

# Exploring Triplet-Quadruplet Fermionic Dark Matter at the LHC and Future Colliders

JW Wang, XJ Bi, QF Xiang, PF Yin, ZH Yu, arXiv:1711.05622, PRD  
Tait, ZH Yu, arXiv:1601.01354, JHEP

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Shanghai, June 22, 2018



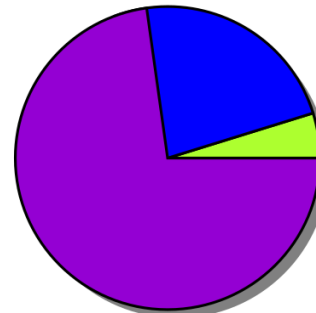
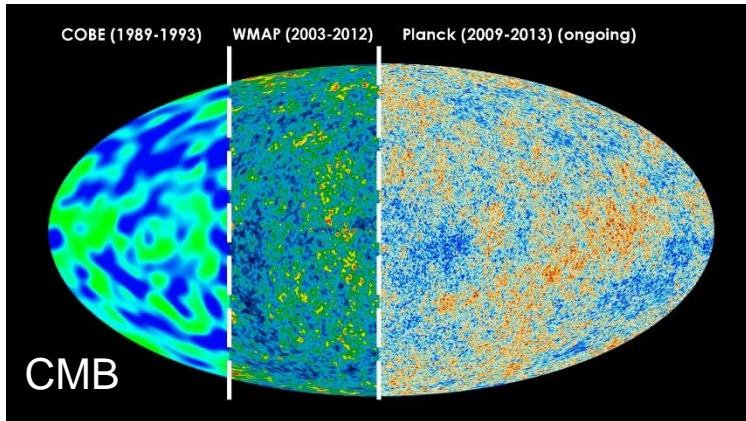
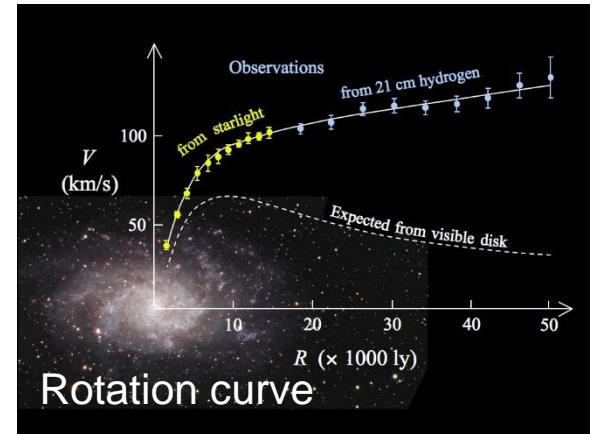
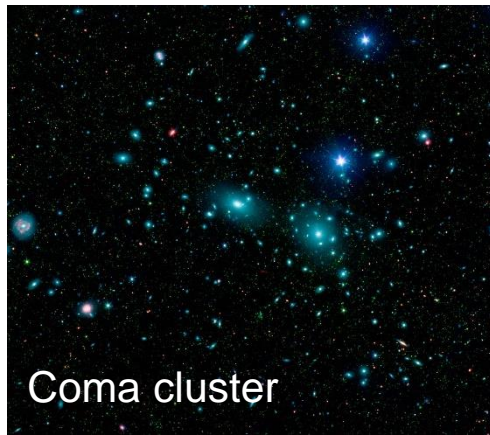
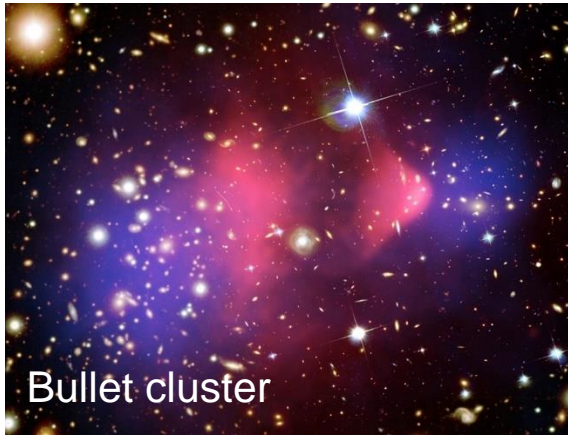
# Outline

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- **Introduction and motivation**
- **Model details**
- **Constrains at proton-proton colliders**
- **Constrains at electron-positron colliders**
- **Summary**

# Dark matter in the Universe

- The astrophysical and cosmological observations have provided compelling evidences of the existence of **dark matter (DM)**.



Planck 2015  
[1502.01589]

Cold DM (25.8%)

$$\Omega_c h^2 = 0.1186 \pm 0.0020$$

Baryons (4.8%)

$$\Omega_b h^2 = 0.02226 \pm 0.00023$$

Dark energy (69.3%)

$$\Omega_\Lambda = 0.692 \pm 0.012$$

# Triplet-quadruplet DM model

Dark sector Weyl fermions ( $SU(2)_L \times U(1)_Y$ ):

$$T = \begin{pmatrix} T^+ \\ T^0 \\ -T^- \end{pmatrix} \in (\mathbf{3}, 0), \quad Q_1 = \begin{pmatrix} Q_1^+ \\ Q_1^0 \\ Q_1^- \\ Q_1^{--} \end{pmatrix} \in (\mathbf{4}, -\frac{1}{2}), \quad Q_2 = \begin{pmatrix} Q_2^{++} \\ Q_2^+ \\ Q_2^0 \\ Q_2^- \end{pmatrix} \in (\mathbf{4}, +\frac{1}{2})$$

Gauge invariant kinetic terms, mass terms and Yukawa couplings:

$$\mathcal{L}_T = iT^\dagger \bar{\sigma}^\mu D_\mu T - (m_T a_{ij} T^i T^j + \text{h.c.})$$

$$\mathcal{L}_Q = iQ_1^\dagger \bar{\sigma}^\mu D_\mu Q_1 + iQ_2^\dagger \bar{\sigma}^\mu D_\mu Q_2 - (m_Q b_{ij} Q_1^i Q_2^j + \text{h.c.})$$

$$\mathcal{L}_{HTQ} = y_1 c_{ijk} Q_1^i T^j H^k + y_2 d_{ijk} Q_2^i T^j \tilde{H}^k + \text{h.c.}$$

There are four independent parameters:  $m_T, m_Q, y_1, y_2$

# State mixing

$$\begin{aligned}\mathcal{L}_{\text{mass}} &= -m_Q Q_1^{--} Q_2^{++} - \frac{1}{2} (T^0, Q_1^0, Q_2^0) \mathcal{M}_N \begin{pmatrix} T^0 \\ Q_1^0 \\ Q_2^0 \end{pmatrix} - (T^-, Q_1^-, Q_2^-) \mathcal{M}_C \begin{pmatrix} T^+ \\ Q_1^+ \\ Q_2^+ \end{pmatrix} + \text{h.c.} \\ &= -m_Q \chi^{--} \chi^{++} - \frac{1}{2} \sum_{i=1}^3 m_{\chi_i^0} \chi_i^0 \chi_i^0 - \sum_{i=1}^3 m_{\chi_i^\pm} \chi_i^\pm \chi_i^\pm + \text{h.c.}\end{aligned}$$

$$\mathcal{M}_N = \begin{pmatrix} m_T & \frac{1}{\sqrt{3}} y_1 v & -\frac{1}{\sqrt{3}} y_2 v \\ \frac{1}{\sqrt{3}} y_1 v & 0 & m_Q \\ -\frac{1}{\sqrt{3}} y_2 v & m_Q & 0 \end{pmatrix}, \quad \mathcal{M}_C = \begin{pmatrix} m_T & \frac{1}{\sqrt{2}} y_1 v & -\frac{1}{\sqrt{6}} y_2 v \\ -\frac{1}{\sqrt{6}} y_1 v & 0 & -m_Q \\ \frac{1}{\sqrt{2}} y_2 v & -m_Q & 0 \end{pmatrix}$$

$$\begin{pmatrix} T^0 \\ Q_1^0 \\ Q_2^0 \end{pmatrix} = \mathcal{N} \begin{pmatrix} \chi_1^0 \\ \chi_2^0 \\ \chi_3^0 \end{pmatrix}, \quad \begin{pmatrix} T^+ \\ Q_1^+ \\ Q_2^+ \end{pmatrix} = C_L \begin{pmatrix} \chi_1^+ \\ \chi_2^+ \\ \chi_3^+ \end{pmatrix}, \quad \begin{pmatrix} T^- \\ Q_1^- \\ Q_2^- \end{pmatrix} = C_R \begin{pmatrix} \chi_1^- \\ \chi_2^- \\ \chi_3^- \end{pmatrix}$$

3 Majorana fermions, 3 singly charged fermions, 1 doubly charged fermion.  
If  $Z_2$  symmetry is conserved,  $\chi_1^0$  will be the excellent DM candidate.

## $y_1 = y_2$ : A custodial $SU(2)_R$ global symmetry limit

When the two Yukawa couplings are equal ( $y = y_1 = y_2$ ), the Lagrangian have an  $SU(2)_L \times SU(2)_R$  invariant form:

$$\begin{aligned} \mathcal{L}_Q + \mathcal{L}_{HTQ} = & i(Q^{\dagger A})_{ij}^k \bar{\sigma}^\mu D_\mu (Q_A)_{ij}^k - \frac{1}{2} [m_Q \varepsilon^{AB} \varepsilon_{il} (Q_A)_k^{ij} (Q_B)_j^{lk} + \text{h.c.}] \\ & + [y \varepsilon^{AB} (Q_A)_i^{jk} T_k^i (H_B)_j + \text{h.c.}] \end{aligned}$$

$$SU(2)_R \text{ doublets: } (Q_A)_k^{ij} = \begin{pmatrix} (Q_1)_k^{ij} \\ (Q_2)_k^{ij} \end{pmatrix}, (H_B)_j = \begin{pmatrix} H_i^\dagger \\ H_i \end{pmatrix}$$

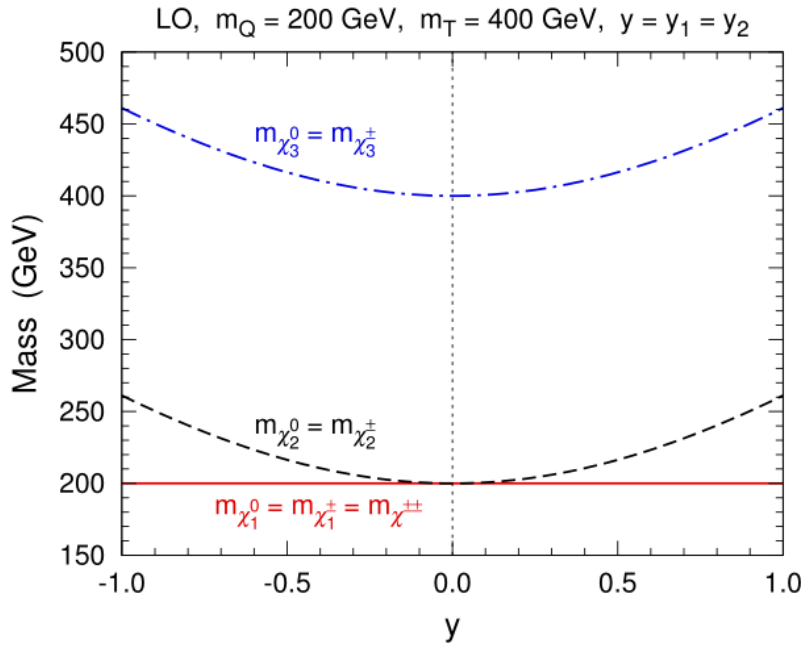
This symmetry is explicitly broken by the hypercharge.

There are still some important properties under this approximate symmetry.

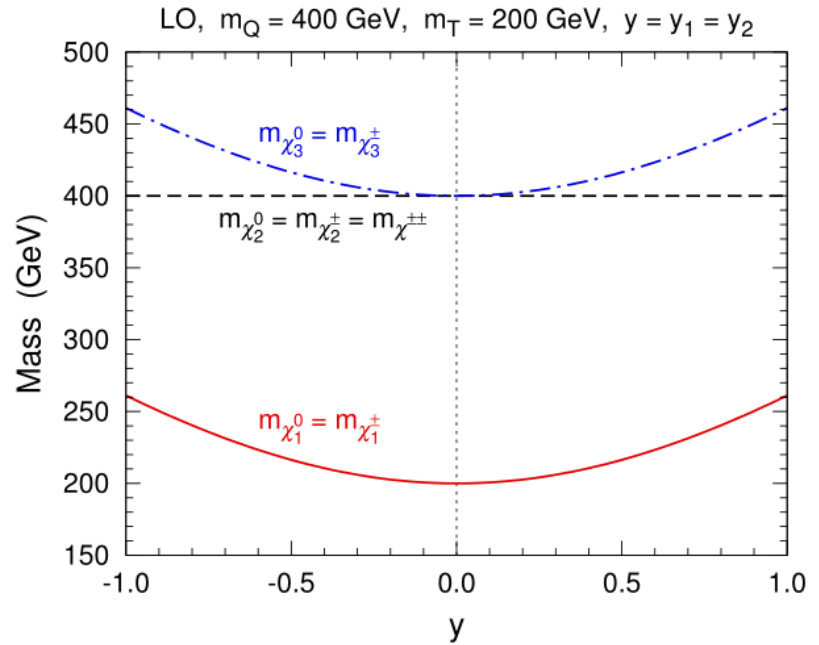
# $y_1 = y_2$ : A custodial $SU(2)_R$ global symmetry limit

In the custodial symmetry limit, each of the dark sector neutral fermions is exactly degenerate in mass with a singly charged fermion at leading order.

So the **mass corrections at the NLO** are required to check if  $m_{\chi_1^0} < m_{\chi_i^\pm}, m_{\chi^{++}}$ .



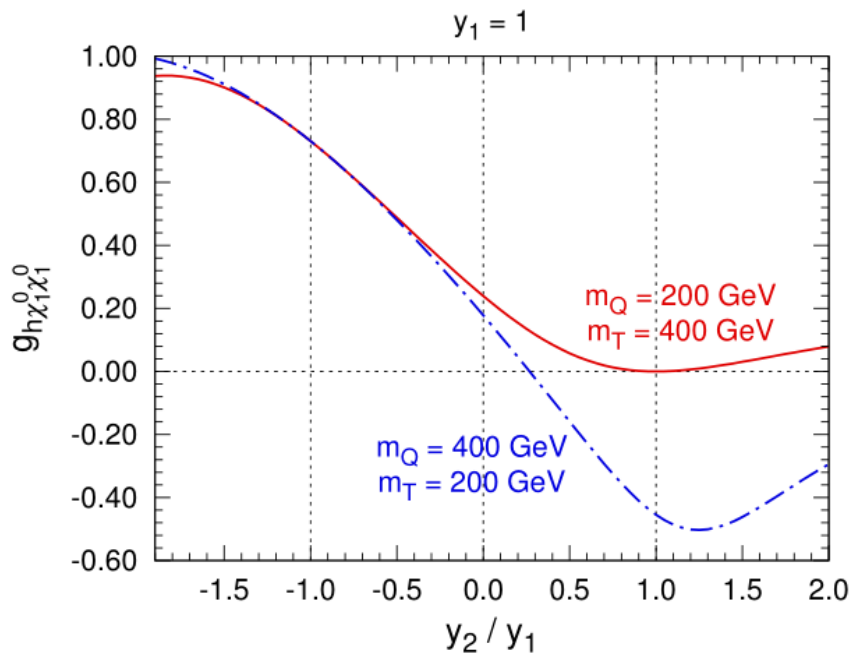
$m_Q < m_T$  case



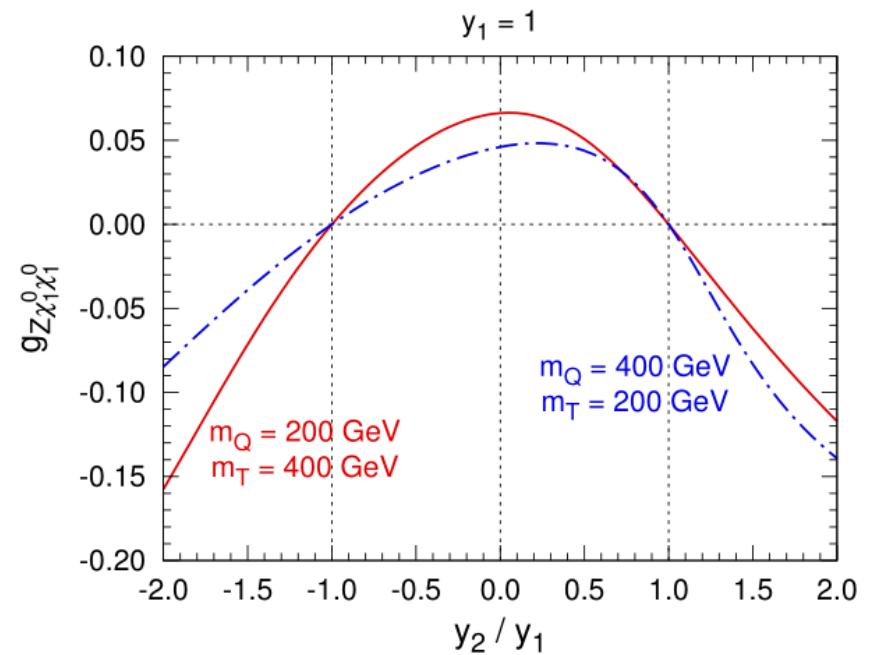
$m_T < m_Q$  case

# $y_1 = y_2$ : A custodial $SU(2)_R$ global symmetry limit

In the custodial symmetry limit, when  $m_Q < m_T$ ,  $\chi_1^0$  will not interact with  $h$  or  $Z$  at the **tree level**. As a result,  $\chi_1^0$  cannot interact with nuclei at the LO and could easily escape from current **DM direct detection bounds**.



$h\chi_1^0\chi_1^0$  coupling



$Z\chi_1^0\chi_1^0$  coupling



# Mass spectrums

When  $m_Q, m_T \gtrsim 1\text{TeV}$

$y_1$  and  $y_2$  will not significantly affect  $m_{\chi_1^0}$ .

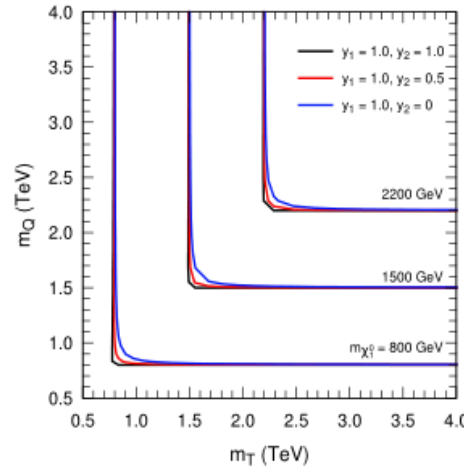
Because the Yukawa couplings affect the mixing between triplet and quadruplets at  $\sim \mathcal{O}(100\text{ GeV})$ .

Even  $y_1 \neq y_2$ , the mass degenerate is ubiquitous.

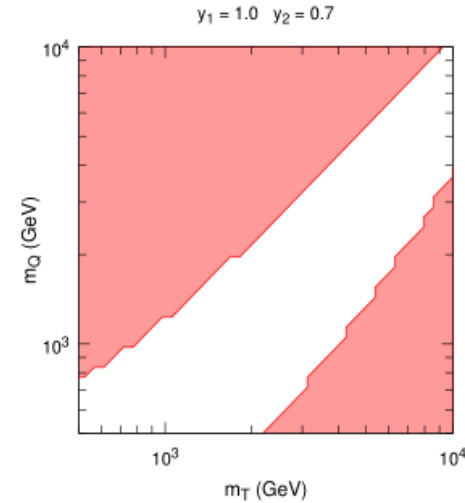
**Blue regions:**  $m_{\chi_1^0}$  is not the lightest.

**Red regions:**  $m_{\chi_1^0} - m_{\chi_1^\pm} \leq 250\text{ MeV}$

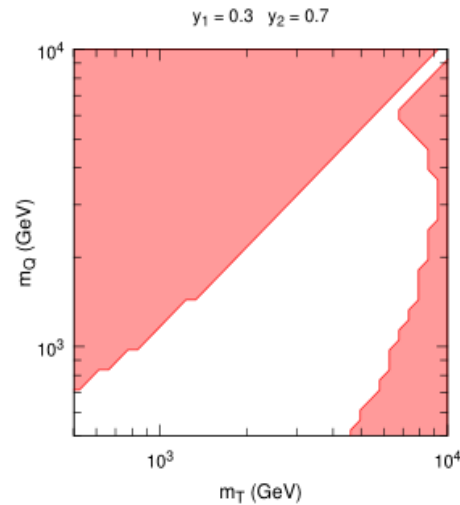
and disappearing track channel can be used.



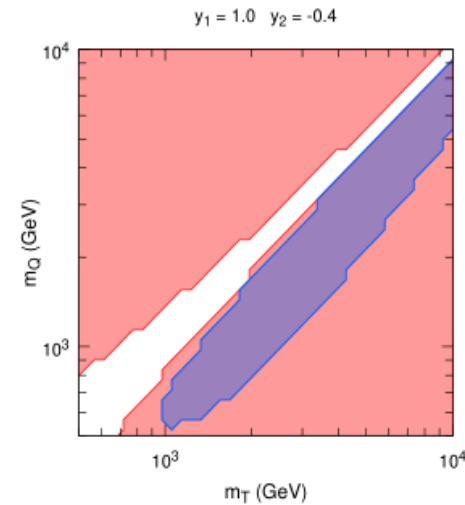
(a)  $m_{\chi_1^0}$  contours



(b)  $y_1 = 1.0, y_2 = 0.7$



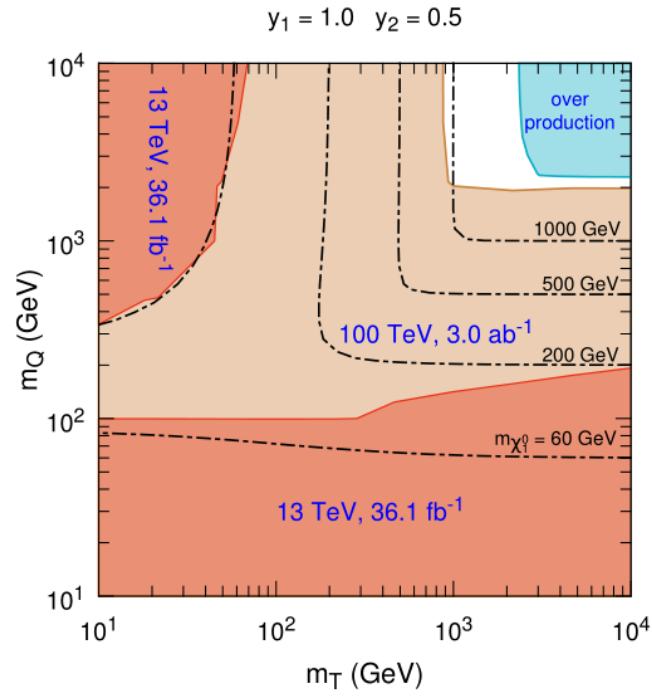
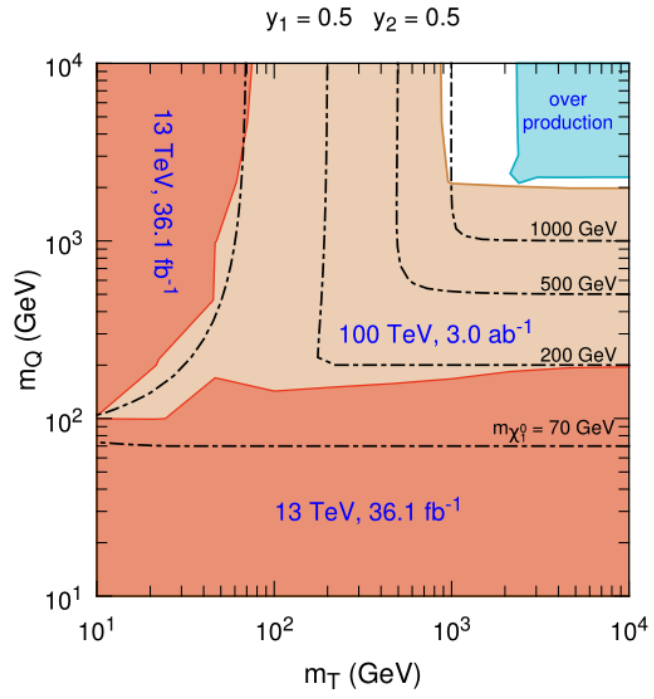
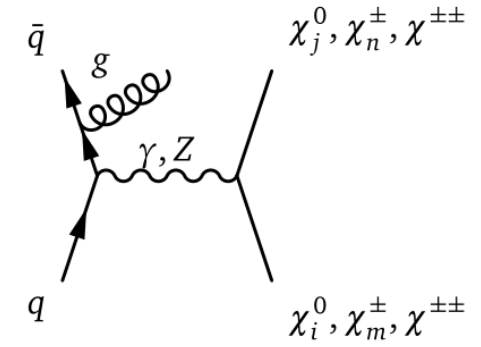
(c)  $y_1 = 0.3, y_2 = 0.7$



(d)  $y_1 = 1.0, y_2 = -0.4$

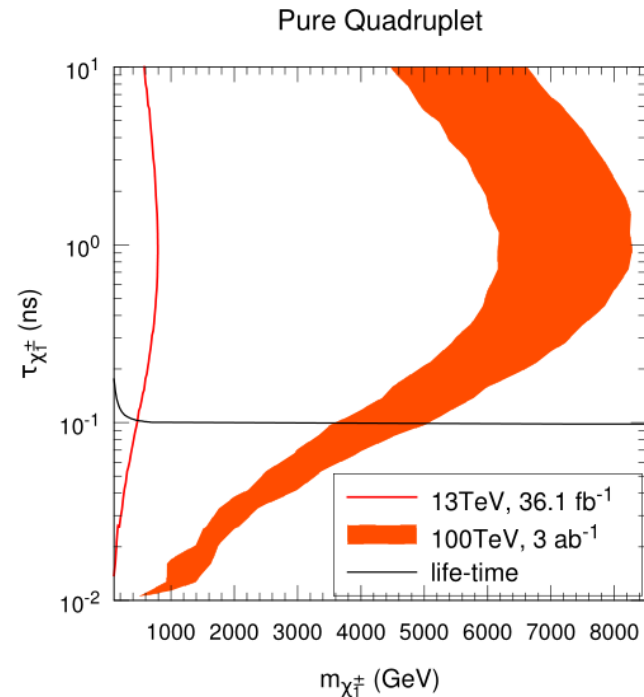
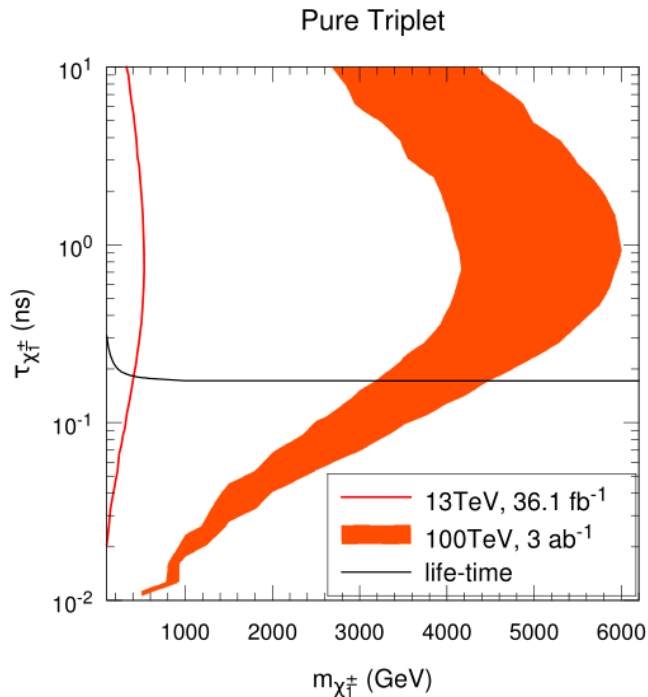
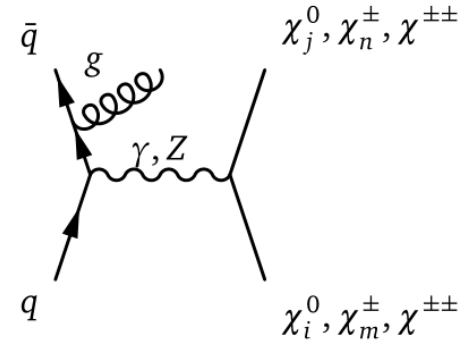
# Constraints from mono-jet like channel

- New light particle may directly produced at high energy colliders.
- The DM candidate  $\chi_1^0$  will be the **missing energy**, additional jets are used to tag the events.
- The **relic density** has been calculated including **coannihilation effects**.



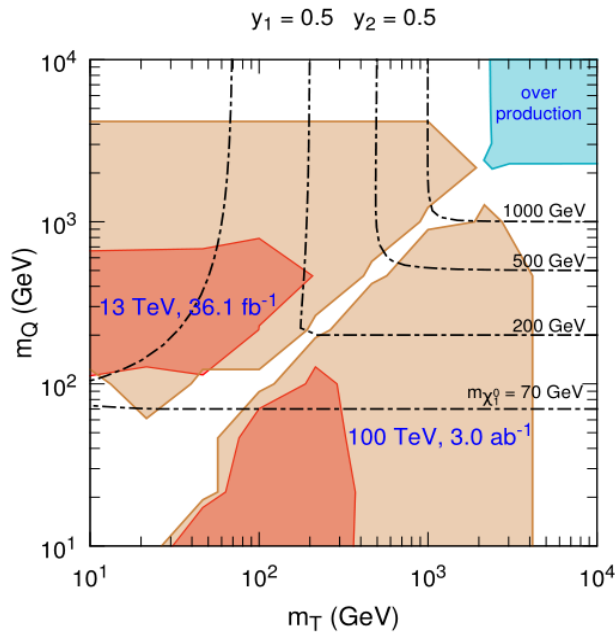
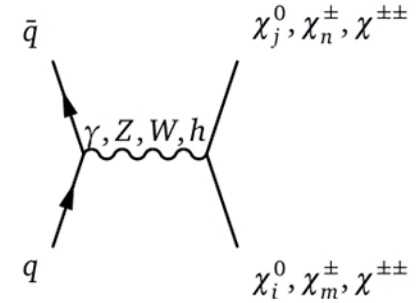
# Constraints from disappearing track channel

- In the **custodial limit**, the mass split only comes from loop correction at order of **167 MeV**.
- Even  $y_1 \neq y_2$ , the mass degenerate is ubiquitous.
- Two different cases are considered: **pure triplet** and **pure quadruplets**.

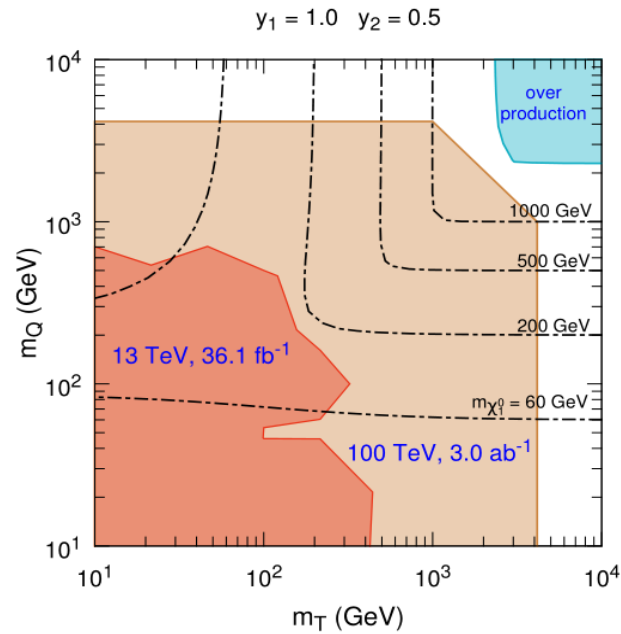


# Constraints from multilepton channel

- The heavier charged and neutral dark sector particles can decay into lighter ones plus leptons ;
- We focus on the cases which contain **two or three leptons in the final state**.
- The **relic density** has been calculated for completeness.



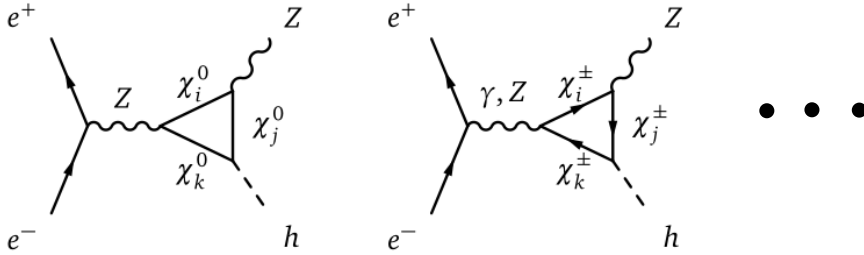
(a)  $y_1 = y_2 = 0.5$



(b)  $y_1 = 1.0, y_2 = 0.5$

# Constraints from $e^+e^- \rightarrow hZ$ channel

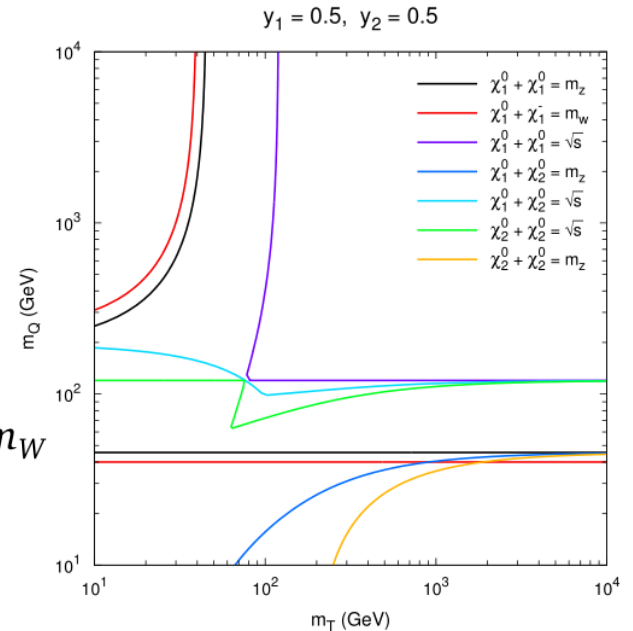
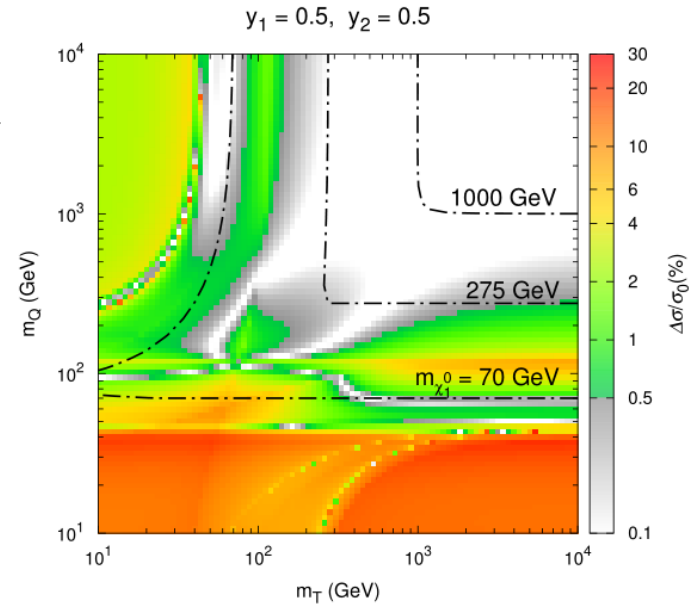
We use **FeynArts** and **FormCalc** to calculate the **one-loop** correction to  $e^+e^- \rightarrow hZ$  channel.



Color regions:  $\Delta\sigma_{ZH}/\sigma_{ZH} \geq 0.5\%$  with  $\sqrt{s} = 240 \text{ GeV}, 5 \text{ ab}^{-1}$

The **threshold effects** have been used to explain the results.

- $m_{\chi_i^0} + m_{\chi_j^0} = m_Z(m_H), m_{\chi_i^\pm} + m_{\chi_j^\pm} = m_Z(m_H), m_{\chi_i^0} + m_{\chi_j^\pm} = m_W$
- $m_{\chi_i^0} + m_{\chi_j^0} = \sqrt{s}, m_{\chi_i^\pm} + m_{\chi_j^\pm} = \sqrt{s}$



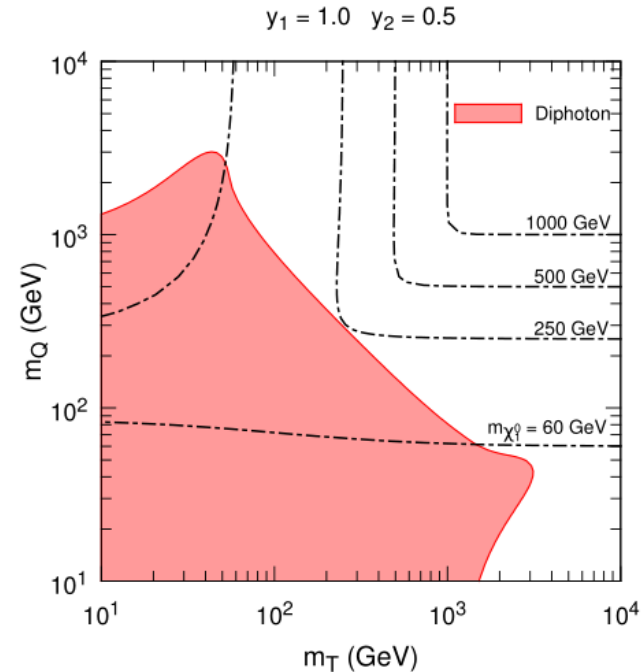
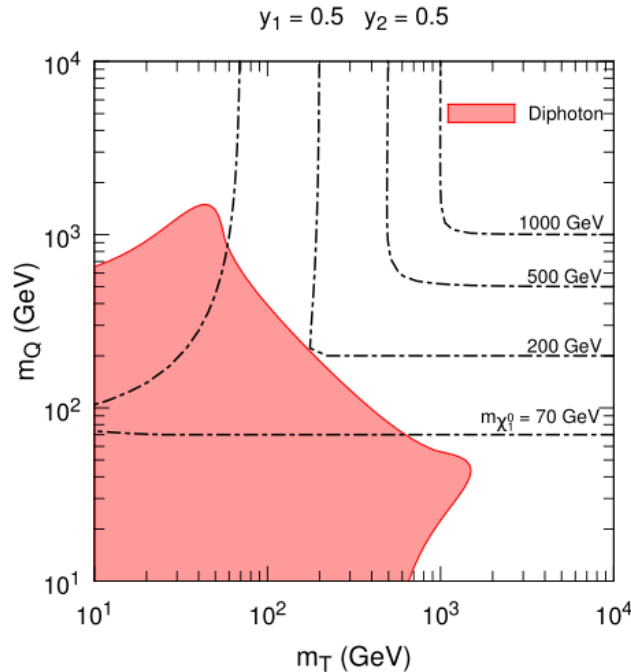
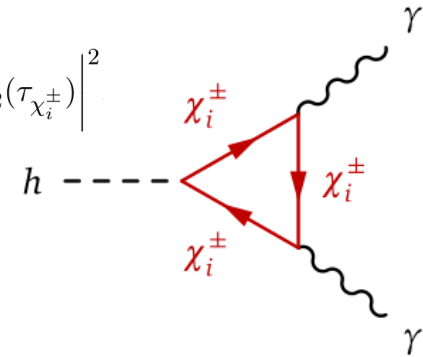
# Constraints from $h \rightarrow \gamma\gamma$ channel

In this model, the dark sector can come into the loop and modified the

partial decay width of higgs. 
$$\Gamma_{\gamma\gamma} = \frac{G_F \alpha^2 m_h^3}{128 \sqrt{2} \pi^3} \left| \sum_f N_c Q_f^2 A_{1/2}(\tau_f) + A_1(\tau_W) + \sum_i \frac{G_{h,ii} v}{m_{\chi_i^\pm}} A_{1/2}(\tau_{\chi_i^\pm}) \right|^2$$

$$G_{h,ii} = \text{Re} \left( -\frac{y_1}{\sqrt{2}} C_{L,2i} C_{R,1i} + \frac{y_1}{\sqrt{6}} C_{L,1i} C_{R,2i} + \frac{y_2}{\sqrt{6}} C_{L,3i} C_{R,1i} - \frac{y_2}{\sqrt{2}} C_{L,1i} C_{R,3i} \right)$$

$\Gamma_{\gamma\gamma} \propto \kappa_\gamma^2$  so the constraints to  $\kappa_\gamma$  can be used to constrain  $\Gamma_{\gamma\gamma}$



# Summary

- I introduce the **motivations** of the DM research, and investigate the **triplet-quadruplet dark matter model**;
- The **approximate custodial symmetry** is studied and the **one-loop mass corrections** are calculated at order of **167 MeV**;
- For the hadron colliders, the mono-jet like channel, disappearing track channel and multilepton channel are considered;
- For the electron colliders, the  $e^+e^- \rightarrow hZ$  channel and  $h \rightarrow \gamma\gamma$  channel are considered;
- The **relic density** also have been calculated with considering the effects of **co-annihilation**.

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Thank you