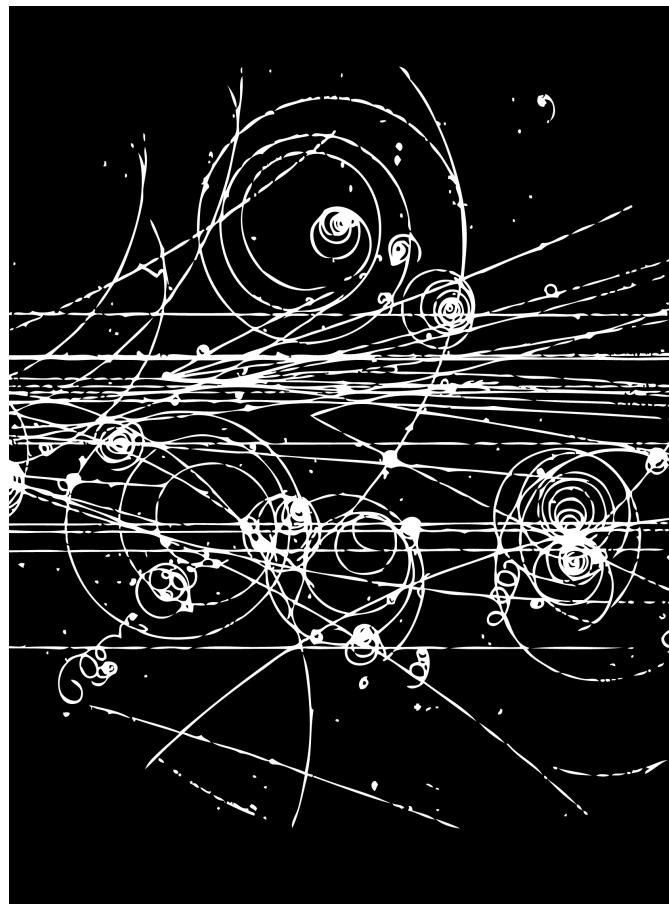


Hadron Spectroscopy



Stephen Lars Olsen

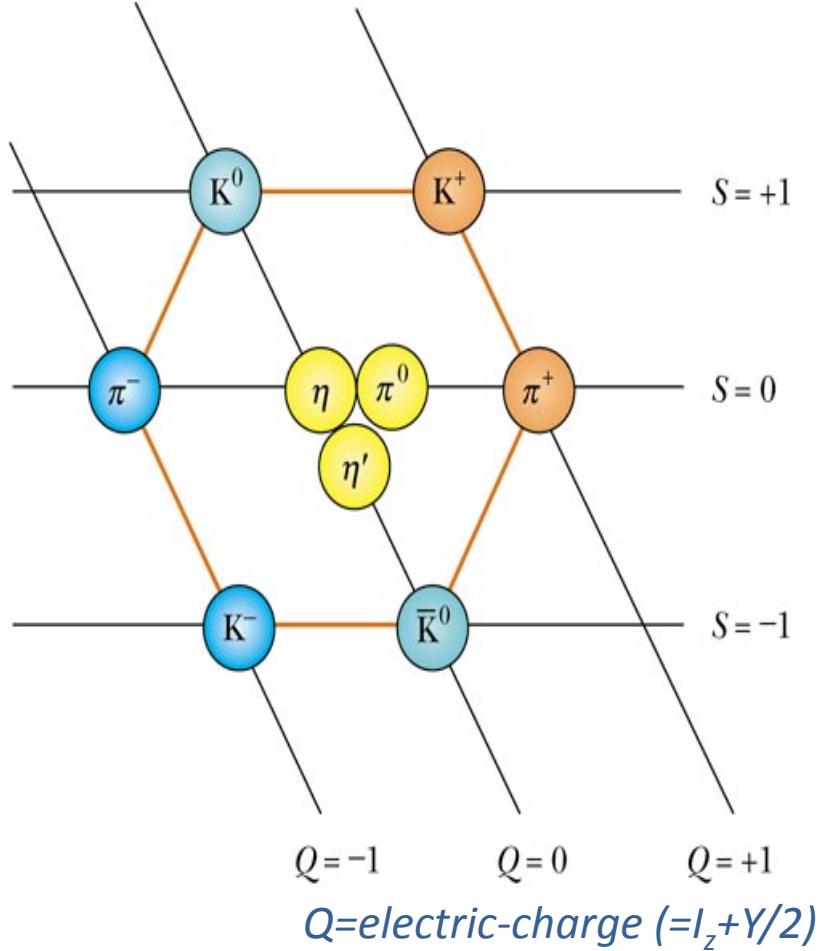
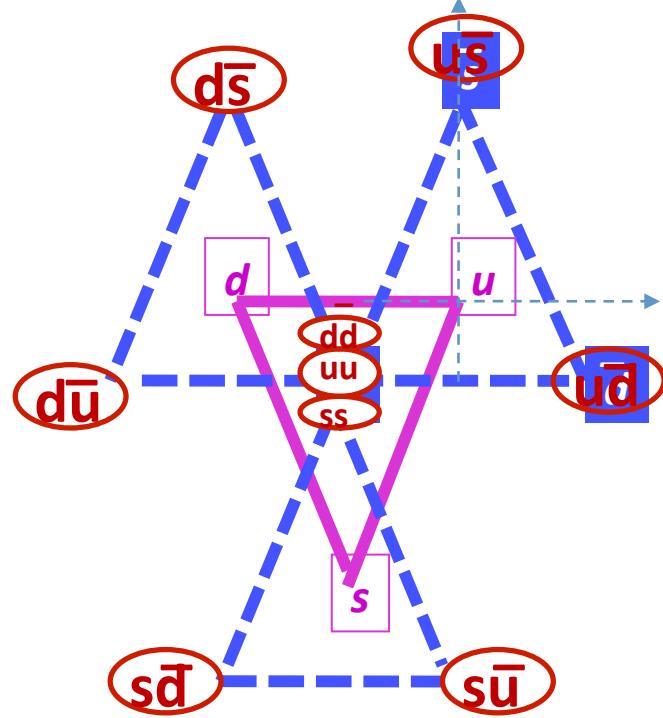
Institute for Basic Science (KOREA)

University of the Chinese Academy of Science

UCAS Physics-department, June 20 – July 6, 2014

Lecture 3: Successes and failures of the quark model.

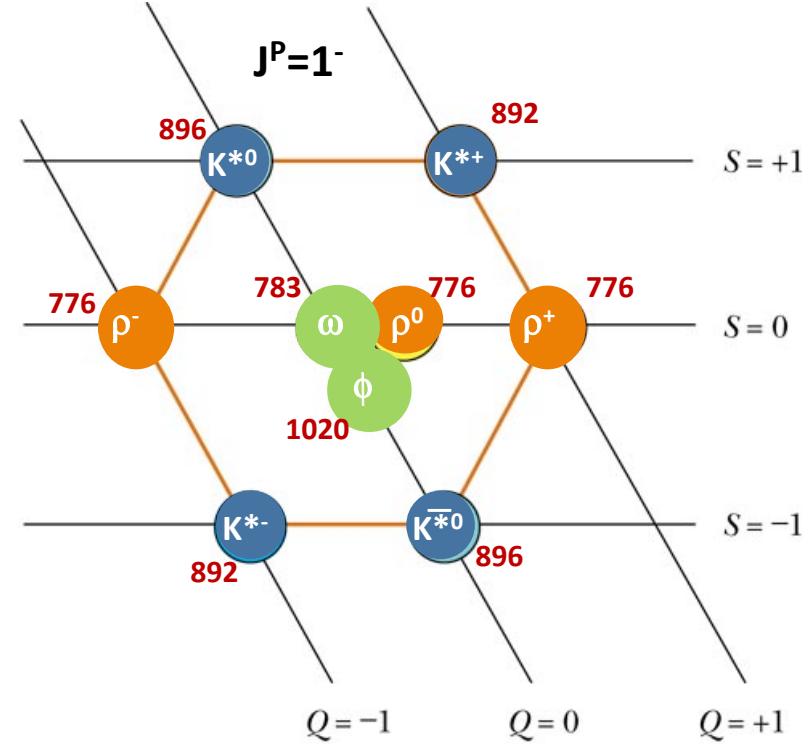
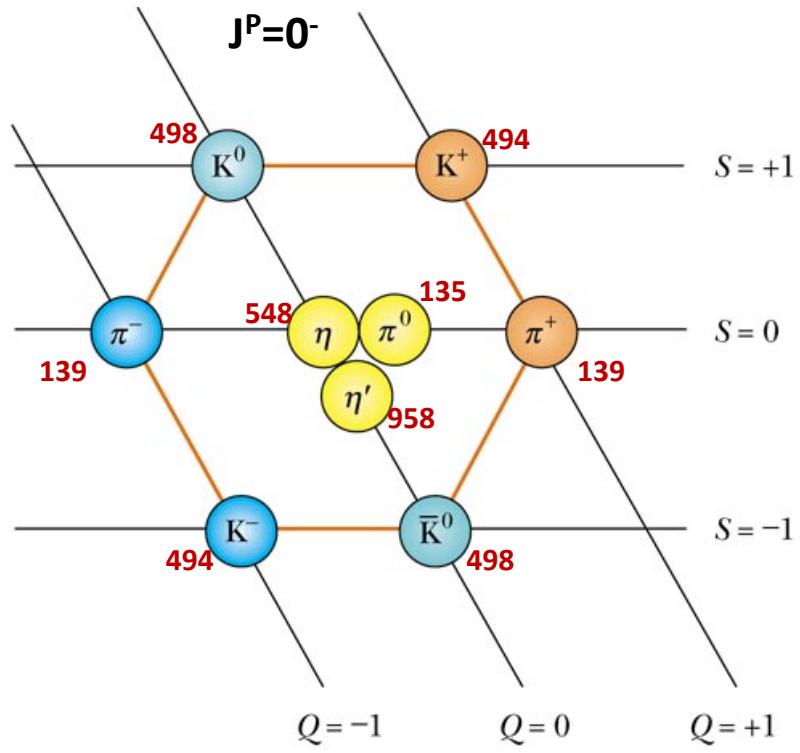
Make mesons from quark-antiquark



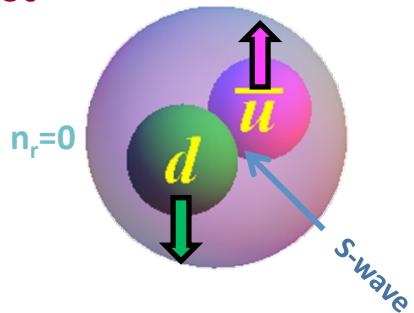
9 states: $3 \otimes \bar{3} = 1 \oplus 8$

$SU(3)$ singlet
+ $SU(3)$ octet

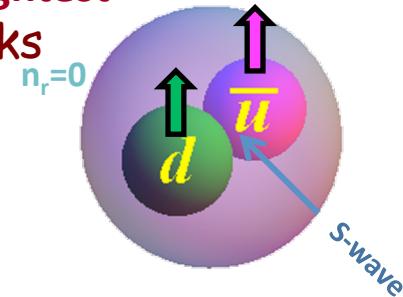
Ground state mesons



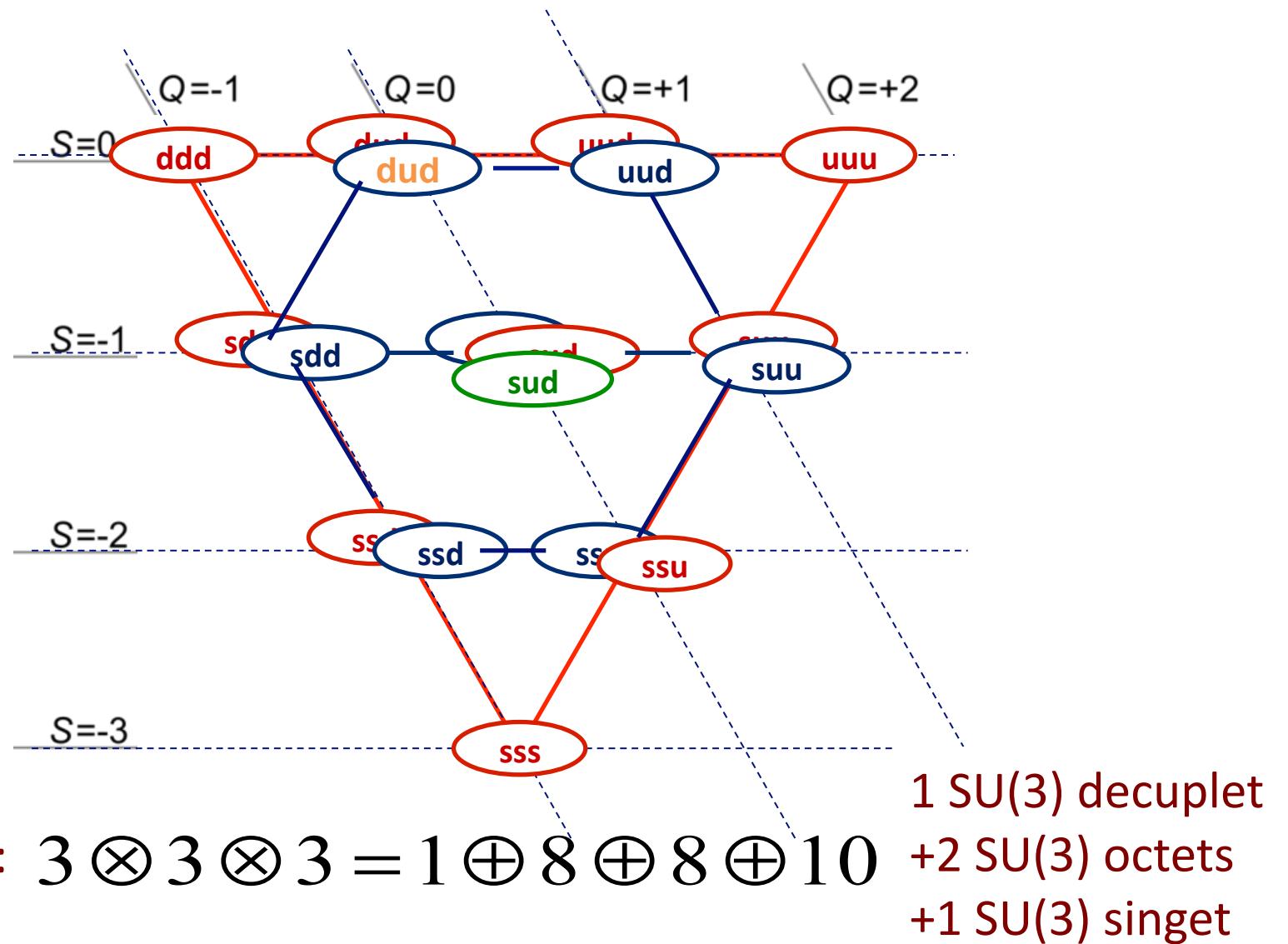
(π^+, π^0, π^-) =lightest
no s-quarks



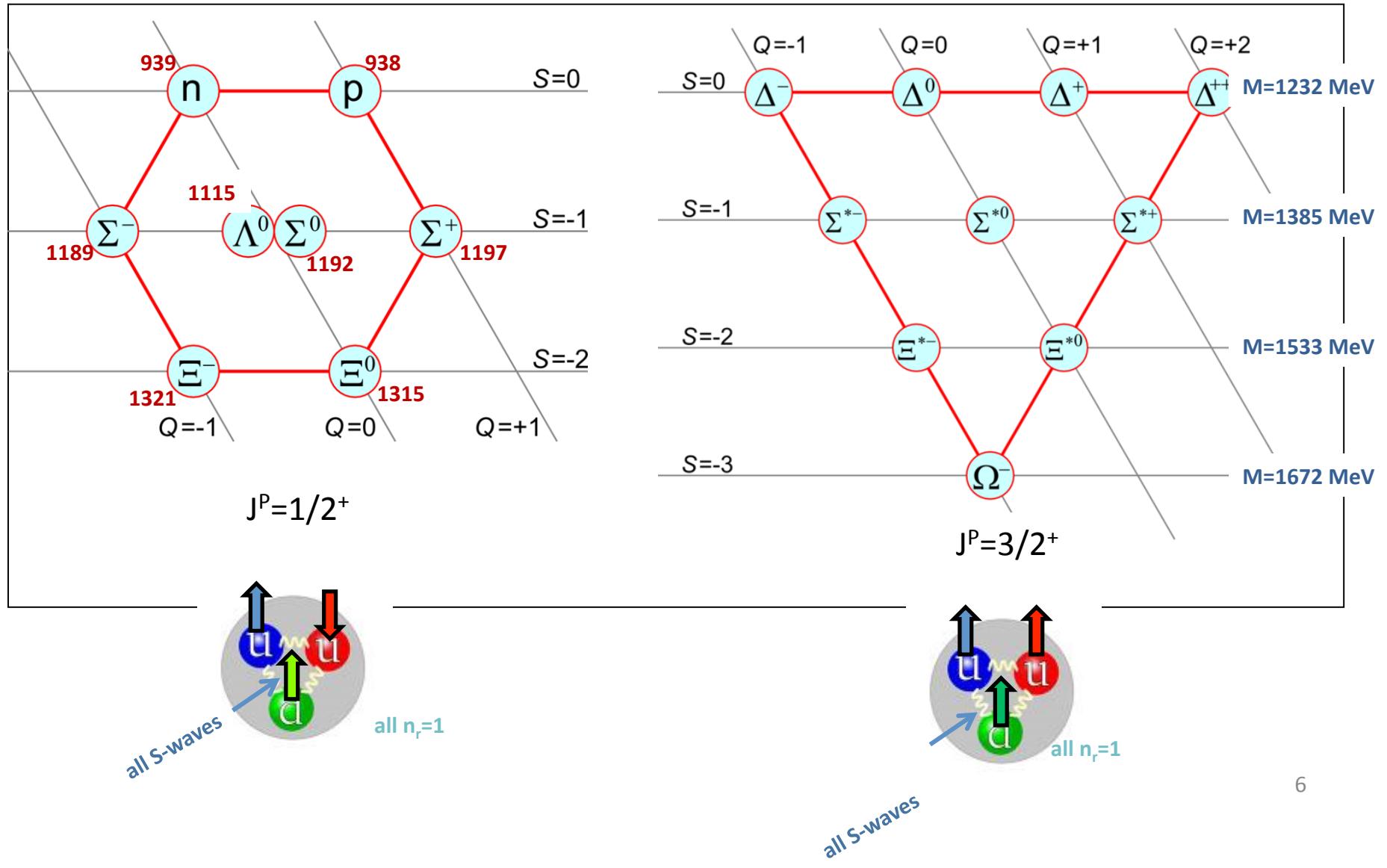
(ρ^+, ρ^0, ρ^-) =lightest
no s-quarks



Baryons = qqq

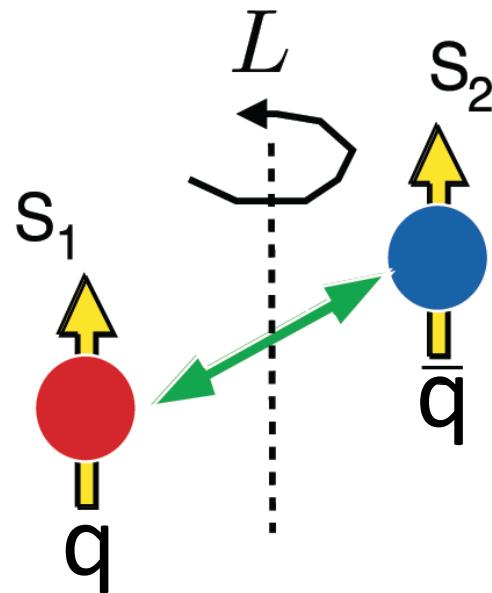


Ground state Baryons

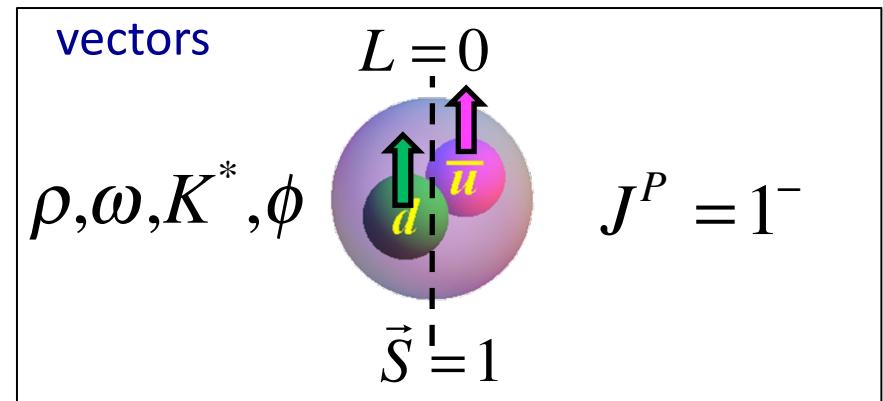
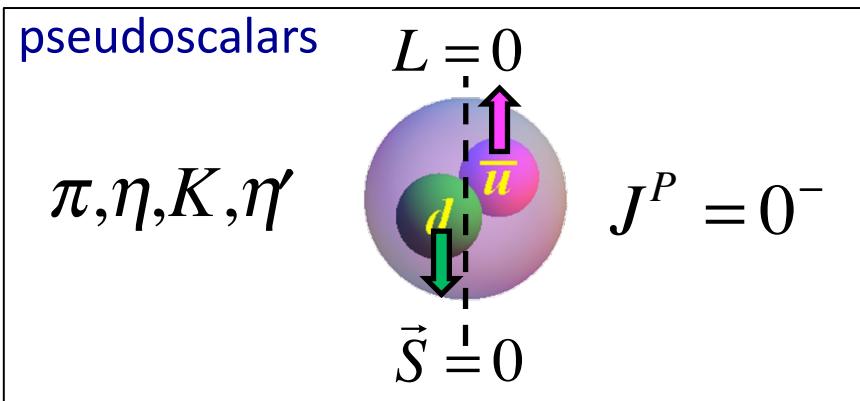


How about excited mesons & baryons?

J^{PC} quantum numbers of $q\bar{q}$ mesons



$\vec{S} = \vec{S}_1 + \vec{S}_2$
 $\vec{J} = \vec{L} + \vec{S}$
 $P = (-1)^{L+1}$
 $C = (-1)^{L+S}$ ← if q & \bar{q} are the same flavor
 +radial excitations



What about P-wave mesons?

$$L = 1$$

$$S = 0, 1$$

$$P = (-1)^{L+1} = +1$$

$$\vec{J} = \vec{L} + \vec{S}$$

$$S=1$$

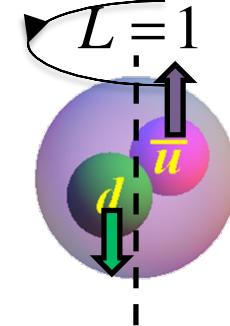
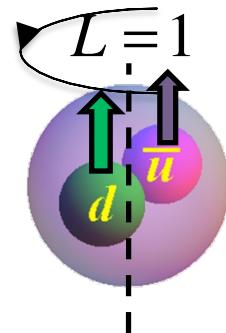
$$\begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \end{array} \begin{array}{c} J=2 \\ J=1 \\ J=0 \end{array}$$

triplet

$$S=0$$

$$\text{---} \quad J=1$$

singlet



COMPASS Experiment at CERN

Two-stage spectrometer at CERNs Prévessin area

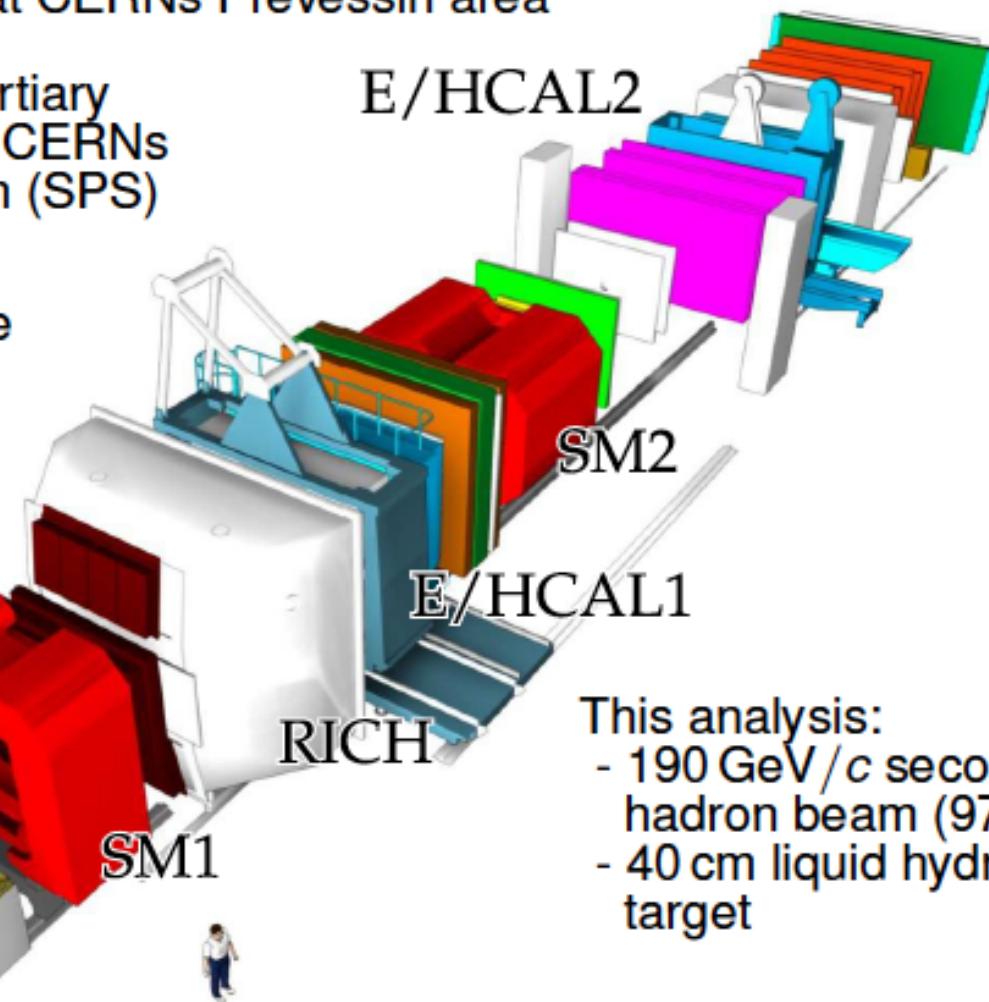
Secondary hadron and tertiary
muon beams supplied by CERNs
Super Proton Synchrotron (SPS)

Good acceptance
over wide kinematic range

Broad physics program
- Spin-structure
- Spectroscopy

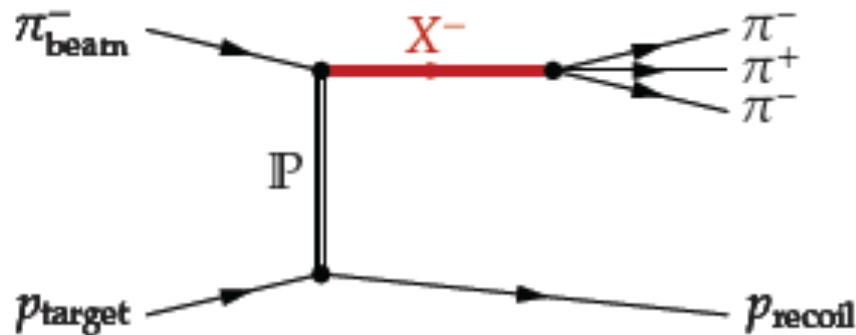
RPD + Target

Beam

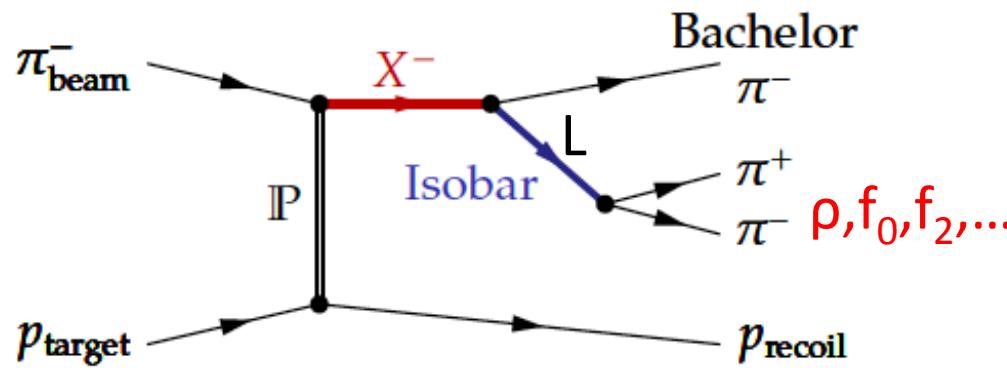


This analysis:
- 190 GeV/c secondary
hadron beam (97% π^-)
- 40 cm liquid hydrogen
target

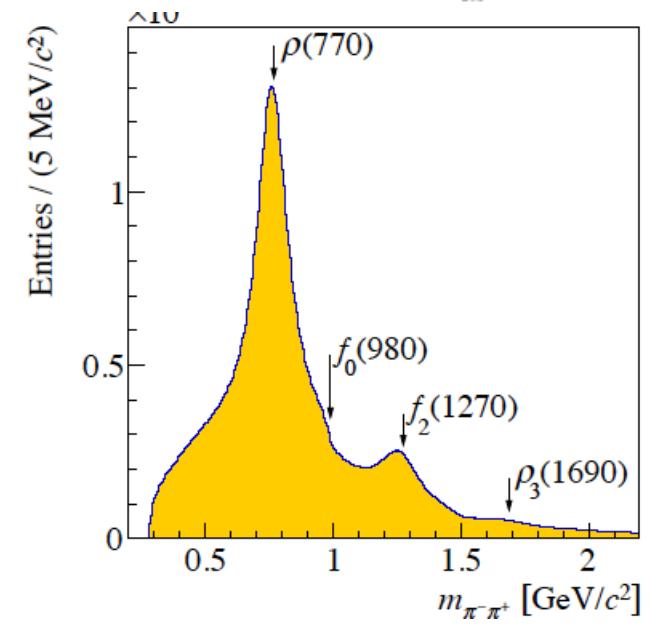
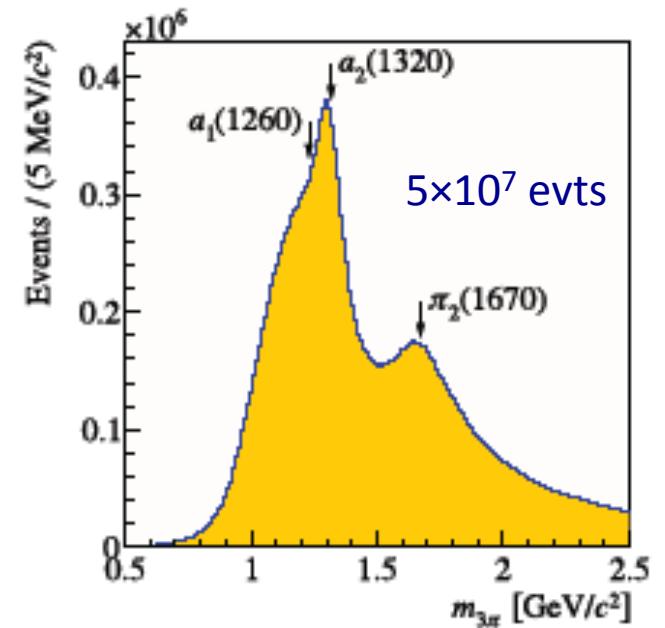
P-wave mesons via $\pi^- p \rightarrow \pi^+ \pi^- \pi^- p$



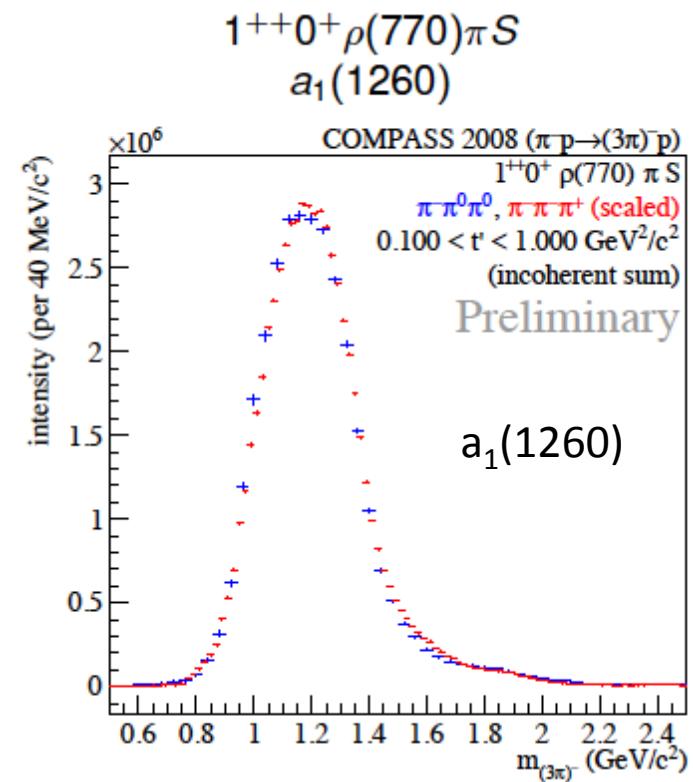
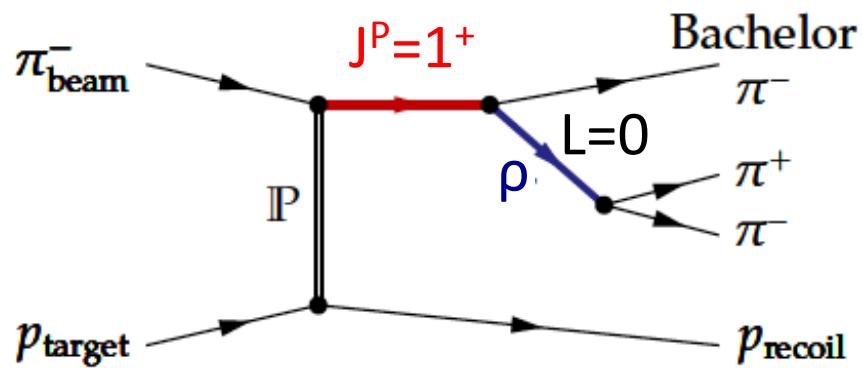
Mostly 2-body process



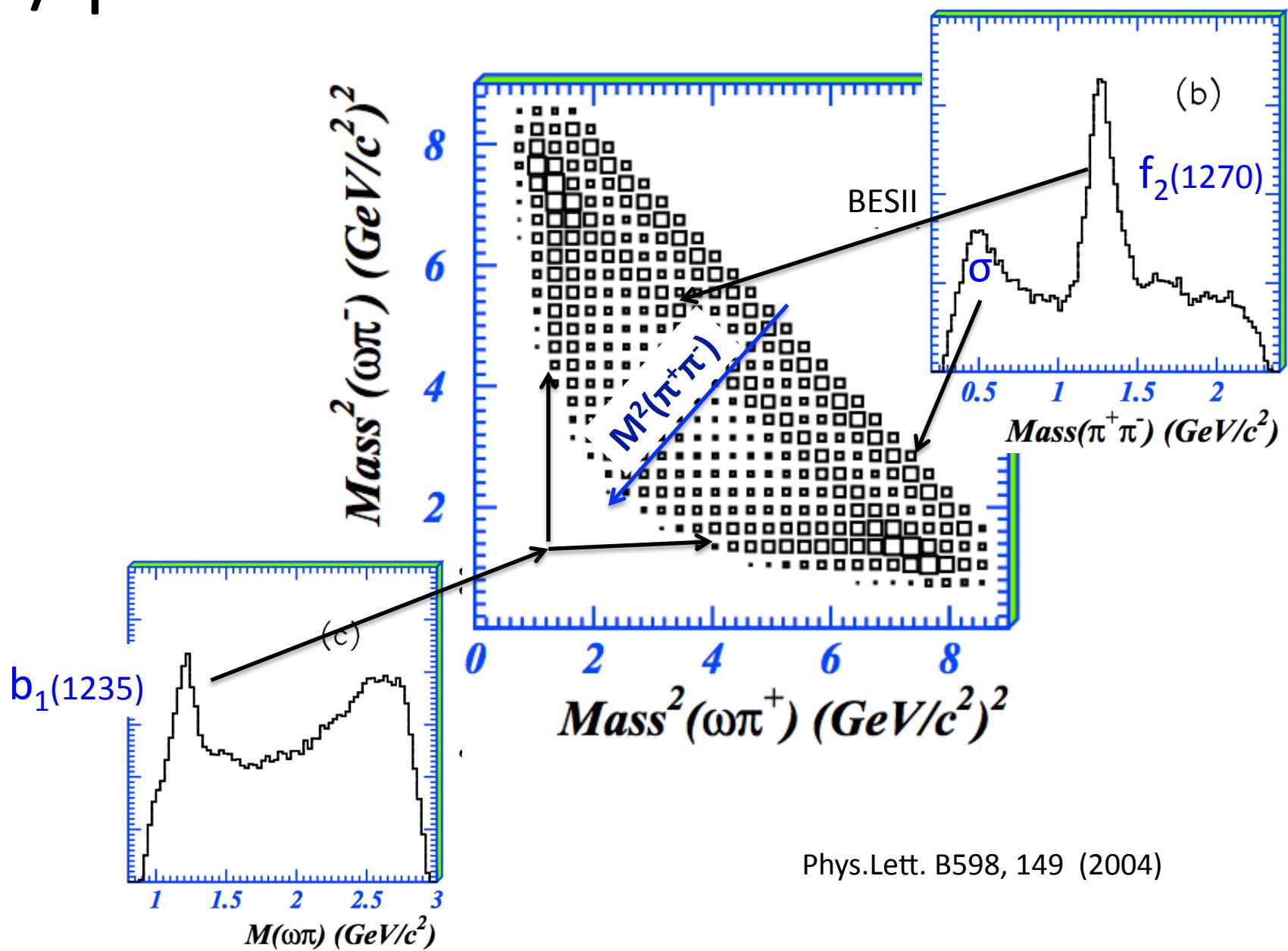
Phys. Rev. Lett. 115, 082001 (2015)



The $J^P=1^+$ $a_1(1260) \rightarrow \pi^- \rho^0$ meson

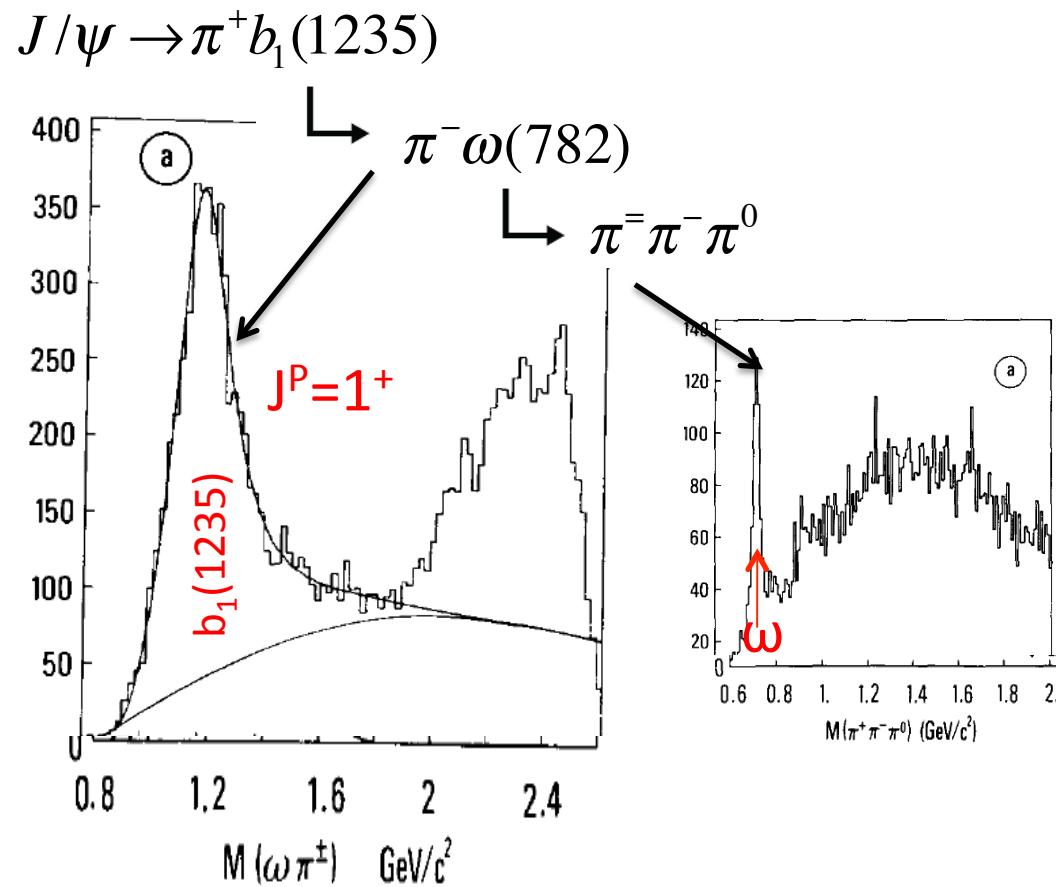


$J/\psi \rightarrow \pi^+\pi^-\omega$ from BESII



Phys.Lett. B598, 149 (2004)

The $J^P=1^+$ $b_1(1235) \rightarrow \pi^- \omega$ meson



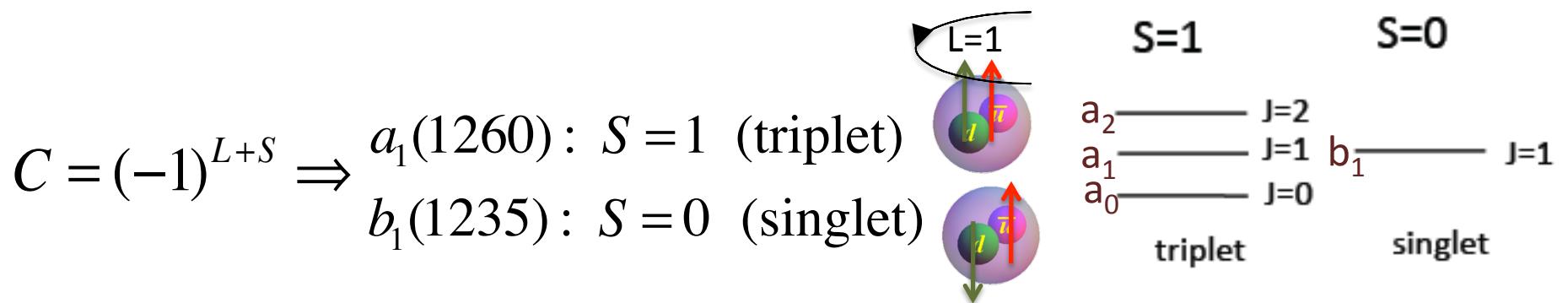
Difference between $a_1(1260)$ & $b_1(1235)$

both have $J^P=1^+$; both have Ispin=1

$$\begin{aligned} a_1(1260) \rightarrow \pi\rho \rightarrow 3\pi &\Rightarrow G(n\pi) = (-1)^n \Rightarrow G(a_1(1260)) = (-1)^3 = -1 \\ b_1(1235) \rightarrow \pi\omega \rightarrow 4\pi &\qquad\qquad\qquad G(b_1(1235)) = (-1)^4 = +1 \end{aligned}$$

C-parity of $I_3=0$
neutral meson

$$G(X) = C_{X^0} e^{i\pi I_2} \stackrel{=-1 \text{ for } l=1}{\Rightarrow} \begin{aligned} C(a_1(1260)^0) &= +1 \\ C(b_1(1235)^0) &= -1 \end{aligned}$$



Other 1^+ mesons from BESII

$f_1(1285)$ and $\eta(1420)$

$|l=0; J^P=1^+$ $|l=0; J^P=0^-$

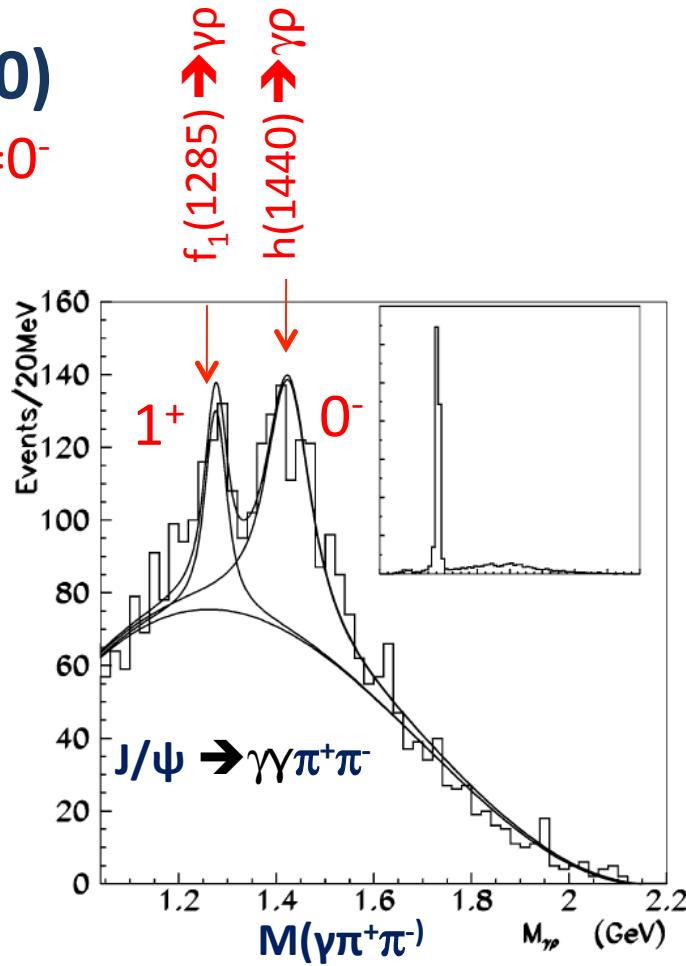
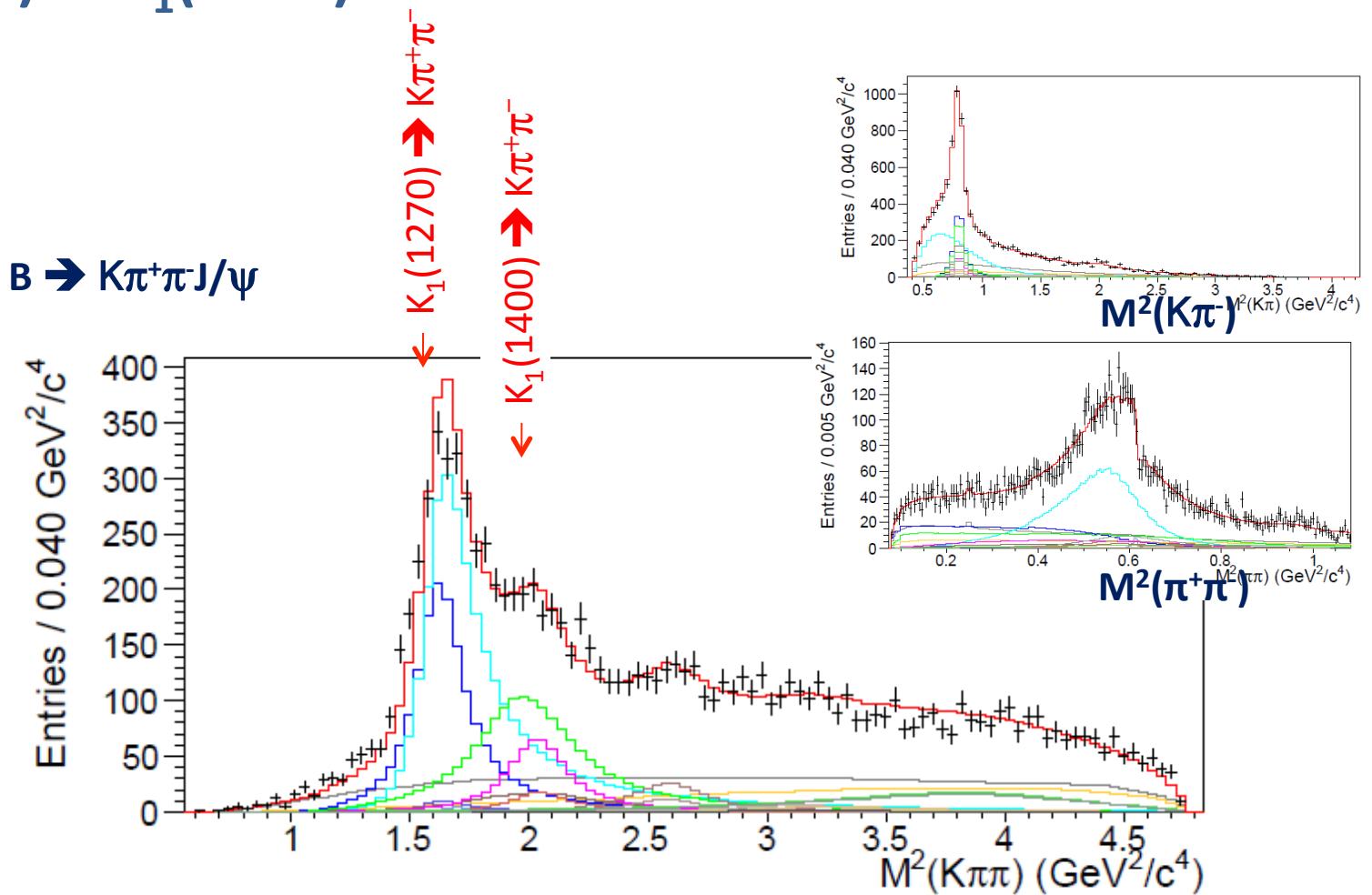


Fig. 2. The $\gamma\rho$ invariant mass distribution. The insert shows the full mass scale where the $\eta(958)$ is clearly observed.

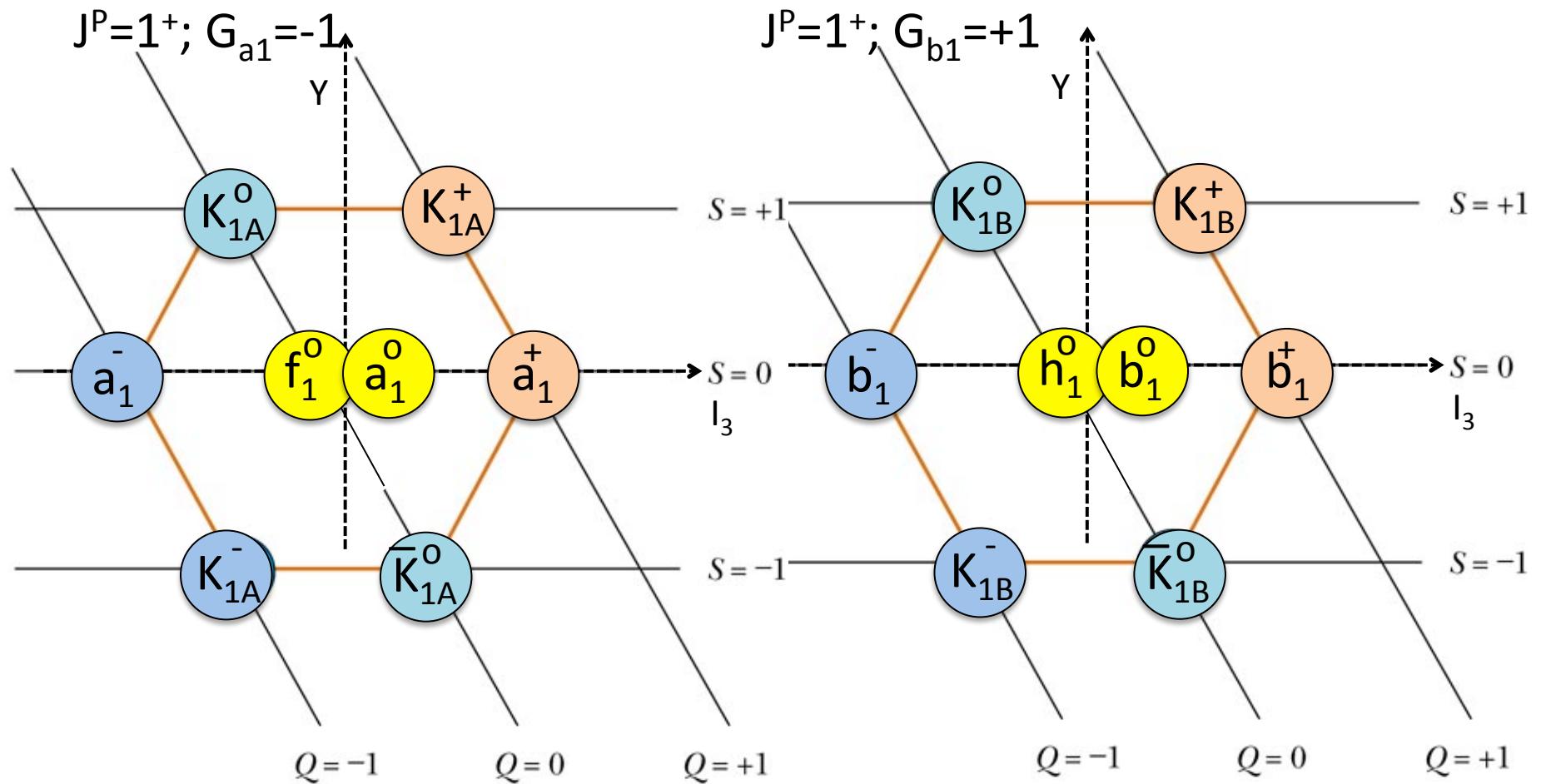
1^+ mesons with $|S|=1$

The $K_1(1270)$ & $K_1(1400)$



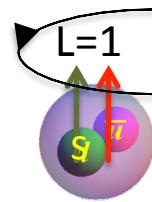
H. Guler et al. (Belle) PRD 83, 032005 (2011)

Axial Vector ($J^P=1^+$) octets

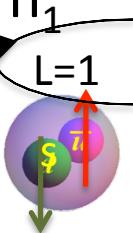


What are the K_{1A} and K_{1B} mesons?

The K_{1A} mesons are the $|S|=1$ octet partners of the a_1 & f_1



The K_{1B} mesons are the $|S|=1$ octet partners of the b_1 & h_1



→ C- and G-parity do not apply to strange mesons

→ only SU(3) quantum numbers distinguish
 K_{1A} from K_{1B} , but SU(3) is badly broken

→ K_{1A} and K_{1B} mix

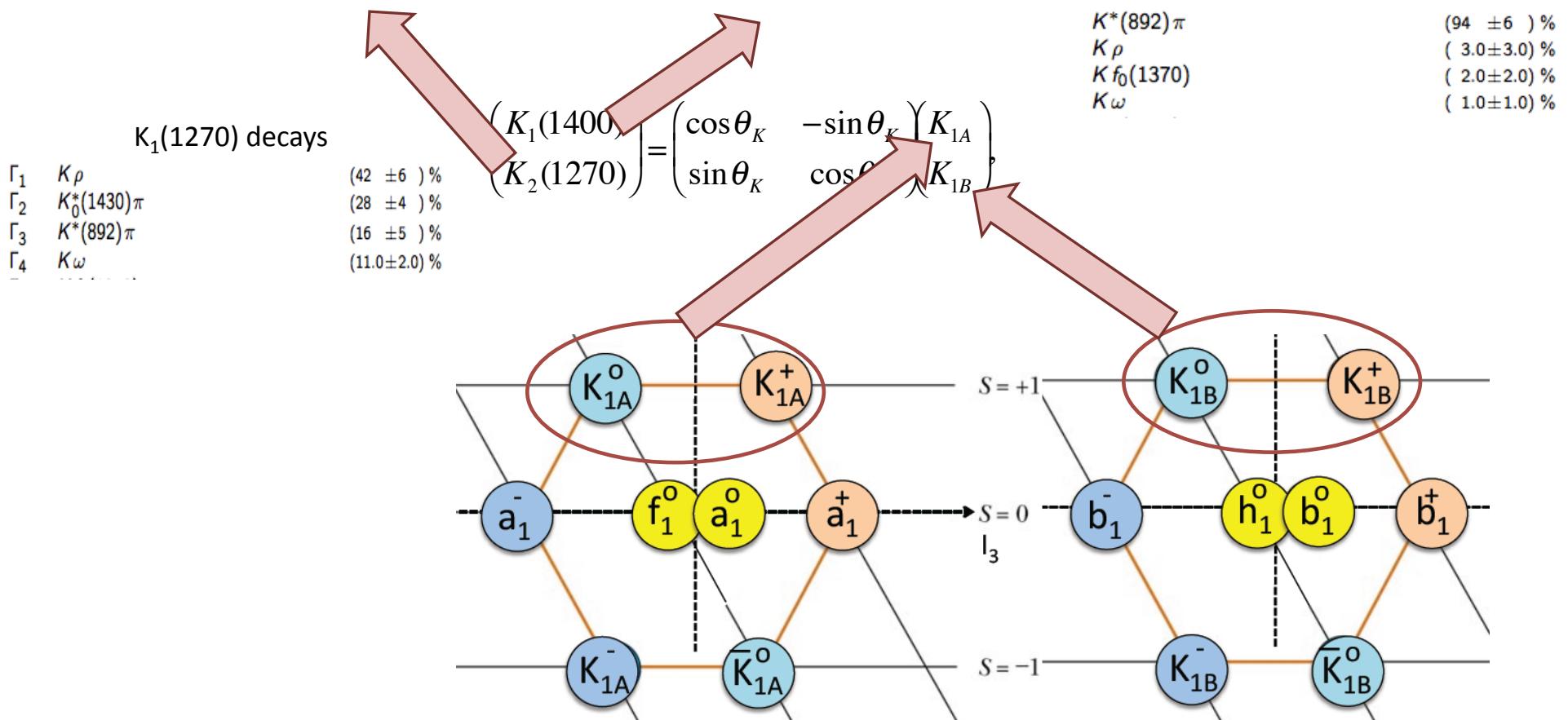
$$\begin{pmatrix} K_1(1400) \\ K_2(1270) \end{pmatrix} = \begin{pmatrix} \cos\theta_K & -\sin\theta_K \\ \sin\theta_K & \cos\theta_K \end{pmatrix} \begin{pmatrix} K_{1A} \\ K_{1B} \end{pmatrix},$$

some model-dependent analysis of K_{1A} & K_{1B} masses and decay widths estimate the "strange axial-vector mixing angle, θ_K , to be:

see, e.g., Eur. Phys. J A28,369 (2006)

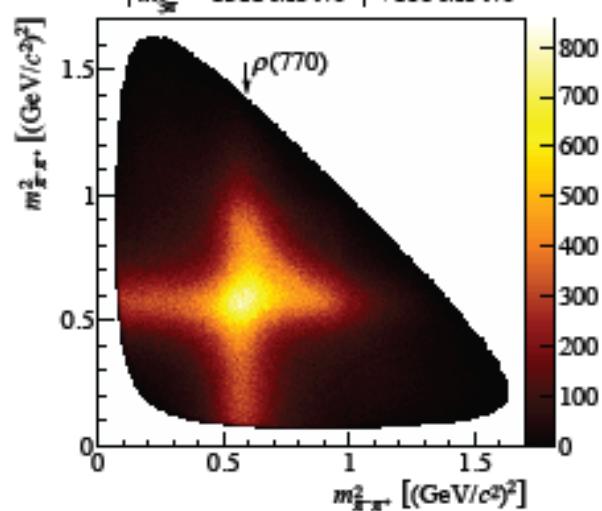
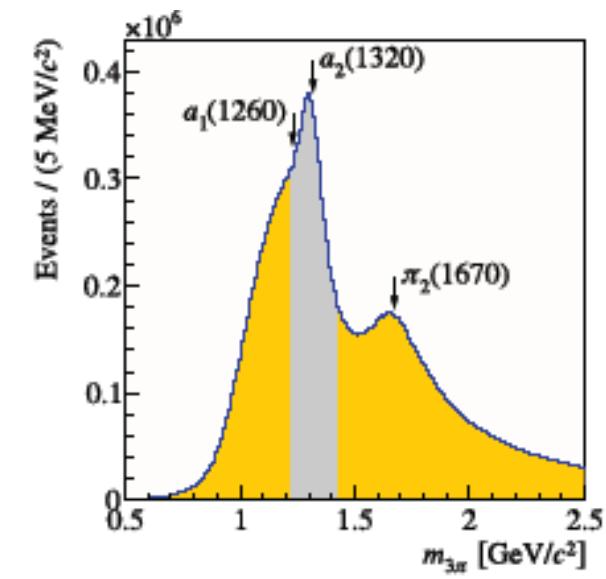
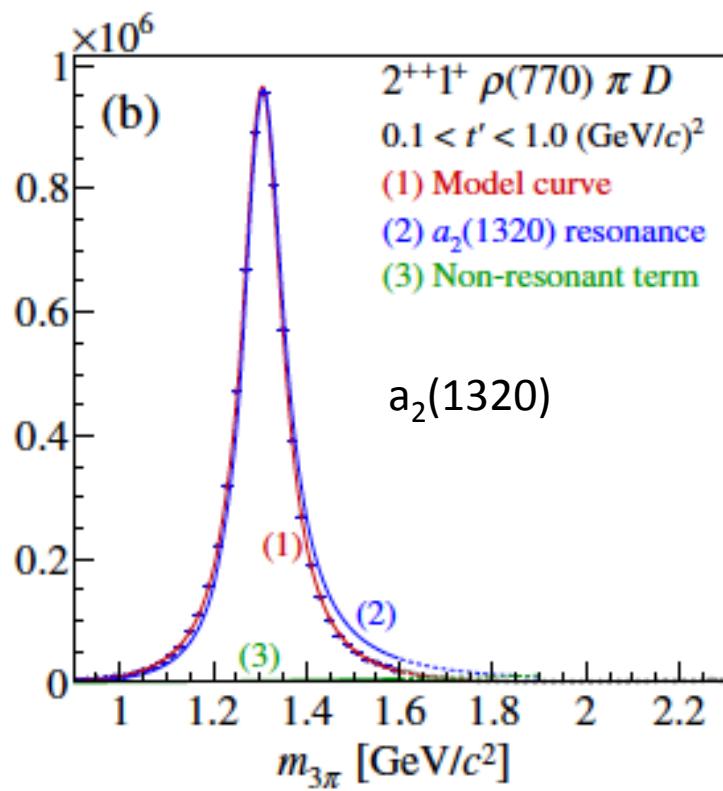
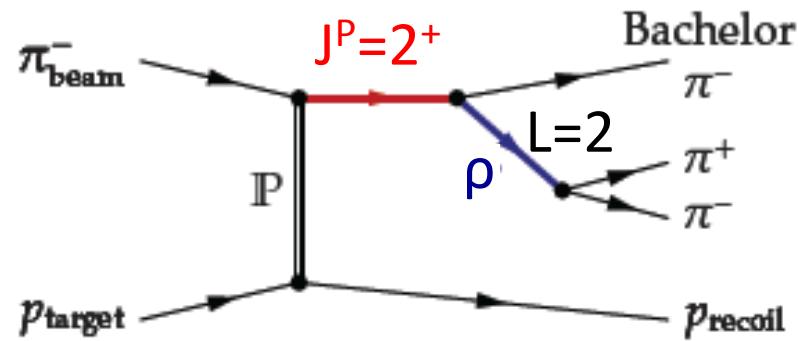
$\theta_K \approx 60^\circ$

$K_1(1270)$ and $K_1(1400)$

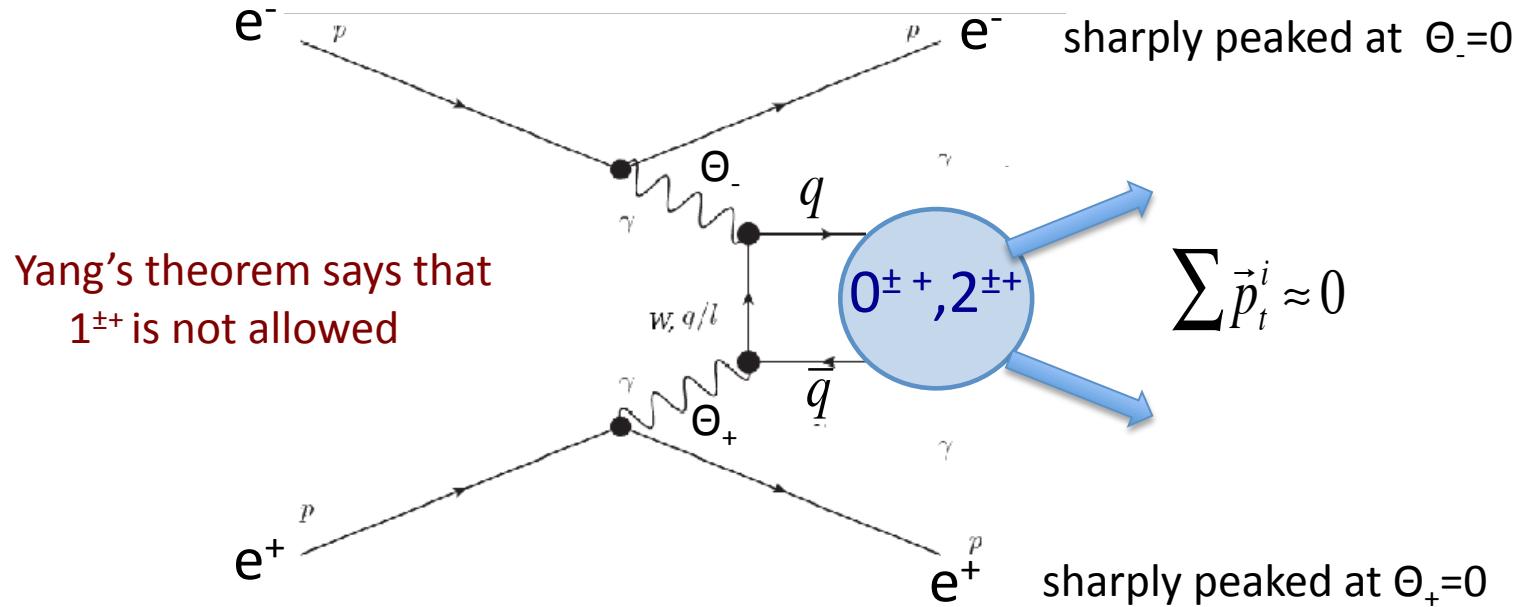


the J=0 and J=2 SU(3) partners of the
 $a_1(1270)$ octet

The $J^P=2^+$ $a_2(1320) \rightarrow \pi^- \rho^0$ meson



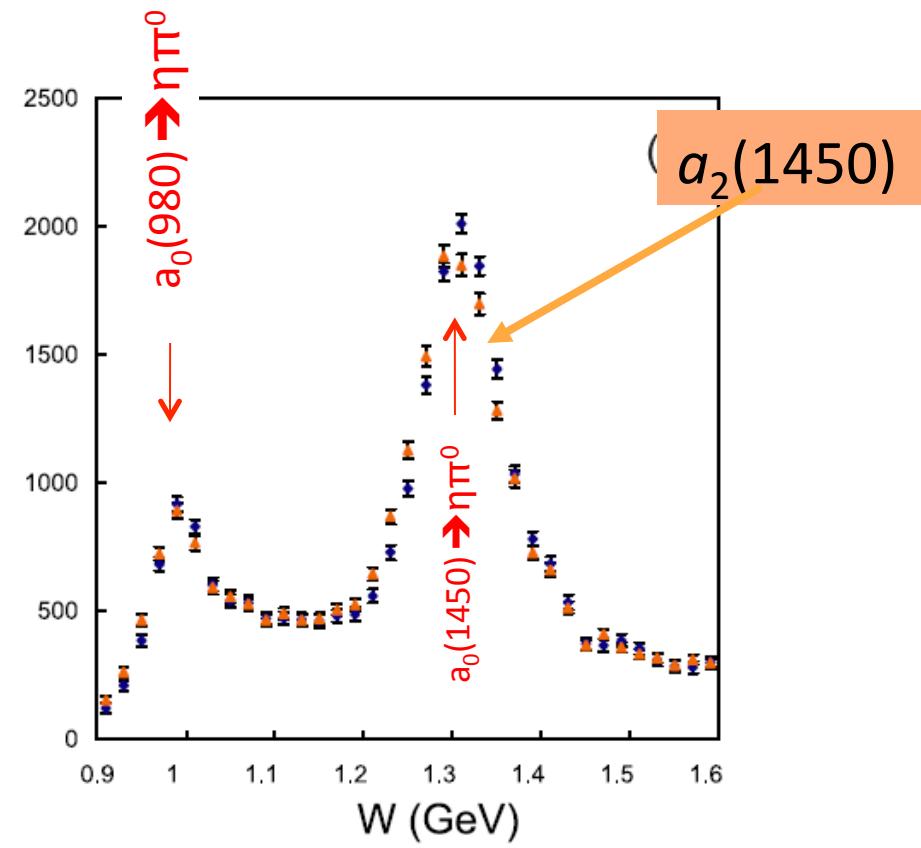
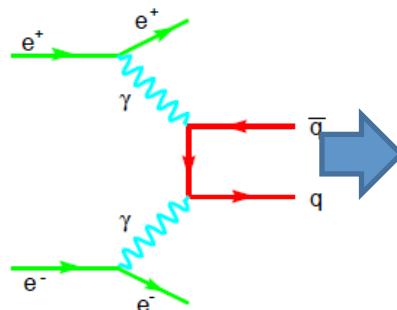
two-photon reactions



For almost “real” photons, Θ_- and $\Theta_+ \approx 0$, the scattered e^- and e^+ are very forward and remain in the beam pipe. The produced particles have a net transverse momentum of zero. production of 0^{++} and 2^{++} is favored although 0^{-+} and 2^{-+} are also allowed.

$a_0(980)$ and $a_0(1450) \rightarrow \eta\pi^0$

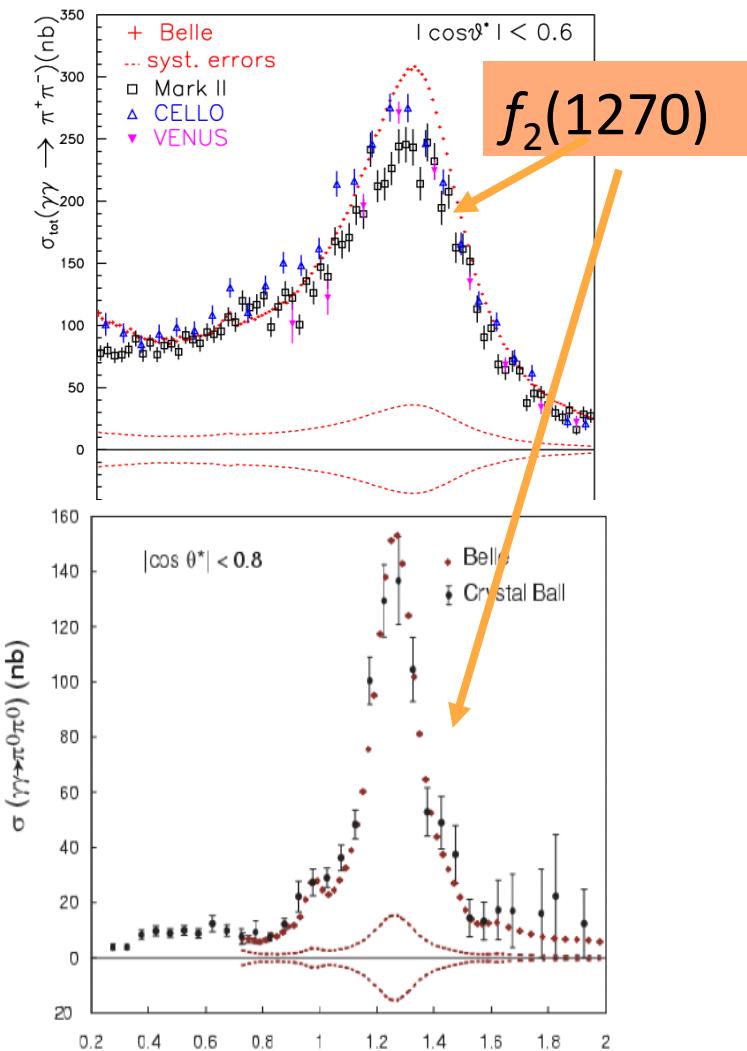
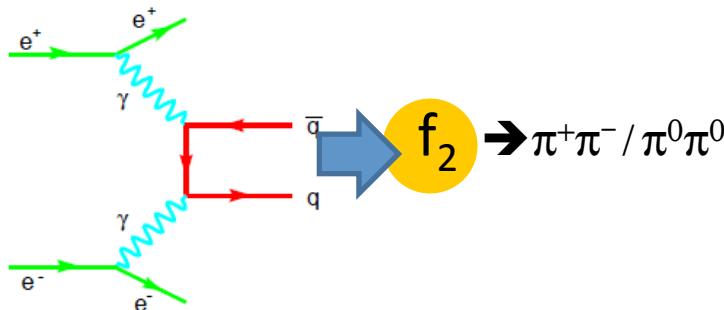
$\gamma\gamma \rightarrow \eta\pi^0$ Belle



PHYSICAL REVIEW D 80, 032001 (2009)

$$\gamma\gamma \rightarrow f_2(1270) \rightarrow \pi^+\pi^- / \pi^0\pi^0$$

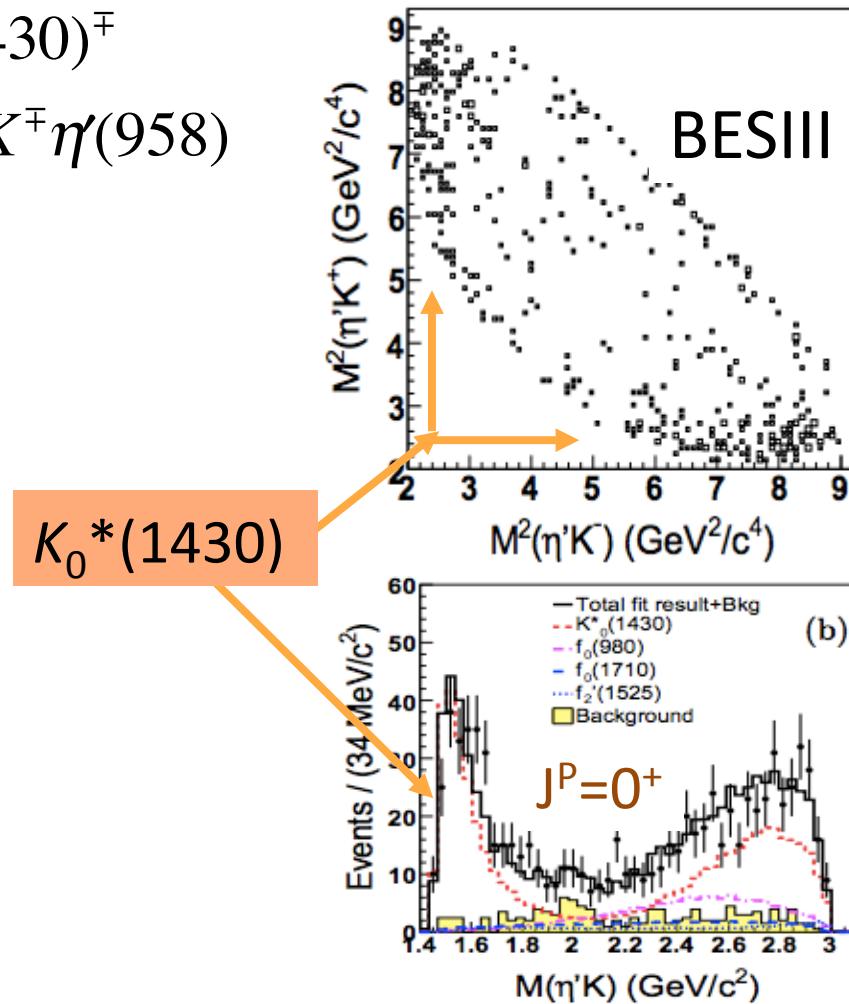
$\gamma\gamma \rightarrow \pi^+\pi^- / \pi^0\pi^0$ at Belle



$$K_0^*(1430)^{\pm} \rightarrow K^{\pm}\eta'(958)$$

$$J/\psi \rightarrow \chi_{c1}(1P)$$

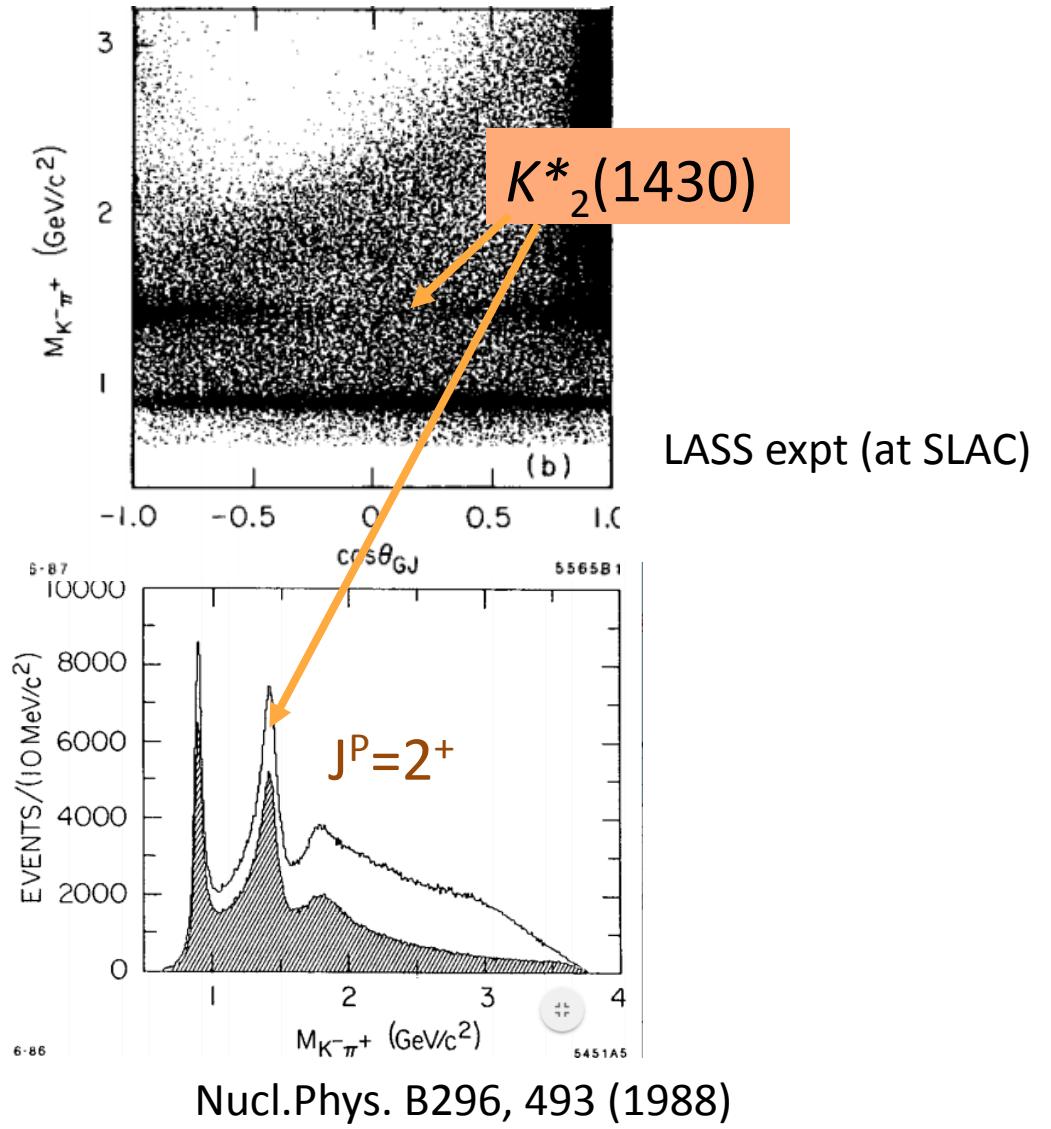
$$\begin{array}{l} \xrightarrow{} K^{\pm} K_0^*(1430)^{\mp} \\ \xrightarrow{} K^{\mp} \eta(958) \end{array}$$



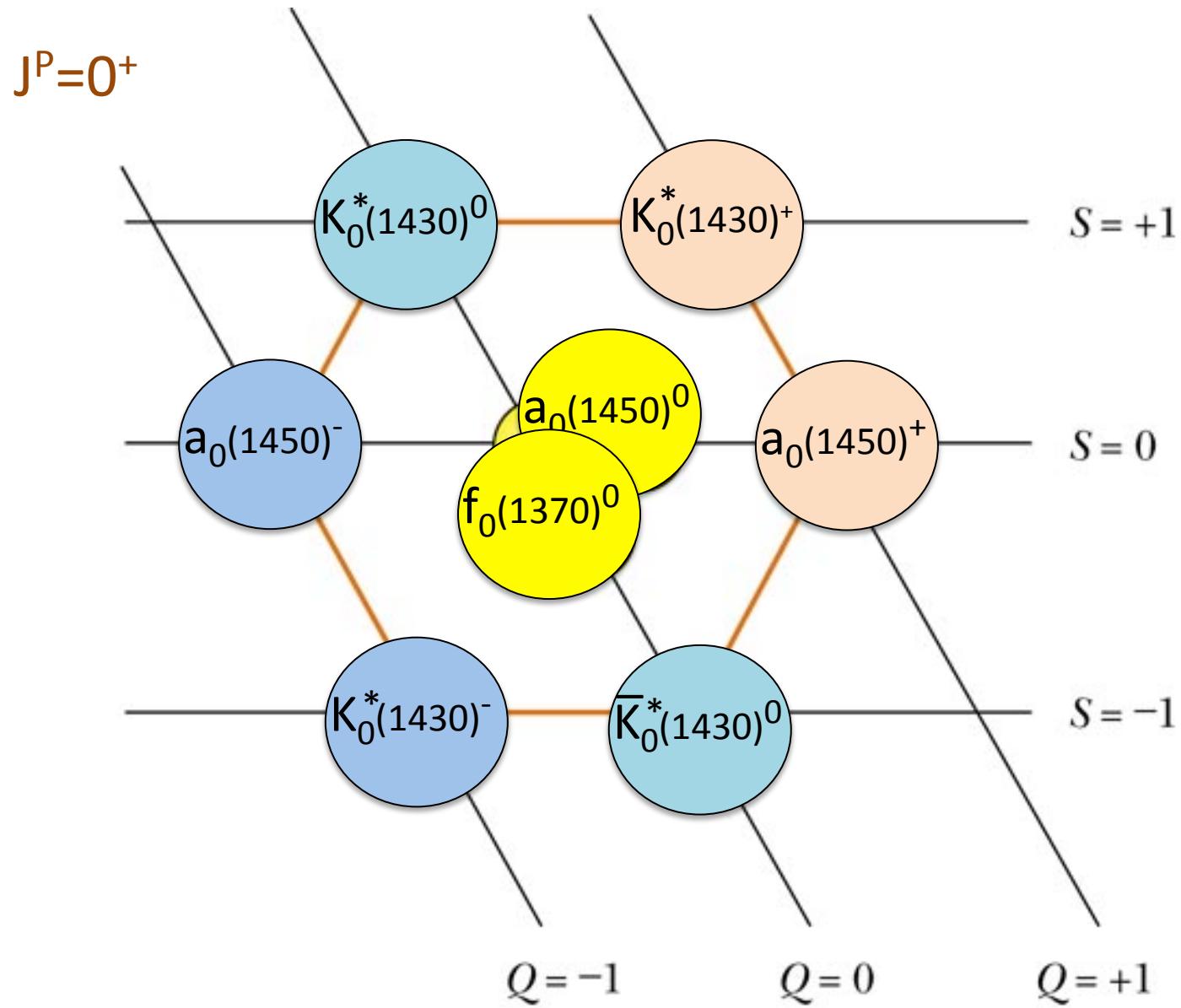
Phys.Rev. D89, 074030 (2014)

$K_2^*(1430) \rightarrow K\pi$

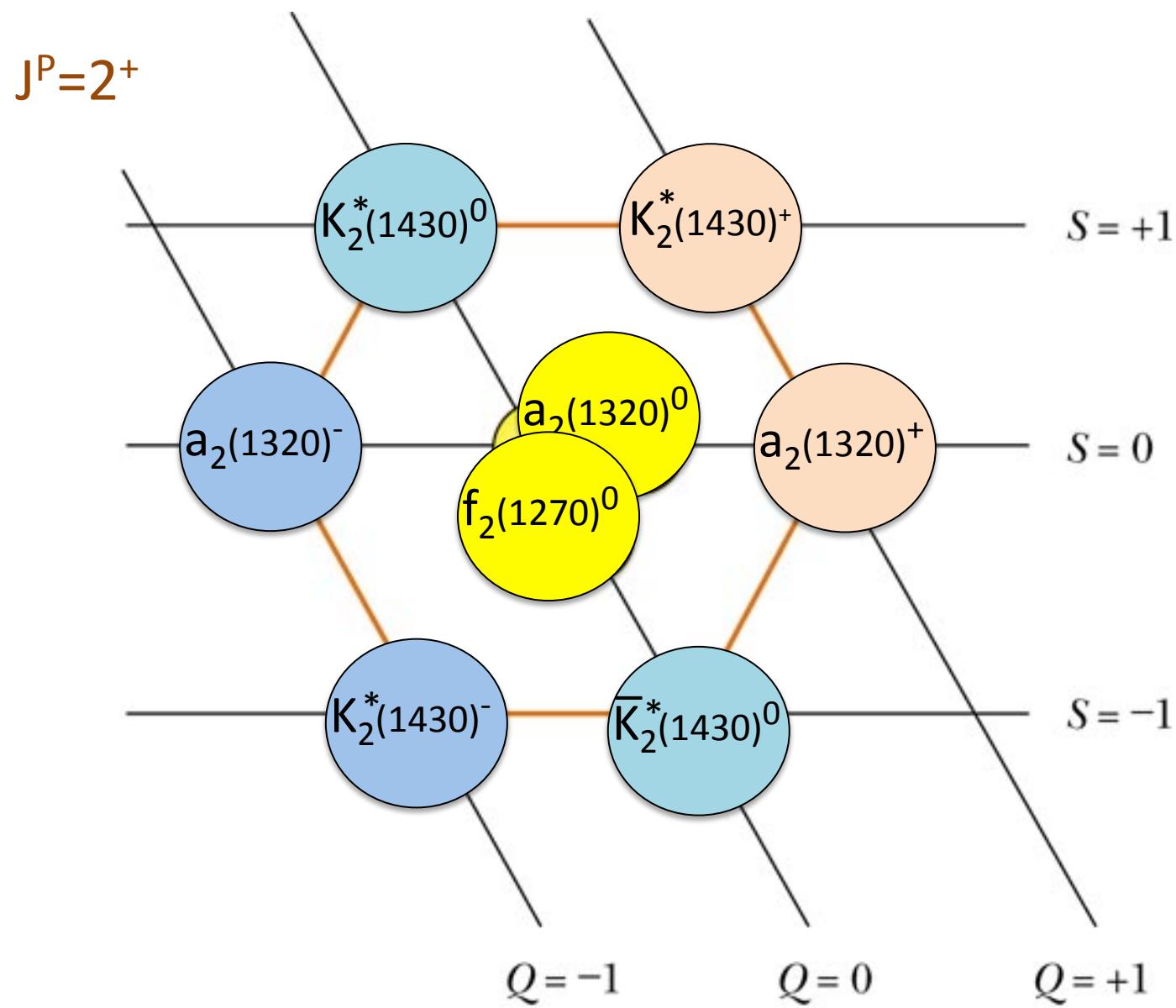
$$\gamma p \rightarrow K^\pm K_2^*(1430)^\mp p \\ \downarrow K^\mp \pi^0$$



The scalar P-wave octet

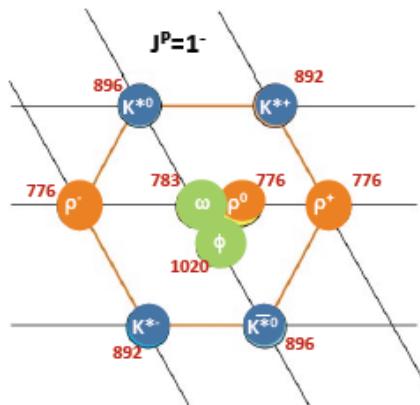


The tensor P-wave octet

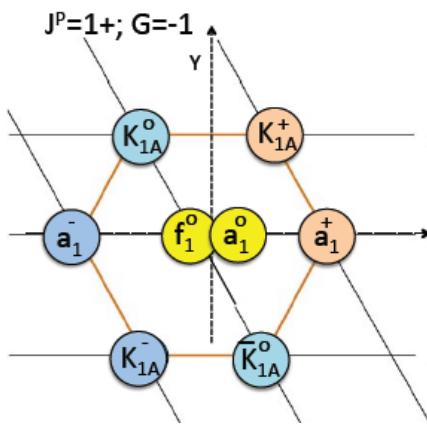


Some features of the P-wave states

S-Wave



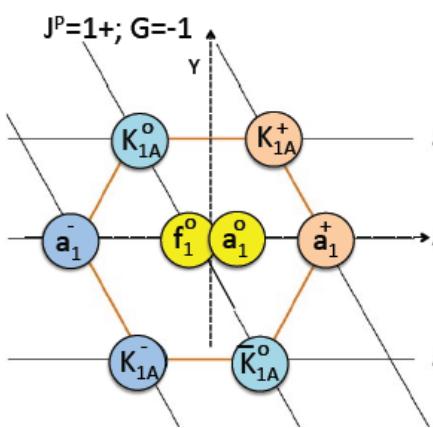
P-Wave



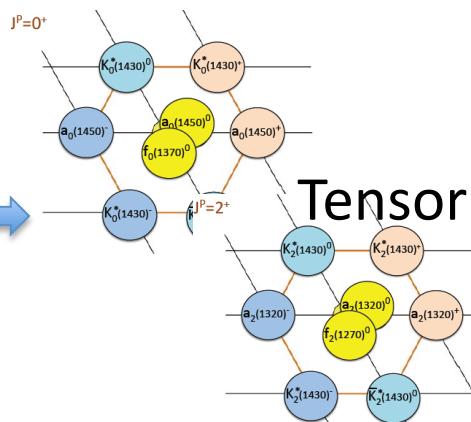
$$\Delta M \approx +400\text{--}500 \text{ MeV}$$

S \rightarrow P costs about 500MeV

Axial Vector



Scalar



$$\delta M \approx 100\text{--}200 \text{ MeV}$$

S=1

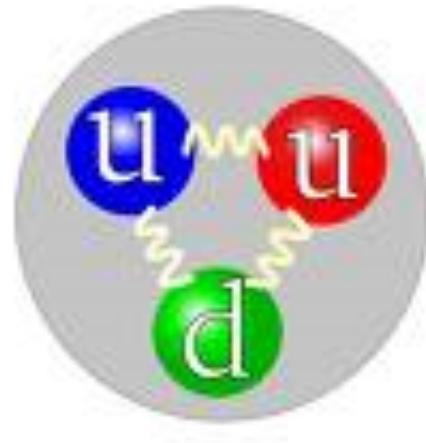
S=0

J=2
J=1
J=0

— J=1

splitting between same L states is ~100MeV

Excited baryons



$$\text{QM: } E = (2(n_r - 1) + L + \frac{3}{2})\hbar\omega$$

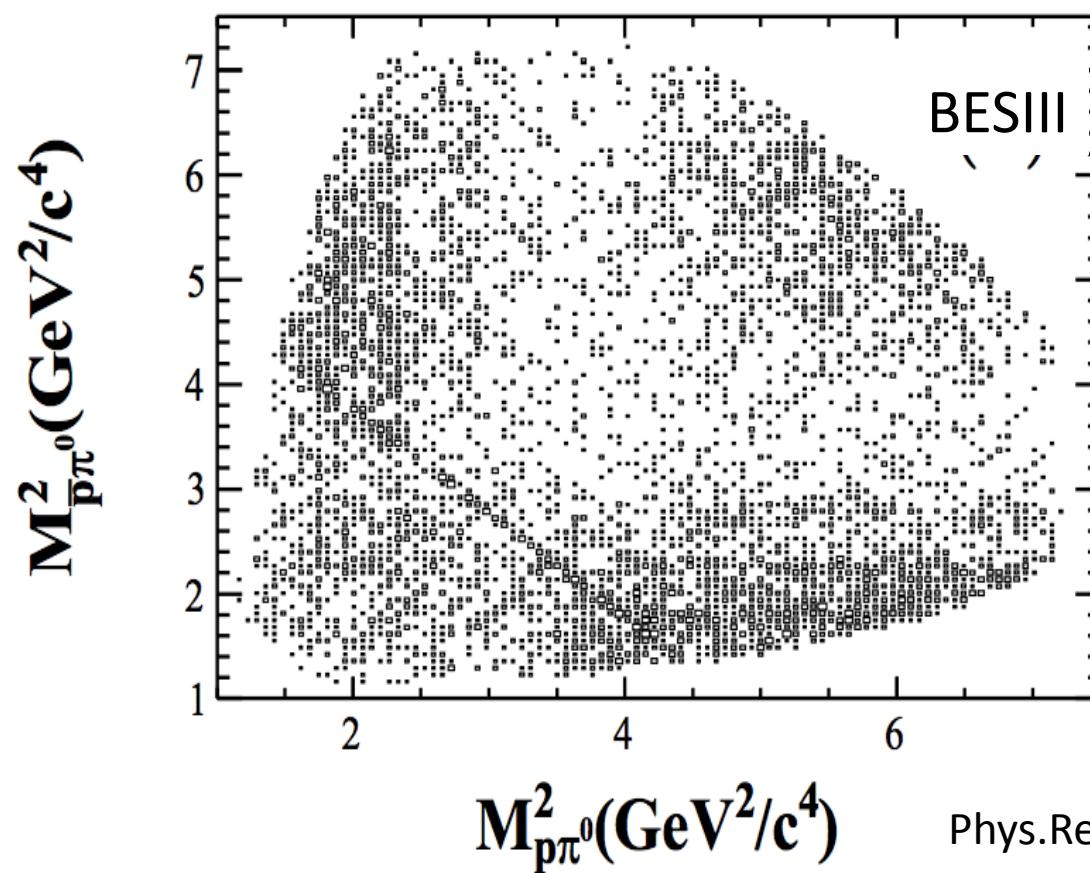
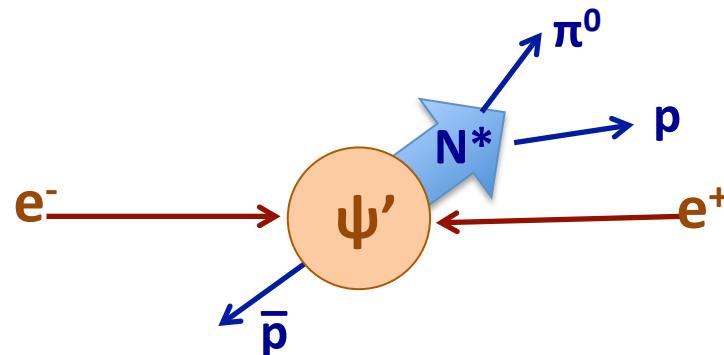
radial excitation has 2 \times the energy from addition of one unit of L

$\psi'(3686) \rightarrow \bar{p} p \pi^0$ at BESIII

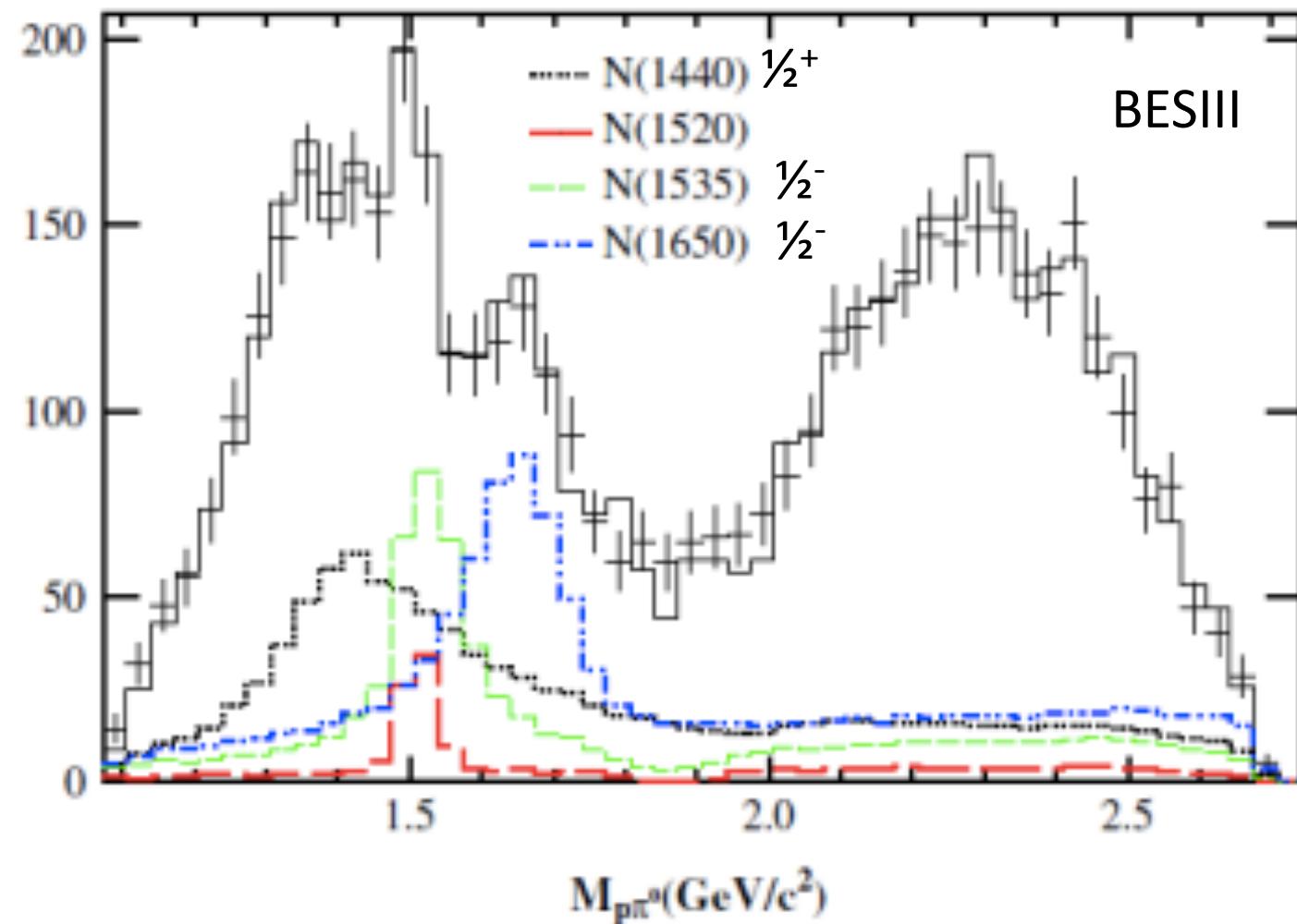
I_{spin}=½ filter

$\psi' \rightarrow \bar{p} N^*$
I=0 I=½

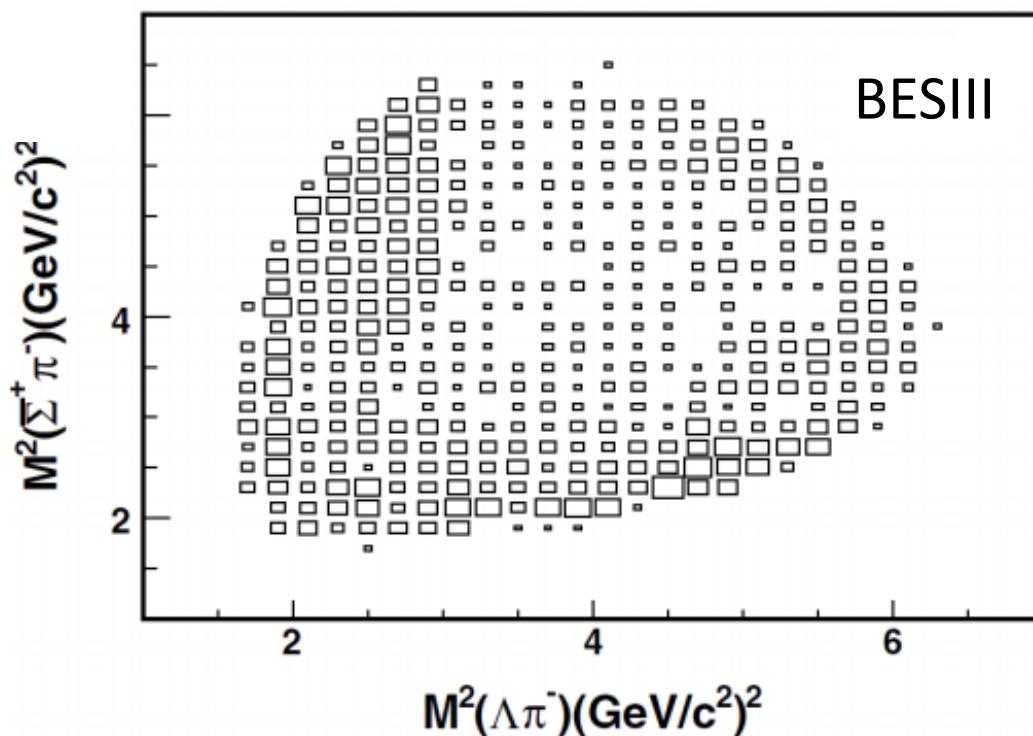
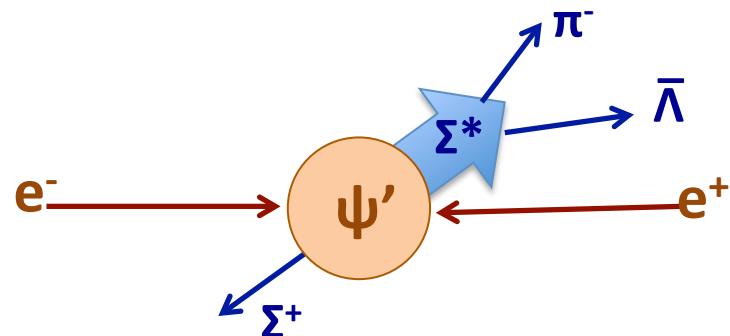
I(N*) must be ½



Excited nucleon states

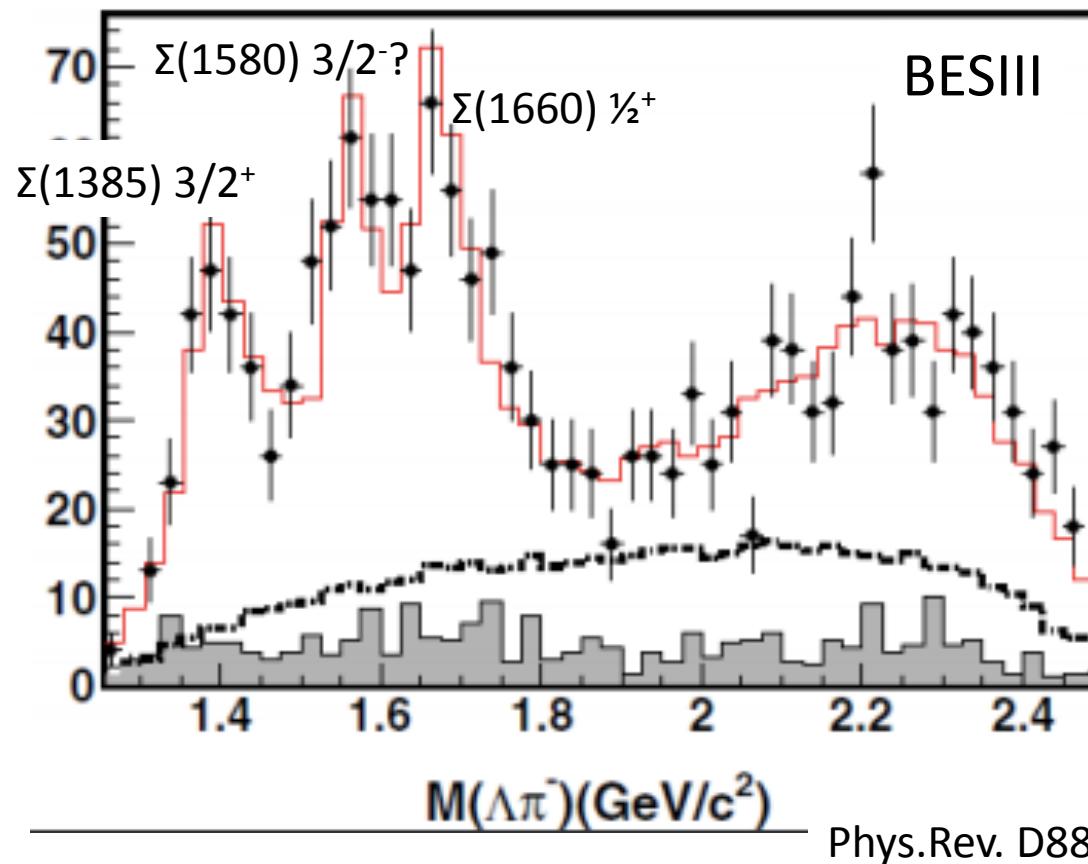


$\psi'(3686) \rightarrow \bar{\Lambda} \Sigma^+ \pi^-$ at BESIII



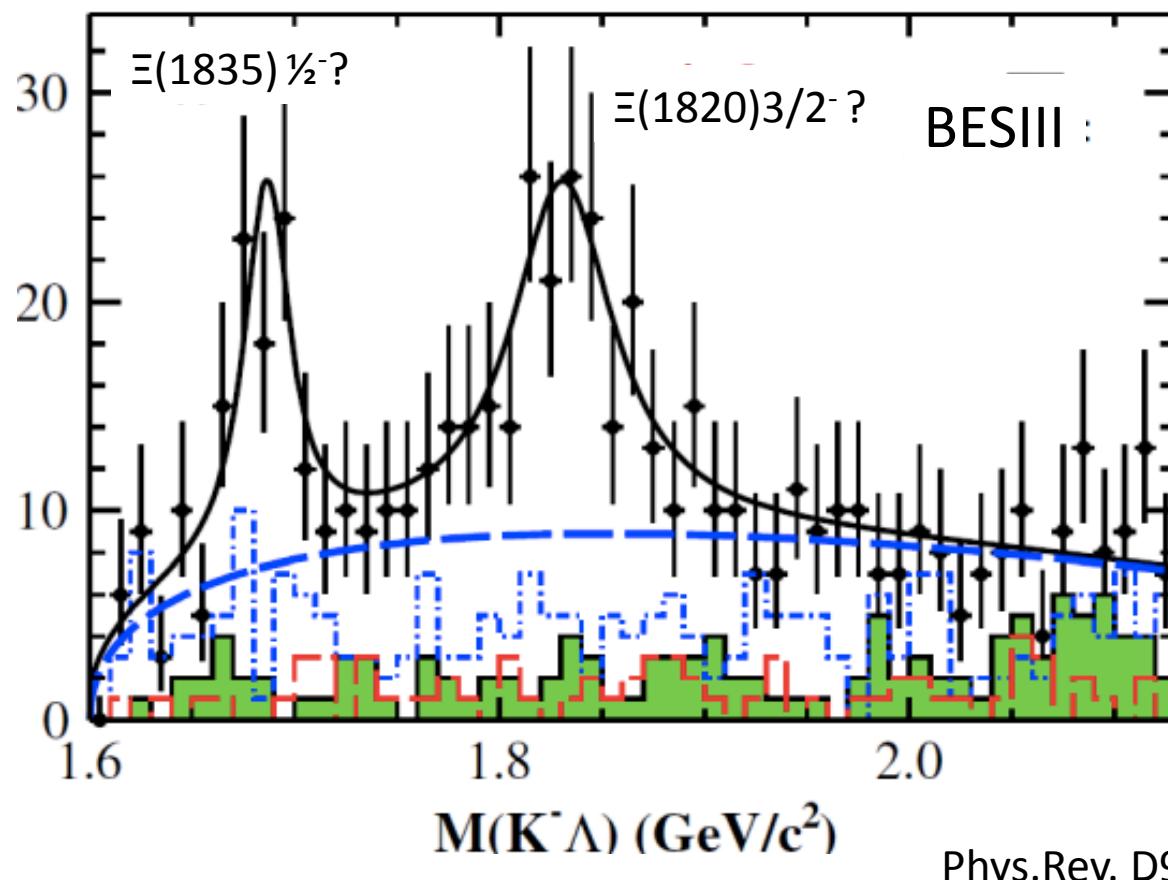
Excited Σ states

$$\psi' \rightarrow \Sigma^+ \bar{\Sigma}^* \\ \downarrow \bar{\Lambda} \pi^-$$



excited Ξ states

$$\psi' \rightarrow \overline{E}^+ E^*{}^- \xrightarrow{\quad} K^- \Lambda$$

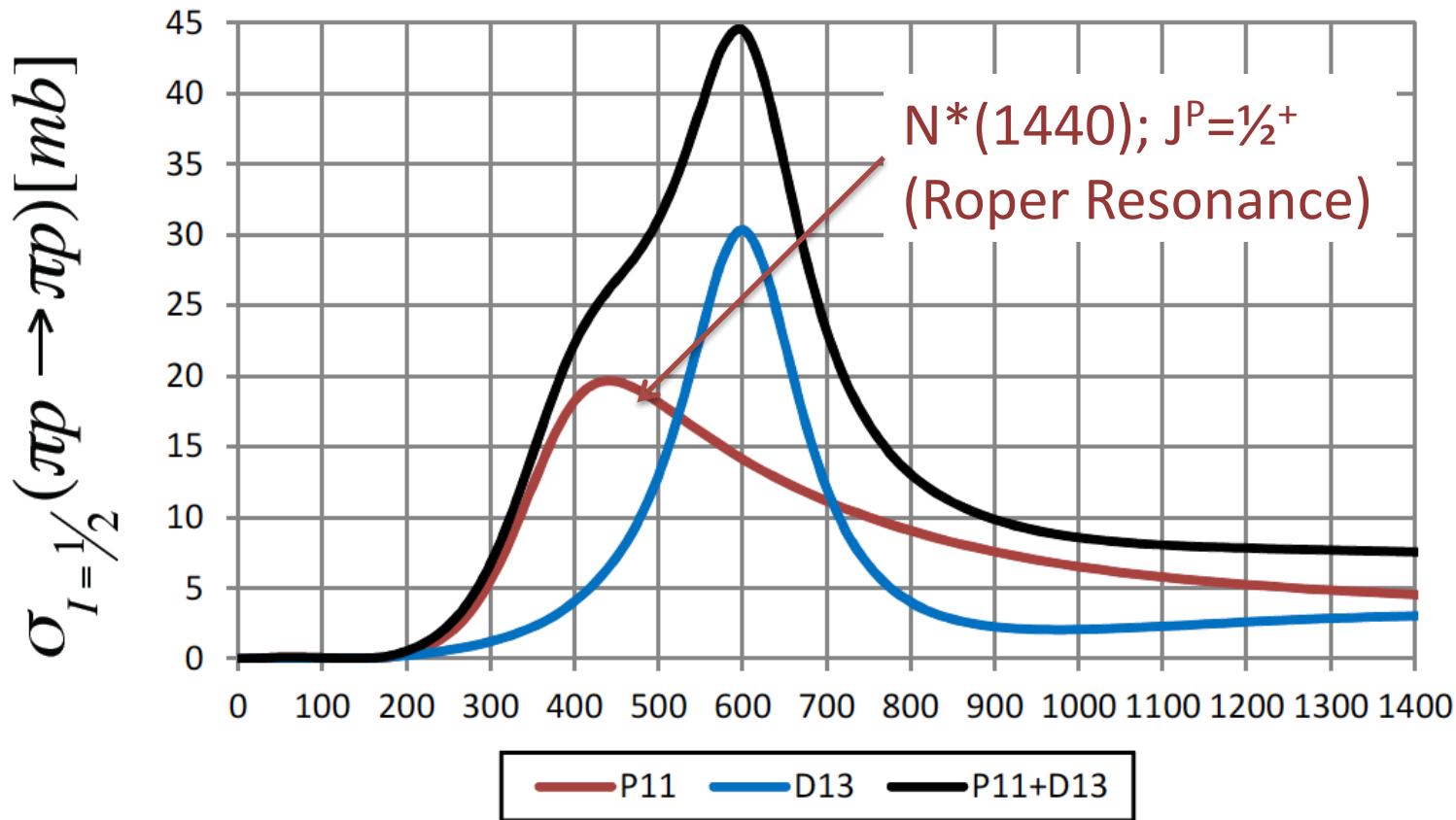


Phys. Rev. D91, 092006 (2015)

Problems with excited Baryons

1st excited nucleon ($I=\frac{1}{2}$) state

-- The “Roper” resonance --



L. David Roper's
MIT PhD Thesis
in 1964

$N^*(1440)$ in the qqq model

$N^*(1440); J^P = \frac{1}{2}^+$ → same spin-parity as proton



Minimal excitation that conserves J^P : $n_r=0 \rightarrow n_r=1$

1st excited Λ predicted in 1959

--pre SU(3); pre quarks--

VOLUME 2, NUMBER 10 pg 425 PHYSICAL REVIEW LETTERS

MAY 15, 1959

1959!!



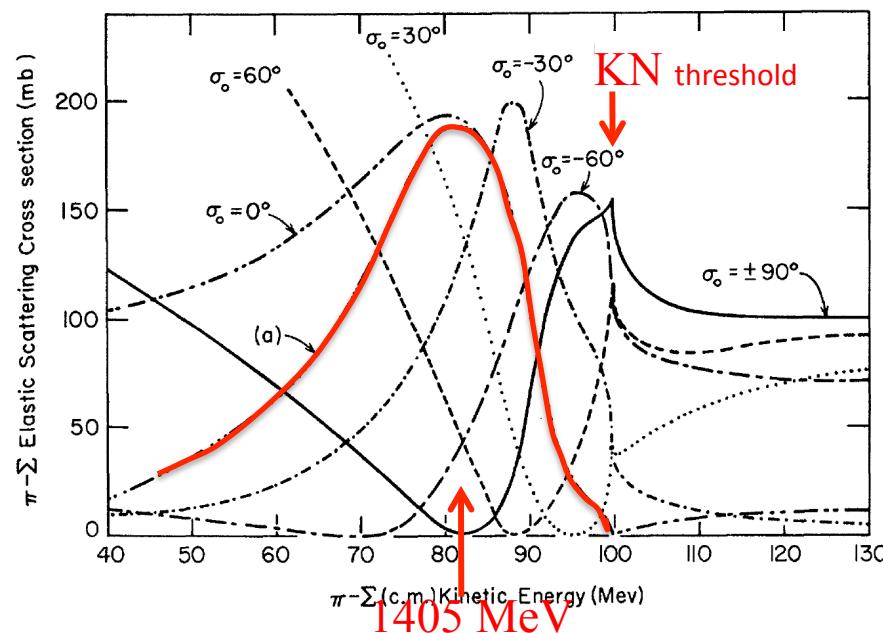
POSSIBLE RESONANT STATE IN PION-HYPERON SCATTERING*

R. H. Dalitz and S. F. Tuan

Enrico Fermi Institute for Nuclear Studies and Department of Physics,
University of Chicago, Chicago, Illinois
(Received April 27, 1959)



Analytic continuation of KN data \rightarrow below KN threshold



Predicted a $\pi\Sigma$ resonance @ 1405

$\Lambda(1405)$ discovered in 1961

VOLUME 6, NUMBER 12 pg 698 PHYSICAL REVIEW LETTERS

JUNE 15, 1961

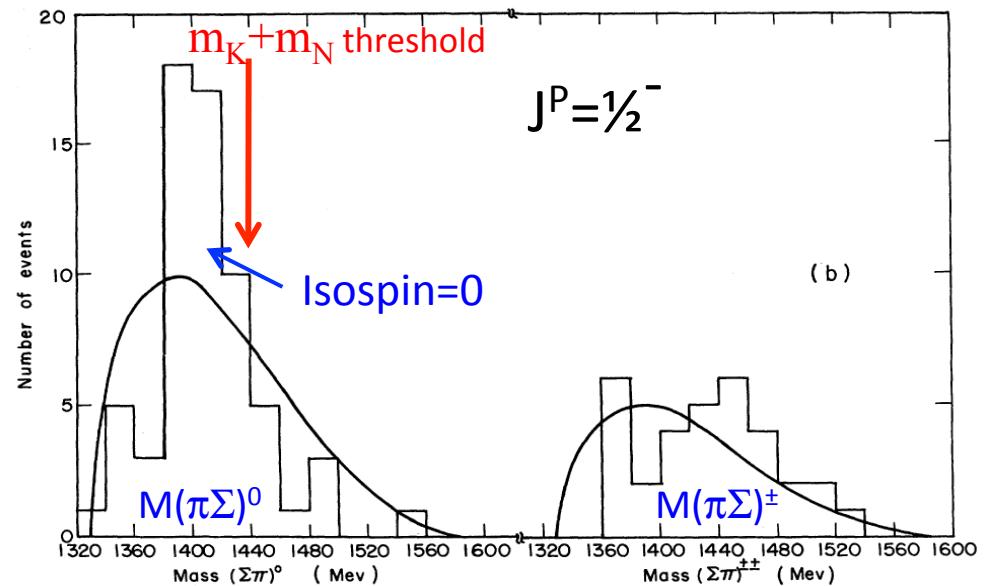
STUDY OF RESONANCES OF THE Σ - π SYSTEM*

Margaret H. Alston, Luis W. Alvarez, Philippe Eberhard,[†] Myron L. Good,[‡]
William Graziano, Harold K. Ticho,^{||} and Stanley G. Wojcicki

Lawrence Radiation Laboratory and Department of Physics, University of California, Berkeley, California

(Received May 8, 1961; revised manuscript received May 31, 1961)

$$\begin{aligned}K^- + p &\rightarrow \Sigma^+ + \pi^- + \pi^- + \pi^+, \\K^- + p &\rightarrow \Sigma^- + \pi^+ + \pi^+ + \pi^-, \\K^- + p &\rightarrow \Sigma^0 + \pi^0 + \pi^+ + \pi^-.\end{aligned}$$



its peak corresponds to a mass of
1405 Mev, and its full width at half maximum is
about 20 Mev after unfolding experimental errors.

⁹R. Dalitz and S. F. Tuan, Phys. Rev. Letters 2,
425 (1959).

$\Lambda(1405)$ in the qqq model

$\Lambda(1405); J^P = \frac{1}{2}^- \rightarrow$ same spin, *opposite-parity* as Λ



Minimal excitation that conserves J^P : $L=0 \rightarrow L=1$

$\Lambda(1405)$ discovered in 1961

VOLUME 6, NUMBER 12 pg 698 PHYSICAL REVIEW LETTERS

JUNE 15, 1961

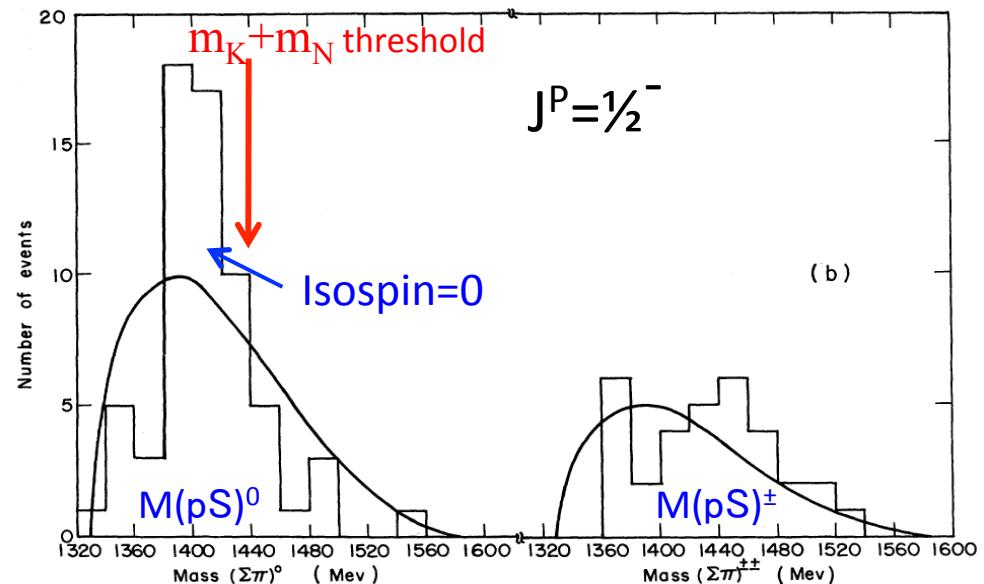
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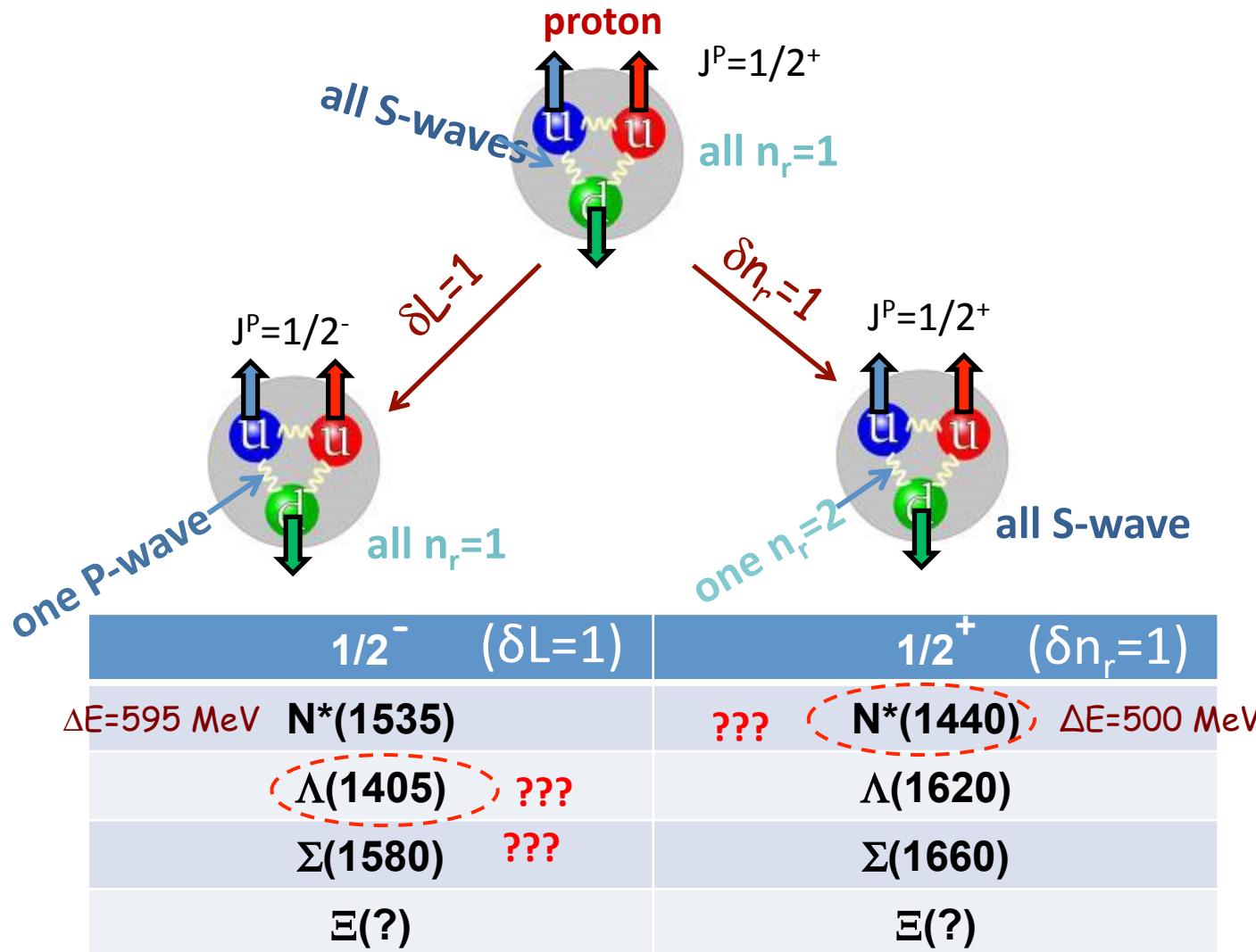
$\Lambda(1405)$ in the qqq model

$\Lambda(1405); J^P = \frac{1}{2}^- \rightarrow$ same spin, *opposite-parity* as Λ



Minimal excitation that conserves J^P : $L=0 \rightarrow L=1$

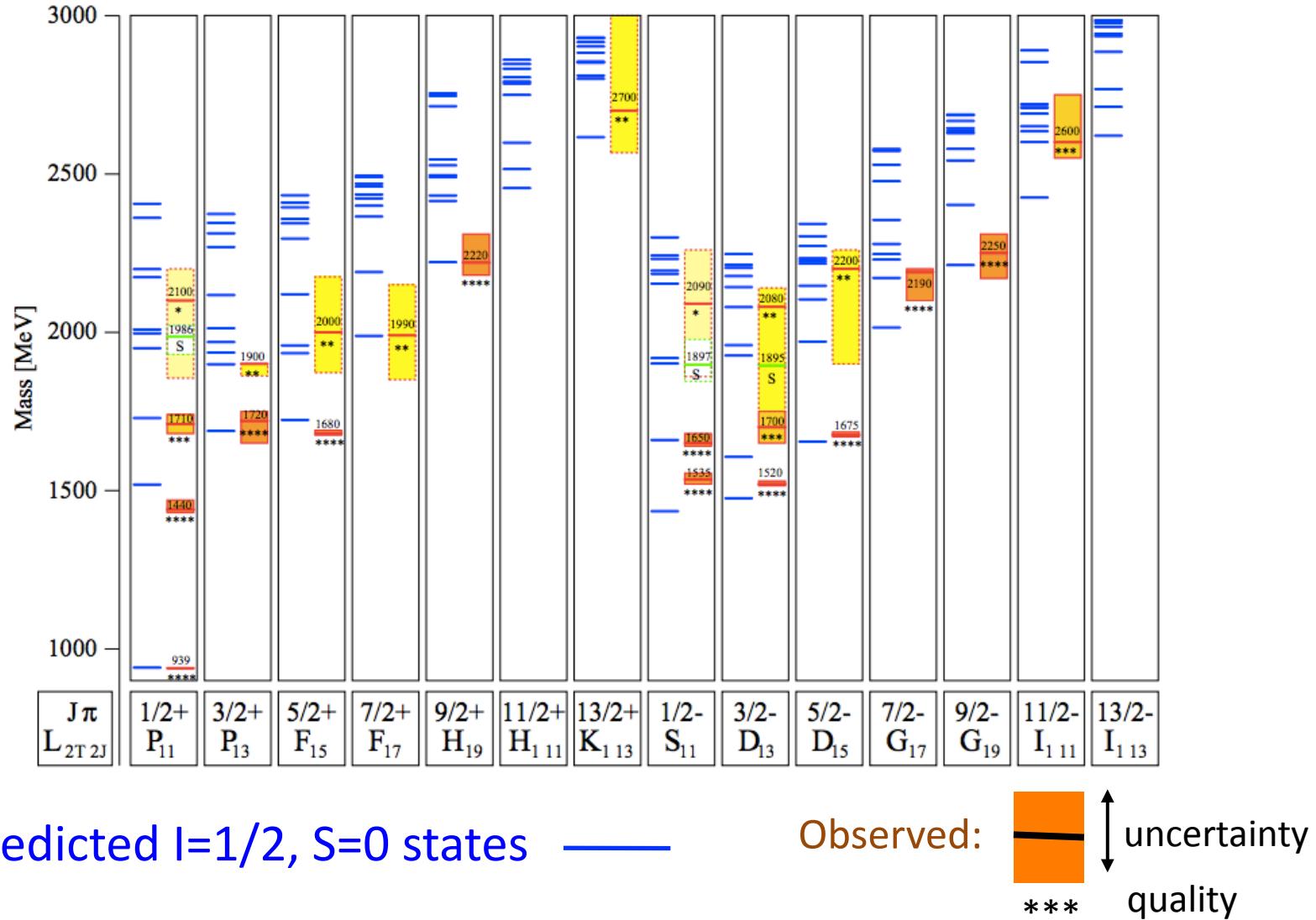
excited baryon octets?



ΔE for $\delta n_r=1$ should be $2 \times \Delta E$ for $\delta L=1$

“Missing” baryon states

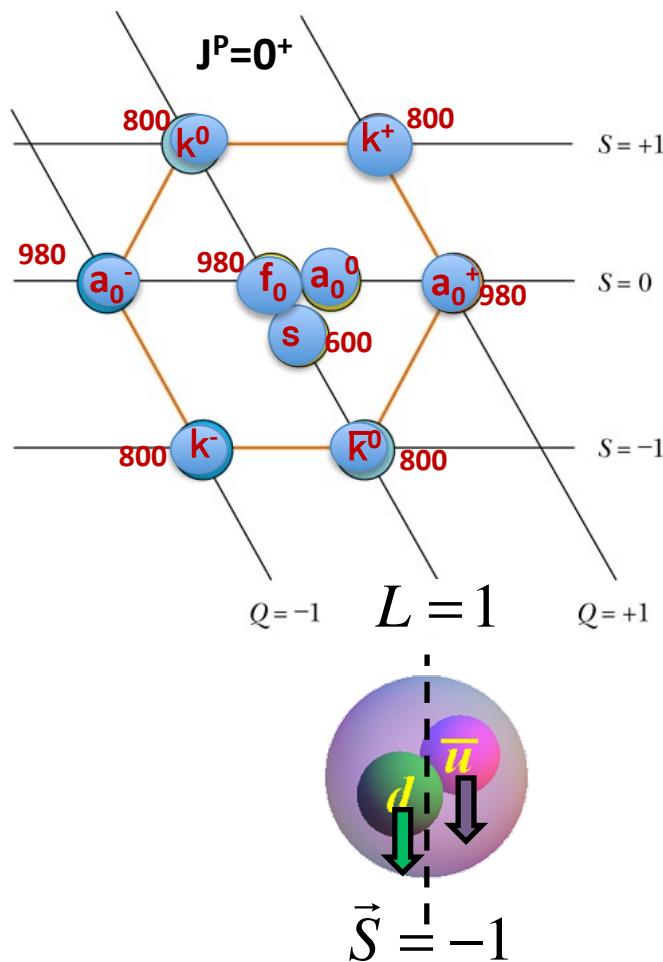
Eur.Phys.J. A!0, 395 (2010)



Problems with mesons

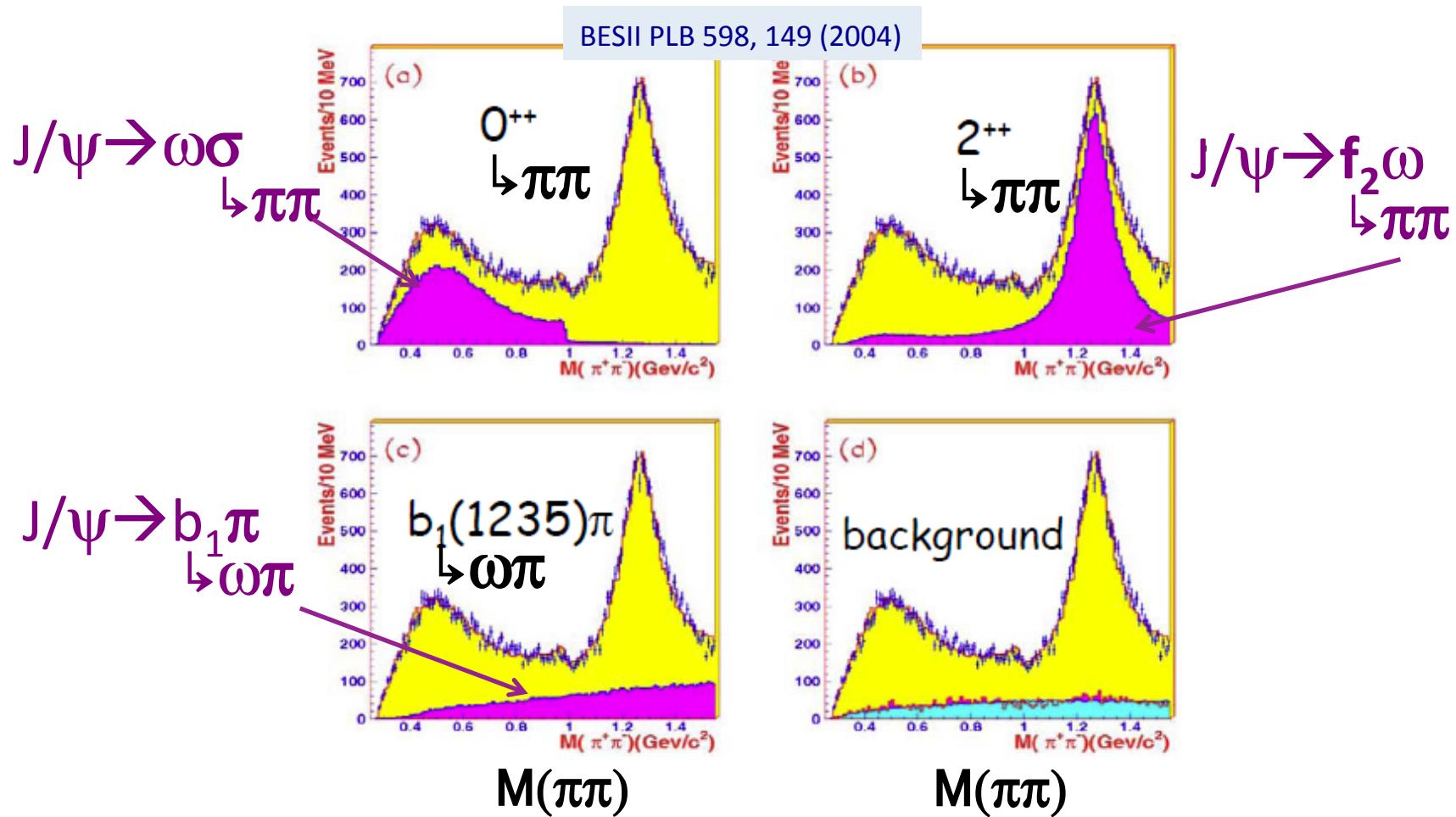
problem with low-mass scalar mesons

the “light” scalar-meson nonet



The $f_0(600)$ (the “ σ ”)

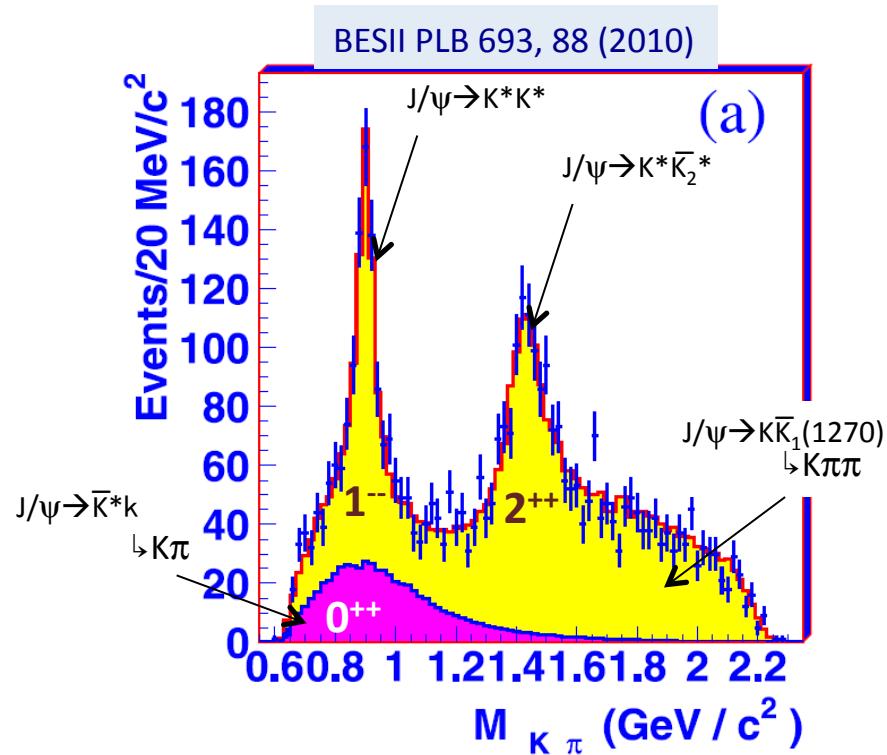
From a Partial Wave Analysis of $J/\psi \rightarrow \omega\pi^+\pi^-$



$$\sigma \text{ pole position: } (541 \pm 39) - i(252 \pm 42) \text{ MeV}$$

$K_0(800)^{\pm}$ (the “ κ^{\pm} ”)

From a Partial Wave Analysis of $J/\psi \rightarrow K^+\pi^0 K_S\pi^-$
with either $M(K^+\pi^0)$ or $M(K_S\pi^-) = M(\kappa^{\pm}) \pm 80$ MeV



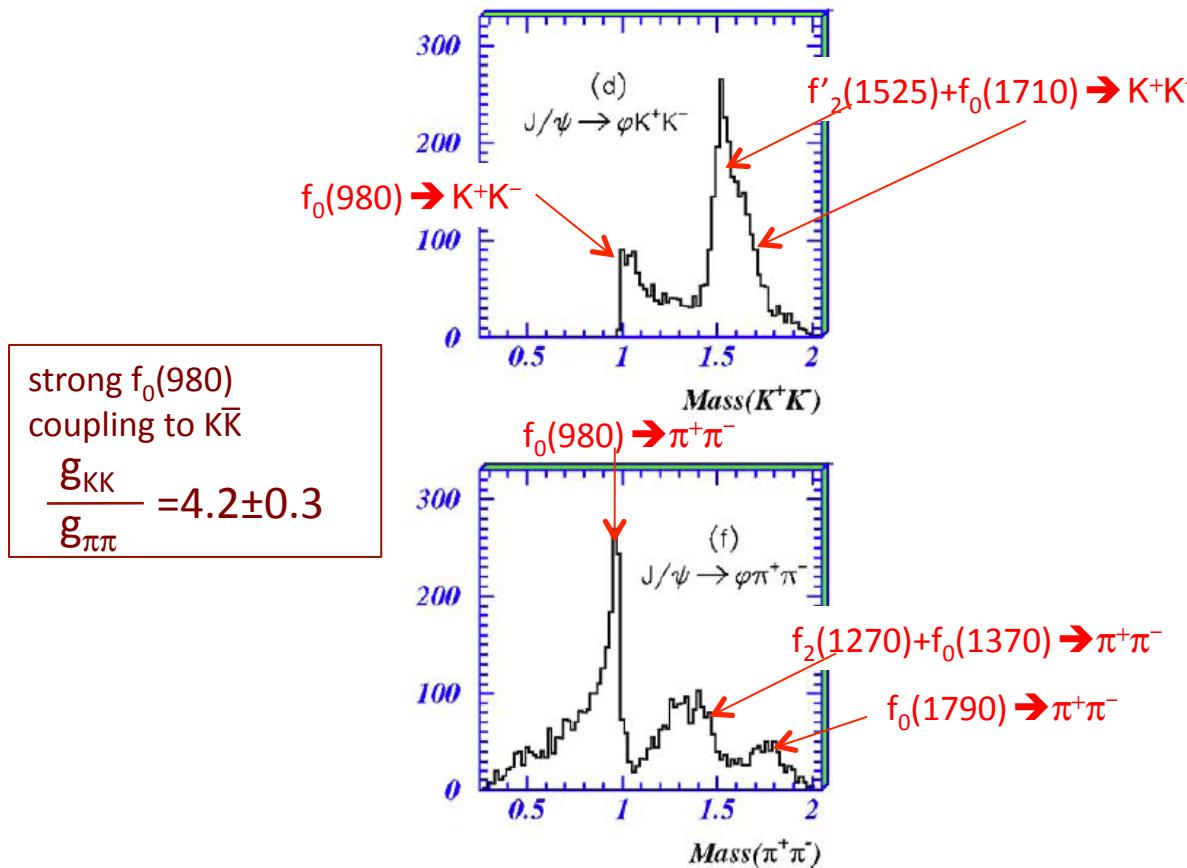
$$\kappa \text{ pole position: } (849 \pm 77^{+18}_{-14}) - i(256 \pm 40^{+46}_{-22}) \text{ MeV}$$

$$Bf(J/\psi \rightarrow K^{*+}K^-) = 10 \pm 3 \times 10^{-4}$$

Signals for $f_0(980) \rightarrow \pi\pi$ & $\rightarrow K^+K^-$

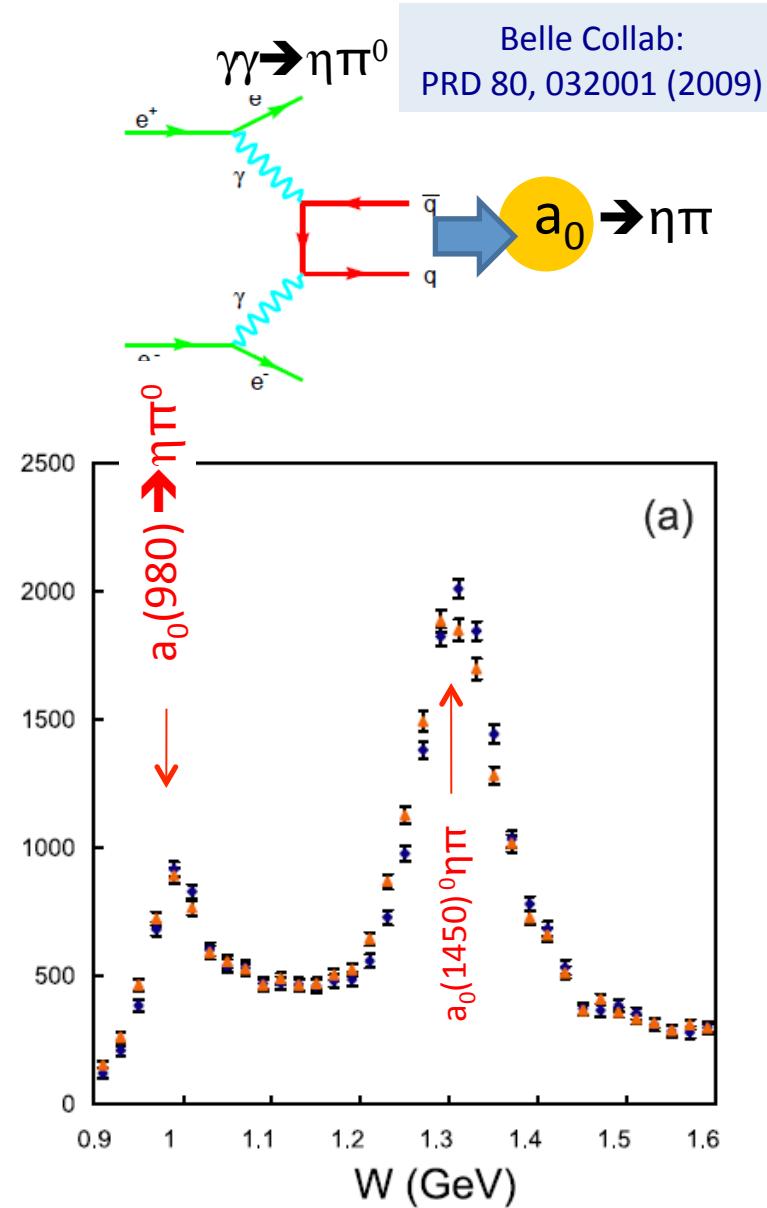
Resonances in $J/\psi \rightarrow \phi\pi^+\pi^-$ and ϕK^+K^-

BESII PLB 607, 243 (2005)



$$Bf(J/\psi \rightarrow ff_0(980)) = 0.32 \pm 0.09 \times 10^{-3}$$

Signal for $a_0(980) \rightarrow \eta\pi$

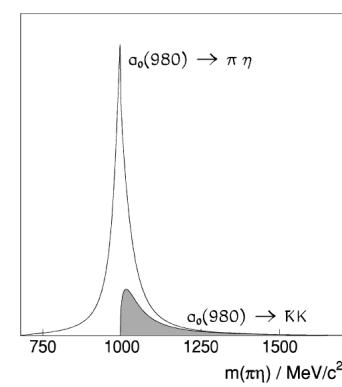
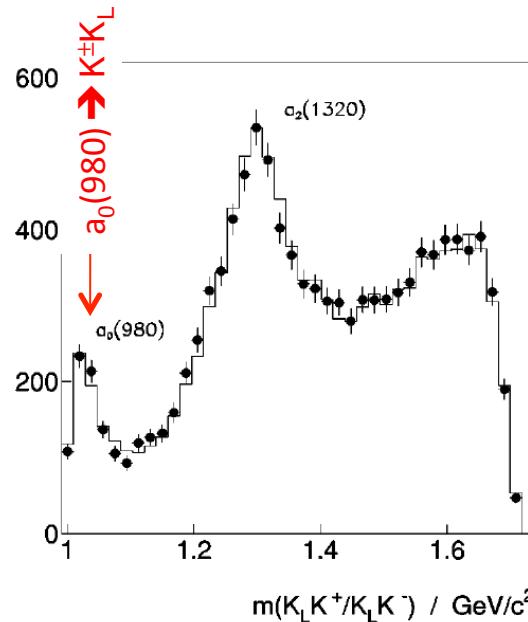


PHYSICAL REVIEW D 80, 032001 (2009)

Signal for $a_0(980) \rightarrow K^+K^-$

$\bar{p}p$ ANNIHILATION AT REST INTO $K_L K^\pm \pi^\mp$

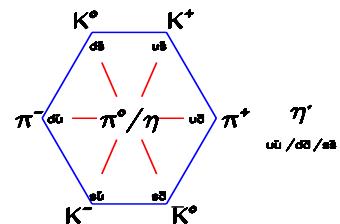
Crystal Barrel Collab: PRD 57, 3860 (1998)



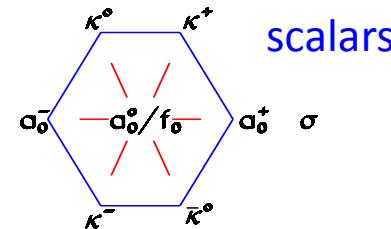
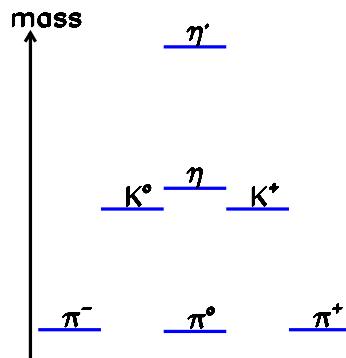
strong $a_0(980)$
coupling to KK
 $\frac{g_{KK}}{g_{\eta\pi}} = 1.03 \pm 0.14$

light scalar nonet masses are inverted

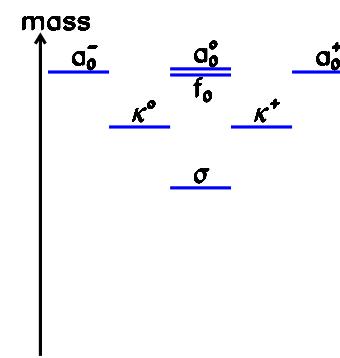
pseudoscalars



typical



unique

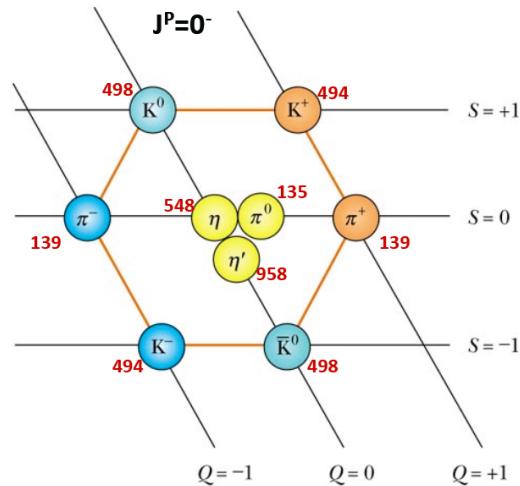


Also:

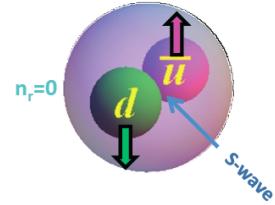
- No “light” $J^P=1^+$ and 2^{++} partner nonets in the same mass range.
- In $q\bar{q}$ meson nonets, the $I=1$ mesons have no s-quarks and are the lightest. However, the $a_0(980)$ $I=1$ mesons are the nonet’s heaviest.
- The $a_0(980)$ triplet has strong couplings to $KK\bar{K}$.
- $m(f_0(980)) \sim m(a_0(980))$ implies “ideal” mixing & ***small*** s-quark content in $f_0(980)$.
- strong $K\bar{K}$ couplings of the $a_0(980)$ & $f_0(980)$ violate OZI-rule for $q\bar{q}$ mesons

Problems with mesons = q \bar{q} model

pseudoscalars

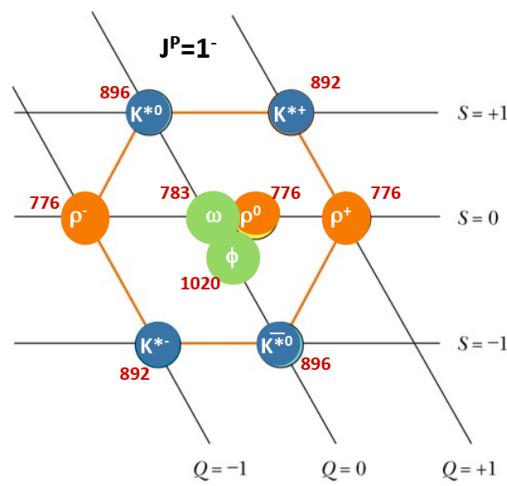


(π^+, π^0, π^-) =lightest

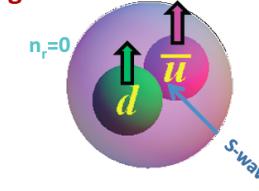


OK

vectors

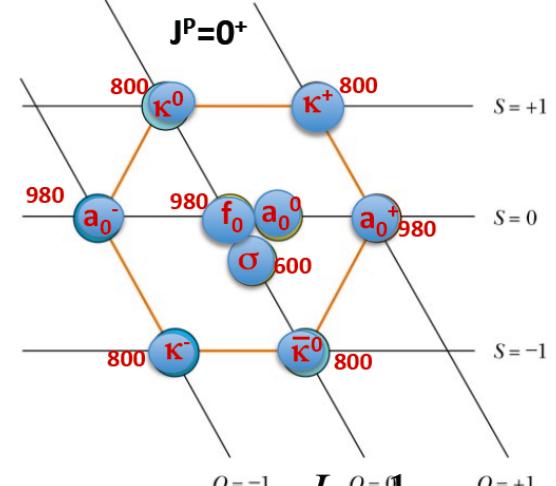


(ρ^+, ρ^0, ρ^-) =lightest

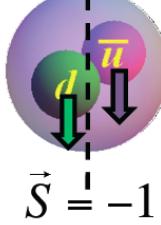


OK

scalars



(a_0^+, a_0^0, a_0^-) =heaviest



NG!

$L=0$

$S=-1$

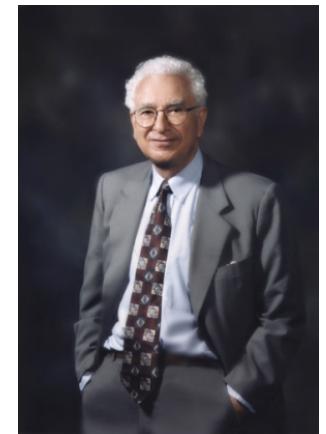
Some fundamental problems with the quark model:

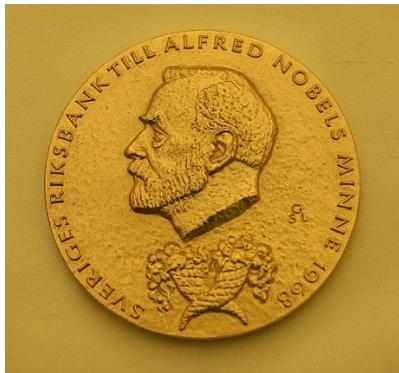
- **Individual quarks are not seen**
- **why only qqq and $q\bar{q}$ combinations?**
- **violation of spin-statistics theorem?**

Are quarks real objects? or just mathematical mnemonics?

助记符

"Are quarks actually real objects?" Gell-Mann asked.
"My experimental friends are making a search for them
in all sorts of places -- in high-energy cosmic ray reactions
and elsewhere. A quark, being fractionally charged,
cannot decay into anything but a fractionally charged
object because of the conservation law of electric charge.
Finally, you get to the lowest state that is fractionally
charged, and it can't decay. So if real quarks exist, there is
an absolutely stable quark. Therefore, if any were ever
made, some are lying around the earth."
But since no one has yet found a quark, Gell-Mann
concluded that we must face the likelihood that quarks are
not real.





The Nobel Prize in Physics 1969

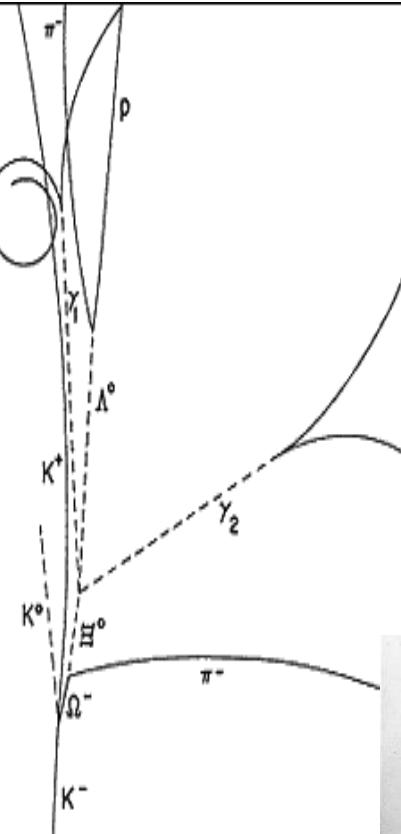
"for his contributions and discoveries concerning the classification of elementary particles and their interactions"



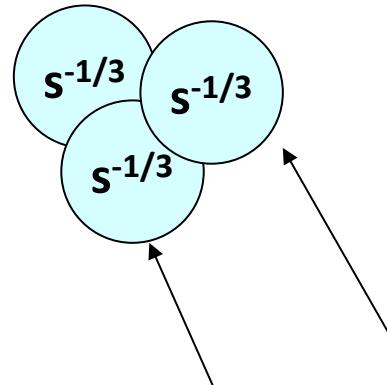
Nobel citation:

This classification of the elementary particles and their interaction discovered by Gell-Mann has turned out to applicable to all strongly interacting particles found later and these are practically all particles discovered after 1953. His discovery is therefore fundamental in elementary particle physics.

No mention of quarks; no prizes for Zweig, Sakata, or Fermi-Yang.



Ω^-



three s-quarks
in the same
quantum state



Das ist verboten!!

The strong interaction “charge” of each quark comes in 3 different varieties

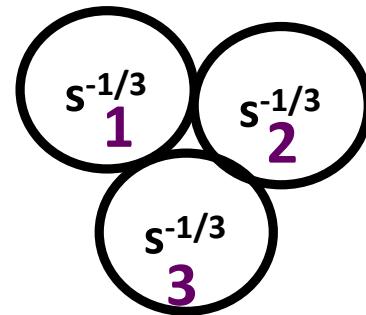
Y. Nambu



M.-Y. Han



Ω^-



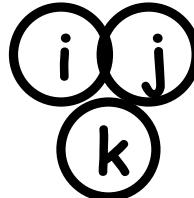
the 3 $s^{-1/3}$ quarks in the Ω^- have different strong charges & evade Pauli

Attractive configurations

Baryons:

$$\epsilon_{ijk} e_i e_j e_k$$

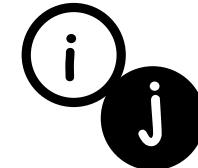
$$\begin{aligned}\epsilon_{ijk} &= 1 \text{ for } i \neq j \neq k \\ &= 0 \text{ otherwise}\end{aligned}$$



Mesons:

$$\delta_{ij} e_i \bar{e}_j$$

$$\begin{aligned}\delta_{ij} &= 1 \text{ for } i=j \\ &= 0 \text{ otherwise}\end{aligned}$$



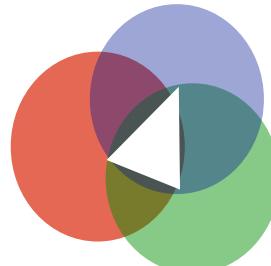
same as the rules for combining colors to get white:

add 3 primary colors or add color+complementary color

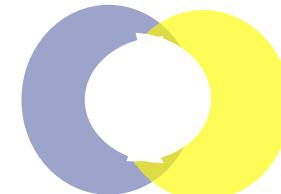
quarks: $e_i e_j e_k \rightarrow$ color charges

antiquarks: $\bar{e}_i \bar{e}_j \bar{e}_k \rightarrow$ anticolor charges

$$\epsilon_{ijk} e_i e_j e_k$$

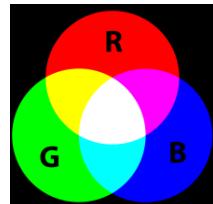


$$\delta_{ij} e_i \bar{e}_j$$

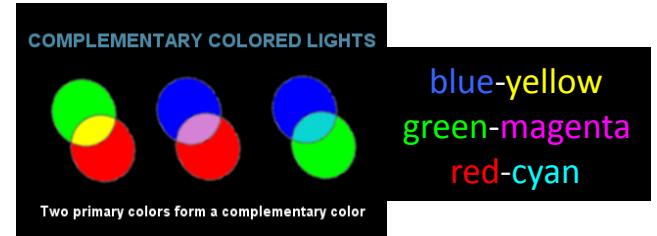


QPM Superseded by QCD in the 1970s: observed particles are color singlets

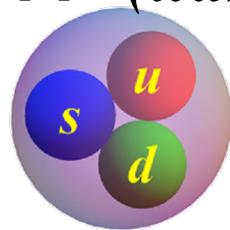
3 primary colors → white



color + complementary color → white

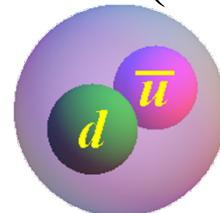


$\Lambda = (uds)$



Baryons are red-blue-green triplets

$\pi^- = (d\bar{u})$

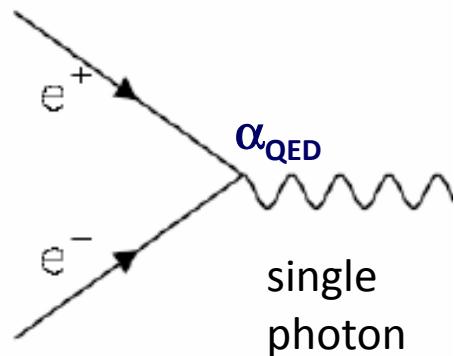


Mesons are color-anticolor pairs

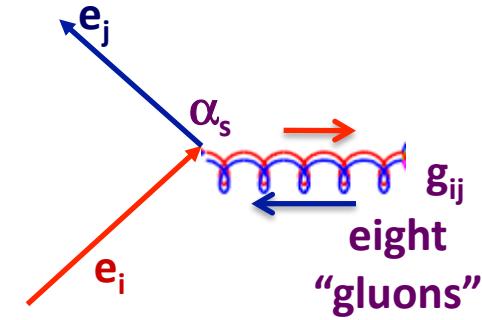
A few remarks about QCD

Quantum Chromodynamics

QED: scalar charge e



QCD triplet charge:

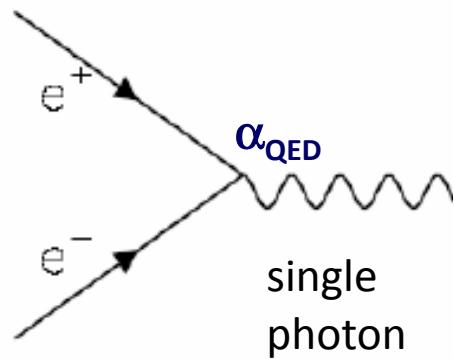


$$\begin{bmatrix} e_r \\ e_b \\ e_g \end{bmatrix}$$

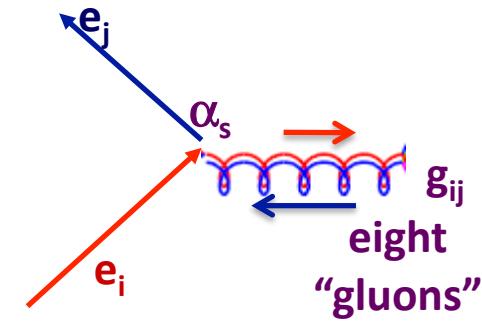
Non-Abelian
extension of QED

Quantum Chromodynamics

QED: scalar charge e



QCD triplet charge:



$$\begin{bmatrix} e_r \\ e_b \\ e_g \end{bmatrix}$$

Non-Abelian
extension of QED

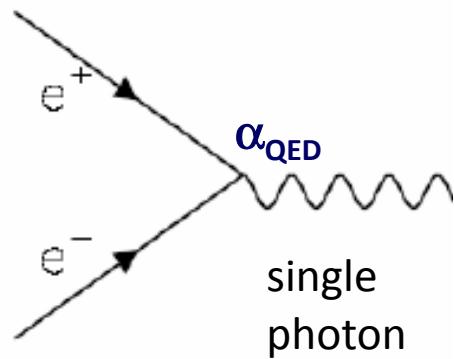
QED gauge transform

$$\vec{\nabla} \rightarrow \vec{\nabla} + i e \vec{A}$$

1 vector
field
(photon)

Quantum Chromodynamics

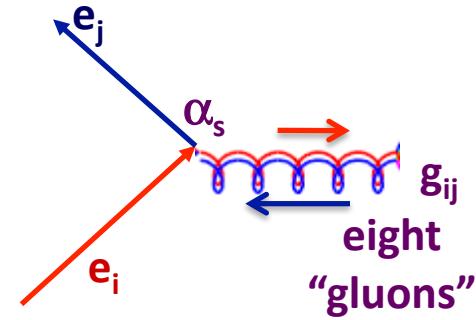
QED: scalar charge e



Non-Abelian extension of QED

QCD triplet charge:

$$\begin{bmatrix} \mathbf{e}_r \\ \mathbf{e}_b \\ \mathbf{e}_g \end{bmatrix}$$



QED gauge transform

$$\vec{\nabla} \rightarrow \vec{\nabla} + i e \vec{A}$$

1 vector field (photon)

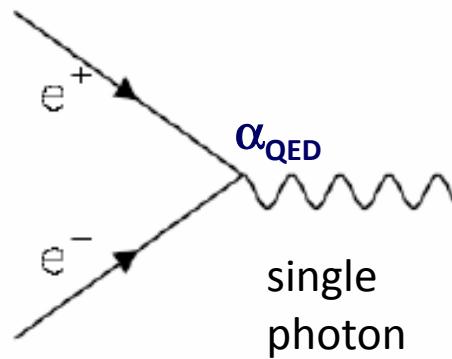
$$\vec{\nabla} \rightarrow \vec{\nabla} + i \alpha_s \lambda_i \vec{G}_i$$

eight 3×3 SU(3) matrices

8 vector fields (gluons)

Quantum Chromodynamics

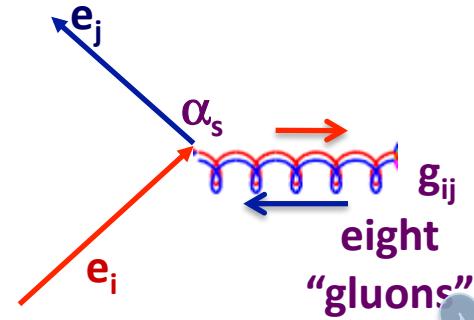
QED: scalar charge e



Non-Abelian extension of QED

QCD triplet charge:

$$\begin{bmatrix} e_r \\ e_b \\ e_g \end{bmatrix}$$



QED gauge transform

$$\vec{\nabla}$$

QED photons are electrically neutral
vector field (photon)

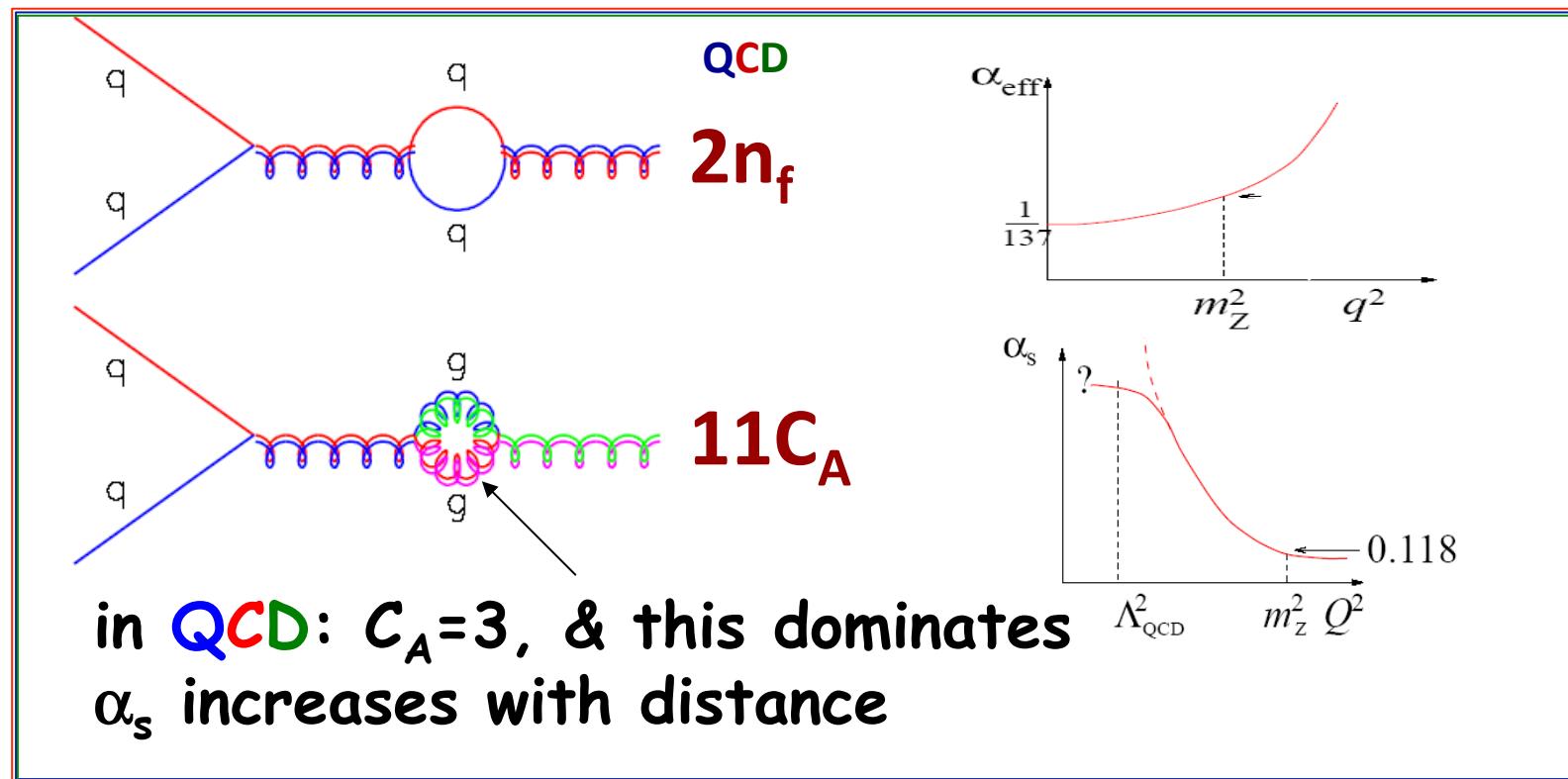
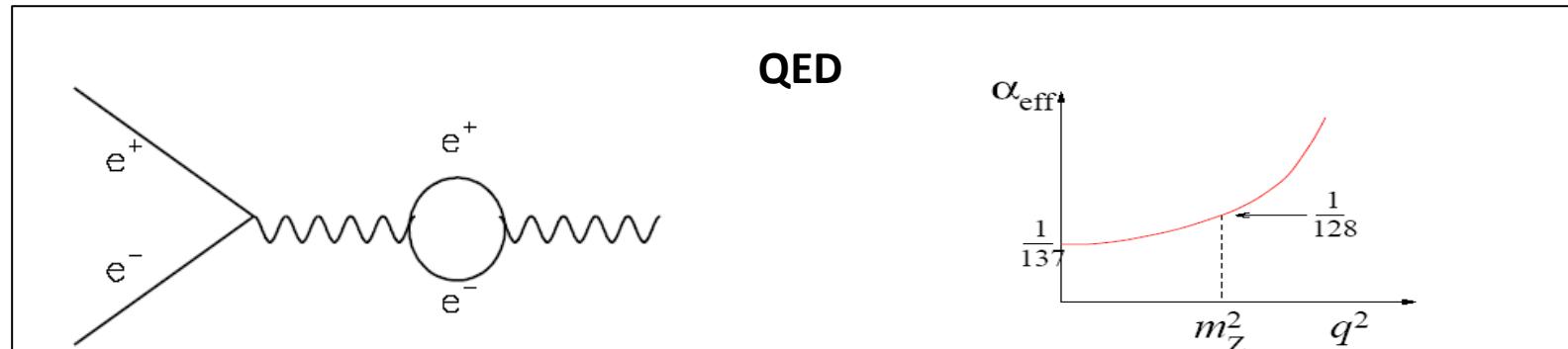
QCD gauge transform

$$\vec{\nabla}$$

QCD gluons have color charges
Eight 3×3 $SU(3)$ matrices
 G_i

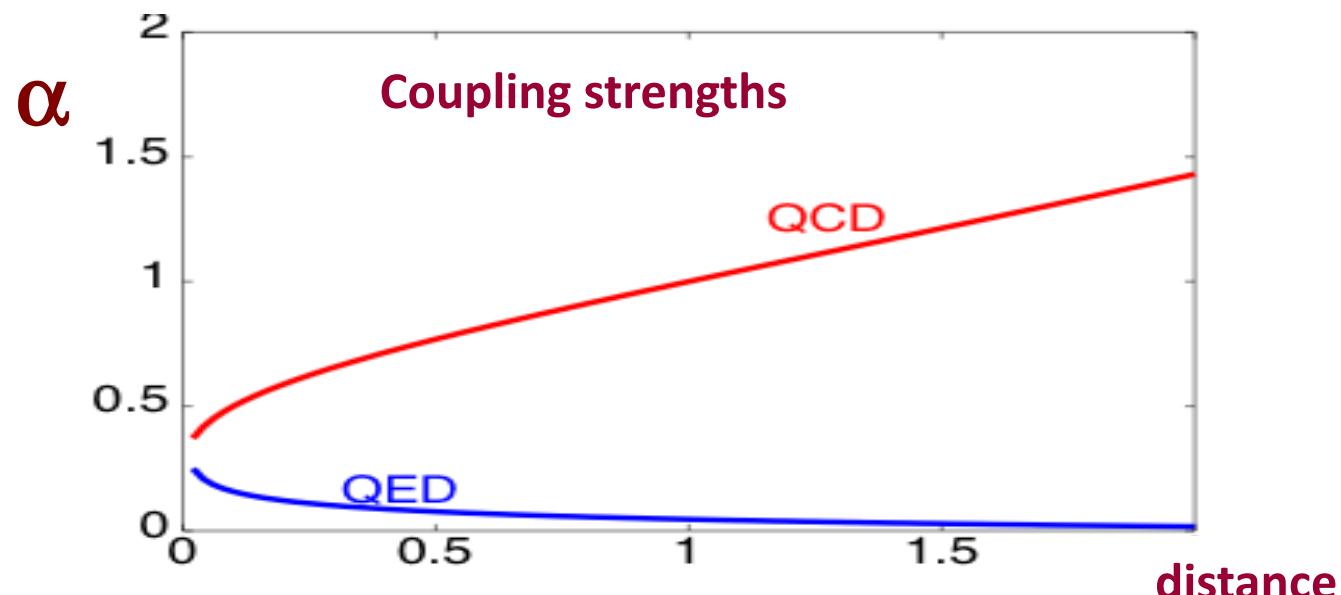
8 vector fields (gluons)

Vacuum polarization QED vs QCD

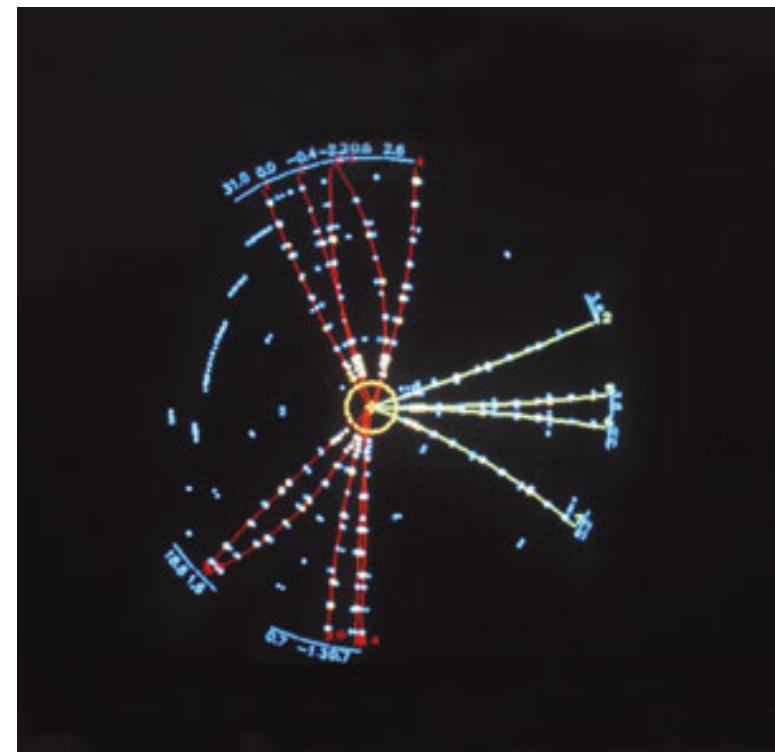
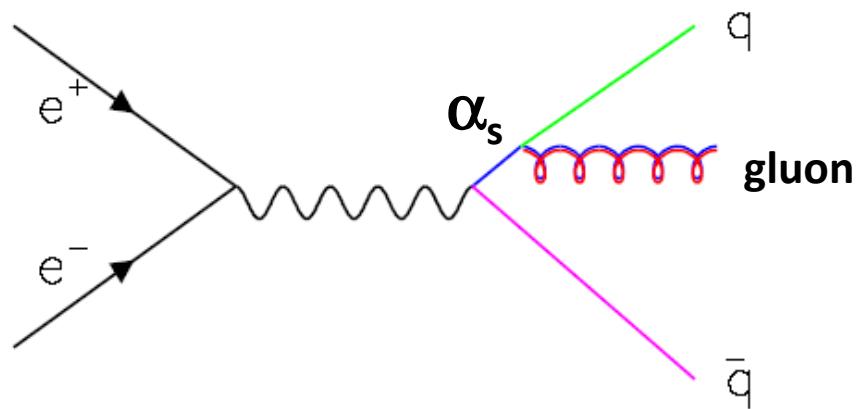


QED: photons have no charge
coupling decreases at large distances

QCD: gluons carry color charges
gluons interact with each other
coupling increases at large distances

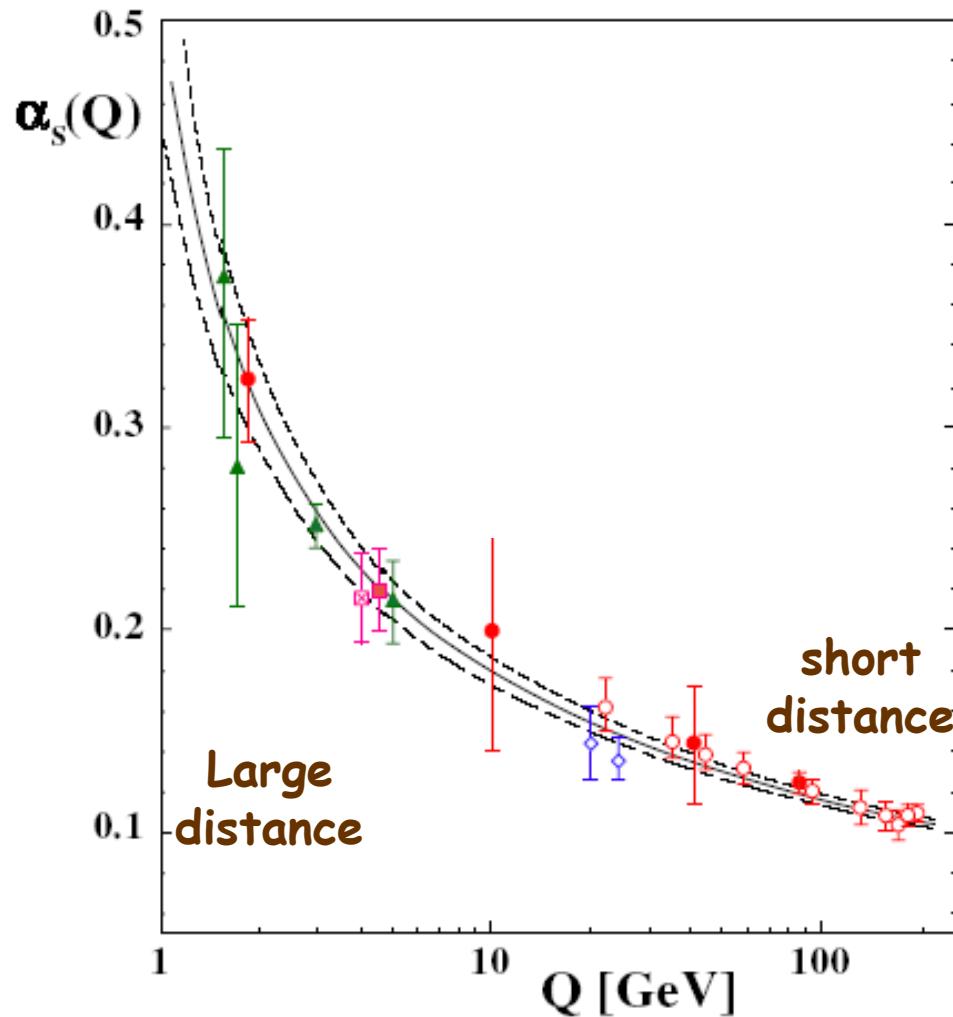


Test QCD with 3-jet events (& deep inelastic scattering)

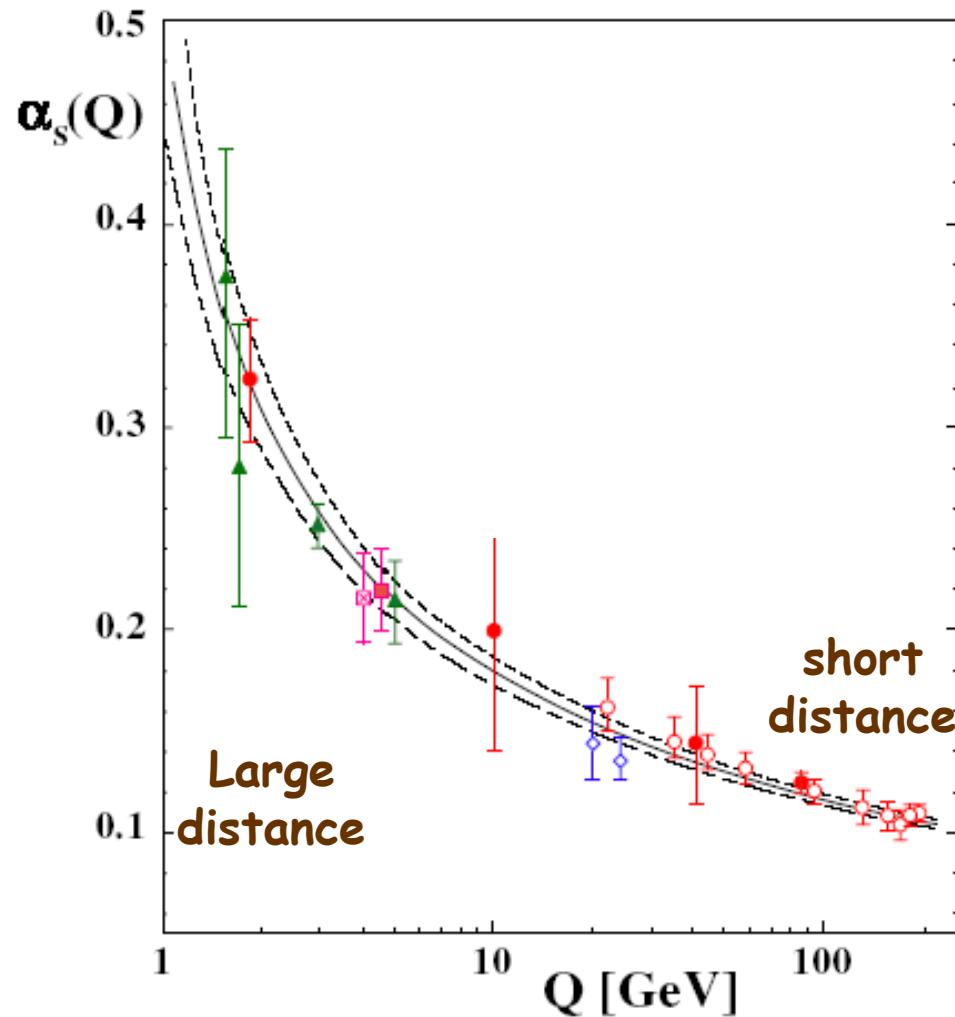


rate for 3-jet events should
decrease with E_{cm}

“running” α_s



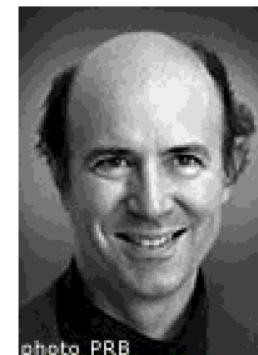
“running” α_s



David J. Gross



H. David
Politzer

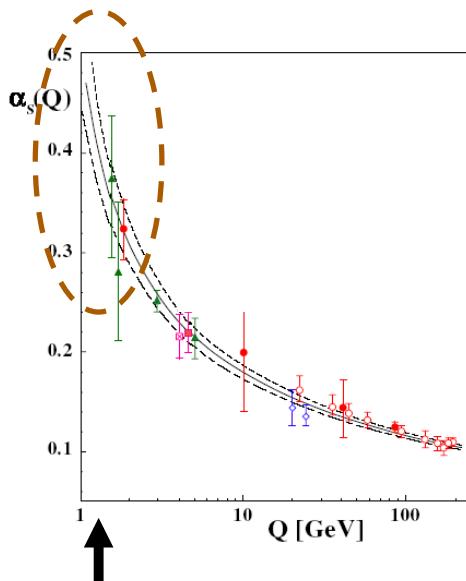


Frank Wilczek

2004 Nobel prize

The QCD particle spectrum hasn't been computed from 1st principles

Quark-binding into
hadrons occurs here
($Q \approx m_p \approx 140$ MeV)
 $\alpha_s(m_p) \sim 0.5$



perturbation theory can't be used

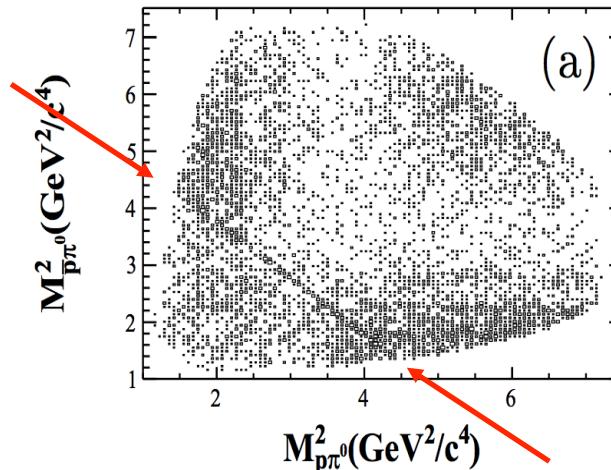
Theorists make "QCD-motivated" models
that must be tested by experiment

Summary (lecture 3)

- The $q\bar{q}$ =mesons and qqq =baryon prescriptions work well for the lowest-lying mesons & baryons, but fail otherwise
 - the mass hierarchy of the lowest-lying scalar mesons is opposite to expectations for $q\bar{q}$ =mesons
 - The masses of the $N^*(1440)$, the 1st excited state of the nucleon, and the $\Lambda(1405)$, the lowest excited state of the Λ , disagree with QM predictions for qqq =baryons
- The quark model seriously violates the Pauli Principle
- Quark model is superseded by Quantum ChromoDynamics
- Quarks come in 3 colors; color force is mediated by 8 gluons

Discussion/HW items

The BESIII $\psi' \rightarrow p\bar{p}\pi^0$ Dalitz plot at the right has a narrow diagonal band of events as indicated by red arrows. What do you think caused this?



The $\Lambda(1405)$ was seen via its $\Lambda(1405) \rightarrow \Sigma\pi$ decay mode, but is not seen in $\Lambda(1405) \rightarrow \Lambda\pi$ decays. Why?

The $a_0(980)$ decays to $\eta\pi$, but not $\pi\pi$, why is $a_0(980) \rightarrow \pi\pi$ a suppressed decay?