



# Higgs inflation and cosmological electroweak phase transition with $N$ scalars in the post-Higgs era

Department of physics, Chongqing University

Speaker: Wei Cheng

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Based on latest work with Ligong-Bian

[arXiv:1805.00199](https://arxiv.org/abs/1805.00199)



# Outline

01

**Motivation**

02

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03

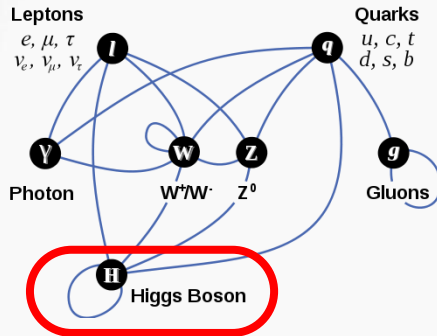
**High scale and low  
scale phenomenologies**

04

**Summary**

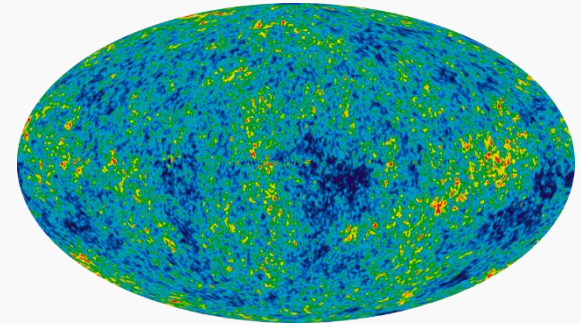
# 1. Motivation

The standard model of particle physics (SM)



## Problems

- Horizon and flatness
- Existence of dark matter
- Baryon asymmetry



CMB

## Solving

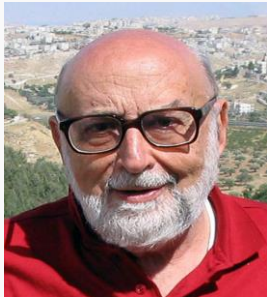
- Cosmic inflation

In order to solve the problems of horizon and flatness in the cosmology of thermal big bang, Guth made it clear in the early 1980s that **the universe**

**under went a period of near exponential acceleration before the big bang.** universe's violent expansion is also called inflation. It was the violent expansion of the universe during the period of The process of the inflation that wiped out the inhomogeneity and anisotropy of the early universe.



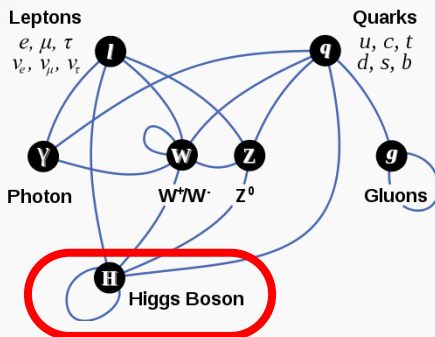
Peter Higgs



François Englert

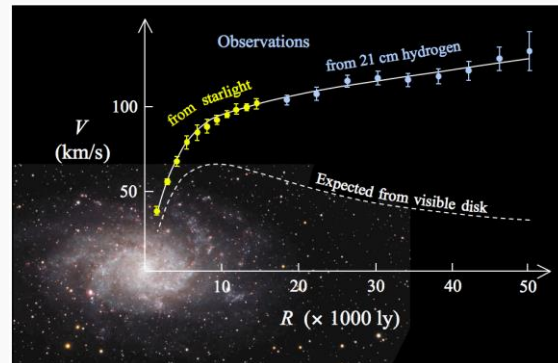
# 1. Motivation

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## Problems

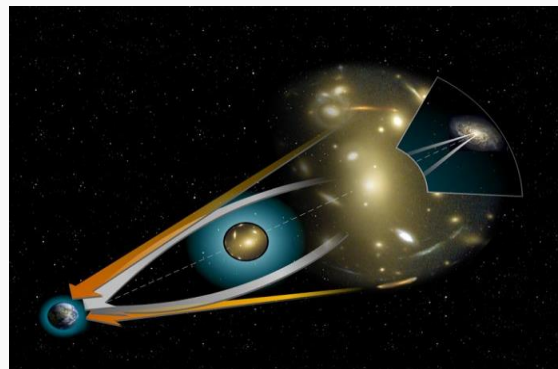
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[Rotation curve of a disc galaxy](#)

## Solving

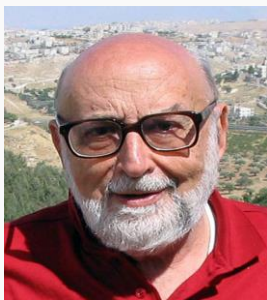
b) Extend SM



[Gravitational lens](#)



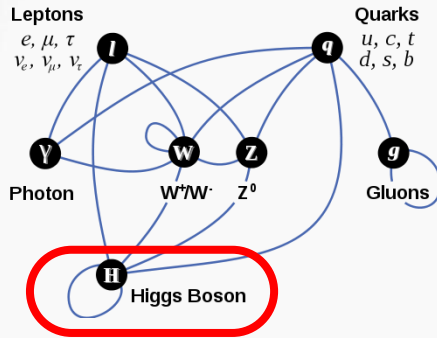
[Peter Higgs](#)



[François Englert](#)

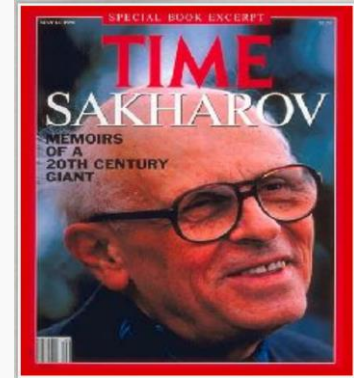
# 1. Motivation

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## Problems

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The Sakharov conditions :

- ★ Baryon number violation
- ★ C&CP violation
- ★ Departure from thermal equilibrium

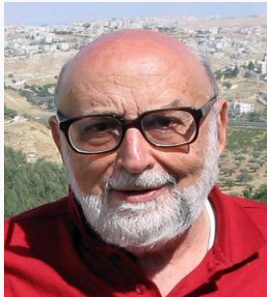
## Solving

- strong first order electroweak phase transitions ( **SFOEWPT** )

The mechanism of Electroweak baryogenesis (EWBG) can solve the puzzle of the BAU with a SFOEWPT occurs at the electroweak scale, followed by the electroweak symmetry breaking.



[Peter Higgs](#)

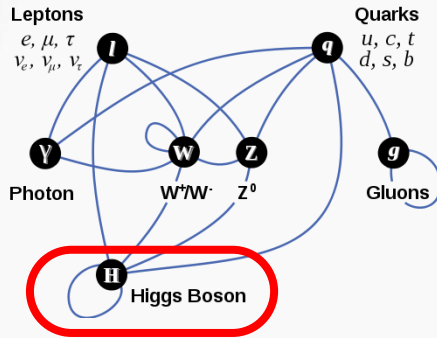


[François Englert](#)



# 1. Motivation

The standard model of particle physics (SM)



## Problems

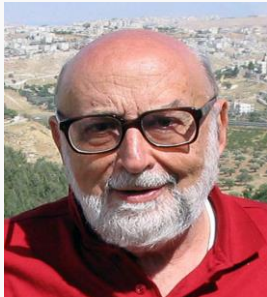
- A. Horizon and flatness
- B. Existence of dark matter
- C. Baryon asymmetry

## Combination of those theory simultaneously

		Inflation	SFOEWPT	Abundant
SM + One singlet scalar		Small $\lambda_{hs}$	Large $\lambda_{hs}$	Under
SM + N singlet scalars	O(N)		☹️	😊
	O(N → N-1)		😊	😊



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## 2 Models

### The zero temperature tree-level potential

$$V_0(H, S) = -\mu_h^2 H^\dagger H + \lambda_h |H^\dagger H|^2 + \frac{\mu_s^2}{2} S_i S_i + \frac{\lambda_s}{4} (S_i S_i)^2 + \frac{1}{2} \lambda_{hs} |H|^2 S_i S_i, \\ \text{with } H^T = (G^+, (v + h + iG^0)/\sqrt{2}).$$

#### 01 $O(N)$ scenario

After the spontaneously symmetry breaking of the Electroweak symmetry, the mass term of  $S_i$  is given as

$$m_{S_i}^2 = \mu_s^2 + \lambda_{hs} v^2 / 2$$

#### 02 $O(N \rightarrow N-1)$ scenario

The  $N$  singlet scalar  $S_i$  with  $O(N)$  being spontaneously broken to  $O(N-1)$  symmetry

$$\left. \frac{dV_0(h, s, A)}{dh} \right|_{h=v} = 0, \quad \left. \frac{dV_0(h, s, A)}{ds} \right|_{s=v_s} = 0$$

$$\mu_h^2 = \lambda_h v^2 + \lambda_{hs} v_s^2 / 2, \quad \mu_s^2 = -(\lambda_{hs} v^2 / 2 + \lambda_s v_s^2).$$

$$\mathcal{M}^2 = \begin{pmatrix} 2v^2 \lambda_h & v v_s \lambda_{hs} \\ v v_s \lambda_{hs} & 2v_s^2 \lambda_s \end{pmatrix} \quad R = \begin{pmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{pmatrix}$$

$$m_{h_1, h_2}^2 = \lambda_h v^2 + \lambda_s v_s^2 \quad \lambda_h = \frac{m_{h_2}^2 \sin^2 \theta + m_{h_1}^2 \cos^2 \theta}{2v^2},$$

$$\mp \frac{\lambda_s v_s^2 - \lambda_h v^2}{\cos 2\theta}, \quad \lambda_s = \frac{m_{h_2}^2 \cos^2 \theta + m_{h_1}^2 \sin^2 \theta}{2v_s^2},$$

$$\lambda_{hs} = \frac{(m_{h_2}^2 - m_{h_1}^2) \sin 2\theta}{2v v_s}.$$

## 2.1 Theoretical constraints

I

### Perturbativity

$$|\lambda_h| < 1, \quad |\lambda_s| < \sqrt{4\pi},$$

$$|\lambda_{sh}| < \sqrt{4\pi}.$$

II

### Vacuum stability

$$\lambda_h > 0, \quad \lambda_s > 0, \quad \lambda_{sh} > 0$$

$$\text{or } \lambda_{sh} > -2\sqrt{\lambda_h\lambda_s}.$$

III

### Perturbative unitarity

$$\frac{1}{32\pi} \left( 3\lambda + (N+2)\lambda_s + \sqrt{(3\lambda - (N+2)\lambda_s)^2 + 4N\lambda_{hs}^2} \right) < \frac{1}{2}$$

## RGE

$$\beta_{g_s} = \frac{g_s^3}{(4\pi)^2}(-7) + \frac{g_s^3}{(4\pi)^4} \left( \frac{11}{6}g'^2 + \frac{9}{2}g^2 - 26g_s^2 - 2x_h y_t^2 \right),$$

$$\beta_g = \frac{g^3}{(4\pi)^2} \left( -\frac{39-x_h}{12} \right) + \frac{g^3}{(4\pi)^4} \left( \frac{3}{2}g'^2 + \frac{35}{6}g^2 + 12g_s^2 - \frac{3}{2}x_h y_t^2 \right),$$

$$\beta_{g'} = \frac{g'^3}{(4\pi)^2} \left( \frac{81+x_h}{12} \right) + \frac{g'^3}{(4\pi)^4} \left( \frac{199}{18}g'^2 + \frac{9}{2}g^2 + \frac{44}{3}g_s^2 - \frac{17}{6}x_h y_t^2 \right),$$

$$\beta_{\lambda_h} = \frac{1}{(4\pi)^2} \left( 6(1+3x_h^2)\lambda_h^2 - 6y_t^4 + \frac{3}{8}(2g^4 + (g^2 + g'^2)^2) + \lambda_h\gamma_h + \frac{Nx_s^2}{2}\lambda_{sh}^2 \right),$$

$$\beta_{\lambda_{sh}} = \frac{\lambda_{sh}}{(4\pi)^2} \left( 12x_h^2\lambda_h + 4x_h x_s \lambda_{sh} + 6Nx_s^2\lambda_s + 6y_t^2 - \frac{9}{2}g^2 - \frac{3}{2}g'^2 \right),$$

$$\beta_{\lambda_s} = \frac{1}{(4\pi)^2} (18Nx_s^2\lambda_s^2 + 2x_h^2\lambda_{sh}^2),$$

$$\beta_{y_t} = \frac{y_t}{(4\pi)^2} \left[ -\frac{9}{4}g^2 - \frac{17}{12}g'^2 - 8g_s^2 + \frac{23+4s}{6}y_t^2 \right].$$

with  $\gamma_h = (-9g^2 - 3g'^2 + 12y_t^2)$ ,  $g$ ,  $g'$  and  $y_t$  are the standard model  $SU(2)$ ,  $U(1)$

and top-quark Yukawa couplings, and

$$x_h = \frac{1 + \xi_h h^2 / M_p^2}{1 + \xi_h h^2 / M_p^2 + 6\xi_h^2 h^2 / M_{pl}^2}, \quad x_s = \frac{1 + \xi_s s^2 / M_p^2}{1 + \xi_s s^2 / M_p^2 + 6\xi_s^2 s^2 / M_{pl}^2}.$$



## 2.2 Higgs precisions

$$\mathcal{L} \supset \frac{c_H}{\Lambda^2} O_H + \frac{c_6}{\Lambda^2} O_6 \quad \text{With } O_H \equiv \frac{1}{2}(\partial|H^\dagger H|)^2 \quad O_6 \equiv |H^\dagger H|^3$$

Tree-level	Loop-level
$c_H^N = N \frac{\lambda_{hs}^2}{2\lambda_s}, \quad c_6^N = 0,$	$c_H^N = \frac{N\lambda_{hs}}{48\pi^2}, \quad c_6^N = -\frac{N\lambda_{hs}^3}{48\pi^2},$
$c_H^{N \rightarrow N-1} = \frac{\lambda_{hs}^2}{2\lambda_s}, \quad c_6^{N \rightarrow N-1} = 0.$	$c_H^{N \rightarrow N-1} = \frac{\lambda_{hs}}{48\pi^2}, \quad c_6^{N \rightarrow N-1} = -\frac{\lambda_{hs}^3}{48\pi^2}.$

$$\mathcal{L}_{eff} \supset (1 + \delta Z_h) \frac{1}{2} (\partial_\mu h)^2$$

with  $\delta Z_h = 2v^2 c_H / m_{S(h_2)}^2$  for  $O(N)$  ( $O(N \rightarrow N-1)$ )

## 2.2 Higgs precisions

### For O(N) scenario

I Confining to N and  $\lambda_{hs,s}$  from LHC, ILC, CEPC, and FCC-ee.

Production cross section of  $e^+e^- \rightarrow hZ$ :

$$\delta\sigma_{Zh} = -2 \frac{v^2 c_H}{m_{S(h_2)}^2} \quad \text{where} \quad c_H^N v^2 / (2m_S^2) \sim N \lambda_{hs}^2 v^2 / (2\lambda_s m_S^2)$$

II Confining from the S and T parameters.

$$\Delta S = \frac{1}{12} c_H \frac{v^2}{m_{S(h_2)}^2} \log\left(\frac{m_{S(h_2)}^2}{m_W^2}\right)$$

$$\Delta T = -\frac{3}{16\pi c_W^2} c_H \frac{v^2}{m_{S(h_2)}^2} \log\left(\frac{m_{S(h_2)}^2}{m_W^2}\right)$$

**Gfitter Group**

**Eur. Phys. J. C 74, 3046 (2014)**

**doi:10.1140/epjc/s10052-014-3046-5**

$S = 0.06 \pm 0.09, T = 0.10 \pm 0.07$

## 2.2 Higgs precisions

For  $O(N \rightarrow N-1)$  scenario

I **Confine from the T parameter.**

$$T = - \left( \frac{3}{16\pi s_W^2} \right) \left\{ \cos^2 \theta \left[ \frac{1}{c_W^2} \left( \frac{m_{h_1}^2}{m_{h_1}^2 - M_Z^2} \right) \ln \frac{m_{h_1}^2}{M_Z^2} - \left( \frac{m_{h_1}^2}{m_{h_1}^2 - M_W^2} \right) \ln \frac{m_{h_1}^2}{M_W^2} \right] + \sin^2 \theta \left[ \frac{1}{c_W^2} \left( \frac{m_{h_2}^2}{m_{h_2}^2 - M_Z^2} \right) \right. \right. \\ \left. \left. \times \ln \frac{m_{h_2}^2}{M_Z^2} - \left( \frac{m_{h_2}^2}{m_{h_2}^2 - M_W^2} \right) \ln \frac{m_{h_2}^2}{M_W^2} \right] \right\},$$

## 2.2 Higgs precisions

For  $O(N \rightarrow N-1)$  scenario

II Confine from the invisible decay.

$$\mathcal{L} \supset \lambda_{h_i h_j h_j} h_i h_j h_j + \lambda_{h_i s_{N-1} s_{N-1}} h_i s_{N-1} s_{N-1}$$

$$\lambda_{h_2 h_1 h_1} = -\frac{m_{h_1}^2}{2v v_s} \sin(2\theta) (v_s \cos\theta + v \sin\theta) (1 + m_{h_2}^2 / 2m_{h_1}^2),$$

$$\lambda_{h_2 s_{N-1} s_{N-1}} = m_{h_2}^2 \cos\theta / (2v_s),$$

$$\lambda_{h_1 s_{N-1} s_{N-1}} = -m_{h_1}^2 \sin\theta / (2v_s),$$

$$\lambda_{h_1 h_2 h_2} = \lambda_{h_1 s_{N-1} s_{N-1}}.$$

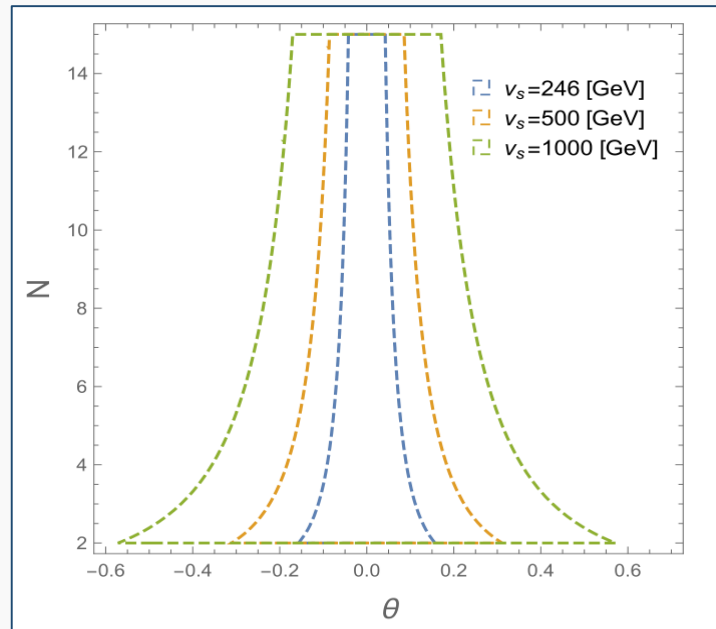
$$\Gamma_{h_2}^{tot} = \Gamma_{h_2}(h_2 \rightarrow h_1 h_1) + \sin^2\theta \Gamma_h \Big|_{m_h \rightarrow m_{h_2}} + (N-1) \Gamma_{h_2}(h_2 \rightarrow s_{N-1} s_{N-1})$$

$$= \Gamma_{h_2}(h_2 \rightarrow h_1 h_1) + \sin^2\theta \Gamma_h^{SM} \Big|_{m_h \rightarrow m_{h_2}} + (N-1) \frac{\lambda_{h_2 s_{N-1} s_{N-1}}^2}{32\pi m_{h_2}}$$

$$\Gamma_{h_1}^{tot} = \cos^2\theta \Gamma_h^{SM} + (N-1) \Gamma_h(h \rightarrow s_{N-1} s_{N-1})$$

$$= \cos^2\theta \Gamma_h^{SM} + (N-1) \frac{\lambda_{h_1 s_{N-1} s_{N-1}}^2}{32\pi m_{h_1}},$$

$$\Gamma(h_2 \rightarrow h_1 h_1) = \frac{\lambda_{h_2 h_1 h_1}^2}{32\pi m_{h_2}} \sqrt{1 - 4m_{h_1}^2/m_{h_2}^2}. \quad \Gamma(h_1 \rightarrow h_2 h_2) = \frac{\lambda_{h_1 h_2 h_2}^2}{32\pi m_{h_1}} \sqrt{1 - 4m_{h_2}^2/m_{h_1}^2}.$$



LHC (ATLAS+CMS) set  $B_{BSM} < 0.34$  at 95% CL.

### 3.1 The Higgs inflation with N singlet scalars

Action

$$\tilde{g}_{\mu\nu} = \Omega^2 g_{\mu\nu}, \quad \Omega^2 \equiv 1 + \frac{\xi_s S^2}{M_{\text{P}}^2} + \frac{\xi_h h^2}{M_{\text{P}}^2}.$$

$$\frac{d\chi_h}{dh} = \sqrt{\frac{\Omega^2 + 6\xi_h^2 h^2/M_{\text{P}}^2}{\Omega^4}}, \quad \frac{d\chi_s}{ds} = \sqrt{\frac{\Omega^2 + 6\xi_s^2 S^2/M_{\text{P}}^2}{\Omega^4}},$$

Conformal Transformation

01

$S_J$

02

$CT$

03

$S_E$

Action in the Jordan frame

$$S_J = \int d^4x \sqrt{-g} \left[ -\frac{M_{\text{P}}^2}{2} R - \xi_h (H^\dagger H) R - \xi_s S^2 R + \partial_\mu H^\dagger \partial^\mu H + (\partial_\mu S)^2 - V(H, S) \right],$$

Action in the Einstein frame

$$S_E = \int d^4x \sqrt{-\tilde{g}} \left( -\frac{1}{2} M_{\text{P}}^2 R + \frac{1}{2} \partial_\mu \chi_h \partial^\mu \chi_h + \frac{1}{2} \partial_\mu \chi_s \partial^\mu \chi_s + A(\chi_s, \chi_h) \partial_\mu \chi_h \partial^\mu \chi_s - U(\chi_s, \chi_h) \right),$$

### 3.1 The Higgs inflation with N singlet scalars

$S_{\text{inf}}$

**h-direction inflation**

$$S_{\text{inf}} = \int d^4x \sqrt{\tilde{g}} \left[ \frac{M_{\text{p}}^2}{2} R + \frac{1}{2} (\partial\chi)^2 - U(\chi) \right],$$

where

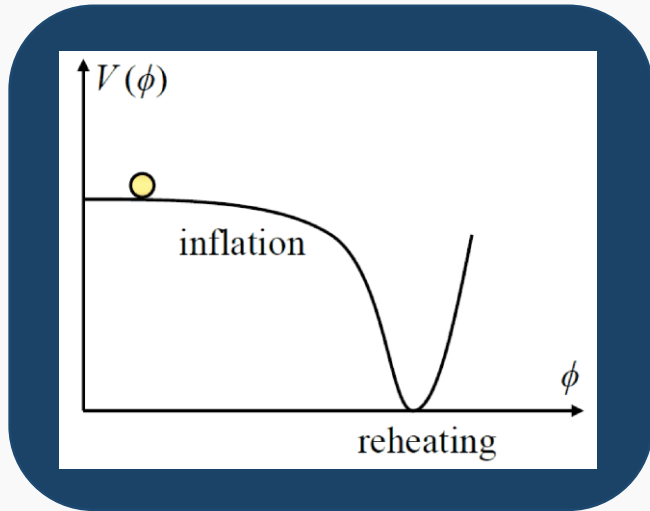
$$U(\chi) = \frac{\lambda_h (h(\chi))^4}{4\Omega^4},$$

$$\frac{d\chi}{dh} \approx \left( (1 + \xi_h h^2 / M_{\text{p}}^2 + 6\xi_h^2 h^2 / M_{\text{p}}^2) / (1 + \xi_h h^2 / M_{\text{p}}^2)^2 \right)^{1/2}$$



### 3.1 The Higgs inflation with N singlet scalars

#### Constrains



Slow-roll inflation

1

The slow-roll parameters

$$\epsilon(\chi) = \frac{M_{\text{P}}^2}{2} \left( \frac{dU/d\chi}{U(\chi)} \right)^2,$$

$$\eta(\chi) = M_{\text{P}}^2 \left( \frac{d^2U/d\chi^2}{U(\chi)} \right).$$

$$(\epsilon \ll 1 \text{ and } |\eta| \ll 1)$$

2

The e-folding numbers

$$N_{e\text{-folds}} = \int_{\chi_{\text{end}}}^{\chi_{\text{in}}} d\chi \frac{1}{M_{\text{P}} \sqrt{2\epsilon}}.$$

$$(N_{e\text{-fold}} \sim 60)$$

## 3.1 The Higgs inflation with N singlet scalars

### Observables

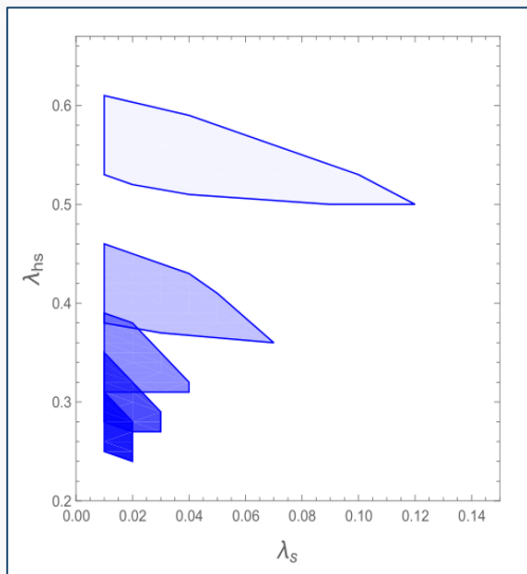
Spectrum index  $n_s = 1 + 2\eta - 6\varepsilon \sim 0.97$

Tensor to scalar  $r = 16\varepsilon < 0.11$

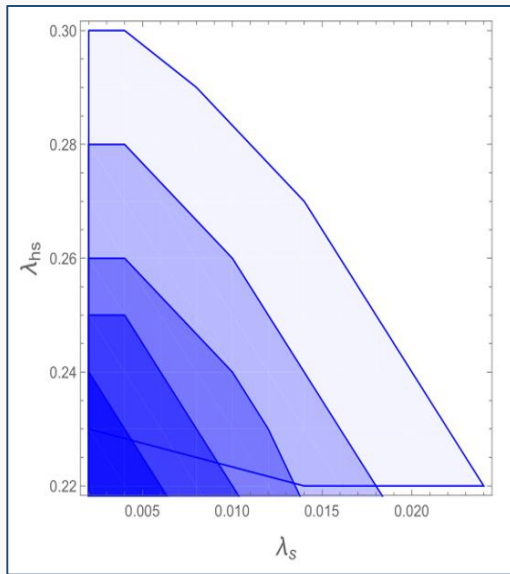
Amplitude of scalar spectrum fluctuations

$$\Delta_{\mathcal{R}}^2 = \frac{1}{24\pi^2 M_{\text{p}}^4} \frac{U(\chi)}{\varepsilon} = 2.2 \times 10^{-9}.$$

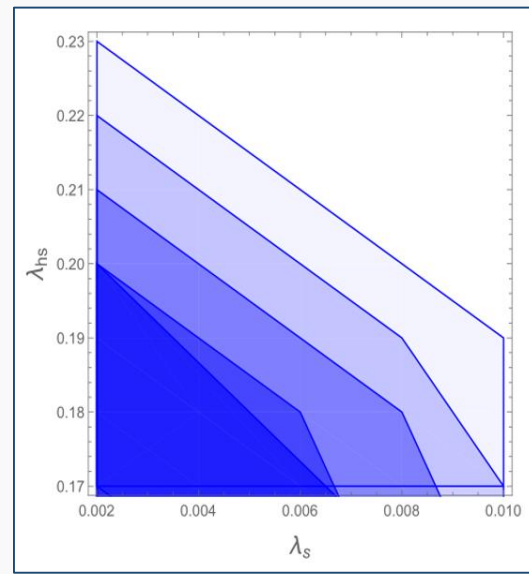
### 3.1.1 $O(N)$ scenario



$N$  are 1  $\rightarrow$  5



$N$  are 6  $\rightarrow$  10

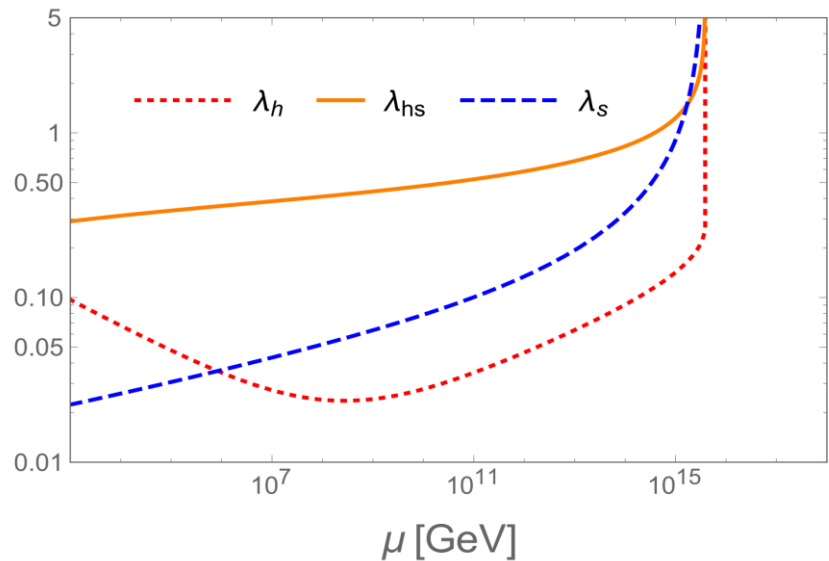
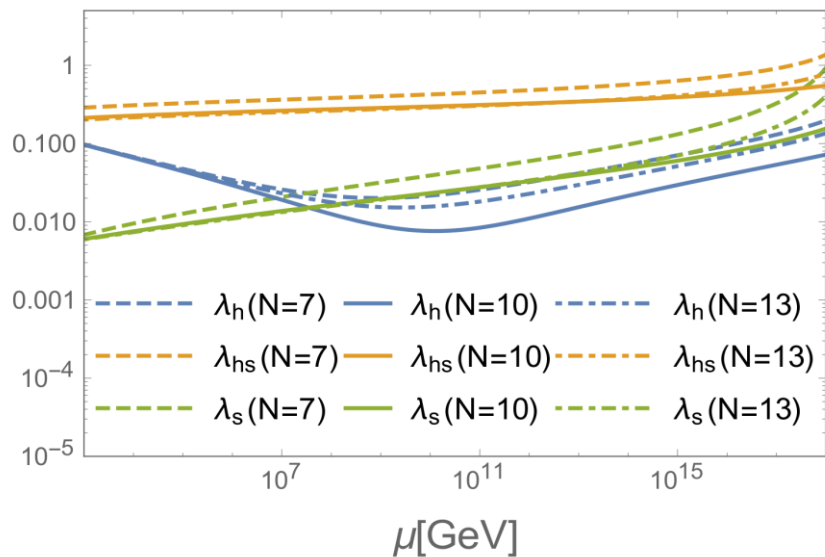


$N$  are 11  $\rightarrow$  15

Inflation feasible  $(\lambda_s, \lambda_{hs})$  plane for different  $N$  with in  $O(N)$  scalar model, the larger  $N$  is shown by the deeper color.

### 3.1.1 O(N) scenario

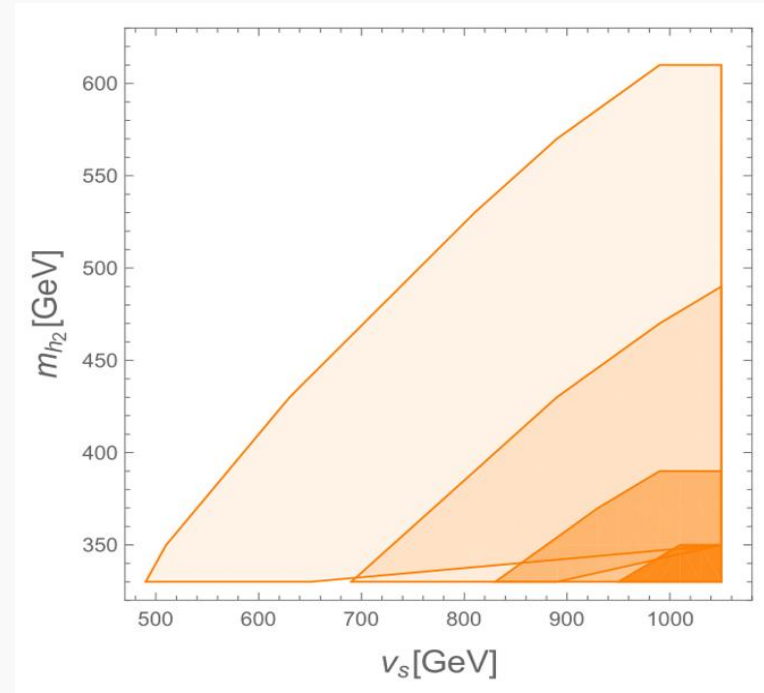
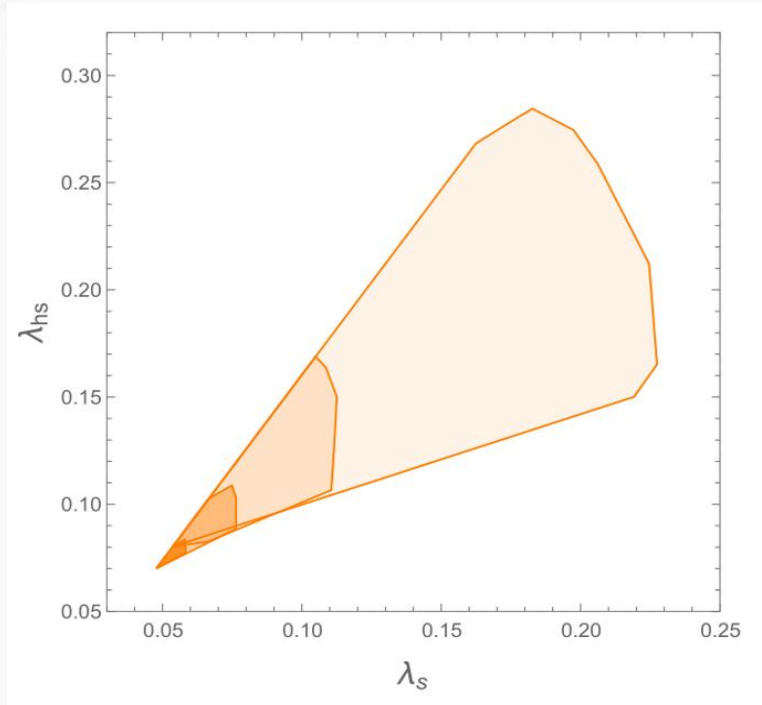
## RG running of couplings



The quartic couplings where the inflation is valid.

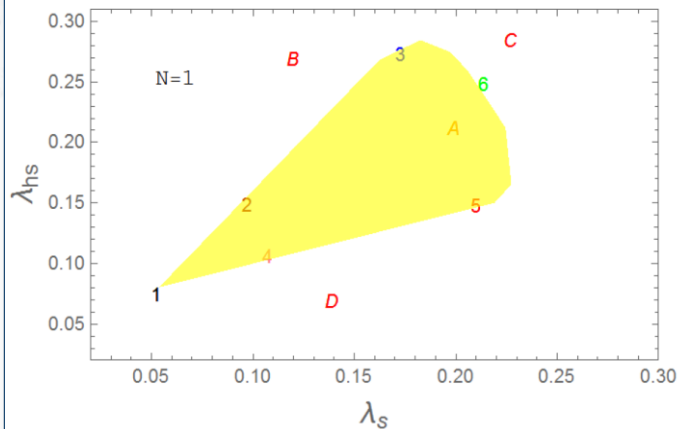
The quartic couplings lives in the parameter region where the inflation is invalid.

### 3.1.2 $O(N \rightarrow N-1)$ scenario

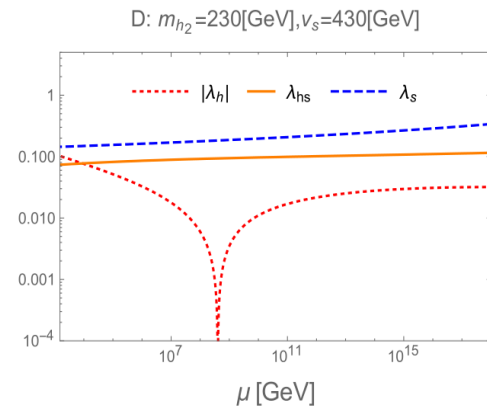
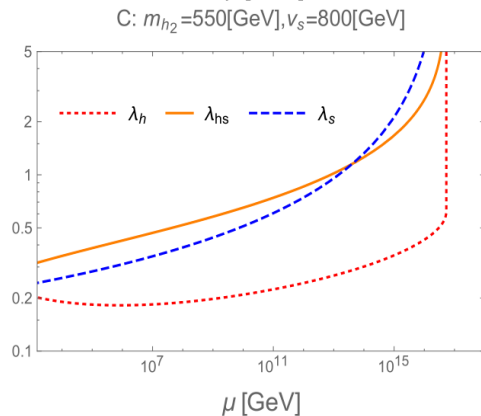
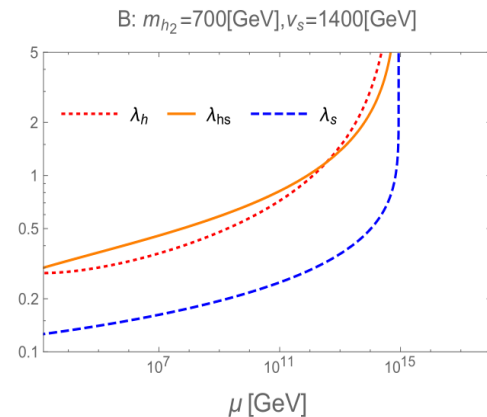
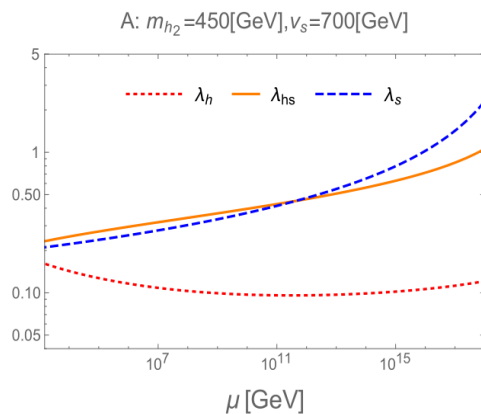


Inflation feasible  $(\lambda_s, \lambda_{h_2})$  and  $(v_s, m_{h_2})$  plane for different  $N$  within  $O(N \rightarrow N-1)$  scalar model, a deeper color corresponds to a larger  $N$ , the corresponding  $N$  are 1, 2, 3 and 4, respectively.

## 3.1.2 $O(N \rightarrow N-1)$ scenario



- 1  $m_{h_2}=330[\text{GeV}], v_s=1000[\text{GeV}]$
- 2  $m_{h_2}=450[\text{GeV}], v_s=1000[\text{GeV}]$
- 3  $m_{h_2}=600[\text{GeV}], v_s=1000[\text{GeV}]$
- 4  $m_{h_2}=330[\text{GeV}], v_s=700[\text{GeV}]$
- 5  $m_{h_2}=330[\text{GeV}], v_s=500[\text{GeV}]$
- 6  $m_{h_2}=500[\text{GeV}], v_s=750[\text{GeV}]$





## 3.2 Electroweak phase transitions

### The effective potential:

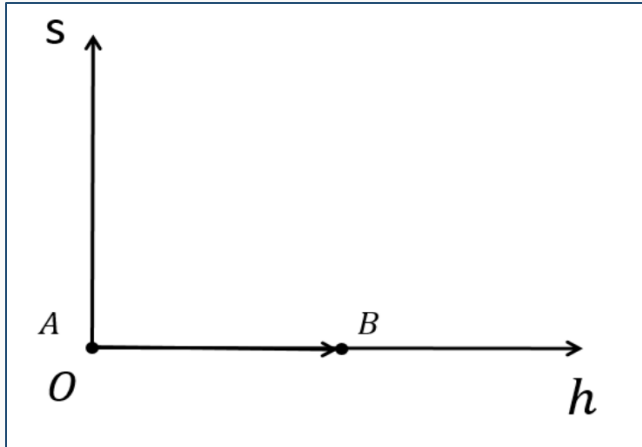
Coleman-Weinberg potential

$$V(h, s, N, T) = V_0(h, s) + V_{CW}(h, n) + V_T(h, n, T) + V_{ring}(h, N, T),$$

Tree level scalar potential

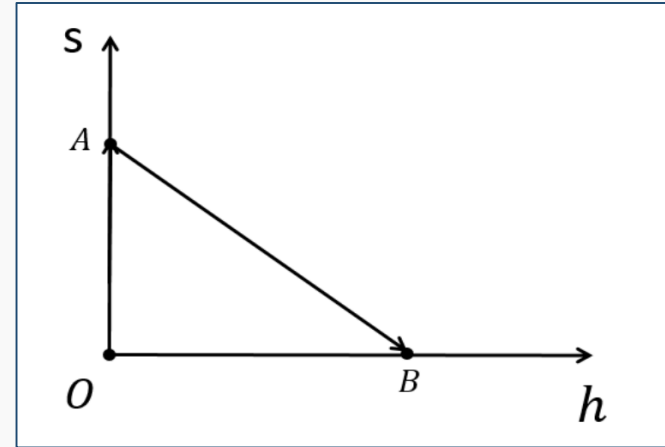
Finite temperature corrections

### 3.2.1 O (N) scenario



One-step EWPT type

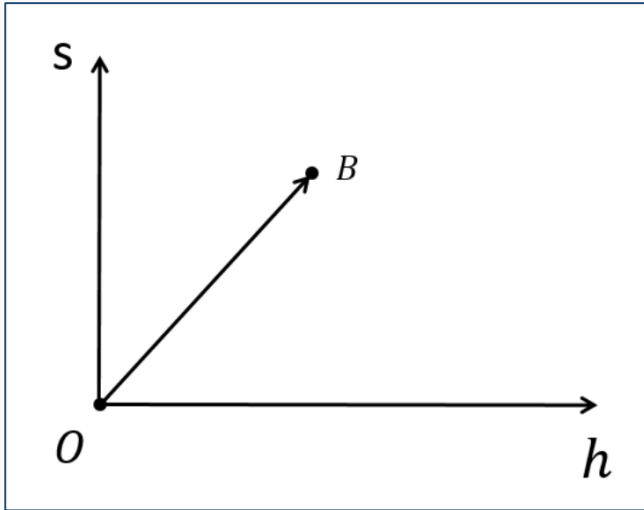
$$V(0,0,N,T_C) = V(h_C^B,0,N,T_C) ,$$
$$\frac{dV(h,0,N,T_C)}{dh} \Big|_{h=h_C^B} = 0 ,$$



Two-step EWPT type

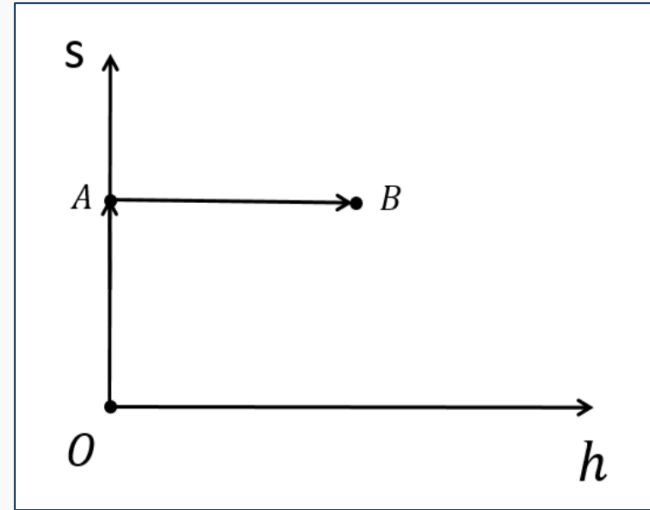
$$V(0,s_C^A,N,T_C) = V(h_C^B,0,N,T_C) ,$$
$$\frac{dV(h,0,N,T_C)}{dh} \Big|_{h=h_C^B} = 0 ,$$

### 3.2.2 $O(N \rightarrow N-1)$ scenario



One-step EWPT type

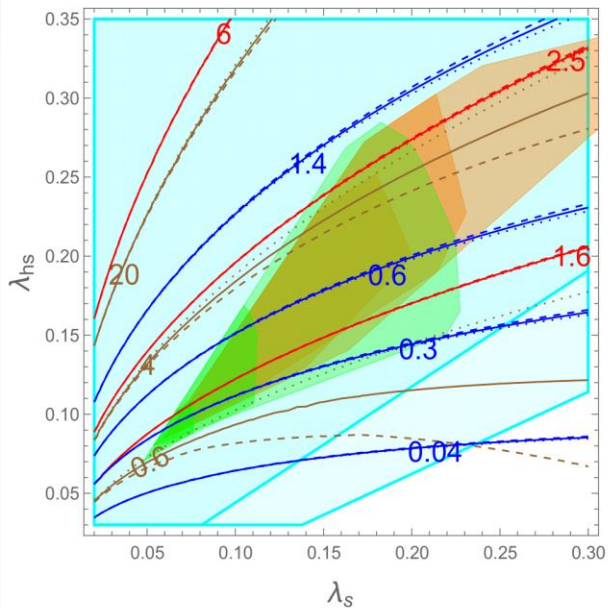
$$V(0, 0, N, T_C) = V(v_C^B, s_C^B, N, T_C),$$
$$\frac{dV(h, s, N, T_C)}{dh} \Big|_{h=h_C^B, s=s_C^B} = 0,$$
$$\frac{dV(h, s, N, T_C)}{ds} \Big|_{h=h_C^B, s=s_C^B} = 0.$$



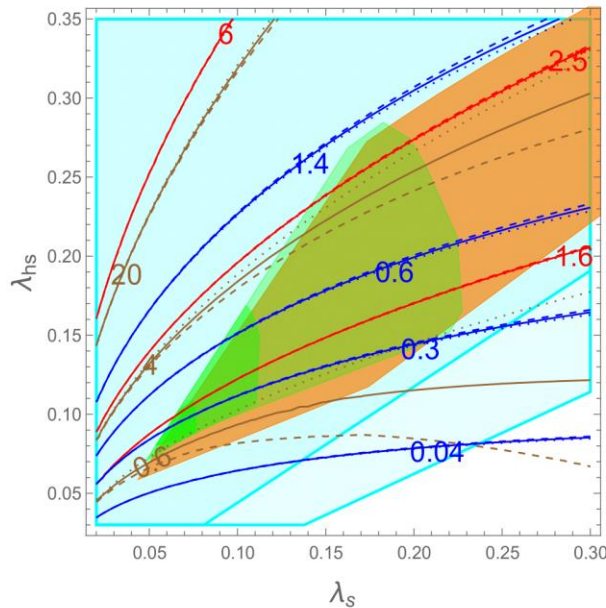
Two-step EWPT type

$$V(0, s_C^A, N, T_C) = V(h_C^B, s_C^B, N, T_C),$$
$$\frac{dV(h, s, N, T_C)}{dh} \Big|_{h=h_C^B, s=s_C^B} = 0,$$
$$\frac{dV(h, s, N, T_C)}{ds} \Big|_{h=h_C^B, s=s_C^B} = 0.$$

### 3.2.2 $O(N \rightarrow N-1)$ scenario



One-step



Two-step

$\lambda_{3h1} / \lambda_{3hSM}$

$\lambda_{h2h1h1} / \lambda_{3hSM}$

$\Gamma_{h2tot}$

SFOEWPT

Inflation

Bin $v$

## 5.Summary

- ◆ The Higgs inflation and the cosmological electroweak phase transition are studied with the N-scalars extended standard model of particle physics (SM).
- ◆ Two scenarios of N singlet scalar extended standard models are discussed in detail. One is the N singlet scalar invariant under  $O(N)$  symmetry, the other one is the N singlet scalar  $s_i$  with  $O(N)$  being spontaneously broken to  $O(N-1)$  symmetry.
- ◆  $O(N)$  can not explain the inflation and EWPT simultaneously, while  $O(N \rightarrow N-1)$  can realize at the same time.

# THANKS

