



COMET Tracking

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New Physics & CLFV

COMET Design Principles

New Tracking Techniques Local-Level GBDT Neighbour-Level GBDT Hough Transform Track-Level GBDT

Backup

Tracking in the COMET Experiment using Machine Learning

Ewen Lawson Gillies

Imperial College London High Energy Particle Physics

> IHEP EPD Seminar May 3rd, 2018



Overview



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COMET is a next generation, high intensity experiment looking for new physics.

- 1 New Physics: Charged Lepton Flavor Violation
- 2 New Designs: The Coherent Muon to Electron Transition (COMET) experiment
- 3 New Techniques: Gradient Boosted Decision Trees (GBDT) and Hough Transforms in Track Finding





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Lepton Flavor Violation



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Lepton flavor is conserved in the Standard Model.

Muon Decay: $\mu^- \rightarrow \nu_{\mu} + e^- + \bar{\nu}_e$ Muon Capture: $\mu^- + N \rightarrow \nu_{\mu} + N'$

Do the charged leptons, (τ, μ, e) , violate this conservation law of the Standard Model?



Current Experimental Limits



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■ Br($\mu^+ \rightarrow e^+ + e^+ + e^-$) < 1.0 × 10⁻¹² (SINDRUM 1988) ■ Br($\mu^+ \rightarrow e^+ + \gamma$) < 4.2 × 10⁻¹³ (MEG 2016) ■ B($\mu^- + Au \rightarrow e^- + Au$) < 7 × 10⁻¹³ (SINDRUM II 2006)

COMET focuses on muon to electron conversion. Without CLFV, this process can only come indirectly with processes involving neutrinos:

$$\mathsf{B}(\mu^- + \mathsf{N}
ightarrow e^- + \mathsf{N}) \sim 10^{-52}$$

In 2018, COMET Phase I aims to achieve the sensitivity of:

$$\mathsf{B}(\mu^- + \mathsf{AI} o e^- + \mathsf{AI}) < 7.2 imes 10^{-15}$$



Possible Channels for Signal







Possible Channels for New Physics



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Four-Fermi contact:

- Increased sensitivity for *µ*-*e* conversion
- Model-independent search

Photonic:

- Still accessible in μ-e conversion search.
- Less sensitive than dedicated µ-e gamma experiments (like MEG).





Complementary Searches





- Relative sensitivity to Four Fermi and Photonic interactions is model dependent.
- Highly complimentary to MEG search

$$egin{split} \mathcal{L} &= rac{1}{1+\kappa} rac{m_{\mu}}{\Lambda^2} ig(ar{\mu}_R \sigma^{\mu
u} e_L F_{\mu
u}ig) \ &+ rac{\kappa}{1+\kappa} rac{1}{\Lambda^2} ig(ar{\mu}_L \gamma^{\mu} e_Lig) ig(ar{q}_L \gamma_{\mu} q_Lig) \end{split}$$



Complementary Searches





- Relative sensitivity to Four Fermi and Photonic interactions is model dependent.
 - Highly complimentary to MEG search



100

PRISM

 $\mathcal{B}(\mu^{-}Al \rightarrow e^{-}Al)$

COMET Phase-II

COMET Phase-I (extended)

 $< 7 \times 10^{-19}$

 $< 3 \times 10^{-17}$

< 7 × 10⁻¹⁶ COMET Phase-I

 $< 7 \times 10^{-15}$

 $< 7 \times 10^{-13}$

SINDRUM-II

 $\mathcal{B}(\mu^{-}Au \rightarrow e^{-}Au)$

Four-Fermi

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Stopped Muon Processes



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Stopped muon cascades to ground state orbital, emitting gamma rays.



Muon stopped in atom



Decay in Orbit



Nuclear Muon Capture



 μ -e Conversion



Background: Nuclear Muon Capture



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Nuclear Muon Capture

A. Edmonds AICAP Experiment Proton Emission Spectrum AlCap (Thick Al - Left Arm - Analyser 1) ž. Rate (0 - 10 MeV) = 0.031 All AlCap Rates Match (0.0195 protons per car AlCap (Thin Al - Left Arm - Analyser 2) Bate (0 - 10 MeV) = 0.036 PRELIMINARY TWIST (A. Gaponenko) Rate (3.4 - 28 MeV) = 0.031 280 TDR (Normalised to AlCap 4 - 8 MeV) Rate (0 - 30 MeV) = 0.04995 Kinetic Energy [keV

AlCap measurements



Background: Muon Decay in Orbit



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Signal Process: μ -e Conversion



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$$\mu^{-} + N(A, Z) \rightarrow e^{-} + N(A, Z)$$

Momentum of Signal Electron:

$$E_e = m_\mu - B_\mu - E_{
m recoil}$$

For Aluminum (COMET):

$$E_e = 104.9 \text{ MeV}$$

$$\tau_{\mu} = 864 \text{ ns}$$









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COMET Phase I Design





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COMET Phase I Design



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COMET Phase I Design



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Section

- 10¹² protons are fired every second at the production target to produce pions.
- Pions decay into muons while flying down the beamline through curved solenoid magnets.



COMET Phase I Design



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Section

- 10¹² protons are fired every second at the production target to produce pions.
- Pions decay into muons while flying down the beamline through curved solenoid magnets.
- 10⁹ muons are stopped in the aluminium target every second. The detector watches for the 105 MeV electrons



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Pulsed Beam and Time Window



- \blacksquare Beam is pulsed at approximately 1 $\rm MHz$
- 8e6 protons in each pulse
- Timing window of the detector waits until after the beam flash

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Phase I Geometry



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Phase I Geometry



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Phase I Geometry









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Cylindrical Detector



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$\mathsf{CDC} \text{ and } \mathsf{CTH}$





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CDC and CTH





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Typical Event [1]









Typical Event [2]









90°



Classification Problem



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"Is this wire a signal hit from a signal track". Algorithm developed with Dr. Alex Rogozhnikov when he was at Yandex.

Define categories of features:

- 1 "Local" Features: Features on the wire itself
- 2 "Neighbour" Features: Features of adjacent wires
- 3 "Shape" Features: Check if the wire forms a circle with other hit wires



Previous Classifier: Cutting on Energy Deposition and the college







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Local-Level GBDT



Local Features of a Hits



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Hits in the Cylindrical Drift Chamber (CDC) have three main properties or "features"

- Radial distance from centre.
- Energy deposited by charged particle (i.e. ADC signal).
- Timing of energy deposition.



Radial Distance Distribution







Relative Timing Distribution





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Neighbour-Level GBDT


Local and Neighbour Features



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Signal hits are often grouped in local clusters, meaning neighbouring wire features are extremely important.

Neighbour-Level Features:

- Radial distance from centre, same for wire and LR neighbours (1 feature)
- Energy deposited on wire, left neighbour, and right neighbour (3 features).
- Timing of hit on wire, left neighbour, and right neighbour (3 features).



Left Neighbour Charge Deposit







Left Neighbour Relative Timing Distribution



1500

COMET Wires with no hits get a very negative time. Tracking Ewen Gillies Relative time of Left Hand Wire. No Hit = -1000 0.018 Signal 0.016 & CLFV Background 0.014 0.012 Vormalised Hit Count 0.010 Neighbour-Level GBDT 0.008 0.006 0.004 0.002 0.000 -500 -1000 500 1000

Relative Time [ns]



Neighbour-Level GBDT Output Distribution







Output of Neighbour-Level GBDT





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- Open circles are original hit locations
- Signal Hits and Background Hits are scaled to the output of the neighbour level GBDT.







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Hough Transform



Circular Hough Transform







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Figure: Points in (x, y) space, blue, thought to be on a circle, red, whose centre lies at the origin, orange. Figure: A mapping from the points in (x, y) space, blue, to possible circle centers in (a, b) space, green.



Hough Implementation





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 Hits with corresponding hough contributions
 Track centers scaled by contributions from hit points.





Executing the Hough Transform



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Hough Transform

Track-Level GBD

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Weight wire *j*'s contribution by its GBDT output:

$$W_j = y_{ ext{Grad.}}\left(f_1^{(j)}, \dots, f_N^{(j)}
ight)$$
 for N features

Apply hough transform between wire *j* and track center *i*:



Hough Track centre



Forward Hough Transform on Neighbour Level Vander College GBDT Output

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- Signal hits scaled by neighbour level GBDT output W_j.
- Background hits also scaled by W_j.
- Hough transform scaled by W_j of corresponding hit.
- Track centers
 scaled by C_i from
 C_i = T_{ij}W_j.





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Reweight the results to highlight maxima:

$$C_i \rightarrow C'_i(\alpha) = \exp(\alpha C_i)$$

Invert the transform:





Inverse Reweighted Hough Transform Output

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- Signal hits scaled by reweighted inverse Hough output W'_j.
 Background hits scaled by W'_j.
 Track centers scaled by C'_i.
- Inverse Hough transform scaled by C'_i of corresponding centre.



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Inverse Hough Output Feature









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Track-Level GBDT Output Distribution







Inverse Reweighted Hough Transform Output

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Track-Level GBDT

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- Signal hits and Background hits scaled by output of track-level GBDT.
- Note: No cuts are placed on scaling of these outputs, this is the full response of the track-level GBDT.



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Inverse Reweighted Hough Transform Output



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- Cut placed on GBDT output that preserves 99% of signal hits.
- Signal hits and Background hits are filled if they pass the cut.



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ROC Curves [1]



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Comparison of cut-based classifier vs GBDT methods.





ROC Curves [2]



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Zoomed ROC curves, note the axes.

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Track Finding Summary



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The track finding algorithm developed with Dr. Alex Rogozhnikov at Yandex is successful.

- This is the first time BDTs have been used in track finding (so far as I know).
- Further development still needed to define tracks as collections of filtered hit points.

Further work: Track Trigger

- Algorithm has been developed with Yandex.
- FPGA firmware developed on similar principles in Japan.
- Implementation is underway

https://github.com/ewengillies/track-finding-yandex







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The COMET Experiment: Phase II



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- Capture backwards scattered pions from proton beam.
- Bent solenoids select low momentum muons.
- Muons stopped in target, conversion occurs here!
- Bent solenoids select high momentum electrons.
- Detector waits for offset fiducial time window.



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Phase II Geometry







Cylindrical Detector: Stereometry





Figure: A projection of a wire array with alternating stereo angles from above.

Figure: A projection at Z = 0 of a wire array with alternating stereo angles from along the beamline.



Decision Tree



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Sample is split by series of threshold cuts. At each stage, cut is taken that improves the "purity" of classification at next node.



Figure: A decision tree, where the features are labelled as $\{xi, xj, xk\}$. The first cut is on xi at value xi = c1. This process is continued until some stopping criteria is reached. The leaf nodes are labelled as background, B, or signal, S.



Gradient Boosted Decision Tree



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Gradient boosting takes a weighted sum of decision trees. The weights are determined to minimize a loss function that describes misclassification rate. For a hit with a vector of features f:

Decision Tree *i*: $h_i(\mathbf{f}) = +1 \text{ or } -1$ GBDT: $y_{\text{Grad}}(\mathbf{f}, \mathbf{b}) = \sum_{i=0}^{N_{\text{trees}}} b_i h_i(\mathbf{f})$ Loss Function: $F(y_{\text{Grad}}, y) = -2 [y \cdot y_{\text{Grad}} + \ln (1 + e^{y_{\text{Grad}}})]$

Minimising this function with respect to the weights ${\bf b}$ fully determines the GBDT.



Shape Feature



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All signal hits should be part of a track that forms a helix in 3D space.

Projecting the track onto a slice of the cylindrical detector gives a circular shape.

Stereo angles of the wire array causes displacement of circle between even and odd layers.





Track Centre Layout



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- Dark outer dots are wires, i.e. points in (x, y).
- Lighter central dots track
 - centers, i.e.
 - points in (*a*, *b*).
- Location of track centers is dictate by geometry, spacial resolution taken to match wire spacing.





Defining the Hough Transform



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Define likelihood that a track centred at position \mathbf{r}_i contains a hit wire j at position \mathbf{r}_j as T_{ij} .

- **T** is the Hough Transform matrix of shape $[N_{\text{tracks}}, N_{\text{wires}}]$
- **W** is the hit wire vector of length [*N*_{wires}], i.e. *W_j* = 1 for a hit and *W_j* = 0 for no hit.
- **C** is the track center vector of length [*N*_{tracks}], where *C_i* is the likelihood that a signal track exists at track centre *i*.



Inverse Transform





Optimizing the Hough Transform [1]



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How do we define T_{ij} ? Recover the distribution of the radii of signal tracks directly from simulation. Each track has an associated particle, with transverse momentum p_T .

Distribution of Signal Track Radius in All Events 0.25 Vormalised Distribution of Signal Tracks 0.20 Average the p_T from each hit in an event, then recover the signal radius 0.15 for the event. Sig.Hits 0.10 $r_{\rm Sig.}$ 0.05 0.00L 10 20 25 30 5 15 35 Event-wise Signal Radius [cm]





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New Tracking Techniques Local-Level GBDT Neighbour-Level GBDT Hough Transform Track-Level GBDT Backup Fit this distribution directly to recover values for T_{ij} . For distance $d_{ij} = |\mathbf{r}_i - \mathbf{r}_j|$ between track centre *j* and wire *i*:

$$T(d_{ij}) = T_{ij} \propto \begin{cases} \exp\left(\frac{[d_{ij} - r_{\rm sig}]^2}{2\sigma_{\rm sig}^2}\right) & : r_{\rm min} < d_{ij} < r_{\rm sig} \\ 1 - \frac{d_{ij} - r_{\rm sig}}{r_{\rm max} - r_{\rm sig} + 0.1} & : r_{\rm sig} < d_{ij} < r_{\rm max} \\ 0 & : \text{ else} \end{cases}$$

This is half a Gaussian centred around the signal radius for smaller radii and a linear drop off for larger radii.

The parameters are the signal radius, r_{sig} , the spread for lower values, σ_{sig} , and the minimal and maximal radii considered, r_{min} and r_{max} .



Optimizing the Hough Transform [3]







ROC Curve: Previous Result



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Zoomed ROC curves for previous sample



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Feature Evaluation



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The feature importance evaluates how often a feature was used to split a node.





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