



Weak decays of doubly heavy baryons: recent progresses

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[Phys.Rev. D98 \(2018\) no.5, 056002](#)

[Chin.Phys. C42 \(2018\) no.12, 123102](#)

[arXiv:1811.xxxxx](#)

In collaboration with Xiao-Hui Hu, Yue-Long Shen, Yu-Ji Shi, Wei Wang, Zhi-Peng Xing, Fu-Sheng Yu

Outline



- Introduction
- Weak decays of doubly heavy baryons: the $1/2 \rightarrow 1/2$ case
- Weak decays of doubly heavy baryons: the $1/2 \rightarrow 3/2$ case
- Weak decays of doubly heavy baryons: the FCNC processes
- Weak decays of doubly heavy baryons: decay constants
- Weak decays of doubly heavy baryons: the form factors
- Summary and outlook



Introduction

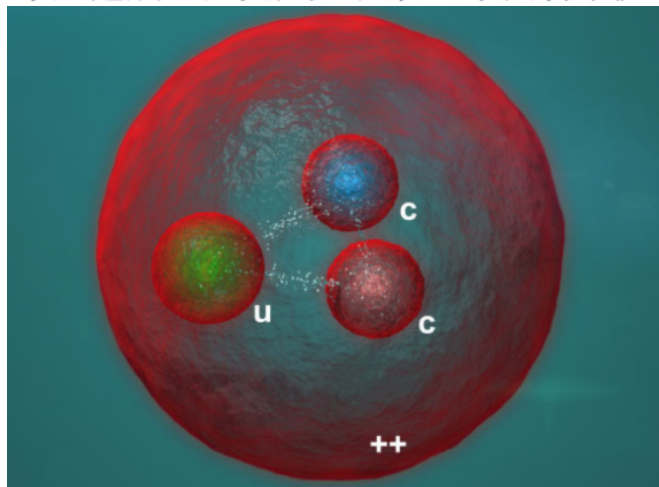


Observation of the doubly charmed baryon Ξ_{CC}^{++}

2017年度中国科学十大进展正式对外发布

日期：2018年03月01日 来源：科技部

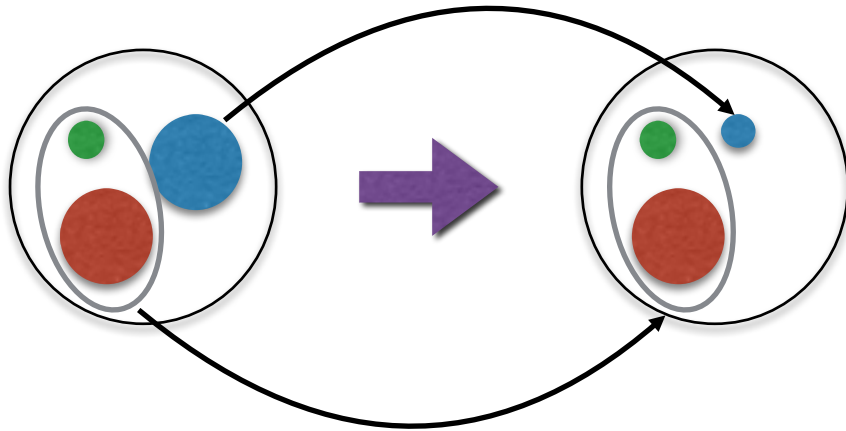
2018年2月27日，科技部基础研究司与科技部基础研究管理中心在北京联合召开“2017年度中国科学十大进展专家解读会”，正式对外公布“2017年度中国科学十大进展”遴选结果，并邀请相关领域专家对十大进展逐项进行解读。科技部基础研究司崔拓副司长，科技部基础研究管理中心刘敏主任、卞曙光副主任，十大进展解读专家，十大进展主要完成人代表，中国科学院和教育部等部门代表，在京高校、科研院所等单位代表，新华社和中央



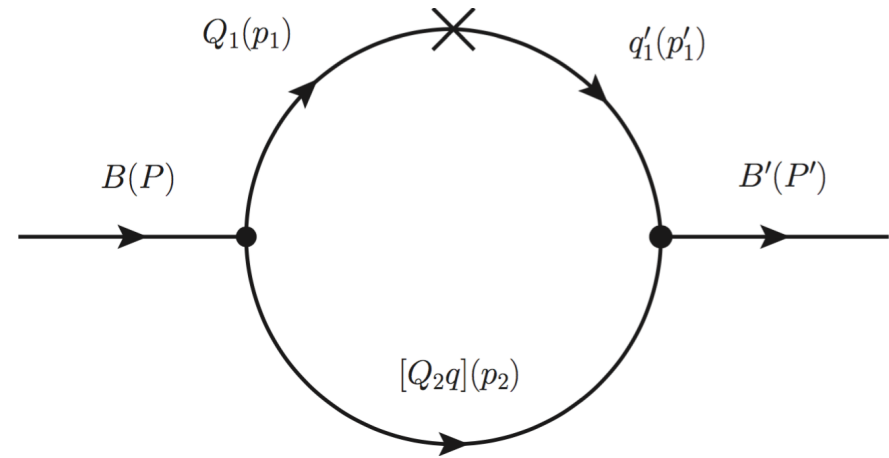
办办单位相关人员等140余人出席了会议，会议由卞曙光副主任主持。

公布了2017年度中国科学十大进展遴选结果：实现星地千公里级量子纠缠化为活疫苗及治疗性药物、首次探测到双粲重子、实验发现三重简并费发出基于共格纳米析出强化的新一代超高强钢、利用量子相变确定性制类化石、酵母长染色体的精准定制合成、研制出可实现自由状态脑成像展入选“2017年度中国科学十大进展”。崔拓副司长、刘敏主任为十大进展选十大进展一一进行了解读。

Basic ideas



diquark
 0^+ or 1^+



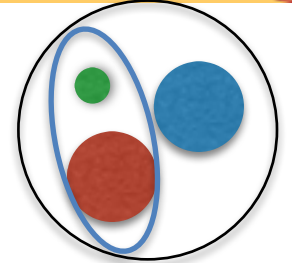
H. W. Ke, X. Q. Li and Z. T. Wei, Phys. Rev. D 77, 014020 (2008)

H. W. Ke, X. H. Yuan, X. Q. Li, Z. T. Wei and Y. X. Zhang, Phys. Rev. D 86, 114005 (2012)

$$|B\rangle^{\text{phys}} = c_S |B, [di]\rangle + c_A |B, \{di\}\rangle$$

c_S and c_A are determined by the flavor-spin wave functions

Overview of LFQM



$$|B(P, S, S_z)\rangle = \int \{d^3 p_1\} \{d^3 p_2\} 2(2\pi)^3 \delta^3(\tilde{P} - \tilde{p}_1 - \tilde{p}_2) \\ \times \sum_{\lambda_1, \lambda_2} \Psi^{SS_z}(\tilde{p}_1, \tilde{p}_2, \lambda_1, \lambda_2) |q_1(p_1, \lambda_1) [di](p_2, \lambda_2)\rangle$$

$$\tilde{p} = (p^+, p_\perp), \quad \{d^3 p\} \equiv \frac{dp^+ d^2 p_\perp}{2(2\pi)^3}, \quad \delta^3(\tilde{p}) = \delta(p^+) \delta^2(p_\perp).$$

$$p^- = \frac{p_\perp^2 + m^2}{p^+}$$

Overview of LFQM



$$\Psi^{SS_z}(\tilde{p}_1, \tilde{p}_2, \lambda_1, \lambda_2) = \sum_{s_1, s_2} \langle \lambda_1 | \mathcal{R}_M^\dagger(x_1, -k_\perp, m_1) | s_1 \rangle \langle \lambda_2 | \mathcal{R}_M^\dagger(x_2, k_\perp, m_2) | s_2 \rangle$$

$$\times \langle \frac{1}{2} s_1; s_{[di]} s_2 | \frac{1}{2} S_z \rangle \varphi(x, k_\perp),$$

$$\frac{1}{\sqrt{2(p_1 \cdot \bar{P} + m_1 M_0)}} \bar{u}(p_1, \lambda_1) \Gamma u(\bar{P}, S_z)$$

0⁺

$$\Gamma = 1$$

1⁺

$$\Gamma = -\frac{1}{\sqrt{3}} \gamma_5 \not{\epsilon}^*(p_2, \lambda_2)$$


H. W. Ke, X. H. Yuan, X. Q. Li, Z. T. Wei and Y. X. Zhang, Phys. Rev. D 86, 114005 (2012)

Overview of LFQM



$$\Psi^{SS_z}(\tilde{p}_1, \tilde{p}_2, \lambda_1, \lambda_2) = \sum_{s_1, s_2} \langle \lambda_1 | \mathcal{R}_M^\dagger(x_1, -k_\perp, m_1) | s_1 \rangle \langle \lambda_2 | \mathcal{R}_M^\dagger(x_2, k_\perp, m_2) | s_2 \rangle$$

$$\times \langle \frac{1}{2} s_1; s_{[di]} s_2 | \frac{1}{2} S_z \rangle \varphi(x, k_\perp),$$



 $A\phi(x, k_\perp)$

0⁺

$$A = 1$$

1⁺

$$A = \sqrt{\frac{3(M_0 m_1 + p_1 \cdot \bar{P})}{3M_0 m_1 + p_1 \cdot \bar{P} + (2p_1 \cdot p_2 p_2 \cdot \bar{P})/m_2^2}}$$

$$\phi(x, \vec{k}_\perp) = 4 \left(\frac{\pi}{\beta^2} \right)^{3/4} \sqrt{\frac{e_1 e_2}{x_1 x_2 M_0}} \exp \left(-\frac{\vec{k}_\perp^2 + k_z^2}{2\beta^2} \right)$$



Singly heavy baryon decays

TABLE X: A comparison with some recent works for semi-leptonic bottomed decays.

channel	this work	other theoretical predictions	experiment [83]
$\Lambda_b^0 \rightarrow pe^- \bar{\nu}_e$	3.14×10^{-4}	2.9×10^{-4} [84], $(4.80 \pm 0.99) \times 10^{-4}$ [51]	$(4.1 \pm 1.0) \times 10^{-4}$
$\Lambda_b^0 \rightarrow \Lambda_c^+ e^- \bar{\nu}_e$	8.83×10^{-2}	6.9×10^{-2} [88], $(5.32 \pm 0.35) \times 10^{-2}$ [51]	$(6.2^{+1.4}_{-1.3}) \times 10^{-2}$

TABLE VIII: A comparison with some recent works for semi-leptonic charmed decays.

channel	this work	other theoretical predictions	experiment [83]
$\Lambda_c^+ \rightarrow ne^+ \nu_e$	2.01×10^{-3}	$(2.7 \pm 0.3) \times 10^{-3}$ [80], 2.07×10^{-3} [84], $(4.10 \pm 0.26) \times 10^{-3}$ [53]	--
$\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e$	1.63×10^{-2}	2.72×10^{-2} [88], $(3.80 \pm 0.22) \times 10^{-2}$ [52]	$(3.6 \pm 0.4) \times 10^{-2}$
$\Xi_c^+ \rightarrow \Sigma^0 e^+ \nu_e$	1.87×10^{-3}	$(0.8 \pm 0.1) \times 10^{-3}$ [80]	--
$\Xi_c^+ \rightarrow \Lambda e^+ \nu_e$	8.22×10^{-4}	$(2.5 \pm 0.4) \times 10^{-4}$ [80]	--
$\Xi_c^+ \rightarrow \Xi^0 e^+ \nu_e$	5.39×10^{-2}	$(3.38^{+2.19}_{-2.26}) \times 10^{-2}$ [81], $(3.0 \pm 0.5) \times 10^{-2}$ [80]	--
$\Xi_c^0 \rightarrow \Sigma^- e^+ \nu_e$	9.47×10^{-4}	$(60 \pm 8) \times 10^{-4}$ [80]	--
$\Xi_c^0 \rightarrow \Xi^- e^+ \nu_e$	1.35×10^{-2}	$(4.87 \pm 1.74) \times 10^{-2}$ [81], $(11.9 \pm 1.6) \times 10^{-2}$ [80]	--



Weak decays of doubly heavy baryons: the $1/2 \rightarrow 1/2$ case

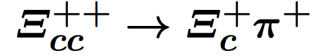
W. Wang, F. S. Yu and Z. X. Zhao, Eur.Phys.J. C77 (2017) no.11, 781



The 1/2 -> 1/2 case

arXiv:1807.01919v2 [hep-ex] 6 Jul 2018

First observation of the doubly charmed baryon decay



LHCb collaboration[†]

Abstract

The doubly charmed baryon decay $\Xi_{cc}^{++} \rightarrow \Xi_c^+ \pi^+$ is observed for the first time, with a statistical significance of 5.9σ , confirming a recent observation of the baryon in the $\Lambda_c^+ K^- \pi^+ \pi^+$ final state. The data sample used corresponds to an integrated luminosity of 1.7 fb^{-1} , collected by the LHCb experiment in pp collisions at a center-of-mass energy of 13 TeV. The Ξ_{cc}^{++} mass is measured to be

$$3620.6 \pm 1.5 (\text{stat}) \pm 0.4 (\text{syst}) \pm 0.3 (\Xi_c^+) \text{ MeV}/c^2,$$

and is consistent with the previous result. The ratio of branching fractions between the decay modes is measured to be

$$\frac{\mathcal{B}(\Xi_{cc}^{++} \rightarrow \Xi_c^+ \pi^+) \times \mathcal{B}(\Xi_c^+ \rightarrow p K^- \pi^+)}{\mathcal{B}(\Xi_{cc}^{++} \rightarrow \Lambda_c^+ K^- \pi^+ \pi^+) \times \mathcal{B}(\Lambda_c^+ \rightarrow p K^- \pi^+)} = 0.035 \pm 0.009 (\text{stat}) \pm 0.003 (\text{syst}).$$

TABLE XXII: Partial decay widths (in units of GeV) and branching ratios for non-leptonic decays of the doubly charmed baryons.

channels	Γ / GeV	\mathcal{B}	channels	Γ / GeV	\mathcal{B}
$\Xi_{cc}^{++} \rightarrow \Lambda_c^+ \pi^+$	8.87×10^{-15}	4.05×10^{-3}	$\Xi_{cc}^{++} \rightarrow \Lambda_c^+ \rho^+$	2.32×10^{-14}	1.06×10^{-2}
$\Xi_{cc}^{++} \rightarrow \Lambda_c^+ a_1^+$	1.02×10^{-14}	4.66×10^{-3}	$\Xi_{cc}^{++} \rightarrow \Lambda_c^+ K^+$	7.79×10^{-16}	3.55×10^{-4}
$\Xi_{cc}^{++} \rightarrow \Lambda_c^+ K^{*+}$	1.09×10^{-15}	4.98×10^{-4}			
$\Xi_{cc}^{++} \rightarrow \Sigma_c^+ \pi^+$	5.75×10^{-15}	2.62×10^{-3}	$\Xi_{cc}^{++} \rightarrow \Sigma_c^+ \rho^+$	2.47×10^{-14}	1.13×10^{-2}
$\Xi_{cc}^{++} \rightarrow \Sigma_c^+ K^{*+}$	1.28×10^{-15}	5.83×10^{-4}	$\Xi_{cc}^{++} \rightarrow \Sigma_c^+ K^+$	4.22×10^{-16}	1.92×10^{-4}
$\Xi_{cc}^{++} \rightarrow \Xi_c^+ \pi^+$	1.57×10^{-13}	7.14×10^{-2}	$\Xi_{cc}^{++} \rightarrow \Xi_c^+ \rho^+$	3.03×10^{-13}	1.38×10^{-1}
$\Xi_{cc}^{++} \rightarrow \Xi_c^+ K^{*+}$	1.19×10^{-14}	5.44×10^{-3}	$\Xi_{cc}^{++} \rightarrow \Xi_c^+ K^+$	1.31×10^{-14}	5.97×10^{-3}
$\Xi_{cc}^{++} \rightarrow \Xi_c'^+ \pi^+$	1.10×10^{-13}	5.00×10^{-2}	$\Xi_{cc}^{++} \rightarrow \Xi_c'^+ \rho^+$	4.12×10^{-13}	1.88×10^{-1}
$\Xi_{cc}^{++} \rightarrow \Xi_c'^+ K^{*+}$	1.87×10^{-14}	8.54×10^{-3}	$\Xi_{cc}^{++} \rightarrow \Xi_c'^+ K^+$	7.48×10^{-15}	3.41×10^{-3}

$$\mathcal{B}(\Xi_{cc}^{++} \rightarrow \Xi_c^+ \pi^+) = 7.14 \times 10^{-2}$$

$$\mathcal{B}(\Xi_{cc}^{++} \rightarrow \Xi_c'^+ \pi^+) = 5.00 \times 10^{-2}$$

$$\Xi_c'^+ \rightarrow \Xi_c^+ \gamma$$

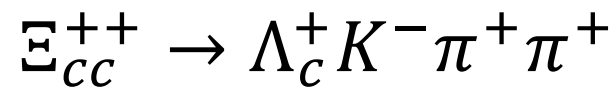
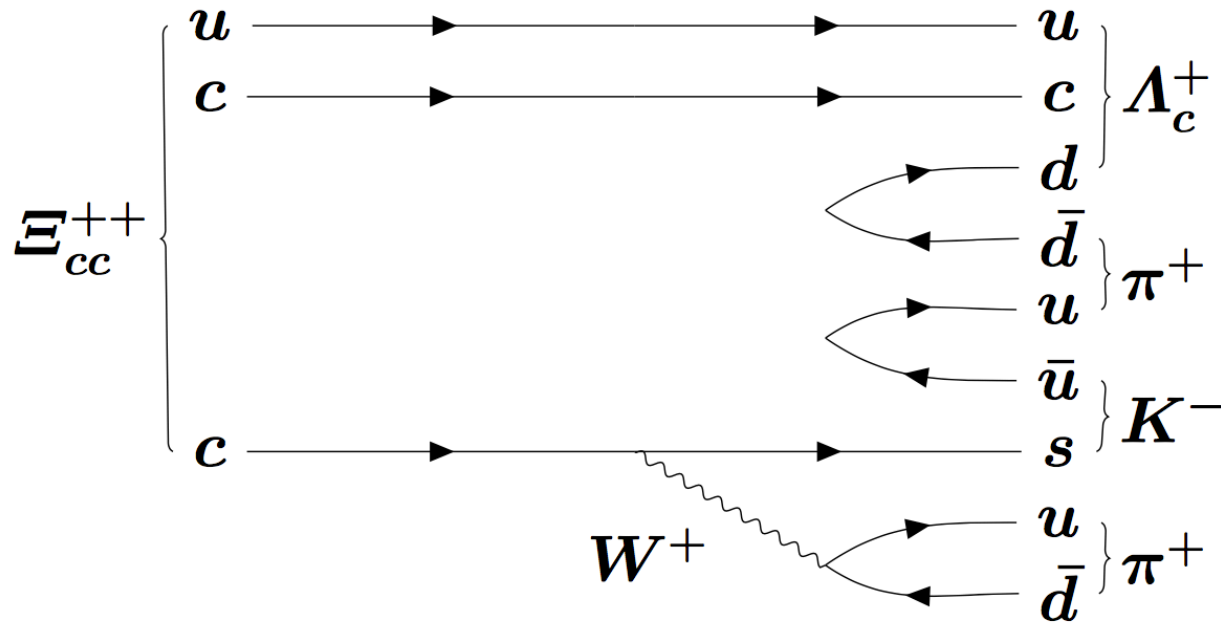
$$m_{\Xi_c'^+} - m_{\Xi_c^+} \approx 107.8 \text{ MeV}$$



Weak decays of doubly heavy baryons: the $1/2 \rightarrow 3/2$ case

Z. X. Zhao, Eur.Phys.J.C78 (2018) no.9, 756

Motivation





- Difficulty: The vectorial spinor for spin-3/2 baryon

$$u^\alpha = (\epsilon^\alpha - \frac{1}{3}(\gamma^\alpha + v^\alpha)\not{v})u$$

$$u^\alpha(p, \lambda) = \sum_{\lambda_1, \lambda_2} \langle \frac{1}{2}, \lambda_1, 1, \lambda_2 | \frac{3}{2}, \lambda \rangle \times u(p, \lambda_1) \epsilon^\alpha(p, \lambda_2)$$

- Conculsion: Approximately one order of magnitude smaller than its 1/2 to 1/2 counterpart



The 1/2 -> 3/2 case

Table 16 Nonleptonic decays for the cc sector

Channels	Γ / GeV	\mathcal{B}	Channels	Γ / GeV	\mathcal{B}
$\Xi_{cc}^{++} \rightarrow \Sigma_c^{*+} \pi^+$	1.16×10^{-15}	5.28×10^{-4}	$\Xi_{cc}^{++} \rightarrow \Sigma_c^{*+} \rho^+$	3.78×10^{-15}	1.73×10^{-3}
$\Xi_{cc}^{++} \rightarrow \Sigma_c^{*+} K^{*+}$	1.60×10^{-16}	7.31×10^{-5}	$\Xi_{cc}^{++} \rightarrow \Sigma_c^{*+} K^+$	4.97×10^{-17}	2.27×10^{-5}
$\Xi_{cc}^{++} \rightarrow \Xi_c'^{*+} \pi^+$	2.23×10^{-14}	1.02×10^{-2}	$\Xi_{cc}^{++} \rightarrow \Xi_c'^{*+} \rho^+$	4.65×10^{-14}	2.12×10^{-2}
$\Xi_{cc}^{++} \rightarrow \Xi_c'^{*+} K^{*+}$	1.25×10^{-15}	5.70×10^{-4}	$\Xi_{cc}^{++} \rightarrow \Xi_c'^{*+} K^+$	6.95×10^{-16}	3.17×10^{-4}
$\Xi_{cc}^+ \rightarrow \Sigma_c^{*0} \pi^+$	2.32×10^{-15}	3.52×10^{-4}	$\Xi_{cc}^+ \rightarrow \Sigma_c^{*0} \rho^+$	7.57×10^{-15}	1.15×10^{-3}
$\Xi_{cc}^+ \rightarrow \Sigma_c^{*0} K^{*+}$	3.21×10^{-16}	4.87×10^{-5}	$\Xi_{cc}^+ \rightarrow \Sigma_c^{*0} K^+$	9.95×10^{-17}	1.51×10^{-5}
$\Xi_{cc}^+ \rightarrow \Xi_c'^{*0} \pi^+$	2.23×10^{-14}	3.39×10^{-3}	$\Xi_{cc}^+ \rightarrow \Xi_c'^{*0} \rho^+$	4.65×10^{-14}	7.07×10^{-3}
$\Xi_{cc}^+ \rightarrow \Xi_c'^{*0} K^{*+}$	1.25×10^{-15}	1.90×10^{-4}	$\Xi_{cc}^+ \rightarrow \Xi_c'^{*0} K^+$	6.95×10^{-16}	1.06×10^{-4}
$\Omega_{cc}^+ \rightarrow \Xi_c'^{*0} \pi^+$	1.10×10^{-15}	1.68×10^{-4}	$\Omega_{cc}^+ \rightarrow \Xi_c'^{*0} \rho^+$	3.64×10^{-15}	5.53×10^{-4}
$\Omega_{cc}^+ \rightarrow \Xi_c'^{*0} K^{*+}$	1.53×10^{-16}	2.32×10^{-5}	$\Omega_{cc}^+ \rightarrow \Xi_c'^{*0} K^+$	4.74×10^{-17}	7.20×10^{-6}
$\Omega_{cc}^+ \rightarrow \Omega_c^{*0} \pi^+$	4.25×10^{-14}	6.47×10^{-3}	$\Omega_{cc}^+ \rightarrow \Omega_c^{*0} \rho^+$	9.49×10^{-14}	1.44×10^{-2}
$\Omega_{cc}^+ \rightarrow \Omega_c^{*0} K^{*+}$	2.63×10^{-15}	4.00×10^{-4}	$\Omega_{cc}^+ \rightarrow \Omega_c^{*0} K^+$	1.36×10^{-15}	2.07×10^{-4}

$$\mathcal{B}(\Xi_{cc}^{++} \rightarrow \Xi_c'^{*+} \pi^+) = 1.02 \times 10^{-2}$$

$$\Xi_c'^{*+} \rightarrow \Xi_c^0 \pi^+$$

$$\Xi_c^0 \rightarrow \Xi^- \pi^+$$



Weak decays of doubly heavy baryons: the FCNC processes

Z. P. Xing and Z. X. Zhao, Phys.Rev. D98 (2018) no.5, 056002



- FCNC processes are considered to be an ideal place to the precise test of Standard Model and the search for new physics, while the discovery of the doubly heavy baryon provides us a new platform.
- With the accumulation of data, we are in an increasingly better position to study these semi-leptonic process.

The FCNC processes

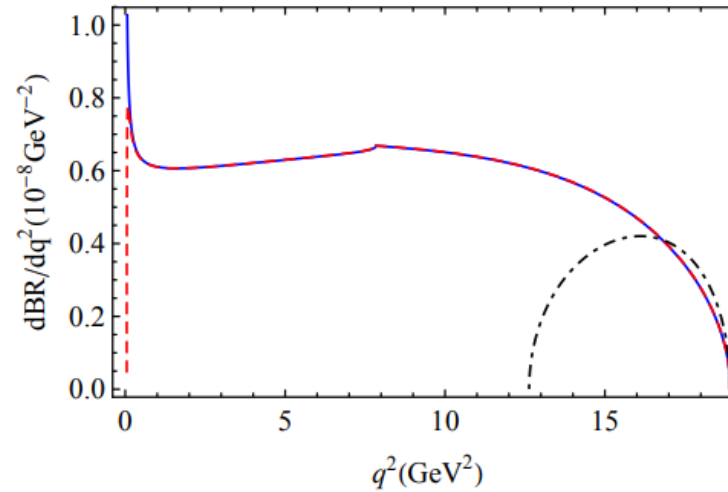


FIG. 3: $d\mathcal{B}/dq^2$ for $\Xi_b^0 \rightarrow \Xi_b^0 l^+ l^-$ with $l = e, \mu, \tau$. The blue solid line, the red dashed line and the black dot-dashed line correspond to the cases of $l = e, \mu, \tau$, respectively. Here the resonant contributions are not taken into account.

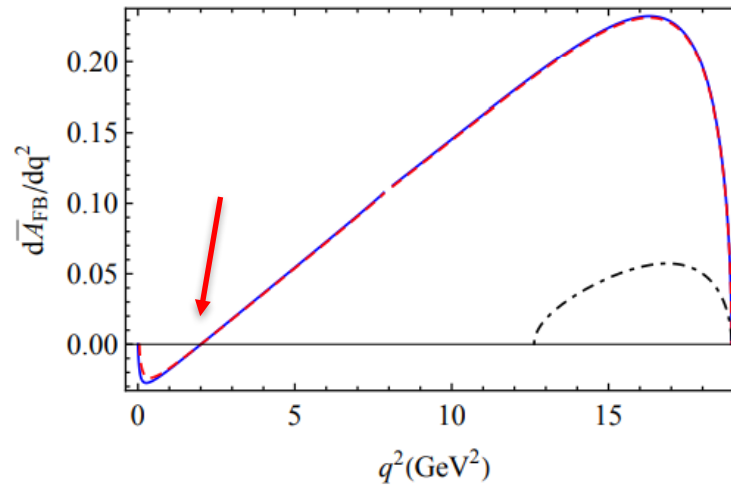


FIG. 4: Same as FIG. 3 but for $d\bar{A}_{FB}/dq^2$.



Zero-crossing points

TABLE XIX: Zero-crossing points of $d\bar{A}_{FB}/dq^2$ and \mathcal{R} defined in Eqs. (51) and (52) for $b \rightarrow s$ process with $l = e/\mu$.

channels	$s_0/ \text{ GeV}^2$	$\mathcal{R}(s_0)$	channels	$s_0/ \text{ GeV}^2$	$\mathcal{R}(s_0)$	channels	$s_0/ \text{ GeV}^2$	$\mathcal{R}(s_0)$
$\Xi_{bb}^0 \rightarrow \Xi_b^0 l^+ l^-$	2.01	0.30	$\Xi_{bc}^+ \rightarrow \Xi_c^+ l^+ l^-$	2.80	0.61	$\Xi_{bc}'^+ \rightarrow \Xi_c^+ l^+ l^-$	3.12	0.68
$\Xi_{bb}^- \rightarrow \Xi_b^- l^+ l^-$			$\Xi_{bc}^0 \rightarrow \Xi_c^0 l^+ l^-$			$\Xi_{bc}'^0 \rightarrow \Xi_c^0 l^+ l^-$		
$\Xi_{bb}^0 \rightarrow \Xi_b'^0 l^+ l^-$	2.88	0.43	$\Xi_{bc}^+ \rightarrow \Xi_c'^+ l^+ l^-$	3.02	0.66	$\Xi_{bc}'^+ \rightarrow \Xi_c'^+ l^+ l^-$	2.87	0.62
$\Xi_{bb}^- \rightarrow \Xi_b'^- l^+ l^-$			$\Xi_{bc}^0 \rightarrow \Xi_c'^0 l^+ l^-$			$\Xi_{bc}'^0 \rightarrow \Xi_c'^0 l^+ l^-$		
$\Omega_{bb}^- \rightarrow \Omega_b^- l^+ l^-$	2.88	0.42	$\Omega_{bc}^0 \rightarrow \Omega_c^0 l^+ l^-$	3.00	0.65	$\Omega_{bc}'^0 \rightarrow \Omega_c^0 l^+ l^-$	2.80	0.60

TABLE XX: Same as XIX but for $b \rightarrow d$ process.

channels	$s_0/ \text{ GeV}^2$	$\mathcal{R}(s_0)$	channels	$s_0/ \text{ GeV}^2$	$\mathcal{R}(s_0)$	channels	$s_0/ \text{ GeV}^2$	$\mathcal{R}(s_0)$
$\Xi_{bb}^0 \rightarrow \Lambda_b^0 l^+ l^-$	1.96	0.29	$\Xi_{bc}^+ \rightarrow \Lambda_c^+ l^+ l^-$	2.81	0.61	$\Xi_{bc}'^+ \rightarrow \Lambda_c^+ l^+ l^-$	3.09	0.67
$\Omega_{bb}^- \rightarrow \Xi_b^- l^+ l^-$	2.00		$\Omega_{bc}^0 \rightarrow \Xi_c^0 l^+ l^-$	2.77	0.60	$\Omega_{bc}'^0 \rightarrow \Xi_c^0 l^+ l^-$	3.11	
$\Xi_{bb}^0 \rightarrow \Sigma_b^0 l^+ l^-$	2.88	0.43	$\Xi_{bc}^+ \rightarrow \Sigma_c^+ l^+ l^-$	3.02	0.66	$\Xi_{bc}'^+ \rightarrow \Sigma_c^+ l^+ l^-$	2.91	0.63
$\Xi_{bb}^- \rightarrow \Sigma_b^- l^+ l^-$			$\Xi_{bc}^0 \rightarrow \Sigma_c^0 l^+ l^-$			$\Xi_{bc}'^0 \rightarrow \Sigma_c^0 l^+ l^-$		
$\Omega_{bb}^- \rightarrow \Xi_b'^- l^+ l^-$	2.88	0.42	$\Omega_{bc}^0 \rightarrow \Xi_c'^0 l^+ l^-$	3.01	0.65	$\Omega_{bc}'^0 \rightarrow \Xi_c'^0 l^+ l^-$	2.84	0.61

$$B \rightarrow K_J^* (\rightarrow K\pi) \mu^+ \mu^- \quad s_0 = (3.1 \pm 0.1) \text{ GeV}^2$$

C. D. Lu and W. Wang, Phys. Rev. D 85, 034014 (2012)



Weak decays of doubly heavy baryons: decay constants (with QCDSR method)

X. H. Hu, Y. L. Shen, W. Wang and Z. X. Zhao, Chin.Phys. C42 (2018) no.12, 123102



An indispensable input for the calculation of

- the form factors
- lifetime

$$\langle 0 | J_H | H(q, s) \rangle = \lambda_H u(q, s)$$

decay constant

“Decay constants”



Baryon	This work #1	This work #2	Ref. [41]	Ref. [42]	Ref. [55]	Experiment
Ξ_{cc}	3.68 ± 0.08	3.61 ± 0.09	4.26 ± 0.19	3.57 ± 0.14	$3.610 \pm 0.023 \pm 0.022$	3.6214 ± 0.0008
Ω_{cc}	3.75 ± 0.08	3.69 ± 0.09	4.25 ± 0.20	3.71 ± 0.14	$3.738 \pm 0.020 \pm 0.020$	--
Ξ_{bb}	10.16 ± 0.09	10.12 ± 0.10	9.78 ± 0.07	10.17 ± 0.14	$10.143 \pm 0.030 \pm 0.023$	--
Ω_{bb}	10.27 ± 0.09	10.19 ± 0.10	9.85 ± 0.07	10.32 ± 0.14	$10.273 \pm 0.027 \pm 0.020$	--
Ξ_{bc}	6.95 ± 0.09	6.89 ± 0.10	6.75 ± 0.05	--	$6.943 \pm 0.033 \pm 0.028$	--
Ω_{bc}	7.01 ± 0.09	6.95 ± 0.09	7.02 ± 0.08	--	$6.998 \pm 0.027 \pm 0.020$	--

Z.G.Wang, Eur.Phys.J.A45,267(2010)

Z. S. Brown, W. Detmold, S. Meinel and K. Orginos, Phys. Rev. D 90, no. 9, 094507 (2014)

Baryon	This work #1	This work #2	Ref. [42]
Ξ_{cc}	0.113 ± 0.029	0.109 ± 0.021	0.115 ± 0.027
Ω_{cc}	0.140 ± 0.033	0.123 ± 0.024	0.138 ± 0.030
Ξ_{bb}	0.303 ± 0.094	0.281 ± 0.071	0.252 ± 0.064
Ω_{bb}	0.404 ± 0.112	0.347 ± 0.083	0.311 ± 0.077
Ξ_{bc}	0.191 ± 0.053	0.176 ± 0.040	--
Ω_{bc}	0.217 ± 0.056	0.188 ± 0.041	--



Weak decays of doubly heavy baryons: the form factors (with QCDSR method)

Y. J. Shi, W. Wang, and Z. X. Zhao, arXiv:1811.xxxxx

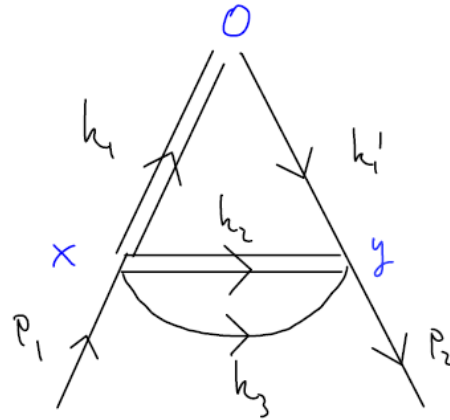
12 Dirac structures



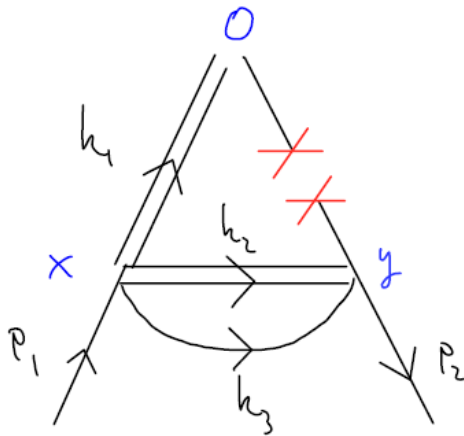
$$\Pi_{\mu} = \lambda_1 \lambda_2 \frac{(\not{p}_2 + M_2)(F_1 \frac{p_{1\mu}}{M_1} + F_2 \frac{p_{2\mu}}{M_2} + F_3 \gamma_{\mu})(\not{p}_1 + M_1)}{(p_1^2 - M_1^2)(p_2^2 - M_2^2)}$$

- 1 $\not{p}_2 p_{1\mu} \not{p}_1$
- 2 $\not{p}_2 p_{1\mu}$
- 3 $\not{p}_2 p_{2\mu} \not{p}_1$
- 4 $\not{p}_2 p_{1\mu}$
- 5 $\not{p}_2 \gamma_{\mu} \not{p}_1$
- 6 $\not{p}_2 \gamma_{\mu}$
- 7 $p_{1\mu} \not{p}_1$
- 8 $p_{1\mu}$
- 9 $p_{2\mu} \not{p}_1$
- 10 $p_{2\mu}$
- 11 $\gamma_{\mu} \not{p}_1$
- 12 γ_{μ}

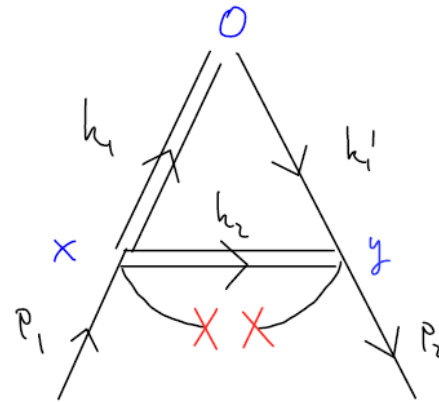
Dim-0 and dim-3



pert

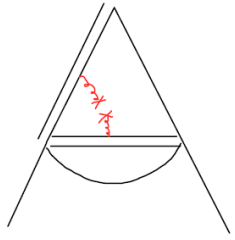


991

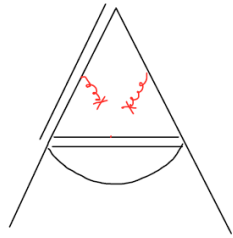


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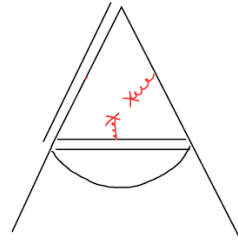
Dim-4



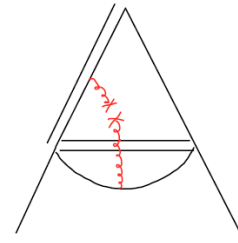
991



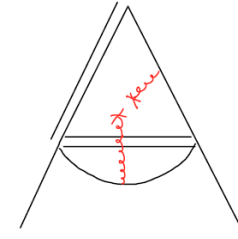
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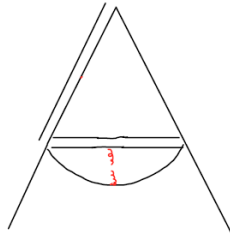
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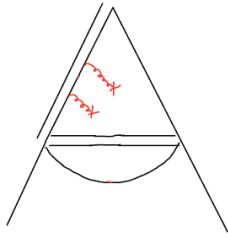
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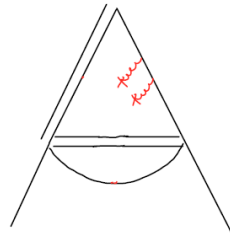
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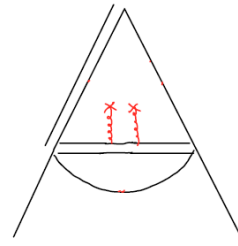
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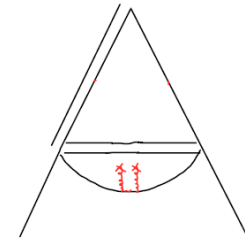
997



998

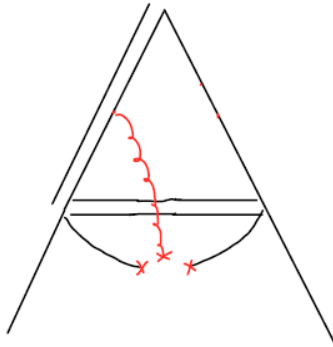


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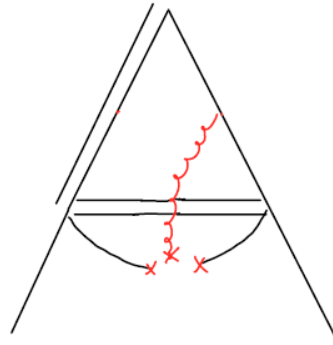


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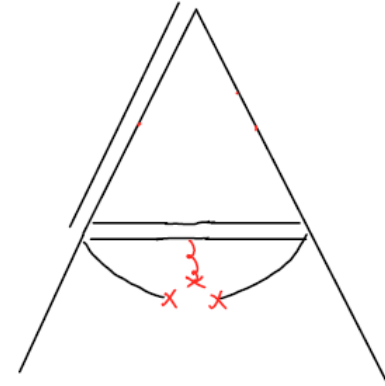
Dim-5



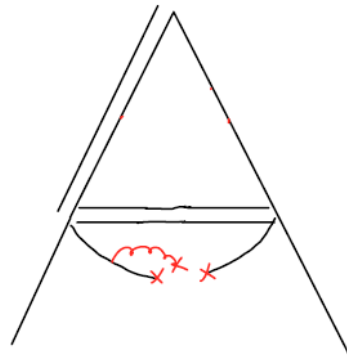
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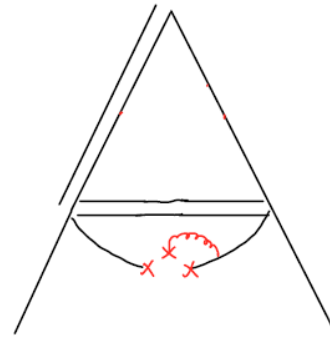
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9993

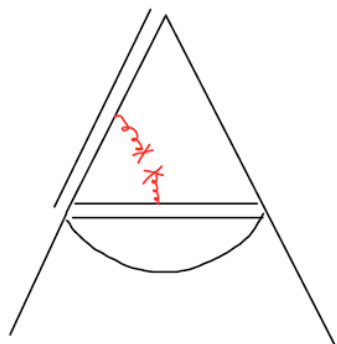


9994



9995

Feynman rules



gg1

$$\begin{aligned}
 &= 2\sqrt{2}i^2 \epsilon_{a'b'c'} \epsilon_{abc} \int \frac{d^4 k_2}{(2\pi)^4} \int \frac{d^4 k_3}{(2\pi)^4} \int \frac{d^4 u}{(2\pi)^4} \int \frac{d^4 v}{(2\pi)^4} \\
 &* \left[\gamma_{\nu'} \gamma_5 \right. \\
 &\quad \left(\frac{i}{\not{k}_2 + \not{p} - m_2} \delta_{c'j'} (ig \Gamma_{j'j}^b \gamma^\beta) \left(\frac{-i}{2} (2\pi)^4 \frac{\partial}{\partial v_\sigma} \delta^4(v) G_{\sigma\beta}^b(0) \right) \frac{i}{\not{k}_2 - m_2} \delta_{jb} \right) \\
 &\quad \gamma^\nu \\
 &\quad \left(\frac{i}{\not{p}_1 - \not{k}_2 - \not{k}_3 + m_1} \delta_{ia} (ig \Gamma_{i'i}^a \gamma^\alpha) \left(\frac{-i}{2} (2\pi)^4 \frac{\partial}{\partial u_\rho} \delta^4(u) G_{\rho\alpha}^a(0) \right) \frac{i}{\not{p}_1 - \not{k}_2 - \not{k}_3 + \not{p} + m_1} \delta_{a''i'} \right) \\
 &\quad \gamma_\mu \\
 &\quad \frac{i}{\not{p}_2 - \not{k}_2 - \not{k}_3 - \not{p} + m'_1} \delta_{b'a''} \\
 &\quad \gamma^{\nu'} \\
 &\quad \frac{i}{\not{k}_3 - m_3} \delta_{a'c} \\
 &\quad \left. \gamma_\nu \gamma_5 \right]
 \end{aligned}$$

1 term, 15 gamma's -> 2 terms, each with 19 gamma's

Contribution < 1%



Summary and outlook

Summary



- Weak decays of doubly heavy baryons: the $1/2 \rightarrow 1/2$ case
- Weak decays of doubly heavy baryons: the $1/2 \rightarrow 3/2$ case
- Weak decays of doubly heavy baryons: the FCNC processes
- Weak decays of doubly heavy baryons: decay constants
- Weak decays of doubly heavy baryons: the form factors



- lifetime ---- HQE + QCD sum rule

Phys. Rev. Lett. 121, 052002 (2018)

$\Xi_{cc}^{++}(\mathbf{ccu})$

$$0.256^{+0.024}_{-0.022} (\text{stat}) \pm 0.014 (\text{syst}) \text{ ps}$$

Phys. Rev. Lett. 121, 092003 (2018)

$\Omega_c^0(\mathbf{css})$

268 fs vs 69 fs

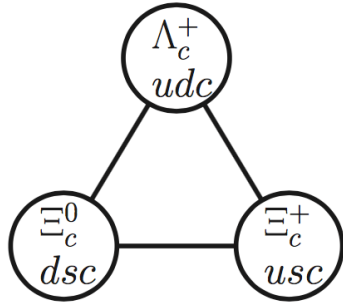


Thank you for your attention!

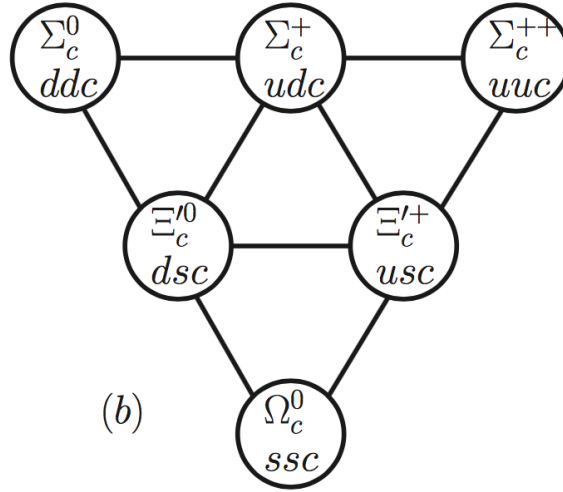


Backup

backup



(a)



(b)

The FCNC processes



$$\frac{d^2\Gamma}{dq^2 d\cos\theta} = \frac{|\vec{P}'||\vec{p}_1|}{16(2\pi)^3 M^2 \sqrt{q^2}} \overline{|\mathcal{M}|^2}$$

$$\overline{|\mathcal{M}|^2} = \frac{1}{2} |\lambda|^2 (I_0 + I_1 \cos\theta + I_2 \cos 2\theta)$$

$$\begin{aligned} I_0 = & (q^2 + 4m_l^2) (|H_{-\frac{1}{2},0}^{V,\frac{1}{2}}|^2 + |H_{\frac{1}{2},0}^{V,-\frac{1}{2}}|^2) + (\frac{3}{2}q^2 + 2m_l^2) (|H_{\frac{1}{2},1}^{V,\frac{1}{2}}|^2 + |H_{-\frac{1}{2},-1}^{V,-\frac{1}{2}}|^2) \\ & + (q^2 - 4m_l^2) (\frac{3}{2}|H_{\frac{1}{2},1}^{A,\frac{1}{2}}|^2 + \frac{3}{2}|H_{-\frac{1}{2},-1}^{A,-\frac{1}{2}}|^2 + |H_{-\frac{1}{2},0}^{A,\frac{1}{2}}|^2 + |H_{\frac{1}{2},0}^{A,-\frac{1}{2}}|^2) \\ & + 8m_l^2 (|H_{-\frac{1}{2},t}^{A,\frac{1}{2}}|^2 + |H_{\frac{1}{2},t}^{A,-\frac{1}{2}}|^2), \end{aligned}$$

$$I_1 = 4\sqrt{q^2(q^2 - 4m_l^2)} \text{Re}(H_{\frac{1}{2},1}^{A,\frac{1}{2}*} H_{\frac{1}{2},1}^{V,\frac{1}{2}} - H_{-\frac{1}{2},-1}^{A,-\frac{1}{2}*} H_{-\frac{1}{2},-1}^{V,-\frac{1}{2}}),$$

$$\begin{aligned} I_2 = & \frac{1}{2}(q^2 - 4m_l^2) (|H_{\frac{1}{2},1}^{V,\frac{1}{2}}|^2 + |H_{-\frac{1}{2},-1}^{V,-\frac{1}{2}}|^2 - 2|H_{-\frac{1}{2},0}^{V,\frac{1}{2}}|^2 - 2|H_{\frac{1}{2},0}^{V,-\frac{1}{2}}|^2 \\ & + |H_{\frac{1}{2},1}^{A,\frac{1}{2}}|^2 + |H_{-\frac{1}{2},-1}^{A,-\frac{1}{2}}|^2 - 2|H_{-\frac{1}{2},0}^{A,\frac{1}{2}}|^2 - 2|H_{\frac{1}{2},0}^{A,-\frac{1}{2}}|^2). \end{aligned} \quad 35$$

The FCNC processes



$$\begin{aligned} \frac{d\Gamma_L}{dq^2} = & |\lambda|^2 \frac{|\vec{P}'||\vec{p}_1|}{12(2\pi)^3 M^2 \sqrt{q^2}} \left\{ (q^2 + 2m_l^2)(|H_{-\frac{1}{2},0}^{V,\frac{1}{2}}|^2 + |H_{\frac{1}{2},0}^{V,-\frac{1}{2}}|^2) \right. \\ & + (q^2 - 4m_l^2)(|H_{-\frac{1}{2},0}^{A,\frac{1}{2}}|^2 + |H_{\frac{1}{2},0}^{A,-\frac{1}{2}}|^2) \\ & \left. + 6m_l^2(|H_{-\frac{1}{2},t}^{A,\frac{1}{2}}|^2 + |H_{\frac{1}{2},t}^{A,-\frac{1}{2}}|^2) \right\}, \end{aligned}$$

$$\begin{aligned} \frac{d\Gamma_T}{dq^2} = & |\lambda|^2 \frac{|\vec{P}'||\vec{p}_1|}{12(2\pi)^3 M^2 \sqrt{q^2}} \left\{ (q^2 + 2m_l^2)(|H_{\frac{1}{2},1}^{V,\frac{1}{2}}|^2 + |H_{-\frac{1}{2},-1}^{V,-\frac{1}{2}}|^2) \right. \\ & \left. + (q^2 - 4m_l^2)(|H_{\frac{1}{2},1}^{A,\frac{1}{2}}|^2 + |H_{-\frac{1}{2},-1}^{A,-\frac{1}{2}}|^2) \right\}. \end{aligned}$$

$$\frac{d\bar{A}_{FB}}{dq^2} \equiv \frac{(\int_0^1 - \int_{-1}^0) d \cos \theta \frac{d^2 \Gamma}{dq^2 d \cos \theta}}{(\int_0^1 + \int_{-1}^0) d \cos \theta \frac{d^2 \Gamma}{dq^2 d \cos \theta}}$$

$$\frac{d\bar{A}_{FB}}{dq^2} = \frac{I_1}{2(I_0 - I_2/3)}$$

“Decay constants”



$$J_{\Xi_{QQ}} = \epsilon_{abc} (Q_a^T C \gamma^\mu Q_b) \gamma_\mu \gamma_5 q_c,$$

$$J_{\Xi_{bc}} = \sqrt{2} \epsilon_{abc} (b_a^T C \gamma^\mu c_b) \gamma_\mu \gamma_5 q_c$$

V. Braun, R. J. Fries, N. Mahnke and E. Stein, Nucl. Phys. B 589, 381 (2000)



Sources of uncertainty

- Input parameters:

- quark masses

$$m_u = m_d = 0.25\text{GeV}, \quad m_s = 0.37\text{GeV}, \quad m_c = 1.4\text{GeV}, \quad m_b = 4.8\text{GeV}.$$

- diquark masses

$$m_{[ud]} = 0.50\text{GeV}, \quad m_{[us]} = m_{[ds]} = 0.60\text{GeV},$$

$$m_{\{uu\}} = m_{\{ud\}} = m_{\{dd\}} = 0.77\text{GeV}, \quad m_{\{us\}} = m_{\{ds\}} = 0.87\text{GeV}, \quad m_{\{ss\}} = 0.97\text{GeV}.$$

- shape parameters

$$\beta_{b[ud]} = 0.66\text{GeV}, \quad \beta_{b[us]} = \beta_{b[ds]} = 0.68\text{GeV}, \quad \beta_{b\{ss\}} = 0.78\text{GeV},$$

$$\beta_{c[ud]} = 0.56\text{GeV}, \quad \beta_{c[us]} = \beta_{c[ds]} = 0.58\text{GeV}, \quad \beta_{c\{ss\}} = 0.66\text{GeV},$$

$$\beta_{s[ud]} = 0.45\text{GeV}, \quad \beta_{s[us]} = \beta_{s[ds]} = 0.46\text{GeV},$$

$$\beta_{d[ud]} = 0.40\text{GeV}, \quad \beta_{d[us]} = \beta_{d[ds]} = 0.41\text{GeV}, \quad \beta_{d\{ss\}} = 0.44\text{GeV},$$

$$\beta_{u[ud]} = 0.40\text{GeV}, \quad \beta_{u[us]} = \beta_{u[ds]} = 0.41\text{GeV}, \quad \beta_{u\{ss\}} = 0.44\text{GeV}.$$



$$\Lambda_c^+ \rightarrow \Lambda$$

Varying the model parameters m_{di} , β_i and β_f by 10% respectively

$$\Gamma(\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e) = (5.36 \pm 0.03 \pm 0.10 \pm 0.07) \times 10^{-14},$$

$$\Gamma(\Lambda_c^+ \rightarrow \Lambda \pi^+) = (4.77 \pm 0.08 \pm 0.14 \pm 0.34) \times 10^{-14},$$

$$\Gamma(\Lambda_c^+ \rightarrow \Lambda \rho^+) = (1.39 \pm 0.01 \pm 0.02 \pm 0.02) \times 10^{-13},$$

$$\Gamma(\Lambda_c^+ \rightarrow \Lambda K^+) = (3.47 \pm 0.04 \pm 0.11 \pm 0.22) \times 10^{-15},$$

$$\Gamma(\Lambda_c^+ \rightarrow \Lambda K^{*+}) = (6.47 \pm 0.02 \pm 0.10 \pm 0.19) \times 10^{-15}.$$

Sources of uncertainty



- For non-leptonic process, we have only considered the external W-emission diagram
- Model hypothesis

