Charm Rare Decays at BESIII

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BESIII-LHCb Workshop, IHEP, Feb 8-9 2018

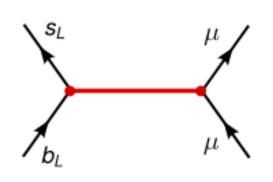




- Rare charm decays offer the possibility to search for signals beyond Standard Model in the up-quark sector.
 - There might be CP conserving and CP violating contributions within the Standard Model and beyond
 - There might be new particles/interactions through loops
- Experimental explorations play important role
 - First principle theoretical calculations have limitations
 - Non-perturbative hadronic effects
 - To calibrate theoretical tools, and searches in other sectors
- Once NP appeared somewhere, it might well also in charm
 - Complementary to s, b, l, v sectors
 - Important ingredients of global "precision search"

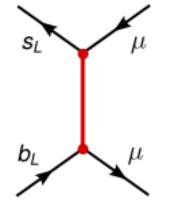
BESIT Different NP models for "the B anomaly"

Model-building: EFT-type considerations =>Simplified models => UV completions



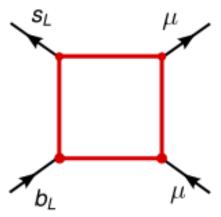
- Z' many ...
- *SU*(2)_{*L*} singlet or triplet
- $U(1)_{L_{\mu}-L_{\tau}}, U(1)_{B_{3}-L_{\mu}}$

arXiv:1403.1269,1501.00993, 1503.03477, 1611.02703...



- Leptoquark
- Scalar (S₁, S₃) or
 Vector (R₂, U₁, U₃)

arXiv: 1511.01900, 1503.01084, 1704.05835 1512.01560, 1511.06024 1408.1627



 New Scalar or Vectors or leptoquarks possible

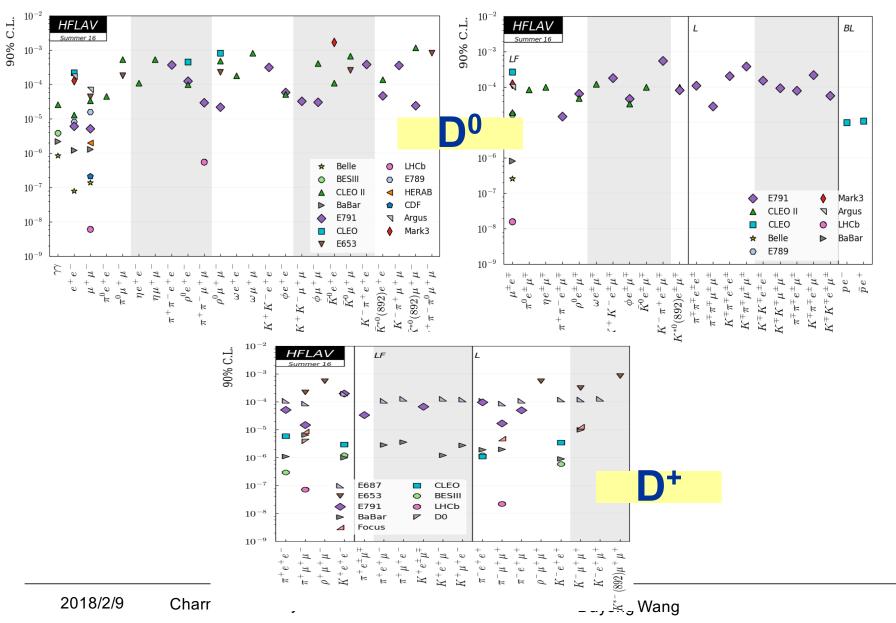
arXiv: hep-ph/0610037 1509.05020, 1608.07832 1704.05438, 1607.01659 1704.07845 ...



Rare D Decays



4





	beam	Sample
E791	π 500 GeV	2.5×10^5 D
CDF	$p\overline{p}$ 1 GeV	$1.5 \times 10^{6} D$
FOCUS	γ 200 GeV	$1 \times 10^{6} D$
CLEO	e^+e^- (Y(4s))	1.5×10^5 D
CLEO-	C $e^+e^-(\psi(3770))$	881 nb $c\overline{c}$
BABAR	e^+e^- (Y(4s))	$6 \times 10^8 \ \mathrm{c}\overline{\mathrm{c}}$
LEP	$e^+e^-(Z^0))$	$1 \times 10^{5} D$
BELLE	e^+e^- (Y(4s))	8×10^8 cc
BESIII	$e^+e^-(\psi(3770))$	~ 10 ⁷ DD
LHCb	pp	~10 ¹⁰ ,
	may further extend ~2031	+ (V Vagnoni talk)

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BEST



BESIII charm data samples

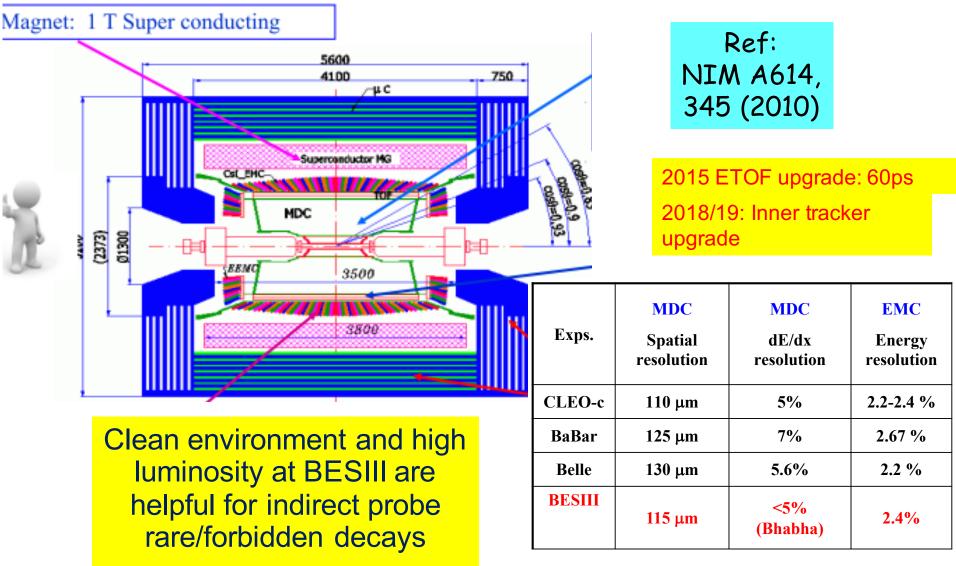


	~ 0.5 B ψ (3686) events	~ 24×CLEO-c
	~ 1.3 B J/ψ events	~ 21×BESII
	~ 2.9/fb $\psi(3770)$	~ 3.5×CLEO-c yellow book: 90M DDbar
	~ 0.482/fb 4.009	Ds study
	~ 0.6/fb Λ_c pairs at threshold	Unique
•	 9/fb XYZ above 4 GeV 20 points for R &QCD Scan: 500/pb finished in May 2015 Y(2175) resonance: 100 /pb 2016: 3/fb Ds data at 4170 MeV 5×CLEO-c 2017: Y(4260), X(3872) 2018: 6-8B J/ψ (NEW) 	0 MARKI DELCO MARKII MARKIII BESII CLEOC BESIII 4.03/4.14 GeV 4.17 GeV 4.009/4.178/4.6 GeV 3000 2000
_	~ other data sets: tau, resonance scan and continuum, etc.	
	2018/2/9 Charm rare decays at BESIII	BES CLEOC BESIII



BESIII Detector







How BESIII compare to LHCb



	LHCb	BESIII		
production	pp collision@LHC	e+e- annhilation@BEPCII		
Cross section*L	10 ¹⁰	10 ⁷		
Particle ID	good	good		
Detector configuraiton	forward	hermetic		
Trigger system	dedicated	comprehensive		
uniqueness	Time-dependent	full kinematic constraint		
Statistics@production Efficiency				
l liabliabt/l laiou an an af DI	Lightent/Lightenages of DECIII			

Highlight/Uniqueness of BESIII

- Pair production near threshold in e+e-
 - Tagging, with extremely low background
 - systematics cancellation in DT,
 - absolute measurement
- Full kinematics available
 - Neutron/anti-neutron
 - Invisible signatures

Low energy photons and electrons well reonstructed

Also pi0

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Good complementary

BESIII is more competitive in channels with low energy electron/photons, neutrons, pi0's





Many common techniques, refer to other BESIII talks:

QC measurements at BES III	Xiaokang Zhou
BR measurements at BES III	Bai-Cian Ke
Leptonic and semileptonic decays	Hailong Ma
Ds+ -> pi+ pi+ pi- Inclusive	Liang Sun
Ac running + measurements	Lei Li

- With statistics up, BESIII is more involved for searches with charmonia, off resonances, dark sector etc.
 - Only cover charmed hadron decays in this talk
- As demonstrations, will focus on
 - Rare decays (with photons)
 - c->u e e, c->u v v (with e/pi0/missing)
 - LFV, LNV, LNV & BNV processes (with e)

Tagging technique at threshold

Double tag analysis

✓ Tagging D⁻(\overline{D}^0), Λ_c^- from

hadronic decay modes

 $M_{
m BC} = \sqrt{E_{
m beam}^2 - p_{ar{D}_{
m tag}}^2}$

 \checkmark (semi-)leptonic decay event can

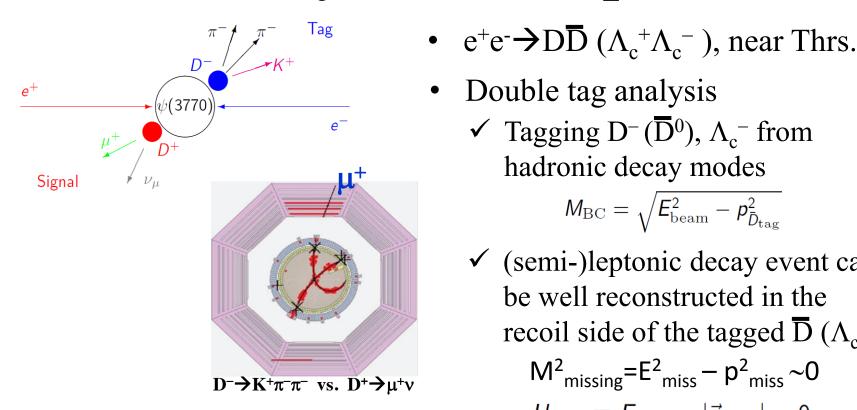
 $M_{missing}^2 = E_{miss}^2 - p_{miss}^2 \sim 0$

 $U_{\rm miss} \equiv E_{\rm miss} - |\vec{p}_{\rm miss}| \sim 0$

recoil side of the tagged \overline{D} (Λ_c^{-})

be well reconstructed in the





- Event is very clean
- □ High tagging efficiency
- Most systematic uncertainties can be cancelled
- Could measure absolute BFs





Charm rare decay with photons

₿€SШ



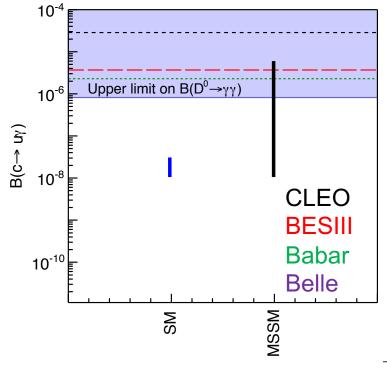
- FCNC mode, forbidden at tree level
- → Larger GIM suppression
- → Short distance: BF~10⁻¹¹ [PRD66 (2002) 014009]
- → Long distance due to VMD: BF~10⁻⁸ [PRD66 (2002) 014009]
- \rightarrow MSSM up to BF~10⁻⁶ [PLB500(2001)304], i.e. c \rightarrow u γ via gluino exchange

Measurements at B factories:

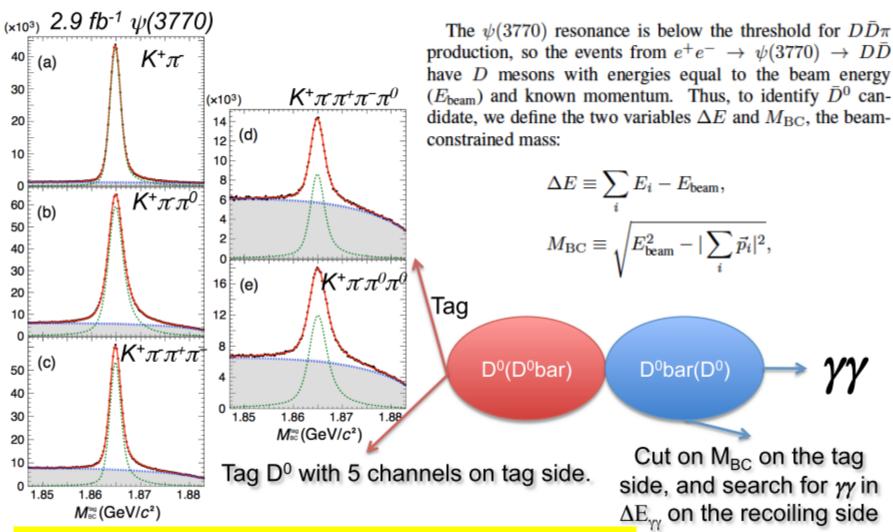
- Reconstruct through D^{*+} → D⁰(→ γγ) π⁺
 normalized by D^{*+} → D⁰(→ K_Sπ⁰) π⁺.
- Peaking background from $D^0 \rightarrow \pi^0 \pi^0$.

Measurement at BESIII

- Double tag
- Fitting delta(E)
- Major background: D⁰->pi⁰pi⁰



D⁰->yy: analysis method



We could use similar technique to perform other D rare decay search, and estimate the sensitivity

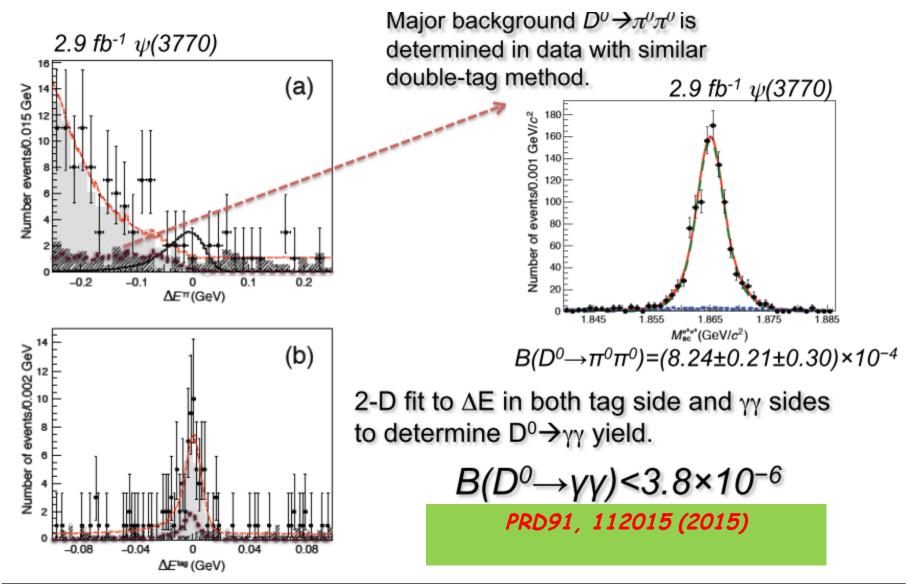
Number of events/0.00025 GeV/c²





D⁰->yy Results

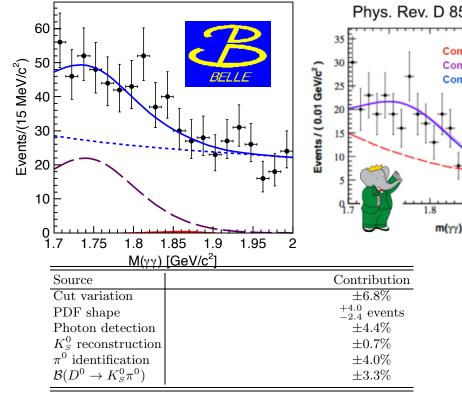




Comparison and prospects

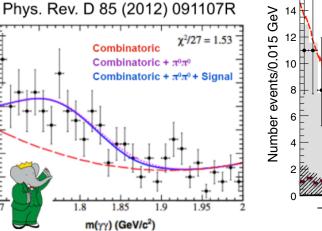


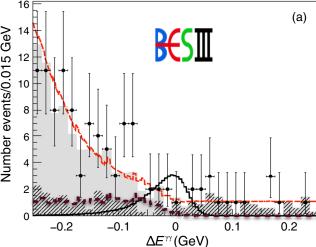
PhysRevD(2016).93.051102



Uncertainties independent of fitting procedure

Source	Relative uncertainty (%)
Photon reconstruction	2.0
$M_{\rm BC}^{\gamma\gamma}$ requirement	3.1
ST D^0 yields	1.0
Total	3.8

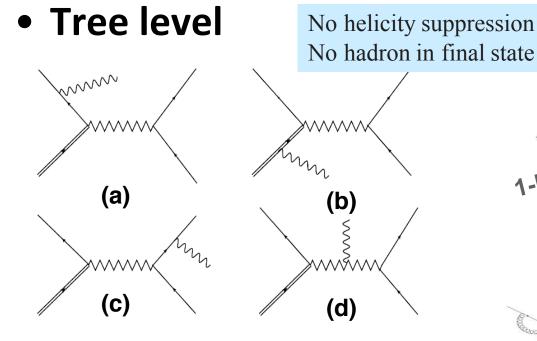




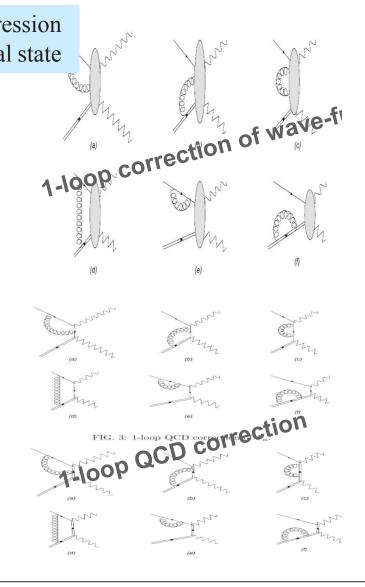
- BESIII has the least background contamination
- **D** and very good control of systematics
- Could still be competitive with the final DDbar sample
- Detailed projection study is needed to check what is the critical points for DDbar sample size

radiative decay $D^{+} \rightarrow \gamma e^{+} v_{e}$



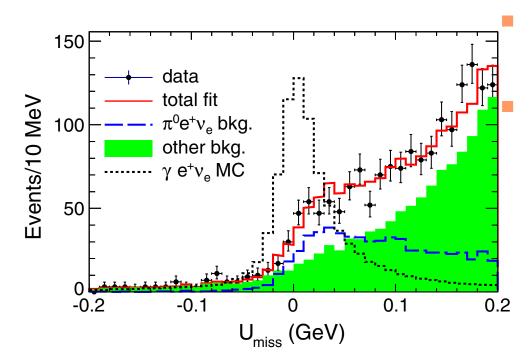


- Figs. (a) and (b) are Structure-Dependent (SD) radiative decays,
- fig. (c) is the Internal Bremsstrahlung (IB) radiative decay.
- (d) Suppressed by a factor of 1/M_w², thus can be neglected.









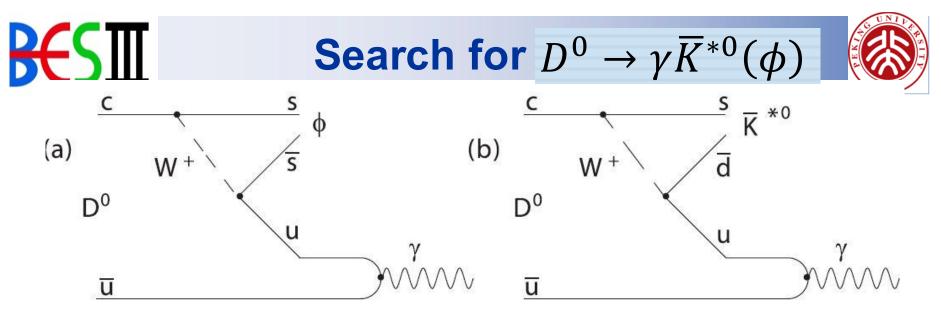
Double Tag analysis with 2.9fb⁻¹ @3.773GeV pi0 e v background normalization with dedicate DT analysis

$$N_{\pi^0}^{\exp} = \frac{N_{\mathrm{DT}}^{\pi^0}}{\sum_{i} \frac{N_{\mathrm{ST}}^i}{\varepsilon_{\mathrm{ST}}^i}} \varepsilon_{\mathrm{DT},\pi^0}^i} \sum_{i} \frac{N_{\mathrm{ST}}^i}{\varepsilon_{\mathrm{ST}}^i} \varepsilon_{\mathrm{DT},\pi^0}^{i,\gamma},$$

$$\mathcal{B}(D^+ \to \gamma e^+ \nu_e) < 3.0 \times 10^{-5}.$$
With E_γ>10MeV

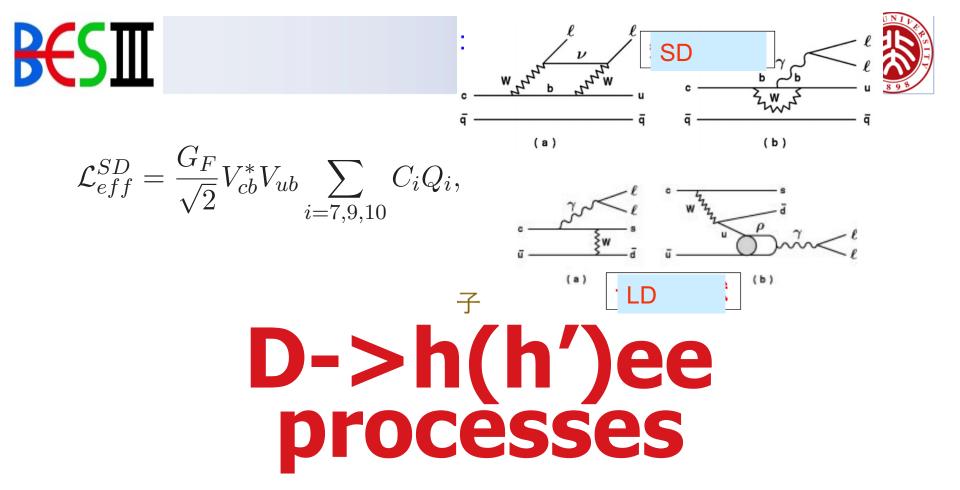
PHYSICAL REVIEW D 95, 071102(R) (2017)

	Relative uncertainty (%)	
model	3.5	
r 2	0.5	
, ,	0.5	
ction	1.0	
ment	4.4	
kgrounds	2.7^{a}	
kgrounds		



- Belle Collaboration (2004)
 - $B(D^0 \to \phi \gamma) = \left[2.60^{+0.70}_{-0.61}(stat)^{+0.15}_{-0.17}(syst)\right] \times 10^{-5}$
- BABAR Collaboration (2008) • $B(D^0 \to \phi \gamma) = (2.78 \pm 0.30 \pm 0.27) \times 10^{-5}$ • $B(D^0 \to \overline{K}^{*0} \gamma) = (3.28 \pm 0.20 \pm 0.27) \times 10^{-4}$
- Belle Collaboration (2017) • $B(D^0 \to \phi \gamma) = (2.76 \pm 0.19 \pm 0.10) \times 10^{-5}$ • $B(D^0 \to \overline{K}^{*0} \gamma) = (4.66 \pm 0.21 \pm 0.21) \times 10^{-4}$

- □ BESIII work in progress
- □ With present data set,
 - gamma K* could be within reach
- Difficult for phi, due to phi pi0 and phi KL backgrounds
- Not so comeptitive with more data



BESI $D^+ \rightarrow h^+ e^+ e^-$ and $D^+ \rightarrow h^- e^+ e^+$



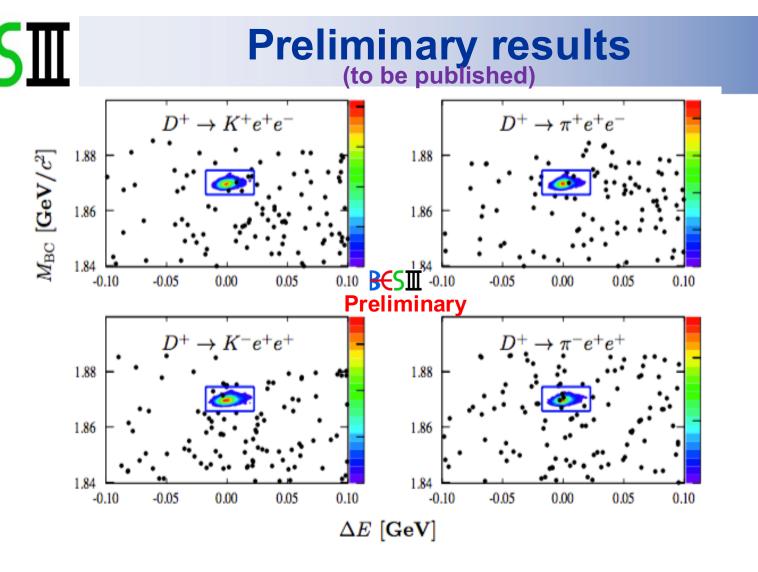
- Flavor Changing Neutral Current (FCNC) (e.g. D⁺→h⁺e⁺e⁻) processes are expected to be very rare since it can not occur at tree level in the SM. Short distance: ~ 10^{-10~-9} level, MPLA8 (1993) 967
 Long distance: ~ 10^{-6~-5} level, PRD76 (2007) 074010
- Lepton Number Violation (LNV) (e.g. D⁺→h⁻e⁺e⁺) decays are forbidden in the SM, while beyond the SM, e.g., Majorana neutrino: ~ 10^{-30~-23} level, PRD64 (2001) 114009 may be greatly enhanced to ~10^{-5~-6} with EPJC71 (2011) 1715)
- Thus, processes of the form D⁺→hee provide a sensitive and an ideal lab for investigating new physics within and beyond the SM. Any observation of definite signals would be clear evidence of NP.
- BESIII has collected a huge open charm data sample, it's expected to get better results for these decays.





$\mathcal{B}(D^+ o) \setminus [imes 10^{-6}]$	$K^+e^+e^-$	$K^-e^+e^+$	$\pi^+ e^+ e^-$	$\pi^- e^+ e^+$
CLEO[1]	-	-	2600	-
MARK2[2]	4800	9100	2500	4800
E687[<mark>3</mark>]	200	120	110	110
E791[4]	200	-	52	96
CLEO ^[5]	3.0	3.5	5.9	1.1
Babar[6]	1.0	0.9	1.1	1.9
PDG[7]	1.0	0.9	1.1	1.1

P. Haas et al. (CLEO Collaboration), Phys. Rev. Lett. 60, 1614 (1988).
 A. J. Weir et al. (MarkII Collaboration), Phys. Rev. D 41, 1384 (1990).
 P. L. Frabetti et al. (E687 Collaboration), Phys. Lett. B 398, 239 (1997).
 E. M. Aitala et al. (E791 Collaboration), Phys. Lett. B 462, 401 (1999).
 P. Rubin el al. (CLEO Collaboration), Phys. Rev. D 82, 092007 (2010).
 J. P. Lees el al. (BaBar Collaboration), Phys. Rev. D 84, 072006 (2011).
 K. A. Olive et al. (Particle Data Group), Chin. Phys. C, 38, 090001 (2014).



Scatter plots for M_{BC} versus ΔE , where the signal regions are shown as a blue rectangle. The contours are determined from MC simulation to enclose 84% of signal events for each channel.



Systematic Errors



Source $[\%]$	$\mathcal{B}_{D^+ ightarrow K^+ e^+ e^-} \ \mathcal{B}_{D^+}$	$+ \rightarrow K^- e^+ e^+$	$\mathcal{B}_{D^+ ightarrow \pi^+ e^+ e^-}$	$\mathcal{B}_{D^+ ightarrow \pi^- e^+ e^+}$
$N_{D^+}^{ m tot}$	1.9	1.9	1.9	1.9
Tracking	3.0	3.0	3.0	3.0
Particle ID	1.2	1.2	1.2	1.2
MC modeling	1.1	1.1	1.8	1.8
Scale factor	3.7	4.6	4.2	5.3
$E_{ m charge}$ Cut	0.1 B€SII Preliminary	0.1	0.1	0.1
$M_{ee} { m Cut}$	0.1	0.1	0.1	0.1
Signal Box Cut	0.1	0.1	0.1	0.1
Total	5.4	6.1	5.9	6.8



D->h(h')ee processes



Decay	Upper limit	Experiment	Year	Ref.
$D^0 \rightarrow \pi^0 e^+ e^-$	45.0	CLEO	1996	[14]
$D^0 ightarrow \eta e^+ e^-$	110.0	CLEO	1996	[14]
$D^0 ightarrow \omega e^+ e^-$	180.0	CLEO	1996	[14]
$D^0 ightarrow \overline{K}{}^0 e^+ e^-$	110.0	CLEO	1996	[14]
$D^0 ightarrow ho e^+ e^-$	124.0	E791	2001	[15]
$D^0 ightarrow \phi e^+ e^-$	59.0	E791	2001	[15]
$D^0 ightarrow \overline{K}^{*0} e^+ e^-$	47.0	E791	2001	[15]
$D^0 \to \pi^+\pi^- e^+ e^-$	370.0	E791	2001	[15]
$D^0 \to K^+ K^- e^+ e^-$	315.0	E791	2001	[15]
$D^0 \to K^- \pi^+ e^+ e^-$	385.0	E791	2001	[15]
$D^+ ightarrow \pi^+ e^+ e^-$	1.1	BaBar	2011	[16]
$D^+ \rightarrow K^+ e^+ e^-$	1.0	BaBar	2011	[16]
$D^+ \to \pi^+ \pi^0 e^+ e^-$				
$D^+ \to \pi^+ K^0_S e^+ e^-$				
$D^+ \rightarrow K^+ \pi^0 e^+ e^-$				
$D^+ \to K^+ \overline{K}{}^0 e^+ e^-$				

In unit of 10⁻⁶
 BESIII could update all of them

D->h(h')ee: ongoing at BESIII



Signal decays	PDG [10] (×10 ⁻⁵)
$D^+ \to \pi^+ \pi^0 e^+ e^-$	-
$D^+ \to K^+ \pi^0 e^+ e^-$	-
$D^+ \rightarrow K^0_S \pi^+ e^+ e^-$	-
$D^+ \rightarrow K^{0}_S K^+ e^+ e^-$	-
$\overline{D^0 \to K^- K^+ e^+ e^-}$	< 31.5
$D^0 \to \pi^+ \pi^- e^+ e^-$	< 37.3
$D^0 \to K^- \pi^+ e^+ e^{-\dagger}$	< 38.5
$D^0 \to \pi^0 e^+ e^-$	< 4.5
$D^0 \to \eta e^+ e^-$	< 11
$D^0 \rightarrow \omega e^+ e^-$	< 18
$D^0 \to K^0_S e^+ e^-$	< 11
[†] in $M_{e^+e^-}$ regions:	
$[0.00, 0.20) \text{ GeV}/c^2$	-
$[0.20, 0.65) \text{ GeV}/c^2$	-
$[0.65, 0.90] \text{ GeV}/c^2$	-

- With double tag technique at threshold, both D0 and D+ FCNC are studied.
- UL for D+ 4-track events could be provided for 1st time
- other FCNC upper limits could be greatly improved
- divide the M(ee) distribution
 into 3 regions for Kpiee to
 help separate LD effect
- The results to be published



Search for $D^0 \to \pi^0 \nu \bar{\nu}$:



- FCNC transitions only occur at loop order in the SM
- Electro-magnetic dynamics is absent for the neutrinos
- LD contributions are suppressed to be lower than SD
- Much clean to study the FCNC transitions.

Decay mode	Experimental limit	$\mathcal{B}r_{S.D.}$	$\mathcal{B}r_{L.D.}$	
$D^+ \rightarrow X^+_{\mu} e^+ e^-$		2×10 ⁻⁸		-
$D^+ \rightarrow \pi^+ e^+ e^-$	$<4.5\times10^{-5}$		2×10^{-6}	
$D^+ \rightarrow \pi^+ \mu^+ \mu^-$	$<1.5\times10^{-5}$		1.9×10^{-6}	
$D^+ \rightarrow \rho^+ e^+ e^-$	$< 1.0 \times 10^{-4}$		4.5×10^{-6}	Unique for
$D^0 \rightarrow X^0_\mu e^+ e^-$		0.8×10^{-8}		•
$D^0 \rightarrow \pi^0 e^+ e^-$	$< 6.6 \times 10^{-5}$		0.8×10^{-6}	BESIII,
$D^0 \rightarrow \rho^0 e^+ e^-$	$< 5.8 \times 10^{-4}$		1.8×10^{-6}	Work ongoing
$D^0 \rightarrow \rho^0 \mu^+ \mu^-$	$<2.3 \times 10^{-4}$		1.8×10^{-6}	Work engeing
$D^+ \rightarrow X_u^+ \nu \overline{\nu}$		1.2×10^{-15}		
$D^+ \rightarrow \pi^+ \nu \overline{\nu}$			5×10^{-16}	
$D^0 \rightarrow \overline{K}^0 \nu \overline{\nu}$			2.4×10^{-16}	
$D_s \rightarrow \pi^+ \nu \overline{\nu}$			8×10^{-15}	
Phys. Rev. D 6	56 014009			







LFV, LNV, BNV processes



R (

Incarnation in Charm



In Charm hadron decays Lepton Flavor Violation (LFV) processes Lepton Number Violation (LNV) processes Baryon Number Violatoin (BNV) processes

BESIII is more competitive in channels with low energy electron/photons, neutrons, pi0's

$\mu^{\pm}e^{\mp}$	LFV
$\pi^0 e^{\pm} \mu^{\mp}$	LFV
$\eta e^{\pm} \mu^{\mp}$	LFV
$\pi^+\pi^-e^\pm\mu^\mp$	LFV
$ ho e^{\pm} \mu^{\mp}$	LFV
$\omega e^{\pm}\mu^{+}$	LFV
$K^+K^-e^{\pm}\mu^+$	LFV
$\phi e^{\pm} \mu^{\mp}$	LFV
$K^0 e^{\pm} \mu^{\mp}$	LFV
$K^-\pi^+e^\pm\mu^\mp$	LFV
$K^{*0}e^{\pm}\mu^{\mp}$	LFV
$\pi^{\mp}\pi^{\mp}e^{\pm}e^{\pm}$	LNV
$\pi^{\mp}\pi^{\mp}\mu^{\pm}\mu^{\pm}$	LNV
$K^{\mp}\pi^{\mp}e^{\pm}e^{\pm}$	LNV
$K^{\mp}\pi^{\mp}\mu^{\pm}\mu^{\pm}$	LNV
$K^{\mp}K^{\mp}e^{\pm}e^{\pm}$	LNV
$K^{\mp}K^{\mp}\mu^{\pm}\mu^{\pm}$	LNV
$\pi^{\mp}\pi^{\mp}e^{\pm}\mu^{\pm}$	LNV
$K^{\mp}\pi^{\mp}e^{\pm}\mu^{\pm}$	LNV
$K^{\mp}K^{\mp}e^{\pm}\mu^{\pm}$	LNV
pe^-	BNV+LNV
$\bar{p}e^+$	BNV+LNV

Here and LNV processes



 $\mathcal{B}(D^0 \to e^\pm \mu^\mp) < 1.5 \times 10^{-8}$ at 90% CL

 $\mathcal{B}(D^+ \to \pi^- \mu^+ \mu^+) < 2.2 \cdot 10^{-8}$ $\mathcal{B}(D^+_s \to \pi^- \mu^+ \mu^+) < 1.1 \cdot 10^{-8}$

Already very stringent limit, these are difficult for BESIII to be competetive,

but BESIII could probe

- $\Lambda_{\rm c}$ and Ds: LFV decays
- LNV: D->hee. hhee
- LNV : c→uµ⁺µ⁺ forbidden in SM
 - ✓ Majorana neutrino: ~ 10^{-30~-23} level, PRD64 (2001) 114009
 - ✓ May be greatly enhanced: ~10^{-5~-6} with EPJC71 (2011) 1715)

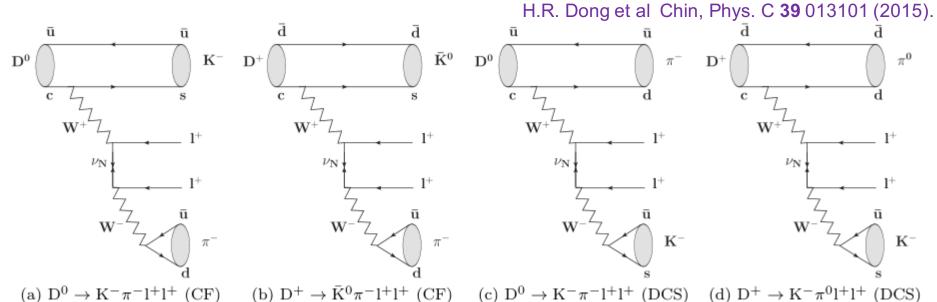
H.R. Dong, F. Feng and H.B. Li, Chin, Phys. C 39 013101 (2015)

Sensitivity estimation based on MCcomparable to the LNV B decays



LNV D \rightarrow K πe^+e^+ decays





- Lepton number violating(LNV) process (ΔL =2)
 - possibly due to a single Majorana neutrino exchange
 - The best previous limit around 10⁻⁴ ~ 10⁻⁵ level by E791 [PRL 86, 3969(2001)].
- BESIII could improve it to ~10⁻⁶
- Further constrain mass-dependent $D \rightarrow Ke^+\nu_N(\pi e^+)$ decay
 - constrain mixing matrix element |V_{eN}|²
- The results to be published



BNV & LNV processes



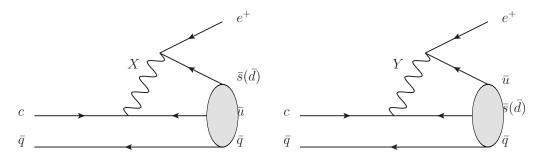
Х

D⁺

 D^+

d

D+->Lambda-bar(Sigma-bar)e+ Ds->Lambda e D+ ->nbar e+ D0 ->pbar e+ All started at BESIII, will benefit from the final charm dataset

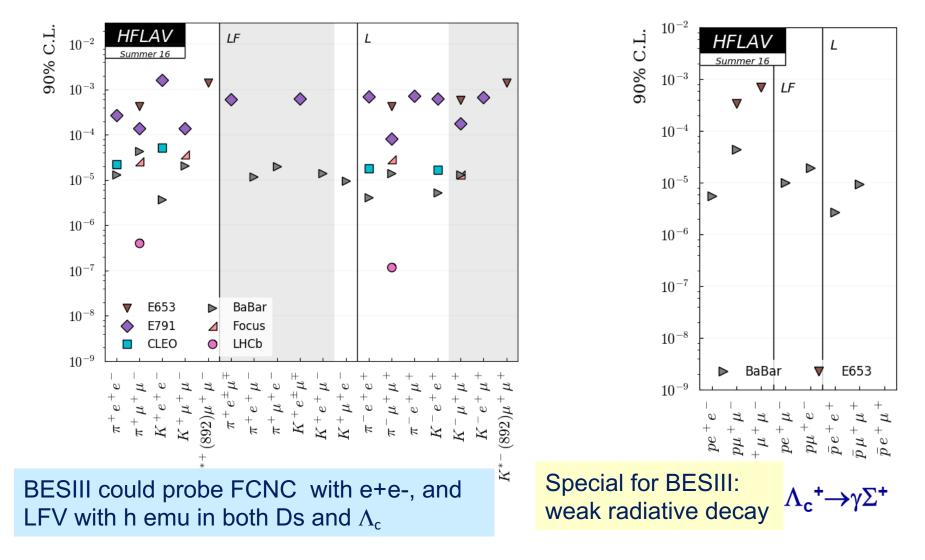


Many standard model (SM) extensions and Grand Unified Theories (GUTs) such as superstring models and SUSY predict proton decays. In this case, baryon number is violated while the difference $\Delta({\rm B-L})$ is conserved.

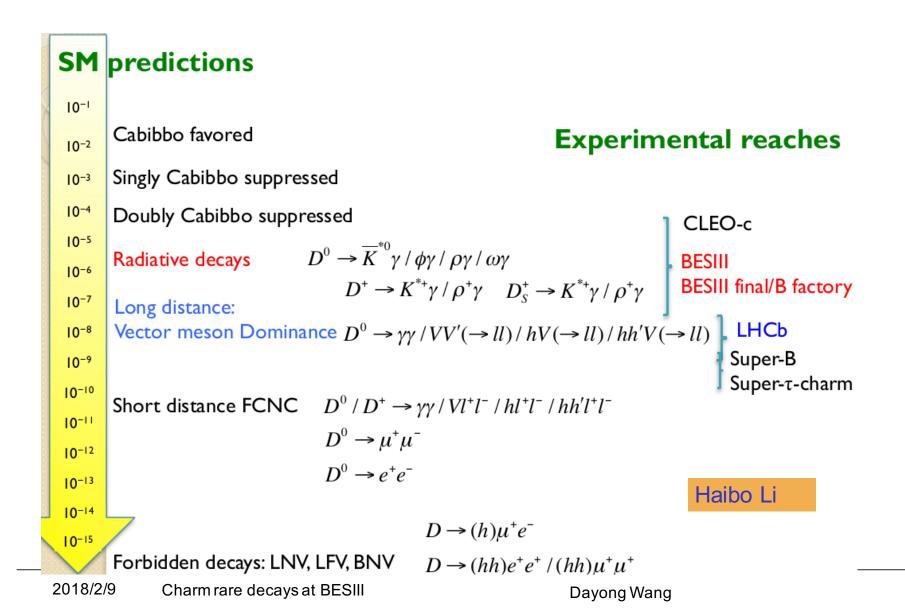
In the assumption of the heavy bosons X (4/3e) and Y (1/3e), there exists baryon number violation processes via $c(u)X\bar{u}$ or $c(u)Y\bar{d}(\bar{s})$ coupling.







BESIII Reach of rare charm decays







Thanks!

Extra slides...

BESIT Preliminary results (to update soo

₿€SII							
Preliminary	$N_{ m inside}^{ m data}$	$N_{ m outside}^{ m data}$	$f_{ m scale}$	ϵ [%]	$\Delta_{\rm sys}$ [%]	s_{90}	$\mathcal{B}[imes 10^{-6}]$
$D^+ ightarrow K^+ e^+ e^-$	5	69	0.08 ± 0.01	22.53	5.4	19.4	< 1.2
$D^+ ightarrow K^- e^+ e^+$	3	55	0.08 ± 0.01	24.08	6.1	10.2	< 0.6
$D^+ ightarrow \pi^+ e^+ e^-$	3	65	0.09 ± 0.02	25.72	5.9	4.2	< 0.3
$D^+ \to \pi^- e^+ e^+$	5	68	0.06 ± 0.02	28.08	6.8	20.5	< 1.2

• Where s₉₀ is estimated with **TROLKE** program, and the upper limit of branching fraction is calculated by

$$\mathcal{B} < rac{s_{90}}{N_{D^+}^{
m tot}}$$

• where $N_{D^+}^{\rm tot} = (1.681 \pm 0.032) \times 10^7$

Here is a set of the set of the



clean exp signature; robust theory calc; high sensitivity

Effective theory: model independent descriptions

$$\mathcal{H}_{\rm eff} = -\frac{4G_F}{\sqrt{2}} V_{\rm tb} V_{\rm tq}^* \sum_i \underbrace{\mathcal{C}_i \mathcal{O}_i}_{i} + \underbrace{\mathcal{C}'_i \mathcal{O}'_i}_{i} + \sum \frac{c}{\Lambda_{\rm NP}^2} \underbrace{\mathcal{O}_{\rm NP}}_{i=3-6,8} \quad \begin{array}{ll} i=1,2 & \text{Tree} \\ i=3-6,8 & \text{Gluon penguin} \\ i=7 & \text{Photon penguin} \\ i=9,10 & \text{EW penguin} \\ i=S,P & (\text{Pseudo)scalar penguin} \end{array}$$

Differenct processes have sensitivities to different operators

 $\begin{array}{cccc} & \mathcal{O}perator \ \mathcal{O}_i & \mathcal{B}_{s,d} \to X_{s,d}\mu^+\mu^- & \mathcal{B}_{s,d} \to \mu^+\mu^- & \mathcal{B}_{s,d} \to X_{s,d}\gamma \\ \\ & \mathcal{O}_7 \sim m_b(\bar{s}_L \sigma^{\mu\nu} b_R) F_{\mu\nu} & \checkmark & \checkmark & \checkmark \\ & \mathcal{O}_9 \sim (\bar{s}_L \gamma^\mu b_L) (\bar{\ell} \gamma_\mu \ell) & \checkmark & \checkmark & \\ & \mathcal{O}_{10} \sim (\bar{s}_L \gamma^\mu b_L) (\bar{\ell} \gamma_5 \gamma_\mu \ell) & \checkmark & \checkmark & \checkmark \\ & \mathcal{O}_{5,P} \sim (\bar{s}b)_{S,P} (\bar{\ell}\ell)_{S,P} & (\checkmark) & \checkmark & \end{array}$