

Transverse Momentum Balance and Angular Correlation of $b\bar{b}$ Dijets in Pb+Pb collisions

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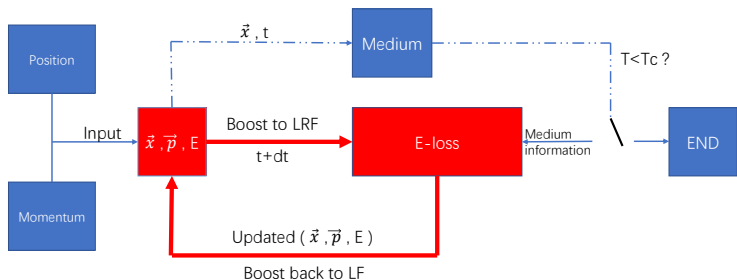
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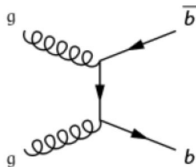
- Heavy flavours are effective and pure probes of the properties of the high energy-density Quark-Gluon Plasma(QGP) formed in the ultrarelativistic nucleus-nucleus collisions.
- The production suppression of heavy mesons in AA collision has been phenomenologically described by various models.
- The detailed mechanisms of heavy flavoured jets propagation and energy loss in dense QCD matter are not yet fully investigated.
- Recently, the transverse momentum balance and azimuthal angle correlations of $b\bar{b}$ dijet have been measured by the CMS and ATLAS collaborations at the LHC.

The Flow Diagram of Simulation

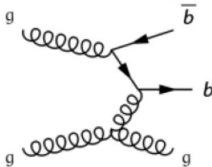


Bottom Production

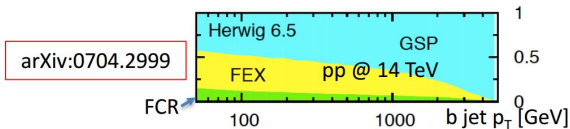
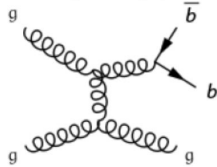
Flavor Creation ("FCR")



Flavor Excitation ("FEX")

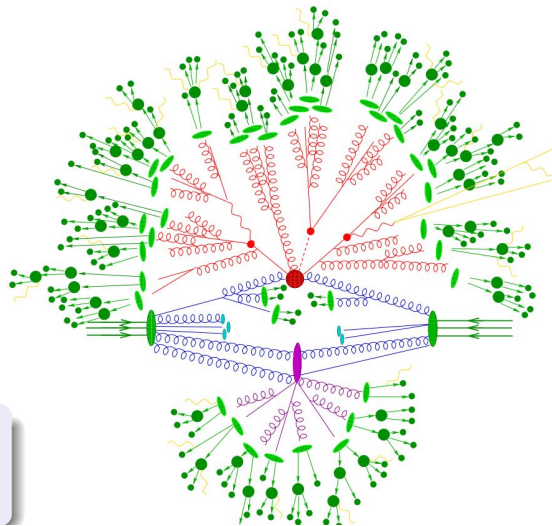


Gluon Splitting ("GSP")



- Herwig(NLO) predicts large contributions from all three production mechanisms in the measured p_T range.

- Initial state parton shower (QCD)
- Underlying event
- Signal process
- Final state parton shower (QCD)
- Fragmentation
- Hadron decays
- QED radiation

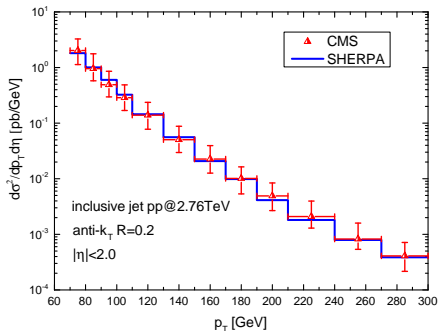


SHERPA is the framework steering these event phases.

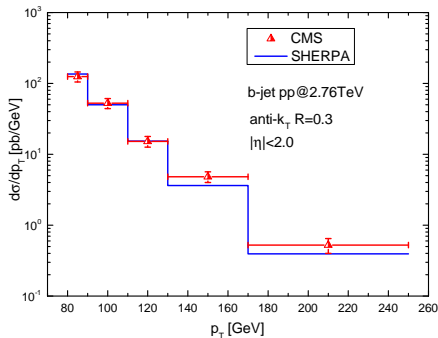
Events Generation and Selection

- The tree-level matrix elements of the cross section are calculated by Amegic[arXiv:0109036 [hep-ph]] and Comix[arXiv:0808.3674 [hep-ph]].
- The one-loop virtual corrections are calculated by BlackHat [Nucl.Phys.Proc.Suppl. 183 (2008) 313-319].
- NNPDF3.0 NNLO PDF[arXiv:1410.8849 [hep-ph]] is used in the calculation.
- Fastjet-3.3.0[Eur.Phys.J.C 72 (2012) 1896] is used for the jet reconstruction at parton level, no hadronization.
- The smooth iEBE-VISHNU hydro[Comput.Phys.Commun.199(2016) 61] has been used for the medium evolution.

The pp Baseline for Jet Production



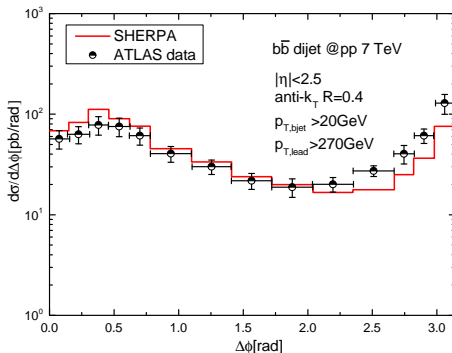
(a) inclusive jet



(b) b-jet

- Sherpa could provide a good description of the production of not only inclusive jet but also b-jet in pp collisions [[Phys.Rev.C 96 \(2017\) no.1, 015202](#); [Phys.Rev.Lett. 113 \(2014\) no.13, 132301](#)].

The pp Baseline for Angular Correlation



- Sherpa could also well describe the azimuthal angle correlation of $b\bar{b}$ dijet by comparing with ATLAS data [[Eur. Phys. J. C 76 \(2016\) no.12, 670](#)].

Collisional Energy Loss: Langevin Equation

- The discrete Langevin equation is used for description of heavy quark propagation in Quark-Gluon Plasma. [[Eur. Phys. J. C 71, 1666 \(2011\)](#); [Physical Review C, 2009, 79\(5\): 054907.](#)]:

$$\vec{x}(t + \Delta t) = \vec{x}(t) + \frac{\vec{p}(t)}{E} \Delta t \quad (1)$$

$$\vec{p}(t + \Delta t) = \vec{p}(t) - \Gamma(p) \vec{p} \Delta t + \vec{\xi}(t) \Delta t \quad (2)$$

the time step $\Delta t = 0.1\text{fm}$ in our simulation, the stochastic term $\vec{\xi}(t)$ obeys a Gaussian white noise distribution:

$$W[\vec{\xi}(t)] = N \exp\left[-\frac{\vec{\xi}(t)^2}{2\kappa}\right] \quad (3)$$

$$\langle \xi_i(t) \rangle = 0 \quad (4)$$

$$\langle \xi_i(t) \xi_j(t') \rangle = \kappa \delta_{ij} (t - t') \quad (5)$$

- The relationship between drag coefficient Γ and the stochastic term $\vec{\xi}(t)$ are determined by Fluctuation-Dissipation Theorem (Einstein Relation): [Kubo R. Reports on progress in physics, 1966, 29(1): 255.]

$$\Gamma = \frac{\kappa}{2ET} \quad (6)$$

where

$$\kappa = \frac{2T^2}{D_s} \quad (7)$$

- The spacial diffusion coefficient D_s is fixed by Lattice calculation as $2\pi TD_s = 3.7 \sim 7.0$ [Phys.Rev.D 92 no.11,(2015) 116003,arXiv:1508.04543 [hep-lat]]

Radiative Energy Loss: Higher-Twist Scheme

- The Higher-Twist calculation for the medium-induced radiative gluon spectra [X.-F. Guo and X.-N. Wang, Phys. Rev. Lett. 85, 3591(2000); B.-W. Zhang, E. Wang, and X.-N. Wang, Phys. Rev. Lett. 93, 072301 (2004); A. Majumder, Phys. Rev. D85, 014023 (2012).]

$$\frac{dN_g}{dx dk_{\perp}^2 dt} = \frac{2\alpha_s C_A P(x) \hat{q}}{\pi k_{\perp}^4} \sin^2\left(\frac{t-t_i}{2\tau_f}\right) \left(\frac{k_{\perp}^2}{k_{\perp}^2 + x^2 M^2}\right)^4 \quad (8)$$

where x is the gluon energy fraction to heavy quark energy, k_{\perp} is the transverse momentum of gluon related to heavy quark, M is mass of heavy quark ($M_c = 1.5 \text{ GeV}$, $M_b = 4.75 \text{ GeV}$), $\alpha_s = 0.3$.

- where $P(x)$ is splitting function [W.-T. Deng and X.-N. Wang, Phys. Rev. C81, 024902 (2010).],

$$P_{Q \rightarrow Qg}(x) = \frac{(1 + (1 - x)^2)(1 - x)}{x} \quad (9)$$

- \hat{q} is QGP transport coefficient [X.F.Chen, C.Greiner, E.Wang, X.N.Wang and Z.Xu, Phys.Rev.C 81(2010)064908]:

$$\hat{q}(\tau, r) = q_0 \frac{\rho^{QGP}(\tau, r)}{\rho^{QGP}(\tau_0, 0)} \frac{p^\mu u_\mu}{p^0} \quad (10)$$

- τ_f is gluon formation time :

$$\tau_f = \frac{2Ex(1-x)}{k_\perp^2 + x^2 M^2} \quad (11)$$

- $t - t_i$ is the interval between t to last radiation time t_i .

Higher-Twist for Light Partons

- The Higher-Twist calculation for massless parton:

$$\frac{dN_g}{dx dk_{\perp}^2 dt} = \frac{2\alpha_s C_i P_i(x) \hat{q}}{\pi k_{\perp}^4} \sin^2\left(\frac{t - t_i}{2\tau_f}\right) \quad (12)$$

- The splitting function for quark and gluon [[W.-T. Deng and X.-N. Wang, Phys. Rev. C81, 024902 \(2010\).](#)]:

$$P_{q \rightarrow qg}(x) = \frac{(1 + (1 - x)^2)(1 - x)}{x} \quad (13)$$

$$P_{g \rightarrow gg}(x) = \frac{2(1 - x + x^2)^3}{x(1 - x)} \quad (14)$$

- Low cut-off of gluon energy: $\omega_0 = xE = m_D = gT\sqrt{1 + n_f/6}$

Gluon Sampling Method

- The average number of radiative gluon during a time step [Phys.Rev. C94 (2016) no.1, 014909]:

$$\langle N_g(t, \Delta t) \rangle = \Delta t \int dx dk_{\perp}^2 \frac{dN_g}{dx dk_{\perp}^2 dt} \quad (15)$$

- Assuming that the number of radiative gluon n obeys the Poisson distribution $P(n) = \frac{\langle N_g \rangle^n}{n!} e^{-\langle N_g \rangle}$, the total probability for radiation during a time step Δt :

$$P_{rad}(t, \Delta t) = 1 - e^{-\langle N_g \rangle} \quad (16)$$

- Then it's available to sample the energy xE and transverse momentum k_{\perp} of the radiative gluons during every time step for arbitrary state (E, T, t) .
- The interval $t - t_i$ would be reset when a radiation occurred.

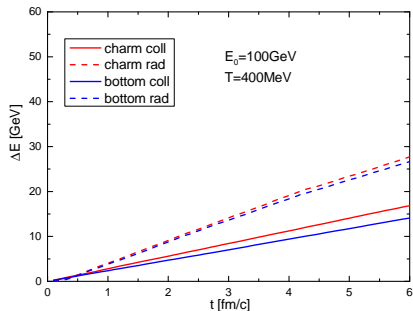
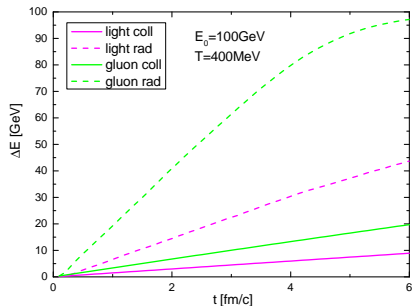
HTL Collisional Energy Loss

Hard Thermal Loop calculation is considered as collisional energy loss of light partons. [J.D. Bjorken, Fermilab preprint PUB-82/59-THY; Markus H.Thoma Physics Letters B 273 (1991)128-132; R.B.Neufeld PRD 83(2011)065012]

$$\frac{dE}{dt} = \frac{\alpha_s C_i m_D^2}{2} \ln \frac{\sqrt{ET}}{m_D} \quad (17)$$

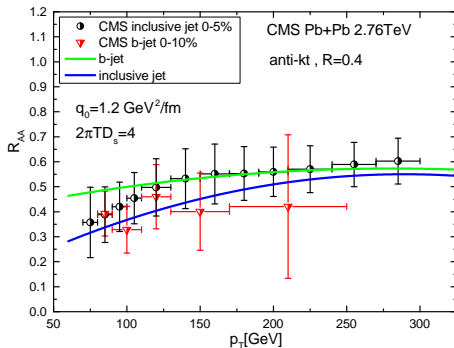
- The Debye screening mass: $m_D^2 = 4\pi\alpha_s T^2(1 + \frac{n_f}{6})$
- The color factor: $C_g = N_c, C_q = \frac{N_c^2 - 1}{2N_c}$

Parton Energy Loss



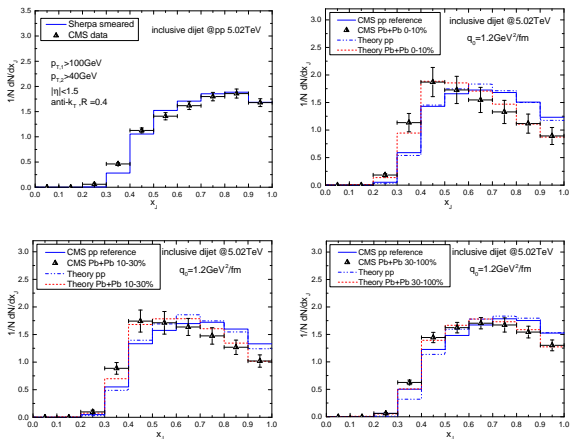
- Radiative energy loss: $\Delta E_g > \Delta E_q > \Delta E_c > \Delta E_b$.
- Collisional energy loss is comparable to radiative energy loss for heavy quarks.

R_{AA} for Inclusive Jet and Inclusive b-jet



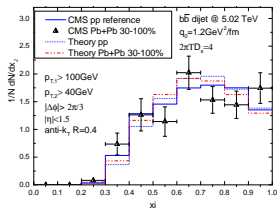
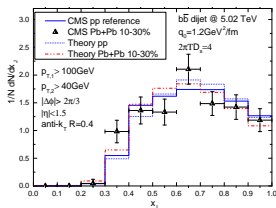
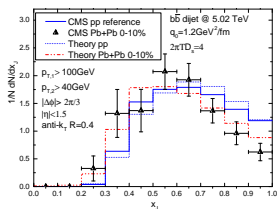
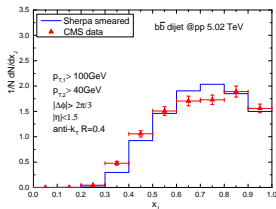
- Establish a framework to describe heavy quark evolution and jet quenching simultaneously [Phys. Rev.C 96 (2017) no.1, 015202; Nucl.Phys.A 932 (2014) 253; arXiv:1806.06332].
- At lower p_T region, the heavy quark suffers less energy loss.
- The mass effect of the jet quenching tends to disappear at higher p_T .

Transverse Momentum Balance of Inclusive Dijet



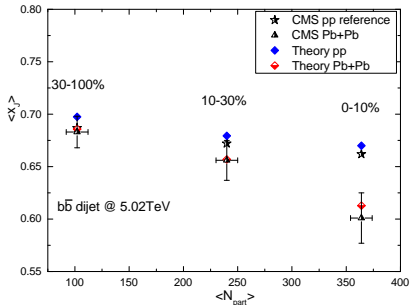
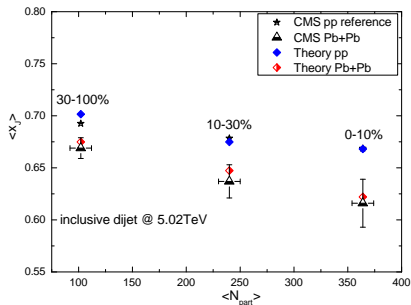
- The x_J shifted to smaller x_J with centrality dependence, the enhancement at the smaller x_J and suppression at larger x_J are observed, where $x_J = \frac{p_{T,2}}{p_{T,1}} [\text{JHEP 1803 (2018) 181; arXiv:1806.06332}]$.

Transverse Momentum Balance of $b\bar{b}$ Dijet



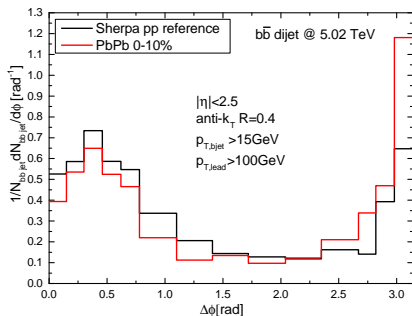
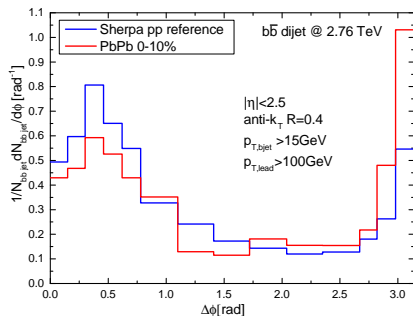
- Similar behaviors are observed in transverse momentum balance of $b\bar{b}$ dijet, where $x_J = \frac{p_{T,b2}}{p_{T,b1}}$ [JHEP 1803 (2018) 181; arXiv:1806.06332].
- Large error bar exits in the experimental data.

$\langle x_J \rangle$ for inclusive dijet and $b\bar{b}$ dijet



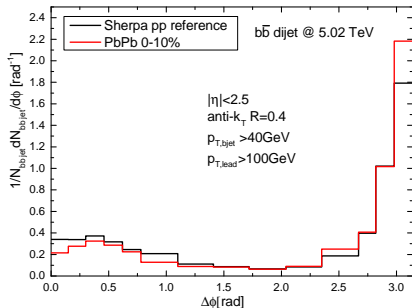
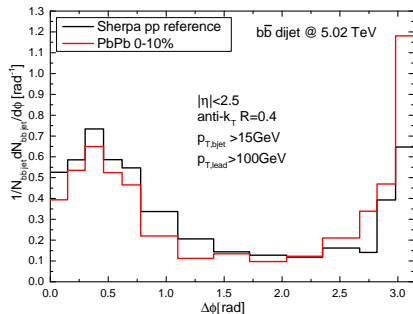
- The imbalance increases with the increasing centrality for inclusive dijet and $b\bar{b}$ dijet.
- The averaged x_J value shift due to the jet quenching effect is much visible in central collision.

The Predictions for Angular Correlations of $b\bar{b}$ Dijet in Pb+Pb Collision



- The two peaks in azimuthal angle distribution are from GSP and FCR.
- The angular correlation of $b\bar{b}$ dijet would be modified by the hot and dense medium.
- The peak on near side suffered more suppression than on away side.

The Predictions for Angular Correlations of $b\bar{b}$ Dijet in Pb+Pb Collision



- The peak on near side disappears when a higher cut $p_{T,bjet} > 40\text{ GeV}$ used for jet reconstruction.
- Suppression on near side is still observed even with low p_T cut.

- The MC framework combines the Langevin transport model to describe the evolution of bottom quark also its collisional energy loss and the higher-twist description to consider the radiative energy loss of both bottom and light quarks.
- We compare the theoretical simulation of inclusive jet and inclusive b -jet R_{AA} in Pb+Pb collisions at 2.76 TeV with the experimental data.
- We also present the theoretical simulation of the momentum balance of the $b\bar{b}$ dijet in Pb+Pb collisions at 5.02 TeV with the recent CMS data for the first time.
- The prediction of the normalized azimuthal angle distribution of the $b\bar{b}$ dijet in Pb+Pb collisions at 5.02 TeV has been reported.

Backup 1

- The initial space information of partons is produced by Glauber binary distribution. The Woods-Saxon form of the nucleon density:
[arXiv:nucl-ex/0701025; ATOMIC DATA AND NUCLEAR DATA TABLES 36,495536 (1987)].

$$\rho(r) = \rho_0 \cdot \frac{1 + \omega(r/R_0)^2}{1 + \exp[\frac{r-R_0}{a}]} \quad (1)$$

And the probability density is available based on:

$$f(\vec{s}) = N \cdot \hat{T}_A(\vec{s} + \frac{\vec{b}}{2}) \hat{T}_B(\vec{s} - \frac{\vec{b}}{2}) \quad (2)$$

where the thickness function:

$$\hat{T}(\vec{s}) = \int \rho(\vec{r}) dz \quad (3)$$

The jet p_T resolution is parametrized according the following form[[arXiv:1607.03663](https://arxiv.org/abs/1607.03663)]:

$$\sigma(p_T)/p_T = \sqrt{C^2 + \frac{S^2}{p_T} + \frac{N^2}{p_T^2}} \quad (4)$$

- In pp collisions, the constant C and stochastic S terms are 0.06 and 0.8 GeV^{-1}
- In Pb+Pb collisions the S term is slightly larger value of 1.0 GeV^{-1} , due to the underlying event.
- The noise parameter (N) depends on collision centrality, according to $N = 14.82 - \text{centrality}(\%)/5.40(\text{GeV}^2)$ subtraction.