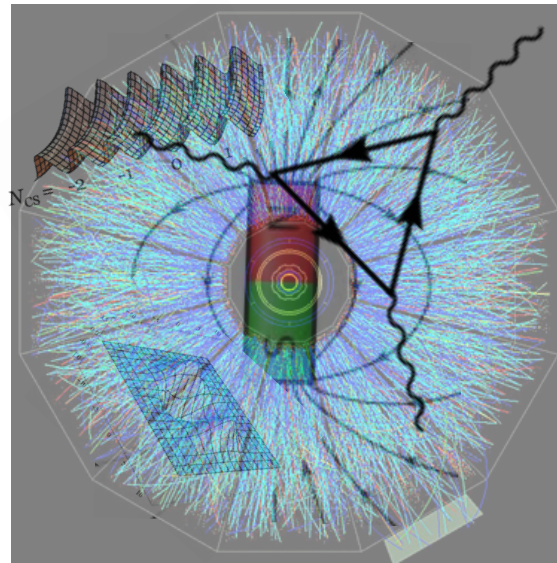


ATHIC2018 @ Hefei **Nov. 3~6, 2018**

Hydrodynamics with Anomaly Transport & CME in Isobaric Collisions



Jinfeng Liao

Indiana University / CCNU

**Research Supported by U.S. NSF & DOE
and by NSFC**



BEST
COLLABORATION

Quantifying the chiral magnetic effect from anomalous-viscous fluid dynamics^{*}

Yin Jiang(姜寅)¹ Shuzhe Shi(施舒哲)² Yi Yin(尹伊)³ Jinfeng Liao(廖劲峰)^{2,4;1)}

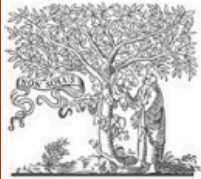
¹ School of Physics and Nuclear Energy Engineering, Beihang University, Beijing 100191, China

² Physics Department and Center for Exploration of Energy and Matter, Indiana University, 2401 N Milo B. Sampson Lane, Bloomington, IN 47408, USA

³ Center for Theoretical Physics, Massachusetts Institute of Technology, Cambridge, MA 02139, USA

⁴ Institute of Particle Physics and Key Laboratory of Quark & Lepton Physics (MOE), Central China Normal University, Wuhan 430079, China

Annals of Physics 394 (2018) 50–72

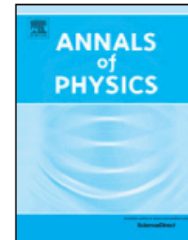


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Anomalous chiral transport in heavy ion collisions from Anomalous-Viscous Fluid Dynamics



Shuzhe Shi^{a,*}, Yin Jiang^{b,c}, Elias Lilleskov^{d,a}, Jinfeng Liao^{a,e,*}

Shuzhe Shi
(McGill; PhD @ IUB)

Yin Jiang (Beihang),
Yi Yin (MIT),
Elias Lilleskov (REU)

The EBE-AVFD “Warriors”

XXVIIth International Conference on Ultrarelativistic Nucleus-Nucleus Collisions
(Quark Matter 2018)

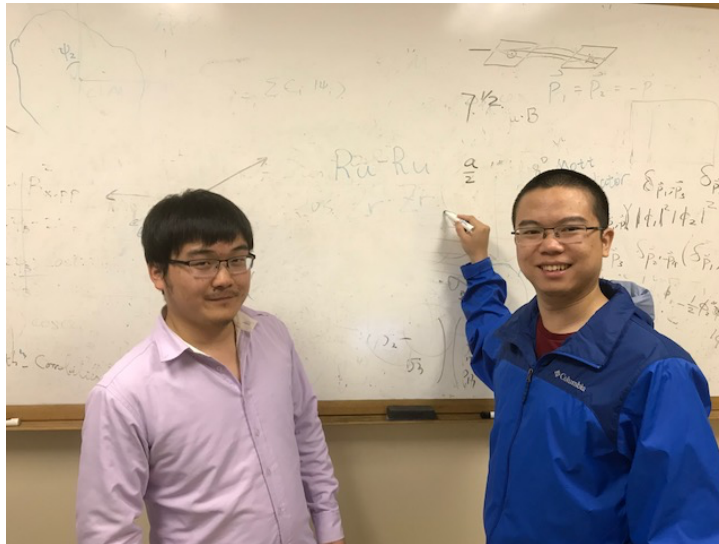
Chiral Magnetic Effect in Isobaric Collisions from Anomalous-Viscous Fluid Dynamics (AVFD)

Shuzhe Shi^a, Hui Zhang^{b,a}, Defu Hou^b, Jinfeng Liao^{* a,b}

^aPhysics Department and Center for Exploration of Energy and Matter, Indiana University, 2401 N Milo B. Sampson Lane,
Bloomington, IN 47408, USA.

^bInstitute of Particle Physics and Key Laboratory of Quark & Lepton Physics (MOE), Central China Normal University, Wuhan,
430079, China.

QM18 proceedings



Hui Zhang

Shuzhe Shi



Defu Hou

Exciting Progress: See Recent Reviews

Progress in Particle and Nuclear Physics 88 (2016) 1–28



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Review

Chiral magnetic and vortical effects in high-energy nuclear collisions—A status report



D.E. Kharzeev^{a,b}, J. Liao^{c,d,*}, S.A. Voloshin^e, G. Wang^f

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^b Department of Physics and RIKEN-BNL Research Center, Brookhaven National Laboratory, Upton, NY 11973-5000, USA

^c Physics Department and Center for Exploration of Energy and Matter, Indiana University, 727 E Third Street, Bloomington, IN 47405, USA

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^e Department of Physics and Astronomy, Wayne State University, 666 W. Hancock, Detroit, MI 48201, USA

^f Department of Physics and Astronomy, University of California, Los Angeles, CA 90095, USA

Prog. Part. Nucl. Phys. 88, 1 (2016)[arXiv:1511.04050 [hep-ph]].

J. Liao, Pramana 84, no. 5, 901 (2015) [arXiv:1401.2500 [hep-ph]].

Outline

- Introductory Discussions
- The AVFD Framework
- AVFD Results for AuAu Collisions
- Predictions for CME in Isobaric Collisions
- Summary

Introductory Discussions

Chiral Symmetry & SSB

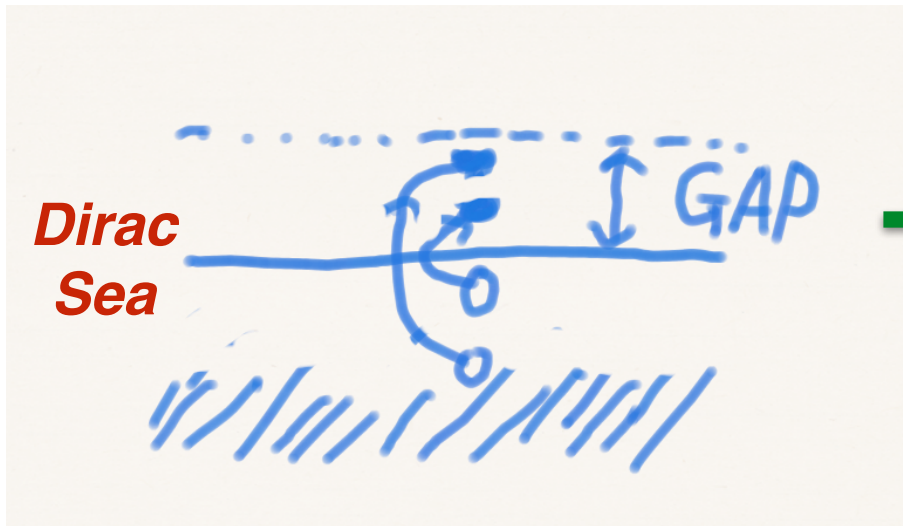
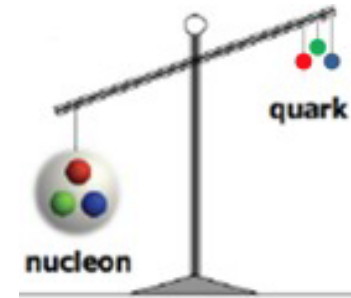
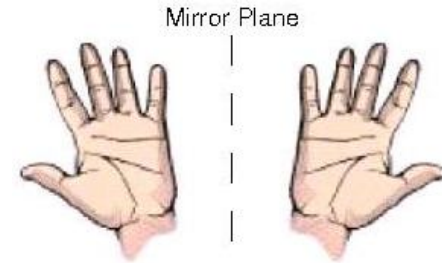
Classical symmetry:

$$\mathcal{L} = i\bar{\Psi}\gamma^\mu\partial_\mu\Psi$$

$$\mathcal{L} \rightarrow i\bar{\Psi}_L\gamma^\mu\partial_\mu\Psi_L + i\bar{\Psi}_R\gamma^\mu\partial_\mu\Psi_R$$

$$\Lambda_A : \Psi \rightarrow e^{i\gamma_5\theta}\Psi$$

$$\partial_\mu J_5^\mu = 0$$



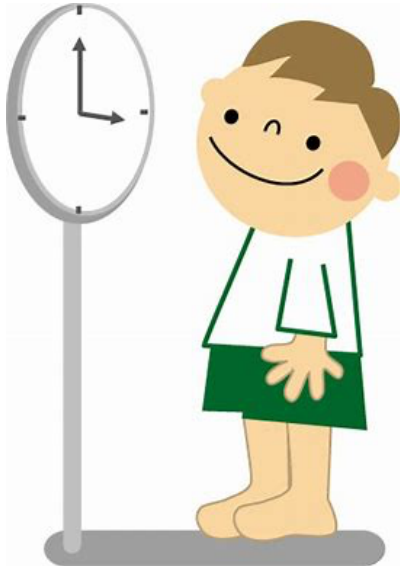
$$M = m - 2G \langle \bar{\psi}\psi \rangle$$

**Constituent
mass**

**Lagrangian
(SM) mass**

The “Origin of Mass”

QCD interactions (via SSB) account for nearly all the visible mass in the Universe.



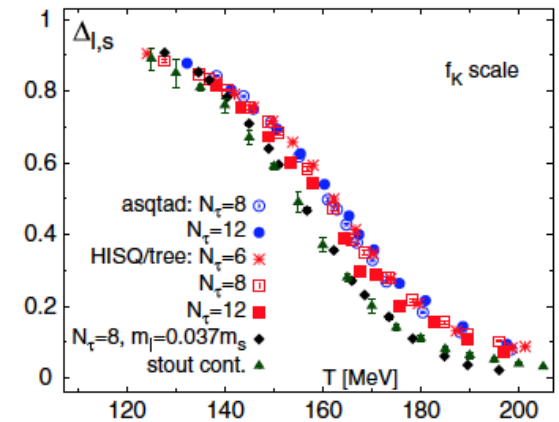
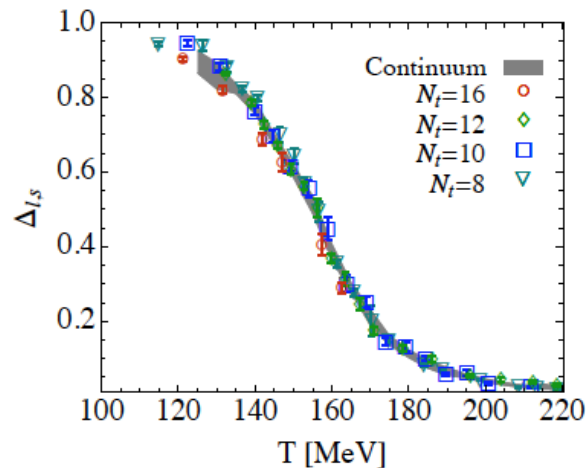
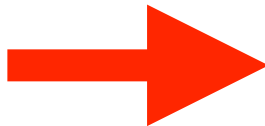
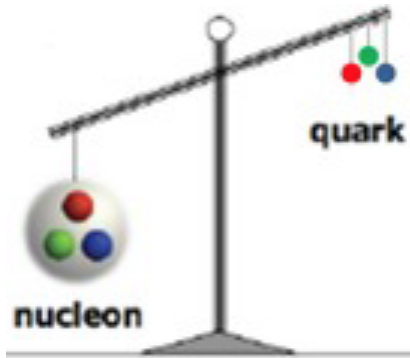
A typical person, say ~ 70 kg
**** Reasonable estimate, dominantly***
H₂O ~ 10 protons + 8 neutrons
~ 28 u quarks + 26 d-quarks

**** Mass from Higgs: ~1.7kg (~2.4%)***
**** Mass from QCD: ~ 68.3kg (~97.6%)***

The QCD chiral symmetry is just of paramount importance!

QCD & Chiral Symmetry

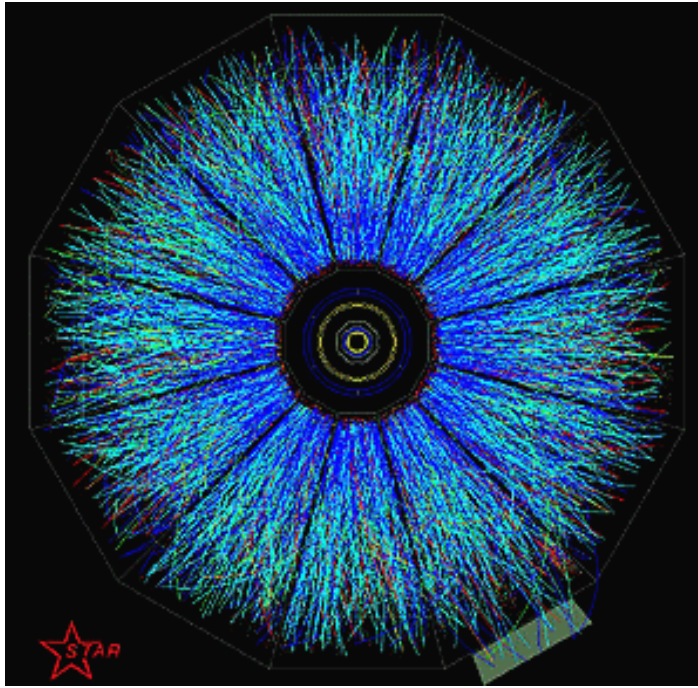
** Spontaneously broken chiral symmetry in the vacuum is a fundamental property of QCD.*



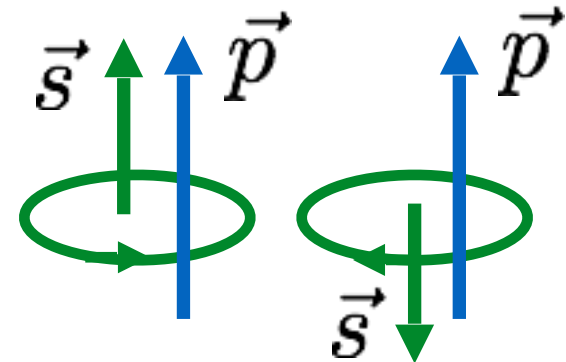
** A chirally symmetric quark-gluon plasma at high temperature is an equally fundamental property of QCD!*

Could we see direct experimental evidence for that?

“Little Bang” in High Energy Nuclear Collision



- * *Quark-gluon plasma (QGP) is created in such collisions.*
- * *It is PRIMORDIALLY HOT ~ trillion degrees ~ early universe.*
- * *Is chiral symmetry restored?*



Chiral Anomaly

Chiral anomaly is a fundamental aspect of QFT with chiral fermions.

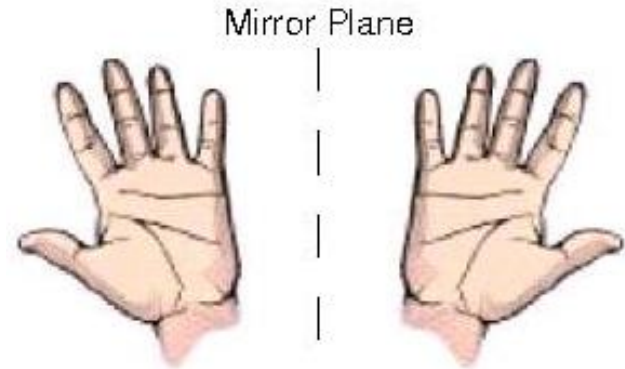
Classical symmetry:

$$\mathcal{L} = i\bar{\Psi}\gamma^\mu\partial_\mu\Psi$$

$$\mathcal{L} \rightarrow i\bar{\Psi}_L\gamma^\mu\partial_\mu\Psi_L + i\bar{\Psi}_R\gamma^\mu\partial_\mu\Psi_R$$

$$\Lambda_A : \Psi \rightarrow e^{i\gamma_5\theta}\Psi$$

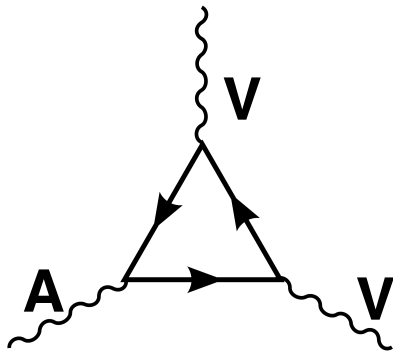
$$\partial_\mu J_5^\mu = 0$$



Broken at QM level:

$$\partial_\mu J_5^\mu = C_A \vec{E} \cdot \vec{B}$$

$$dQ_5/dt = \int_{\vec{x}} C_A \vec{E} \cdot \vec{B}$$



[e.g. $\pi^0 \rightarrow 2 \text{ gamma}$]

- * C_A is universal anomaly coefficient
- * Anomaly is intrinsically QUANTUM effect

The Chiral Magnetic Effect (CME)

Chirality & Anomaly & Topology

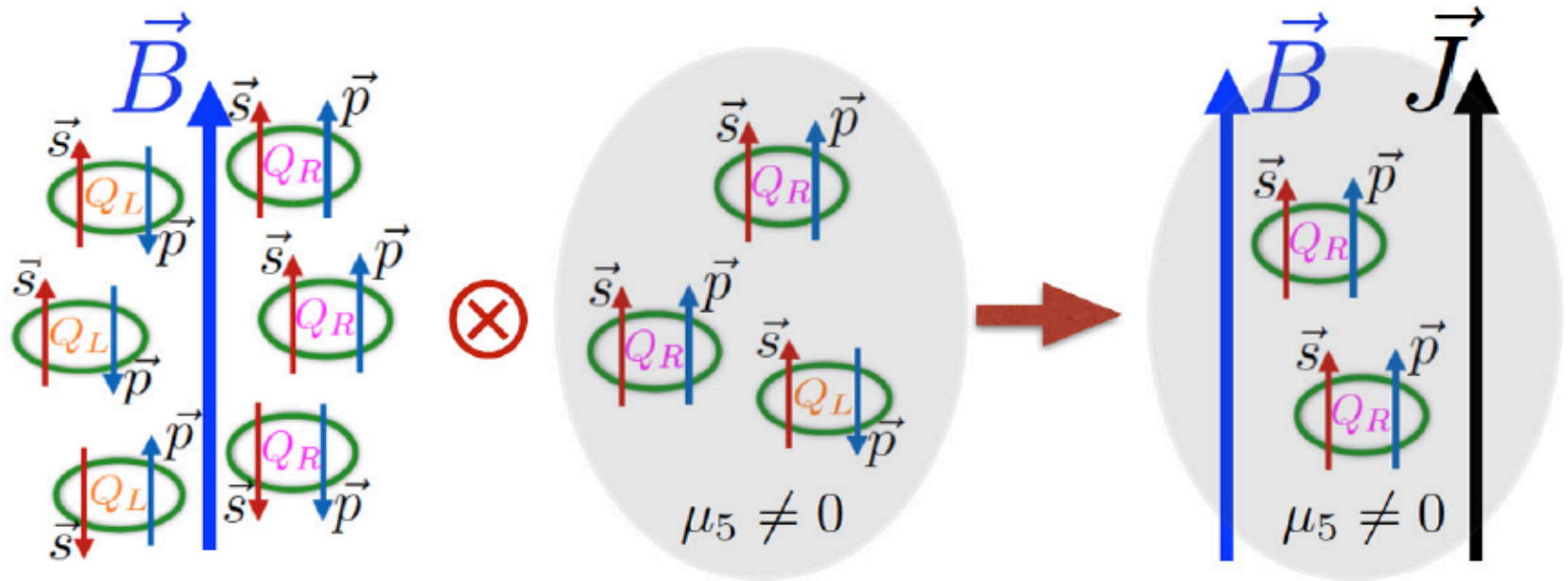
$$\vec{J} = \frac{Q^2}{2\pi^2} \mu_5 \vec{B}$$

Electric
Current

Magnetic
Field

Q.M. Transport

Intuitive Picture of CME



Intuitive understanding of CME:

Magnetic polarization \rightarrow
correlation between micro.
SPIN & EXTERNAL FORCE



Chiral imbalance \rightarrow
correlation between directions of
SPIN & MOMENTUM



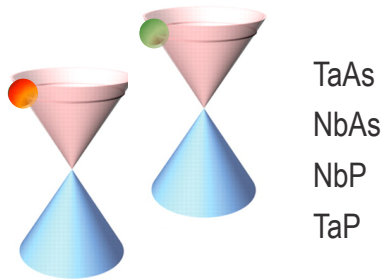
Transport current along magnetic field

$$\vec{J} = \frac{Q^2}{2\pi^2} \mu_5 \vec{B}$$

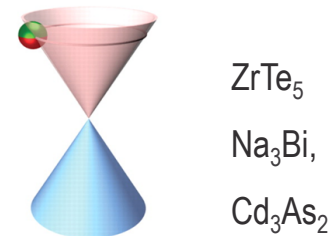
Searching for CME in Laboratories

CME was observed via negative magnetoresistance in semimetals.

Weyl semimetal
(non-degenerated bands)



Dirac semimetal
(doubly degenerated bands)

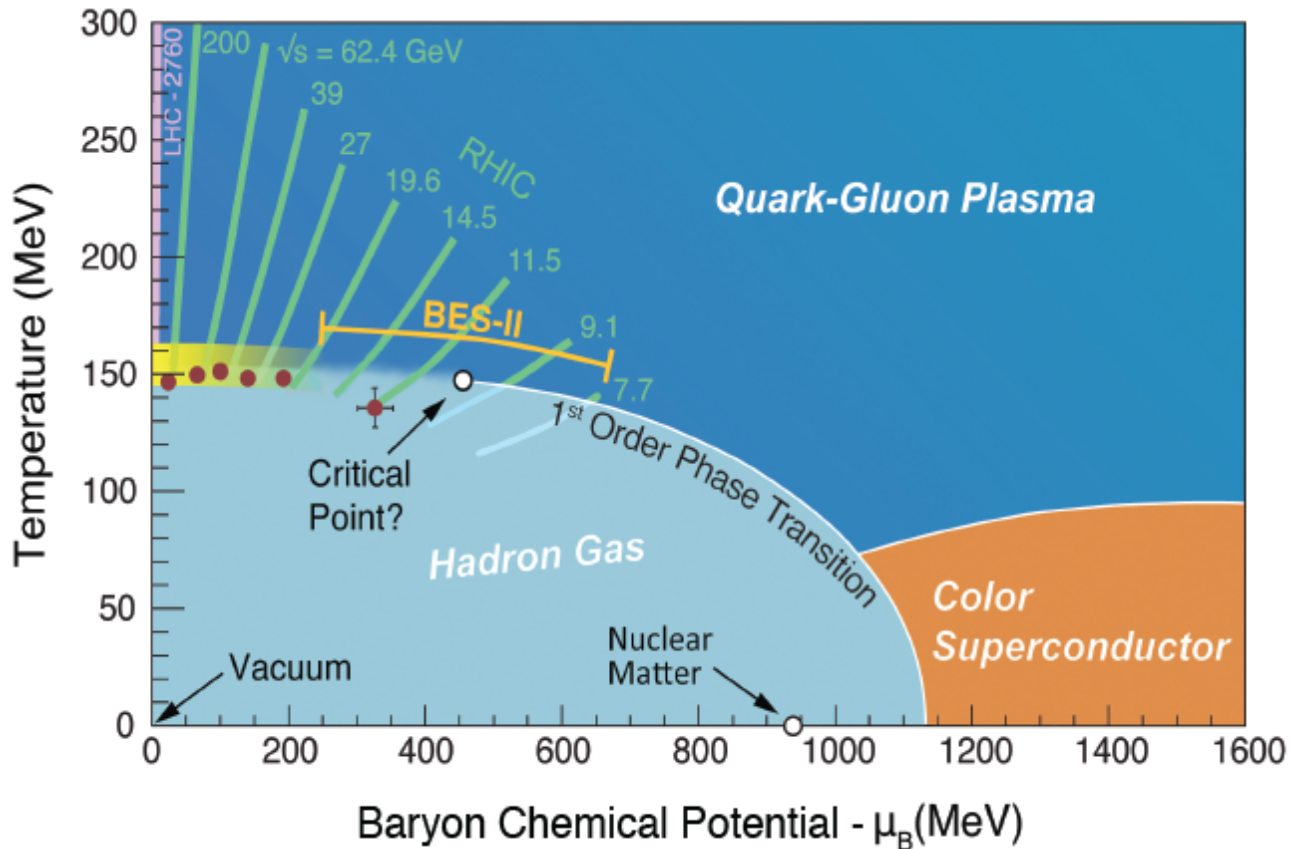


Observe CME for the subatomic chiral matter in heavy ion collisions?

- 1) (nearly) chiral quarks***
- 2) chirality imbalance***
- 3) strong magnetic field***

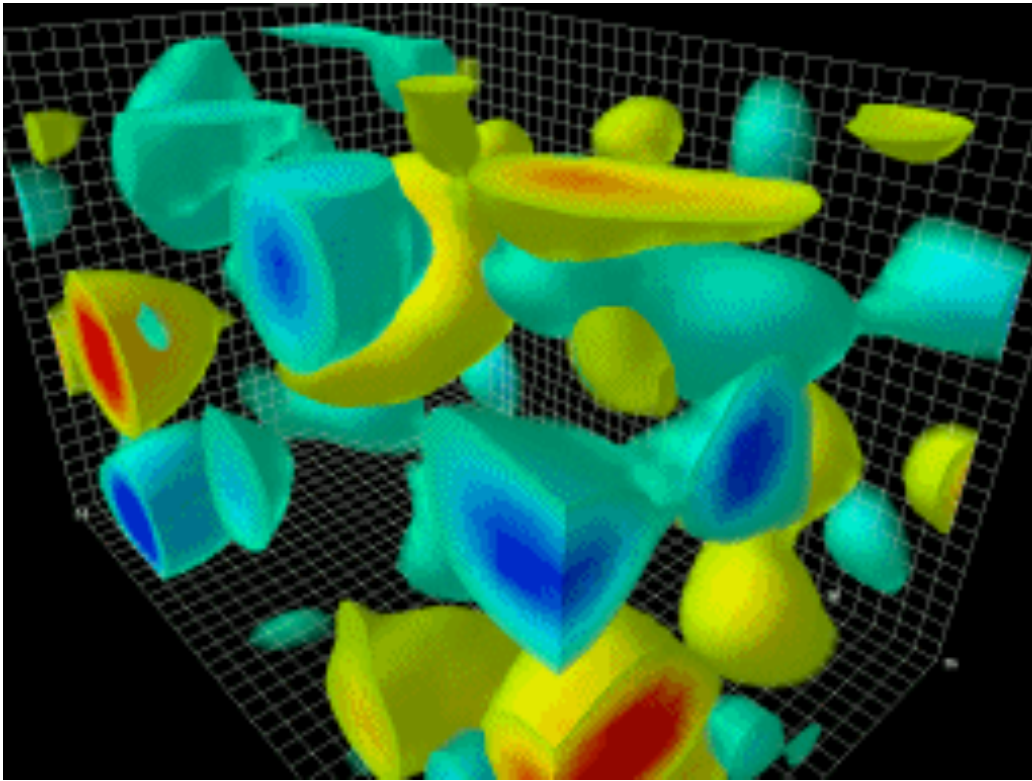
CME and Beam Energy Scan

**Restoration of chiral symmetry only at high enough beam energy
—> beam energy dependence is crucial!**



- * **We'd like to see a chiral QGP above certain threshold energy via CME**
- * **We'd like to see its turning off at low enough energy**

From Gluon Topology to Quark Chirality



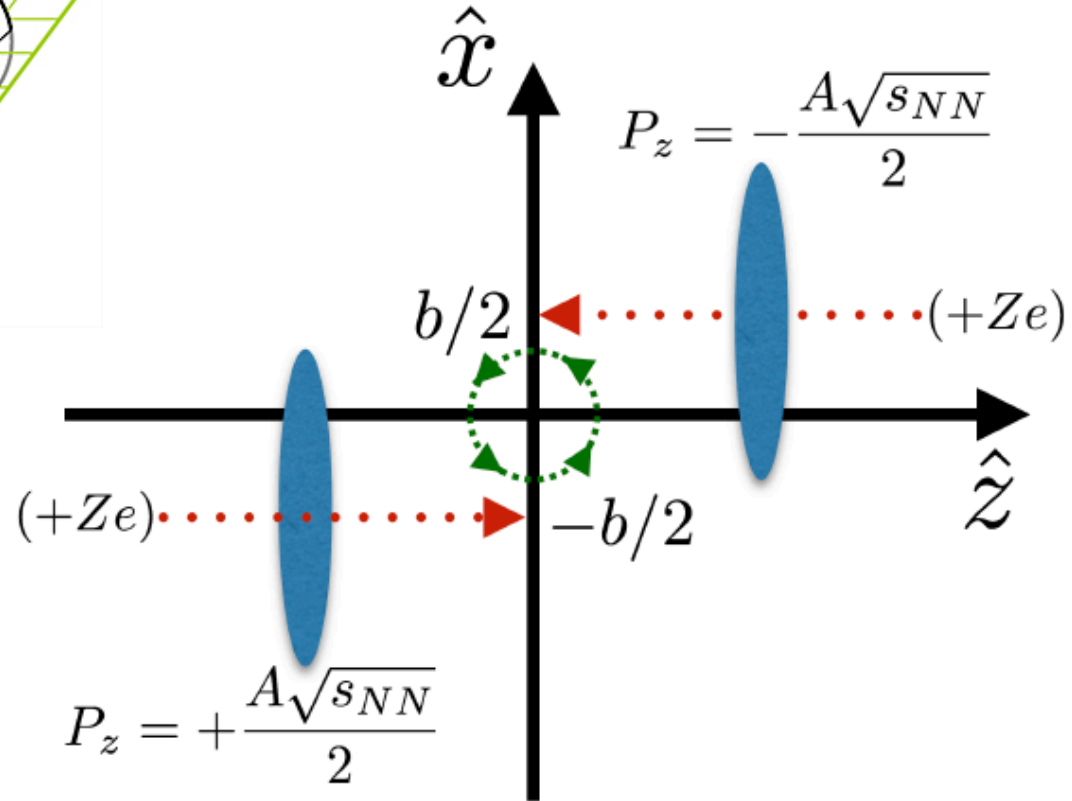
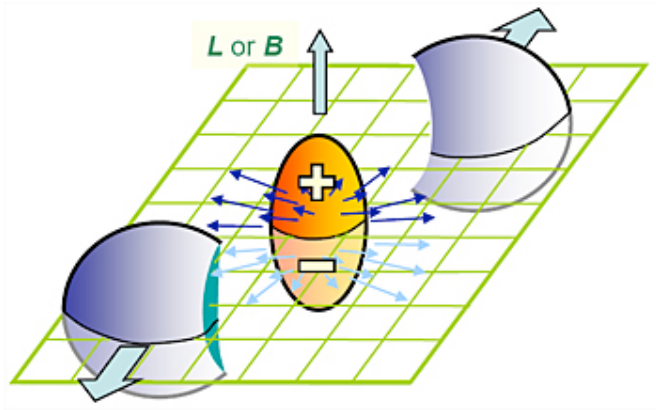
$$Q_w = \frac{1}{32\pi^2} \int d^4x (gG_a^{\mu\nu}) \cdot (g\tilde{G}_{\mu\nu}^a)$$

$$N_5(t \rightarrow +\infty) - N_5(t \rightarrow -\infty) = \frac{g^2}{16\pi^2} \int dt d^3\mathbf{r} G_a^{\mu\nu} \tilde{G}_{\mu\nu}^a$$

QCD anomaly: gluon topology \rightarrow chirality imbalance

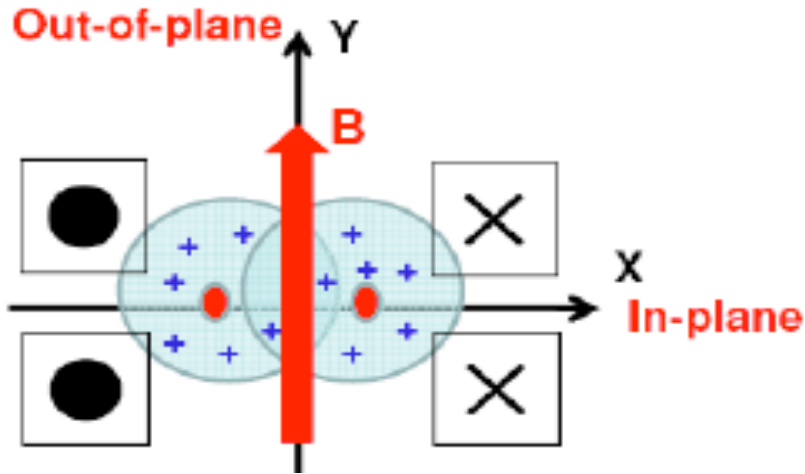
$$N_R - N_L = N_5 = 2Q_w$$

Strong Electromagnetic Fields

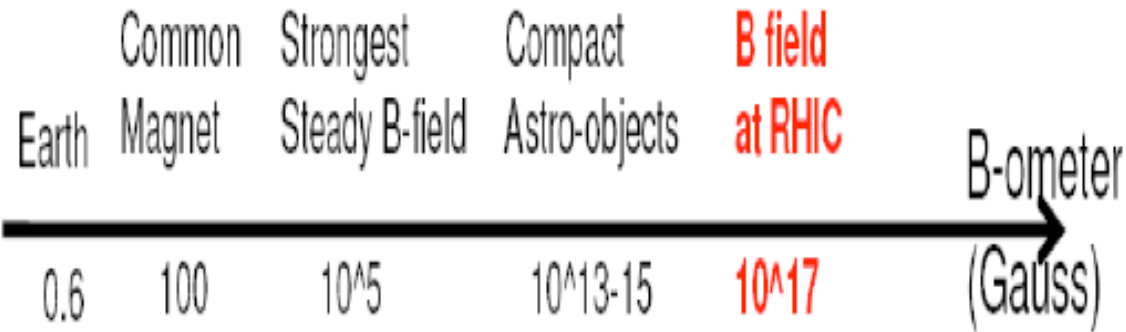


**Large angular momentum together with large (+Ze) nuclear charge
→ strong magnetic field!**

Strong Electromagnetic Fields



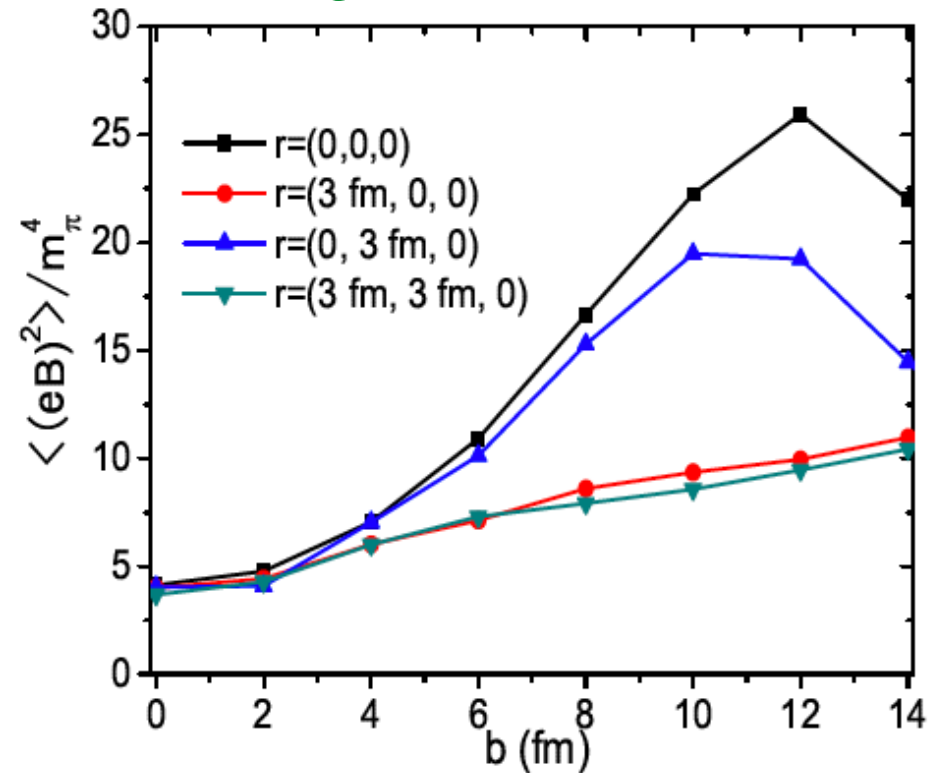
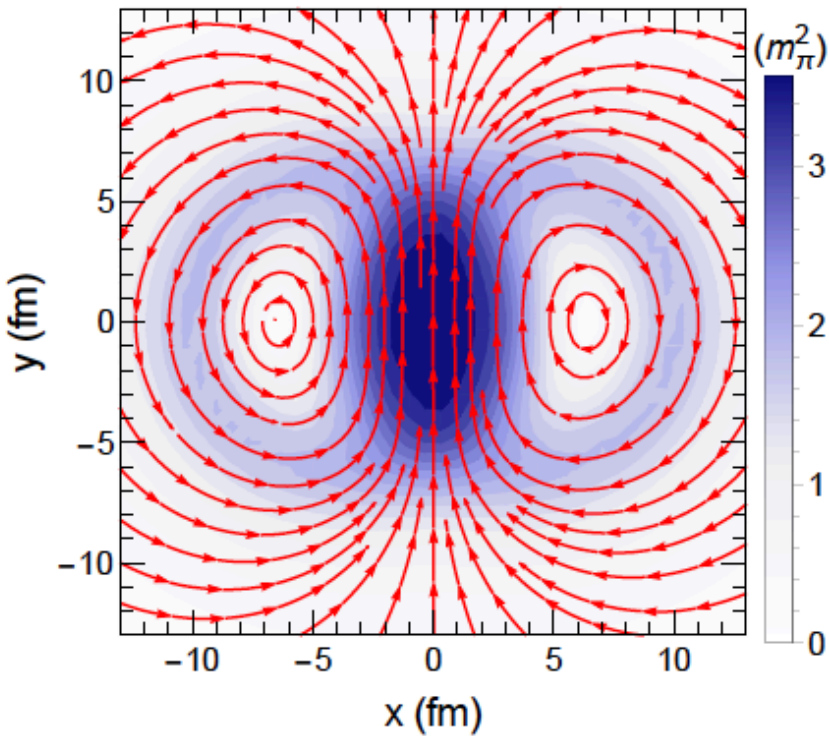
$$E, B \sim \gamma \frac{Z\alpha_{EM}}{R_A^2} \sim 3m_\pi^2$$



- **Strongest B field (and strong E field as well) naturally arises!**
[Kharzeev, McLerran, Warringa; Skokov, et al; Bzdak-Skokov; Deng-Huang; Skokov-McLerran; Tuchin; ...]
- “Out-of-plane” orientation (approximately)
[Bloczynski-Huang-Zhang-Liao]

Strong Electromagnetic Fields

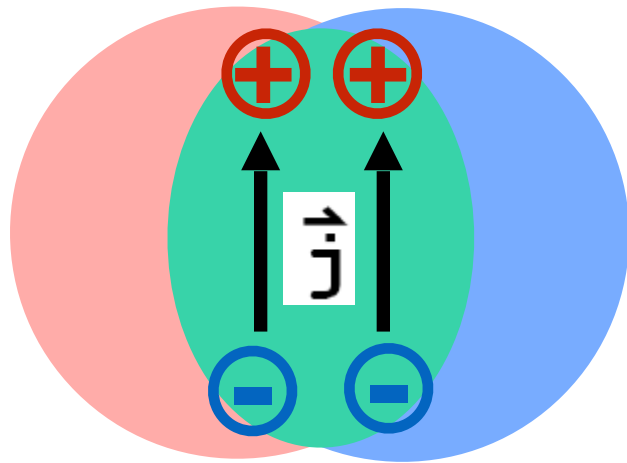
Huang, Liao, et al PLB2012



Quantitative simulations confirm the existence of such extreme fields!

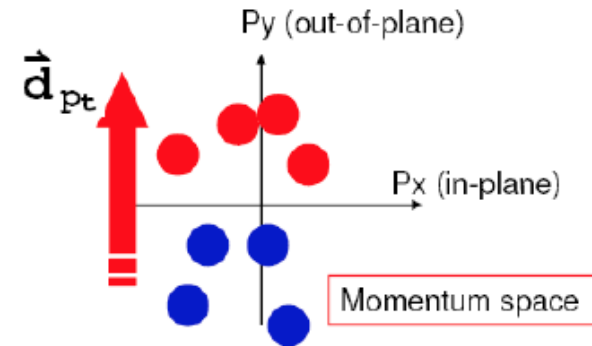
[STAR measurements of di-electron — direct hint?! PRL2018]

From CME Current to Charge Separation



$$\vec{J} = \sigma_5 \mu_5 \vec{B}$$

**strong radial blast:
position \rightarrow momentum**



**Charge Separation or
Electric Dipole in Pt Space
(along out-of-plane)**

[Kharzeev 2004; Kharzeev, McLerran, Warringa, 2008; ...]

$$\frac{dN_{\pm}}{d\phi} \propto \dots + a_{\pm} \sin(\phi - \Psi_{RP})$$

$$\langle a_{\pm} \rangle \sim \pm \langle \mu_5 \rangle B$$

Very difficult measurement:

- * **Zero average, only nonzero variance;**
- * **Correlation measurement with significant backgrounds;**
- * **Signal likely very small**

Experimental Observable

charge separation \Rightarrow charge dept. two-particle correlation

Voloshin, 2004

$$\gamma = \langle \cos(\Delta\phi_i + \Delta\phi_j) \rangle = \langle \cos\Delta\phi_i \cos\Delta\phi_j \rangle - \langle \sin\Delta\phi_i \sin\Delta\phi_j \rangle$$

$$\delta = \langle \cos(\Delta\phi_i - \Delta\phi_j) \rangle = \langle \cos\Delta\phi_i \cos\Delta\phi_j \rangle + \langle \sin\Delta\phi_i \sin\Delta\phi_j \rangle$$

$$\gamma = \kappa v_2 F - H$$

F: Bulk Background

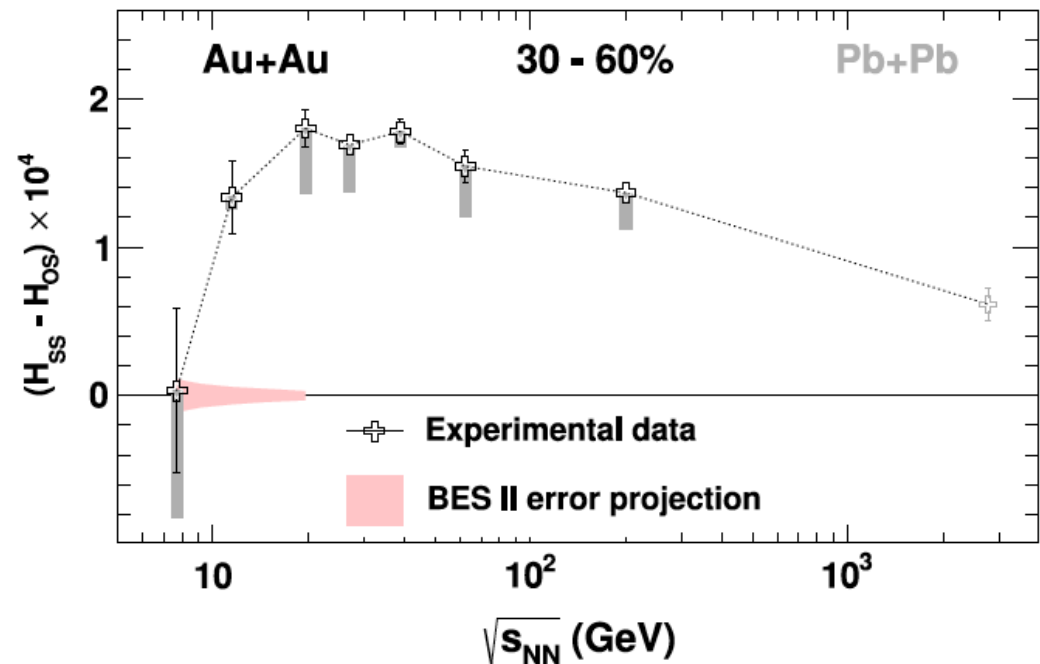
$$\delta = F + H$$

H: Possible Pure CME Signal = $(a_{1,CME})^2$

Bzdak, Koch, JL, 2012

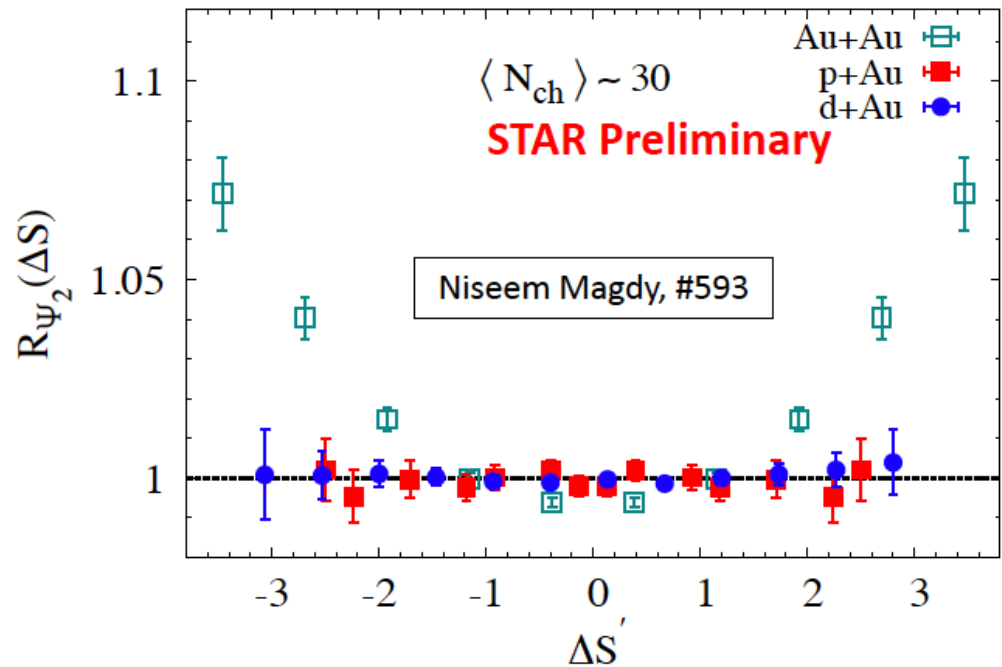
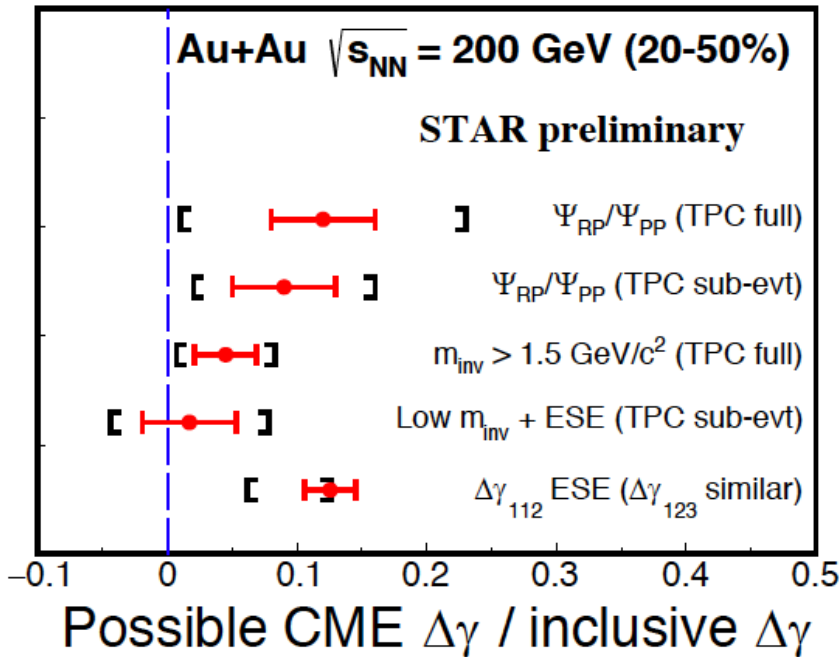
$$H_{SS} - H_{OS} \leftrightarrow 2(a_1)^2$$

*Many interesting proposals
of new observables!*



STAR PRL2014

Recent Exp. Search Status



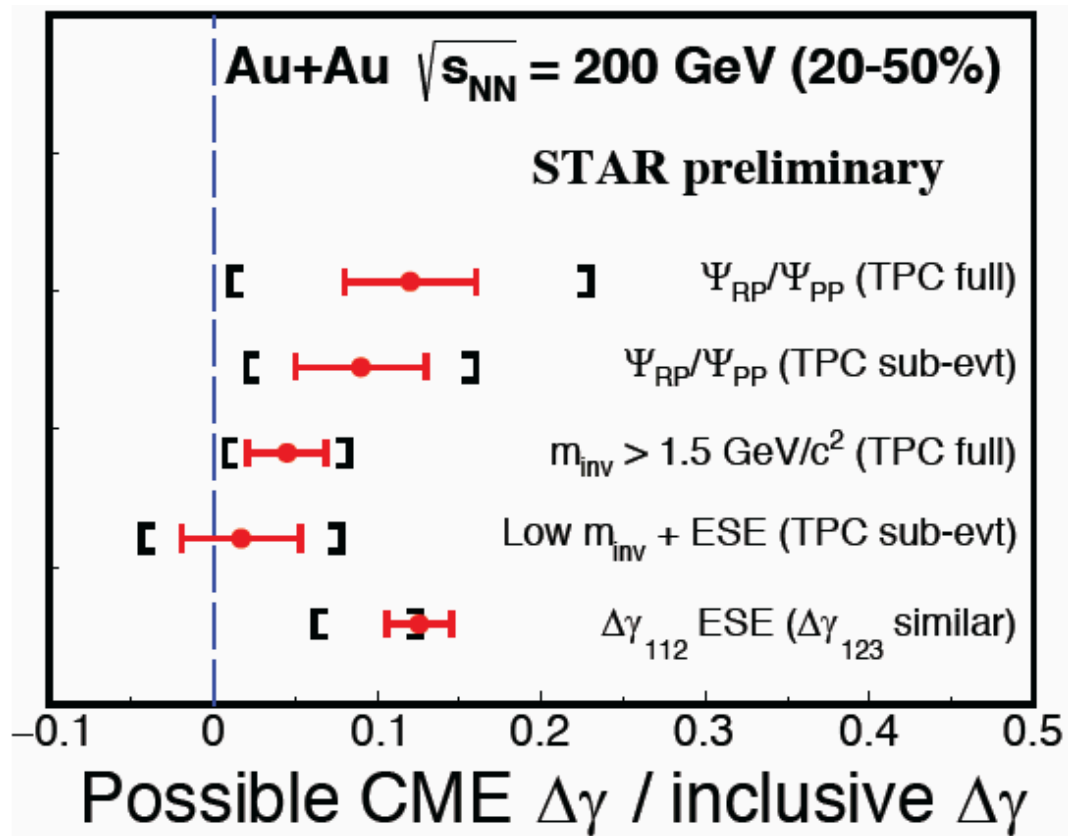
[From Z. Ye, STAR Summary Talk @ QM2018]

ALICE @ LHC 2.76TeV: signal level possibly about 8~10%

CMS @ LHC 5.02TeV: signal level no more than 4%

The trend with beam energy seems in line with expectation!

MORE Consistent with Being NONZERO?!



A “naive” statistical interpretation: (8.5 +/- 1.2) % .
It is MORE consistent with being NONZERO @ 200GeV!

Encouraging experimental evidence for CME in QGP
— can we quantitatively compute CME signal?

AVFD Framework

**[Not discussed here: calculations based on transport framework,
e.g. works by X. Huang, G. Ma, Y. Ma, J. Xu, C.M. Ko,]**

Fluid Dynamics That Knows Left & Right

conservation
law:

$$\partial_\mu J^\mu = 0 \longrightarrow \partial_\mu J^\mu = C E^\mu B_\mu$$

constituent
relation:

$$J^\mu = n u^\mu + \nu^\mu$$

$$\partial_\mu S^\mu \geq 0$$

$$\nu^\mu = -\sigma T P^{\mu\nu} \partial_\nu \left(\frac{\mu}{T} \right) + \sigma E^\mu + \xi \omega^\mu + \xi_B B^\mu$$

[Son, Surowka, 2009;...]

CVE

CME

**Microscopic quantum anomaly emerges as
macroscopic anomalous hydrodynamic currents!**

*It would be remarkable to actually “see” this new
hydrodynamics at work in real world materials!*

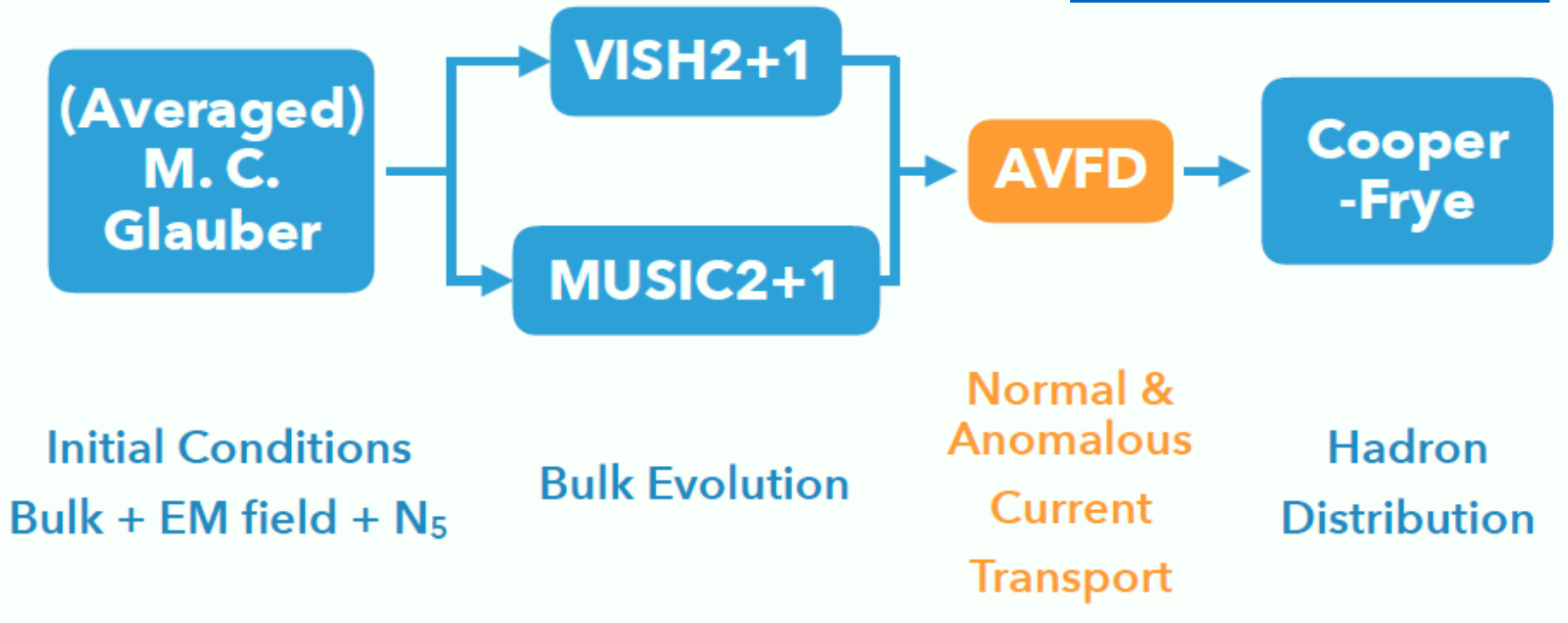
The AVFD Framework



The AVFD Framework

[arXiv:1611.04586](https://arxiv.org/abs/1611.04586)

[arXiv:1711.02496](https://arxiv.org/abs/1711.02496)



AVFD:
Anomalous-Viscous Fluid Dynamics

The AVFD Framework

Anomalous-Viscous Fluid Dynamics

$$D_\mu J_R^\mu = + \frac{N_c q^2}{4\pi^2} E_\mu B^\mu \quad D_\mu J_L^\mu = - \frac{N_c q^2}{4\pi^2} E_\mu B^\mu$$

$$J_R^\mu = n_R u^\mu + v_R^\mu + \frac{N_c q}{4\pi^2} \mu_R B^\mu \quad \text{CME}$$

$$J_L^\mu = n_L u^\mu + v_L^\mu - \frac{N_c q}{4\pi^2} \mu_L B^\mu$$

Viscous Effect

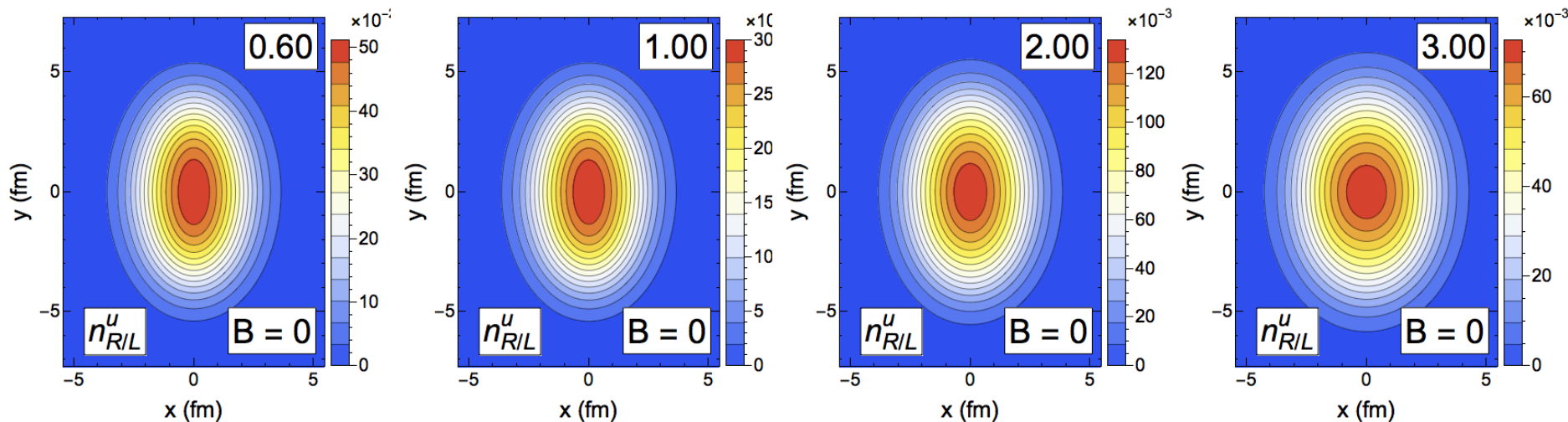
$$\Delta^{\mu\nu} d v_{R,L}^\nu = - \frac{1}{\tau_{\text{rlx}}} (v_{R,L}^\mu - v_{\text{NS}}^\mu)$$

$$v_{\text{NS}}^\mu = \frac{\sigma}{2} T \Delta^{\mu\nu} \partial_\nu \frac{\mu}{T} + \frac{\sigma}{2} q E^\mu$$

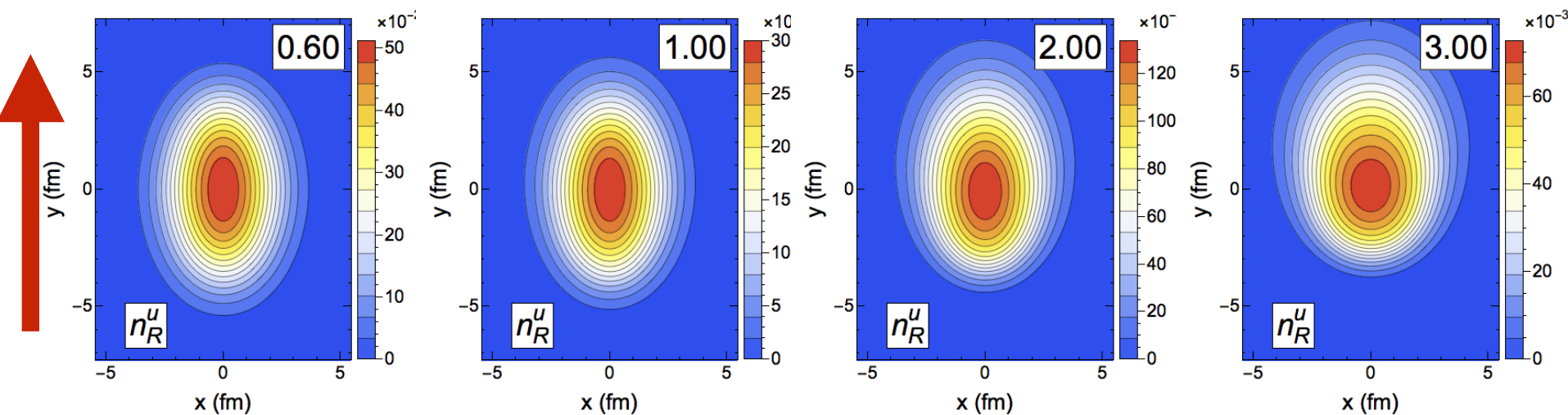
on top of VISH2+1D -- OSU Group

[We now also have MUSIC-AVFD!]

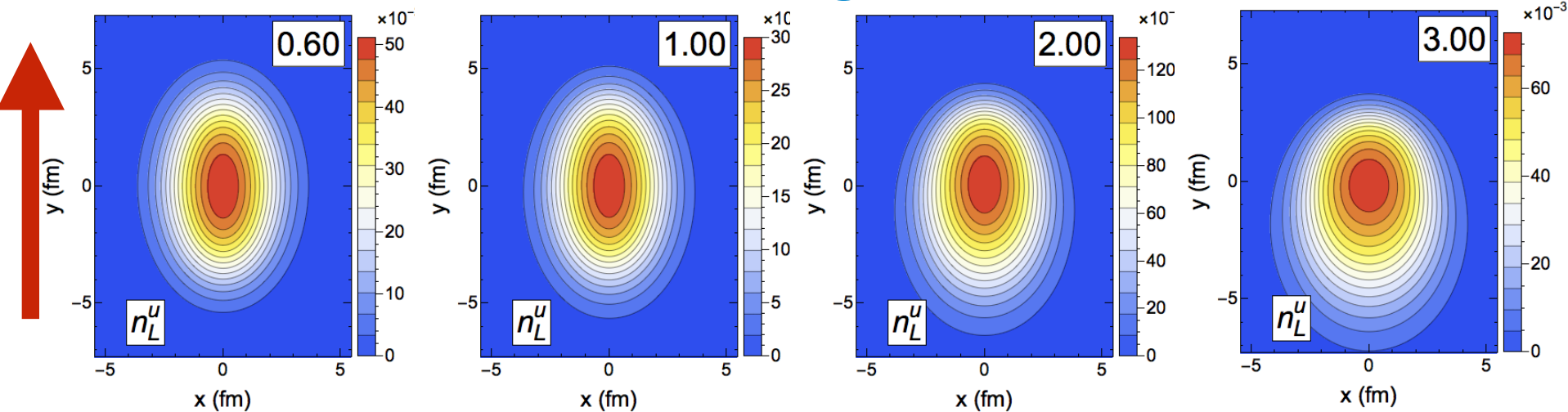
Demonstrating the AVFD



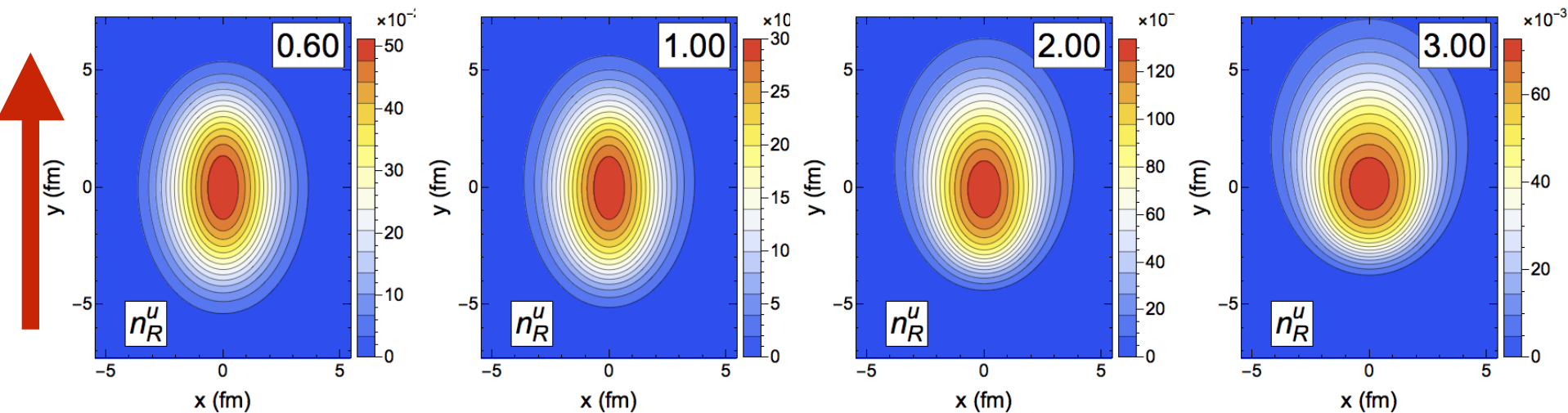
Upper: NO magnetic field
Lower: with B field (along y+ direction)



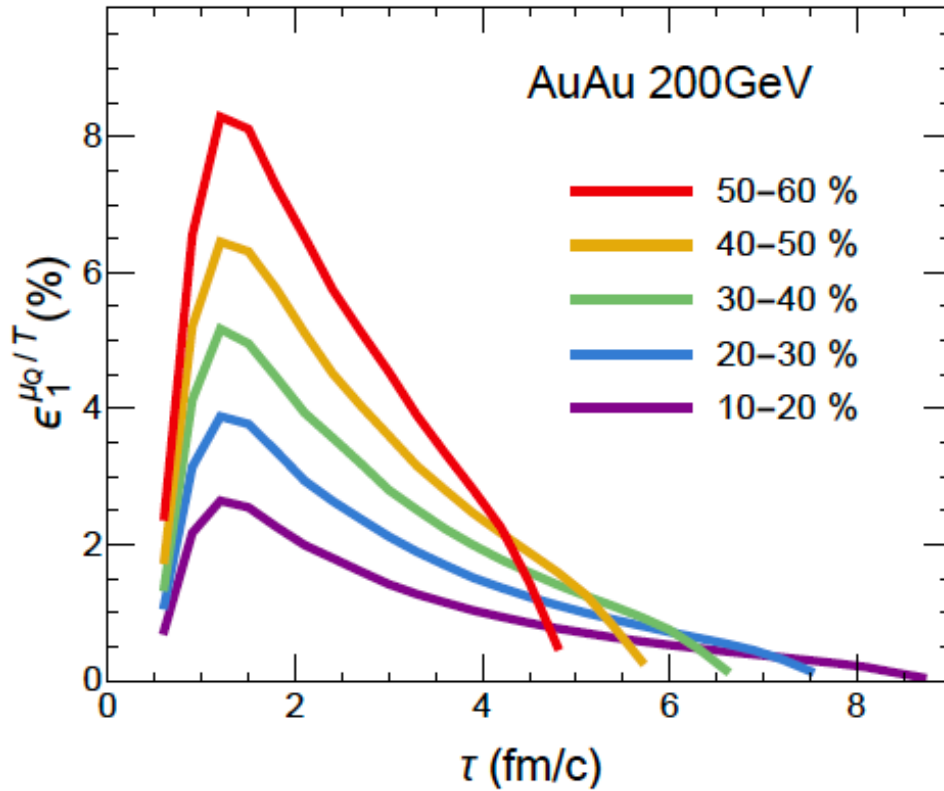
Demonstrating the AVFD



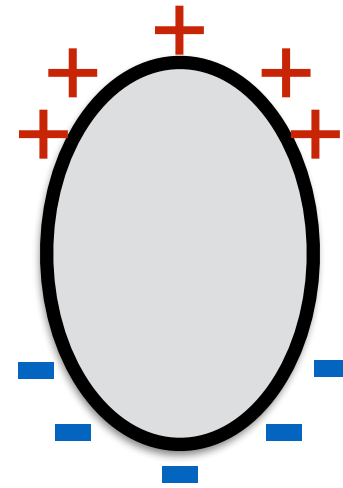
Upper: Left-Handed (LH), with B field (along y+ direction)
Lower: Right-Handed (RH), with B field (along y+ direction)



The Charge Separation from AVFD



$$E \frac{dN}{d^3p}(x^\mu, p^\mu) = \frac{g}{(2\pi)^3} \int_{\Sigma_{fo}} p^\mu d^3\sigma_\mu f(x, p)$$



B field $\otimes \mu_5 \Rightarrow$ current \Rightarrow dipole (charge separation)

$$dN_{\pm}/d\phi \propto 1 + 2 a_{1\pm} \sin(\phi - \psi_{RP}) + \dots$$

$$H_{SS} - H_{OS} \leftrightarrow 2(a_1)^2$$

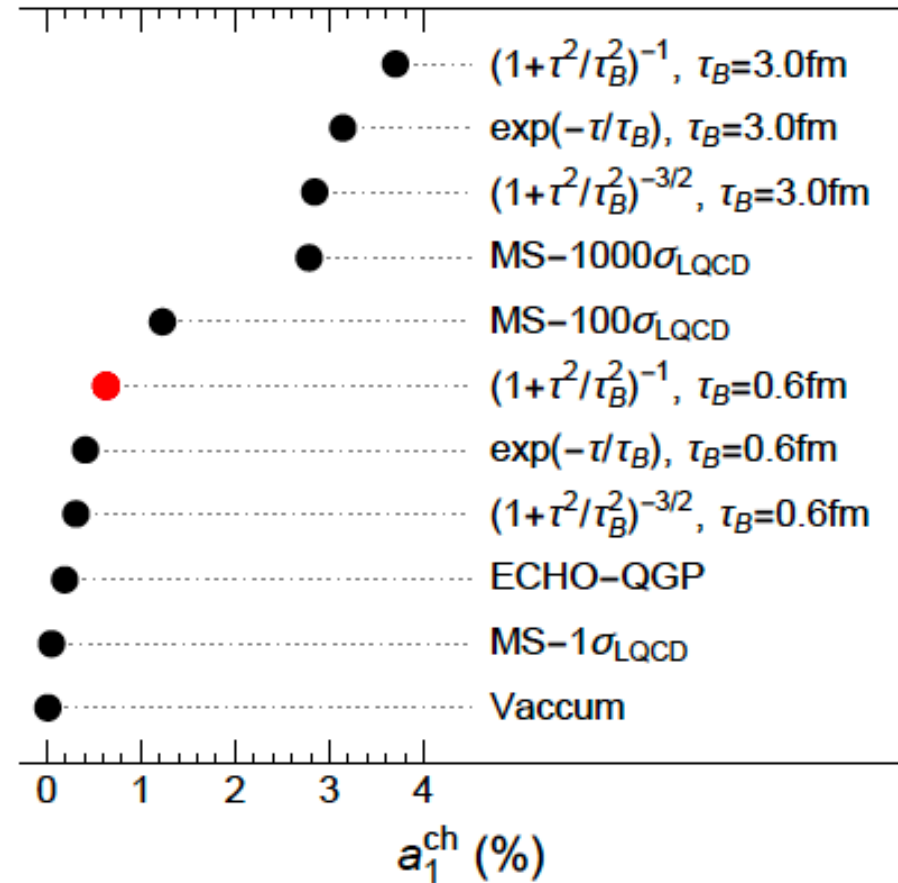
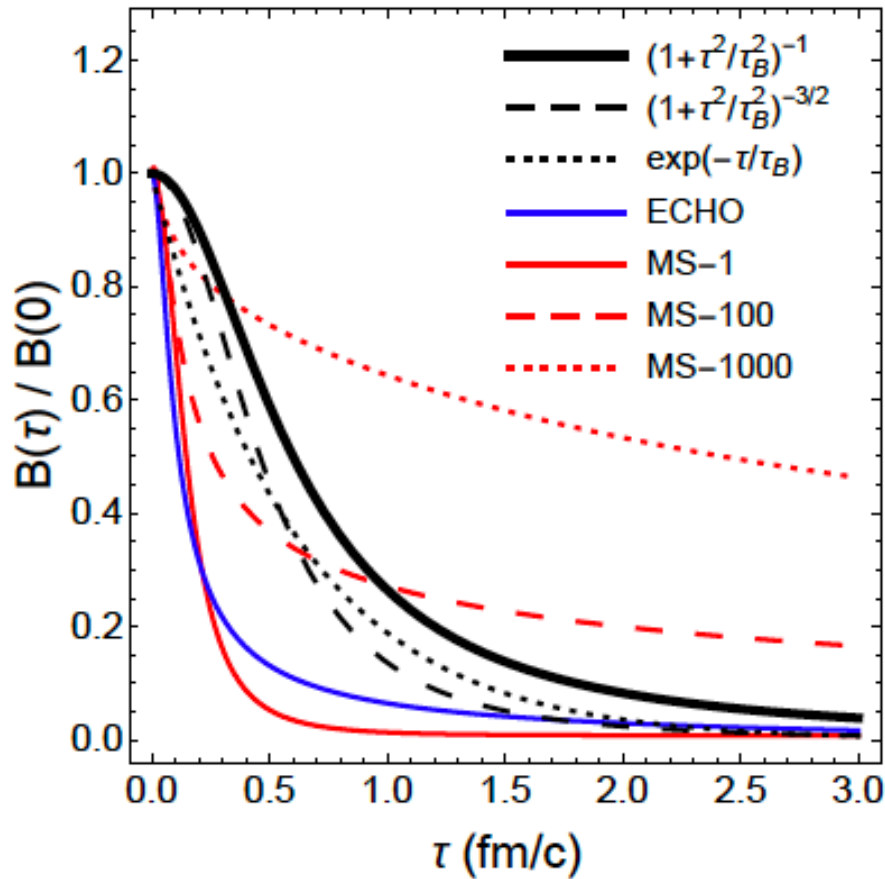
AVFD Results for AuAu Collisions

We now have a versatile tool to quantitatively understand and answer many important questions about CME in heavy ion collisions!

arXiv:1611.04586

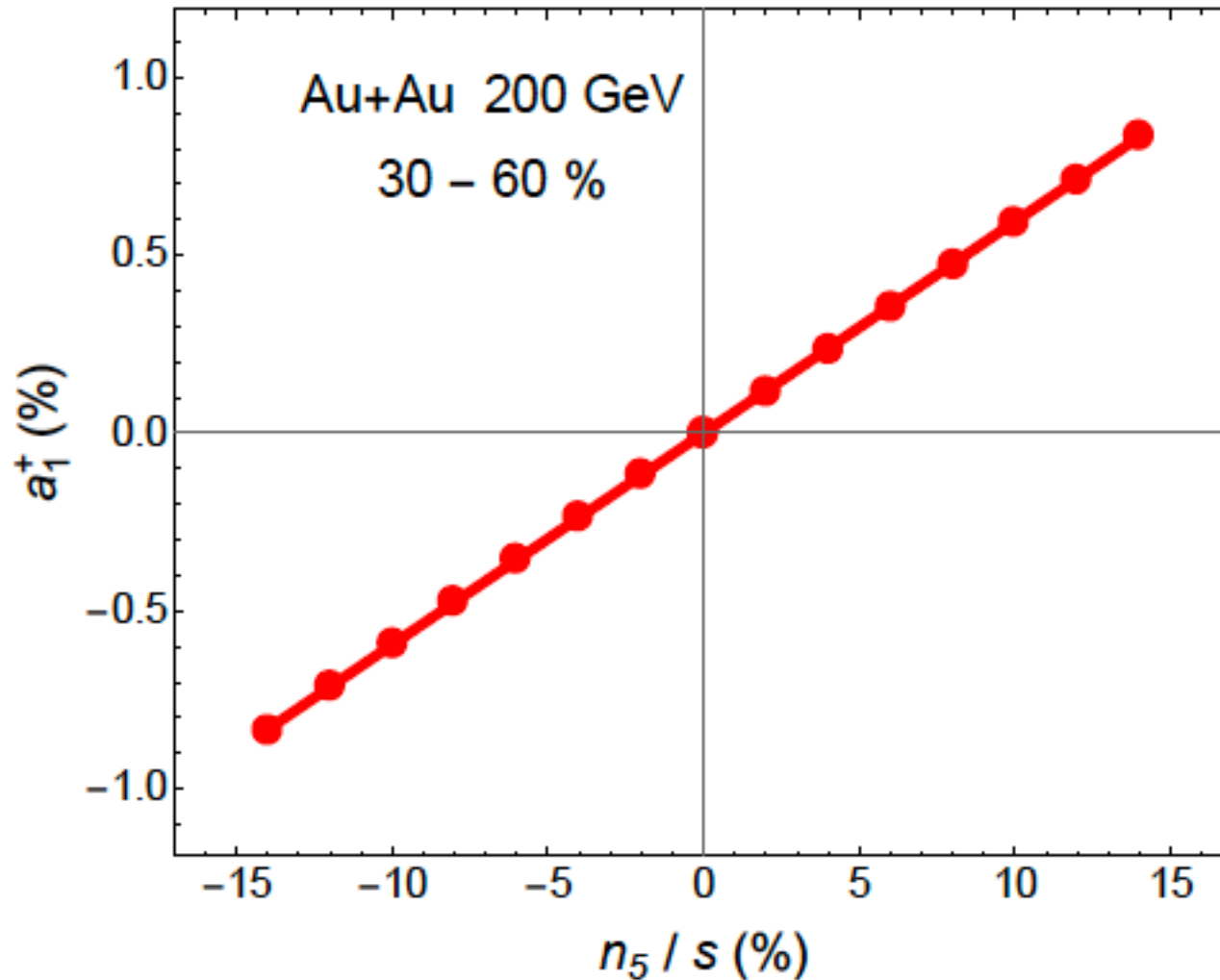
arXiv:1711.02496

The Influence of the Magnetic Field



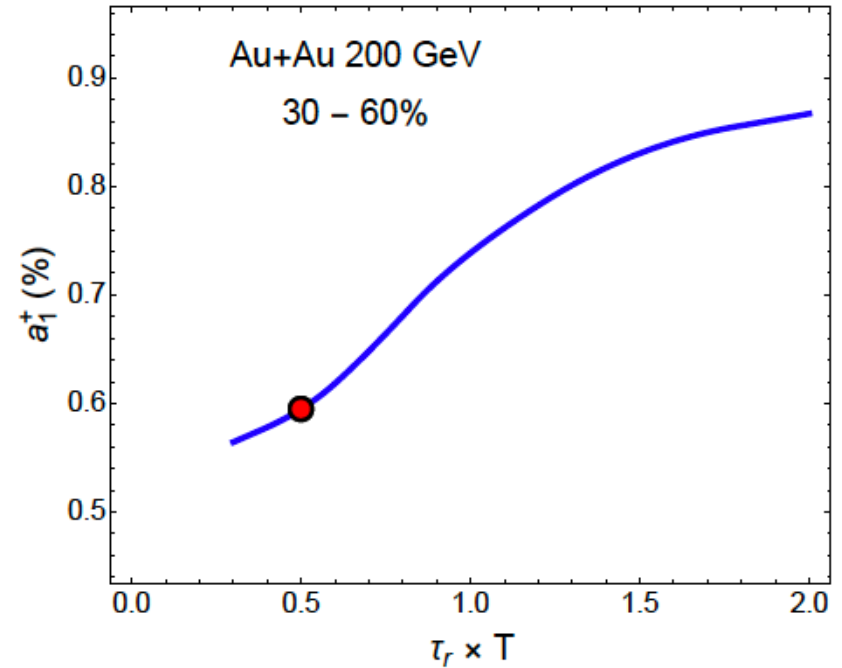
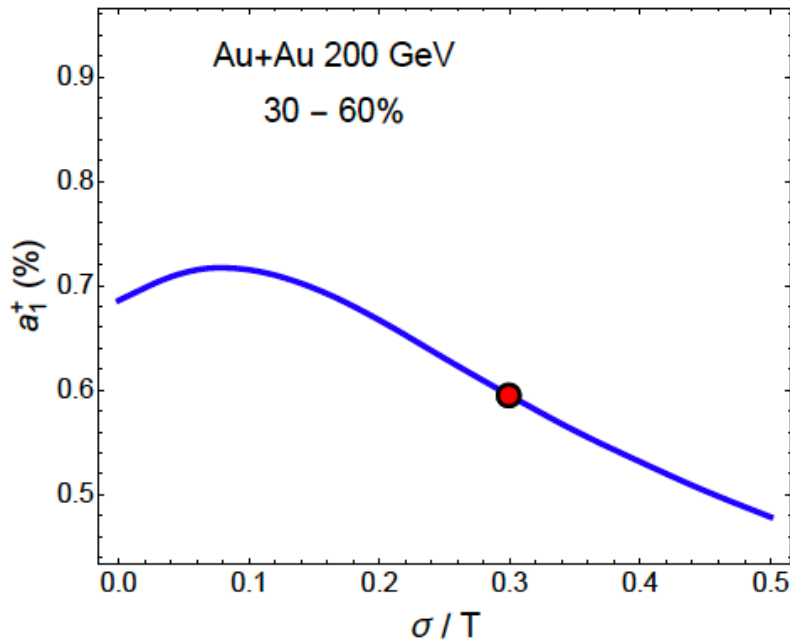
**Strong influence by B field evolution;
Significant theoretical uncertainty!**

The Axial Charge Initial Condition



**Very sensitive to initial axial charge;
Significant theoretical uncertainty!**

The Influence of the Viscous Transport

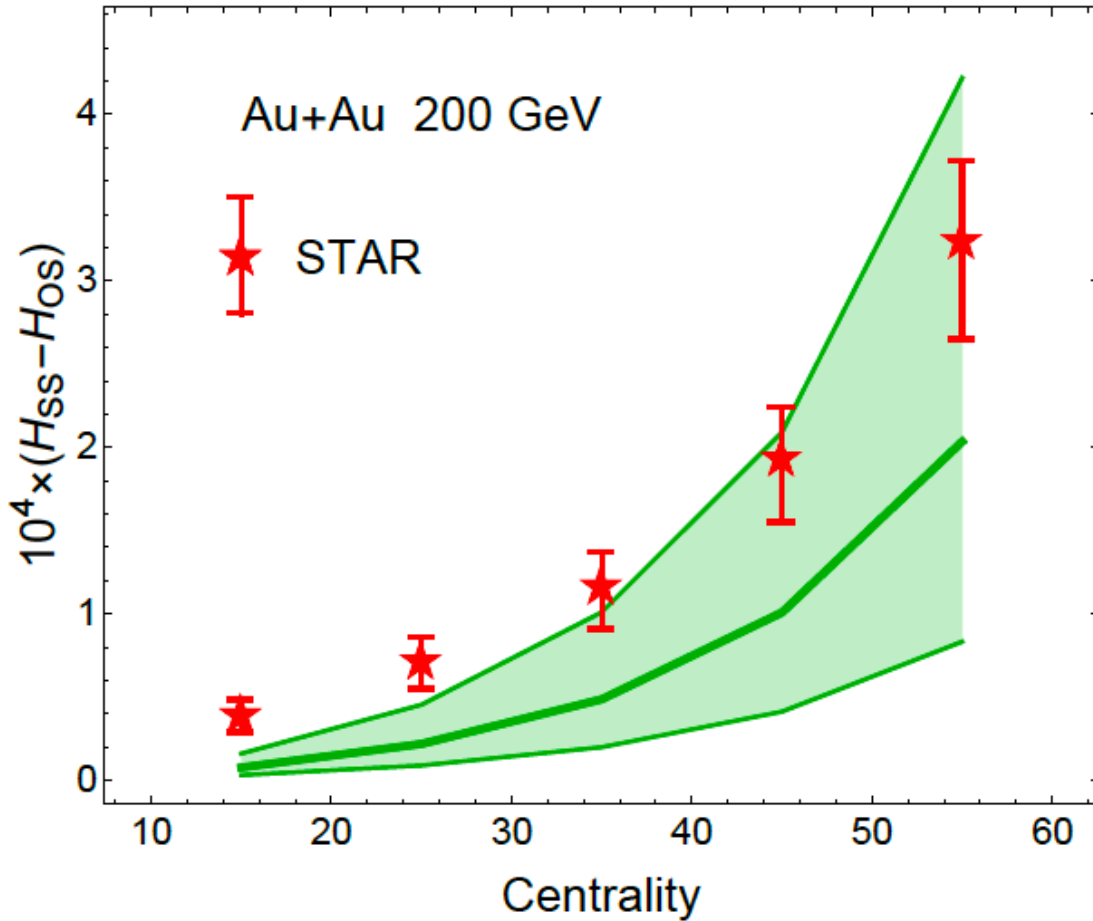


$$\Delta_{\nu}^{\mu} d v_{R,L}^{\nu} = -\frac{1}{\tau_{\text{rlx}}} (v_{R,L}^{\mu} - v_{\text{NS}}^{\mu})$$

$$v_{\text{NS}}^{\mu} = \frac{\sigma}{2} T \Delta^{\mu\nu} \partial_{\nu} \frac{\mu}{T} + \frac{\sigma}{2} q E^{\mu}$$

First calibration for the influence of the viscous transport on charge separation signal!

AVFD Predictions v.s Experimental Data



$$B(\tau) = \frac{B_0}{1 + (\tau/\tau_B)^2}$$

$$\tau_B = 0.6 \text{ fm}/c$$

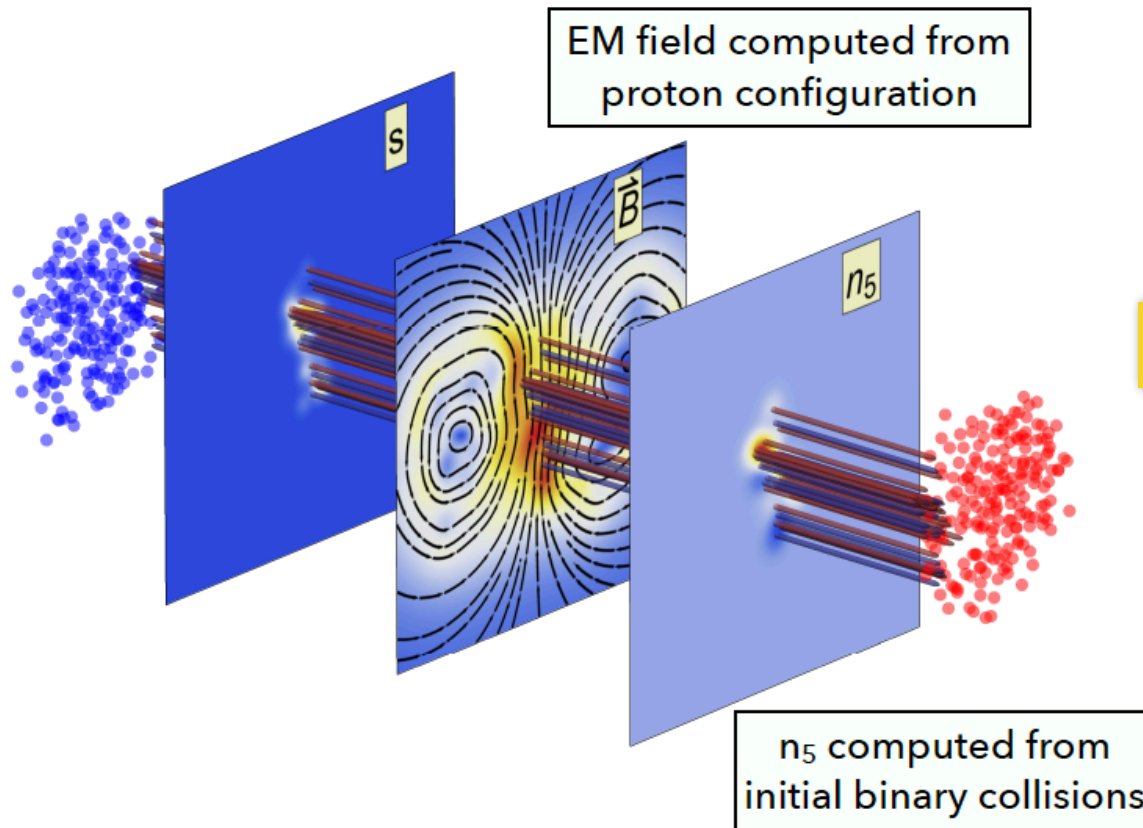
$$\sqrt{\langle n_5^2 \rangle} \simeq \frac{Q_s^4 (\pi \rho_{tube}^2 \tau_0) \sqrt{N_{coll.}}}{16\pi^2 A_{overlap}}$$

Good agreement !

centrality bin	10-20%	20-30%	30-40%	40-50%	50-60%
$eB_0(m_\pi^2)$	2.34	3.10	3.62	4.01	4.19
n_5/s	0.065	0.078	0.095	0.119	0.155

Table 1. Centrality dependence of magnetic field peak strength and the initial chirality imbalance. The n_5/s shown here is obtained with a saturation scale $Q_s^2 = 1.25 \text{ GeV}^2$.

Event-By-Event AVFD



Include EBE fluctuations:

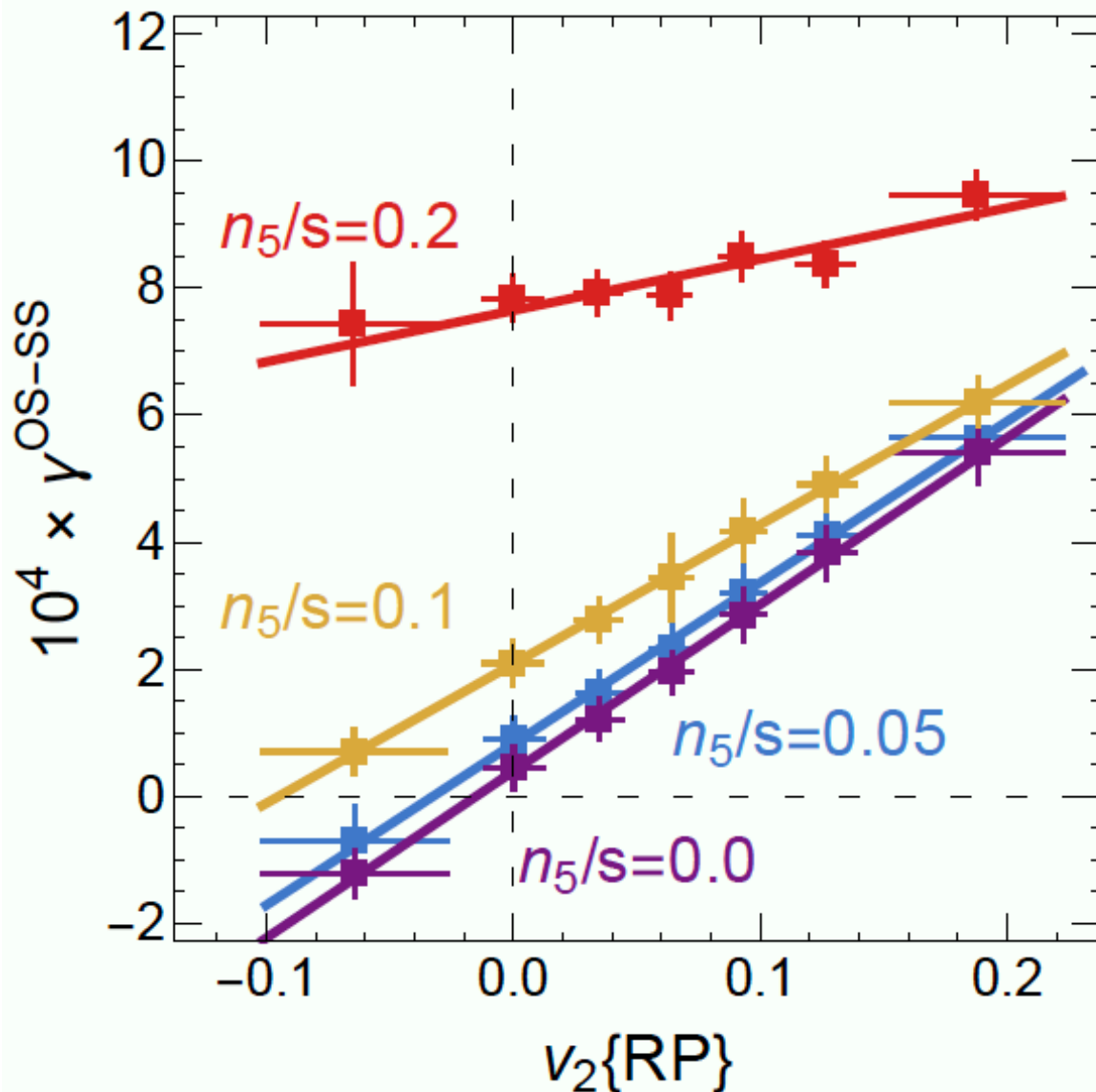
- ▶ Initial Conditions
- ▶ Statistic @ Freeze-out
- ▶ Hadron Cascade

Important for better understanding:

- * *Interplay between signal and BKG;*
- * *Experimental analysis methods*

EBE-AVFD for Event-Shape Engineering

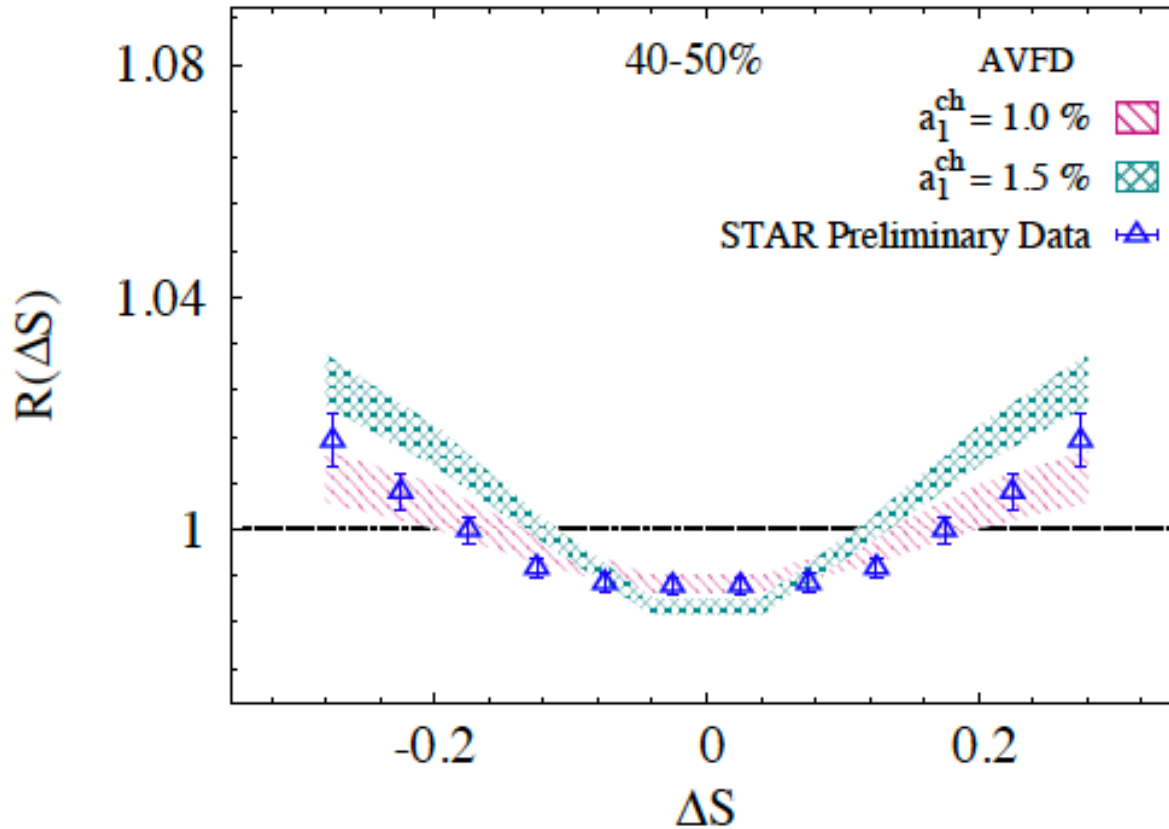
Au-Au @ 200GeV 50-60%



The intercept is very sensitive to the CME contribution!

Slope depends on CME too: naive subtraction may not be good.

EBE-AVFD for R-Correlator



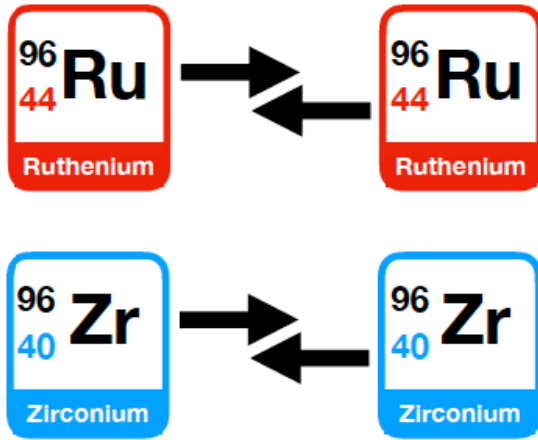
*Magdy, Lacey, et al,
arXiv:1710.01717;
arXiv:1803.02416*

R-correlator sensitively responds to CME contribution.

EBE-AVFD Predictions for CME in Isobaric Collisions (Newest results!)

*Shi, Zhang, Hou, JL, in final preparation, to appear soon;
Shi, Zhang, Hou, JL, contribution in QM18 proceedings.*

Using Isobaric Collisions for CME Search



Key idea: contrasting two systems with identical bulk, varied magnetic fields.

***Charge Asymmetry
Correlation Measurement***

Background

Signal

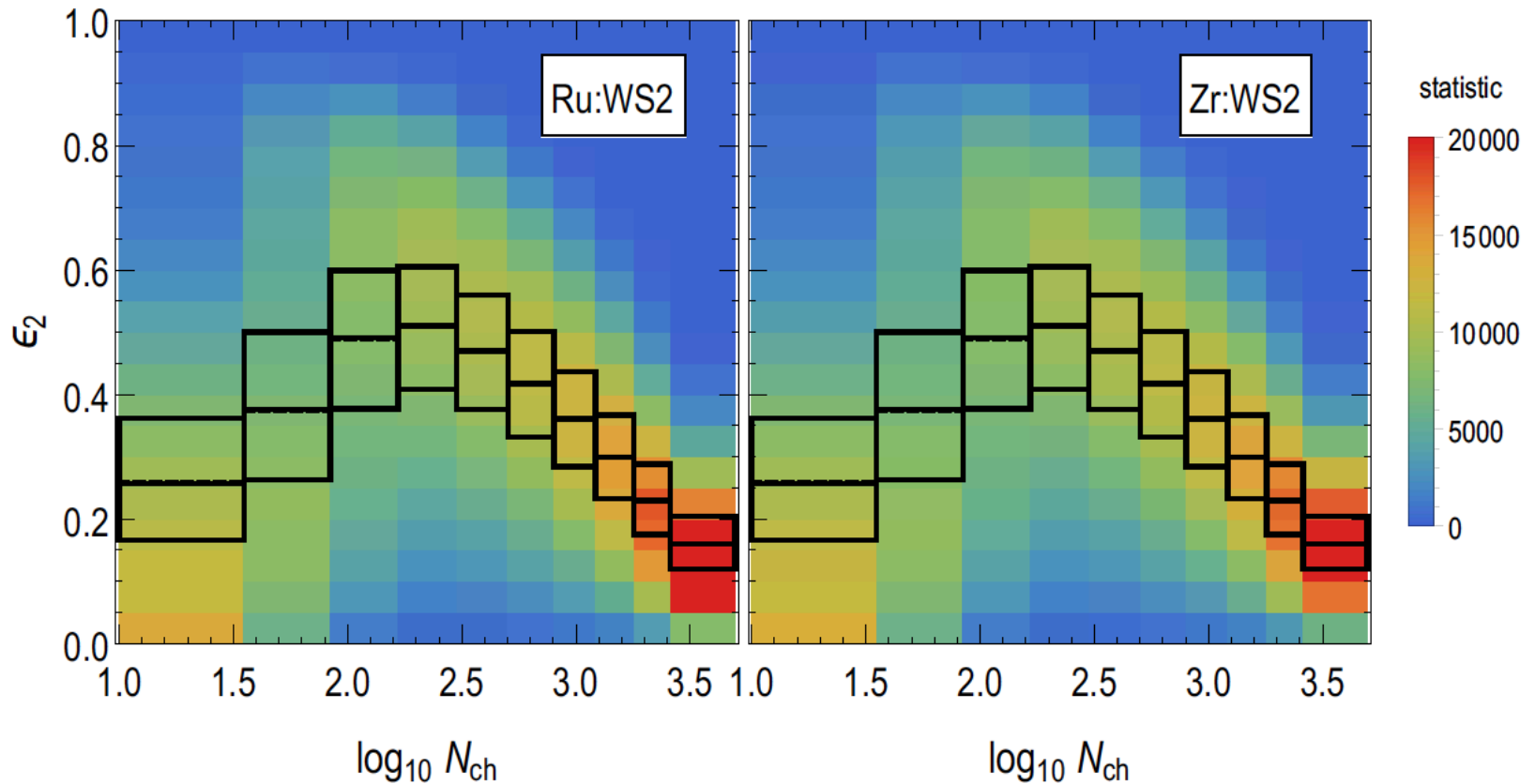
RuRu

Background

Signal

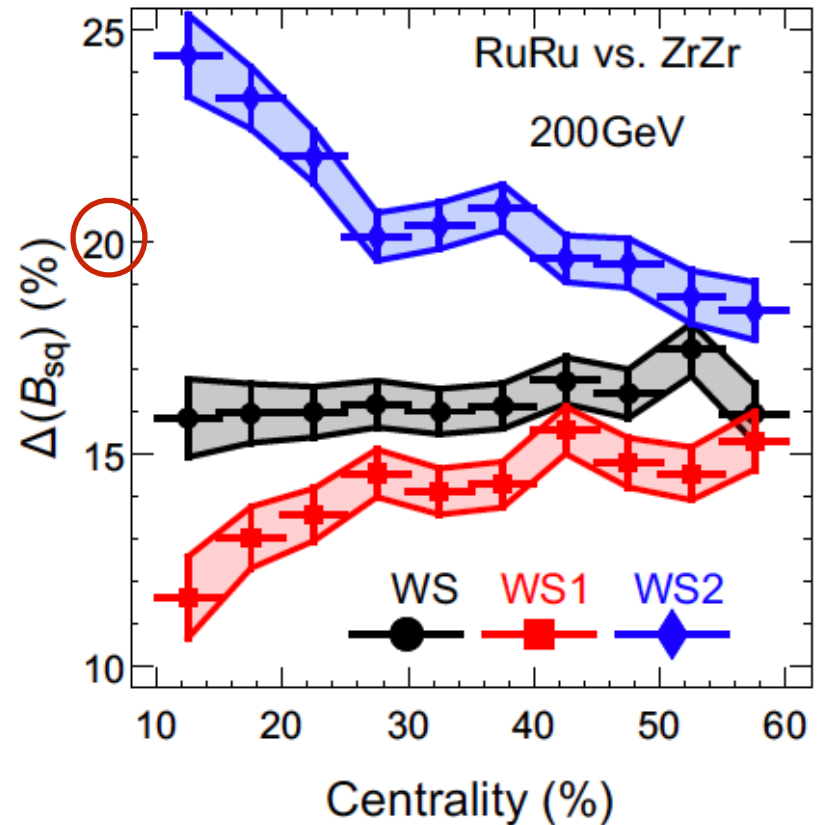
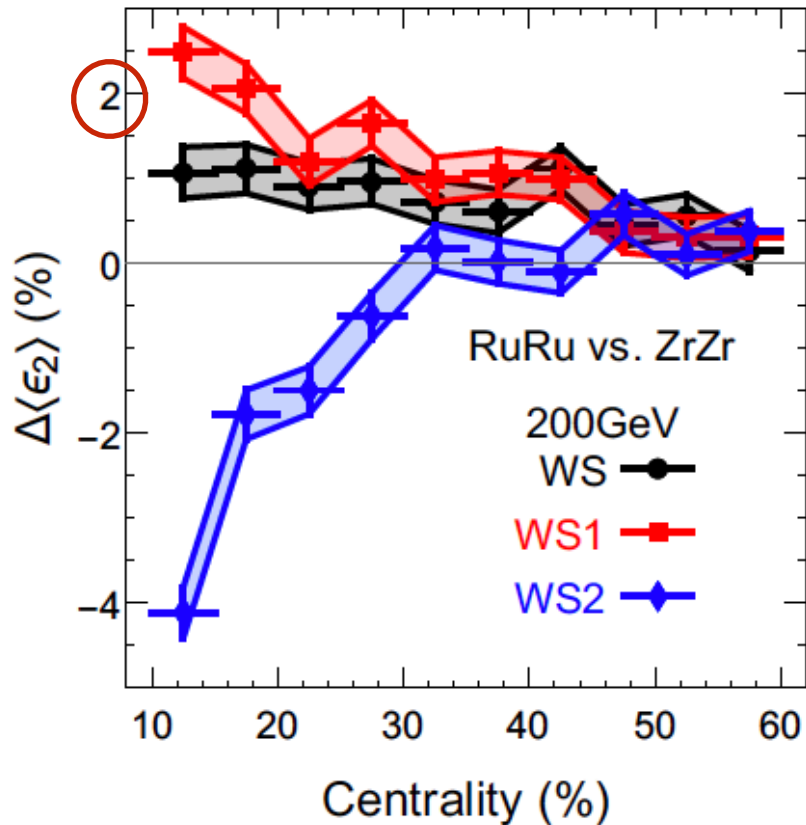
ZrZr

How to Choose Identical Systems?



*Insight from initial conditions:
joint cut on Multiplicity-Eccentricity*

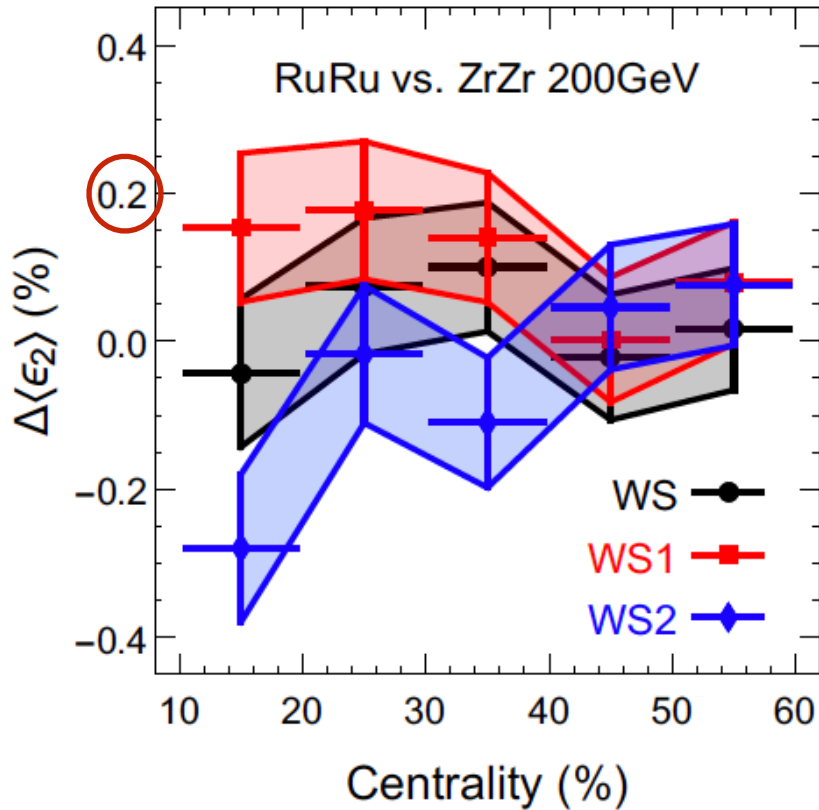
How to Choose Identical Systems?



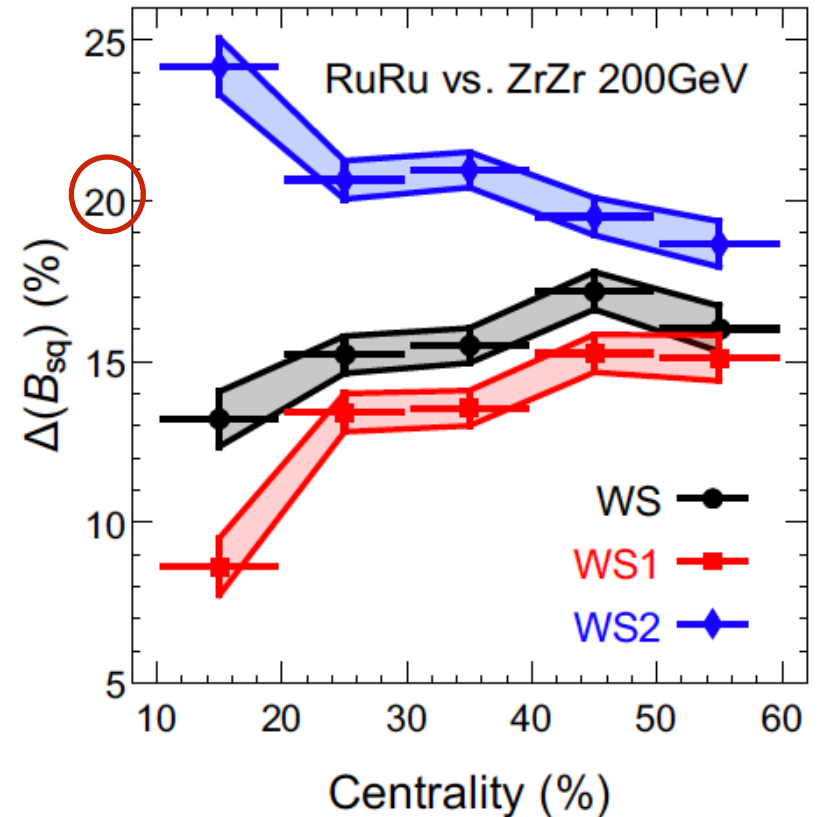
**Conventional centrality bin (without joint-cut):
A few percent level of difference in bulk geometry**

How to Choose Identical Systems?

Eccentricity is guaranteed the same!

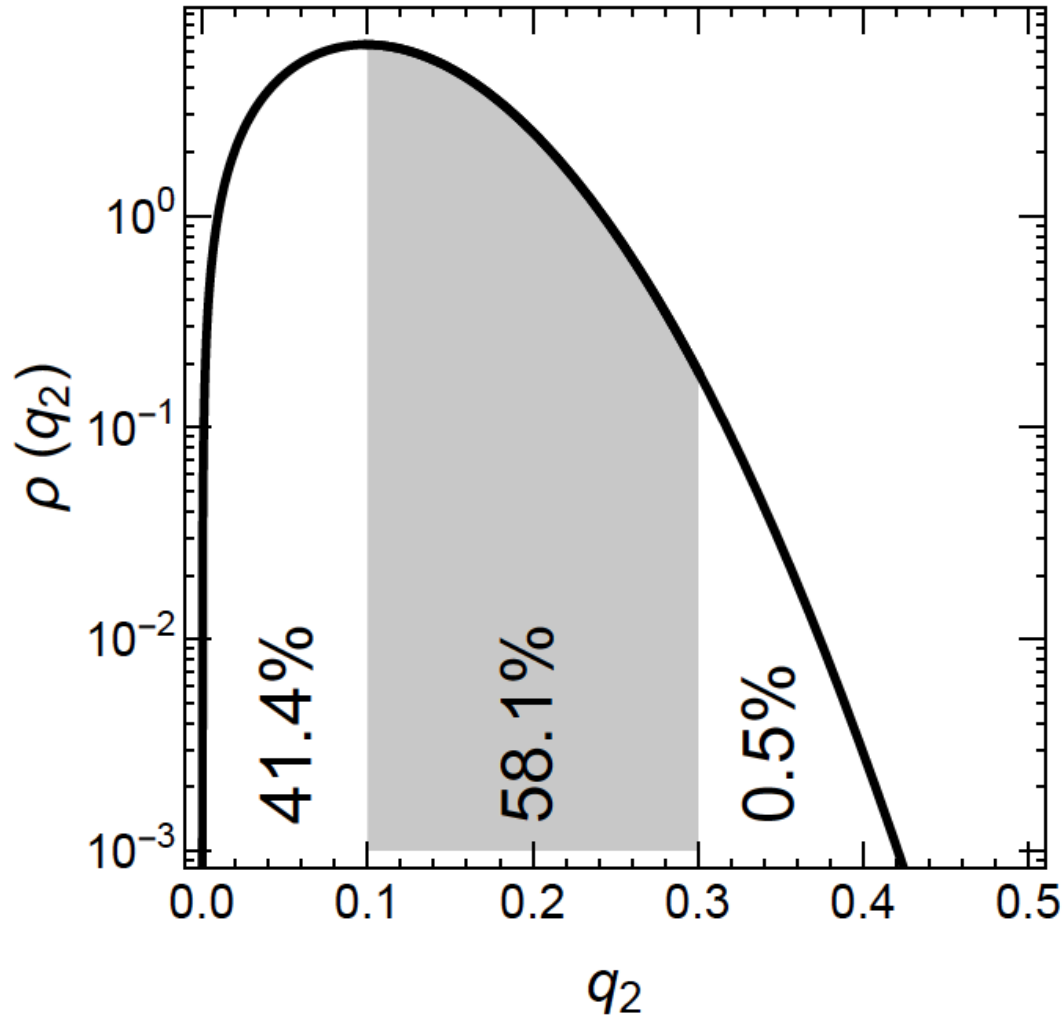


B field differs by 12~20% !



After joint-cut:
Vanishing difference in eccentricity,
Sizable difference in magnetic fields!!!

Analyzing Actual EBE-AVFD Events for Isobars

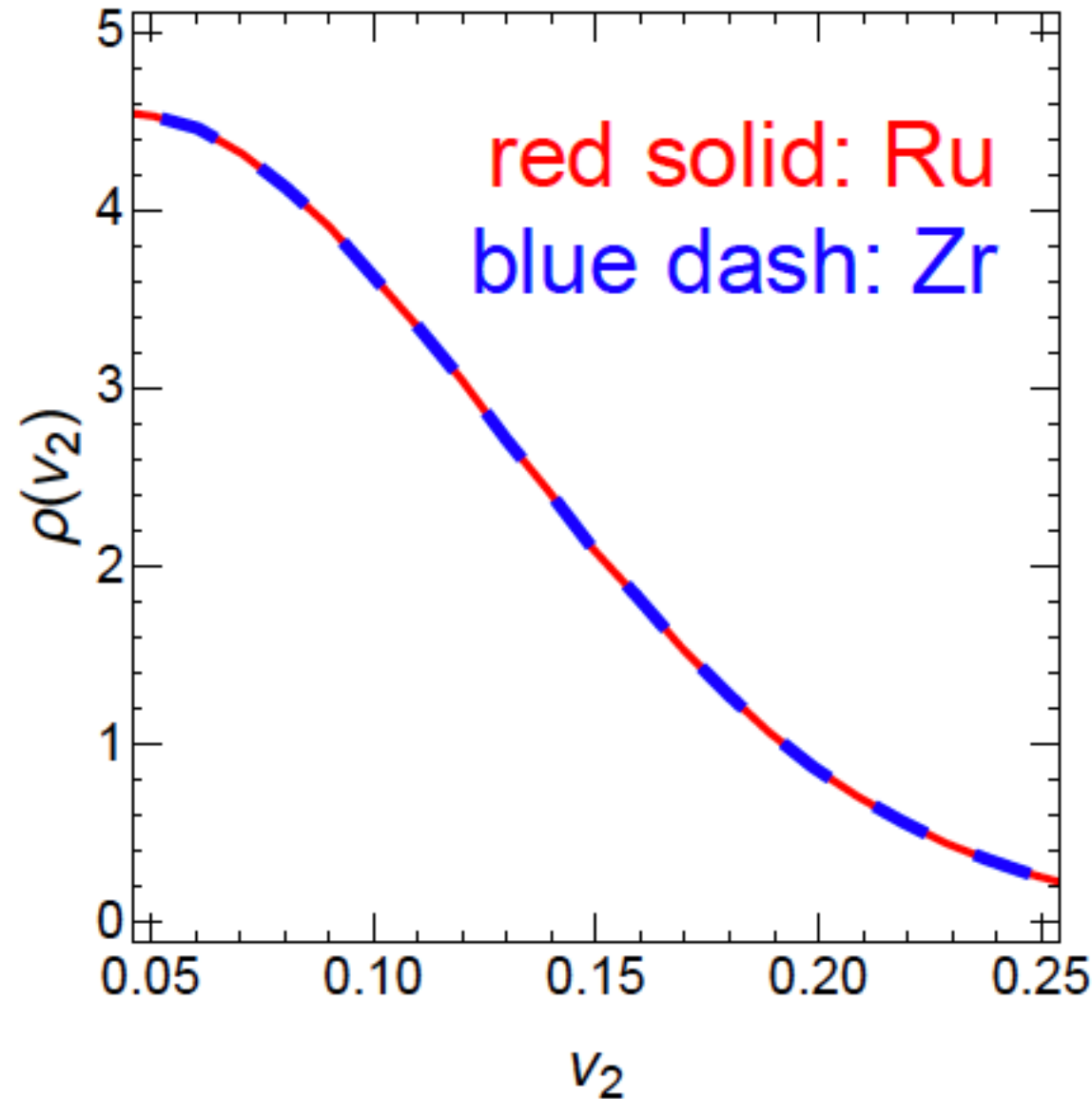


**100M EBE-AVFD events:
Subject to joint-cut**

$64 < N_{\text{ch}}, |y| < 1 < 96$

$0.1 < q_2 < 0.3$

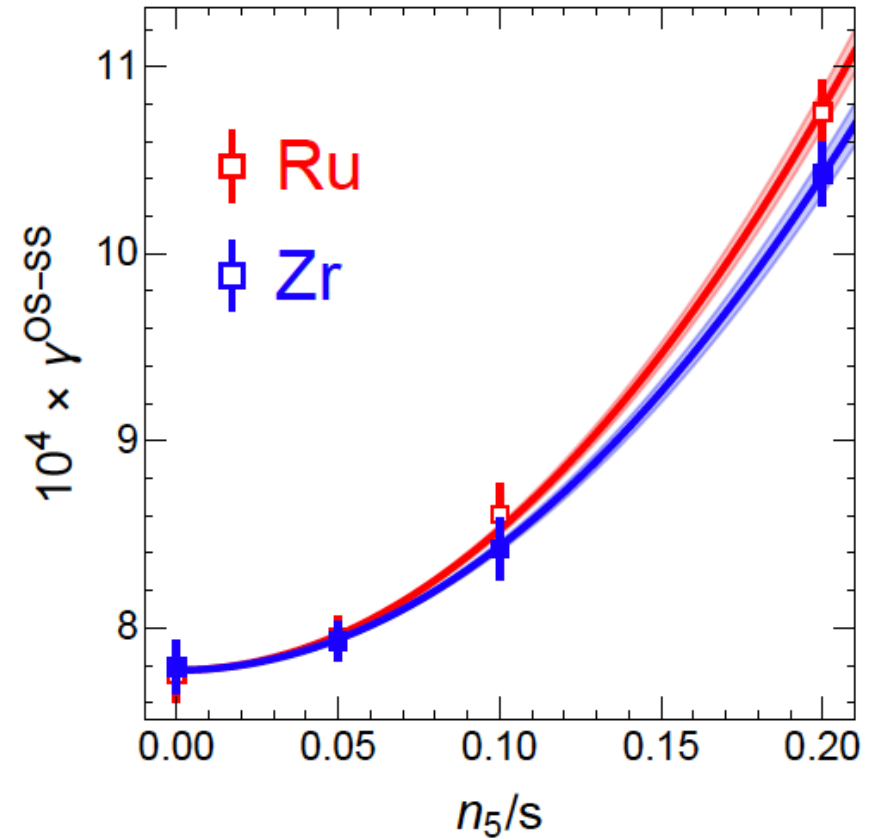
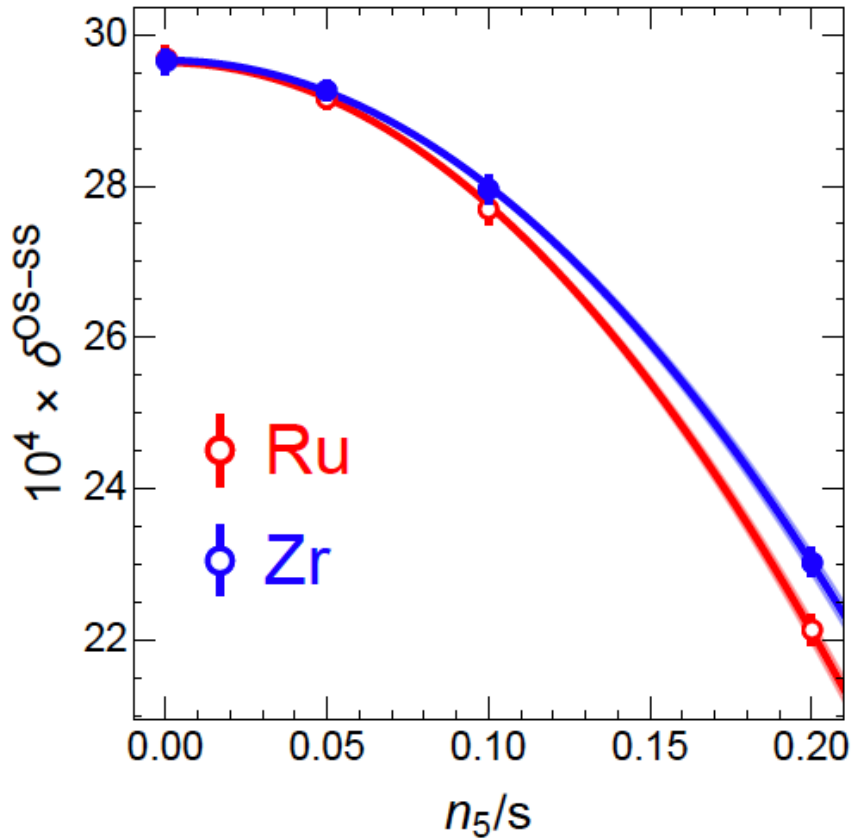
Analyzing Actual EBE-AVFD Events for Isobars



**Post-selection
double-check:
Identical v_2 !**

*Getting two identical
sample of isobar
events for contrast*

Correlation Observables of Isobars from AVFD

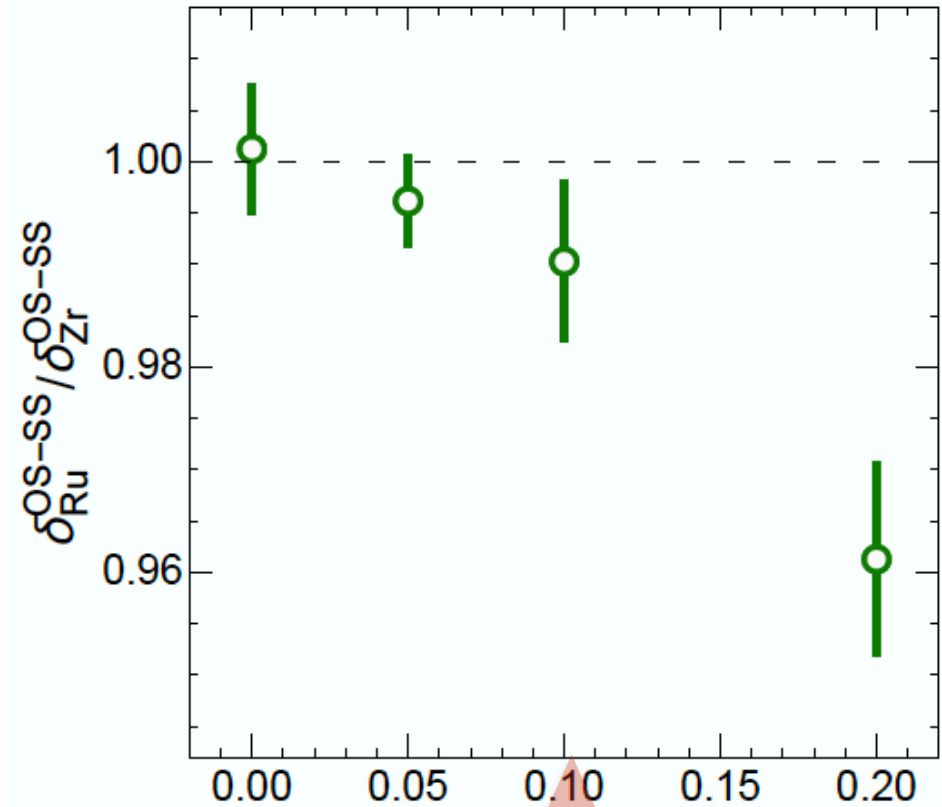
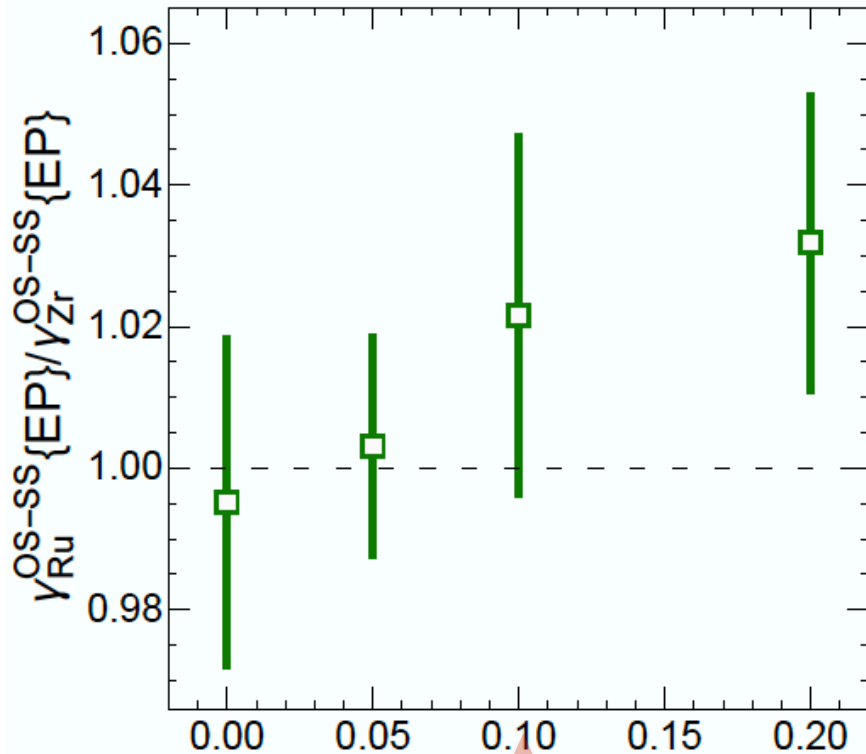


Difference in correlations is very sensitive to CME contribution!

Both gamma and delta are important to look at!

Correlation Observables of Isobars from AVFD

Exp. statistics are expected to shrink error bar by a factor of ~10



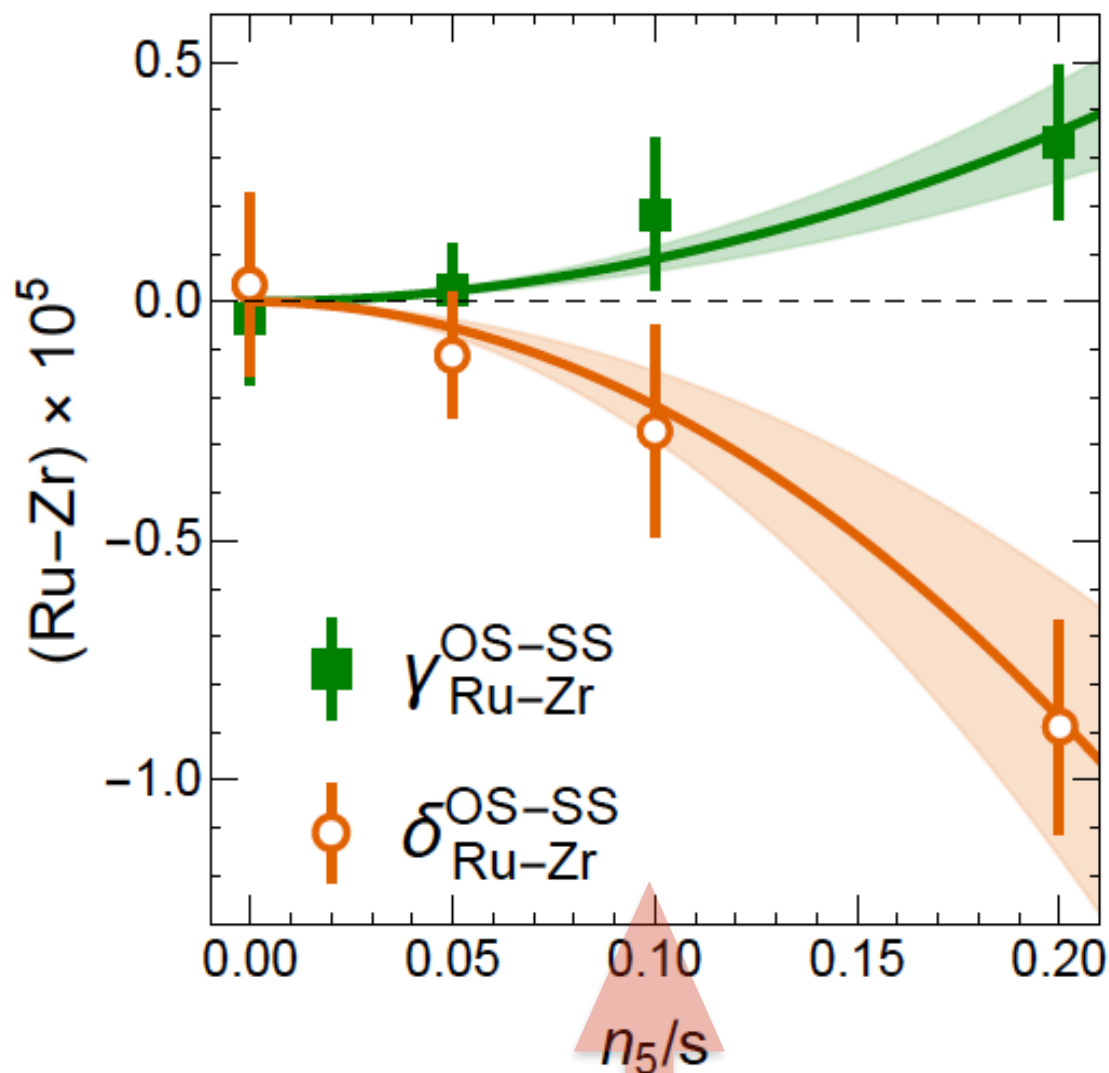
n_5/s

*Projected axial charge level
based on comparison AuAu data*

n_5/s

Both gamma and delta are important to look at!

Absolute Difference between Isobars from AVFD



Exp. statistics are expected to shrink error bar by a factor of ~10

The absolute difference between isobars, after identical multiplicity + elliptic flow cuts: very sensitive and clean probe of CME signal !

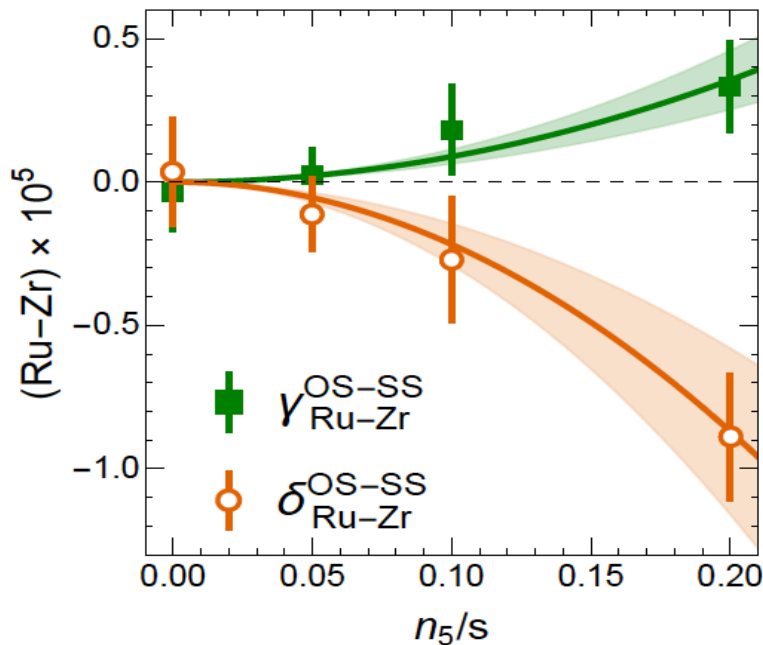
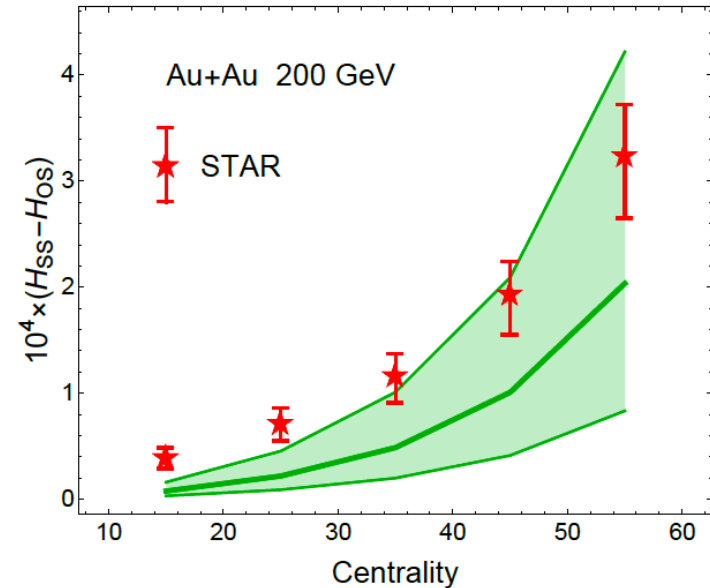
Projected axial charge level based on comparison AuAu data

Summary & Outlook

Summary

AVFD:

A versatile tool for an era of quantitative study of CME signals in heavy ion collisions !

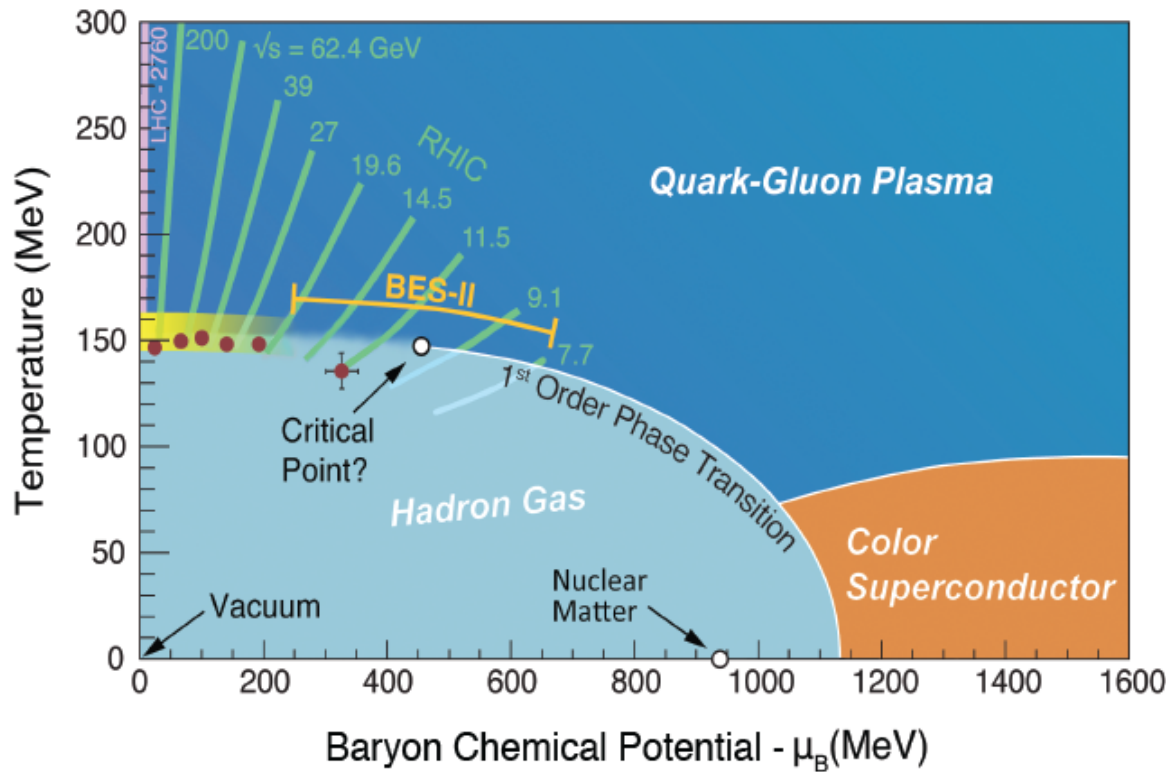


EBE-AVFD for the Isobars:

- 1) Event selection for truly identical bulk!***
- 2) Both gamma & delta needed!***
- 2) Absolute difference in correlations sensitive to CME!***

Mapping Out the Phases of QCD Matter

- * Establishing a chiral QGP at higher energy via anomalous chiral effects
- * IF hints of CME at 200GeV \rightarrow Isobar exp. at BES energies is crucial!



BEST
COLLABORATION

Stay tuned for
exciting news
in the near future!

Beam Energy Scan Theory (BEST) Collaboration:
BNL, IU, LBNL, McGill U, Michigan State U, MIT, NCSU, OSU,
Stony Brook U, U Chicago, U Conn, U Huston, UIC

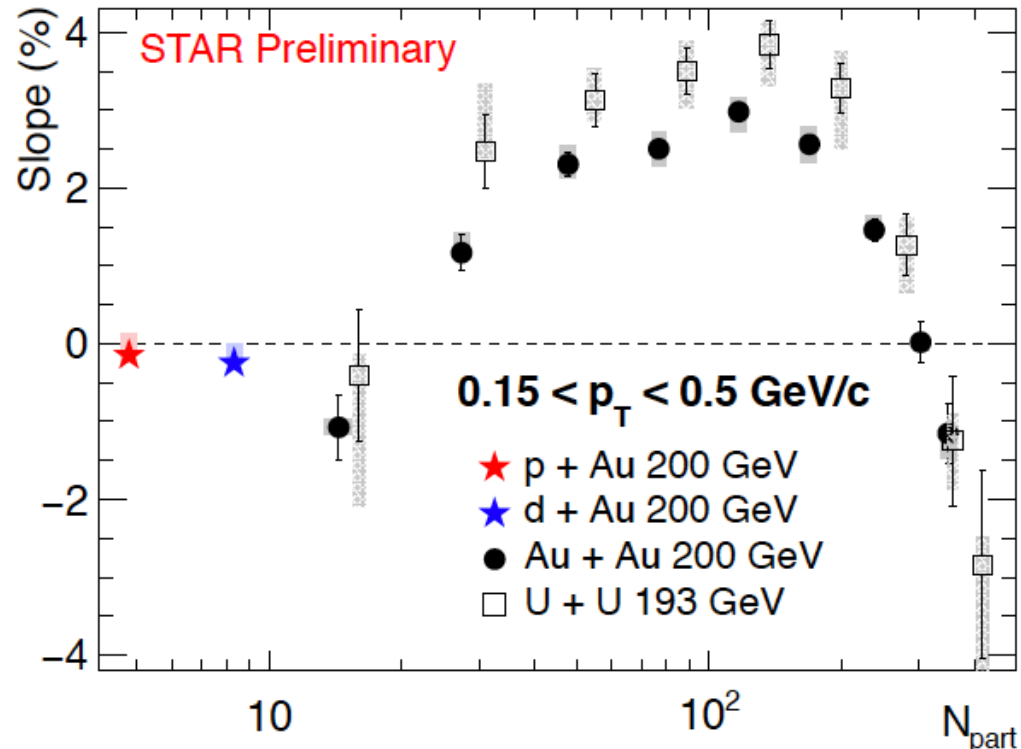
Backup Slides

CMW Induced Flow Splitting

CMW \rightarrow charge quadrupole of QGP \rightarrow elliptic flow splitting

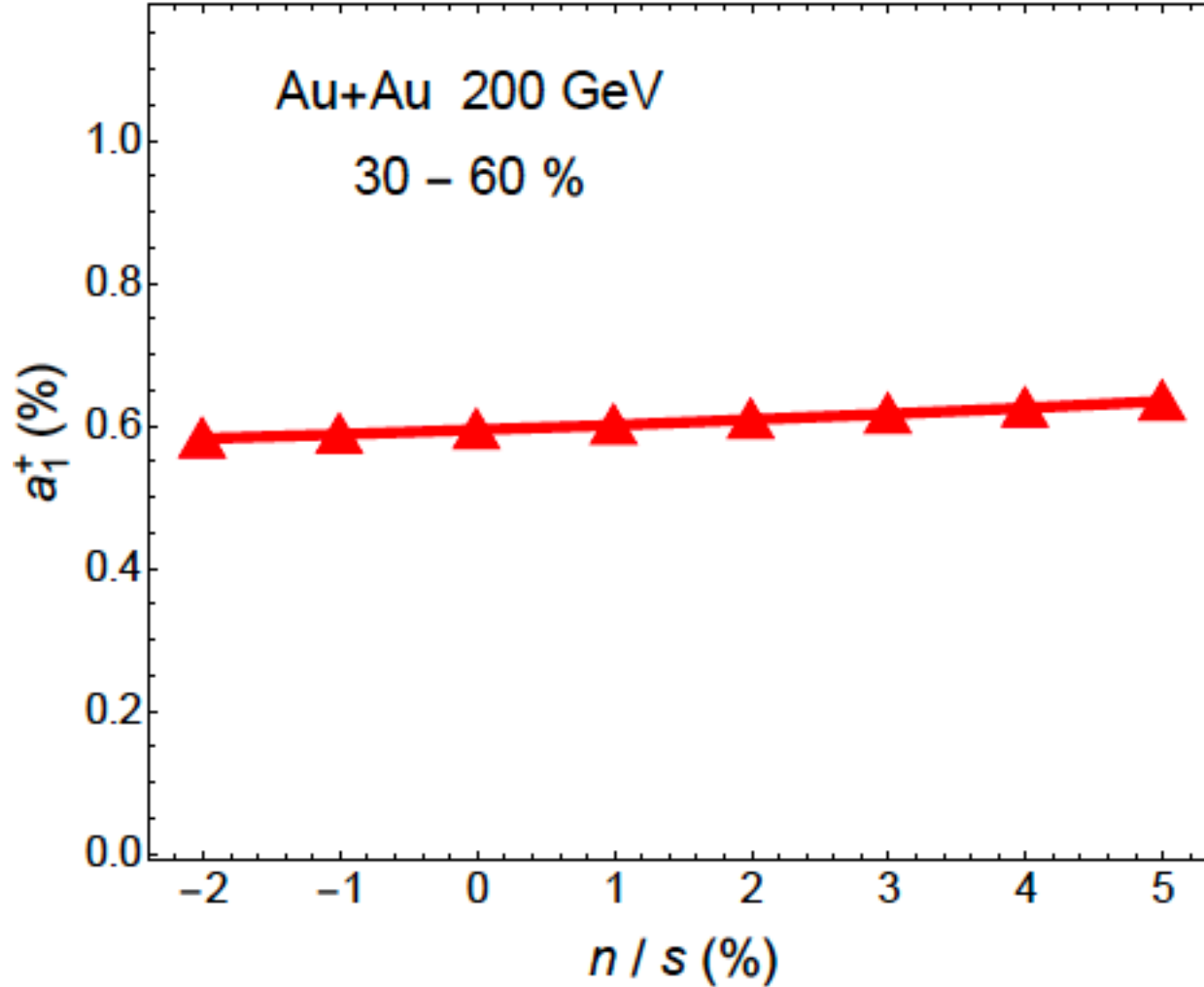
[Burnier, Kharzeev, JL, Yee, PRL2011; and arXiv: 1208.2537]

$$v_2^- - v_2^+ = r_e A$$



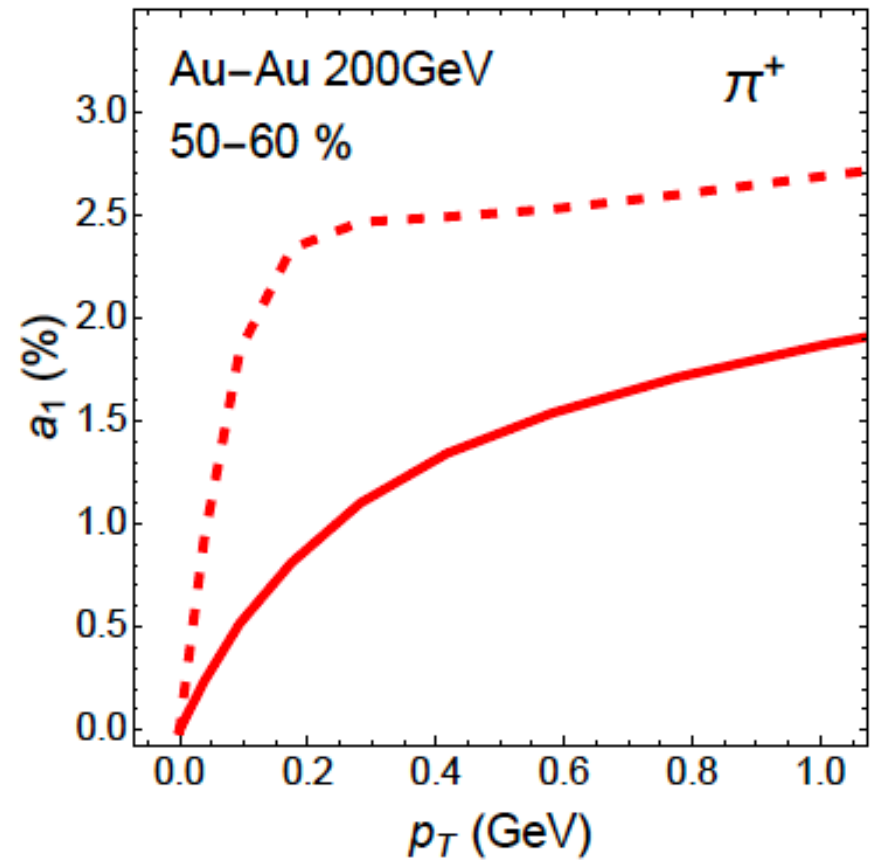
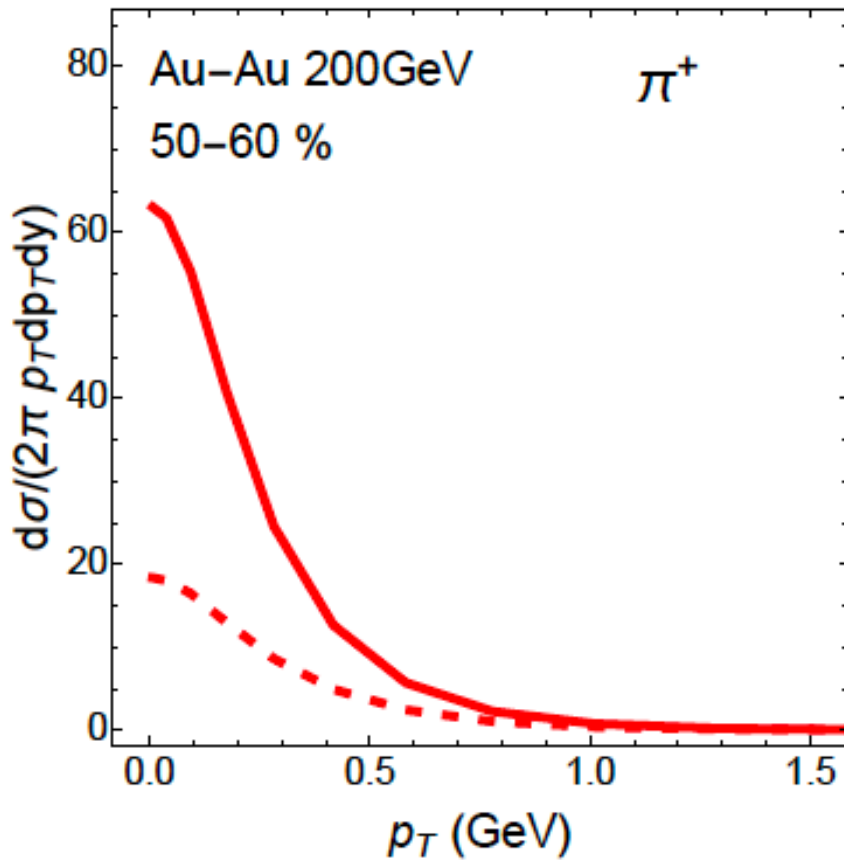
[STAR, QM2018]

The Vector Charge Initial Condition



Insensitive to nonzero vector charge density

The Influence of the Resonance Decays



**Considerable impact from resonance decays;
Must be included for quantitative results!**

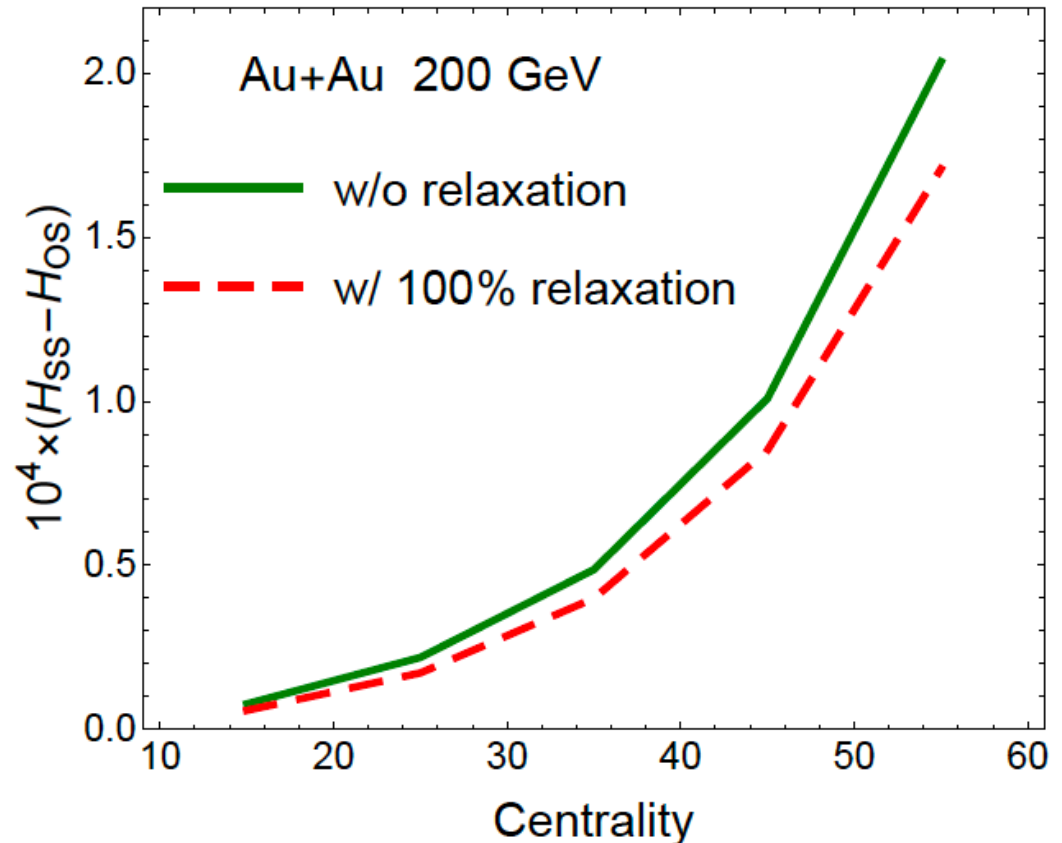
Relaxation Effect for the CME Current ??

$$\hat{D}_\mu J_{\chi,f}^\mu = \chi \frac{N_c Q_f^2}{4\pi^2} E_\mu B^\mu$$

$$J_{\chi,f}^\mu = n_{\chi,f} u^\mu + \nu_{\chi,f}^\mu$$

$$\Delta_\nu^\mu \hat{d}(\nu_{\chi,f}^\nu) = -\frac{1}{\tau_r} \left[(\nu_{\chi,f}^\mu) - (\nu_{\chi,f}^\mu)_{NS} \right]$$

$$(\nu_{\chi,f}^\mu)_{NS} = \frac{\sigma}{2} T \Delta^{\mu\nu} \partial_\nu \left(\frac{\mu_{\chi,f}}{T} \right) + \frac{\sigma}{2} Q_f E^\mu + \chi \frac{N_c Q_f}{4\pi^2} \mu_{\chi,f} B^\mu$$



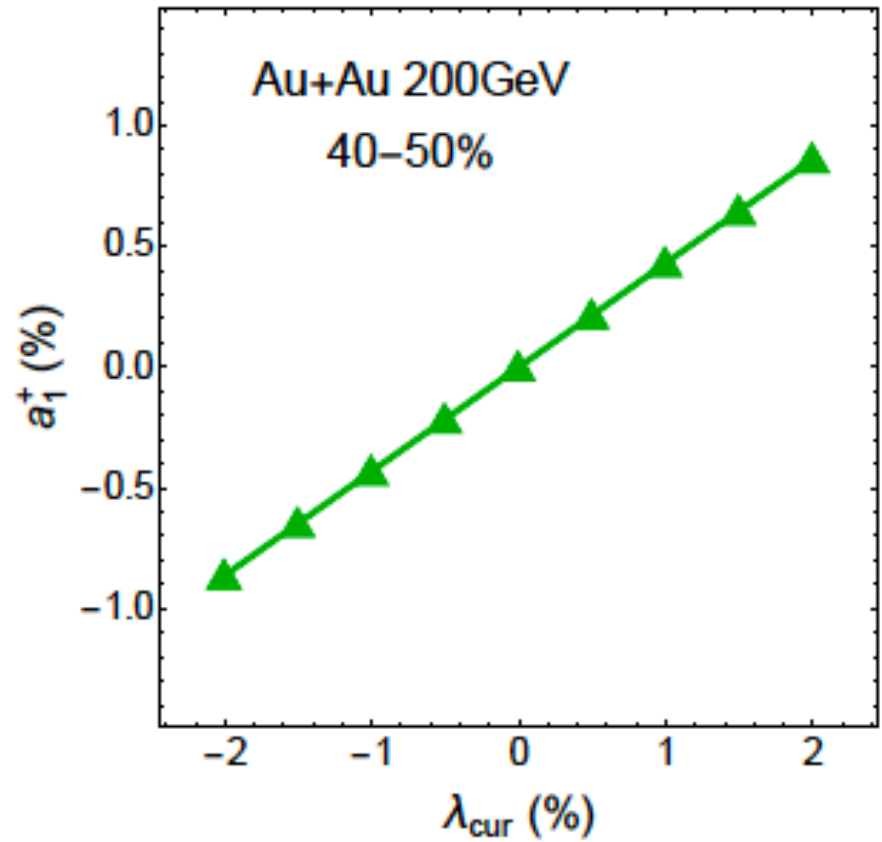
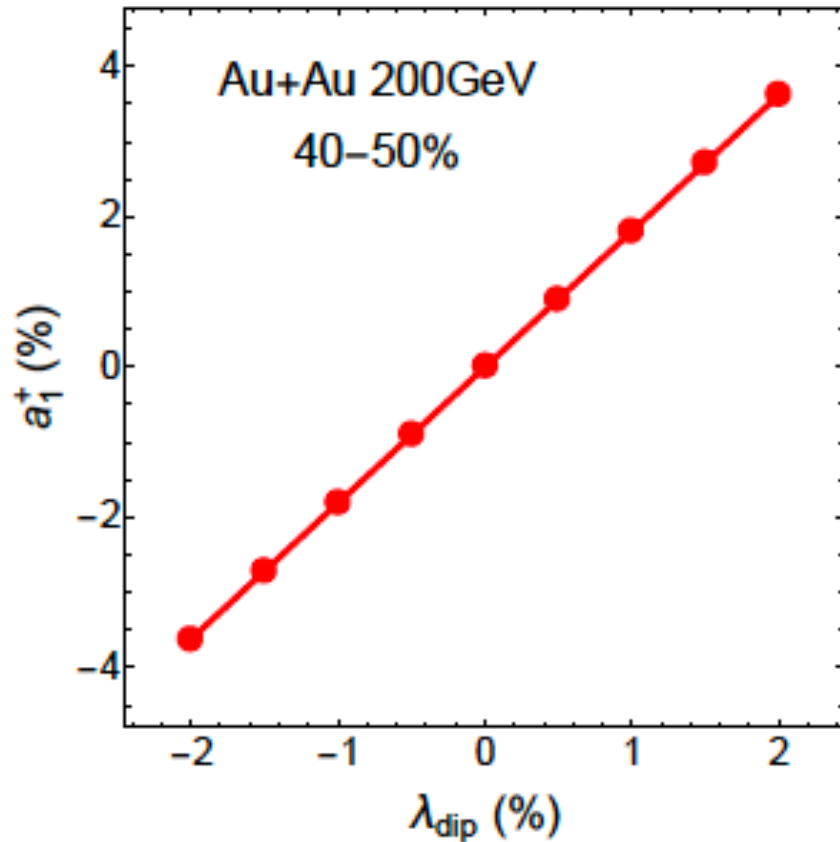
Pre-Hydro CME ??

$$n_{\text{ini},f} = (\lambda_{0,f} + \lambda_{\text{dip},f} \sin \phi) s_0.$$

$$\lambda_{\text{dip}} \equiv \lambda_{\text{dip},u} = -2\lambda_{\text{dip},d},$$

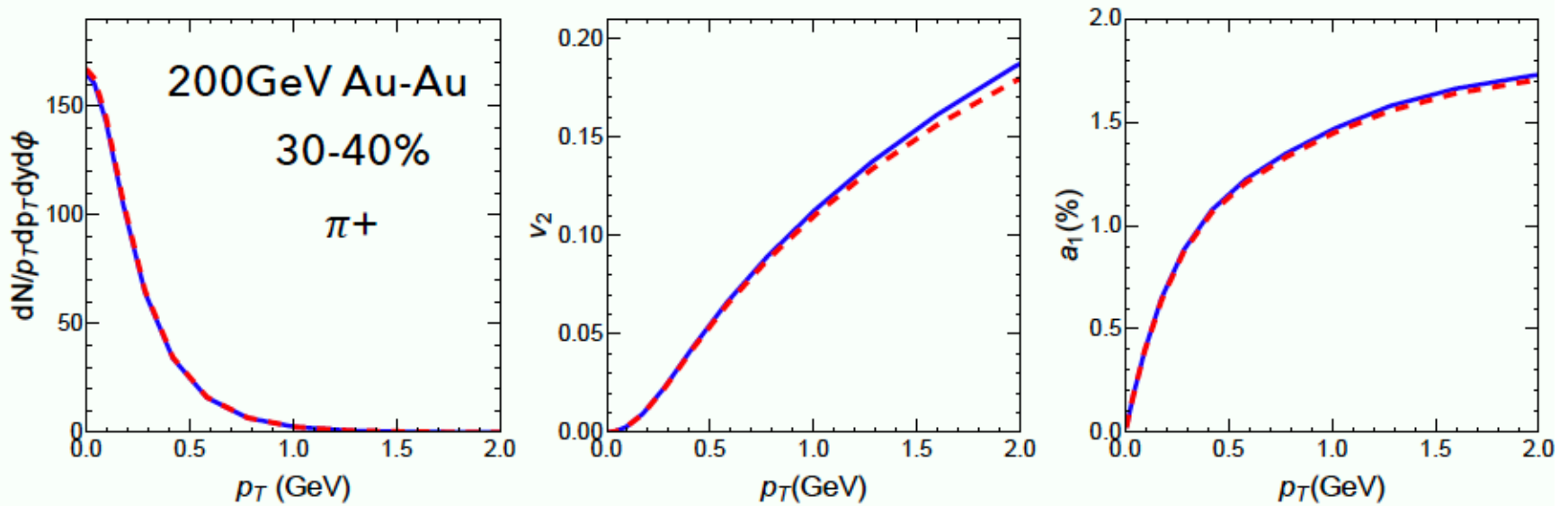
$$\nu_f|_{\tau=\tau_0} = J_{\text{ini},f} = \lambda_{\text{cur},f} s_0 \hat{y},$$

$$\lambda_{\text{cur}} \equiv \lambda_{\text{cur},u} = -2\lambda_{\text{cur},d}.$$



MUSIC-AVFD

MUSIC(2+1) + AVFD versus VISH(2+1) + AVFD

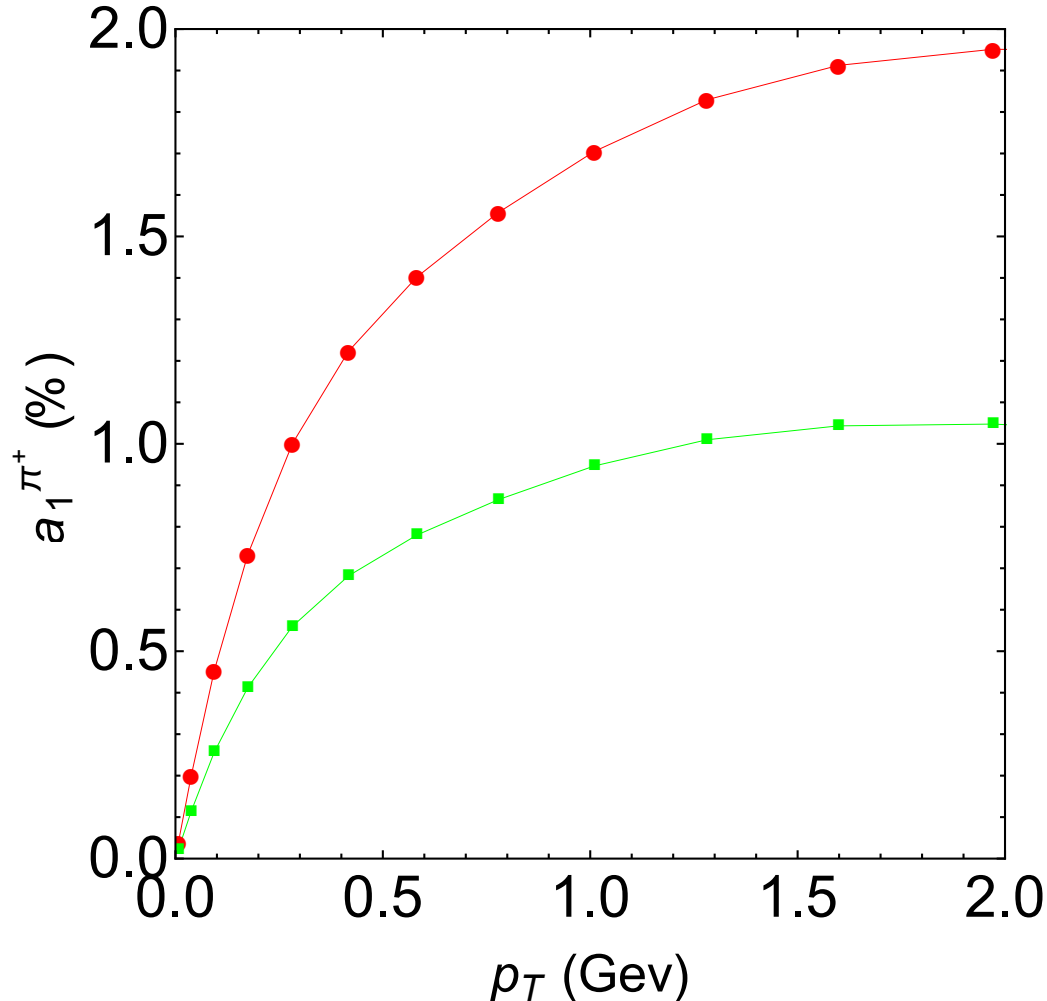


Blue = MUSIC(2+1) + AVFD

Red = VISH(2+1) + AVFD

match with each other
(with the same set-up)

Axial Charge Relaxation



The axial charge non-conservation is important and can be quantified in AVFD.