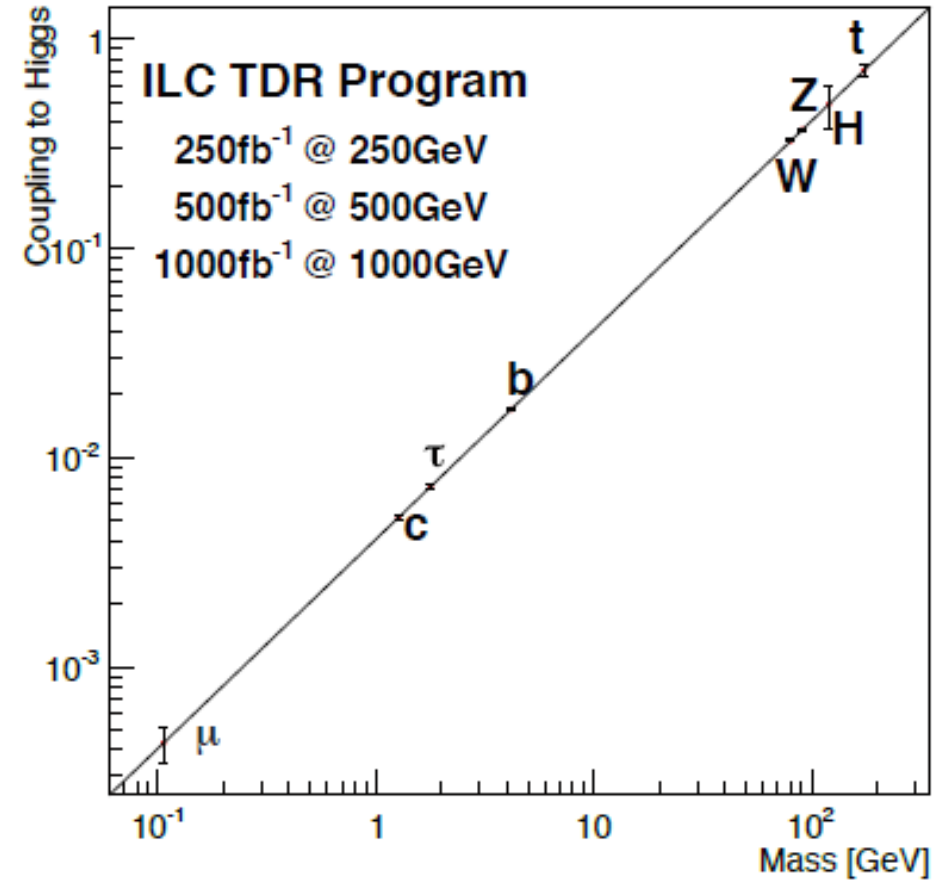
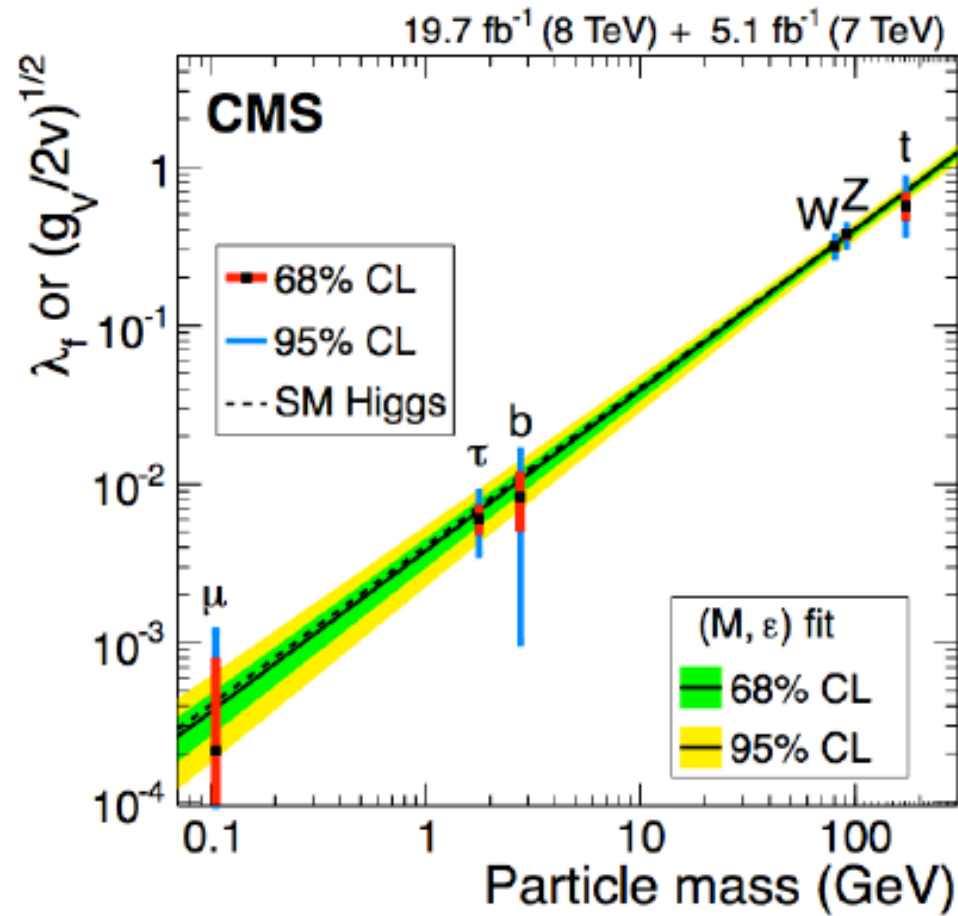


# Topic around the Higgs couplings

# Couplings and the Particle Mass



What is Higgs coupling

# Interaction related with the Higgs term

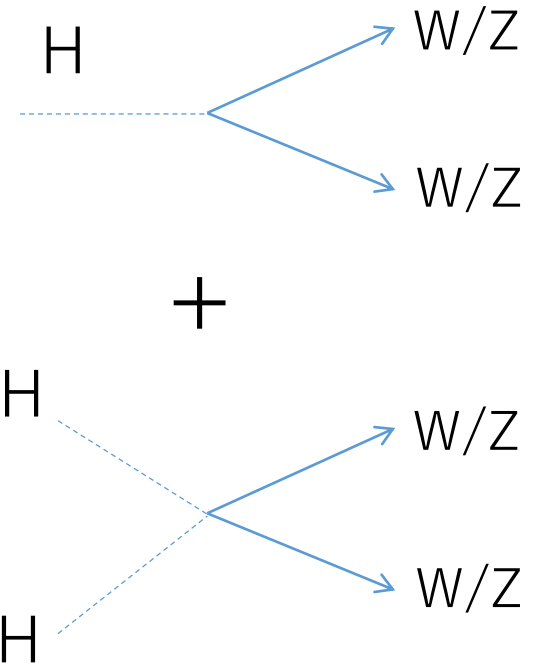
- **W/Z boson - Higgs**

$$\mathcal{L}_1^{\text{HB}} = \frac{1}{2} v g^2 W_\alpha^\dagger W^\alpha \sigma + \frac{1}{4} g^2 W_\alpha^\dagger W^\alpha \sigma^2 + \frac{v g^2}{4 \cos^2 \theta_W} Z_\alpha Z^\alpha \sigma + \frac{g^2}{8 \cos^2 \theta_W} Z_\alpha Z^\alpha \sigma^2.$$

$$\frac{1}{2\nu} m_W^2$$

$$m_W = \frac{1}{2} v g, \quad m_Z = m_W / \cos \theta_W, \quad m_H = \sqrt{(-2\mu^2)},$$

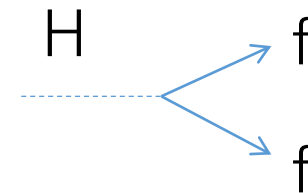
Coupling (x v)  $\propto m_W^2$



- **Fermion - Higgs**

$$\mathcal{L}_1^{\text{HL}} = -\frac{1}{v} m_f \bar{\psi}_f \psi_f \sigma - \frac{1}{v} m_{\nu_f} \bar{\psi}_{\nu_f} \psi_{\nu_f} \sigma.$$

Coupling (x v)  $\propto m_f$

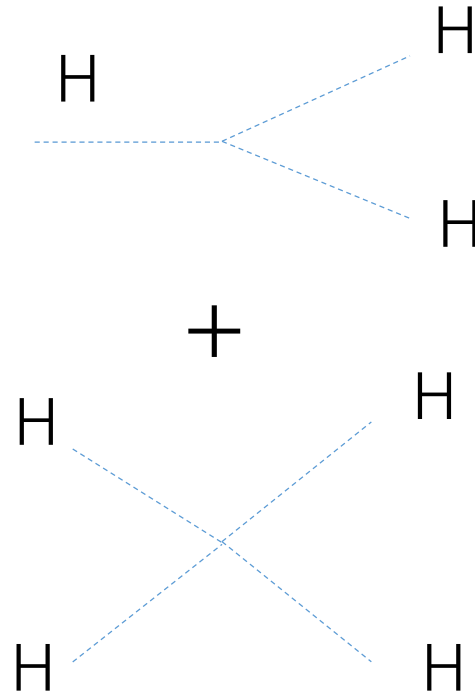


# Interaction related with the Higgs term

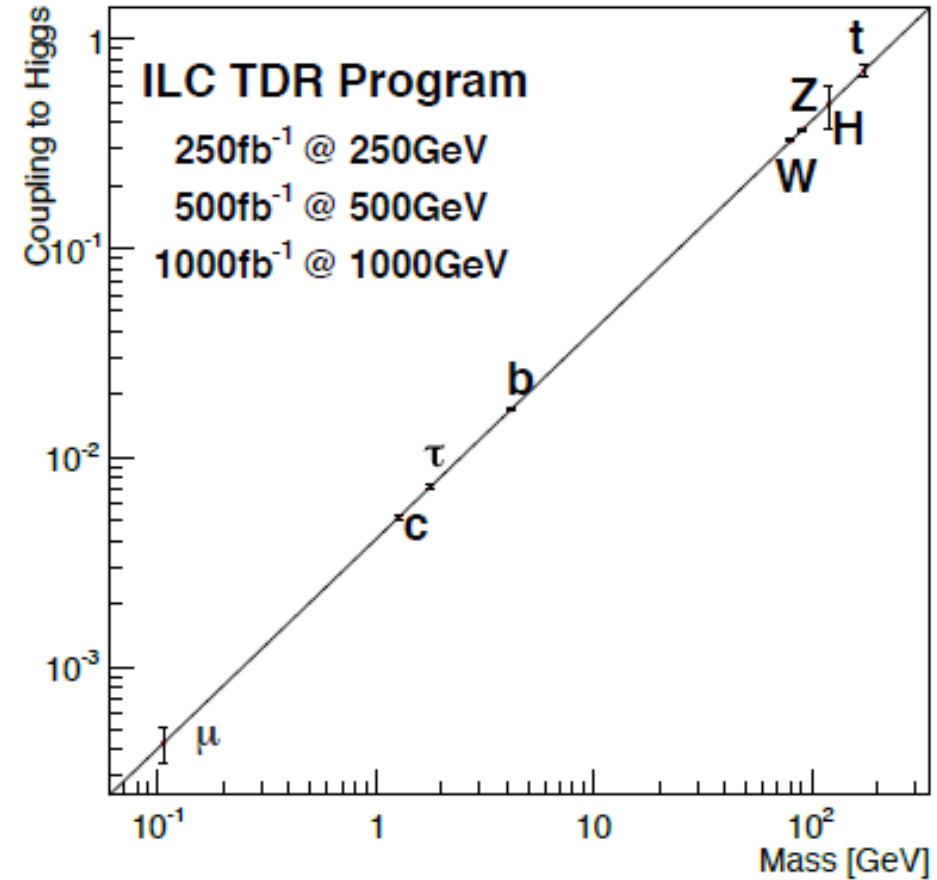
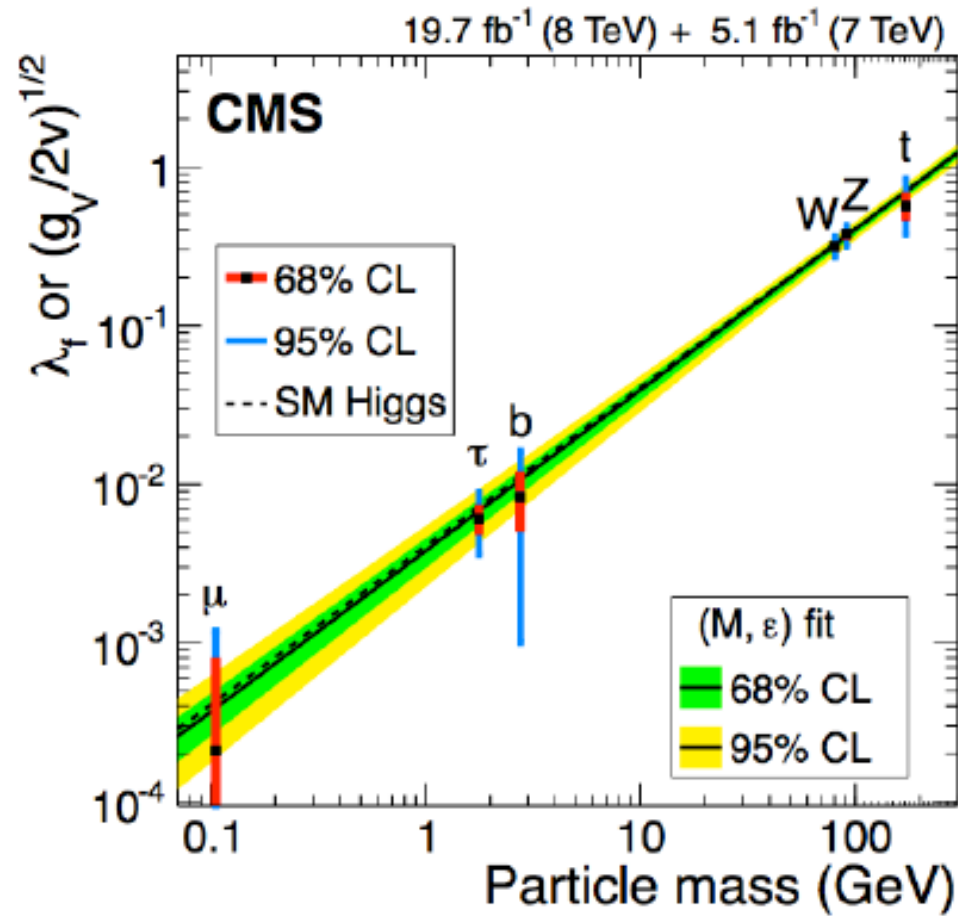
- **Higgs - Higgs**

$$\mathcal{L}_1^{\text{HH}} = -\frac{1}{4}\lambda\sigma^4 - \lambda v\sigma^3$$

-- need higher energy than 250 GeV (CEPC) to explore this coupling.



# Couplings and the Particle Mass



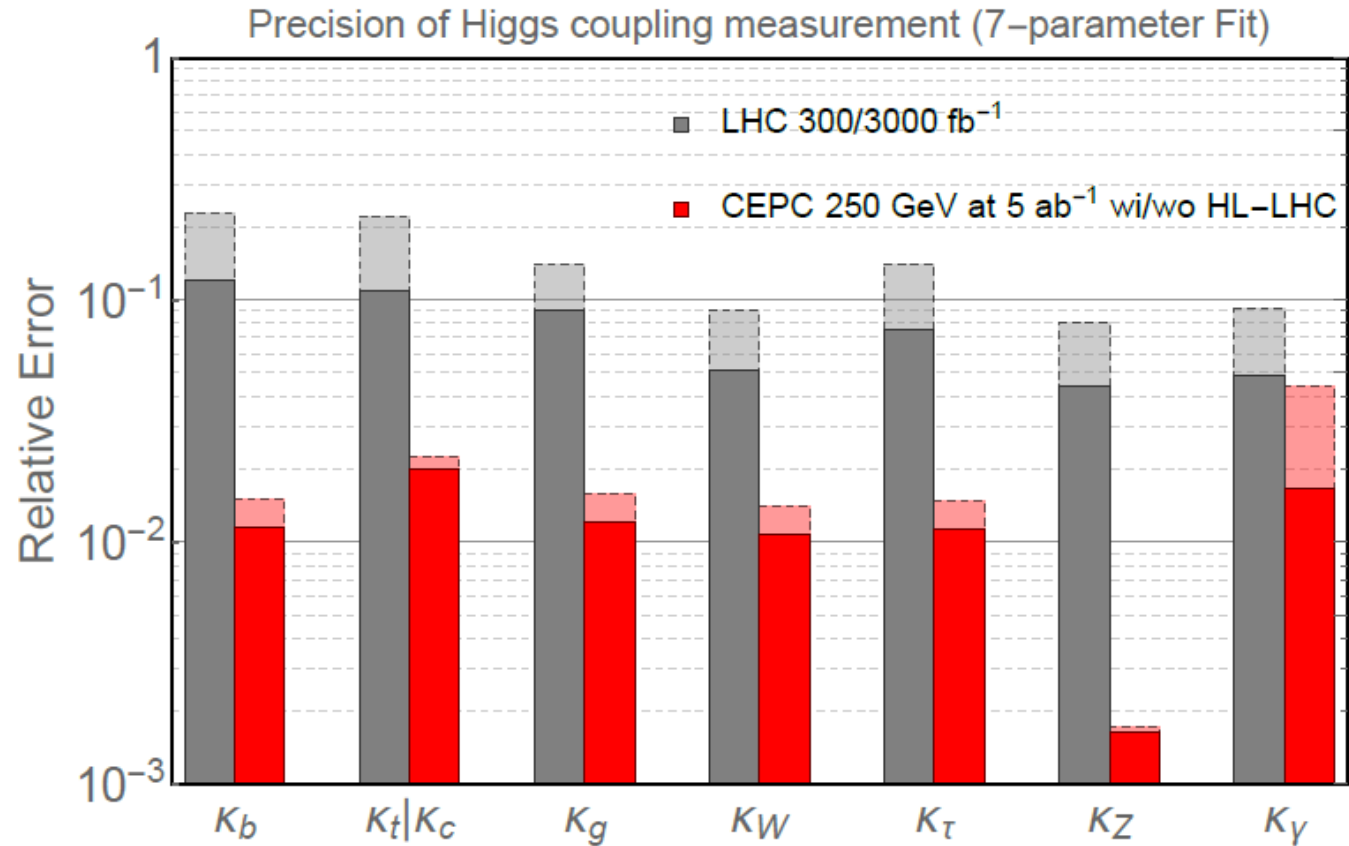
Which precision on the  
measurement of the couplings ,  
we want/need to achieve

# Comparison of precision of the Higgs coupling

$\kappa$  : ratio of the coupling constant (with the SM prediction)

$$\kappa_V = \frac{g(hVV)}{g(hVV; \text{SM})}$$

$$\kappa_f = \frac{g(hff)}{g(hff; \text{SM})},$$



**Figure 15.** The 7 parameter fit result, and comparison with the HL-LHC [45]. The projections for the CEPC at 250 GeV with 5 ab<sup>-1</sup> integrated luminosity are shown. The CEPC results without combination with the HL-LHC input are shown with dashed edges. The LHC projections for an integrated luminosity of 300 fb<sup>-1</sup> are shown in dashed edges.



# Example of Higgs coupling deviation

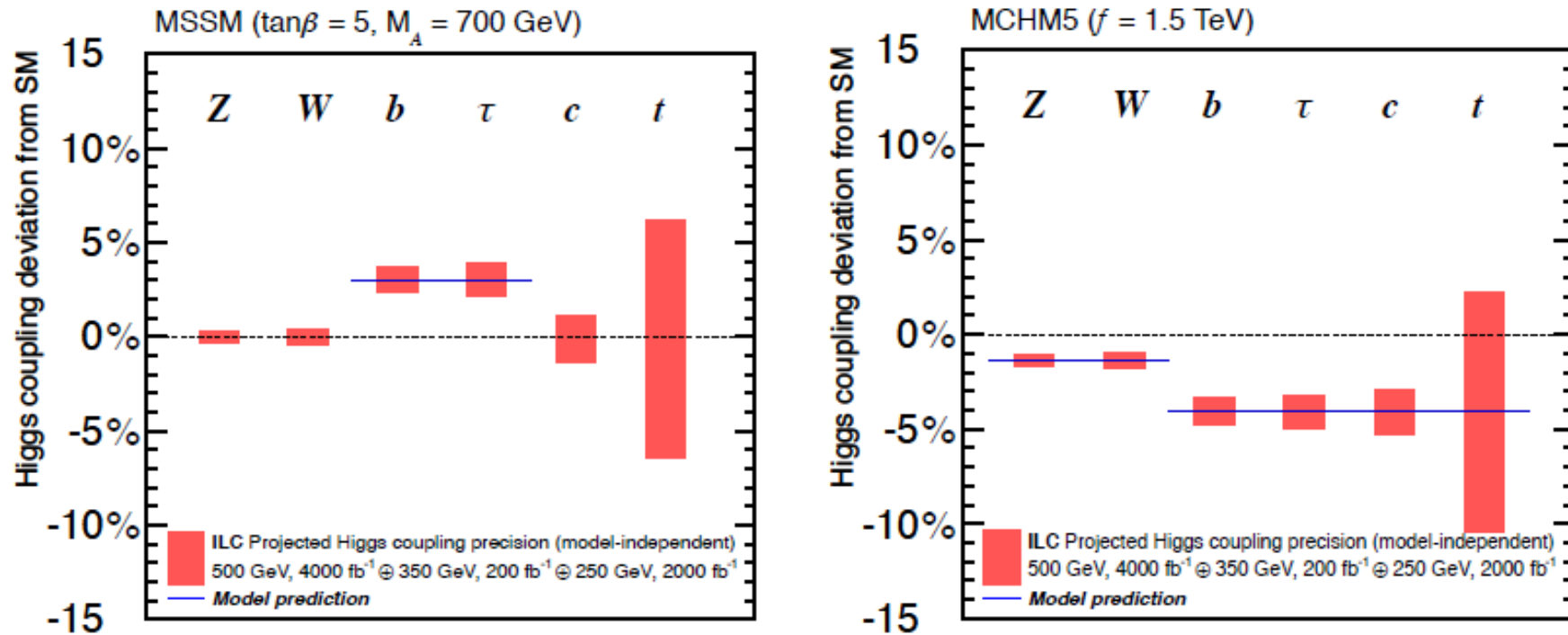
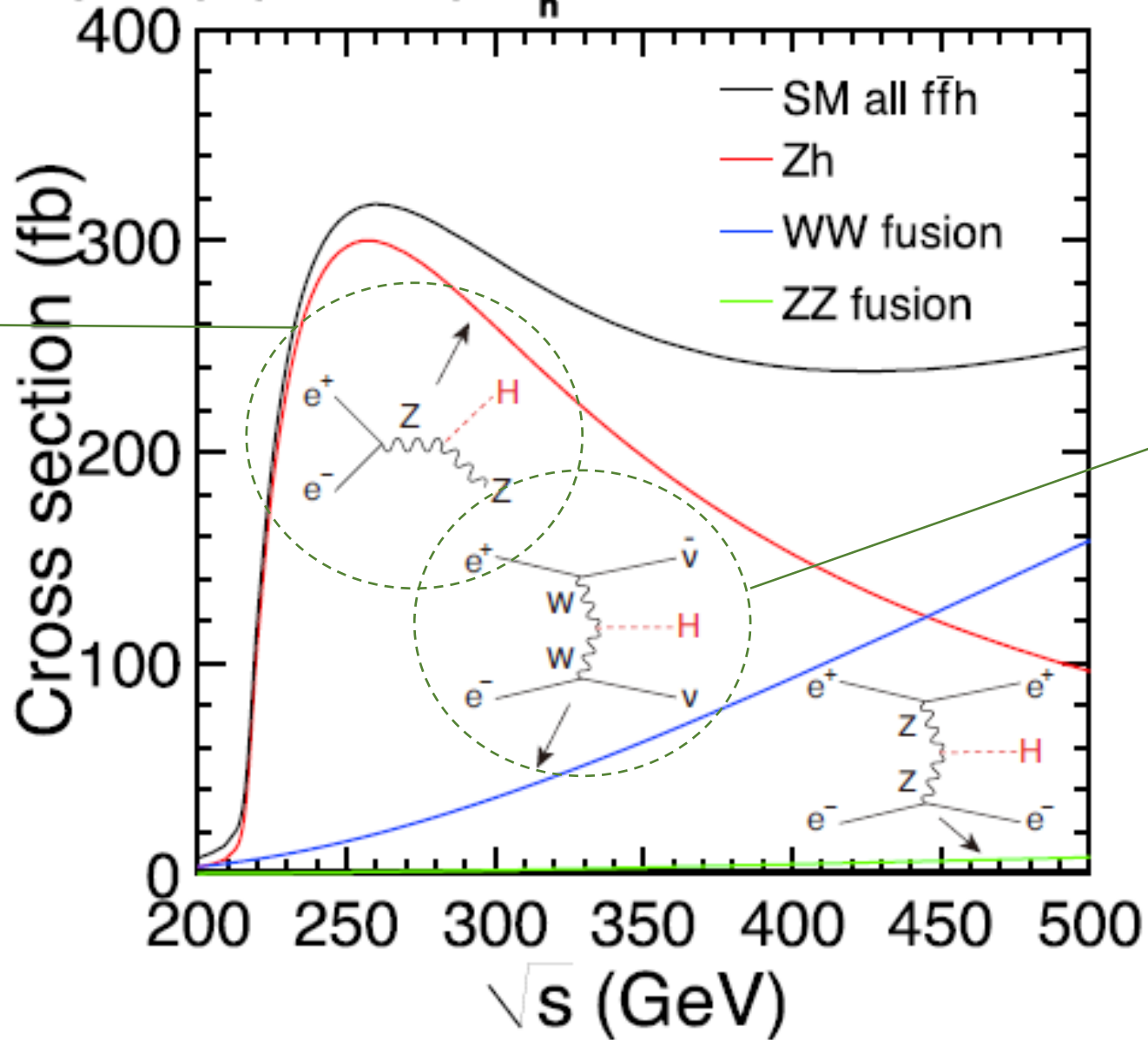


Figure 6: Two examples of models of new physics and their predicted effects on the pattern of Higgs boson couplings. Left: a supersymmetric model. Right: a model with Higgs boson compositeness. The error bars indicate the  $1\sigma$  uncertainties expected from the model-independent fit to the full ILC data set.

This is quite model dependent !!

How to measure/determine  
the couplings

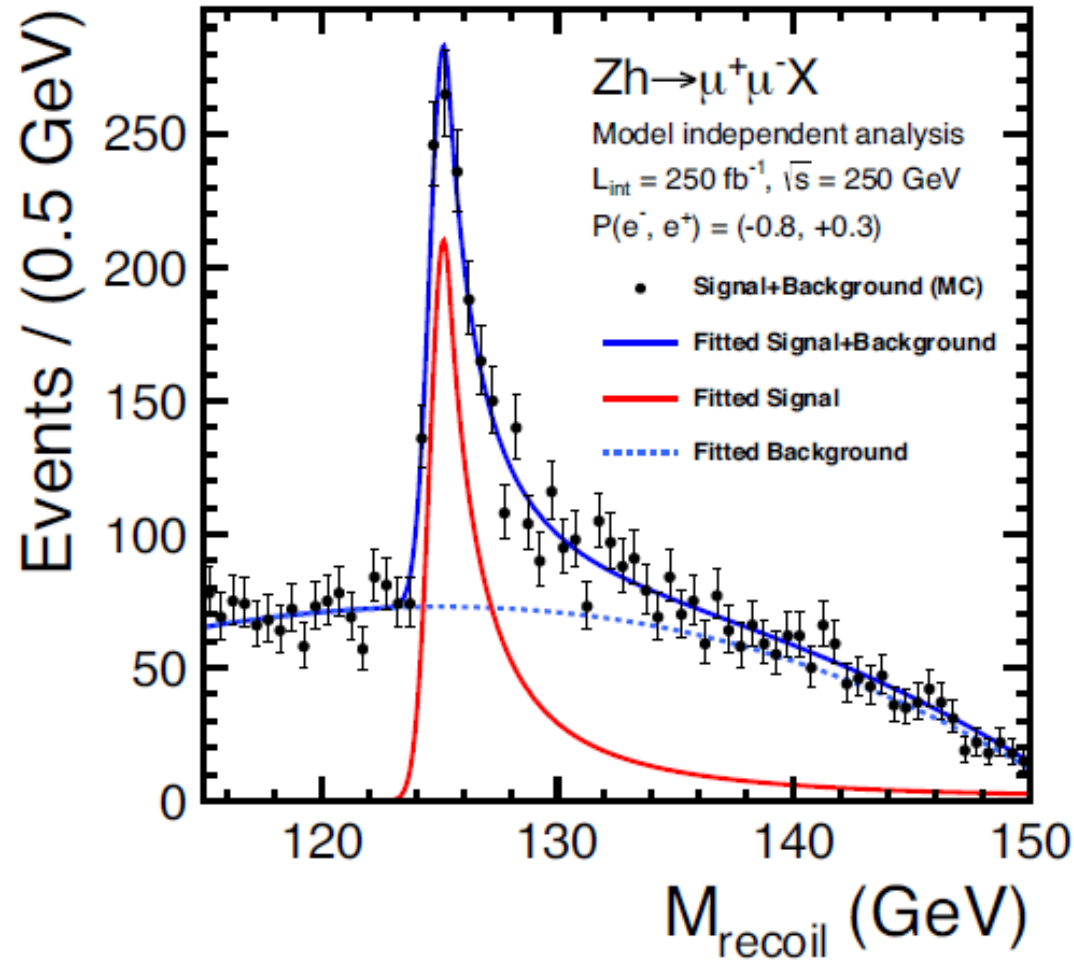
$$P(e^-, e^+) = (-0.8, 0.3), M_h = 125 \text{ GeV}$$



Determine precisely the coupling of  $H \rightarrow ZZ$

Determine precisely the coupling of  $H \rightarrow WW$


Higgs Cross section (  $Z^* \rightarrow ZH \Leftrightarrow H \rightarrow ZZ$  ) can be obtained by using the inclusive Higgs decay




### Note : the Higgs total width is expected as  $\sim 4 \text{ MeV}$ , which can not measure directly, even with this inclusive analysis.

# How to obtain the couplings

---

1.  $\Gamma_h = \frac{\Gamma_{ZZ}}{BR_{ZZ}} = \frac{\Gamma_{WW}}{BR_{WW}}$   By measuring the BRs, total width of Higgs boson is obtained .

2.  $BR(h \rightarrow A\bar{A}) = \Gamma(h \rightarrow A\bar{A})/\Gamma_h$

 By measuring the BRs for each particle, combined with the total width of Higgs, the partial width  $\rightarrow$  coupling constant can be obtained.

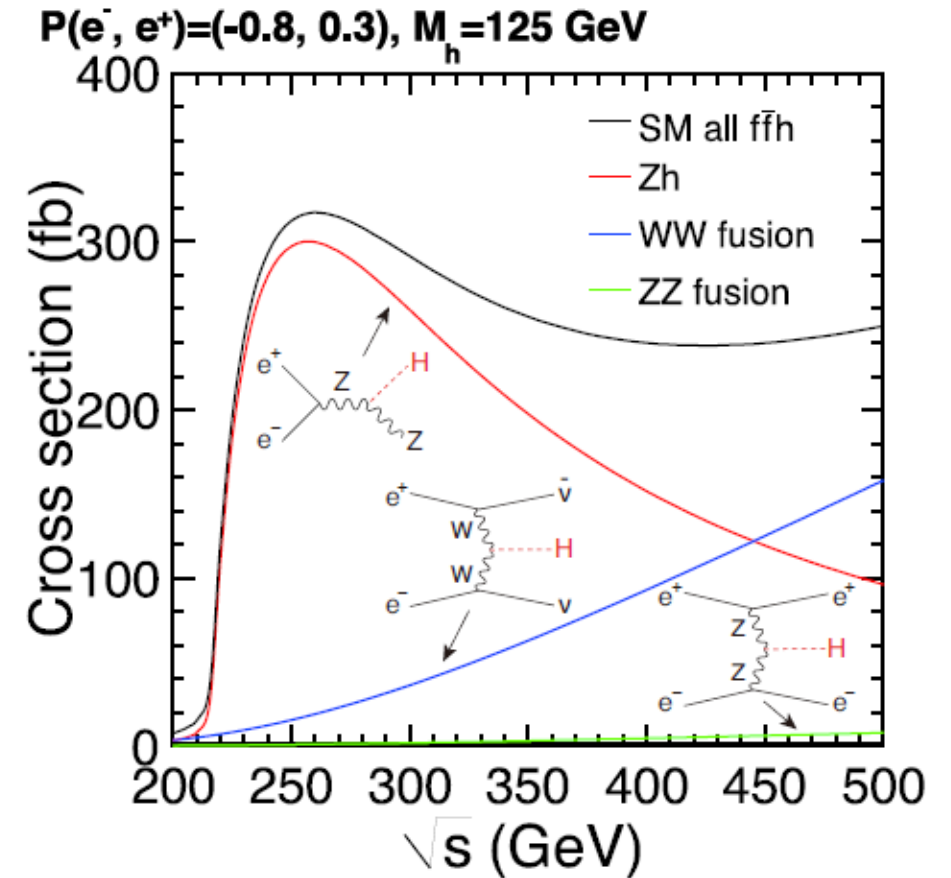
# How to obtain the couplings

[ Key Point ]

$$\Gamma_h = \frac{\Gamma_{ZZ}}{BR_{ZZ}} = \frac{\Gamma_{WW}}{BR_{WW}}$$

--  $\Gamma_{ZZ}/\Gamma_{WW}$  can be determined relatively precise ( less than 1% ).

-- Precision of the  $Br(ZZ)$  is limited by the statistics ! ( next page )



Seems to be , , ,  $\Gamma_h$  will be decided from WW side.

**Table 9.** Estimated precision of Higgs boson property measurements at the CEPC. All precision are relative except for  $m_H$  and  $\text{BR}(H \rightarrow \text{inv})$  for which  $\Delta m_H$  and 95% CL upper limit are quoted respectively.

$\Delta m_H$	$\Gamma_H$	$\sigma(ZH)$	$\sigma(\nu\bar{\nu}H) \times \text{BR}(H \rightarrow b\bar{b})$
5.9 MeV	3.3%	0.50%	3.1%

Decay mode	$\sigma(ZH) \times \text{BR}$	BR
$H \rightarrow b\bar{b}$	0.28%	0.57%
$H \rightarrow c\bar{c}$	3.3%	3.4%
$H \rightarrow gg$	1.3%	1.4%
$H \rightarrow \tau^+\tau^-$	0.8%	0.9%
$H \rightarrow WW^*$	1.1%	1.2%
$H \rightarrow ZZ^*$	5.1%	5.1%
$H \rightarrow \gamma\gamma$	8.2%	8.3%
$H \rightarrow \mu^+\mu^-$	16%	16%
$(H \rightarrow \text{inv})_{\text{BSM}}$	—	$< 0.32\%$

# Comments

It is also mentioned that there is a significant contamination of ZH “background”,  $Z \rightarrow \nu\nu$ ,  $H \rightarrow b\bar{b}$ , for the WW fusion, for 250 GeV... and it is not clear for me ( but at present ) this effect .

reference from the ILC

and less significant beamstrahlung effect. On the other hand, the lowered energy is expected to have a significant impact on the measurement of the WW fusion process ( $e^+e^- \rightarrow \nu\bar{\nu}h$ ), the cross section of which becomes almost a factor of 10 smaller. Moreover, due to the limited available phase space at 250 GeV, the missing mass spectrum in the  $\nu\bar{\nu}h$  process is significantly overlapping with that in the  $Zh$ ,  $Z \rightarrow \nu\bar{\nu}$

reference from the CEPC

The precision from the method of 5.3 is 5.4%, dominated by the statistics of  $e^+e^- \rightarrow ZH$  events with  $H \rightarrow ZZ^*$ , after ignoring the measurements correlation with other channels. Keeping only the correlations between the measured sub channels appearing in the expression of 5.4, the precision on Higgs width is 3.7%, dominated by the statistics of  $e^+e^- \rightarrow \nu\bar{\nu}H$  events with  $H \rightarrow b\bar{b}$ . This method uses the large  $Br(H \rightarrow b\bar{b})$  value to compensate the smaller cross section of the W fusion process  $\sigma_{\nu\nu H}$ . The combined precision of the two measurements is 3.3%.

