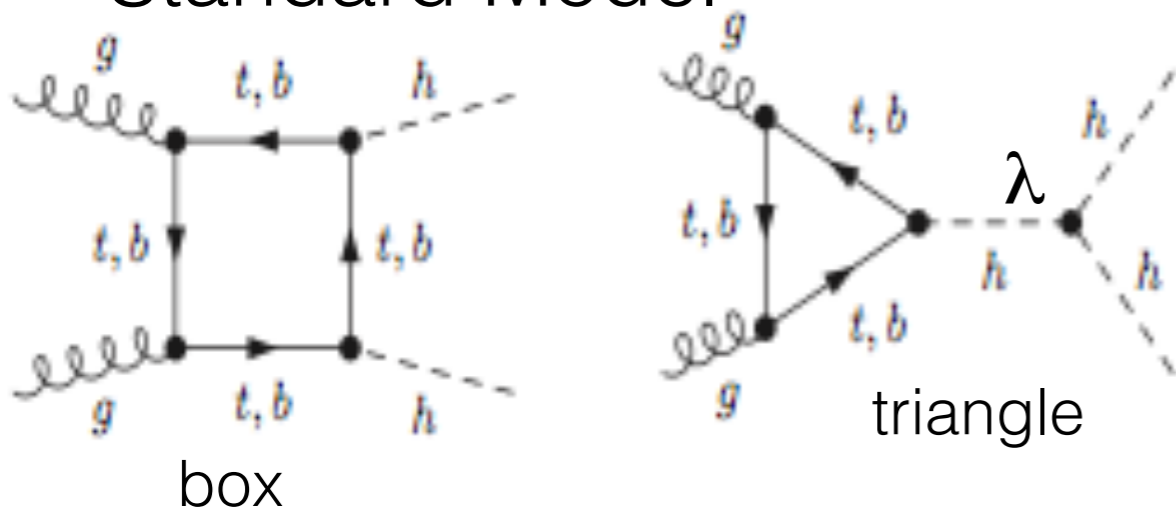
The strength of the **triple and quartic couplings** is fully fixed by the potential shape.

Why is it relevant?

- 1) it is the last missing ingredient of the SM, like the Higgs boson was the last missing particle, we need to prove that things really behave like we expect;
- 2) It has implications on the stability of the Vacuum;
- 3) It could make the Higgs boson a good inflation field (see backup)

HH production and decay

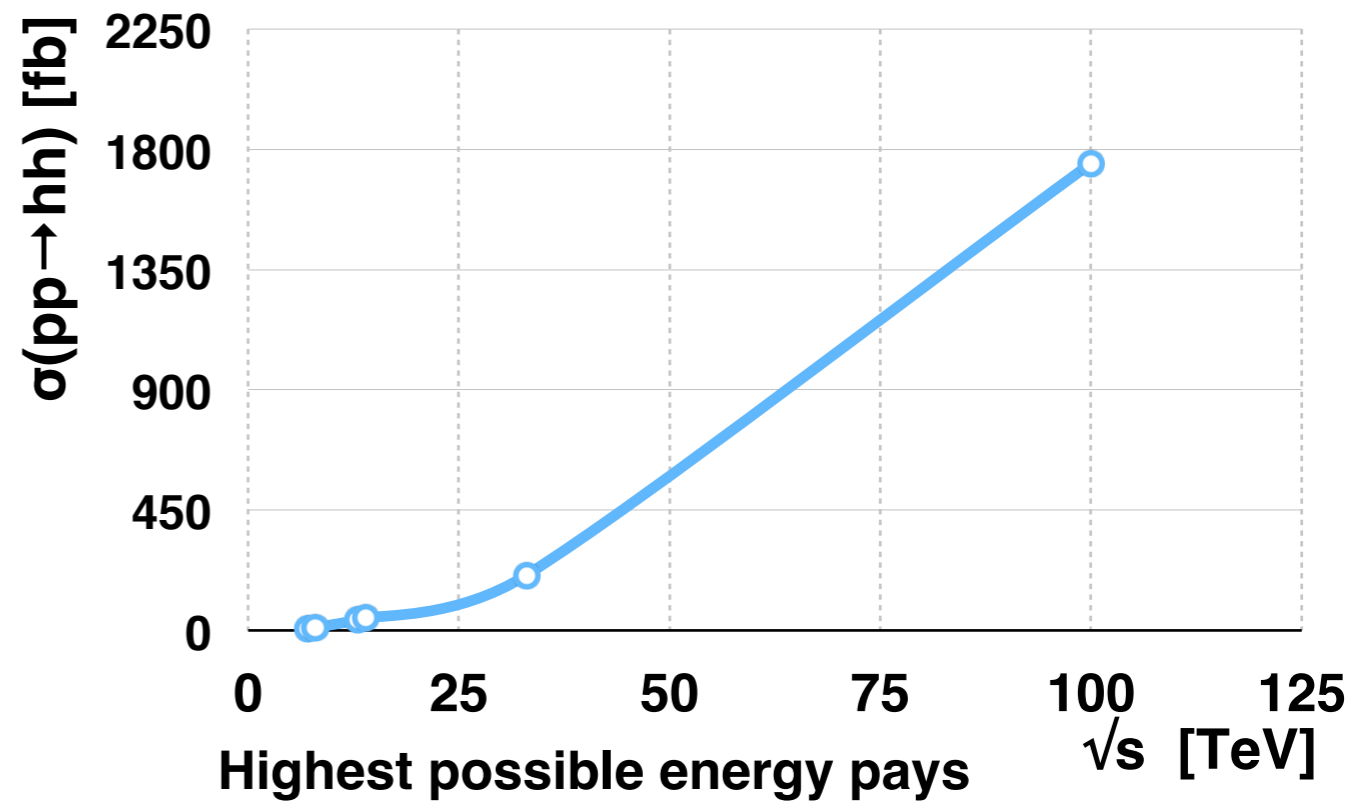
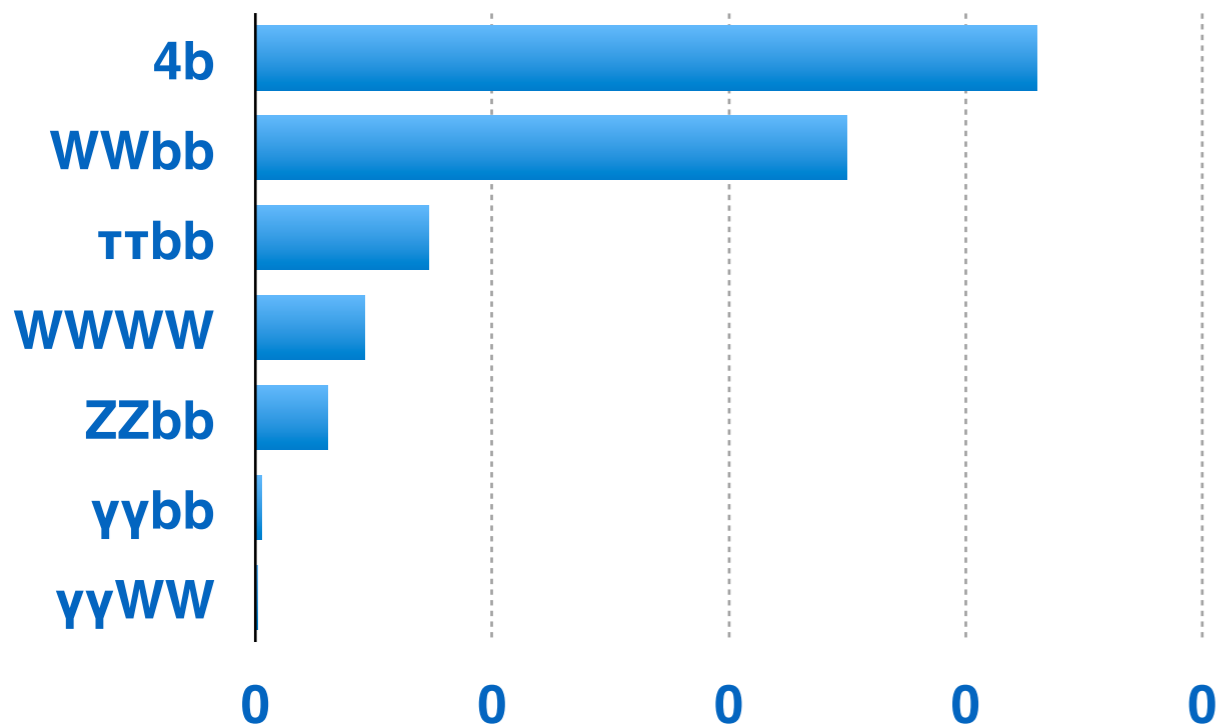
Standard Model



NNLO with full top mass *NLO $m_t \rightarrow \infty$

$m_h = 125.09$ GeV	$\sigma(\text{fb})$	scale unc. (%)	PDF unc. (%)	α_s unc.
$\sqrt{s} = 7$ TeV	7,71	+4.0/-5.7	± 3.4	± 2.8
$\sqrt{s} = 8$ TeV	11,17	+4.1/- 5.7	± 3.1	± 2.6
$\sqrt{s} = 13$ TeV	37,91	+4.3/-6.0	± 2.1	± 2.3
$\sqrt{s} = 14$ TeV	45,00	+4.4-6.0	± 2.1	± 2.2
$\sqrt{s} = 33$ TeV*	206,6	+15.1 - 12.5	+5.8/-5.0	
$\sqrt{s} = 100$ TeV	1748	+5.1/-6.5	± 1.7	± 2.0

Higgs decay branching fraction



Current status @LHC

	\sqrt{s} [TeV]	L (fb ⁻¹)	σ (fb) 95% C.L.	σ/σ_{SM} 95%C.L.
ATLAS: 4b, bb $\tau\tau$, bb $\gamma\gamma$, WW $\gamma\gamma$ WWWW	8	20,3	< 470	< 48
ATLAS: 4b	13	13,3	< 1000	< 29
CMS: 4b	13	2,32	< 11760	< 310
ATLAS: WW $\gamma\gamma$	13	13,3	< 12900	< 340
ATLAS: bb $\gamma\gamma$	13	3,2	< 5400	< 142
CMS: bb $\tau\tau$	13	39,5	< 950	< 25
CMS: WWbb	13	36	< 3270	< 86

HL-LHC $\sqrt{s} = 14$ TeV, L = 3000 fb ⁻¹	Exp. sign	λ/λ_{SM} 95% C.L.	exp σ/σ_{SM}
ATLAS: bb $\gamma\gamma$	1.05 σ	[-0.8, 7.7]	< 1.7 [recalc.]
CMS: bb $\gamma\gamma$	1.6 σ		< 1.3
ATLAS: 4b	?	[0.2, 7.0] _{stat.} , [-3.5, 11]	< 1.5 _{stat.} , 5.2
CMS: 4b	0,67		< 2.9 _{stat.} , 7
ATLAS: bb $\tau\tau$	0.6 σ	[-4, 12]	< 4.3
CMS: bb $\tau\tau$	0,39		< 3.9 _{stat.} , 5.2
CMS: VVbb	0,45		< 4.6 _{stat.} , 4.9

Present best channel 4b, situation will change with higher statistics when syst. dominated channels will saturate their sensitivity.

HL-LHC doesn't seem able to provide a useful constraint on λ , it could probably provide an observation of the whole process.

FCC studies

- Main references

- Physics at a 100 TeV pp collider [arXiv:1606.09408]
- 1st FCC-hh Physics Workshop - 16-20 January 2017 CERN
- FCC-hh physics analysis meetings
- FCC week 2017 @ Berlin
- studies performed with different level of details, in particular trigger, eff. simulation and pile-up studies need to be implemented in many of them, but first bulk of phys. potentiality ready.

Physics at a 100 TeV pp collider: Higgs and EW symmetry breaking studies

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FCC studies: $HH \rightarrow bb\gamma\gamma$

Selection:

- 2γ , 2 b-jet $|\eta| < 4.5$, $p_T^{\text{sub}} > 35$, $p_T^{\text{lead}} > 60$ GeV
- $|m_{\gamma\gamma} - m_h| < 2.0$, $100 < m_{bb} < 150$ GeV
- $p_T^{bb}, p_T^{\gamma\gamma} > 100$ GeV, $\Delta R_{bb}, \Delta R_{\gamma\gamma} < 3.5$

Simulation:

- 6T magnetic field
- Signal LO samples
- Pythia6 showering
- No pile-up simulation

Process	Acceptance cuts [fb]	Final selection [fb]	Events ($L = 30 \text{ ab}^{-1}$)
$h(b\bar{b})h(\gamma\gamma)$ (SM)	0.73	0.40	12061
$bbj\gamma$	132	0.467	13996
$jj\gamma\gamma$	30.1	0.164	4909
$t\bar{t}h(\gamma\gamma)$	1.85	0.163	4883
$b\bar{b}\gamma\gamma$	47.6	0.098	2947
$b\bar{b}h(\gamma\gamma)$	0.098	7.6×10^{-3}	227
$bj\gamma\gamma$	3.14	5.2×10^{-3}	155
Total background	212	1.30	27118

S/\sqrt{B} 23 [3 ab^{-1}] 73 [30 ab^{-1}]

$\Delta\sigma/\sigma = 1.6\%$ [30 ab^{-1}] $\Delta\lambda/\lambda = 6\%$ [2.5% sig. syst.]

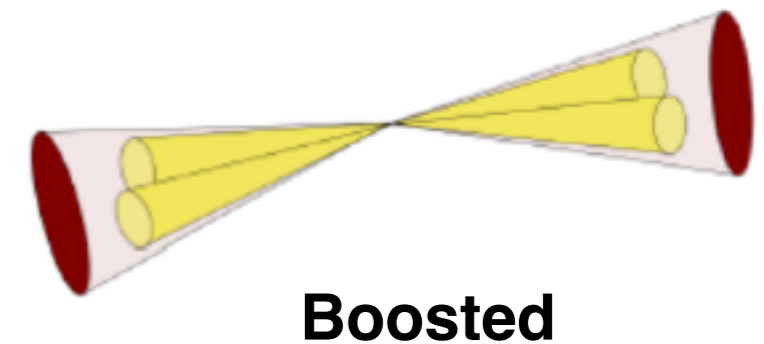
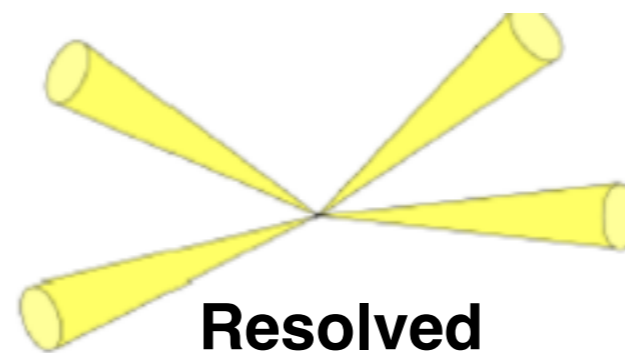
FCC studies: $HH \rightarrow bbbb$

Main background: multi-jet 4b

Strategy: truth level study,

resolved + boosted analysis

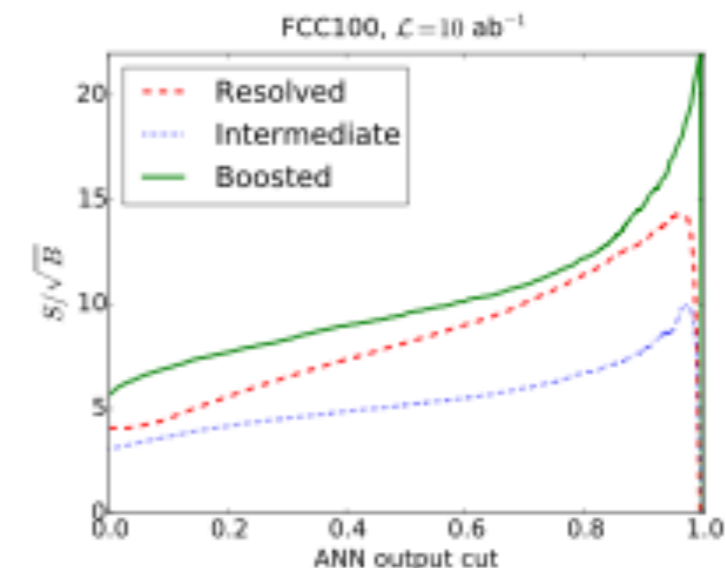
(Neural Network used as signal discriminator)



- R 0.4 jets $p_T > 40$ GeV, $|\eta| < 2.5$
- R 1.0 jets $p_T > 200$ GeV, $|\eta| < 2.0$
- R 0.3 jets ghost ass. to R 1.0 $p_T > 50$ $|\eta| < 2.5$

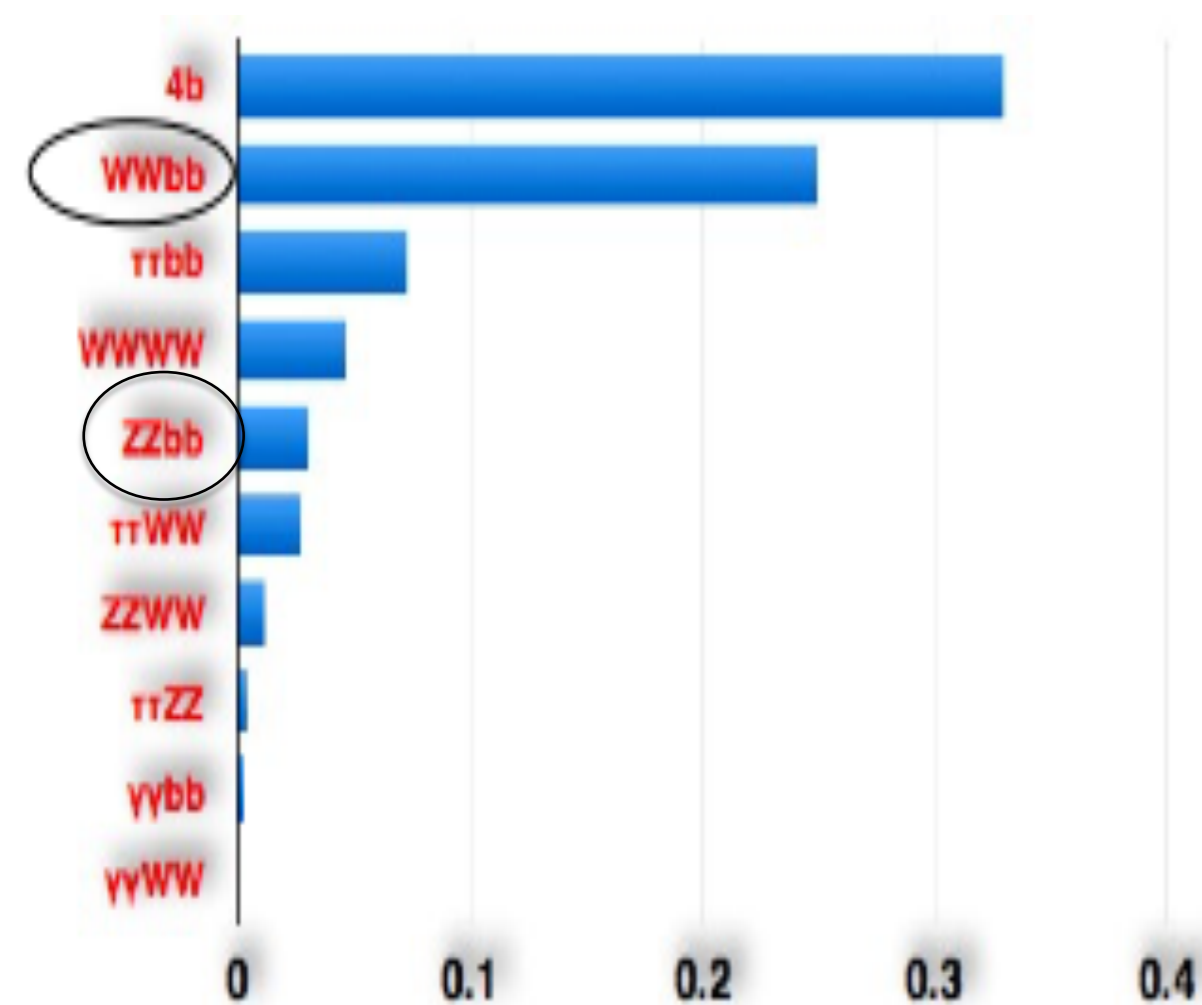
$L = 10 \text{ ab}^{-1}$

Category		N_{ev} signal	N_{ev} back	S/\sqrt{B}	S/B
Boosted	$y_{cut} = 0$	$5 \cdot 10^4$	$8 \cdot 10^7$	6	$6 \cdot 10^{-4}$
	$y_{cut} = 0.99$	$2 \cdot 10^4$	$1 \cdot 10^6$	22	$2 \cdot 10^{-2}$
Intermediate	$y_{cut} = 0$	$3 \cdot 10^4$	$1 \cdot 10^8$	3	$3 \cdot 10^{-4}$
	$y_{cut} = 0.98$	$2 \cdot 10^4$	$2 \cdot 10^6$	10	$7 \cdot 10^{-3}$
Resolved	$y_{cut} = 0$	$1 \cdot 10^5$	$8 \cdot 10^8$	4	$1 \cdot 10^{-4}$
	$y_{cut} = 0.95$	$6 \cdot 10^4$	$2 \cdot 10^7$	15	$4 \cdot 10^{-3}$



25% on σ with $S/B \sim 4 \cdot 10^{-3}$,
 $\Delta B/B \sim 10^{-3}$ (very challenging)

Current studies: Italian contribution



Between the final state from the HH decay:

- 4b, WWbb are dominant
- $\gamma\gamma bb$, ZZbb are the cleanest

The Italian community started to work in 2016 on:

- WWbb, lnuqqbb
- ZZbb, 4lbb

Typically low yield and low background thanks to the multi-lepton final state

- We used a fast simulation tool (Delphes)
- Pileup simulation with 50, 200, 900 events

Last contributions to conferences:

- B. Di Micco, IFAE – Trieste – April 19-21 2017
- B. Di Micco, FCC Week – Berlin – May 29 – June 1 2017

$L=30 \text{ ab}^{-1}$	$\Delta\sigma/\sigma$	$\Delta\lambda/\lambda$
$\gamma\gamma bb$	1.3%	2.5%
4b	25% (S/B ~2%)	200%
ZZbb, 4l	~30%	~40%

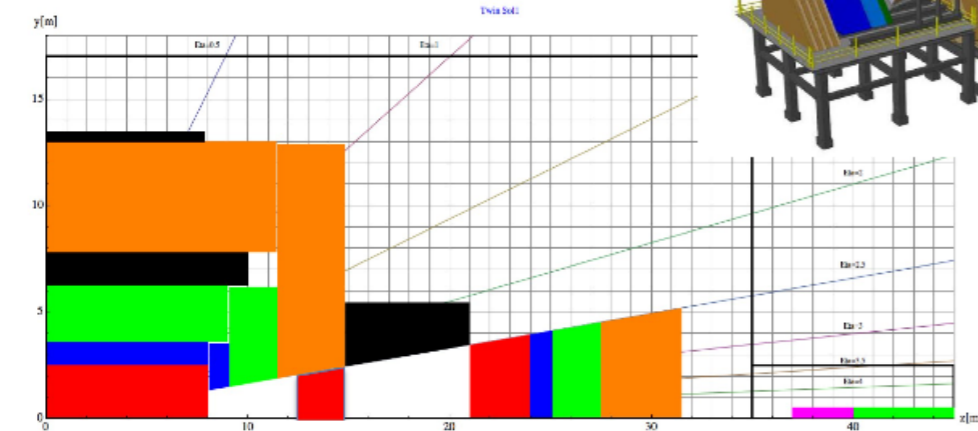
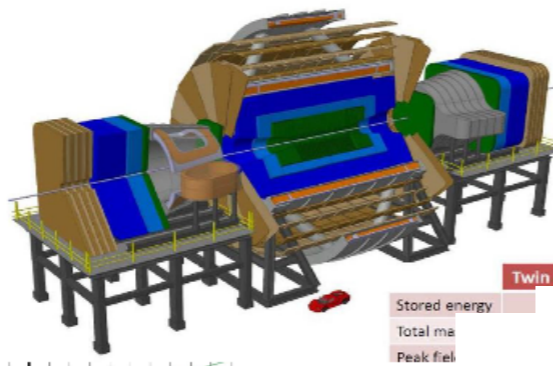
Pile-up and det. simulation with Delphes

S. Braibant (Bologna), B. Di Micco, M. Testa, M. Verducci (Roma 3)

pile-up configuration used in this presentation
(when used), simulated with Delphes using **CMS HL-LHC cards**

- 50, 200, 900 vertices

Base-line geometry
Twin solenoid +
Dipole magnetic system



Tracker
EMCAL
HCAL
Coil+Cryostat
Muon system

Fwd Tracker
Dipole

Detector simulation with
Delphes or simple
smearing of truth level
objects

7

Simulation of the 5 ns low and high luminosity phase and of the 25 ns high luminosity phase

Calorimetry

ECAL granularity:

0.0125 x 0.0125 $|\eta| < 2.5$

0.025 x 0.025 $2.5 < |\eta| < 4.0$

0.05 x 0.05 $4.0 < |\eta| < 6.0$

ECAL Energy Resolution:

$\sigma(E)/E = 10\% / \sqrt{E} \oplus 1\%$

$|\eta| < 6.0$

HCAL granularity:

0.05 x 0.05 $|\eta| < 2.5$

0.1 x 0.1 $2.5 < |\eta| < 4.0$

0.2 x 0.2 $4.0 < |\eta| < 6.0$

HCAL Energy Resolution:

$\sigma(E)/E = 50\% / \sqrt{E} \oplus 3\%$ $|\eta| < 4.0$

$\sigma(E)/E = 100\% / \sqrt{E} \oplus 5\%$ $|\eta| < 6.0$

Tracking

Efficiency c-quark jets:

4 % $|\eta| < 2.5$

3 % $2.5 < |\eta| < 4.0$

Efficiency light-quark jets:

0.1 % $|\eta| < 2.5$

0.075 % $2.5 < |\eta| < 4.0$

Efficiency b-quark jets:

75% WWbb 85 % ZZbb $|\eta| < 2.5$

64% $2.5 < |\eta| < 4.0$

z_0 resolution (*)

• in $|\eta| < 2.5$

$\sigma(z_0) = 0.01$ mm, $p_T < 5$ GeV

$\sigma(z_0) = 0.005$ mm, $p_T > 5$ GeV

• In $2.5 < |\eta| < 4$

$\sigma(z_0) = 0.1$ mm, $p_T < 5$ GeV

$\sigma(z_0) = 0.05$ mm, $p_T > 5$ GeV

• In $4.0 < |\eta| < 6.0$

$\sigma(z_0) = 1.0$ mm, $p_T < 5$ GeV

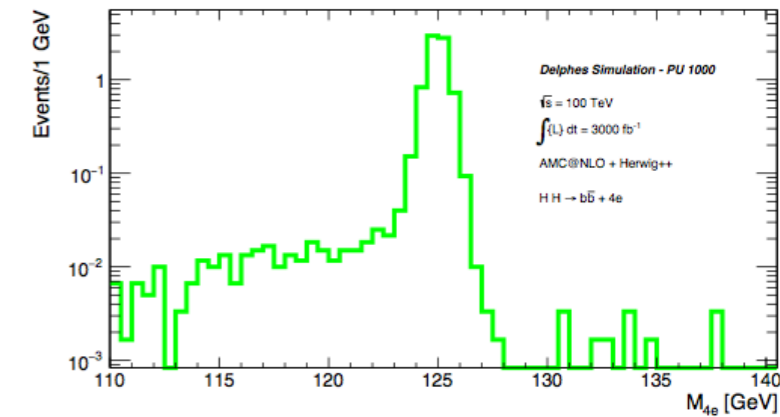
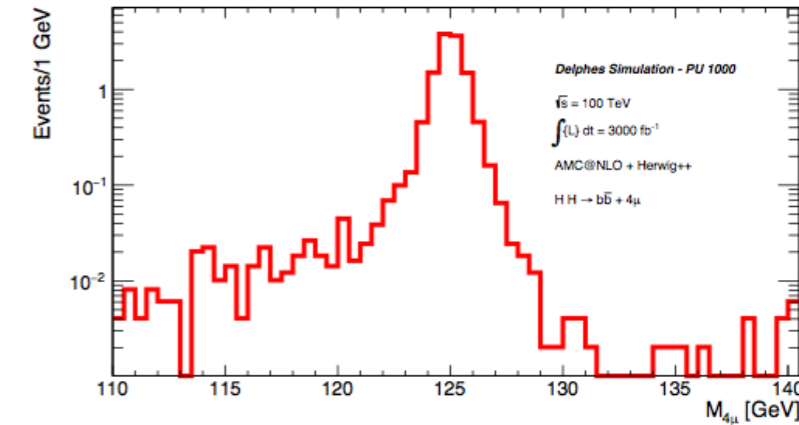
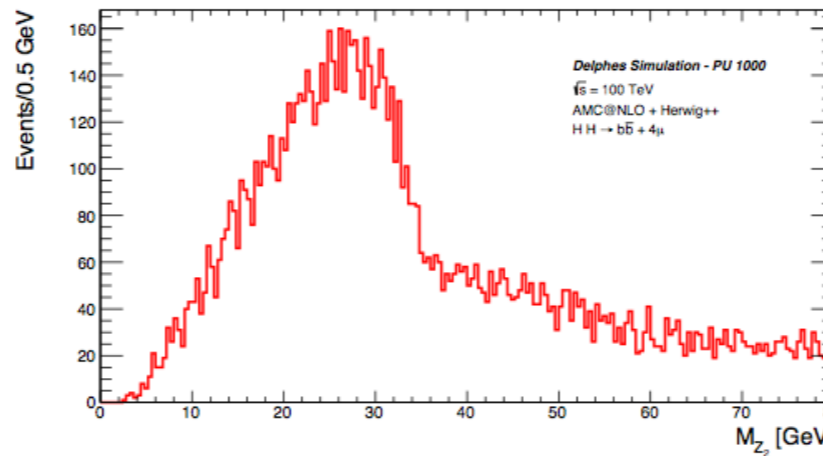
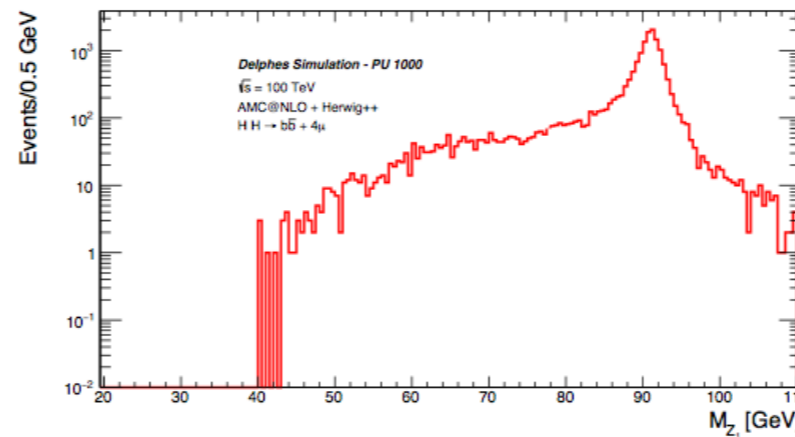
$\sigma(z_0) = 0.5$ mm, $p_T > 5$ GeV

HH → ZZbb → 4lbb, l=e,μ

N. De Filippis (Bari), S. Braibant (Bologna)

- ≥ 4 muons with $p_T > 5$ GeV, $|\eta| < 4.0$
- ≥ 4 electrons with $p_T > 7$ GeV, $|\eta| < 4.0$
- Z₁ selection: l^+l^- pair with mass close to the nominal Z boson mass
40 GeV < m_{Z1} < 120 GeV
- Z₂ selection: second l^+l^- pair
12 GeV < m_{Z2} < 120 GeV
- Among the 4 selected leptons: at least one with p_T>20 GeV and one with p_T>1 GeV
- QCD suppression: m(l⁺l⁻) > 4 GeV
- Kinematic cuts: m_{4l} > 120 GeV, m_{4l} < 130 GeV
- At least 2 b-jets with p_T > 30 GeV

$$\mathcal{L} = 3 \text{ ab}^{-1}$$



	$\sigma \cdot \mathcal{L} \cdot \text{Br}(hh \rightarrow ZZbb \rightarrow 4lbb)$	no b-jet req.	with b-jet	ϵ (no b-jet)	ϵ (b-jet)
4e					
4μ	161	61	12,1	38%	7,4%
4e	161	40	7,7	25%	4,8%
Tot	322	101	20	31%	6,2%

- forward b-tagging can be an important ingredient of the analysis, need to test configuration with fwd dipole
- big impact from lepton isolation cut (not presented here) → bug found in Delphes

Object in PU environment [WWbb analysis]

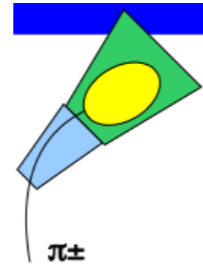
B. Di Micco, M. Testa, M. Verducci (Roma 3)

◆ Particle Flow Reconstruction

- Using charged hadrons, muons, electrons and calorimeter towers to build particle-flow objects
- Tracks from pile-up are rejected if $|Z_0 - Z_{PV}| > \sqrt{\sigma^2(Z_0) + \sigma^2(Z_{PV})}$

◆ Jets

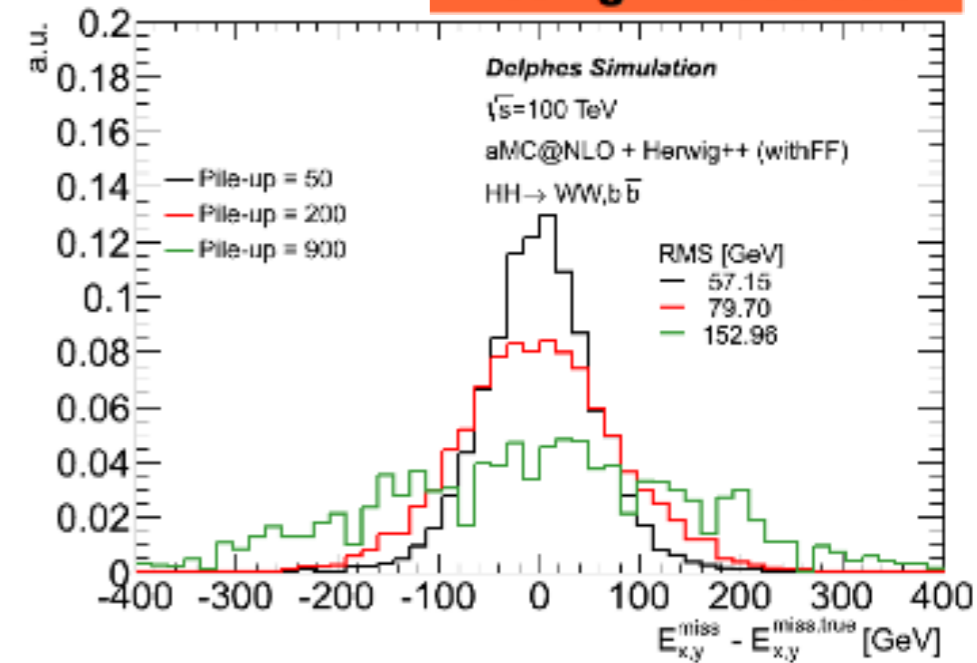
- Anti-Kt (Fast Jet) algorithm
- particle-flow objects as inputs
- $R = 0.4$
- Jet Area pile-up correction:
- private calibration to particle level $p_T^{\text{corrected}} = p_T^{\text{raw}} - \rho \cdot \text{JetArea}$
- $p_T^{\text{jet}} > 20 \text{ GeV}$



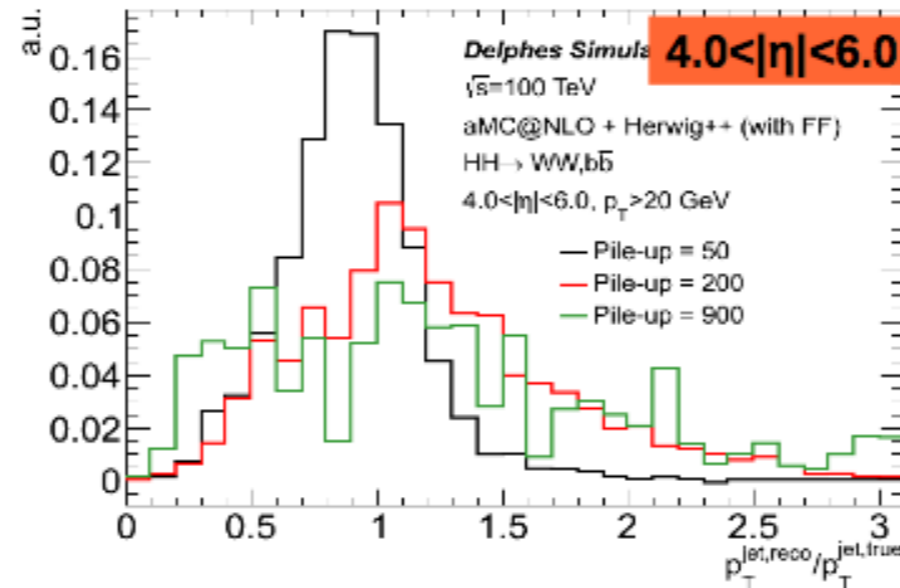
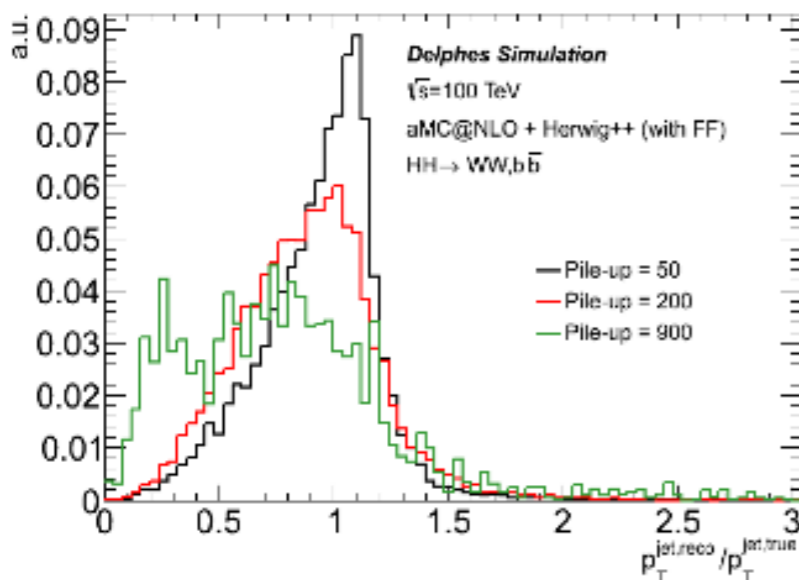
◆ Missing Transverse Energy

- Anti-Kt (Fast Jet) algorithm
- negative vector sum of Jets, after pile-up correction and calibration

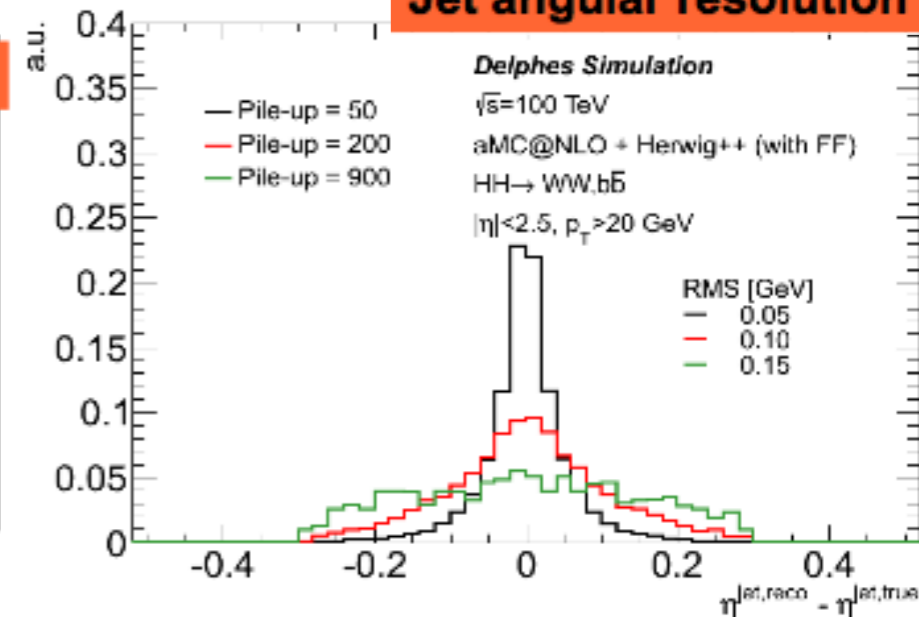
Missing ET resolution



Jet pT response



Jet angular resolution



HH → WWbb → lvqqbb: MVA analysis

B. Di Micco, M. Testa, M. Verducci (Roma 3)

Input variables:

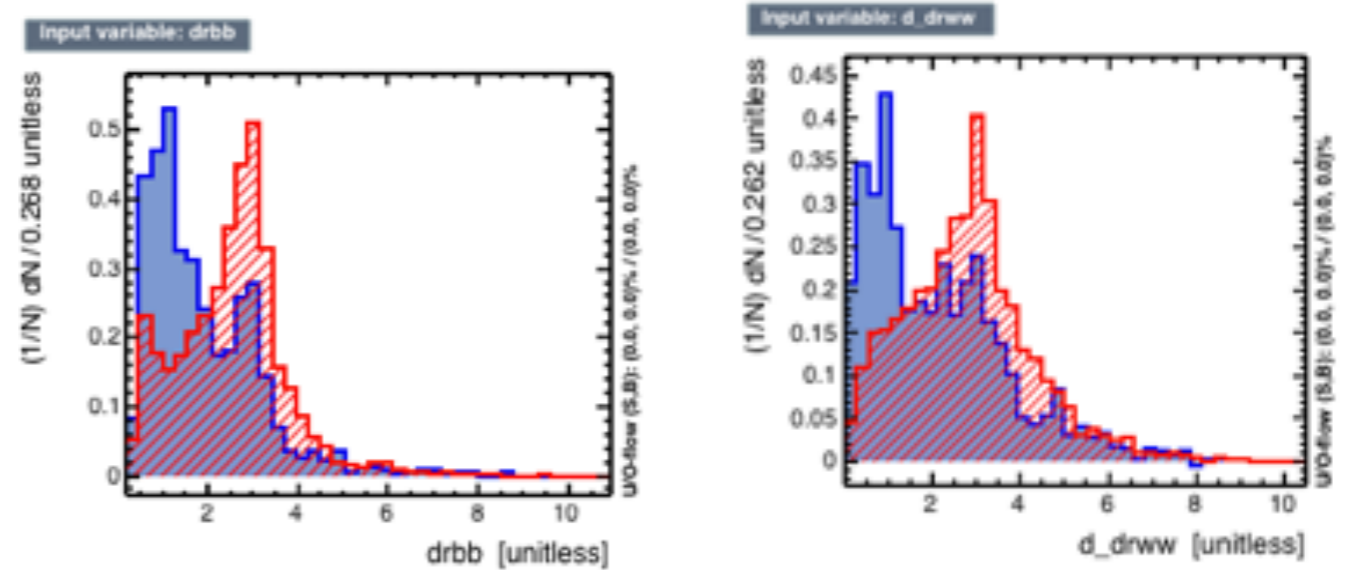
$$\Delta R_{jj}, \Delta R_{bb}, \Delta R_{WW}, m_T^{WW}, m_{bb}$$

$$m_{jj}, p_T^{bb}, p_T^{WW}, E_T^{\text{miss}}, m_T^W, m_{WW}$$

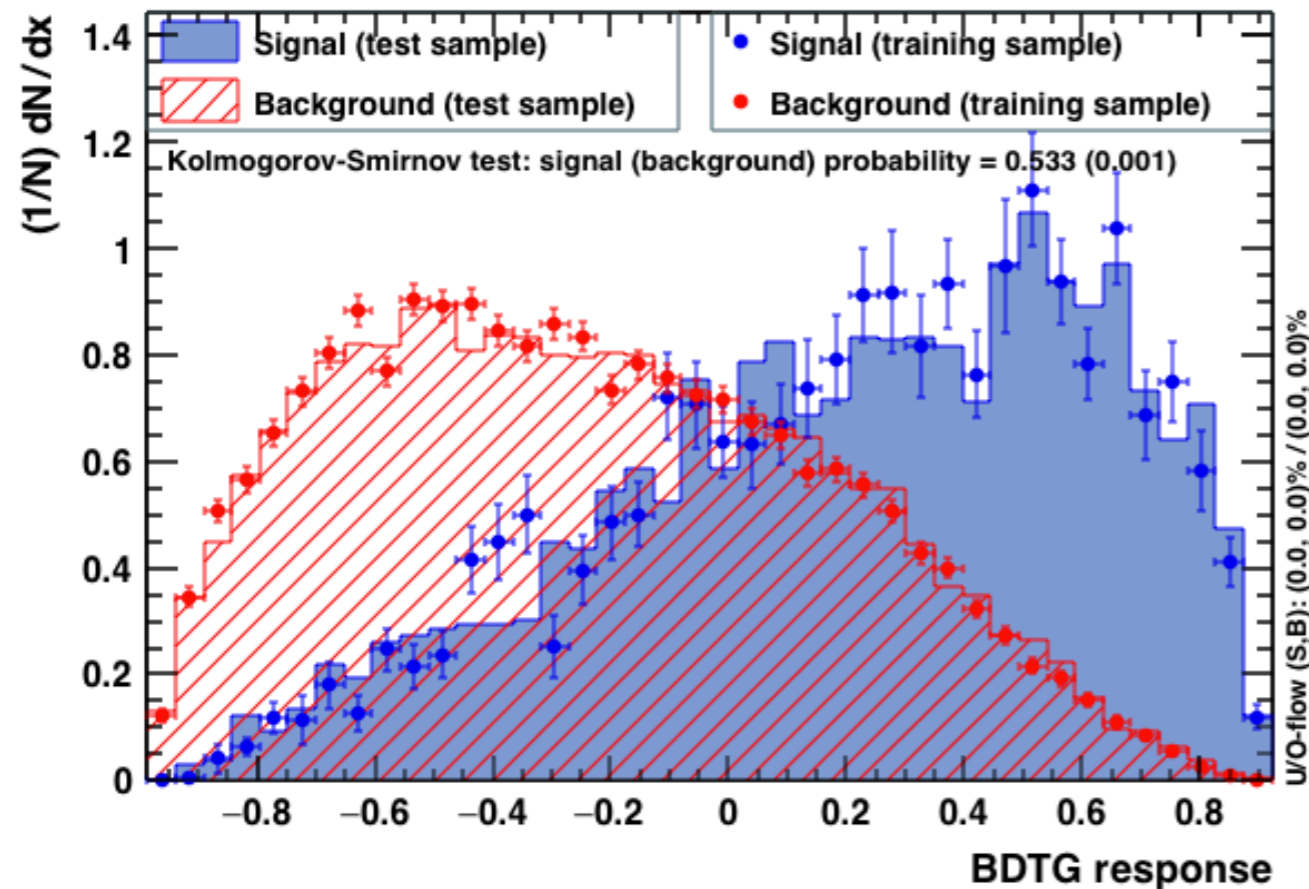
Pre-training cuts:

$$p_T^{WW}, p_T^{bb} > 150, 80 < m_{bb} < 180 \text{ GeV}$$

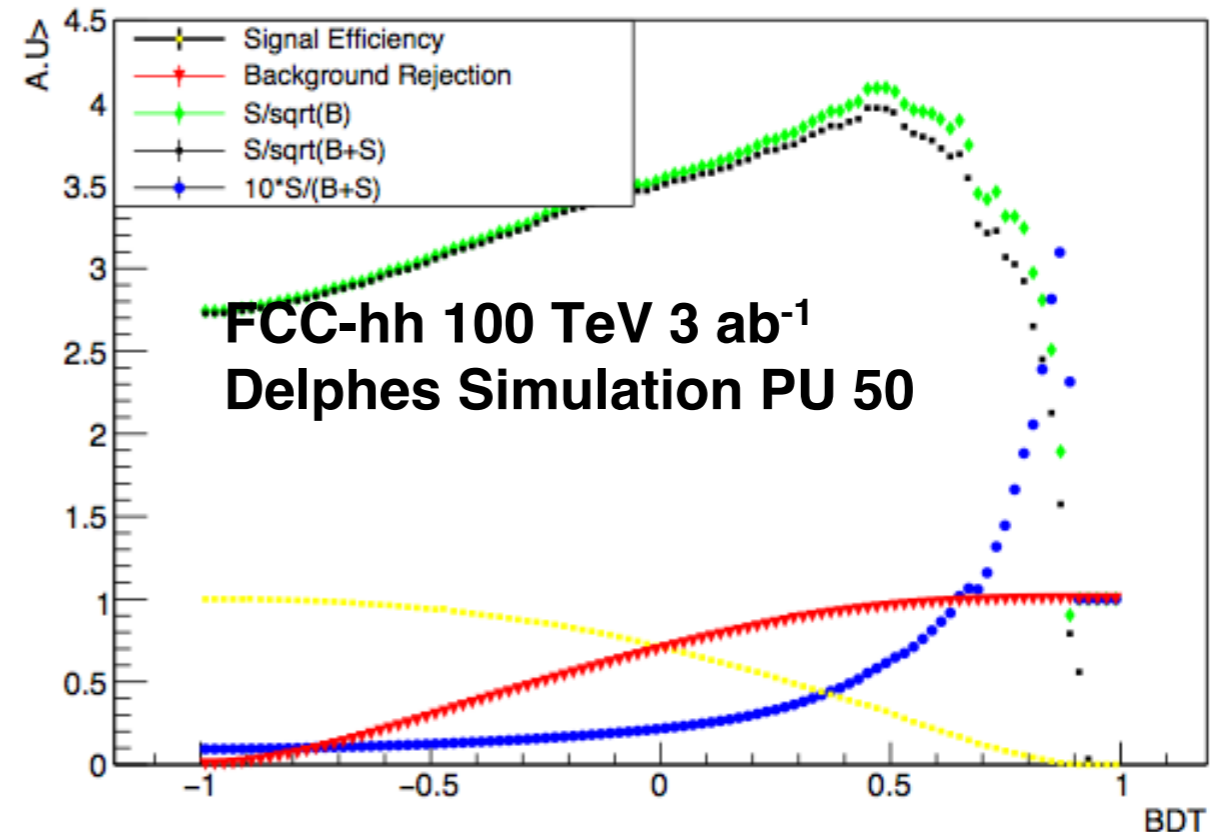
$$\Delta R_{bb} < 2.0$$



TMVA overtraining check for classifier: BDTG



stat. sign. 4.1σ with S/B 0.06, 13σ @ 30 ab^{-1}

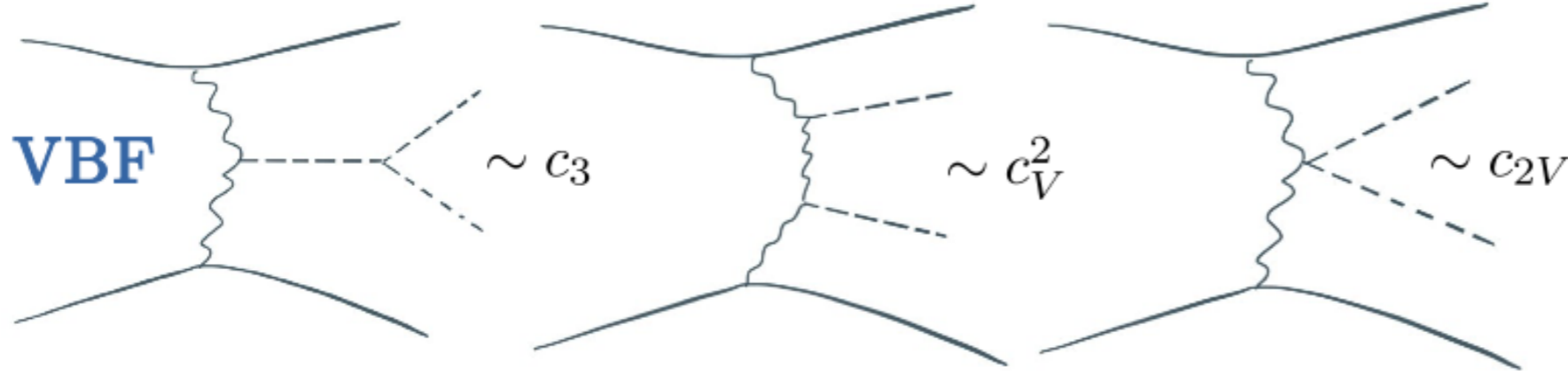


Conclusion and plans

- Fix the Delphes configuration and the handling of pileup (all+Michele Selvaggi)
- Simulation of the background for ZZbb and WWbb in various pileup scenario is our close-term priority (S. Braibant, N. De Filippis, B. Di Micco) – End September
- Optimization of the analyses with delphes (isolation, ID, pileup rejection) (all) - October
- Provide an internal document about those analyses (S. Braibant, N. De Filippis, B. Di Micco) – September – October → eventually contribute to CDR
- From now on we are going to follow and contribute regularly to CepC and FCC meetings.

Backup

VBF hh production



SM

$$c_V = c_{2V} = c_3 = 1$$

$$\sigma/\sigma_{SM} = 1 + a\delta + b\delta^2$$

$$\delta_i \equiv c_i - 1$$

dashed : before cuts
solid : after cuts

VBF jets at high η go in the very forward region, 50% event loss with η acceptance of 4 instead of 5

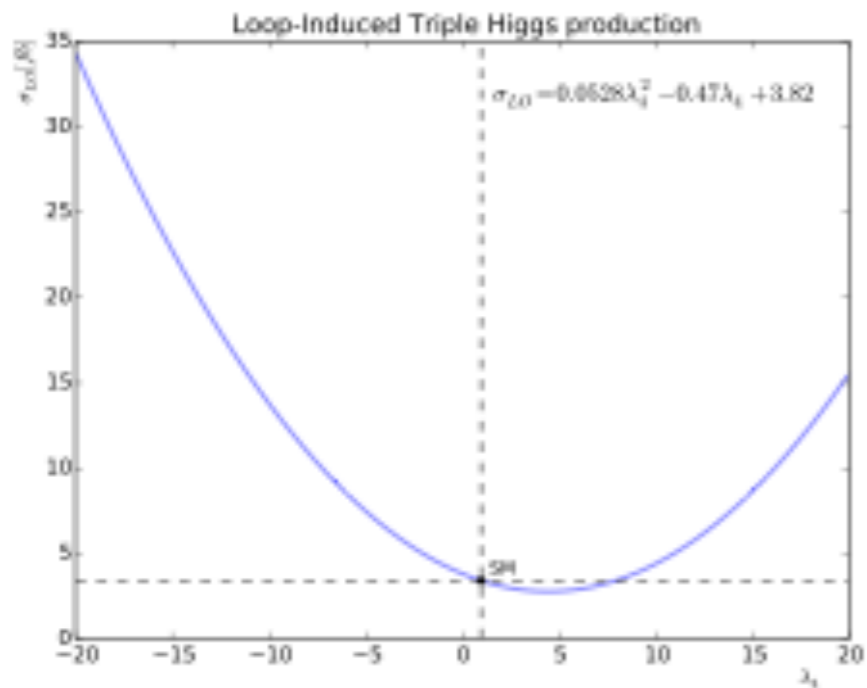
Not strong sensitivity to SM hh production, but adds information on New Physics operators

		14 TeV	100 TeV
Acceptance cuts	p_{T_j} (GeV) \geq	25	40
	p_{T_b} (GeV) \geq	25	35
	$ \eta_j \leq$	4.5	6.5
	$ \eta_b \leq$	2.5	3.0
VBF cuts	$ \Delta y_{jj} \geq$	5.0	5.0
	m_{jj} (GeV) \geq	700	1000
	Central jet veto: $p_{T_{j3}}$ (GeV) \leq	45	65
	m_{hh} (GeV) \geq	500	1000

	68% probability interval on $\delta_{c_{2V}}$	
	$1 \times \sigma_{\text{bkg}}$	$3 \times \sigma_{\text{bkg}}$
LHC ₁₄	[-0.37, 0.45]	[-0.43, 0.48]
HL-LHC	[-0.15, 0.19]	[-0.18, 0.20]
FCC ₁₀₀	[0, 0.01]	[-0.01, 0.01]

	95% probability upper limit on μ	
	$1 \times \sigma_{\text{bkg}}$	$3 \times \sigma_{\text{bkg}}$
LHC ₁₄	109	210
HL-LHC	49	108
FCC ₁₀₀	12	23

Higgs quartic coupling



observable	selection cut
$p_{T,b_{\{1,2,3,4\}}}$	$> \{80, 50, 40, 40\}$ GeV
$ \eta_b $	< 3.0
$m_{bb}^{\text{close},1}$	$\in [100, 160]$ GeV
$m_{bb}^{\text{close},2}$	$\in [90, 170]$ GeV
$\Delta R_{bb}^{\text{close},1}$	$\in [0.2, 1.6]$
$\Delta R_{bb}^{\text{close},2}$	no cut
$p_{T,\gamma_{(1,2)}}$	$> \{70, 40\}$ GeV
$ \eta_\gamma $	< 3.5
$\Delta R_{\gamma\gamma}$	$\in [0.2, 4.0]$
$m_{\gamma\gamma}$	$\in [124, 126]$ GeV

	Signal	$b\bar{b}j\gamma\gamma$	$Ht\bar{t}$	S/B	S/\sqrt{B}
preselection	50	2.3×10^5	2.2×10^4	2.5×10^{-4}	0.14
$\chi_{H,min}^2 < 6.1$	26	4.6×10^4	9.9×10^3	5.0×10^{-4}	0.14
$ m_{H}^{rec} - 126 \text{ GeV} < 5.1 \text{ GeV}$	20	1.7×10^4	7.0×10^3	8.1×10^{-4}	0.15

30 ab^{-1} : $-4 < \lambda_4 < 16$

Multi-leptons: $HH \rightarrow bbZZ, bbWW, bb\mu\mu$

$$hh \rightarrow (b\bar{b})(ZZ^*) \rightarrow (b\bar{b})(4\ell), hh \rightarrow (b\bar{b})(WW^*)/(\tau^+\tau^-) \rightarrow (b\bar{b})(\ell^+\ell^-), hh \rightarrow (b\bar{b})(\mu^+\mu^-) \text{ and } \tilde{h}h \rightarrow (b\bar{b})(Z\gamma) \rightarrow (b\bar{b})(\ell^+\ell^-\gamma)$$

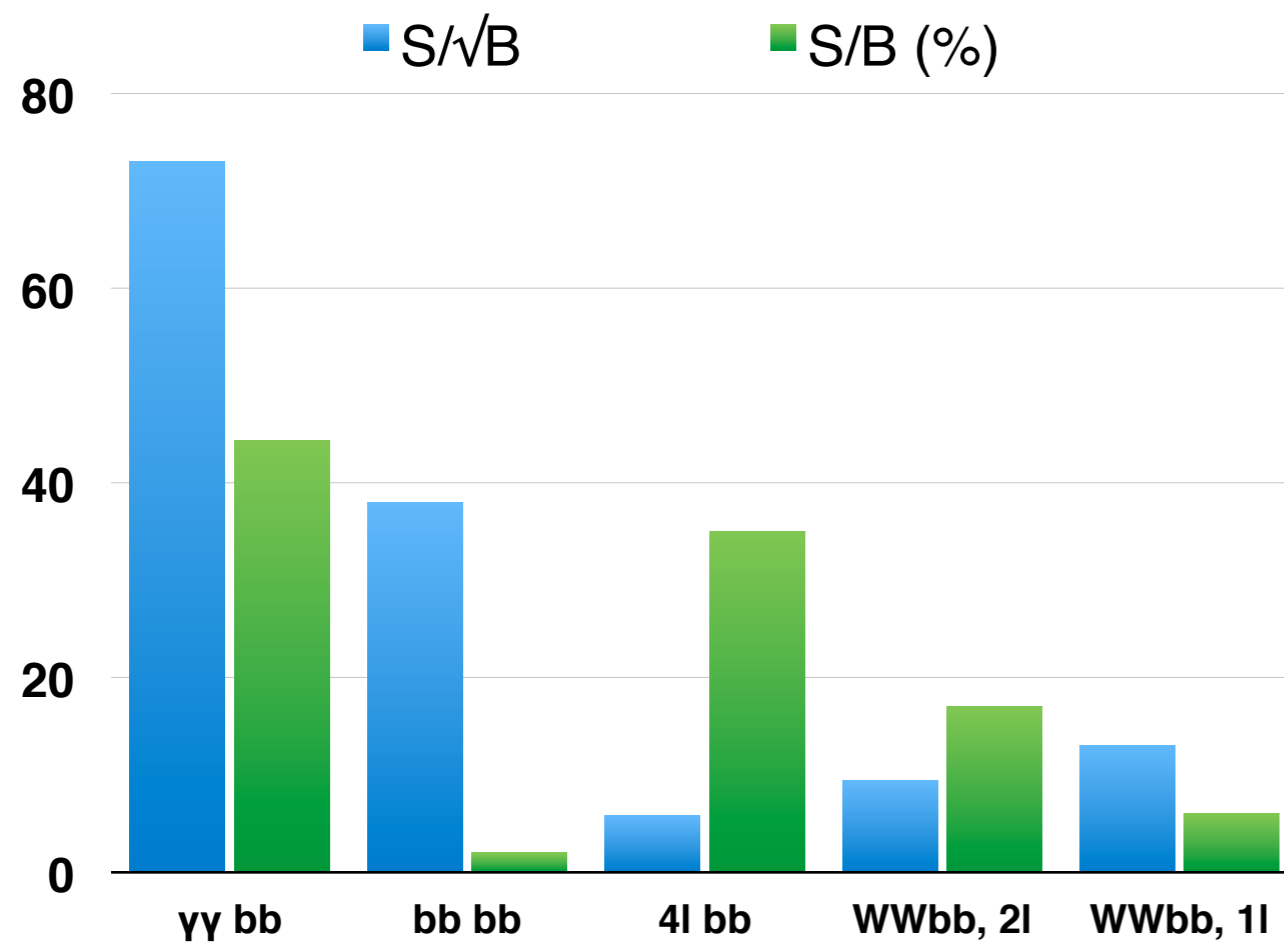
- Typically low yield and low background thanks to the multi-lepton final state;
- Exception for WWbb \rightarrow llbb (high top background)

channel	$\sigma(100 \text{ TeV})$ (fb)	$N_{30 \text{ ab}^{-1}}$ (ideal)	$N_{30 \text{ ab}^{-1}}$ (LHC)
$hh \rightarrow (b\bar{b})(\ell^+\ell^-\ell'^+\ell'^-)$	0.26	130	41
$t\bar{t}h \rightarrow (\ell^+b\nu_\ell)(\ell'^-\bar{b}\bar{\nu}_{\ell'}) (2\ell)$	193.6	304	109
$t\bar{t}Z \rightarrow (\ell^+b\nu_\ell)(\ell'^-\bar{b}\bar{\nu}_{\ell'}) (2\ell)$	256.7	66	25
$Zh \rightarrow (b\bar{b})(4\ell)$	2.29	$\mathcal{O}(1)$	$\mathcal{O}(1)$
$ZZZ \rightarrow (4\ell)(b\bar{b})$	0.53	$\mathcal{O}(1)$	$\mathcal{O}(1)$
$b\bar{b}h \rightarrow b\bar{b}(4\ell) \quad (p_{T,b} > 15 \text{ GeV})$	0.26	$\mathcal{O}(10)$	$\mathcal{O}(1)$
$ZZh \rightarrow (4\ell)(b\bar{b})$	0.12	$\mathcal{O}(10^{-2})$	$\mathcal{O}(10^{-2})$

30 ab⁻¹

channel	$\sigma(100 \text{ TeV})$ (fb)	$N_{30 \text{ ab}^{-1}}$ (ideal)	$N_{30 \text{ ab}^{-1}}$ (LHC)	Channel	S/ $\sqrt{S+B}$	S/B
$hh \rightarrow (b\bar{b})(W^+W^-) \rightarrow (b\bar{b})(\ell^+\nu_{\ell'}\ell^-\bar{\nu}_{\ell'})$	27.16	209	199	4l	5,8	0,35
$hh \rightarrow (b\bar{b})(\tau^+\tau^-) \rightarrow (b\bar{b})(\ell^+\nu_{\ell'}\bar{\nu}_\tau\ell^-\bar{\nu}_{\ell'}\nu_\tau)$	14.63	385	243			
$t\bar{t} \rightarrow (\ell^+b\nu_\ell)(\ell'^-\bar{b}\bar{\nu}_{\ell'}) \quad (\text{cuts as in Eq. 49})$	25.08×10^3	343_{-94}^{+232}	158_{-48}^{+153}	2l	9,4	0,17
$b\bar{b}Z \rightarrow b\bar{b}(\ell^+\ell^-) \quad (p_{T,b} > 30 \text{ GeV})$	107.36×10^3	2580_{-750}^{+2040}	4940_{-1130}^{+2250}			
$ZZ \rightarrow b\bar{b}(\ell^+\ell^-)$	356.0	$\mathcal{O}(1)$	$\mathcal{O}(1)$	bb $\mu\mu$, bbl γ have a negligible contribution		
$hZ \rightarrow b\bar{b}(\ell^+\ell^-)$	99.79	498	404			
$b\bar{b}h \rightarrow b\bar{b}(\ell^+\ell^-) \quad (p_{T,b} > 30 \text{ GeV})$	26.81	$\mathcal{O}(10)$	$\mathcal{O}(10)$			

FCC studies: S/N ratio



- $\gamma\gamma$ bb looks to be the golden channel;
- need to reach maximal accuracy in this channel simulation, implementing pile-up simulation and more accurate fake estimate;
- detector design should be driven by minimisation of systematics on it;
- more work needed on WWbb to fully exploit its potentiality;
- highly boosted topologies are less useful for λ measurement, sensitivity to λ from low m_{hh} region

FCC-hh looks to have a strong physics case

Higgs boson as inflaton

Gravitational action coupled to the SM sector

$$S = \int \left[\frac{1}{2} M_{\text{pl}}^2 R + \mathcal{L} \right] d^4x \sqrt{-g} = \int \left[\frac{1}{2} M_{\text{pl}}^2 R - \frac{1}{2} \partial_\mu h \partial^\mu h + V(h) + \dots \right] d^4x \sqrt{-g}$$

Inflation model

- need a scalar field (h is a scalar field)
- need a well shaped potential, with a slow-roll condition

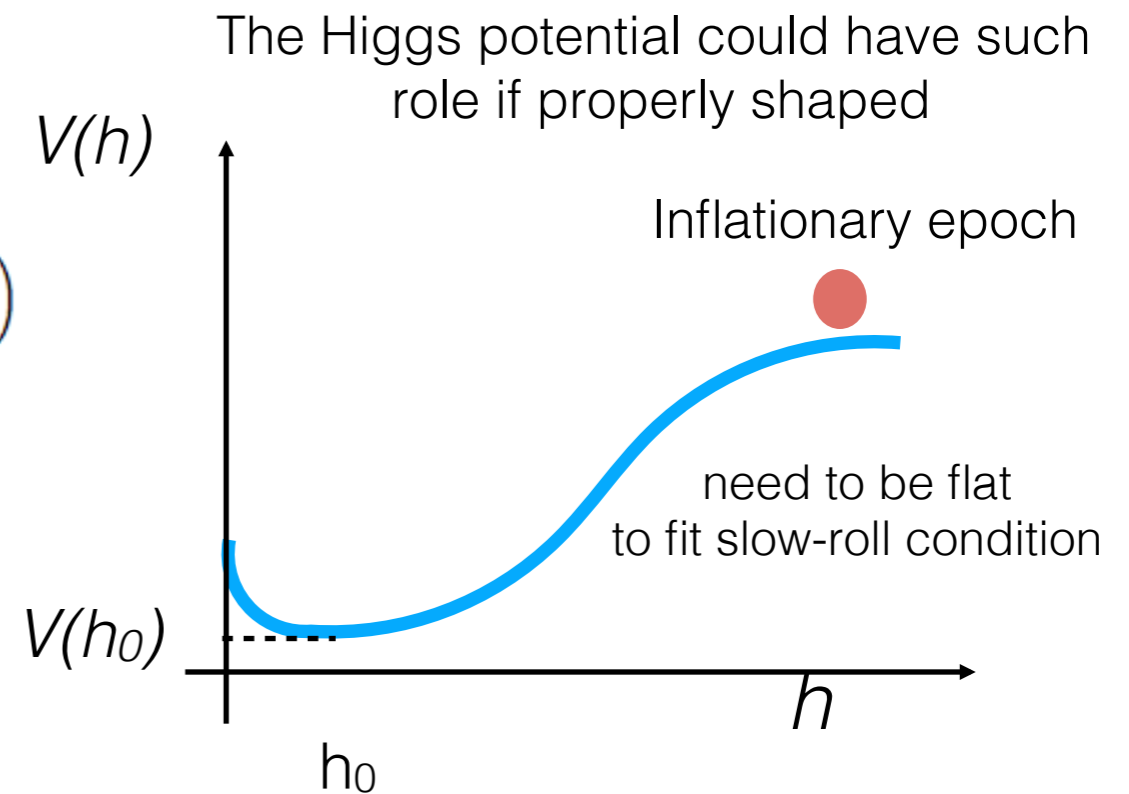
$$V(\phi) \gg \frac{1}{2} \dot{\phi}^2 \longrightarrow H^2 = \frac{8\pi G}{3} V(\phi) \simeq \text{const.} \longrightarrow a(t) \simeq e^{Ht} \quad \left(H(t) = \frac{\dot{a}}{a} \right)$$

universe radius, exponentially expanding during inflation

In order to make this to work

$$h \gg h_0 \quad V(h) \sim \lambda h^4 \quad \lambda \sim 10^{-13}$$

Intriguing, λ nearly vanishes for high h value with the present value of top and Higgs mass.



$$h_0 = \langle 0 | h | 0 \rangle$$

Understanding the Higgs potential is the last missing piece of the SM, and it could have fundamental cosmological implications.