Optics aberration at IP and Beam-beam effects

K. Ohmi (KEK) IHEP, 8, Nov. 2018

Introduction

- How to get the target luminosity
- Optics aberration degrade luminosity in beam-beam simulations.
- Optics correction at IP was one of key issues, since starting KEKB.
- The optics aberration is serious in SuperKEKB.
- The aberration is related to QCS mainly and also to other lattice magnets.
- 1. Design stage
- 2. Starting Phase II
- 3. Toward Phase III

Study in the design stage of SuperKEKB

- Weak-strong beam-beam simulation using SAD.
- Luminosity degradation has been seen from low bunch current.
- Interplay of beam-beam effect with lattice nonlinearity
- Skew sextupole component degrade luminosity (Y. Zhang).
- Where is the source of the nonlinearity.
- Focusing to QCS/Interaction Regin.

IR magnets and their nonlinearity

- There are many nonlinear field components in IR magnets.
- Chromatic coupling
 - ► Realistic lattice: lum. drops at low beam currents
 - ► Crab-waist:
 - To cancel beam-beam driven resonances
 - Work well at high currents, but not well at low currents



D. Zhou, SKEKB MAC 2015

BBWS : arc expressed by simple transfer matrix SAD: complex lattice structure

Y. Zhang's (IHEP) work at KEK

- Vertical orbit is induced by a large horizontal betatron oscillation.
- Skew sextupole term at IP, x²y, is suspected for the luminosity degradation.



QCS superconducting magnet system



QC1RP漏れ磁場キャンセル磁石(b3,b4,b5,b6):4台 超伝導補正ソレノイド:3台

2017/09/08

超伝導補正ソレノイド:1台

SuperKEKB 国内レビュー(2017年9月)

N. Ohuchi et al.



N. Ohuchi et al.

• Compensation solenoids [ESL, ESR1, ESR2 and ESR3]





Evaluation of nonlinear term

- Focus on skew sextupole component.
- Reference axes in solenoid is chosen as a straight line with half crossing angle.
- Magnet components are defined on the reference orbit.
- Beam orbit deviate from the reference orbit.
- Skew sextupole component is induced by Skew sextupole and octupole with a vertical orbit.



C₁₀ from SK2 and K3+yCOD

- Contribution to SK2 is coming from explicit Skew Sext SK2₀ and octupole, K3+COD
- No contribution from higher order than K3.



Skew sextupole coming from higher order nonlinearity is small.

Commissioning of SuperKEKB β^* is squeezed step-by-step

- c_{10} =0.072 m is kept for β *change, because IR magnets are fixed in SuperKEKB.
- For normalized coordinates, $P_i = \sqrt{\beta_i} p_i$, $X_i = x_i / \sqrt{\beta_i}$

$$C_{10} = \frac{c_{10}}{\beta_x^* \sqrt{\beta_y^*}} \qquad \qquad H = c_{10} p_x^2 p_y \qquad \qquad H_N = C_{10} P_x^2 P_y$$

- C_{10} =136.9 m^{-1/2} for β_x *=3.2cm, β_y *=0.27mm
- Normalized C₁₀ directly affects the beam dynamics. $\Delta Y = C_{10}P_x^2$

 $\Delta Y = C_{10} P_x^2 \approx 136.9 \varepsilon_x \approx 0.15 \sqrt{\varepsilon_y} \qquad \text{for } \beta_x^* = 3.2 \text{cm}, \beta_y^* = 0.27 \text{mm}$

- The effect is reduced by Detune of β^* .
- C₁₀ is 4.4% for 8x8, 8.8% for 4x8.
- This nonlinearity does not affect commissioning stage. (MAC2018)

Phase II commissioning stage

- Collision starts the end of April 2018.
- Beta was squeezed to 8->6->4->3mm. Clear luminosity gain did not have the first 1.5 month of the beam-beam commissioning. Rather it worsened.
- Collision tools (offset, optics/emittance, waist, x-y coupling ...) are developed during the period.
- Many works were done simultaneously
 - Develop machine protection interlock.
 - Injection tuning. Linac tuning. Back ground.
 - Beam current increase.
 - •

Lspec at June 10, 2018



Blow-up of e- beam was serious.

21^h

0^h0^m

6/11

3^h

LER HER

$$L_{sp} = \frac{1}{2\pi\sigma_{xc}\sigma_{yc}e^2f_0}$$

$$\sigma_{yc} = \sqrt{\sigma_{y+}^2 + \sigma_{y-}^2}$$

Luminosity in a weak-strong simulation

 BBWS, strong e- beam 5% coupling 285mA, βx=200mm, βy=4mm, early stage of parameters

weak e+ beam 1% coupling 340mA



Even in very conservative condition of the simulation, measured luminosity was half of simulation.

R scan in the simulation



- Required tuning range R1 O(mrad), R2 O(mm), R3 O(1m⁻¹), R4 O(0.1)
- R2 scanned O(0.01-0.1mm)
- Lack of tuning range especially in R2.



IP coupling and beam distribution at IP



We do not change IR magnets for squeezing β^* , R2 is kept. Effect of R2 is enhanced for squeezing β^* .

Beam shape at IP with IP coupling high current low current • R1 • R2 **Discrepancy from L calculated** Better agreement with L by the measured beam size calculated by the measured beam

• In either case, luminosity better agree with that given by the measured beam size at high current,

size

• Emittance growth is remarkable for beam with coupling.

HER R2 scan in June 15, 2018

Increase tuning range of R2, R2 correction scheme is changed so using sextupole bump as is done in KEKB, although there are side effects.

- R2=-3.9mm
- I+=340mA
- I-=285mA
- 789 bunch
- no inj

$$\Delta \sigma_y = \frac{R_2}{\beta_x} \sigma_x = 0.8 \mu m$$
$$= 2\sigma_y$$





Relation of R and skew strength of QC1 in a simple model

• Transformation of R2,



$$H = \pm R_2 p_x p_y \qquad \qquad y = y \pm R_2 p_x$$

• Assume $\pi/2$ for phase difference between IP to both QC1.

$$H = \pm \frac{R_2}{\sqrt{\beta_x^* \beta_{x,1}}} \sqrt{\beta_y^* \beta_{y,1}} xy \approx \pm R_2 xy$$

- Skew quad at QC1 is B'L/B ρ =R₂, which is independent of β^* .
- Deviation from $\pi/2$ induces R3.
- Control of inside of π section is hard from outside. It should be corrected by both side of skew. (like waist correction)

$$RM_{2\times 2}R^{-1} = e^{-R_2 p_x p_y} M_{2\times 2} e^{R_2 p_x p_y}$$

- We do not change IR magnets for squeezing β^* , R2 is kept.
- Effect of R2 is enhanced for squeezing β^* .

 $H = ds p_y^2$ waist shift



 $M_{rev,R}(k_{1L},k_{1R}) = M_0 T_{1L}^{-1} K_{1L} T_{1R} K_{1R} T_{1R}^{-1} \qquad R_{1-4,L} \text{ are also given. } R_{1-4,L}$

Skew correction at realistic IR

- β_x*=0.1, β_y*=0.003, (MKS)
- $\beta_{x,1}$ =4.46, $\alpha_{x,1}$ =-7.52, $\phi_{x,1}$ =0.236, $\beta_{y,1}$ =329, $\alpha_{y,1}$ =-12.3, $\phi_{y,1}$ =0.2495
- R_1 =-14.9 k_{L1} -14.9 k_{R1} , R_2 =-0.716 k_{L1} +0.716 k_{R1} ,
- R_3 =-487 k_{L1} +487 k_{R1} , R_4 =-1156 k_{L1} -1156 k_{R1}
- For k_{L1}= -k_{R1}=0.0021, R₁=R₄=0, R₂=0.003, R₃=-2.05.
- R_3 leaks outside of IR due to the deviation of betatron phase from $\pi/2$.
- Correct x-y coupling due to the leakage of R_3 globally.
- Detailed values are determined by SAD (Ohnishi).



TbT measurement

• y motion in X mode.

$$\begin{array}{l} \textbf{notion in X mode.} \\ \textbf{x} = RBX \\ R = \begin{pmatrix} r_0 & 0 & r_4 & -r_2 \\ 0 & r_0 & -r_3 & r_1 \\ -r_1 & -r_2 & r_0 & 0 \\ -r_3 & -r_4 & 0 & r_0 \end{pmatrix} \\ \end{array} \qquad \begin{array}{l} B = \begin{pmatrix} B_X & 0 \\ 0 & B_Y \end{pmatrix} \\ B_X = \begin{pmatrix} \sqrt{\beta_X} & 0 \\ -\alpha_X/\sqrt{\beta_X} & 1/\sqrt{\beta_X} \end{pmatrix} \end{array}$$

r_i=R_i

r1: cos component of y for x betatron motion ,r2: sin component

$$y = -r_1 x - r_2 p_x = -r_1 a \cos \phi(s) + r_2 \left[\frac{a}{\beta} \sin \phi(s) + \frac{\alpha}{\sqrt{\beta}} a \cos \phi(s) \right]$$

$$= c \cos(2\pi nv_x + \phi_y) \qquad \qquad \phi(s) = 2\pi nv_x + \phi_x$$
$$\frac{c}{a} \cos(\phi_y - \phi_x) = \left(-r_1 + r_2 \frac{\alpha}{\sqrt{\beta}}\right) \qquad \qquad \frac{c}{a} \sin(\phi_y - \phi_x) = -\frac{r_2}{\beta}$$

r3: cos component of y for px betatron motion ,r4: sin component $p_{y} = -r_{3}x - r_{4}p_{x} = -r_{3}a\cos\phi(s) + r_{4}\left[\frac{a}{\beta}\sin\phi(s) + \frac{\alpha}{\sqrt{\beta}}a\cos\phi(s)\right]$ $= d\cos(2\pi n\nu_x + \phi_q)$

$$\frac{d}{a}\cos(\phi_q - \phi_x) = \left(-r_3 + r_4\frac{\alpha}{\sqrt{\beta}}\right) \qquad \qquad \frac{d}{a}\sin(\phi_q - \phi_x) = -\frac{r_4}{\beta}$$

FFT of BPM data

• Small y_{IP} , but enough $p_{yIP}=q_{IP}$.







Toward Phase III

 Squeezing beta*, Luminosity increase is not trivial at all without IP optics tuning.



Luminosity is half at $I_+I_-=0.4$ mA². Beam-beam tune shift is limited 0.021. Design 1.5 mA². $\beta_y * 1/10$ Beam-beam simulation considering optics aberrations at IP

- Linear
- Nonlinear
- Chromatic
- Recent operation showed e+ beam is weaker than e- beam. Weak(e+)-strong(e-) simulation is performed.

Weak(e+)-strong(e-) simulation with errors

- Error strengths of R3 and R4 are much larger than measurement. Discard.
- R1 and R2 were already scanned and given optimum.
- We cleared linear aberrations in Phase-II.



Nonlinear aberrations

- $p_x^2 p_y$ term was studied before commission.
- $p_x^2 p_y$ term well reproduces measured L_{sp} .
- The strength is 100 times larger than the value given by design of QCS. c₁₀=c(p_x²p_y)=0.07.



Chromatic coupling

- R3' and R4' were measured to be R3'=300, R4'=20.
- The behaviors for R1' and R2' are plausible.
- R1' and R2' are hard to be measured in the present monitor. R1' ~-10 in measurement?



Optics at IR (LER Phase II)

• βx=0.2m βy=3mm



IP

Chromatic coupling in SAD (Y. Ohnishi)

Chromatic XY Coupling







Y/x amplitude at QC monitors

• y/x amplitude for Betatron H mode in LER



Phase difference of x-y motion at QC monitors

• Betatron Phase difference in LER, $\phi_v - \phi_x$.



Measured Chromatic coupling at LER-IR

- R1, R1', R2 and R2'
- The values are much larger than SAD model
- The behavior of R2' is different from SAD



Measured Chromatic coupling at LER-IR

- R3, R3', R4 and R4'
- The values are much larger than SAD model



Source/correction of chromatic coupling

• Generatng function at IP

 $G=R_{1}^{\prime }xp_{y}\delta +R_{2}^{\prime }p_{x}p_{y}\delta$

• Chromatic coupling at QC1 rotation

$$\begin{split} G &= K_1 \theta [x + p_x (1 - \delta)s] \big[y + p_y (1 - \delta)s \big] \approx -2K_1 \theta p_x p_y \delta \\ &\approx -K_1 \theta s x p_y \delta - 2K_1 \theta s p_x p_y \delta \\ \bullet \ \mathsf{R}_1' \mathsf{=} \mathsf{K}_1 \theta \mathsf{s} \ \ \mathsf{R}_2' \mathsf{=} \mathsf{-} \mathsf{2} \mathsf{K}_1 \theta \mathsf{s} \ \ \mathsf{s}^{\sim} \mathsf{1}, \mathsf{K} \mathsf{1}^{\sim} \mathsf{1} \ \mathsf{small contribution} \end{split}$$

Skew sextupoles

$$G = \sqrt{\frac{\beta_x \beta_y^* \beta_y}{\beta_x^*}} SK_2 x p_y \eta_x \delta + \sqrt{\beta_x^* \beta_x \beta_y^* \beta_y} SK_2 p_x p_y \eta_x \delta$$

Local chromaticity correction

• Rotation/coupling of sextupole at local chromaticity correction (rough estimation for phase ϕx)

$$G = \sqrt{\frac{\beta_x \beta_y^* \beta_y}{\beta_x^*}} K_2 \theta x p_y \eta_x \delta + \sqrt{\beta_x^* \beta_x \beta_y^* \beta_y} K_2 \theta p_x p_y \eta_x \delta$$

- SLY K2=2.9, bx=13.4m by=179m, hx=-0.46m
 - R1'=80, R2'= 1.60
- SLX K2=0.48,bx=100m, by=9.8m, hx=0.6m
 - R1'=1.10, R2'= 0.220
- Not symmetric. Peridodic solution should be studied.

$$C(p_x^2 p_y)$$

Local chromaticity correction

$$G = \beta_x^* \beta_x \sqrt{\beta_y^* \beta_y} K_2 \theta p_x^2 p_y$$

- SLY K2=2.9, βx=13.4m βy=179m, ηx=-0.46m
 c=5.7θ
- SLX K2=0.48, βx=100m, βy=9.8m, ηx=0.6m
 - c=1.60

Chromatic coupling in KEKB

 Y. Ohnishi et al., PRSTAB 12, 091002 (2009)



FIG. 3. (Color) Measured chromatic X-Y coupling at IP in HER. The blue plots indicate those before and the red plots indicate those after the skew sextupole correction. The dashed line indicates the natural chromatic X-Y coupling estimated using the model lattice by SAD.

TABLE I. Natural chromatic X-Y coupling estimated using the model lattice by SAD. Errors are the rms of the deviations obtained from the lattice simulation and include a rotation error of each normal sextupole magnet (see text).

	LER	HER
$\partial r_1 / \partial \delta$	-0.059 ± 0.006	-0.207 ± 0.007
$\partial r_2 / \partial \delta$ (m)	$+0.048 \pm 0.007$	$+0.266 \pm 0.009$
$\partial r_3 / \partial \delta (1/\mathrm{m})$	$+33.03 \pm 1.35$	$+38.61 \pm 1.05$
$\partial r_4 / \partial \delta$	-30.48 ± 0.99	-132.54 ± 1.71



FIG. 4. (Color) Measured chromatic X-Y coupling at IP in LER. The blue plots indicate those before and the red plots indicate those after the skew sextupole correction. The dashed line indicates the natural chromatic X-Y coupling estimated using the model lattice by SAD.

IR aberration (LER)



- Possible error to explain the Lsp behavior.
- Simulation showed R1'=12, R2'=3m or c(px2py)=8m.
- R3* and R4* is clearly measured, but R1* and R2* are ambiguous.
- Behavior of R's at IR is different from SAD model.
- R1' and R2' are doubtful.

Summary

- SuperKEKB is squeezing β^{*} step-by-step in the commissioning.
- Luminosity increase proportional to $\beta_{\text{y}}{}^{*}$ is not trivial at all.
- High Luminosity is only achieved, when the optics aberration at IP are perfectly corrected.
- QCS as error source and corrector is key component.
- Errors induced at QCS are enhanced for squeezing β^* .
- Correction of nonlinear aberration is next target in Phase-III commissioning.
- Final target, $Lsp=220x10^{30}cm^{-2}s^{-1}mA^{-2}$ at $I_{+}I_{-}=1.5mA^{2}$.

Thank you for your attention

Transfer matrix, M $M = RBUB^{-1}R^{-1} = RM_{2\times 2}R^{-1}$ • Matrix transformation for R. Therefore K. $R = \begin{pmatrix} r_0 & 0 & r_4 & -r_2 \\ 0 & r_0 & -r_3 & r_1 \\ -r_1 & -r_2 & r_0 & 0 \\ -r_3 & -r_4 & 0 & r_0 \end{pmatrix} \qquad B_X = \begin{pmatrix} B_X & 0 \\ 0 & B_Y \end{pmatrix}$ $U = \begin{pmatrix} U_X & 0 \\ 0 & U_Y \end{pmatrix} \qquad B_X = \begin{pmatrix} \sqrt{\beta_X} & 0 \\ -\alpha_X/\sqrt{\beta_X} & 1/\sqrt{\beta_X} \end{pmatrix}$ $\overline{y} = r_0 y - r_1 x - r_2 p_x$ $\bar{p}_y = r_0 p_y - r_3 x - r_4 p_x$ $U_X = \begin{pmatrix} \cos \phi_X & \sin \phi_X \\ -\sin \phi_X & \cos \phi_X \end{pmatrix}$ Corresponding canonical transformation for R. $G_2(x,\bar{p}_x,y,\bar{p}_y) = x\bar{p}_x + y\bar{p}_y + axy + b\bar{p}_xy - cx\bar{p}_y - d\bar{p}_x\bar{p}_y$ $\bar{y} = \frac{\partial G_2}{\partial \bar{p}_v} = y - cx - d\bar{p}_x$ $p_y = \frac{\partial G_2}{\partial v} = \bar{p}_y + ax + b\bar{p}_x$ $\bar{x} = \frac{\partial G_2}{\partial \bar{p}_x} = x + by - d\bar{p}_y$ $p_x = \frac{\partial G_2}{\partial x} = \bar{p}_x + ay - c\bar{p}_y$ $a(\delta) \approx r_3(\delta) \quad b(\delta) \approx r_4(\delta)$ $c(\delta) \approx r_1(\delta) \quad d(\delta) \approx r_2(\delta)$

6D transfer map for chromatic coupling

• 4D transfer for $a(\delta)$, $b(\delta)$, $c(\delta)$, $d(\delta)$

• Z transfer

 $c(\delta) \approx r_1(\delta) \quad d(\delta) \approx r_2(\delta)$

 $a(\delta) \approx r_3(\delta) \quad b(\delta) \approx r_4(\delta)$

$$\bar{z} = \frac{\partial G_2}{\partial \bar{p}_z} = z + a'xy + b'\bar{p}_xy - c'x\bar{p}_y - d'\bar{p}_x\bar{p}_y$$

Take Fourier transformation of the BPM position



FFT amp.

FFT amp.

HER





FFT amp.

FFT amp.



FFT amp.

FFT amp.





Beam motion at Interaction Region (IR)



BX EX s(m) AX NX Element AY BY NY # 118.364 190.713 -.2414 .00147 MQC2RE 3013.81 -135.99 263.746 -.2501 5691 5.29905 2.90873 -.2204 1.95E-6 MQC1RE 3015.78 176.638 93.6284 -.2491 6474 -9.E-13 .10000 .00000 1.2E-13 IP.1 .000000 3.0E-12 .00300 .00000 1 -5.2990 2.90874 .22032 -1.9E-6 MQC1LE .53000 -176.63 93.6286 .24910 112 -106.71 142.968 .24102 -.00130 MQC2LE 2.2500 168.532 291.140 .24998 793

Betatron phase, betatron tune

Beam position variation

 $x_n = a \cos(2\pi n \nu_x + \phi_x)$

 ϕ_{χ} : Initial betatron phase at a position.

 $X = \sqrt{W} \begin{pmatrix} \cos \phi(s) \\ -\sin \phi(s) \end{pmatrix} = \begin{pmatrix} \frac{x}{\sqrt{\beta}} \\ \frac{\alpha x + \beta p_x}{\sqrt{\beta}} \end{pmatrix}$

 $\phi(s)=2\pi n\nu_x+\phi_x$

• Fourier transformation of beam position

$$x_{\nu} = \sum_{n=0}^{\infty} x_n \exp(-2\pi i \nu n) \qquad x_{\nu} = \frac{a}{2} \exp(i\phi_x)$$

- Betatron amplitude and phase $a = \sqrt{\beta W} = 2|x_{\nu}|$ $\phi_x = \tan^{-1}\left(\frac{\operatorname{Im} x_{\nu}}{\operatorname{Re} x_{\nu}}\right)$
- α, β are determined by Fourier transformation of p_x . $p_n = -\frac{a}{\beta}\sin(2\pi nv_x + \phi_x) - \frac{a}{\sqrt{\beta}}a\cos(2\pi nv_x + \phi_x)$ $p_v = \frac{b}{2}\exp(i\phi_p) = \frac{a}{2}\left(\frac{i}{\beta} - \frac{\alpha}{\sqrt{\beta}}\right)\exp(-i\phi_x)$ $\beta = \frac{a}{b}\sin(\phi_p - \phi_x)$ $\left(\frac{i}{\beta} - \frac{\alpha}{\sqrt{\beta}}\right) = \frac{b}{a}\exp(i(\phi_p - \phi_x))$ $\alpha = -\frac{a\beta}{b}\cos(\phi_p - \phi_x)$

Tune 75 nu= 0.539297

 #
 real
 imag
 phx/2p
 real
 imag
 phy/2p

 L
 -47.348487
 436.662161
 0.267190
 -28.252748
 -10.712758
 -0.442318

 R
 -110.801772
 -417.576000
 -0.291280
 39.633016
 26.146045
 0.092814

 L2
 2.944297
 3478.970627
 0.249865
 -97.595958
 -12.765645
 -0.479300

 R2
 -421.541901
 -3431.803912
 -0.269452
 54.409751
 1.071608
 0.003134

Tune 75 nu= 0.539297

x -79.613824 9.250941 0.481589 5.179247 0.947493 0.028797
p 60.033105 806.052591 0.238168 -61.666732 -34.973067 -0.417892
x2 -86.52538 121.238292 0.348652 318.590162 184.654037 0.083601
p2 49.458256 853.005395 0.240782 -119.215526 -21.533290 -0.471559





• No dependence in R3