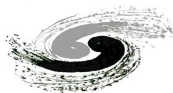


Some Compelling Aspects of Neutrino Physics

Newton Nath



中國科學院高能物理研究所
Institute of High Energy Physics
Chinese Academy of Sciences

Theoretical Physics Division, IHEP,
Beijing - 100049, China

March - 27, 2018

Personal Details

- ▶ Obtained my **Bachelor of Science** (B.Sc.) degree in Physics (Honours) with 70.75% marks from Assam University, Silchar, Assam, India during 2007 - 2010.
- ▶ Obtained my **Master of Science** (M.Sc.) with a specialization in Particle Physics with 9.51 CGPA from University of Hyderabad, Hyderabad, India during 2010 - 2012.
- ▶ Completed my **Doctor of Philosophy** (Ph.D.) degree in *Neutrino Physics* under the supervision of Prof. Srubabati Goswami from Physical Research Laboratory, Ahmedabad, India during 2012 - 2017.
- ▶ Currently (2017 -) working as a **Post-Doctoral Fellow** (PDF) in *Neutrino Physics* with Prof. Zhi-zhong Xing at Institute of High Energy Physics, Beijing, China.

Publication List

- ▶ **Newton Nath**, Zhi-zhong Xing, Jue Zhang : $\mu - \tau$ Reflection Symmetry Embedded in Minimal Seesaw, **Eur. Phys. J. C** (2018), arXiv:1801.09931 [hep-ph].
- ▶ K. N. Deepthi, Srubabati Goswami, **Newton Nath** : Can nonstandard interactions jeopardize the hierarchy sensitivity of DUNE?,
Phys. Rev. D **96**, 075023 (2017), arXiv:1612.00784 [hep-ph].
- ▶ **Newton Nath**, Monojit Ghosh, Srubabati Goswami, Shivani Gupta : Phenomenological study of extended seesaw model for light sterile neutrino,
JHEP03(2017)075, arXiv:1610.09090 [hep-ph].
- ▶ Anjan S. Joshipura, **Newton Nath** : Neutrino masses and mixing in A_5 with flavour antisymmetry, **Phys.Rev. D****94**, 036008 (2016), arXiv:1606.01697[hep-ph].
- ▶ **Newton Nath**, Monojit Ghosh, Shivani Gupta : Light Sterile Neutrino Mass Matrix with Texture Zero and a Vanishing Mass,
Int. J. Mod. Phys. A **31**, 1650132 (2016), arXiv:1512.00635[hep-ph].
- ▶ **Newton Nath**, Monojit Ghosh, Srubabati Goswami : The Physics of antineutrinos in DUNE and resolution of octant degeneracy,
Nucl.Phys. B**913** (2016) 381-404, arXiv:1511.07496[hep-ph].
- ▶ Monojit Ghosh, Pomita Ghoshal, Srubabati Goswami, **Newton Nath**, Sushant K. Raut : A new look to the degeneracies in the neutrino oscillation parameters and their resolution by T2K, $NO\nu A$ and ICAL,
Phys. Rev. D**93**, 013013 (2016) , arXiv :1504.06283[hep-ph].

Conference Proceedings¹

- ▶ N.D. Kuchibhatla[†], S. Goswami, **N. Nath** : Effect of non-standard neutrino interactions on the sensitivities of DUNE, **NuFact2017**, **PoS(NuFact2017)162**.
- ▶ **Newton Nath**[†], Srubabati Goswami and K. N. Deepthi: Generalized degeneracies and their resolution in neutrino oscillation experiments, **XXII DAE-BRNS SYMPOSIUM 2016**, **Springer Proceedings in Physics 203**, arXiv:1703.00245 [hep-ph].
- ▶ **Newton Nath**[†], Monojit Ghosh and Srubabati Goswami: What antineutrinos can tell about octant and δ_{CP} in DUNE?, **ICHEP2016**, **PoS(ICHEP2016)979**, arXiv:1611.03635 [hep-ph].
- ▶ **Newton Nath**[†], Monojit Ghosh and Srubabati Goswami: The Physics of antineutrinos in DUNE and resolution of octant degeneracy, **Neutrino2016**, **J. Phys.: Conf. Ser. 888 012261**, arXiv:1610.01183 [hep-ex].

¹'†' Corresponding Author

Neutrino oscillations

- ▶ Neutrino oscillation \Rightarrow Transition from one flavor to another

time=0;

ν_e ;

\longrightarrow

time= t ;

distance= L ;

\longrightarrow

ν_e, ν_μ, ν_τ ;

The 3-flavor ν -oscillation probability can be written as:

$$P_{\alpha\beta} = \delta_{\alpha\beta} - 4 \sum_{i < j} \text{Re}[U_{\alpha i}^* U_{\beta j}^* U_{\beta i} U_{\alpha j}] \sin^2 \frac{\Delta_{ij} L}{4E} + 2 \sum_{i < j} \text{Im}[U_{\alpha i}^* U_{\beta j}^* U_{\beta i} U_{\alpha j}] \sin 2 \frac{\Delta_{ij} L}{4E} \quad (1)$$

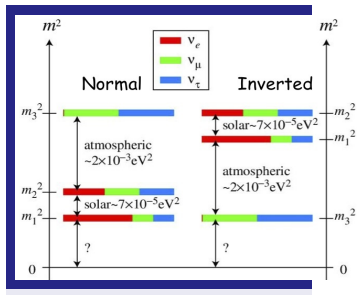
where, $\Delta_{ij} = m_i^2 - m_j^2$

Parameters of neutrino oscillation:

- ▶ Elements of U: 3-mixing \angle 's ($\theta_{12}, \theta_{23}, \theta_{13}$) and 1-Dirac phase (δ_{CP})
- ▶ 2-(mass)² differences appears in $P_{\alpha\beta}$
 $\Delta_{21} = m_2^2 - m_1^2, \Delta_{31} = |m_3^2 - m_1^2|$

Unknowns:

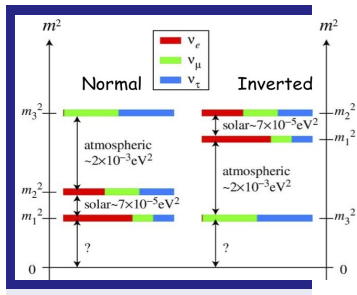
- ▶ Various ν -oscillations experiments have measured these parameters.
- ▶ Unknowns in Neutrino Physics.



- ▶ The sign of Δm_{31}^2 i.e.
 $\Delta m_{31}^2 > 0 \Rightarrow$ Normal Hierarchy (NH)
or
 $\Delta m_{31}^2 < 0 \Rightarrow$ Inverted Hierarchy (IH).

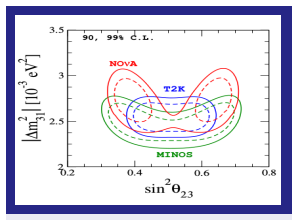
Unknowns:

- ▶ Various ν -oscillations experiments have measured these parameters.
- ▶ Unknowns in Neutrino Physics.



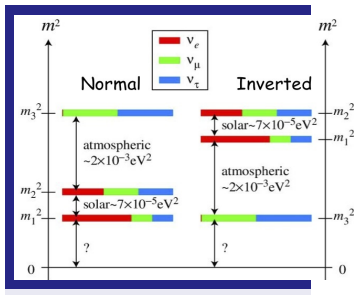
- ▶ The sign of Δm_{31}^2 i.e.
 $\Delta m_{31}^2 > 0 \Rightarrow$ Normal Hierarchy (NH)
or
 $\Delta m_{31}^2 < 0 \Rightarrow$ Inverted Hierarchy (IH).

- ▶ The octant of θ_{23} i.e.
 $\theta_{23} > 45^\circ \Rightarrow$ Higher Octant (HO) or
 $\theta_{23} < 45^\circ \Rightarrow$ Lower Octant (LO).



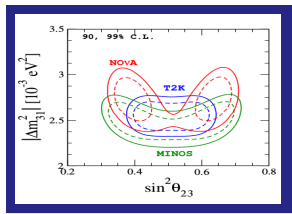
Unknowns:

- ▶ Various ν -oscillations experiments have measured these parameters.
- ▶ Unknowns in Neutrino Physics.



- ▶ The sign of Δm_{31}^2 i.e.
 $\Delta m_{31}^2 > 0 \Rightarrow$ Normal Hierarchy (NH)
 or
 $\Delta m_{31}^2 < 0 \Rightarrow$ Inverted Hierarchy (IH).

- ▶ The octant of θ_{23} i.e.
 $\theta_{23} > 45^\circ \Rightarrow$ Higher Octant (HO) or
 $\theta_{23} < 45^\circ \Rightarrow$ Lower Octant (LO).



- ▶ The Dirac CP phase δ_{CP} , where $\delta_{CP} \neq 0^\circ, \pm 180^\circ \Rightarrow$ CP violation. There already exists hints that CP phase may be nearly maximal. [Salas et al., arXiv:1708.01186]

Current status of the oscillation parameters²

Parameter	best fit	3σ range
$\Delta m_{21}^2 [10^{-5} eV^2]$	7.56	7.05–8.14
$ \Delta m_{31}^2 [10^{-3} eV^2]$ (NH)	2.55	2.43–2.67
$ \Delta m_{31}^2 [10^{-3} eV^2]$ (IH)	2.49	2.37–2.61
$\theta_{12} (deg)$	34.5	31.5–38
$\theta_{23} (deg)$ (NH)	41.0	38.3–52.8
$\theta_{23} (deg)$ (IH)	50.5	38.5–53.0
$\theta_{13} (deg)$ (NH)	8.44	7.9–8.9
$\theta_{13} (deg)$ (IH)	8.41	7.9–8.9
δ/π (NH)	1.40	0.0–2.0
δ/π (IH)	1.44	0.0–2.0

- ▶ Recent T2K result favors : NH, $\delta_{CP} = -\pi/2$, $\theta_{23} \sim 45^\circ$.
[PRL, 118(2017), 151801]
- ▶ NO ν A favors : NH-HO with 0.2σ and disfavors : maximal θ_{23} with 0.8σ and IH- $\delta_{CP} = \pi/2$ with more than 3σ . [NO ν A Collaboration, 2018]

²Salas et.al., arXiv:1708.01186

Definition of Degeneracy

Problem: Existence of parameter degeneracy

Degeneracy: Two different sets of neutrino oscillation parameters giving rise to same oscillation probability i.e.,

$$P_{\alpha\beta}(x) = P_{\alpha\beta}(y)$$

x, y : different sets of oscillation parameters i.e.,
 $x = x(\theta_{ij}, \delta_{CP}, \Delta_{ij}), y = y(\theta'_{ij}, \delta'_{CP}, \Delta'_{ij})$

Conclusion:

Extraction of x will be confused with extraction of y

Probability Channels

The relevant probability channels:

- ▶ Appearance Channel:

$$P_{\mu e} = 4s_{13}^2 s_{23}^2 \frac{\sin^2(A-1)\Delta}{(A-1)^2} + \alpha^2 \cos^2 \theta_{23} \sin^2 2\theta_{12} \frac{\sin^2 A\Delta}{A^2} \quad (2)$$

$$+ \alpha s_{13} \sin 2\theta_{12} \sin 2\theta_{23} \cos(\Delta + \delta_{cp}) \frac{\sin(A-1)\Delta}{(A-1)} \frac{\sin A\Delta}{A} \quad (3)$$

where, $s_{ij} = \sin \theta_{ij}$, $i < j = 1, 2, 3$

- ▶ Disappearance Channel:

$$P_{\mu\mu} = 1 - \sin^2 2\theta_{23} \sin^2 \Delta + \mathcal{O}(\alpha, s_{13})$$

- ▶ $\Delta = \frac{\Delta_{31}L}{4E}$ and $\alpha = \Delta_{21}/\Delta_{31}$ are +ve(-ve) for NH (IH)
 $A = 2EV/\Delta_{31} = +ve (-ve)$ for $\nu(\bar{\nu})$, V is matter potential.

Generalized Degeneracy

- ▶ For unknown hierarchy, octant and δ_{CP} :

$$P_{\mu e}(\theta_{23}, \Delta, \delta_{CP}) = P_{\mu e}(\theta'_{23}, -\Delta', \delta'_{CP})$$

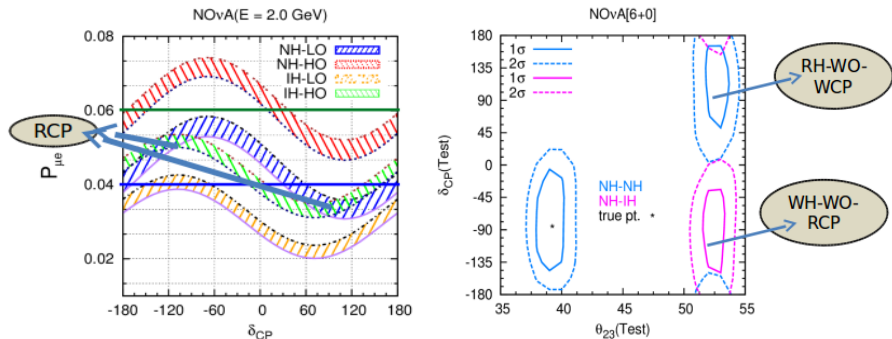
⇒ generalized (hierarchy- θ_{23} - δ_{CP}) degeneracy.³

- ▶ **Eight possibilities:**

Solution with (right δ_{CP})	Solution with (wrong δ_{CP})
1) RH-RO-R δ_{CP}	5) WH-WO-W δ_{CP}
2) RH-WO-R δ_{CP}	6) RH-RO-W δ_{CP}
3) WH-RO-R δ_{CP}	7) RH-WO-W δ_{CP}
4) WH-WO-R δ_{CP}	8) WH-RO-W δ_{CP}

here, R=Right, W=Wrong

Degeneracies at $\text{NO}\nu\text{A}$ are ⁴,



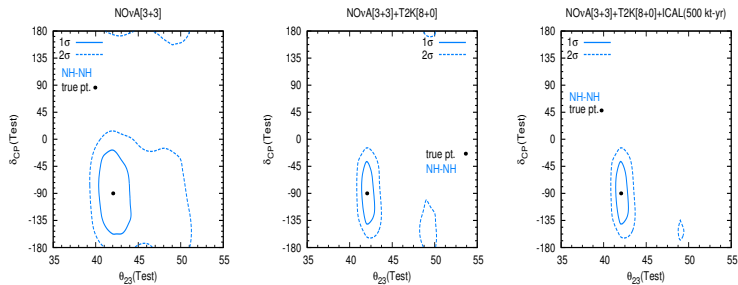
At Probability

- ▶ Overlapping region around $-120^\circ, +90^\circ \Rightarrow \text{WH-WO-R}\delta_{CP}$.
- ▶ Same probability value for NH-LO and IH-LO $\Rightarrow \text{WH-RO-W}\delta_{CP}$.
- ▶ Same probability value for NH-HO and NH-LO $\Rightarrow \text{RH-WO-W}\delta_{CP}$.
- ▶ For NH-HO at $(48^\circ, -180^\circ)$ and $(48^\circ, 45^\circ) \Rightarrow \text{RH-RO-W}\delta_{CP}$.
- ▶ For NH-LO $(39^\circ, -180^\circ)$ and IH-HO $(51^\circ, 0^\circ) \Rightarrow \text{WH-WO-W}\delta_{CP}$.

⁴Ghosh, Ghoshal, Goswami, NN and Raut, PRD93,013013 (2016)

Resolution of various degeneracies

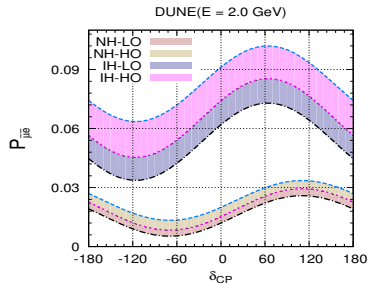
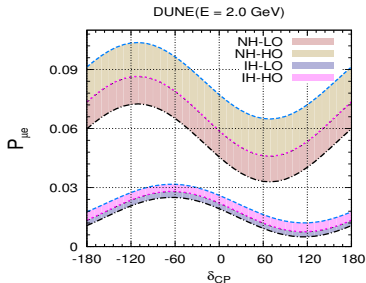
- ▶ Resolution of degeneracies with $\text{NO}\nu\text{A}$, T2K, ICAL ,



- ▶ Addition of $\bar{\nu}$ removes WO-WH solution.
- ▶ Addition of more data provides better precision on θ_{23} .

[Ghosh, Ghoshal, Goswami, NN and Raut, PRD93,013013 (2016)]

► Probability level study at DUNE⁵ :



- No overlapping between NH and IH bands \Rightarrow no hierarchy degeneracy.
- Same probability at different δ_{CP} \Rightarrow degeneracy occurring for $W\delta_{CP}$.

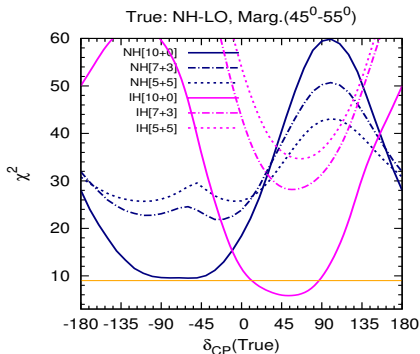
Octant Degeneracy	ν	$\bar{\nu}$
LHP, LO	degenerate with UHP, HO	no degeneracy
UHP, LO	no degeneracy	degenerate with LHP,HO
LHP, HO	no degeneracy	degenerate with UHP, LO
UHP, HO	degenerate with LHP,LO	no degeneracy

Table: The octant degenerate parameter space for neutrinos and antineutrinos.

- **Note:** ($\nu + \bar{\nu}$) runs are help full to resolve octant- δ_{CP} degeneracy.

Octant discovery χ^2 :

- ▶ NH-LO ($\theta_{23}^{\text{true}} = 39^\circ$):



$$\mapsto \chi^2 = \left(\frac{\theta_{23}^{\text{true}} - \theta_{23}^{\text{test}}}{\sigma(\theta_{23}^{\text{true}})} \right)^2$$

- ▶ Known hierarchy $\Rightarrow 3\sigma$ octant discovery χ^2 for all values of δ_{CP} for DUNE in ν mode.
- ▶ Unknown hierarchy \Rightarrow octant degeneracy at 3σ in UHP but not at 2σ for all δ_{CP} for [10+0].
- ▶ (7+3) runs \Rightarrow octant discovery at more than 4σ for any value of δ_{CP} .

Impact of New Physics

- ▶ DUNE(L=1300 km) has large matter effect \Rightarrow able to resolve hierarchy (if there is no new-physics).

[Acciarri (Fermilab) et al. 1512.06148]

- ▶ "**New-physics**" effect at DUNE can ruin mass hierarchy determination.

Liao, Marfatia, Whisnant 1601.00927, Coloma, Schwetz 1604.05772, Masud, Mehta 1606.05662, Dutta, Ghoshal, Roy 1609.07094

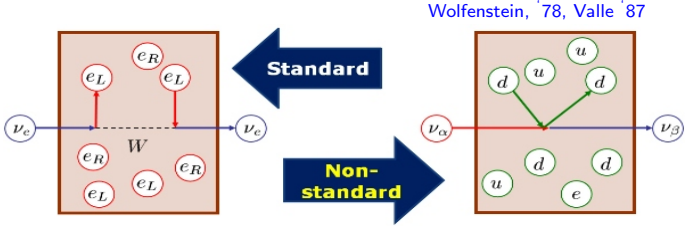
- ▶ Various possible **new-physics** are non-standard interactions (NSIs), non-unitarity, sterile neutrino, large extra-dimension, etc...

Blennow, Coloma, Martinez, Garcia, Pavon 1609.08637, Tang, Zhang, Li, 1708.04909, Berryman, Gouvea, Kelly, Peres, Tabrizi, 1603.00018.

Non-standard interactions

- ▶ Dimension 6, exotic couplings involving ν 's can affect neutrinos propagation through matter,

$$\mathcal{L}_{\text{NSI}}^{\text{NC}} = (\bar{\nu}_\alpha \gamma^\rho P_L \nu_\beta) (\bar{f} \gamma_\rho P_C f) 2\sqrt{2} G_F \epsilon_{\alpha\beta}^{fC} + \text{h.c.} \quad (4)$$



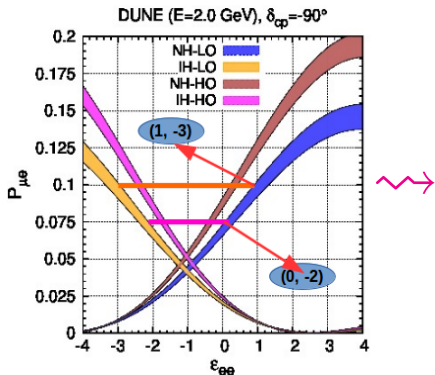
where,

$$\epsilon_{\alpha\beta} e^{i\phi_{\alpha\beta}} = A \begin{pmatrix} 1 + \epsilon_{ee} & \epsilon_{e\mu} e^{i\phi_{e\mu}} & \epsilon_{e\tau} e^{i\phi_{e\tau}} \\ \epsilon_{e\mu} e^{-i\phi_{e\mu}} & \epsilon_{\mu\mu} & \epsilon_{\mu\tau} e^{i\phi_{\mu\tau}} \\ \epsilon_{e\tau} e^{-i\phi_{e\tau}} & \epsilon_{\mu\tau} e^{-i\phi_{\mu\tau}} & \epsilon_{\tau\tau} \end{pmatrix}. \quad (5)$$

- ▶ Model-independent bounds, $|\epsilon_{ee}| < 4.2, |\epsilon_{e\tau}| < 3.0$

Probability level

- ▶ Considering only ϵ_{ee} (for $\delta_{CP} = -90^\circ$),



- ▶ $\epsilon_{ee} \rightarrow -\epsilon_{ee} - 2 \Rightarrow$ WH-RO-RCP.
- ▶ For $\epsilon_{ee} > 2 \Rightarrow$ no WH-RO-RCP solution.

- ▶ $\epsilon_{ee} = -1 \Rightarrow$ "region of confusion" since same ϵ_{ee} for both NH & IH.

[Deepthi, Goswami, NN PRD, 96, 075023 (2017)]
see also, Liao, Marfatia Whisnant, PRD 93, 093016 (2016), Coloma, Schwetz, PRD 94, 055005 (2016)

- ▶ We extend similar study on the determination of δ_{CP} ,

[Deepthi, Goswami, NN arXiv:1711.04840 [hep-ph]]

Existence of light sterile neutrino

- ▶ Understanding the masses and mixings of one-zero textures in $3 + 1$ scenario

[NN, Ghosh and Gupta, IJMPA 31, 1650132 (2016)]

- ▶ Phenomenological study of extended seesaw model for light sterile neutrino

[NN, Ghosh, Goswami and Gupta, JHEP 1703 (2017) 075]

Flavor Symmetry

Theoretical framework

- ▶ One should have theoretical understanding also to understand this beautiful mixing pattern.
- ▶ Flavor symmetries provide concrete framework to do this.
- ▶ We assume Majorana neutrino mass matrix M_ν obey flavor anti-symmetry instead of flavor symmetry ⁶,

$$S_\nu^T M_\nu S_\nu = -M_\nu \quad (6)$$

⁶ Grimus, Kaneko, Lavoura, Sawanaka and Tanimoto, JHEP 01 (2006) 110, Joshipura, JHEP 1511 (2015) 186.

A_5 group

- ▶ Alternating group A_5 is the even permutations of 5 distinct objects.
- ▶ It has 60 different elements and 5 conjugacy classes:

$$1C_1, 15C_2, 20C_3, 12C_5^1 \text{ and } 12C_5^2. \quad (7)$$

- ▶ It has 5-irreducible representations: **1, 3, 3', 4 and 5**.
- ▶ All representations except singlet are **faithful**.
- ▶ The Abelian subgroups are \mathbf{Z}_2 (15 elements), \mathbf{Z}_3 (20 elements) and \mathbf{Z}_5 (24 elements).
- ▶ 15 elements of \mathbf{Z}_2 contain 5 distinct $\mathbf{Z}_2 \times \mathbf{Z}_2$ subgroups.
- ▶ Generators in 3-dimensional representations are,

$$H = \frac{1}{2} \begin{bmatrix} -1 & \mu_- & \mu_+ \\ \mu_- & \mu_+ & -1 \\ \mu_+ & -1 & \mu_- \end{bmatrix}; \quad E = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{bmatrix}; \quad F = \begin{bmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{bmatrix}$$

here $\mu_{\pm} = (-1 \pm \sqrt{5})/2$

Case I: $S_\nu = Z_2$ and $T_l = Z_5$

$$\theta \neq 0, \beta = 0$$

$$\theta \neq 0, \beta \neq 0$$

$$|U_{PMNS}| = \begin{bmatrix} 0.2181 & 0.9616 & 0.1644 \\ 0.6901 & 0.1940 & 0.6972 \\ 0.6901 & 0.1940 & 0.6972 \end{bmatrix}; \begin{bmatrix} 0.2196 & 0.9603 & 0.1716 \\ 0.7118 & 0.1883 & 0.6766 \\ 0.6671 & 0.2055 & 0.7160 \end{bmatrix}$$

[Joshi and NN, PRD 94 (2016) 036008]

- ▶ L.H.S. $|U_{PMNS}| \Rightarrow |U_{\mu 3}| = |U_{\tau 3}| \Rightarrow$ maximal θ_{23} and correct θ_{13} but not correct θ_{12} .
- ▶ R.H.S $|U_{PMNS}| \Rightarrow$ non-maximal θ_{23} and δ_{CP} with correct θ_{13} .
- ▶ Both of these are for a massless ν and a pair of degenerate ν s.
- ▶ A small perturbation in the ν -mass matrix M_ν leads to correct mass ratio and mixing \angle 's
- ▶ Similar results also obtain for $T_l = Z_3$

$\mu - \tau$ Reflection Symmetry⁷

- ▶ This symmetry predicts,

$$\theta_{23} = \pi/4, \delta = \pm\pi/2, \rho, \sigma = 0, \pi/2. \quad (8)$$

- ▶ Demanding the left and right-handed neutrino fields transform under $\mu - \tau$ reflection symmetry we get,

$$M_D = \begin{pmatrix} b & b^* \\ c & d \\ d^* & c^* \end{pmatrix}; \quad M_R = \begin{pmatrix} m_{22} & m_{23} \\ m_{23} & m_{22}^* \end{pmatrix} \quad (9)$$

[NN, Xing, Zhang, EPJC (2018), arXiv:1801.09931]

- ▶ In type - I seesaw formalism, this leads us to,

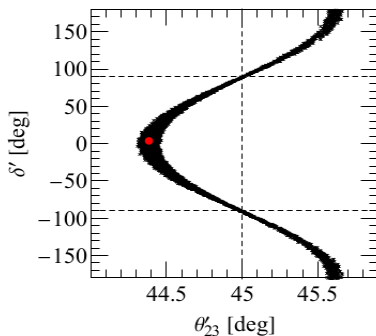
$$-M_\nu = M_D M_R^{-1} M_D^T = \begin{pmatrix} A & B & B^* \\ B & C & D \\ B^* & D & C^* \end{pmatrix}, \quad (10)$$

⁷Harrison and Scott, PLB547, 219 (2002)

Cont...

- ▶ Breaking of $\mu - \tau$ reflection symmetry,

$$M_D = \begin{pmatrix} b & b^*(1 + \epsilon) \\ c & d \\ d^* & c^* \end{pmatrix} \quad (11)$$



[NN, Xing, Zhang, EPJC (2018), arXiv:1801.09931]

Ongoing works :

- ▶ Non-standard neutrino Interaction in modified ν 2HDM, [with U.K. Dey, S. Sadhukhan]
- ▶ Testing of 'partial $\mu - \tau$ reflection' symmetry and its predictions with respect to DUNE, [with S. Goswami, A. Joshipura.]
- ▶ $\mu - \tau$ reflection symmetry and leptogenesis in littlest seesaw formalism, [with S. Zhou.]

Future plans:

- ▶ Implication of Gauge $L_\mu - L_\tau$ symmetry considering type-II seesaw formalism, [with S. Zhou.]
- ▶ Neutrino mixing patterns and leptogenesis considering A_4 -flavor model, [with B. Karmakar.].
- ▶ Study of the effective Majorana neutrino mass in the $0\nu\beta\beta$ decay, [with Yu-feng Li.].
- ▶ Correlations of neutrino oscillation parameters from various flavor models and their testability at neutrino oscillation experiments.
- ▶ Impact of new physics on the determination of neutrino oscillation parameters in neutrino oscillation experiments.

Summary and Conclusions

- ▶ We have introduced generalized “*hierarchy*- θ_{23} - δ_{CP} ” degeneracy to observe different degenerate solutions.
- ▶ We discuss the combine effect of NOVA+T2K+ICAL@INO for the resolutions of various degeneracies.
- ▶ For DUNE, we emphasize on the importance of $\bar{\nu}$ run in resolving octant ambiguity and increasing CP sensitivity.
- ▶ We discuss the impact of digonal NSI on the determination of neutrino mass hierarchy considering DUNE.
- ▶ We introduce, $(\epsilon_{ee}, \delta_{CP}) \longrightarrow (-\epsilon_{ee} - 2, \delta'_{CP})$ generalized degeneracy in presence of NSI.

Cont...

- ▶ We also focus on the consequences of assuming Majorana neutrino mass matrix display flavor anti-symmetry property.
- ▶ In this respect, we have studied A_5 group and its various Abelian subgroups which lead to phenomenologically allowed neutrino mixing matrix.
- ▶ Demanding left as well as right-handed neutrino fields transform under $\mu - \tau$ reflection symmetry, we obtain low energy neutrino mass matrix which obey this symmetry.
- ▶ To investigate the low energy neutrino phenomenology, we study the breaking of such symmetry.

Cont...

- ▶ We also focus on the consequences of assuming Majorana neutrino mass matrix display flavor anti-symmetry property.
- ▶ In this respect, we have studied A_5 group and its various Abelian subgroups which lead to phenomenologically allowed neutrino mixing matrix.
- ▶ Demanding left as well as right-handed neutrino fields transform under $\mu - \tau$ reflection symmetry, we obtain low energy neutrino mass matrix which obey this symmetry.
- ▶ To investigate the low energy neutrino phenomenology, we study the breaking of such symmetry.

Thank you