

# Global and local $\Lambda$ polarization in heavy-ion collisions

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2018,06,22 at CHEP2018, Shanghai

# Contents

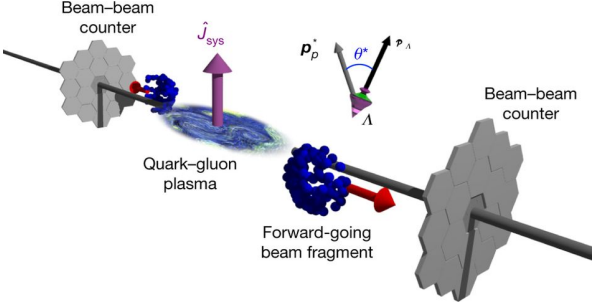
- ▶  $\Lambda$  global polarization
  - why global polarization **decreases** with **increasing**  $\sqrt{s_{NN}}$ .
  
- ▶  $\Lambda$  local polarization
  - rich information for **local vorticity** field.
  
- ▶ Summary

**Li, Pang, Wang, XLX, Phys. Rev. C 96, no. 5, 054908 (2017)**  
**XLX, Li, Tang, Wang, arXiv:1803.00867**

$\Lambda$  **global polarization**

# Brief history of $\Lambda$ global polarization

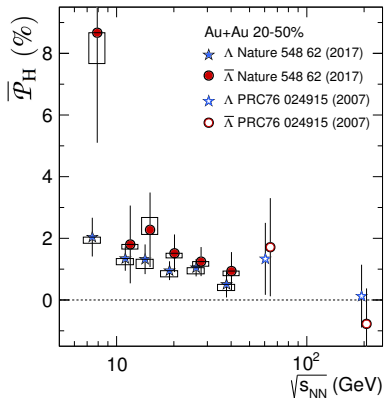
- ▶ Liang, Wang 2004, Voloshin 2004  
Orbital angular momentum in non-central collisions, spin-orbital coupling  $\Rightarrow$  **global polarization**.



**global polarization**: average effect of  $\omega$  field on hyper-surface (**net vorticity**)

# Brief history of $\Lambda$ global polarization

- ▶ Liang, Wang 2004, Voloshin 2004  
**global polarization** is proposed.
- ▶ STAR 2017



## $\Lambda$ polarization probes $\omega$ and $\mathbf{B}$

- ▶ Statistical-hydro model
  - Becattini et al 2008, 2013**
  - Fang, Pang, Wang, Wang 2016**
- ▶ For small fields

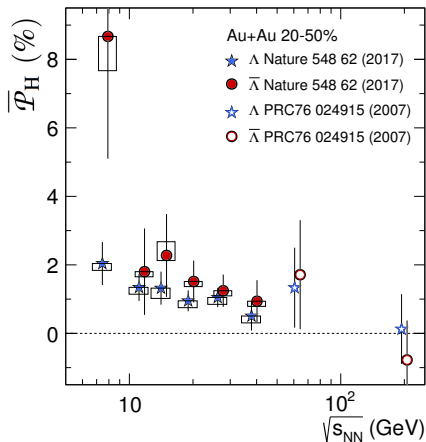
$$\mathbf{P}_\Lambda \simeq \frac{\omega}{2T} + \frac{\mu_\Lambda \mathbf{B}}{T}$$
$$\mathbf{P}_{\bar{\Lambda}} \simeq \frac{\omega}{2T} - \frac{\mu_\Lambda \mathbf{B}}{T}$$

**Becattini, Karpenko, Lisa, Upsal, Voloshin 2017**

- ▶ Important inputs for studies on effects of  $\omega$  and  $\mathbf{B}$ :
  - ▶ CME/CVE/CMW ...
  - ▶ effects on QCD phase diagram.
  - ▶ ...

I focus on  $\omega$ -induced  $\Lambda$  polarization in this talk.

# STAR result 2017



- ▶ **global polarization:**  
effect of **net vorticity**

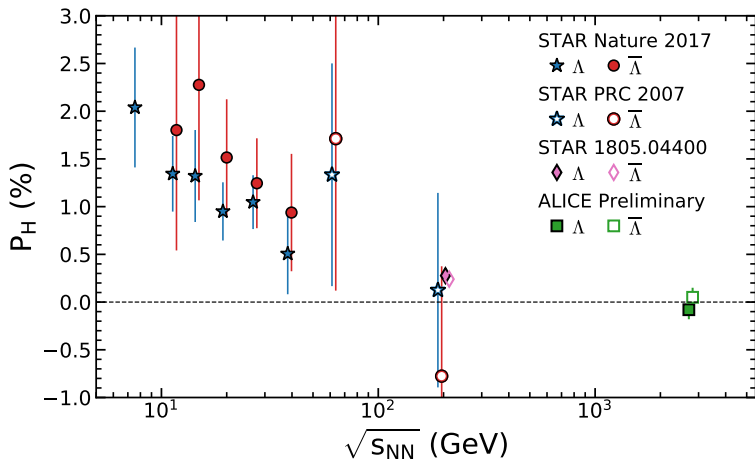
- ▶ the most vortical fluid:

$$\langle \omega_y \rangle \sim 0.01 \text{ fm}^{-1} \sim 10^{21} \text{ s}^{-1}$$

$$\mathbf{P}_\Lambda \simeq \frac{\boldsymbol{\omega}}{2T} + \frac{\mu_\Lambda \mathbf{B}}{T}$$

$$\mathbf{P}_{\bar{\Lambda}} \simeq \frac{\boldsymbol{\omega}}{2T} - \frac{\mu_\Lambda \mathbf{B}}{T}$$

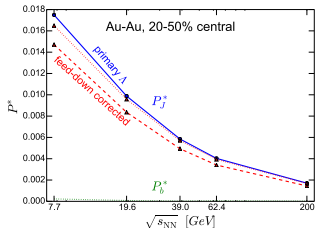
# $\Lambda$ global polarization vs $\sqrt{s_{NN}}$



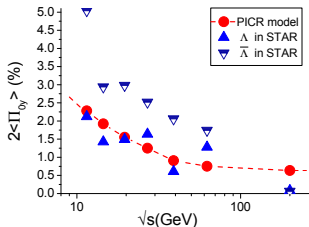
- ▶  $\Lambda$  global polarization **decreases** with **increasing**  $\sqrt{s_{NN}}$ .
- ▶ In contrast to total angular momentum vs  $\sqrt{s_{NN}}$ .



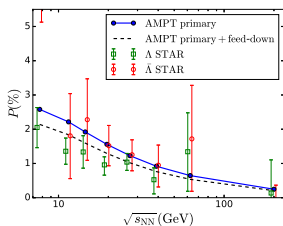
# $\Lambda$ global polarization in varied models



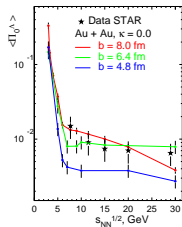
Karpenko, Becattini 2016



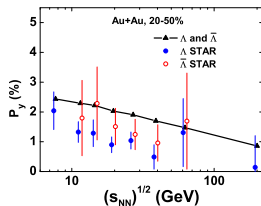
Xie, Wang, Csernai 2016



Li, Pang, Wang, Xia 2017

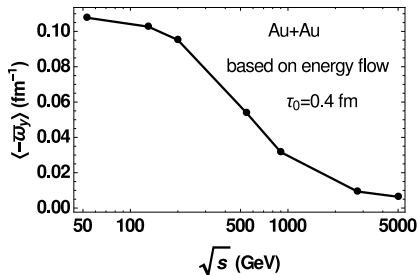


Baznat et al 2017

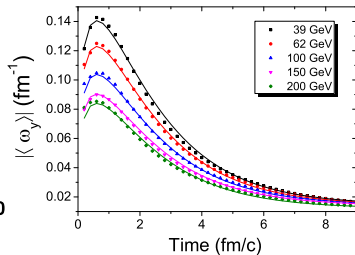


Sun, Ko 2017

# Consistent with $\langle \omega_y \rangle (\sqrt{s_{NN}})$



Deng, Huang 2016, HIJING

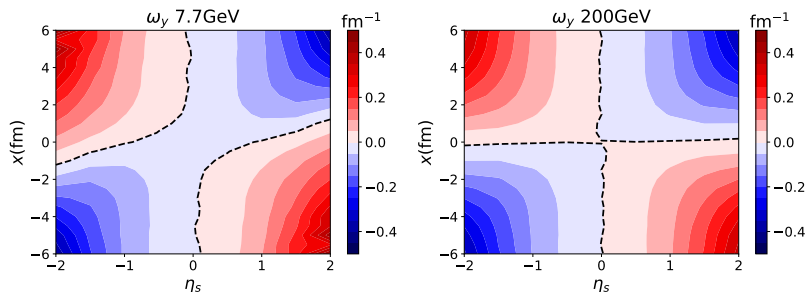


Jiang, Lin, Liao 2016, AMPT

- ▶  $\langle \omega_y \rangle$ : averaged vorticity, weighted by matter or energy density (**net vorticity**)
- ▶  $\langle \omega_y \rangle$  decreases with  $\sqrt{s_{NN}}$ .

# Vorticity distribution

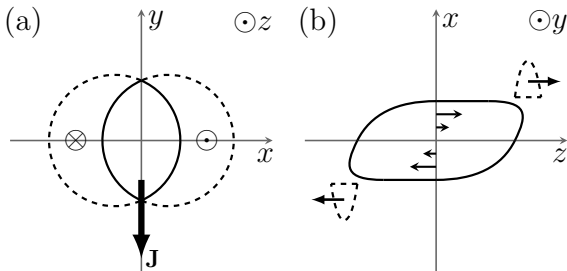
$\omega_y$  on  $zx$  plane at  $t = 5\text{fm}/c$  in 20-30% Au+Au collisions:



- ▶ **Net vorticity**  $\langle \omega_y \rangle$  is larger at lower  $\sqrt{s_{\text{NN}}}$ .
- ▶ Quadrupole pattern: **local vorticity** (see next section).

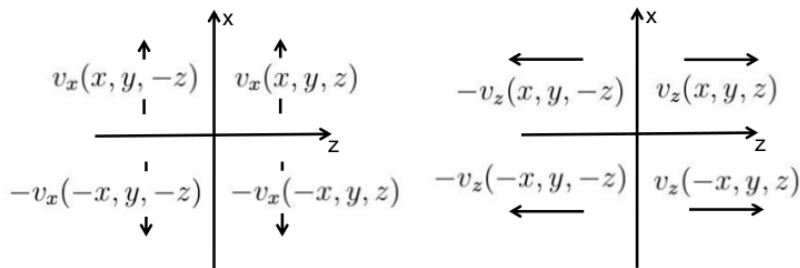
# How to understand?

- ▶ **Net vorticity** and **global polarization** are generated from the fireball's titled shape on the reaction plane.



## Central vs non-central collisions

- In central collisions, **net vorticity** vanishes due to the reflection symmetry  $x \rightarrow -x$  and  $z \rightarrow -z$ .



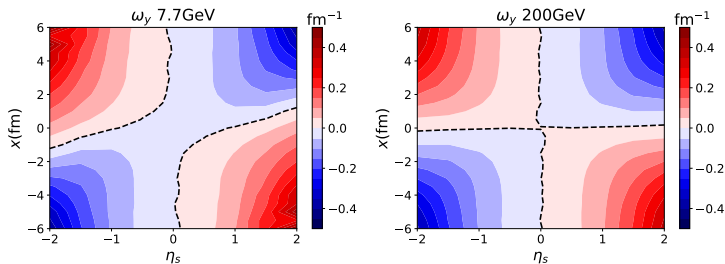
	$x \rightarrow -x$	$z \rightarrow -z$
$v_x$	odd	even
$v_z$	even	odd
$\omega_y$	odd	odd

$$\omega_y = \frac{1}{2}(\partial_z v_x - \partial_x v_z)$$

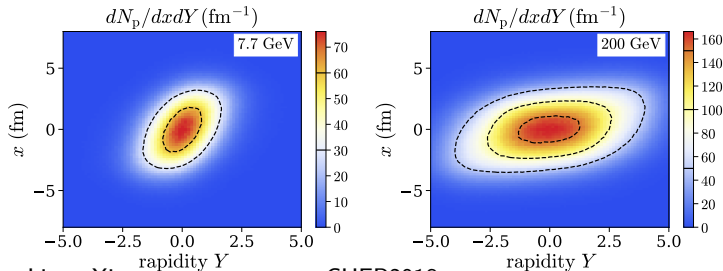
- In non-central collisions, the reflection symmetry breaks  $\langle \omega_y \rangle \neq 0$

# Vorticity and matter distribution

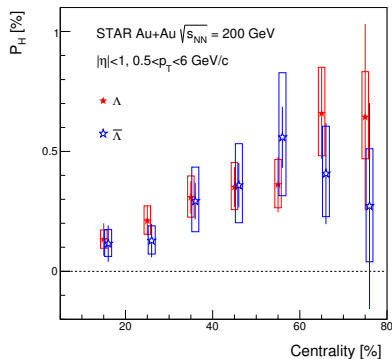
$\omega_y$  on  $zx$  plane at  $t = 5\text{fm}/c$  in 20-30% Au+Au collisions:



Initial parton distribution:



# $\Lambda$ global polarization vs centrality



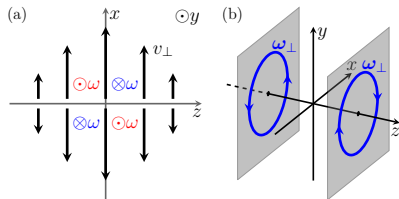
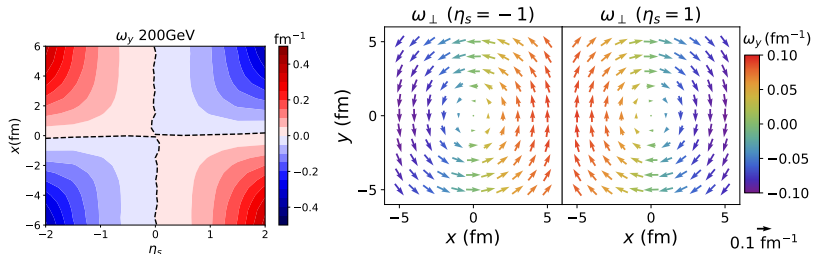
**STAR 1805.04400**

- ▶  $\Lambda$  global polarization increases with centrality,
- ▶ consistent to the tilted shape scenario.

**Local vorticity** and  $\Lambda$  **local polarization**



# Circular transverse vorticity $\omega_{\perp} = (\omega_x, \omega_y)$



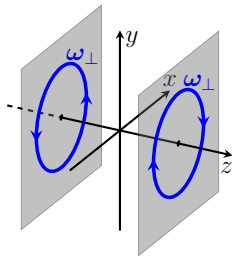
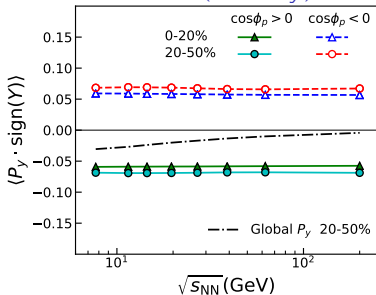
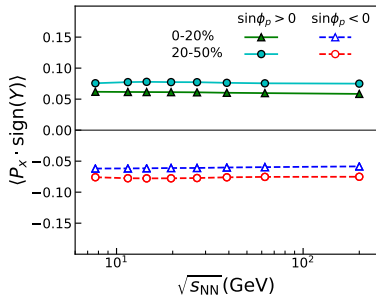
On  $xz$  plane: quadrupole  $\omega_y$   
 In 3D view: circular  $\omega_{\perp}$

$$\mathbf{v}_{\perp} = v_{\perp}(z)\mathbf{e}_r$$

$$\omega_{\perp} \equiv \frac{1}{2}(\nabla \times \mathbf{v})_{\perp} = \frac{1}{2}\partial_z v_{\perp}(z)\mathbf{e}_{\phi}$$

$$\partial v_{\perp} / \partial |z| < 0.$$

# Circular transverse polarization $\mathbf{P}_\perp = (P_x, P_y)$



$$\langle \mathbf{P}_\perp \cdot \text{sign}(Y) \rangle = \frac{\mathbf{P}_\perp(\phi_p, Y > 0) - \mathbf{P}_\perp(\phi_p, Y < 0)}{2}, \quad |Y| < 1$$

$\phi_p$ : azimuthal angle of  $\Lambda$ 's momentum.

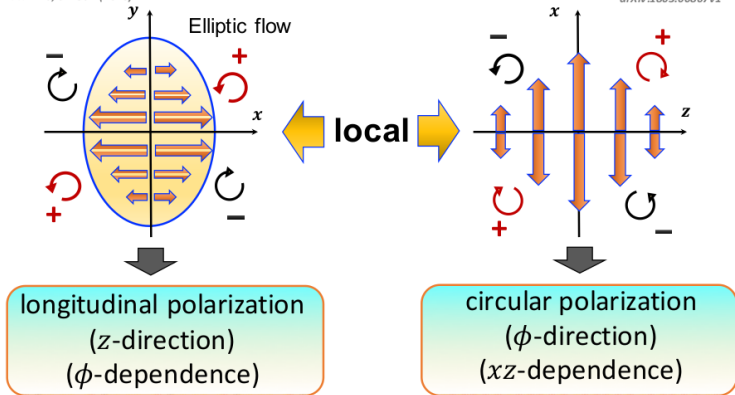
$Y$ :  $\Lambda$ 's rapidity.

- insensitive with  $\sqrt{s_{NN}}$ ,  
can be tested at 200 GeV and LHC energy.

# Local polarization

PRL 120, 012302 (2018)

arXiv:1803.00867v1

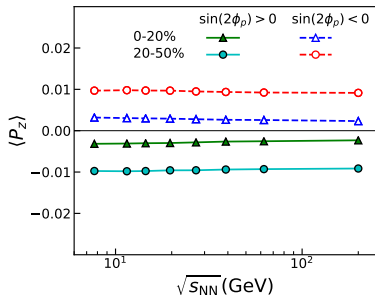


- ▶ quadrupole  $P_z$  from  $\partial_\phi v_\perp$   
Becattini, Karpenko 2017  
Voloshin 2017

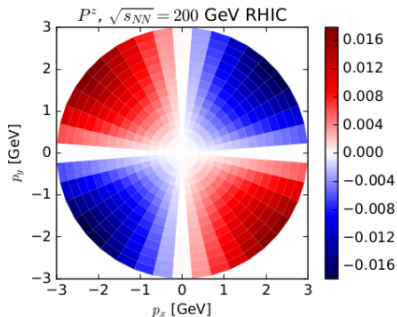
- ▶ circular  $\mathbf{P}_\perp$  from  $\partial_z v_\perp$   
XLX, Li, Tang, Wang 2018

above slide from Zhoudunming Tu's talk at QM2018

# Quadrupole pattern of $P_z$



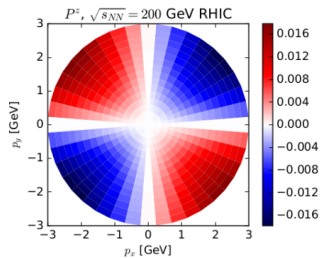
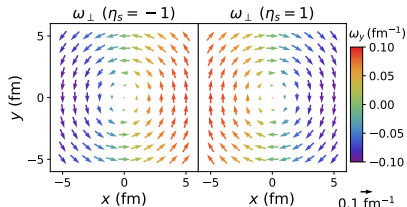
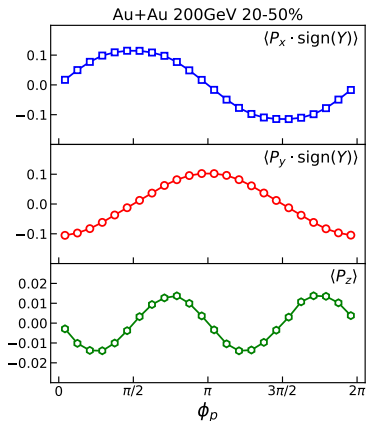
XLX, Li, Tang, Wang 2018  
AMPT



Becattini, Karpenko 2017  
hydro+UrQMD

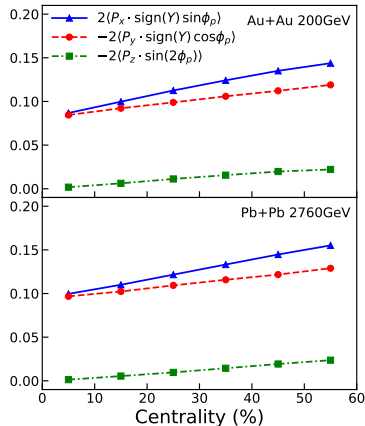
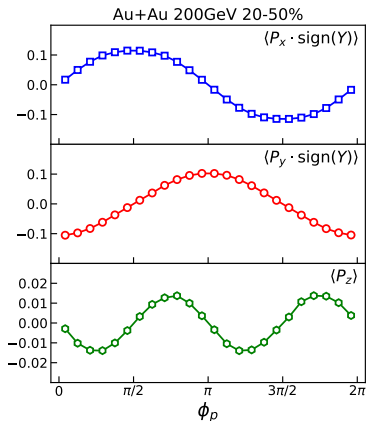
- ▶ consistent with Becattini and Karpenko's result.

# Local polarization, harmonic behaviors



- ▶  $(P_x, P_y) \cdot \text{sign}(Y) \sim -\mathbf{e}_{\phi} \sim (\sin \phi_p, -\cos \phi_p)$ ;
- ▶  $P_z \sim -\sin(2\phi_p)$

# Local polarization, Fourier coefficients



- ▶ Local polarization is sizable, c.f. global polarization  $< 0.003$  at 200 GeV and smaller at LHC energies.
- ▶  $P_z$  and  $|P_x - P_y|$  increases with centrality: elliptic flow.

# Summary

- ▶ The **net vorticity** and **global polarization** are from the fireball's *titled shape* on reaction plane.
  - ▶ Decreases with  $\sqrt{s_{NN}}$  in mid-rapidity;
  - ▶ Increases with centrality.
- ▶ **Local vorticity** and **local polarization**:
  - ▶ circular structure of  $\omega_{\perp}$  and  $\mathbf{P}_{\perp}$ , from  $\partial_z v_{\perp}$ .
  - ▶ quadrupole pattern of  $\omega_z$  and  $P_z$ , from  $\partial_{\phi} v_{\perp}$ .
- ▶ **Local polarization** is sizable at 200 GeV and LHC energies, can be tested.

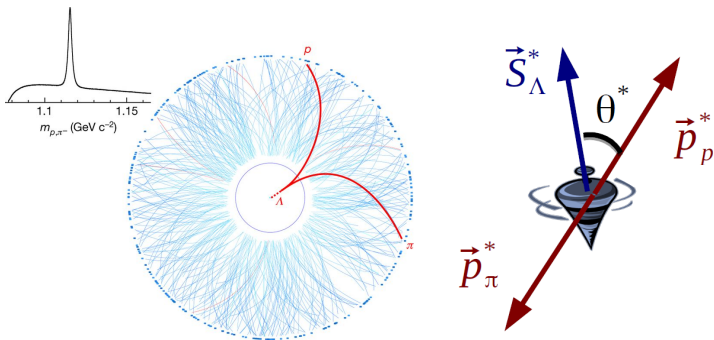
Thanks for listening

Backup



# How to measure $\Lambda$ polarization?

- ▶  $\Lambda$  is “self-analyzing”



Weak decay  $\Lambda \rightarrow p + \pi^-$

$$\frac{dN}{d\cos\theta^*} = \frac{1}{2}(1 + \alpha_H |\mathbf{P}_H| \cos\theta^*)$$

$$\alpha_\Lambda = -\alpha_{\bar{\Lambda}} = 0.642 \pm 0.013$$

## $\Lambda$ polarization induced by $\omega$ and $\mathbf{B}$

- ▶ Polarization from  $\omega$  and  $\mathbf{B}$

$$\rho \sim \exp\left(\frac{\omega \cdot \hat{\mathbf{S}} + \mathbf{B} \cdot \mu_{\Lambda} \hat{\mathbf{S}}/S}{T}\right)$$

$$\mathbf{P} \equiv \langle \mathbf{S} \rangle / S = \text{tr}(\rho \hat{\mathbf{S}}) / S$$

- ▶ For small fields

$$\mathbf{P}_{\Lambda} \simeq \frac{\omega}{2T} + \frac{\mu_{\Lambda} \mathbf{B}}{T}$$

$$\mathbf{P}_{\bar{\Lambda}} \simeq \frac{\omega}{2T} - \frac{\mu_{\Lambda} \mathbf{B}}{T}$$

$$\mu_{\Lambda} = -\mu_{\bar{\Lambda}} = -0.6138\mu_N$$

- ▶  $\omega$ -induced  $\Lambda/\bar{\Lambda}$  polarizations are along  $\omega$ ;
- ▶  $\mathbf{B}$ -induced  $\Lambda/\bar{\Lambda}$  polarizations are along  $\mp \mathbf{B}$ .

$$\omega = (\mathbf{P}_{\Lambda} + \mathbf{P}_{\bar{\Lambda}}) T$$

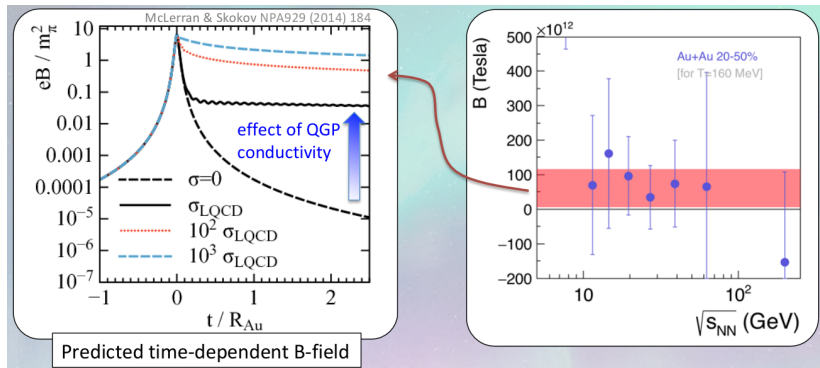
$$\mathbf{B} = (\mathbf{P}_{\Lambda} - \mathbf{P}_{\bar{\Lambda}}) T / (2\mu_{\Lambda})$$

$\Lambda/\bar{\Lambda}$  polarization can be used to probe  $\omega$  and  $\mathbf{B}$ .

Becattini, Karpenko, Lisa, Upsal, Voloshin 2017

# B-field from $\Lambda$ global polarization

$$\mathbf{B} = (\mathbf{P}_\Lambda - \mathbf{P}_{\bar{\Lambda}}) T / (2\mu_\Lambda)$$



above picture from Lisa's talk at Florence workshop, 2018

- Uncertainties on both experimental and theoretical sides.