



Theoretical Overview of B Physics

→ personal perspectives ←

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Outline

Introduction

Theoretical tools for B physics

$B - \bar{B}$ mixings: $\Delta M_{s,d}$, $\Delta \Gamma_{s,d}$, $a_{fs}^{s,d}$

$B_{s,d} \rightarrow \mu^+ \mu^-$: powerful model killing

Semi-leptonic decays: $|V_{ub}|$, $|V_{cb}|$ and $R(D^{(*)})$

Exclusive $b \rightarrow s \ell^+ \ell^-$ decays: several anomalies

Non-leptonic decays: higher-order pert. corrs

Conclusion

Why B physics:

- **What is B physics:** properties, productions and decays of various hadrons containing at least one bottom quark;

$B_{u,d,s,c}$ mesons, Λ_b baryon

- **Why study B physics:** three main motivations;

Measure the SM parameters related to flavour;
Test of the CKM mechanism of flavor and CP violation;
Indirect probe or constrain on various New Physics;

complementary to EWP tests (@LEP)
and direct searches at high-energy
frontier (@ LHC, Tevatron);

operator product expansion;
various effective field theories;
factorization theorems;

Deepen our understanding of strong interactions
both the pert. and non-pert. aspects QCD.

Test and probe the internal hadronic structure
in B-hadron and its decay products.

theoretical and phenomenological
input for other hadron processes;

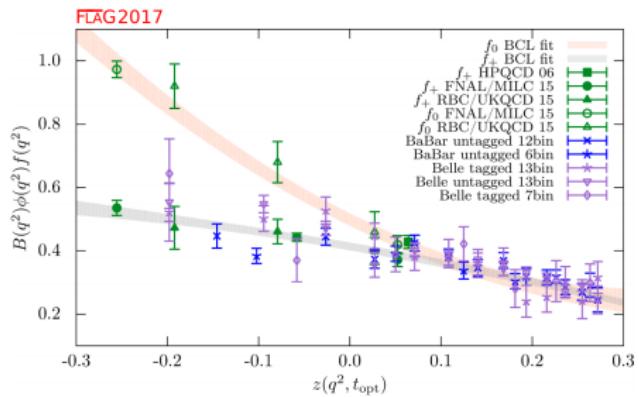
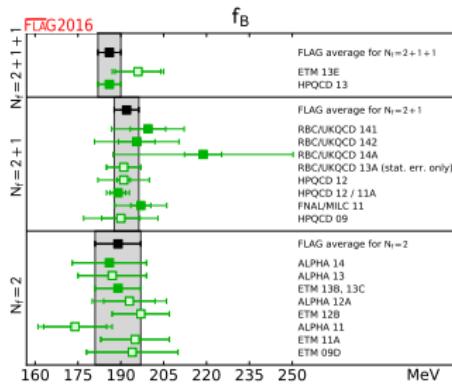
Dedicated B-physics experiments:

- ▶ **Past:** first observation of $B \rightarrow X_s \gamma$ by CLEO in 1994; continued by Tevatron @ Fermilab and the two B-factories: BaBar @ SLAC and Belle @ KEK with many key measurements; [*A. J. Bevan et al., "The Physics of the B Factories," 1406.6311*]
- ▶ **Current:** dedicated LHCb (also ATLAS and CMS) @ LHC with many exciting results; [*I. Bediaga et al., "Physics case for an LHCb Upgrade II - Opportunities in flavour physics, and beyond, in the HL-LHC era," arXiv:1808.08865*]
- ▶ **Future:** besides LHCb @ LHC, also Belle II @ SuperKEKB expected to start data taking in 2018, designed to find NP beyond the SM of particle physics; [<https://confluence.desy.de/display/Bl/B2TiP+WebHome>; 1808.10567]

± 5.4	± 49	± 10.0	± 2.6	± 90	LHCb Current
± 1.5		± 3.6	± 0.50	± 34	Belle II ATLAS/CMS LHCb 2025
± 1.5	± 14	± 2.2	± 0.72		
± 0.35	± 22	± 0.70	± 0.20	± 21	$\frac{B(B^0 \rightarrow \mu^+ \mu^-)}{B(B_s^0 \rightarrow \mu^+ \mu^-)}$ [%] HL-LHC
$\gamma [^\circ]$	$\phi_s [mrad]$	$R_K [\%]$	$R(D^*) [\%]$		

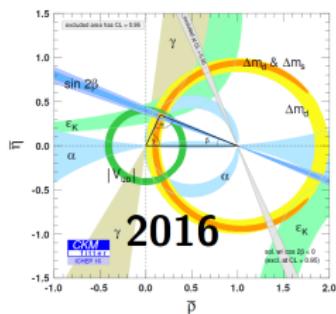
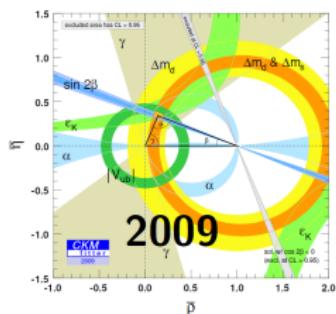
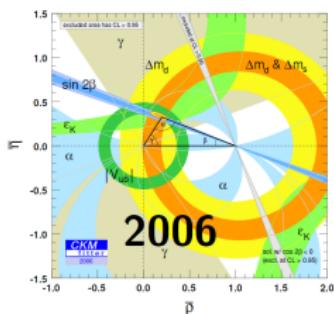
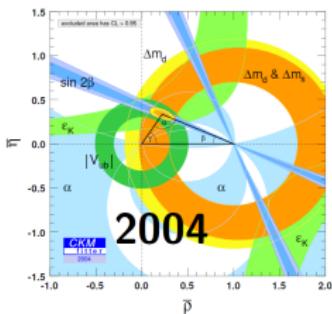
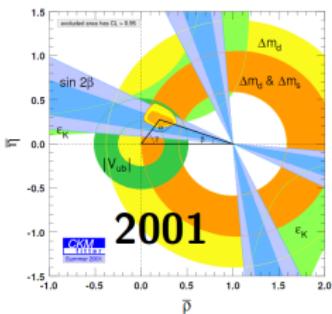
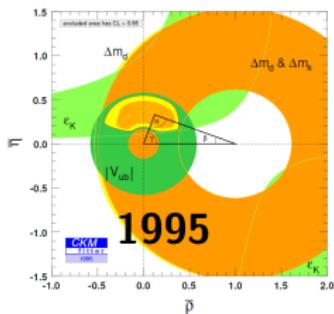
Theoretical tasks for B physics:

- Main task: try to improve the theory predictions to match the more and more precise exp. data;
- Many dynamical frameworks developed: HQET, SCET, NRQCD, QCDF, pQCD, ... \hookrightarrow based on QCD, and separate pert. from non-pert. strong interaction effects \leftrightarrow factorization theorem;
- For the non-pert. objects: mostly from Lattice QCD and LCSR, ...; [for reviews see: <http://flag.unibe.ch/>, and <https://hflav.web.cern.ch/>]



Current status of B physics:

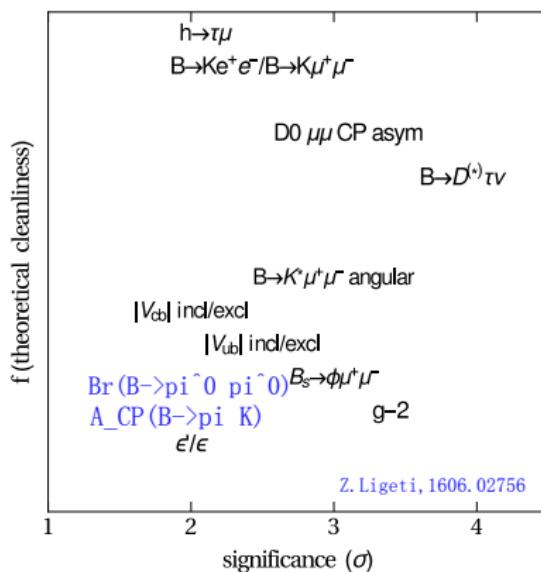
- The CKM mechanism of flavor & CP violation well established! \rightarrow 2008 Nobel Prize for Kobayashi and Maskawa;



- Information on UT from tree- and loop-level processes well consistent!

Current status of B physics:

- ▶ Remember: $\mathcal{O}(20\%)$ NP contributions to most FCNC processes still allowed by the current data;
- ▶ Several intriguing tensions/anomalies do observed in flavour physics, might be any BSM signals?



- + all of them not yet conclusive: theo. uncertainties or exp. fluctuations?
- + except for theo. cleanest modes, more cross-checks needed;
- + exp. measurements of related observables needed;
- + indep. theory and lattice calculations needed;

How to describe B-hadron weak decays:

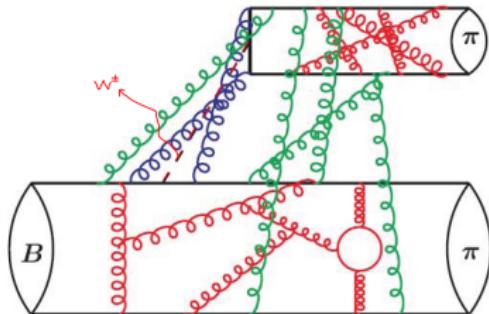
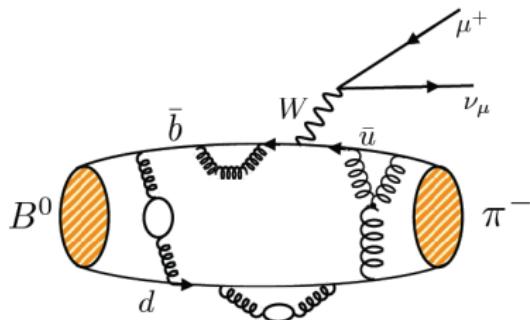
- At the quark level: B-hadron weak decays mediated by weak charged-current J_{cc}^μ coupled to W^\pm ;

$$\mathcal{L}_{cc} = -\frac{g_2}{\sqrt{2}} J_{cc}^\mu W_\mu^\dagger + \text{h.c.}, \quad J_{cc}^\mu = (\bar{u}_L, \bar{c}_L, \bar{t}_L) \gamma^\mu V_{\text{CKM}} \begin{pmatrix} d_L \\ s_L \\ b_L \end{pmatrix}$$

↪ V_{CKM} : describes flavor violation, and very predictive, especially for CPV!

- In the real world: no free quarks due to confinement; quarks always confined inside hadrons through soft-gluon exchanges;

↪ In B physics, simple weak decays overshadowed by complex strong interactions!



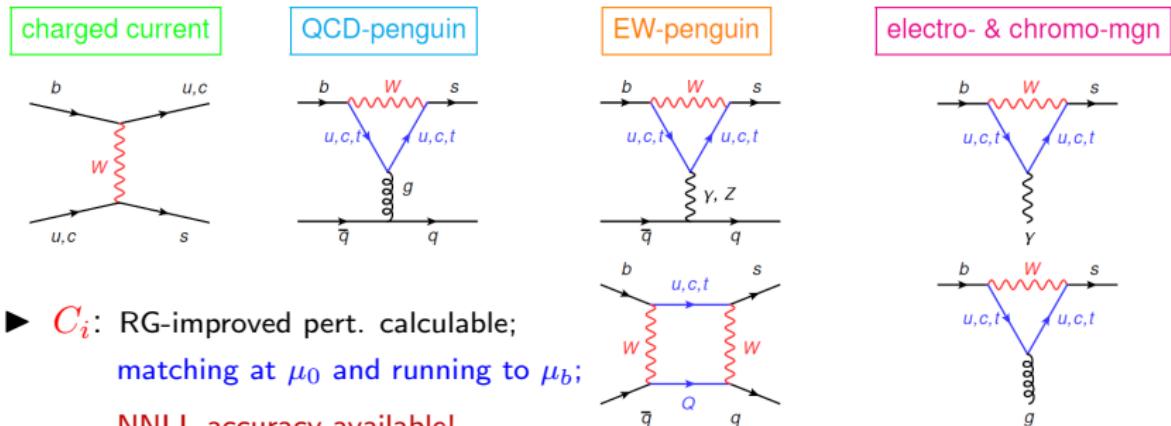
Typical features for B-hadron weak decays:

- A typical multi-scale problem and scales are highly hierarchical;

$$\begin{array}{lclclcl} \text{EW interaction scale} & \gg & \text{ext. mom'a in B rest frame} & \gg & \text{QCD-bound state effects} \\ m_W \sim 80.4 \text{ GeV} & \gg & m_b \sim 4.8 \text{ GeV} & \gg & \Lambda_{\text{QCD}} \sim 1 \text{ GeV} \end{array}$$

- Starting point \mathcal{L}_{eff} : integrate out heavy d.o.f. ($m_{W,Z,t} \gg m_b$), physics above (below) $\mu \sim m_b$ contained in C_i ($\langle \mathcal{O}_i \rangle$); [A. J. Buras, 1102.5650]

$$\mathcal{L}_{\text{eff}} \sim G_F V_{\text{CKM}} \times \left[\sum_{p=u,c} \sum_{i=1,2} C_i \mathcal{O}_i^p + \sum_{3,\dots,6} C_i \mathcal{O}_i + \sum_{7,\dots,10} C_i \mathcal{O}_i + \sum_{7\gamma,8g} C_i \mathcal{O}_i \right]$$



Hadronic matrix elements for B-hadron weak decays:

- How to evaluate $\langle f | \mathcal{O}_i | B \rangle$: $\langle 0 | \mathcal{O}_i | B \rangle$, $\langle \pi | \mathcal{O}_i | B \rangle$, $\langle \pi\pi | \mathcal{O}_i | B \rangle$, $\langle \bar{B} | \mathcal{O}_i | B \rangle$,

⋮

Quark-hadron duality,
Heavy-quark mass expansion,
HQE, OPE,
...

Effective theories,
Factorization,
Approximate symmetries
Lattice QCD, LCSR, ...

Inclusive decays

$$B \rightarrow X_s \gamma, B \rightarrow X_s \ell^+ \ell^-$$

$$B \rightarrow X_u \ell \nu, B \rightarrow X_c \ell \nu$$

Exclusive decays

$$B_s \rightarrow \mu^+ \mu^- \rightarrow \langle 0 | \mathcal{O} | B_s \rangle$$

$$B - \bar{B} \text{ mixing} \rightarrow \langle B | \mathcal{O} | \bar{B} \rangle$$

$$B \rightarrow \pi l \nu \rightarrow \langle \pi | \mathcal{O} | B \rangle$$

$$B \rightarrow \pi \pi \rightarrow \langle \pi\pi | \mathcal{O} | B \rangle$$

Increasingly difficult

- $\langle M_1 M_2 | \mathcal{O}_i | B \rangle$: not yet possible in lattice QCD; expressed in terms of (few) universal non-pert. hadronic quantities with pert. calculable coefficients;

- dynamical approaches based on factorization theorems: PQCD, QCDF, SCET, ⋮;

[Keum, Li, Sanda, Lü, Yang '00;

Beneke, Buchalla, Neubert, Sachrajda, '00;

Bauer, Flemming, Pirjol, Stewart, '01]

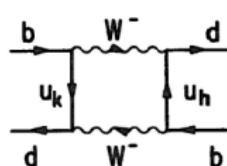
- (approximate) symmetries of QCD: Isospin, U-Spin, V-Spin, and flavor SU(3) symmetries, ⋮;

[Zeppenfeld, '81;

London, Gronau, Rosner, Chiang, Cheng et al.]

$B - \bar{B}$ mixings:

- **Motivation:** strongly suppressed in SM; highly sensitive to BSM effects;



$$\text{SM: } \frac{C_{\text{SM}}}{m_W^2}$$



$$\text{NP: } \frac{C_{\text{NP}}}{\Lambda^2}$$

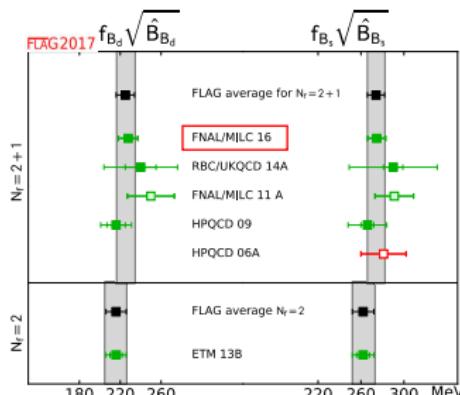
General parametrization:

$$M_{12} = M_{12}^{\text{SM}} \times (1 + h e^{2i\sigma})$$

↑
NP parameters

$$\hookrightarrow \boxed{\Lambda \geq 10^3 \text{ TeV}}$$

- $\Delta M_{s,d} \doteq 2|M_{12}^{s,d}|$: calculated from box diagrams with internal virtual particles; main uncertainty from Bag parameters $\langle B_q | \mathcal{O}_i | \bar{B}_q \rangle \propto f_{B_q}^2 B_q^{(i)}$;



$$\Delta M_d^{\text{SM}} = (0.53^{+0.03}_{-0.04}) \text{ ps}^{-1}$$

$$\Delta M_d^{\text{HFAG}} = (0.5065 \pm 0.0019) \text{ ps}^{-1}$$

$$\Delta M_s^{\text{SM}} = (18.1^{+1.1}_{-1.2}) \text{ ps}^{-1}$$

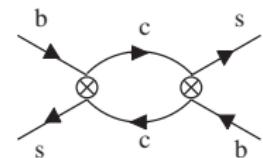
$$\Delta M_s^{\text{HFAG}} = (17.757 \pm 0.021) \text{ ps}^{-1}$$

[Kirk, Lenz and Rauh, 1711.02100;
T. Rauh, talk given at CKM2018]

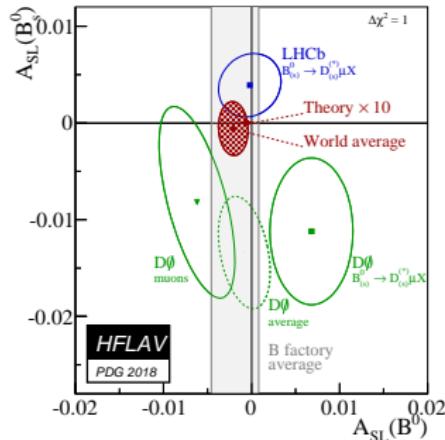
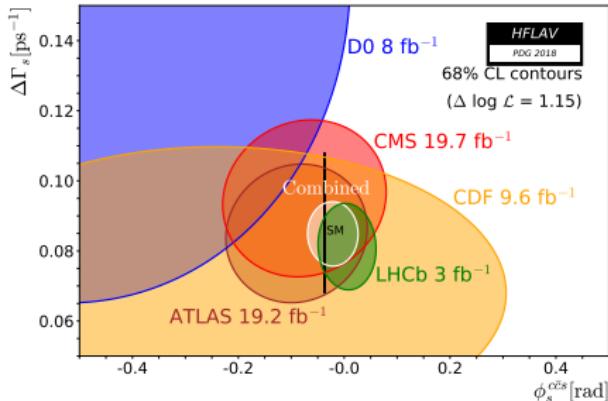
$B - \bar{B}$ mixings:

- $\Delta\Gamma_{s,d} \doteq 2|\Gamma_{12}^{s,d}| \cos \phi_{12}^{s,d}$: arise from absorptive part of box diagrams, dominated by tree-level $b \rightarrow c\bar{s}(d)$ transitions; [Artuso/Borissov/Lenz, 1511.09466]

$$\begin{aligned}\Gamma_{12}^s &= \frac{\Lambda^3}{m_b^3} \left[\Gamma_3^{s,(0)} + \frac{\alpha_s}{4\pi} \Gamma_3^{s,(1)} + \left(\frac{\alpha_s}{4\pi} \right)^2 \Gamma_3^{s,(2)} + \dots \right] \\ &\quad + \frac{\Lambda^4}{m_b^4} \left(\Gamma_4^{s,(0)} + \dots \right) + \dots \text{[H. M. Asatrian et al, 1709.02160]}\end{aligned}$$

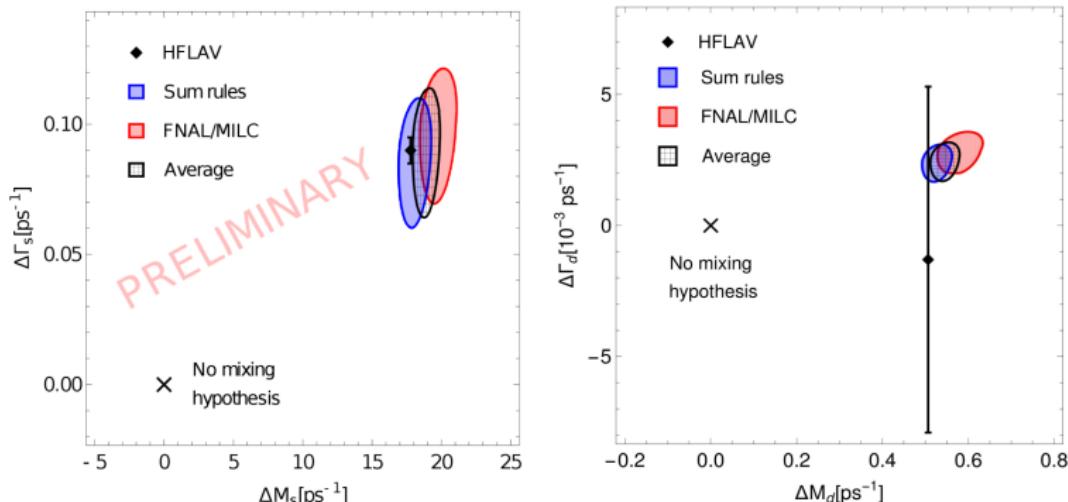


- $a_{fs}^{s,d} \doteq \left| \frac{\Gamma_{12}^{s,d}}{M_{12}^{s,d}} \right| \sin \phi_{12}^{s,d}$: motivated by 2013 D0 dimuon charge asymmetry!



$B - \bar{B}$ mixing:

- $\Delta M_{s,d}$ vs $\Delta\Gamma_{s,d}$: state-of-the-art comparison; [Kirk, Lenz and Rauh, 1711.02100; T. Rauh, talk given at CKM2018]



- SM predictions and exp. averages consistent with each other!

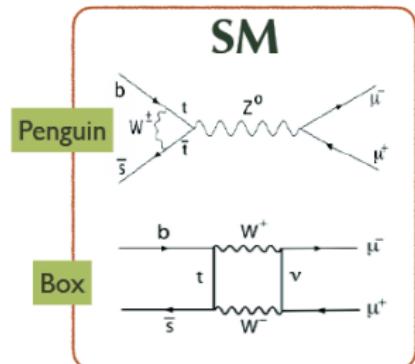
↪ Large NP effect in $B_{s,d}$ mixings now closed!

$B_{s,d} \rightarrow \mu^+ \mu^-$:

- Facts about $B_{s,d} \rightarrow \mu^+ \mu^-$: highly suppressed within the SM;

- helicity suppressed, by a factor of $(m_\mu/m_B)^2$;
- FCNC process, forbidden at tree-level, proceed only via loop diagrams;
- CKM suppressed by $|V_{tb} V_{ts}^*|^2$;

↪ very sensitive to NP, especially from $\mathcal{O}_{S(P)}$;



- Theory status: C_A now to NNLO QCD + NLO EW; enhanced EM correction included; [Bobeth et al., 1311.0903; Beneke, Bobeth and Szafron, 1708.09152]

$$\mathcal{H}_{\text{eff}} = -\frac{G_F \alpha}{\sqrt{2}\pi s_W^2} \left[V_{tb} V_{tq}^* \sum_i^{A,S,P} (C_i \mathcal{O}_i + C'_i \mathcal{O}'_i) + \text{h.c.} \right]$$

$$\mathcal{O}_A = (\bar{q} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \gamma_5 \ell), \quad \mathcal{O}_{S(P)} = m_b (\bar{q} P_R b) [\bar{\ell} (\gamma_5) \ell]$$

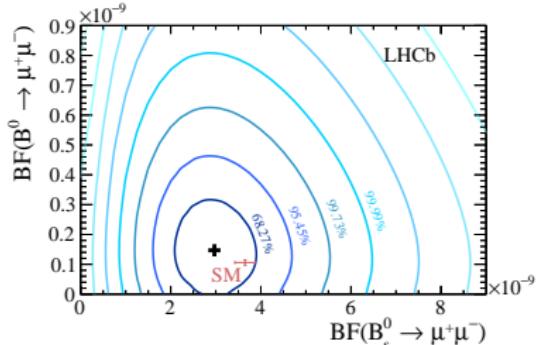
$$\bar{\mathcal{B}}(B_s \rightarrow \mu^+ \mu^-) = (3.57 \pm 0.17) \times 10^{-9}, \quad \bar{\mathcal{B}}(B_d \rightarrow \mu^+ \mu^-) = (1.06 \pm 0.09) \times 10^{-10}$$

$B_{s,d} \rightarrow \mu^+ \mu^-$:

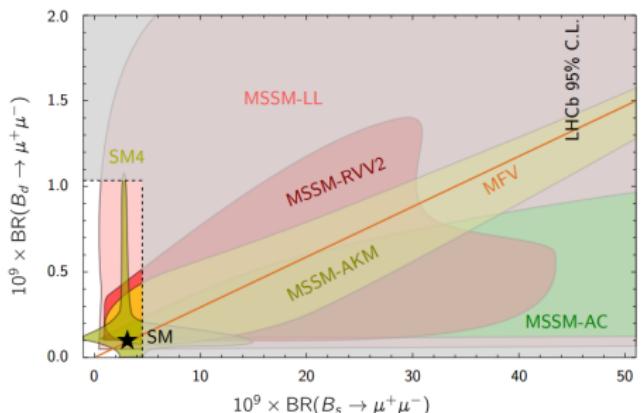
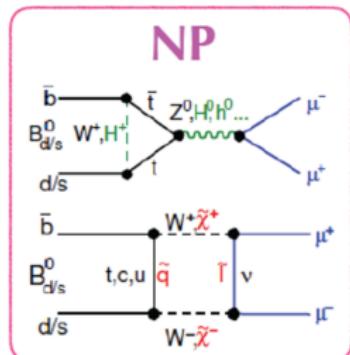
- CMS + LHCb and LHCb updated results: [1411.4413, 1703.05747]

$$\bar{\mathcal{B}}(B_s \rightarrow \mu^+ \mu^-) = (3.0 \pm 0.6^{+0.3}_{-0.2}) \cdot 10^{-9} \text{ (7.8\sigma);}$$

$$\bar{\mathcal{B}}(B_d \rightarrow \mu^+ \mu^-) = (3.9^{+1.6}_{-1.4}) \cdot 10^{-10} \text{ (3.0\sigma);}$$



- Powerful in model killing: good consistency between SM and exp. data; [D. Straub, 1205.6094]



$B_{s,d} \rightarrow \mu^+ \mu^-$:

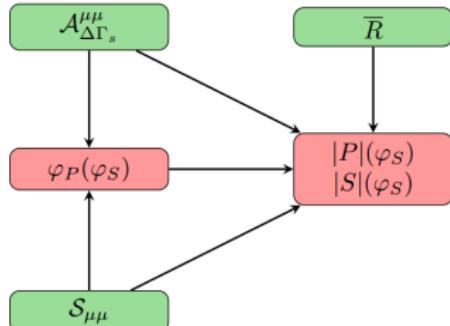
- Time-dependent observables: due to sizeable $\Delta\Gamma_s$; [De Bruyn et al., 1204.1737; Fleischer et al., 1703.10160; 1709.04735]

$$\mathcal{C}_{\mu\mu}^\lambda \equiv \frac{1 - |\xi_\lambda|^2}{1 + |\xi_\lambda|^2} = -\eta_\lambda \left[\frac{2|PS| \cos(\varphi_P - \varphi_S)}{|P|^2 + |S|^2} \right] \equiv -\eta_\lambda \mathcal{C}_{\mu\mu}$$

$$S_{\mu\mu}^\lambda \equiv \frac{2 \Im(\xi_\lambda)}{1 + |\xi_\lambda|^2} = \frac{|P|^2 \sin(2\varphi_P - \phi_s^{\text{NP}}) - |S|^2 \sin(2\varphi_S - \phi_s^{\text{NP}})}{|P|^2 + |S|^2} \equiv S_{\mu\mu}$$

$$A_{\Delta\Gamma_s}^{\mu\mu,\lambda} \equiv \frac{2 \Re(\xi_\lambda)}{1 + |\xi_\lambda|^2} = \frac{|P_{\mu\mu}|^2 \cos(2\varphi_P^{\mu\mu} - \phi_s^{\text{NP}}) - |S_{\mu\mu}|^2 \cos(2\varphi_S^{\mu\mu} - \phi_s^{\text{NP}})}{|P_{\mu\mu}|^2 + |S_{\mu\mu}|^2}$$

- With the updated LHC: these observables provide new d.o.f. for NP searches; [Fleischer, Jaarsma, Tetlalmatzi-Xolocotzi, 1703.10160; 1709.04735]



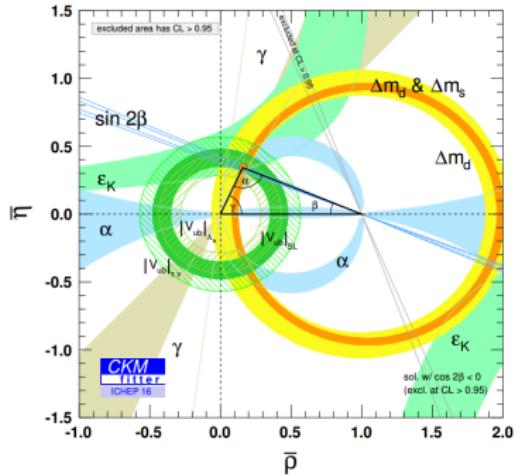
$$P_{\ell\ell} \equiv \frac{C_{10}^{\ell\ell} - C_{10}^{\ell\ell'}}{C_{10}^{\text{SM}}} + \frac{M_{B_s}^2}{2 \textcolor{red}{m}_\ell} \left(\frac{m_b}{m_b + m_s} \right) \left[\frac{C_P^{\ell\ell} - C_P^{\ell\ell'}}{C_{10}^{\text{SM}}} \right]$$

$$S_{\ell\ell} \equiv \sqrt{1 - 4 \frac{m_\ell^2}{M_{B_s}^2} \frac{M_{B_s}^2}{2 \textcolor{red}{m}_\ell} \left(\frac{m_b}{m_b + m_s} \right) \left[\frac{C_S^{\ell\ell} - C_S^{\ell\ell'}}{C_{10}^{\text{SM}}} \right]}$$

$|V_{ub}|$ and $|V_{cb}|$ problem:

- Importance of $|V_{xb}|$: play a key role in determining the apex of UT;

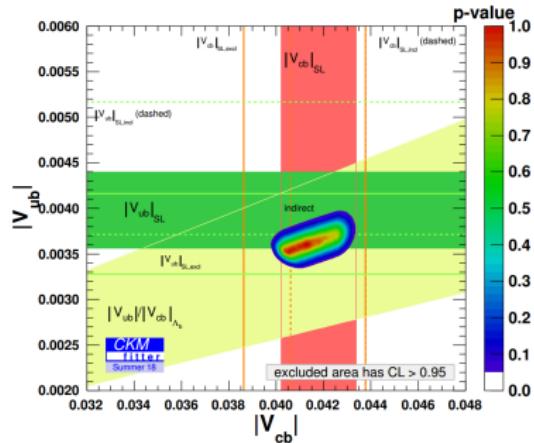
- $|V_{ub}|$ or $|V_{ub}/V_{cb}|$ constraints directly the UT;
 - $b \rightarrow s$ induced FCNC processes $\propto |V_{tb}V_{ts}^*|^2 \simeq |V_{cb}|^2 [1 + \mathcal{O}(\lambda^2)]$;
 - $\epsilon_K \simeq x|V_{cb}|^2 + \dots$;
- ↳ More precise determination of $|V_{xb}|$ is of utmost importance!



- Incl. vs excl. methods: [Nandi, Gambino, Tackmann, talks at CKM 2016]
 - Inclusive $|V_{cb}|$: OPE/HQE, dominated by theory uncertainties, especially by correlations of theoretical parameters;
 - Inclusive $|V_{ub}|$: OPE/HQE, limited knowledge of leading and subleading SFs;
 - Exclusive $|V_{xb}|$: how precise can the form factors be calculated by LQCD or LCSR;

$|V_{ub}|$ and $|V_{cb}|$ problem:

- Status of global fit for $|V_{xb}|$: [Gambino, Silva, Bona, talks at CKM2018]



- Results for CKM2018:

[Silva, Bona, talks at CKM2018]

$$|V_{cb}|_{\text{incl.}} = (42.2 \pm 0.4 \pm 0.6) \cdot 10^{-3},$$

$$|V_{ub}|_{\text{incl.}} = (4.44 \pm 0.17 \pm 0.31) \cdot 10^{-3}$$

$$|V_{cb}|_{\text{excl.}} = (41.2 \pm 0.6 \pm 0.9 \pm 0.2) \cdot 10^{-3},$$

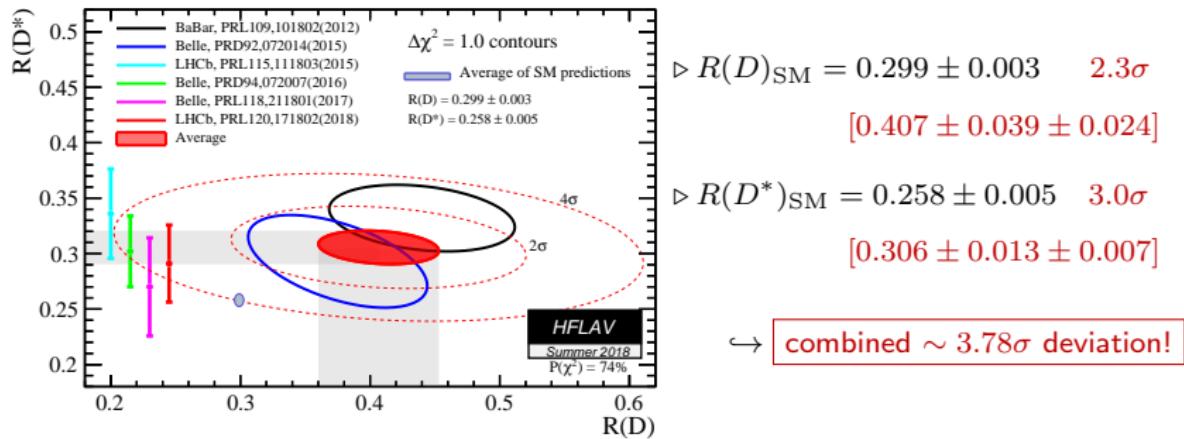
$$|V_{ub}|_{\text{excl.}} = (3.72 \pm 0.09 \pm 0.22) \cdot 10^{-3}$$

→ $|V_{xb}|$ tension significantly reduced, especially for $|V_{cb}|$!

→ global fit favours $|V_{ub}|_{\text{excl.}}$ & $|V_{cb}|_{\text{incl.}}$!

$R(D)$ and $R(D^*)$ anomalies:

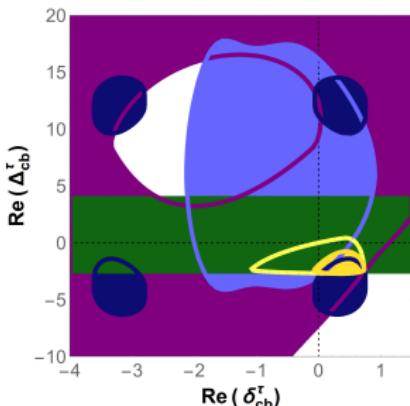
- $B \rightarrow D^{(*)}\tau\bar{\nu}$ decays: tree-level processes; massive τ makes them sensitive to tree-level NP like RH currents, charged Higgs, leptoquarks, ...;
- Current status: $R(D^{(*)}) = \frac{\text{Br}(B \rightarrow D^{(*)}\tau\bar{\nu}_\tau)}{\text{Br}(B \rightarrow D^{(*)}\ell\bar{\nu}_\ell)}$; [BaBar, 1205.5442, 1303.0571; Belle, 1507.03233, 1607.07923, 1612.00529; LHCb, 1506.08614, 1708.08856]



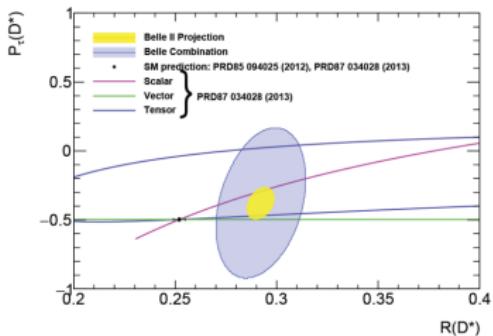
- Theo.: more precise lattice calculations for $B \rightarrow D^{(*)}$ FFs at non-zero recoil!
- Exp.: $A_\lambda^{D^{(*)}}$, $R_L^{D^*}$, $\Lambda_b \rightarrow \Lambda_c \tau \bar{\nu}$, $B_s \rightarrow D_s^{(*)} \tau \bar{\nu}$, $B_c \rightarrow J/\Psi(\eta_c) \tau \bar{\nu}$, $B \rightarrow X_c \tau \bar{\nu}$;

$R(D)$ and $R(D^*)$ anomalies:

- Importance of other observables: [Celis, Jung, Li, Pich, 1612.07757]



$$\delta_{cb}^\ell \equiv \frac{(g_L^{cb\ell} + g_R^{cb\ell})(m_B - m_D)^2}{m_\ell (\tilde{m}_b - \tilde{m}_c)}, \quad \Delta_{cb}^\ell \equiv \frac{(g_L^{cb\ell} - g_R^{cb\ell})m_B^2}{m_\ell (\tilde{m}_b + \tilde{m}_c)},$$



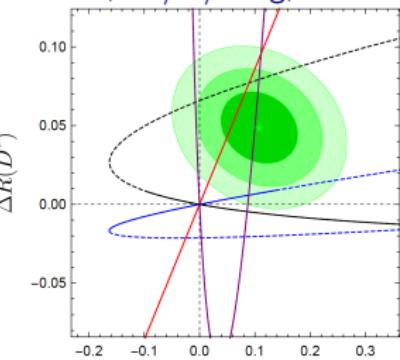
- B_c -lifetime constraint: [Li/Yang/Zhang, 1605.09308; Hu/Li/Yang, 1810.04939]

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}}^{(4)} + \frac{1}{\Lambda^2} \sum_i C_i(\Lambda) Q_i,$$

$$Q_{lq}^{(3)} = (\bar{l}\gamma_\mu \tau^I l)(\bar{q}\gamma^\mu \tau^I q), \quad Q_{lequ}^{(1)} = (\bar{l}^j e)\varepsilon_{jk}(\bar{q}^k u)$$

$$Q_{ledq} = (\bar{l}^j e)(\bar{d}q^j), \quad Q_{lequ}^{(3)} = (\bar{l}^j \sigma_{\mu\nu} e)\varepsilon_{jk}(\bar{q}^k \sigma^{\mu\nu} u)$$

→ **$V - A$ and/or tensor Lorentz structure needed!**



$R(D)$ and $R(D^*)$ anomalies:

- The observed tension is model independent: **exclusive already over-saturates inclusive**; [M. Freytsis, Z. Ligeti, J. Ruderman, 1506.08896]

- ▷ The data on $R(D)$ and $R(D^*)$ imply:

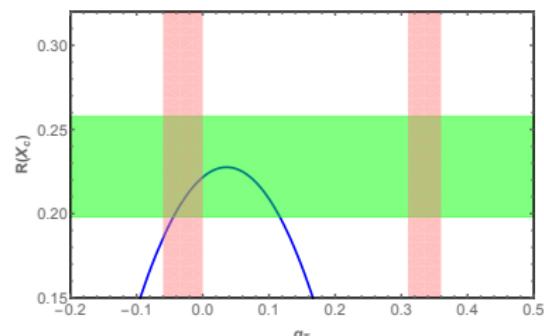
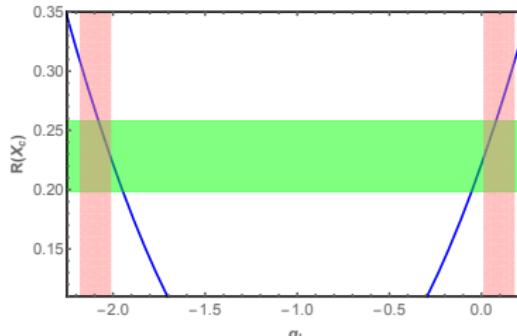
$$\text{Br}(\bar{B} \rightarrow D^* \tau \bar{\nu}) + \text{Br}(\bar{B} \rightarrow D \tau \bar{\nu}) = (2.78 \pm 0.25)\%$$

- ▷ Including the four lightest orbitally excited D meson states:

$$\text{Br}(\bar{B} \rightarrow D^{(*)} \tau \bar{\nu}) + \text{Br}(\bar{B} \rightarrow D^{**} \tau \bar{\nu}) \sim 3\%$$

- ▷ From $\text{inclusive} = \sum \text{exclusive}$: $\text{Br}(b \rightarrow X_c \tau \bar{\nu}) = (2.35 \pm 0.23)\%$ (LEP)

- $R(X_c)$ constraint: [Kamali/Rashed/Datta, 1801.08259; Lai/Li/Li/Yang, w.i.p.]

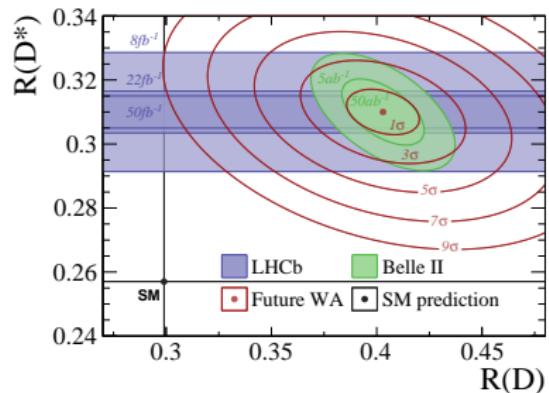
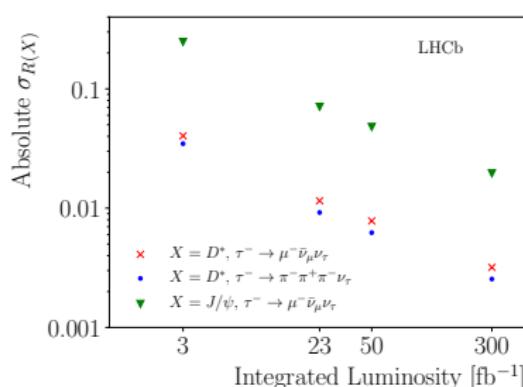


$R(D)$ and $R(D^*)$ anomalies:

- Another hint of LFUV: around 1.7σ above SM; [LHCb, 1711.05623; Cohen/Lamm/Lebed, 1807.02730; Wang/Zhu, 1808.10830]

$$R(J/\psi) = \frac{\text{Br}(B_c \rightarrow J/\psi \tau \nu_\tau)}{\text{Br}(B_c \rightarrow J/\psi \ell \nu_\ell)} = 0.71 \pm 0.17 \pm 0.18 \quad \text{vs} \quad 0.20 \sim 0.39 \text{ (theo.)}$$

- Future prospects with Belle-II and LHCb very promising! [Albrecht et al., 1709.10308; I. Bediaga et al., 1808.08865]

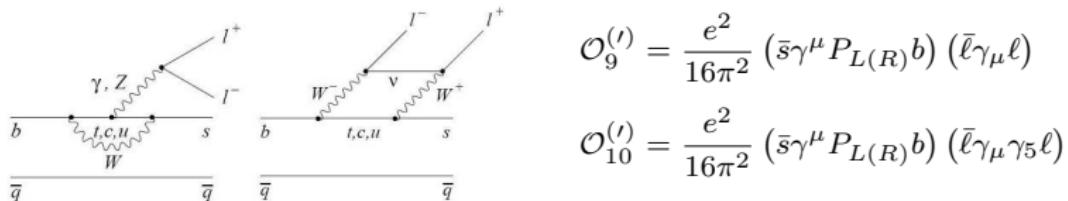


- Maybe the first tantalizing hint for BSM? Let's stay tuned!

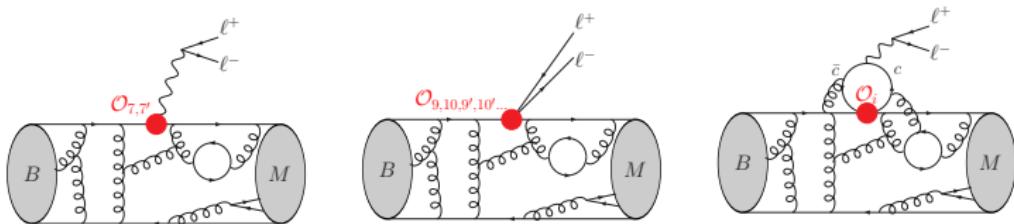
Exclusive $b \rightarrow s\ell^+\ell^-$ decays:

- \mathcal{H}_{eff} for $b \rightarrow s\ell^+\ell^-$: [Bobeth, Gambino, Gorbahn, Haisch, hep-ph/0312090]

$$\mathcal{H}_{\text{eff}}^{b \rightarrow s} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_i (C_i O_i + C'_i O'_i), \quad O_7^{(\prime)} = \frac{e}{16\pi^2} \bar{m}_b (\bar{s} \sigma^{\mu\nu} P_{R(L)} b) F_{\mu\nu}$$



- Amplitudes for exclusive decays: [Descotes-Genon, talk at FPCP 2016; Bobeth, Chrzaszcz, Dyk, and Virto, arXiv:1707.07305]



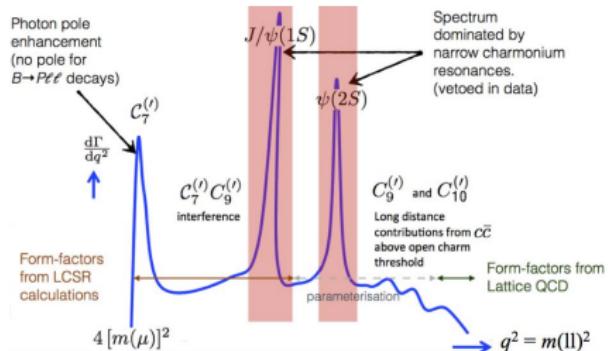
$$\mathcal{A}_\lambda^{(\ell) L, R} = \mathcal{N}_\lambda^{(\ell)} \left\{ (C_9^{(\ell)} \mp C_{10}^{(\ell)}) \mathcal{F}_\lambda(q^2) + \frac{2m_b M_B}{q^2} [C_7^{(\ell)} \mathcal{F}_\lambda^T(q^2) - 16\pi^2 \frac{M_B}{m_b} \mathcal{H}_\lambda(q^2)] \right\}$$

Exclusive $b \rightarrow s\ell^+\ell^-$ decays:

- Hadronic matrix elements of \mathcal{O}_i : [Beneke/Feldmann/Seidel, 0106067, 0412400; Grinstein/Pirjol, hep-ph/0404250; Beylich/Buchalla/Feldmann, 1101.5118]

† Large recoil (low- q^2)

- very low- q^2 ($\leq 1 \text{ GeV}^2$) dominated by \mathcal{O}_7 ;
- low- q^2 ($[1, 6] \text{ GeV}^2$) dominated by $\mathcal{O}_{9,10}$;
- QCDF or SCET, LCSR;



† Small recoil (high- q^2)

- dominated by $\mathcal{O}_{9,10}$;
- local OPE + HQET;

- Key issues: how large of power corrs from $b \rightarrow scc \rightarrow s\ell^+\ell^-$ for $q^2 \leq 6 \text{ GeV}^2$ and from fact. FF terms? [Descotes-Genon et al., 1510.04239]

$$\begin{aligned}
 h_\lambda(q^2) &= \frac{\epsilon_\mu^*(\lambda)}{m_B^2} \int d^4x e^{i\vec{q}\cdot\vec{x}} \left\langle K_\lambda^{(*)} \left| T \left\{ j_\mu^{\text{em}}(x), \sum_i C_i \mathcal{O}_i(0) \right\} \right| \mathcal{B}(p) \right\rangle \\
 &\approx \underbrace{[\text{LO in } 1/m_b]}_{\text{QCDF}} + h_\lambda^{(0)} + \frac{q^2}{1\text{GeV}^2} h_\lambda^{(1)} + \frac{q^4}{1\text{GeV}^4} h_\lambda^{(2)}, \quad h_\lambda^{(0,1,2)} \in \mathbb{C}
 \end{aligned}$$

$$F(q^2) = F^{\text{soft}}(\xi_{\perp,\parallel}(q^2)) + \Delta F^{\alpha_s}(q^2) + a_F + b_F \frac{q^2}{m_B^2} + \dots$$

Exclusive $b \rightarrow s\ell^+\ell^-$ decays:

- Parametrisation of $\mathcal{H}_\lambda(q^2)$: [Khodjamirian et al., 1006.4945; Bobeth et al., 1707.07305;]

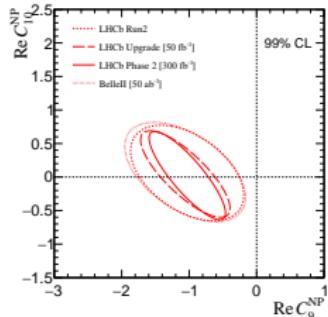
$$\mathcal{A}_\lambda^{L,R} = \mathcal{N}_\lambda \left\{ (C_9 \mp C_{10}) \mathcal{F}_\lambda(q^2) + \frac{2m_b M_B}{q^2} [C_7 \mathcal{F}_\lambda^T(q^2) - 16\pi^2 \frac{M_B}{m_b} \mathcal{H}_\lambda(q^2)] \right\}$$

$$\mathcal{H}_\lambda(z) = \frac{1 - z z_{J/\psi}^*}{z - z_{J/\psi}} \frac{1 - z z_{\psi(2S)}^*}{z - z_{\psi(2S)}} \hat{\mathcal{H}}_\lambda(z), \quad \hat{\mathcal{H}}_\lambda(z) = \left[\sum_{k=0}^K \alpha_k^{(\lambda)} z^k \right] \mathcal{F}_\lambda(z)$$

$$z(q^2) \equiv \frac{\sqrt{t_+ - q^2} - \sqrt{t_+ - t_0}}{\sqrt{t_+ - q^2} + \sqrt{t_+ - t_0}}$$

- Based on analyticity + data and valid for $-7 \leq q^2 \leq m_{\psi(2S)}^2$: [Bobeth et al., 1707.07305; Chrzaszcz et al., 1805.06378; Mauri et al., 1805.06401]

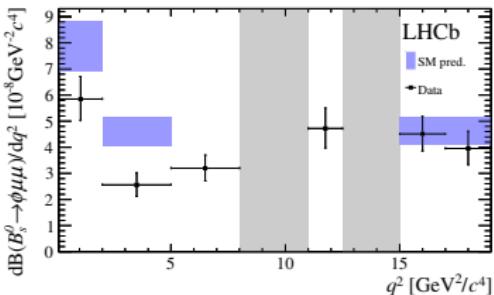
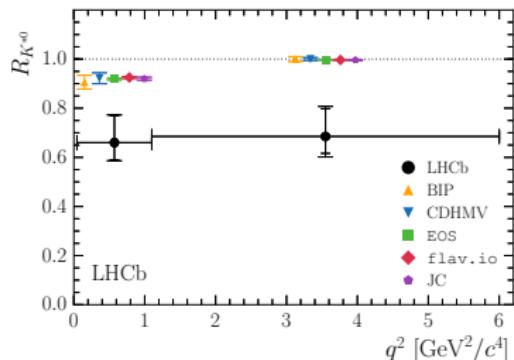
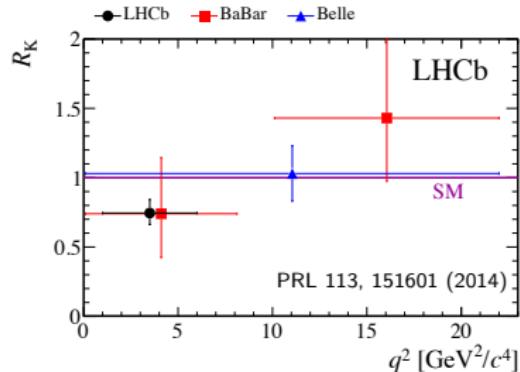
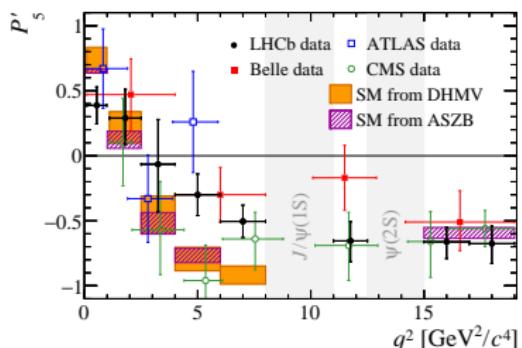
k	0	1	2
$\text{Re}[\alpha_k^{(\perp)}]$	-0.06 ± 0.21	-6.77 ± 0.27	18.96 ± 0.59
$\text{Re}[\alpha_k^{(\parallel)}]$	-0.35 ± 0.62	-3.13 ± 0.41	12.20 ± 1.34
$\text{Re}[\alpha_k^{(0)}]$	0.05 ± 1.52	17.26 ± 1.64	—
$\text{Im}[\alpha_k^{(\perp)}]$	-0.21 ± 2.25	1.17 ± 3.58	-0.08 ± 2.24
$\text{Im}[\alpha_k^{(\parallel)}]$	-0.04 ± 3.67	-2.14 ± 2.46	6.03 ± 2.50
$\text{Im}[\alpha_k^{(0)}]$	-0.05 ± 4.99	4.29 ± 3.14	—



Exclusive $b \rightarrow sl^+l^-$ decays:

► Observed anomalies:

[Dettori, Langenbruch, talks at Moriond 2018]



- **Comments:** 1, P'_5 stat. fluctuation unlikely; 2, precise evaluation of QED effect in $R_K^{(*)}$ very necessary; 3, cross-checks about hadronic nuisance parameters needed;

Exclusive $b \rightarrow s\ell^+\ell^-$ decays:

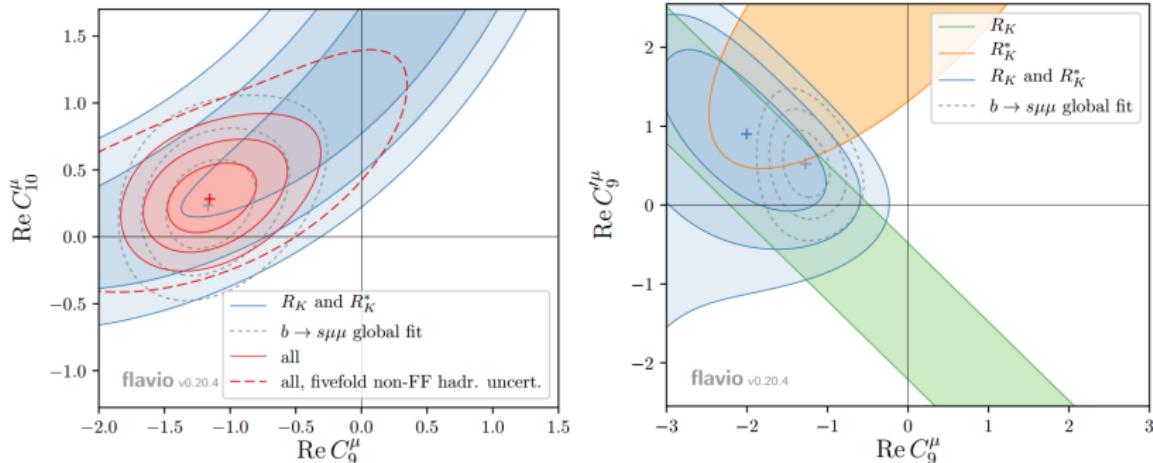
- Global fits to $b \rightarrow s\ell^+\ell^-$ data: [Danny van Dyk, talk at CKM2018]

who	approach	data set	references
global fits			
AS+	QCDF+	$b \rightarrow s\mu\mu$ / LFU	Altmannshofer, Straub et al. [1703.09189] [1704.05435]
[1412.3183] [1704.05446]			
CJ+	QCDF++	$b \rightarrow s\mu\mu$ + LFU	Camalich, Jäger et al.
[1510.04329] [1704.05340]			
DGMV+	QCDF+	$b \rightarrow s\mu\mu$ + LFU	Descotes-Genon, Matias, Virto et al.
[1603.00865] [1806.02791]			
HM+	QCDF++	$b \rightarrow s\mu\mu$ + LFU	Hurth, Mahmoudi et al.
[1704.05447]			
Rome	QCDF++	$b \rightarrow s\mu\mu$ + LFU	Ciuchini, Coutinho, Fedele, Franco, Paul, Silvestrini, Valli
fits to $B \rightarrow K^*\mu\mu$ only			
BCvDV	z-param	$B \rightarrow K^*\mu\mu$ (LHCb)	Bobeth, Chrzaszcz, DvD, Virto

- Conclusion: while different in the treatment of local and non-local hadronic contributions, all groups agree on a negative shift to C_9 by $-1.1...-1.76 \simeq -25...40\%$ of the SM value, although other contributions are also possible.

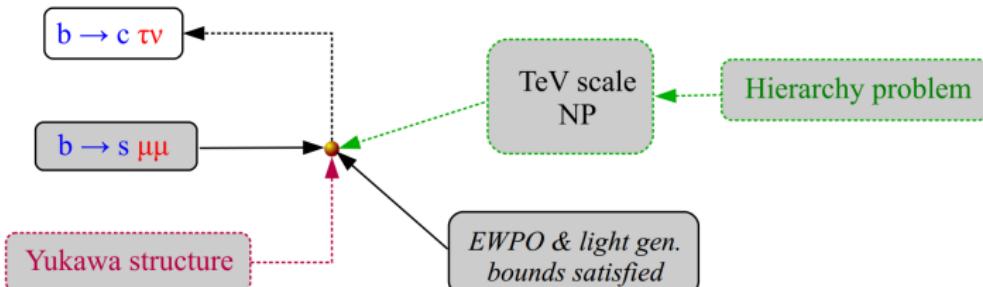
Exclusive $b \rightarrow sl^+l^-$ decays:

- New global fits: [Capdevila et al., 1704.05340; D. Straub, talk at CKM2018]



- New directions for model builders:

[G. Isodro, talk at CKM2018]

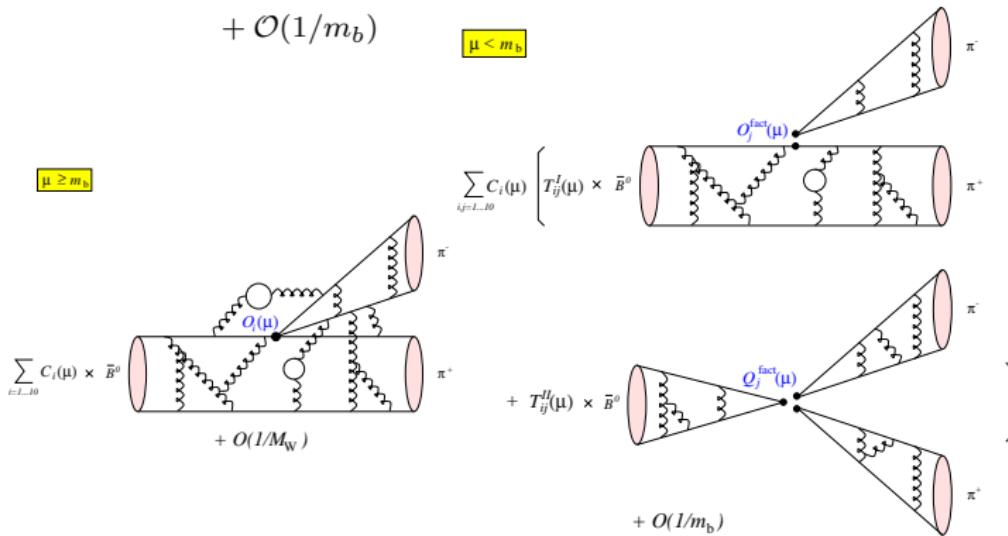


Non-leptonic B decays:

- To leading power in the heavy-quark expansion, $\langle M_1 M_2 | \mathcal{O}_i | \bar{B} \rangle$ obeys the following factorization formula: [Beneke, Buchalla, Neubert, Sachrajda, '99-'04]

$$\begin{aligned} \langle M_1 M_2 | \mathcal{O}_i | \bar{B} \rangle &\simeq m_B^2 F_+^{BM_1}(0) f_{M_2} \int du \quad T_i^I(u) \phi_{M_2}(u) + (M_1 \leftrightarrow M_2) \\ &+ f_B f_{M_1} f_{M_2} \int d\omega dv du \quad T_i^{II}(\omega, v, u) \phi_B(\omega) \phi_{M_1}(v) \phi_{M_2}(u) \\ &+ \mathcal{O}(1/m_b) \end{aligned}$$

$\boxed{\mu \leq m_b}$



- Systematic framework to all orders in α_s , but limited accuracy by $1/m_b$ corrs.

Non-leptonic B decays:

- Status of the hard kernels $T^{I,II}$: [Bell/Beneke/Huber/Li, from '09]

Two hard-scattering kernels for each operator insertion: T^I (vertex), T^{II} (spectator)

$$\langle M_1 M_2 | \mathcal{O}_i | B \rangle \simeq F^{BM_1} T_i^I \otimes \phi_{M_2} + T_i^{II} \otimes \phi_B \otimes \phi_{M_1} \otimes \phi_{M_2}$$

and two classes of topological amplitudes: "Tree", "Penguin".

	T^I , tree	T^I , penguin	T^{II} , tree	T^{II} , penguin
LO: $\mathcal{O}(1)$				
NLO: $\mathcal{O}(\alpha_s)$ BBNS '99-'04				
NNLO: $\mathcal{O}(\alpha_s^2)$	 Bell '07,'09 Beneke, Huber, Li '09	 Kim, Yoon '11, Bell Beneke, Huber, Li '15	 Beneke, Jager '05 Kivel '06, Pilipp '07	 Beneke, Jager '06 Jain, Rothstein, Stewart '07

- Missing NNLO pieces: 2-loop tree with insertion of penguin operators Q_{3-6} ; 2-loop penguin with insertion of penguin operators Q_{3-6} ; work in progress!

Non-leptonic B decays:

- ▶ How to deal with power corrections of order $\mathcal{O}(1/m_b)$;

Main limitation of QCDF approach, e.g. weak annihilation


$$\sim \int d\omega du dv T(\omega, u, v) \phi_B(\omega) \phi_{M_1}(v) \phi_{M_2}(u) ?$$

- ▶ convolutions diverge at endpoints \Rightarrow non-factorisation in SCET-2
- ▶ currently modelled with arbitrary soft rescattering phase

Pure annihilation decays

HFAG averages including LHCb Collaboration, (R. Aaij et al), LHCb-PAPER-2016-036

$$0.084^{+/-0.024}$$
$$10^6 \text{ Br}(B_d \rightarrow K^+ K^-) = 0.13 \pm 0.05 \quad (\Delta D = 1, \text{ exchange topology})$$

$$0.671^{+/-0.083}$$
$$10^6 \text{ Br}(B_s \rightarrow \pi^+ \pi^-) = 0.76 \pm 0.13 \quad (\Delta S = 1, \text{ penguin annihilation})$$

\Rightarrow extract weak annihilation amplitudes from data

[Wang, Zhu 13; Bobeth, Gorbahn, Vickers 14;
Chang, Sun, Yang, Li 14]

- ▶ New insights from collider-physics applications like collinear anomaly/rapidity divergence? [Becher/Neubert '10; Becher/Bell '11; Chiu/Jain/Neill/Rothstein '12]

↪ our next task: how to evaluate the power corrections?

Non-leptonic B decays:

► Tree-dominated decays: Brs [$\times 10^{-6}$]

[Beneke, Huber, Li '09]

	Theory I	Theory II	Experiment
$B^- \rightarrow \pi^- \pi^0$	$5.43^{+0.06+1.45}_{-0.06-0.84}$ (★)	$5.82^{+0.07+1.42}_{-0.06-1.35}$ (★)	$5.59^{+0.41}_{-0.40}$
$\bar{B}_d^0 \rightarrow \pi^+ \pi^-$	$7.37^{+0.86+1.22}_{-0.69-0.97}$ (★)	$5.70^{+0.70+1.16}_{-0.55-0.97}$ (★)	5.16 ± 0.22
$\bar{B}_d^0 \rightarrow \pi^0 \pi^0$	$0.33^{+0.11+0.42}_{-0.08-0.17}$	$0.63^{+0.12+0.64}_{-0.10-0.42}$	1.55 ± 0.19
BELLE CKM 14:			0.90 ± 0.16
$B^- \rightarrow \pi^- \rho^0$	$8.68^{+0.42+2.71}_{-0.41-1.56}$ (★★)	$9.84^{+0.41+2.54}_{-0.40-2.52}$ (★★)	$8.3^{+1.2}_{-1.3}$
$B^- \rightarrow \pi^0 \rho^-$	$12.38^{+0.90+2.18}_{-0.77-1.41}$ (★)	$12.13^{+0.85+2.23}_{-0.73-2.17}$ (★)	$10.9^{+1.4}_{-1.5}$
$\bar{B}^0 \rightarrow \pi^+ \rho^-$	$17.80^{+0.62+1.76}_{-0.56-2.10}$ (★)	$13.76^{+0.49+1.77}_{-0.44-2.18}$ (★)	15.7 ± 1.8
$\bar{B}^0 \rightarrow \pi^- \rho^+$	$10.28^{+0.39+1.37}_{-0.39-1.42}$ (★★)	$8.14^{+0.34+1.35}_{-0.33-1.49}$ (★★)	7.3 ± 1.2
$\bar{B}^0 \rightarrow \pi^\pm \rho^\mp$	$28.08^{+0.27+3.82}_{-0.19-3.50}$ (†)	$21.90^{+0.20+3.06}_{-0.12-3.55}$ (†)	23.0 ± 2.3
$\bar{B}^0 \rightarrow \pi^0 \rho^0$	$0.52^{+0.04+1.11}_{-0.03-0.43}$	$1.49^{+0.07+1.77}_{-0.07-1.29}$	2.0 ± 0.5
$B^- \rightarrow \rho_L^- \rho_L^0$	$18.42^{+0.23+3.92}_{-0.21-2.55}$ (★★)	$19.06^{+0.24+4.59}_{-0.22-4.22}$ (★★)	$22.8^{+1.8}_{-1.9}$
$\bar{B}_d^0 \rightarrow \rho_L^+ \rho_L^-$	$25.98^{+0.85+2.93}_{-0.77-3.43}$ (★★)	$20.66^{+0.68+2.99}_{-0.62-3.75}$ (★★)	$23.7^{+3.1}_{-3.2}$
$\bar{B}_d^0 \rightarrow \rho_L^0 \rho_L^0$	$0.39^{+0.03+0.83}_{-0.03-0.36}$	$1.05^{+0.05+1.62}_{-0.04-1.04}$	$0.55^{+0.22}_{-0.24}$

Theory I: $f_+^{B\pi}(0) = 0.25 \pm 0.05$, $A_0^{B\rho}(0) = 0.30 \pm 0.05$, $\lambda_B(1 \text{ GeV}) = 0.35 \pm 0.15 \text{ GeV}$

Theory II: $f_+^{B\pi}(0) = 0.23 \pm 0.03$, $A_0^{B\rho}(0) = 0.28 \pm 0.03$, $\lambda_B(1 \text{ GeV}) = 0.20^{+0.05}_{-0.00} \text{ GeV}$

► Theory II: small λ_B and form-factor hypothesis are more favoured;

► Colour-allowed modes well described, but colour-suppressed modes less;

Non-leptonic B decays:

- Penguin-dominated decays: $A_{CP} [\times 10^{-2}]$ [Bell, Beneke, Huber, Li '15]

f	NLO	NNLO	NNLO + LD	Exp
$\pi^- \bar{K}^0$	$0.71^{+0.13+0.21}_{-0.14-0.19}$	$0.77^{+0.14+0.23}_{-0.15-0.22}$	$0.10^{+0.02+1.24}_{-0.02-0.27}$	-1.7 ± 1.6
$\pi^0 K^-$	$9.42^{+1.77+1.87}_{-1.76-1.88}$	$10.18^{+1.91+2.03}_{-1.90-2.62}$	$-1.17^{+0.22+20.00}_{-0.22-6.62}$	4.0 ± 2.1
$\pi^+ K^-$	$7.25^{+1.36+2.13}_{-1.36-2.58}$	$8.08^{+1.52+2.52}_{-1.51-2.65}$	$-3.23^{+0.61+19.17}_{-0.61-3.36}$	-8.2 ± 0.6
$\pi^0 \bar{K}^0$	$-4.27^{+0.83+1.48}_{-0.77-2.23}$	$-4.33^{+0.84+3.29}_{-0.78-2.32}$	$-1.41^{+0.27+5.54}_{-0.25-6.10}$	1 ± 10
$\delta(\pi \bar{K})$	$2.17^{+0.40+1.39}_{-0.40-0.74}$	$2.10^{+0.39+1.40}_{-0.39-2.86}$	$2.07^{+0.39+2.76}_{-0.39-4.55}$	12.2 ± 2.2
$\Delta(\pi \bar{K})$	$-1.15^{+0.21+0.55}_{-0.22-0.84}$	$-0.88^{+0.16+1.31}_{-0.17-0.91}$	$-0.48^{+0.09+1.09}_{-0.09-1.15}$	-14 ± 11

$$\delta(\pi \bar{K}) = A_{CP}(\pi^0 K^-) - A_{CP}(\pi^+ K^-)$$

$$\Delta(\pi \bar{K}) = A_{CP}(\pi^+ K^-) + \frac{\Gamma_{\pi^- \bar{K}^0}}{\Gamma_{\pi^+ K^-}} A_{CP}(\pi^- \bar{K}^0) - \frac{2\Gamma_{\pi^0 K^-}}{\Gamma_{\pi^+ K^-}} A_{CP}(\pi^0 K^-) - \frac{2\Gamma_{\pi^0 \bar{K}^0}}{\Gamma_{\pi^+ K^-}} A_{CP}(\pi^0 \bar{K}^0)$$

- “NLO” and “NNLO”: including only pert. calculable SD contribution;
- “NNLO+LD”: power-suppressed spectator and annihilation terms included back;
- For πK , NNLO change minor, since the total penguin $\hat{\alpha}_4^c = a_4^c + r_\chi^\pi a_6^c + \beta_3^c$;
- NNLO correction does not help resolving the observed πK CP asymmetry puzzle;

Non-leptonic B decays:

- Brs and ratios: 10^{-3} ($b \rightarrow c\bar{u}d$), 10^{-4} ($b \rightarrow c\bar{u}s$) [Huber, Kräckl, Li '16]

Decay mode	LO	NLO	NNLO	Exp.
$\bar{B}_d \rightarrow D^+ \pi^-$	3.58	$3.79^{+0.44}_{-0.42}$	$3.93^{+0.43}_{-0.42}$	2.68 ± 0.13
$\bar{B}_d \rightarrow D^{*+} \pi^-$	3.15	$3.32^{+0.52}_{-0.49}$	$3.45^{+0.53}_{-0.50}$	2.76 ± 0.13
$\bar{B}_d \rightarrow D^+ \rho^-$	9.51	$10.06^{+1.25}_{-1.19}$	$10.42^{+1.24}_{-1.20}$	7.5 ± 1.2
$\bar{B}_d \rightarrow D^{*+} \rho^-$	8.45	$8.91^{+0.74}_{-0.71}$	$9.24^{+0.72}_{-0.71}$	6.0 ± 0.8
$\bar{B}_d \rightarrow D^+ K^-$	2.74	$2.90^{+0.33}_{-0.31}$	$3.01^{+0.32}_{-0.31}$	1.97 ± 0.21
$\bar{B}_d \rightarrow D^{*+} K^-$	2.37	$2.50^{+0.39}_{-0.36}$	$2.59^{+0.39}_{-0.37}$	2.14 ± 0.16
$\bar{B}_d \rightarrow D^+ K^{*-}$	4.79	$5.07^{+0.65}_{-0.62}$	$5.25^{+0.65}_{-0.63}$	4.5 ± 0.7
$\bar{B}_d \rightarrow D^{*+} K^{*-}$	4.30	$4.54^{+0.41}_{-0.40}$	$4.70^{+0.40}_{-0.39}$	—
$\Lambda_b \rightarrow \Lambda_c^+ \pi^-$	2.60	$2.75^{+0.53}_{-0.53}$	$2.85^{+0.54}_{-0.54}$	$4.30^{+0.36}_{-0.35}$
$\Lambda_b \rightarrow \Lambda_c^+ \rho^-$	7.46	$7.88^{+1.44}_{-1.43}$	$8.17^{+1.47}_{-1.47}$	—
$\Lambda_b \rightarrow \Lambda_c^+ a_1^-$	9.57	$10.11^{+1.75}_{-1.72}$	$10.47^{+1.78}_{-1.77}$	—
$\Lambda_b \rightarrow \Lambda_c^+ K^-$	2.02	$2.14^{+0.40}_{-0.39}$	$2.21^{+0.40}_{-0.40}$	3.42 ± 0.33
$\Lambda_b \rightarrow \Lambda_c^+ K^{*-}$	3.86	$4.07^{+0.74}_{-0.73}$	$4.22^{+0.75}_{-0.75}$	—

- For \bar{B}_d decays, NNLO Brs higher than the data; for Λ_b decays, NNLO Brs smaller than the data; ↵ non-negligible power corrections with natural size $\sim 10 - 15\%$?

Conclusion and outlook

- ▶ High-luminosity frontier is very complementary to high-energy frontier, especially for NP searches;
- ▶ Great progress achieved in both theo. and exp. sides for B physics, and also a very promising future ([LHCb](#) and [Belle II](#), …);
- ▶ CKM mechanism of flavor and CP violation well established. However, 20% NP effects in most FCNC processes often possible;
- ▶ Several deviations observed at $2 \sim 4\sigma$ in $b \rightarrow c\tau\bar{\nu}$ and $b \rightarrow s\mu\bar{\mu}$ decays, implications of LFUV? Lets stay tuned!
- ▶ QCDF at leading power and at NNLO in QCD established and almost complete. Any further breakthroughs welcome;

Thank You for Your Attention!