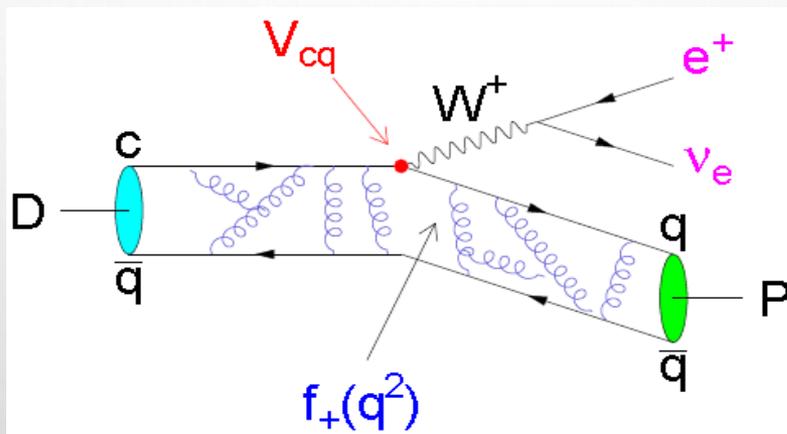




BESIII

Charmed Meson Semi-leptonic Decays At BESIII



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(On Behalf of BESIII collaboration)

CHEP2018, Shanghai

Outline

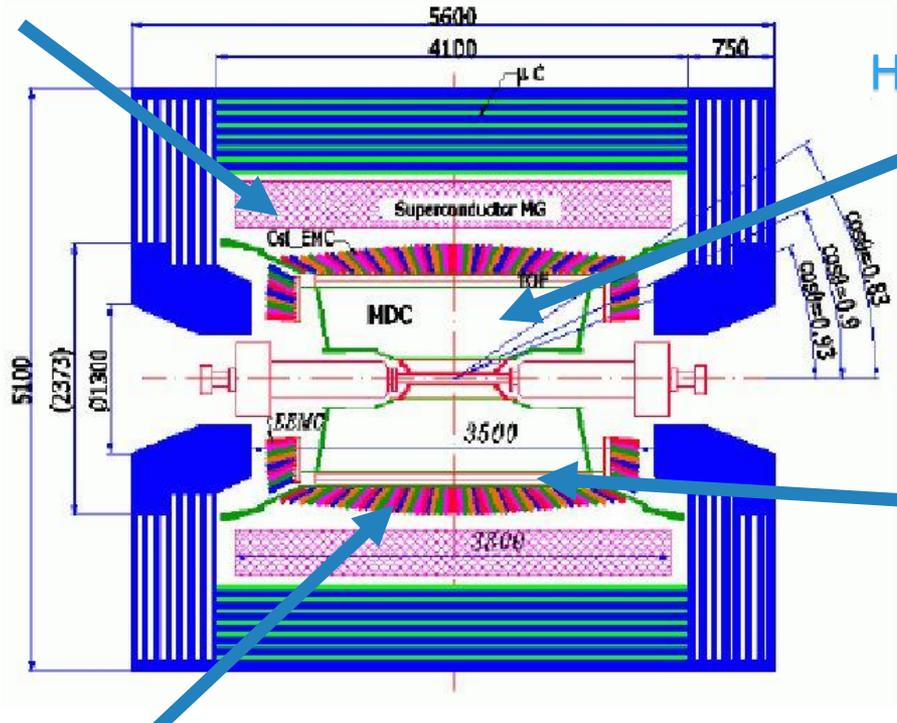
- BESIII detector
- Charm meson semileptonic decay
 - $D_s^+ \rightarrow \eta^{(\prime)} e^+ \nu_e$ decays
 - Rare semileptonic decays of D
 - $D^+ \rightarrow D^0 e^+ \nu_e$ decay
 - $D^+ \rightarrow \gamma e^+ \nu_e$ decay
 - $D^{+(0)} \rightarrow a^0(980)^{0(-)} e^+ \nu_e$ decays
- Summary

BEPCII



BESIII Detector

Magnet: 1 T Super conducting



MDC: small cell & Gas:
He/C₃H₈ (60/40), 43 layers

$$\sigma_{xy} = 130 \mu m$$

$$\sigma_p/p = 0.5\% @ 1 \text{ GeV}$$

$$dE/dx = 6\%$$

TOF: $\sigma_T < 70 \text{ ps}$

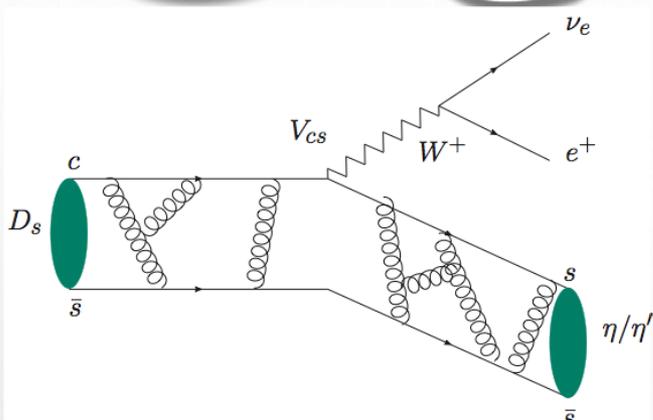
EMC: Csl crystal, 28 cm

$$\Delta E/E = 2.5\% @ 1 \text{ GeV}$$

$$\sigma_z = 0.6 \text{ cm} / \sqrt{E}$$

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$$D_s^+ \rightarrow \eta^{(\prime)} e^+ \nu_e$$



➤ η - η' mixing angle

$$\begin{pmatrix} |\eta\rangle \\ |\eta'\rangle \end{pmatrix} = \begin{pmatrix} \cos\phi_P & -\sin\phi_P \\ \sin\phi_P & \cos\phi_P \end{pmatrix} \begin{pmatrix} |\eta_q\rangle \\ |\eta_s\rangle \end{pmatrix}$$

$$\frac{\Gamma(D_s^+ \rightarrow \eta' e^+ \nu) / \Gamma(D_s^+ \rightarrow \eta e^+ \nu)}{\Gamma(D^+ \rightarrow \eta' e^+ \nu) / \Gamma(D^+ \rightarrow \eta e^+ \nu)} \simeq \cot^4 \phi_P$$

- Measurements of $f_+^{D_s \rightarrow \eta^{(\prime)}}(0)$ will be crucial to calibrate the theoretical calculations
- Extraction of $|V_{cs}|$ provides complementary data to test the unitarity of the CKM matrix
- The ratio of $B[D_s^+ \rightarrow \eta e^+ \nu_e] / B[D_s^+ \rightarrow \eta' e^+ \nu_e]$ helps to determine $\eta - \eta'$ mixing angle (ϕ_P)

➤ Differential partial widths

$$\Gamma(D_s^+ \rightarrow \eta^{(\prime)} e^+ \nu_e) = \frac{G_f^2}{24\pi^3} |V_{cs}|^2 |\vec{p}_{\eta^{(\prime)}}|^3 |f_+^{\eta^{(\prime)}}(q^2)|^2 dq^2$$

Simple pole

$$f_+(q^2) = \frac{f_+(0)}{1 - \frac{q^2}{M_{pole}^2}} \rightarrow f_+^{\eta^{(\prime)}}(0) |V_{cs}|$$

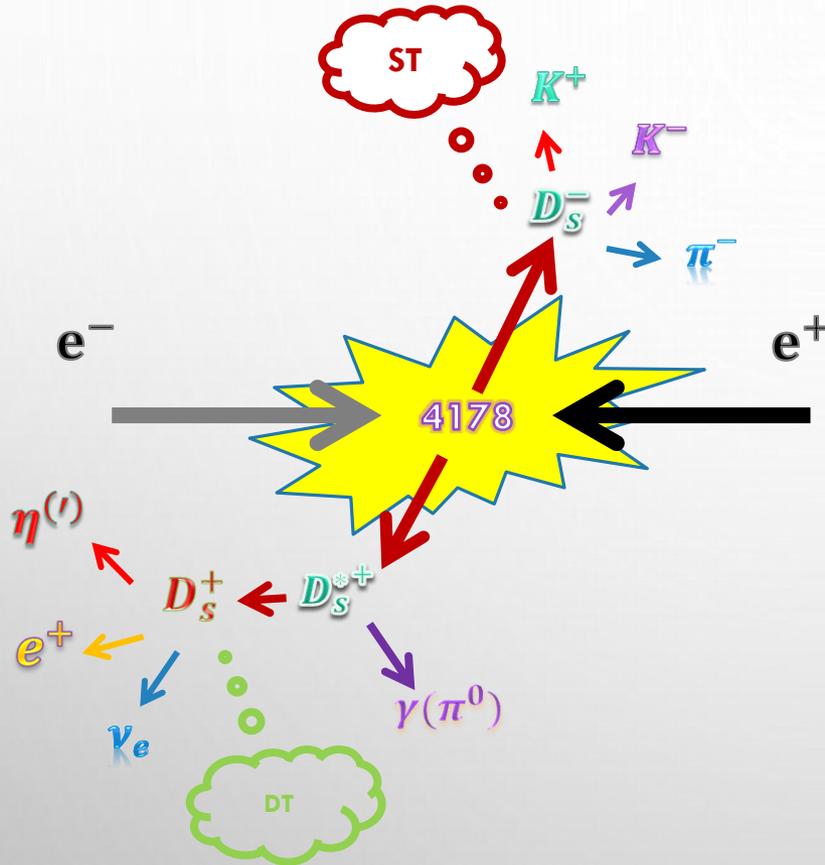
Modified pole

$$f_+(q^2) = \frac{f_+(0)}{(1 - \frac{q^2}{M_{pole}^2})(1 - \alpha \frac{q^2}{M_{pole}^2})}$$

Series expansion

$$f_+(t) = \frac{1}{P(t)\Phi(t, t_0)} a_0(t_0) \left(1 + \sum_{i=1}^{\infty} r_k(t_0) [z(t, t_0)]^k\right)$$

Analysis Technique



Single tag yield:

$$N_{ST}^i = 2 \times N_{D_s^{*+} D_s^-} \times B_{ST}^i \times \epsilon_{ST}^i$$

Double tag yield:

$$N_{DT}^i = 2 \times N_{D_s^{*+} D_s^-} \times B_{ST}^i \times B_{SL} \times \epsilon_{STvs.SL}^i$$

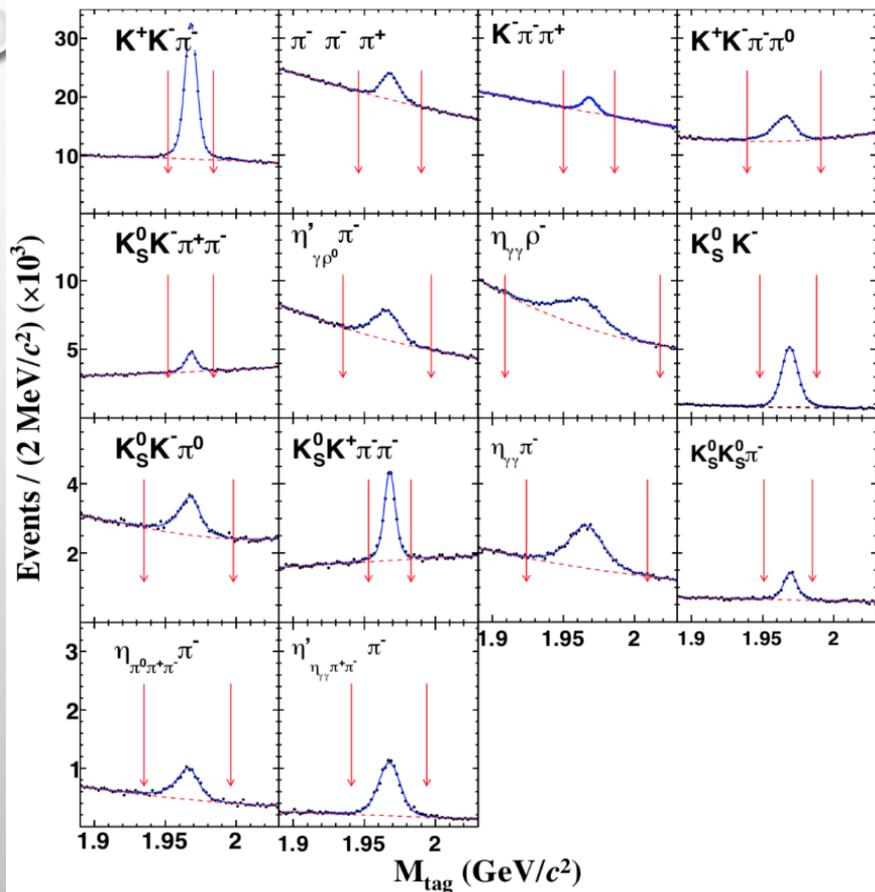
Branching fraction:

$$B_{SL} = \frac{N_{DT}}{N_{ST}^{tot} \times \bar{\epsilon}_{SL}}, N_{ST}^{tot} = \sum_i N_{ST}^i$$

Average efficiency:

$$\bar{\epsilon}_{SL} = \frac{\sum_{i=1}^N (N_{ST}^i \times \epsilon_{STvs.SL}^i / \epsilon_{ST}^i)}{\sum_{i=1}^N N_{ST}^i}$$

Single Tag D_S^-

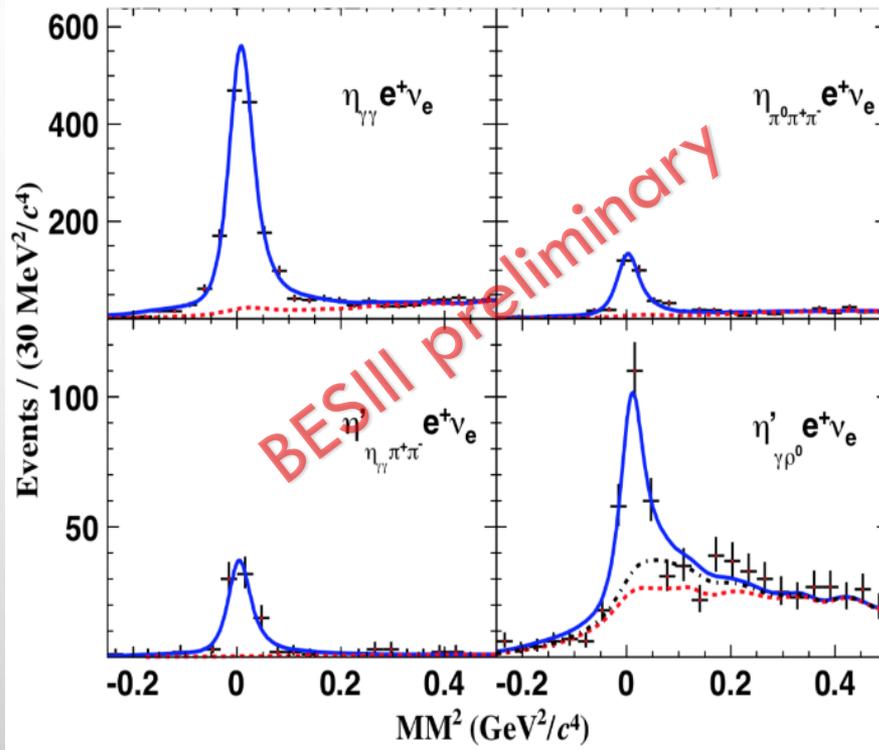


- The blue curves are total fits: signal MC shape convoluted Gaussian + polynomial function
- The red dotted curves are the fitted combinatorial backgrounds: polynomial function

$$e^+e^- \rightarrow D_S^{*+}D_S^-, D_S^{*+} \rightarrow (\gamma/\pi^0)D_S^+ + \text{c.c.}$$

395142 ± 1923 tagged D_S mesons
with 3.2 fb^{-1} @4178 MeV

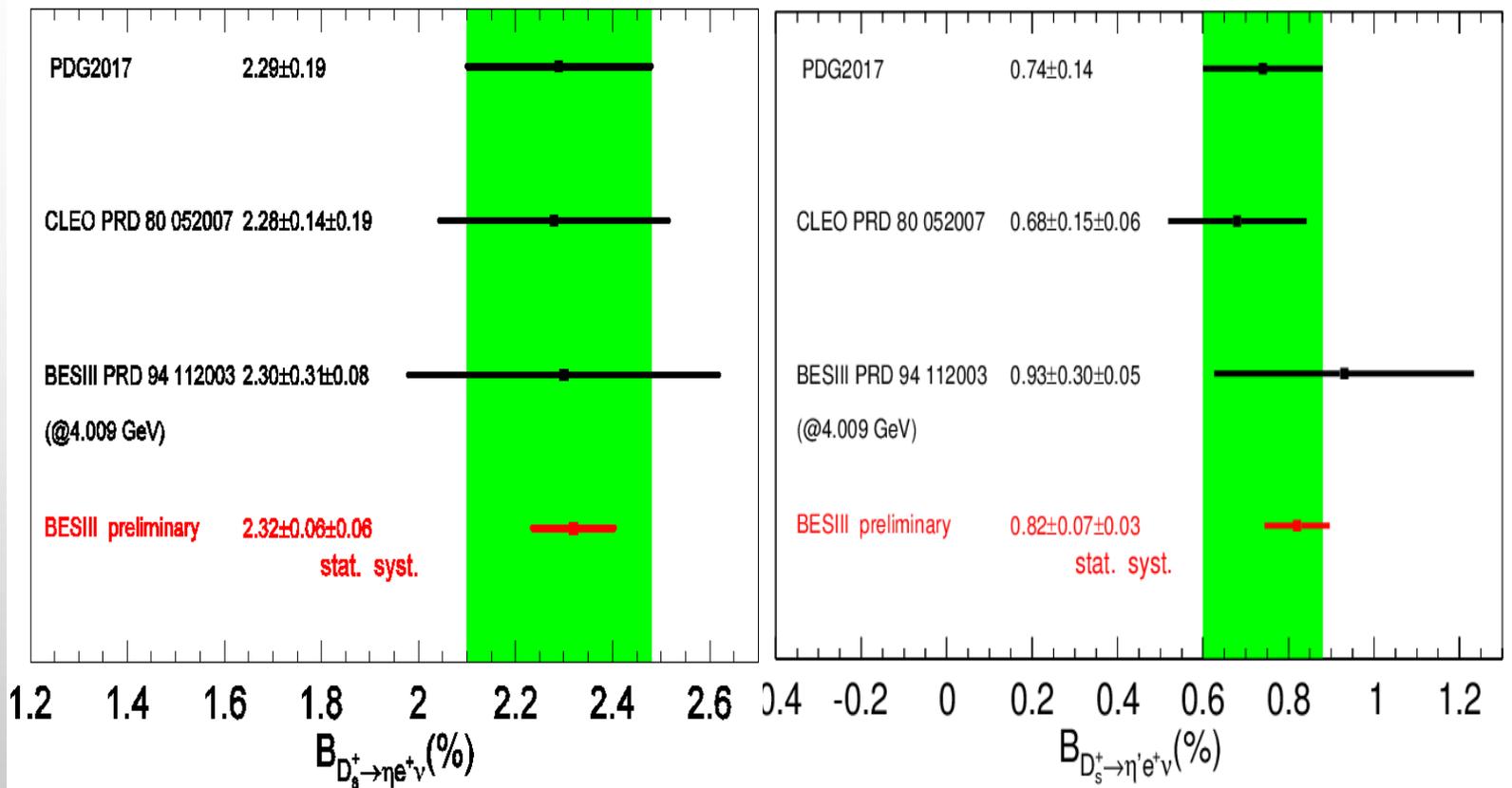
Fits To MM^2 of Semileptonic Candidates



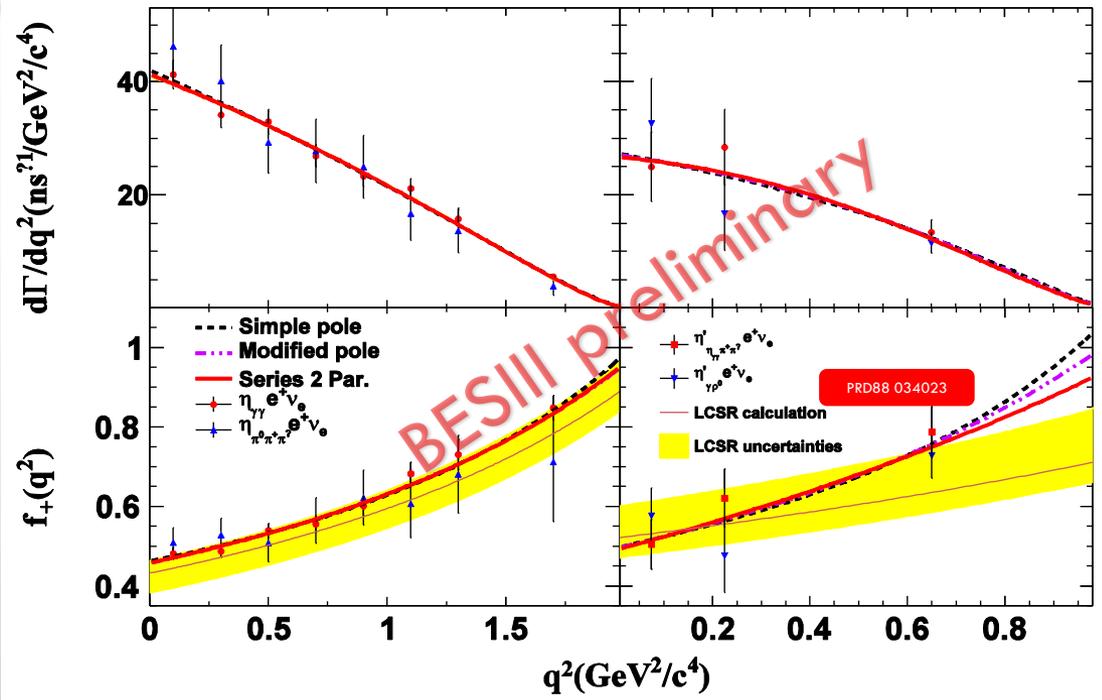
- The blue curves are total fits:
- Signal shape: MC simulated shape convolved with Gaussian
- Black dotted-dashed curve is the fitted background from $D_s^+ \rightarrow \phi e^+ \nu_e$: MC simulated shape
- Red dotted curve are fitted combinatorial background in signal side: MC simulated shape
- Constraint fit: The branching fractions of $D_s^+ \rightarrow \eta e^+ \nu_e$ or $D_s^+ \rightarrow \eta' e^+ \nu_e$ for two different $\eta^{(\prime)}$ subdecays are constrained to be same

Decay	$\eta^{(\prime)}$ decay	$\epsilon_{\gamma(\pi^0)\text{SL}} (\%)$	$N_{\text{DT}}^{\text{tot}}$	$\mathcal{B}_{\text{SL}} (\%)$
$\eta e^+ \nu_e$	$\gamma\gamma$	41.11 ± 0.27	1834 ± 47	$2.32 \pm 0.06 \pm 0.06$
	$\pi^0 \pi^+ \pi^-$	16.06 ± 0.31		
$\eta' e^+ \nu_e$	$\eta \pi^+ \pi^-$	14.07 ± 0.10	261 ± 22	$0.82 \pm 0.07 \pm 0.03$
	$\gamma \rho^0$	18.98 ± 0.10		

Comparisons Of Branching Fractions



Fits to partial decay rates and projections on form factors



- Partial decay rates are fitted simultaneously by two η/η' subdecays
- Based on the result extracted with the series 2 Parameters, we determine $|V_{CS}|$ and $f_+^{\eta^{(\prime)}}(0)$

Nominal result

Case	Simple pole			Modified pole			Series 2 Par.		
	$f_+^{\eta^{(\prime)}}(0) V_{CS} $	M_{pole}	χ^2/NDOF	$f_+^{\eta^{(\prime)}}(0) V_{CS} $	α	χ^2/NDOF	$f_+^{\eta^{(\prime)}}(0) V_{CS} $	r_1	χ^2/NDOF
$\eta e^+ \nu_e$	0.450(5)(3)	3.77(8)(5)	12.2/14	0.445(5)(3)	0.30(4)(3)	11.4/14	0.446(5)(4)	-2.2(2)(1)	11.5/14
$\eta' e^+ \nu_e$	0.494(45)(10)	1.88(54)(5)	1.8/4	0.481(44)(10)	1.62(91)(11)	1.8/4	0.477(49)(11)	-13.1(76)(11)	1.9/4

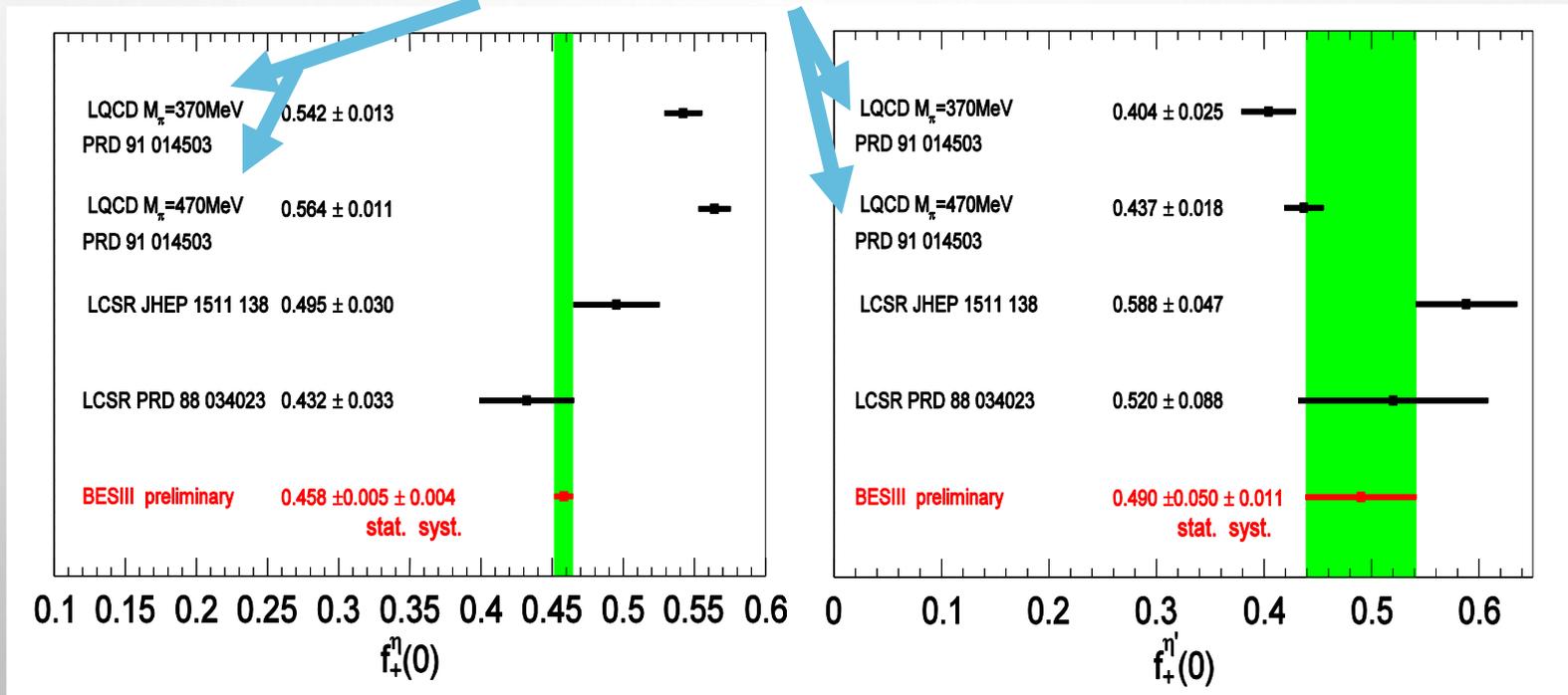
Uncertainties on the least significant digits are shown in parentheses, where the first (second) uncertainties are statistical (systematic)

Comparisons of form factors

Taking $|V_{cs}|$ CKMfitter and $f_+^{\eta^{(\prime)}}(0) |V_{cs}|$ extracted with the series 2 Parameters as input, we obtain

$$f_+^{\eta}(0) = 0.458 \pm 0.005_{stat} \pm 0.004_{syst} \quad f_+^{\eta'}(0) = 0.490 \pm 0.050_{stat} \pm 0.011_{syst}$$

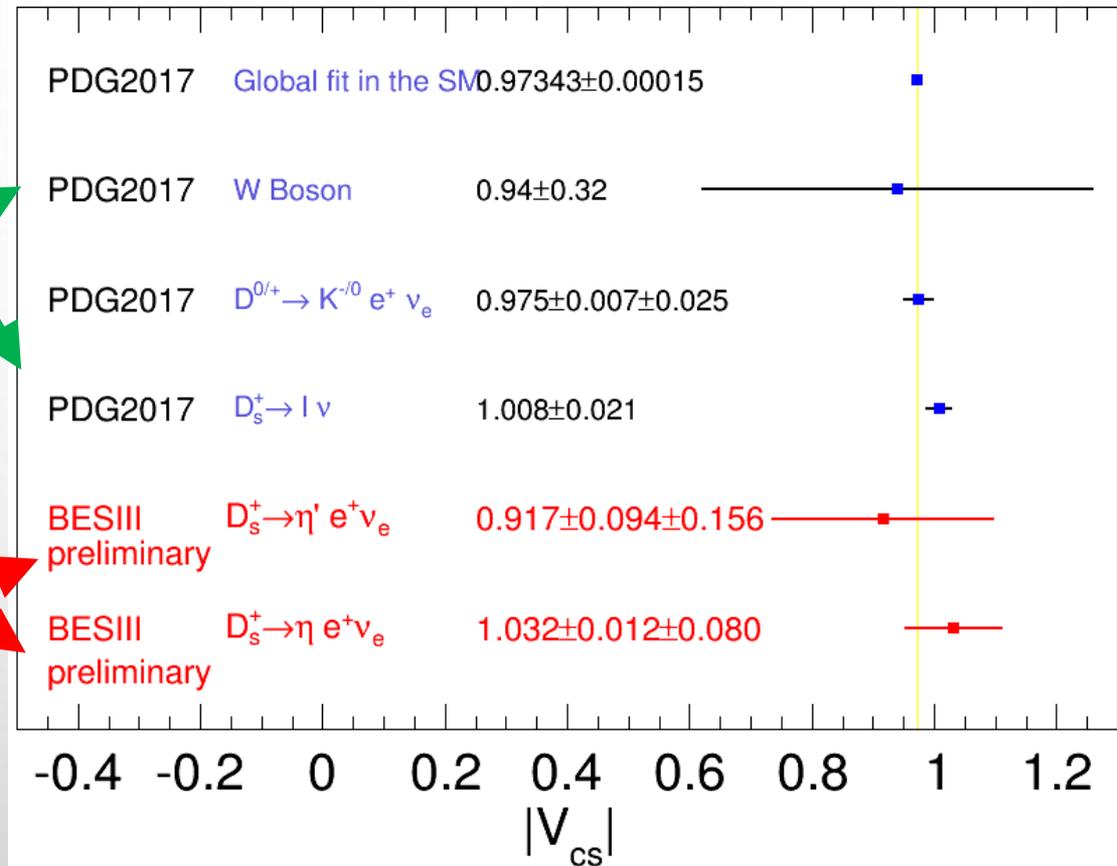
No systematic uncertainty is considered



Comparison of $|V_{cs}|$

Only reported one uncertainty, but include both statistical and systematic

Taking $f_+^{D_s \rightarrow \eta^{(\prime)}}(0)$
PRD88 034023 as
input, we obtain

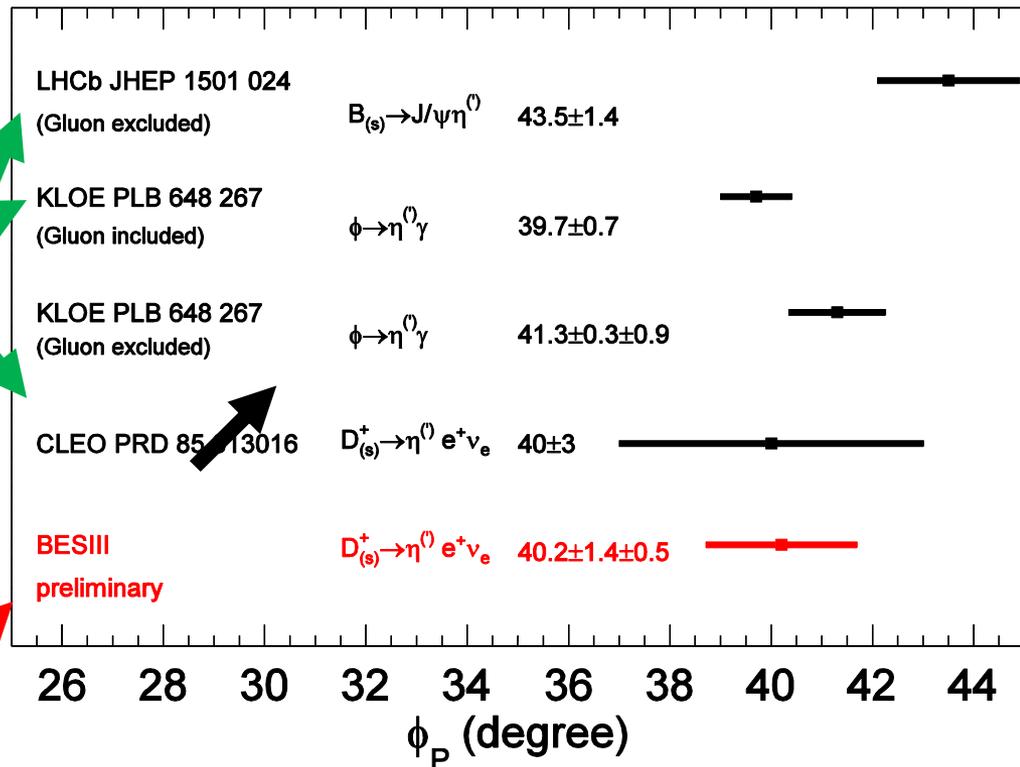


Comparison of mixing angle

Paper only reported one uncertainty, but include both statistical and systematic

Combining the branching fractions measured in this work and $B[D^+ \rightarrow \eta e^+ \nu_e] = (10.74 \pm 0.81 \pm 0.51) \times 10^{-4}$, $B[D^+ \rightarrow \eta' e^+ \nu_e] = (1.91 \pm 0.51 \pm 0.13) \times 10^{-4}$ (BESIII Phys. Rev. D 97, 092009 (2018)) into below equation, we obtain

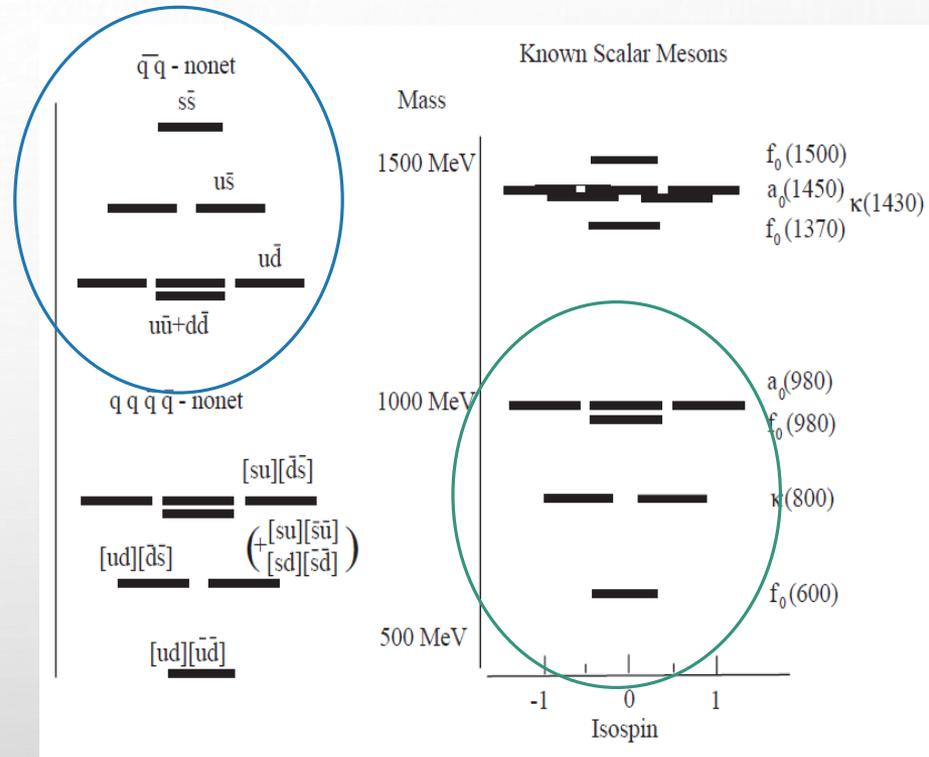
$$\frac{\Gamma(D_s^+ \rightarrow \eta' e^+ \nu) / \Gamma(D_s^+ \rightarrow \eta e^+ \nu)}{\Gamma(D^+ \rightarrow \eta' e^+ \nu) / \Gamma(D^+ \rightarrow \eta e^+ \nu)} \simeq \cot^4 \phi_P$$



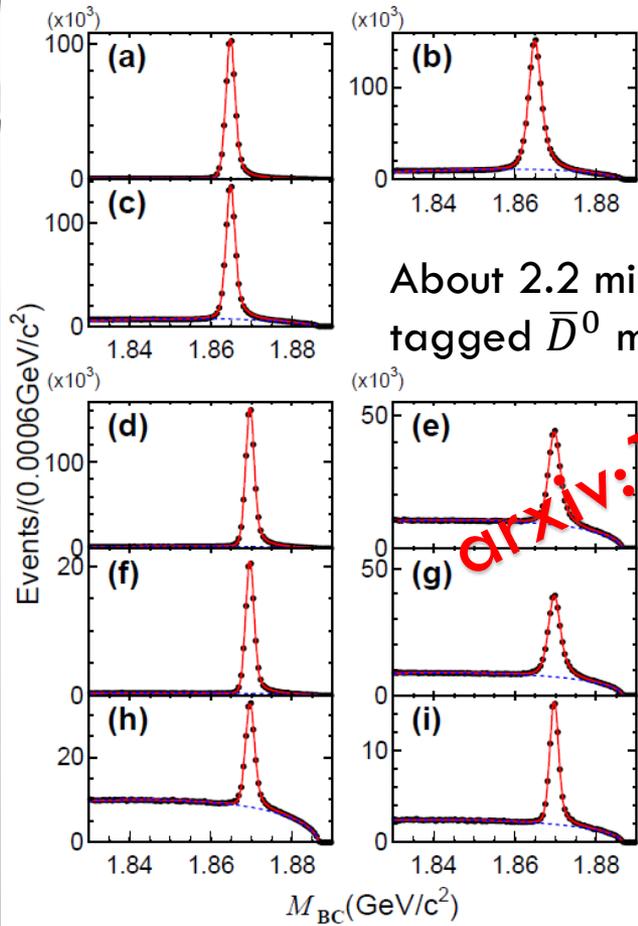
Rare Semileptonic Decay of D

$$D^{+(0)} \rightarrow a_0(980)^{0(-)} e^+ \nu_e$$

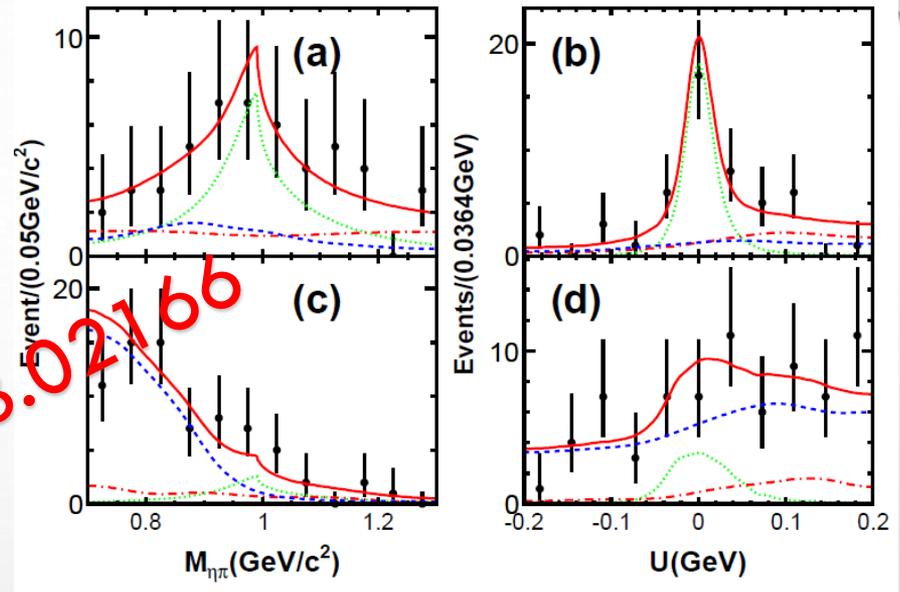
- Study of the nature of light scalar $a_0(980)$ and $f_0(980)$ is one of the central problems of nonperturbative QCD
- This study are important for understanding the way that chiral symmetry is realized in the low-energy region and confinement physics
- Explore the nontrivial internal structure of light hadron mesons, traditional $q\bar{q}$ states, tetra quark system
- Improve understanding of classification of light scalar mesons



$$R \equiv \frac{B(D^+ \rightarrow f_0 \ell^+ \nu) + B(D^+ \rightarrow \sigma \ell^+ \nu)}{B(D^+ \rightarrow a_0 \ell^+ \nu)}$$



About 2.2 million
tagged \bar{D}^0 mesons



$$5.4 \sigma B(D^0 \rightarrow a_0(980)^- e^+ \nu_e) \times B(a_0(980)^- \rightarrow \eta \pi^-) = (1.33_{-0.29}^{+0.33} \pm 0.09) \times 10^{-4}$$

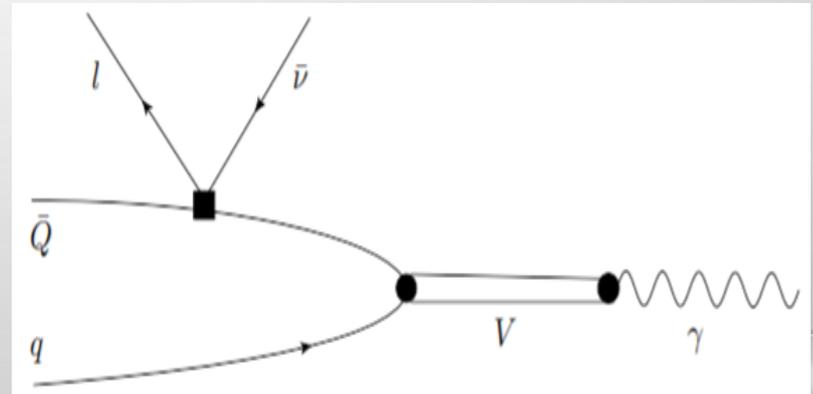
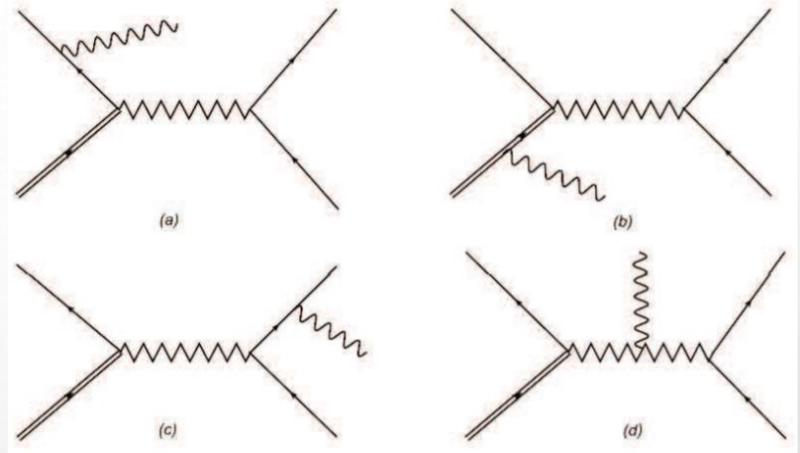
$$2.9 \sigma B(D^+ \rightarrow a_0(980)^0 e^+ \nu_e) \times B(a_0(980)^0 \rightarrow \eta \pi^0) = (1.66_{-0.66}^{+0.81} \pm 0.11) \times 10^{-4}$$

$$B(D^+ \rightarrow a_0(980)^0 e^+ \nu_e) \times B(a_0(980)^0 \rightarrow \eta \pi^0) < 3.0 \times 10^{-4}$$

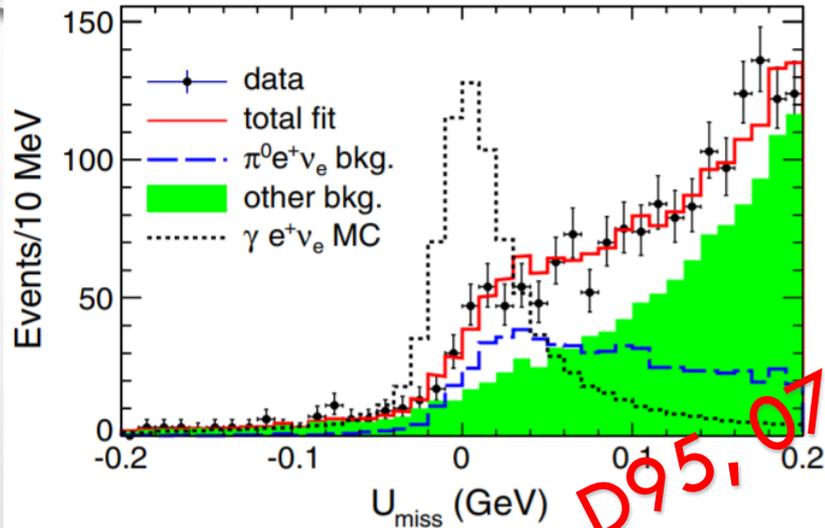
About 1.5 million
tagged D^- mesons

$$D^+ \rightarrow \gamma e^+ \nu_e$$

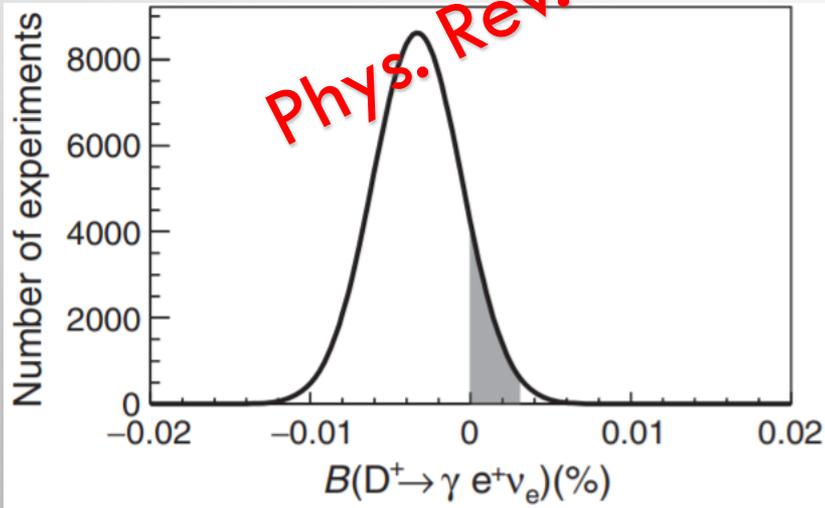
- Not subject to the helicity suppression rule due to the presence of a radiative photon.
- Nonperturbative strong interaction effects in theoretical calculations is relatively simple without final-state hadron
- Long-distance contribution is considered via the vector meson dominance model and the decay rate may be enhanced significantly



$$D^+ \rightarrow \gamma e^+ \nu_e$$



Source	Relative uncertainty (%)
Signal MC model	3.5
e^+ tracking	0.5
e^+ PID	0.5
γ reconstruction	1.0
Lateral moment	4.4
$\pi^0 e^+ \nu_e$ backgrounds	2.7 ^a

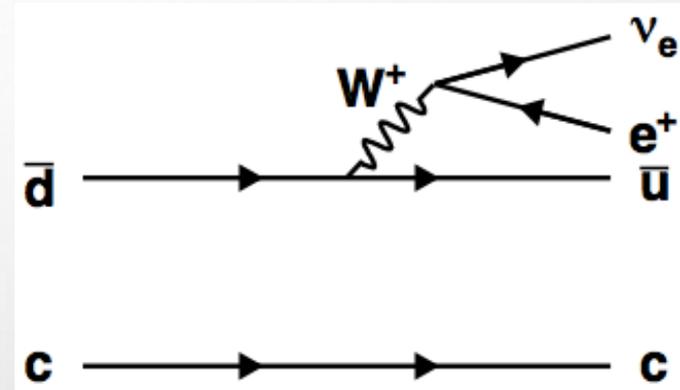


$B(D^+ \rightarrow \gamma e^+ \nu_e) < 3.0 \times 10^{-5}$ @ 90% C.L..

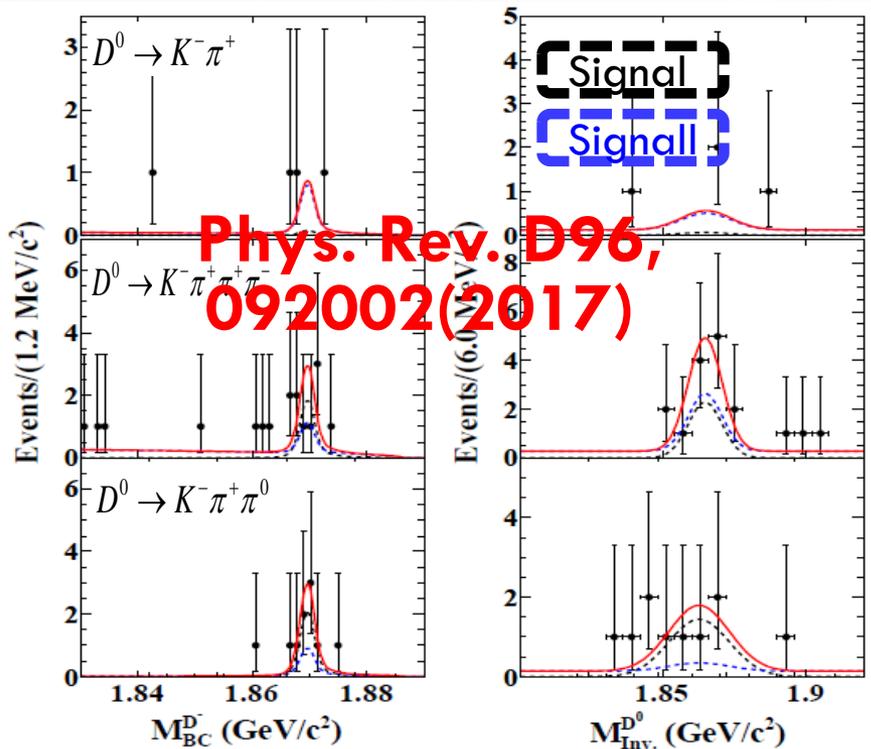
Approach to the factorization method prediction: 1.92×10^{-5} (Nucl. Phys. B914, 301 (2017).)

$$D^+ \rightarrow D^0 e^+ \nu_e$$

- In the rare decay processes of $D^+ \rightarrow D^0 e^+ \nu_e$, the heavy-quark flavors (c) remain unchanged, and the weak decays are managed by the light-quark sectors.
- Applying the SU(3) symmetry for the light quarks, this rare decay branching fraction can be predicted by theoretical calculation and its theoretical value is 2.78×10^{-13} [EPJC, 59:841-845(2009)].
- Measuring this decay may share light on testing the SM predictions for the rare semileptonic decays.



$$D^+ \rightarrow D^0 e^+ \nu_e$$



Source	$D^0 \rightarrow K^- \pi^+$	$D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$	$D^0 \rightarrow K^- \pi^+ \pi^0$
Tracking	2.0	4.0	2.0
PID	2.0	4.0	2.0
Quoted branching fraction	1.3	2.6	3.6
π^0 reconstruction	-	-	2.0
Summation of Signal side	3.1	6.2	5.0
Signal side		3.8	
Background estimation		11.5	
MC statistics		0.5	
M_{BC} fit (ST)		0.5	
Probability requirement		2.6	
2D fit		2.9	
Total		12.7	

Two dimensional fit

$$B(D^+ \rightarrow D^0 e^+ \nu_e) < 1.0 \times 10^{-4} @ 90\% \text{C.L.}$$

Summary

- With $2.93, 3.19 \text{ fb}^{-1}$ data taken at $3.773, 4.178 \text{ GeV}$, BESIII have studied dynamics of $D_s^+ \rightarrow \eta^{(\prime)} e^+ \nu_e$, and search for $D^{+(0)} \rightarrow a^0(980)^{0(-)} e^+ \nu_e, \gamma e^+ \nu_e$ and $D^0 e^+ \nu_e$
- First measurement of form factor $f_+^{\eta^{(\prime)}}(0)$ helps to tune the LQCD calculation
- Determination of quark mixing matrix element $|V_{cs}|$ and $\eta - \eta'$ mixing angle ϕ_P provide complementary result
- First measurement of branching fraction $B(D^{+(0)} \rightarrow a^0(980)^{0(-)} e^+ \nu_e)$ opens one more interest page in investigation of the nature of puzzling $a^0(980)$ states.