## Strong Decays of the Orbitally Excited Scalar $D_{0}^{*}$ Mesons

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## Introduction

In this work, We calculate the two-body strong decays of the orbitally excited scalar mesons $D_{0}^{*}(2400)$ and $D_{J}^{*}(3000)$.
The LHCb collaboration announced several new charmed structures in 2013, including the $D_{J}^{*}(3000)$ [1]

$$
\begin{align*}
M_{D_{J}^{*}(3000)} & =3008.1 \pm 4.0 \mathrm{MeV}  \tag{1}\\
\Gamma_{D_{J}^{*}(3000)} & =110.5 \pm 11.5 \mathrm{MeV}
\end{align*}
$$

Its parity is still uncertain in present experiments. From its decay mode of $D \pi$, many authors treat it as a natural parity particle. Considering that its mass is around 3000 MeV , the assignments of $2^{3} P_{0}, 1^{3} F_{4}, 3^{3} S_{1}, 1^{3} F_{2}$ and $2^{3} P_{2}$ are possible.
The $D^{*} \pi$ channel is forbidden for the ${ }^{3} P_{0}$ states and other assignments have both $D \pi$ and $D^{*} \pi$ decay modes. However, $D_{J}(3000)$ was only found in $D^{*} \pi$ spectrum, while $D_{J}^{*}(3000)$ only in $D \pi$ spectrum in LHCb experiment. Thus, the assignment of $2^{3} P_{0}$ for $D_{J}^{*}(3000)$ is more reasonable.

## Method

We take the channel $D_{0}^{*}(2400)^{0} \rightarrow D^{+} \pi^{-}$as an example.


Figure 1: Feynman diagram for $D_{0}^{e}(2400)^{0} \rightarrow D^{+} \pi^{-}$(with the low-energy
approximation).
By using the reduction formula, the transition matrix element can be written as

$$
\begin{align*}
T & =\left\langle D^{+}\left(P_{f 1}\right) \pi^{-}\left(P_{f 2}\right) \mid D_{0}^{*}\left(P_{i}\right)\right\rangle \\
& =\int \mathrm{d}^{4} x \mathrm{e}^{\mathrm{i} P_{f 2} \cdot x}\left(M_{f 2}^{2}-P_{f 2}^{2}\right)\left\langle D^{+}\left(P_{f 1}\right)\right| \phi_{\pi}(x)\left|D_{0}^{*}\left(P_{i}\right)\right\rangle \tag{2}
\end{align*}
$$

where, $\phi_{\pi}$ is the light pseudo-scalar meson field. By using PCAC rules, the field can be expressed as

$$
\begin{equation*}
\phi_{\pi}(x)=\frac{1}{M_{f 2}^{2} f_{\pi}} \partial^{\mu}\left(\bar{u} \gamma_{\mu} \gamma_{5} d\right) \tag{3}
\end{equation*}
$$

Inserting Eq. (3) into Eq. (2), the transition matrix can be written as

$$
\begin{align*}
T & =\frac{-\mathrm{i} P_{f 2}^{\mu}\left(M_{f 2}^{2}-P_{f 2}^{2}\right)}{M_{f 2} f_{\pi}} \int \mathrm{d}^{4} x \mathrm{e}^{i P_{f 2} \cdot x}\left\langle D^{+}\left(P_{f 1}\right)\right| \bar{u} \gamma_{\mu} \gamma_{5} d\left|D_{0}^{*}\left(P_{i}\right)\right\rangle  \tag{4}\\
& \approx-\mathrm{i} \frac{P_{f 2}^{\mu}}{f_{\pi}}(2 \pi)^{4} \delta^{4}\left(P_{i}-P_{f 1}-P_{f 2}\right)\left\langle D^{+}\left(P_{f 1}\right)\right| \bar{u} \gamma_{\mu} \gamma_{5} d\left|D_{0}^{*}\left(P_{i}\right)\right\rangle
\end{align*}
$$

Within the Mandelstam formalism, we can write the transition amplitude as:

$$
\begin{align*}
\mathcal{M} & =-\mathrm{i} \frac{P_{f 2}^{\mu}}{f_{\pi}}\left\langle D^{+}\left(P_{f 1}\right)\right| \bar{u} \gamma_{\mu} \gamma_{5} d\left|D_{0}^{*}\left(P_{i}\right)\right\rangle  \tag{5}\\
& =-i \frac{P_{f 2}^{\mu}}{f_{\pi}} \int \frac{\mathrm{d}^{3} q}{(2 \pi)^{3}} \operatorname{Tr}\left[\bar{\varphi}_{P_{f 1}}^{++}\left(q_{f 1 \perp}\right) \frac{P_{i}}{M_{i}} \varphi_{P_{i}}^{++}\left(q_{\perp}\right) \gamma_{\mu} \gamma_{5}\right]
\end{align*}
$$

If $\rho$ or $\omega$ meson appears in the final states, we choose the effective Lagrangian method to calculate the transition amplitude. The Lagrangian of quark-meson coupling can be expressed as

$$
\begin{equation*}
\mathcal{L}_{q q V}=\bar{q}_{i}\left(a \gamma_{\mu}+\frac{\mathrm{i} b}{2 M_{P_{f 2}}} \sigma_{\mu \nu} P_{f 2}^{v}\right) V_{i j}^{\mu} q_{j} \tag{6}
\end{equation*}
$$

The transition amplitudes can be expressed as

$$
\begin{equation*}
\mathcal{M}=-\mathrm{i} \int \frac{\mathrm{~d}^{3} q}{(2 \pi)^{3}} \operatorname{Tr}\left[\bar{\varphi}_{P_{f 1}}^{++}\left(q_{f 1 \perp}\right) \frac{P_{i}}{M_{i}} \varphi_{P_{i}}^{++}\left(q_{\perp}\right)\left(a \gamma_{\mu}+\frac{\mathrm{i} b}{2 M_{f 2}} \sigma_{\mu \nu} P_{f 2}^{v}\right) \varepsilon_{2}^{\mu}\right] \tag{7}
\end{equation*}
$$

The two-body decay width is

$$
\begin{equation*}
\Gamma=\frac{1}{8 \pi} \frac{\left|\vec{P}_{f 1}\right|}{M_{i}^{2}}|\mathcal{M}|^{2} \tag{8}
\end{equation*}
$$

## Results and Discussion

The results of $D_{0}^{*}(2400)^{0,+}$ as $0^{+}(1 P)$ state are shown in Table 1 . Under the assumption of $0^{+}(2 P)$ state, the results of $D_{0}^{*}(3000)^{0,+}$ are shown in Table 2-3. Considering many theoretical predictions of mass have divergence with present experimental data, we also calculate the total width changing with the mass, which is shown in Fig. 2.

Table 1: $D_{0}^{*}(2400)^{0,+}$ strong decay widths (MeV).

| Chanel | Ours | Ref. [2] | Ref. [3] | Ref. [4] | Exp. [5] |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $D_{0}^{*}(2400)^{0} \rightarrow$$D^{+} \pi^{-}$ <br> $D^{0} \pi^{0}$ | 151.5 | 74.8 | 266 | 283 | 277 | $267 \pm 40$ |
| $D^{+} \pi^{0}$ | 81.6 |  |  |  |  |  |
| $D_{0}^{*}(2400)^{+} \rightarrow$  <br> $D^{0} \pi^{+}$ 164.3 | $\square$ | $\square$ | $\square$ | $230 \pm 17$ |  |  |

Table 2: Two-body strong decay widths ( MeV ) of $D_{J}^{*}(3000)^{0}$ as the $2 P\left(0^{+}\right)$state. "-" means forbidden, "口" means not included.

| Chanel | Final States | Ours | Ref. [6] | Ref. [7] | Ref. [8] | Ref. [9] |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $D\left({ }^{1} S_{0}\right) \pi$ | $D^{+} \pi^{-}$ | 11.6 | 23.94 | 49 | 25.4 | 66.2 |
|  | $D^{0} \pi^{0}$ | 6.1 | 11.97 |  |  | 33.3 |
| $\boldsymbol{D}\left(2^{1} \boldsymbol{S}_{0}\right) \boldsymbol{\pi}$ | $D(2550)^{+} \pi^{-}$ | $6.9$ | $\square$ | $\square$ | 18.6 | $\square$ |
|  | D (2550) |  |  |  |  |  |
| $D \eta$ | $D^{0} \eta^{0}$ | 0.51 | 4.26 | 8.8 | 1.53 | 10.8 |
| $D \eta^{\prime}$ | $D^{0} \eta^{\prime 0}$ | 6.0 | 1.07 | 2.7 | 4.94 | $\square$ |
| $D_{s} K$ | $D_{s}^{+} K^{-}$ | $\sim 10^{-3}$ | 2.85 | 6.6 | 0.76 | 54.2 |
| $D_{1}(2420) \pi$ | $D_{1}(2420)^{0} \pi^{0}$ | $18.7$ | $26.20$ | 38 | 96.1 $\left({ }^{1} P_{1}\right)$ | $\square$ |
| $D_{1}(2420) \eta$ | $D_{1}(2420)^{0} \eta^{0}$ | 0.85 | 1.37 | 1.1 | $\square$ | $\square$ |
| $D_{1}(2430) \pi$ | $D_{1}(2430)^{0} \pi^{0}$ $D_{1}(2430$${ }^{+} \pi^{-}$ | 2.1 | 6.69 | 30 | $\square$ | $\square$ |
|  | $D_{1}(2430)^{+} \pi^{-}$ $D_{1}(2430)^{0} \eta^{0}$ | 4.1 | $\square$ 0.35 | 0.91 | $\square$ | $\square$ |
| $D_{s}(2460) K$ | $D_{s 1}(2460)^{+} K^{-}$ | 1.2 | 0.35 12.81 | 0.91 1.5 | $\square$ | $\square$ |
| $D^{*} \rho$ | $\begin{aligned} & D^{*}(2007)^{0} \rho^{0} \\ & D^{*}(2010)^{+} \rho^{-} \end{aligned}$ | $\begin{gathered} 7.0 \\ 13.3 \end{gathered}$ | $\begin{aligned} & 31.60 \\ & 62.01 \end{aligned}$ | 41 | 32 | $\square$ |
| $D^{*} \omega$ | $D^{*}(2007)^{0} \omega^{0}$ | 7.5 | 29.91 | 13 | 10.2 | $\square$ |
| $D_{s}^{*} K^{*}$ | $D_{s}^{*+} K^{*}(892)^{-}$ | 4.1 | 3.06 | 1.0 | $\square$ | $\square$ |
| $D_{s}(2536) K^{-}$ | $D_{s 1}(2536)^{+} K^{-}$ | - | 6.40 | - | - | - |
| TotalExperimental value |  | 130.2 | 224.5 | 193.6 | 189.5 | 164.5 |
|  |  |  | $110.5 \pm 11.5$ |  |  |  |

Table 3: Two-body strong decay widths ( MeV ) of $D_{J}^{*}(3000)^{+}$as the $2 P\left(0^{+}\right)$state.

| Chanel | Final States | Width | Chanel | Final States | Width |  |  |
| :--- | :--- | :---: | :--- | :--- | :---: | :---: | :---: |
| $D\left({ }^{1} S_{0}\right) \boldsymbol{\pi}$ | $D^{+} \pi^{0}$ | 6.5 | $D\left(2^{1} S_{0}\right) \pi$ | $D^{0} \pi^{+}$ | 3.8 |  |  |
| $D \eta$ | $D^{0} \pi^{+}$ | 13.5 | $D^{0} \pi^{+}$ | 7.7 |  |  |  |
|  | $D^{0} \eta^{0}$ | 0.56 | $D \eta^{\prime}$ | $D^{0} \eta^{\prime 0}$ | 5.7 |  |  |
| $D(2420) \pi$ | $D_{1}(2420)^{+} \pi^{0}$ | 18.3 | $D(2430) \pi$ | $D_{1}(2430)^{+} \pi^{0}$ | 2.1 |  |  |
| $D(2420) \eta$ | $D_{1}(2420)^{0} \pi^{+}$ | 37.4 | $D_{1}(2430)^{0} \pi^{+}$ | 4.3 |  |  |  |
| $D^{*} \rho$ | $D_{1}(2420)^{+} \eta^{0}$ | 0.77 | $D(2430) \eta$ | $D_{1}(2430)^{+} \eta^{0}$ | 0.11 |  |  |
| $D_{s} K$ | $D^{*}(2010)^{+} \rho^{0}$ | 6.1 | $D^{*} \omega$ | $D^{*}(2010)^{+} \omega^{0}$ | 6.5 |  |  |
|  | $D^{*}(2007)^{0} \rho^{-}$ | 12.9 | $D_{s}(2460) K$ | $D_{s 1}(2460)^{+} K^{0}$ | 1.2 |  |  |
|  | $D_{s}^{+} K^{0}$ | 0.05 | $D_{s}^{*} K^{*}$ | $D_{s}^{*+} K^{*}(892)^{0}$ | 3.8 |  |  |
|  | Total |  | 131.3 |  |  |  |  |



## References

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