

Investigation of h_c Decay Patterns at BESIII

Meike Küßner

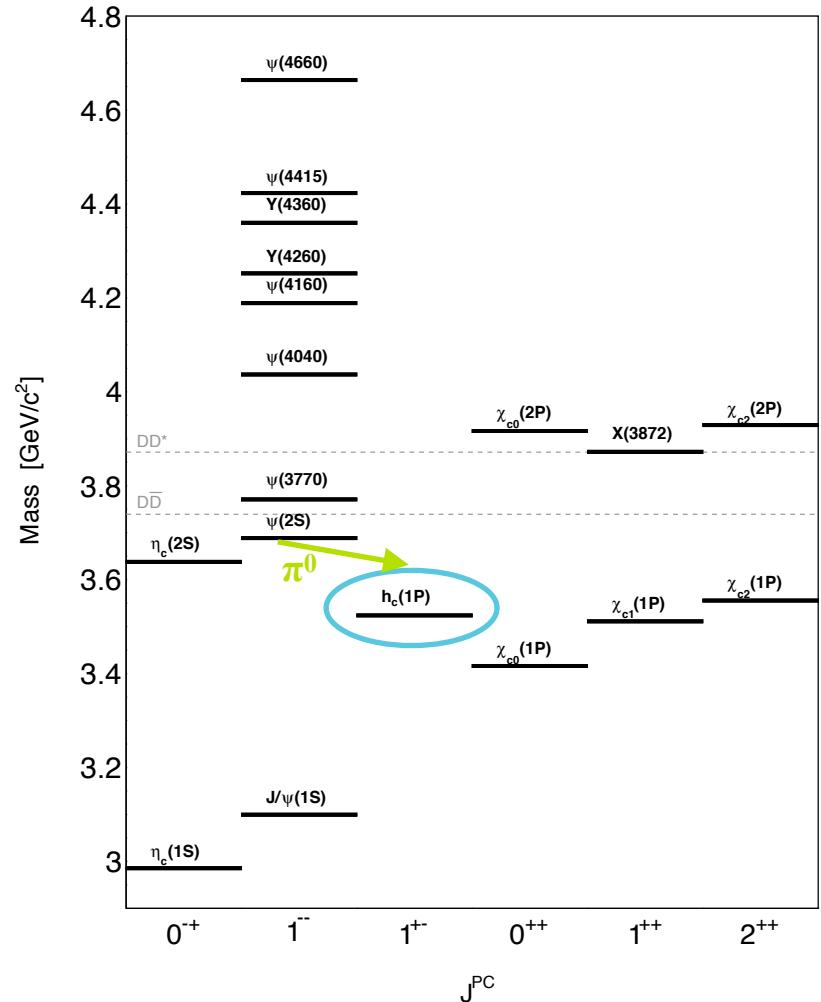
Ruhr University Bochum – Institute for Experimental Physics I

BESIII Charmonium Group Meeting

Introduction

- h_c singlet P-wave charmonium state
- experimentally observed 1992 in $\bar{p}p$ reactions [Phys. Rev. Lett. 69, 2337]
- not directly accessible in $e^+ e^-$ annihilation
- decay pattern still not well known

process	$BF(h_c \rightarrow X)$
$\gamma\eta_c$	$51 \pm 6\%$
$\gamma\eta$	$(4.7 \pm 2.1) \cdot 10^{-4}$
$\gamma\eta'$	$(1.5 \pm 0.4) \cdot 10^{-3}$
$\pi^+\pi^-\pi^0$	$(1.60 \pm 0.63) \cdot 10^{-3}$
$2(\pi^+\pi^-)\pi^0$	$(7.76 \pm 2.07) \cdot 10^{-3}$
$3(\pi^+\pi^-)\pi^0$	$< 8.67 \cdot 10^{-3}$
$\bar{p}p$	$< 1.5 \cdot 10^{-4}$



Final States Analyzed

3-body final states

- $h_c \rightarrow K^+K^-\pi^0, K_S^0K^\pm\pi^\mp$
- $h_c \rightarrow K^+K^-\eta$

4-body final states

- $h_c \rightarrow \pi^+\pi^-\pi^0\eta$
- $h_c \rightarrow K^+K^-\pi^0\eta$
- $h_c \rightarrow \bar{p}p\pi^0\pi^0$

5-body final states

- $h_c \rightarrow K^+K^-\pi^+\pi^-\pi^0, K_S^0K^\pm\pi^\mp\pi^+\pi^-$
- $h_c \rightarrow K^+K^-\pi^+\pi^-\eta$
- $h_c \rightarrow 2(K^+K^-)\pi^0$

Final States Analyzed

3-body final states

- $h_c \rightarrow K^+K^-\pi^0, K_S^0K^\pm\pi^\mp$
- $h_c \rightarrow K^+K^-\eta$

5-body final states

- $h_c \rightarrow K^+K^-\pi^+\pi^-\pi^0, K_S^0K^\pm\pi^\mp\pi^+\pi^-$

- $h_c \rightarrow K^+K^-\pi^+\pi^-\eta$

- $h_c \rightarrow 2(K^+K^-)\pi^0$

4-body final states

- $h_c \rightarrow \pi^+\pi^-\pi^0\eta$
- $h_c \rightarrow K^+K^-\pi^0\eta$
- $h_c \rightarrow \bar{p}p\pi^0\pi^0$

Data sets

- Using production via $\psi' \rightarrow \pi^0 h_c$
- Production using XYZ data via $X \rightarrow \pi^+ \pi^- h_c$ not suitable due to smaller reconstruction efficiency and lower production rate

Beam data: $448.1 \cdot 10^6 \psi'$ events

inclusive MC: $506 \cdot 10^6$ events

Signal MC: $1 \cdot 10^6$ events per final state

Boss Version: 664p03

General selection criteria

Good charged track criteria

Poca: $R_{xy} < 1 \text{ cm}$, $R_z < 10 \text{ cm}$

Polar angle: $|\cos \theta| < 0.93$

PID criteria

using dE/dx information from MDC and
TOF information

p-Value: $P(X) > 10^{-3}$,

$P(X) > P(Y)$, $X \neq Y$

Good photon criteria

Separation from tracks: $\Delta\Omega > 10^\circ$

EMC time info: $t < 700 \text{ ns}$

Barrel: $E_\gamma > 25 \text{ MeV}$,

$|\cos \theta| < 0.8$

Endcaps: $E_\gamma > 50 \text{ MeV}$,

$0.86 < |\cos \theta| < 0.92$

Reconstruction of π^0 candidates

$|M(\gamma\gamma) - M(\pi^0)| < 30 \text{ MeV}/c^2$

mass constrained fit

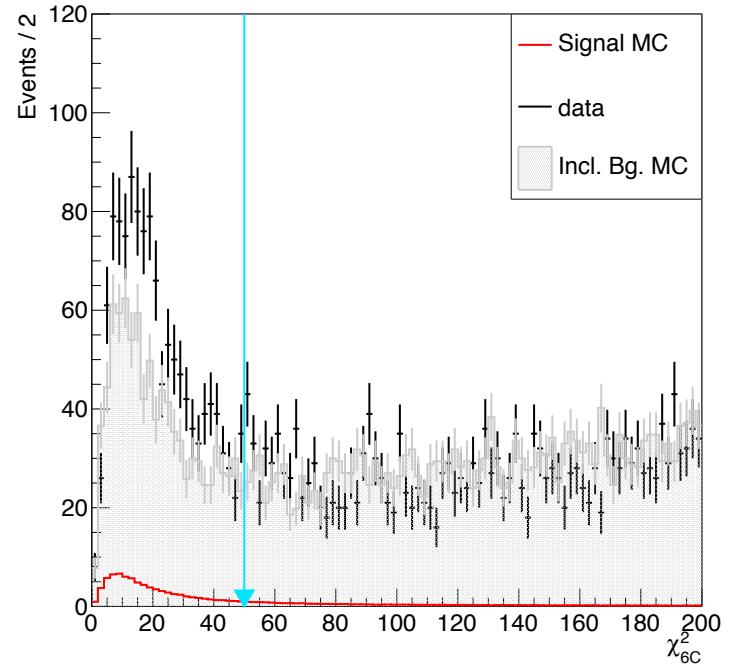
Reconstruction of η candidates

$|M(\gamma\gamma) - M(\eta)| < 30 \text{ MeV}/c^2$

mass constrained fit

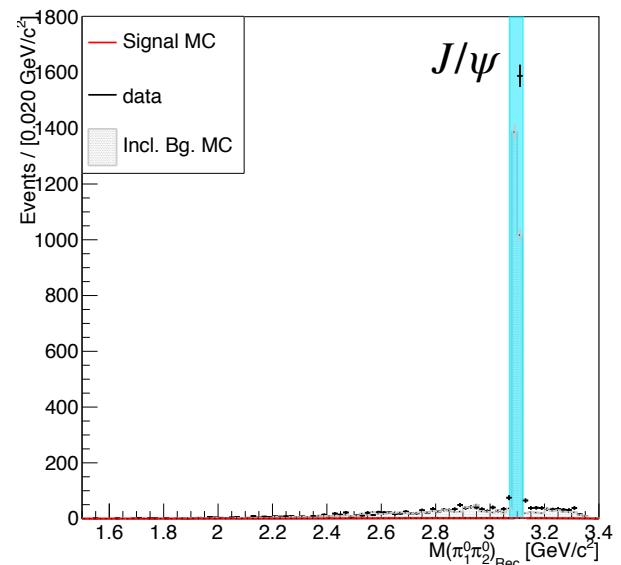
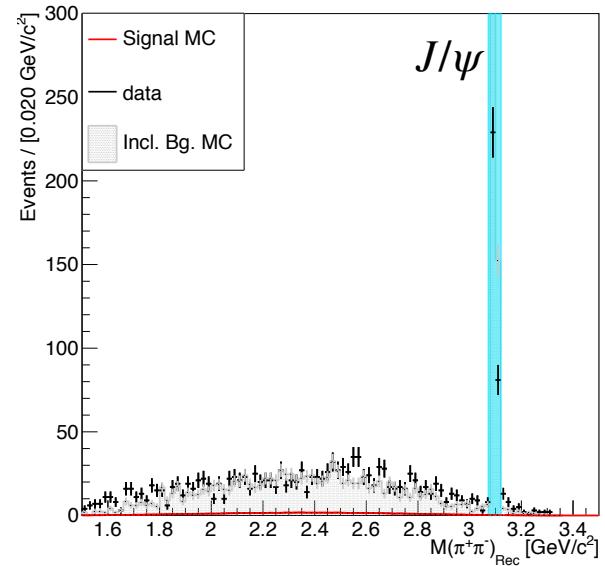
Analysis of $h_c \rightarrow K^+K^-\pi^+\pi^-\pi^0$

- Common vertex ensured by converged vertex fit
- $N_\pi = 2, N_K = 2, N_\gamma \geq 4$
- Limit goodness of 6C Fit: $\chi^2_{6C} < 50$



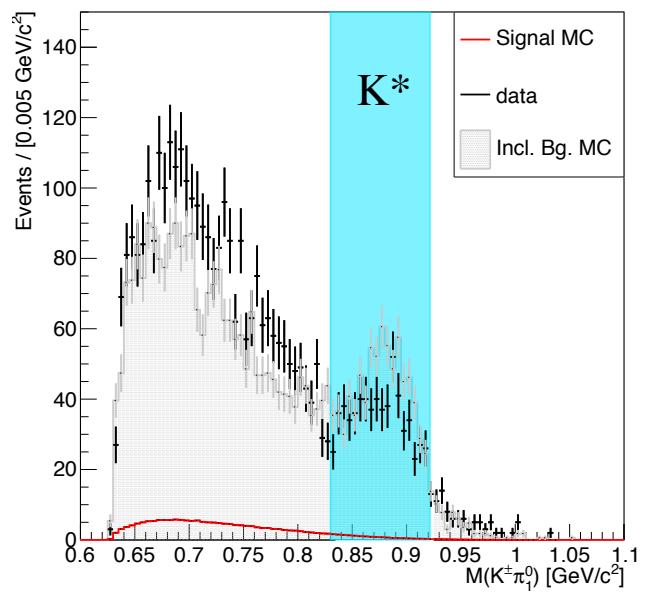
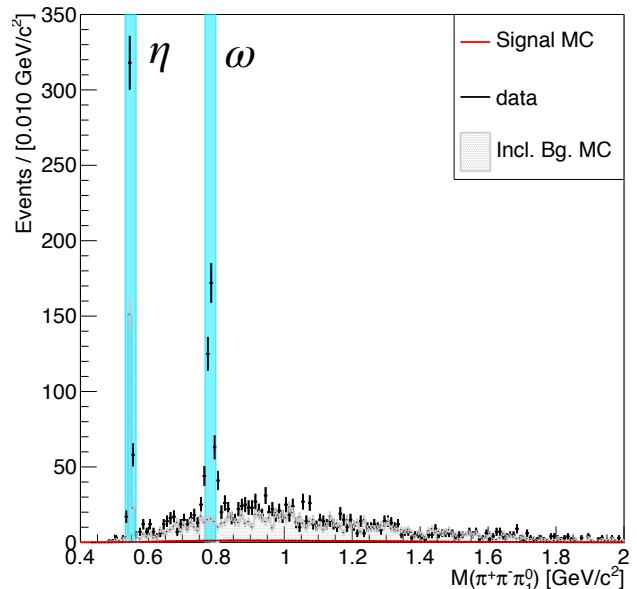
Analysis of $h_c \rightarrow K^+K^-\pi^+\pi^-\pi^0$

- Common vertex ensured by converged vertex fit
- $N_\pi = 2, N_K = 2, N_\gamma \geq 4$
- Limit goodness of 6C Fit: $\chi^2_{6C} < 50$
- additional 4C fit under hypothesis $3\gamma K^+K^-\pi^+\pi^-$ to veto background from
 - $\psi' \rightarrow \gamma\chi_{cJ}$: $\chi^2_{4C} < \chi^2_{3\gamma}$
- reject background from $\psi' \rightarrow \pi^+\pi^- J/\psi, \pi^0\pi^0 J/\psi$:
 - $|M(\pi^+\pi^-)_{Rec} - M(J/\psi)| > 25 \text{ MeV}/c^2$
 - $|M(\pi^0\pi^0)_{Rec} - M(J/\psi)| > 25 \text{ MeV}/c^2$



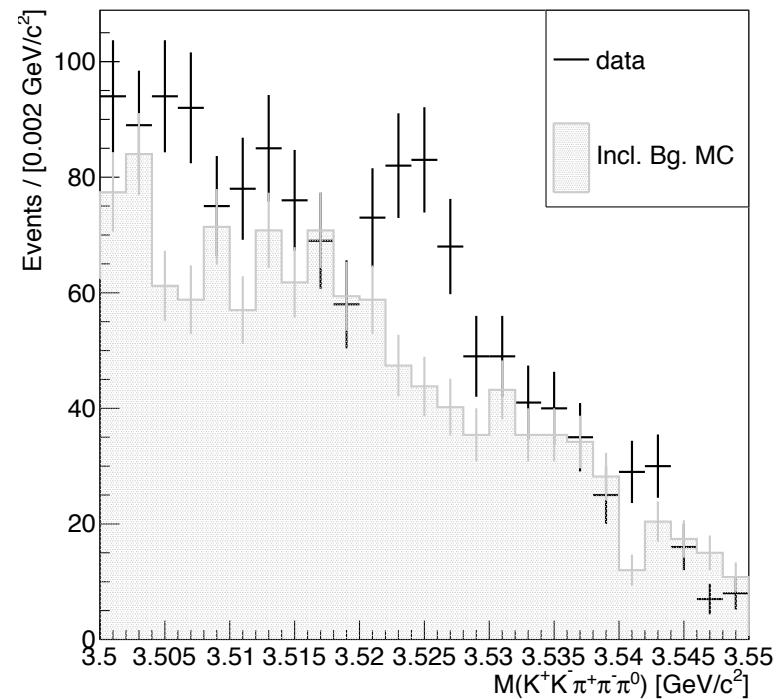
Analysis of $h_c \rightarrow K^+K^-\pi^+\pi^-\pi^0$

- Common vertex ensured by converged vertex fit
- $N_\pi = 2, N_K = 2, N_\gamma \geq 4$
- Limit goodness of 6C Fit: $\chi^2_{6C} < 50$
- additional 4C fit under hypothesis $3\gamma K^+K^-\pi^+\pi^-$ to veto background from
 - $\psi' \rightarrow \gamma\chi_{cJ}$: $\chi^2_{4C} < \chi^2_{3\gamma}$
- reject background from $\psi' \rightarrow \pi^+\pi^- J/\psi, \pi^0\pi^0 J/\psi$:
 - $|M(\pi^+\pi^-)_{Rec} - M(J/\psi)| > 25 \text{ MeV}/c^2$
 - $|M(\pi^0\pi^0)_{Rec} - M(J/\psi)| > 25 \text{ MeV}/c^2$
- π^0 from ψ' decay should not from other resonances:
 - $|M(\pi^+\pi^-\pi^0) - M(\eta)| > 16 \text{ MeV}/c^2$
 - $|M(\pi^+\pi^-\pi^0) - M(\omega)| > 20 \text{ MeV}/c^2$
 - $0.82 \text{ GeV}/c^2 \leq M(K^\pm\pi_1^0) \leq 0.92 \text{ GeV}/c^2$



Analysis of $h_c \rightarrow K^+K^-\pi^+\pi^-\pi^0$

- Common vertex ensured by converged vertex fit
 - $N_\pi = 2, N_K = 2, N_\gamma \geq 4$
 - Limit goodness of 6C Fit: $\chi_{6C}^2 < 50$
 - additional 4C fit under hypothesis $3\gamma K^+K^-\pi^+\pi^-$ to veto background from
 - $\psi' \rightarrow \gamma\chi_{cJ}$: $\chi_{4C}^2 < \chi_{3\gamma}^2$
 - reject background from $\psi' \rightarrow \pi^+\pi^- J/\psi, \pi^0\pi^0 J/\psi$:
 - $|M(\pi^+\pi^-)_{Rec} - M(J/\psi)| > 25 \text{ MeV}/c^2$
 - $|M(\pi^0\pi^0)_{Rec} - M(J/\psi)| > 25 \text{ MeV}/c^2$
 - π^0 from ψ' decay should not from other resonances:
 - $|M(\pi^+\pi^-\pi^0) - M(\eta)| > 16 \text{ MeV}/c^2$
 - $|M(\pi^+\pi^-\pi^0) - M(\omega)| > 20 \text{ MeV}/c^2$
 - $0.82 \text{ GeV}/c^2 \leq M(K^\pm\pi_1^0) \leq 0.92 \text{ GeV}/c^2$
- obtained efficiency 6.5%



Background studies

- Non-resonant contribution dominates (99%)

process	N_{rem}
$K^{*0} K^{*\pm} \pi^\mp \pi^0$	437
$K^{*\pm} K^{*\mp} \pi^+ \pi^-$	230
$K^{*0} K^{*\pm} \rho^\mp$	185
$K^{*+} K^{*-} \rho^0$	25

- Study of peaking background caused by radiative decays:

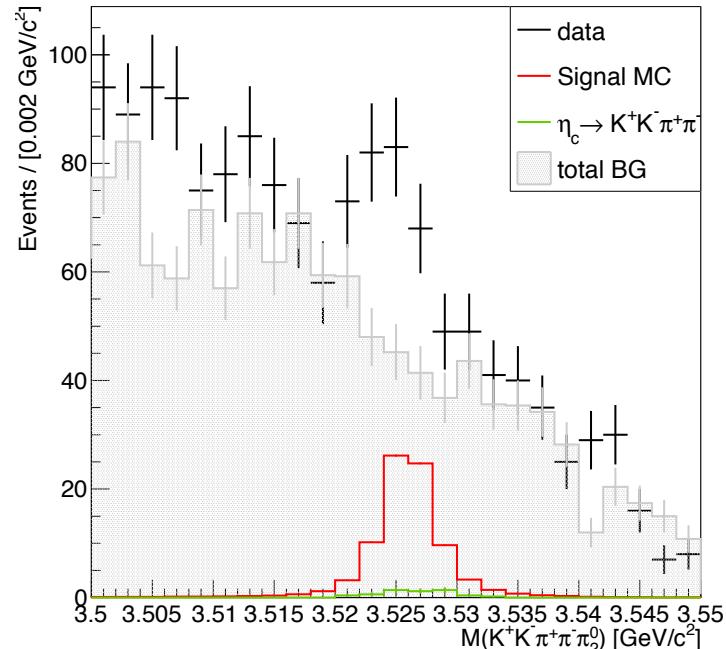
- $h_c \rightarrow \gamma \eta_c, \gamma \chi_{c1}, \gamma \chi_{c0}$

✖ Problem: decay modes mostly unknown, explicit search limited by statistics and dominated by background

→ But theoretical predictions exist, used to estimate:

- $\text{BF}(h_c \rightarrow \gamma \chi_{c1}) \sim 3.4 \cdot 10^{-7}$ (suppressed by PHSP)
- $\text{BF}(h_c \rightarrow \gamma \chi_{c1}) \sim 8.6 \cdot 10^{-4}$ [Phys. Rev. D 89 11 (2014)]

→ remaining peaking background taken into account within fit



- known decay modes scaled to PDG value
- unknown decay modes generated using LUND Model
- additional sets similar to final state have been generated (see next slide)

Background studies

List of explicitly generated final states

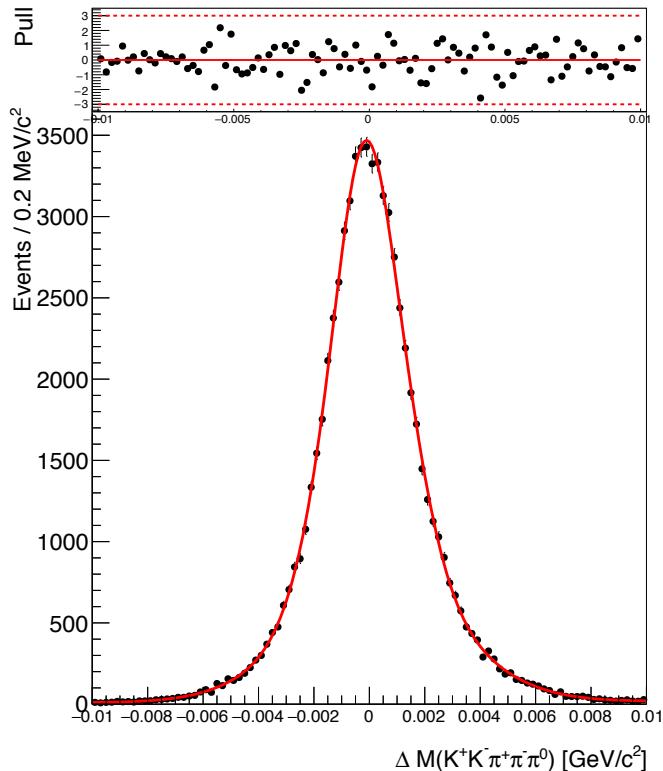
process $h_c \rightarrow \gamma X$	intermediate states	N_{rem}	N_{expected}
$\eta_c \rightarrow K^+ K^- \pi^+ \pi^-$	$K^{*0} K^{*\pm} \pi^\mp$	12	3
$\eta_c \rightarrow K^+ K^- \pi^+ \pi^-$	PSHP	10	2
$\eta_c \rightarrow K^+ K^- \pi^+ \pi^- \pi^0 \pi^0$	PHSP	2	0
$\eta_c \rightarrow K^+ K^- \pi^+ \pi^- \pi^0 \pi^0$	$K^{*+} K^{*-} \pi^0 \pi^0$	1	0
$\eta_c \rightarrow K^+ K^- \pi^+ \pi^- \pi^0 \eta$	PHSP	0	0
$\eta_c \rightarrow K^+ K^- \pi^+ \pi^- \pi^0 \eta$	$K^{*+} K^{*-} \pi^0 \eta$	0	0
$\eta_c \rightarrow K^+ K^- \pi^+ \pi^- \eta \eta$	PHSP	0	0
χ_{c0}	PHSP	5	0
χ_{c1}	PHSP	0	0

No background process identified,
which could describe the complete observed structure

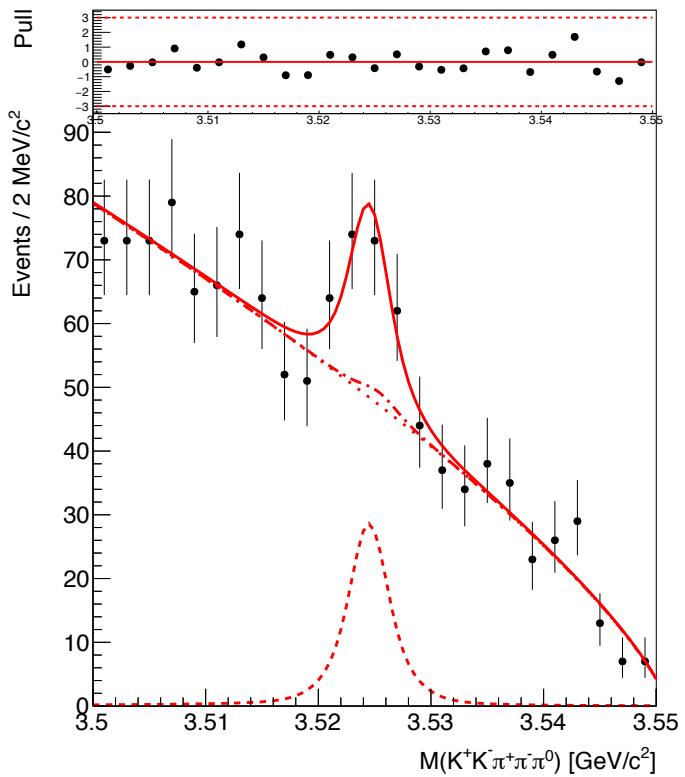
Determination of branching fraction of $h_c \rightarrow K^+K^-\pi^+\pi^-\pi^0$

Resolution

$$= \begin{cases} e^{\frac{\sigma_L^2}{2} + \sigma_L \left(\frac{m-\mu}{\sigma} \right)^2}, & \frac{m-\mu}{\sigma} \leq -\sigma_L \\ e^{-\frac{1}{2} \left(\frac{m-\mu}{\sigma} \right)^2}, & -\sigma_L < \frac{m-\mu}{\sigma} \leq \sigma_H \\ e^{\frac{\sigma_H^2}{2} - \sigma_H \left(\frac{m-\mu}{\sigma} \right)^2}, & \sigma_H < \frac{m-\mu}{\sigma} \end{cases} + 3 \text{ Gaussian}$$



Breit-Wigner \otimes Resolution + Argus



Significance calculated to 6.0σ

$$M(h_c) = 3524.9 \pm 0.6 \text{ MeV}/c^2$$

$$\Gamma(h_c) = 0.8 \pm 0.5 \text{ MeV}$$

$$\begin{aligned} BF(h_c \rightarrow K^+K^-\pi^+\pi^-\pi^0) \\ = (3.0 \pm 0.4 \pm 0.4 \pm 0.6) \cdot 10^{-3} \end{aligned}$$

BES III

Systematic studies

Selection procedure

- variation of selection criteria

cut	nominal value	range	step size	uncertainty
χ^2_{6C}	50	30-70	1	2.8 %
$ M(\pi^+\pi^-)_{Rec} - M(J/\psi) [MeV/c^2]$	25	10-40	1	0.5 %
$ M(\pi^0\pi^0)_{Rec} - M(J/\psi) [MeV/c^2]$	25	10-40	1	1.4 %
$ M(\pi^0K^\pm) - M(K^{*\pm}) [MeV/c^2]$	30	10-50	1	3.8 %
$ M(\pi^+\pi^-\pi^0) - M(\eta) [MeV/c^2]$	16	6-26	1	1.3 %
$ M(\pi^+\pi^-\pi^0) - M(\omega) [MeV/c^2]$	20	10-30	1	2.5 %

- Kinematic fit using helix correction method: 1.5%

Generator model

- including intermediate resonances to generator model leads efficiency difference of at most **5.1%**

Fit model

- Describing background by Chebychev polynomial instead of Argus function: **1.2%**
- Fitting range: **0.9%**

Tracking

- 1% per track \rightarrow 4%

Photon reconstruction

- 1% per photon \rightarrow 4%

PID

- 1% per track \rightarrow 4%

π^0 reconstruction

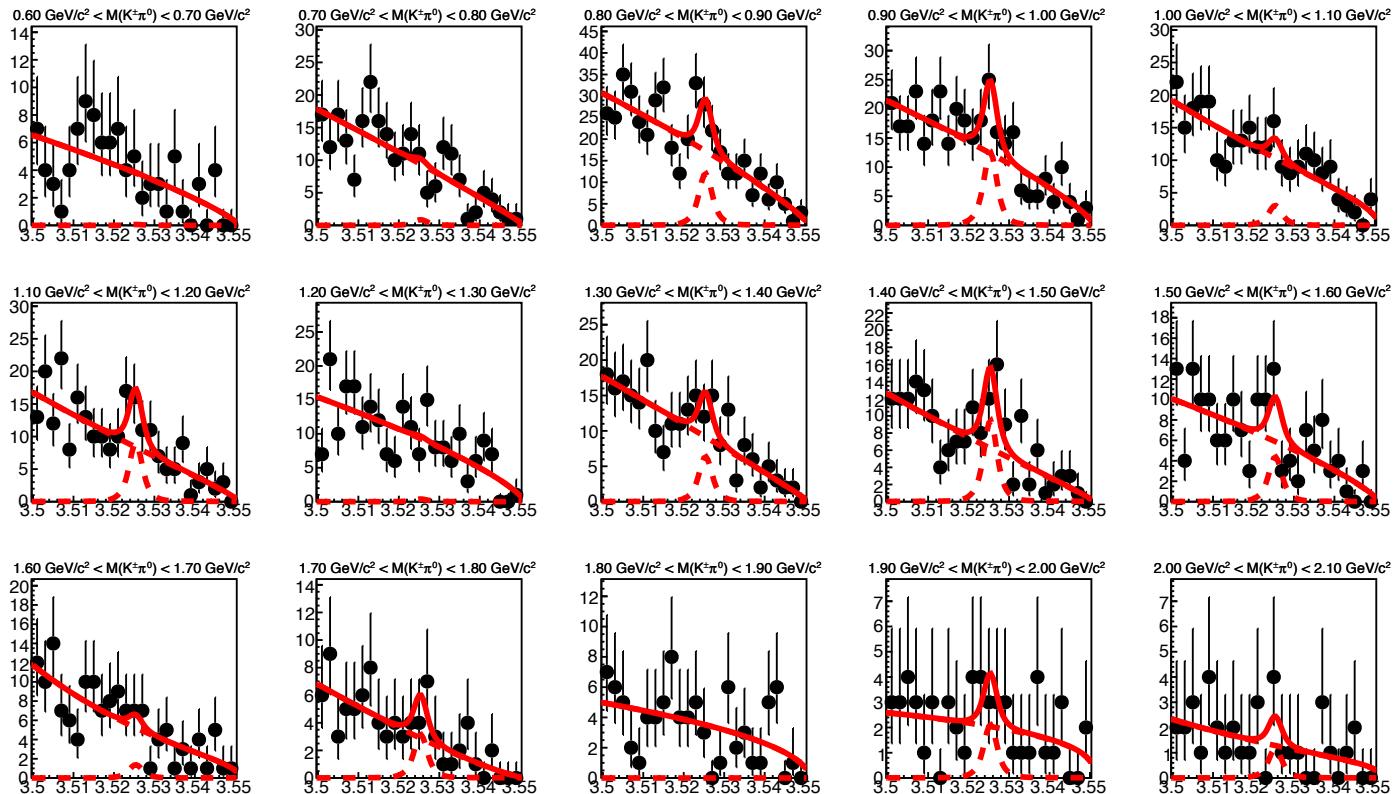
- 1% per $\pi^0 \rightarrow$ 2%

total 10.7% + 15.1% caused by involved branching fractions!

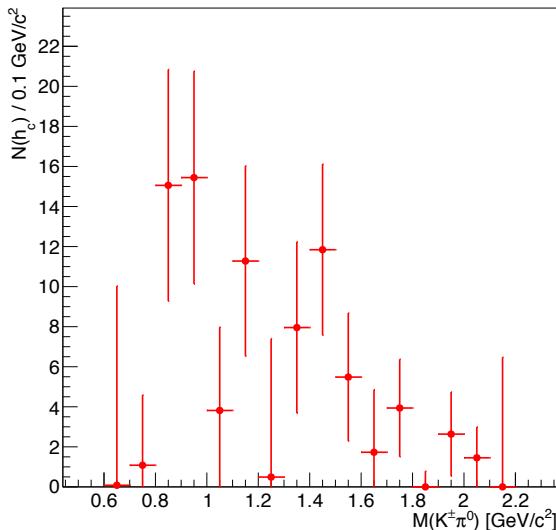
Study of intermediate resonances

- **Problem:** Background dominated process, sideband subtraction not suitable
- **Idea:** Extracting signal yield in slices of subsystems
- same fitting procedure used as before in subregions

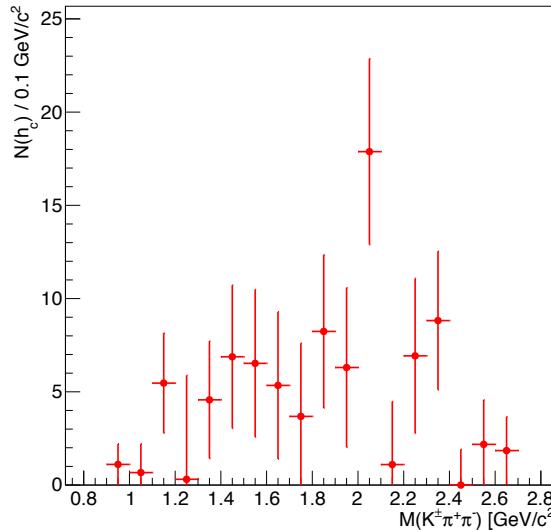
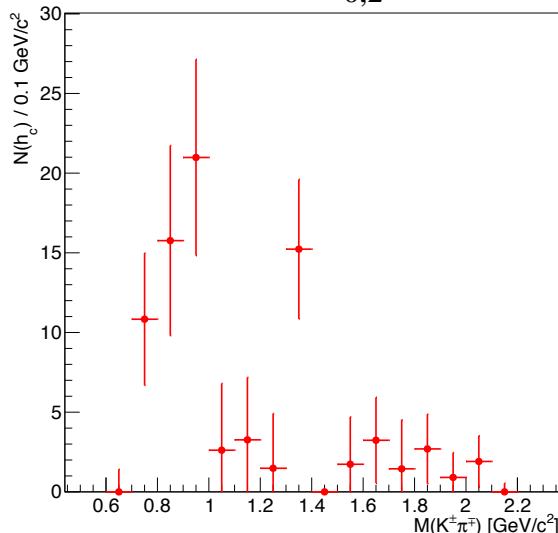
For example fit in slices of $K\pi$ mass



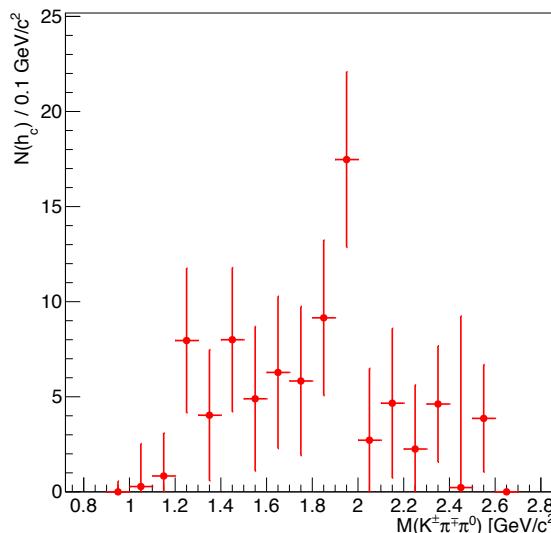
Study of intermediate resonances



$K^*(892), K_{0,2}^*(1430)$



$K_2(1820), K_2^*(1980)$

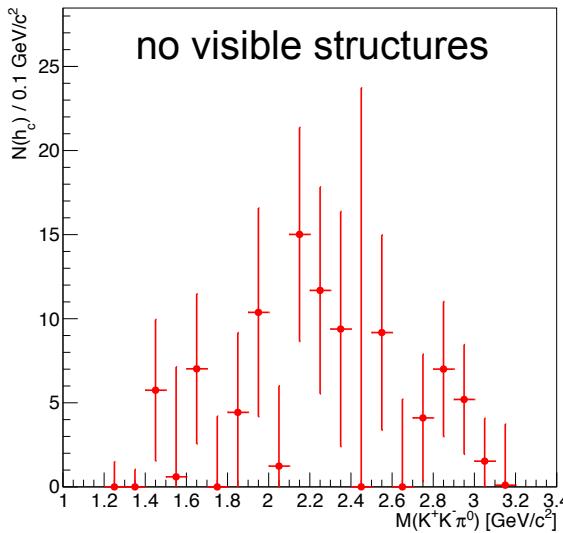
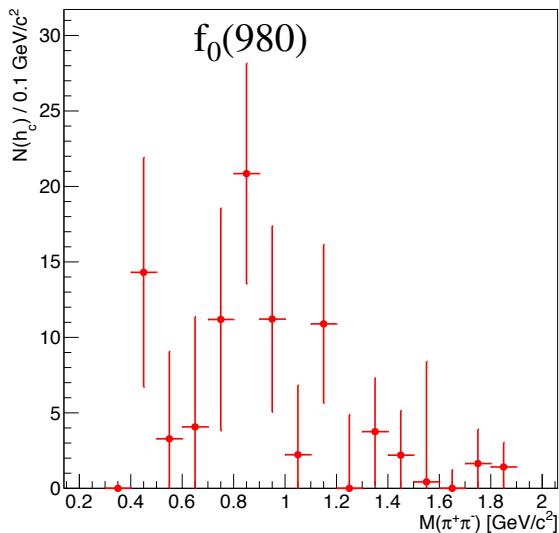
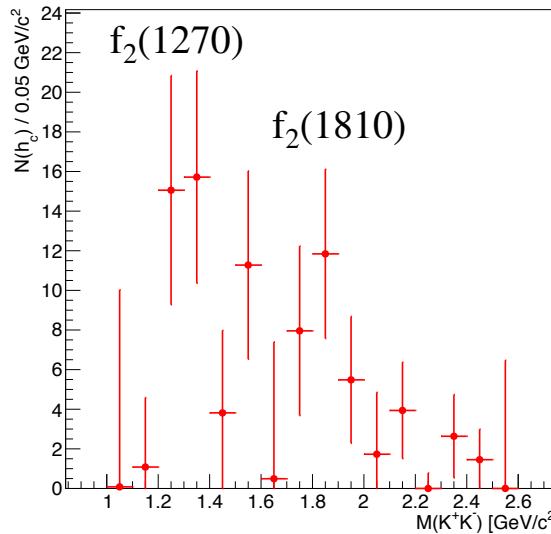
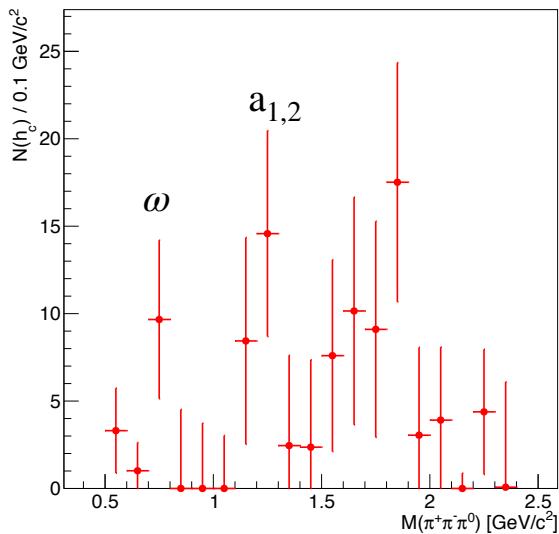


- shown error bars are statistical only
- similar structures in charged and neutral mode
- indication for intermediate reactions like:

$$h_c \rightarrow \left(K^*(892)/K_{0,2}^*(1430) \right)$$

$$\left(K_2(1820)/K_2^*(1980) \right)$$

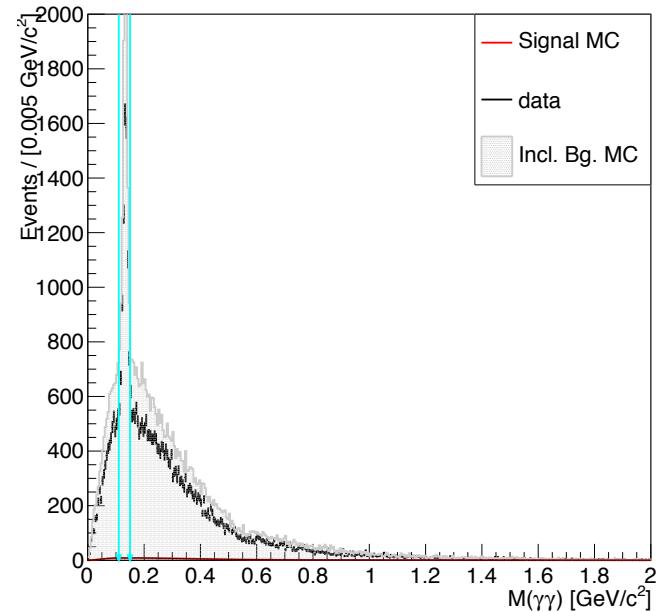
Study of intermediate resonances



- $h_c \rightarrow (\pi^+\pi^-\pi^0)(K^+K^-)$ seems to be more favored than $h_c \rightarrow (\pi^+\pi^-)(\pi^0K^+K^-)$
- Correlations between subsystems have been investigated by generating the supposed intermediate reactions

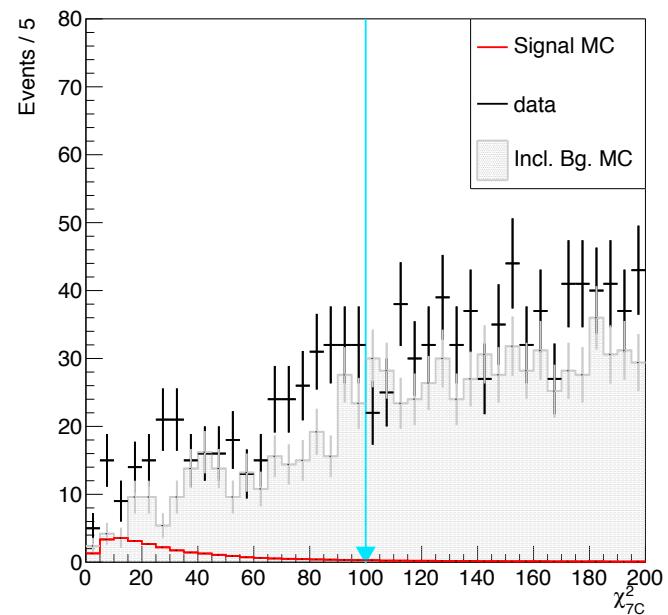
Analysis of $h_c \rightarrow \pi^+ \pi^- \pi^0 \eta$

- Common vertex ensured by converged vertex fit
- $N_\pi = 2, N_\gamma \geq 6$
- no pair of photons from different particles should form a π^0 :
 - $|M(\gamma\gamma) - M(\pi^0)| > 15 \text{ MeV}/c^2$



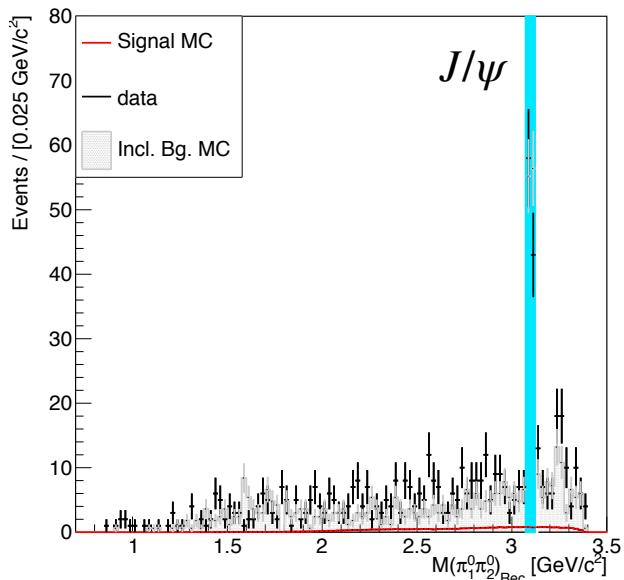
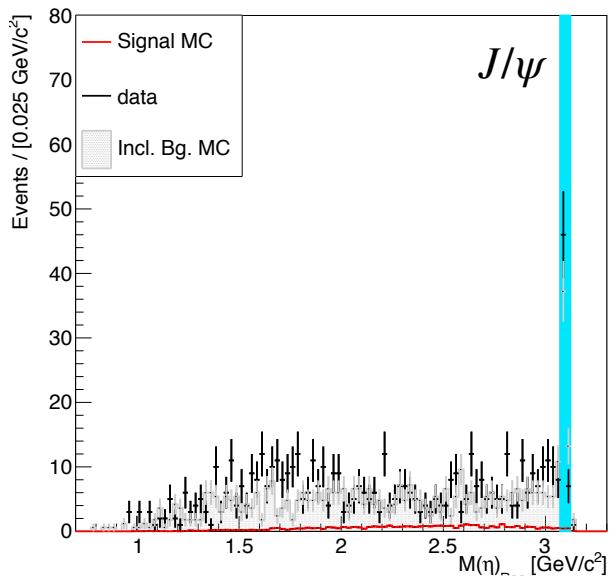
Analysis of $h_c \rightarrow \pi^+ \pi^- \pi^0 \eta$

- Common vertex ensured by converged vertex fit
- $N_\pi = 2, N_\gamma \geq 6$
- no pair of photons from different particles should form a π^0 :
 - $|M(\gamma\gamma) - M(\pi^0)| > 15 \text{ MeV}/c^2$
- Limit goodness of 7C-Fit: $\chi^2_{7C} < 100$



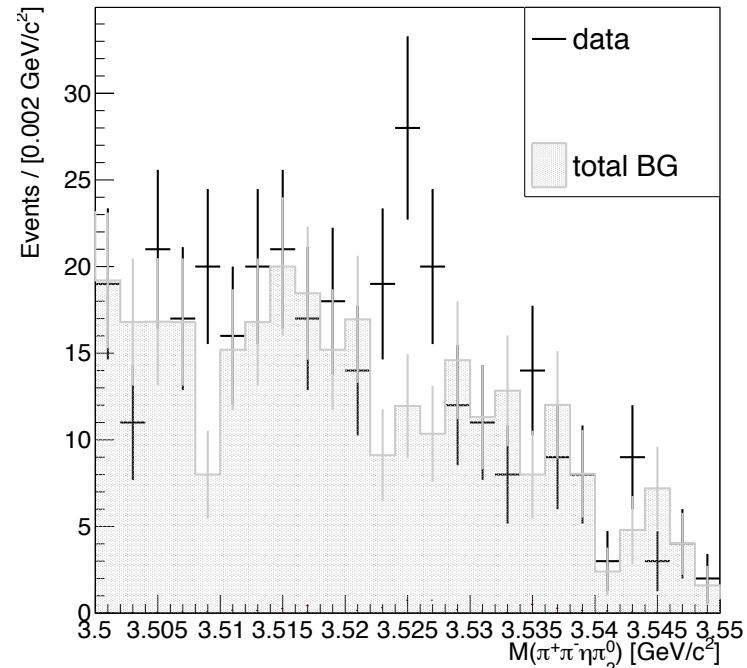
Analysis of $h_c \rightarrow \pi^+ \pi^- \pi^0 \eta$

- Common vertex ensured by converged vertex fit
- $N_\pi = 2, N_\gamma \geq 6$
- no pair of photons from different particles should form a π^0 :
 - $|M(\gamma\gamma) - M(\pi^0)| > 15 \text{ MeV}/c^2$
- Limit goodness of 7C-Fit: $\chi^2_{7C} < 100$
- π^0 from ψ' decay should not form resonances with other final state particles:
 - $|M(\pi^+ \pi^- \pi^0) - M(\eta)| > 16 \text{ MeV}/c^2$
 - $|M(\pi^+ \pi^- \pi^0) - M(\omega)| > 20 \text{ MeV}/c^2$
- reject background from $\psi' \rightarrow \pi^0 \pi^0 J/\psi, \eta J/\psi$:
 - $|M(\pi^0 \pi^0)_{Rec} - M(J/\psi)| > 30 \text{ MeV}/c^2$
 - $|M(\eta)_{Rec} - M(J/\psi)| > 30 \text{ MeV}/c^2$



Analysis of $h_c \rightarrow \pi^+ \pi^- \pi^0 \eta$

- Common vertex ensured by converged vertex fit
- $N_\pi = 2, N_\gamma \geq 6$
- no pair of photons from different particles should form a π^0 :
 - $|M(\gamma\gamma) - M(\pi^0)| > 15 \text{ MeV}/c^2$
- Limit goodness of 7C-Fit: $\chi^2_{7C} < 100$
- π^0 from ψ' decay should not form resonances with other final state particles:
 - $|M(\pi^+ \pi^- \pi^0) - M(\eta)| > 16 \text{ MeV}/c^2$
 - $|M(\pi^+ \pi^- \pi^0) - M(\omega)| > 20 \text{ MeV}/c^2$
- reject background from $\psi' \rightarrow \pi^0 \pi^0 J/\psi, \eta J/\psi$:
 - $|M(\pi^0 \pi^0)_{Rec} - M(J/\psi)| > 30 \text{ MeV}/c^2$
 - $|M(\eta)_{Rec} - M(J/\psi)| > 30 \text{ MeV}/c^2$

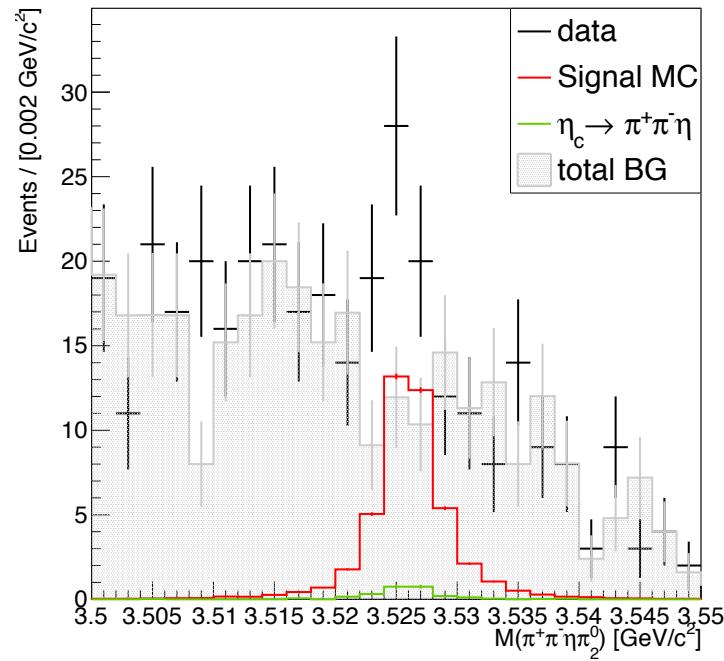


→ obtained efficiency 3.9 %

Background studies

- Dominating contribution from $e^+e^- \rightarrow 4\gamma\pi^+\pi^-\eta$
- Study of peaking background caused by radiative decays:
 - $h_c \rightarrow \gamma\chi_{c1}, \gamma\chi_{c0}$
 - negligible contribution
- $h_c \rightarrow \gamma\eta_c$

process	N_{rem}	N_{expected}
$\eta_c \rightarrow \pi^+\pi^-\pi^0$	16	3
$\eta_c \rightarrow \pi^+\pi^-\pi^0\pi^0$	7	1



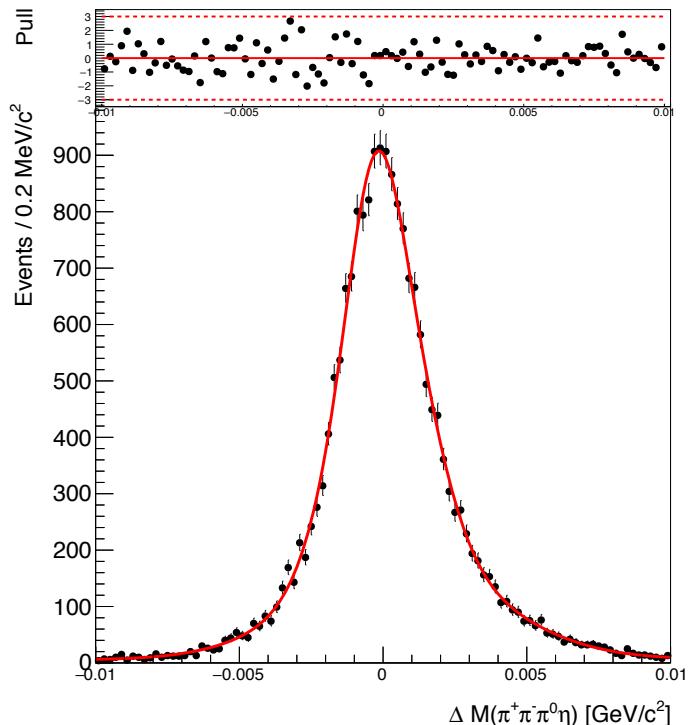
- known decay modes scaled to PDG value
- unknown decay modes generated using LUND Model

- peaking background is taken into account within the fit to determine the effective signal yield

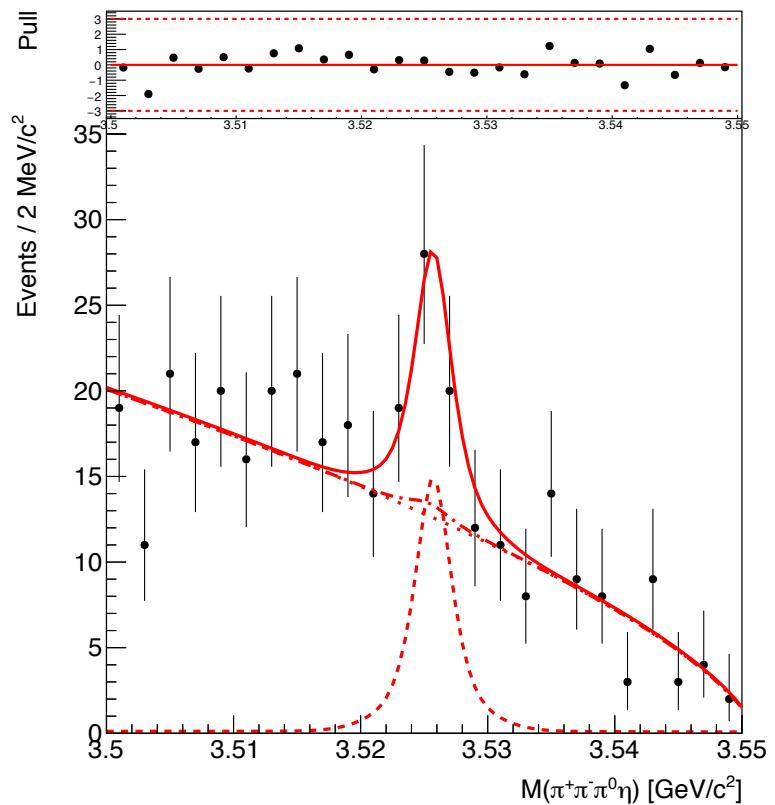
Determination of branching fraction of $h_c \rightarrow \pi^+ \pi^- \pi^0 \eta$

Resolution

$$= \begin{cases} e^{\frac{\sigma_L^2}{2} + \sigma_L \left(\frac{m-\mu}{\sigma} \right)^2}, & \frac{m-\mu}{\sigma} \leq -\sigma_L \\ e^{-\frac{1}{2} \left(\frac{m-\mu}{\sigma} \right)^2}, & -\sigma_L < \frac{m-\mu}{\sigma} \leq \sigma_H \\ e^{\frac{\sigma_H^2}{2} - \sigma_H \left(\frac{m-\mu}{\sigma} \right)^2}, & \sigma_H < \frac{m-\mu}{\sigma} \end{cases} + 3 \text{ Gaussian}$$



Breit-Wigner \otimes Resolution + Argus



$$\text{BF}(h_c \rightarrow \pi^+ \pi^- \pi^0 \eta) = (9.9 \pm 1.6 \pm 1.2 \pm 1.5) \cdot 10^{-3}$$

Significance calculated to 3.8σ

Systematic studies

Selection procedure

- variation of selection criteria

cut	nominal value	range	step size	uncertainty
χ^2_{7C}	100	80-120	1	3.1
$ M(\eta)_{\text{Rec}} - M(J/\psi) [\text{MeV}/c^2]$	30	15-45	1	1.3
$ M(\pi^0\pi^0)_{\text{Rec}} - M(J/\psi) [\text{MeV}/c^2]$	30	20-40	1	1.5
$ M(\gamma\gamma) - M(\pi^0) [\text{MeV}/c^2]$	15	5-25	1	2.8
$ M(\pi^+\pi^-\pi^0) - M(\eta) [\text{MeV}/c^2]$	16	6-26	1	1.6
$ M(\pi^+\pi^-\pi^0) - M(\omega) [\text{MeV}/c^2]$	20	10-30	1	2.2

- Kinematic fit using helix correction method: 2.1%

Generator model

- including intermediate resonances to generator model leads efficiency difference of at most **6.3%**

Fit model

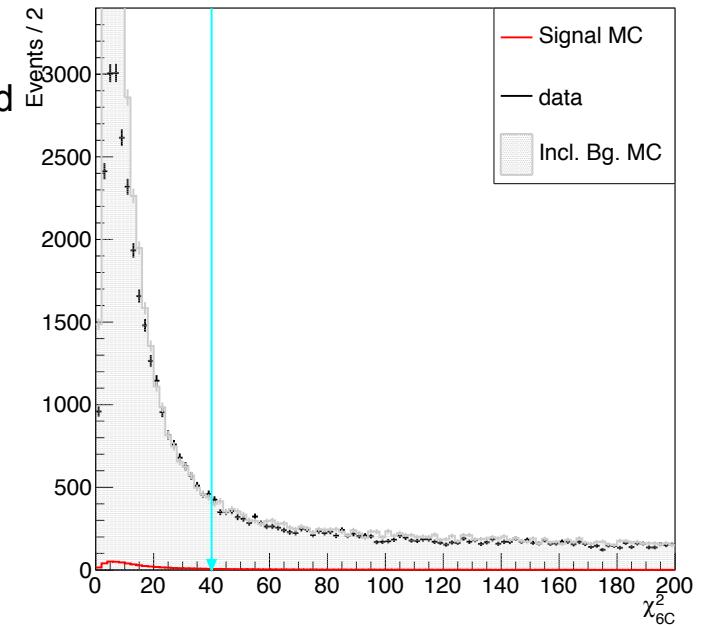
- Describing background by Chebychev polynomial instead of Argus function: **2.1%**
- Fitting range: **1.1%**

Tracking	Photon reconstruction	PID	π^0, η reconstruction
■ 1% per track \rightarrow 2%	■ 1% per photon \rightarrow 6%	■ 1% per track \rightarrow 2%	■ 1% per π^0 or η \rightarrow 3%

total 11.5% + 15.1% caused by involved branching fractions!

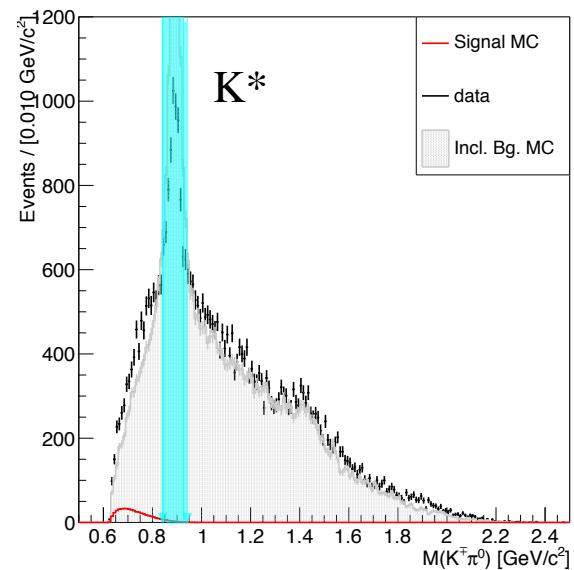
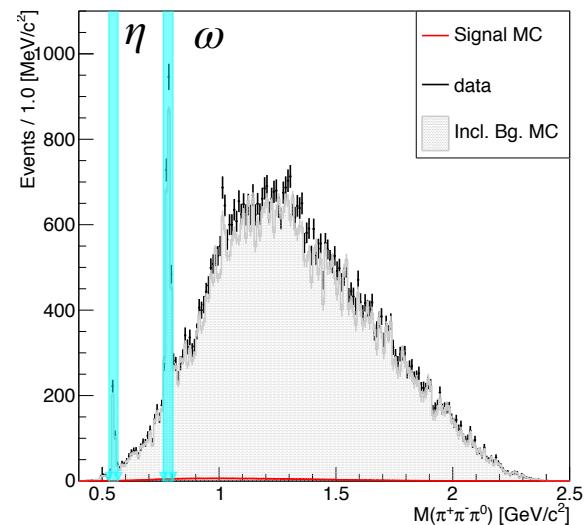
Analysis of $h_c \rightarrow K_S^0 K^\pm \pi^\mp \pi^+ \pi^-$

- $N_\pi = 5, N_K = 1, N_\gamma \geq 2$
- K_S^0 reconstruction:
 - Limit decay length and error determined by secondary vertex fit: $\lambda/\Delta\lambda < 2$
 - $0.487 \text{ MeV}/c^2 \leq M(\pi^+ \pi^-) \leq 0.511 \text{ MeV}/c^2$
- Common vertex ensured by converged vertex fit for all charged particles
- Limit goodness of 6C-Fit: $\chi_{6C}^2 < 40$



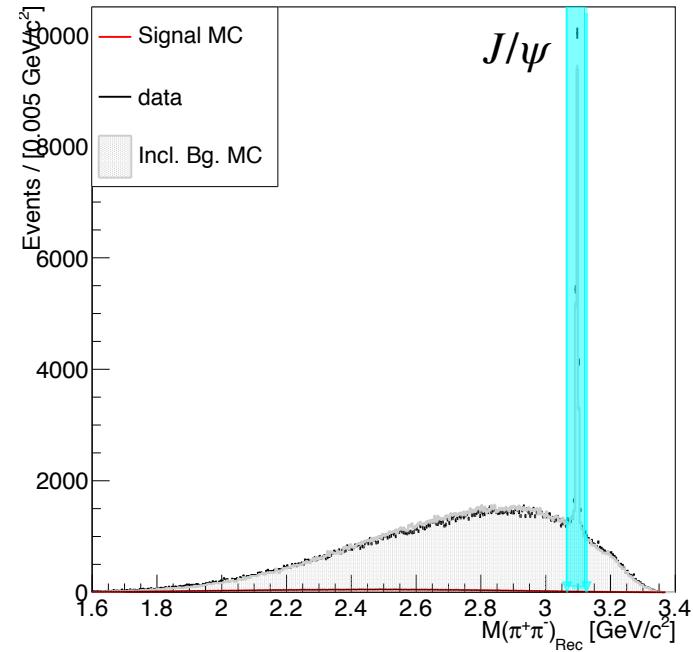
Analysis of $h_c \rightarrow K_S^0 K^\pm \pi^\mp \pi^+ \pi^-$

- $N_\pi = 5, N_K = 1, N_\gamma \geq 2$
- K_S^0 reconstruction:
 - Limit decay length and error determined by secondary vertex fit: $\lambda/\Delta\lambda < 2$
 - $0.487 \text{ MeV}/c^2 \leq M(\pi^+\pi^-) \leq 0.511 \text{ MeV}/c^2$
- Common vertex ensured by converged vertex fit for all charged particles
- Limit goodness of 6C-Fit: $\chi_{6C}^2 < 40$
- π^0 from ψ' decay should not from other resonances:
 - $|M(\pi^+\pi^-\pi^0) - M(\eta)| > 20 \text{ MeV}/c^2$
 - $|M(\pi^+\pi^-\pi^0) - M(\omega)| > 20 \text{ MeV}/c^2$
- No $K\pi$ system should form a K^* meson thus:
 - $|M(K^\pm\pi^0) - M(K^*)| > 50 \text{ MeV}/c^2$
 - $|M(K_S^0\pi^0) - M(K^*)| > 50 \text{ MeV}/c^2$



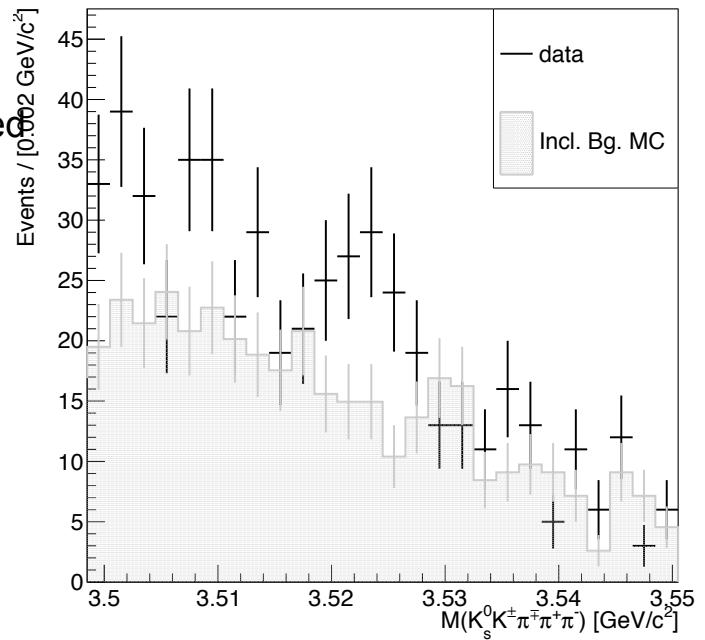
Analysis of $h_c \rightarrow K_S^0 K^\pm \pi^\mp \pi^+ \pi^-$

- $N_\pi = 5, N_K = 1, N_\gamma \geq 2$
- K_S^0 reconstruction:
 - Limit decay length and error determined by secondary vertex fit: $\lambda/\Delta\lambda < 2$
 - $0.487 \text{ MeV}/c^2 \leq M(\pi^+\pi^-) \leq 0.511 \text{ MeV}/c^2$
- Common vertex ensured by converged vertex fit for all charged particles
- Limit goodness of 6C-Fit: $\chi_{6C}^2 < 40$
- π^0 from ψ' decay should not from other resonances:
 - $|M(\pi^+\pi^-\pi^0) - M(\eta)| > 20 \text{ MeV}/c^2$
 - $|M(\pi^+\pi^-\pi^0) - M(\omega)| > 20 \text{ MeV}/c^2$
- No $K\pi$ system should form a K^* meson thus:
 - $|M(K^\pm\pi^0) - M(K^*)| > 50 \text{ MeV}/c^2$
 - $|M(K_S^0\pi^0) - M(K^*)| > 50 \text{ MeV}/c^2$
- No $\pi^+\pi^-$ pair not resulting from the K_S^0 decay should form a K_S^0 :
 - $|M(\pi^+\pi^-) - M(K_S^0)| > 20 \text{ MeV}/c^2$
- Background from $\psi' \rightarrow \pi^+\pi^- J/\psi$ is suppressed by:
 - $|M(\pi^+\pi^-)_{Rec} - M(J/\psi)| > 30 \text{ MeV}/c^2$



Analysis of $h_c \rightarrow K_S^0 K^\pm \pi^\mp \pi^+ \pi^-$

- $N_\pi = 5, N_K = 1, N_\gamma \geq 2$
- K_S^0 reconstruction:
 - Limit decay length and error determined by secondary vertex fit: $\lambda/\Delta\lambda < 2$
 - $0.487 \text{ MeV}/c^2 \leq M(\pi^+ \pi^-) \leq 0.511 \text{ MeV}/c^2$
- Common vertex ensured by converged vertex fit for all charged particles
- Limit goodness of 6C-Fit: $\chi_{6C}^2 < 40$
- π^0 from ψ' decay should not from other resonances:
 - $|M(\pi^+ \pi^- \pi^0) - M(\eta)| > 20 \text{ MeV}/c^2$
 - $|M(\pi^+ \pi^- \pi^0) - M(\omega)| > 20 \text{ MeV}/c^2$
- No $K\pi$ system should form a K^* meson thus:
 - $|M(K^\pm \pi^0) - M(K^*)| > 50 \text{ MeV}/c^2$
 - $|M(K_S^0 \pi^0) - M(K^*)| > 50 \text{ MeV}/c^2$
- No $\pi^+ \pi^-$ pair not resulting from the K_S^0 decay should form a K_S^0 :
 - $|M(\pi^+ \pi^-) - M(K_S^0)| > 20 \text{ MeV}/c^2$
- Background from $\psi' \rightarrow \pi^+ \pi^- J/\psi$ is suppressed by:
 - $|M(\pi^+ \pi^-)_{Rec} - M(J/\psi)| > 30 \text{ MeV}/c^2$

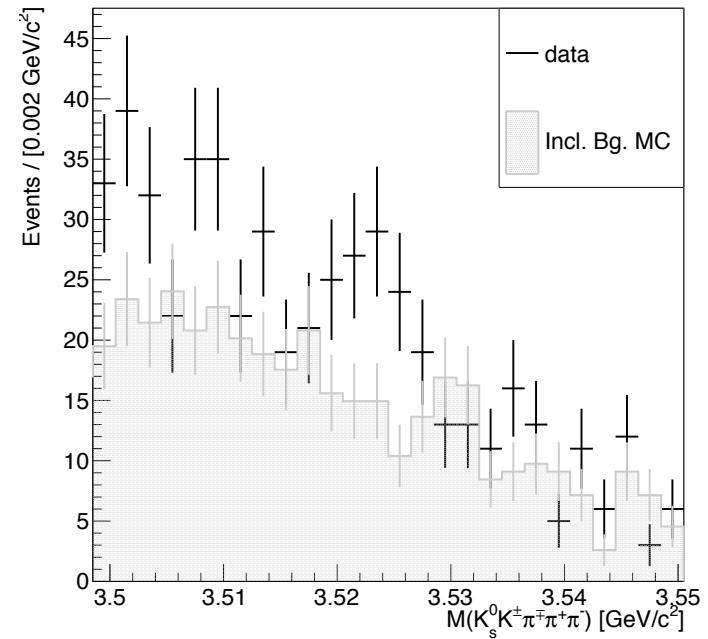


- ➡ obtained efficiency 6.4%
- ➡ structure as expected due to $h_c \rightarrow K^+ K^- \pi^+ \pi^- \pi^0$ channel but smaller yield

Background studies

- Here no peaking background can result from $h_c \rightarrow \gamma \eta_c$ due to misidentification of a π^0
- Main background contributions are:

process	final state	N_{rem}	N_{expected}
$K^{*+} K^{*-} \pi^+ \pi^-$	$K_S^0 K^\pm \pi^\mp \pi^+ \pi^- \pi^0$	114	35 %
$K^{*0} \bar{K}^{*0} \pi^+ \pi^-$	$K_S^0 K^\pm \pi^\mp \pi^+ \pi^- \pi^0$	98	30 %
$K^{*0} K^{*\pm} \pi^\mp \pi^0$	$K_S^0 K^\pm \pi^\mp \pi^+ \pi^- \pi^0$	92	28 %

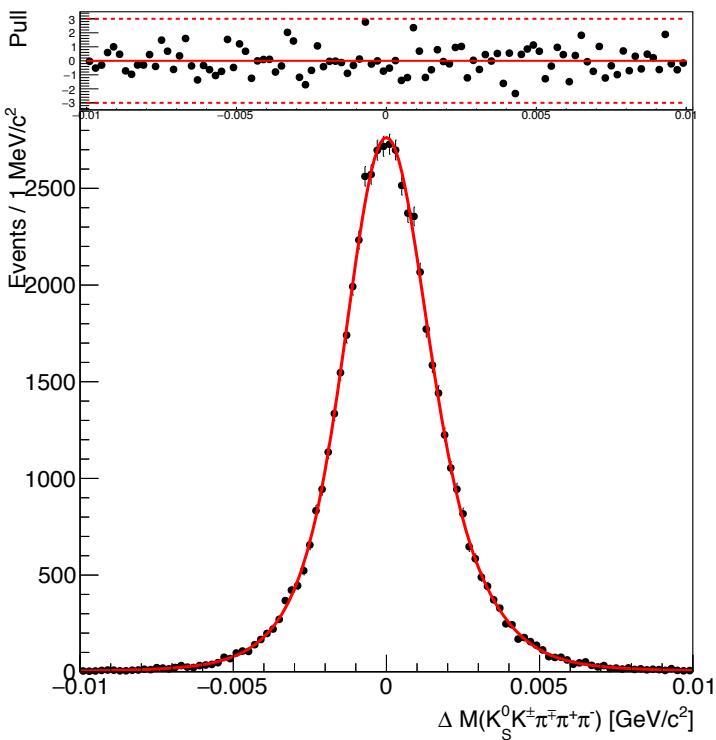


- despite the criterion to reduce K^* resonances, events in which the π^0 meson contributes to a K^* , remain

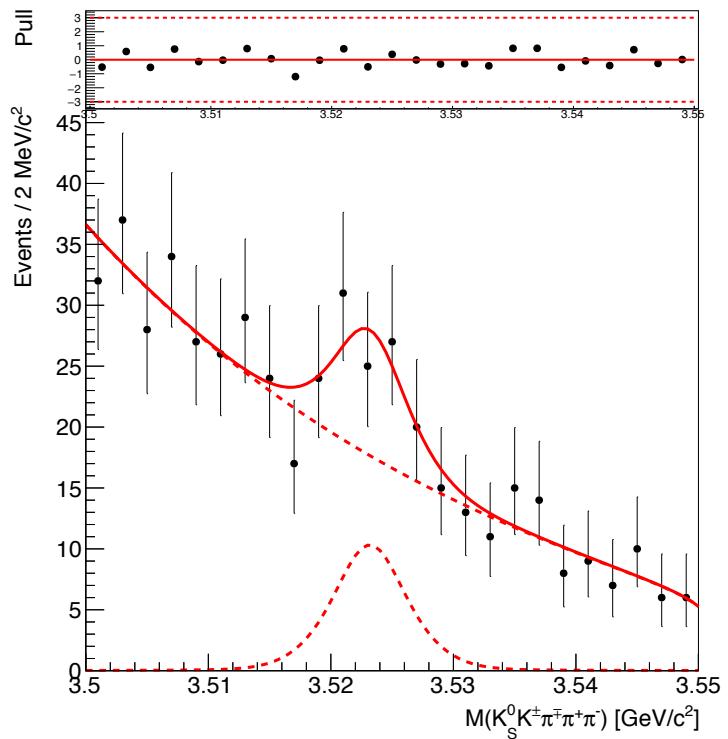
Determination of branching fraction of $h_c \rightarrow K_S^0 K^\pm \pi^\mp \pi^+ \pi^-$

Resolution

$$= \begin{cases} e^{\frac{\sigma_L^2}{2} + \sigma_L \left(\frac{m-\mu}{\sigma} \right)^2}, & \frac{m-\mu}{\sigma} \leq -\sigma_L \\ e^{-\frac{1}{2} \left(\frac{m-\mu}{\sigma} \right)^2}, & -\sigma_L < \frac{m-\mu}{\sigma} \leq \sigma_H \\ e^{\frac{\sigma_H^2}{2} - \sigma_H \left(\frac{m-\mu}{\sigma} \right)^2}, & \sigma_H < \frac{m-\mu}{\sigma} \end{cases} + 2 \text{ Gaussian}$$



Breit-Wigner \otimes Resolution + Argus



$$\text{BF}(h_c \rightarrow K_S^0 K^\pm \pi^\mp \pi^+ \pi^-) = (7.6 \pm 1.7 \pm 0.9 \pm 1.1) \cdot 10^{-3}$$

Significance calculated to 3.2σ

Overview of Selection Criteria

final state	χ^2_{NC}	$M(\pi_1^0 \pi_2^0)_{\text{Rec}}$	J/ ψ Veto on $M(\pi^+ \pi^-)_{\text{Rec}}$	$M(\eta)_{\text{Rec}}$	η	ω	$K^{*\pm}$	K_S^0	π^0 Veto on $M(\gamma\gamma)$
$K^+ K^- \pi^+ \pi^- \pi^0$	✓	✓	✓		✓	✓	✓		
$K_S^0 K^\pm \pi^\mp \pi^+ \pi^-$	✓		✓		✓	✓	✓	✓	
$\pi^+ \pi^- \pi^0 \eta$	✓	✓		✓	✓				✓
$2(K^+ K^-) \pi^0$	✓	✓					✓		
$K^+ K^- \pi^0$	✓	✓					✓		
$K^+ K^- \eta$	✓								✓
$K^+ K^- \pi^0 \eta$	✓	✓		✓					
$K^+ K^- \pi^+ \pi^- \eta$	✓		✓	✓			✓		✓
$K_S^0 K^\pm \pi^\mp$	✓		✓				✓		
					η	Δ^+	Σ^+		
$p\bar{p} \pi^0 \pi^0$	✓	✓			✓	✓	✓		✓

- Limit Goodness of kinematic fit to suppress background
- Veto J/ψ in recoil systems
- π^0 from ψ' decay should not from other resonances
- avoid fake π^0

Overview of Selection Criteria

final state	χ^2_{NC}	J/ ψ Veto on			Veto on			π^0 Veto on	
		$M(\pi_1^0 \pi_2^0)_{\text{Rec}}$	$M(\pi^+ \pi^-)_{\text{Rec}}$	$M(\eta)_{\text{Rec}}$	η	ω	$K^{*\pm}$	K_S^0	$M(\gamma\gamma)$
$K^+ K^- \pi^+ \pi^- \pi^0$	✓	✓	✓		✓	✓	✓		
$K_S^0 K^\pm \pi^\mp \pi^+ \pi^-$	✓		✓		✓	✓	✓	✓	
$\pi^+ \pi^- \pi^0 \eta$	✓	✓		✓	✓				✓
$2(K^+ K^-) \pi^0$	✓	✓					✓		
$K^+ K^- \pi^0$	✓	✓					✓		
$K^+ K^- \eta$	✓								✓
$K^+ K^- \pi^0 \eta$	✓	✓		✓					
$K^+ K^- \pi^+ \pi^- \eta$	✓		✓	✓			✓		✓
$K_S^0 K^\pm \pi^\mp$	✓		✓				✓		
					η	Δ^+	Σ^+		
$p\bar{p} \pi^0 \pi^0$	✓	✓			✓	✓	✓		✓

- Limit Goodness of kinematic fit to suppress background
- Veto J/ψ in recoil systems
- π^0 from ψ' decay should not from other resonances
- avoid fake π^0

Overview of Selection Criteria

final state	χ^2_{NC}	J/ ψ Veto on			Veto on			π^0 Veto on
		$M(\pi_1^0 \pi_2^0)_{\text{Rec}}$	$M(\pi^+ \pi^-)_{\text{Rec}}$	$M(\eta)_{\text{Rec}}$	η	ω	$K^{*\pm}$	K_S^0
$K^+ K^- \pi^+ \pi^- \pi^0$	✓	✓	✓		✓	✓	✓	
$K_S^0 K^\pm \pi^\mp \pi^+ \pi^-$	✓		✓		✓	✓	✓	✓
$\pi^+ \pi^- \pi^0 \eta$	✓	✓		✓	✓			✓
$2(K^+ K^-) \pi^0$	✓	✓					✓	
$K^+ K^- \pi^0$	✓	✓					✓	
$K^+ K^- \eta$	✓							✓
$K^+ K^- \pi^0 \eta$	✓	✓		✓				
$K^+ K^- \pi^+ \pi^- \eta$	✓		✓	✓			✓	✓
$K_S^0 K^\pm \pi^\mp$	✓		✓				✓	
					η	Δ^+	Σ^+	
$p\bar{p} \pi^0 \pi^0$	✓	✓			✓	✓	✓	✓

- Limit Goodness of kinematic fit to suppress background
- Veto J/ψ in recoil systems
- π^0 from ψ' decay should not from other resonances
- avoid fake π^0

Overview of Selection Criteria

final state	χ^2_{NC}	J/ ψ Veto on			Veto on				π^0 Veto on $M(\gamma\gamma)$
		$M(\pi_1^0 \pi_2^0)_{\text{Rec}}$	$M(\pi^+ \pi^-)_{\text{Rec}}$	$M(\eta)_{\text{Rec}}$	η	ω	$K^{*\pm}$	K_S^0	
$K^+ K^- \pi^+ \pi^- \pi^0$	✓	✓	✓		✓	✓	✓		
$K_S^0 K^\pm \pi^\mp \pi^+ \pi^-$	✓		✓		✓	✓	✓	✓	
$\pi^+ \pi^- \pi^0 \eta$	✓	✓		✓	✓				✓
$2(K^+ K^-) \pi^0$	✓	✓					✓		
$K^+ K^- \pi^0$	✓	✓					✓		
$K^+ K^- \eta$	✓								✓
$K^+ K^- \pi^0 \eta$	✓	✓		✓					
$K^+ K^- \pi^+ \pi^- \eta$	✓		✓	✓			✓		✓
$K_S^0 K^\pm \pi^\mp$	✓		✓				✓		
<hr/>									
$p\bar{p} \pi^0 \pi^0$	✓	✓			η	Δ^+	Σ^+		✓
<hr/>									

- Limit Goodness of kinematic fit to suppress background
- Veto J/ψ in recoil systems
- π^0 from ψ' decay should not from other resonances
- avoid fake π^0

Overview of Selection Criteria

final state	χ^2_{NC}	J/ ψ Veto on			Veto on				π^0 Veto on $M(\gamma\gamma)$
		$M(\pi_1^0 \pi_2^0)_{\text{Rec}}$	$M(\pi^+ \pi^-)_{\text{Rec}}$	$M(\eta)_{\text{Rec}}$	η	ω	$K^{*\pm}$	K_S^0	
$K^+ K^- \pi^+ \pi^- \pi^0$	✓	✓	✓		✓	✓	✓		
$K_S^0 K^\pm \pi^\mp \pi^+ \pi^-$	✓		✓		✓	✓	✓	✓	
$\pi^+ \pi^- \pi^0 \eta$	✓	✓		✓	✓				✓
$2(K^+ K^-) \pi^0$	✓	✓					✓		
$K^+ K^- \pi^0$	✓	✓					✓		
$K^+ K^- \eta$	✓								✓
$K^+ K^- \pi^0 \eta$	✓	✓		✓					
$K^+ K^- \pi^+ \pi^- \eta$	✓		✓	✓			✓		✓
$K_S^0 K^\pm \pi^\mp$	✓		✓				✓		
					η	Δ^+	Σ^+		
$p\bar{p} \pi^0 \pi^0$	✓	✓			✓	✓	✓		✓

- Limit Goodness of kinematic fit to suppress background
- Veto J/ψ in recoil systems
- π^0 from ψ' decay should not from other resonances
- avoid fake π^0

Determination of Upper Limits

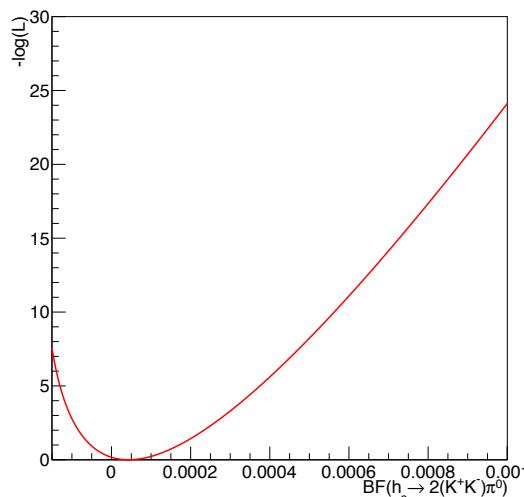
- Using Bayesian method:

$$0.9 = \sum_{\theta_0 \leq \theta_{up}} d\theta_0 \mathbb{P}(\theta = \theta_0 | x) = \frac{\sum_{\theta_0 \leq \theta_{up}} d\theta_0 \mathcal{L}(x|\theta_0) \mathbb{P}(\theta = \theta_0)}{\sum_{\theta' \in \Theta} d\theta' \mathcal{L}(x|\theta') \mathbb{P}(\theta = \theta')}$$

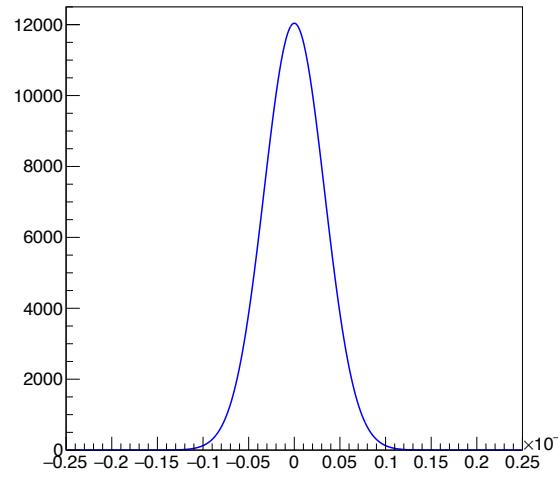
- Taking systematic uncertainties into account by folding the likelihood with a gaussian distribution

Replace $\mathcal{L}(x|\theta)$ by

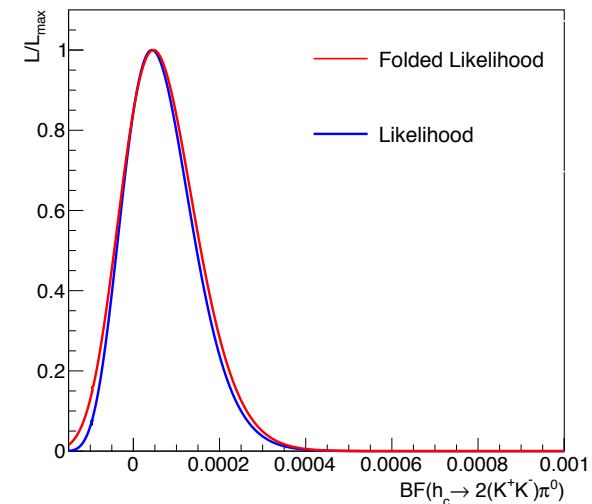
$$\mathcal{L}_{sys}(x|\theta) = \int dx'_i \mathcal{L}(x_1, x_2, \dots, x'_i, \dots, x_k|\theta) \cdot G(x_i - x'_i, \mu_i, \Delta x_i), \quad x_i \text{ fehlerbehaftete Größe mit Fehler } \Delta x_i$$



*

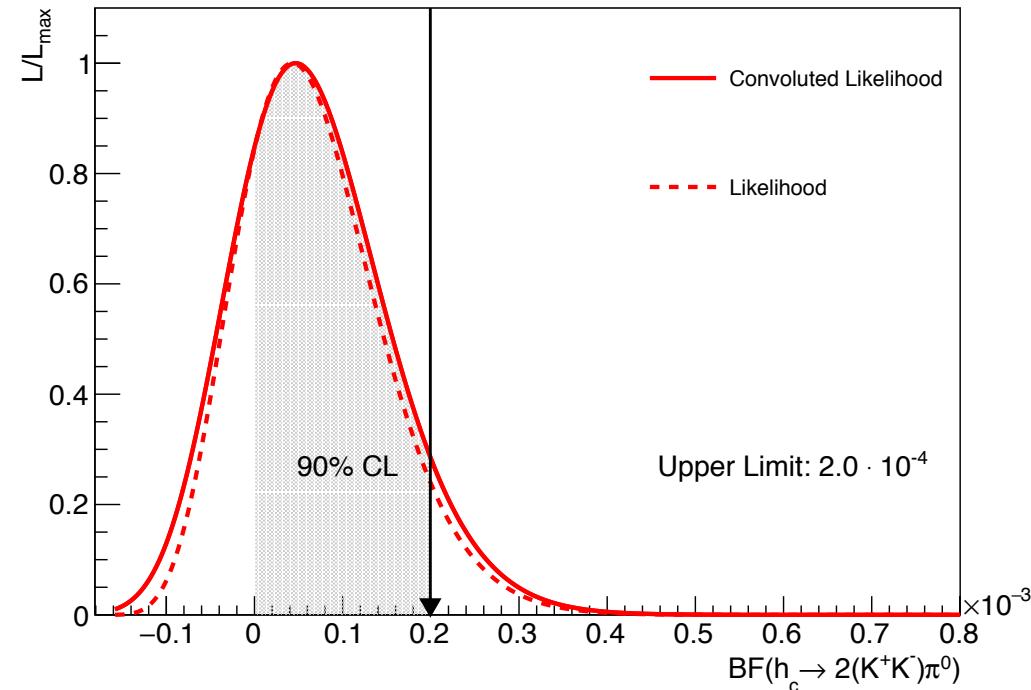
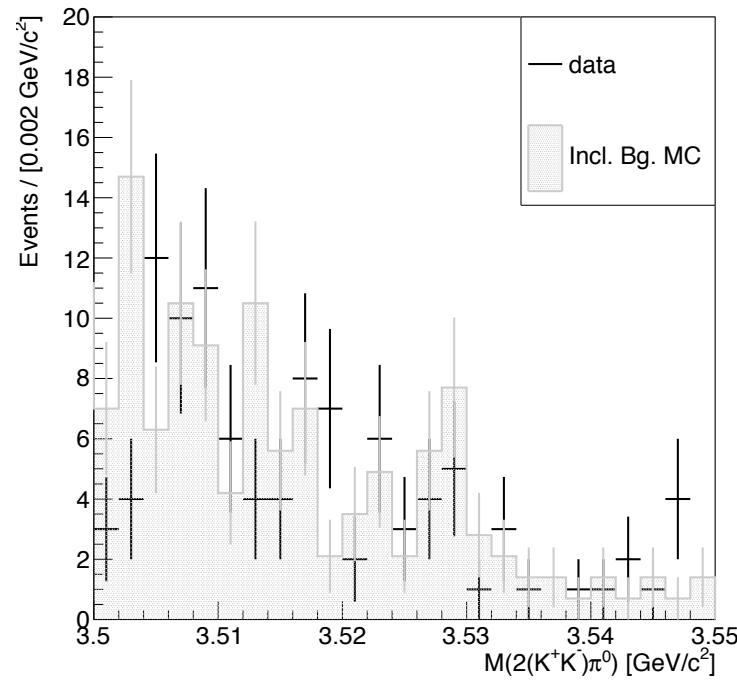


=



At the Example of $h_c \rightarrow 2(K^+K^-)\pi^0$

- After applying all selection criteria, no evidence for a signal contribution is visible!

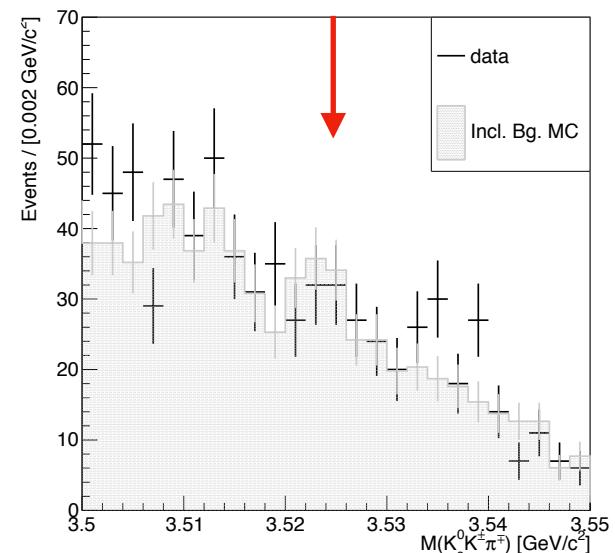
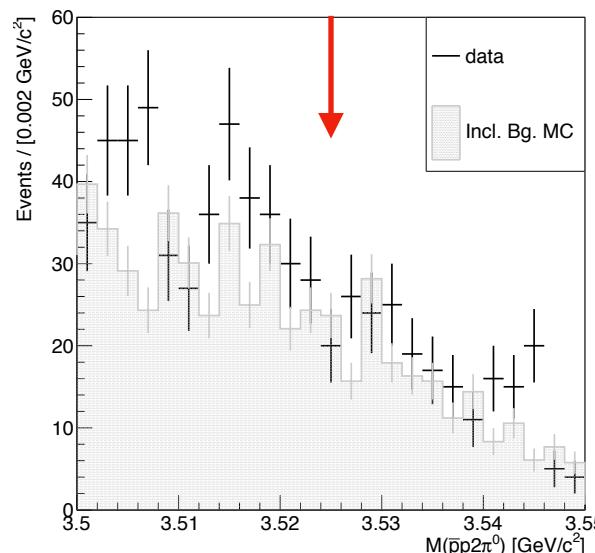
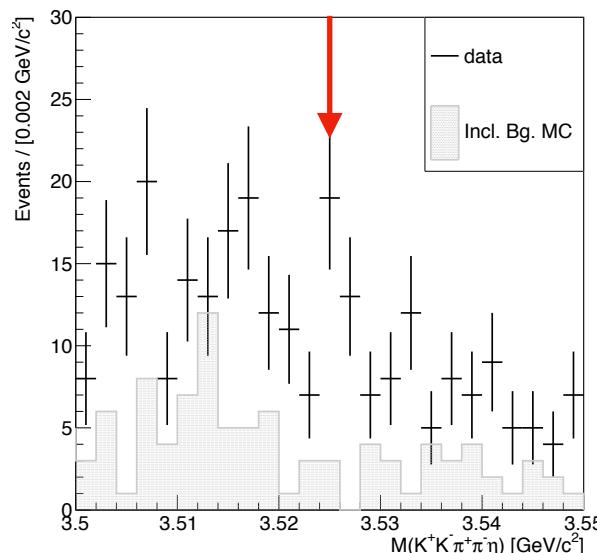
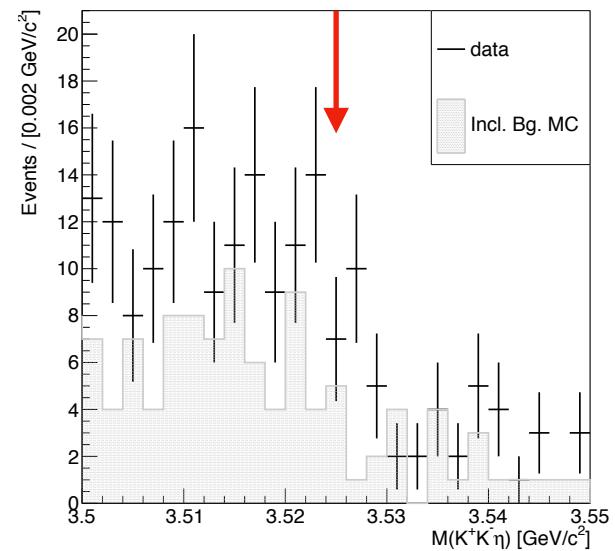
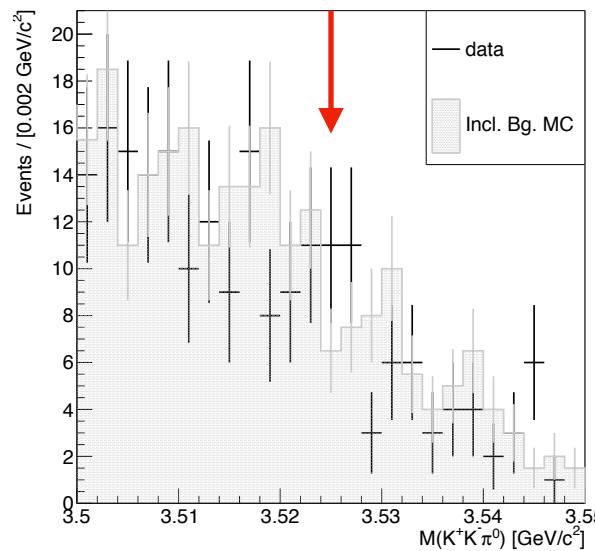
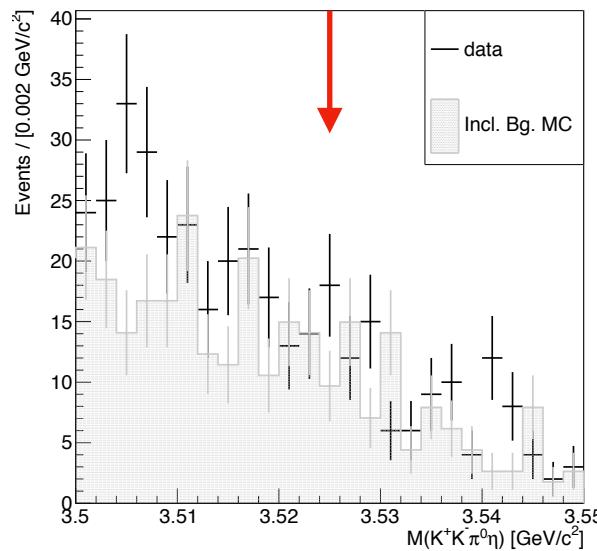


→ determine an upper limit

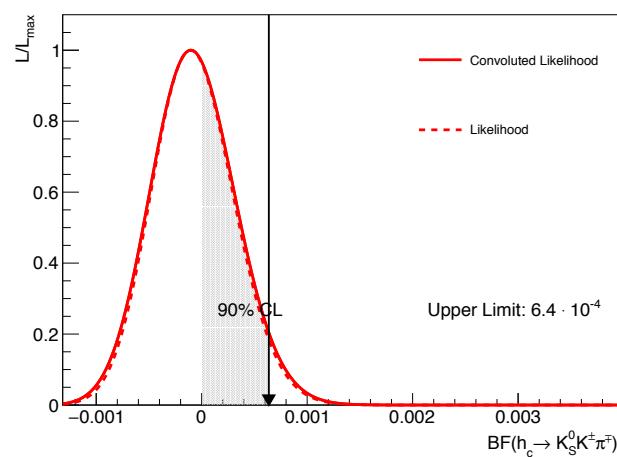
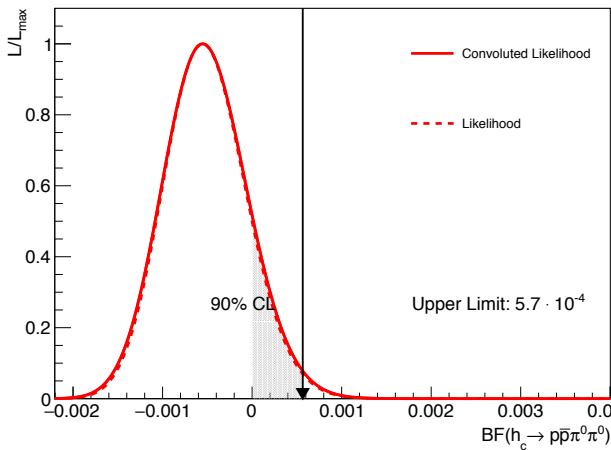
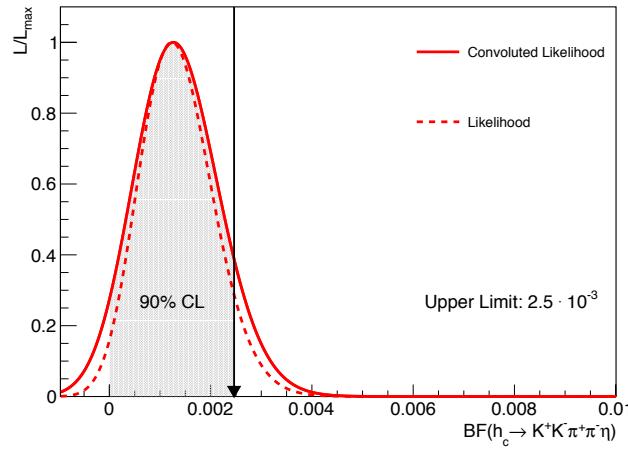
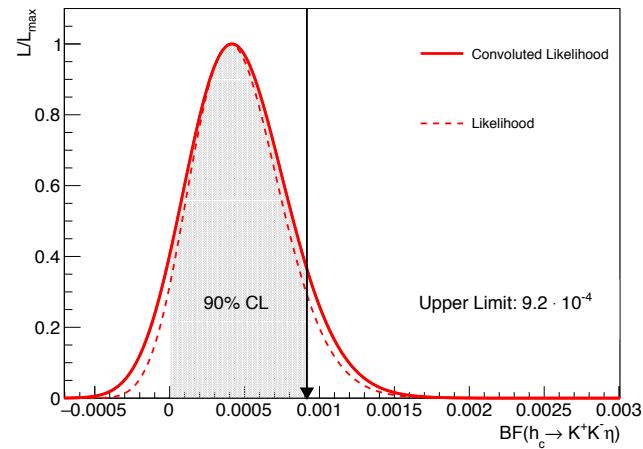
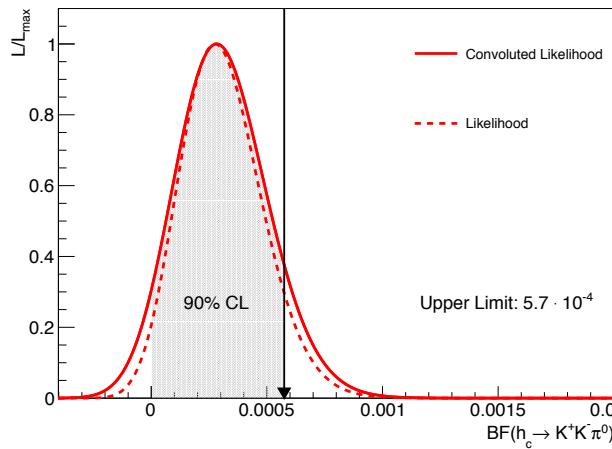
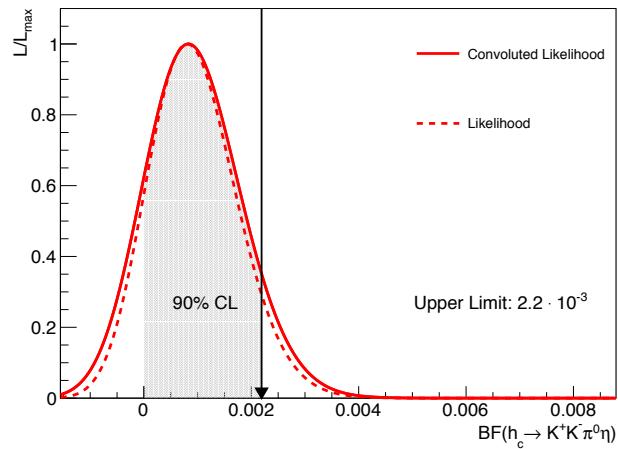
$$BF(h_c \rightarrow 2(K^+K^-)\pi^0) < 2.0 \cdot 10^{-4}$$

- systematic uncertainty of 18.5% taken into account

Same Procedure for other Final States



Same Procedure for other Final States



Summary and Outlook

- In total 10 final states have been analyzed which have never been measured before
- It was possible to find hints for 3 new decay modes of the h_c
- Furthermore indications for contributing intermediate resonances have been found for $h_c \rightarrow K^+K^-\pi^+\pi^-\pi^0$
- For all other final states upper limits have been determined
- Comprehensive systematic studies have been performed for all final states

final state	BF($h_c \rightarrow X$)
$K^+K^-\pi^+\pi^-\pi^0$	$(3.3 \pm 0.4 \pm 0.3 \pm 0.5) \cdot 10^{-3}$
$K_S^0 K^\pm \pi^\mp \pi^+ \pi^-$	$(7.6 \pm 1.7 \pm 0.9 \pm 1.1) \cdot 10^{-3}$
$\pi^+\pi^-\pi^0\eta$	$(7.3 \pm 1.9 \pm 0.8 \pm 1.1) \cdot 10^{-3}$
$2(K^+K^-)\pi^0$	$< 2.0 \cdot 10^{-4}$
$K^+K^-\pi^0$	$< 5.7 \cdot 10^{-4}$
$K^+K^-\eta$	$< 9.2 \cdot 10^{-4}$
$K^+K^-\pi^0\eta$	$< 2.2 \cdot 10^{-3}$
$K^+K^-\pi^+\pi^-\eta$	$< 2.5 \cdot 10^{-3}$
$K_S^0 K^\pm \pi^\mp$	$< 6.4 \cdot 10^{-4}$
$p\bar{p}\pi^0\pi^0$	$< 5.7 \cdot 10^{-4}$

- Looking forward to taking further steps and preparing a Memo!



Thank You!

Overview of Systematic Uncertainties

final state	PID and reconstruction	Selektion	kinematic fit	efficiency	fit	BF	$\sqrt{\sum \Delta_i^2}$
$K^+K^-\pi^+\pi^-\pi^0$	7.2	5.7	1.5	5.1	1.5	15.1	18.5
$\pi^+\pi^-\pi^0\eta$	7.3	5.4	2.1	6.3	2.3	15.1	19
$2(K^+K^-)\pi^0$	7.2	4.7	2.3	5.2	3	15.1	18.5
$K^+K^-\pi^0$	5.3	4.2	1.9	4.1	3.3	15.1	17.5
$K^+K^-\eta$	5.3	3.5	1.9	3.7	3.1	15.1	17.2
$K^+K^-\pi^0\eta$	7.3	3.9	2	4.5	3.5	15.1	18.2
$K^+K^-\pi^+\pi^-\eta$	7.2	5	1.6	3.4	4.2	15.1	18.3
$K_S^0 K^\pm \pi^\mp$	6.4	4.4	2.1	4	2.8	15.1	17.8
$K_S^0 K^\pm \pi^\mp \pi^+\pi^-$	9	4.5	3.9	5.3	3.5	15.1	19.6
$p\bar{p}\pi^0\pi^0$	7.3	6.1	2.7	4.9	3	15.1	18.9