



# The study of a new time reconstruction method for MRPC read out by waveform digitizer

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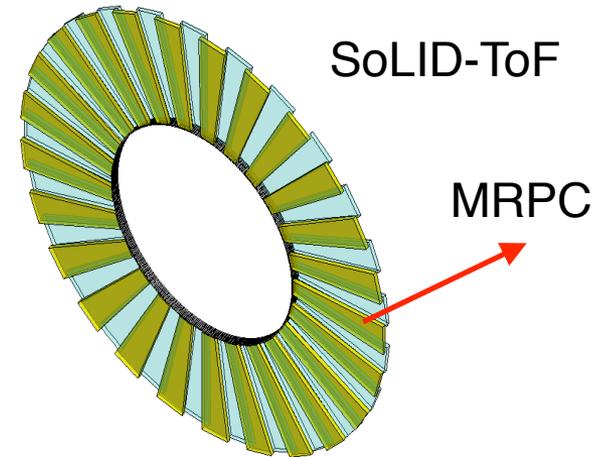
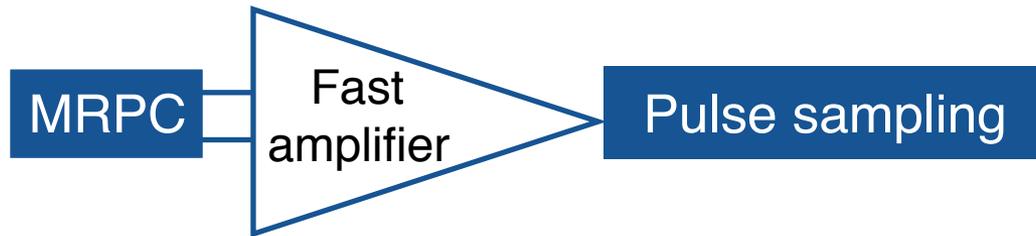
# Outline

- Introduction and Motivation
- The framework of analysis method
  - MRPC detector simulation
  - Different neural networks
- The results
  - Simulation
  - Experiment
- Conclusions



# Motivation

- Multi-gap Resistive Plate Chamber (MRPC)
- In physics experiments, MRPC is used in the Time-of-Flight(ToF) system as a timing detector
- In Solenoidal Large Intensity Device (SoLID) experiment:
  - pi/k separation up to 7GeV/c
  - Time resolution ~ 20ps

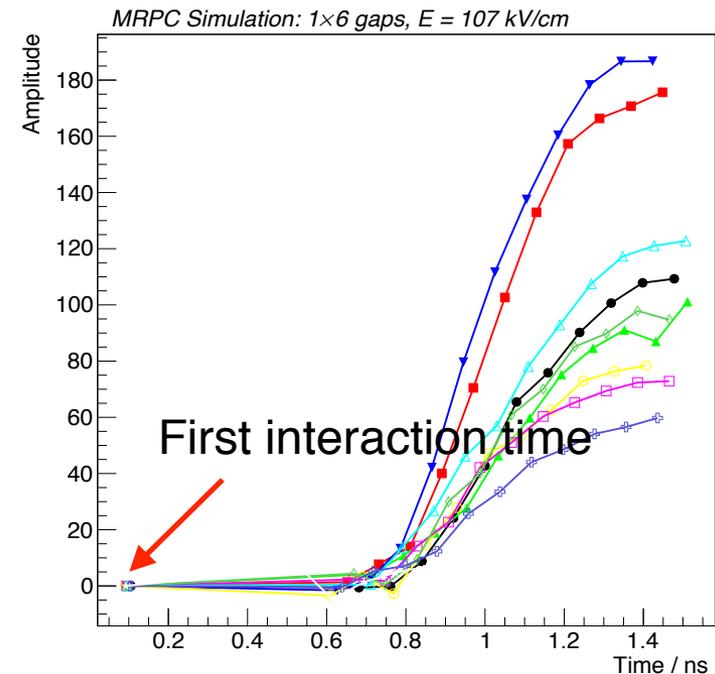
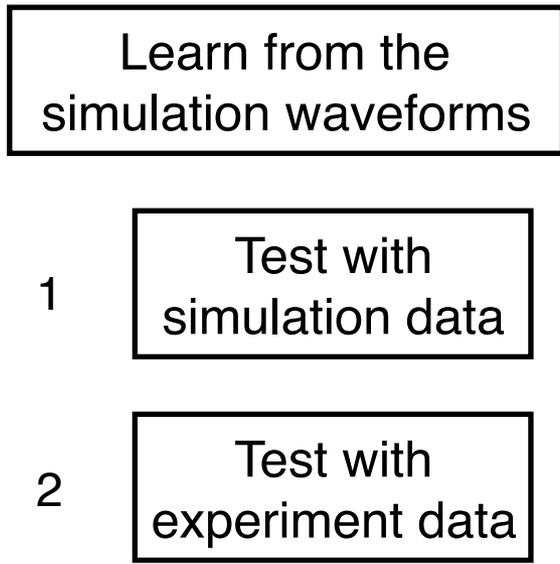


- Challenge for both MRPC and electronics.
- Electronics: Fast amplifier + pulse sampling
- **New** analysis method: take the advantage of the entire waveform



# Analysis method

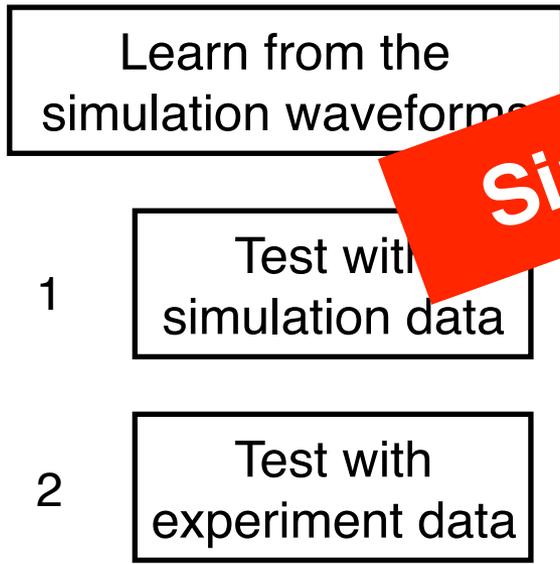
- The analysis method is based on the **neural network**.
- Artificial neural network(NN): powerful && widely used in high energy physics
- Introduce NN to obtain good time resolution:
  - — Find out the patterns from the MRPC signal and estimate the particle 1st interaction time more precisely.



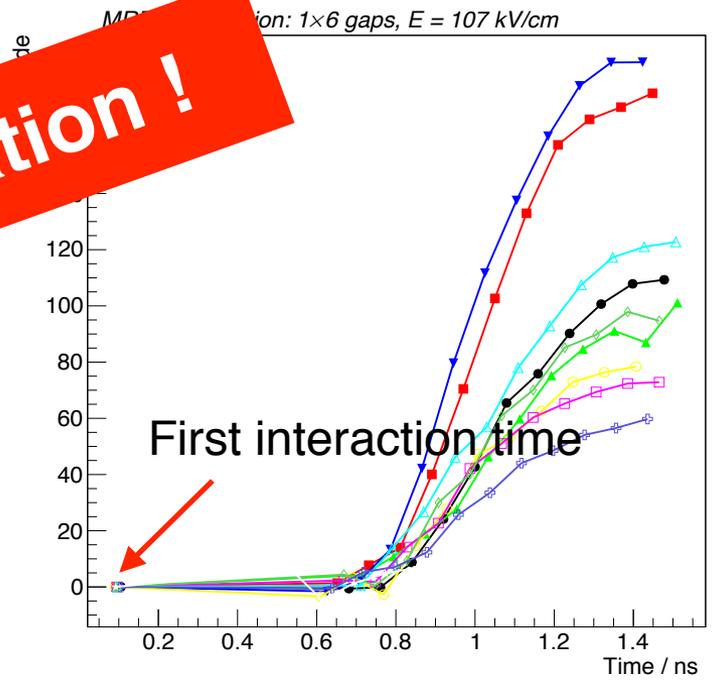


# Analysis method

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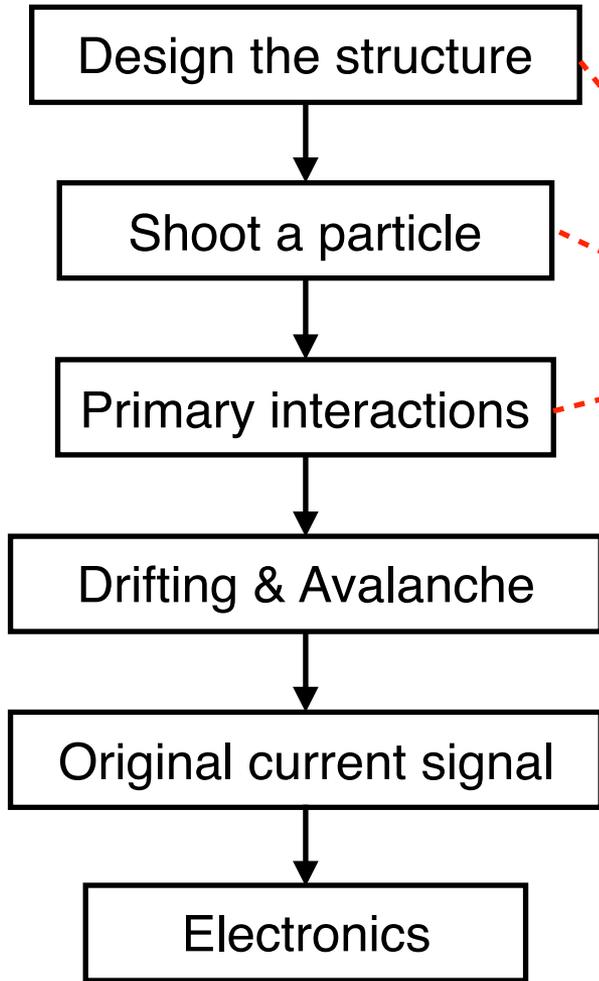


**Simulation !**



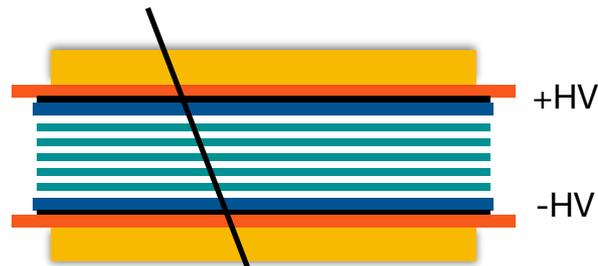


# Waveform simulation



- MRPC structure
- 6-gas MRPC
- Gap/glass thickness: 0.25/0.7 mm
- Gas: 90% C<sub>2</sub>H<sub>2</sub>F<sub>4</sub>, 5% C<sub>4</sub>H<sub>10</sub> and 5% SF<sub>6</sub>

Geant4



Cosmic muons: ~ 4GeV

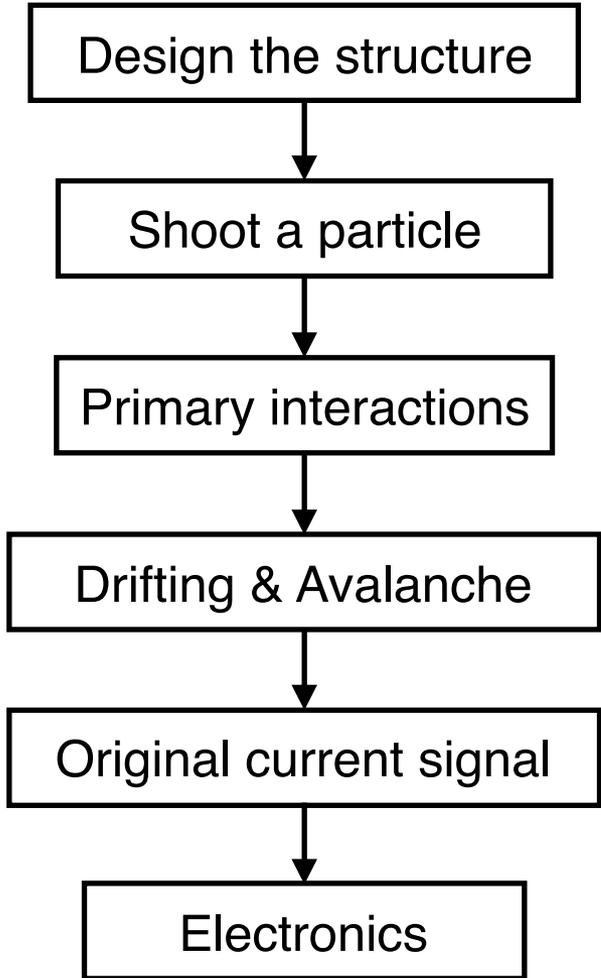
- Avalanche through drifting

$$\frac{d\bar{n}}{dx} = (\alpha - \eta)\bar{n} \quad \alpha: \text{Townsend coefficient} \quad \eta: \text{Attachment coefficient}$$

\*F. Wang, et al., A standalone simulation framework of the mrpc detector read out in waveforms, arXiv:1805.02387.



# Waveform simulation



- $P(n,x)$ : Prob(one electron  $\xrightarrow{x}$   $n$  electrons)

$$\begin{aligned}
 P(n, x + dx) = & P(n - 1, x)(n - 1)\alpha dx(1 - (n - 1)\eta dx) \\
 & + P(n, x)(1 - n\alpha dx)(1 - n\eta dx) \\
 & + P(n, x)n\alpha dx n\eta dx \\
 & + P(n + 1, x)(1 - (n + 1)\alpha dx)(n + 1)\eta dx
 \end{aligned}$$

- Divide the gap into  $\sim 500$  steps, and simulate the multiplication in every step
- Finally, avalanche growth like:  $e^{(\alpha - \eta)x}$
- Space charge effect:  $\sim 10^6$  electrons

- Induced current:

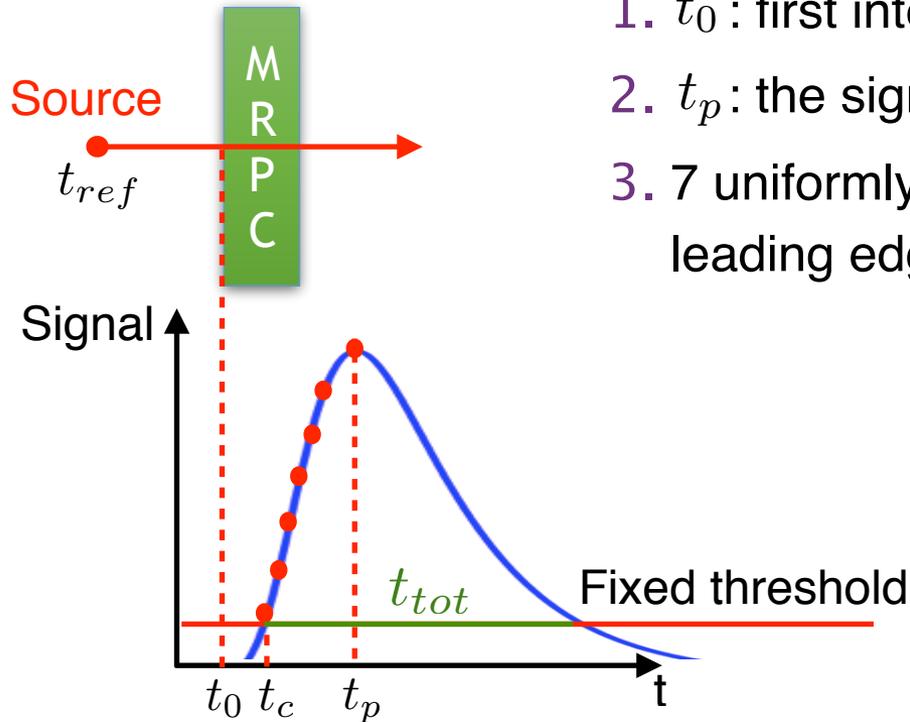
$$i(t) = \frac{E_W \cdot v}{V_W} e_0 N(t)$$

- Front-end electronics + noise

\*F. Wang, et al., A standalone simulation framework of the mrpc detector read out in waveforms, arXiv:1805.02387.



# Simulation data



## Simulation dataset :

1.  $t_0$  : first interaction happens
2.  $t_p$  : the signal reach the peak
3. 7 uniformly distributed points along the leading edge

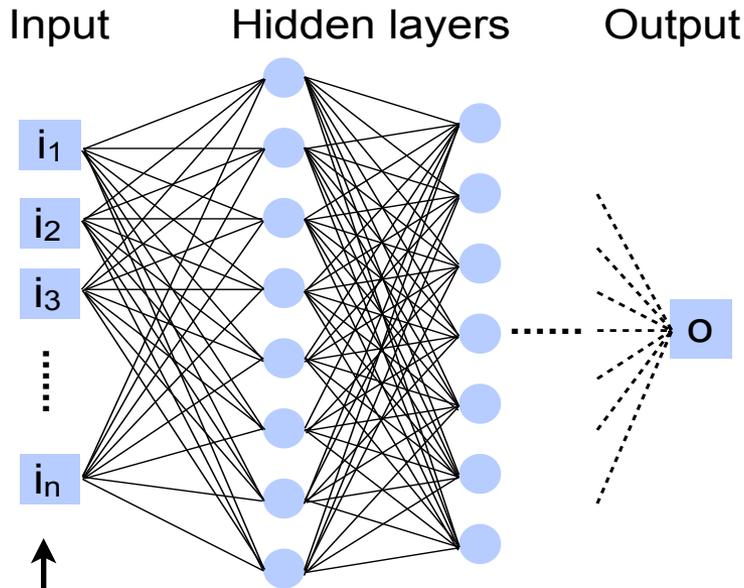


# Multilayer perceptron (MLP)

## Multilayer perceptron (MLP)

$$\underbrace{F_i(\vec{x})}_{\text{Output}} = h\left(\sum_j (\omega_{ij}^2 g(\dots g(\sum_k (\omega_{jk}^1 g(\sum_l (\omega_{kl}^0 x_l + \chi_k^0) \dots + \chi_j^1) + \chi_i^2))\right)$$

Input



- Activation function:  $g$  and  $h$  — —  $\tanh$
- Weights:  $\omega^{0,1\dots}, \chi^{0,1\dots}$
- “Dropout”: avoid overfitting

The length of the leading edge  $t_l$

Time of the very first interaction:  $t_0 = t_p - t_l$

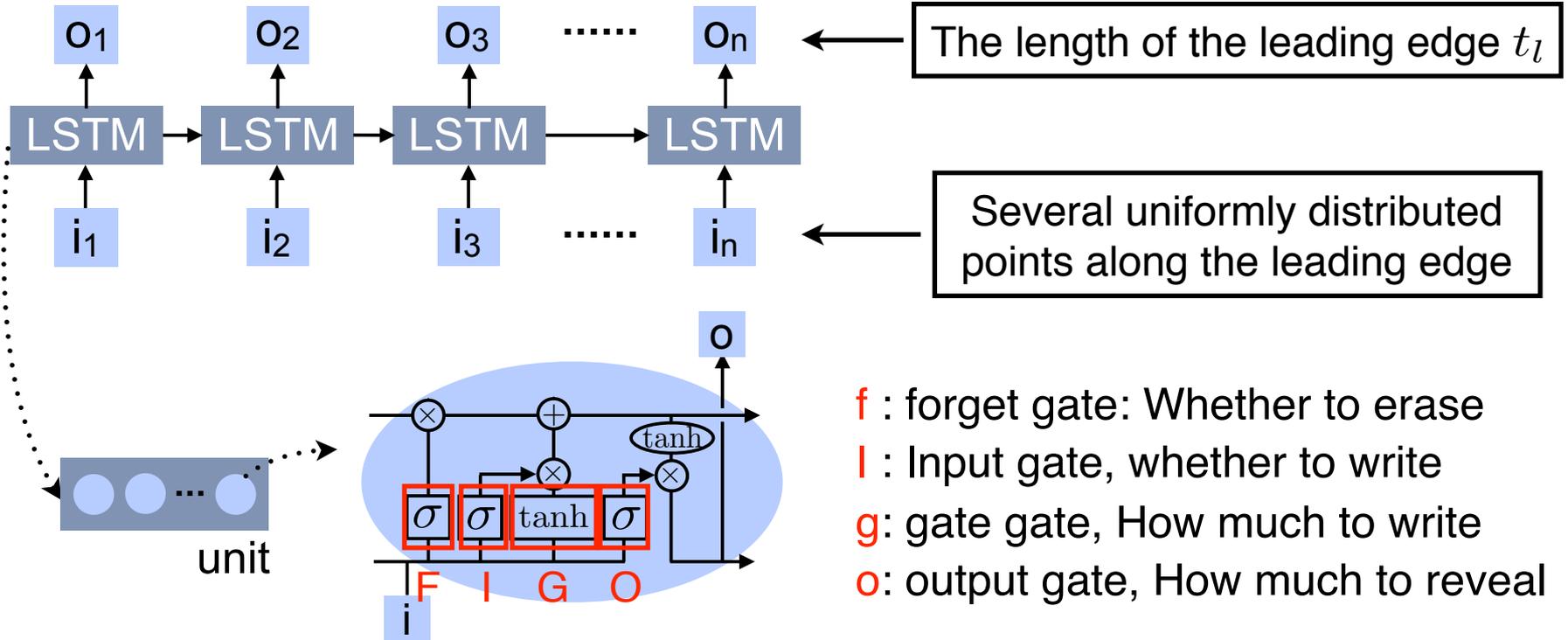
Several uniformly distributed points along the leading edge

- Train/validate/test set: 20/10/10 k
- Tensorflow & GPU: GTX 1080 Ti
- ~ 10 mins for training



# LSTM

- Recurrent neural networks(RNN): Long Short Term Memory network(LSTM)



- Train/validate/test set: 20/10/10 k
- Tensorflow & GPU: GTX 1080 Ti

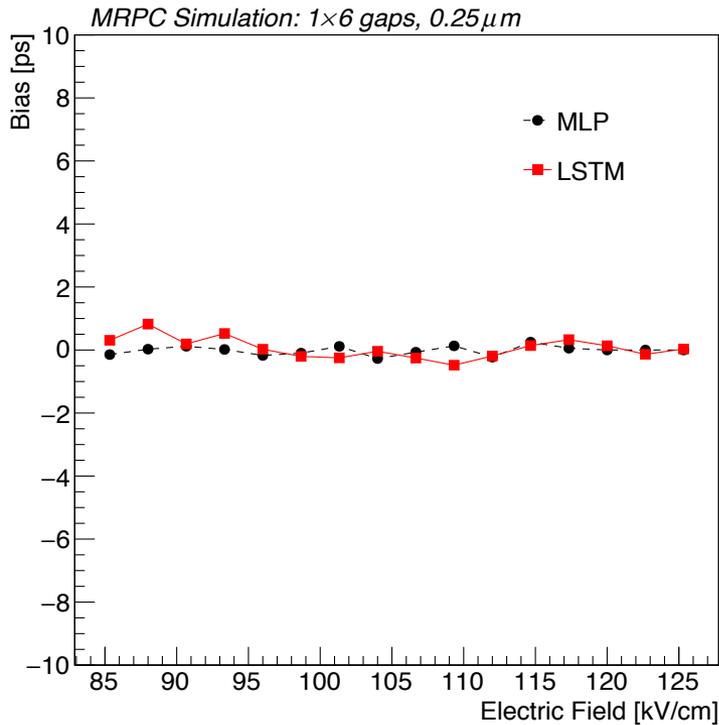
> 30 mins for training



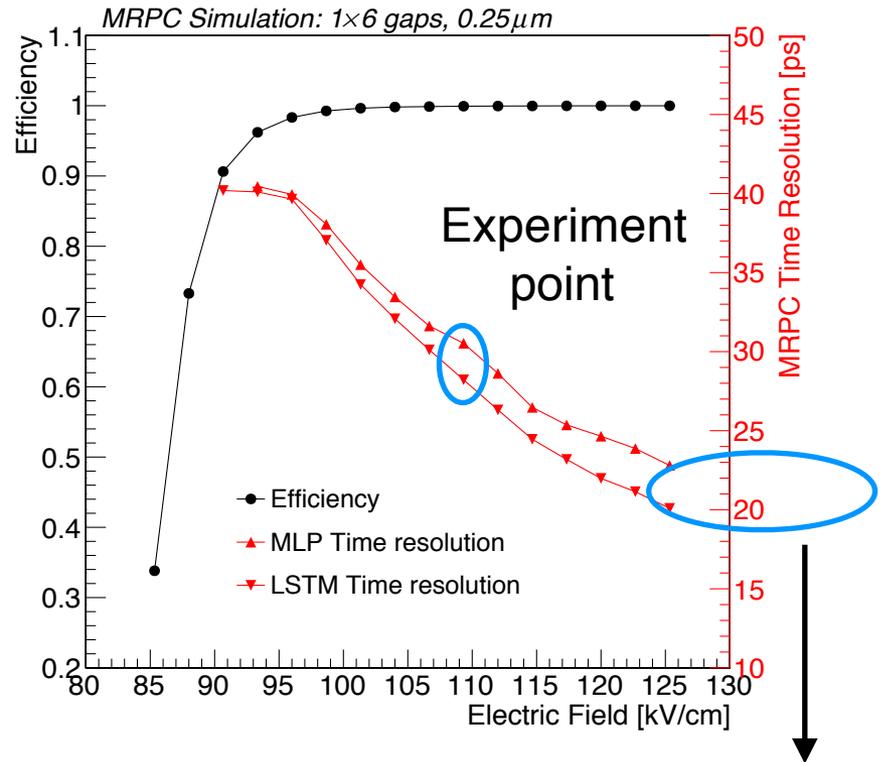
# Results of simulation

- Define bias:  $t_{estimate} - t_{truth}$

## Accuracy



## Precision



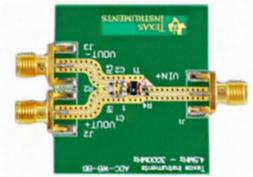
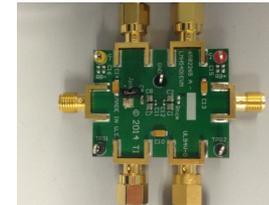
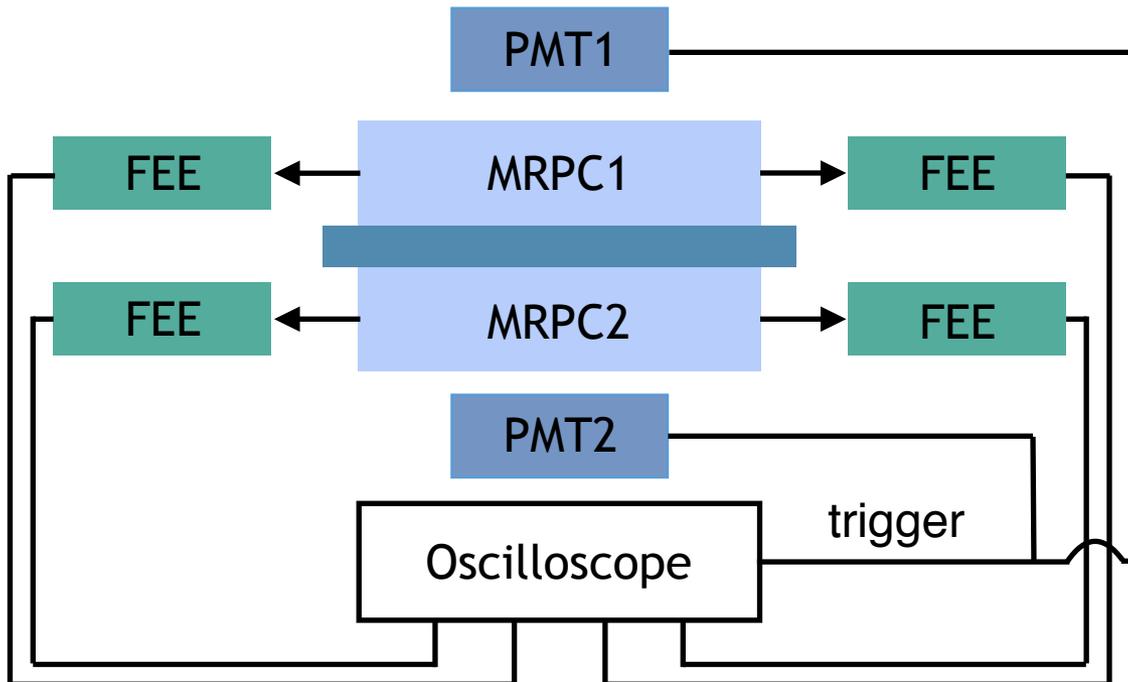
- Accuracy is good and stable
- The best time resolution can reach around 20 ps.

Streamer may happen



# Experiment setup

- Experiment of the cosmic ray
- 2 identical MRPC: 6-gap, 0.25mm gap, working at  $E=109$  kV/cm



- Oscilloscope bandwidth: 1 GHz
- Sampling rate: 10 GS/s

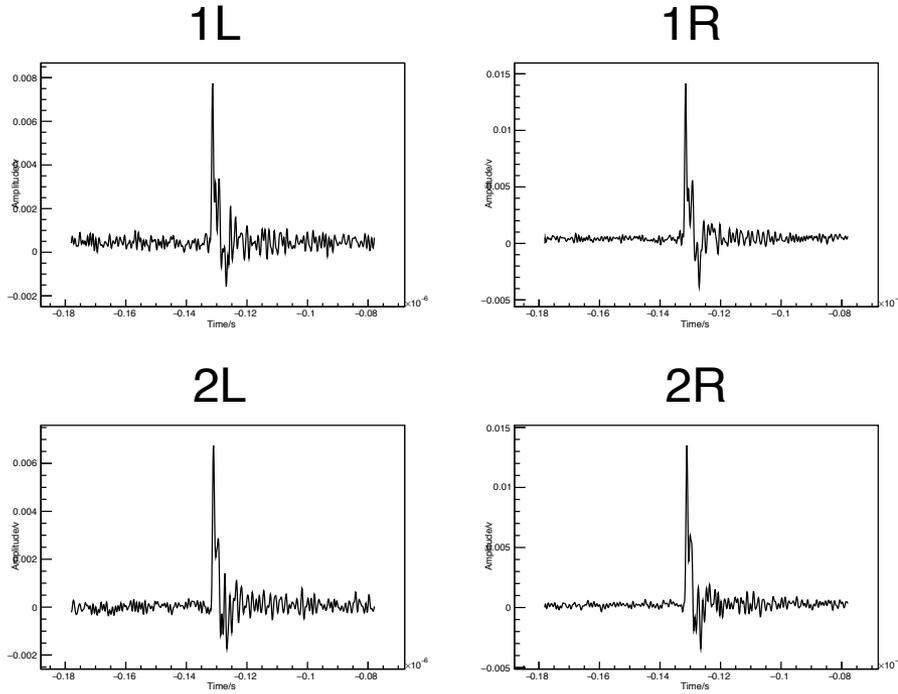
Leading edge: 700~800 ps

7~8 points along the edge

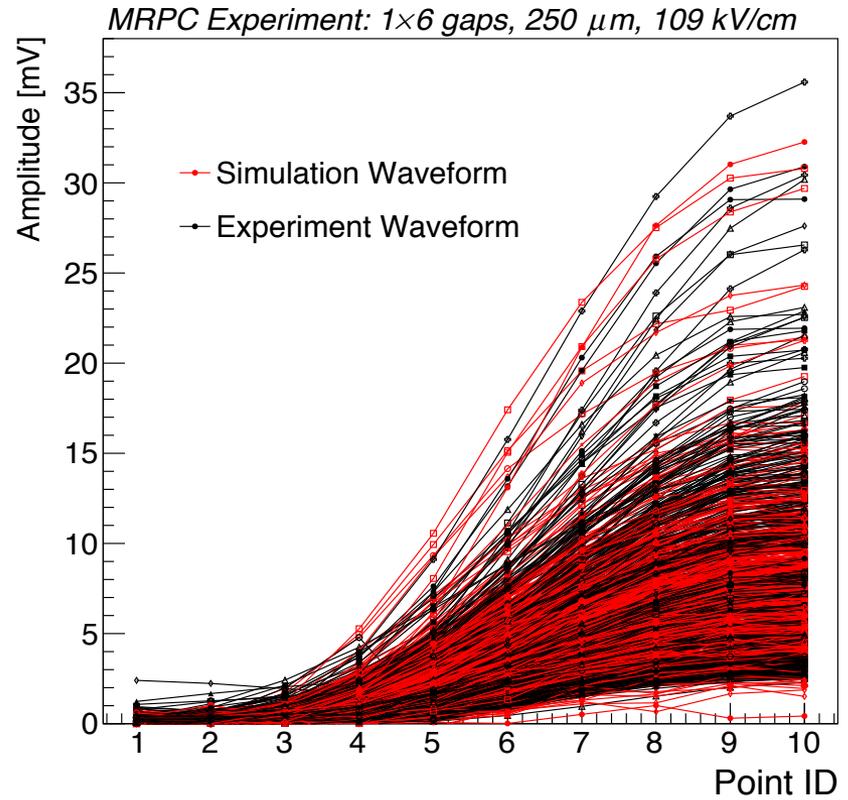


# Experiment waveform

- Compare the waveform



Waveforms of 1 event



Nearly the same!

Still with differences!



# Experiment result

- The 4 waveforms are estimated by the LSTM models separately
- Define:  $\Delta t = t_{MRPC1} - t_{MRPC2}$  for vertical particles

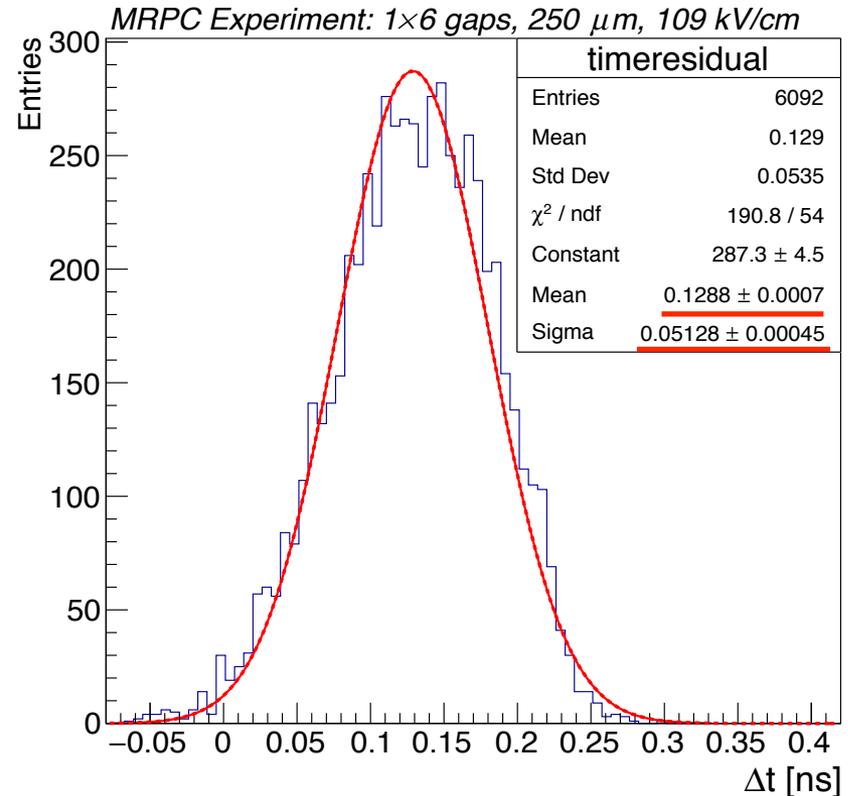
$$\Delta t_{true} = \frac{d_{MRPC} + d_{block}}{v} = \sim 130 \text{ ps}$$

- The time resolution of two MRPCs are independent:

$$\sigma_{MRPC} = \frac{\sigma(\Delta t)}{\sqrt{2}}$$

- With LSTM model, for vertical particles, the time resolution is:

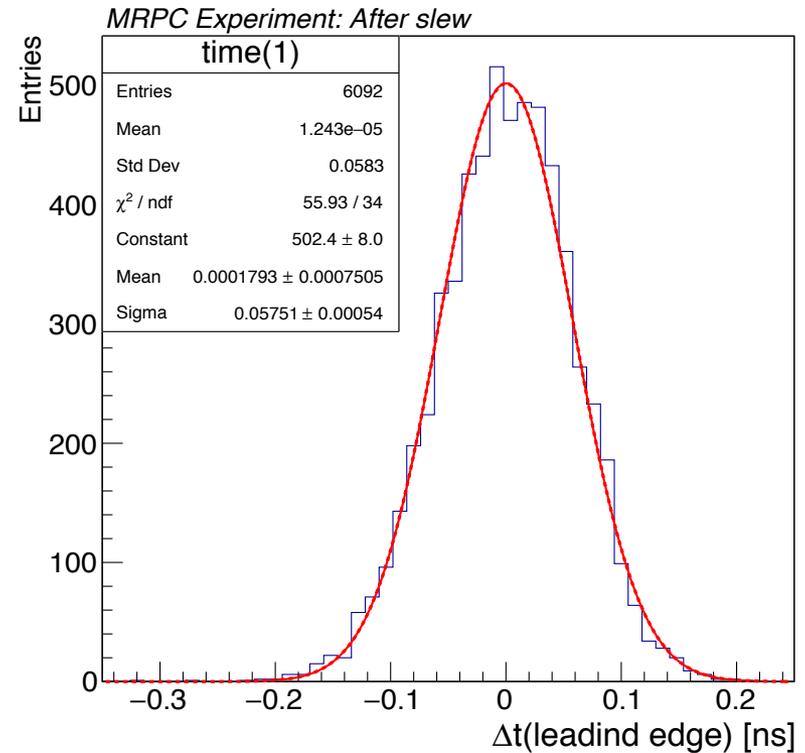
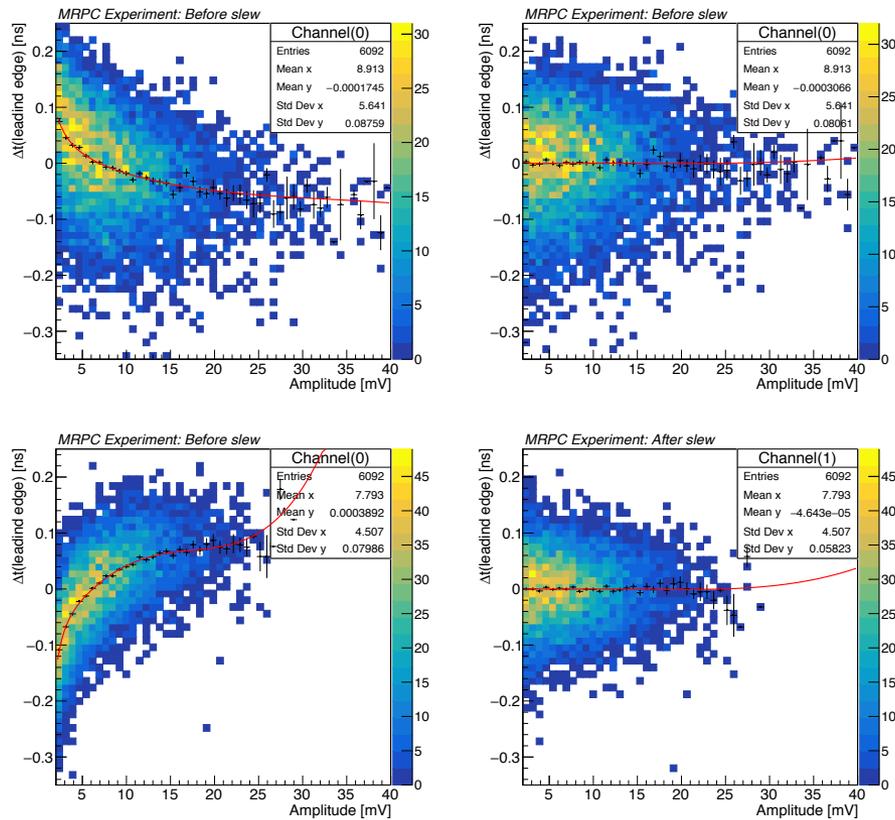
$$51.28 / \sqrt{2} = 36.3 \text{ ps}$$





# Experiment result

1. Much better than the typical time resolution of the 0.25 mm MRPC
2. Better than the state-of-the-art analysis method (Time over threshold (ToT) + slewing correction)



$$57.5 / \sqrt{2} = 40.7 \text{ ps}$$



# Conclusion

- A new time reconstruction method based on the neural network is proposed.
- Two sets of the networks(MLP and LSTM) are analyzed with the simulation data — — LSTM works better than MLP.
- The network models are also used in the experiment data, and the time resolution of 36 ps is achieved with 0.25mm thick MRPC.
  - Better than the typical time resolution
  - Better than the state-of-the-art analysis method
- Further studies on the thin gap MRPC is under consideration

# Thank you

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# Backup

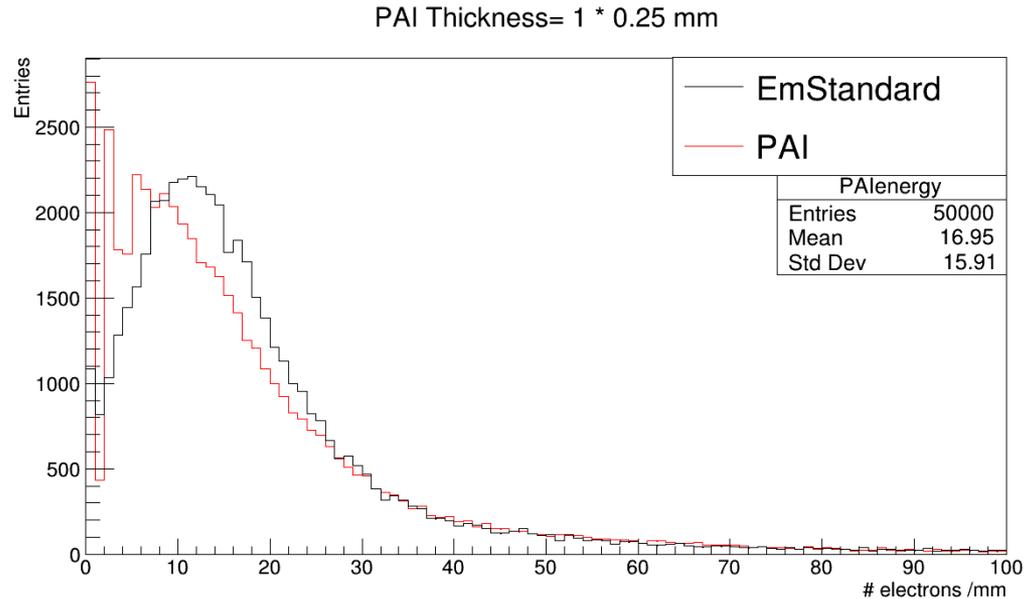
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# Physics List

- EMstandard: is most commonly used in LHC simulation,
- However, does not include shell electron effect — — only excellent for **thick** sensors.
- Photo Absorption Ionization (PAI) model: based on a corrected table of photo-absorption cross section coefficients and works for various elements.
- PAI: The simulated energy loss is in good agreement with the experiment data for moderately thin sensors\*.





# Charge Digitization

- Primary energy loss — — ionize electron-ion pairs.  $W = 30 \text{ eV}$
- Avalanche multiplication — — Townsend effect:

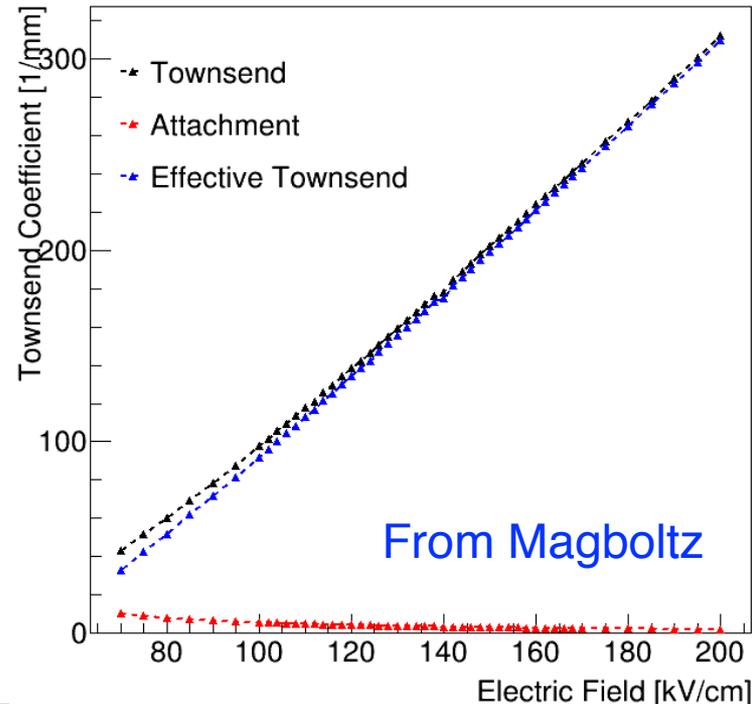
## Assumptions:

1. Every step of the multiplication is independent
2. Uniform electric field

$$\frac{d\bar{n}}{dx} = (\alpha - \eta)\bar{n}$$

$\alpha$  : Townsend coefficient

$\eta$  : Attachment coefficient





# Charge Digitization

## Multiplication in a small step:

- $P(n,x)$ : Prob(one electron  $\xrightarrow{x}$   $n$  electrons)

$$\begin{aligned}
 P(n, x + dx) = & P(n - 1, x)(n - 1)\alpha dx(1 - (n - 1)\eta dx) \\
 & + P(n, x)(1 - n\alpha dx)(1 - n\eta dx) \\
 & + P(n, x)n\alpha dx n\eta dx \\
 & + P(n + 1, x)(1 - (n + 1)\alpha dx)(n + 1)\eta dx
 \end{aligned}$$

- Divide the gap into  $\sim 300$  steps, and simulate the multiplication in every step
- Generate a random number according to  $P(n,x)^*$ :

$$n \begin{cases} 0, & s < k \frac{\bar{n}(x)-1}{\bar{n}(x)-k} \\ 1 + \text{Trunc}\left[\frac{1}{\ln(1-\frac{1-k}{\bar{n}(x)-k})} \ln\left(\frac{(\bar{n}(x)-k)(1-s)}{\bar{n}(x)(1-k)}\right)\right], & s > k \frac{\bar{n}(x)-1}{\bar{n}(x)-k} \end{cases}$$

$k = \frac{\eta}{\alpha}$   
 $s$ : uniform random number from (0,1)

- Finally, avalanche growth like:  $e^{(\alpha-\eta)x}$



# Original signal current

- Electrons drifting in the electric field: induce a signal on the read out strips
- Ramo theory:

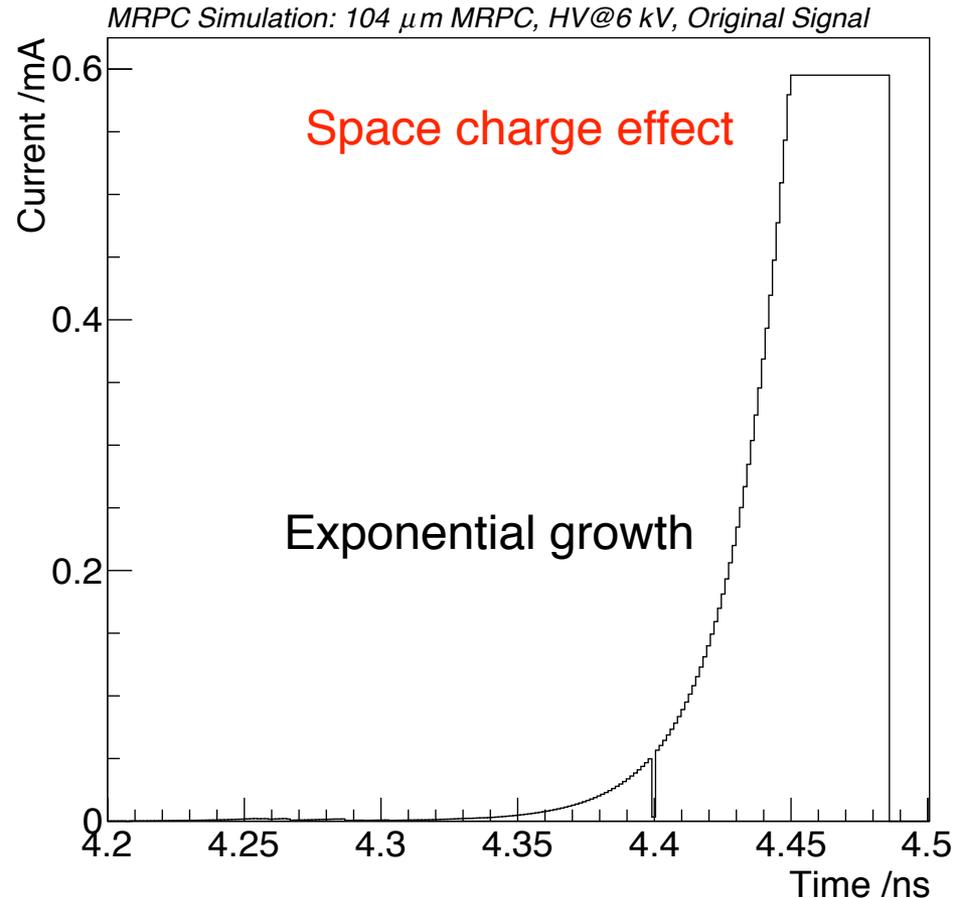
$$i(t) = \frac{E_W \cdot v}{V_W} e_0 N(t)$$

- Weighting field:

$$\frac{E_W}{V_W} = \frac{\varepsilon}{ng\varepsilon + (n + 1)d}$$

0.71 mm<sup>-1</sup>

- Space charge effect:  
~10<sup>6</sup> electrons

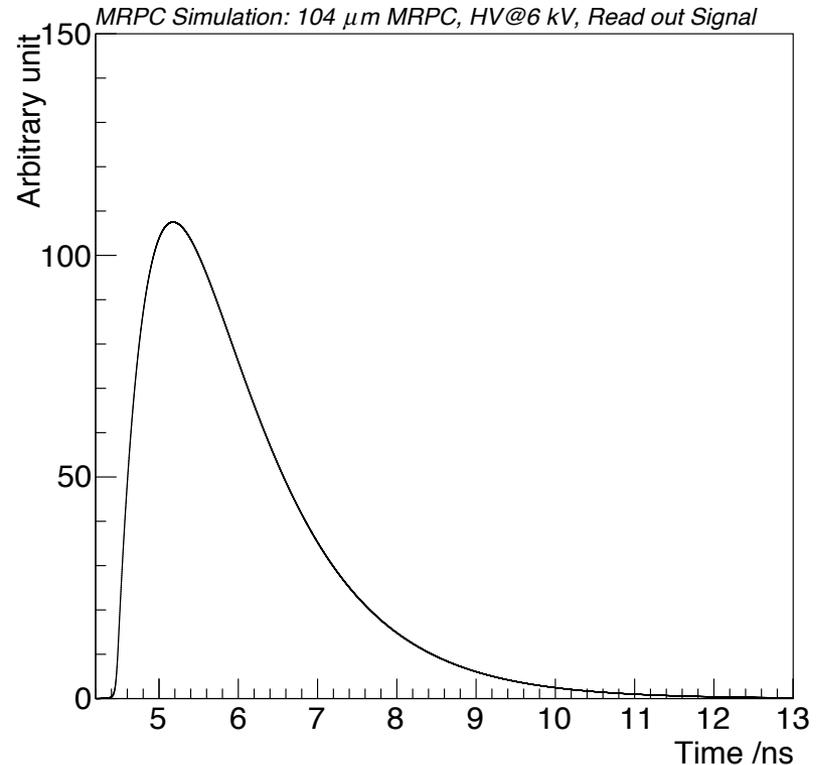




- Include the Front-end electronics response by convolving the original current with a simplified FEE response function:

$$f(t) = A(e^{-t/\tau_1} - e^{-t/\tau_2})$$

- $\tau_1$  : corresponds to the length of the leading edge
- $\tau_2$  : corresponds to the length of the trailing edge
- Noise is introduced by adding a random number sampled from  $\text{Gauss}(0, \sigma)$  to every time bin
- The signal without noise



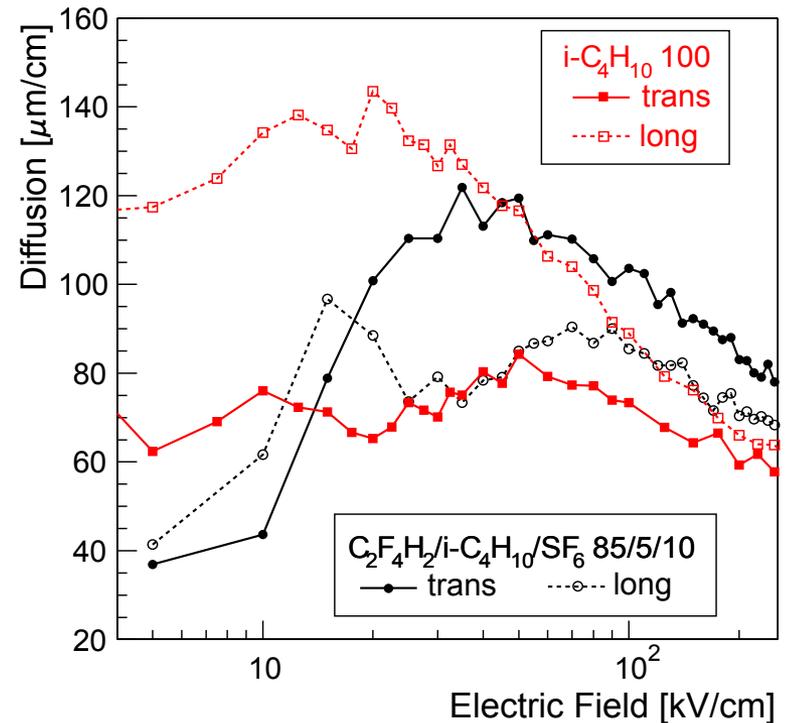


# Space charge effect

- Assumption:
  - — the electrons cluster grows like a circle in the transverse direction
- transverse diffusion length:  $\sim 100 \mu\text{m}/\sqrt{\text{cm}}$  at  $E \approx 100\text{kV}/\text{cm}$
- In the surface,  $10^6$  electrons:

$$E = \frac{Ne_0}{4\pi\epsilon_0 r^2} = 50 \text{ kV}/\text{cm}$$

- Comparable to the applied electric field

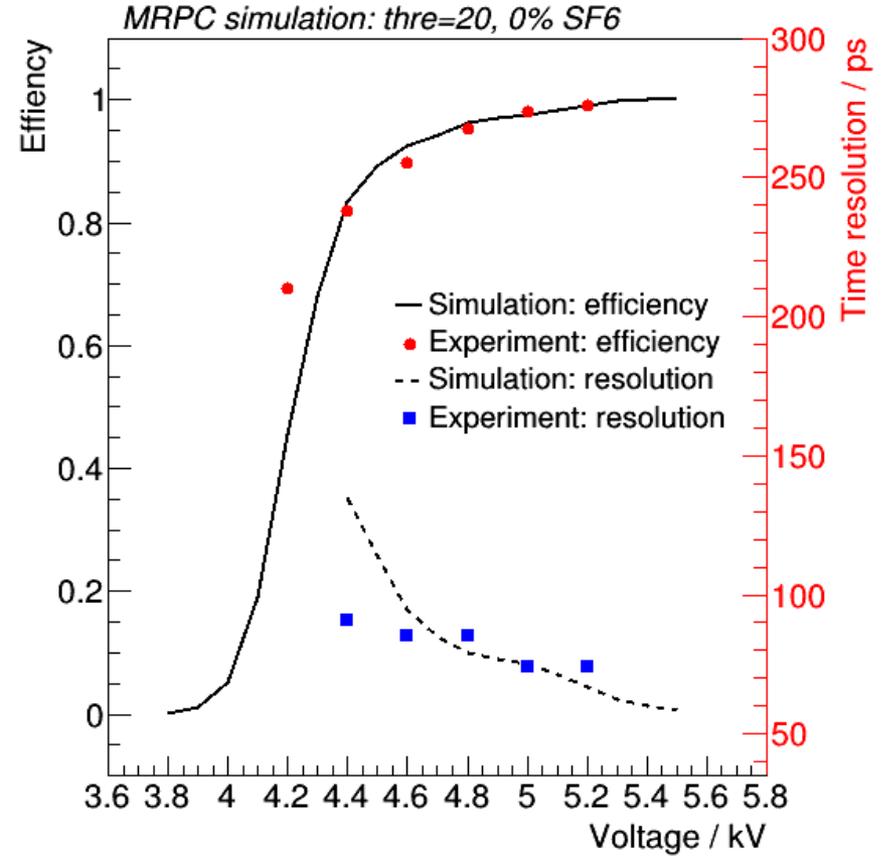
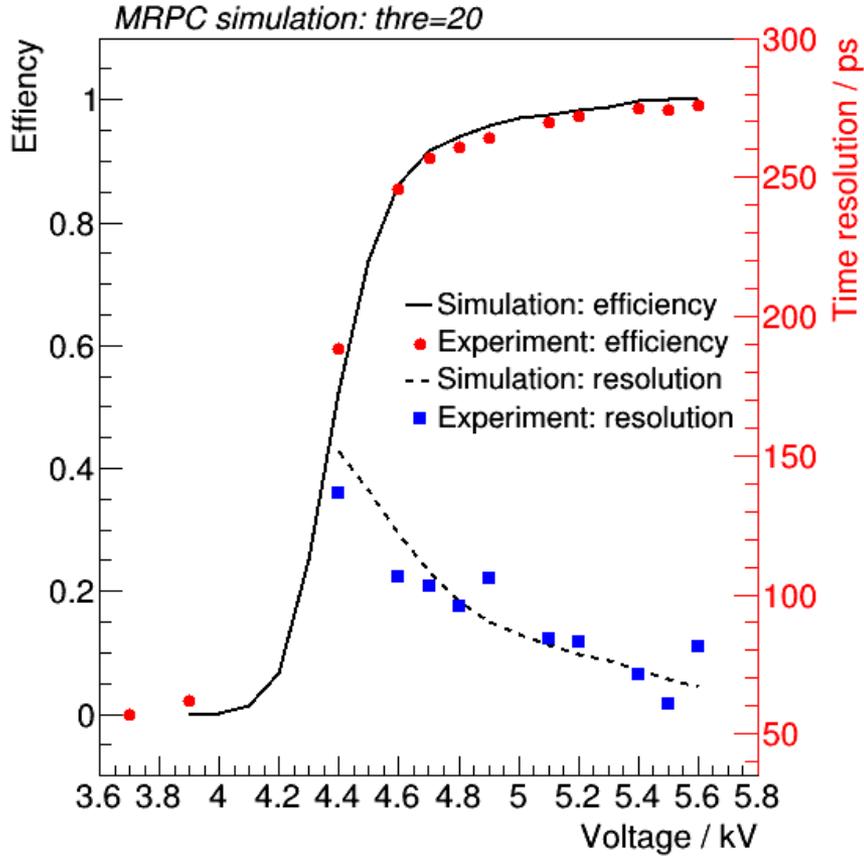


\*C. Lippmann, Detector physics of resistive plate chambers, Ph.D. thesis, Frankfurt U. (2003).



# simulation result

- 2\*4 gaps, 0.25 mm





# Time resolution

- Since both of the MRPCs are read out at double end — — 4 waveforms for every signal: 1L, 1R, 2L, 2R.
- The estimate time  $t_{est1,2}$  of each MRPC is the average of the left and right
- To eliminate the influence of the trigger, we calculate the difference of the two MRPC time:

$$\Delta t = t_{est2} - t_{est1}$$

- The difference of the 2 MRPC's truth time is a constant:

$$\sigma(\Delta t) = \sigma(t_{est2} - t_{true2} + t_{true1} - t_{est1}) = \sigma(t_{res1} - t_{res2})$$

- Then:

$$\sigma(\Delta t) = \sigma(t_{res1} - t_{res2}) = \sqrt{\sigma^2(t_{resi1}) + \sigma^2(t_{resi2})} = \sqrt{2\sigma_{MRPC}^2}$$

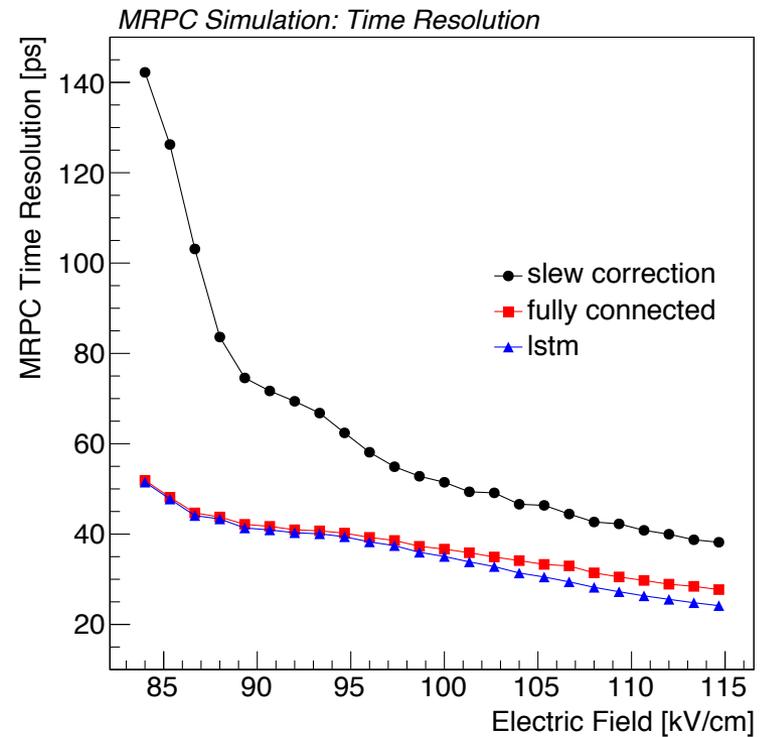
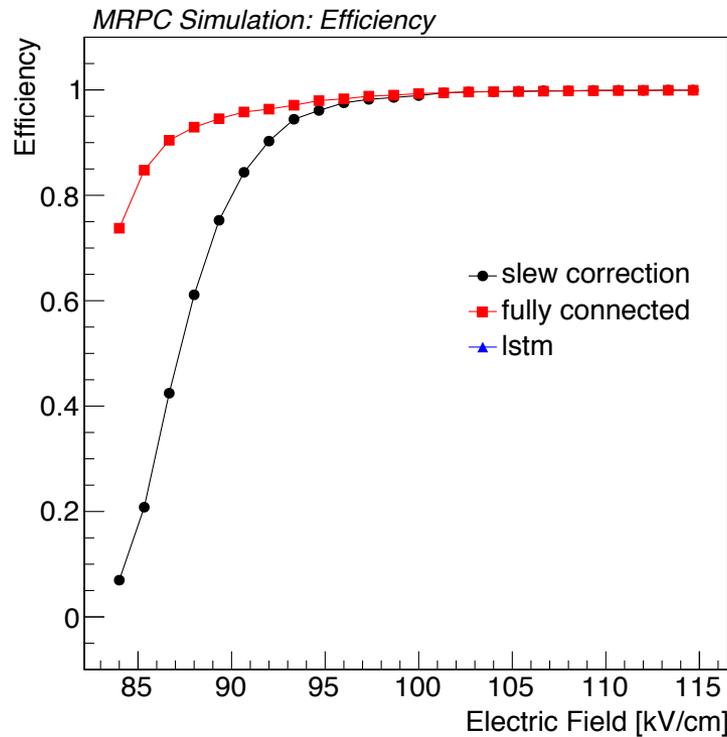
- Therefore:

$$\sigma_{MRPC} = \frac{\sigma(\Delta t)}{\sqrt{2}}$$



# Previous method

- Read out with time-over-threshold(ToT) + slewing correction





	Single-stack MRPC
Gas Gap Width	250 um (fishing line)
Number of Gas Gaps	1 stack x 6 layers = 6
Float Glass Thickness	700 um
Readout strip	7 mm x 270mm(3 mm internal)
Readout	differential, both ends
honey	6mm
PCB	0.8mm
mylar	0.25mm