

Cross checks for BAM116

$$e^+e^- \rightarrow J/\psi \rightarrow (\Lambda \rightarrow p\pi^-)(\bar{\Lambda} \rightarrow \bar{p}\pi^+)$$

Andrzej Kupsc

Apply Jiao Jiao efficiency correction

Tools for checking efficiencies in $e^+e^- \rightarrow J/\psi \rightarrow \Lambda \bar{\Lambda}$

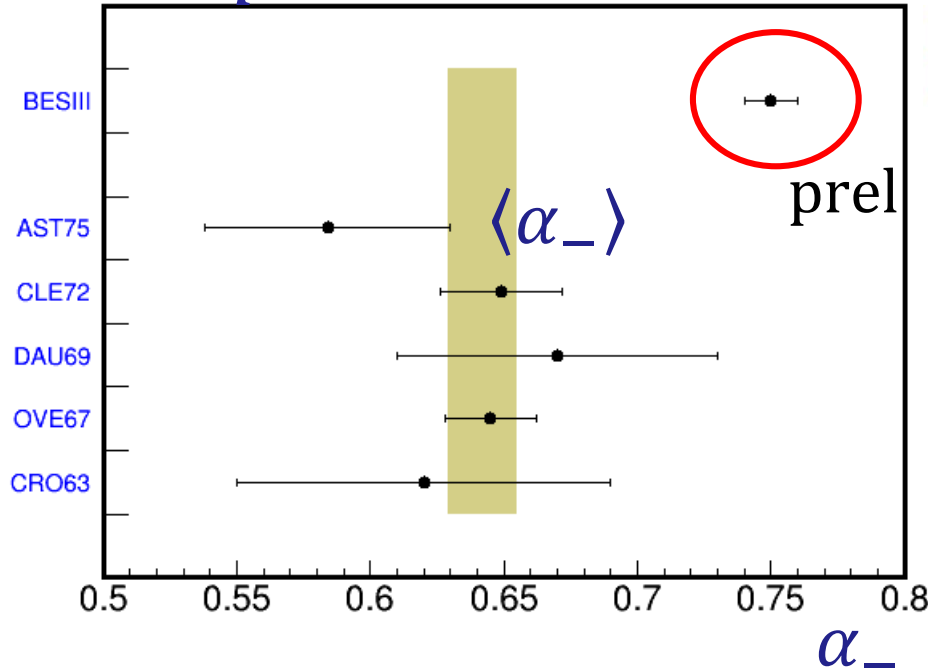
⇒ Systematical uncertainties are correct

⇒ Room for improvement with larger statistics

...

Observation of the spin polarization of Λ hyperons in the $J/\psi \rightarrow \Lambda \bar{\Lambda}$ decay

$\Lambda \rightarrow p\pi^-: \alpha_-$



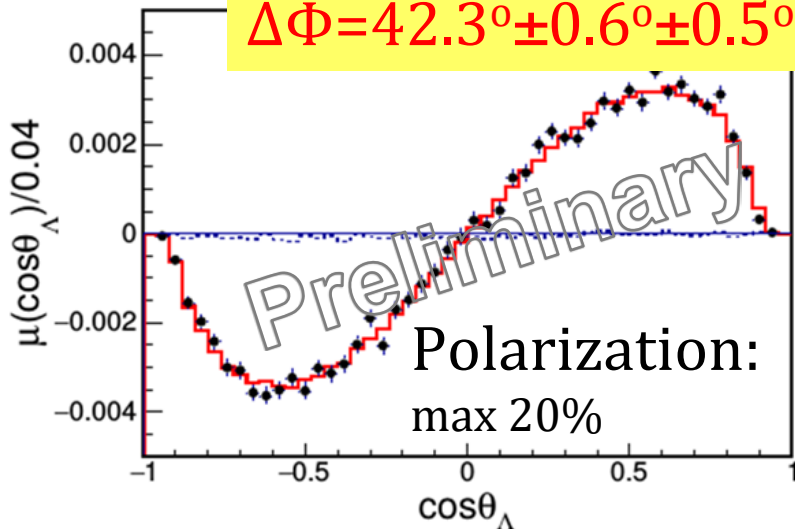
BESIII

17% larger than PDG avg
> 5 σ difference

CP test

$$A_{CP} = \frac{\alpha_- + \alpha_+}{\alpha_- - \alpha_+}$$

$\Delta\Phi = 42.3^\circ \pm 0.6^\circ \pm 0.5^\circ$



$A_{CP} = -0.006 \pm 0.012 \pm 0.007$

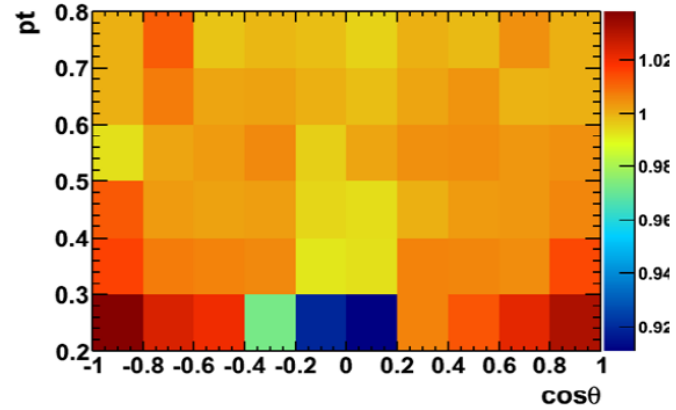
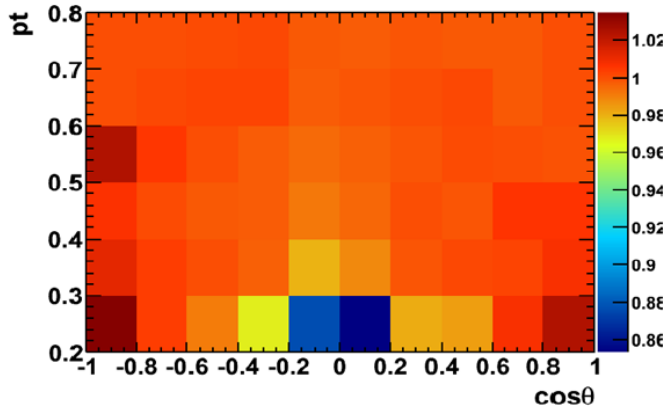
prel

$A_{CP} = 0.013 \pm 0.021$

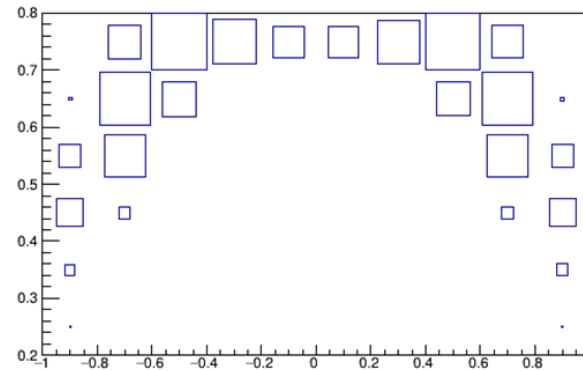
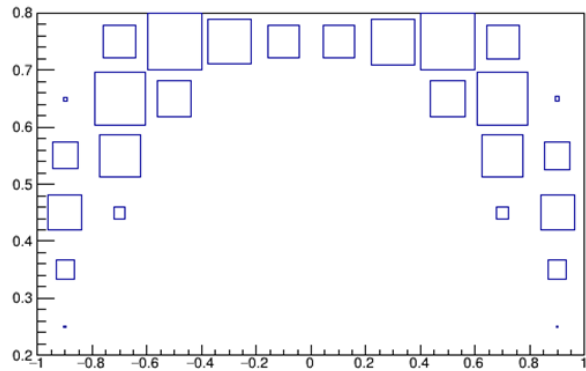
PS185 PRC54(96)1877

CKM $A_{CP} \sim 10^{-4}$

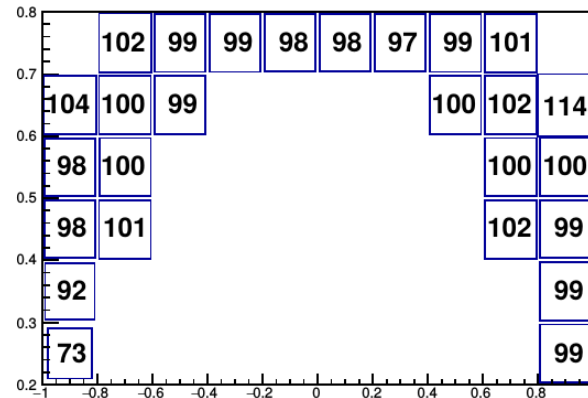
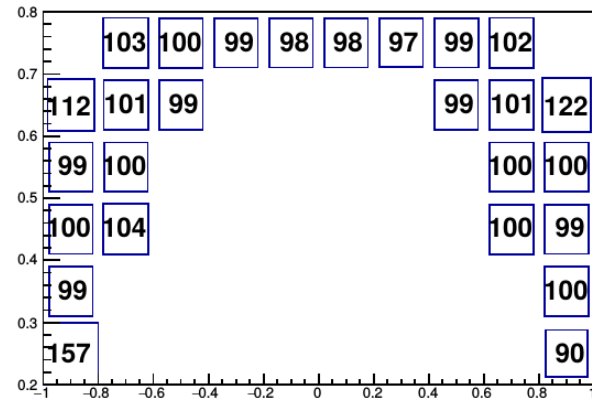
p, \bar{p} track eff pT vs $\cos(\theta)$



JiaoJiao

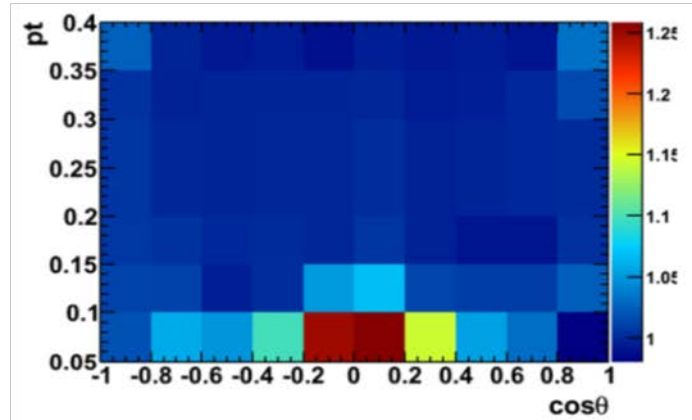
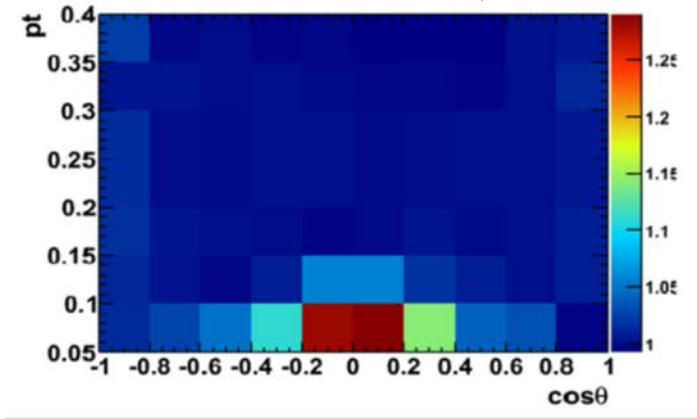


Data

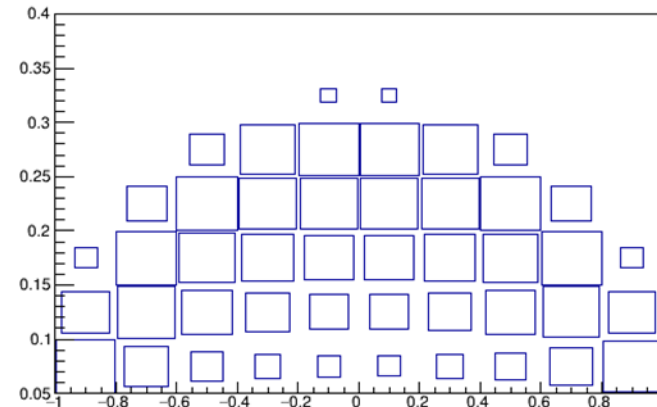
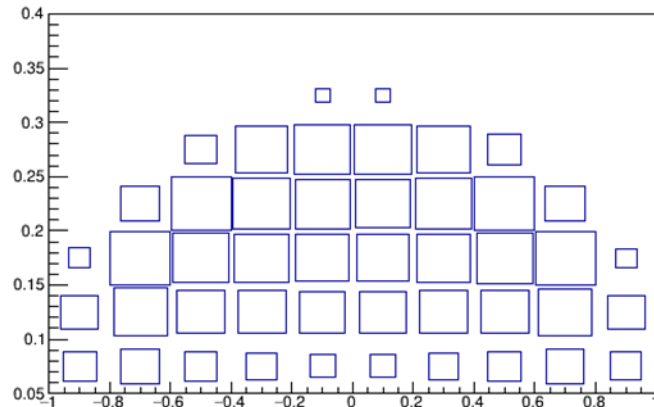


Data/MC

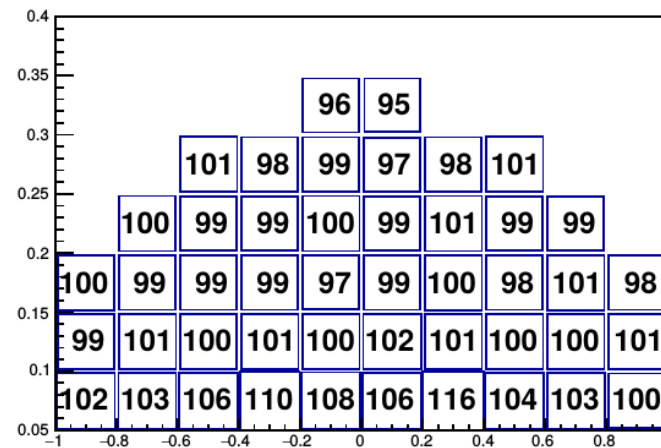
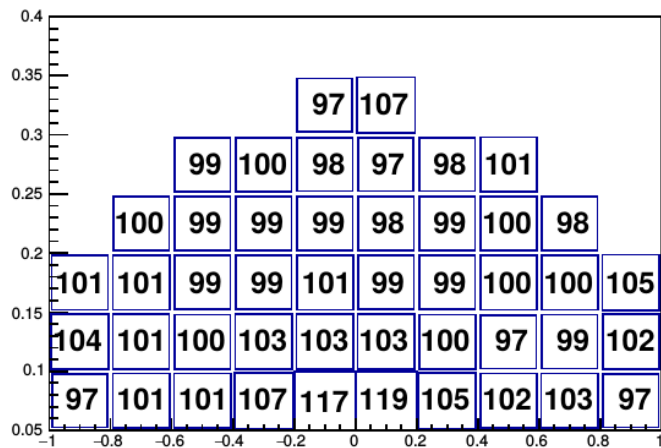
π^-, π^+ track eff pT vs $\cos(\theta)$



Jiaojiao

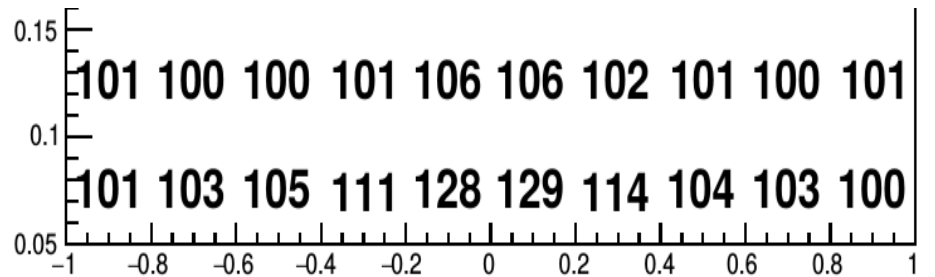
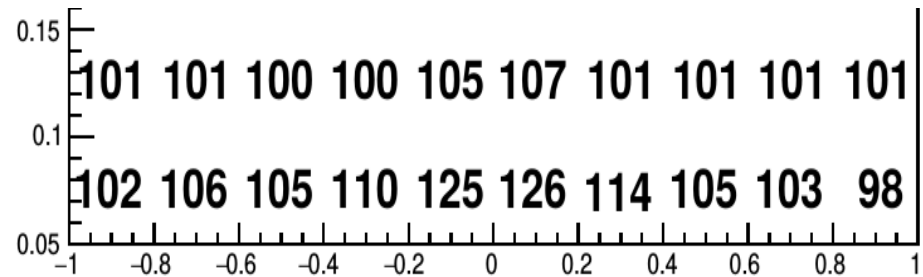
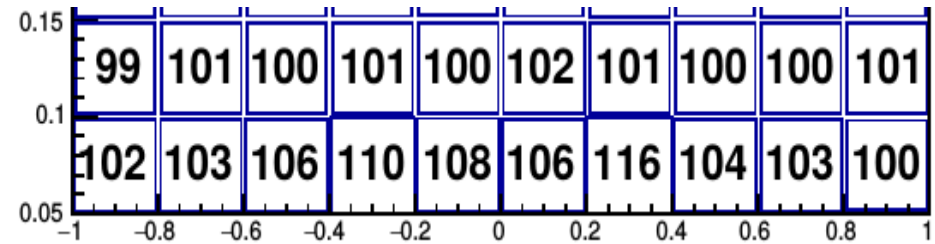
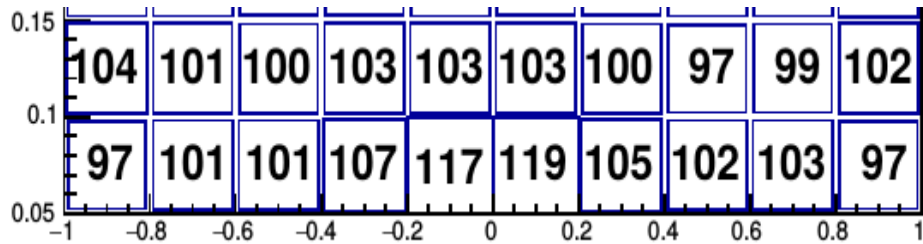


Data



Data/MC

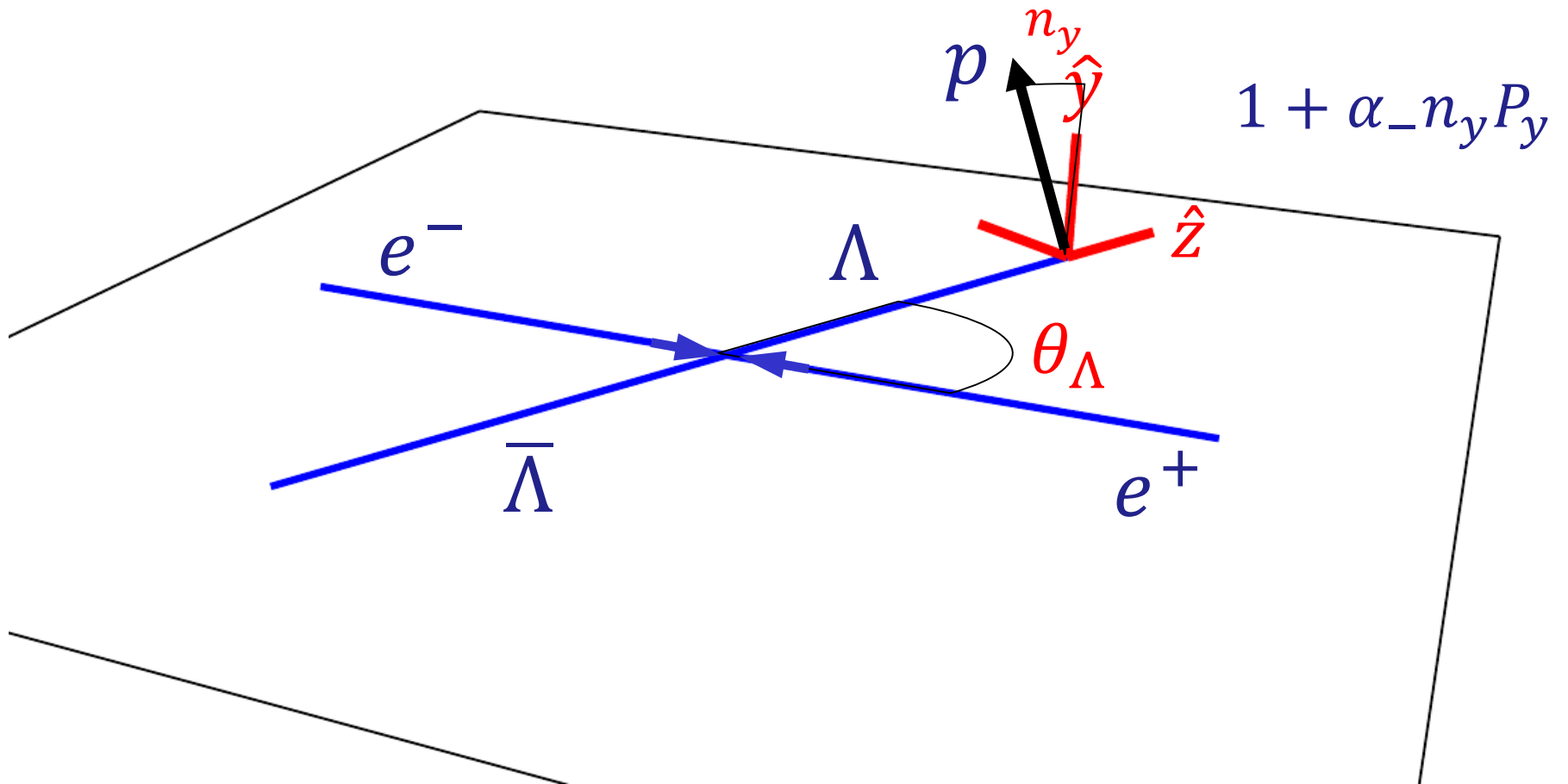
π^-, π^+ track eff pT vs $\cos(\theta)$



Only pions are affected

Apply Jiaojiao correction (eff1)
or first iteration to self consistent method (eff2)

$$e^+ e^- \rightarrow (\Lambda \rightarrow p \pi^-) \bar{\Lambda}$$



$$\Lambda \rightarrow p \pi^- : \Omega_1 = (\cos \theta_1, \phi_1) : \alpha_1 \rightarrow \alpha_-$$

Hyperon polarization determined using
angular distribution of the baryon from the weak decay

Exclusive decay distributions

$$e^+e^- \rightarrow (\Lambda \rightarrow p\pi^-)(\bar{\Lambda} \rightarrow \bar{p}\pi^+)$$

$$d\Gamma \propto \mathcal{W}(\xi)d\xi = \mathcal{W}(\xi)d\cos\theta_\Lambda d\Omega_1 d\Omega_2$$

$$\xi : (\cos\theta_\Lambda, \Omega_1, \Omega_2)$$

$$\Lambda \rightarrow p\pi^- : \Omega_1 = (\cos\theta_1, \phi_1) \quad : \alpha_1 \rightarrow \alpha_-$$

$$\bar{\Lambda} \rightarrow \bar{p}\pi^+ (\text{or } \bar{n}\pi^0) : \Omega_2 = (\cos\theta_2, \phi_2)$$

$$\bar{\Lambda} \rightarrow \bar{p}\pi^+ : \alpha_2 \rightarrow \alpha_+$$

$$\mathcal{W}(\xi) = 1 + \alpha_\psi \cos^2\theta_\Lambda$$

$$+ \alpha_1 \alpha_2 (\sin^2\theta_\Lambda \sin\theta_1 \sin\theta_2 \cos\phi_1 \cos\phi_2 + \cos^2\theta_\Lambda \cos\theta_1 \cos\theta_2)$$

$$+ \alpha_1 \alpha_2 \sqrt{1 - \alpha_\psi^2} \cos(\Delta\Phi) \{ \sin\theta_\Lambda \cos\theta_\Lambda (\sin\theta_1 \cos\theta_2 \cos\phi_1 + \cos\theta_1 \sin\theta_2 \cos\phi_2) \}$$

$$+ \alpha_1 \alpha_2 \alpha_\psi (\cos\theta_1 \cos\theta_2 - \sin^2\theta_\Lambda \sin\theta_1 \sin\theta_2 \sin\phi_1 \sin\phi_2)$$

$$+ \sqrt{1 - \alpha_\psi^2} \sin(\Delta\Phi) \sin\theta_\Lambda \cos\theta_\Lambda (\alpha_1 \sin\theta_1 \sin\phi_1 + \alpha_2 \sin\theta_2 \sin\phi_2)$$

Spin correlations

Exclusive decay distributions

$$e^+e^- \rightarrow (\Lambda \rightarrow p\pi^-)(\bar{\Lambda} \rightarrow \bar{p}\pi^+)$$

$$d\Gamma \propto \mathcal{W}(\xi)d\xi = \mathcal{W}(\xi)d\cos\theta_\Lambda d\Omega_1 d\Omega_2$$

$$\xi : (\cos\theta_\Lambda, \Omega_1, \Omega_2)$$

$$\Lambda \rightarrow p\pi^- : \Omega_1 = (\cos\theta_1, \phi_1) \quad : \alpha_1 \rightarrow \alpha_-$$

$$\bar{\Lambda} \rightarrow \bar{p}\pi^+ \text{ (or } \bar{n}\pi^0\text{)} : \Omega_2 = (\cos\theta_2, \phi_2)$$

$$\bar{\Lambda} \rightarrow \bar{p}\pi^+ : \alpha_2 \rightarrow \alpha_+$$

Just 4 (3) global parameters

$$\mathcal{W}(\xi) = 1 + \alpha_\psi \cos^2\theta_\Lambda$$

$$+ \alpha_- \alpha_+ \left[\sin^2\theta_\Lambda (n_{1,x}n_{2,x} - \alpha_\psi n_{1,y}n_{2,y}) + (\cos^2\theta_\Lambda + \alpha_\psi) n_{1,z}n_{2,z} \right]$$

$$+ \alpha_- \alpha_+ \sqrt{1 - \alpha_\psi^2} \cos(\Delta\Phi) \sin\theta_\Lambda \cos\theta_\Lambda (n_{1,x}n_{2,z} + n_{1,z}n_{2,x})$$

$$+ \sqrt{1 - \alpha_\psi^2} \sin(\Delta\Phi) \sin\theta_\Lambda \cos\theta_\Lambda (\alpha_- n_{1,y} + \alpha_+ n_{2,y}) .$$

Spin correlations

General two spin 1/2 particle state

$$\rho_{1/2, \overline{1/2}} = \frac{1}{4} \sum_{\mu\nu} C_{\mu\overline{\nu}} \sigma_{\mu} \otimes \sigma_{\overline{\nu}}$$

16 parameters for each θ :
I(θ), polarizations (6)
Spin correlations (9)

$$\mathcal{W}(\xi) = \mathcal{I}(\theta) \left\{ 1 + \alpha_{\Lambda} \sum_k P_k(\theta) \mathbf{n}_k + \alpha_{\overline{\Lambda}} \sum_{\overline{k}} P_{\overline{k}}(\theta) \mathbf{n}_{\overline{k}} + \alpha_{\Lambda} \alpha_{\overline{\Lambda}} \sum_{\overline{k}k} C_{\overline{k}k}(\theta) \mathbf{n}_{\overline{k}} \mathbf{n}_k \right\}$$

polarizations (6)

Spin correlations (9)

$$P_y(\theta) = \sqrt{1 - \alpha_{\psi}^2} \frac{\cos \theta \sin \theta}{1 + \alpha_{\psi} \cos^2 \theta} \sin(\Delta\Phi)$$

$$P_{\overline{y}}(\theta) = P_y(\theta).$$

$$\mathcal{I}(\theta) = 1 + \alpha_{\psi} \cos^2 \theta.$$

$$C_{\overline{z}z}(\theta) \mathcal{I}(\theta) = -\alpha_{\psi} + \cos^2 \theta$$

$$C_{\overline{x}x}(\theta) \mathcal{I}(\theta) = -\sin^2 \theta$$

$$C_{\overline{y}y}(\theta) \mathcal{I}(\theta) = -\alpha_{\psi} \sin^2 \theta$$

$$C_{\overline{x}z}(\theta) \mathcal{I}(\theta) = -\sqrt{1 - \alpha_{\psi}^2} \cos \theta \sin \theta \cos(\Delta\Phi)$$

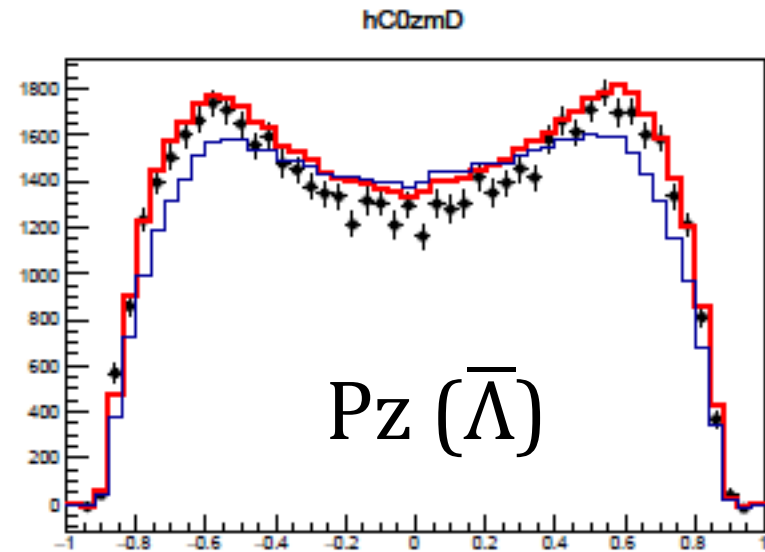
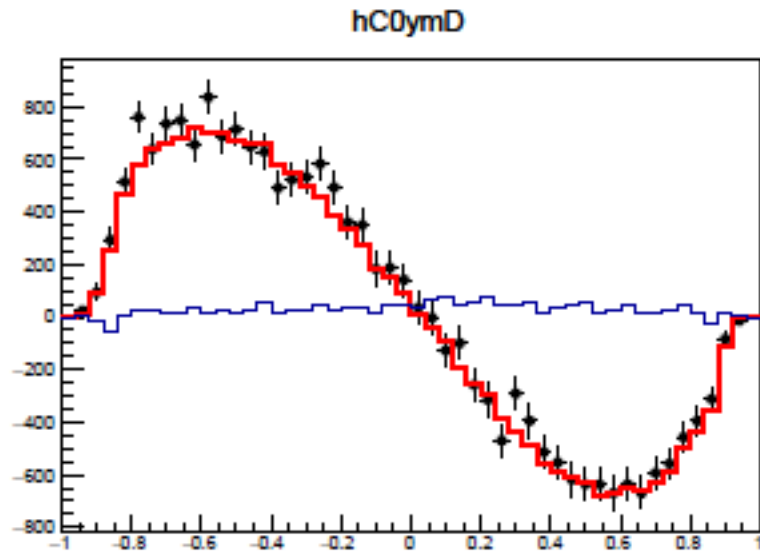
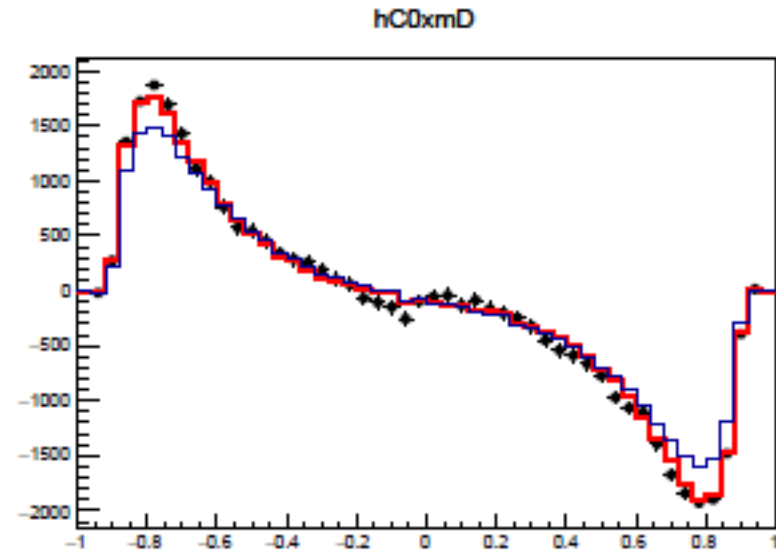
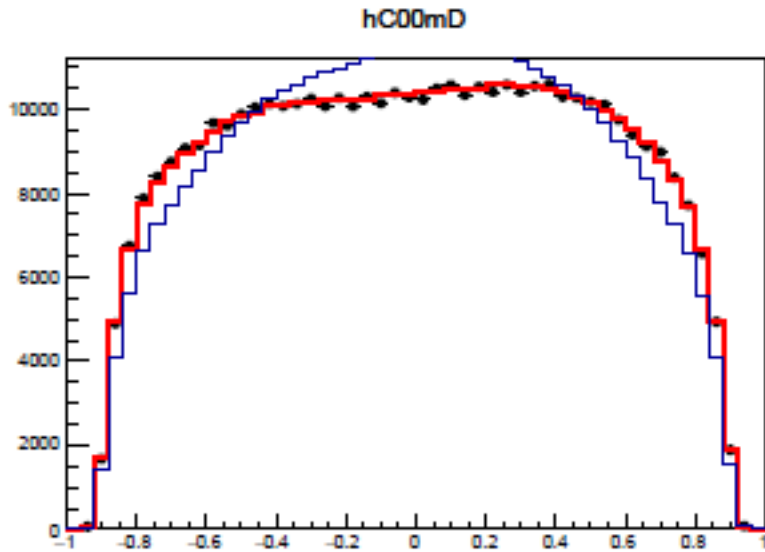
$$C_{\overline{z}x}(\theta) = C_{\overline{x}z}(\theta)$$

moments:

$$M(\theta) = \sum_i^{N(\theta)} \mathbf{n}_{\mu}^i \mathbf{n}_{\nu}^i$$

(uncorrected for acceptance)

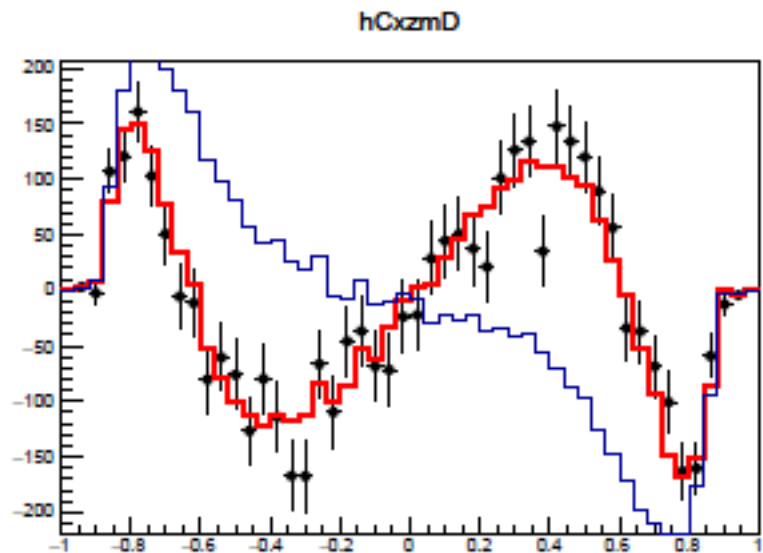
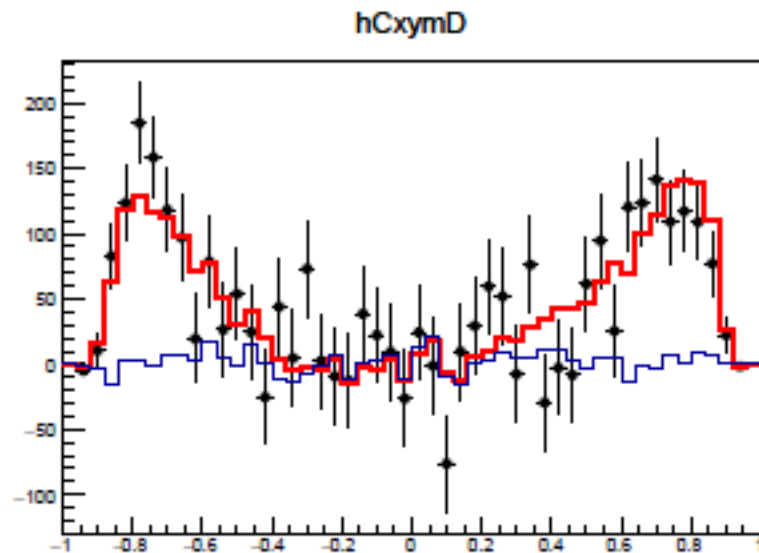
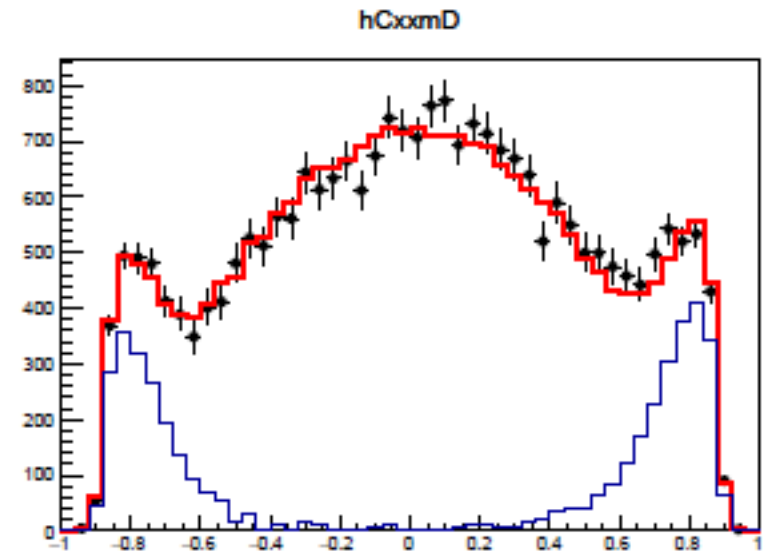
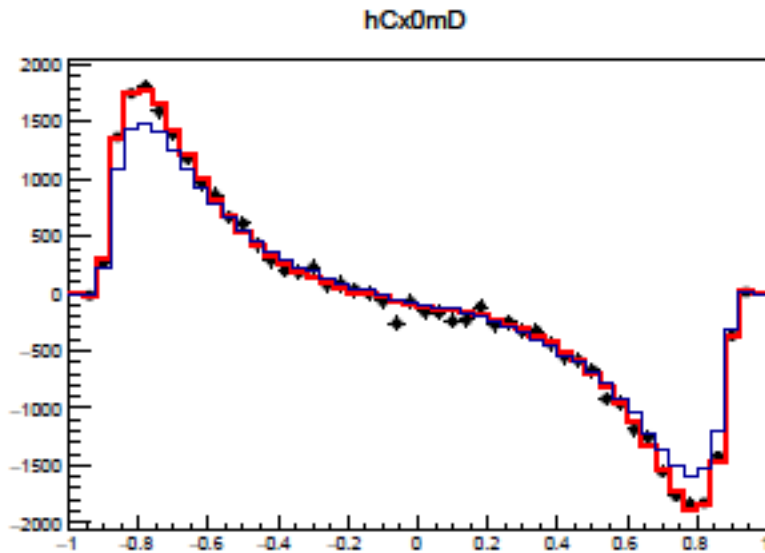
$$e^+e^- \rightarrow J/\psi \rightarrow (\Lambda \rightarrow p\pi^-)(\bar{\Lambda} \rightarrow \bar{p}\pi^+)$$



(blue) Phase Space

(red) Fit

$$e^+e^- \rightarrow J/\psi \rightarrow (\Lambda \rightarrow p\pi^-)(\bar{\Lambda} \rightarrow \bar{p}\pi^+)$$

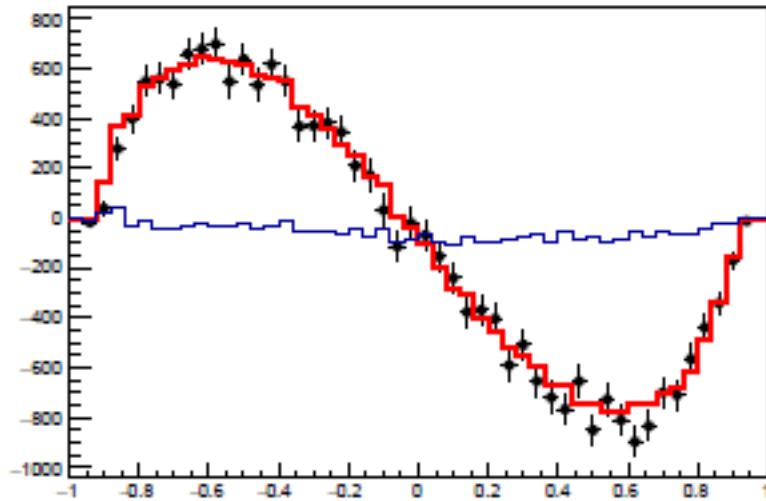


(blue) Phase Space

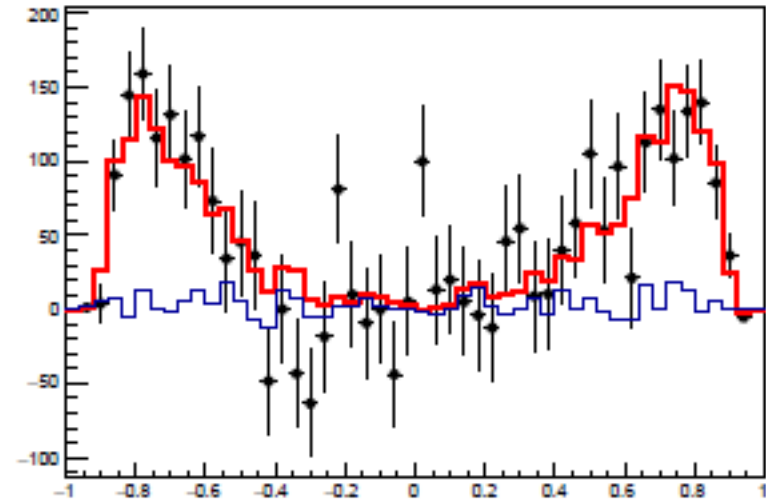
(red) Fit

$$e^+e^- \rightarrow J/\psi \rightarrow (\Lambda \rightarrow p\pi^-)(\bar{\Lambda} \rightarrow \bar{p}\pi^+)$$

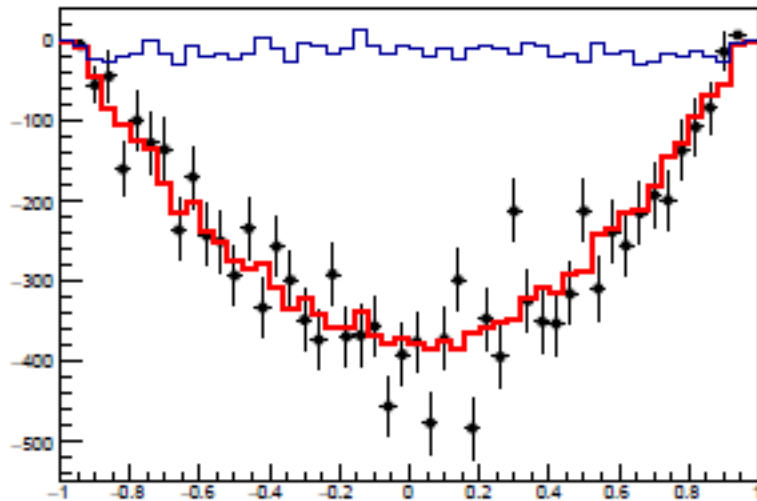
hCy0mD



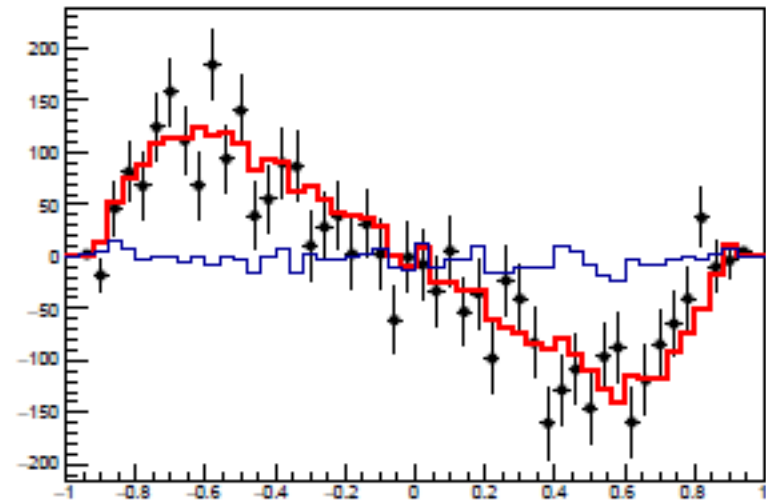
hCyxmD



hCyymD



hCyzmD

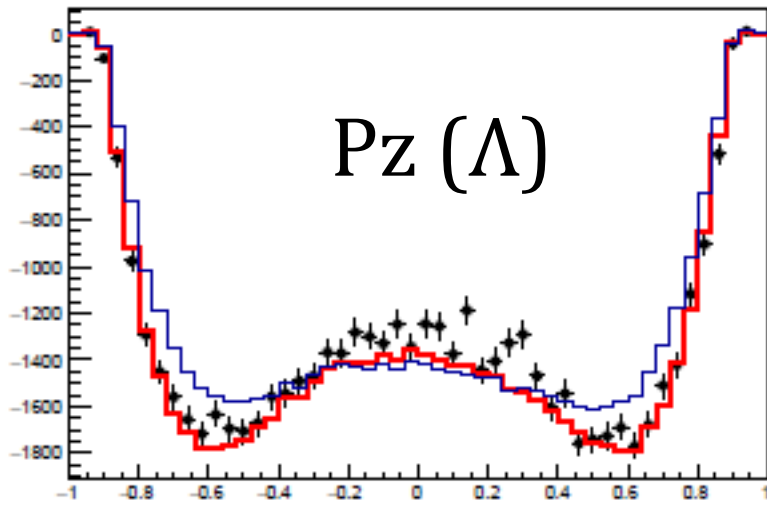


(blue) Phase Space

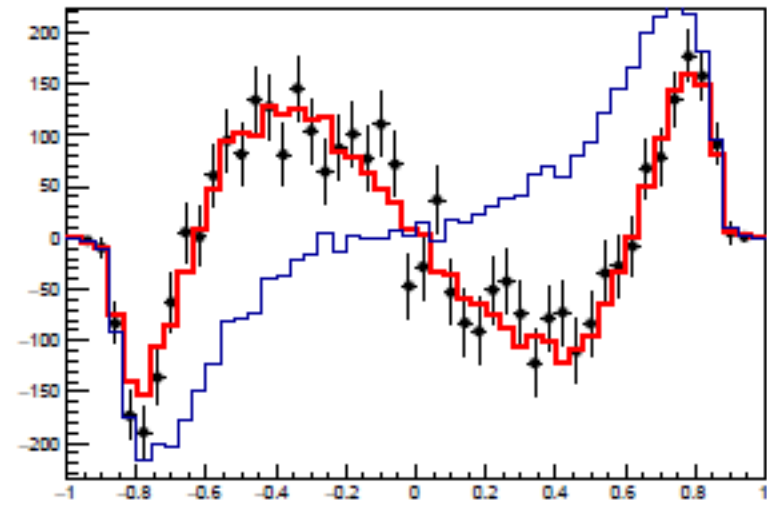
(red) Fit

$$e^+e^- \rightarrow J/\psi \rightarrow (\Lambda \rightarrow p\pi^-)(\bar{\Lambda} \rightarrow \bar{p}\pi^+)$$

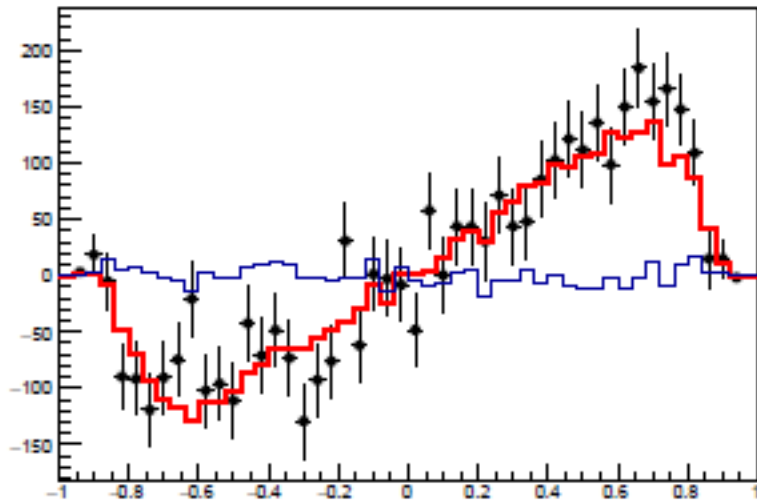
hCz0mD



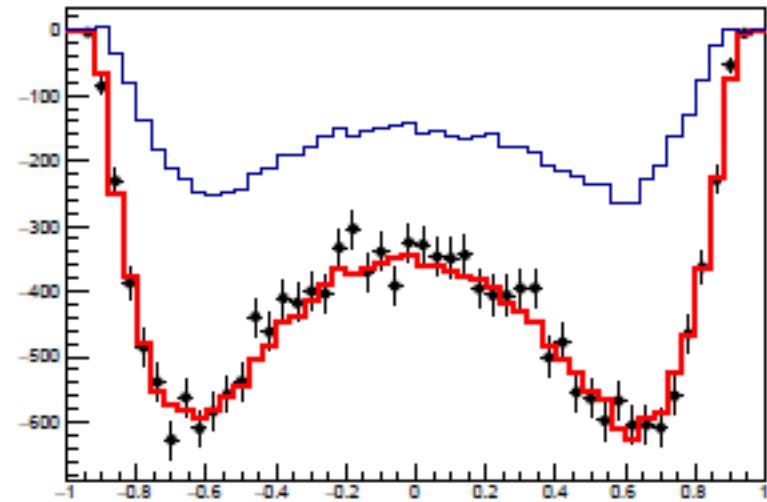
hCzxmD



hCzymD



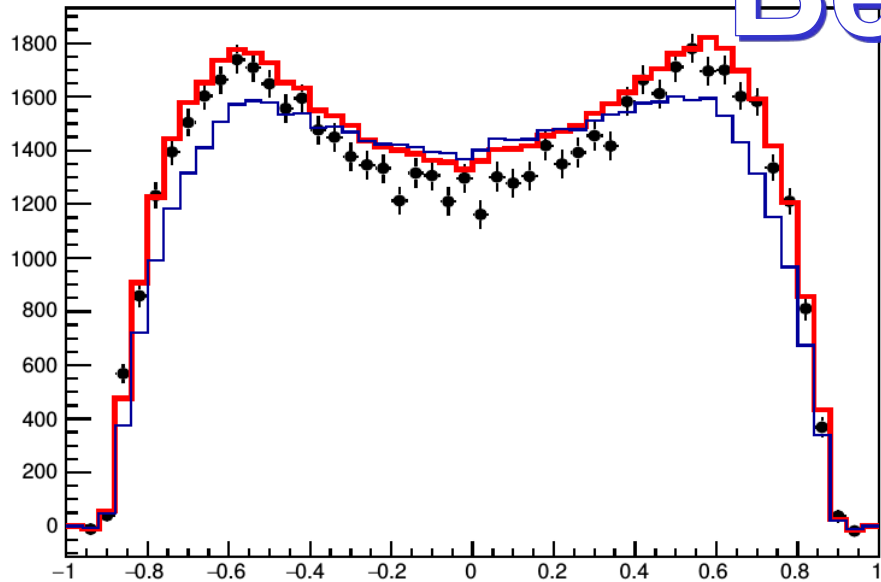
hCzzmD



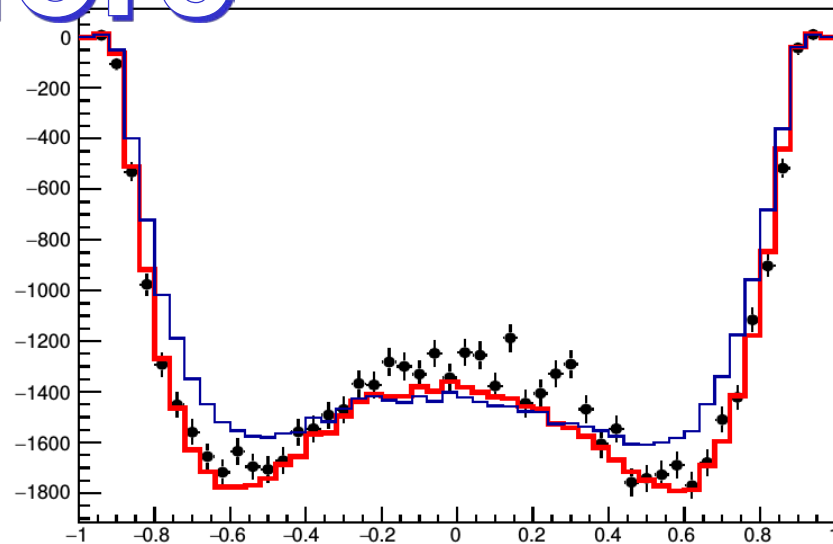
(blue) Phase Space

(red) Fit

Before

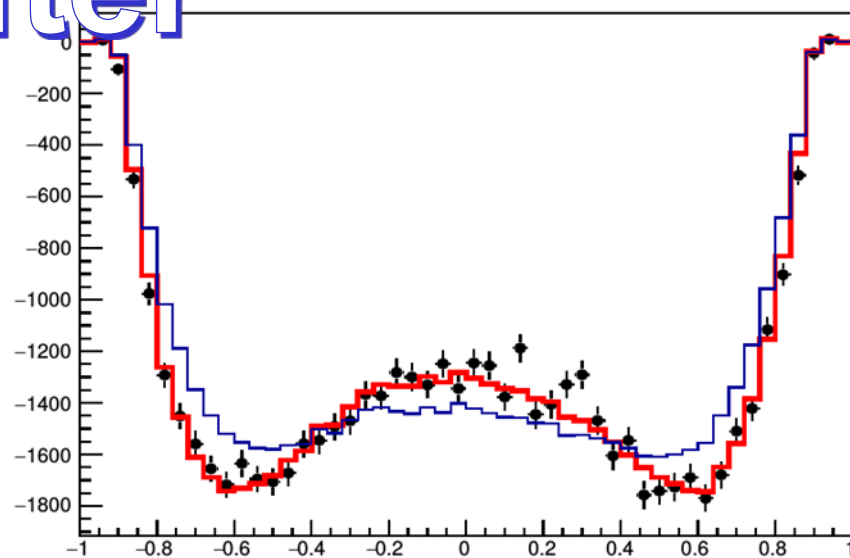
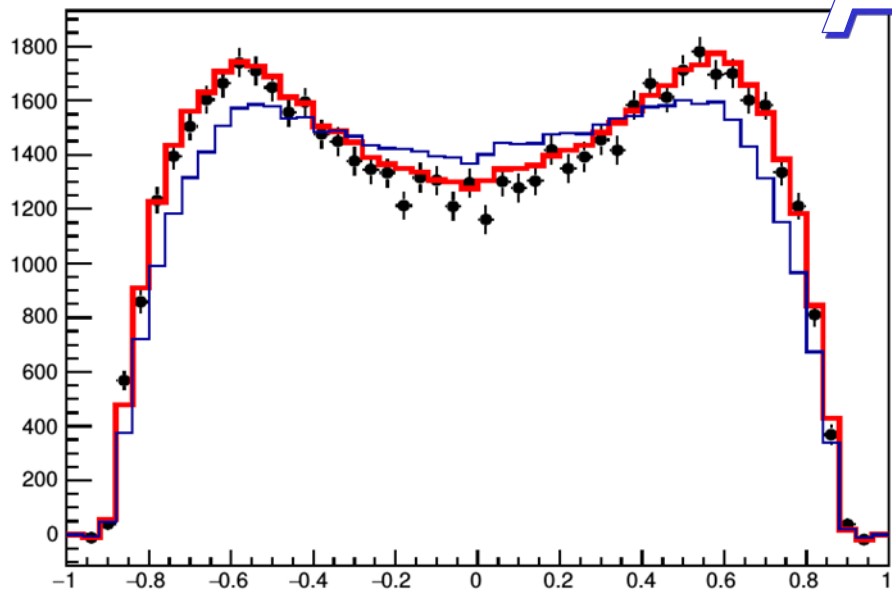


$P_z(\bar{\Lambda})$



$P_z(\Lambda)$

After



		Stat	syst	eff 1	eff2	
1	a	4.595e-01	0.0058	0.007	0.0077	-0.0013
2	a-	7.488e-01	0.0098	0.004	0.0034	0.0024
3	DPhi	7.383e-01	0.0109	0.008	0.0050	-0.0019
4	a+	-7.593e-01	0.0099	-0.007	-0.0029	-0.0025

Parameters	This work	Previous results
α_ψ	$0.461 \pm 0.006 \pm 0.007$	0.469 ± 0.027 ²³
$\Delta\Phi$ (rad)	$0.740 \pm 0.010 \pm 0.008$	–
α_-	$0.750 \pm 0.009 \pm 0.004$	0.642 ± 0.013 ²⁵
α_+	$-0.758 \pm 0.010 \pm 0.007$	-0.71 ± 0.08 ²⁵
$\bar{\alpha}_0$	$-0.692 \pm 0.016 \pm 0.006$	–
A_{CP}	$-0.006 \pm 0.012 \pm 0.007$	0.006 ± 0.021 ²⁵
$\bar{\alpha}_0/\alpha_+$	$0.913 \pm 0.028 \pm 0.012$	–