

Leptonic and semileptonic D decays

Status and prospects at BESIII

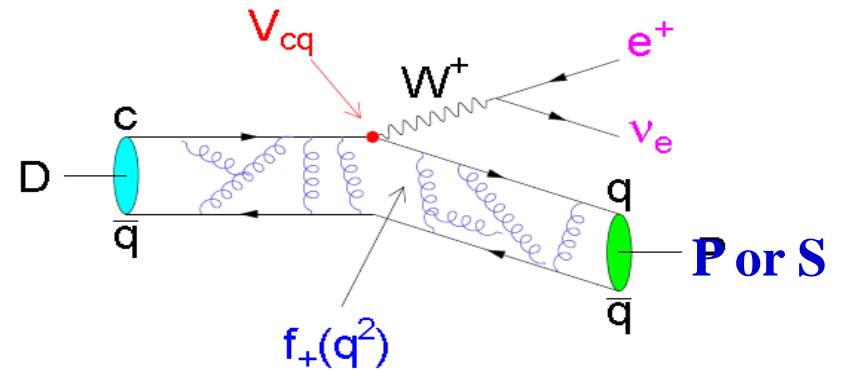
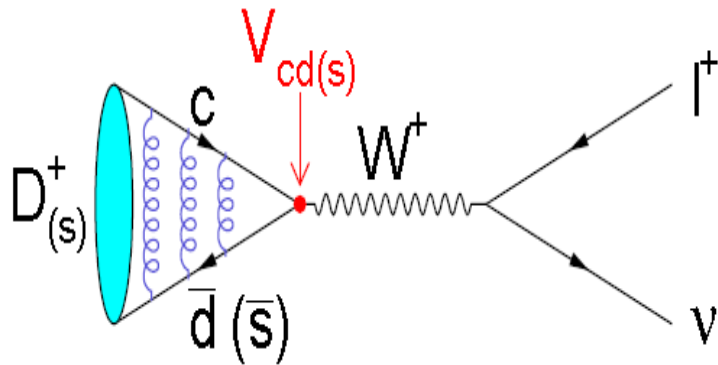
Hailong Ma (IHEP&BESIII)



Joint BESIII-LHCb workshop in 2018

Feb. 8-9 2018, IHEP, Beijing

Main physics goals



$$\Gamma(D_{(s)}^+ \rightarrow l^+ \nu_l) = \frac{G_F^2 f_{D_{(s)}^+}^2}{8\pi} |V_{cd(s)}|^2 m_\ell^2 m_{D_{(s)}^+} \left(1 - \frac{m_\ell^2}{m_{D_{(s)}^+}^2}\right)^2$$

$$\frac{d\Gamma}{dq^2} = X \frac{G_F^2 |V_{cd(s)}|^2}{24\pi^3} p^3 |f_+(q^2)|^2$$

1. $f_{D_{(s)}^+}$, $f_{\pi^+}^{K(\pi)}$: better calibrate LQCD

2. $|V_{cs(d)}|$: better test on CKM matrix unitarity

3. Test on lepton flavor universality (LFU)

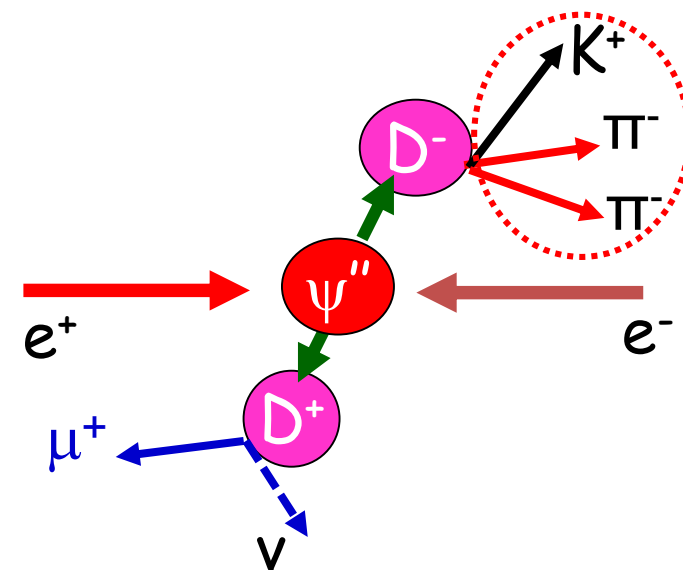
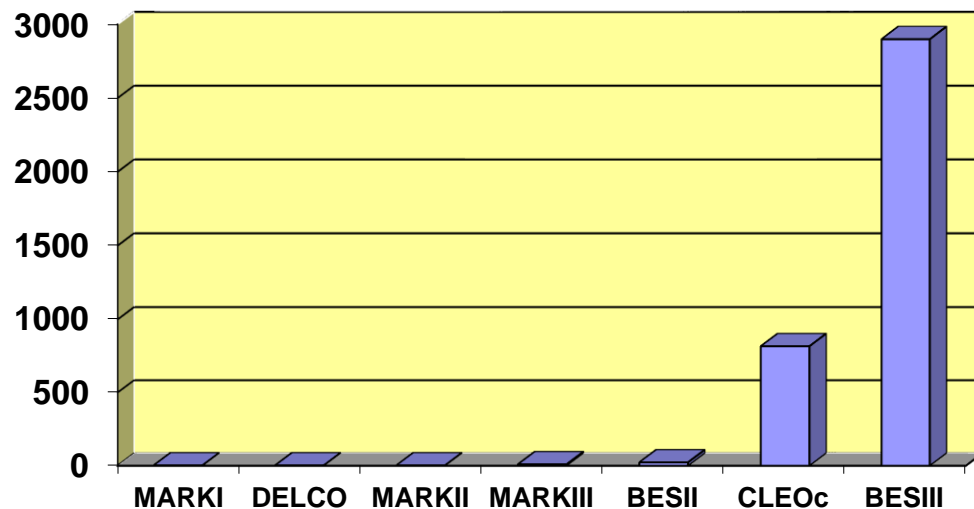
4. Search for new semileptonic decays

$$U = \begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix}$$

Samples of $D^{0(+)}$ and D_s^+ at BESIII

➤ $D^{0(+)}$ samples

2010-2011
3.773 GeV



$$N_{ST}^i = 2 \times N_{D\bar{D}} \times B_{ST}^i \times \epsilon_{ST}^i$$

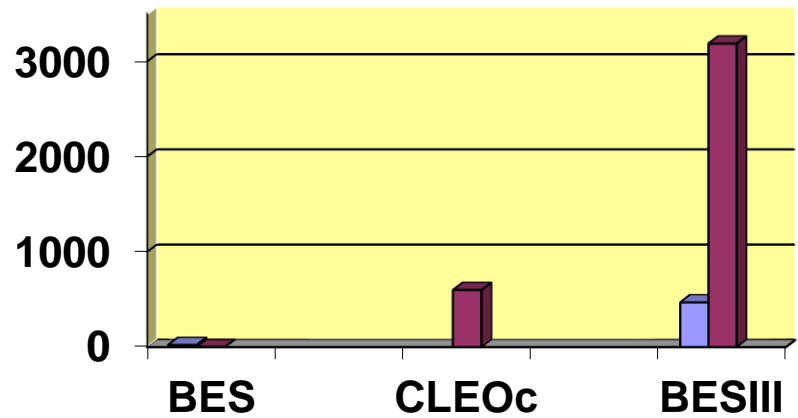
$$N_{DT}^i = 2 \times N_{D\bar{D}} \times B_{ST}^i \times B_{sig} \times \epsilon_{ST vs. sig}^i$$

$$B_{sig} = \frac{N_{DT}^{tot}}{N_{ST}^{tot} \times \bar{\epsilon}_{sig}}$$

$$\bar{\epsilon}_{sig} = \sum_{i=1}^N (N_{ST}^i \times \epsilon_{ST vs. sig}^i / \epsilon_{ST}^i) / \sum_{i=1}^N N_{ST}^i$$

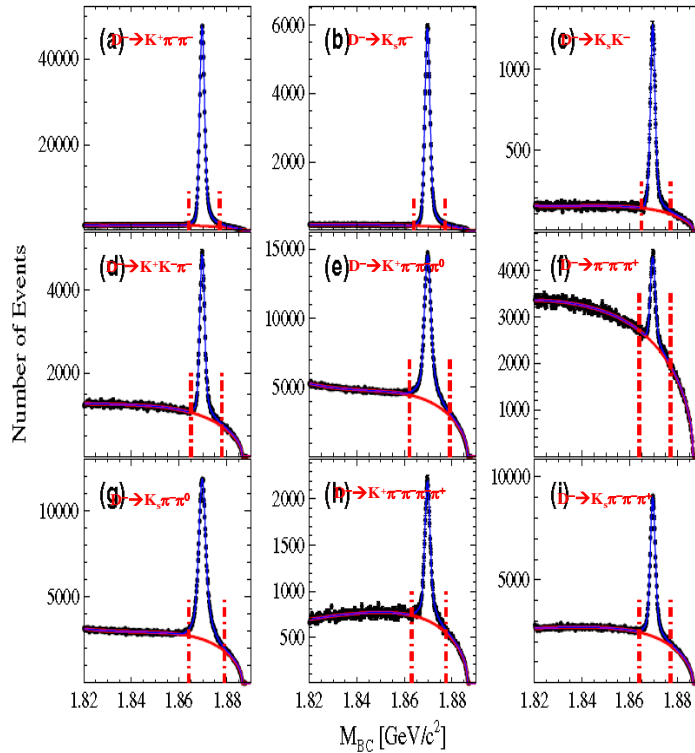
➤ D_s^+ samples

2011/2016
4.03/4.14 GeV 4.17 GeV 4.009/4.178



Single tag $D^{0(+)}$ at BESIII

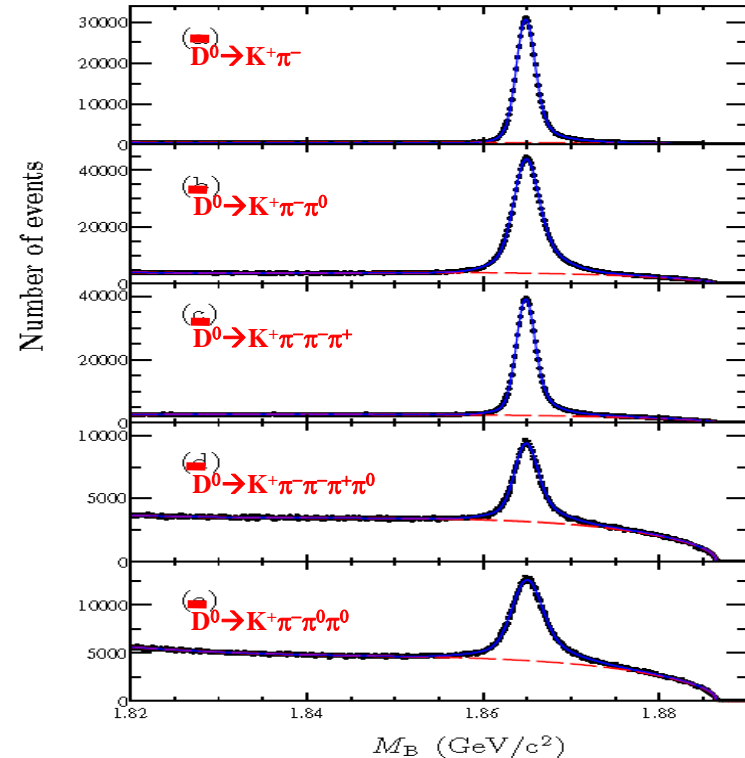
$$e^+e^- \rightarrow \psi(3770) \rightarrow D^+D^-$$



$$N_{D_{\text{tag}}^-} = (170.31 \pm 0.34) \times 10^4$$

6 largest tag modes
give 1.5 M D^- tags

$$e^+e^- \rightarrow \psi(3770) \rightarrow D^0\bar{D}^0$$



$$N_{D_{\text{tag}}^0} = (279.33 \pm 0.37) \times 10^4$$

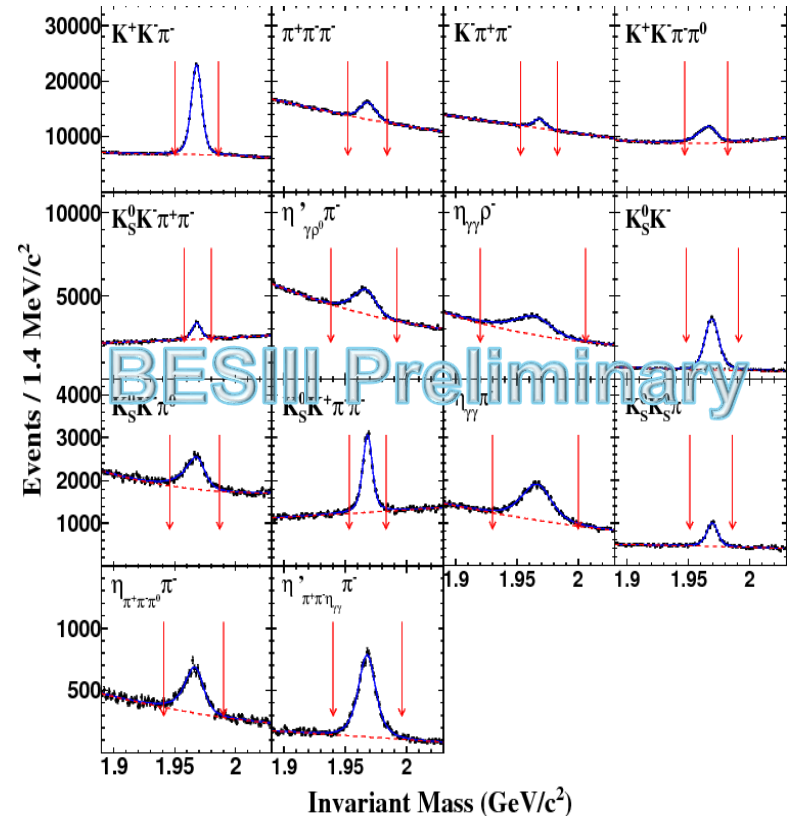
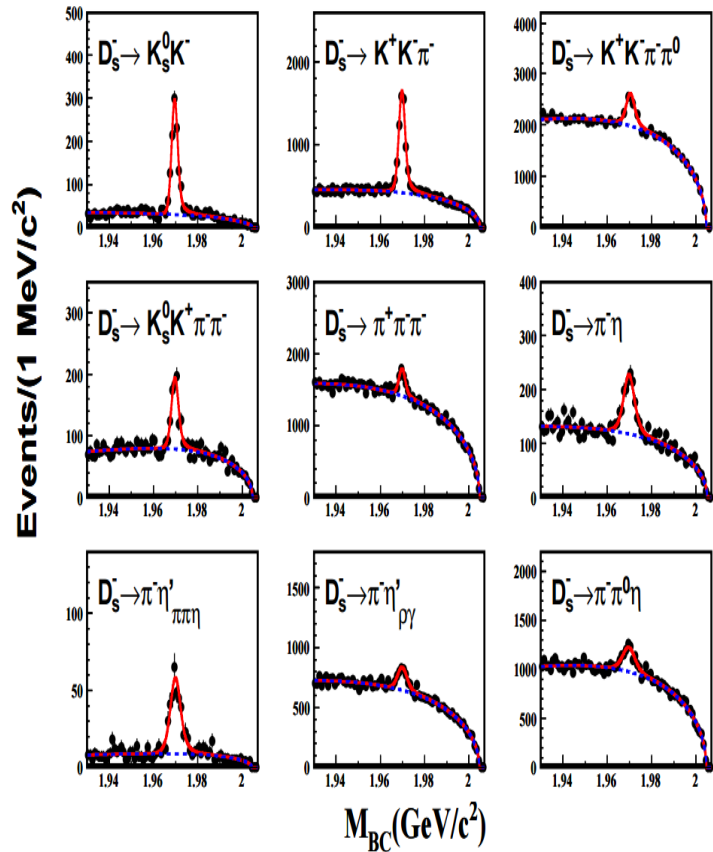
3 largest tag modes
give 2.3 M D^0 tags

Charge conjugations are included

Single tag D_s^+ at BESIII

$e^+e^- \rightarrow D_s^+ D_s^- @ 4.009 \text{ GeV}$

$e^+e^- \rightarrow D_s^{*+} D_s^- + \text{c.c.} @ 4.178 \text{ GeV}$



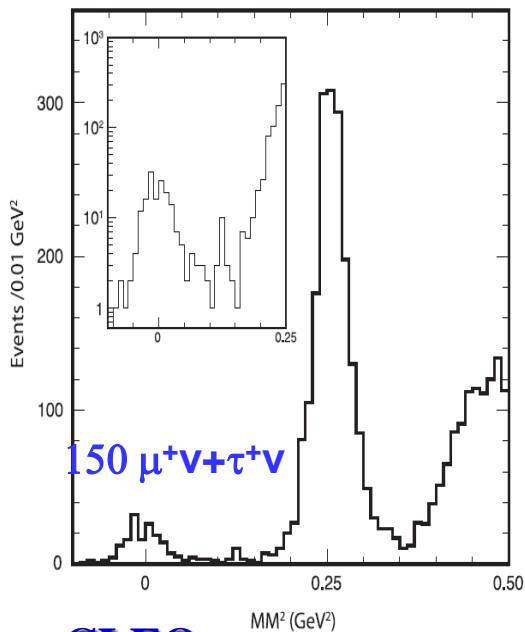
$$N_{D_s^- \text{tag}} = 15127 \pm 312$$

0.39 M ST D_s^- mesons

Measurement of $D^+ \rightarrow l^+ \nu$

818 pb⁻¹ at $\psi(3770)$
(2004–2008)

PRD78(2008)052003



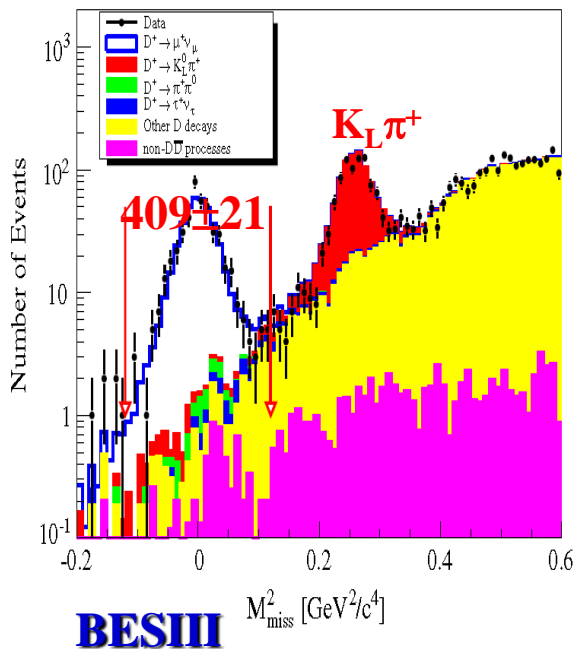
CLEO

$$B_{D^+ \rightarrow \mu^+ \nu} = (3.82 \pm 0.32 \pm 0.09) \times 10^{-4}$$

$$f_{D^+} = 205.8 \pm 7.5 \pm 2.5 \text{ MeV}$$

2.93 fb⁻¹ data@3.773 GeV

PRD89(2014)051104R



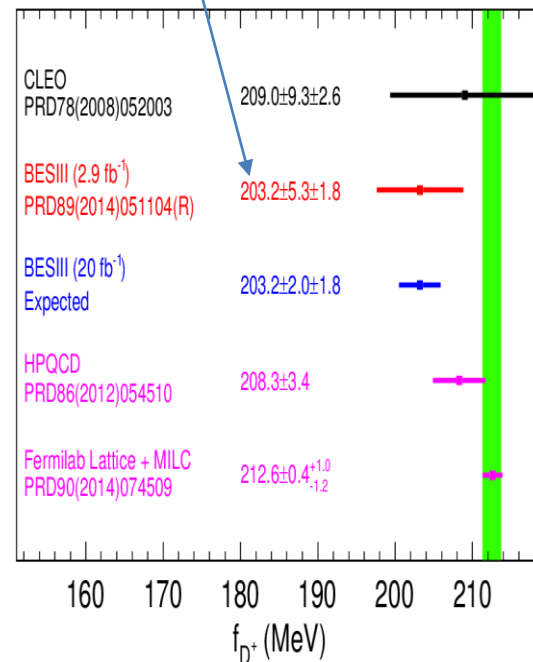
BESIII

$$B_{D^+ \rightarrow \mu^+ \nu} = (3.71 \pm 0.19 \pm 0.06) \times 10^{-4}$$

$$f_{D^+} = (203.2 \pm 5.3 \pm 1.8) \text{ MeV}$$

$$|V_{cd}| = 0.2210 \pm 0.0058 \pm 0.0047$$

BESIII result has been
re-calculated with the
latest LQCD calculation

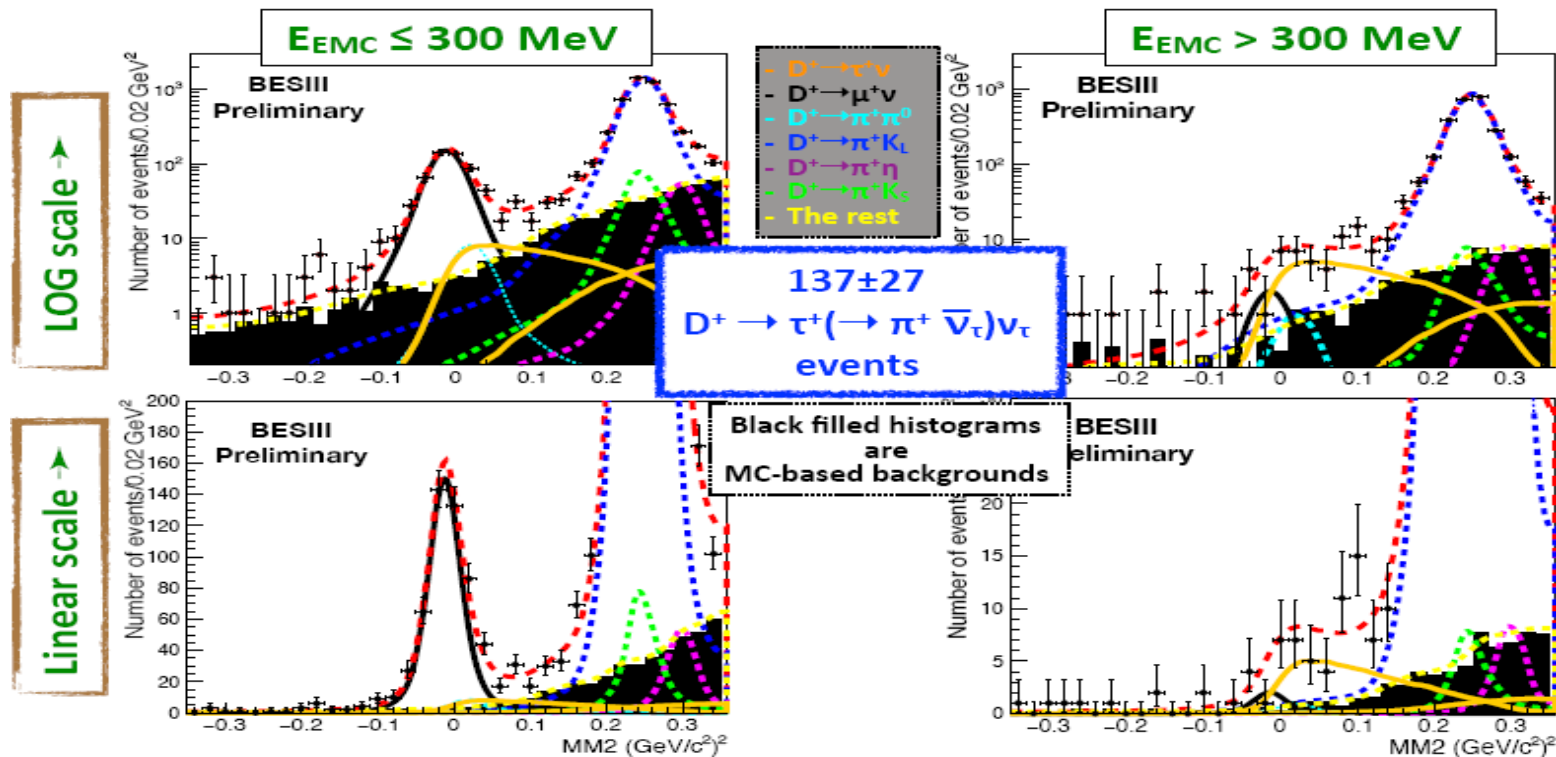


20 fb⁻¹ data help to
reduce the uncertainty
of f_{D^+} to 1%

Search for $D^+ \rightarrow \tau^+ \nu$

11

Fitting to DATA



4σ

$$B[D^+ \rightarrow \tau^+ \nu] = (1.20 \pm 0.24_{\text{stat.}}) \times 10^{-3}$$

20 fb⁻¹ data help to reduce the uncertainty to 8%

$$R \equiv \frac{\Gamma(D^+ \rightarrow \tau^+ \nu)}{\Gamma(D^+ \rightarrow \mu^+ \nu)} = \frac{m_{\tau^+}^2 \left(1 - \frac{m_{\tau^+}^2}{M_{D^+}^2}\right)^2}{m_{\mu^+}^2 \left(1 - \frac{m_{\mu^+}^2}{M_{D^+}^2}\right)^2}$$

SM prediction: 2.66

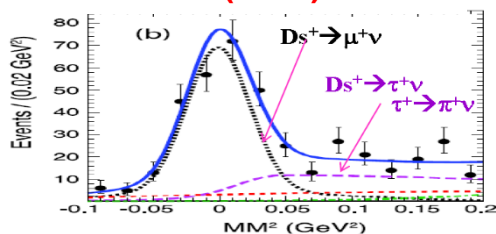
BESIII: 3.21 ± 0.64

Previous measurements of $D_s^+ \rightarrow l^+ \nu$

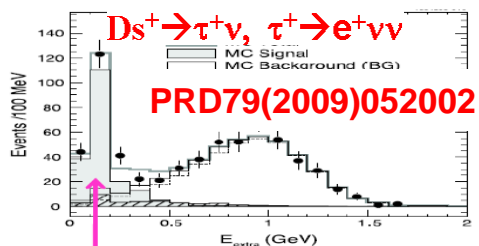
In the past 30 years, $D_s^+ \rightarrow l^+ \nu$ has been studied by WA75, CLEOII, E653, BESII, L3, OPAL, ALPHA, **CLEO-c, BELLE, Babar**

■ $D_s^+ D_s^-$, 600 pb⁻¹
@ 4.17 GeV [697 $l^+ \nu$]

PRD79(2009)052001

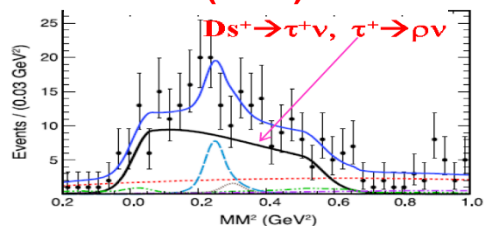


$f_{D_s^+} = 263.3 \pm 8.2 \pm 1.9$ MeV



Signal for $D_s^+ \rightarrow \tau^+ \nu$
 $f_{D_s^+} = 252.2 \pm 11.1 \pm 5.2$ MeV

PRD80(2009)112004

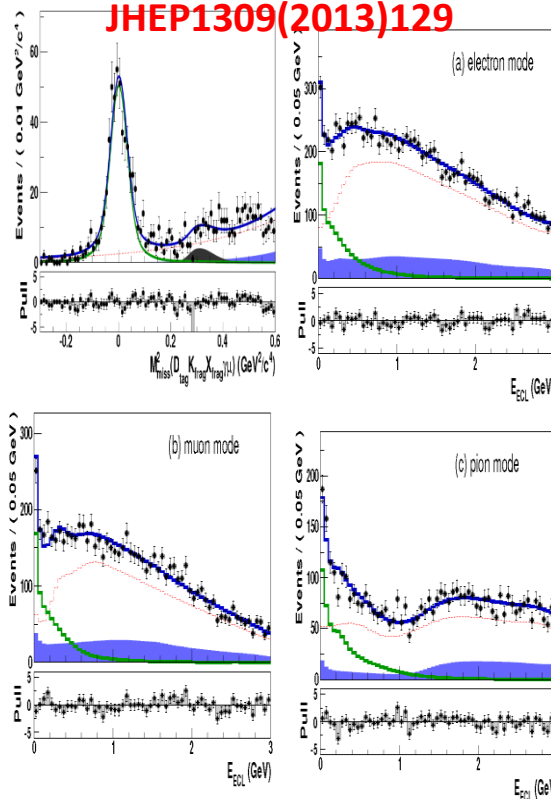


$f_{D_s^+} = 257.8 \pm 13.3 \pm 5.2$ MeV

■ Belle, 913 fb⁻¹ at
10.58 GeV [2698 $l^+ \nu$]

$$e^+ e^- \rightarrow DKXD_s^{*-}$$

JHEP1309(2013)129

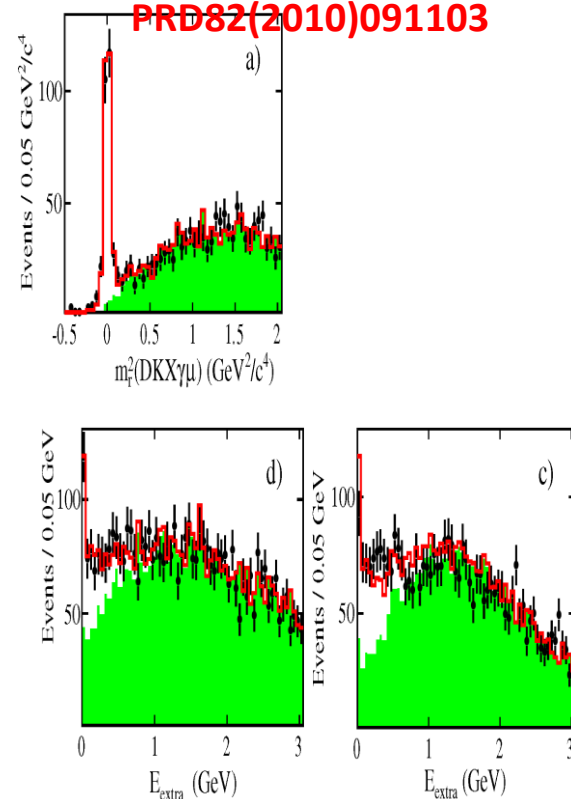


$f_{D_s^+} = 255.5 \pm 4.2 \pm 5.1$ MeV

■ Babar, 521 fb⁻¹ at
10.58 GeV [1023 $l^+ \nu$]

$$e^+ e^- \rightarrow DKXD_s^{*-}$$

PRD82(2010)091103



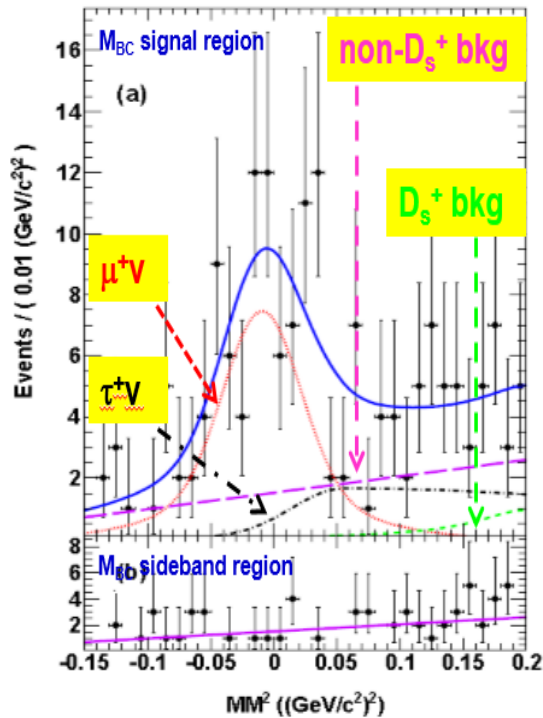
$f_{D_s^+} = 258.6 \pm 6.4 \pm 7.5$ MeV

Measurement of $D_s^+ \rightarrow l^+ \nu$

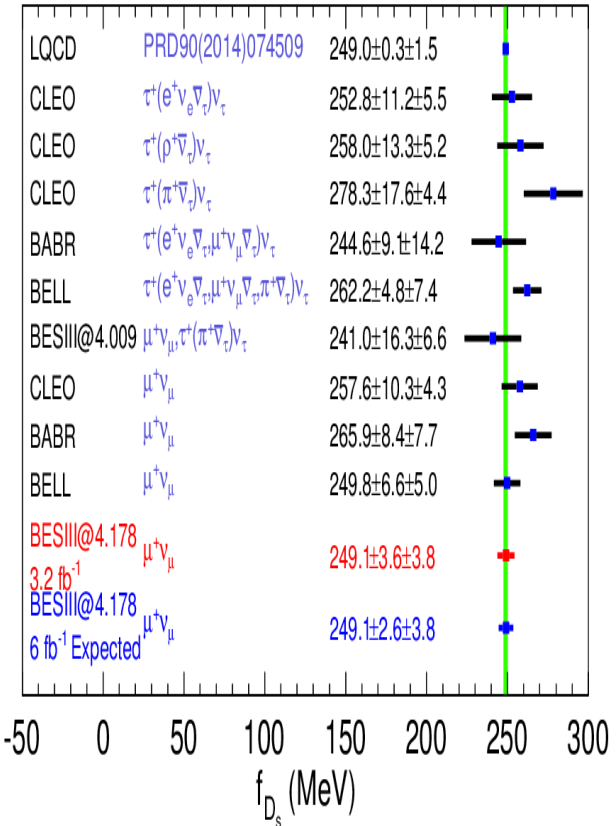
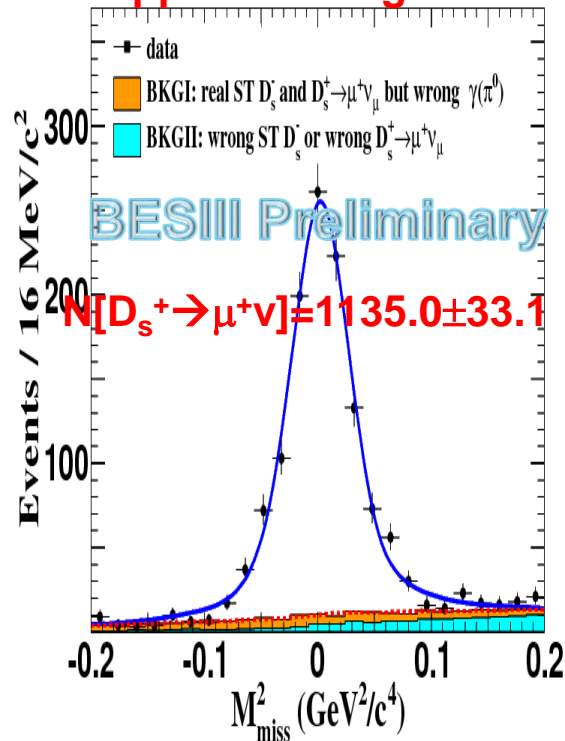
0.482 fb⁻¹ data
@4.009 GeV

3.19 fb⁻¹ data
@4.178 GeV

PRD94(2016)072004



Use μ counter to
suppress background



$$f_{D_{s^+}} = (241.0 \pm 16.3 \pm 6.6) \text{ MeV}$$

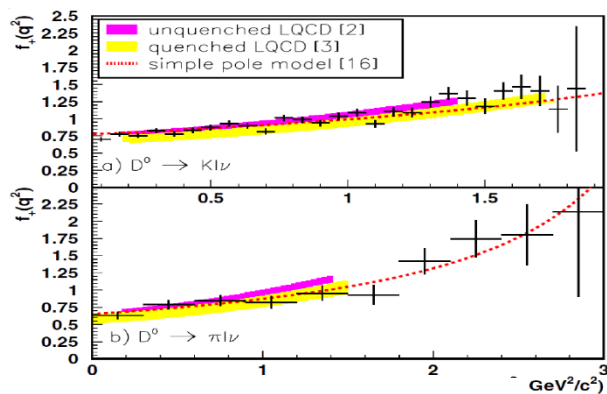
$$f_{D_{s^+}} |V_{cs}| = 242.5 \pm 3.5 \pm 3.7 \text{ MeV}$$

Uncertainty of $f_{D_{s^+}}$ with $\mu/\tau \nu$ is expected to reach 1.5% with 3.19 fb⁻¹ data

Previous measurements of $D \rightarrow K(\pi)l^+ \nu$

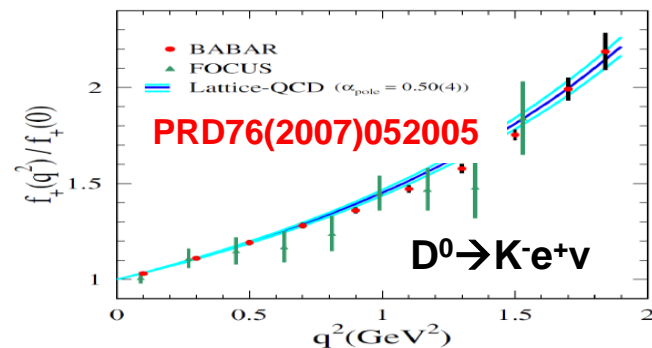
In the past 30 years, studies of $D \rightarrow K(\pi)l^+ \nu$ were made by MARKIII, E691, CLEO, CLEOII, BESII, FOCUS, **BELLE**, **Babar** and **CLEO-c**

■ **BELLE, 282 fb⁻¹ at 10.58 GeV**



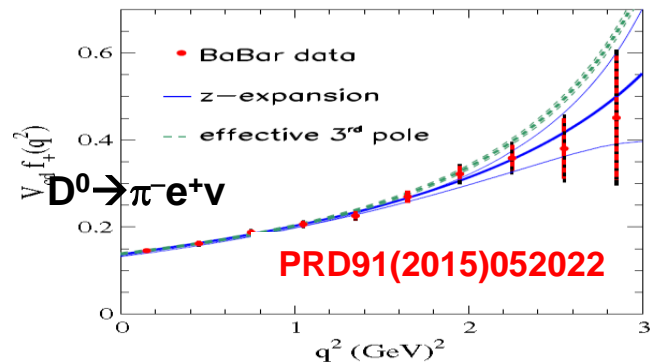
PRL97(2006)061804

■ **Babar, 75 fb⁻¹ at 10.58 GeV**



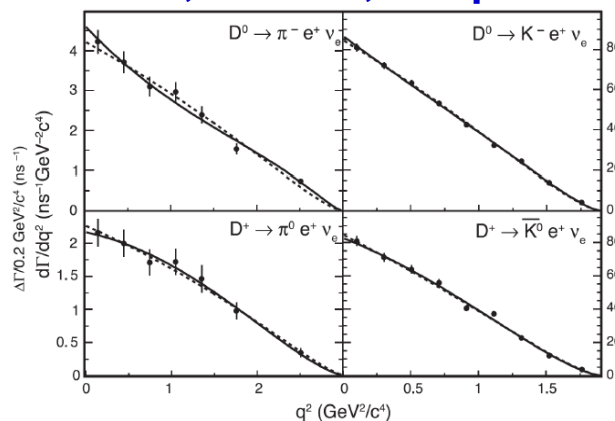
PRD76(2007)052005

■ **Babar, 347.2 fb⁻¹ at 10.58 GeV**



PRD91(2015)052022

■ **2004-2009, CLEO-c, 818 pb⁻¹ at psi''**



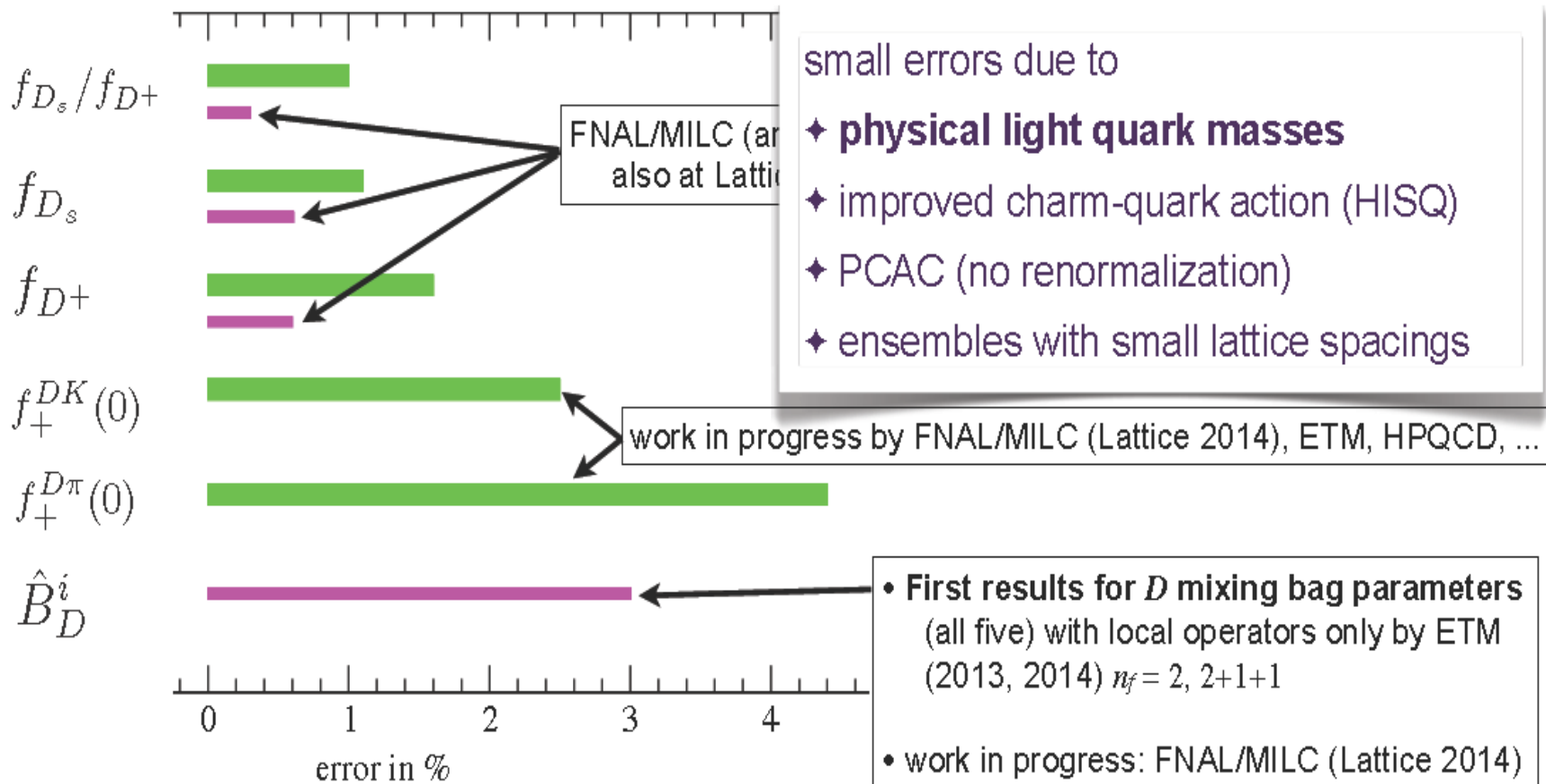
PRD80(2009)032005

Before 2010, the LQCD calculated $f_+^{D \rightarrow K(\pi)}(0)$ precision is at 10% level, thus limiting $|V_{cs(d)}|$ measurement

Progress in LQCD calculations

Taking from Aida X. El-Khadra's talk at Beauty2014

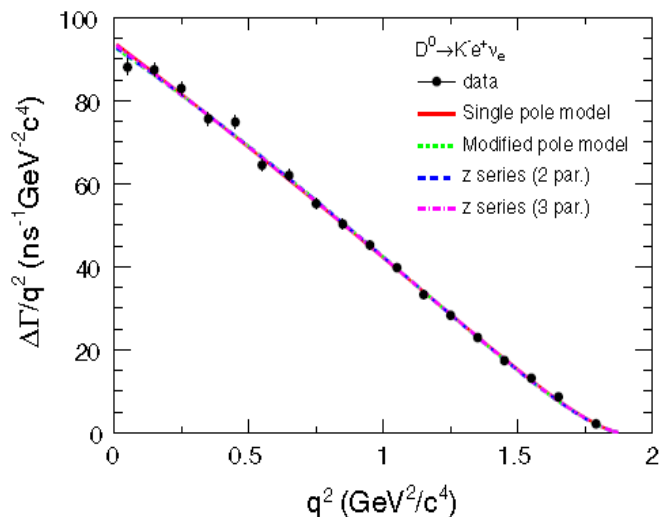
errors (in %) comparison: **FLAG-2 averages** vs. **new results**



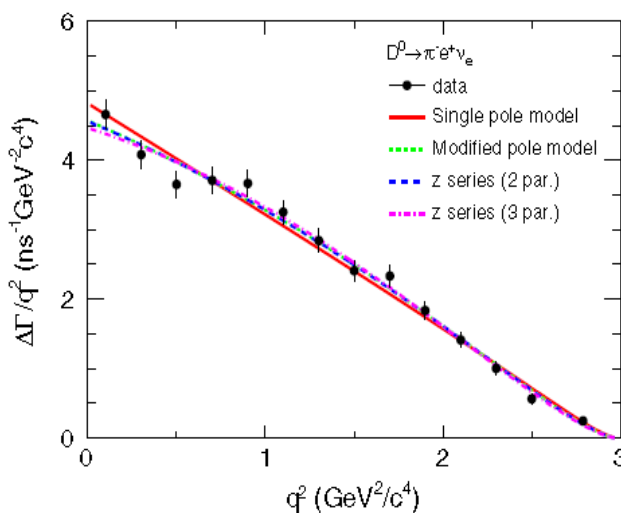
Analysis of $D^0 \rightarrow K(\pi)^- e^+ \nu$

PRD92(2015)072012

$$B_{D^0 \rightarrow K^- e^+ \nu} = (3.505 \pm 0.014 \pm 0.033)\%$$



$$B_{D^0 \rightarrow \pi^- e^+ \nu} = (0.2950 \pm 0.0041 \pm 0.0026)\%$$



Different parameterizations of form factor

– Single pole

$$f_+(q^2) = \frac{f_+(0)}{1 - \frac{q^2}{M_{\text{pole}}^2}}$$

– Modified pole

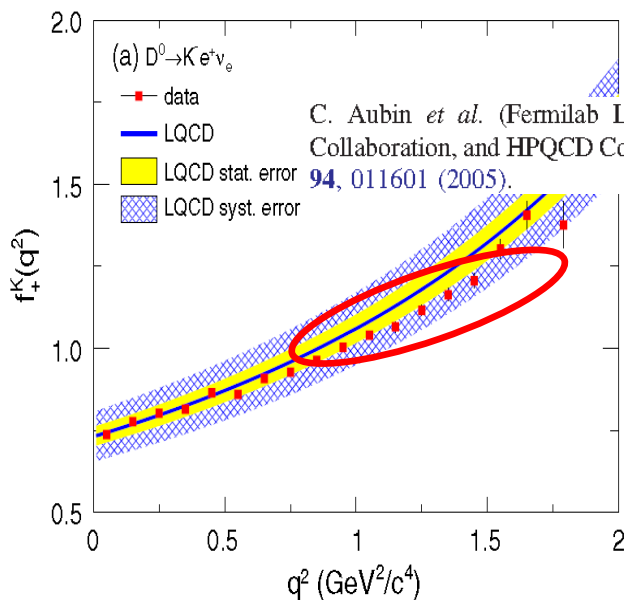
$$f_+(q^2) = \frac{f_+(0)}{(1 - \frac{q^2}{M_{\text{pole}}^2})(1 - \alpha \frac{q^2}{M_{\text{pole}}^2})}$$

– ISGW2

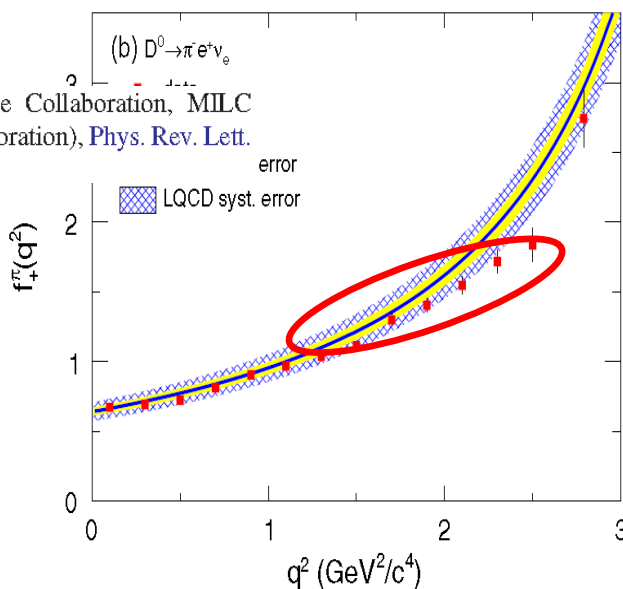
$$f_+(q^2) = f_+(q_{\text{max}}^2) \left(1 + \frac{r_{\text{ISGW2}}^2}{12} (q_{\text{max}}^2 - q^2) \right)^{-2}$$

– Series expansion

$$f_+(t) = \frac{1}{P(t)\Phi(t, t_0)} a_0(t_0) \left(1 + \sum_{k=1}^{\infty} r_k(t_0) [z(t, t_0)]^k \right)$$



C. Aubin *et al.* (Femilab Lattice Collaboration, MILC Collaboration, and HPQCD Collaboration), *Phys. Rev. Lett.* **94**, 011601 (2005).



Analysis of $D^+ \rightarrow K_L e^+ \nu$

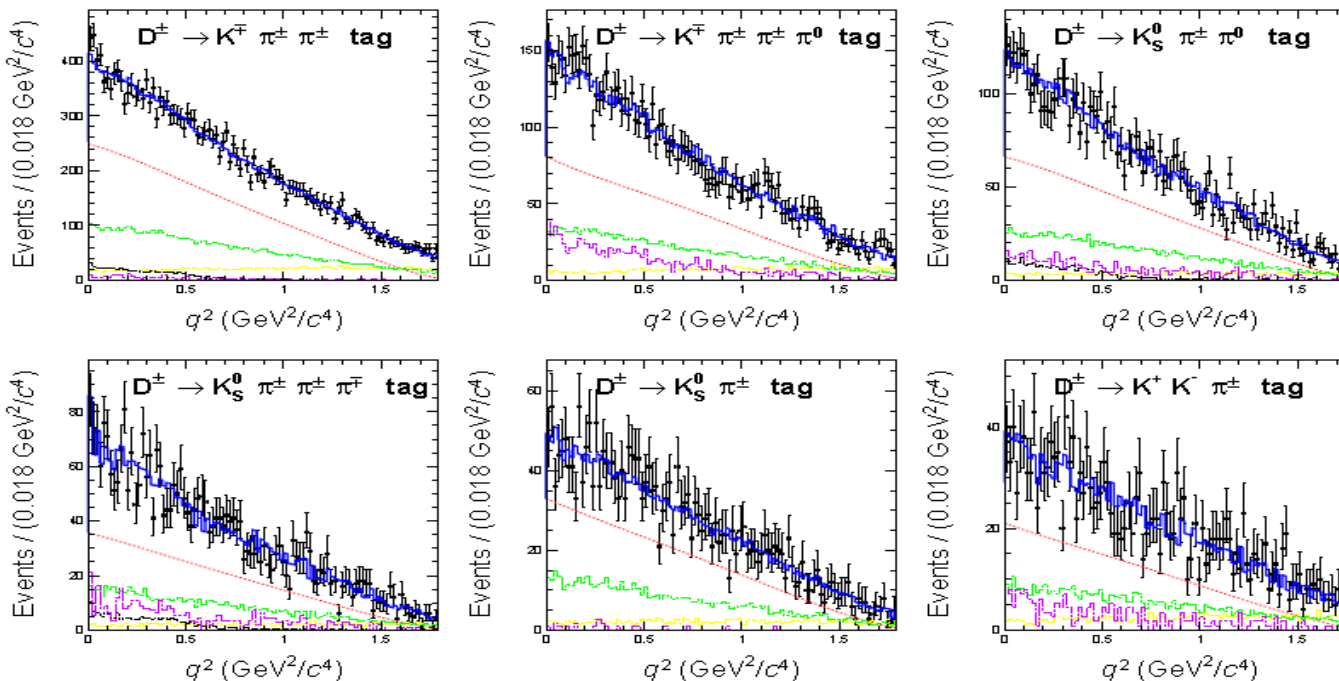
PRD92(2015)112008

Simultaneous fit to event density $I(q^2)$ with 2-par. series Form Factor

$$\bar{B}(D^+ \rightarrow K_L e^+ \nu) = (4.482 \pm 0.027 \pm 0.103)\%$$

$$A_{CP} \equiv \frac{\mathcal{B}(D^+ \rightarrow K_L^0 e^+ \nu_e) - \mathcal{B}(D^- \rightarrow K_L^0 e^- \bar{\nu}_e)}{\mathcal{B}(D^+ \rightarrow K_L^0 e^+ \nu_e) + \mathcal{B}(D^- \rightarrow K_L^0 e^- \bar{\nu}_e)}$$

$$A_{CP}^{D^+ \rightarrow K_L e^+ \nu} = (-0.59 \pm 0.60 \pm 1.50)\%$$



$D^+ \rightarrow K_L e^+ \nu$ is measured for the first time

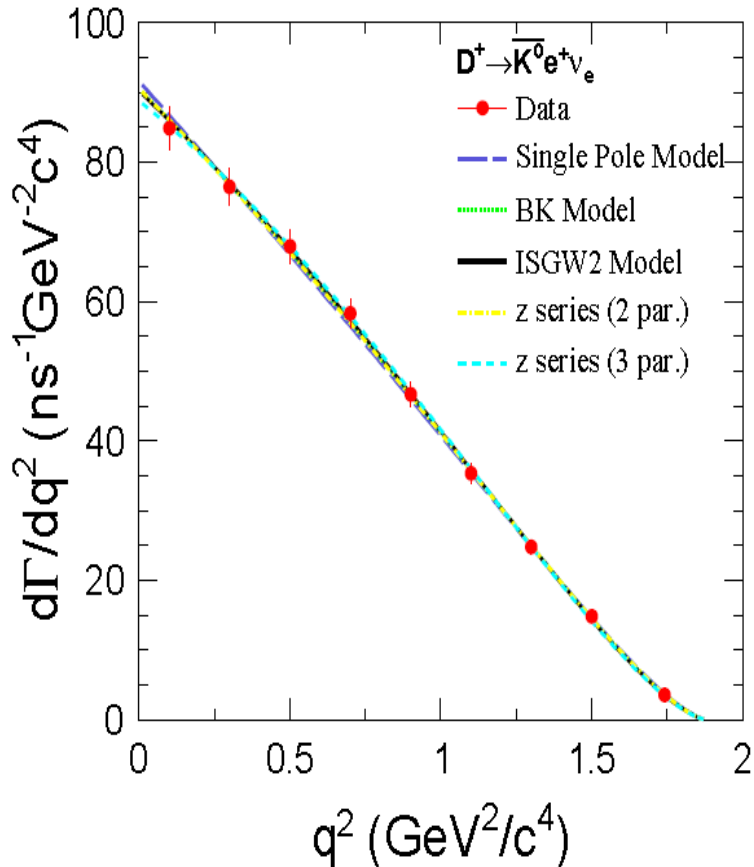
$$f_+^{K^0}(0)|V_{cs}| = 0.728 \pm 0.006 \pm 0.011$$

Analysis of $D^+ \rightarrow \bar{K}(\pi)^0 e^+ \nu$

PRD96(2017)012002

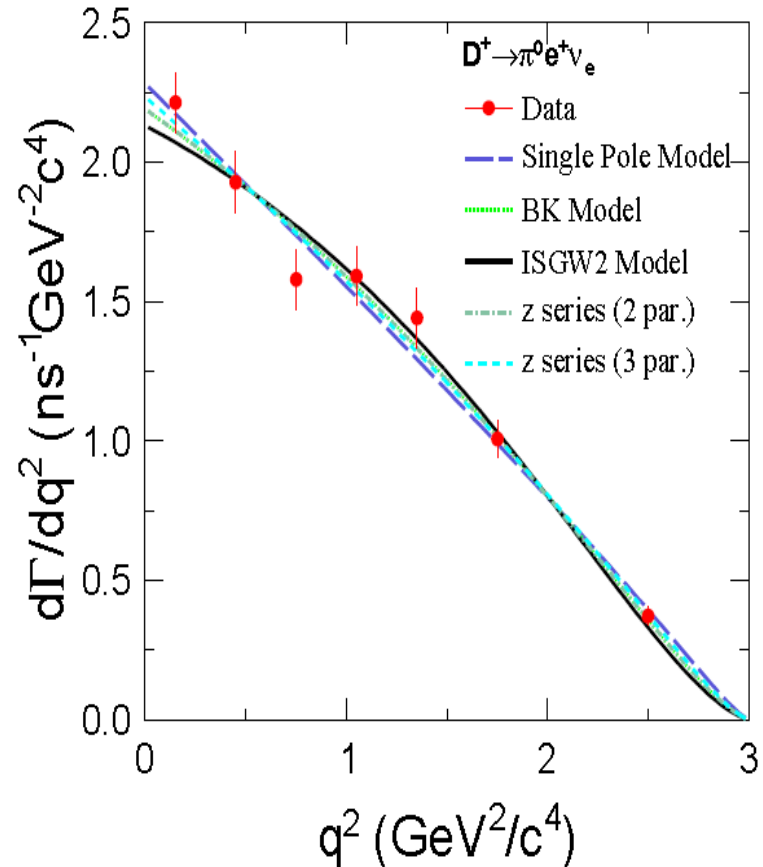
$$B[D^+ \rightarrow \bar{K}^0 e^+ \nu] = (8.604 \pm 0.056 \pm 0.151)\%$$

$$I_K \equiv \frac{\Gamma(D^0 \rightarrow K^- e^+ \nu_e)}{\Gamma(D^+ \rightarrow \bar{K}^0 e^+ \nu_e)} = 1.03 \pm 0.01 \pm 0.02$$

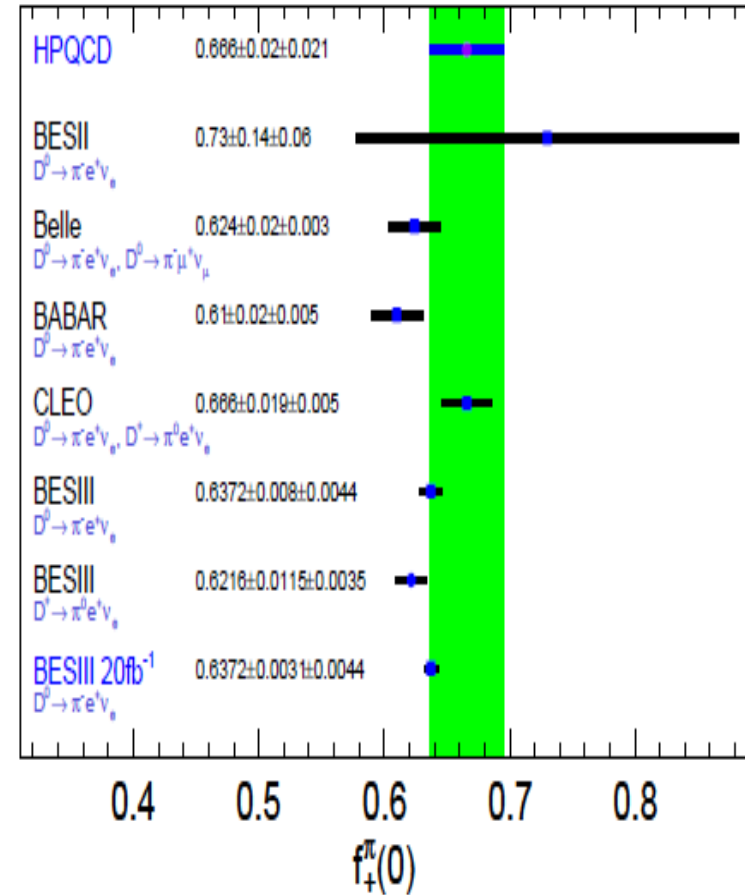
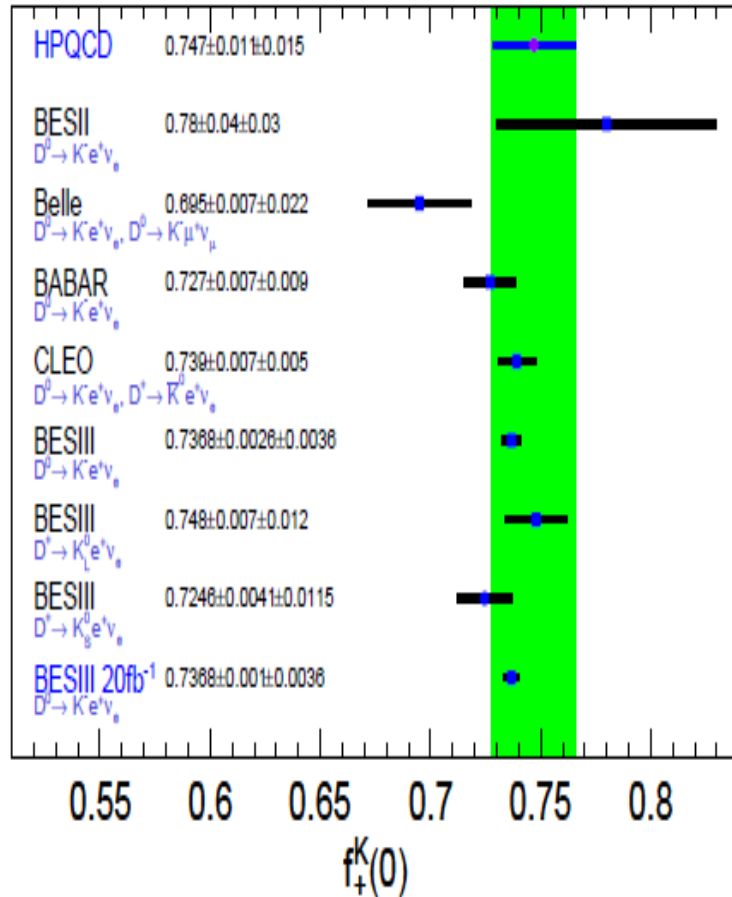


$$B[D^+ \rightarrow \pi^0 e^+ \nu] = (3.631 \pm 0.075 \pm 0.051) \times 10^{-3}$$

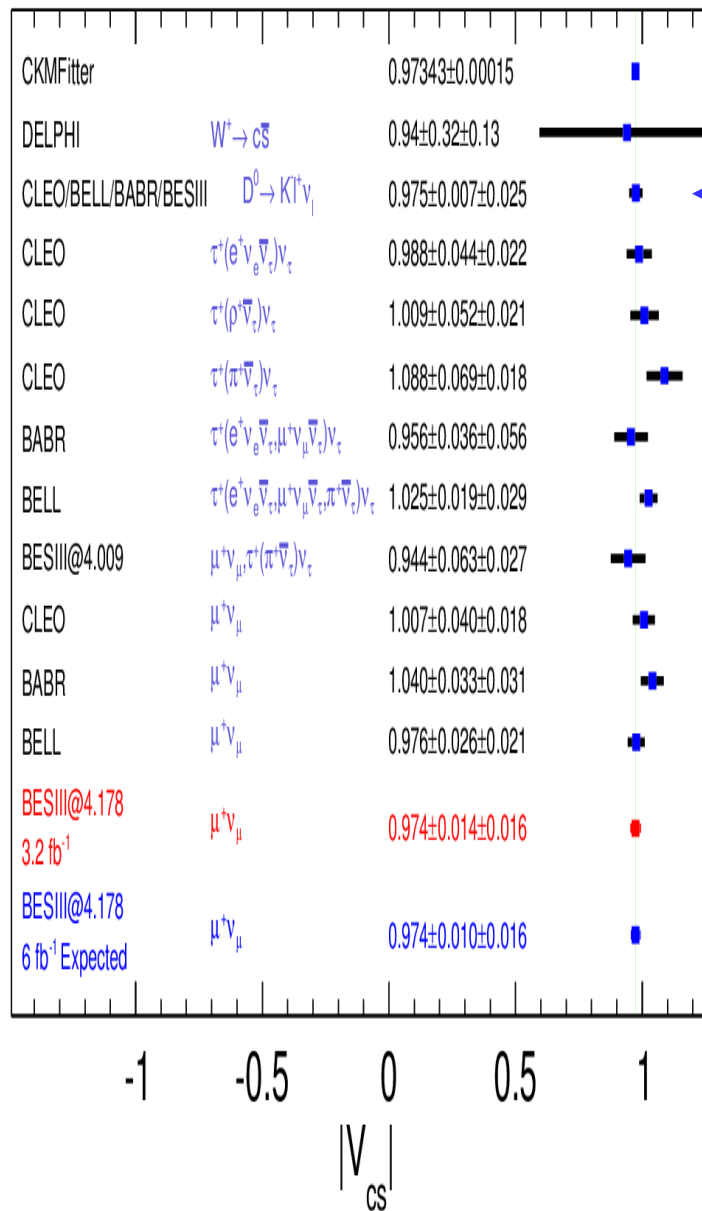
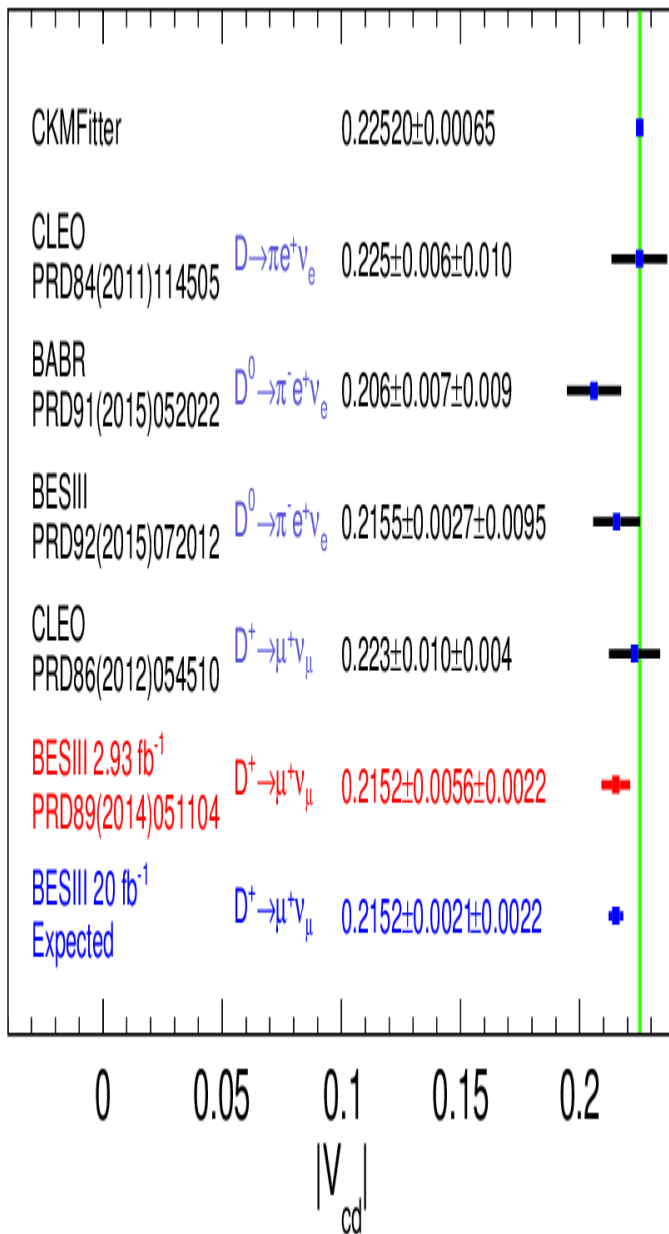
$$I_\pi \equiv \frac{\Gamma(D^0 \rightarrow \pi^- e^+ \nu_e)}{2\Gamma(D^+ \rightarrow \pi^0 e^+ \nu_e)} = 1.03 \pm 0.03 \pm 0.02$$



Comparisons of $f^{D \rightarrow K(\pi)}_+(0)$



Measurements of $|V_{cs(d)}|$

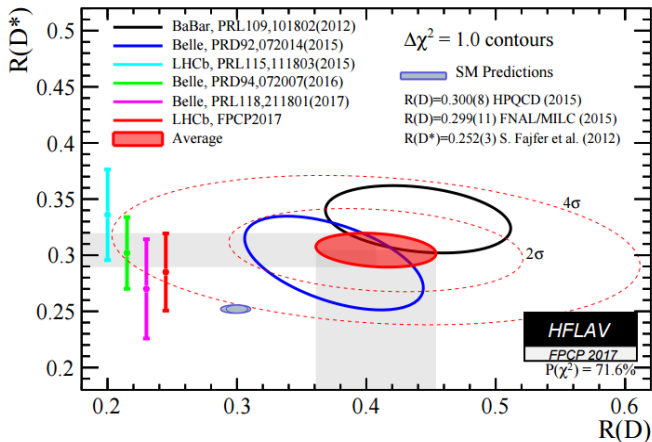


Taken from PDG, and the SL method suffers about 2.4% error from LQCD

Test of LFU in $D^{0(+)} \rightarrow \pi l^+ \nu$ decays

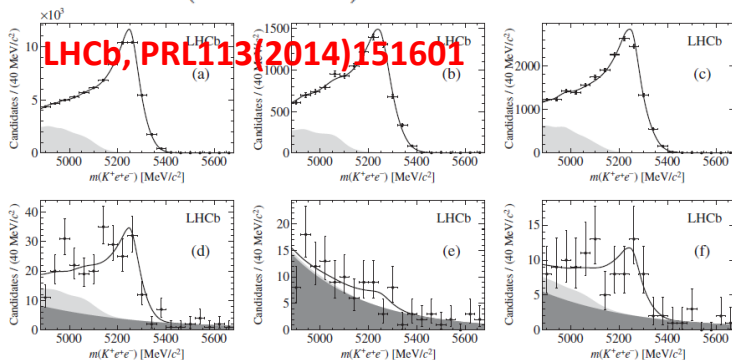
Evidence of LFV at 4σ in

$$R(D^{(*)}) = \frac{B(B \rightarrow D^{(*)} \tau \nu)}{B(B \rightarrow D^{(*)} l \nu)}$$



Evidence of LFV at 2.6σ in FCNC decays $B^+ \rightarrow K^+ \mu^+ \mu^- / K^+ e^+ e^-$

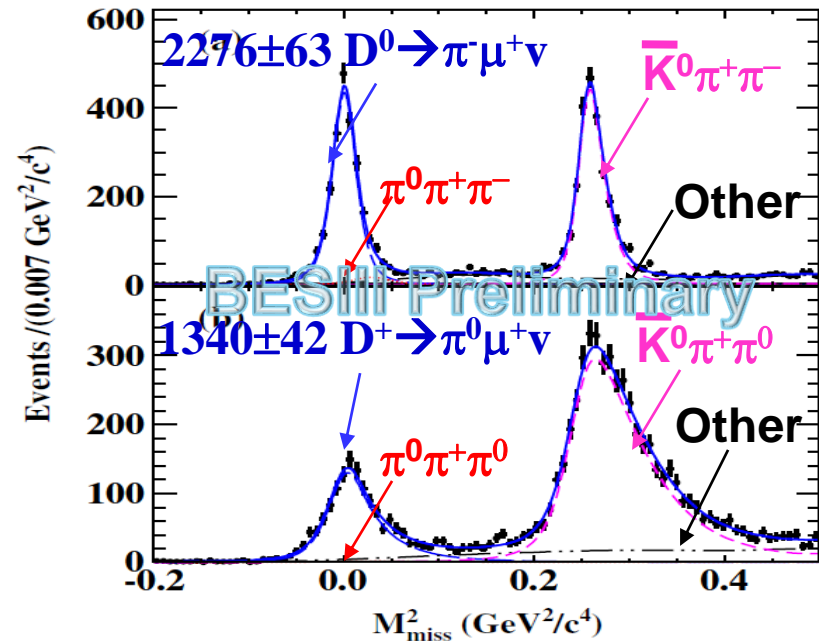
$$R_K = \frac{\Gamma(\bar{B} \rightarrow \bar{K} \mu^+ \mu^-)}{\Gamma(\bar{B} \rightarrow \bar{K} e^+ e^-)} = 0.745^{+0.090}_{-0.074} \pm 0.036$$



$$R_{LU}^{0(+)} = \frac{B(D^{0(+)} \rightarrow \pi^{-(0)} \mu^+ \nu)}{B(D^{0(+)} \rightarrow \pi^{-(0)} e^+ \nu)} \sim 0.97$$

B^{PDG16}: $R_{LU}^0 = 0.82 \pm 0.08$ ($\sim 2.0\sigma$)

$$B(D^0 \rightarrow \pi^- \mu^+ \nu) = (0.237 \pm 0.024)\%$$



$$B[D^0 \rightarrow \pi^- \mu^+ \nu] = (0.267 \pm 0.007 \pm 0.007)\%$$

$$B[D^+ \rightarrow \pi^0 \mu^+ \nu] = (0.342 \pm 0.011 \pm 0.010)\%$$

$$R_{LU}^0 = 0.918 \pm 0.036$$

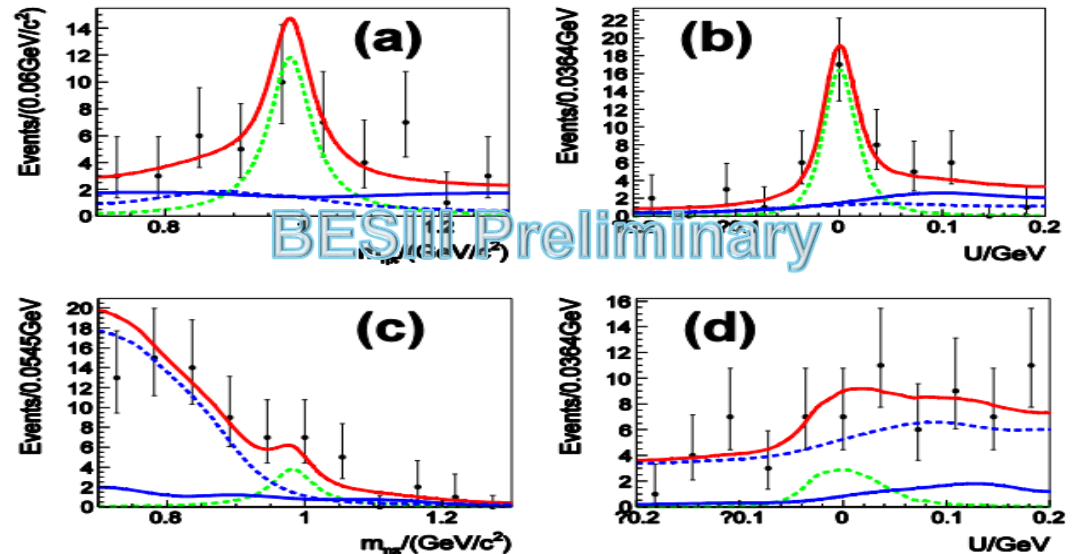
$$R_{LU}^+ = 0.921 \pm 0.045$$

Observation of $D \rightarrow \text{Se}^+ \nu$

- Explore the nontrivial internal structure of light hadron mesons, traditional $q\bar{q}$ states, tetra quark system.
- With chiral unitarity approach in the coupled channels, BF is predicted to be order of $5(6) \times 10^{-5}$ for $D^{0(+)}$ decays
- Improve understanding of classification of light scalar mesons

$$R \equiv \frac{B(D^+ \rightarrow f_0 l^+ \nu) + B(D^+ \rightarrow \sigma l^+ \nu)}{B(D^+ \rightarrow a_0 l^+ \nu)}$$

$R=1(3)$ if traditional $q\bar{q}$ (tetra quark) system



$$\odot B(D^0 \rightarrow a_0(980)^- e^+ \nu_e) \times B(a_0(980)^- \rightarrow \eta \pi^-) = (1.12^{+0.31}_{-0.28}(\text{stat}) \pm 0.10(\text{syst})) \times 10^{-4}$$

5.9σ

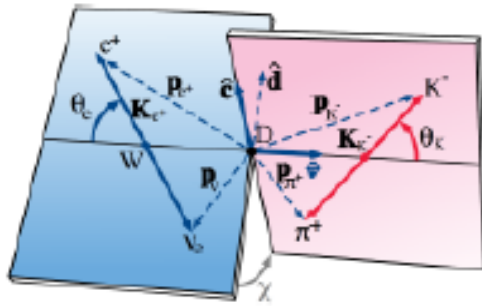
$$\odot B(D^+ \rightarrow a_0(980)^0 e^+ \nu_e) \times B(a_0(980)^0 \rightarrow \eta \pi^0) = (1.47^{+0.73}_{-0.59}(\text{stat}) \pm 0.14(\text{syst})) \times 10^{-4}$$

3.0σ

$$\odot B(D^+ \rightarrow a_0(980)^0 e^+ \nu_e) \times B(a_0(980)^0 \rightarrow \eta \pi^0)$$

$< 2.7 \times 10^{-4}$ @ 90% C.L.

Form factors of $D \rightarrow V e^+ \nu$



- $m^2 = (p_{\pi^+} + p_{K^-})^2$

- $\cos(\theta_K) = \frac{\hat{v} \cdot \mathbf{K}_{K^-}}{|\mathbf{K}_{K^-}|}$

- $\cos(\chi) = \hat{c} \cdot \hat{d}$

- $q^2 = (p_{e^+} + p_{\nu_e})^2$

- $\cos(\theta_e) = -\frac{\hat{v} \cdot \mathbf{K}_{e^+}}{|\mathbf{K}_{e^+}|}$

- $\sin(\chi) = (\hat{c} \times \hat{v}) \cdot \hat{d}$

Decay rate depend on **5 variables** and **3 form factors**

$$d^5\Gamma = \frac{G_F^2 |V_{cs}|^2}{(4\pi)^6 m_D^2} X \beta \mathcal{I}(m^2, q^2, \theta_K, \theta_e, \chi) dm^2 dq^2 d\cos(\theta_K) d\cos(\theta_e) d\chi$$

- $X = p_{K\pi} m_D$, $p_{K\pi}$ is the momentum of the $K\pi$ system in the D rest frame
- $\beta = 2p^*/m$, p^* is the breakup momentum of the $K\pi$ system in its rest frame
- \mathcal{I} can be expressed in terms of helicity amplitudes $H_{0,\pm}$:

$$H_0(q^2) = \frac{1}{2m_q} \left[(m_D^2 - m^2 - q^2)(m_D + m) A_1(q^2) - 4 \frac{m_D^2 p_{K\pi}^2}{m_D + m} A_2(q^2) \right]$$

$$H_{\pm}(q^2) = (m_D + m) A_1(q^2) \mp \frac{2m_D p_{K\pi}}{m_D + m} V(q^2)$$

- Vector form factor: $V(q^2) = \frac{V(0)}{1 - q^2/m_V^2}$; or: FF ratio $r_V = V(0)/A_1(0)$

- Axial-vector form factor: $A_1(q^2) = \frac{A_1(0)}{1 - q^2/m_A^2}$, $A_2(q^2) = \frac{A_2(0)}{1 - q^2/m_A^2}$; or: FF ratio $r_2 = A_2(0)/A_1(0)$

PWA of $D^+ \rightarrow K^- \pi^+ e^+ \nu$

PRD94(2016)032001

Fractions with $>5\sigma$ significance

$$f(D^+ \rightarrow (K^- \pi^+)_{K^{*0}(892)} e^+ \nu_e) = (93.93 \pm 0.22 \pm 0.18)\%$$

$$f(D^+ \rightarrow (K^- \pi^+)_{S\text{-wave}} e^+ \nu_e) = (6.05 \pm 0.22 \pm 0.18)\%$$

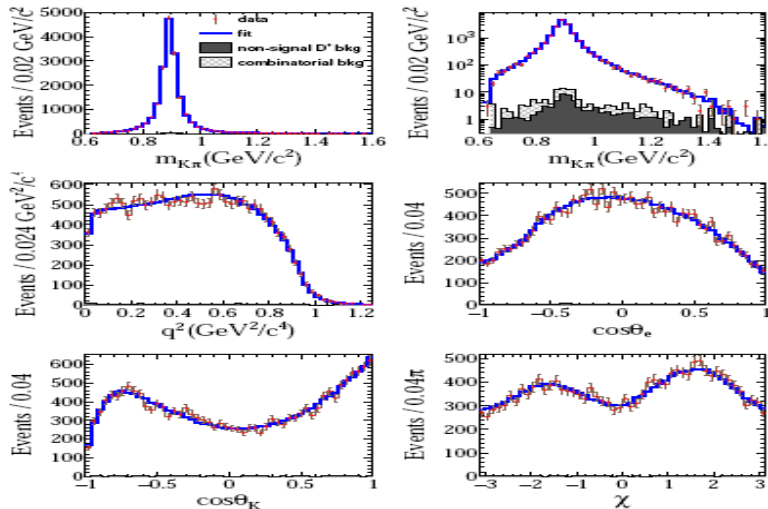
Properties of different $K\pi$ (non-) resonant amplitudes

$$m_{K^{*0}(892)} = (894.60 \pm 0.25 \pm 0.08) \text{ MeV}/c^2$$

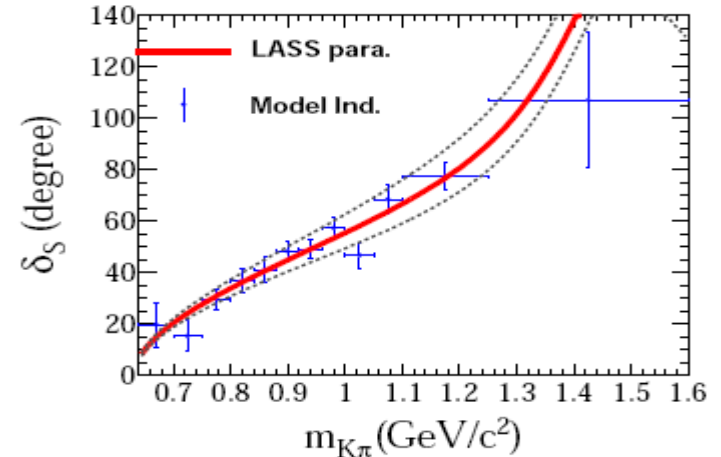
$$\Gamma_{K^{*0}(892)} = (46.42 \pm 0.56 \pm 0.15) \text{ MeV}/c^2$$

$$r_{BW} = (3.07 \pm 0.26 \pm 0.11) (\text{GeV}/c^2)^{-1}$$

q^2 dependent form factors in $D^+ \rightarrow \bar{K}^{*0}(892) e^+ \nu$



Model independent S-wave phase measurement



$$V(q^2) = \frac{V(0)}{1 - q^2/m_V^2}, \quad A_{1,2}(q^2) = \frac{A_{1,2}(0)}{1 - q^2/m_A^2}$$

$M_{V/A}$ is expected to be $M_{D^*(1/+)}$

$$m_V = (1.81^{+0.25}_{-0.17} \pm 0.02) \text{ GeV}/c^2$$

$$m_A = (2.61^{+0.22}_{-0.17} \pm 0.03) \text{ GeV}/c^2$$

$$A_1(0) = 0.573 \pm 0.011 \pm 0.020$$

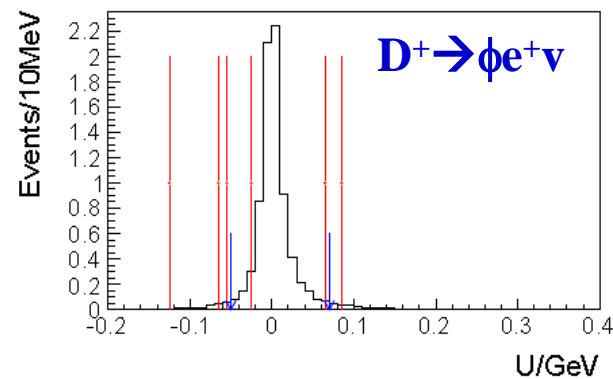
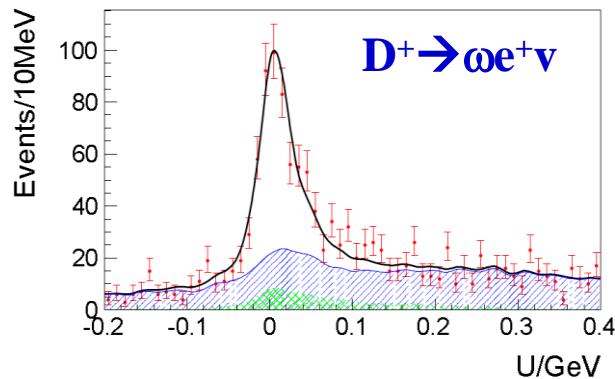
$$r_V = V(0)/A_1(0) = 1.411 \pm 0.058 \pm 0.007$$

$$r_2 = A_2(0)/A_1(0) = 0.788 \pm 0.042 \pm 0.008$$

Model independent form factors

Study of $D^+ \rightarrow \omega e^+ \nu$ and search for $D^+ \rightarrow \phi e^+ \nu$

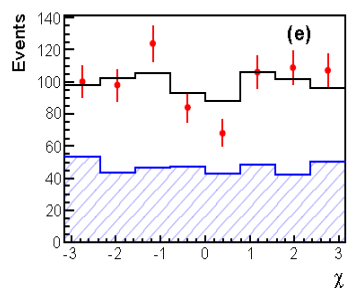
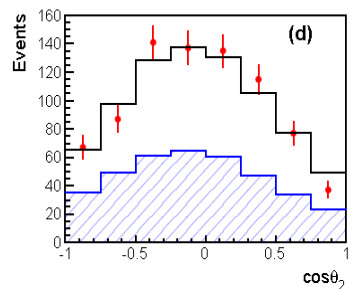
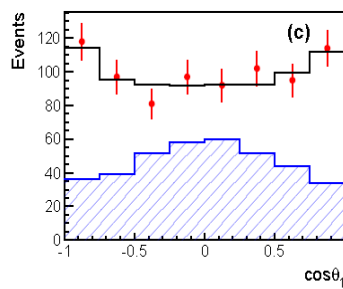
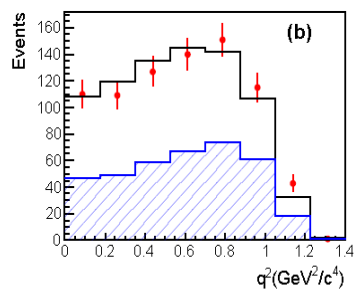
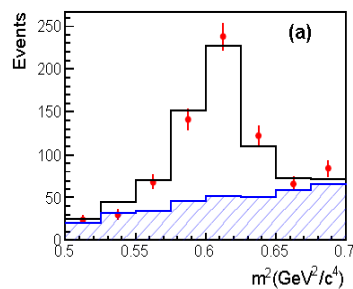
PRD92(2015)071101(RC)



$$B[D^+ \rightarrow \omega e^+ \nu] = (1.63 \pm 0.11 \pm 0.08) \times 10^{-3}$$

$$B[D^+ \rightarrow \phi e^+ \nu] < 1.3 \times 10^{-5} \text{ at 90\% C.L.}$$

Better precision or sensitivity

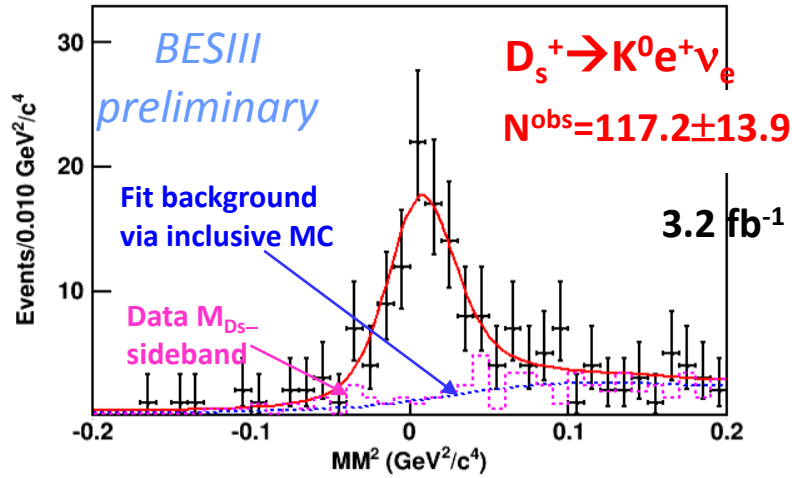


Amplitude analysis of $D^+ \rightarrow \omega e^+ \nu$ is performed for the first time

$$r_V = V(0)/A_1(0) = 1.24 \pm 0.09 \pm 0.06$$

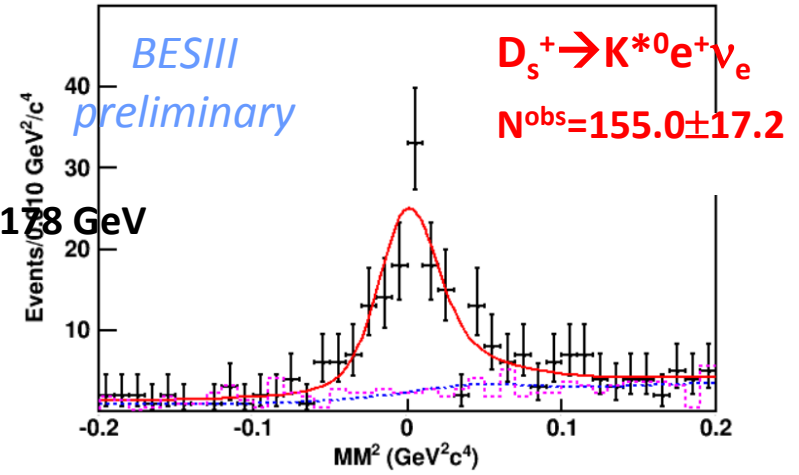
$$r_2 = A_2(0)/A_1(0) = 1.06 \pm 0.15 \pm 0.05$$

Studies of $D_s^+ \rightarrow K^{(*)0} e^+ \nu$ at 4.178 GeV



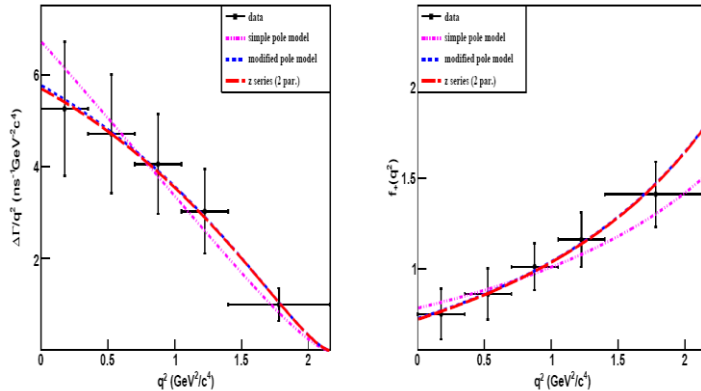
$$B[D_s^+ \rightarrow K^0 e^+ \nu_e] = (3.25 \pm 0.38_{\text{stat}} \pm 0.14_{\text{syst}}) \times 10^{-3}$$

$$(3.9 \pm 0.9) \times 10^{-3} \text{ [PDG17]}$$



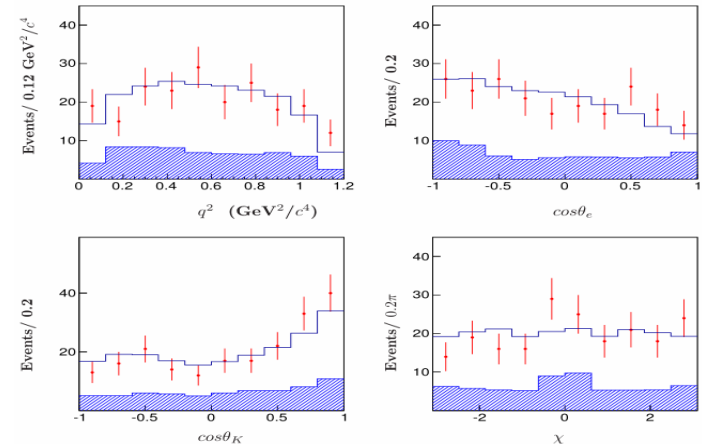
$$B[D_s^+ \rightarrow K^{*0} e^+ \nu_e] = (2.38 \pm 0.26_{\text{stat}} \pm 0.12_{\text{syst}}) \times 10^{-3}$$

$$(1.8 \pm 0.4) \times 10^{-3} \text{ [PDG17]}$$



Model	Parameter	Value	$f_+(0)$
Simple pole	$f_+(0) V_{cd} $	$0.175 \pm 0.010 \pm 0.001$	$0.778 \pm 0.044 \pm 0.004$
Modified pole model	$f_+(0) V_{cd} $	$0.163 \pm 0.017 \pm 0.003$	$0.725 \pm 0.076 \pm 0.013$
	α	$0.45 \pm 0.44 \pm 0.02$	
Series two parameters	$f_+(0) V_{cd} $	$0.162 \pm 0.019 \pm 0.003$	$0.720 \pm 0.084 \pm 0.013$
	r_1	$-2.94 \pm 2.32 \pm 0.14$	

Four dimensional un-binned likelihood fit is performed. K^* parameters are fixed



$$r_V = 1.67 \pm 0.34 \pm 0.16$$

$$r_2 = 0.77 \pm 0.28 \pm 0.07$$

Taking $|V_{CKMfitter}^{cd}|$ as input

Summary

■ With $\sim 3/3 \text{ fb}^{-1}$ data taken at 3.773/4.178 GeV by BESIII, the leptonic decay of $D_{(s)}^+ \rightarrow l^+ \nu$ and some semi-leptonic D decays, and improved measurements of $|V_{cs(d)}|$, decay constants, form factors have been obtained

■ More results are expected in the near future

$D_s^+ \rightarrow \tau^+ \nu$, $f_{D_{s^+}}$ and $|V_{cs}|$

$D_s^+ \rightarrow \eta^{(\prime)} e^+ \nu$, form factors and $|V_{cs}|$

$D_s^+ \rightarrow K^+ K^- / \pi^+ \pi^- e^+ \nu$, form factors

$D^0 \rightarrow K^- \mu^+ \nu$, $f_K^+(q^2)$ and $|V_{cs}|$

$D \rightarrow K_1(1270) e^+ \nu$

$D_{(s)}^{0(+)} \rightarrow X e^+ \nu$

All Cabibbo-suppressed $D^{0(+)}$ decays and D_s^+ decays are restricted by the limited data

Prospects at BESIII

- With 20/6 fb⁻¹ data taken at 3.773/4.178 GeV, some elementary constants can be further improved

	Systematic error	Statistical error	
		~3 fb ⁻¹	Expected with 20/6 fb ⁻¹
$\Delta f_{D^+}/f_{D^+}$	0.9%	2.6%	0.5%
$\Delta f_{D_s^+}/f_{D_s^+}$	1.5%	1.5%	~1%
$\Delta f_{D \rightarrow K}/f_{D \rightarrow K}$	0.5%	0.4%	0.15%
$\Delta f_{D \rightarrow \pi}/f_{D \rightarrow \pi}$	0.7%	1.3%	0.5%
$ V_{cs} ^{D_s^+ \rightarrow l^+ \nu}$	1.5%	1.5%	~1%
$ V_{cs} ^{D^0 \rightarrow K^+ e^+ \nu}$	2.5% (2.4% LQCD)	0.4%	0.15%
$ V_{cd} ^{D^+ \rightarrow \mu^+ \nu}$	0.9%	2.6%	~1%
$ V_{cd} ^{D^0 \rightarrow \pi^+ e^+ \nu}$	4.5% (4.4% LQCD)	1.3%	0.5%

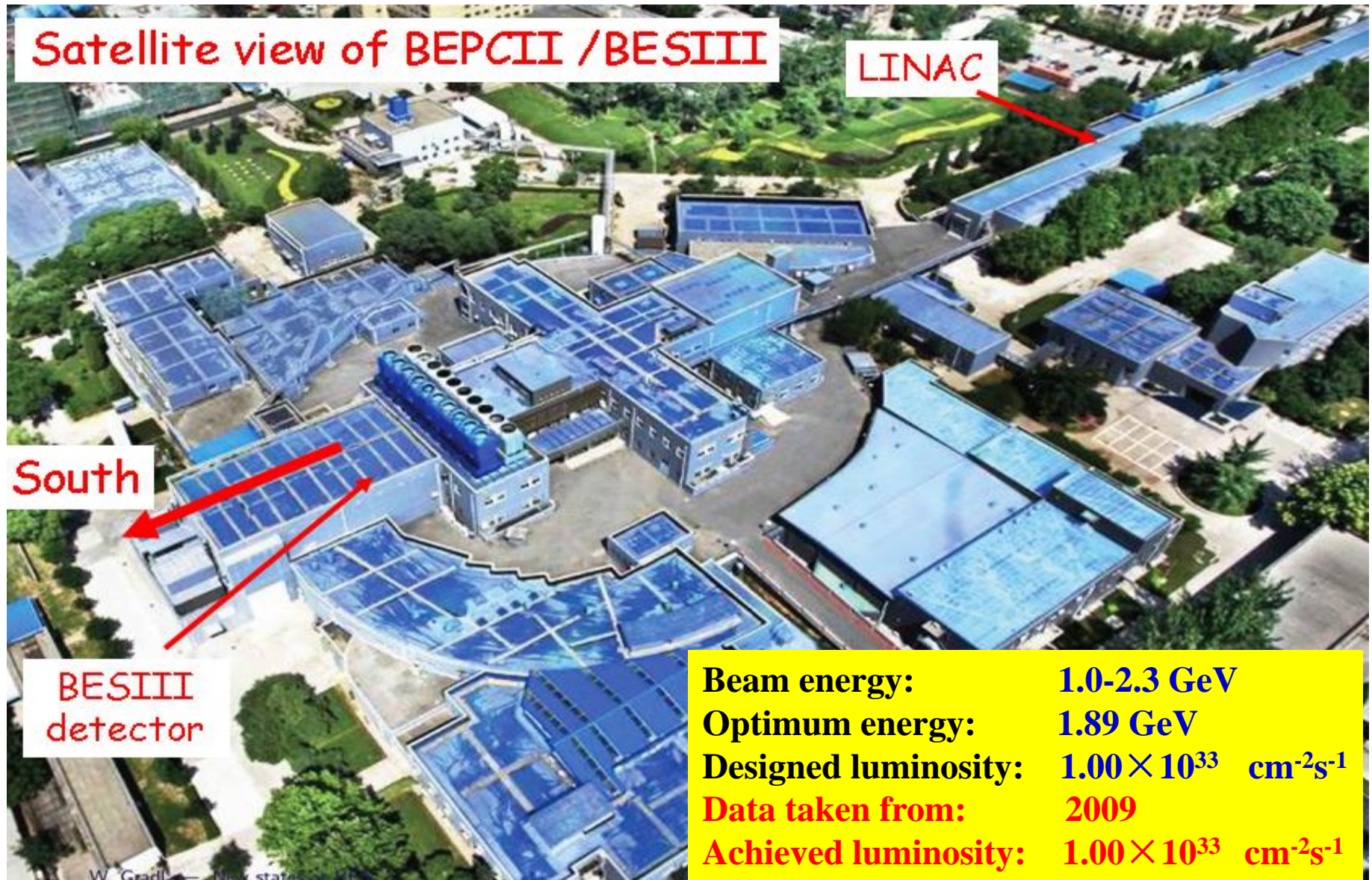
Only $D_s^+ \rightarrow \mu^+ \nu$ is considered. The contribution of $D_s^+ \rightarrow \tau^+ \nu$ will be comparable or slightly better than $D_s^+ \rightarrow \mu^+ \nu$

Once LQCD uncertainties reach <1% level, the $|V_{cs(d)}|$ will be much improved

- More or improved measurements of form factors of semileptonic decays, containing scalar or axial-vector meson, which are now statistically limited

Thank you!

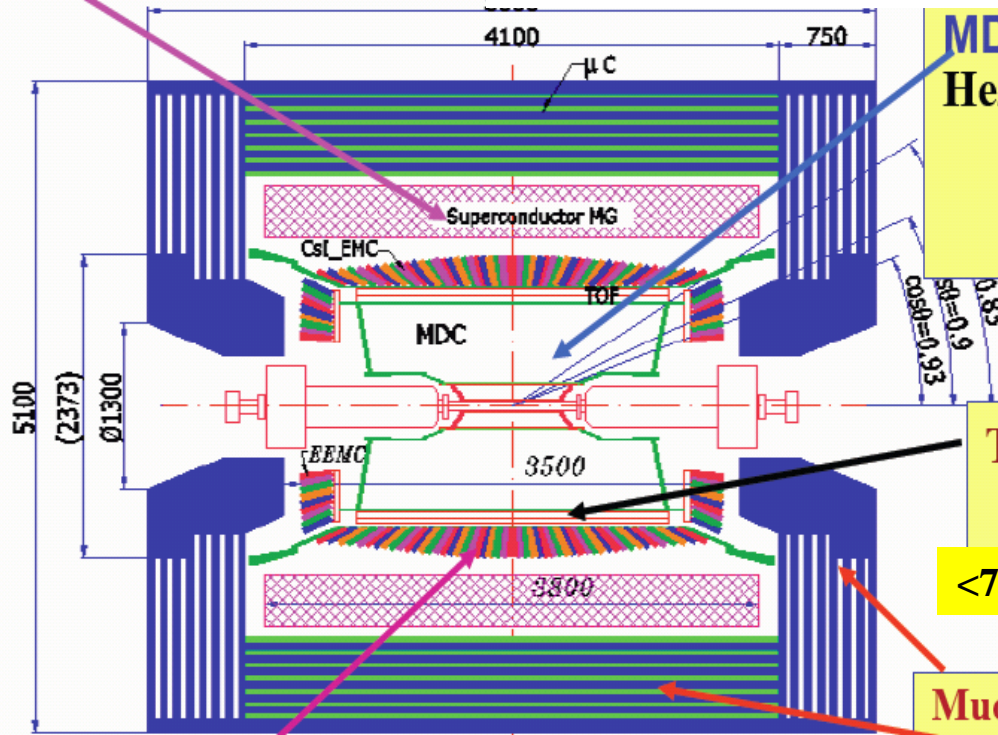
BEP CII collider



BESIII detector

Magnet: 1 T Super conducting

Nucl. Instr. Meth. A614, 345 (2010)



MDC: small cell & Gas:
He/C₃H₈ (60/40), 43 layers
 $\sigma_{xy} = 130 \mu\text{m}$
 $\sigma_p/p = 0.5\% @ 1\text{GeV}$
 $dE/dx = 6\%$

TOF:
 $\sigma_T = 100 \text{ ps}$ Barrel
<70 ps endcap updated in 2015

Muon ID: 9 layers RPC
8 layers for endcap

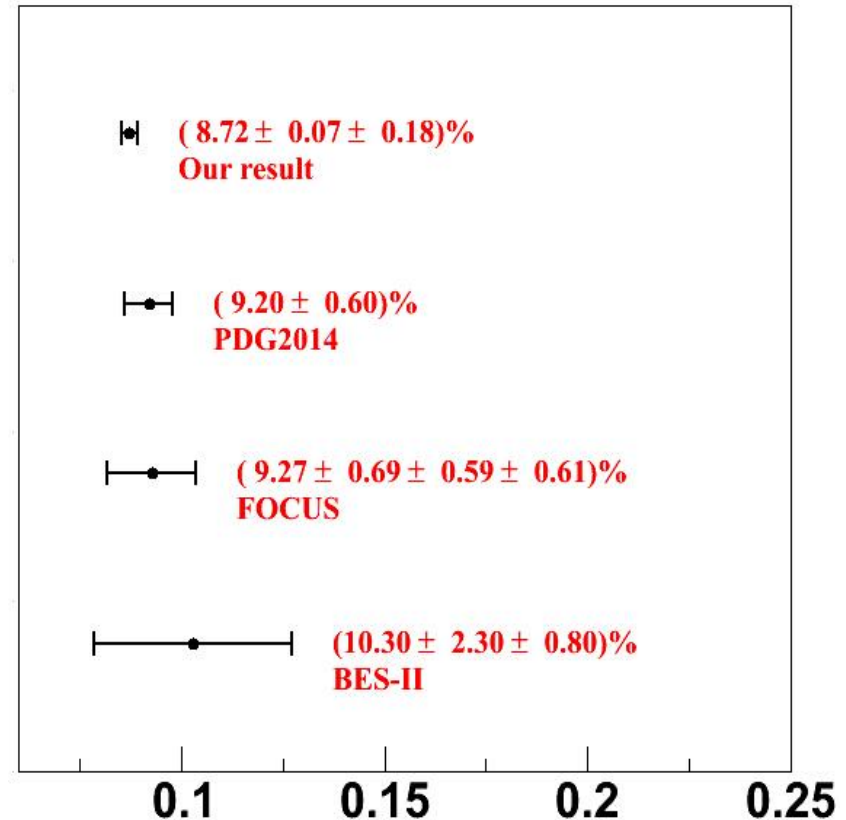
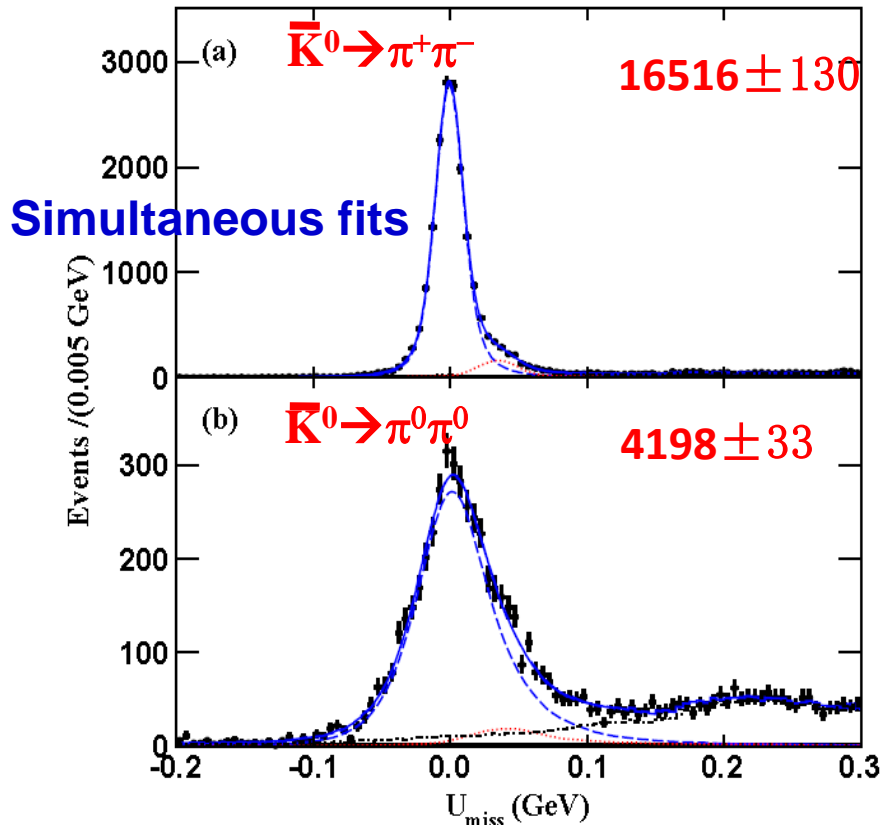
EMC: CsI crystal, 28 cm
 $\Delta E/E = 2.5\% @ 1 \text{ GeV}$
 $\sigma_z = 0.6 \text{ cm}/\sqrt{E}$

Data Acquisition:
Event rate = 4 kHz
Total data volume ~ 50 MB/s

Improved BF for $D^+ \rightarrow \bar{K}^0 \mu^+ \nu$

With 6 dominant D^- single tag

EPJC76(2016)369



Taking $B[D^0 \rightarrow K^- \mu^+ \nu]$
and $B[D^+ \rightarrow \bar{K}^0 e^+ \nu]$
from the PDG as input

$$\frac{\Gamma[D^0 \rightarrow K^- \mu^+ \nu]}{\Gamma[D^+ \rightarrow \bar{K}^0 \mu^+ \nu]} = 0.963 \pm 0.044$$

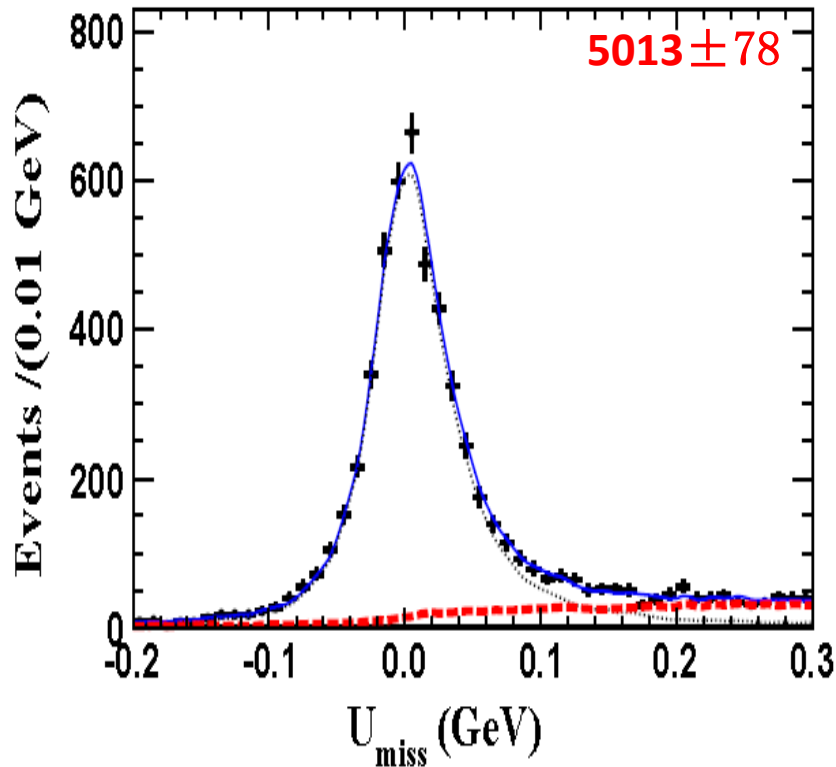
$$\frac{\Gamma[D^+ \rightarrow \bar{K}^0 \mu^+ \nu]}{\Gamma[D^+ \rightarrow \bar{K}^0 e^+ \nu]} = 0.988 \pm 0.033$$

Support isospin conservation in
these two decays within errors

Consistent with theory
prediction 0.97 within error

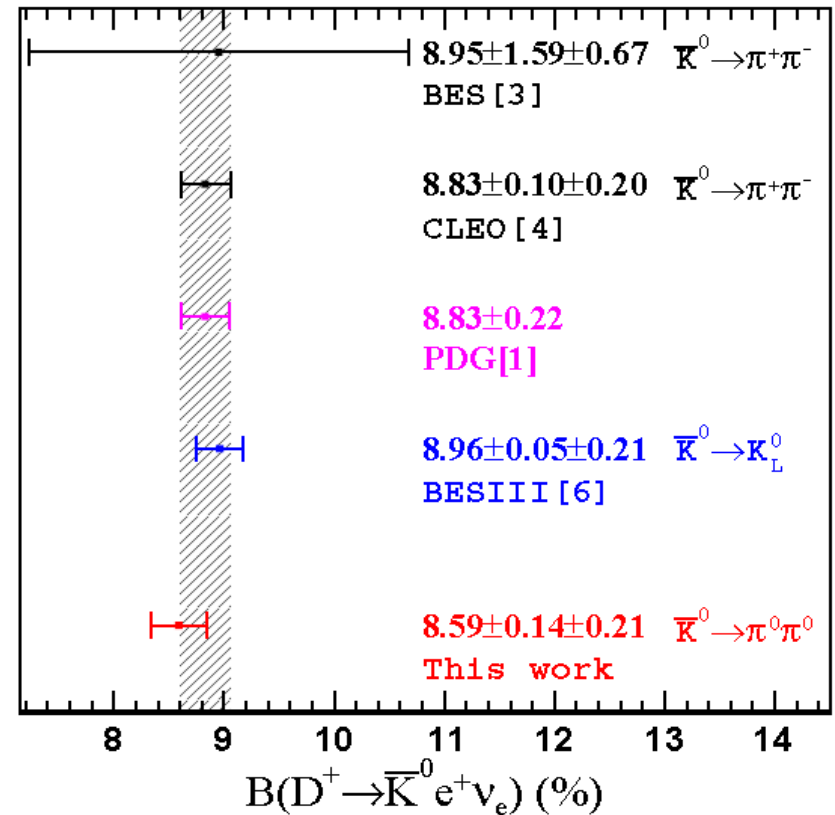
Absolute BF for $D^+ \rightarrow \bar{K}^0 e^+ \nu$ via $\bar{K}^0 \rightarrow \pi^0 \pi^0$

With 6 dominant D^- single tag



Taking τ_{D^+} , τ_{D^0} , $B[D^0 \rightarrow K^- e^+ \nu]$ and $B[D^+ \rightarrow \bar{K}^0 e^+ \nu]$ from the PDG as input

CPC40(2016)113001



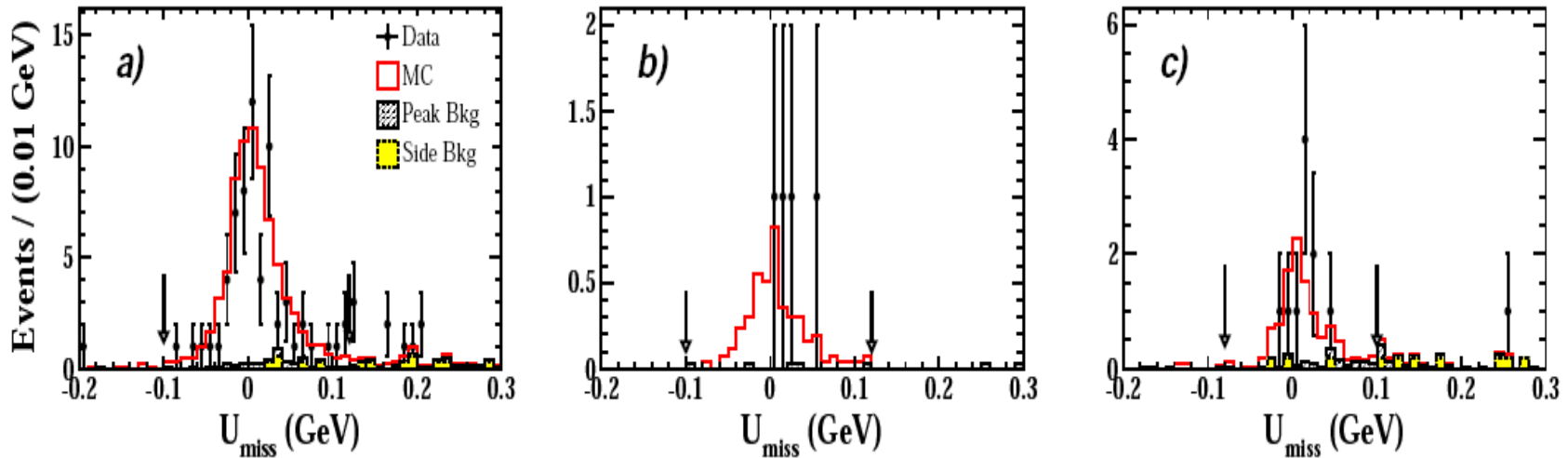
$$\frac{\Gamma[D^0 \rightarrow K^- e^+ \nu]}{\bar{\Gamma}[D^+ \rightarrow \bar{K}^0 e^+ \nu]} = 0.969 \pm 0.025$$

Agrees with isospin conservation within 1.2σ

Measurements of BFs of $D_s^+ \rightarrow \eta^{(\prime)} e^+ \nu$

- Benefit the understanding of the source of difference of inclusive decay rates of $D^{0(+)}$ and D_s^+
- Complementary information to understand η - η' mixing

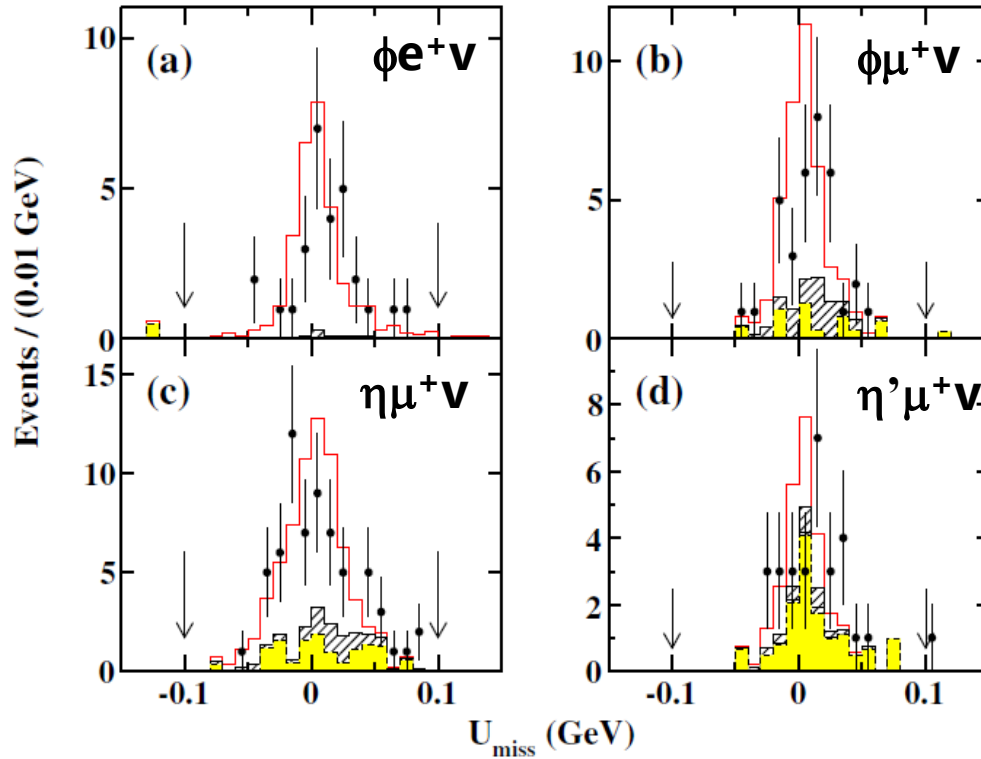
482 pb⁻¹ data@4.009 GeV, PRD94(2016)112003



	BESIII	CLEOII 95	CLEOc09	CLEOc15	PDG [4]
$B(D_s^+ \rightarrow \eta e^+ \nu_e)$ [%]	$2.30 \pm 0.31 \pm 0.08$	—	$2.48 \pm 0.29 \pm 0.13$	$2.28 \pm 0.14 \pm 0.20$	2.67 ± 0.29
$B(D_s^+ \rightarrow \eta' e^+ \nu_e)$ [%]	$0.93 \pm 0.30 \pm 0.05$	—	$0.91 \pm 0.33 \pm 0.05$	$0.68 \pm 0.15 \pm 0.06$	0.99 ± 0.23
$\frac{B(D_s^+ \rightarrow \eta' e^+ \nu_e)}{B(D_s^+ \rightarrow \eta e^+ \nu_e)}$	$0.40 \pm 0.14 \pm 0.02$	$0.35 \pm 0.09 \pm 0.07$	—	—	—

Measurements of BFs of $D_s^+ \rightarrow \phi/\eta^{(\prime)}\mu^+\nu$

482 pb⁻¹ data@4.009 GeV, PRD97(2018)012006



The ratios of BFs

$$\frac{\Gamma[D_s^+ \rightarrow \phi\mu^+\nu]}{\Gamma[D_s^+ \rightarrow \phi e^+\nu]} = 0.86 \pm 0.29$$

$$\frac{\Gamma[D_s^+ \rightarrow \eta\mu^+\nu]}{\Gamma[D_s^+ \rightarrow \eta e^+\nu]} = 1.05 \pm 0.24$$

$$\frac{\Gamma[D_s^+ \rightarrow \eta'\mu^+\nu]}{\Gamma[D_s^+ \rightarrow \eta' e^+\nu]} = 1.14 \pm 0.68$$

μ^+ mode	$\mathcal{B}_{\text{BESIII}} (\%)$	$\mathcal{B}_{\text{PDG}} (\%)$	e^+ mode	$\mathcal{B}_{\text{BESIII}} (\%)$	$\mathcal{B}_{\text{PDG}} (\%)$
$D_s^+ \rightarrow \phi\mu^+\nu_\mu$	$1.94 \pm 0.53 \pm 0.09$...	$D_s^+ \rightarrow \phi e^+\nu_e$	$2.26 \pm 0.45 \pm 0.09$	2.39 ± 0.23
$D_s^+ \rightarrow \eta\mu^+\nu_\mu$	$2.42 \pm 0.46 \pm 0.11$...	$D_s^+ \rightarrow \eta e^+\nu_e$	$2.30 \pm 0.31 \pm 0.08$ [8]	2.28 ± 0.24
$D_s^+ \rightarrow \eta'\mu^+\nu_\mu$	$1.06 \pm 0.54 \pm 0.07$...	$D_s^+ \rightarrow \eta' e^+\nu_e$	$0.93 \pm 0.30 \pm 0.05$ [8]	0.68 ± 0.16

BFs of semi-muonic decays are measured for the first time