

# Excitation functions of kinetic freeze-out temperature and transverse flow velocity in proton-proton collisions

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# Outline

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**Background**

**2**

**Formalism and method**

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**Results and discussion**

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**Summary and Conclusion**

# Bankgroud

Excitation degree

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graph TD; A[Excitation degree] --> B[Chemical freeze-out]; A --> C[Thermal and kinetic freeze-out]; B --> D[Chemical freeze-out temperature]; C --> E[Kinetic freeze-out temperature]; D --> F[Ratios of particles]; E --> G[Transverse momentum spectra];
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Chemical freeze-out

Thermal and kinetic freeze-out

Chemical freeze-out temperature

**Kinetic freeze-out temperature**

Ratios of particles

**Transverse momentum spectra**

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Kinetic freeze-out temperature

Transverse momentum spectra

Hydrodynamical model

Blast-wave model

Boltzmann-Gibbs statistics

Tsallis statistics

Random thermal motion reflect the excitation degree

Transverse flow reflect the collective expansion

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- The excitation function of the kinetic freeze-out temperature is very interesting for us to study the properties of high energy collisions.
- Although there are many similar studies on this topic, the results seem to be inconsistent.
- The excitation function of the chemical freeze-out temperature shows initially increases and then consistently saturates with collision energy.

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## Blast-wave model

### Boltzmann-Gibbs statistics and Tsallis statistics

Inelastic (INEL) or nonsingle-diffractive (NSD)  $pp$  collisions which are closer to peripheral nuclear collisions comparing with central nuclear collisions.

- SPS : NA61/SHINE
- RHIC : PHENIX、 STAR
- LHC : ALICE、 CMS

# Formalism and method

For the soft excitation process

The **blast-wave model** with **Boltzmann-Gibbs statistics** results in the probability density distribution of  $p_T$

$$f_1(p_T) = \frac{1}{N} \frac{dN}{dp_T} = C_1 p_T m_T \int_0^R r dr \times I_0 \left[ \frac{p_T \sinh(\rho)}{T_0} \right] K_1 \left[ \frac{m_T \cosh(\rho)}{T_0} \right]$$

E. Schnedermann, J. Sollfrank, U. Heinz  
Phys. Rev. C 48, 2462 (1993)

# Formalism and method

The **blast-wave model** with **Tsallis statistics** results in the probability density distribution of  $p_T$

$$f_2(p_T) = \frac{1}{N} \frac{dN}{dp_T} = C_2 p_T m_T \int_{-\pi}^{\pi} d\phi \int_0^R r dr \left\{ 1 + \frac{q-1}{T_0} [m_T \cosh(\rho) - p_T \sinh(\rho) \cos(\phi)] \right\}^{-1/(q-1)}$$

Z.B. Tang, Y.C. Xu, L.J. Ruan, G. van Buren, F.Q. Wang, Z.B. Xu, Phys. Rev. C 79, 051901(R) (2009).

# Formalism and method

For the hard scattering process

Inverse power-law

$$f_H(p_T) = \frac{1}{N} \frac{dN}{dp_T} = A p_T \left( 1 + \frac{p_T}{p_0} \right)^{-n}$$

R. Odorico, Phys. Lett. B  
118, 151 (1982).

Hagedorn function

$$f_H(p_T) = \frac{1}{N} \frac{dN}{dp_T} = A \frac{p_T^2}{m_T} \left( 1 + \frac{p_T}{p_0} \right)^{-n}$$

ALICE Collaboration (K. Aamodt *et al.*)  
Phys. Lett. B, 693, 53 (2010).

$$f_H(p_T) = \frac{1}{N} \frac{dN}{dp_T} = A p_T \left( 1 + \frac{p_T^2}{p_0^2} \right)^{-n}$$

A. De Falco (for the ALICE collaboration)  
J. Phys. G, 38, 124083 (2011).

Modified  
Hagedorn functions

$$f_H(p_T) = \frac{1}{N} \frac{dN}{dp_T} = A \left( 1 + \frac{p_T^2}{p_0^2} \right)^{-n}$$

ALICE Collaboration (B. Abelev *et al.*)  
Phys. Lett. B, 708, 265 (2012).

# Formalism and method

The experimental  $p_T$  spectrum distributed in a wide range can be described by a superposition of the soft excitation and hard scattering processes.

$$f_3(p_T) = kf_s(p_T) + (1-k)f_H(p_T)$$

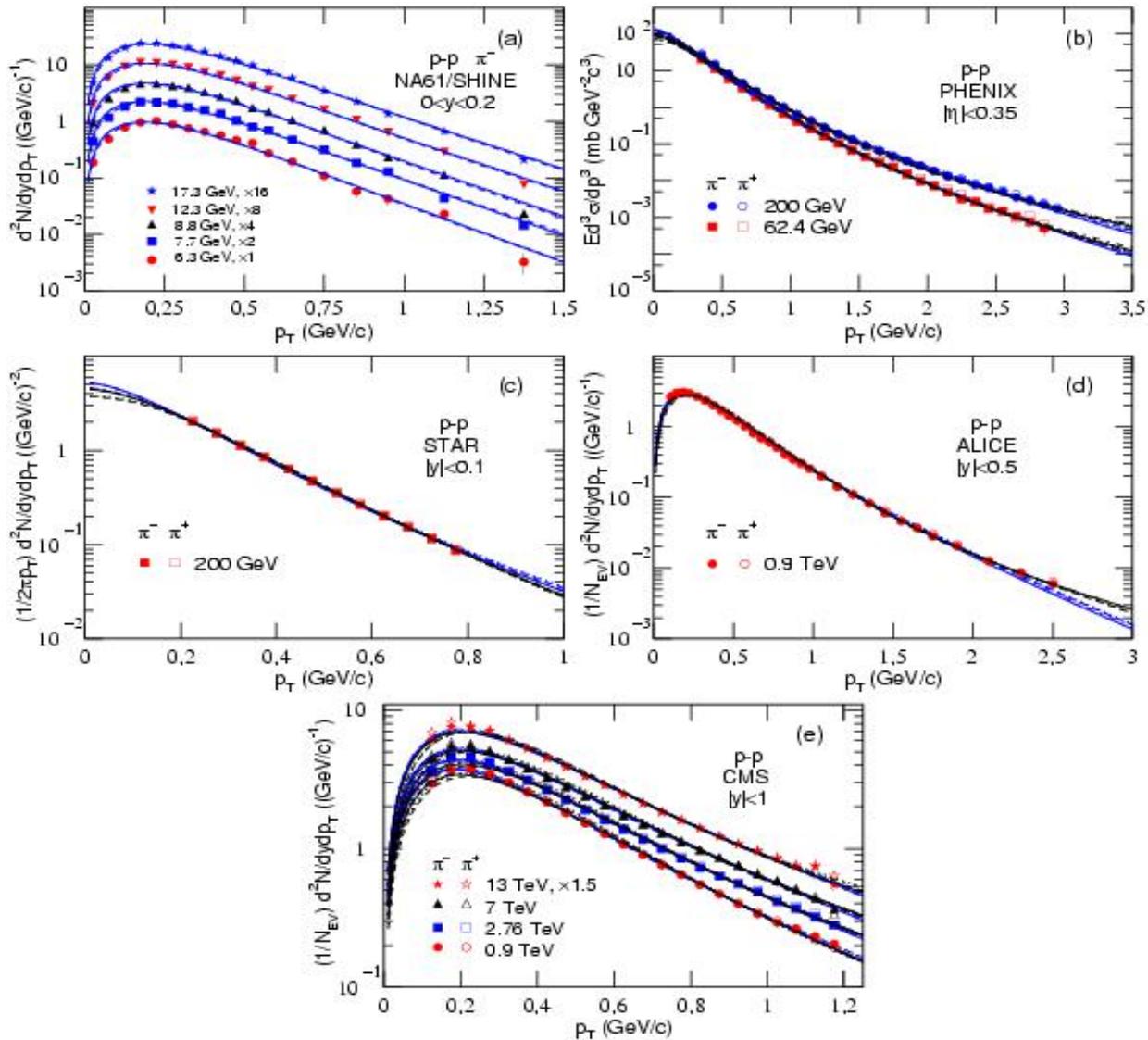
$$f_4(p_T) = A_1\theta(p_1 - p_T)f_S(p_T) + A_2\theta(p_T - p_1)f_H(p_T)$$

# Results and discussion

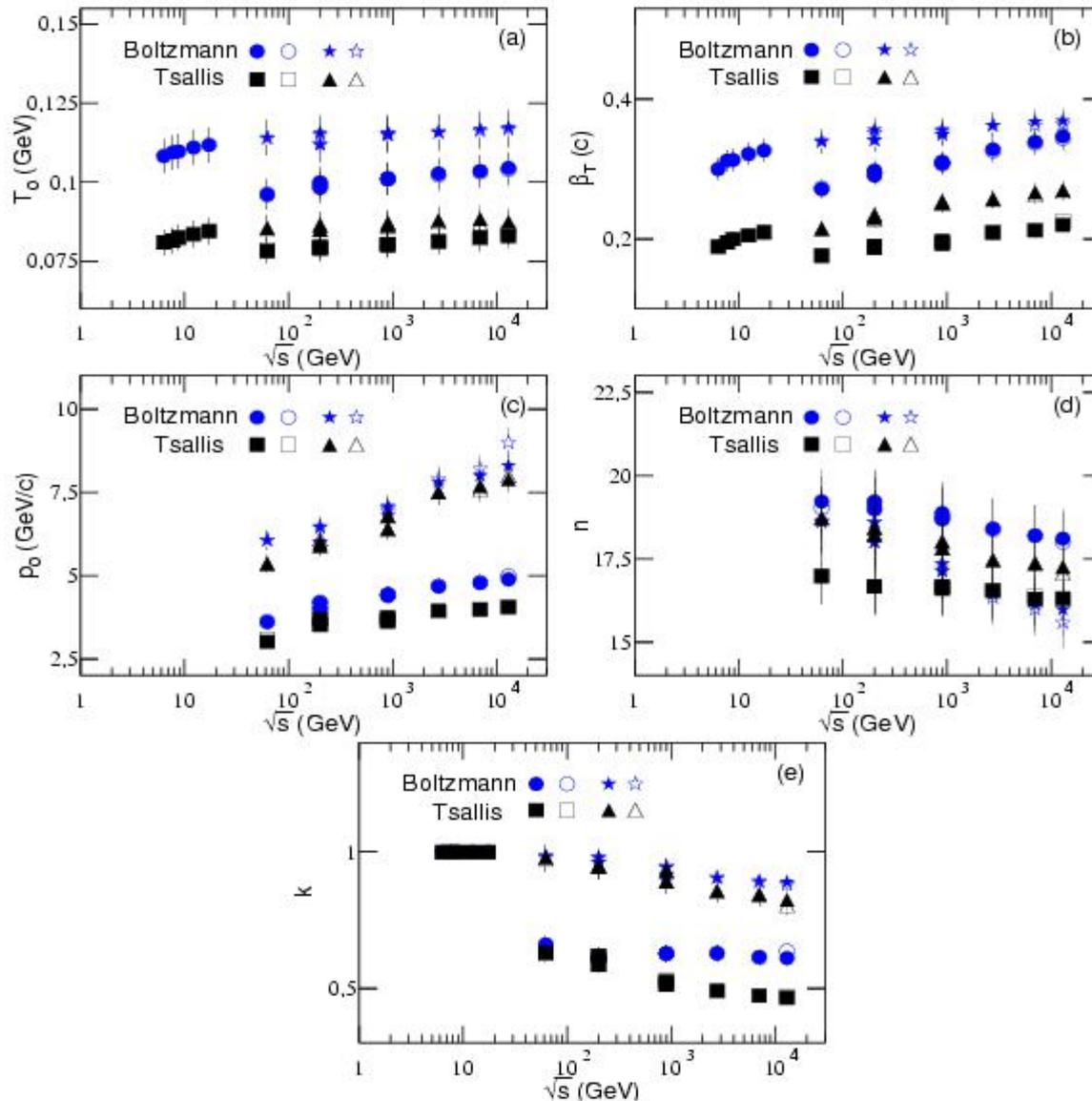
Transverse momentum spectra of  $\pi^-$  and  $\pi^+$  produced at mid-(pseudo)rapidity in pp collisions at high center-of-mass energies.

合作组	能量(GeV)
NA61/SHINE	6.3 7.7 8.8 12.3 17.3
PHENIX	62.4 200
STAR	200
ALICE	900
CMS	900 2760 7000 13000

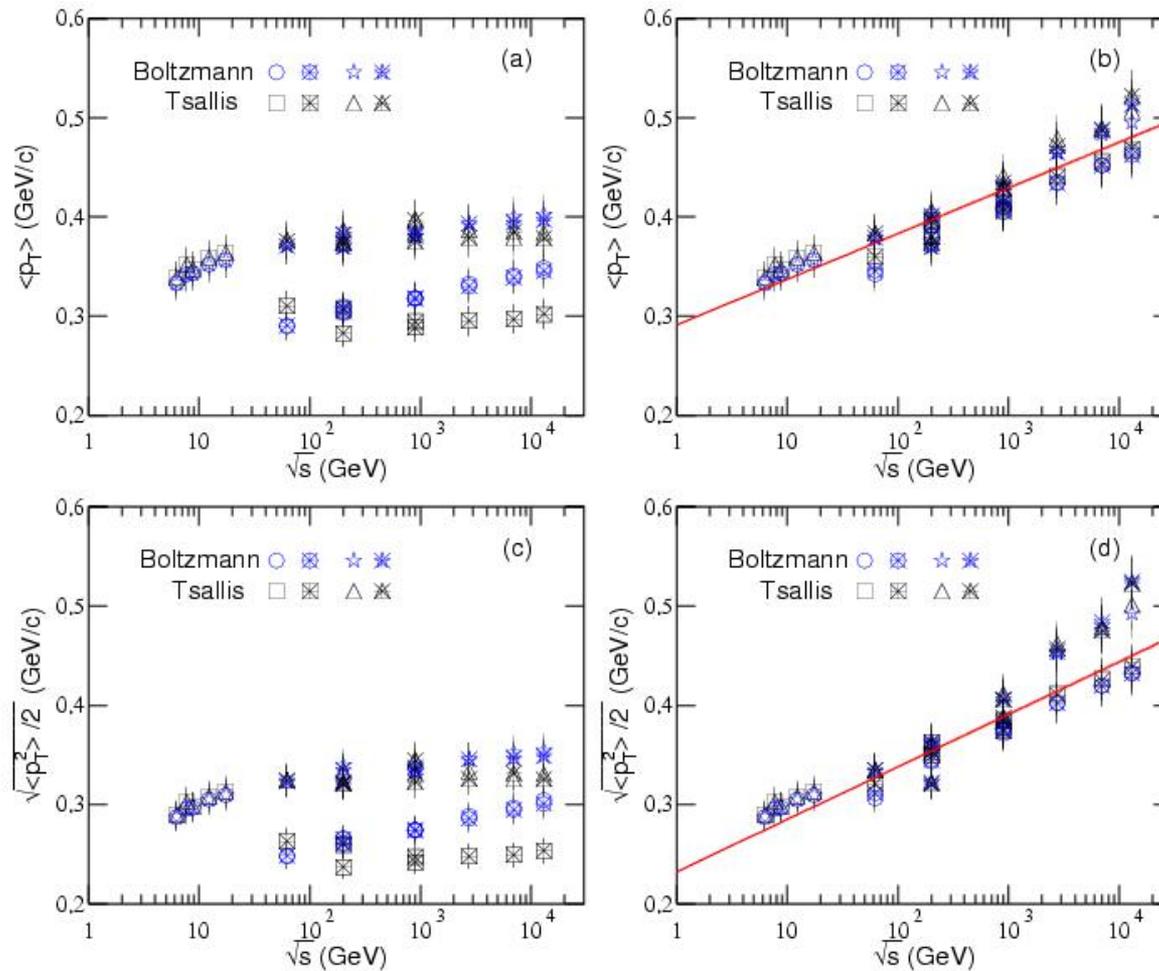
$$f_3(p_T) = kf_s(p_T) + (1-k)f_H(p_T)$$



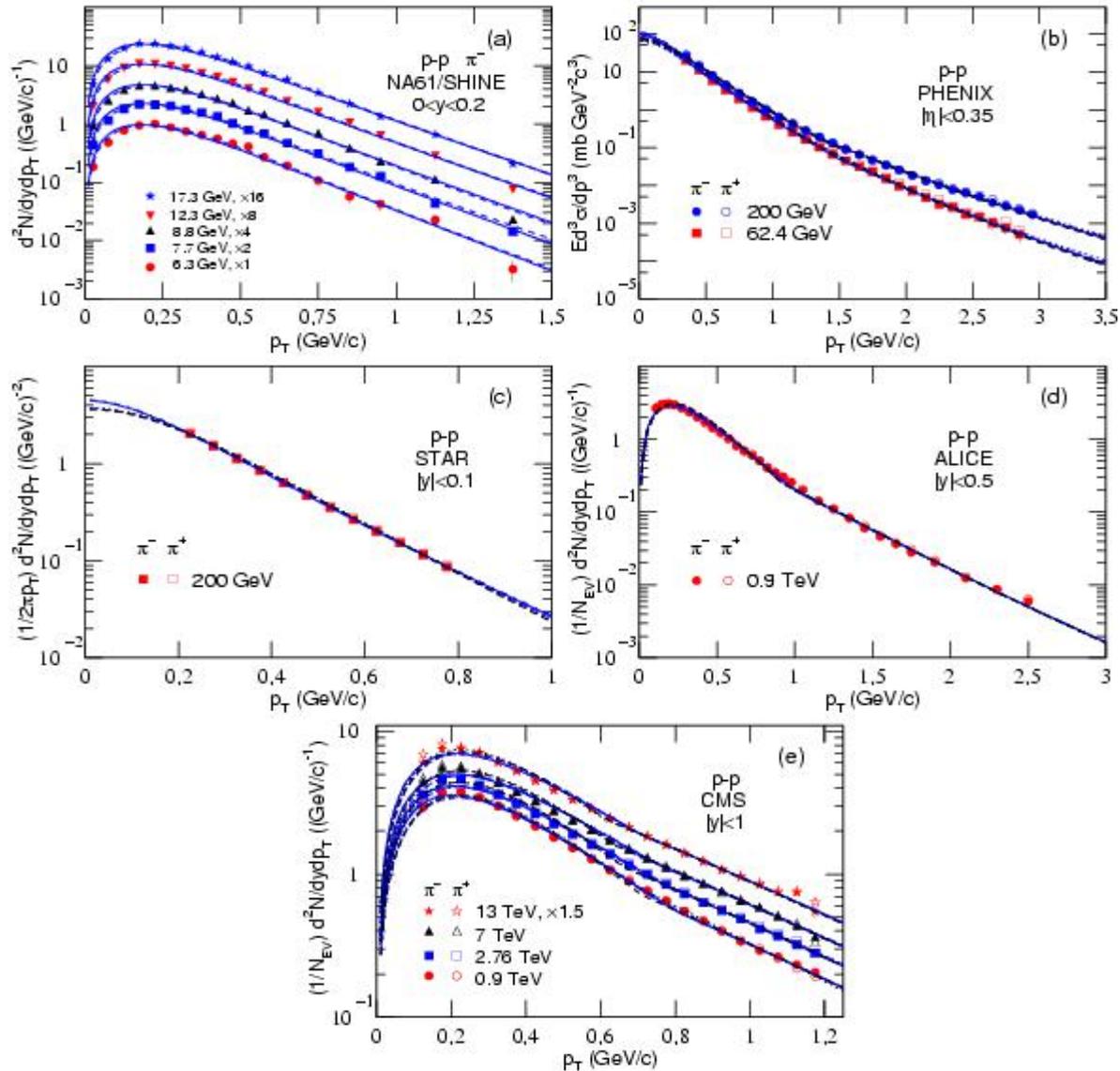
$$f_3(p_T) = kf_s(p_T) + (1-k)f_H(p_T)$$



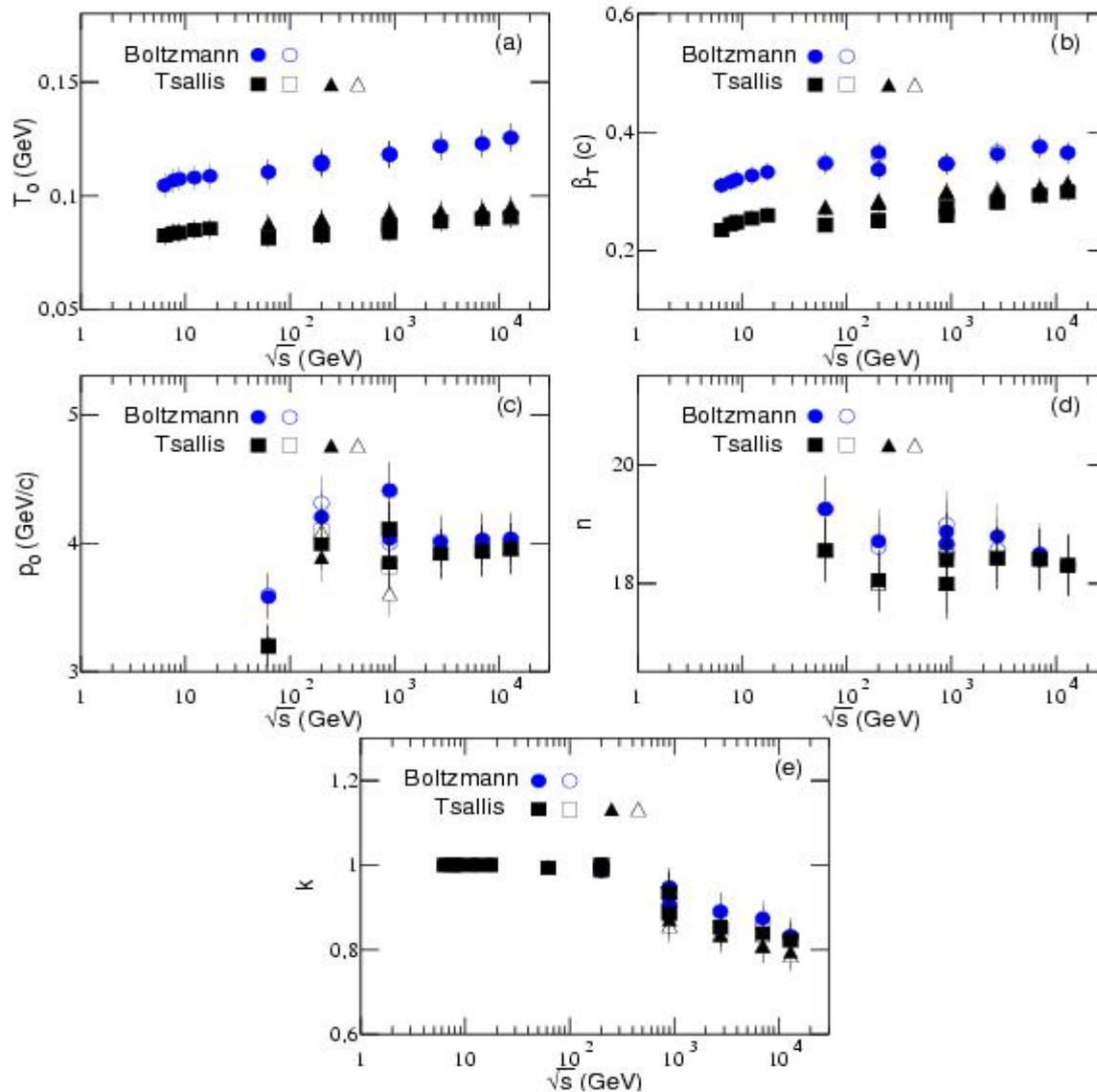
$$f_3(p_T) = kf_s(p_T) + (1-k)f_H(p_T)$$



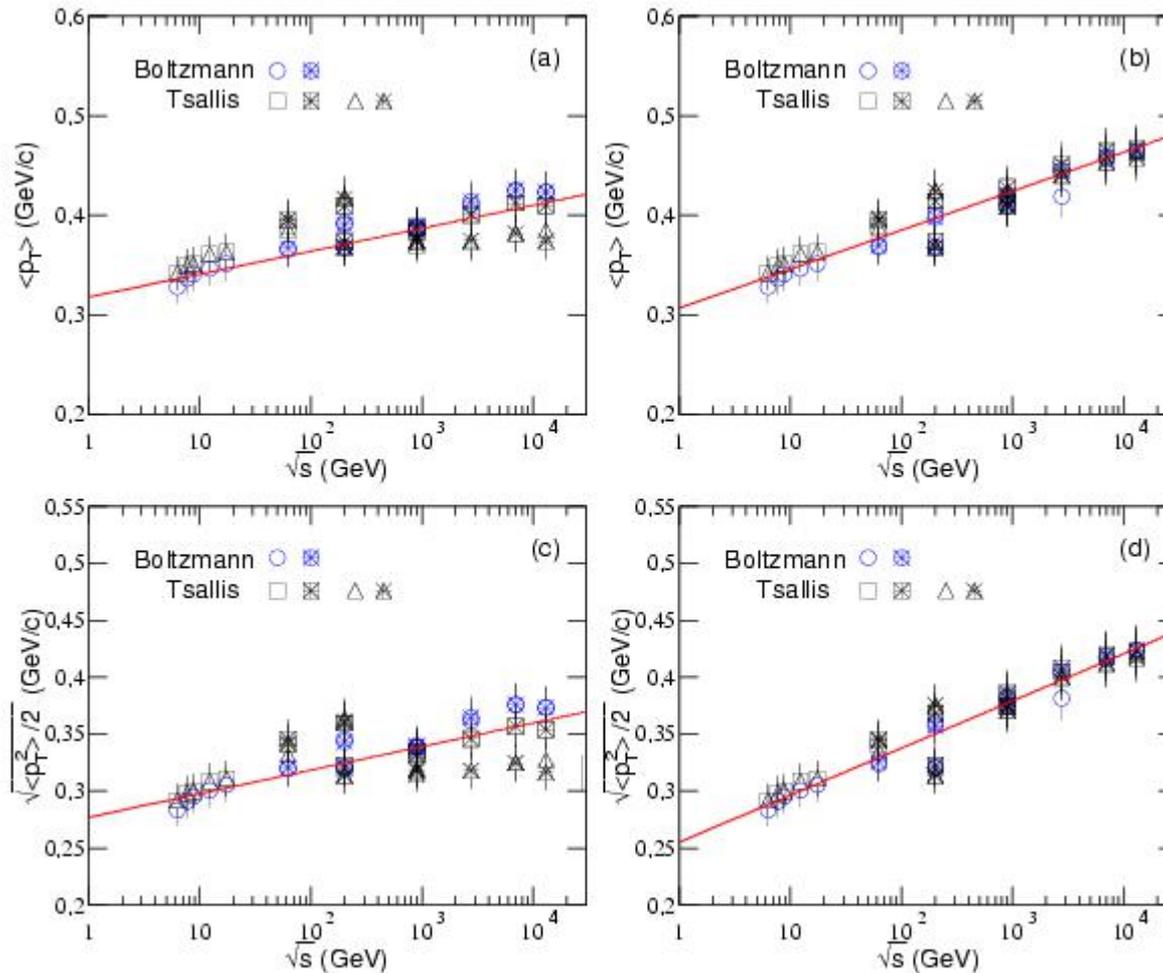
$$f_4(p_T) = A_1 \theta(p_1 - p_T) f_S(p_T) + A_2 \theta(p_T - p_1) f_H(p_T)$$



$$f_4(p_T) = A_1 \theta(p_1 - p_T) f_S(p_T) + A_2 \theta(p_T - p_1) f_H(p_T)$$



$$f_4(p_T) = A_1 \theta(p_1 - p_T) f_S(p_T) + A_2 \theta(p_T - p_1) f_H(p_T)$$



# Summary and Conclusion

➤ Excitation functions of  $T_0$  and  $\beta_T$

Blast-wave model with **Boltzmann-Gibbs** show a hill at  $\sqrt{s} \approx 10 \text{ GeV}$ , a drop at dozen of GeV, and an increase from dozens of GeV to above 10 TeV.

Blast-wave model with **Tsallis** only have a very low hill.

➤ The **mean transverse momentum** and the **initial temperature** increase approximately linearly with the increase of logarithmic collision energy.

➤ At around 10 GeV, a transition from a **baryon-dominated** to a **meson-dominated** intermediate and final state takes place.

From dozens of GeV to above 10 TeV, a transition from a **meson-dominated** to a **parton-dominated** intermediate takes place.

➤ It is a long-term target to search for **the critical energy** at which a parton-dominated intermediate state appears initially.

# Thanks for your attention!

This work was supported by the National Natural Science Foundation of China (Nos. 11575103 and 11747319), the Shanxi Provincial Natural Science Foundation (No. 201701D121005), and the Fund for Shanxi “1331 Project” Key Subjects Construction.