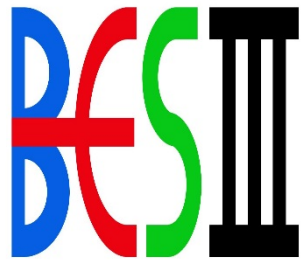


Light Meson Decays at BESIII



Shuangli Yang

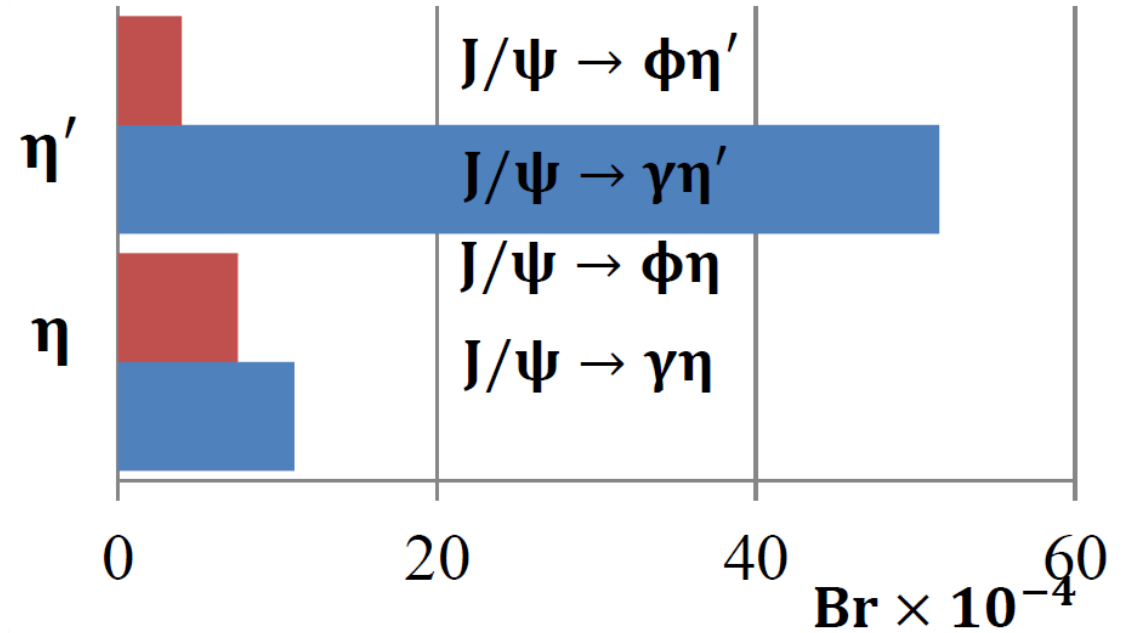
(On behalf of BESIII collaboration)

Jun 20, 2018 / Shanghai



- ◆ Introduction
- ◆ Recent results on light meson decays
 - η/η' decays
 - $a_0 - f_0$ mixing
- ◆ Summary

η/η' from J/ψ decays



- BESIII: τ –charm factory
- High production rate of light mesons in J/ψ decays
- Also a factory for light mesons ($\eta/\eta'/\omega \dots$)
- η/η' from J/ψ radiative decays
 - $7.2 \times 10^6 \eta'$
 - $2.4 \times 10^6 \eta$

η/η' : a rich physics field

η	η'
$M = 584 \text{ MeV}, \Gamma = 1.3 \text{ keV}$	$M = 958 \text{ MeV}, \Gamma = 197 \text{ keV}$
Hadronic Decays	
$\eta \rightarrow \pi^0 \pi^0 \pi^0$ 32.6%	$\eta' \rightarrow \pi^+ \pi^- \eta$ 42.9%
$\eta \rightarrow \pi^+ \pi^- \pi^0$ 22.9%	$\eta' \rightarrow \pi^0 \pi^0 \eta$ 22.2%
Radiative Decays	
$\eta \rightarrow \gamma \gamma$ 39.4%	$\eta' \rightarrow \rho^0 \gamma$ 29.1%
$\eta \rightarrow \pi^+ \pi^- \gamma$ 4.2%	$\eta' \rightarrow \omega \gamma$ 2.7%
	$\eta' \rightarrow \gamma \gamma$ 2.2%
99.1%	99.1%

➤ text predictions by ChPT

➤ transition form factors

➤ text fundamental symmetries

➤ probe physics beyond the SM

◆ Hadronic decays

➤ $\eta' \rightarrow \pi^+ \pi^- \pi^0, \pi^0 \pi^0 \pi^0$

➤ $\eta' \rightarrow \pi^+ \pi^- \eta, \pi^0 \pi^0 \eta$

◆ Radiative decays

➤ $\eta' \rightarrow \gamma \gamma \pi^0$

➤ $\eta' \rightarrow \gamma \pi^+ \pi^-$

➤ $\eta' \rightarrow 3\pi$ are isospin-violating processes due to the $d - u$ quark mass difference

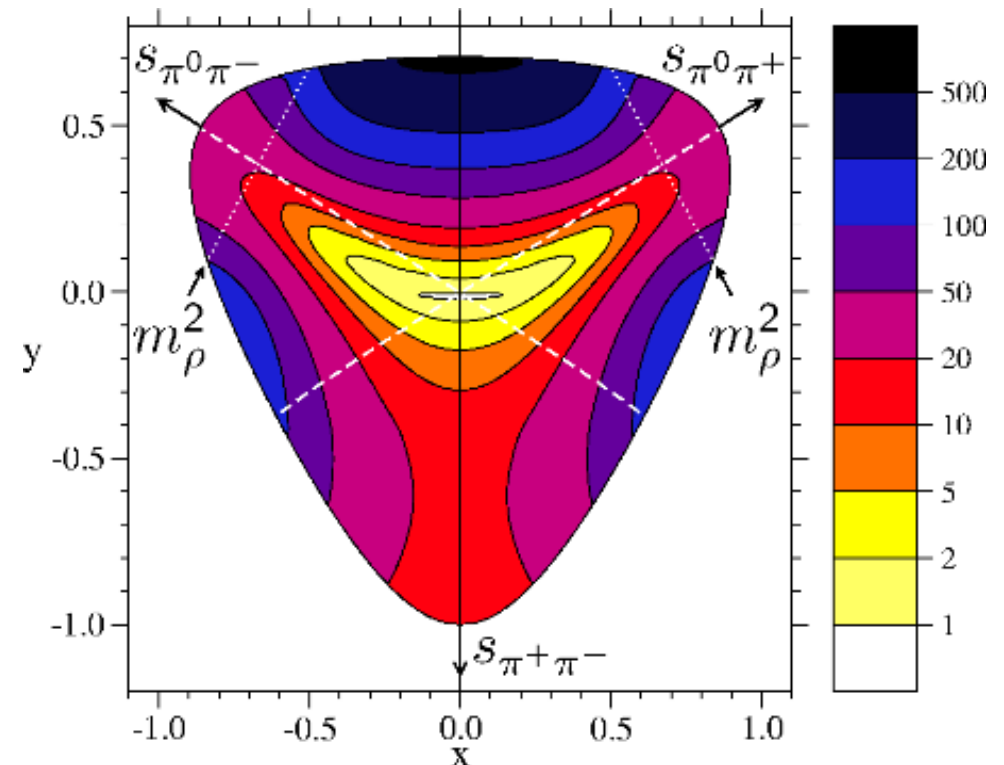
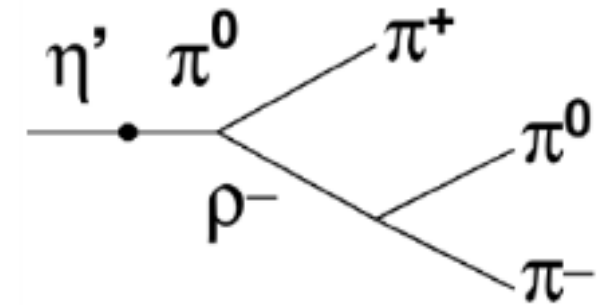
➤ light quark mass ratio $(m_d - m_u)/m_s$ can be extracted by the ratio of decay widths:

$$r = \frac{\Gamma_{\eta' \rightarrow \pi^+ \pi^- \pi^0}}{\Gamma_{\eta' \rightarrow \eta \pi^+ \pi^-}} \approx (16.8) \frac{3}{16} \left(\frac{m_d - m_u}{m_s} \right)^2$$

D. Gross et al., Phys. Rev. D. 19, 2188 (1979)

➤ Using ChPT, large P-wave contribution of $\eta' \rightarrow \rho^\pm \pi^\mp$ is predicted in $\eta' \rightarrow \pi^+ \pi^- \pi^0$ [[Eur. Phys. J. A 26, 383\(2005\)](#)]

➤ So far, no direct experimental evidence of $\eta' \rightarrow \rho^\pm \pi^\mp$ in $\eta' \rightarrow \pi^+ \pi^- \pi^0$



Amplitude analysis of the decays $\eta' \rightarrow 3\pi$

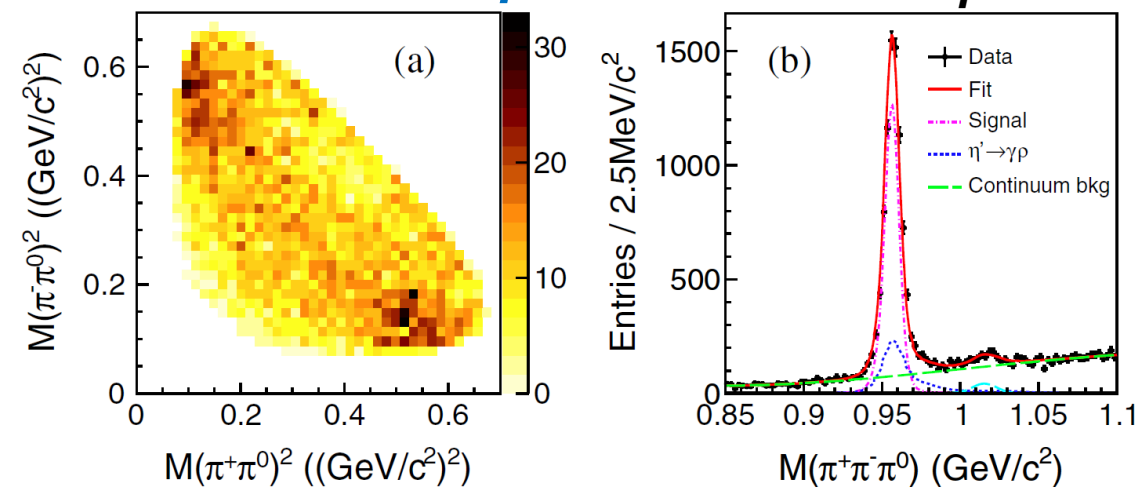
- Based on 1310M J/ψ data, η' from $J/\psi \rightarrow \gamma\eta'$
- Two clusters of events corresponding to $\eta' \rightarrow \rho^\pm\pi^\mp$ are observed
- The decay $\eta' \rightarrow \gamma\rho$ and $\eta' \rightarrow \pi^0\pi^0\eta$ result in the peaking background

$$\mathcal{B}(\eta' \rightarrow \pi^+\pi^-\pi^0) = (35.91 \pm 0.54 \pm 1.74) \times 10^{-4}$$

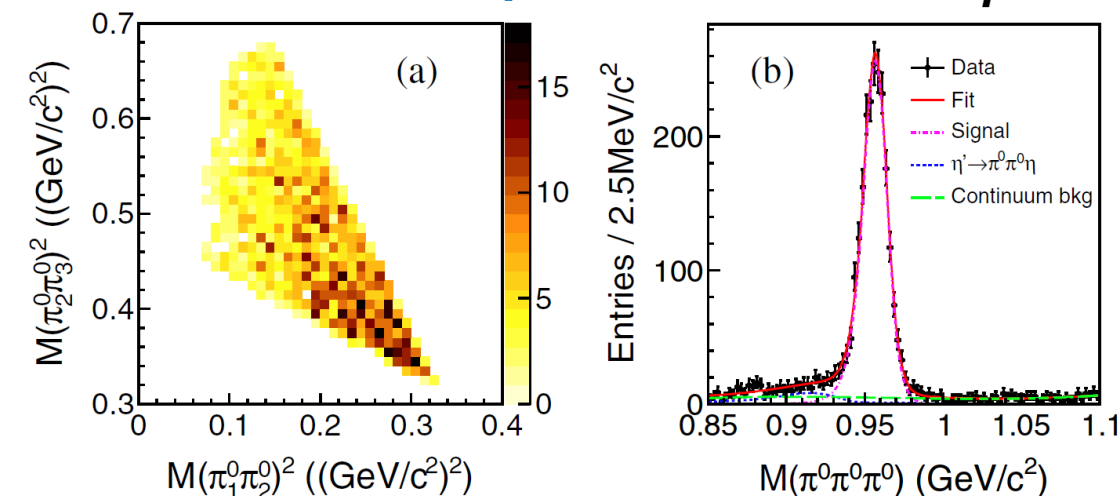
$$\mathcal{B}(\eta' \rightarrow \pi^0\pi^0\pi^0) = (35.22 \pm 0.82 \pm 2.54) \times 10^{-4}$$

- The branching fractions of $\eta' \rightarrow \pi^+\pi^-\pi^0$ and $\eta' \rightarrow \pi^0\pi^0\pi^0$ are in good agreement with previous BESIII results ([Phys. Rev. Lett. 108, 182001 \(2012\)](#))

$\eta' \rightarrow \pi^+\pi^-\pi^0$ 8267 η' events

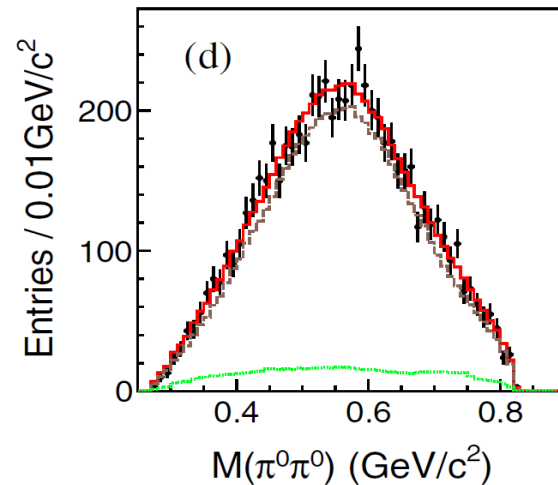
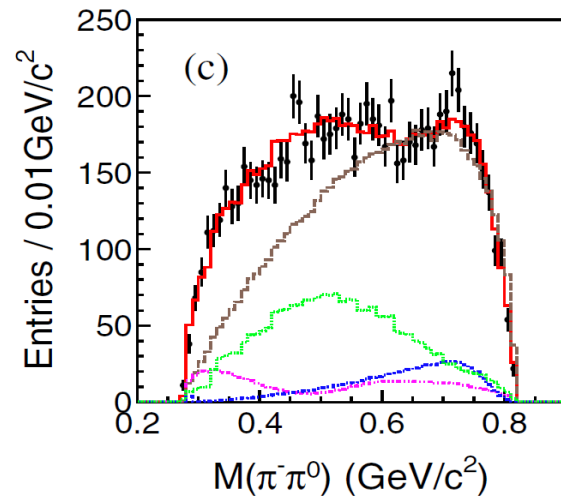
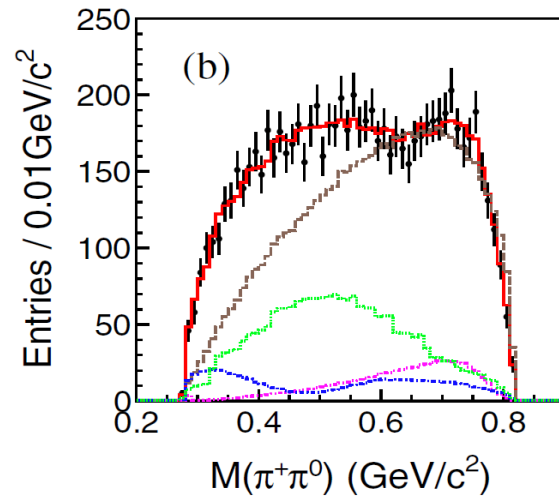
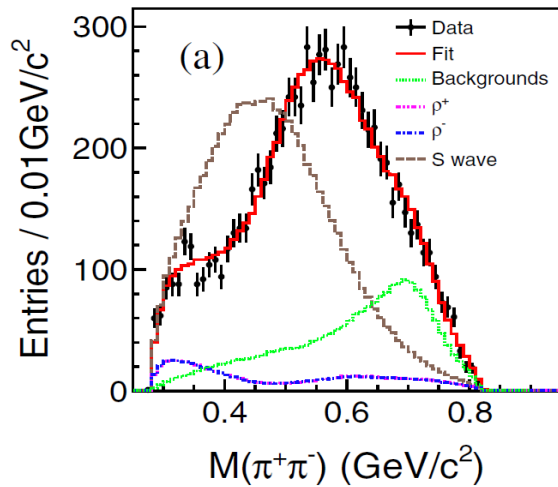


$\eta' \rightarrow \pi^0\pi^0\pi^0$ 2237 η' events



Amplitude analysis of the decays $\eta' \rightarrow 3\pi$

Phys. Rev. Lett. **118**, 012001 (2017)



Decay Mode	$B(10^{-4})$
$\pi^+ \pi^- \pi^0$	$35.91 \pm 0.54 \pm 1.74$
$\pi^0 \pi^0 \pi^0$	$35.22 \pm 0.82 \pm 2.54$
$\rho^\pm \pi^\mp$	$7.44 \pm 0.60 \pm 1.26 \pm 1.84$
$(\pi^+ \pi^- \pi^0)_S$	$37.63 \pm 0.77 \pm 2.22 \pm 4.48$

- Amplitude analysis combining $\eta' \rightarrow \pi^+ \pi^- \pi^0$ and $\eta' \rightarrow \pi^0 \pi^0 \pi^0$.
- Described by three components: P wave $\rho^\pm \pi^\mp$, resonant S wave ($\sigma \pi^0$), phase-space S wave ($\pi \pi \pi$)
- The P-wave contribution from ρ^\pm is observed for the first time with high statistical significance.

- Obtained decay width ratios:

$$r_\pm = (8.77 \pm 1.19) \times 10^{-3}$$

$$r_0 = (15.86 \pm 1.33) \times 10^{-3}$$

- Impact of gluon component on the dynamics of η' decays
- Comparison to the theoretical calculations with the effective ChPT
- Previous measurements on the dalitz plot of $\eta' \rightarrow \pi\pi\eta$ are from VES, GAMS and CLEO

$$X = \frac{\sqrt{3}(T_{\pi^+} - T_{\pi^-})}{Q}, \quad Y = \frac{m_\eta + 2m_\pi}{m_\pi} \frac{T_\eta}{Q} - 1$$

$T_{\pi,\eta}$ denote the kinetic energies of a pion and η in the η' rest frame

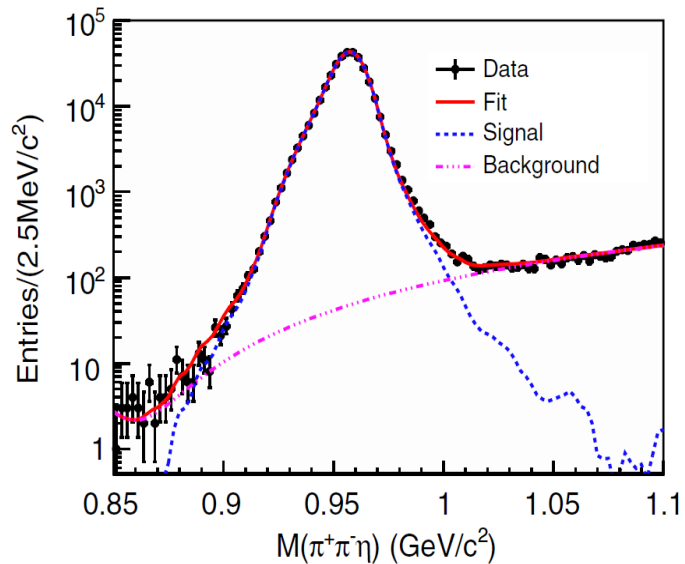
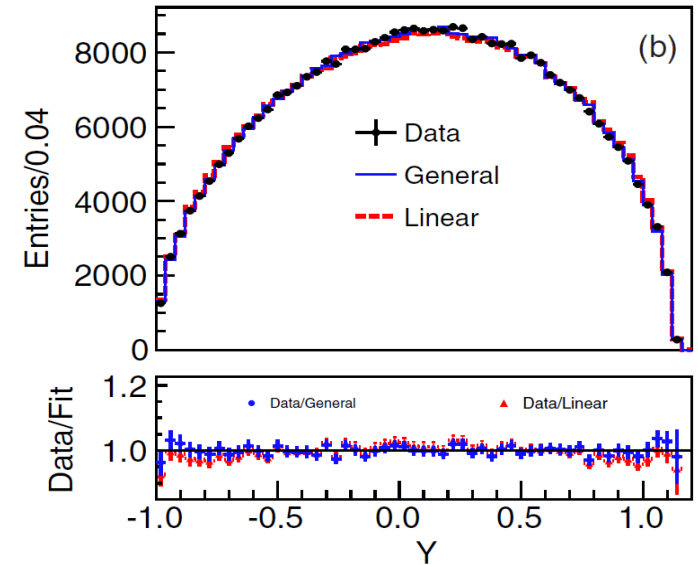
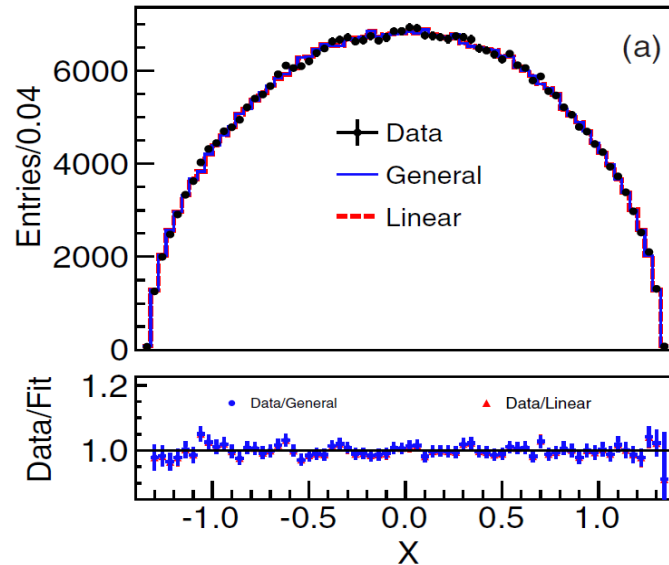
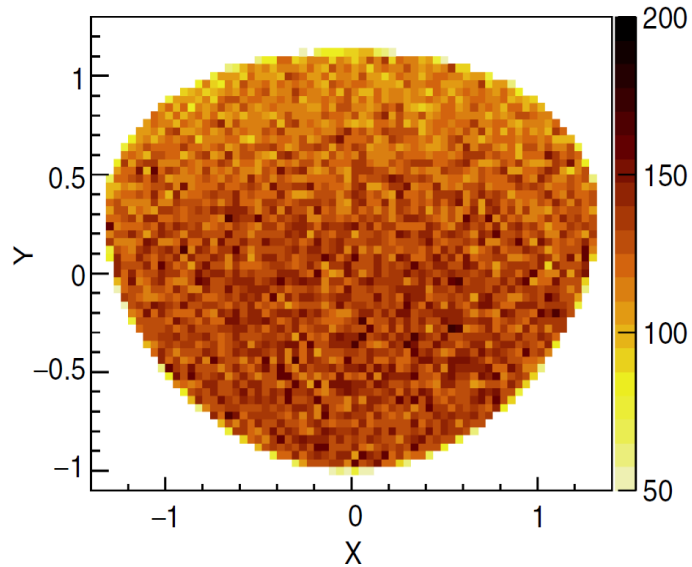
$$Q = T_\eta + T_{\pi^+} + T_{\pi^-} = m_{\eta'} - m_\eta - 2m_\pi$$

Two representations used

$$|M(X, Y)|^2 = N(1 + aY + bY^2 + cX + dX^2 + \dots) \text{ (general representation)}$$

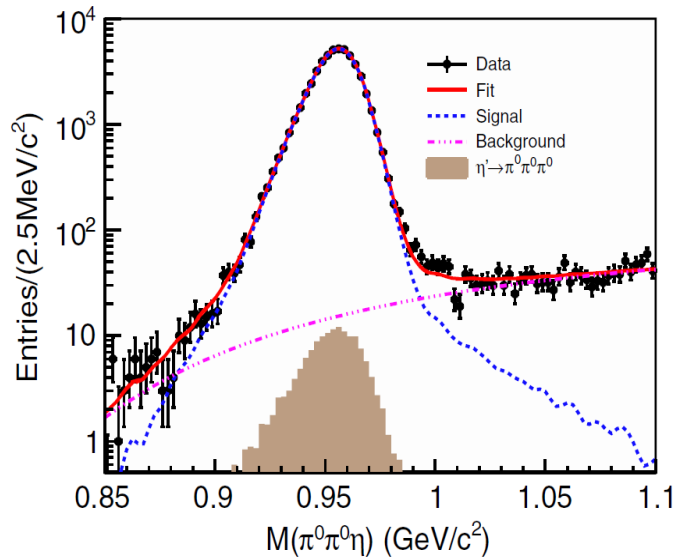
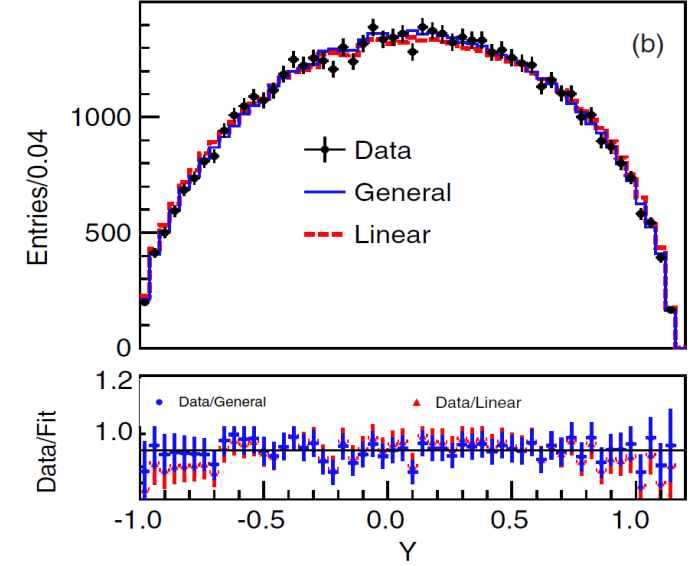
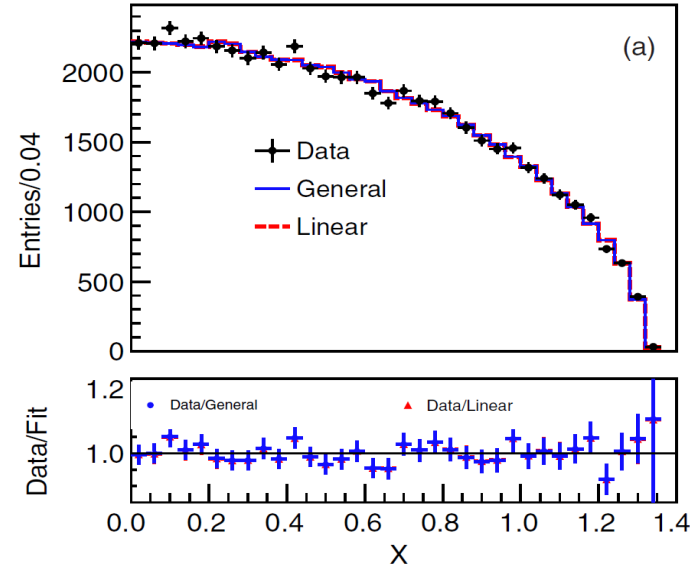
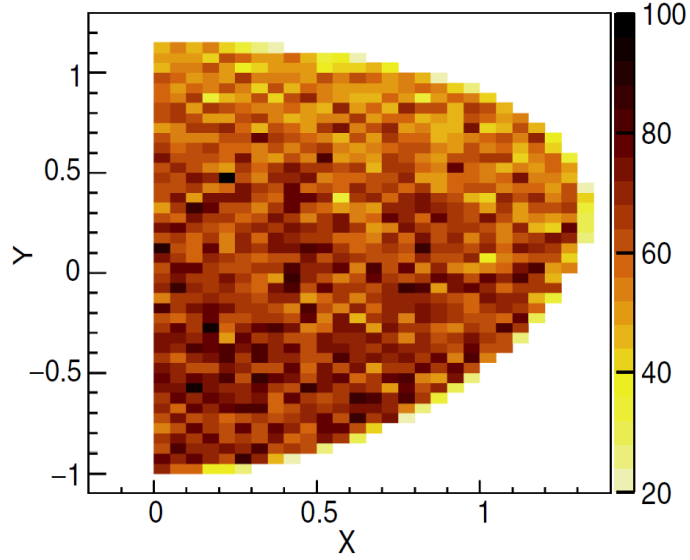
$$|M(X, Y)|^2 = N(|1 + \alpha Y|^2 + cX + dX^2 + \dots) \text{ (linear representation)}$$

Matrix elements for the decays $\eta' \rightarrow \pi^+ \pi^- \eta, \pi^0 \pi^0 \eta$



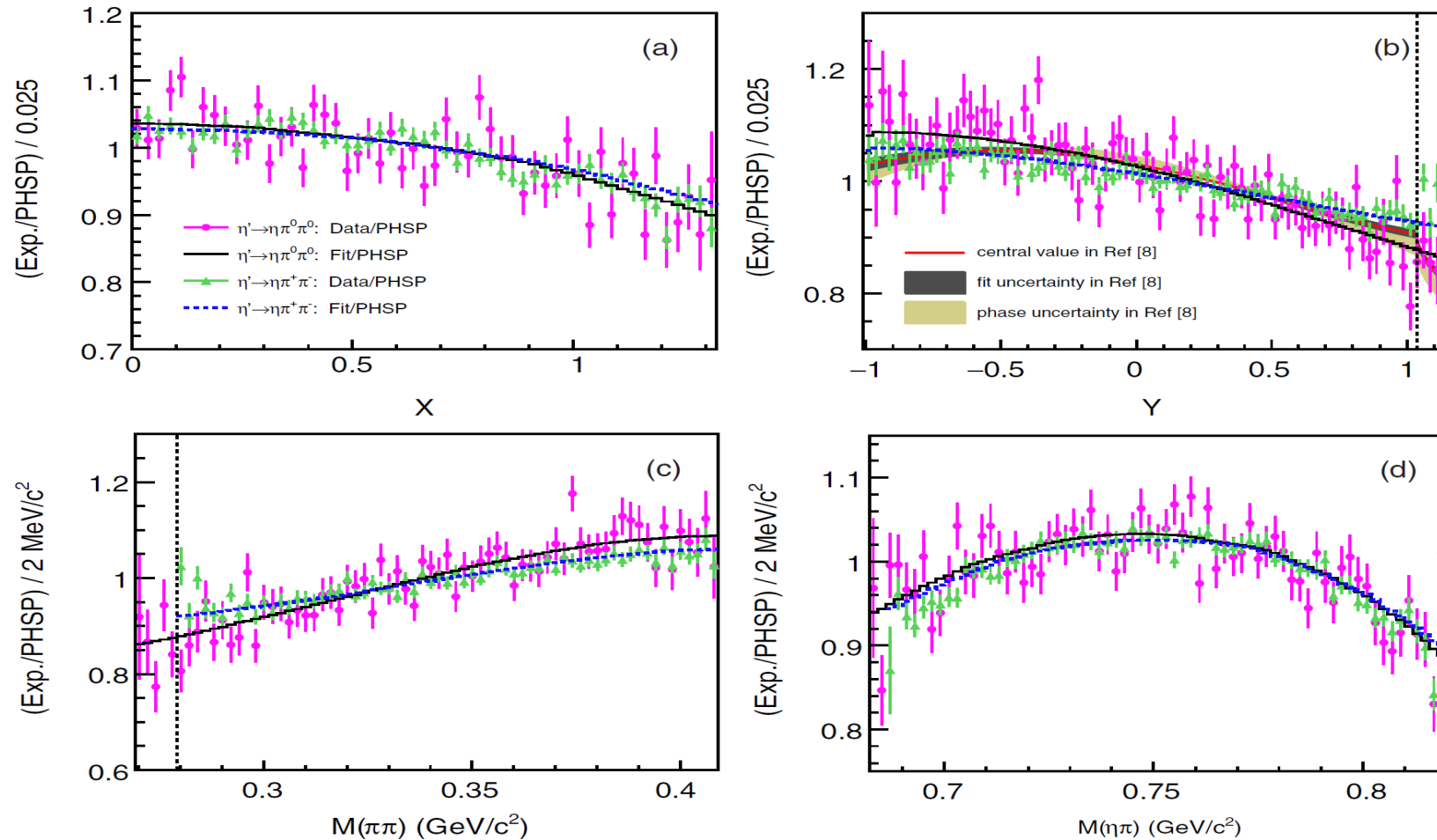
$\eta' \rightarrow \eta \pi^+ \pi^-$					
Parameter	EFT [5]	Large N_C [7]	RChT [7]	VES [10]	This work
a	-0.116(11)	-0.098(48) (fixed)	-0.127(18)	-0.056(4)(2)	
b	-0.042(34)	-0.050(1)	-0.033(1)	-0.106(32)	-0.049(6)(6)
c	+0.015(18)	0.0027(24)(18)
d	+0.010(19)	-0.092(8)	-0.072(1)	-0.082(19)	-0.063(4)(3)
$\Re(\alpha)$	-0.072(14)	-0.034(2)(2)
$\Im(\alpha)$	0.000(100)	0.000(19)(1)
c	+0.020(19)	0.0027(24)(15)
d	-0.066(34)	-0.053(4)(4)

Matrix elements for the decays $\eta' \rightarrow \pi^+ \pi^- \eta, \pi^0 \pi^0 \eta$



Parameter	$\eta' \rightarrow \eta \pi^0 \pi^0$		
	EFT [5]	GAMS-4 π [12]	This work
a	$-0.127(9)$	$-0.067(16)$	$-0.087(9)(6)$
b	$-0.049(36)$	$-0.064(29)$	$-0.073(14)(5)$
c
d	$+0.011(21)$	$-0.067(20)$	$-0.074(9)(4)$
$\Re(\alpha)$...	$-0.042(8)$	$-0.054(4)(1)$
$\Im(\alpha)$...	$0.000(70)$	$0.000(38)(2)$
c
d	...	$-0.054(19)$	$-0.061(9)(5)$

Search for cusp effect in $\eta' \rightarrow \pi^0 \pi^0 \eta$



➤ With current statistics, it is difficult to establish cusp effect near the $\pi\pi$ mass threshold.

➤ Test QCD calculations on the transition form factor

➤ Check the high order of ChPT

➤ In experiment, only an upper limit of

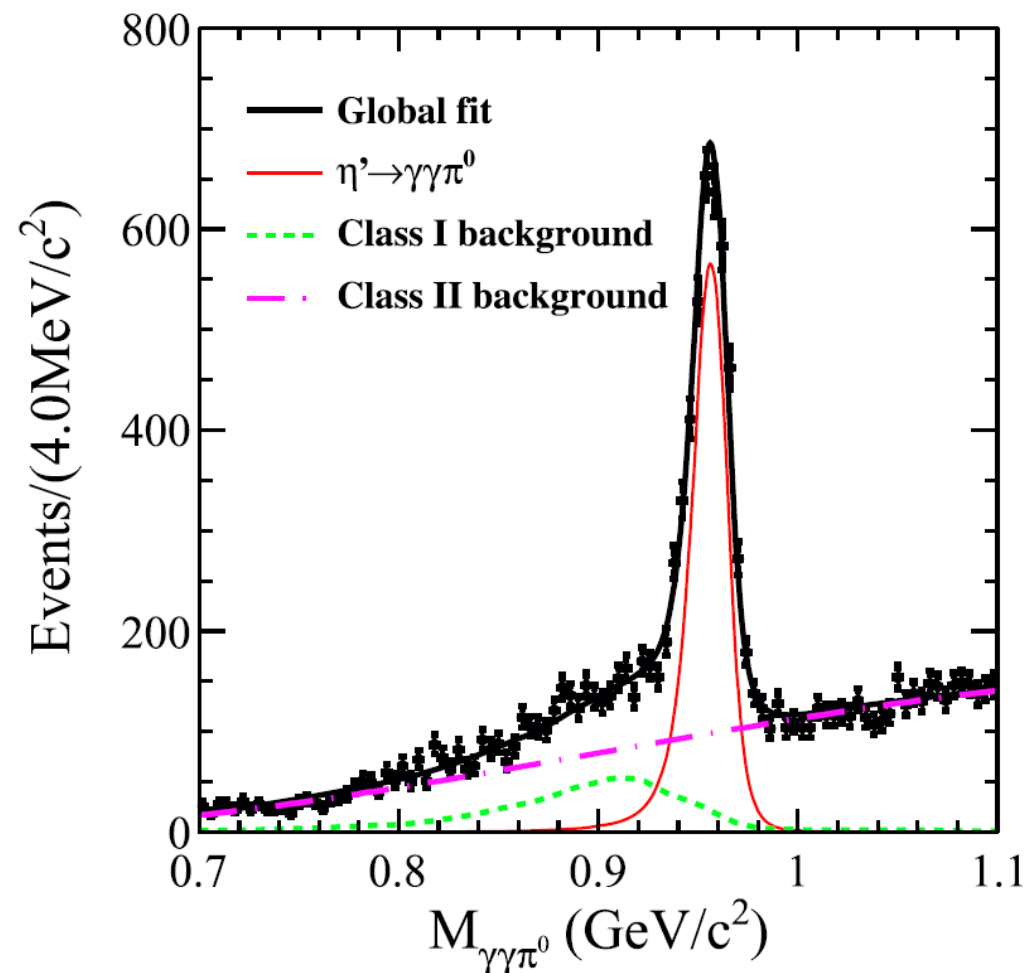
$$\mathcal{B}(\eta' \rightarrow \gamma\gamma\pi^0) < 8 \times 10^{-4} \text{ at 90\% C.L.}$$

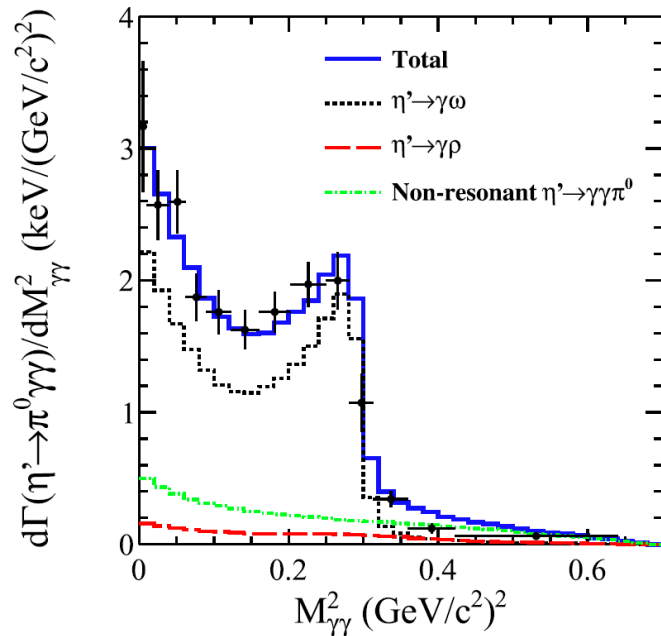
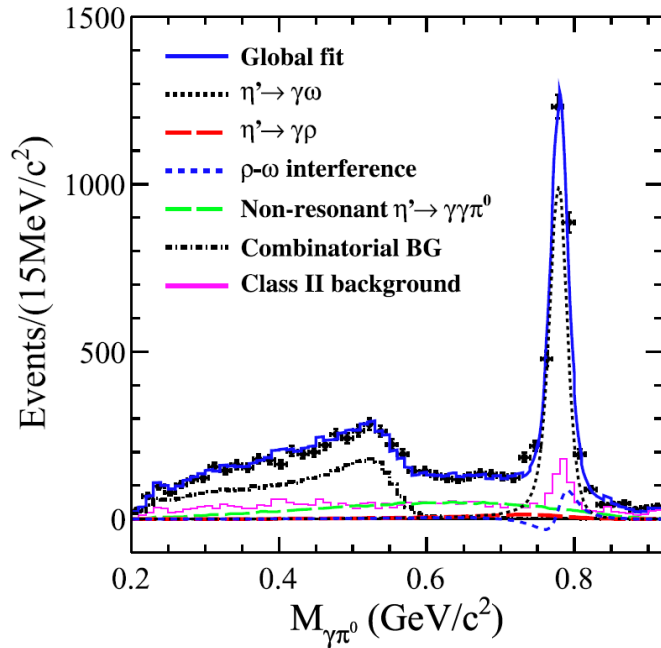
† $\eta' \rightarrow \gamma\gamma\pi^0$: Signal shape from MC, incoherent mixture of ρ , ω and non-resonant components.

† Class-I background: $J/\psi \rightarrow \gamma\eta'$ with η' decaying into other final states other than the signal final state.

† Class-II background: J/ψ decays without η' ($J/\psi \rightarrow \gamma\pi^0\pi^0$ and $J/\psi \rightarrow \omega\eta$ with $\omega \rightarrow \gamma\pi^0$ and $\eta \rightarrow \gamma\gamma$)

Phys. Rev. D **96**, 012005(2017)





	$\eta' \rightarrow \gamma\gamma\pi^0$ (Inclusive)	$\eta' \rightarrow \gamma\omega, \omega \rightarrow \gamma\pi^0$	$\eta' \rightarrow \gamma\gamma\pi^0$ (Non-resonant)
$N^{\eta'}$	$3435 \pm 76 \pm 244$	$2340 \pm 141 \pm 180$	$655 \pm 68 \pm 71$
ϵ	16.1%	14.8%	15.9%
$\mathcal{B} (10^{-4})$	$32.0 \pm 0.7 \pm 2.3$	$23.7 \pm 1.4 \pm 1.8^a$	$6.16 \pm 0.64 \pm 0.67$
$\mathcal{B}_{PDG} (10^{-4})$	—	21.7 ± 1.3^b	< 8 [9]
Predictions (10^{-4})	57 [7], 65 [8]	—	—

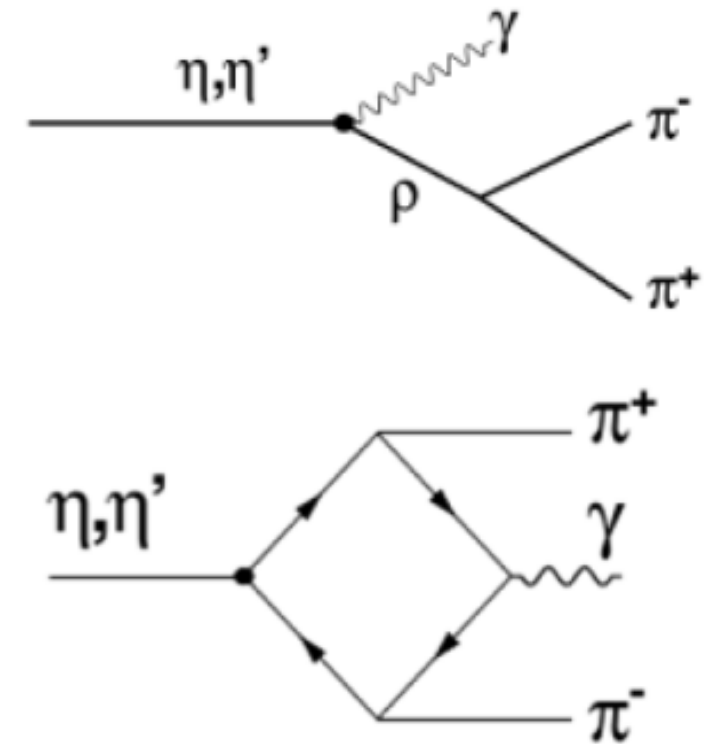
Linear σ model & VMD

[7] R. Jora, Nucl. Phys. Proc. Suppl. 207-208, 224(2010);

[8] R. Escribano, Proc. Sci., QNP2012 (2012) 079;

[9] D. Alde et al. (GAMS-2000), Z. Phys. C 36, 603 (1987).

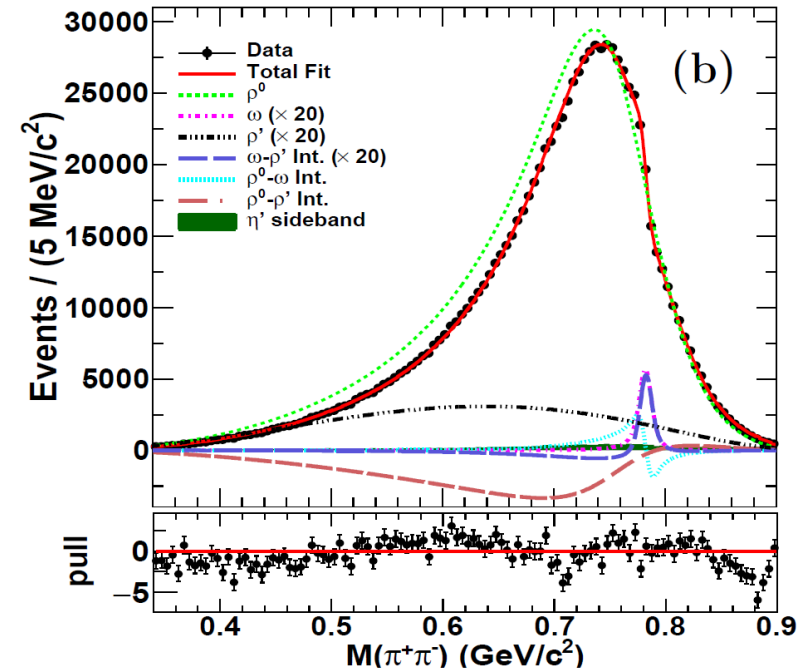
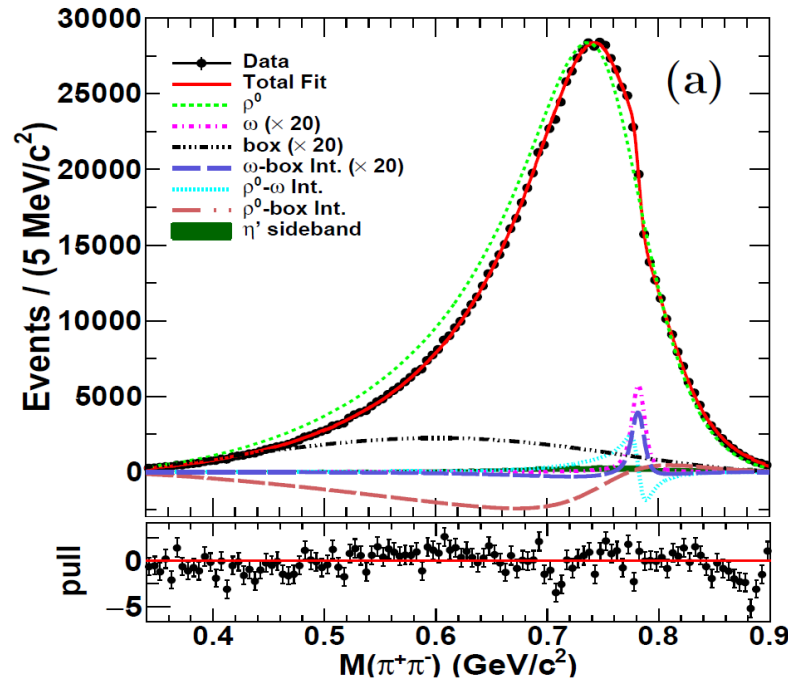
- $\eta' \rightarrow \gamma\pi^+\pi^-$ is the second most decay mode, with $(29.1 \pm 0.5)\%$
- In Vector Meson Dominance (VMD) model, this process is dominated by $\eta' \rightarrow \gamma\rho(770)$
- Studied by several experiments, a lone ρ^0 contribution did not describe the exp. data
- This discrepancy could be attributed to the Wess-Zumino-Witten anomaly in the ChPT, known as the box anomaly.
- Recently a model-independent approach based on ChPT are proposed



The dipion mass differential rate :

$$\frac{d\Gamma}{dM(\pi^+\pi^-)} = \frac{k_\gamma^3 q_\pi^3(s)}{48\pi^3} |A|^2$$

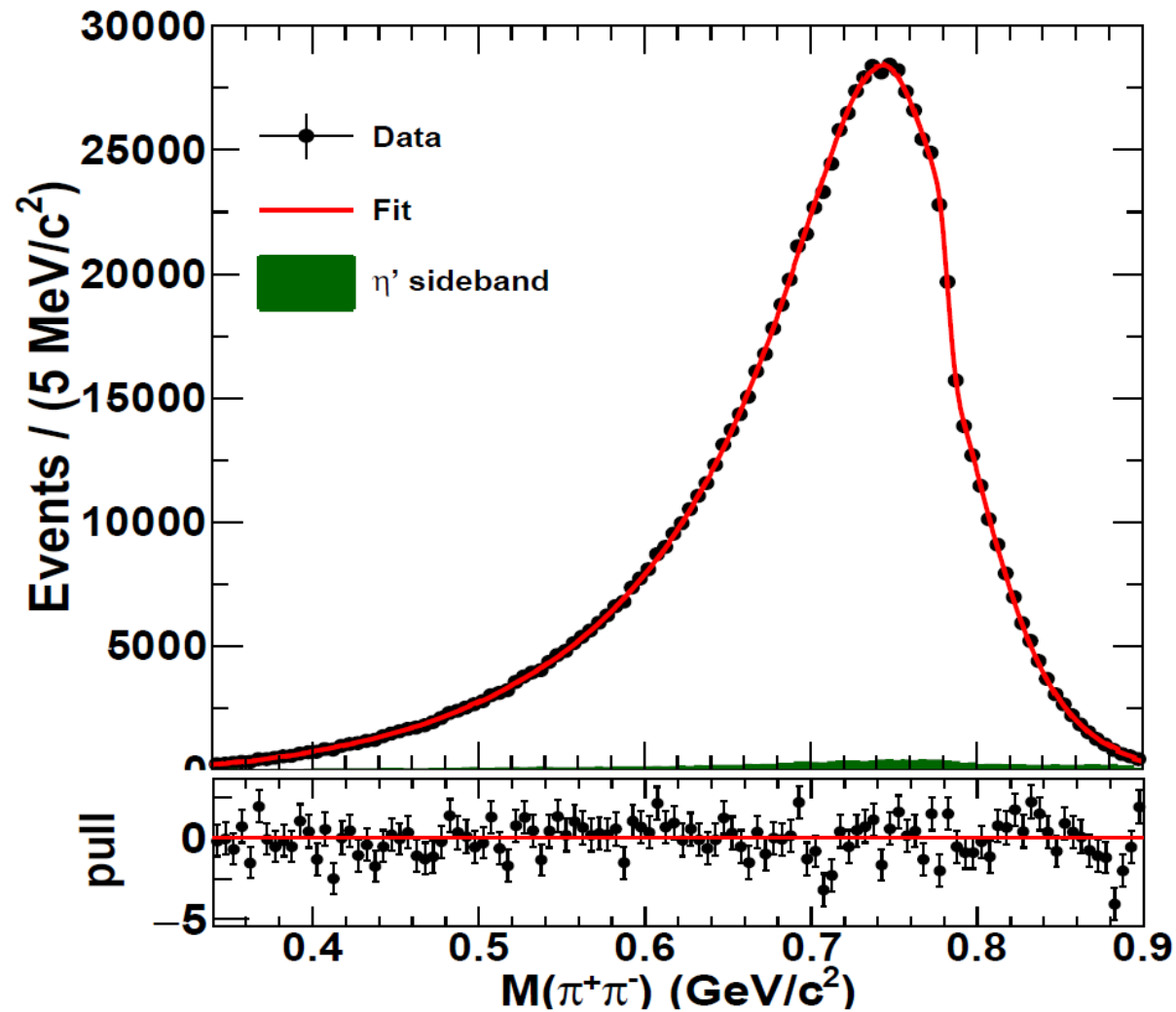
- 1). fit with $\rho(770) - \omega$ -box anomaly 2). fit with $\rho(770) - \omega - \rho(1450)$



- Besides $\rho(770)$, the ω is needed
- $\rho(770) - \omega$ cannot describe data well
- Extra contribution (maybe $\rho(1450)$ or box-anomaly, maybe both of them) is also necessary to provide a good description of data

Model-dependent fit

Phys. Rev. Lett. **120**, 242003(2018),



Model independent fit

- $A = N \cdot P(s) \cdot F_V(s)$
- $P(s) = 1 + \kappa \cdot s + \lambda \cdot s^2 + \xi \cdot BW_\omega + \mathcal{O}(s^4)$
- $F_V(s)$ is the pion vector form factor

Fit results:

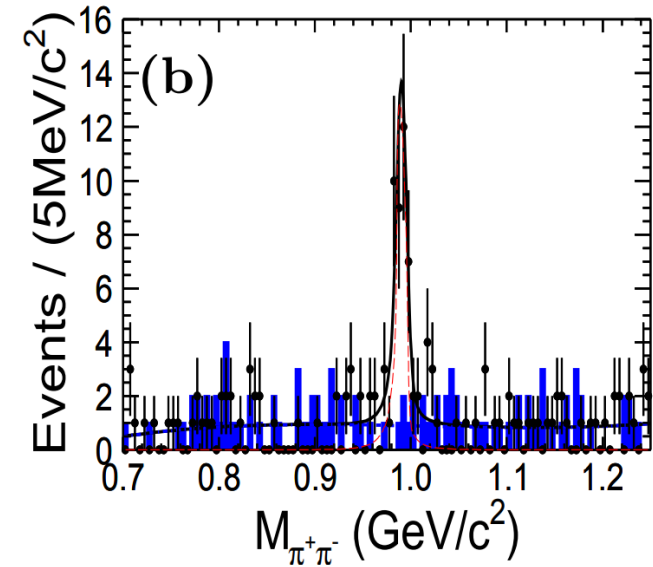
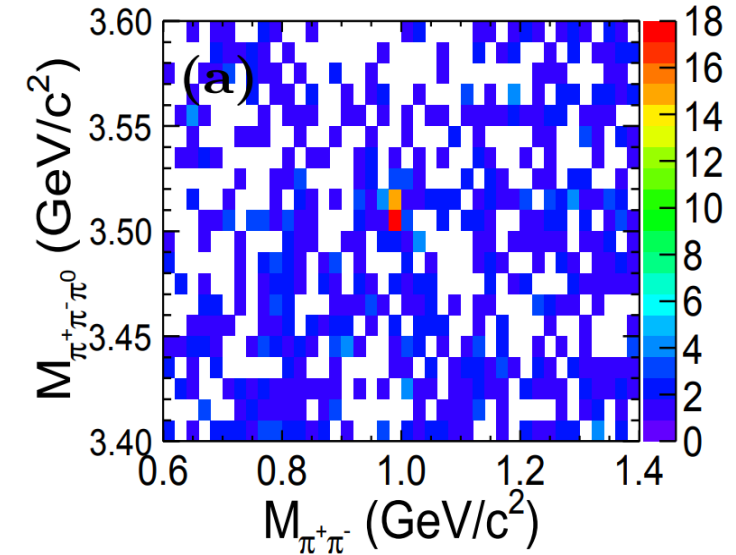
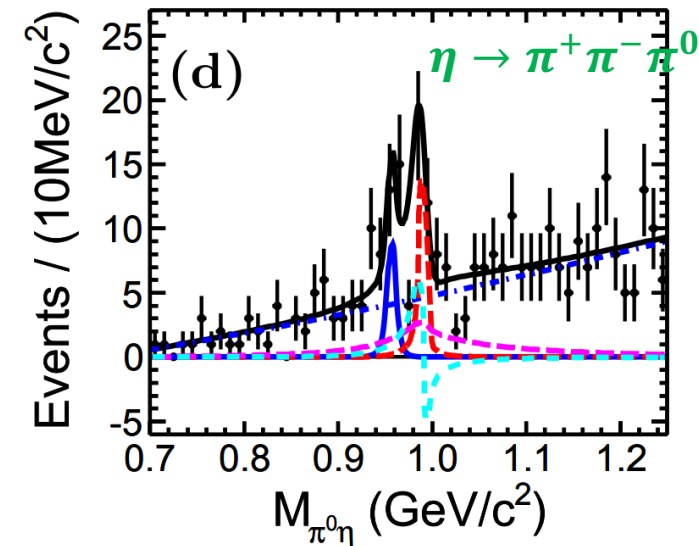
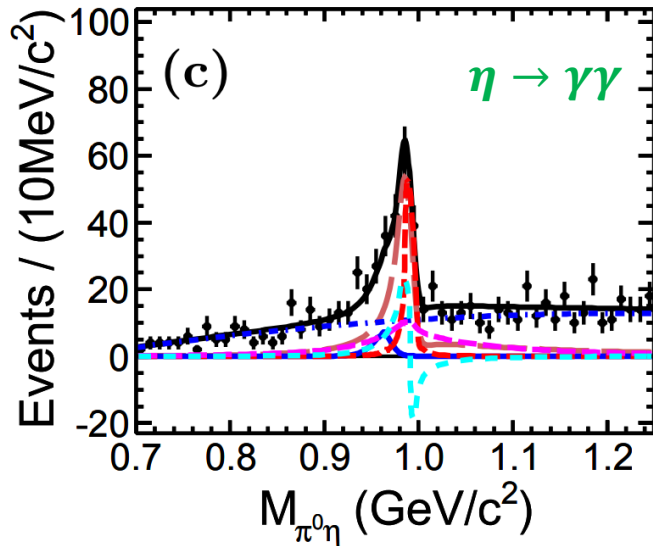
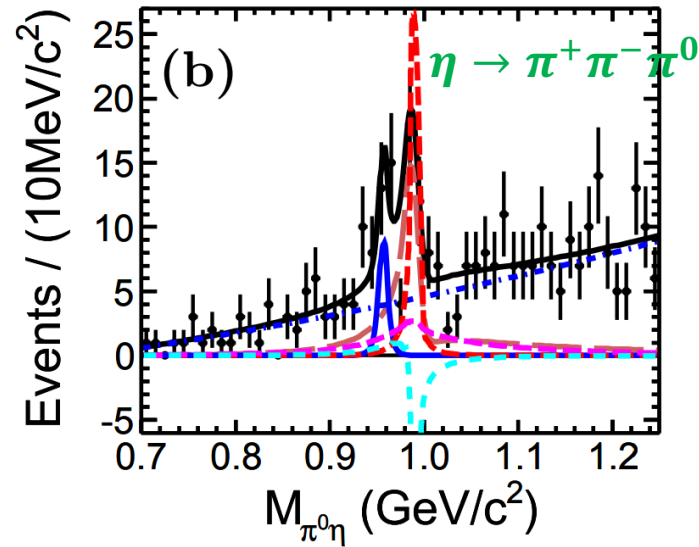
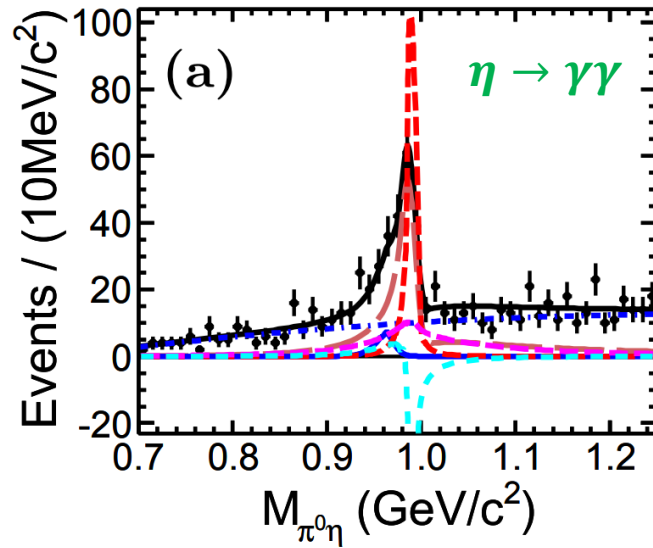
- $\kappa = (0.992 \pm 0.039 \pm 0.067 \pm 0.163)\text{GeV}^{-2}$
 - $\lambda = (-0.523 \pm 0.039 \pm 0.066 \pm 0.181)\text{GeV}^{-4}$
 - $\xi = 0.199 \pm 0.006 \pm 0.011 \pm 0.007$
- The ω is necessary
 - Quadratic term and the ω contribution are significant, linear polynomial is insufficient

Phys. Rev. Lett. **120**, 242003(2018),

Observation of $a_0(980) - f_0(980)$ Mixing

$$J/\psi \rightarrow \phi f_0(980) \rightarrow \phi a_0^0(980) \rightarrow \phi \eta \pi^0$$

$$\chi_{c1} \rightarrow \pi^0 a_0^0(980) \rightarrow \pi^0 f_0(980) \rightarrow \pi^0 \pi^+ \pi^-$$



arXiv:1802.00583 Accepted by PRL

- Mixing intensity is crucial to understand the nature of $a_0(980)$ and $f_0(980)$

$$\text{➤ } \xi_{fa} = \frac{\mathcal{B}(J/\psi \rightarrow \phi f_0(980) \rightarrow \phi a_0^0(980) \rightarrow \phi \eta \pi^0)}{\mathcal{B}(J/\psi \rightarrow \phi f_0(980) \rightarrow \phi \pi \pi)}$$

$$\text{➤ } \xi_{af} = \frac{\mathcal{B}(\chi_{c1} \rightarrow \pi^0 a_0^0(980) \rightarrow \pi^0 f_0(980) \rightarrow \pi^0 \pi^+ \pi^-)}{\mathcal{B}(\chi_{c1} \rightarrow \pi^0 a_0^0(980) \rightarrow \pi^0 \pi^0 \eta)}$$

- Final results of the branching fractions and the intensities of the $a_0^0(980) - f_0(980)$ mixing

Channel	$f_0(980) \rightarrow a_0^0(980)$		$a_0^0(980) \rightarrow f_0(980)$
	Solution I	Solution II	
$\mathcal{B}(\text{mixing}) (10^{-6})$	$3.18 \pm 0.51 \pm 0.38 \pm 0.28$	$1.31 \pm 0.41 \pm 0.39 \pm 0.43$	$0.35 \pm 0.06 \pm 0.03 \pm 0.06$
$\mathcal{B}(\text{EM}) (10^{-6})$	$3.25 \pm 1.08 \pm 1.08 \pm 1.12$	$2.62 \pm 1.02 \pm 1.13 \pm 0.48$	—
$\mathcal{B}(\text{total}) (10^{-6})$	$4.93 \pm 1.01 \pm 0.96 \pm 1.09$	$4.37 \pm 0.97 \pm 0.94 \pm 0.06$	—
$\xi (\%)$	$0.99 \pm 0.16 \pm 0.30 \pm 0.09$	$0.41 \pm 0.13 \pm 0.17 \pm 0.13$	$0.40 \pm 0.07 \pm 0.14 \pm 0.07$

- ◆ A unique place to study light meson decays
 - Observation of $\eta' \rightarrow \rho^\pm \pi^\mp$ in $\eta' \rightarrow \pi\pi\pi$
 - Dalitz plot of $\eta' \rightarrow \pi^+ \pi^- \eta, \pi^0 \pi^0 \eta$
 - Study of $\eta' \rightarrow \gamma \pi^+ \pi^-$ decay dynamics
 - Observation of $\eta' \rightarrow \gamma \gamma \pi^0$
 - First observation of $a_0^0(980) - f_0(980)$ mixing
- ◆ BESIII is an ideal laboratory to study light meson decays
- ◆ 1.3 billion + 3.7 billion (2017-2018) J/ψ events
- ◆ More interesting light meson decays are expected

Thanks for your attention!

- * $\eta' \rightarrow \pi^+\pi^-\eta$ [Phys. Rev. D **83**, 012003 \(2011\)](#)
- * $\eta/\eta' \rightarrow \pi^+\pi^-, \pi^0\pi^0$ [Phys. Rev. D **84**, 032006 \(2011\)](#)
- * $\eta' \rightarrow \pi^+\pi^-\pi^0, \pi^0\pi^0\pi^0$ [Phys. Rev. Lett. **108**, 182001 \(2012\)](#)
- * $\eta/\eta' \rightarrow$ invisible [Phys. Rev. D **87**, 012009 \(2013\)](#)
- * weak decay [Phys. Rev. D **87**, 032006 \(2013\)](#)
- * $\eta' \rightarrow \pi^+\pi^-l^+l^-$ [Phys. Rev. D **87**, 092011 \(2013\)](#)
- * $\eta' \rightarrow 3(\pi^+\pi^-)$ [Phys. Rev. D **88**, 091502 \(2013\)](#)
- * $\eta' \rightarrow 2(\pi^+\pi^-), \pi^+\pi^-\pi^0\pi^0$ [Phys. Rev. Lett **112**, 251801 \(2014\)](#)
- * $\eta' \rightarrow \gamma e^+e^-$ [Phys. Rev. D **92**, 012001 \(2015\)](#)
- * $\eta \rightarrow \pi^+\pi^-\pi^0, \eta/\eta' \rightarrow \pi^0\pi^0\pi^0$ [Phys. Rev. D **92**, 012014 \(2015\)](#)
- * $\eta' \rightarrow \omega e^+e^-$ [Phys. Rev. D **92**, 051101 \(2015\)](#)
- * $\eta' \rightarrow K\pi$ [Phys. Rev. D **93**, 072008 \(2016\)](#)
- * $\eta' \rightarrow \rho\pi$ [Phys. Rev. Lett. **118**, 012001 \(2017\)](#)
- * $\eta' \rightarrow \gamma\gamma\pi^0$ [Phys. Rev. D **96**, 012005 \(2017\)](#)
- * $\eta' \rightarrow \pi^+\pi^-\eta, \eta' \rightarrow \pi^0\pi^0\eta$ [Phys. Rev. D **97**, 012003 \(2018\)](#)
- * $\eta' \rightarrow \gamma\pi^+\pi^-$ [arXiv:1712.01525 Accepted by PRL](#)