



CTEQ

# Recent developments in the CTEQ-TEA global analysis

Tie-Jiun Hou

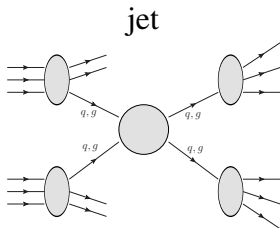
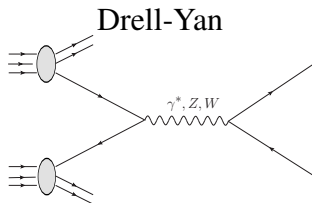
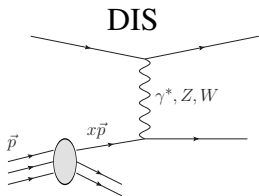
CTP-XJU

August 16, 2018 at SI2018

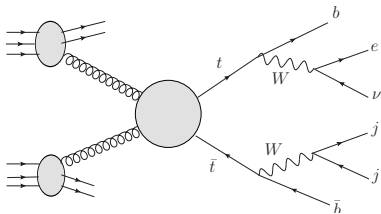
# CTEQ-TEA group

- CTEQ – Tung et al. (TEA)  
in memory of Prof. Wu-Ki Tung, who established  
CTEQ Collaboration in early 90's.
- Current members:  
Sayipjamal Dulat, Tie-Jiun Hou, Ibrahim Sitiwaldi  
(Xinjiang U.)  
Jun Gao (Shanghai Jiaotong U.)  
Marco Guzzi (Kennesaw State U.)  
Pavel Nadolsky, Timothy Hobbs, Keping Xie, Boting  
Wang (Southern Methodist U.)  
Joey Huston, Jon Pumplin, Carl Schmidt, Dan Stump,  
Jan Winter, C.-P. Yuan (Michigan State U.)

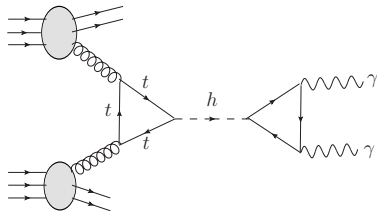
# PDF $f(x, Q)$ is universal



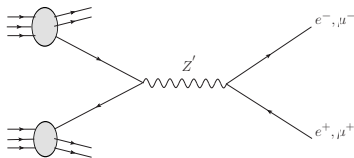
PDF (Parton distribution function) tell us the probability to find out a parton in a proton with particular momentum fraction  $x$  and energy  $Q$ .

$t\bar{t}$ 

Higgs



To determine the EW parameters via precision measurements requires knowing PDFs.



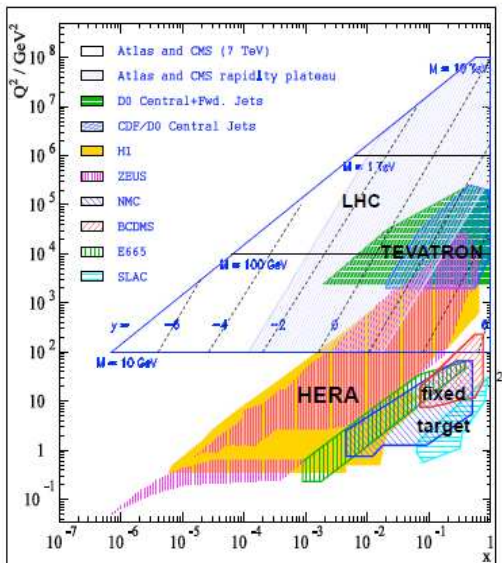
Probing New Physics requires knowing PDFs

## PDF evolve

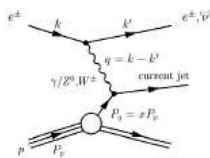
$$\begin{aligned}\frac{\partial q_i(x, \mu^2)}{\partial \ln \mu^2} &= P_{qq}^v \otimes q_i + P_{q\bar{q}}^v \otimes \bar{q}_i + P_{qq}^s \otimes \sum_k^{N_f} q_k + P_{q\bar{q}}^s \otimes \sum_k^{N_f} \bar{q}_k + P_{qg} \otimes g \\ \frac{\partial \bar{q}_i(x, \mu^2)}{\partial \ln \mu^2} &= P_{q\bar{q}}^v \otimes q_i + P_{q\bar{q}}^v \otimes \bar{q}_i + P_{q\bar{q}}^s \otimes \sum_k^{N_f} q_k + P_{q\bar{q}}^s \otimes \sum_k^{N_f} \bar{q}_k + P_{qg} \otimes g \\ \frac{\partial g(x, \mu^2)}{\partial \ln \mu^2} &= P_{gq} \otimes \sum_k^{N_f} (q_k + \bar{q}_k) + P_{gg} \otimes g\end{aligned}$$

DGLAP tells us how to evolve from the low energy scale, the input energy scale, to the high energy scale, the energy scale of interaction. But it does not tell us about its  $x$ -dependence. We need to use data to determine  $f(x, Q)$  as a function of  $x$  at  $Q_0$  scale.

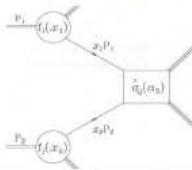
# Experimental access to the proton structure



HERA: low and medium  $x$



LHC: important constraints on  $g(x)$ ,  
flavour separation



Fixed Target: high  $x$ , nuclear PDFs

CT global analysis takes  $Q_0 = 1.3\text{GeV} \gg \Lambda_{QCD}$ , and assume

$$xf_a(x, Q_0, \{a_1, a_2, \dots\}) = x^{a_1}(1-x)^{a_2}P_a(x)$$

- $x \rightarrow 0$ :  $f \propto x^{a_1}$ , Regge-like behavior
- $x \rightarrow 1$ :  $f \propto (1-x)^{a_2}$ , quark counting rules
- $P(x; a_3, a_4, \dots)$ : affects intermediate  $x$ ; In CT14, Bernstein polynomial is applied.

For every proton flavor:

$$g, \quad u_v, \quad d_v, \quad s, \quad \bar{u}_s = u_s, \quad \bar{d}_s = d_s$$

Where  $u = u_v + u_s$ , and  $d = d_v + d_s$ .

In total, there are about 28 shape parameters used in CT14.

# Requirements for PDF parametrization

- Valence quark number sum rule

$$\int_0^1 [u(x) - \bar{u}(x)] dx = 2, \int_0^1 [d(x) - \bar{d}(x)] dx = 1$$

$$\int_0^1 [s(x) - \bar{s}(x)] dx = 0$$

Where  $u = u_v + \bar{u}$ ,  $d = d_v + \bar{d}$ . ( $s(x) - \bar{s}(x)$ ) can be non-zero.

- Momentum sum rule

$$\sum_{a=q,\bar{q},g} \int_0^1 x f_{a/p}(x, Q) dx = 1$$

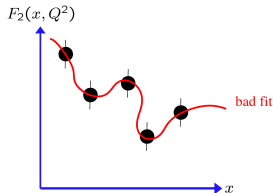
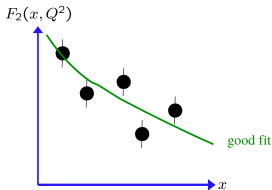
Where

$$\int_0^1 x g(x, Q) dx \sim 0.45$$



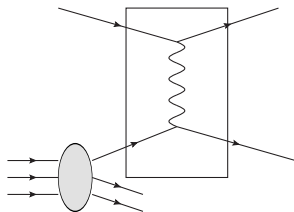
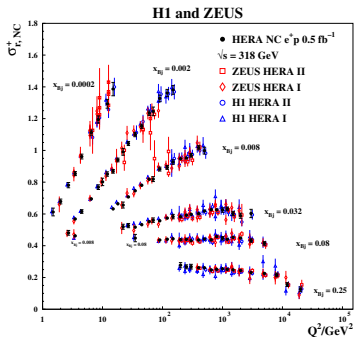
# Requirements for PDF parametrization

- A valid PDF set must not produce unphysical predictions for observables
  - Any conceivable hadron cross section  $\sigma$  must be non-negative:  $\sigma > 0$ . This is typically realized by requiring  $f_{a/p}(x, Q) > 0$ .
  - Any cross section asymmetry  $A$  must lie in the range  $-1 \leq A \leq 1$ . This constrains the range of allowed PDF parametrizations.
- PDF parametrization for  $f_{i/p}(x, Q)$  must be "flexible just enough" to reach agreement with the data, without reproducing random fluctuation.



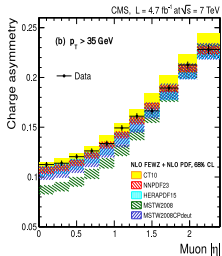
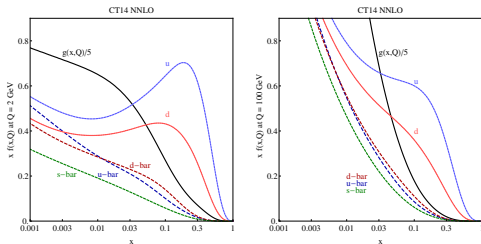
PDF is determined by comparing data and hard cross section

$$\sigma = f(x, Q^2, \{a\}) \otimes \hat{\sigma}$$

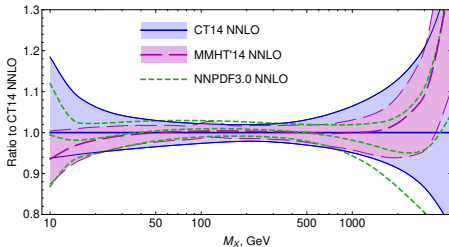


PDF	Hard part
LO	LO
NLO	NLO
NNLO	NNLO

PDF will then contribute to the precision measurement and search for new physics.



Gluon-gluon luminosity,  $\sqrt{s} = 13 \text{ TeV}$ , 68% c.l.



# Criteria for determine PDFs

Define

$$\chi_{global}^2 = \sum_i \frac{[D_i - \sum_k \lambda_k \beta_{ki} - T_i(\{a\})]^2}{\sigma_i^2} + \sum_k \lambda_k^2.$$

Where

$D_i$  is the central value of data,

$T_i(\{a\})$  is the theoretical prediction of the data,

$\sigma_i^2$  is the quadratic sum of the statistical error and uncorrelated error,

$\beta_{ki}$  is the matrix for correlated error,

and  $\lambda_k$  are the nuisance parameters.

The PDF is obtained by minimize the global  $\chi^2$  function respect to  $\{a\}$  and  $\{\lambda\}$ .

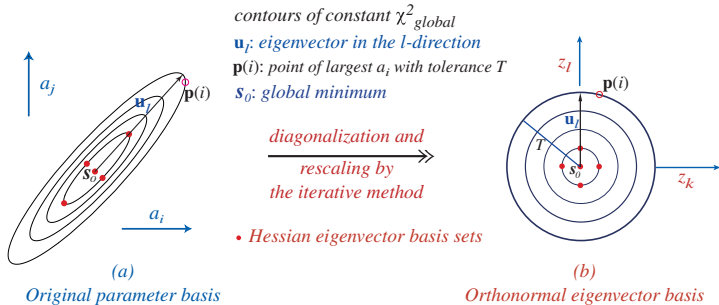
# Probe the uncertainty of PDFs

The uncertainty of the PDF is estimated by the Hessian method.

$$\chi^2 = \chi_0^2 + \sum_{i,j} H_{ij} y_i y_j, \quad H_{ij} = \frac{1}{2} \left( \frac{\partial^2 \chi^2}{\partial y_i \partial y_j} \right)_0,$$

Where  $y_i = a_i - a_i^0$  with  $a_i^0$  to be the parameters at minimal  $\chi_0^2$ .

*2-dim (i,j) rendition of d-dim (~16) PDF parameter space*



Let  $X = X(\{a_i\})$  to be the observable as a function of fitting parameter. Using the linear approximation of parameter  $\{z_i\}$ , the symmetry uncertainty of  $X$  is,

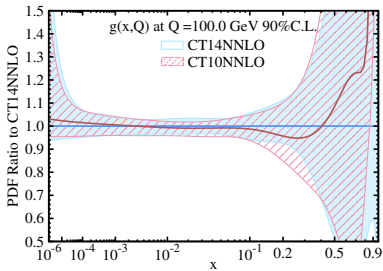
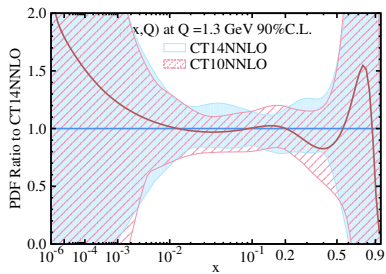
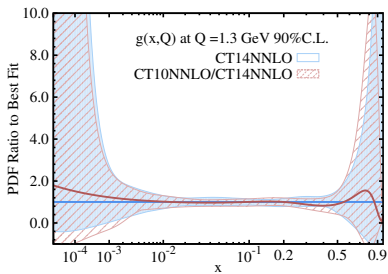
$$\Delta X = \frac{1}{2} \left( \sum_{i=1}^{N_p} [X(\{z_i^+\}) - X(\{z_i^-\})]^2 \right)^{1/2},$$

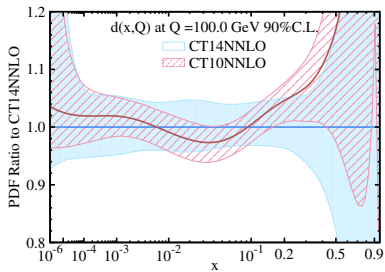
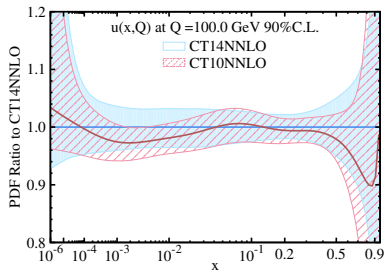
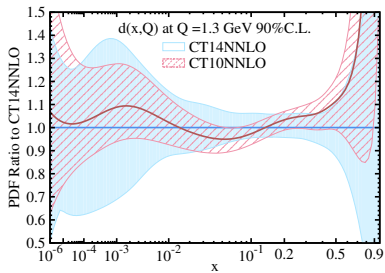
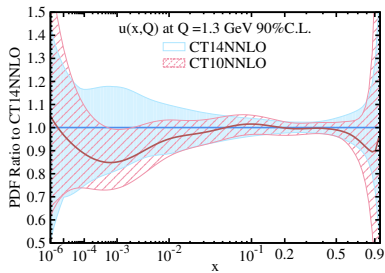
Where  $\{z_1^\pm\} = \{\pm T, 0, \dots\}$ ,  $\{z_2^\pm\} = \{0, \pm T, 0, \dots\}$  and so on. The asymmetry uncertainty of  $X$  is,

$$\delta^+ X = \sqrt{\sum_{i=1}^{N_a} \left[ \max \left( X_i^{(+)} - X_0, X_i^{(-)} - X_0, 0 \right) \right]^2},$$

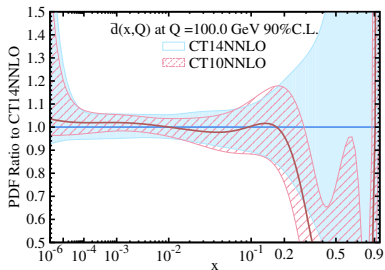
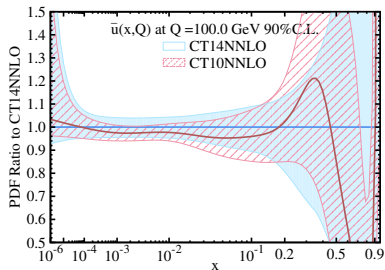
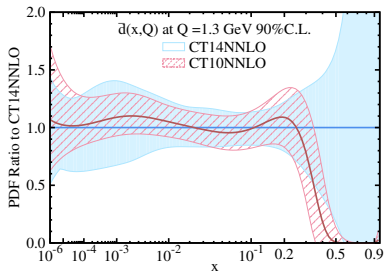
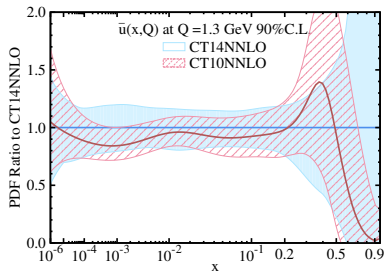
$$\delta^- X = \sqrt{\sum_{i=1}^{N_a} \left[ \max \left( X_0 - X_i^{(+)}, X_0 - X_i^{(-)}, 0 \right) \right]^2},$$

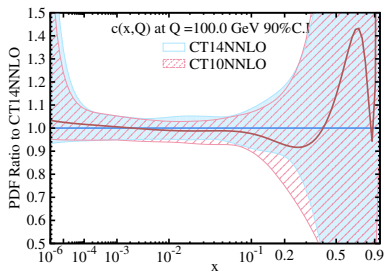
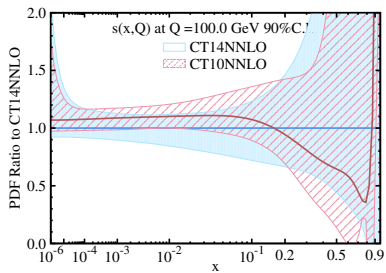
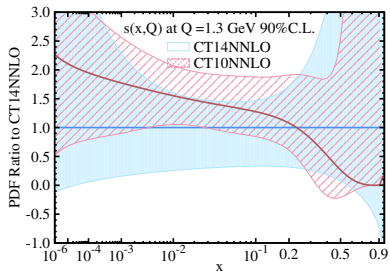
$$g(x, Q)$$



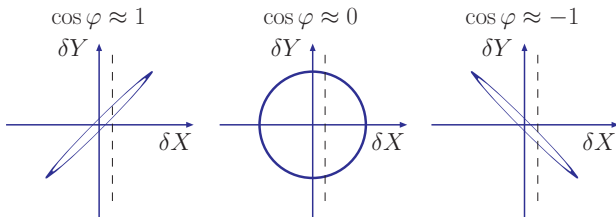
$u(x, Q)$  $d(x, Q)$ 



$\bar{u}(x, Q)$  $\bar{d}(x, Q)$ 

$S(x, Q)$  $c(x, Q)$ 

Is there a way to see the potential impact to PDF  
before real global analysis?



In the framework of the Hessian, the correlation between two variables  $X$  and  $Y$  can be worked out as.

$$\cos \varphi = \frac{\vec{\nabla}X \cdot \vec{\nabla}Y}{\Delta X \Delta Y} = \frac{1}{4\Delta X \Delta Y} \sum_{\alpha=1}^N \left( X_{\alpha}^{(+)} - X_{\alpha}^{(-)} \right) \left( Y_{\alpha}^{(+)} - Y_{\alpha}^{(-)} \right)$$

where the  $\Delta X$  and  $\Delta Y$  are their symmetric uncertainties. By this correlation angle  $\varphi$ , the tolerance ellipse is defined by

$$X = X_0 + \Delta X \cos \theta, \quad Y = Y_0 + \Delta Y \cos(\theta + \varphi),$$

- The correlation cosine between PDF  $f(x, \mu)$  and theoretical prediction  $T_i$  contains no information of the experimental uncertainty.
- The correlation cosine  $C_f(x_i, \mu_i)$  between PDF  $f(x, \mu)$  and residual  $r_i$  contains no information of the experimental uncertainty in practice

$$C_f(x_i, \mu_i) = \frac{\vec{\nabla} f(x_i, \mu_i) \cdot \vec{\nabla} r_i}{\Delta f(x_i, \mu_i) \Delta r_i}, \quad \text{where}$$

$$\chi^2 = \sum_i^N r_i^2 + \sum_k \lambda_k^2, \quad r_i(\vec{a}) = \frac{D_i - \sum_k \lambda_k \beta_{ki} - T_i(\{a\})}{\sigma_i}$$

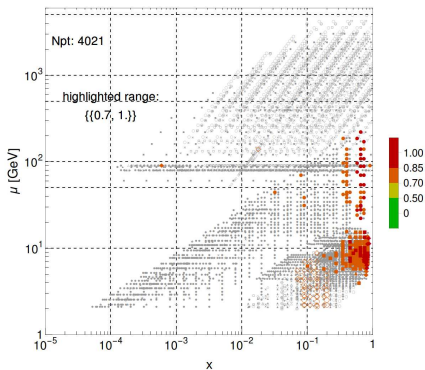
- Instead, we concern the "sensitivity"  $S_f(x_i, \mu_i)$

$$S_f(x_i, \mu_i) = C_f(x_i, \mu_i) \frac{\Delta r_i}{\sqrt{\frac{\sum_i^N r_i^2}{N}}}$$

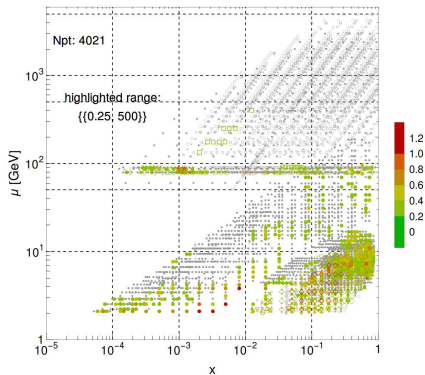
The sensitivity  $S_f(x_i, \mu_i)$  help us to visualize the potential impact on PDF in  $x - Q$  plane.

$$u(x, \mu)$$

|  $C_f$  | for  $u(x, \mu)$ , CT14HERA2NNLO

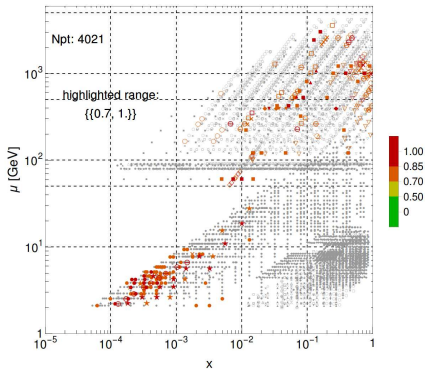


|  $S_f$  | for  $u(x, \mu)$ , CT14HERA2NNLO

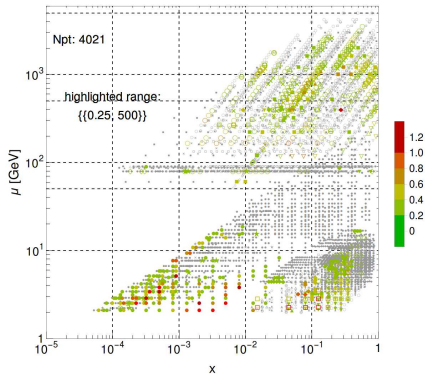


$$g(x, \mu)$$

|  $C_f$  | for  $g(x, \mu)$ , CT14HERA2NNLO



|  $S_f$  | for  $g(x, \mu)$ , CT14HERA2NNLO



# Hessian Updating

- Updated Chi-square function :

$$\Delta\chi^2(Z) = \Delta\chi_{old}^2(Z) + (X_i^E - X_i(Z))C_{ij}^{-1}(X_j^E - X_j(Z))$$

- Hessian approximation :

$$\Delta\chi_{old}^2(Z) = T^2 Z^2 \quad (T = \text{tolerance parameter})$$

$$X_i(Z) = X_i(0) + \Delta X_i \cdot Z \quad \text{with} \quad \Delta X_i^\alpha = \frac{1}{2}(X_i(+e)^\alpha - X_i(-e)^\alpha)$$

- Minimize to find new best fit:

$$Z_{new}^2 = (1 + M)^{-1} A \quad \text{with}$$

$$A^\alpha = \frac{1}{T^2}(X_i^E - X_i(0))C_{ij}^{-1}\Delta X_j^\alpha,$$

$$M^{\alpha\beta} = \frac{1}{T^2}\Delta X_i^\alpha C_{ij}^{-1}\Delta X_j^\beta$$



## Updated PDF set

- New best-fit PDF :

$$f_{new}^0 = f^0 + \Delta f \cdot Z$$

- New error PDFs :

$$f^{\pm(r)} = f_{new}^0 \pm \frac{1}{\sqrt{1 + \lambda^{(r)}}} \Delta f \cdot U^{(r)}$$

where  $\lambda^{(r)}$  and  $U^{(r)}$  are the eigenvalues and eigenvectors of matrix  $M$ .

- Direct update of other observables:

$$Y_{new}^0 = Y^0 + \Delta Y \cdot Z$$

$$|\Delta Y| = \Delta Y \cdot (1 + M)^{-1} \Delta Y$$

# ePump

## Error PDF Updating Method Package

FullICT14HERA2.in - Edited

```

+++ N(EV pairs)          N(Data Sets)  PDFtype(C/L/N)  Dyn_Tol?(Y/N)  Tol_squared
+++ ObservableFile      27              C                Y              100.0

```

	N(Observables)	Data?(Y/N)	Error_type	Weight
CT14HERA2ex/tabs/E160.If1363	1120	Y	1	1.0
CT14HERA2ex/tabs/E101.If1363	337	Y	1	1.0
CT14HERA2ex/tabs/E102.If1363	250	Y	1	1.0
CT14HERA2ex/tabs/E104.If1363	123	Y	1	1.0
CT14HERA2ex/tabs/E108.If1363	85	Y	1	1.0
CT14HERA2ex/tabs/E109.If1363	96	Y	1	1.0
CT14HERA2ex/tabs/E110.If1363	69	Y	1	1.0
CT14HERA2ex/tabs/E111.If1363	86	Y	1	1.0
CT14HERA2ex/tabs/E124.If1363	38	Y	1	1.0
CT14HERA2ex/tabs/E125.If1363	33	Y	1	1.0
CT14HERA2ex/tabs/E126.If1363	40	Y	1	1.0
CT14HERA2ex/tabs/E127.If1363	38	Y	1	1.0
CT14HERA2ex/tabs/E147.If1363	47	Y	1	1.0
CT14HERA2ex/tabs/E145.If1363	10	Y	1	1.0
CT14HERA2ex/tabs/E169.If1363	9	Y	1	1.0
CT14HERA2ex/tabs/E201.If1363	119	Y	1	1.0
CT14HERA2ex/tabs/E203.If1363	15	Y	1	1.0
CT14HERA2ex/tabs/E204.If1363	104	Y	1	1.0
CT14HERA2ex/tabs/E225.If1363	11	Y	1	1.0
CT14HERA2ex/tabs/E227.If1363	11	Y	1	1.0
CT14HERA2ex/tabs/E234.If1363	9	Y	1	1.0
CT14HERA2ex/tabs/E260.If1363	28	Y	1	1.0
CT14HERA2ex/tabs/E261.If1363	29	Y	1	1.0
CT14HERA2ex/tabs/E267.If1363	11	Y	1	1.0
CT14HERA2ex/tabs/E268.If1363	41	Y	1	1.0
CT14HERA2ex/tabs/E240.If1363	14	Y	1	1.0
CT14HERA2ex/tabs/E241.If1363	5	Y	1	1.0
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CT14HERA2ex/tabs/E514.If1363	110	Y	1	1.0
CT14HERA2ex/tabs/E535.If1363	90	Y	1	1.0
CT14HERA2ex/tabs/E538.If1363	133	Y	1	1.0

```

+++ PDFin          PDFout
PDFs/CT14HERA2ex/If1363  CT14HERA2ex/PDFtmp/If1363

```

“.in” file

# How to use ePump

```

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27
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CT14HERA2ex/tabs/E514.If1363
CT14HERA2ex/tabs/E535.If1363
CT14HERA2ex/tabs/E538.If1363

+++ PDFIn PDFOut
PDFs/CT14HERA2ex/If1363 CT14HERA2ex/PDFtmp/If1363

```

```

* DRS15 electron charge asymmetry from W decays from D0 Run-2 9.7 fb^-1 (1412.2062)
* Easy for electron Et>25 GeV and neutrino Et>25 GeV; sqrt(S)=1960 GeV, uncorrelated
* MG15 NLO & NNLO ratios K(W-)/K(W+) for CT14 NNLO. normalized to CT-package LO: + th
3 : NormErr, # of corr_err, Ecm, M_W, METran
# of corr_err, Data Column, StatErr Column, UncSys Column, corr_err Col
6 4 5 7 9
vMid pTEMIN pTEMAX Easy StatErr TotSys UncSys lob e01% e04% e05% e06
0.1 25.0 9.80E+02 0.021 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
0.3 25.0 9.80E+02 0.0523 0.0011 0.0014 0.0006 2 0.11 0.34 0.50 1.43
0.5 25.0 9.80E+02 0.0916 0.0011 0.0018 0.0007 2 0.13 0.27 0.38 1.15
0.7 25.0 9.80E+02 0.1197 0.0011 0.0025 0.0007 2 0.06 0.28 0.41 1.1
0.9 25.0 9.80E+02 0.1452 0.0012 0.0032 0.0008 2 0.08 0.25 0.37 1.18
1.1 25.0 9.80E+02 0.1559 0.0018 0.0041 0.0013 2 0.06 0.24 0.35 1.55
1.39 25.0 9.80E+02 0.1537 0.0067 0.0061 0.0018 2 0.02 0.25 0.38 2.67
1.7 25.0 9.80E+02 0.1100 0.0031 0.0049 0.0016 2 0.10 0.2 0.31 3.06
1.9 25.0 9.80E+02 0.0666 0.0120 0.0053 0.0027 2 0.51 0.08 0.15 6.32
2.1 25.0 9.80E+02 -0.0155 0.0053 0.0061 0.0046 2 2.39 0.26 0.45 21.48
2.3 25.0 9.80E+02 -0.0997 0.0071 0.0088 0.0077 2 0.19 0.02 0.05 3.41
2.54 25.0 9.80E+02 -0.1910 0.0041 0.0116 0.0103 2 0.11 0.15 0.25 2.22
2.92 25.0 9.80E+02 -0.3997 0.0090 0.0223 0.0210 2 0.01 0.2 0.33 0.87

```

".data" file

".in" file

# How to use ePump

```

+++ N(EV pairs)
27
+++ ObservableFile
CT14HERA2ex/tabs/E160.f1f1363
CT14HERA2ex/tabs/E101.f1f1363
CT14HERA2ex/tabs/E102.f1f1363
CT14HERA2ex/tabs/E104.f1f1363
CT14HERA2ex/tabs/E108.f1f1363
CT14HERA2ex/tabs/E109.f1f1363
CT14HERA2ex/tabs/E110.f1f1363
CT14HERA2ex/tabs/E111.f1f1363
CT14HERA2ex/tabs/E124.f1f1363
CT14HERA2ex/tabs/E125.f1f1363
CT14HERA2ex/tabs/E126.f1f1363
CT14HERA2ex/tabs/E127.f1f1363
CT14HERA2ex/tabs/E147.f1f1363
CT14HERA2ex/tabs/E145.f1f1363
CT14HERA2ex/tabs/E169.f1f1363
CT14HERA2ex/tabs/E201.f1f1363
CT14HERA2ex/tabs/E203.f1f1363
CT14HERA2ex/tabs/E204.f1f1363
CT14HERA2ex/tabs/E225.f1f1363
CT14HERA2ex/tabs/E227.f1f1363
CT14HERA2ex/tabs/E234.f1f1363
CT14HERA2ex/tabs/E260.f1f1363
CT14HERA2ex/tabs/E261.f1f1363
CT14HERA2ex/tabs/E267.f1f1363
CT14HERA2ex/tabs/E268.f1f1363
CT14HERA2ex/tabs/E240.f1f1363
CT14HERA2ex/tabs/E241.f1f1363
CT14HERA2ex/tabs/E281.f1f1363
CT14HERA2ex/tabs/E266.f1f1363
CT14HERA2ex/tabs/E504.f1f1363
CT14HERA2ex/tabs/E514.f1f1363
CT14HERA2ex/tabs/E535.f1f1363
CT14HERA2ex/tabs/E538.f1f1363

+++ PDFin PDFout
PDFs/CT14HERA2ex/f1f1363 CT14HERA2ex/PDFtmp/f1f1363

DRS15 electron charge asymmetry from W decays from D0 Run-2 9.7 fb^-1 (1412.2862)
Easy for electron Et>25 GeV and neutrino Et>25 GeV; sqrt(S)=1960 GeV, uncorrelated
MG15 NLO & NNLO ratios K(W-)/K(W+) for CT14 NNLO. normalized to CT-package LO: + th
3 : NormErr, # of corr_err, Ecn, M_W, METran
# of corr_err, Data Column, StatErr Column, UncSys Column, corr_err.Col
y.mid, pTMIN, pTMAX, Easy, StatErr, TotSys, UncSys, lob, e04, e05, e06
0.1 25.0 9.80E+02 0.021 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
0.3 25.0 9.80E+02 0.021 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
0.5 25.0 9.80E+02 0.021 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
0.7 25.0 9.80E+02 0.021 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
0.9 25.0 9.80E+02 0.021 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
0.25 25.0 9.80E+02 0.021 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
1.1 25.0 9.80E+02 0.021 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
1.39 25.0 9.80E+02 0.021 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
1.7 25.0 9.80E+02 0.021 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
1.9 25.0 9.80E+02 0.021 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
2.1 25.0 9.80E+02 0.021 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
2.3 25.0 9.80E+02 0.021 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
2.54 25.0 9.80E+02 0.021 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
2.92 25.0 9.80E+02 0.021 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33

DATA SET 281 : NORM Fac = 1.00000 ; # of pts = 13 ;
R^2, r(k) = 4.934 0.110 0.001 0.069 -2.206 0.
Y Rs Exp Th./Norm
Theory Column
5
Data : f1f1363.00.dta
1.000E-01 8.039E+01 1.960E+03 2.10000E-02 1.93596E-02
3.000E-01 8.039E+01 1.960E+03 5.23000E-02 5.53549E-02
5.000E-01 8.039E+01 1.960E+03 9.16000E-02 9.12121E-02
7.000E-01 8.039E+01 1.960E+03 1.19700E-01 1.22005E-01
9.000E-01 8.039E+01 1.960E+03 1.45200E-01 1.47812E-01
1.100E+00 8.039E+01 1.960E+03 1.55900E-01 1.62549E-01
1.390E+00 8.039E+01 1.960E+03 1.53700E-01 1.62790E-01
1.700E+00 8.039E+01 1.960E+03 1.10000E-01 1.26935E-01
1.900E+00 8.039E+01 1.960E+03 6.66000E-02 7.59711E-02
2.100E+00 8.039E+01 1.960E+03 -1.55000E-02 2.17415E-03
2.300E+00 8.039E+01 1.960E+03 -9.97000E-02 -9.28367E-02
2.540E+00 8.039E+01 1.960E+03 -1.91000E-01 -2.23084E-01
2.920E+00 8.039E+01 1.960E+03 -3.99700E-01 -4.31176E-01
Data : f1f1363.01.dta
1.000E-01 8.039E+01 1.960E+03 2.10000E-02 1.96980E-02
3.000E-01 8.039E+01 1.960E+03 5.23000E-02 5.63528E-02
5.000E-01 8.039E+01 1.960E+03 9.16000E-02 9.28178E-02
7.000E-01 8.039E+01 1.960E+03 1.19700E-01 1.24136E-01
9.000E-01 8.039E+01 1.960E+03 1.45200E-01 1.49556E-01
1.100E+00 8.039E+01 1.960E+03 1.55900E-01 1.65373E-01
1.390E+00 8.039E+01 1.960E+03 1.53700E-01 1.65749E-01
1.700E+00 8.039E+01 1.960E+03 1.10000E-01 1.29627E-01
1.900E+00 8.039E+01 1.960E+03 6.66000E-02 7.82553E-02
2.100E+00 8.039E+01 1.960E+03 -1.55000E-02 3.88933E-03
    
```

“.data” file

“.in” file

“.theory” file

# How to use ePump

```
+++ (NEV pairs)
27
+++ ObservedFile
CT14HERA2ex/tabs/E160.If1363
CT14HERA2ex/tabs/E101.If1363
CT14HERA2ex/tabs/E102.If1363
CT14HERA2ex/tabs/E104.If1363
CT14HERA2ex/tabs/E108.If1363
CT14HERA2ex/tabs/E109.If1363
CT14HERA2ex/tabs/E110.If1363
CT14HERA2ex/tabs/E111.If1363
CT14HERA2ex/tabs/E124.If1363
CT14HERA2ex/tabs/E125.If1363
CT14HERA2ex/tabs/E126.If1363
CT14HERA2ex/tabs/E127.If1363
CT14HERA2ex/tabs/E147.If1363
CT14HERA2ex/tabs/E145.If1363
CT14HERA2ex/tabs/E169.If1363
CT14HERA2ex/tabs/E201.If1363
CT14HERA2ex/tabs/E203.If1363
CT14HERA2ex/tabs/E204.If1363
CT14HERA2ex/tabs/E225.If1363
CT14HERA2ex/tabs/E227.If1363
CT14HERA2ex/tabs/E234.If1363
CT14HERA2ex/tabs/E260.If1363
CT14HERA2ex/tabs/E261.If1363
CT14HERA2ex/tabs/E267.If1363
CT14HERA2ex/tabs/E268.If1363
CT14HERA2ex/tabs/E240.If1363
CT14HERA2ex/tabs/E241.If1363
CT14HERA2ex/tabs/E281.If1363
CT14HERA2ex/tabs/E266.If1363
CT14HERA2ex/tabs/E504.If1363
CT14HERA2ex/tabs/E514.If1363
CT14HERA2ex/tabs/E535.If1363
CT14HERA2ex/tabs/E538.If1363
+++ PDFIn PDFOut
PDFs/CT14HERA2ex/If1363 CT14HERA2ex/PDF.tmp/If1363

DRS15 electron charge asymmetry from W decays from D0 Run-2 9.7 fb^-1 (1412.2862)
Easy for electron Et>25 GeV and neutrino Et>25 GeV; sqrt(S)=1960 GeV, uncorrelated
MG15 NLO & NNLO ratios K(W-)/K(W+) for CT14 NNLO. normalized to CT-geant LO: + th
3 : NormErr, # of corr_err, Ecn, M_W, METran
# of sqrt_err, Data Column, StatErr Column, UncSys Column, sqrt_err Col
6 4 5 7 9
ymid, pTEMIN pTEMAX Easy StatErr TotSys UncSys lob e04% e05% e06%
0.1 25.0 9.80E+02 0.021 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
0.3 25.0 9.80E+02 0.03 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
0.5 25.0 9.80E+02 0.04 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
0.7 25.0 9.80E+02 0.05 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
0.9 25.0 9.80E+02 0.06 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
1.1 25.0 9.80E+02 0.07 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
1.39 25.0 9.80E+02 0.1 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
1.7 25.0 9.80E+02 0.11 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
1.9 25.0 9.80E+02 0.12 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
2.1 25.0 9.80E+02 0.13 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
2.3 25.0 9.80E+02 0.14 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
2.54 25.0 9.80E+02 0.15 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33
2.92 25.0 9.80E+02 0.16 0.0012 0.0011 0.0006 2 0.29 0.14 0.19 1.33

DATA SET 201 : NORM Fac = 1.00000 ; # of pts = 13 ;
R^2, r(k) = 4.934 0.110 0.001 0.069 -2.206 0.
Y Q Rs Exp Th./Norm
Theory Column
Data : If1363.00.dta
1.000E-01 8.039E+01 1.960E+03 2.10000E-02 1.93596E-02
3.000E-01 8.039E+01 1.960E+03 5.23000E-02 5.53549E-02

./bin/UpdatePDFs CT14HERA2ex/FullCT14HERA2
1.700E+00 8.039E+01 1.960E+03 1.10000E-01 1.26935E-02
1.900E+00 8.039E+01 1.960E+03 6.66000E-02 7.59711E-03
2.100E+00 8.039E+01 1.960E+03 -1.55000E-02 2.17415E-03
2.300E+00 8.039E+01 1.960E+03 -9.97000E-02 -9.28367E-02
2.540E+00 8.039E+01 1.960E+03 -1.91000E-01 -2.23808E-01
2.920E+00 8.039E+01 1.960E+03 -3.99700E-01 -4.31176E-01
Data : If1363.01.dta
1.000E-01 8.039E+01 1.960E+03 2.10000E-02 1.96900E-02
3.000E-01 8.039E+01 1.960E+03 5.23000E-02 5.63528E-02
5.000E-01 8.039E+01 1.960E+03 9.16000E-02 9.28178E-02
7.000E-01 8.039E+01 1.960E+03 1.19700E-01 1.24136E-01
9.000E-01 8.039E+01 1.960E+03 1.45200E-01 1.49556E-01
1.100E+00 8.039E+01 1.960E+03 1.55900E-01 1.65373E-01
1.390E+00 8.039E+01 1.960E+03 1.53700E-01 1.65749E-01
1.700E+00 8.039E+01 1.960E+03 1.10000E-01 1.29627E-01
1.900E+00 8.039E+01 1.960E+03 6.66000E-02 7.82553E-02
2.100E+00 8.039E+01 1.960E+03 -1.55000E-02 3.88933E-03
```

“.data” file

```
./bin/UpdatePDFs CT14HERA2ex/FullCT14HERA2
```

Updated best-fit and Hessian Error PDFs

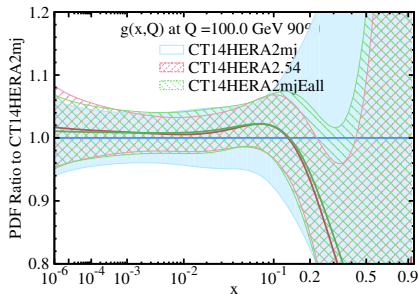
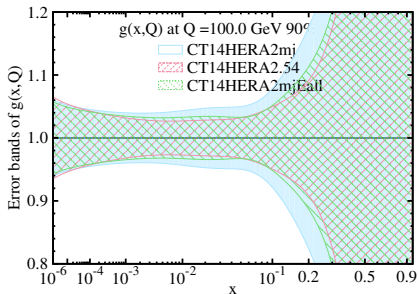
A few seconds later...

“.in” file

“.theory” file

# Test 1: CT14HERA2 minus Jets

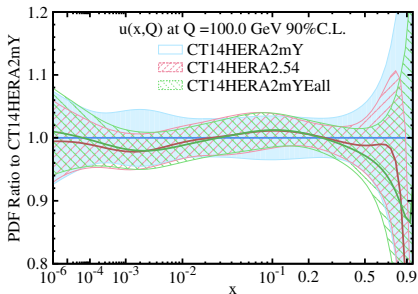
- Remove all CDF, D0, ATLAS 7TeV, CMS TeV jet data from CT14HERA2 and refit  $\rightarrow$  CT14HERA2mj.
- Add back the 4 data sets to CT14HERA2mj by ePump and compare with CT14HERA2.



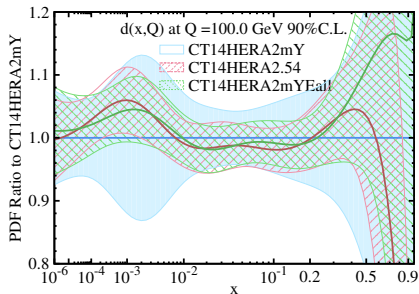
gluon - PDF

## Test 2: CT14HERA2 minus Drell-Yan

- Remove 19 Drell-Yan data sets (fixed target exp., Tevatron and LHC) from CT14HERA2 and refit  $\rightarrow$  CT14HERA2mY.
- Add back the 19 data sets to CT14HERA2mY by ePump and compare with CT14HERA2.



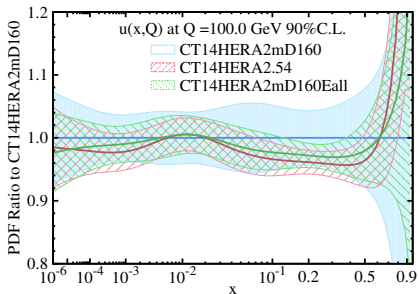
**u-PDF**



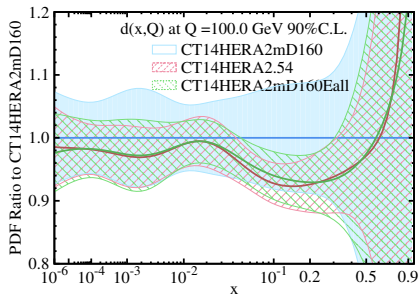
**d-PDF**

## Test 3: CT14HERA2 minus DIS

- Remove 14 DIS data sets (excluding HERA1+2) from CT14HERA2 and refit  $\rightarrow$  CT14HERA2mD160.
- Add back the 14 data sets to CT14HEA2mD160 by ePump and compare with CT14HERA2.



**u-PDF**

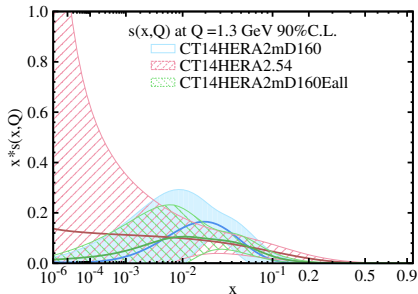


**d-PDF**



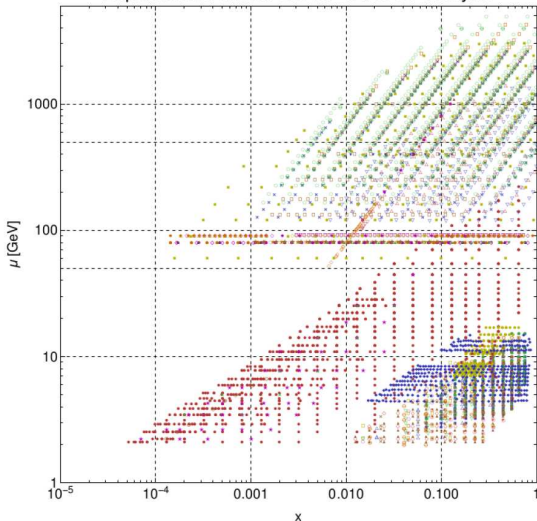
## Test 3: CT14HERA2 minus DIS (2)

- Almost all of constraints on s-PDF are from NuTeV and CCFR neutrino dimuon data.



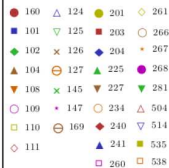
ePump work well in the  $x$  region constrained by data.

## Experimental data in CTEQ-TEA PDF analysis



### Experiments

#### In CT14HERA2



#### New

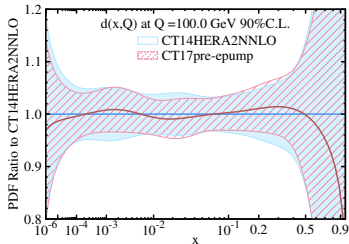
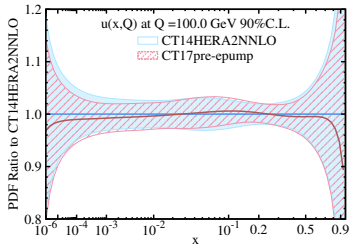
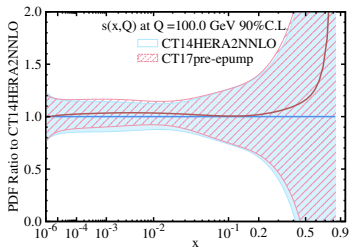
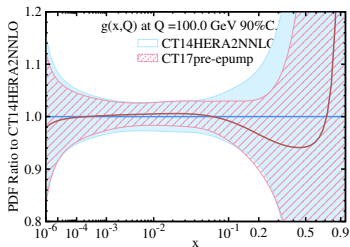


ID#	Experimental dataset	$N_{pt}$
245	LHCb 7 TeV Z/W muon forward- $\eta$ Xsec (1.0 fb $^{-1}$ )	33
246	LHCb 8 TeV Z electron forward- $\eta$ $d\sigma/dy_Z$ (2.0 fb $^{-1}$ )	17
247	ATLAS 7 TeV $d\sigma/dp_T^2$ (4.7 fb $^{-1}$ )	8
249	CMS 8 TeV W muon, Xsec, $A_\mu(\eta^0)$ (18.8 fb $^{-1}$ )	33
250	LHCb 8 TeV W/Z muon, Xsec, $A_\mu(\eta^0)$ (2.0 fb $^{-1}$ )	42
252	ATLAS 8 TeV Z ( $d^2\sigma/d y d m_{ll}$ ) (20.3 fb $^{-1}$ )	48
253	ATLAS 8 TeV ( $d^2\sigma/dp_T^2 dm_{ll}$ ) (20.3 fb $^{-1}$ )	45
542	CMS 7 TeV incl. jet, R=0.7, ( $d^2\sigma/dp_T^2 dy_j$ ) (5 fb $^{-1}$ )	158
544	ATLAS 7 TeV incl. jet, R=0.6, ( $d^2\sigma/dp_T^2 dy_j$ ) (4.5 fb $^{-1}$ )	140
545	CMS 8 TeV incl. jet, R=0.7, ( $d^2\sigma/dp_T^2 dy_j$ ) (19.7 fb $^{-1}$ )	185
565	ATLAS 8 TeV $t\bar{t} d\sigma/dp_T^2$ (20.3 fb $^{-1}$ )	8
566	ATLAS 8 TeV $t\bar{t} d\sigma/dy_{<1,\bar{1}>}$ (20.3 fb $^{-1}$ )	5
567	ATLAS 8 TeV $t\bar{t} d\sigma/dm_{t\bar{t}}$ (20.3 fb $^{-1}$ )	7
568	ATLAS 8 TeV $t\bar{t} d\sigma/dy_{t\bar{t}}$ (20.3 fb $^{-1}$ )	5

# Adding New Data with ePump

$$g(x, Q)$$

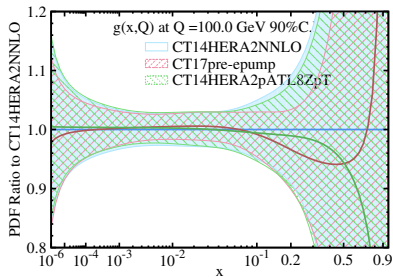
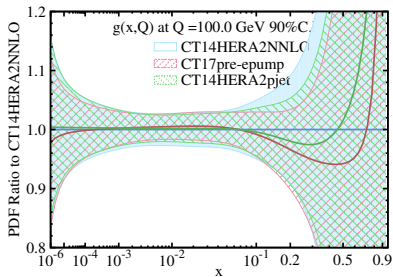
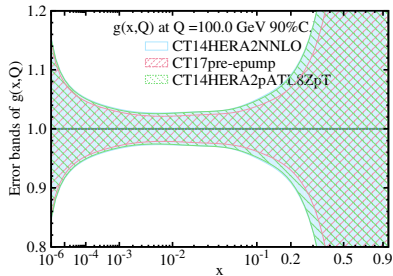
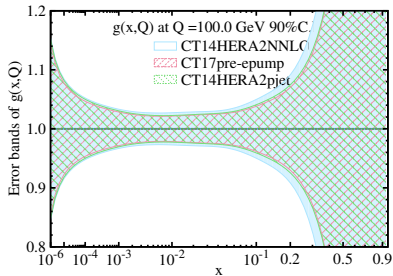
$$s(x, Q)$$



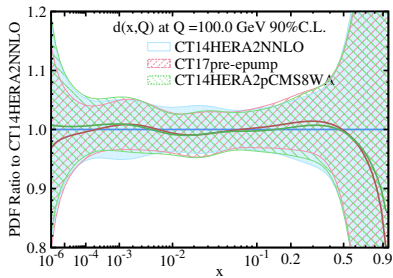
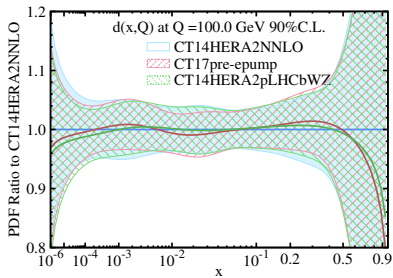
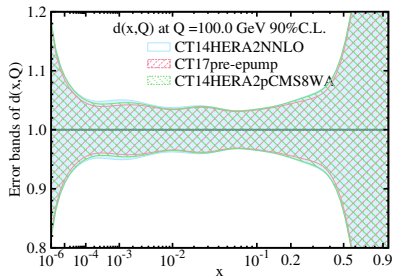
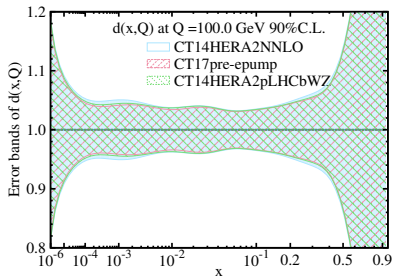
$$u(x, Q)$$

$$d(x, Q)$$

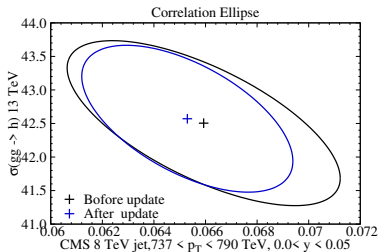
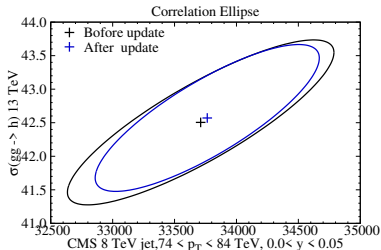
The update on gluon PDF is dominated by jet data.



# The update on d quark come from LHCb WZ production and CMS W-asym data.



# Effect of Updating on $\sigma(gg \rightarrow H)$



	$\sigma(gg \rightarrow h)$ 7 TeV
CT14HERA2	$14.60 \pm 0.44$
updated	$14.62 \pm 0.40$
	$\sigma(gg \rightarrow h)$ 8 TeV
CT14HERA2	$18.60 \pm 0.55$
updated	$18.64 \pm 0.49$
	$\sigma(gg \rightarrow h)$ 13 TeV
CT14HERA2	$42.56 \pm 1.23$
updated	$42.69 \pm 1.07$
	$\sigma(gg \rightarrow h)$ 14 TeV
CT14HERA2	$47.99 \pm 1.39$
updated	$48.14 \pm 1.20$

# Summary

- The **Sensitivity**  $S_f(x_i, \mu_i)$  provide an easy way to visualize the potential impact to PDF in  $x - Q$  plane (arxiv:1803.02777).
- The **PDFsense**, which can work out the sensitivity, is public available at  
<http://metapdf.hepforge.org/PDFSense/>
- **UpdatePDFs** function in **ePump** package is a fast and efficient method to estimate the effect of new data on the a current set of best-fit and Hessian error PDFs (arxiv:1806.07950).
- Extensively cross-checked against CT14 global fits
- ePump code is public available at  
<http://hep.pa.msu.edu/epump/>