

# Jet substructure in heavy-ion collisions

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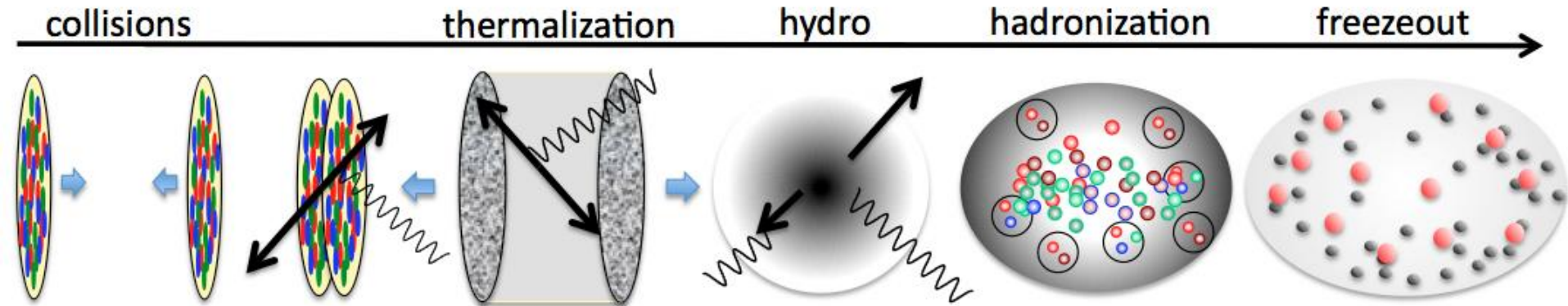
*In collaboration with  
Shanshan Cao, Yayun He, Guang-You Qin and Xin-Nian Wang*

# Outline

- Introduction
- A Linear Boltzmann Transport (LBT) model
- Jet modification in heavy ion collisions
- Summary and Outlook

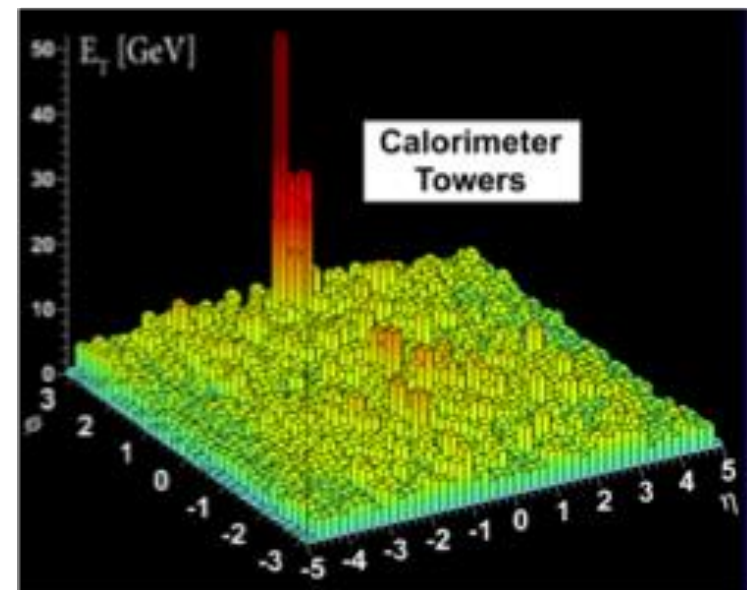
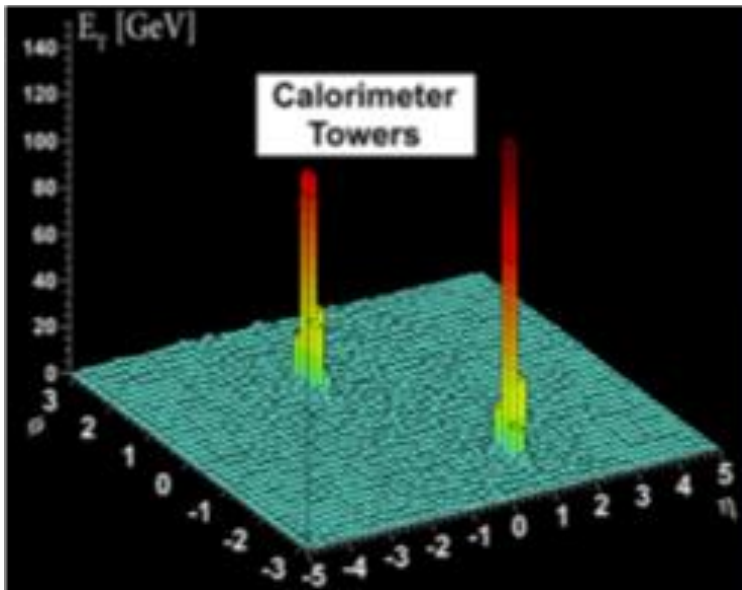
# Introduction

## Jets in heavy ion collisions



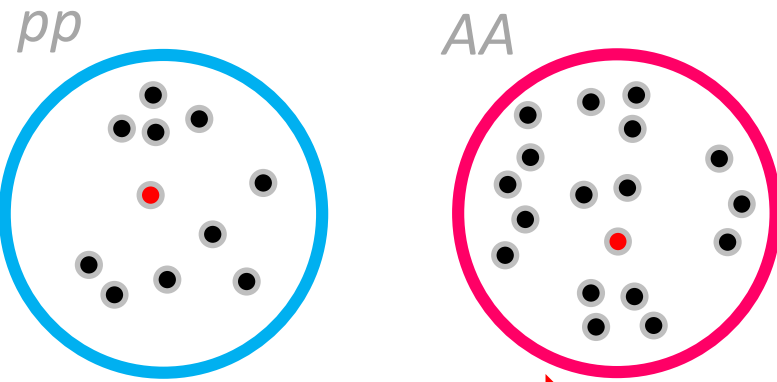
Nonaka, Chihoe et al. PTEP 2012 (2012) 01A208

*What are in the background of a reconstructed jet?*

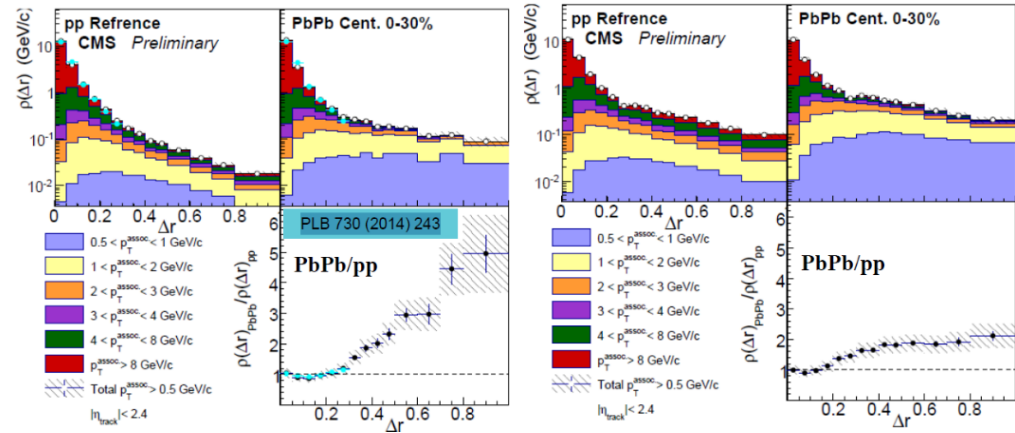


# Introduction

## The jet shape and transverse momentum imbalance in *Dijet* events



**Medium modification of the jet structure**

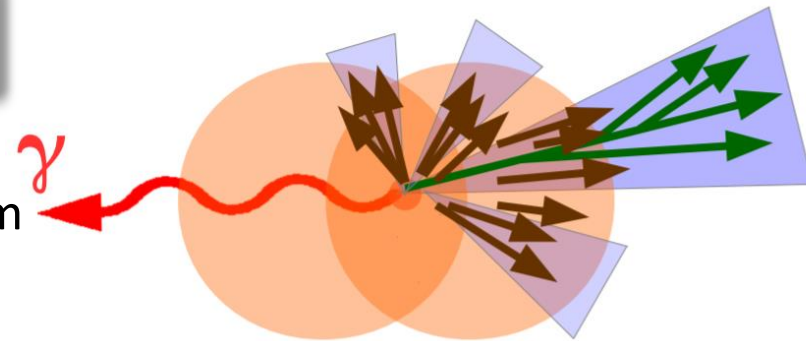


arXiv:1609.02466 CMS

**Gamma-jet** → *The golden channel*

XN Wang, Z Huang Phys. Rev. Lett. 77, 231 (1996)

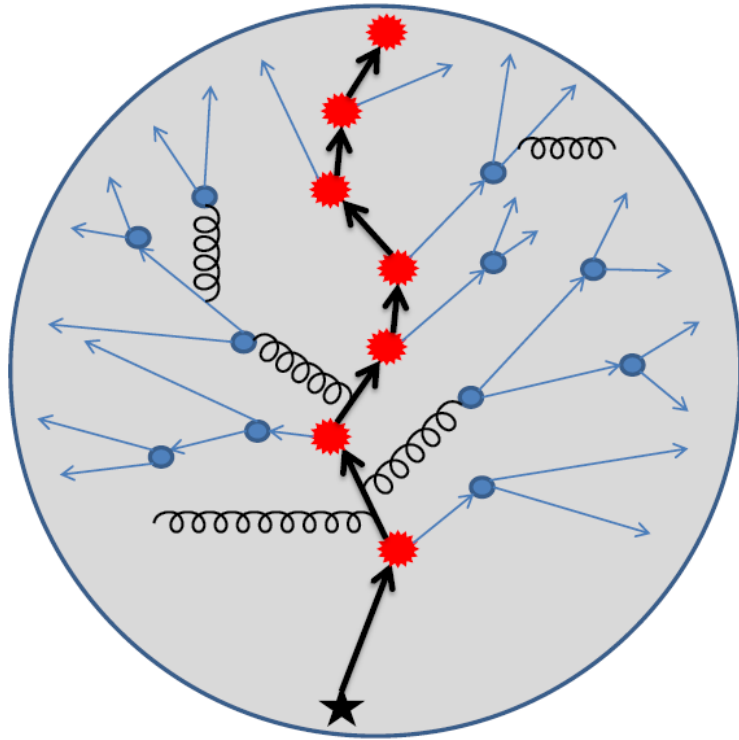
- High  $p_T$  photons are unmodified by the medium
- No “surface bias” in triggered events which dijet events suffer



Kaya Tatar

# A Linear Boltzmann Transport (LBT) Model

$$p_1 \cdot \partial f_1(x_1, p_1) = E_1 (C_{elastic} + C_{inelastic})$$



Jet induced medium excitation

## Linear Approximation

It works when the jet induced medium excitation  $\delta f \ll f$ .

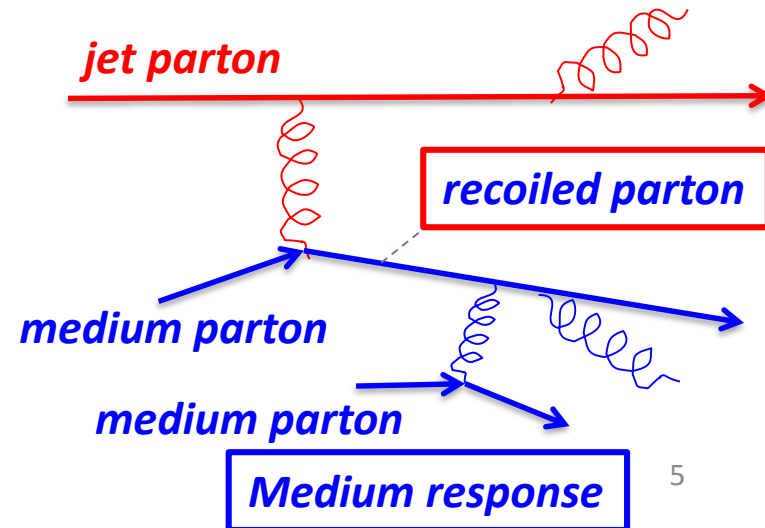
## Linear Boltzmann jet Transport

Elastic collision + Induced gluon radiation.

Follow the propagation of recoiled parton.

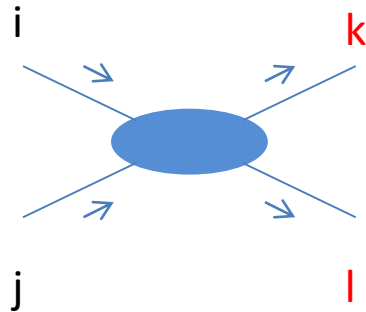
Back reaction of the Boltzmann transport.

("Negative" parton for the **back reaction**)



# Complete set of elastic processes

## Single scattering



$i, j = g, u, d, s, c, b, \bar{u}, \bar{d}, \bar{s}, \bar{c}, \bar{b}$

Jussi Auvinen, Kari J. Eskola, Thorsten Renk

Phys.Rev. C82 024906

- Scattering rate for a process  $ij \rightarrow kl$  in the local rest frame of the fluid

$$\Gamma_{ij \rightarrow kl} = \frac{1}{2E_1} \int \frac{d^3 p_2}{(2\pi)^3 2E_2} \int \frac{d^3 p_3}{(2\pi)^3 2E_3} \int \frac{d^3 p_4}{(2\pi)^3 2E_4} \times f_j(p_2 \cdot u, T)$$

$$\times |M|_{ij \rightarrow kl}^2(s, t, u) \times S_2(s, t, u) \times (2\pi)^4 \delta^4(P_1 + P_2 - P_3 - P_4)$$

$$S_2(s, t, u) = \theta(s \geq 2\mu_D^2) \theta(-s + \mu_D^2 \leq t \leq -\mu_D^2) \quad \mu_D^2 = \left(\frac{3}{2}\right) 4\pi\alpha_s T^2$$

- The mean free path

$$\Gamma_i = \sum_{j,(kl)} \Gamma_{ij \rightarrow kl} = 1/\lambda_0$$

$$P(\Delta t) = 1 - e^{-\Gamma_i \Delta t}$$

$$P(ij \rightarrow kl) = \frac{\Gamma_{ij \rightarrow kl}}{\Gamma_i}$$

# Medium-induced gluon radiations

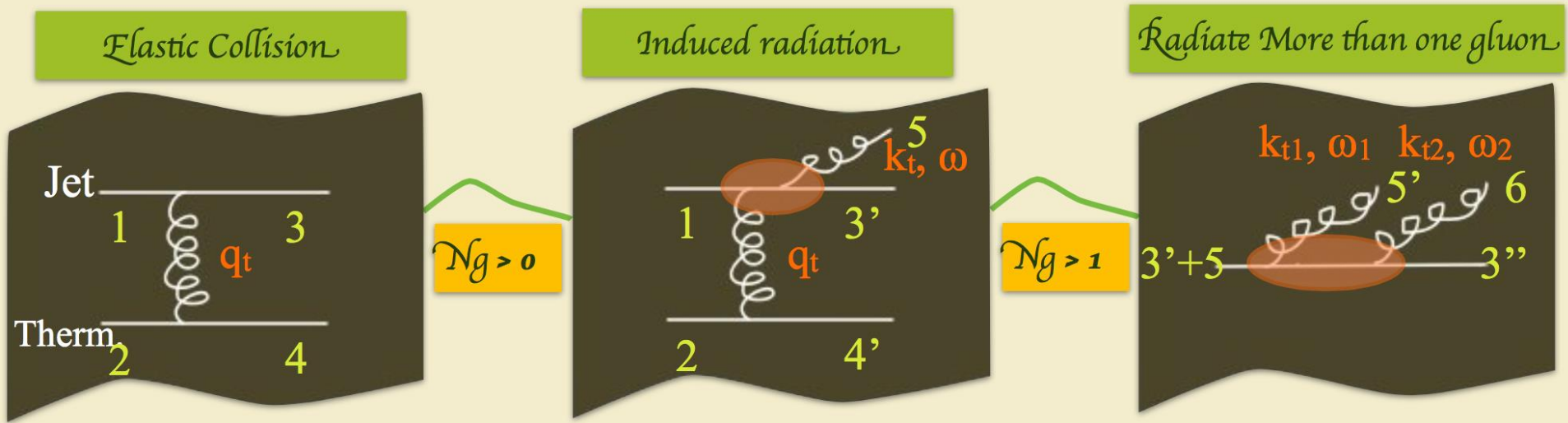
**Radiated gluon distribution:** Guo and Wang (2000), Majumder (2012); Zhang, Wang and Wang (2004)

$$\frac{dN_g}{dx dk_{\perp}^2 dt} = \frac{2C_A \alpha_s P(x) k_{\perp}^4}{\pi(k_{\perp}^2 + x^2 M^2)^4} \hat{q} \sin^2 \frac{t-t_i}{2\tau_f} \quad \tau_f = 2Ex(1-x) / (k_{\perp}^2 + x^2 M^2)$$

**Multiple gluon emissions:** 
$$P(N_g, \langle N_g \rangle) = \frac{\langle N_g \rangle^{N_g} e^{-\langle N_g \rangle}}{N_g!}$$

**Induced radiations are accompanied by elastic collisions.**

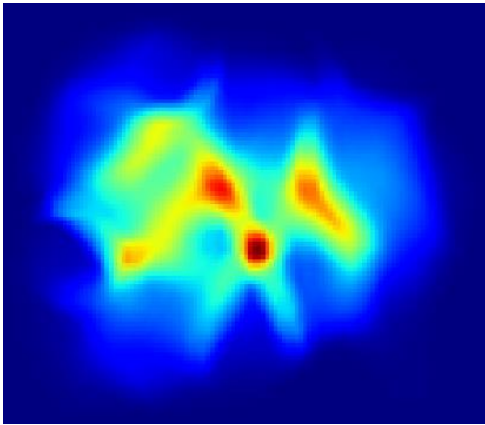
## Jet medium Interaction:



# Jets in a 3+1D hydro

Initial jet shower partons from a p+p collision (Pythia or Hijing)

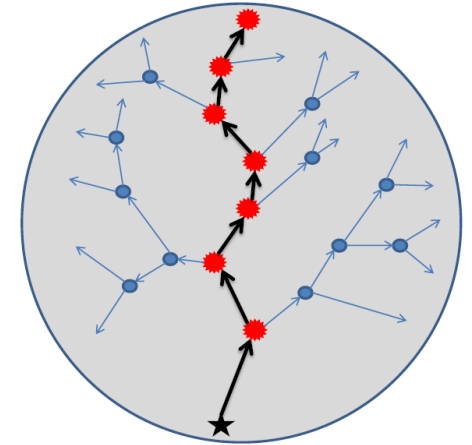
- 3+1D Ideal hydro



$\epsilon T u$

LBT Model

- Location of jets are decided according probability of binary collision.



L-G. Pang, Q. Wang, X-N. Wang  
Phys.Rev. C86 (2012) 024911

M. Cacciari, G. P. Salam and G. Soyez  
Eur. Phys. J. C 72, 1896 (2012).

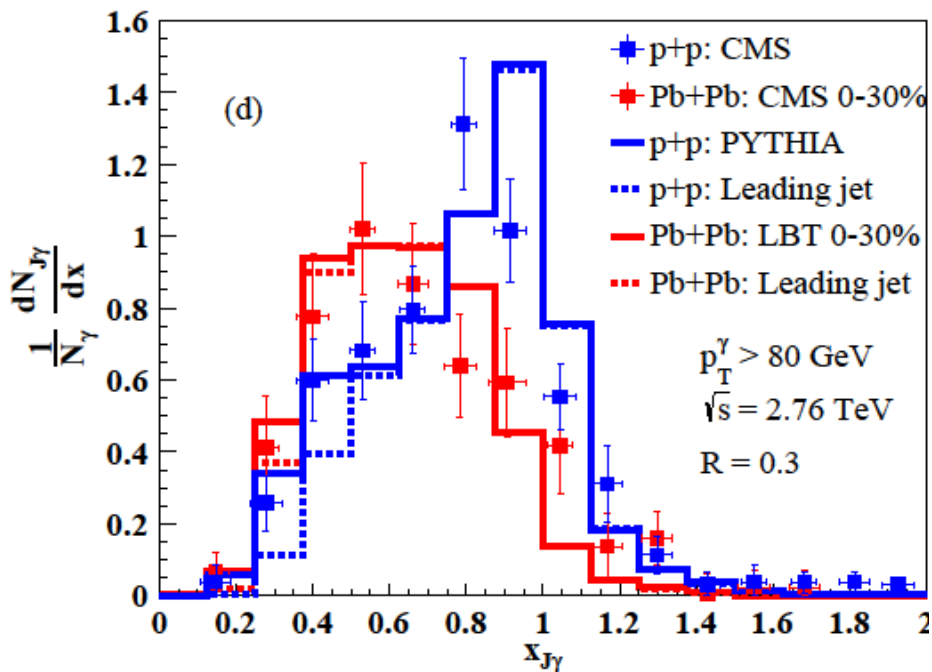
Jet reconstruction (Fastjet)



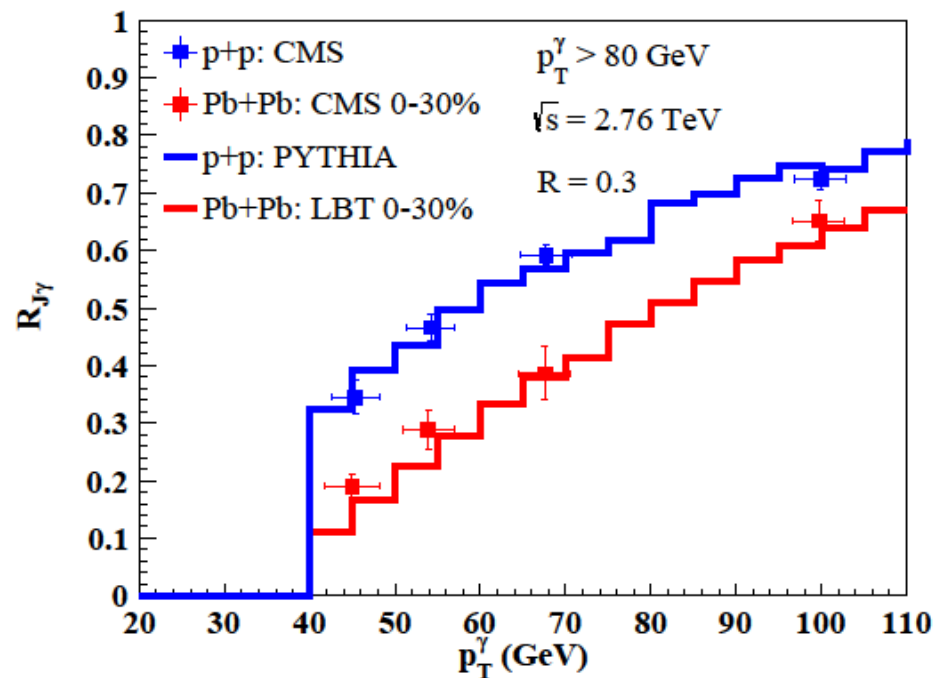
# Gamma-jet energy loss

**Gamma-jet** Luo, Cao, He & XNW, arXiv:1803.06785

- The only parameter effective strong coupling constant  $\alpha_s$  is fixed. (fix the strength of jet-medium interaction)



gamma-jet asymmetry

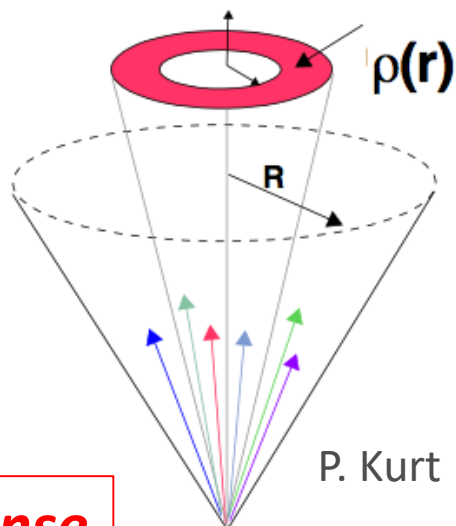


gamma-jet ratio

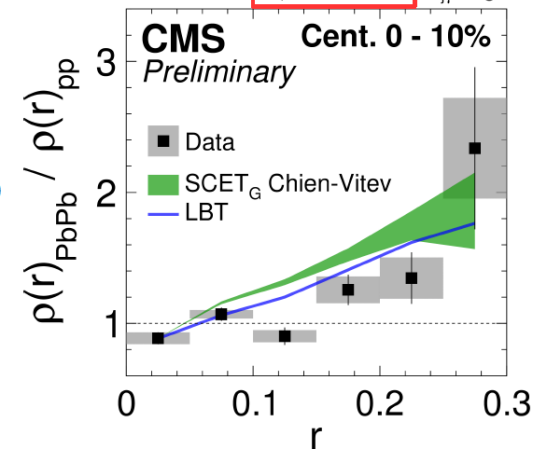
# Jet shape of gamma-jet in heavy-ion collisions

## Jet shape

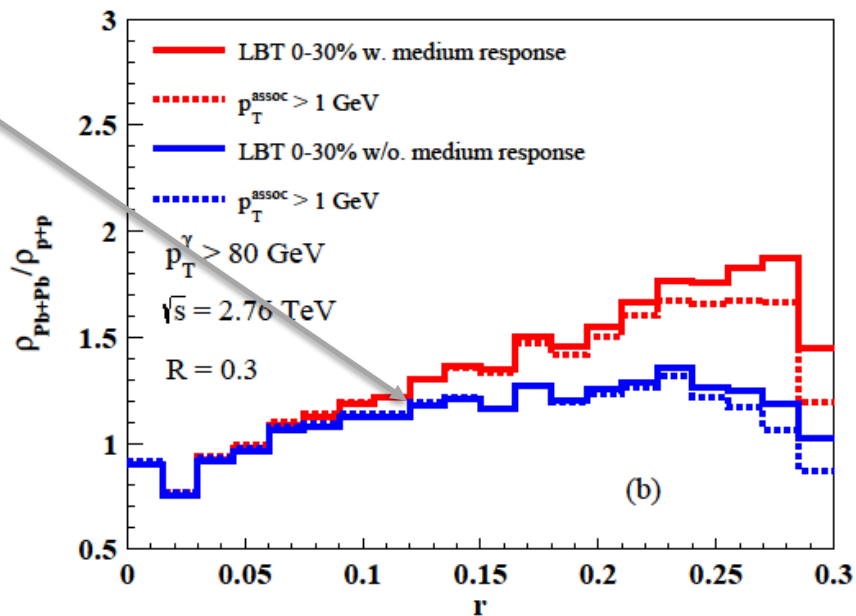
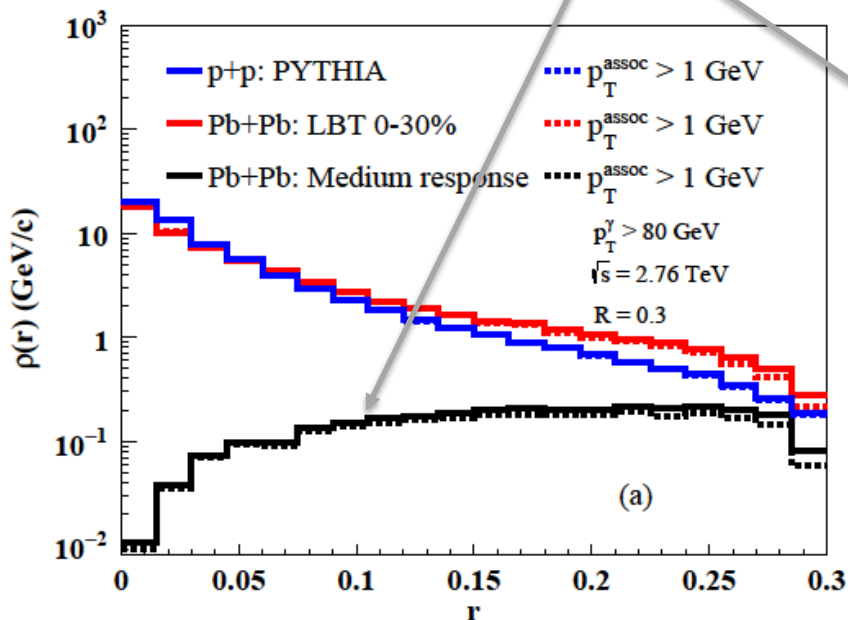
$$\rho(r) = \frac{1}{\Delta r} \frac{1}{N_{jet}} \sum_{jets} \frac{p_t(r - \frac{\Delta r}{2}, r + \frac{\Delta r}{2})}{p_t(0, R)}$$



$\sqrt{s_{NN}} = 5.02 \text{ TeV}$   $p_T^\gamma > 60 \text{ GeV}/c$   
 PbPb  $404 \mu\text{b}^{-1}$  anti- $k_T$  jet  $R = 0.3$   
 pp  $27.4 \text{ pb}^{-1}$   $p_T^{jet} > 30 \text{ GeV}/c, \Delta\phi_{j\gamma} > \frac{7\pi}{8}$

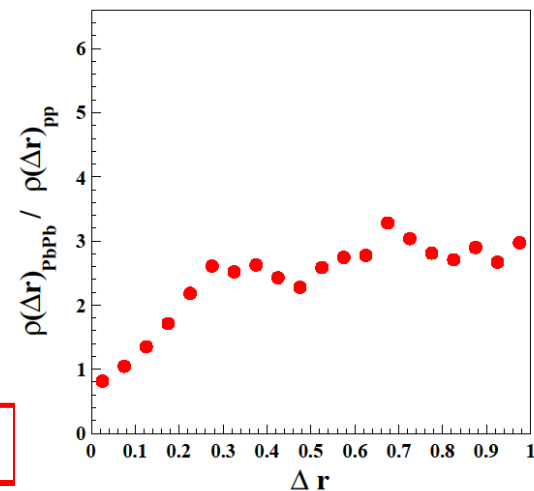
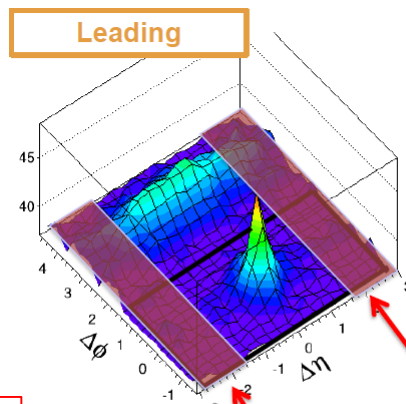


**Medium response**



# Jet shape of gamma-jet in heavy-ion collisions

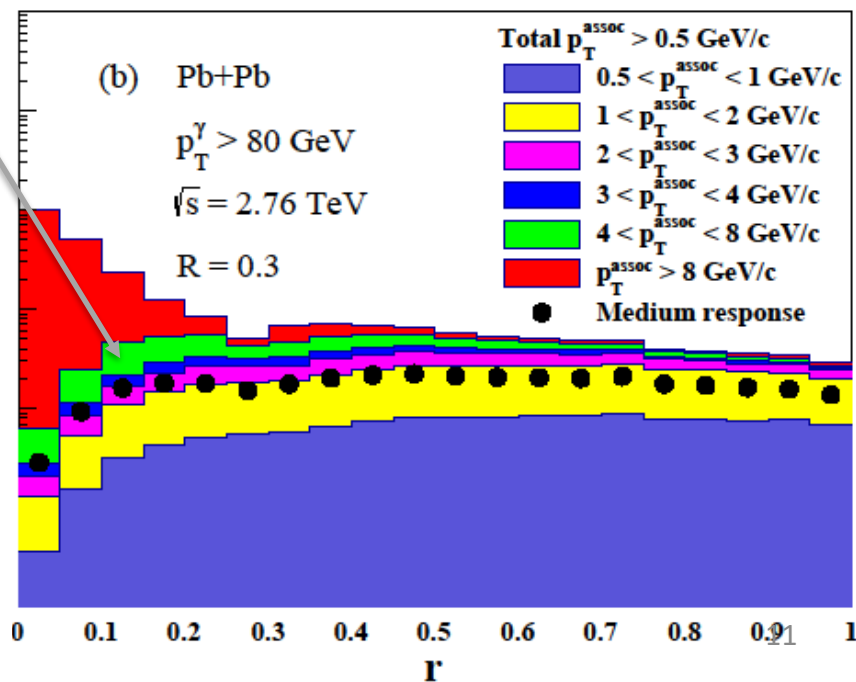
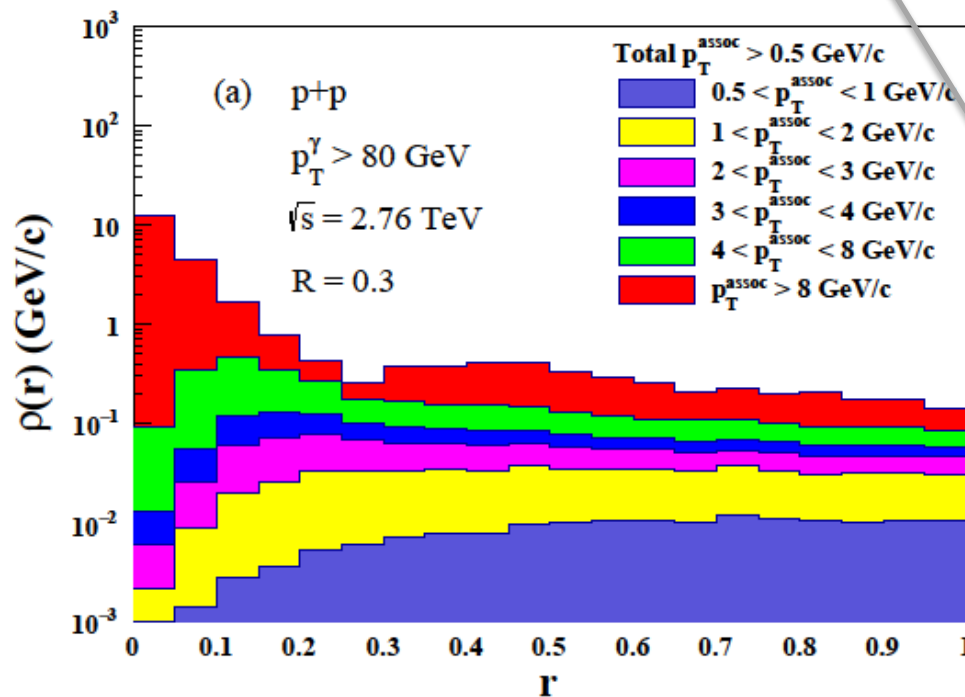
- Energy lost by the hard parton is transport out of the jet cone by the soft parton.



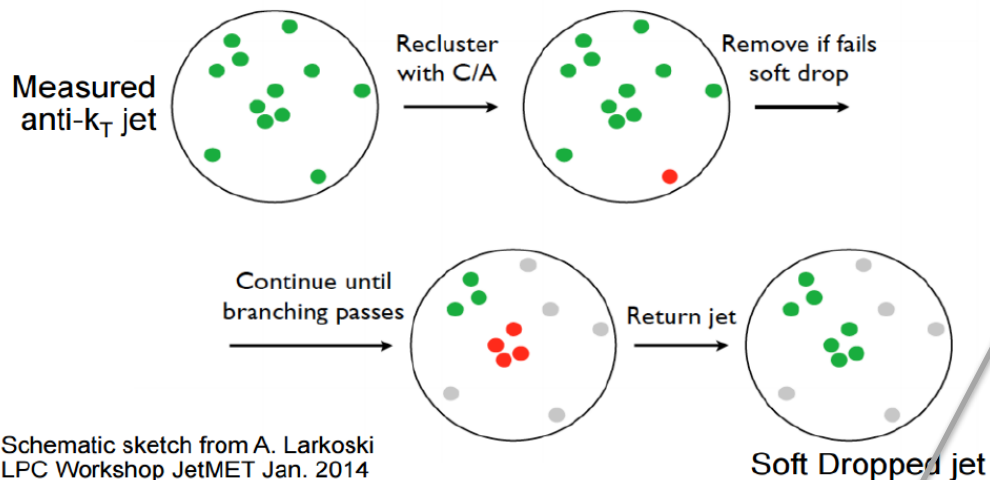
**Medium response**

“Sideband” region  
 $1.5 < |\Delta\eta| < 2.5$

Luo, Cao, He & XNW, arXiv:1803.06785



# Jet substructure (jet grooming)

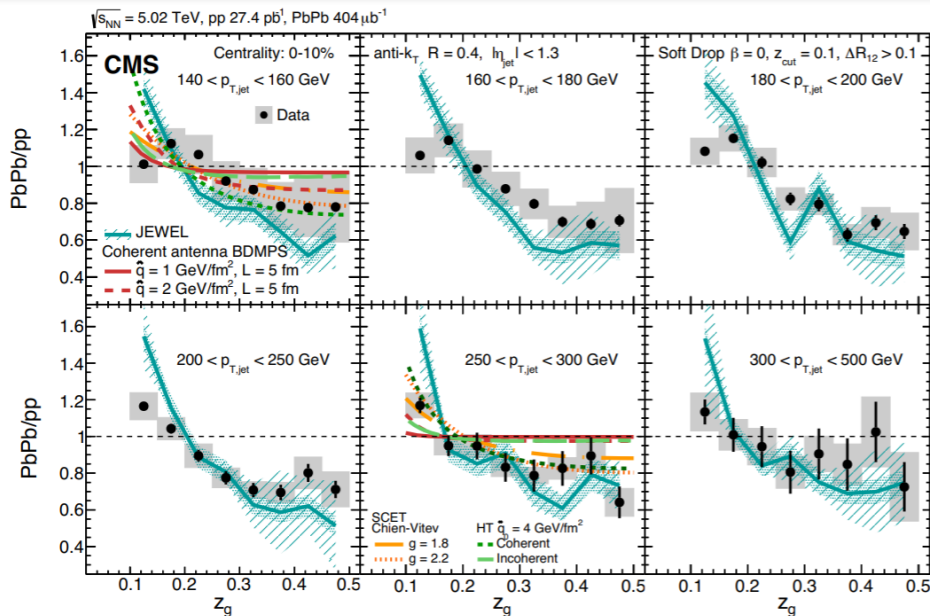


$$z_g \equiv \frac{\min(p_{T1}, p_{T2})}{p_{T1} + p_{T2}} > z_{cut} \left(\frac{\Delta R}{R_0}\right)^\beta$$

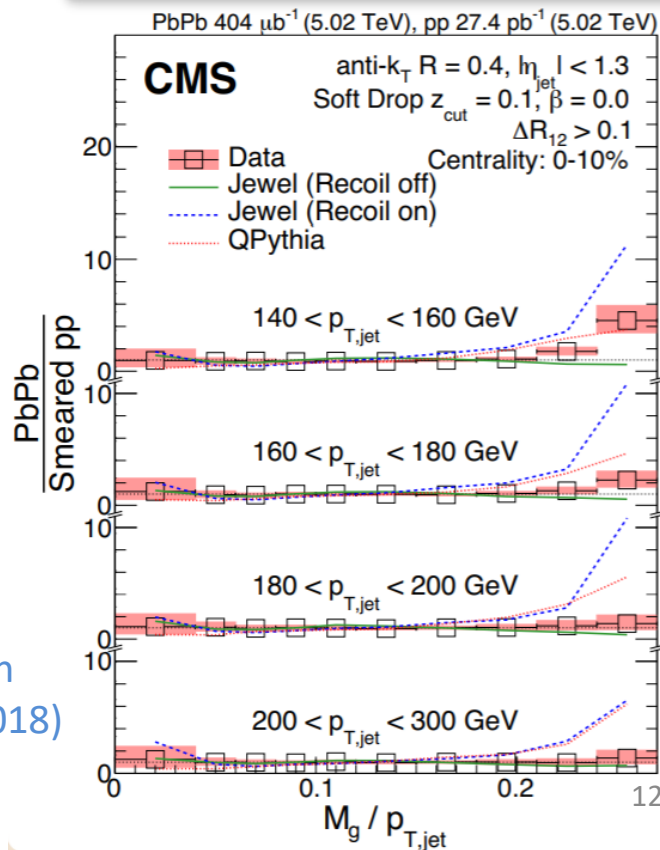
$$\frac{M_g}{p_T^{jet}} = \frac{\sqrt{(E_1 + E_2)^2 - (\vec{p}_1 + \vec{p}_2)^2}}{p_T^{jet}}$$

Groomed jet mass

Groomed Jet splitting function



Yi Chen  
(QM2018)

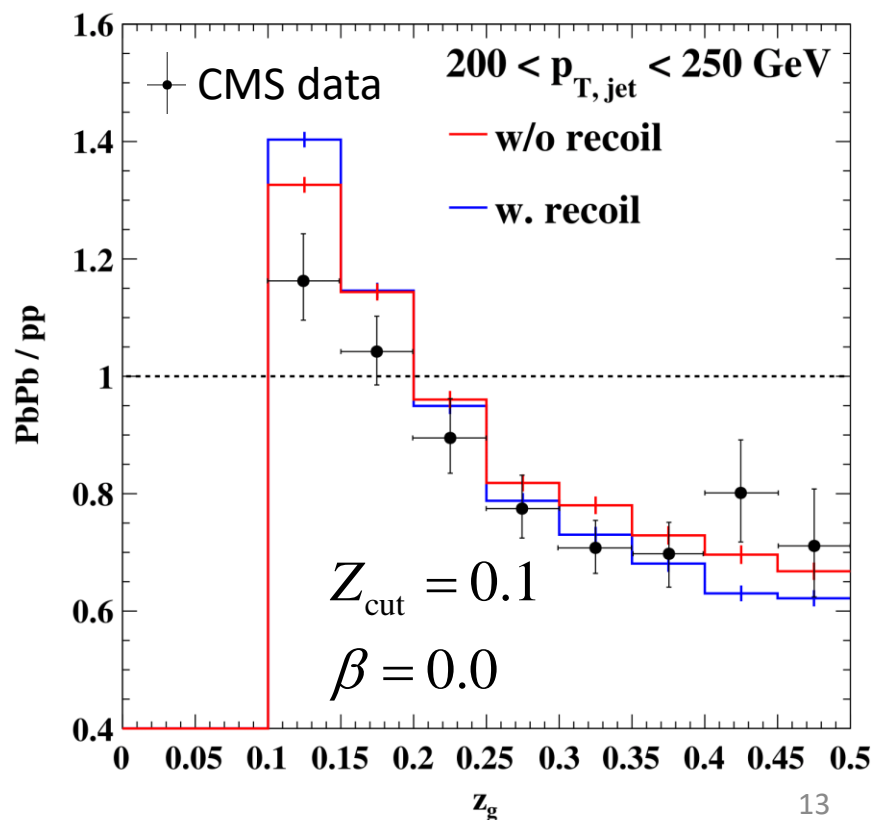
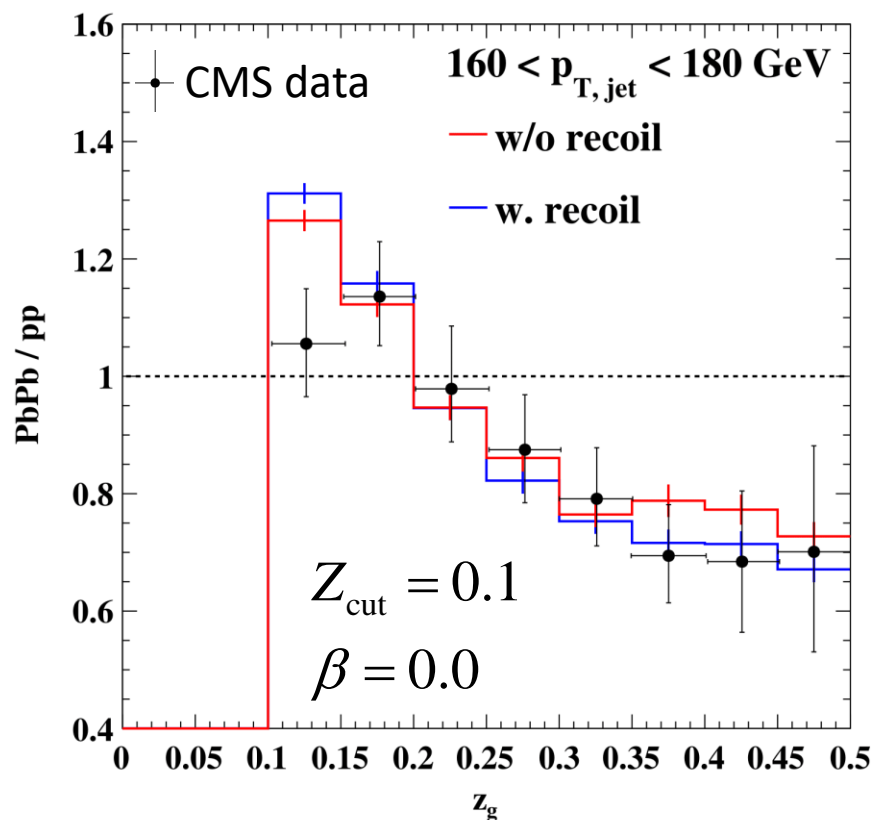


# Groomed jet splitting function

- The inclusion of the recoil (medium response) will lead to stronger modification of the groomed jet splitting function.

preliminary

$$z_g = \frac{\min(p_{T1}, p_{T2})}{p_{T1} + p_{T2}}$$

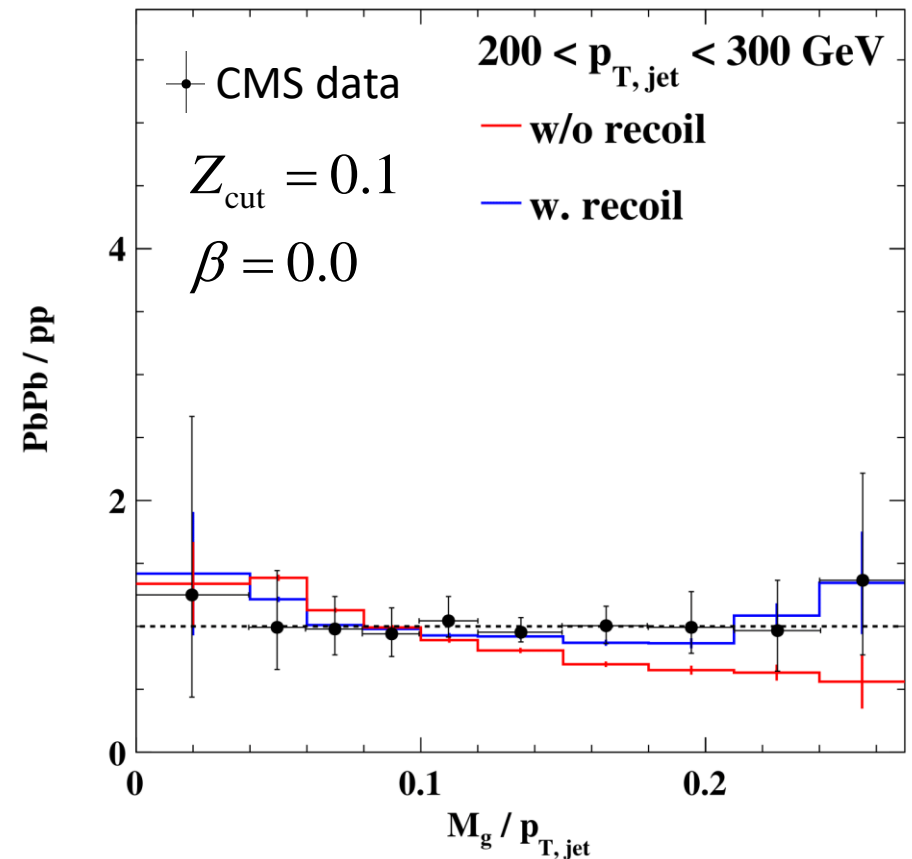
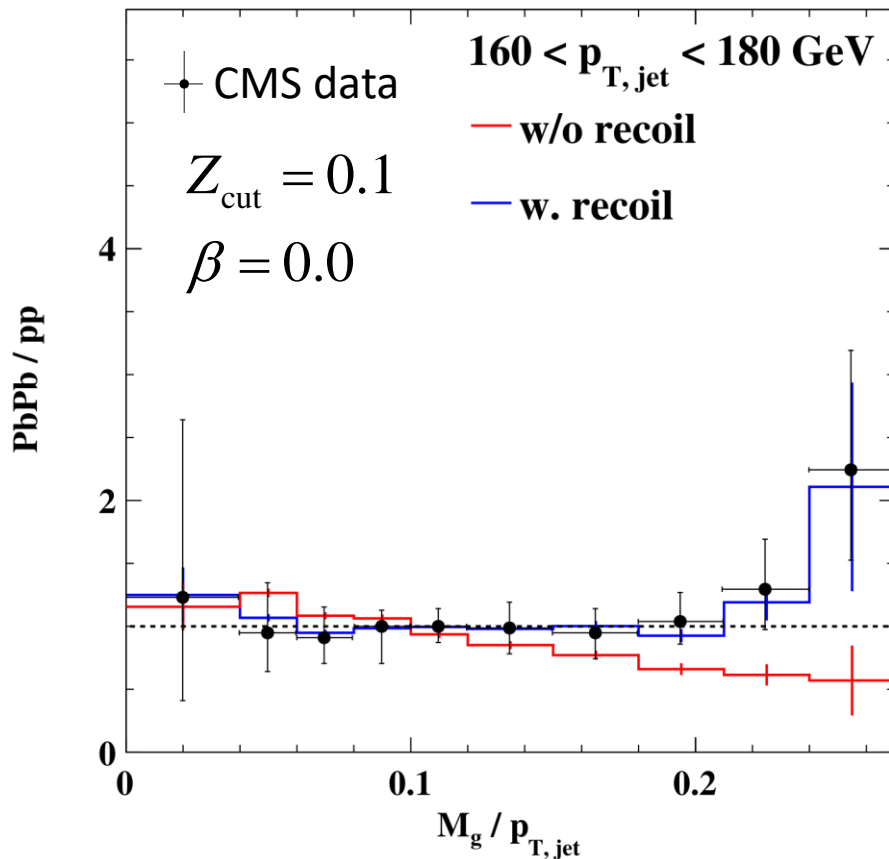


# Groomed jet mass

- The inclusion of recoiled partons will lead to the enhancement of the large groomed mass tail.

preliminary

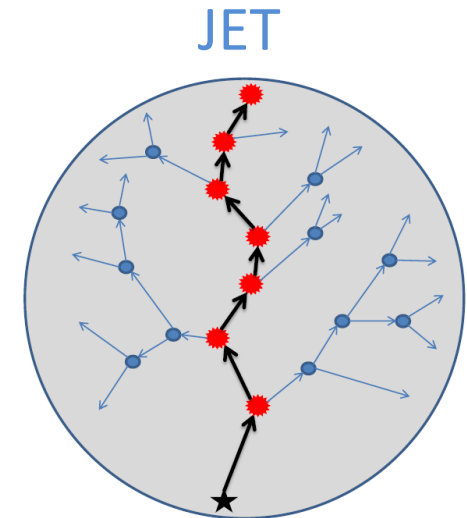
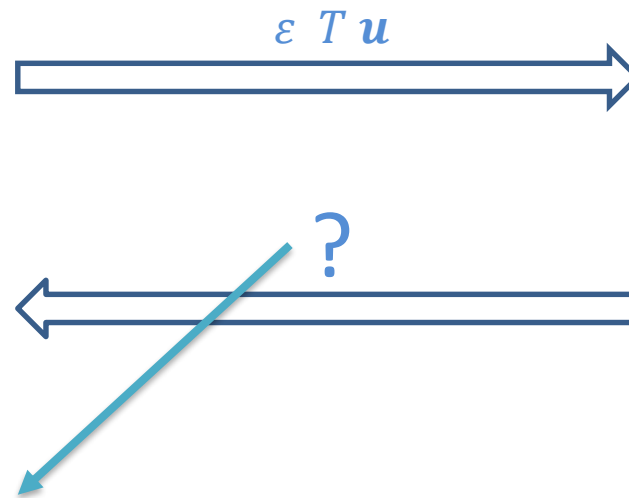
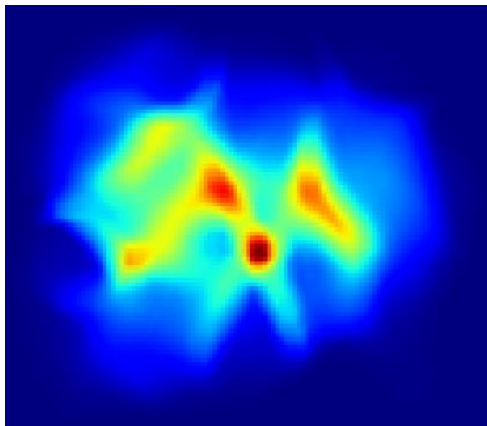
$$\frac{M_g}{p_T^{jet}} = \frac{\sqrt{(E_1 + E_2)^2 - (\vec{p}_1 + \vec{p}_2)^2}}{p_T^{jet}}$$



# Beyond LBT model (modified medium background)

- Linear approximation : jet induced medium excitation  $\delta f \ll f$ .
- Jet-Medium interaction : Where is the modification of the thermal background ?

## Modified medium background



Energy and momentum deposited from the jets as source terms into hydro

**Phys.Lett. B777 (2018) 86-90** W Chen, SS Cao, T Luo, LG Pang, XN Wang

# CoLBT-hydro

(A coupled LBT Hydro (3+1D) Model)

# Summary

- We present a computation of jets modification in QGP within the Linear Boltzmann Transport (**LBT**) model in which both the elastic and inelastic processes are included.
- We find it is crucial to include medium response to describe the modification of jet structure in heavy ion collisions.

# Outlook

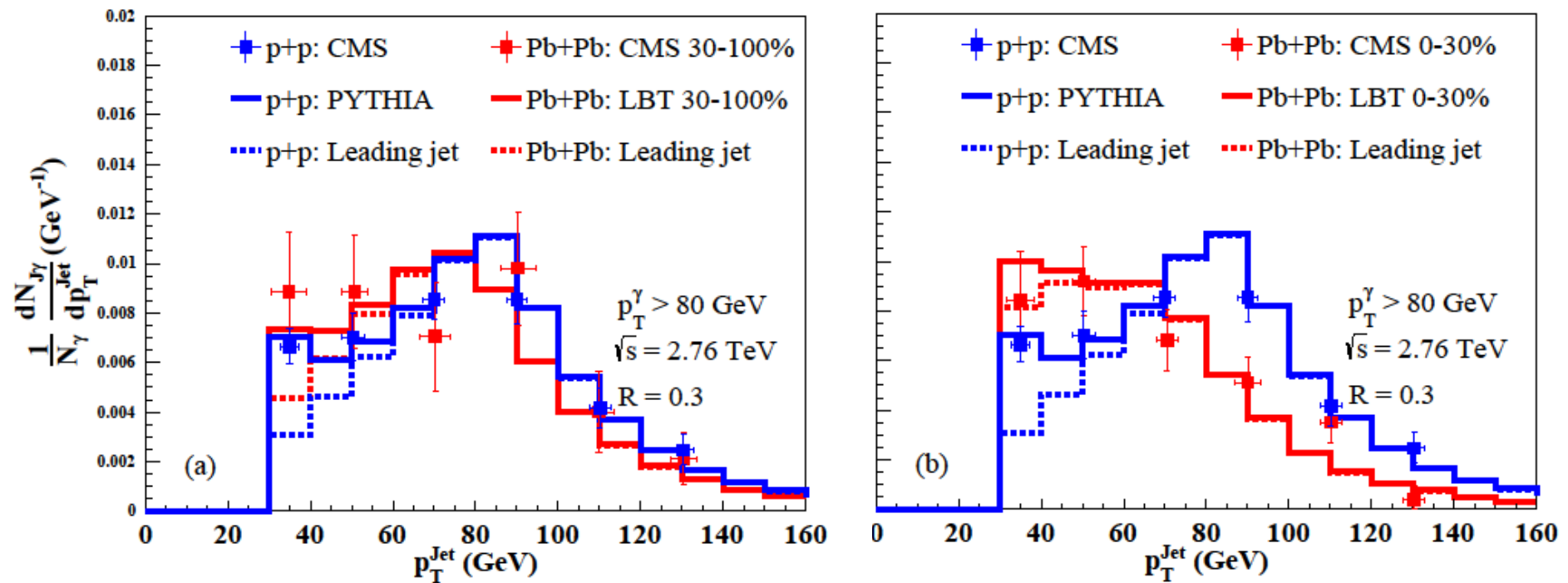
- *Jet in hadron level. (Hardon jet, Heavy flavor jet)  
(with the **recombination model** developed by Texas A&M group)*
- *Heavy quarkonium.*
- *JETSCAPE*



*Thanks*

# $p_T$ distribution of gamma-jet in heavy-ion collisions

- Shift of the peak of the  $p_T$  distribution
- Path length dependence of the energy loss



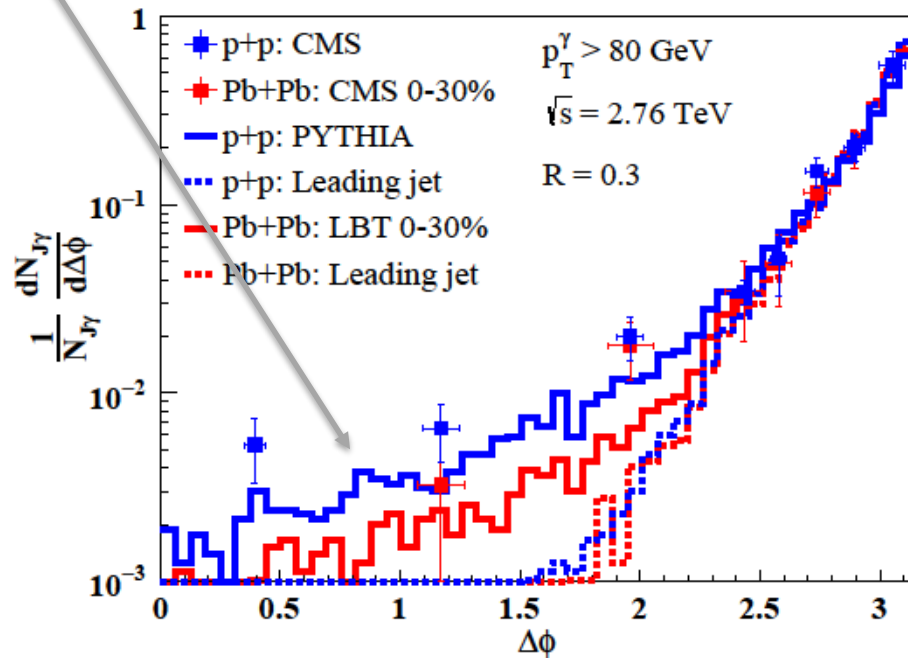
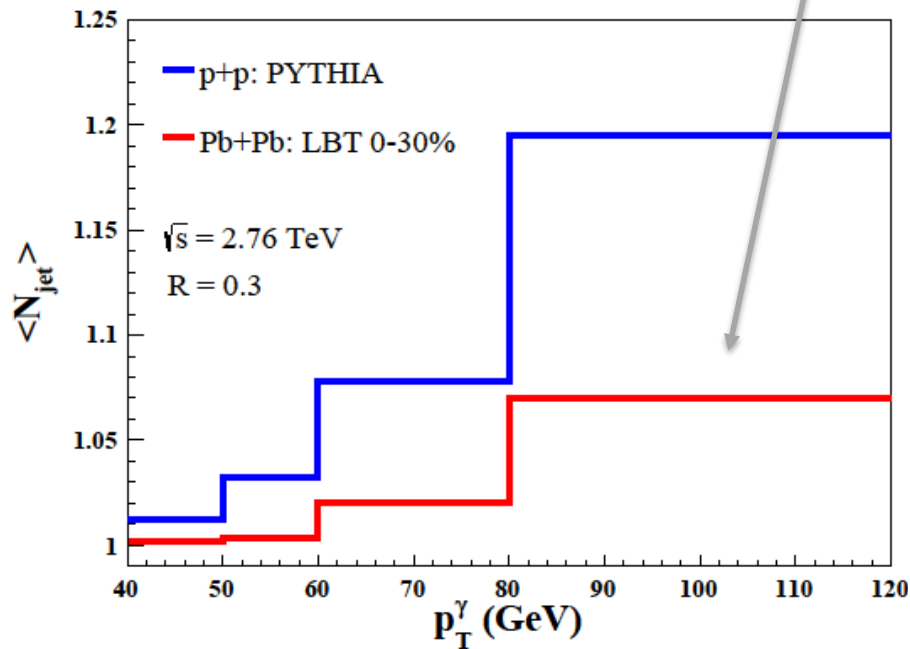
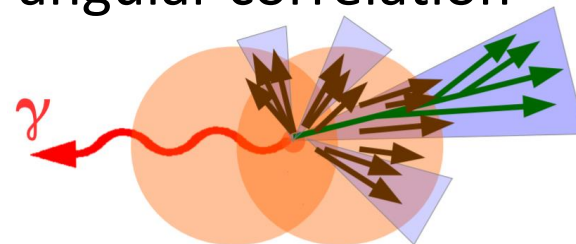
# Azimuthal distribution of gamma-jet in heavy-ion collisions

- Dominance of the initial state radiation in angular correlation

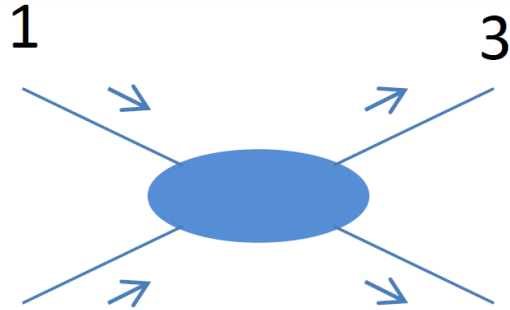
L Chen, GY Qin, SY Wei, BW Xiao, HZ Zhang [arXiv:1607.01932](#)

A. H. Mueller, B Wu, BW Xiao, F Yuan [arXiv:1604.04250](#)

- Multiple jets in gamma-jets events



# Energy distribution of the recoiled parton



## Single scattering

Dominance of small angle scattering.

Switch of flavor and species of the leading parton.



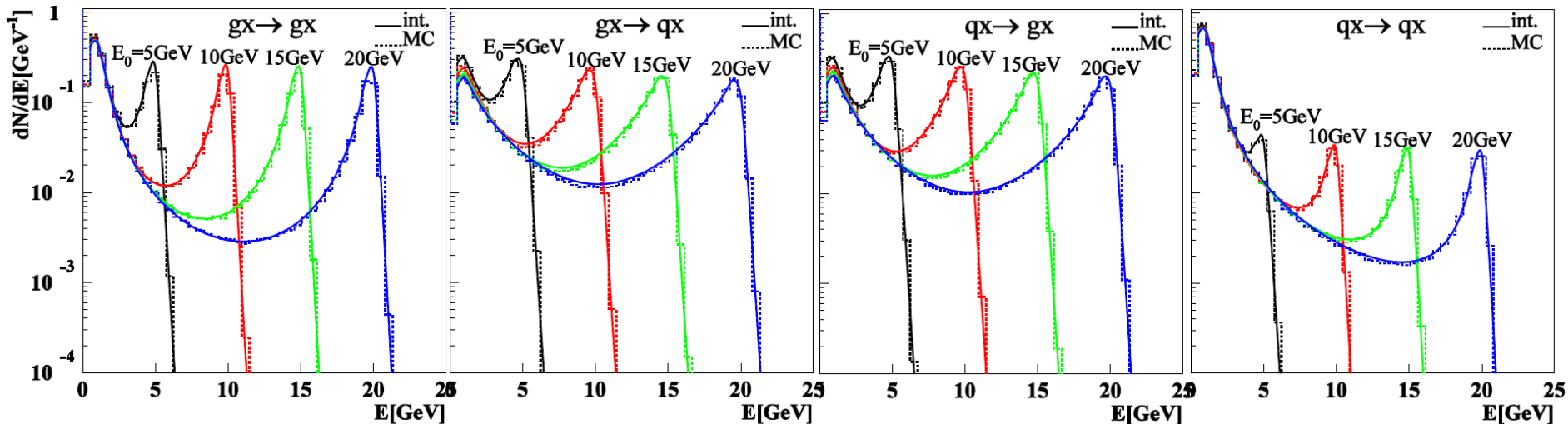
$$gg \rightarrow gg$$

$$gq \rightarrow gq + g\bar{q} \rightarrow g\bar{q}$$

$$gg \rightarrow q\bar{q}$$

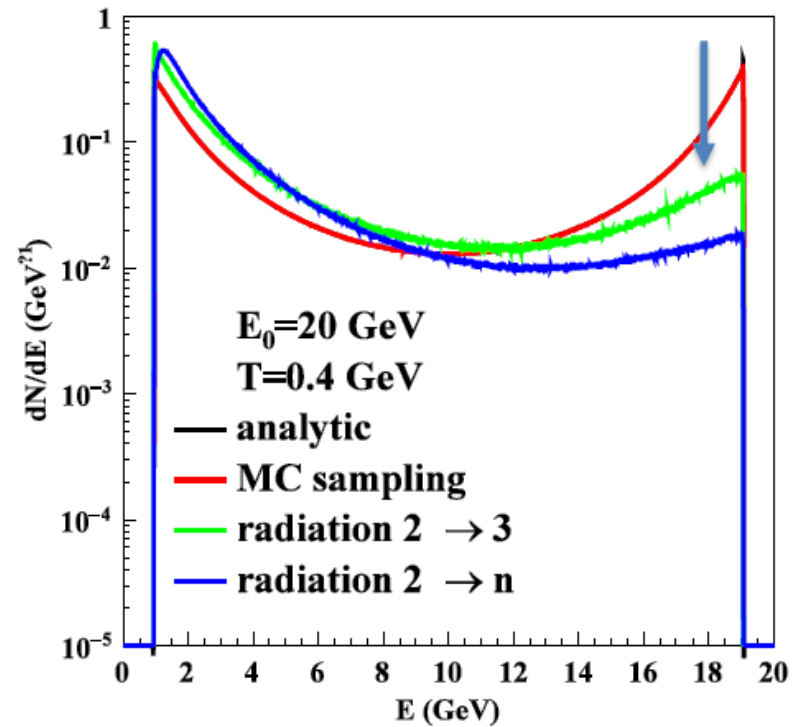
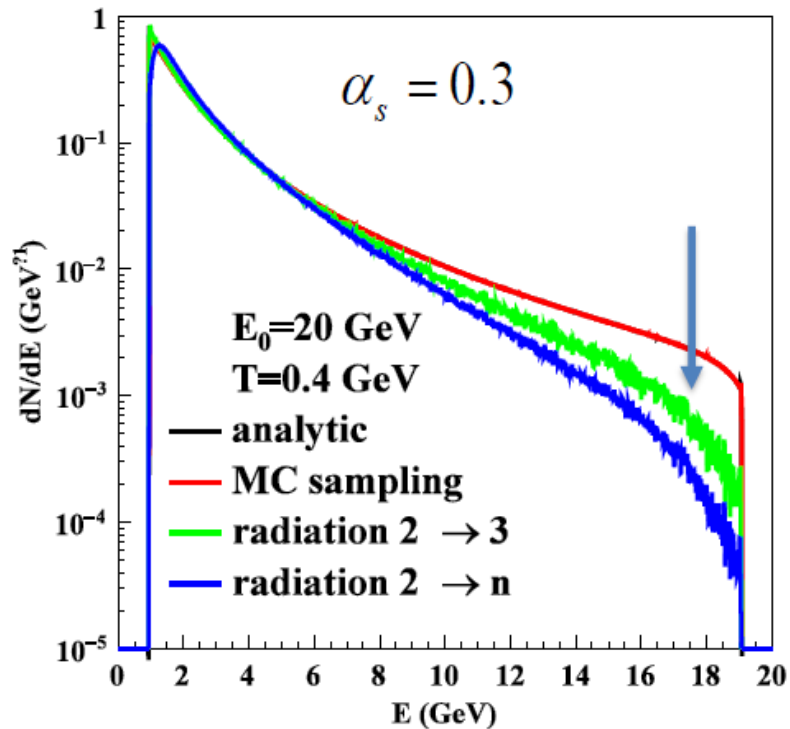
$$q_i \bar{q}_i \rightarrow gg$$

$$\begin{array}{ll} q_i \bar{q}_i \rightarrow q_j \bar{q}_j & q_i g \rightarrow q_i g \\ q_i \bar{q}_i \rightarrow q_i \bar{q}_i & q_i q_j \rightarrow q_i q_j \\ & q_i \bar{q}_i \rightarrow q_i \bar{q}_i \end{array}$$



# Energy distribution of the radiated gluon

Global energy-momentum conservation in 2->3 and 2->n processes



$$P_{q \rightarrow qg}(x) = \frac{(1-x)(1+(1-x)^2)}{x}$$

$$P_{g \rightarrow gg}(x) = \frac{2(1-x+x^2)^3}{x(1-x)}$$

# Jet induced medium excitation (Energy distribution in space)

Initial jet parton: gluon

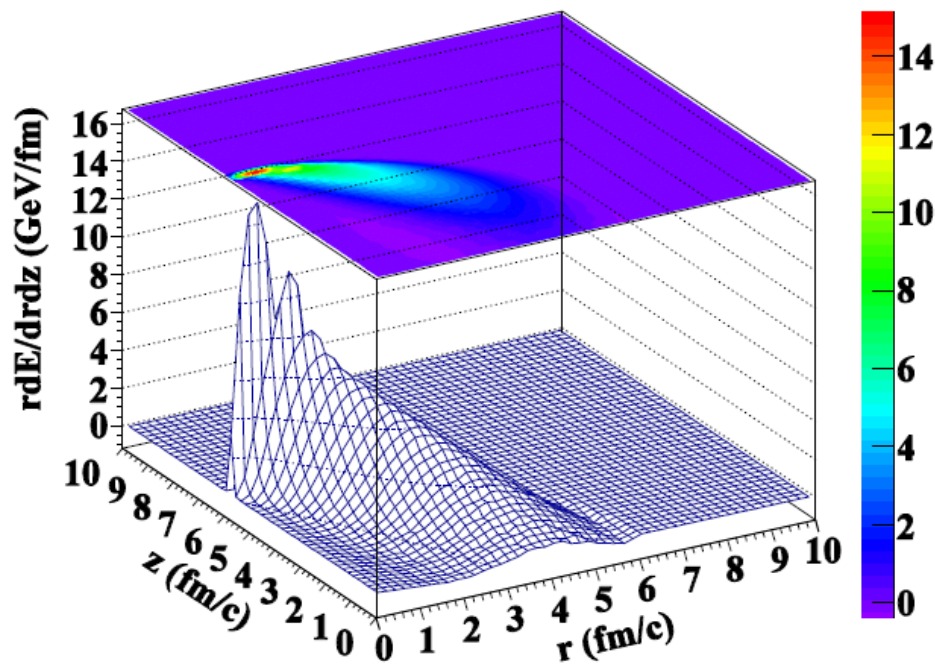
$E = 100 \text{ GeV}$

$T = 0.4 \text{ GeV}$        $\alpha_s = 0.3$

- Mach Cone like wave and the diffusion wake.

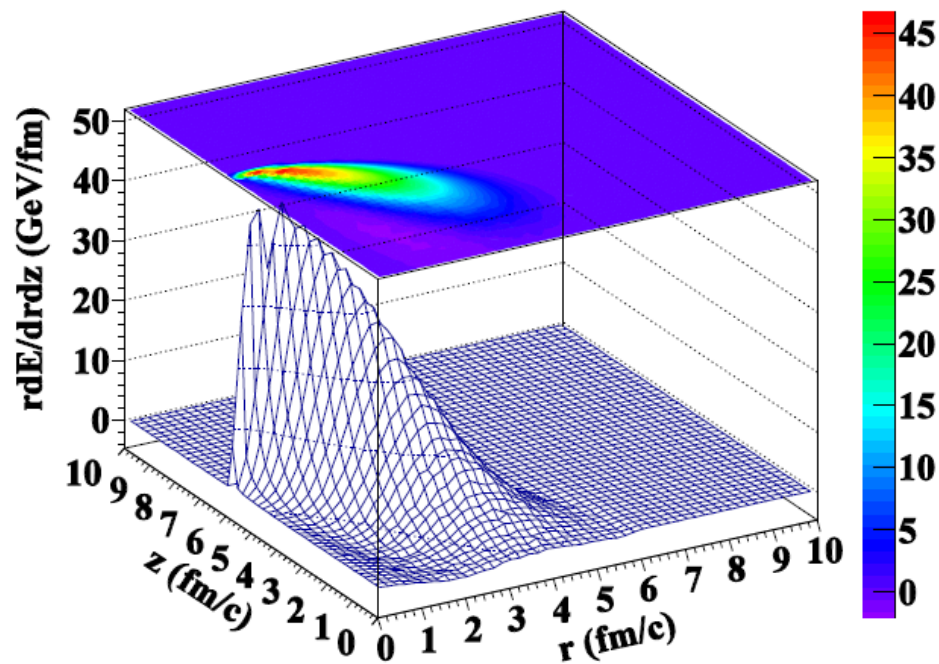
*Elastic only*

gluon: elastic only at  $t=6 \text{ fm/c}$

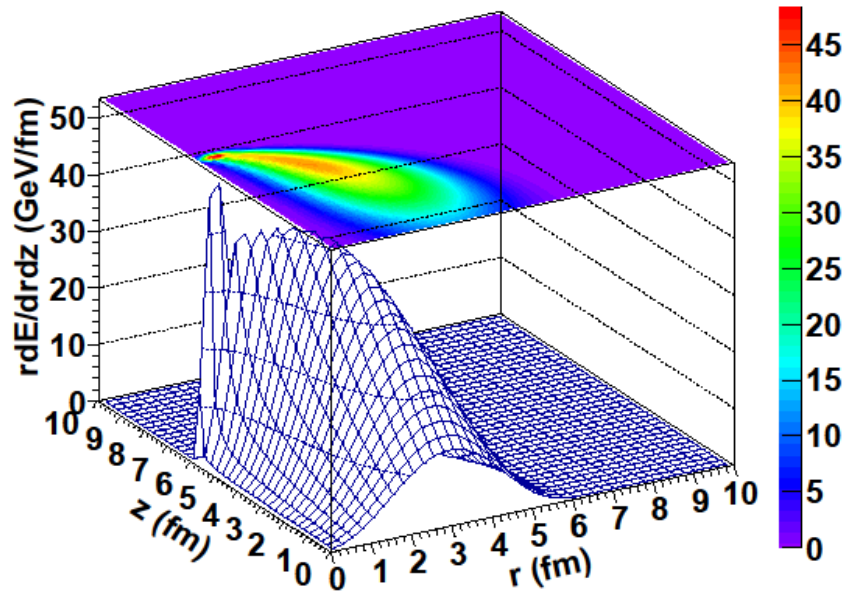


*Elastic + Radiation*

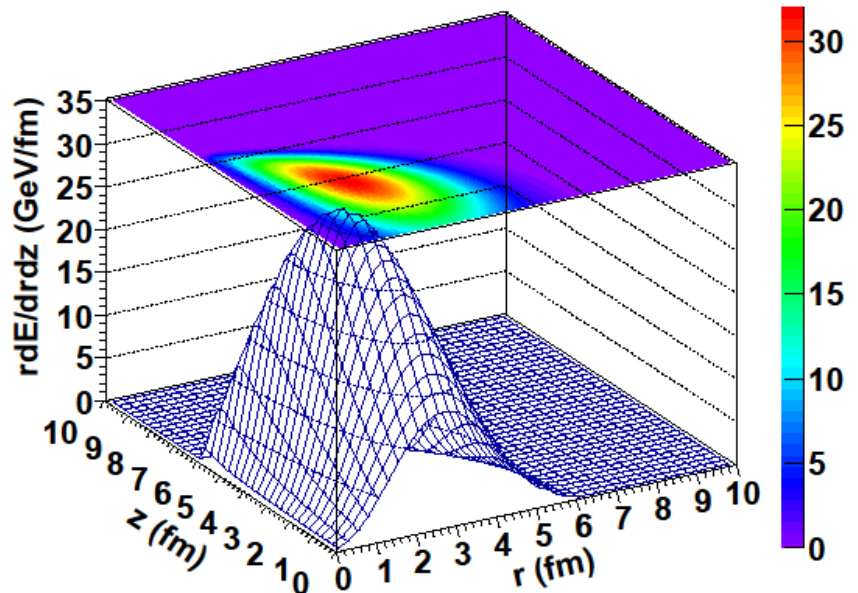
gluon: elastic + radiation at  $t=6 \text{ fm/c}$



(c)  $t=6 \text{ fm}/c$

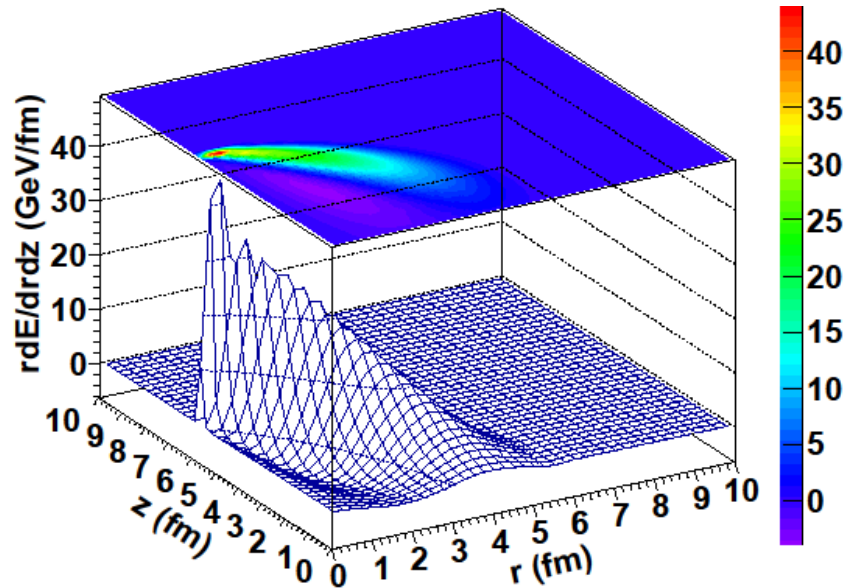


(c)  $t=6 \text{ fm}/c$



**Positive**

(recoiled parton  
+ emitted gluon)



**Negative**

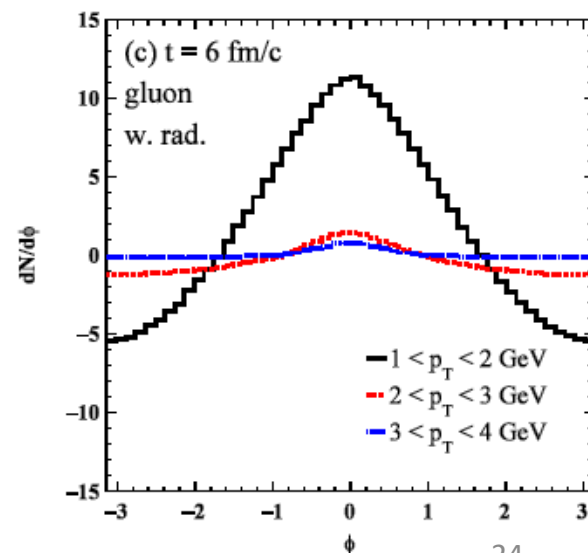
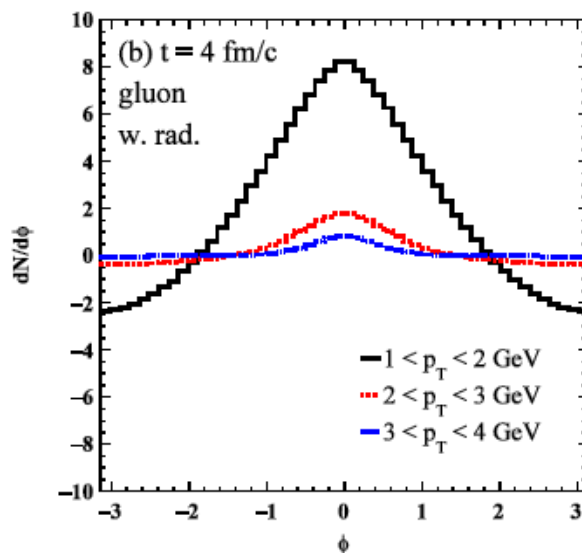
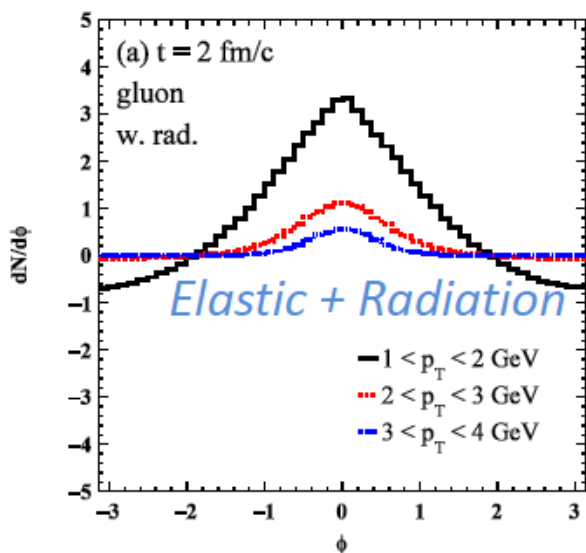
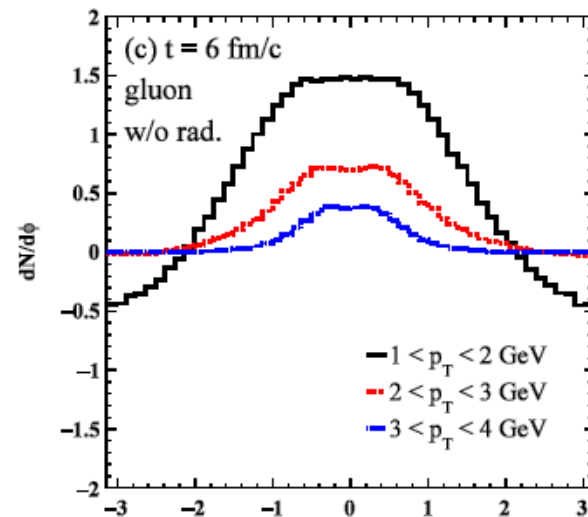
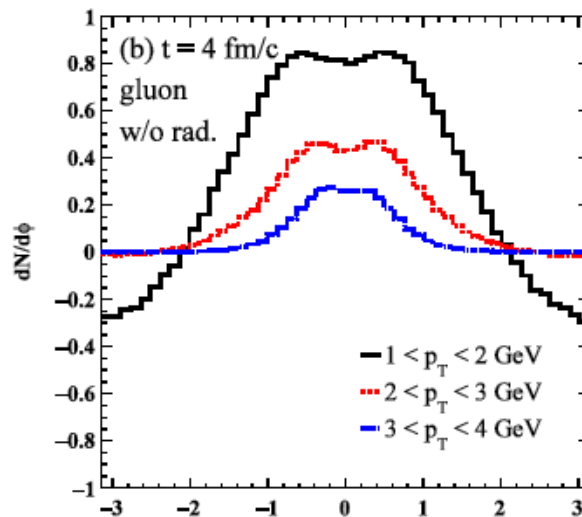
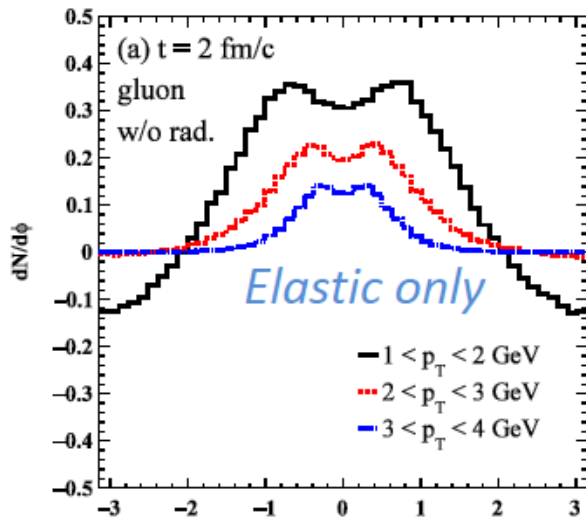
(initial thermal parton)

# Jet induced medium excitation (Angular distribution)

$t = 2 \text{ fm}$

$t = 4 \text{ fm}$

$t = 6 \text{ fm}$

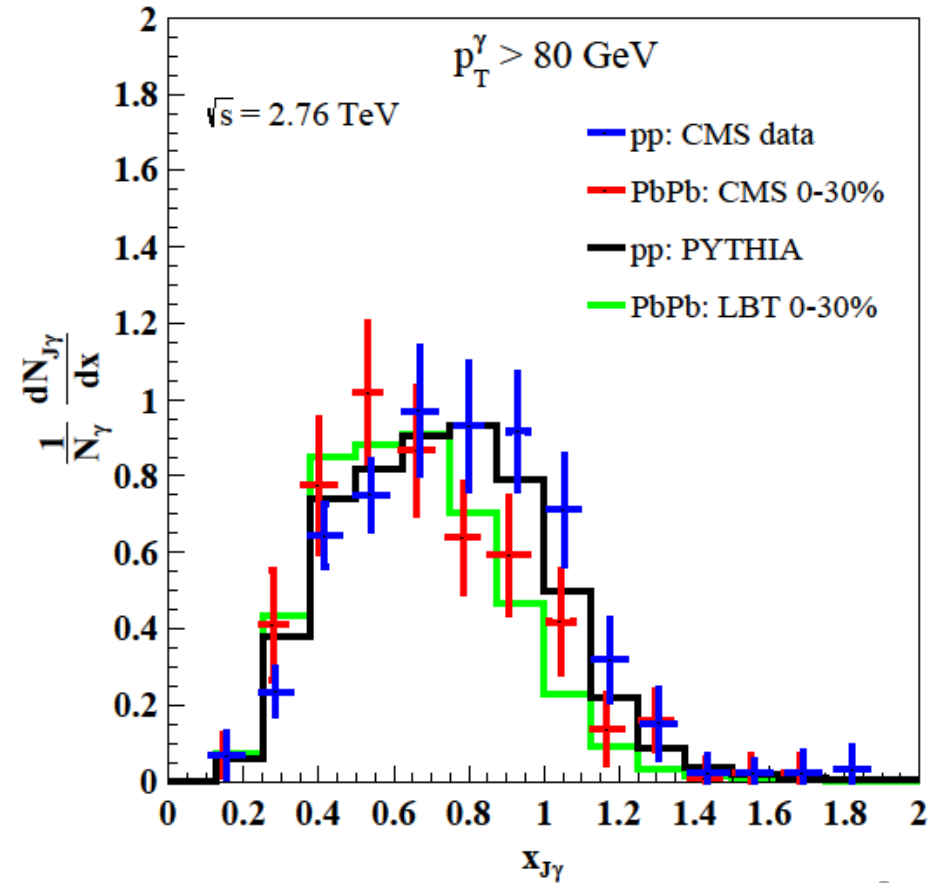




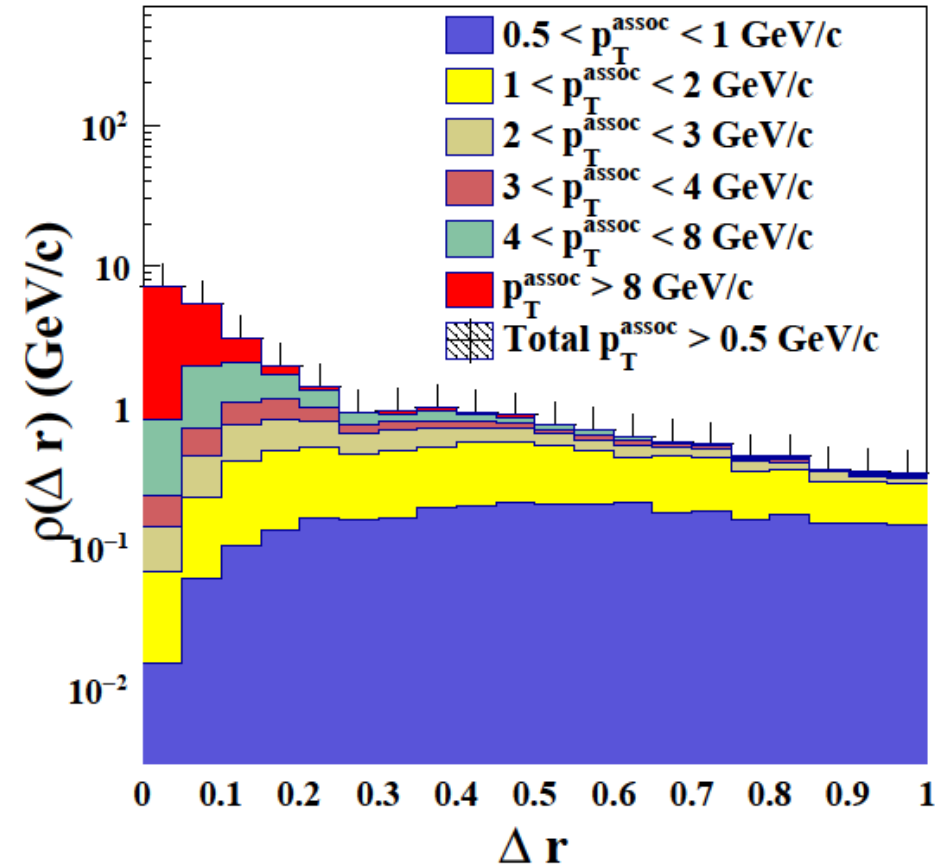
# Jet reconstruction on hadron level with recombination model

Han, Fries and Ko, Phys. Rev. C93 (2016) 045207

## Gamma-jet asymmetry

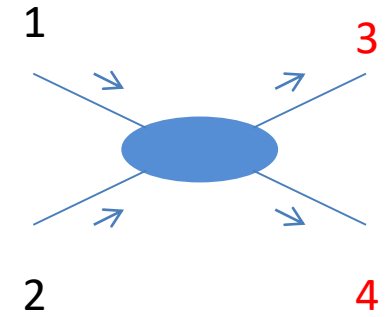
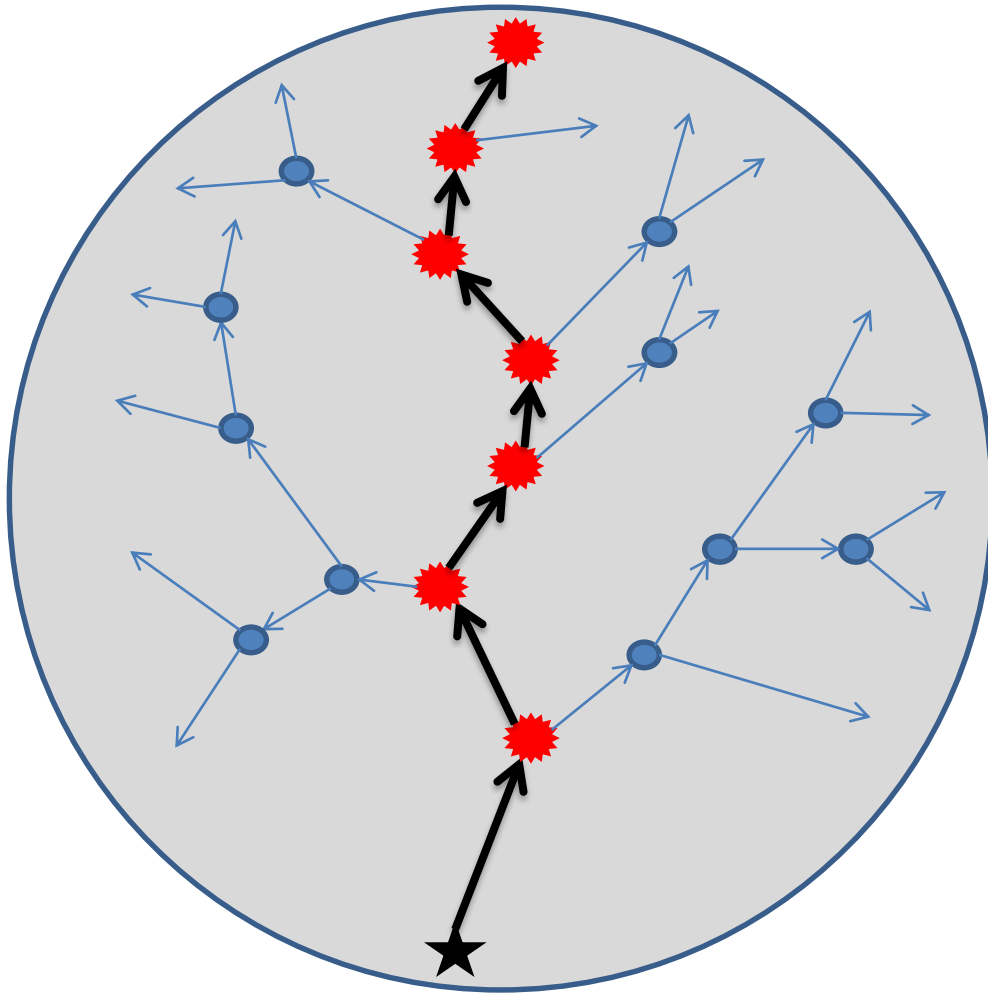



## Jet shape




preliminary

# Jet induced medium excitation: recoiled parton



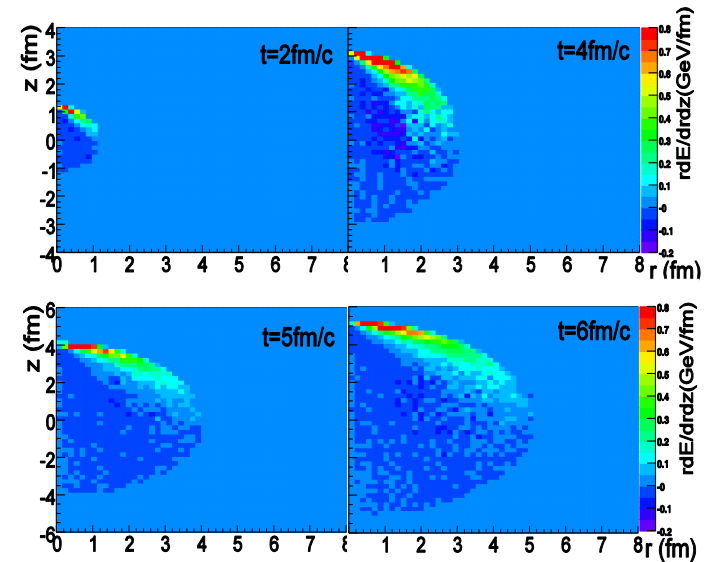
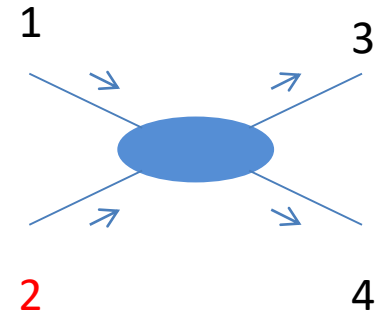
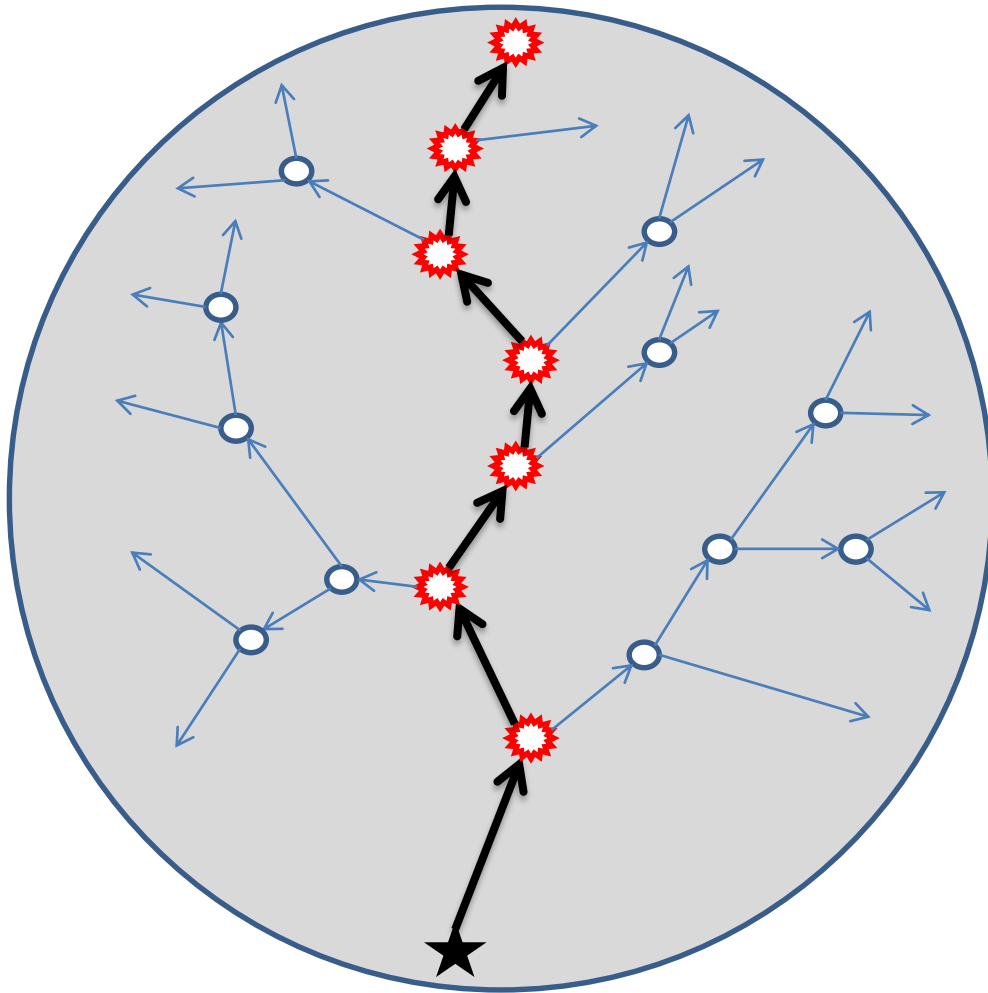
 Leading parton-----thermal parton scattering

 recoiled parton-----thermal parton scattering

*Linearized Boltzmann jet transport*  
neglect scatterings between recoiled medium partons.

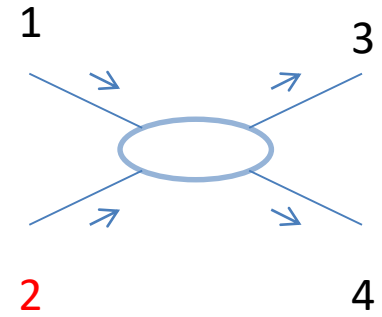
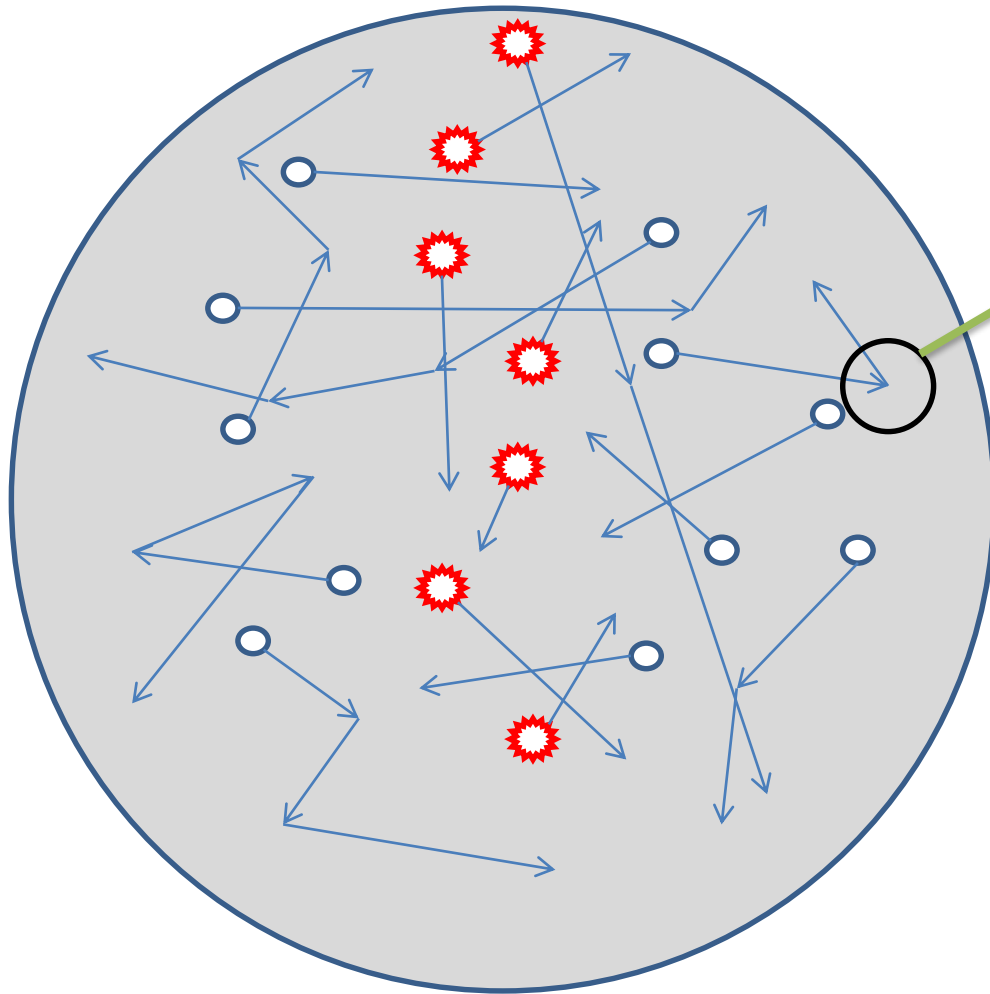
It's a good approximation when the jet induced medium excitation  $\delta f \ll f$ .

# Jet induced medium excitation: particle hole



One has to subtract the 4-momentum of negative particle when combine it to jet

# Jet induced medium excitation: back reaction



thermal parton-----thermal parton  
scattering

the negative particle is also traveling in  
the medium

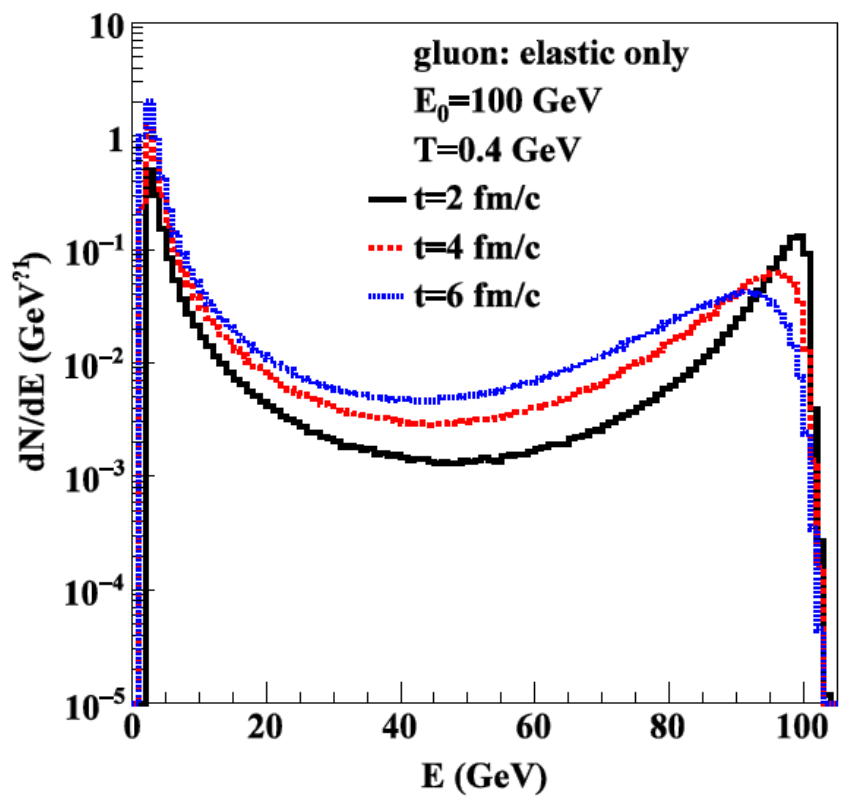
One has to subtract the 4-momentum of  
negative particle when combine it to jet

# Jet induced medium excitation (Energy distribution at different time)

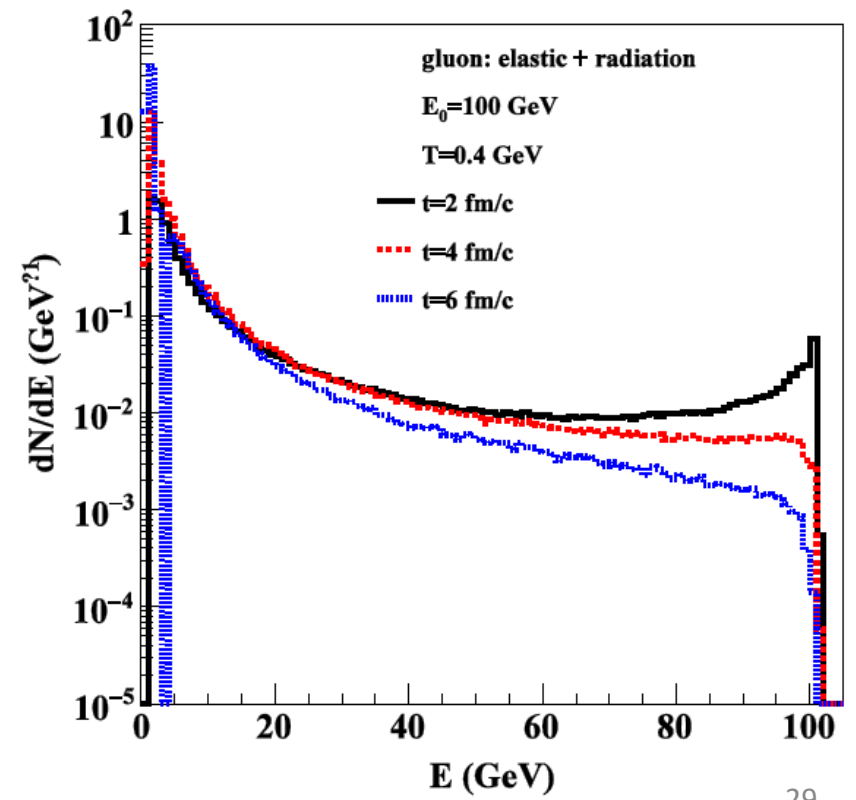
Initial jet parton: gluon  
 $E = 100 \text{ GeV}$   
 $T = 0.4 \text{ GeV}$        $\alpha_s = 0.3$

- Depletion of the energy of the leading parton.

*Elastic only*



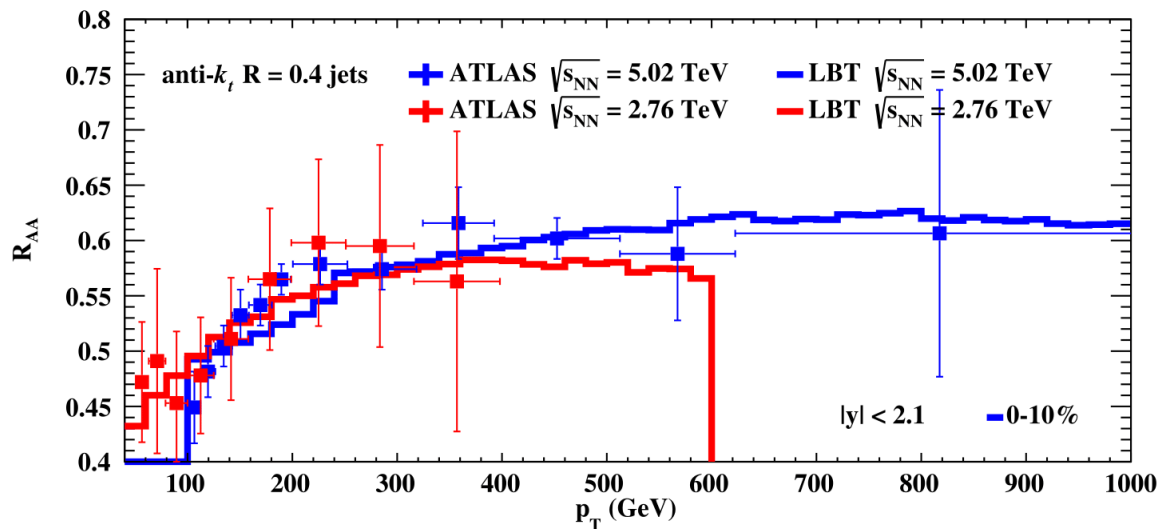
*Elastic + Radiation*



# Jet energy loss

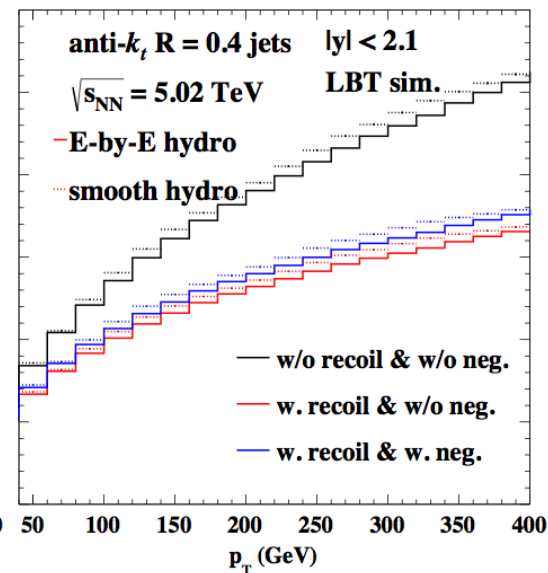
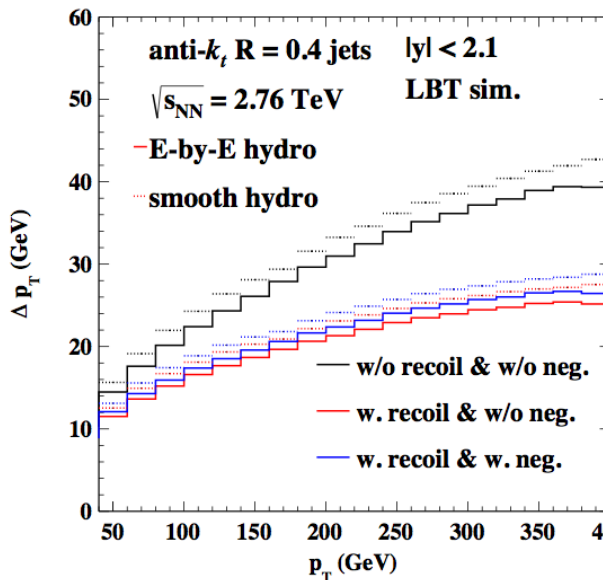
- Single jet  $R_{AA}$

The only parameter effective strong coupling constant  $\alpha_s$  is fixed. (fix the strength of jet-medium interaction)



He, Cao, Luo & XNW to be published

- Fluctuation effect  
(solid vs dotted)
- Recoiled effect  
(black vs blue)
- Back reaction effect  
(red vs blue)



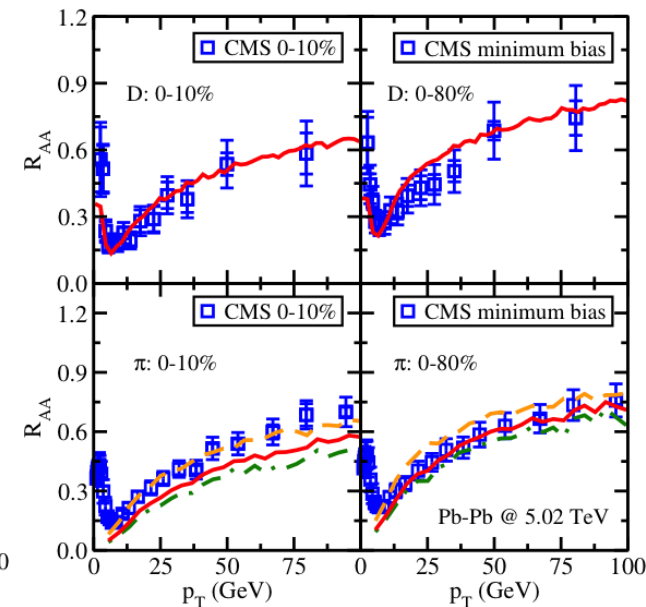
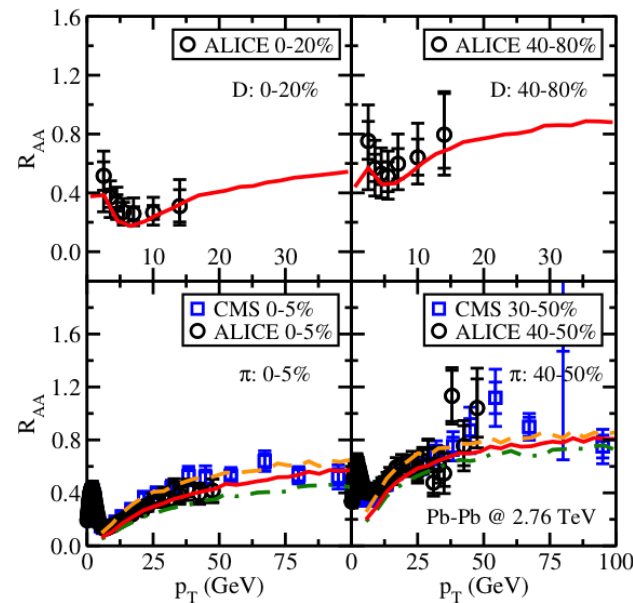
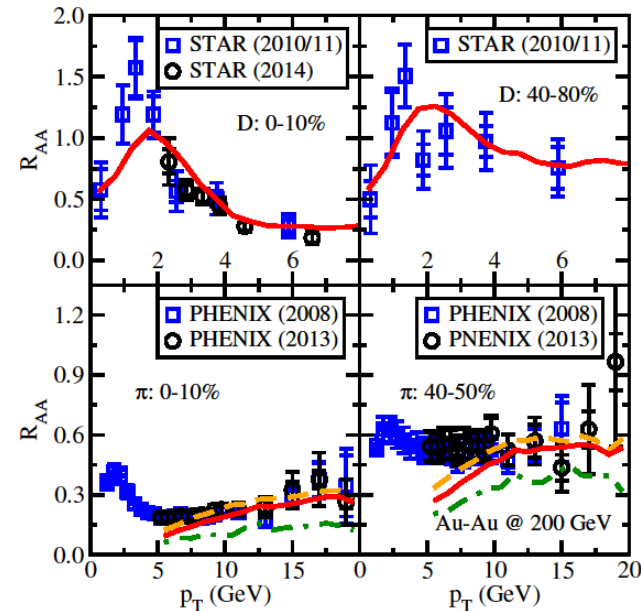
# Hadron $R_{AA}$ in heavy ion collision

- Simultaneous description of single hadron  $R_{AA}$  from RHIC to LHC ( AuAu@200GeV, PbPb@2760GeV and PbPb@5020GeV, 2 centrality bins for each system, 6 data sets in total )

AuAu@200GeV

PbPb@2760GeV

PbPb@5020GeV

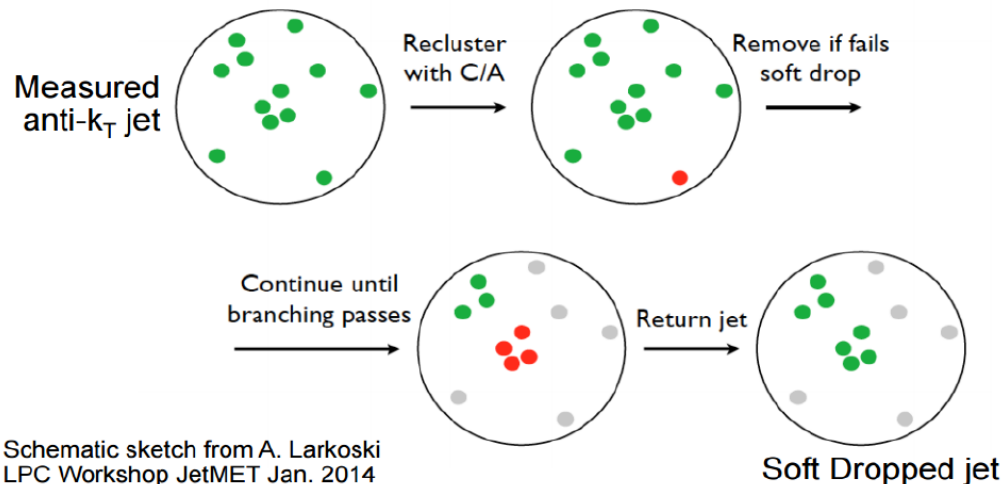


# Jet substructure

## Jet grooming

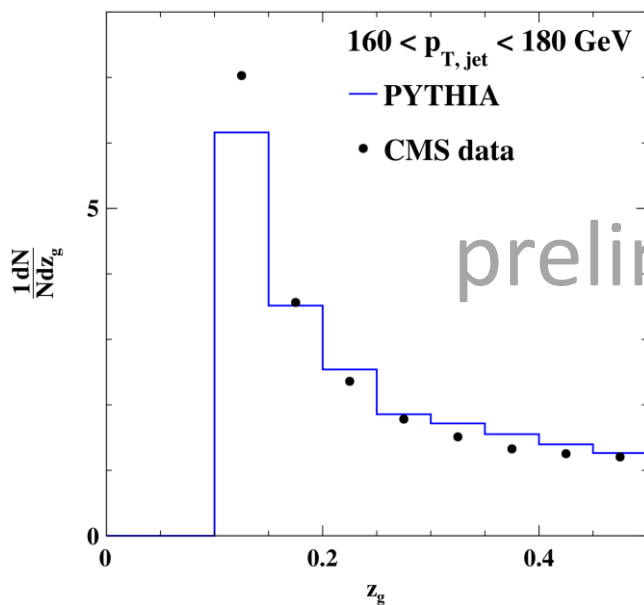
$$z_g \equiv \frac{\min(p_{T1}, p_{T2})}{p_{T1} + p_{T2}} > z_{cut} \left( \frac{\Delta R}{R_0} \right)^\beta$$

$$\frac{M_g}{p_T^{jet}} = \frac{\sqrt{(E_1 + E_2)^2 - (\vec{p}_1 + \vec{p}_2)^2}}{p_T^{jet}}$$

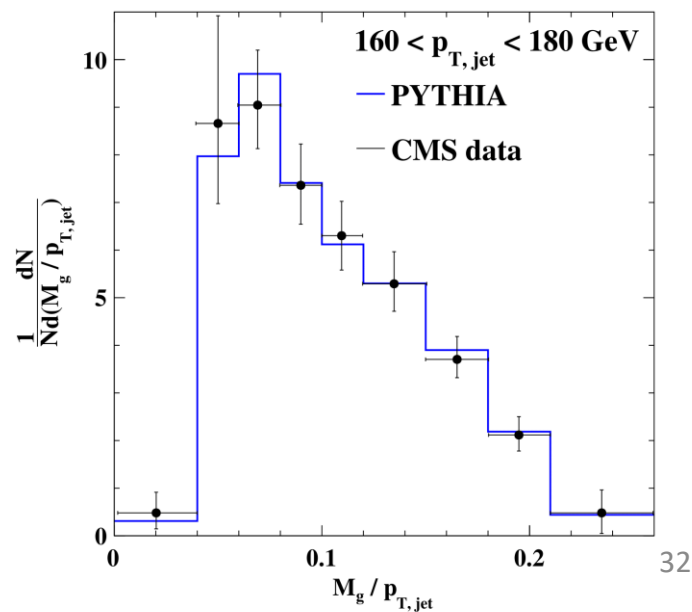


## Groomed Jet splitting function (pp)

## Groomed jet mass (pp)



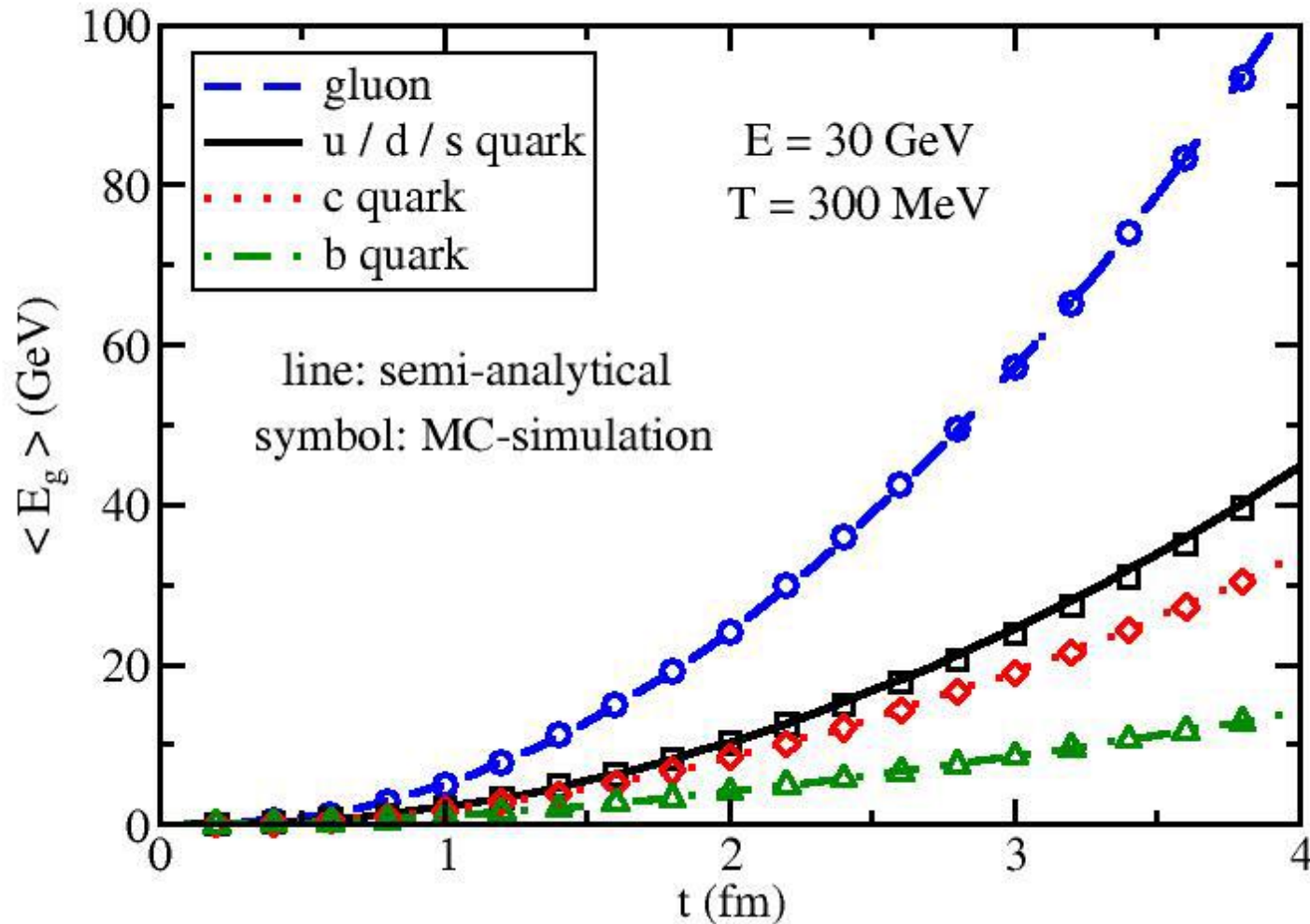
preliminary





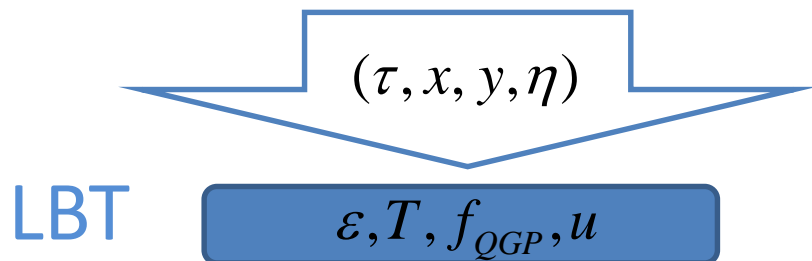
# Energy loss from radiation process in an uniform medium

- Energy of the leading parton is recovered at each time step in MC to compare with the semi-analytical calculation. (a crosscheck of the MC implementation in LBT)

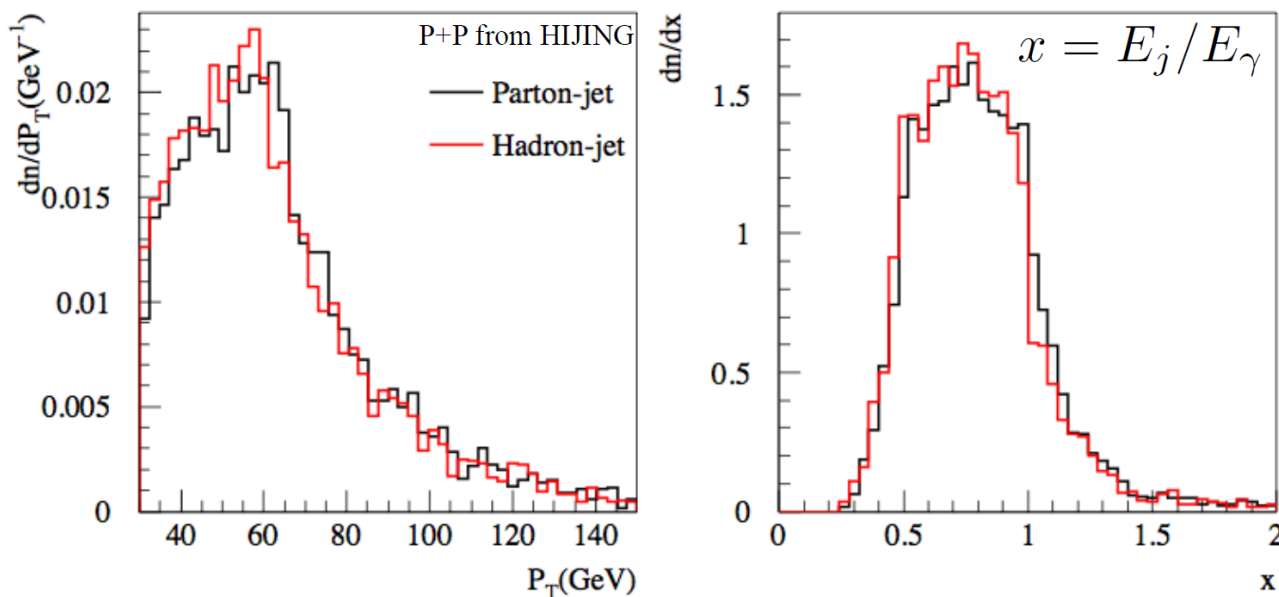


# Gamma-jets in a 3+1D hydro

- 3+1D Ideal hydro Longgang Pang, Qun Wang, Xin-Nian Wang Phys.Rev. C86 (2012) 024911



- Location of gamma-jet is decided according probability of binary collision.
- Small difference between parton-jet and hadron-jet.



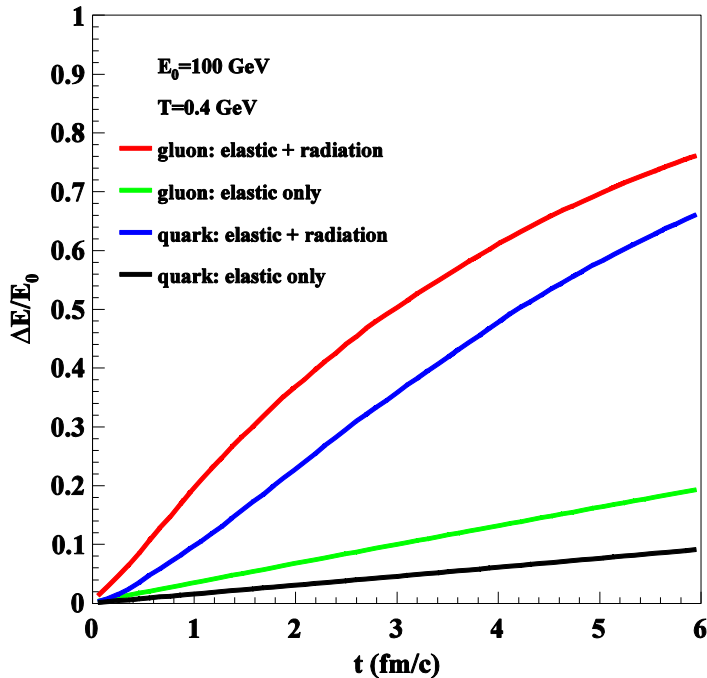
# Nontrivial path length dependence on parton energy loss

## Leading parton energy loss

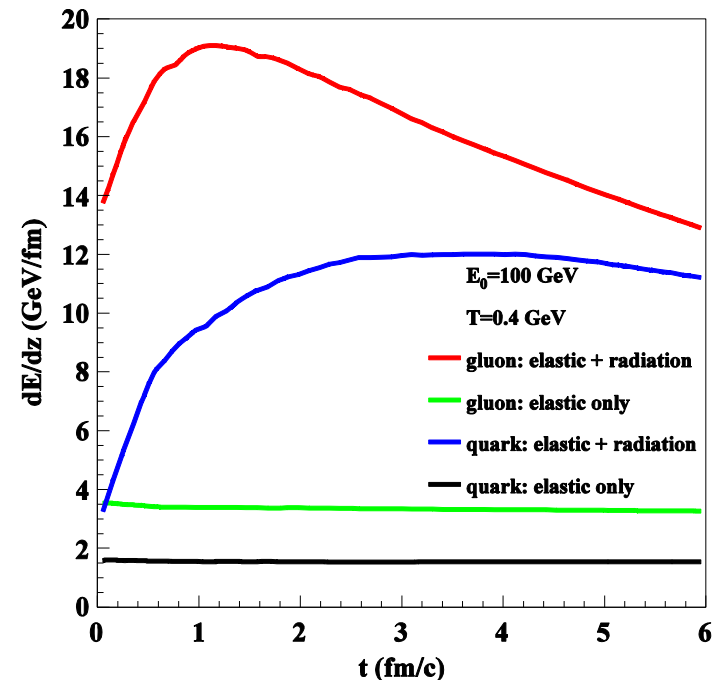
Propagation of a single initial jet parton in a uniform medium

$$\alpha_s = 0.3 \quad E = 100 \text{ GeV} \quad T = 0.4 \text{ GeV}$$

### Fractional energy loss



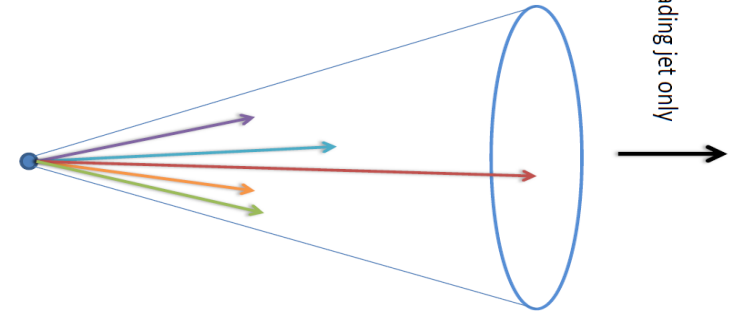
### Energy loss per unit length



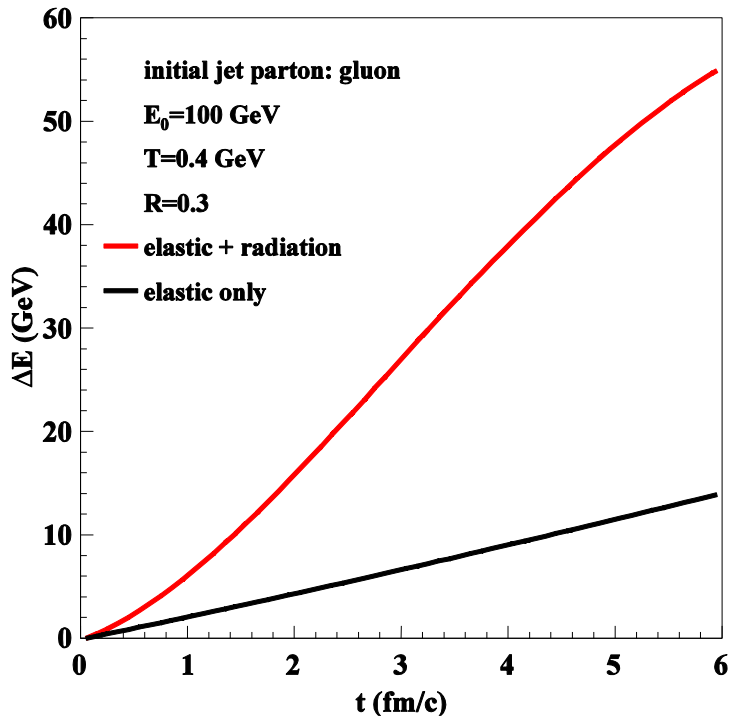
# Path length dependence on parton energy loss

## Leading jet energy loss

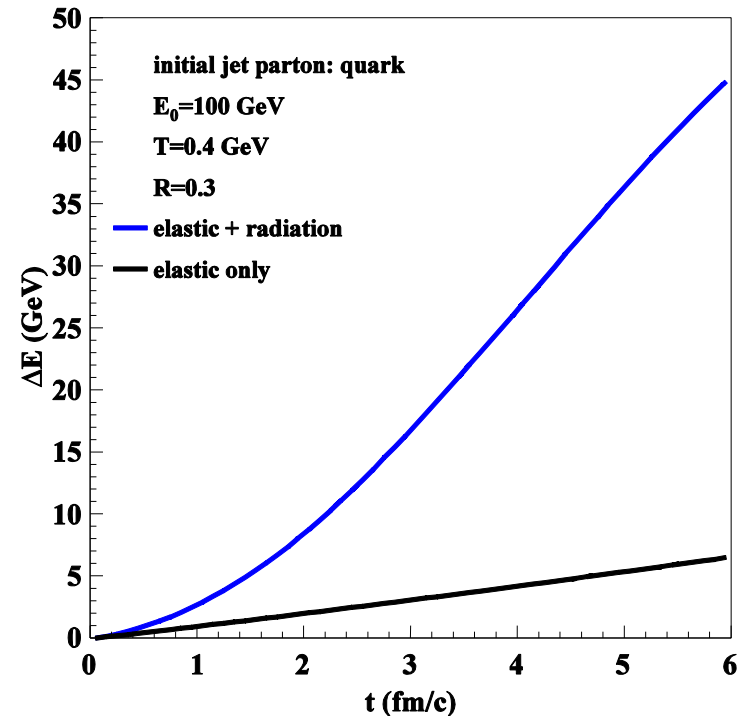
- Leading jet recover some of the energy lost by the leading parton.



### Initial jet parton: gluon



### Initial jet parton: quark



# Jet shape of leading jet in heavy-ion collisions

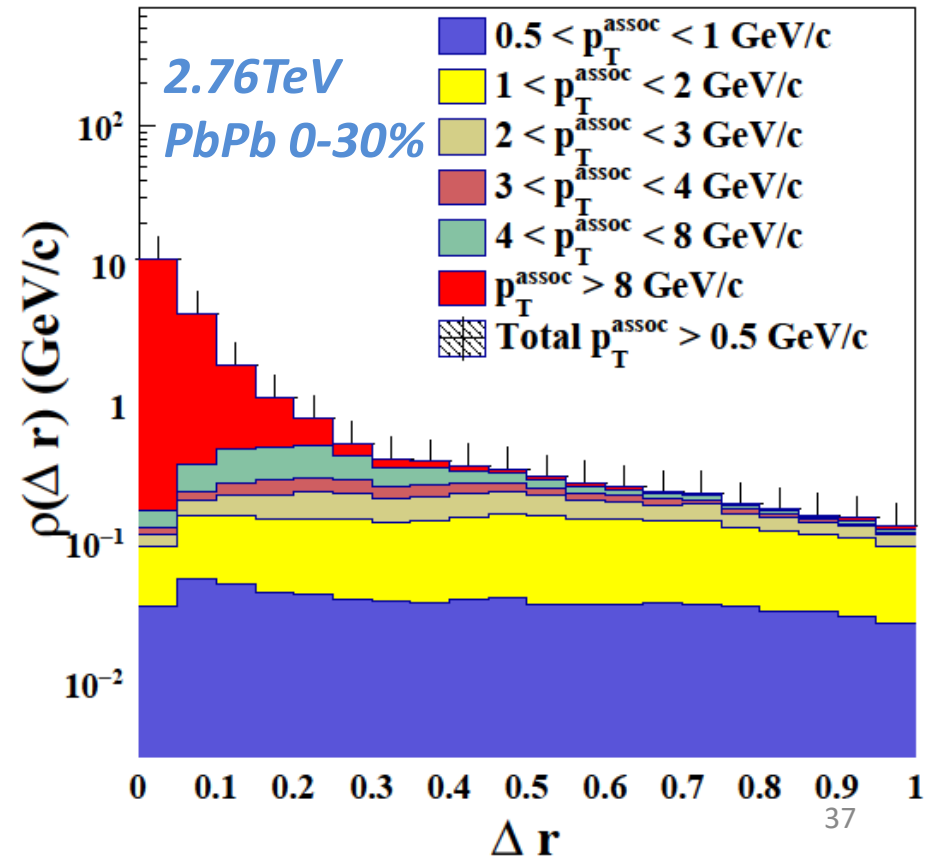
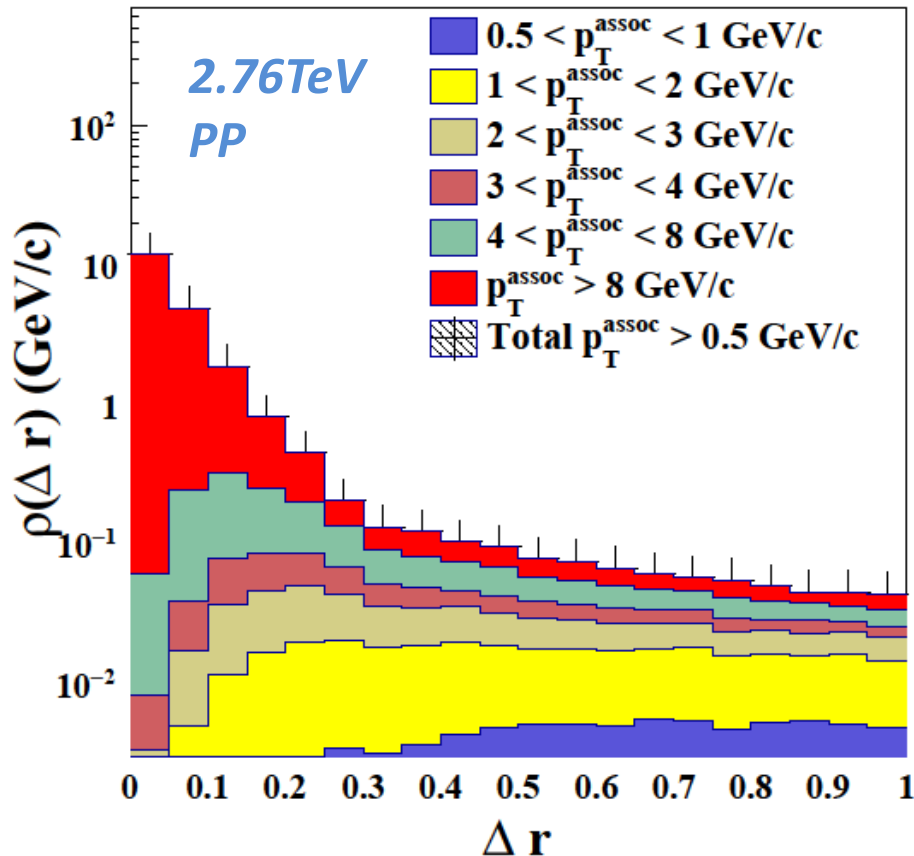
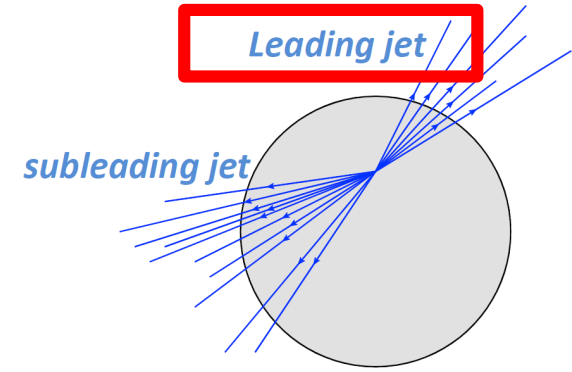
preliminary

$$P_{T\text{leadingjet}} > 120\text{GeV}$$

$$P_{T\text{subleadingjet}} > 50\text{GeV}$$

$$|\eta_{\text{jet}}| < 1.6$$

$$\Delta_\phi > 5/6\pi$$



# Jet shape of leading jet in heavy-ion collisions

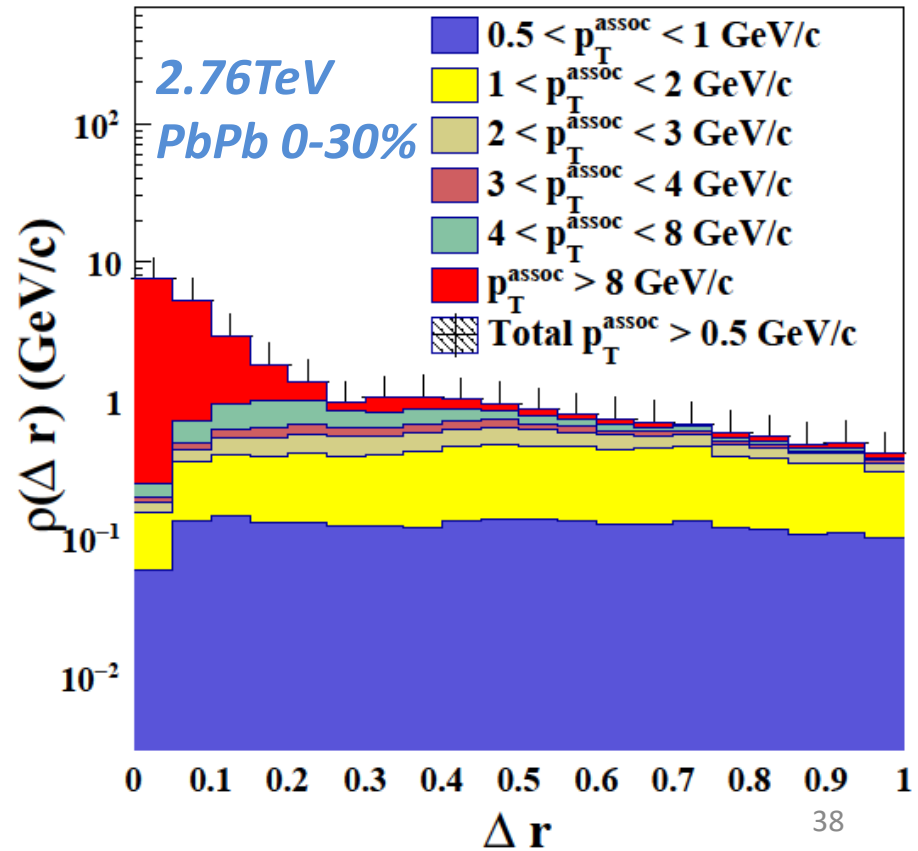
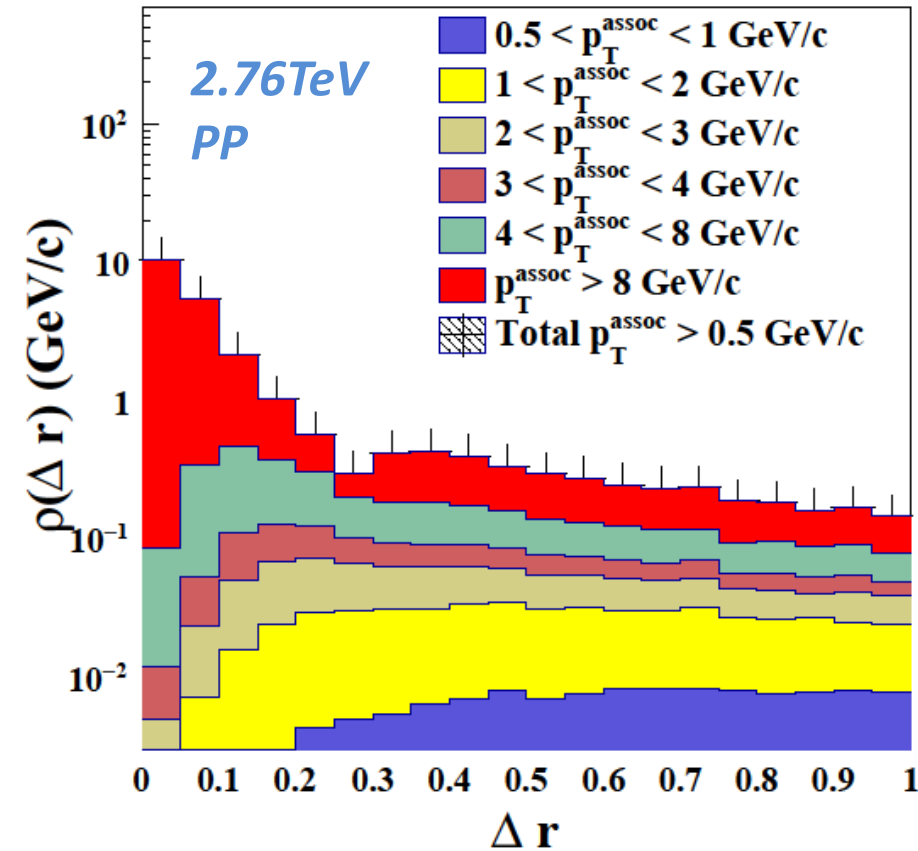
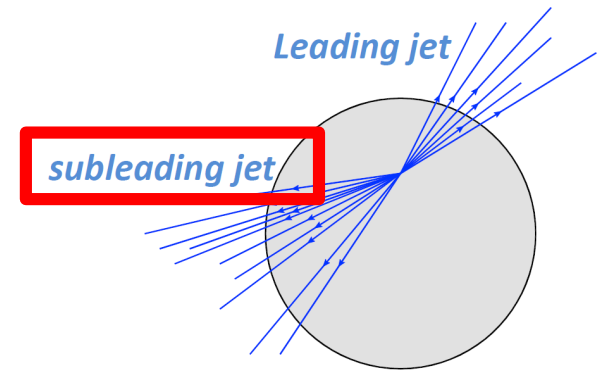
preliminary

$$P_{T\text{leadingjet}} > 120\text{GeV}$$

$$P_{T\text{subleadingjet}} > 50\text{GeV}$$

$$|\eta_{\text{jet}}| < 1.6$$

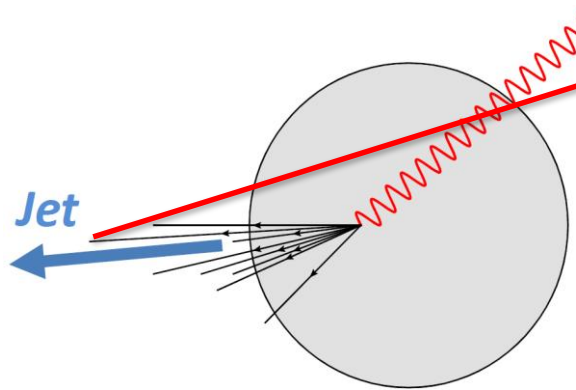
$$\Delta_\phi > 5/6\pi$$



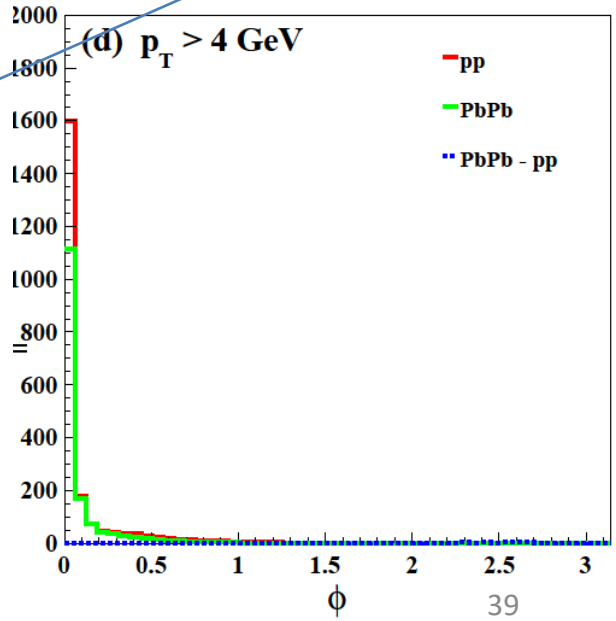
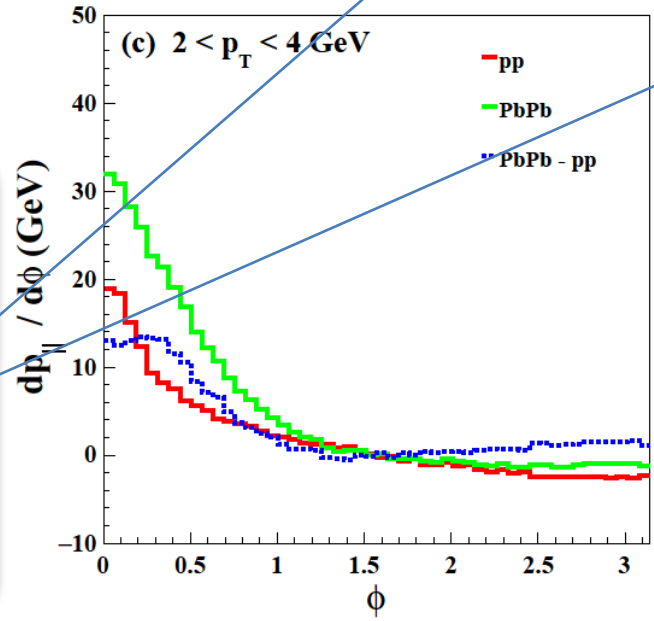
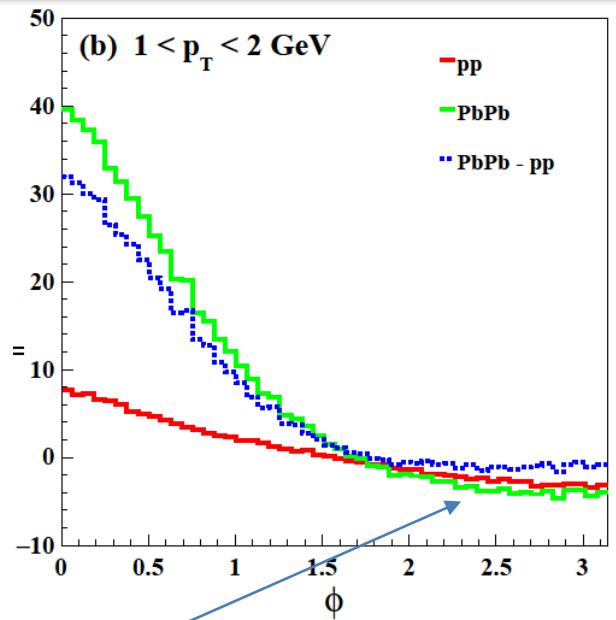
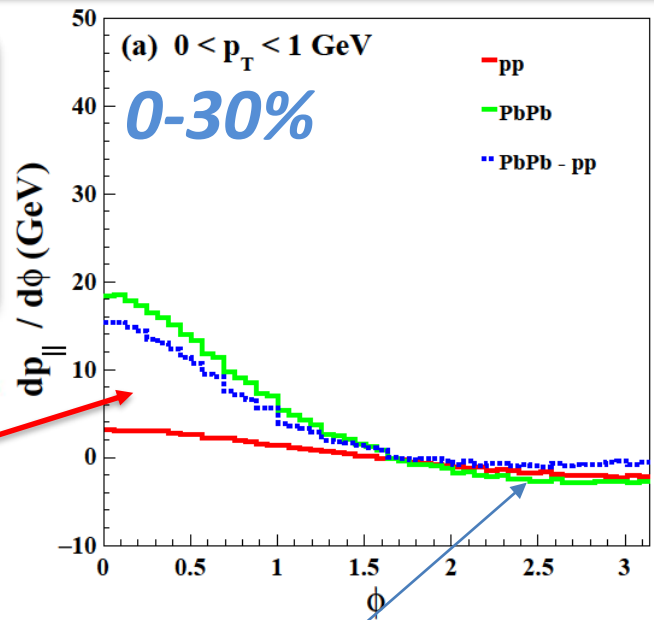
# Energy flow in gamma-jets events

$$P_{\parallel} = \sum_i P_{i(parton)} * \cos \theta_{i(parton-leadingjet)}$$

$$\phi = | \phi_{parton} - \phi_{leadingjet} |$$

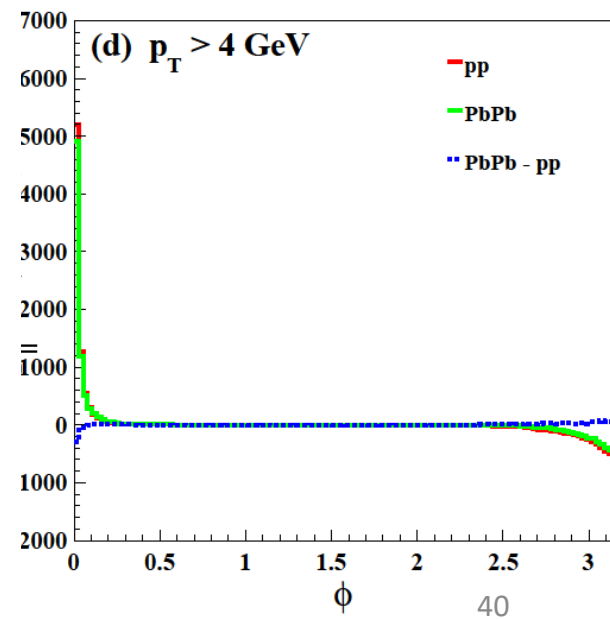
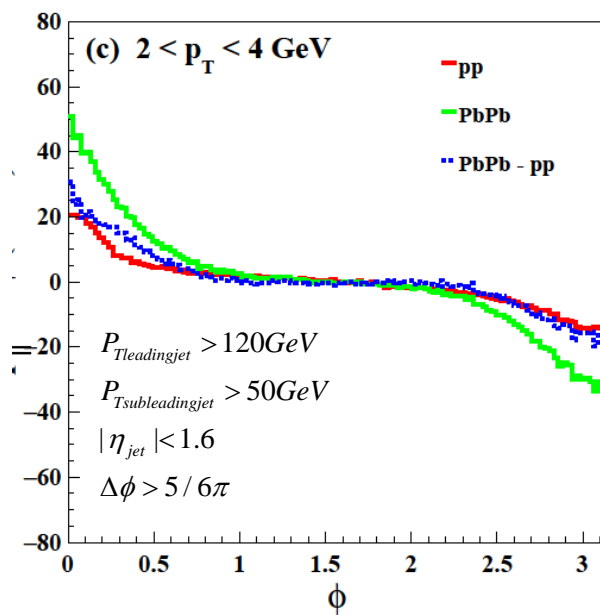
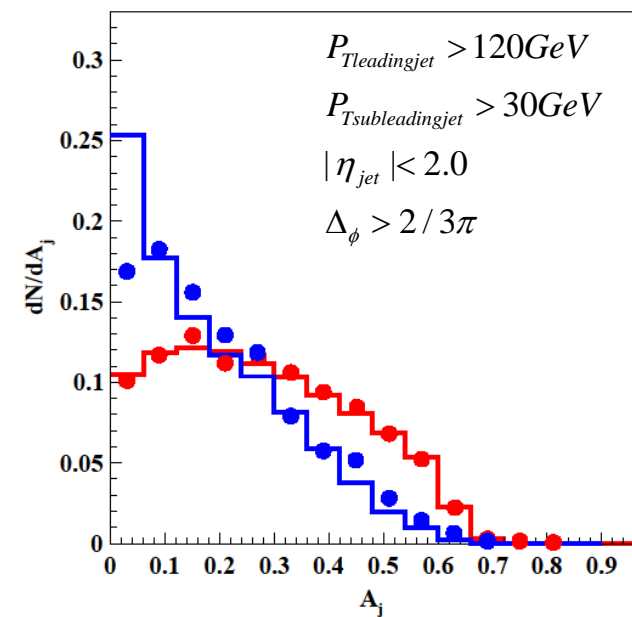
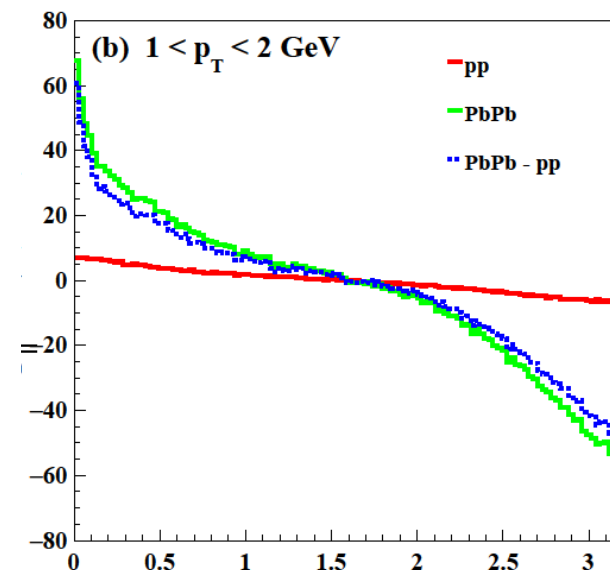
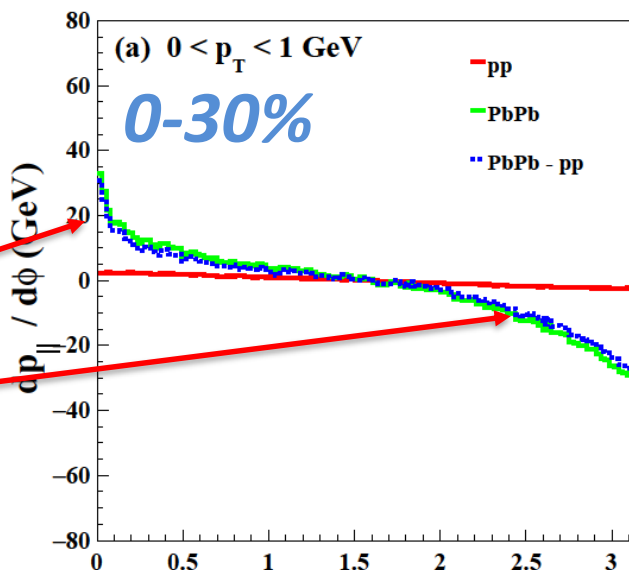
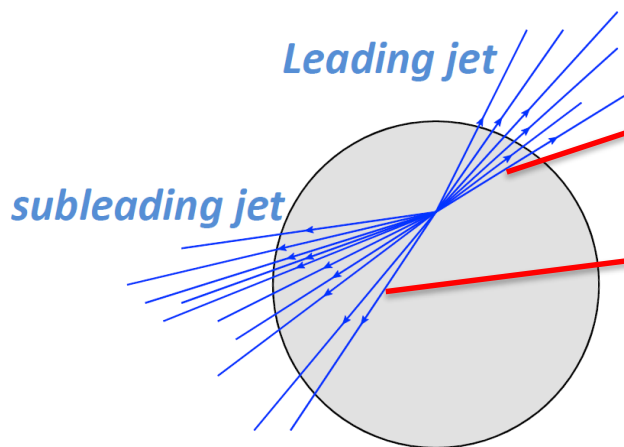


- Suppression of the hard parton, enhancement of the soft parton.
- Energy flow to the opposite direction of the jet



# Energy flow in dijet events

preliminary





# $p_T$ imbalance of dijet in heavy-ion collisions

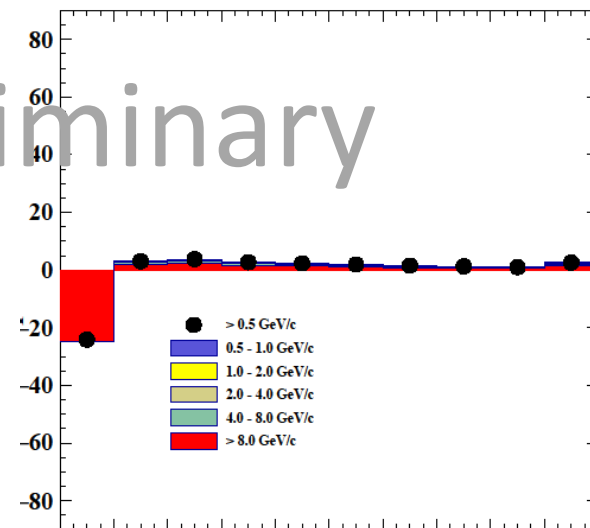
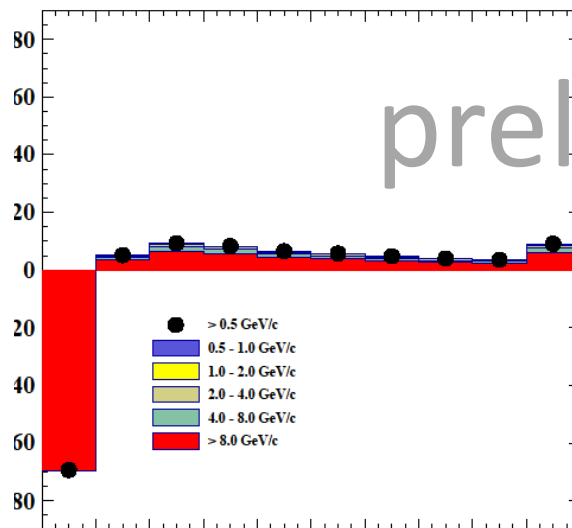
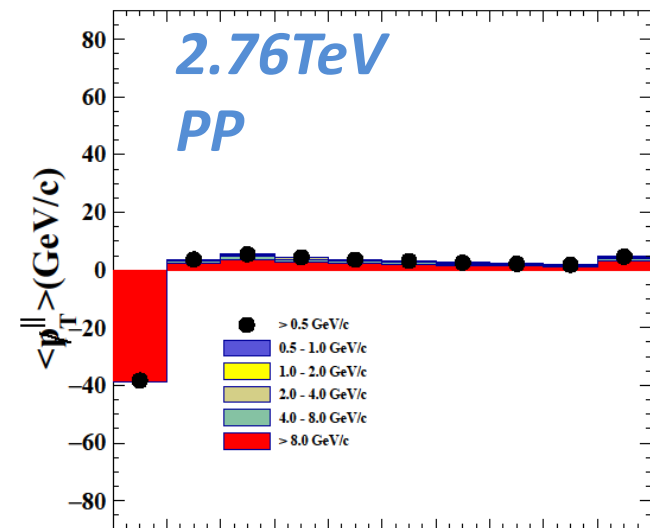
$A_j$  inclusive

$A_j > 0.22$

$A_j < 0.22$

2.76TeV  
PP

preliminary



2.76TeV  
PbPb 0-30%

