

# THE 2018 INTERNATIONAL WORKSHOP ON HIGH ENERGY CIRCULAR ELECTRON POSITRON COLLIDER

## QCD AND EW CORRECTIONS IN LIGHT OF PRECISION MEASUREMENTS AT CEPC-SPPC

HUA-SHENG SHAO



12 NOVEMBER 2018

- **Energy frontier in lab:**

- Direct and/or indirect to probe BSM and to improve our knowledge of SM

- hadron-hadron colliders: LHC, SppC, FCC-hh

- They are mainly QCD machines.
- Require the good knowledge of PDF for hard probes.
- The precision measurements are gained by large yields.

- lepton-lepton colliders: CEPC, FCC-ee, ILC, CLIC

- Importance of initial-state radiations and possible beamstrahlung.
- Low background and large reconstruction efficiency.

- lepton-hadron colliders: LHeC, FCC-eh, EIC

- They are dedicated QCD machines.
- Determine initial conditions for hadron-hadron colliders.

◆ Running

◆ In plan

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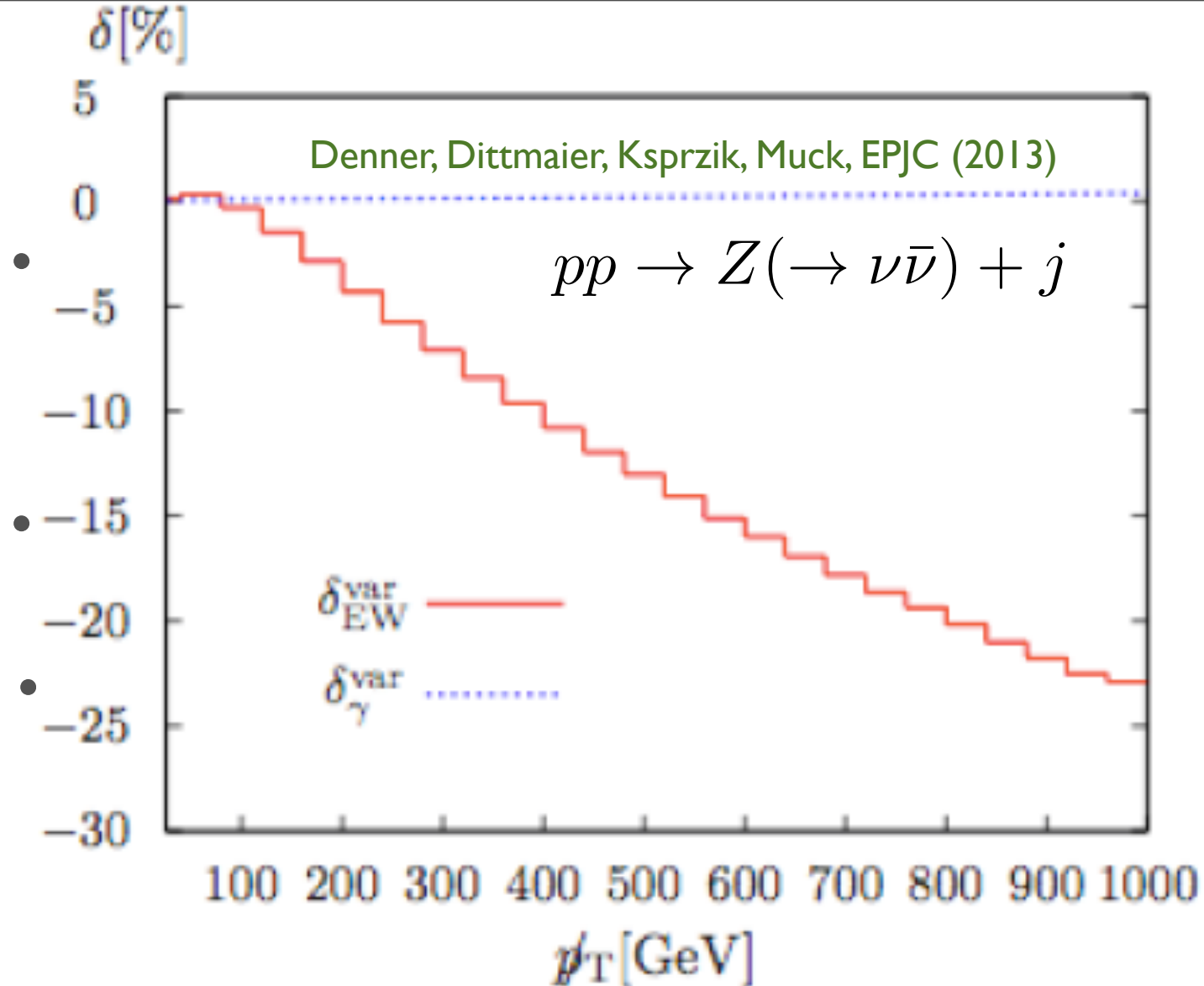
◆ In plan

*Precision Theory Meets Precision Measurements*

# FRONTIER OF PRECISION THEORY

- LHC runs at 13 TeV and future colliders at 100 TeV
  - energy reaches deeper into multi-TeV region & high integrated luminosity
  - many processes (even rare processes before) reach precision era (present)
- NLO QCD becomes standard: automation (e.g. MG5\_aMC)
  - scale uncertainty reaches to 10% level
- Frontier of precision theory for ElectroWeak scale observables
  - Goal: to achieve the percent level predictions
  - Request: NNLO QCD and NLO EW  $\alpha_s^2 \simeq \alpha \simeq 1\%$
  - Automation: NLO EW (done at fixed order) and NNLO QCD (long way)
- Necessity of NLO EW corrections:
  - First opportunity to explore TeV scale kinematics, where EWC  $\sim 10\%$
  - High precision measurements are present or in planned
    - cross section ratios, e.g. different center-of-mass energy, different processes
    - fundamental parameters, e.g. W mass
    - (differential) cross sections for candle processes, e.g. top quark pair xs, Z pt

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bro**W**Weak scale observables  
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$$\alpha \simeq 1\%$$

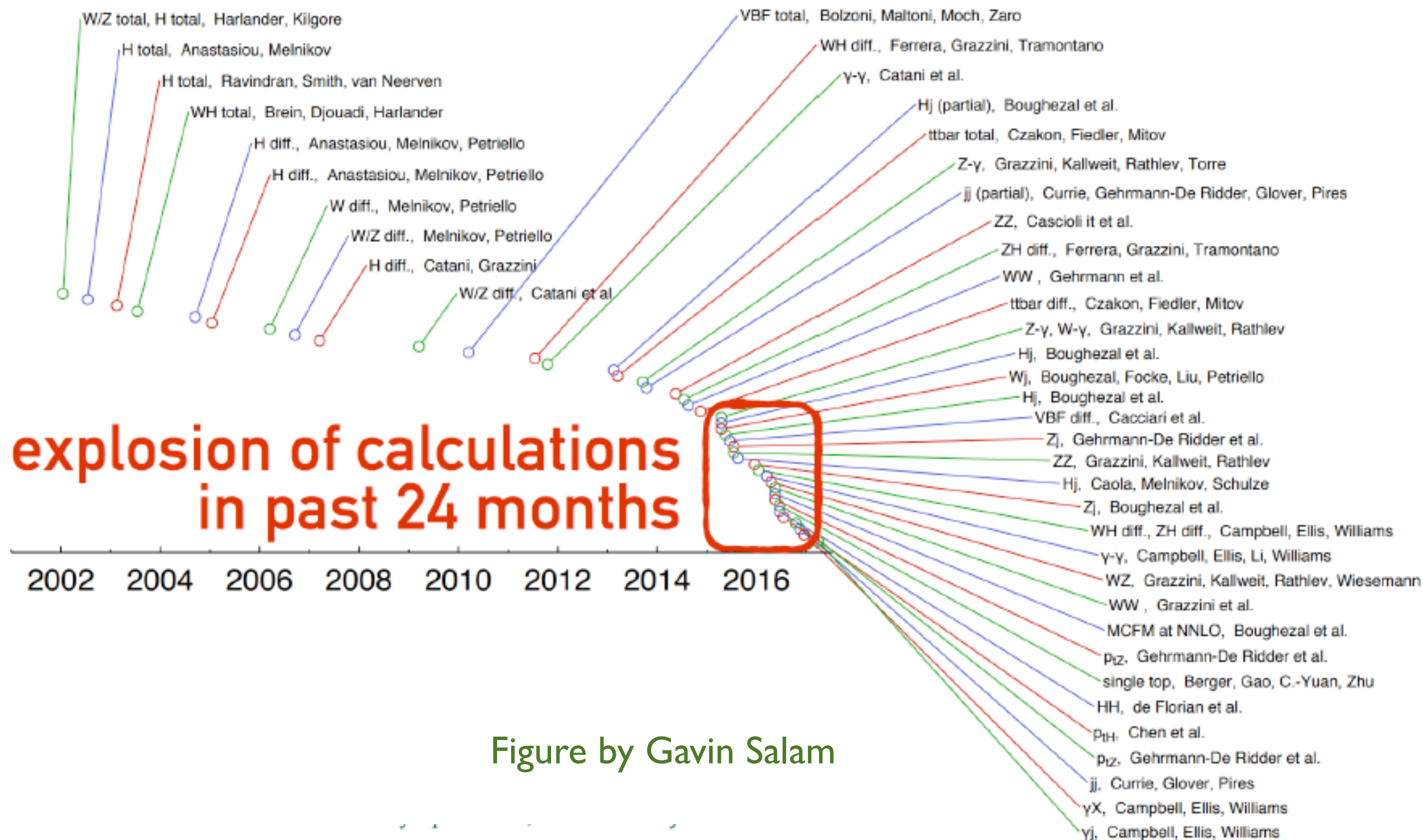
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# FRONTIER OF PRECISION THEORY



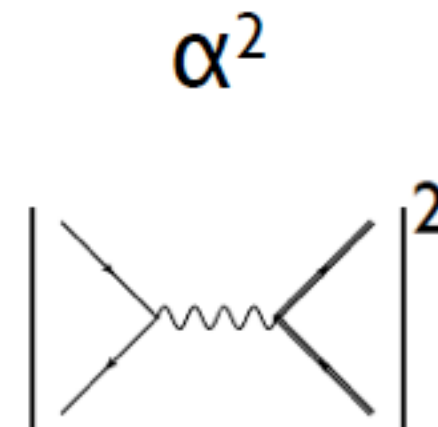
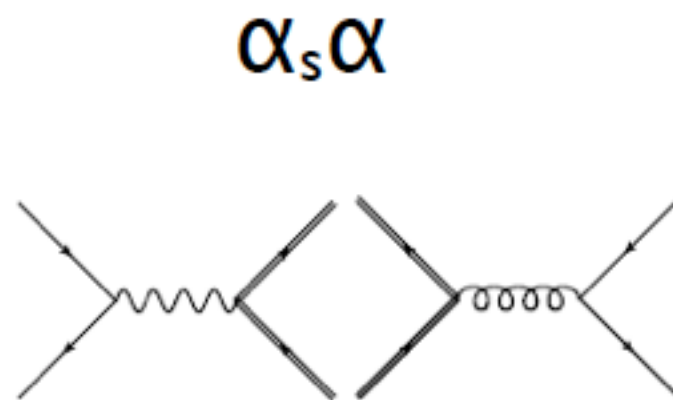
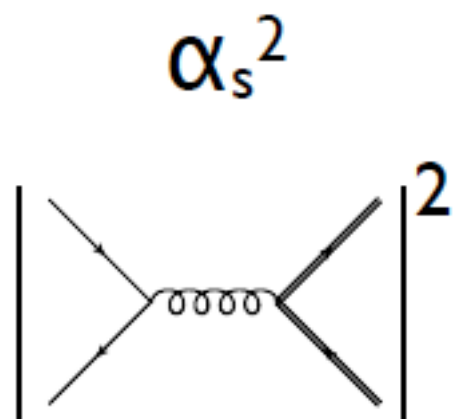
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- Explosion of NNLO QCD calculations
  - Necessary to reduce QCD scale uncertainty

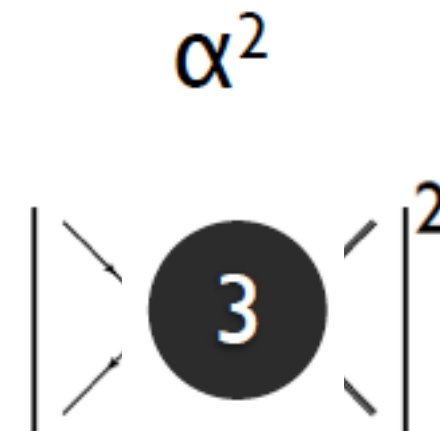
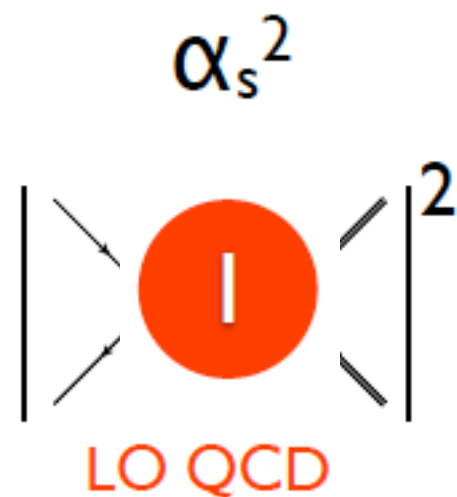
# PERTURBATIVE CALCULATIONS

- **Perturbative expansion in the Standard Model**
  - **Take dijet hadroproduction as an example** Frederix, Frixione, Hirschi, Pagani, HSS, Zaro, JHEP (2017)



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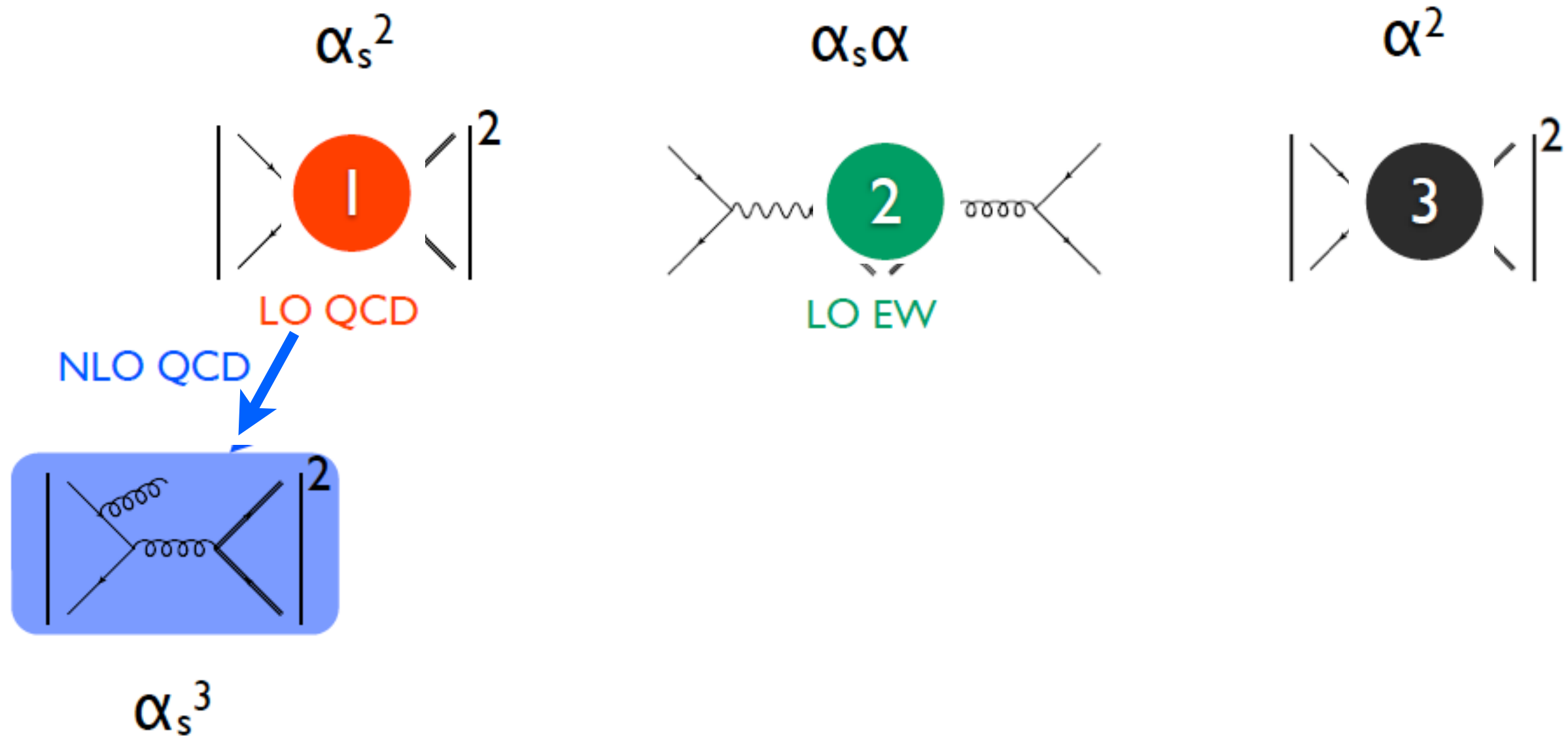
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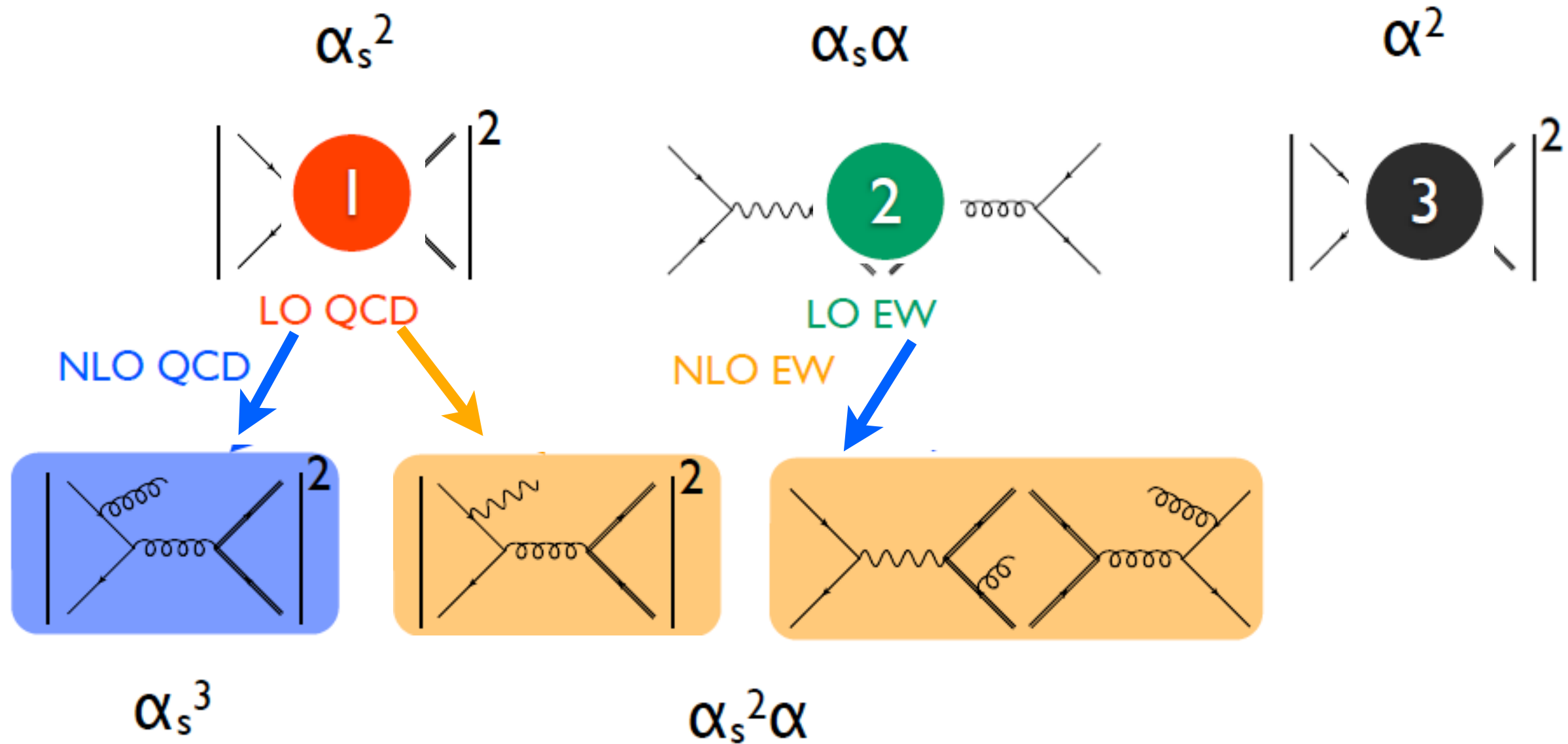
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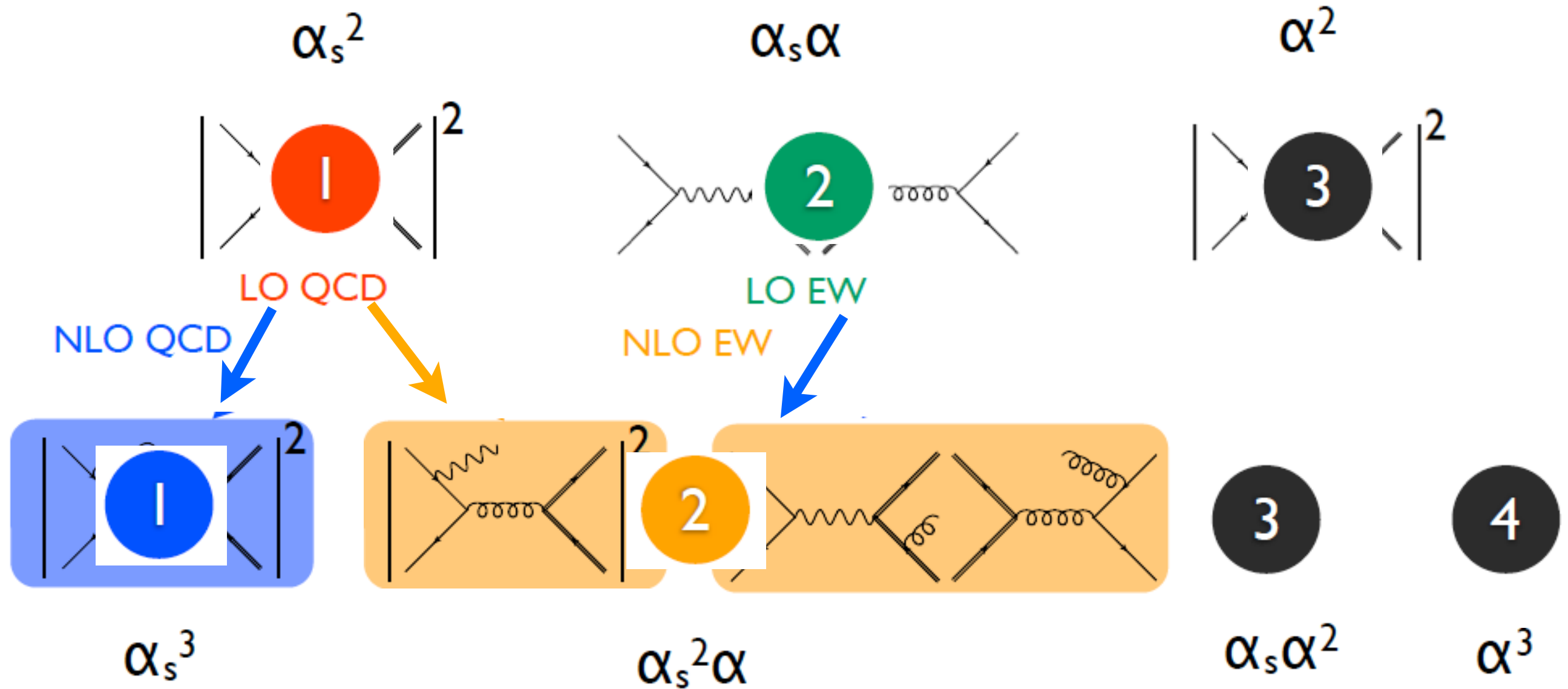
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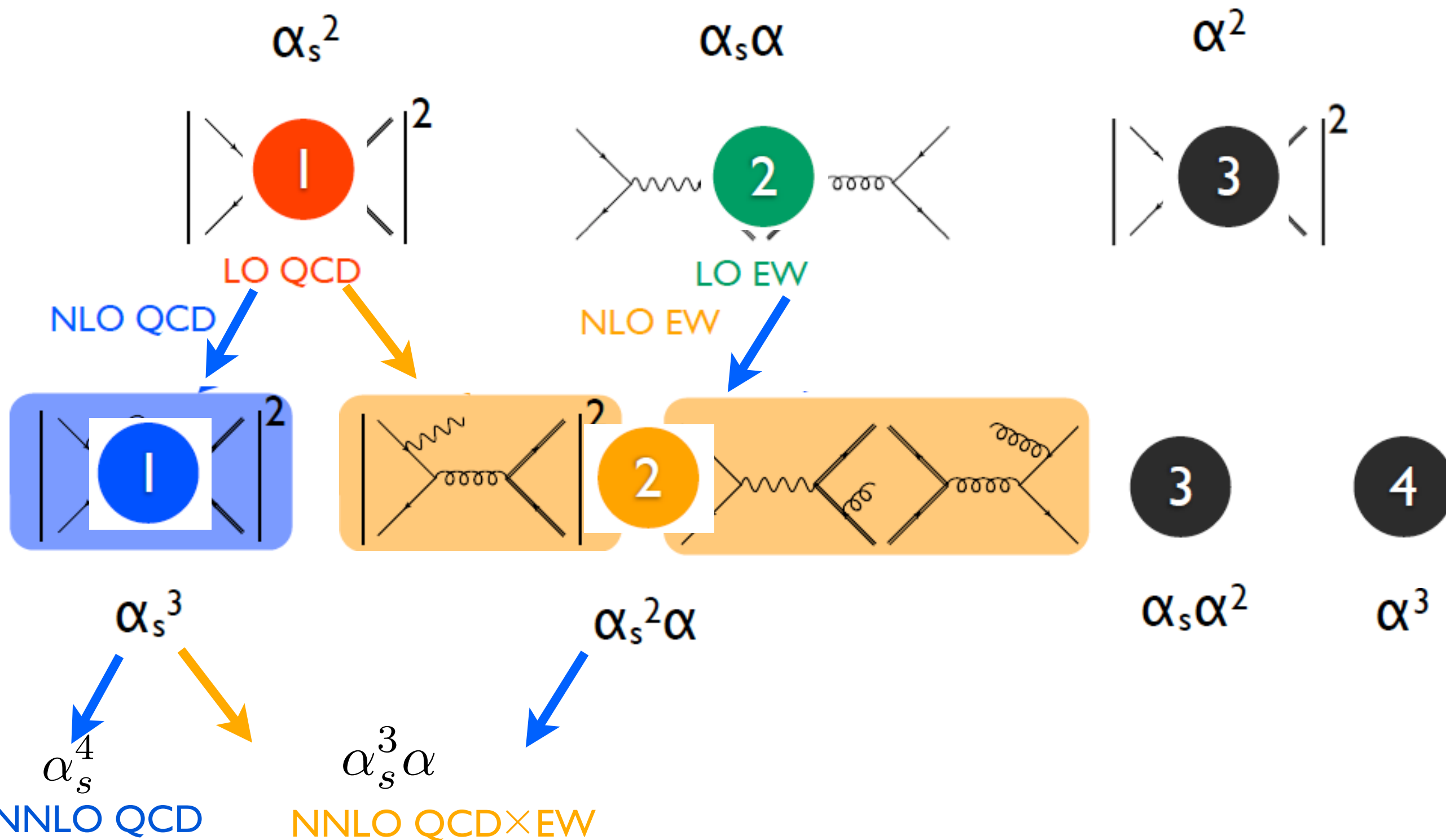
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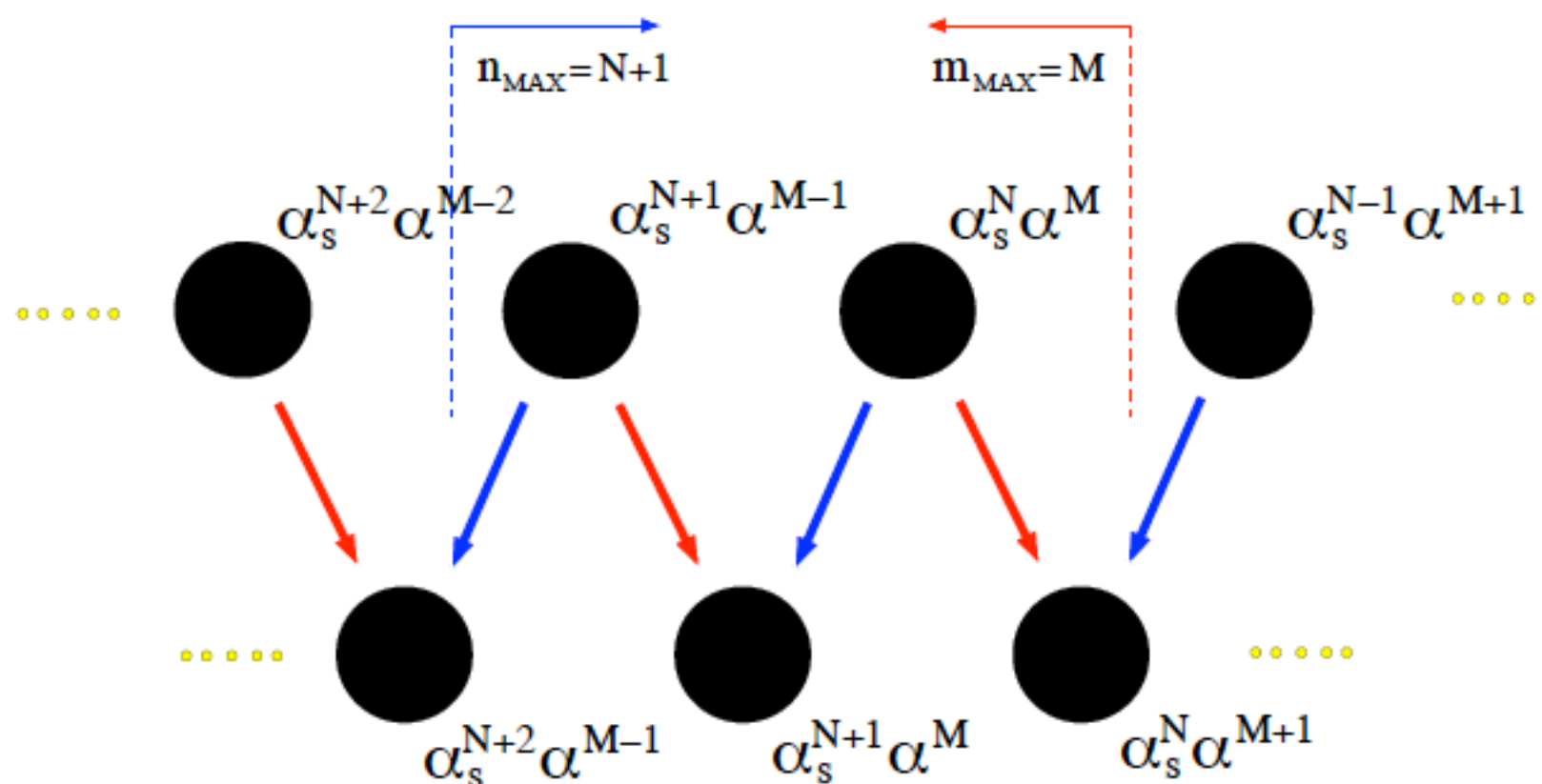
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# AUTOMATION OF COMPLETE NLO

- In MadGraph5\_aMC@NLO v3.X Frederix, Frixione, Hirschi, Pagani, HSS, Zaro, JHEP (2018)

MG5\_aMC> generate p1 p2 > p3 p4 p5 p6 QCD= $n_{\max}$  QED= $m_{\max}$  [QCD QED]

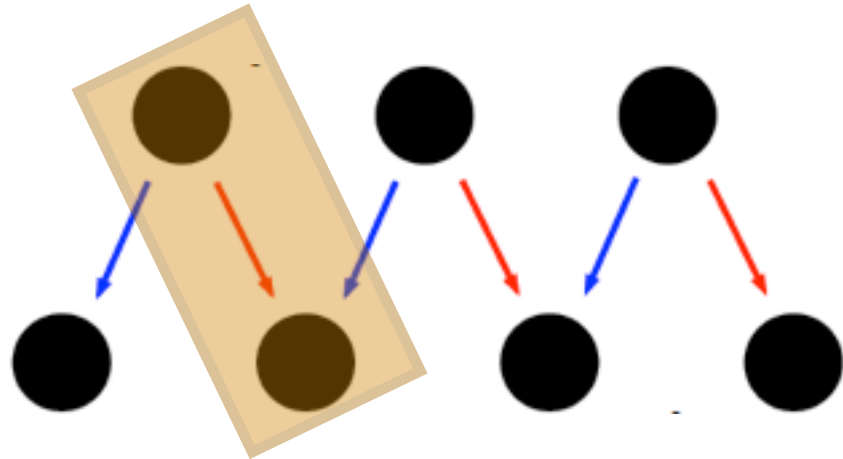


LO :  $\alpha_s^n \alpha^m$ ,  $n \leq n_{\max}$ ,  $m \leq m_{\max}$ ,  $n + m = k_0$ ,

NLO :  $\alpha_s^n \alpha^m$ ,  $n \leq n_{\max} + 1$ ,  $m \leq m_{\max} + 1$ ,  $n + m = k_0 + 1$

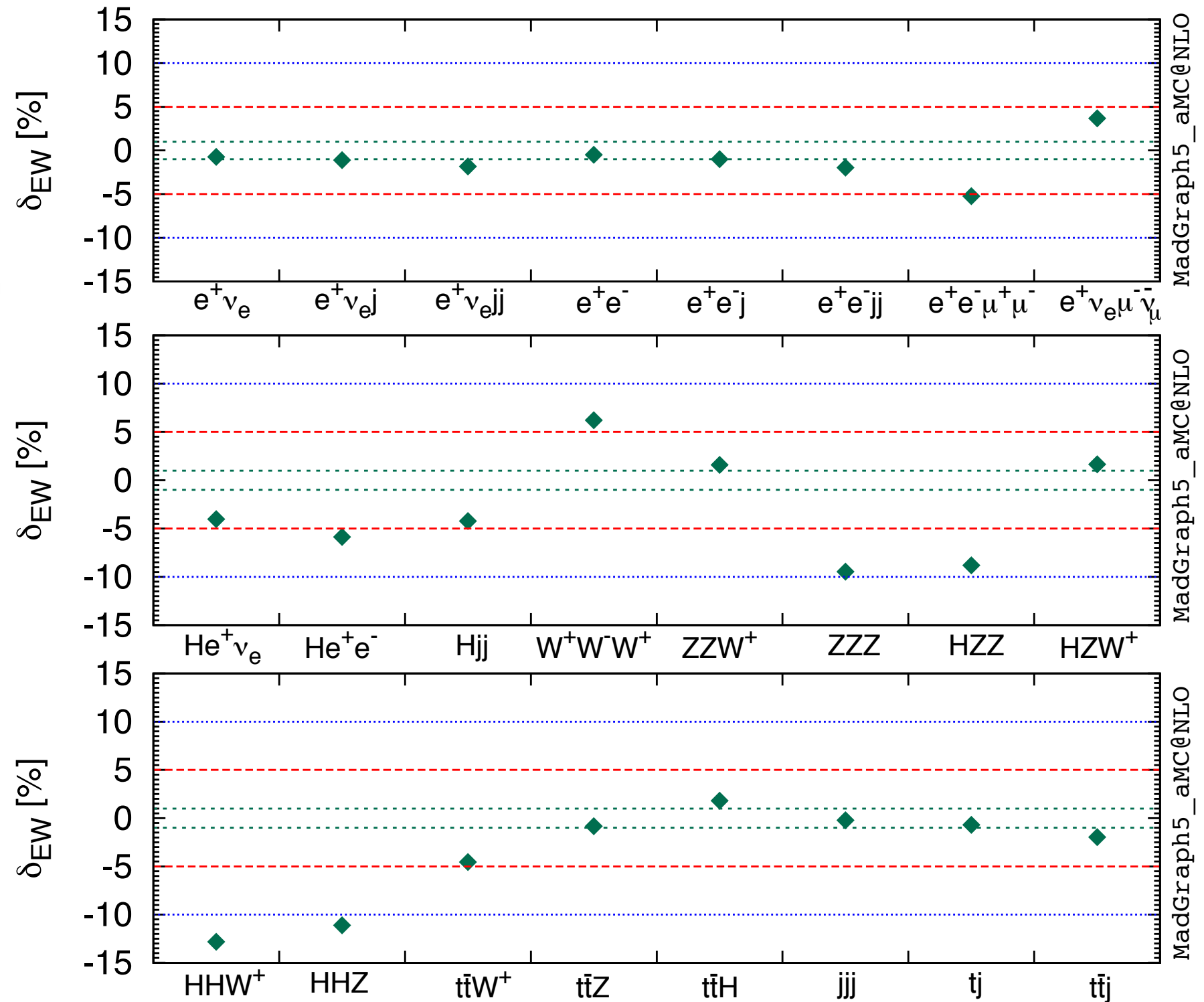


- Inclusive cross sections



Frederix, Frixione, Hirschi, Pagani, HSS, Zaro, JHEP (2018)

$$\delta_{EW} = \frac{NLO_2}{LO_1}$$



# **FUTURE ELECTRON-POSITRON COLLIDERS**

# GENERATOR ISSUES FOR LEPTON COLLIDER



- Processes at  $e^+e^-$  without beam issues is an easier case of those at pp

MG5\_aMC paper, JHEP (2014)

Process	Cross section (pb)				$\delta_{\text{QCD}} = \text{NLO}_1/\text{LO}_1$	
	Heavy quarks and jets	LO 1 TeV	NLO 1 TeV			
i.1	$e^+e^- \rightarrow jj$	$6.223 \pm 0.005 \cdot 10^{-1}$	+0.0% -0.0%	$6.389 \pm 0.013 \cdot 10^{-1}$	+0.2% -0.2%	+2.7%
i.2	$e^+e^- \rightarrow jjj$	$3.401 \pm 0.002 \cdot 10^{-1}$	+9.6% -8.0%	$3.166 \pm 0.019 \cdot 10^{-1}$	+0.2% -2.1%	-6.9%
i.3	$e^+e^- \rightarrow jjjj$	$1.047 \pm 0.001 \cdot 10^{-1}$	+20.0% -15.3%	$1.090 \pm 0.006 \cdot 10^{-1}$	+0.0% -2.8%	+4.1%
i.4	$e^+e^- \rightarrow jjjjj$	$2.211 \pm 0.006 \cdot 10^{-2}$	+31.4% -22.0%	$2.771 \pm 0.021 \cdot 10^{-2}$	+4.4% -8.6%	+25%
i.5	$e^+e^- \rightarrow t\bar{t}$	$1.662 \pm 0.002 \cdot 10^{-1}$	+0.0% -0.0%	$1.745 \pm 0.006 \cdot 10^{-1}$	+0.4% -0.4%	+5.0%
i.6	$e^+e^- \rightarrow t\bar{t}j$	$4.813 \pm 0.005 \cdot 10^{-2}$	+9.3% -7.8%	$5.276 \pm 0.022 \cdot 10^{-2}$	+1.3% -2.1%	+9.6%
i.7*	$e^+e^- \rightarrow t\bar{t}jj$	$8.614 \pm 0.009 \cdot 10^{-3}$	+19.4% -15.0%	$1.094 \pm 0.005 \cdot 10^{-2}$	+5.0% -6.3%	+27%
i.8*	$e^+e^- \rightarrow t\bar{t}jjj$	$1.044 \pm 0.002 \cdot 10^{-3}$	+30.5% -21.6%	$1.546 \pm 0.010 \cdot 10^{-3}$	+10.6% -11.6%	+48%
i.9*	$e^+e^- \rightarrow t\bar{t}t\bar{t}$	$6.456 \pm 0.016 \cdot 10^{-7}$	+19.1% -14.8%	$1.221 \pm 0.005 \cdot 10^{-6}$	+13.2% -11.2%	+89%
i.10*	$e^+e^- \rightarrow t\bar{t}t\bar{t}j$	$2.719 \pm 0.005 \cdot 10^{-8}$	+29.9% -21.3%	$5.338 \pm 0.027 \cdot 10^{-8}$	+18.3% -15.4%	+96%
i.11	$e^+e^- \rightarrow b\bar{b}$ (4f)	$9.198 \pm 0.004 \cdot 10^{-2}$	+0.0% -0.0%	$9.282 \pm 0.031 \cdot 10^{-2}$	+0.0% -0.0%	+0.9%
i.12	$e^+e^- \rightarrow b\bar{b}j$ (4f)	$5.029 \pm 0.003 \cdot 10^{-2}$	+9.5% -8.0%	$4.826 \pm 0.026 \cdot 10^{-2}$	+0.5% -2.5%	-4.0%
i.13*	$e^+e^- \rightarrow b\bar{b}jj$ (4f)	$1.621 \pm 0.001 \cdot 10^{-2}$	+20.0% -15.3%	$1.817 \pm 0.009 \cdot 10^{-2}$	+0.0% -3.1%	+12%
i.14*	$e^+e^- \rightarrow b\bar{b}jjj$ (4f)	$3.641 \pm 0.009 \cdot 10^{-3}$	+31.4% -22.1%	$4.936 \pm 0.038 \cdot 10^{-3}$	+4.8% -8.9%	+36%
i.15*	$e^+e^- \rightarrow b\bar{b}b\bar{b}$ (4f)	$1.644 \pm 0.003 \cdot 10^{-4}$	+19.9% -15.3%	$3.601 \pm 0.017 \cdot 10^{-4}$	+15.2% -12.5%	+119%
i.16*	$e^+e^- \rightarrow b\bar{b}b\bar{b}j$ (4f)	$7.660 \pm 0.022 \cdot 10^{-5}$	+31.3% -22.0%	$1.537 \pm 0.011 \cdot 10^{-4}$	+17.9% -15.3%	+101%
i.17*	$e^+e^- \rightarrow t\bar{t}b\bar{b}$ (4f)	$1.819 \pm 0.003 \cdot 10^{-4}$	+19.5% -15.0%	$2.923 \pm 0.011 \cdot 10^{-4}$	+9.2% -8.9%	+61%
i.18*	$e^+e^- \rightarrow t\bar{t}b\bar{b}j$ (4f)	$4.045 \pm 0.011 \cdot 10^{-5}$	+30.5% -21.6%	$7.049 \pm 0.052 \cdot 10^{-5}$	+13.7% -13.1%	+74%

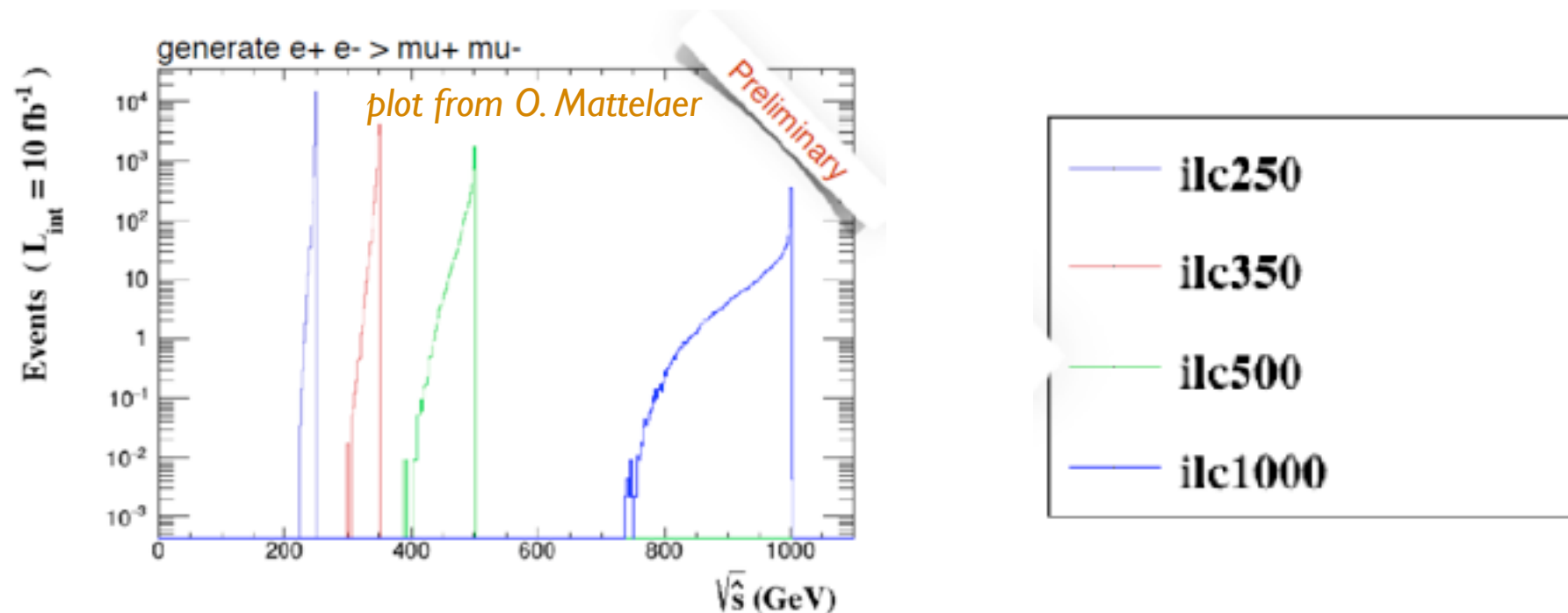
# GENERATOR ISSUES FOR LEPTON COLLIDER



- Processes at  $e^+e^-$  without beam issues is an easier case of those at  $pp$   
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- The following aspects to be improved in order to have realistic simulations at lepton-lepton colliders
  - Beam polarization
  - Photon initial state: improved Weizsaecker-Williams formula (elastic)
  - Initial-state radiation
  - Beamstrahlung technical-related feature, important at ILC

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# A FEW PROCESSES AT CEPC

- A (developing and not public) MG5\_aMC branch is under construction to solve all the mentioned beam issues at lepton-lepton colliders. Frixione, Zaro, Zhao, ...
- I take the branch with rush runs at CEPC (240 GeV) WITH **initial-state radiation** (beamstrahlung is expected to be small within CEPC configuration).

*Democratic jet (include gluon, light quark, photon, light charged lepton)*  
 $\text{anti-}k_T, R = 1.0, p_T(j) > 10 \text{ GeV}, |\eta(j)| < 4.5$

**PRELIMINARY**

$\sqrt{S} = 240 \text{ GeV}$	$\sigma(e^+e^- \rightarrow jj) \text{ [pb]}$	$\sigma(e^+e^- \rightarrow jjj) \text{ [pb]}$	$\sigma(e^+e^- \rightarrow jjjj) \text{ [pb]}$
LO <sub>1</sub>	Blocked	Blocked	Blocked
LO <sub>2</sub>		Blocked	Blocked
LO <sub>3</sub>			Blocked
NLO <sub>1</sub>	Blocked	Blocked	Blocked
NLO <sub>2</sub>	Blocked	Blocked	Blocked
NLO <sub>3</sub>		Blocked	Blocked
NLO <sub>4</sub>			Blocked
Sum	Blocked	Blocked	Blocked

\* Gmu scheme and same parameter setup as done in Frederix, Frixione, Hirschi, Pagani, HSS, Zaro, JHEP (2018)

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LO <sub>1</sub>	$2.78 \cdot 10^3$	Running	Blocked
LO <sub>2</sub>		Running	Blocked
LO <sub>3</sub>			Blocked
NLO <sub>1</sub>	$1.44 \cdot 10^0$	Running	Blocked
NLO <sub>2</sub>	$6.76 \cdot 10^1$	Running	Blocked
NLO <sub>3</sub>		Running	Blocked
NLO <sub>4</sub>			Blocked
Sum	$2.85 \cdot 10^3 \pm 0.03\%_{\text{scale}}$	Running	Blocked

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**PRELIMINARY**

$\sqrt{S} = 240 \text{ GeV}$	$\sigma(e^+e^- \rightarrow ZH) \text{ [pb]}$	$\sigma(e^+e^- \rightarrow ZZ) \text{ [pb]}$	$\sigma(e^+e^- \rightarrow W^+W^-) \text{ [pb]}$
LO <sub>1</sub>	$2.05 \cdot 10^{-1}$	$1.11 \cdot 10^0$	$1.67 \cdot 10^1$
LO <sub>2</sub>			
LO <sub>3</sub>			
NLO <sub>1</sub>			
NLO <sub>2</sub>	$-4.1 \cdot 10^{-3}$	$-5.0 \cdot 10^{-2}$	$-4.0 \cdot 10^{-2}$
NLO <sub>3</sub>			
NLO <sub>4</sub>			
Sum	$2.01 \cdot 10^{-1} \pm 0.1\%_{\text{scale}}$	$1.06 \cdot 10^0 \pm 0.05\%_{\text{scale}}$	$1.67 \cdot 10^1 \pm 0.03\%_{\text{scale}}$

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# BEYOND NLO EXAMPLE: ZH

Gong, Li, Xu, Yang, Zhang, PRD (2017);  
Sun, Feng, Jia, Sang, PRD (2017)

$\sqrt{s}$	schemes	$\sigma_{\text{LO}}$ (fb)	$\sigma_{\text{NLO}}$ (fb)	$\sigma_{\text{NNLO}}$ (fb)
240	$\alpha(0)$	$223.14 \pm 0.47$	$229.78 \pm 0.77$	$232.21^{+0.75+0.10}_{-0.75-0.21}$
	$\alpha(M_Z)$	$252.03 \pm 0.60$	$228.36^{+0.82}_{-0.81}$	$231.28^{+0.80+0.12}_{-0.79-0.25}$
	$G_\mu$	$239.64 \pm 0.06$	$232.46^{+0.07}_{-0.07}$	$233.29^{+0.07+0.03}_{-0.06-0.07}$
250	$\alpha(0)$	$223.12 \pm 0.47$	$229.20 \pm 0.77$	$231.63^{+0.75+0.12}_{-0.75-0.21}$
	$\alpha(M_Z)$	$252.01 \pm 0.60$	$227.67^{+0.82}_{-0.81}$	$230.58^{+0.80+0.14}_{-0.79-0.25}$
	$G_\mu$	$239.62 \pm 0.06$	$231.82 \pm 0.07$	$232.65^{+0.07+0.04}_{-0.07-0.07}$

- Fixed order without initial state radiations (and beamstrahlung).
- The inclusion of NLO EW corrections significantly reduce the EW scheme dependence.
- NNLO QCD $\times$ EW increases the cross section around 1-3 fb.
- The remaining dominant uncertainty is from the EW scheme dependence, which is expected to be reduced only when one includes NNLO EW (pure EW) corrections.

# LOOP-INDUCED NLO EXAMPLE: H+PHOTON

Sang, Chen, Feng, Jia, Sun, PLB (2017)

$\sqrt{s}(\text{GeV})$	150	200	220	240	250	270	290	310	330	340
$\sigma^{\text{LO}} (10^{-2} \text{ fb})$	1.054	6.214	7.339	7.758	7.764	7.479	6.909	6.134	5.151	4.522
$T_{\gamma,5}(10^{-2}\text{GeV}^{-1})$	-0.793	-0.378	-0.112	0.251	0.485	1.12	2.11	3.90	8.16	14.26
$\sigma^{\text{NLO}}/\sigma^{\text{LO}}$	0.56%	0.30%	0.09%	-0.21%	-0.41%	-0.96%	-1.86%	-3.45%	-6.85%	-10.59%
$\sqrt{s}(\text{GeV})$	360	380	400	420	500	600	700	800	900	1000
$\sigma^{\text{LO}} (10^{-2} \text{ fb})$	2.570	2.977	3.433	3.763	4.079	3.604	3.018	2.518	2.118	1.801
$T_{\gamma,5} (10^{-2}\text{GeV}^{-1})$	-2.26 +28.2 <i>i</i>	-11.6 +16.6 <i>i</i>	-13.4 +9.81 <i>i</i>	-13.24 +5.76 <i>i</i>	-9.65 -1.29 <i>i</i>	-6.31 -3.21 <i>i</i>	-4.45 -3.48 <i>i</i>	-3.35 -3.38 <i>i</i>	-2.63 -3.19 <i>i</i>	-2.13 -3.00 <i>i</i>
$\sigma^{\text{NLO}}/\sigma^{\text{LO}}$	-4.99%	16.81%	19.87%	19.24%	13.67%	9.60%	7.37%	5.98%	5.02%	4.31%

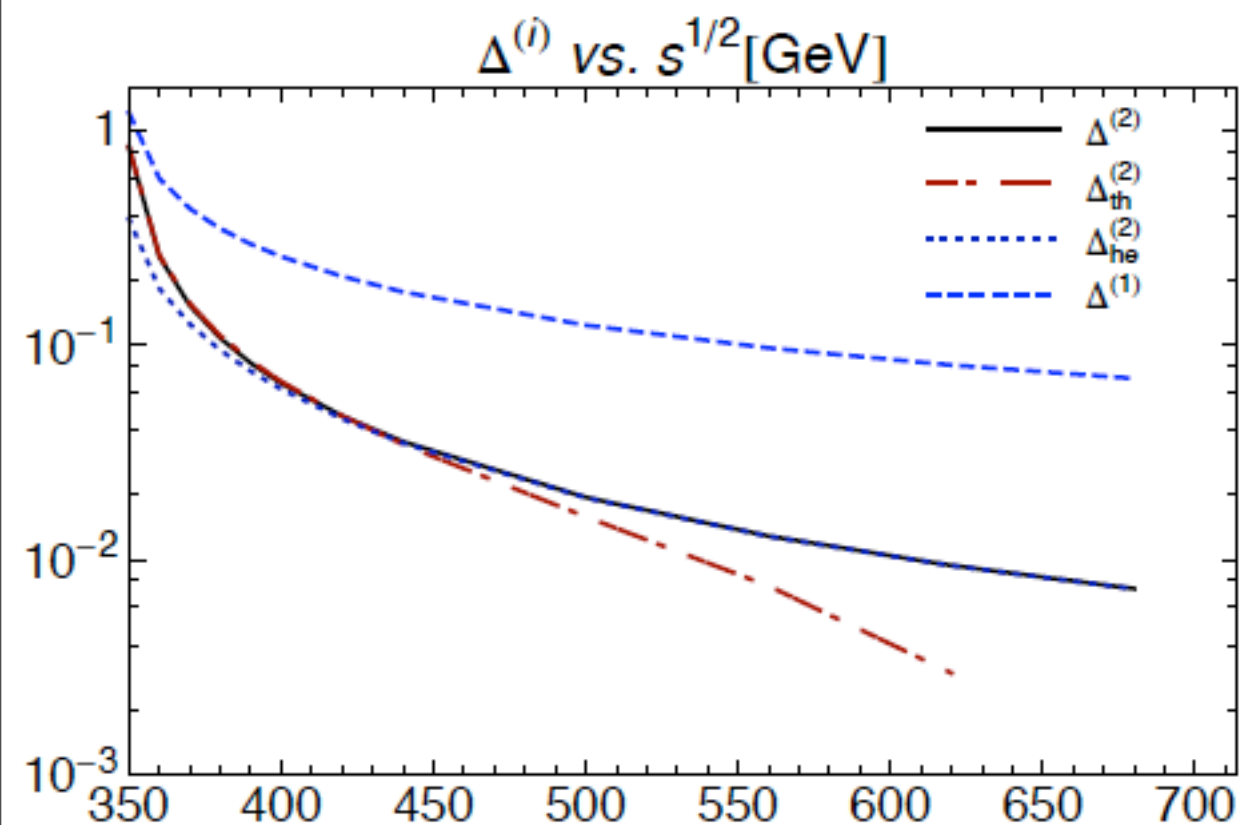
- Fixed order without initial state radiations (and beamstrahlung).
- NLO QCD correction is quite small (-0.21%) at 240 GeV but increases quickly to  $\sim 20\%$  when top-quark pair threshold is opened.



# BEYOND NLO EXAMPLE: TOP PAIR

Gao, Zhu, PRL (2014); Chen, Dekkers, Heisler, Bernreuther, Si, JHEP (2016)

$$\sigma_{NNLO} = \sigma_{LO} \left( 1 + \Delta^{(1)} + \Delta^{(2)} \right)$$



- NNLO QCD corrections (fixed order without ISR)
- The large QCD correction is from the threshold region, in which there are higher order corrections known.  
Beneke, Kiyo, Marquard, Penin, Piclum, Steinhauser, PRL (2015);  
Beneke, Maier, Rauh, Ruiz-Femenia, JHEP (2018)
- The NNLO QCD correction decreases when energy increases. It is around percent level  $> 400$  GeV.

# **FUTURE 100 TEV HADRON COLLIDERS**

# CURRENT THEORETICAL PRECISION

Theoretical uncertainty on production rates (FCC-hh physics report arXiv:1606.09408)

100 TeV	cross section [pb]	pert. error	param. error
$gg \rightarrow H$	802	6-7%	4-5%
WH	15.710	0.1%	0.2%
ZH	11.178	0.5%	0.2%
VBF H	69.0	1%	2%
ttH	32.1	8%	2%

# EXAMPLE: TtH VS TtZ

- Theoretical calculations of  $t\bar{t}H$  and  $t\bar{t}Z$  are known at complete NLO level  
Frederix, Hirschi, Pagani, HSS, Zaro, JHEP (2015,2018)
- NLO EW contributes -3% ( $t\bar{t}H$ ) and -5% ( $t\bar{t}Z$ ) for inclusive cross sections.

$t\bar{t}H : \delta(\%)$	100 TeV
NLO QCD	$40.8^{+9.3}_{-9.1} \pm 1.0$
LO EW	$0.0 \pm 0.2$
LO EW no $\gamma$	$-0.6 \pm 0.0$
NLO EW	$-2.7 \pm 0.0$
NLO EW no $\gamma$	$-2.7 \pm 0.0$
HBR	0.91

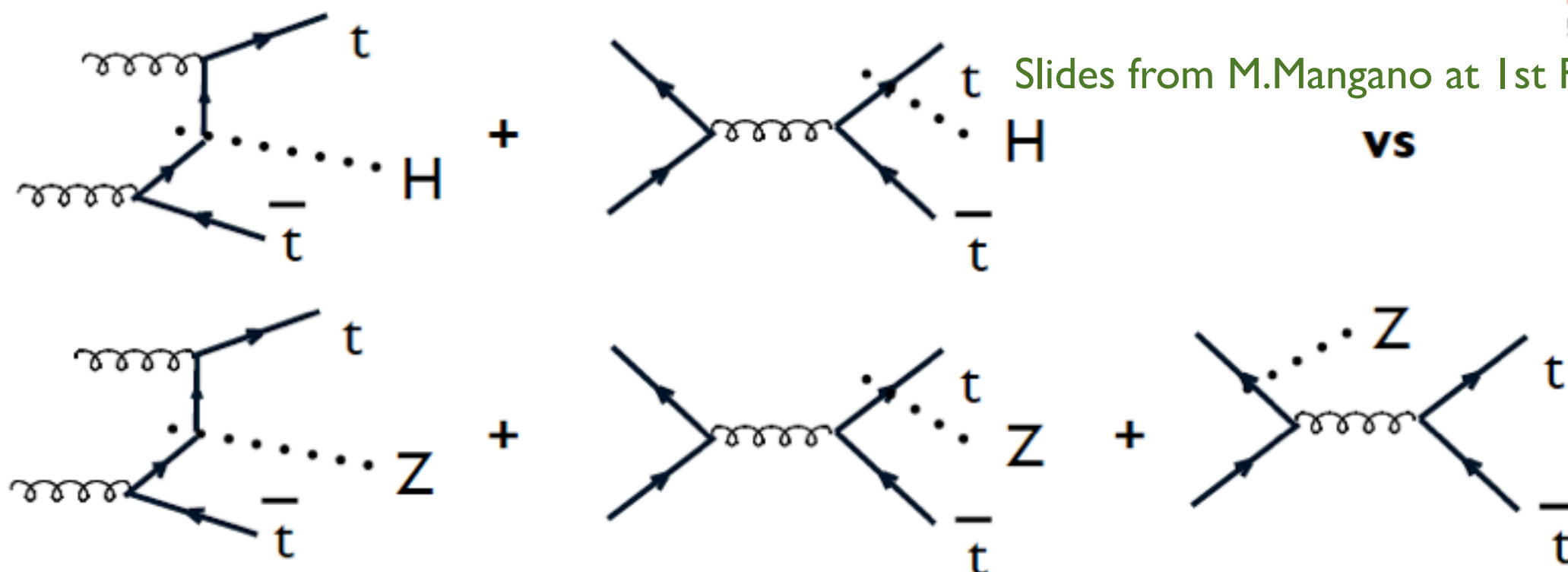
$t\bar{t}Z : \delta(\%)$	100 TeV
NLO QCD	$50.4^{+11.4}_{-10.9} \pm 1.1$
LO EW	$-1.1 \pm 0.2$
LO EW no $\gamma$	$-1.6 \pm 0.0$
NLO EW	$-5.2 \pm 0.1$
NLO EW no $\gamma$	$-5.4 \pm 0.0$
HBR	0.85

- Subleading NLO terms are  $< 1\%$  for inclusive cross sections (at 13 TeV).
- QCD scale uncertainty does not capture these EW corrections
- How to measure percent-level Higgs Yukawa coupling ?
  - NNLO QCD corrections
  - Measure and calculate  $t\bar{t}H/t\bar{t}Z$

Mangano, Plehn, Reimitz, Pagani, Schell, HSS, JPG (2015)

# $pp \rightarrow tt H$ vs $pp \rightarrow tt Z$

Slides from M.Mangano at 1st FCC-hh Workshop



To the extent that the  $qq\bar{q} \rightarrow tt Z/H$  contributions are subdominant:

**- Identical production dynamics:**

- o correlated QCD corrections, correlated scale dependence
- o correlated  $\alpha_s$  systematics

**-  $m_Z \sim m_H \Rightarrow$  almost identical kinematic boundaries:**

- o correlated PDF systematics
- o correlated  $m_{top}$  systematics

**For a given  $y_{top}$ , we expect  $\sigma(ttH)/\sigma(ttZ)$  to be predicted with great precision**



	$\sigma(t\bar{t}H)[\text{pb}]$	$\sigma(t\bar{t}Z)[\text{pb}]$	$\frac{\sigma(t\bar{t}H)}{\sigma(t\bar{t}Z)}$
13 TeV	$0.475^{+5.79\%+3.33\%}_{-9.04\%-3.08\%}$	$0.785^{+9.81\%+3.27\%}_{-11.2\%-3.12\%}$	$0.606^{+2.45\%+0.525\%}_{-3.66\%-0.319\%}$
100 TeV	$33.9^{+7.06\%+2.17\%}_{-8.29\%-2.18\%}$	$57.9^{+8.93\%+2.24\%}_{-9.46\%-2.43\%}$	$0.585^{+1.29\%+0.314\%}_{-2.02\%-0.147\%}$

- Scale uncertainty reduces to 2% for the ratio.
- PDF+ $\alpha_s$  uncertainty reduces to < 1% level

$\mu_0 = H_T/2, NLO$  QCD

		$\sigma(t\bar{t}H)[\text{pb}]$	$\sigma(t\bar{t}Z)[\text{pb}]$	$\frac{\sigma(t\bar{t}H)}{\sigma(t\bar{t}Z)}$
13 TeV	MSTW2008	$0.475^{+5.79\%+2.02\%}_{-9.04\%-2.50\%}$	$0.785^{+9.81\%+1.93\%}_{-11.2\%-2.39\%}$	$0.606^{+2.45\%+0.216\%}_{-3.66\%-0.249\%}$
	CT10	$0.450^{+5.70\%+6.00\%}_{-8.80\%-5.34\%}$	$0.741^{+9.50\%+5.91\%}_{-10.9\%-5.29\%}$	$0.607^{+2.34\%+0.672\%}_{-3.47\%-0.675\%}$
	NNPDF2.3	$0.470^{+5.26\%+2.22\%}_{-8.58\%-2.27\%}$	$0.771^{+8.97\%+2.16\%}_{-10.6\%-2.16\%}$	$0.609^{+2.23\%+0.205\%}_{-3.41\%-0.205\%}$
100 TeV	MSTW2008	$33.9^{+7.06\%+0.94\%}_{-8.29\%-1.26\%}$	$57.9^{+8.93\%+0.90\%}_{-9.46\%-1.20\%}$	$0.585^{+1.29\%+0.0526\%}_{-2.02\%-0.0758\%}$
	CT10	$32.4^{+6.87\%+2.29\%}_{-8.11\%-2.95\%}$	$55.5^{+8.73\%+2.16\%}_{-9.27\%-2.78\%}$	$0.584^{+1.27\%+0.189\%}_{-1.99\%-0.260\%}$
	NNPDF2.3	$33.2^{+6.62\%+0.78\%}_{-6.47\%-0.78\%}$	$56.9^{+7.62\%+0.75\%}_{-7.29\%-0.75\%}$	$0.584^{+1.29\%+0.0493\%}_{-2.01\%-0.0493\%}$

5-6%

0.5%

# EXAMPLE: TTH VS TTZ

Mangano, Plehn, Reimitz, Schell, HSS, JPG (2015)

Parameter	value	Parameter	value
$G_\mu$	$1.1987498350461625 \cdot 10^{-5}$	$n_{lf}$	5
$m_t$	173.3	$y_t$	173.3
$m_W$	80.419	$m_Z$	91.188
$m_H$	125.0	$\alpha^{-1}$	128.930

		$\sigma(t\bar{t}H)[\text{pb}]$	$\sigma(t\bar{t}Z)[\text{pb}]$	$\frac{\sigma(t\bar{t}H)}{\sigma(t\bar{t}Z)}$
13 TeV	default	$0.475^{+5.79\%}_{-9.04\%}$	$0.785^{+9.81\%}_{-11.2\%}$	$0.606^{+2.45\%}_{-3.66\%}$
	$\mu_0 = m_t + m_{H,Z}/2$	$0.529^{+5.96\%}_{-9.42\%}$	$0.885^{+9.93\%}_{-11.6\%}$	$0.597^{+2.45\%}_{-3.61\%}$
	$m_t = y_t v = 174.1 \text{ GeV}$	$0.474^{+5.74\%}_{-9.01\%}$	$0.773^{+9.76\%}_{-11.2\%}$	$0.614^{+2.45\%}_{-3.66\%}$
	$m_t = y_t v = 172.5 \text{ GeV}$	$0.475^{+5.81\%}_{-9.05\%}$	$0.795^{+9.82\%}_{-11.2\%}$	$0.597^{+2.45\%}_{-3.65\%}$
	$m_H = 126.0 \text{ GeV}$	$0.464^{+5.80\%}_{-9.04\%}$	$0.785^{+9.81\%}_{-11.2\%}$	$0.593^{+2.42\%}_{-3.62\%}$
100 TeV	default	$33.9^{+7.06\%}_{-8.29\%}$	$57.9^{+8.93\%}_{-9.46\%}$	$0.585^{+1.29\%}_{-2.02\%}$
	$\mu_0 = m_t + m_{H,Z}/2$	$39.0^{+9.76\%}_{-9.57\%}$	$67.2^{+10.9\%}_{-10.6\%}$	$0.580^{+1.16\%}_{-1.80\%}$
	$m_t = y_t v = 174.1 \text{ GeV}$	$33.9^{+7.01\%}_{-8.27\%}$	$57.2^{+8.90\%}_{-9.42\%}$	$0.592^{+1.27\%}_{-2.00\%}$
	$m_t = y_t v = 172.5 \text{ GeV}$	$33.7^{+6.99\%}_{-8.31\%}$	$58.6^{+8.93\%}_{-9.46\%}$	$0.576^{+1.27\%}_{-1.99\%}$
	$m_H = 126.0 \text{ GeV}$	$33.2^{+7.04\%}_{-8.28\%}$	$57.9^{+8.93\%}_{-9.46\%}$	$0.575^{+1.25\%}_{-1.95\%}$

- Scale choice from dynamical scale to fixed scale, the results are well embed in scale uncertainty
- Mass dependences are similar at percent level for the ratio.

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		$\alpha(m_Z)$ scheme			$G_\mu$ scheme		
		$\sigma(t\bar{t}H)$ [pb]	$\sigma(t\bar{t}Z)$ [pb]	$\frac{\sigma(t\bar{t}H)}{\sigma(t\bar{t}Z)}$	$\sigma(t\bar{t}H)$ [pb]	$\sigma(t\bar{t}Z)$ [pb]	$\frac{\sigma(t\bar{t}H)}{\sigma(t\bar{t}Z)}$
13 TeV	NLO QCD	0.475	0.785	0.606	0.462	0.763	0.606
	$\mathcal{O}(\alpha_S^2\alpha^2)$ Weak	-0.006773	-0.02516		0.004587	-0.007904	
	$\mathcal{O}(\alpha_S^2\alpha^2)$ EW	-0.0045	-0.022		0.0071	-0.0033	
	NLO QCD+Weak	0.468	0.760	0.617	0.467	0.755	0.619
	NLO QCD+EW	0.471	0.763	0.617	0.469	0.760	0.618
100 TeV	NLO QCD	33.9	57.9	0.585	32.9	56.3	0.585
	$\mathcal{O}(\alpha_S^2\alpha^2)$ Weak	-0.7295	-2.146		0.0269	-0.8973	
	$\mathcal{O}(\alpha_S^2\alpha^2)$ EW	-0.65	-2.0		0.14	-0.77	
	NLO QCD+Weak	33.1	55.8	0.594	32.9	55.4	0.594
	NLO QCD+EW	33.2	55.9	0.594	33.1	55.6	0.595

- (E)WK can be negative. Its impact is also at 2% level.

# EXAMPLE: HW

Mangano, Zanderighi et al., FCC-hh Physics report: SM processes '16



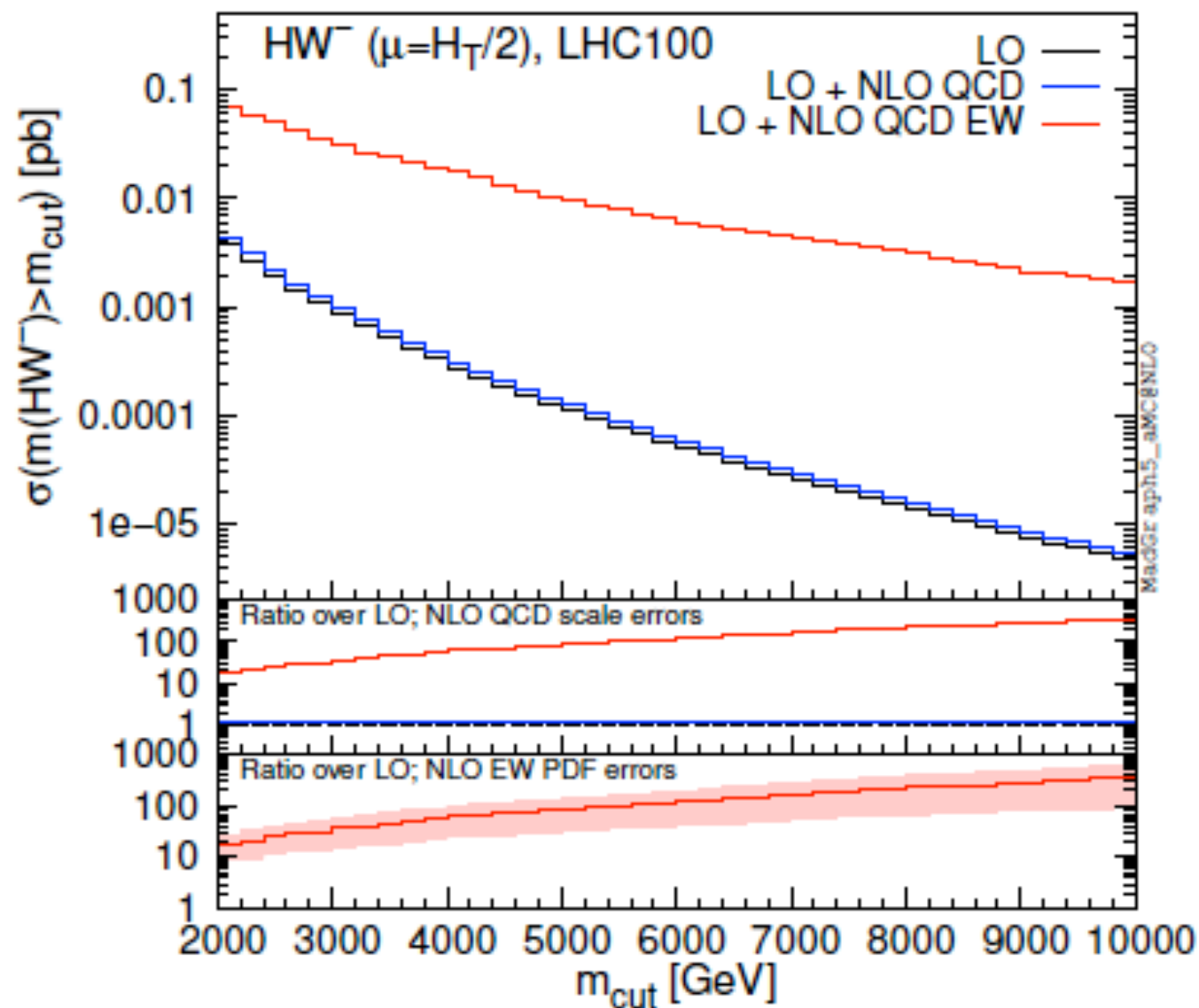
- **A funny example is HW production**
  - **NLO EW:** Ciccolini, Dittmaier, Kramer '03
  - **NLO EW with W decay:** Denner, Dittmaier, Kallweit, Much '12



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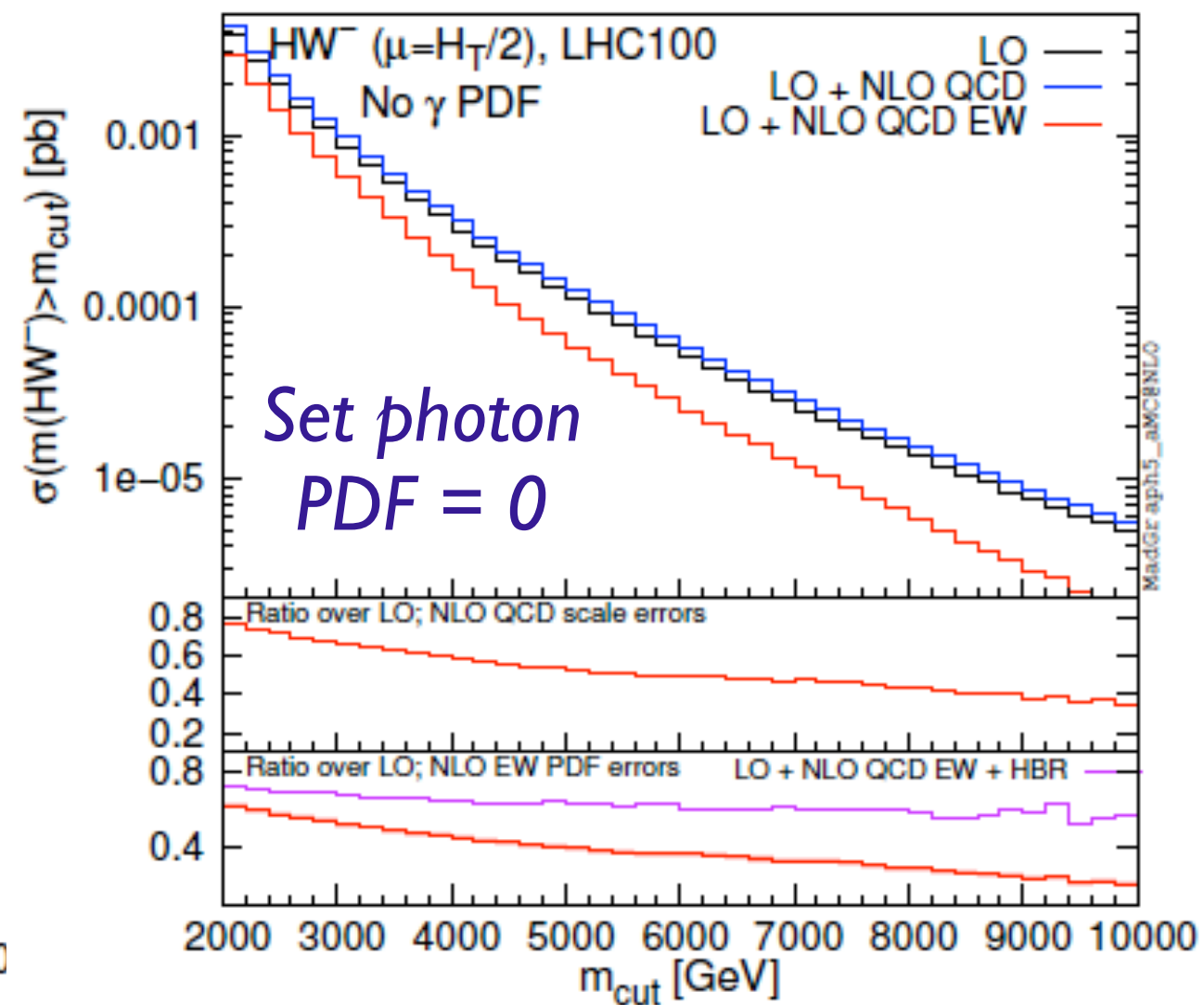
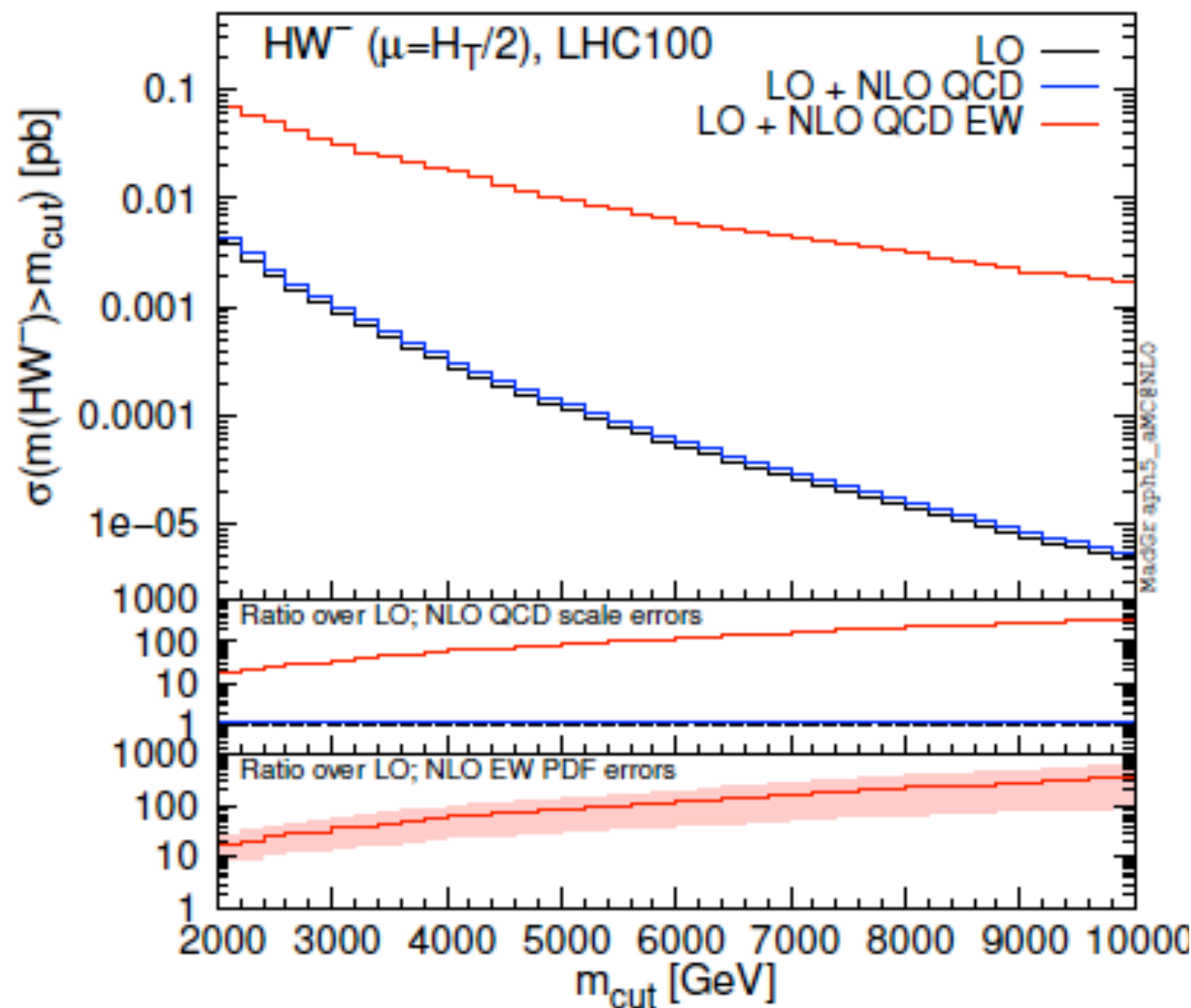
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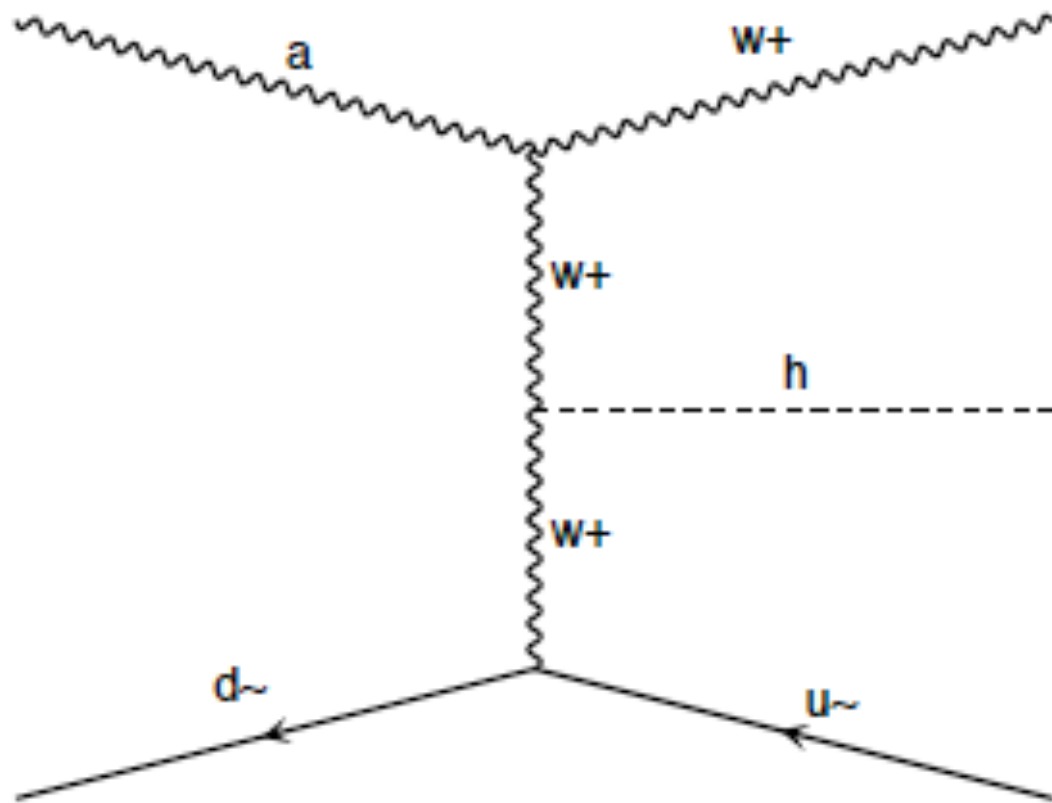




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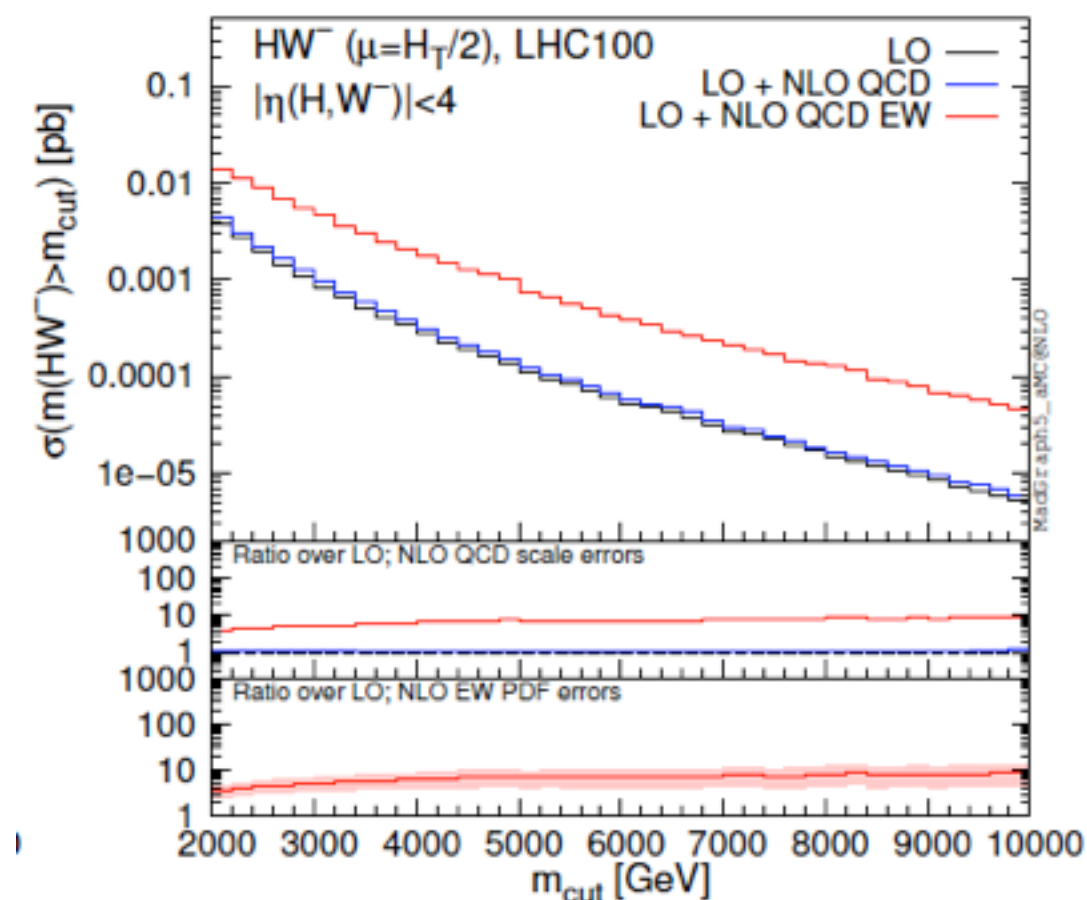
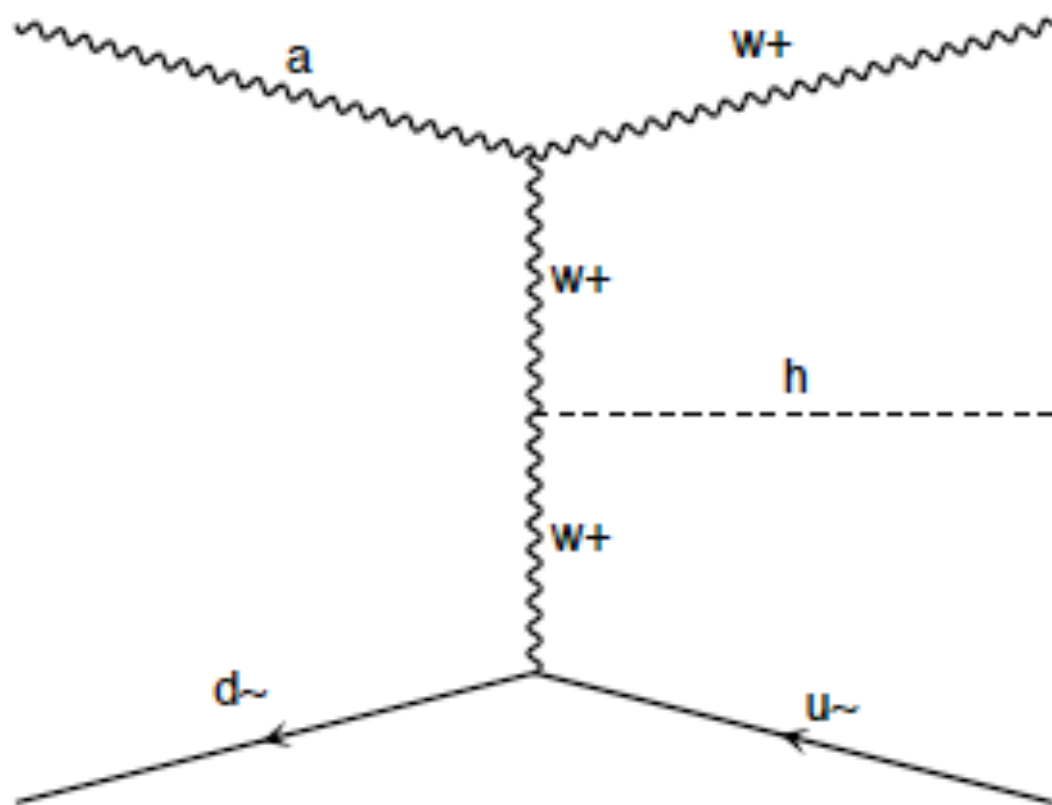
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  - It is mainly coming from photon initial state
  - There is no photon-quark or gluon-quark for H+jet at Born, when W soft/coll.
  - At Born, HW is produced via s-channel only, while NLO introduces t-channel
  - At large inv. mass, t-channel is dominant



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# EXAMPLE: 4-TOP AND TTW

- Large subleading NLO corrections were found in 4-top and  $t\bar{t}W$  due to  $t\bar{t}$  and  $tW$  scattering appears.

Frederix, Pagani, Zaro, JHEP (2018)

$$\sqrt{S} = 100 \text{ TeV} \quad pp \rightarrow t\bar{t}t\bar{t}$$

$$pp \rightarrow t\bar{t}W^\pm$$

$\delta[\%]$	$\mu = H_T/8$	$\mu = H_T/4$	$\mu = H_T/2$
LO <sub>2</sub>	-18.7	-20.7	-22.8
LO <sub>3</sub>	26.3	31.8	37.8
LO <sub>4</sub>	0.05	0.07	0.09
LO <sub>5</sub>	0.03	0.05	0.08
NLO QCD			
NLO EW			
NLO <sub>1</sub>	33.9	68.2	98.0
NLO <sub>2</sub>	-0.3	-5.7	-11.6
NLO <sub>3</sub>	-3.9	1.7	8.9
NLO <sub>4</sub>	0.7	0.9	1.2
NLO <sub>5</sub>	0.12	0.14	0.16
NLO <sub>6</sub>	< 0.01	< 0.01	< 0.01
NLO <sub>2</sub> + NLO <sub>3</sub>	-4.2	-4.0	2.7

$\delta[\%]$	$\mu = H_T/4$	$\mu = H_T/2$	$\mu = H_T$
LO <sub>2</sub>	-	-	-
LO <sub>3</sub>	0.9	1.1	1.3
NLO <sub>1</sub>	159.5 (69.8)	149.5 (71.1)	142.7 (73.4)
NLO <sub>2</sub>	-5.8 (-6.4)	-5.6 (-6.2)	-5.4 (-6.1)
NLO <sub>3</sub>	67.5 (55.6)	68.8 (56.6)	70.0 (57.6)
NLO <sub>4</sub>	0.2 (0.1)	0.2 (0.2)	0.3 (0.2)

# SUMMARY

- CEPC-SppC will provide many invaluable studies on particle physics, which requires the theoretical predictions at least at the same precision level.
- The proposal will trigger new theoretical discussions and new theoretical calculations in the new collider environment, where the main studies are still LHC oriented.
- Complete NLO (QCD and EW) calculations were automated in the proton-proton collision case and will be automated soon in the electron-positron collision case.

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*Stay tuned and thanks for listening !*