

Probe the Form Factors in decay $J/\psi \rightarrow \Sigma^0 \bar{\Sigma}^0$

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Outline

- 1 *The angular distribution*
- 2 *Determine the $\alpha_{J/\psi}$ and Φ*
- 3 *Summary*

Update

The angular distribution

A) The amplitude of $\Sigma^0 \rightarrow \Lambda \gamma$ decay

$$M(\Sigma^0 \rightarrow \Lambda \gamma, \Lambda \rightarrow p \pi^-) \sim 1 + \beta_{\Sigma} \mathbf{s}_{\Sigma} \cdot \mathbf{p}_{\Lambda} \quad (1)$$

B) The distribution is

$$\begin{aligned} & \beta_{\Sigma} \beta_{\Sigma} \left(-\cos(\theta_1) \left(\sqrt{1 - \alpha_{\psi}^2} \sin(2\theta) \sin(\theta_2) \cos(\Phi) \cos(\phi_2) + 2 \cos(\theta_2) \cos^2(\theta) \right) + \right. \\ & \quad \left. \sin(\theta_1) \cos(\phi_1) \left(\sqrt{1 - \alpha_{\psi}^2} \sin(2\theta) \cos(\theta_2) \cos(\Phi) + 2 \sin(\theta_2) \sin^2(\theta) \cos(\phi_2) \right) + \right. \\ & \quad \left. \alpha_{\psi} \left(2 \sin^2(\theta) \sin(\theta_1) \sin(\theta_2) \sin(\phi_1) \sin(\phi_2) - 2 \cos(\theta_1) \cos(\theta_2) \right) \right) - \\ & 2 \sqrt{1 - \alpha_{\psi}^2} \sin(\theta) \sin(\theta_2) \cos(\theta) \sin(\Phi) \sin(\phi_2) \beta_{\Sigma} + \\ & \sqrt{1 - \alpha_{\psi}^2} \beta_{\Sigma} \sin(2\theta) \sin(\theta_1) \sin(\Phi) \sin(\phi_1) + \\ & \alpha_{\psi} \cos(2\theta) + \alpha_{\psi} + 2 \end{aligned}$$

✓ Where:

$$\frac{4 \alpha_{\Lambda} \left((m_{\Lambda}^2 + m_{\Sigma}^2) (m_{\Lambda}^2 + m_p^2 - m_{\pi}^2) - 4 m_{\Lambda}^2 p_p \cdot p_{\Sigma} \right)}{m_{\Lambda} m_{\Sigma} \left(\frac{(m_{\Lambda}^2 - m_{\Sigma}^2)^2}{m_{\Sigma}^2} \right)^{3/2} \sqrt{\frac{(m_{\pi}^2 - m_{\Lambda}^2)^2 - 2(m_{\Lambda}^2 + m_{\pi}^2) m_p^2 + m_p^4}{m_{\Lambda}^2}}}$$

A) PDF: $\mathcal{W}(\alpha, \dots; \theta, \dots)$

B) Likelihood

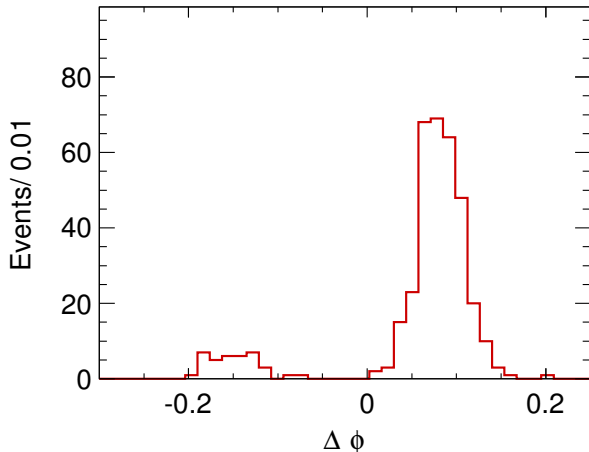
$$\mathcal{L} = \prod_{data} \frac{\mathcal{W}}{\mathcal{N}} \quad (2)$$

✓ The normalization factor \mathcal{N} obtained by MC integral

$$\mathcal{N} = \sum \mathcal{W} \quad (3)$$

Multiple Solutions

- A) There two local minimum FCNs
- ✓ Choose the solution with the minimum FCN



Fit result

A) The fit result

parameters	value
$\alpha_{J/\psi}$	-0.426 ± 0.011
Φ	0.088 ± 0.022
α_{Λ}	0.85 ± 0.20
$\alpha_{\bar{\Lambda}}$	-0.70 ± 0.17

B) fix α_{Λ} and $\alpha_{\bar{\Lambda}}$

parameters	value
$\alpha_{J/\psi}$	-0.426 ± 0.011
Φ	0.092 ± 0.022
α_{Λ}	0.75 (fixed)
$\alpha_{\bar{\Lambda}}$	-0.75 (fixed)

Comparisons

$$T_1 = \sin^2(\theta) \sin(\theta_1) \sin(\theta_2) \cos(\phi_1) \cos(\phi_2) + \cos(\theta_1) \cos(\theta_2) \cos^2(\theta)$$

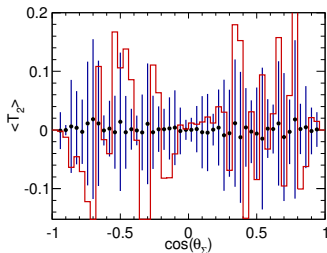
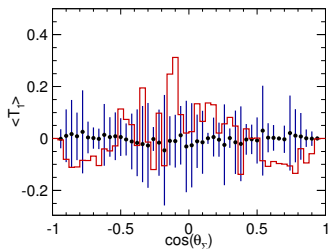
$$T_2 = \sin(\theta) \cos(\theta) (\sin(\theta_1) \cos(\theta_2) \cos(\phi_1) + \sin(\theta_2) \cos(\theta_1) \cos(\phi_2))$$

$$T_3 = \sin(\theta) \sin(\theta_1) \cos(\theta) \sin(\phi_1)$$

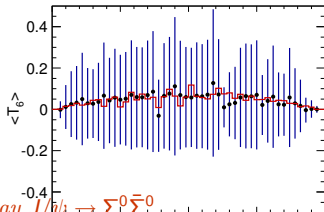
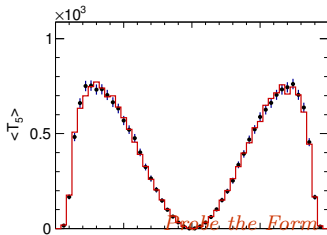
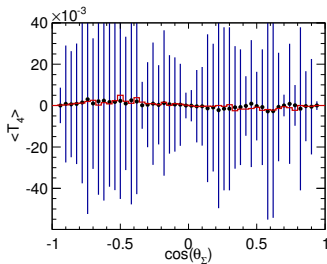
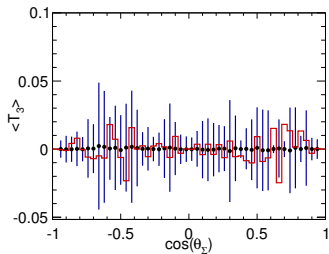
$$T_4 = \sin(\theta) \sin(\theta_2) \cos(\theta) \sin(\phi_2)$$

$$T_5 = \cos^2(\theta)$$

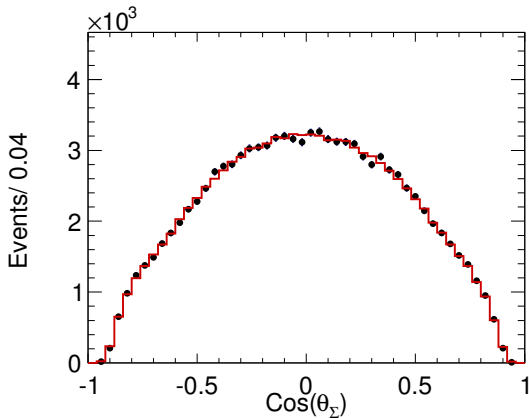
$$T_6 = \cos(\theta_1) \cos(\theta_2) - \sin^2(\theta) \sin(\theta_1) \sin(\theta_2) \sin(\phi_1) \sin(\phi_2)$$



Comparisons (2)

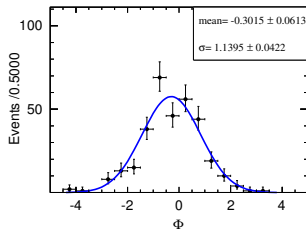
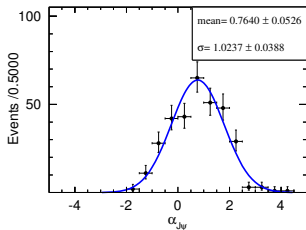


Comparisons(3)

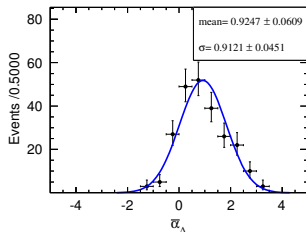
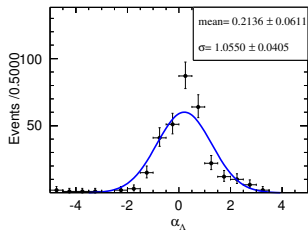


I/O check

- A) Generate the MC sample with the same size as data
- B) Repeat 300 times
- C) pull value : $\frac{\text{output} - \text{input}}{\sigma}$

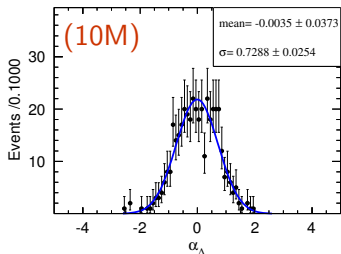
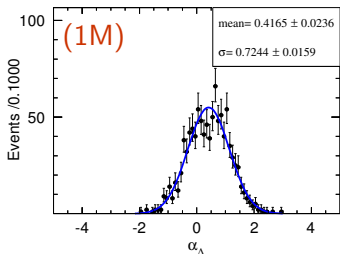


I/O check (2)



I/O check (3)

- A) The small bias may be partly raised by the limited integral MC sample
- B) Based on the MC truth information without any events selection requirements



Summary

- A) The α_Λ and $\alpha_{\bar{\Lambda}}$ can't be determined well, must be fixed.
- B) The phase angle Φ is first measured, and $\alpha_{J/\psi}$ is consisted with the previous value.