

# Dynamical FIMP DM with EWPT

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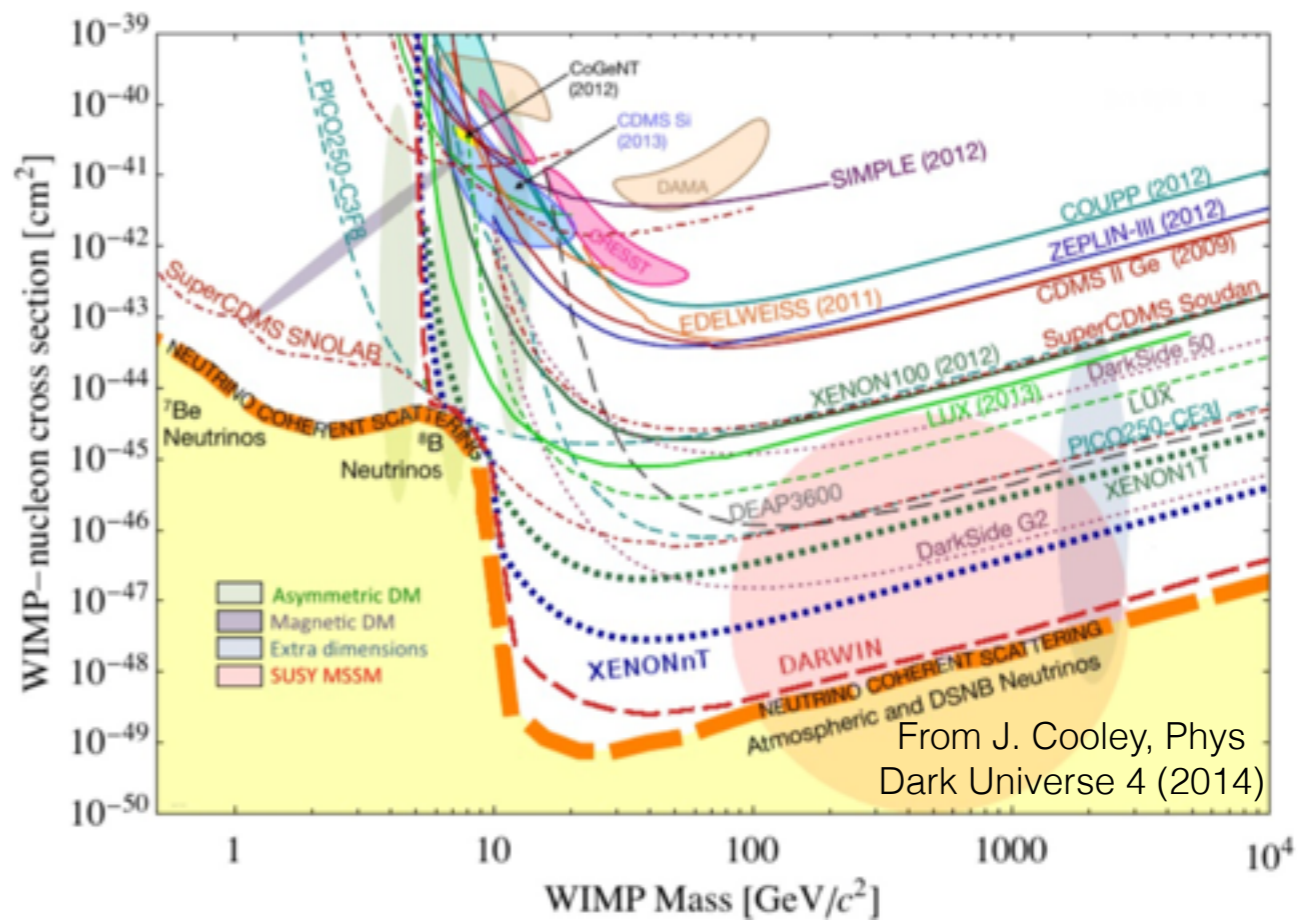
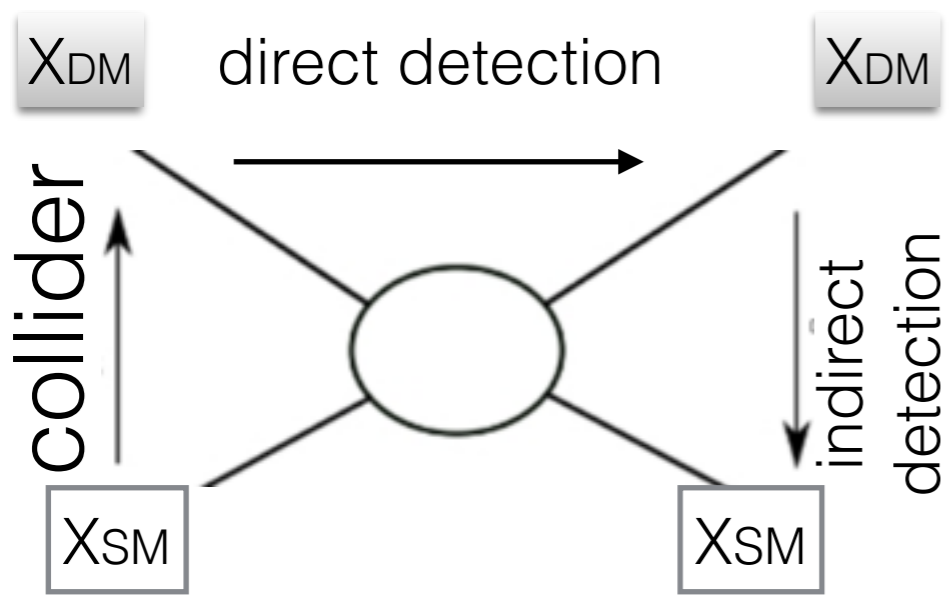
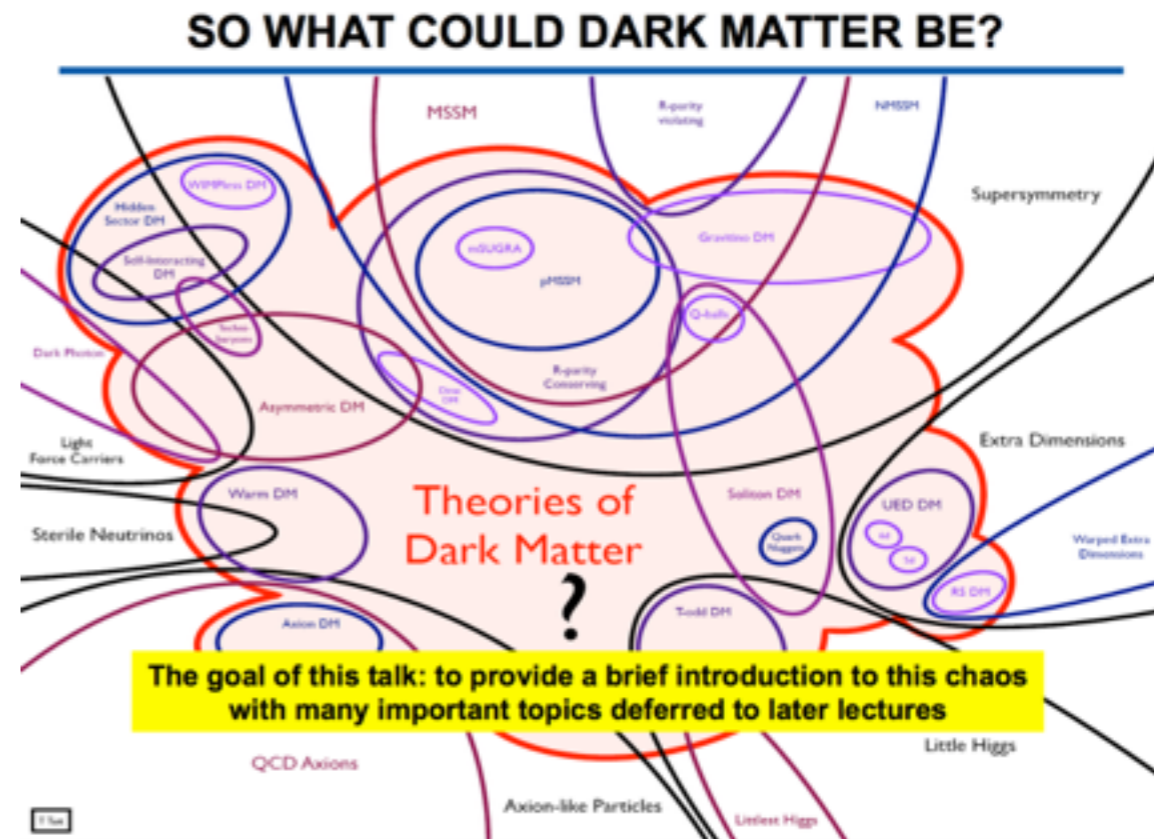
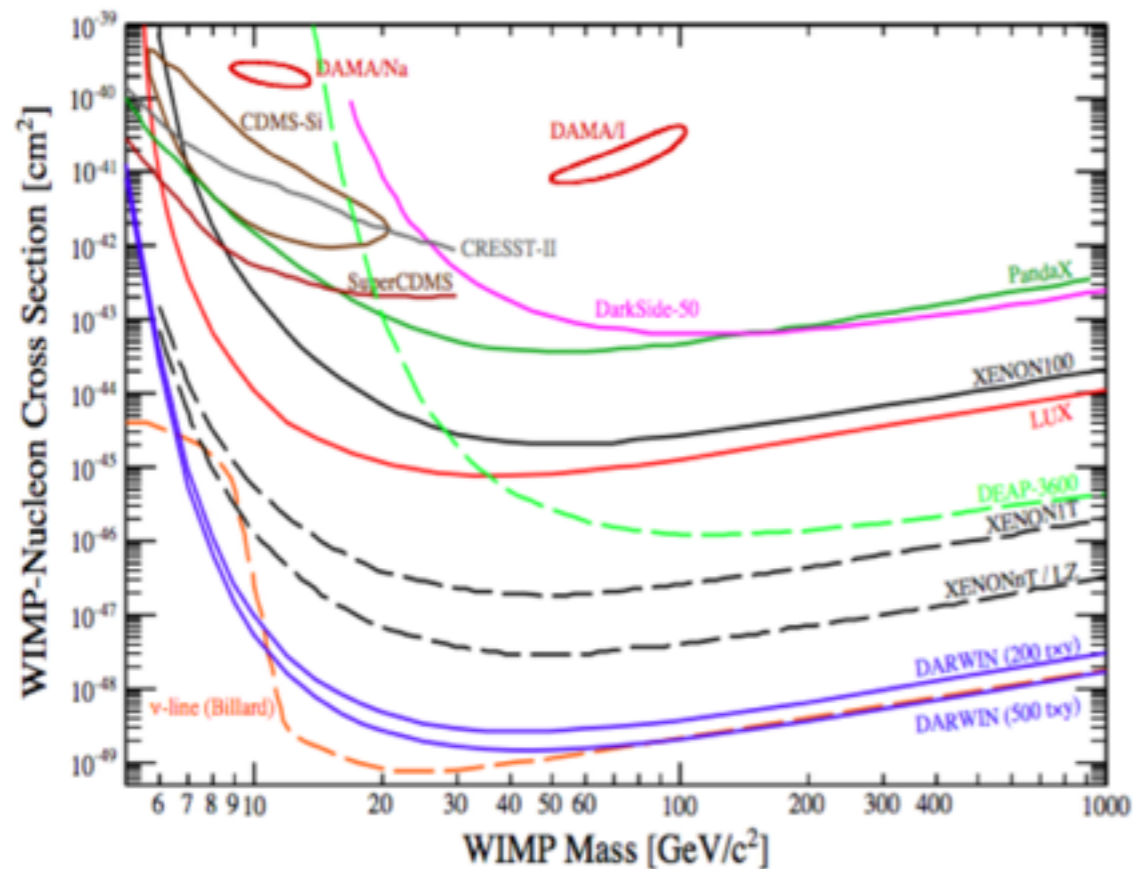
email: [lgbycl@cqu.edu.cn](mailto:lgbycl@cqu.edu.cn), [ligongbian@gmail.com](mailto:ligongbian@gmail.com)

Based on arXiv:1811.03279  
with 刘学文

# Outline

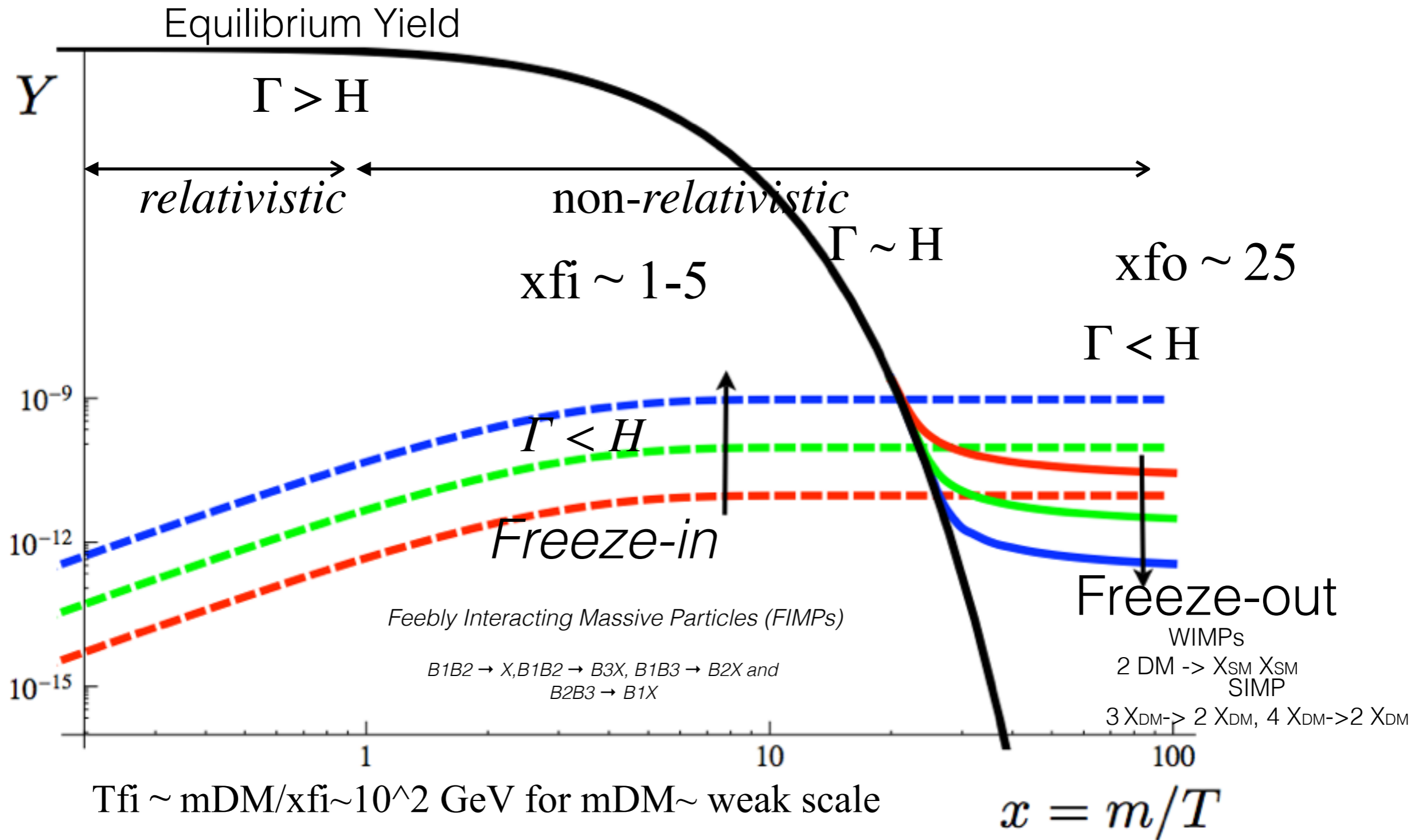
- Motivation
- The scotogenic Model
- The thermal corrected masses
- Dynamical DM
- Gravitational Waves
- Collider searches

# WIMPs under tension



From J. Cooley, Phys Dark Universe 4 (2014)

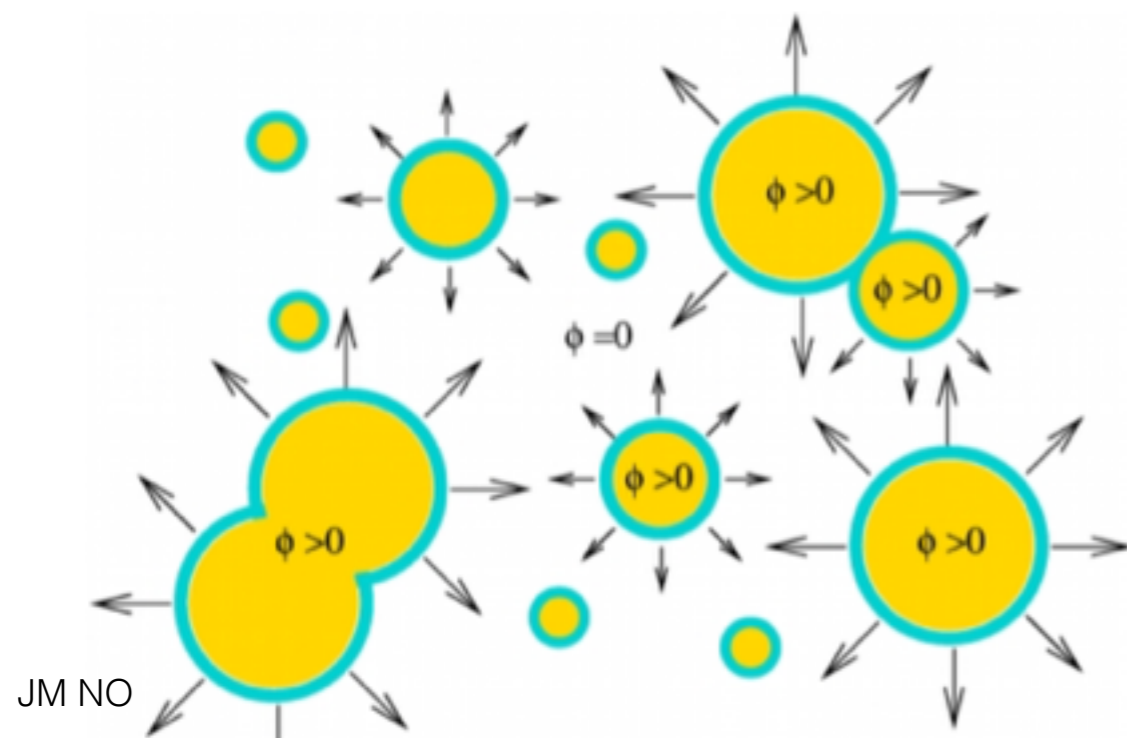
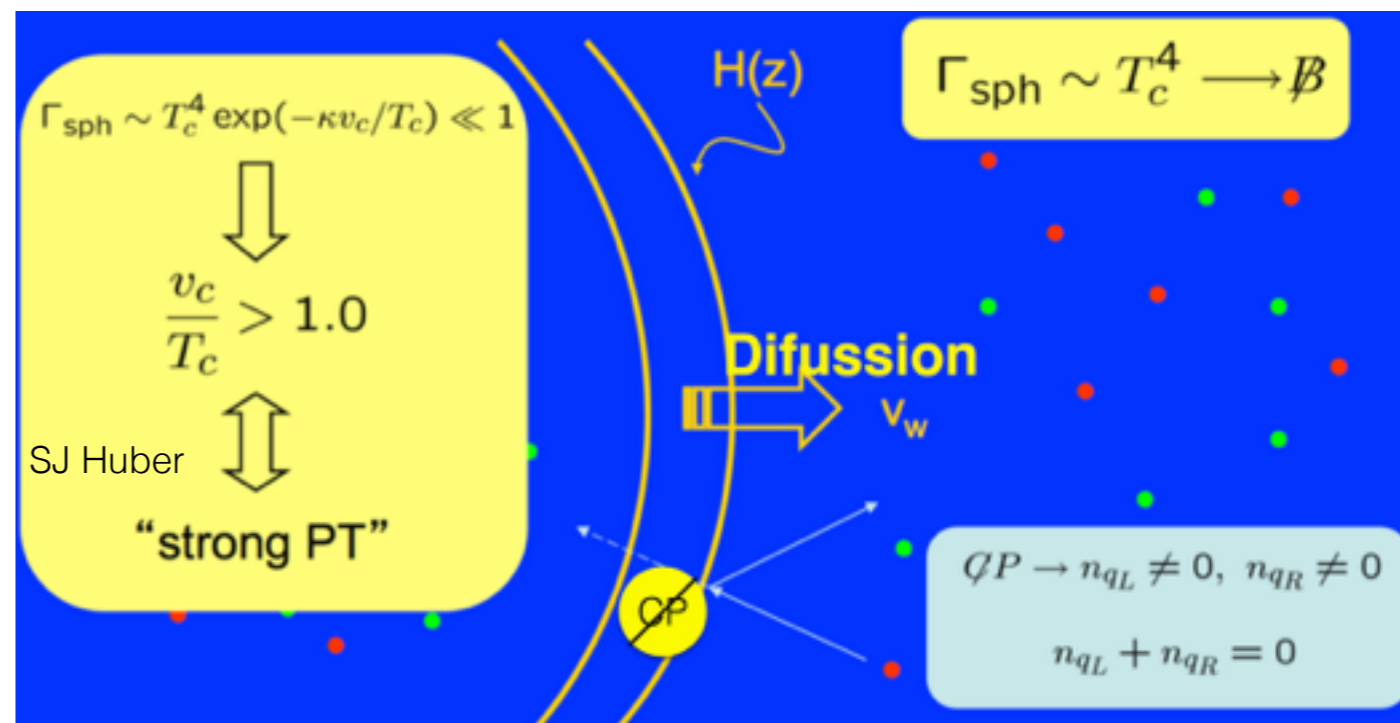
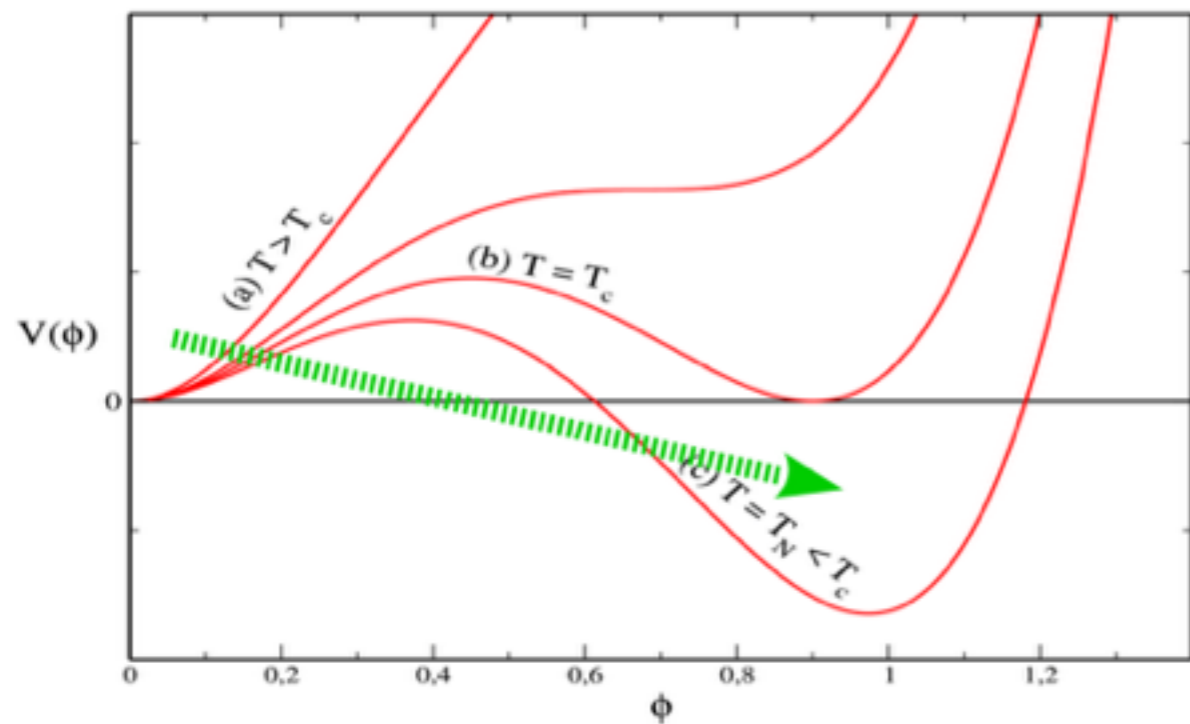
# Freeze-in and Freeze-out



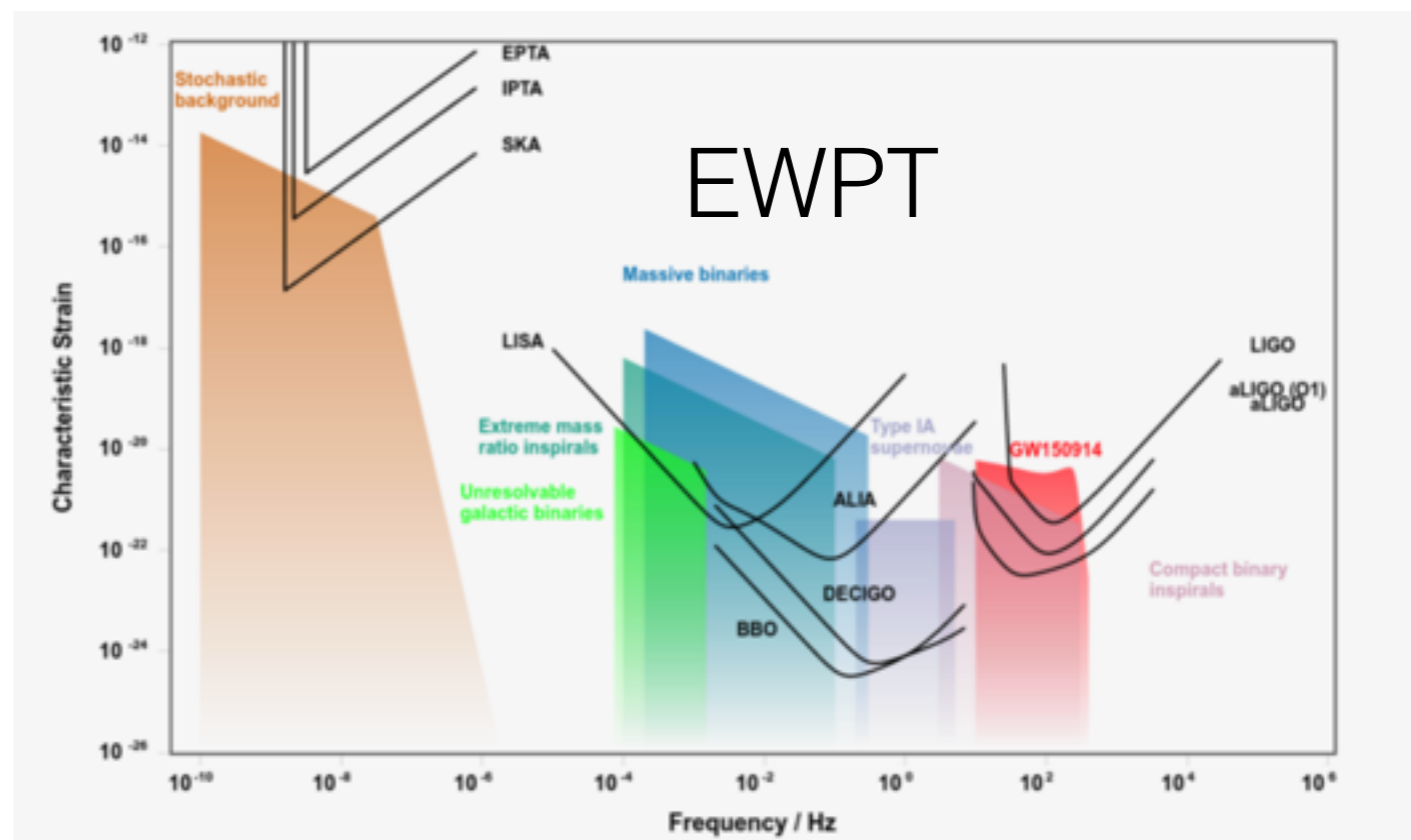
$T_n \sim 10^2 \text{ GeV}$

# EWSB

h

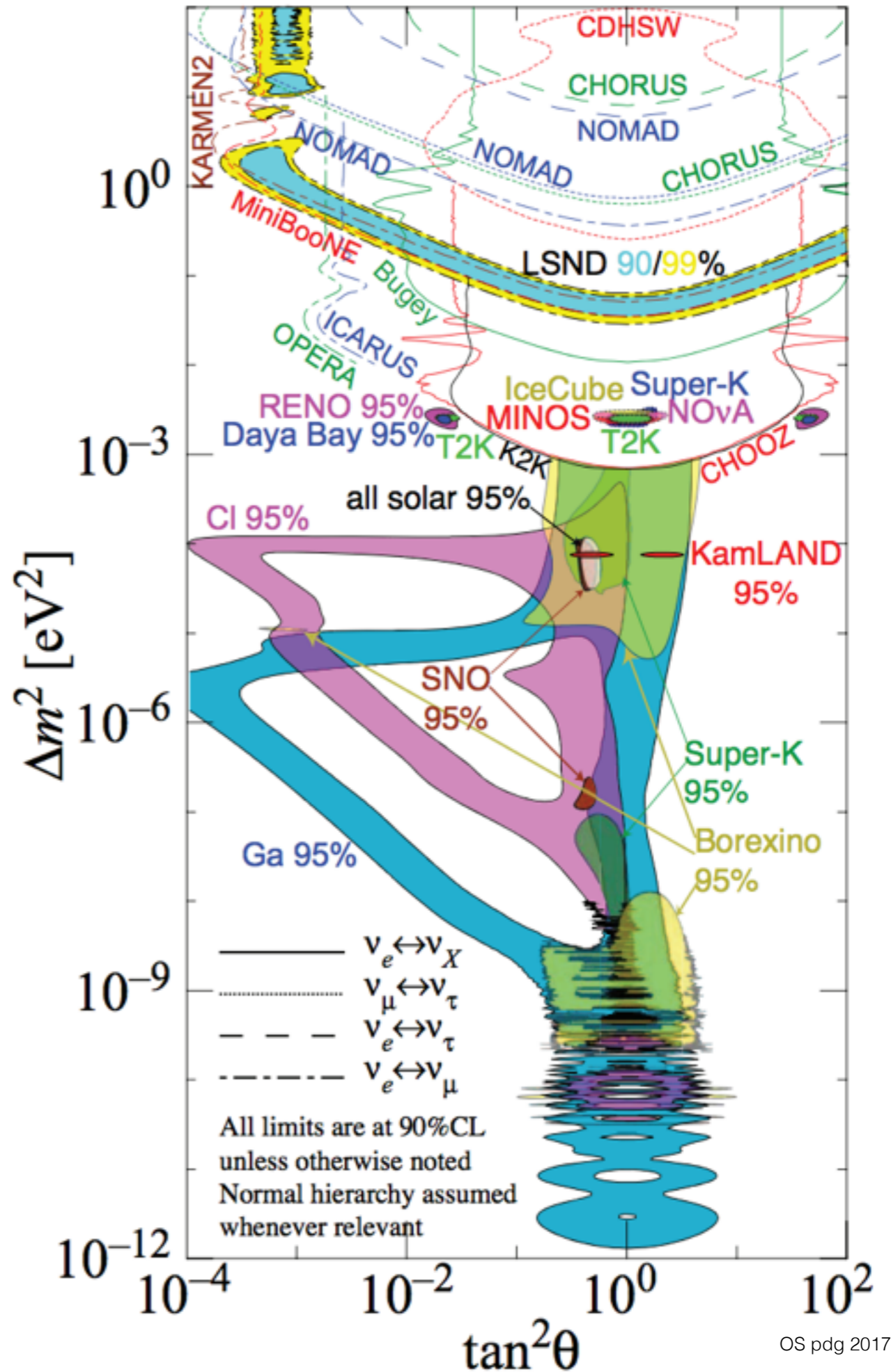
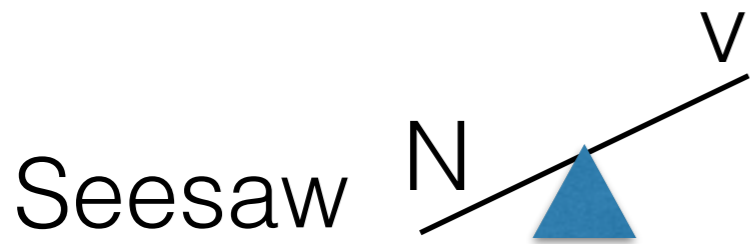
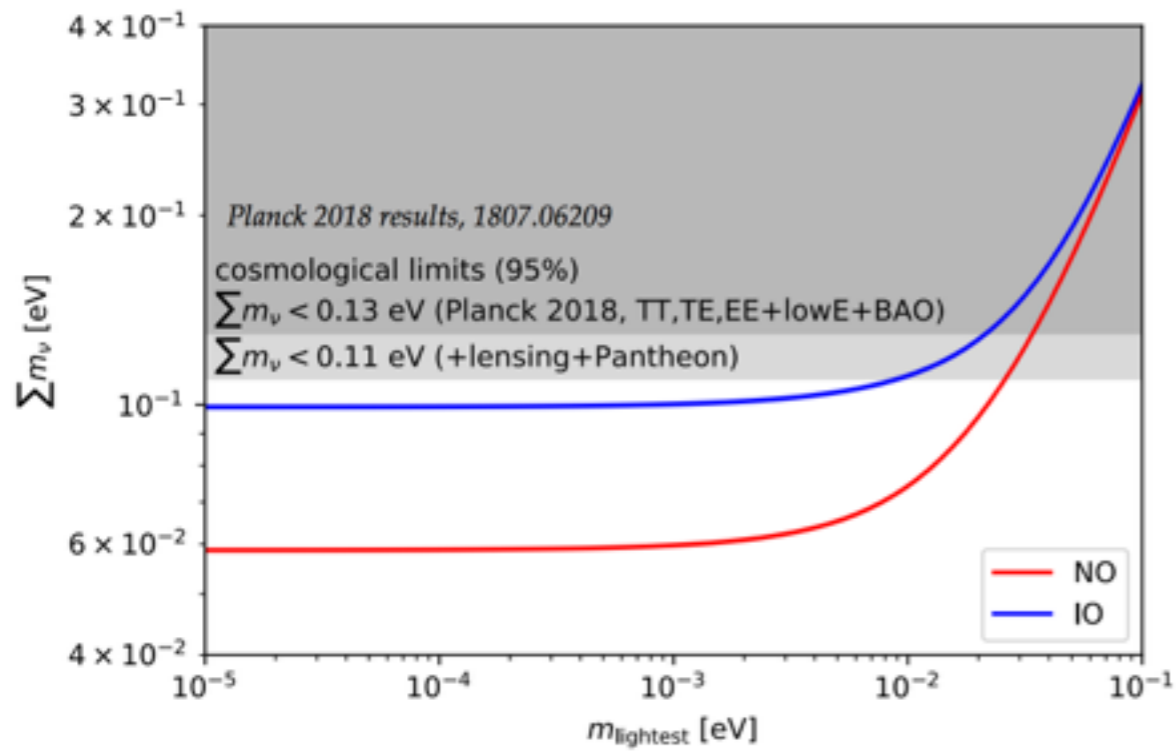


JM NO

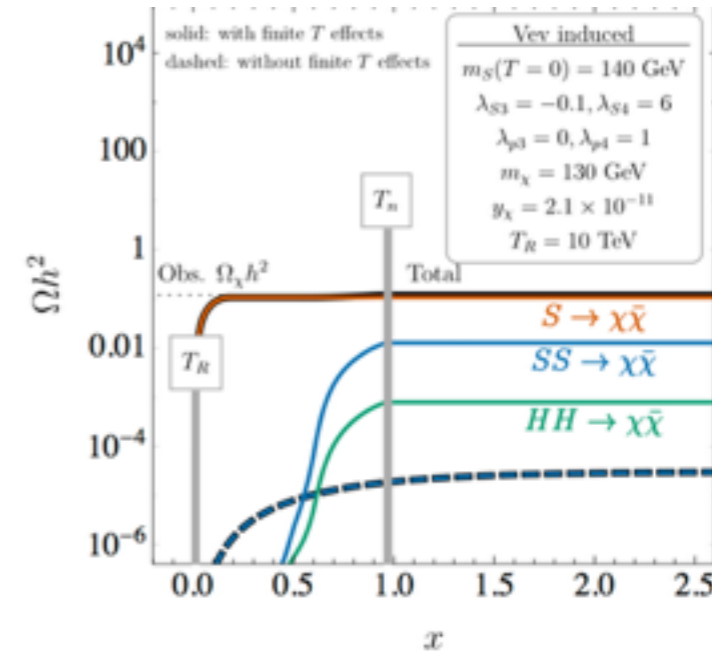
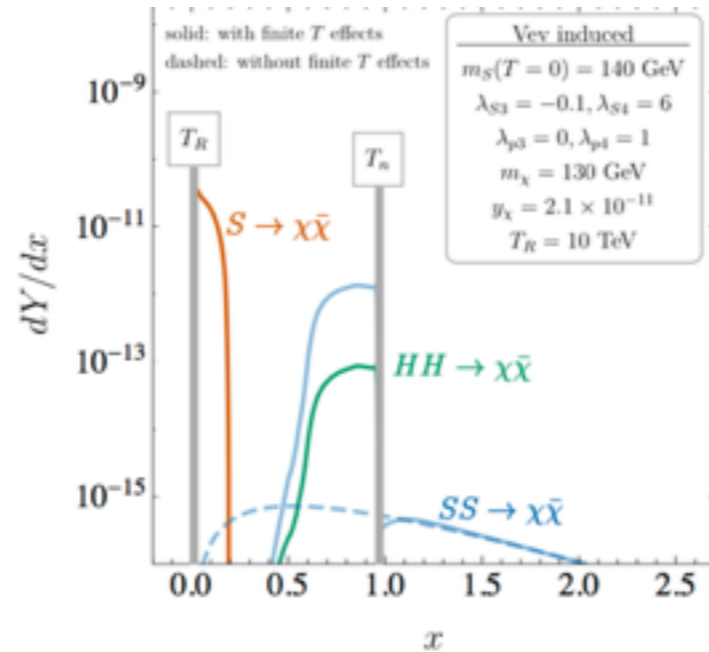
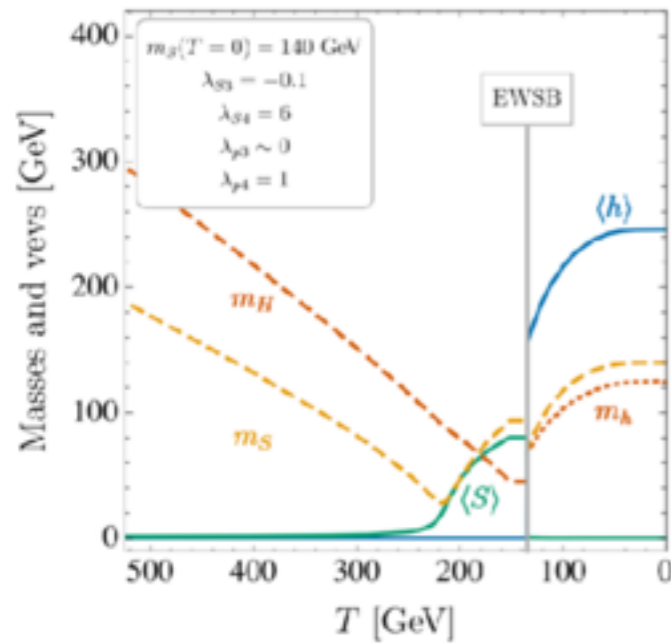




# Massive neutrinos



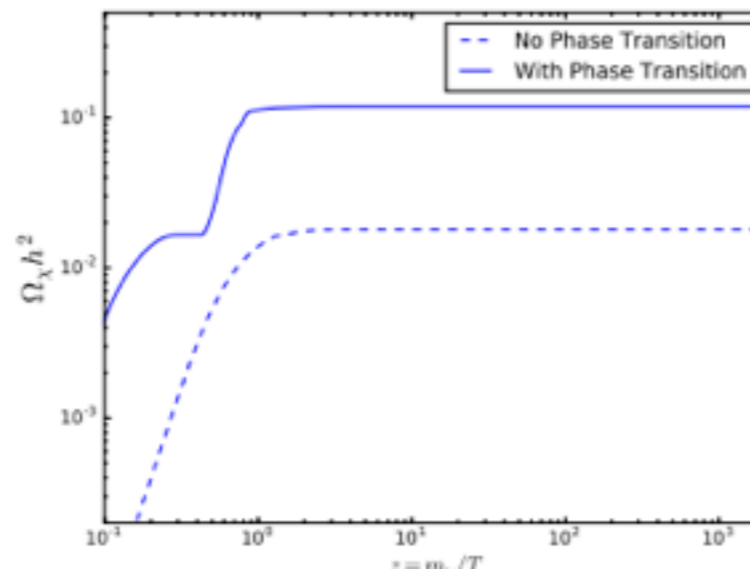
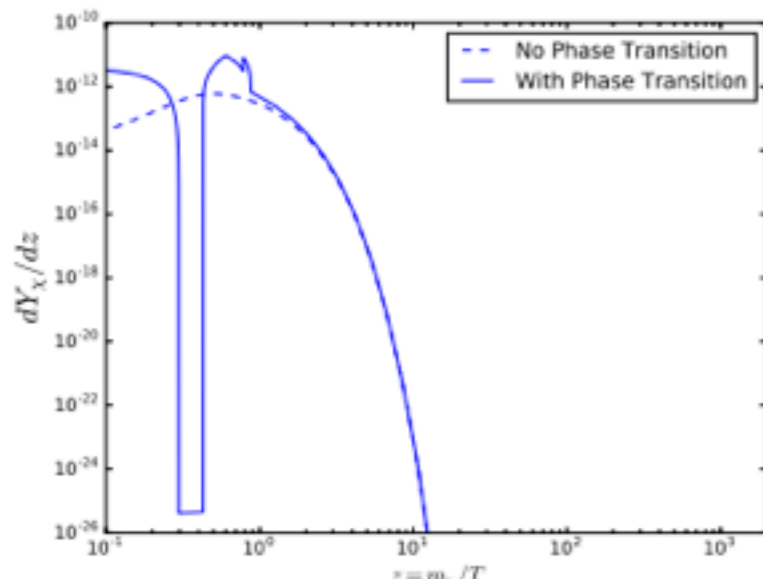
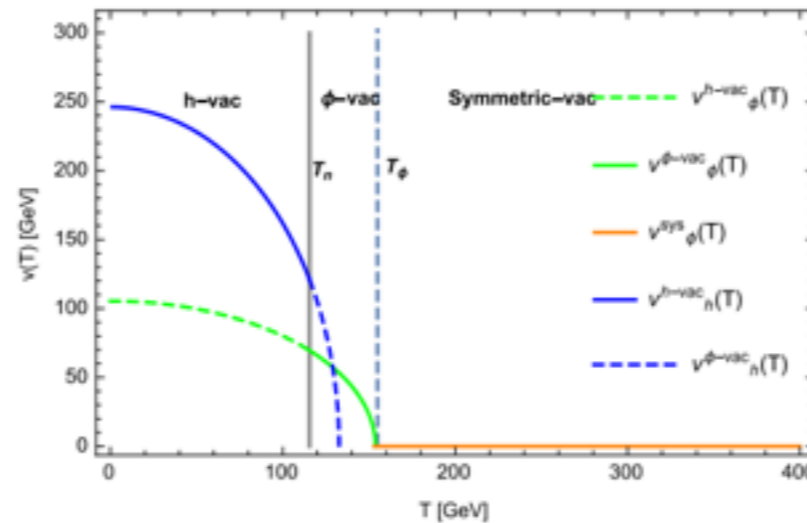
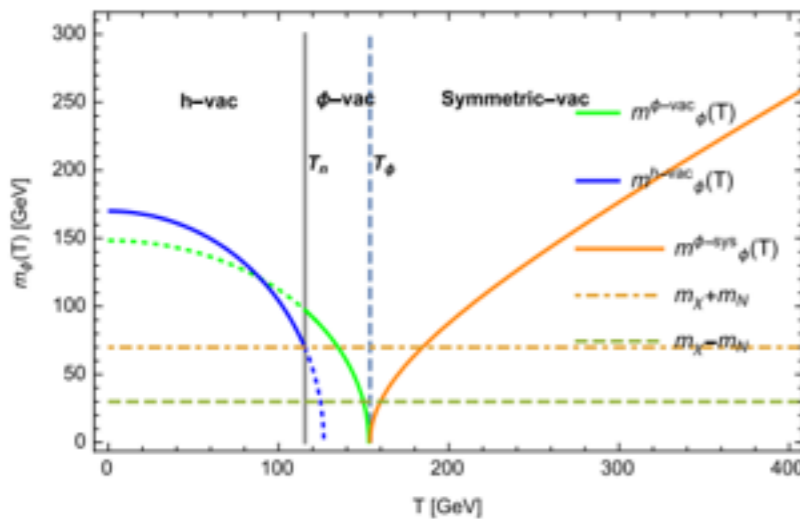
# Previous studies



1712.03962, Michael J. Baker et al.

Amplified effects:  
larger thermal  
masses before PT

temporarily open of  
decay channel



1810.03172, L. Bian, Y. Tang

# The Scotogenic model

$$\mathcal{L}_Y = f_{\alpha\kappa} \bar{N}_\kappa \left( \frac{1 - \gamma_5}{2} \right) (\nu_\alpha H_0 - l_\alpha H^+) + h_{\kappa\beta} \bar{N}_\kappa \left( \frac{1 + \gamma_5}{2} \right) \nu_\beta S + \text{h.c.}$$

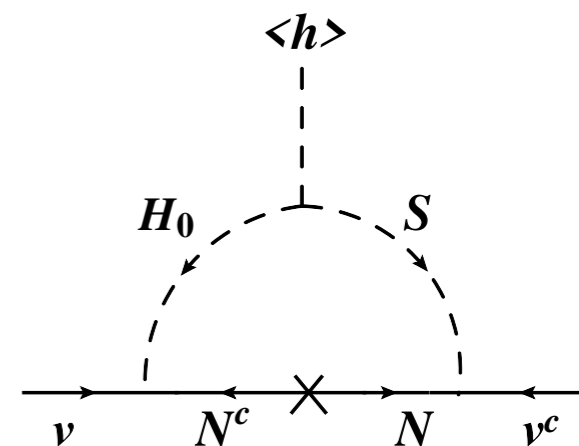
FIMP  $f \ll 1 \rightarrow$  avoiding flavor-changing charged-lepton radiative decays,  
E. Molinaro, C. E. Yaguna and O. Zapata, JCAP 1407, 015 (2014)

$h$ : not constrained by flavor-changing charged-lepton radiative decays,

Y. Farzan and E. Ma, Phys. Rev. D 86, 033007 (2012)

The one-loop Dirac neutrino mass matrix is given by,

$$(M_\nu)_{\alpha\beta} = \frac{\sin 2\theta}{32\sqrt{2}\pi^2} \sum_\kappa f_{\alpha\kappa} h_{\kappa\beta} m_{N_\kappa} \left[ \frac{m_\chi^2}{m_\chi^2 - m_{N_\kappa}^2} \log \frac{m_\chi^2}{m_{N_\kappa}^2} - \frac{m_H^2}{m_H^2 - m_{N_\kappa}^2} \log \frac{m_H^2}{m_{N_\kappa}^2} \right]$$



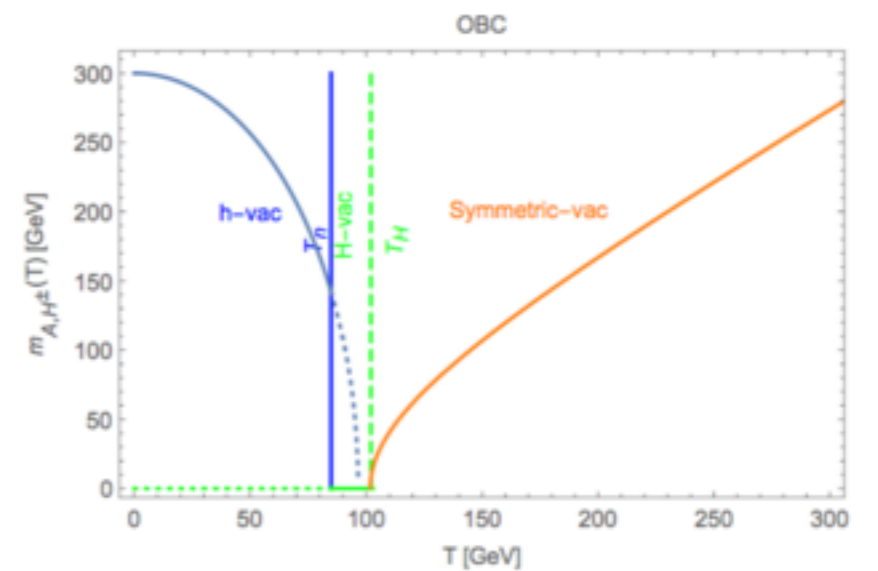
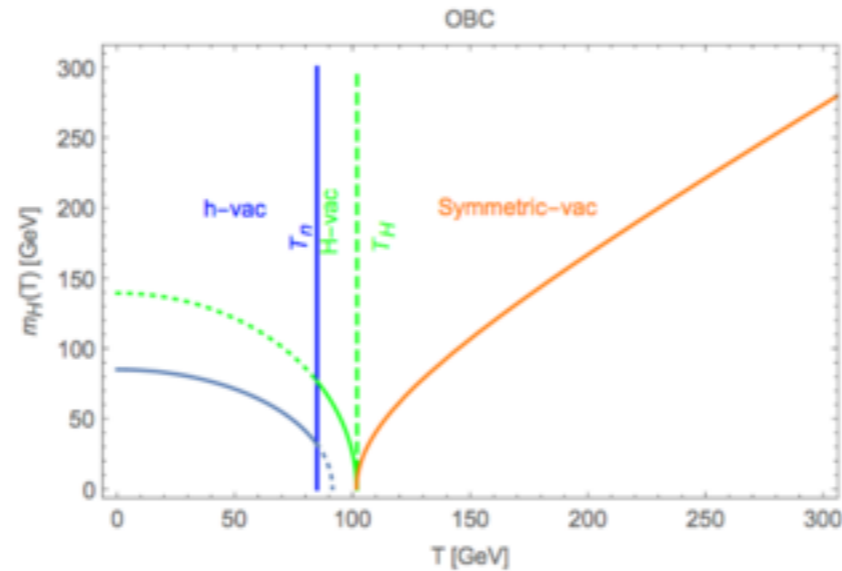
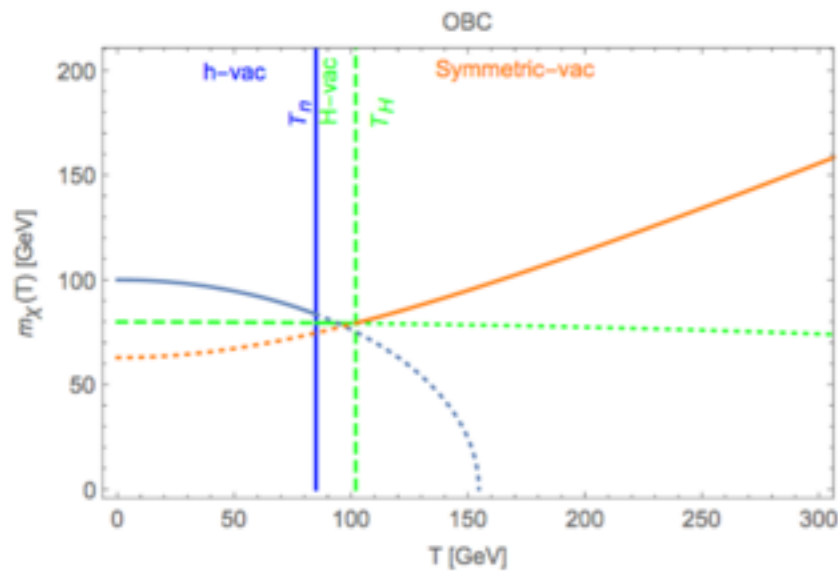
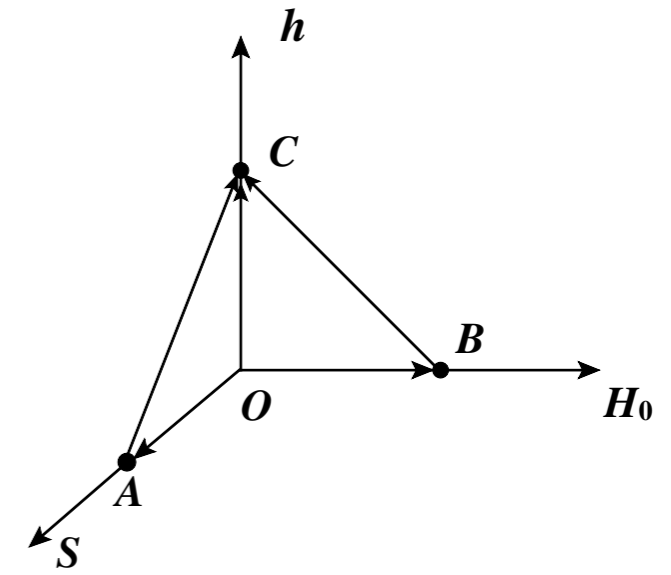
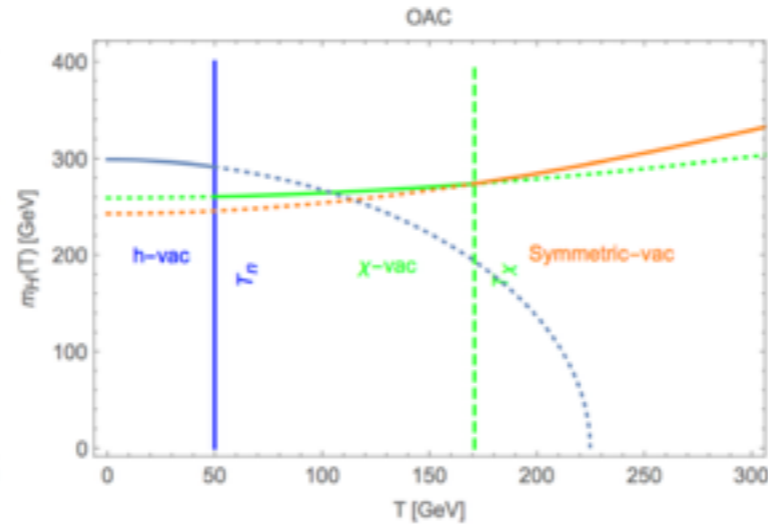
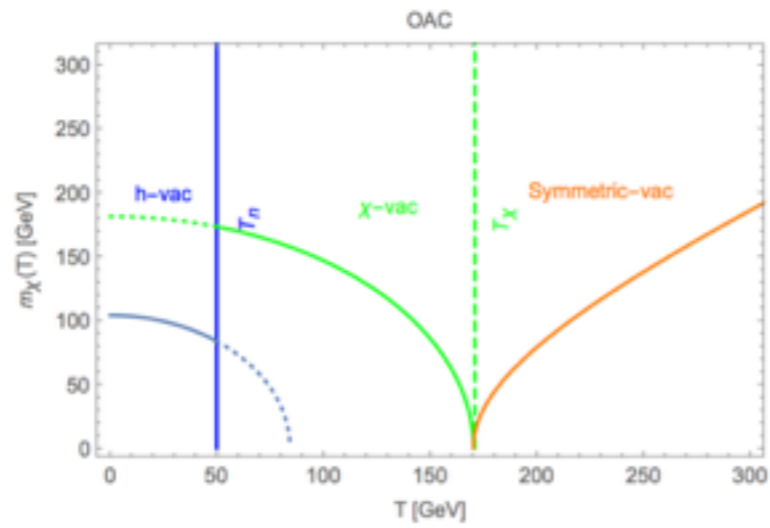
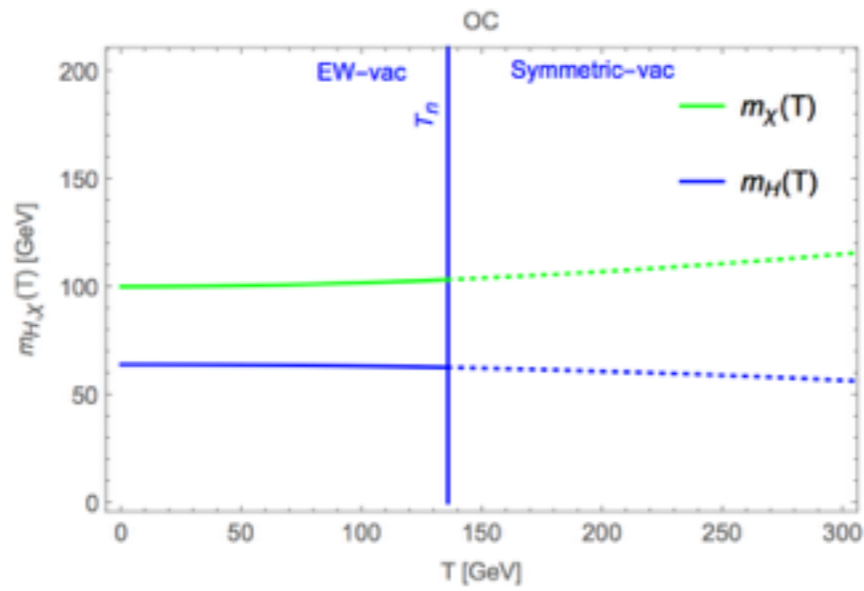
$$\begin{aligned} V = & \mu_\Phi^2 \Phi^\dagger \Phi + \mu_\eta^2 \eta^\dagger \eta + \frac{\mu_S^2}{2} S^2 + \lambda_1 (\Phi^\dagger \Phi)^2 + \lambda_2 (\eta^\dagger \eta)^2 + \lambda_3 (\Phi^\dagger \Phi) (\eta^\dagger \eta) \\ & + \lambda_4 (\eta^\dagger \Phi) (\Phi^\dagger \eta) + \frac{1}{2} \lambda_5 [(\eta^\dagger \Phi)^2 + (\Phi^\dagger \eta)^2] + \frac{\lambda_s}{4} S^4 + \lambda_{s\phi} S^2 (\Phi^\dagger \Phi) \\ & + \lambda_{s\eta} S^2 (\eta^\dagger \eta) + \mu_{\text{soft}} S (\Phi^\dagger \eta + \eta^\dagger \Phi), \end{aligned}$$

$$\Phi = \begin{pmatrix} G^+ \\ \frac{1}{\sqrt{2}}(v + h + iG^0) \end{pmatrix}, \quad \eta = \begin{pmatrix} H^+ \\ \frac{1}{\sqrt{2}}(H_0 + iA) \end{pmatrix}, \quad \begin{pmatrix} S \\ H_0 \end{pmatrix} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} \chi \\ H \end{pmatrix}$$

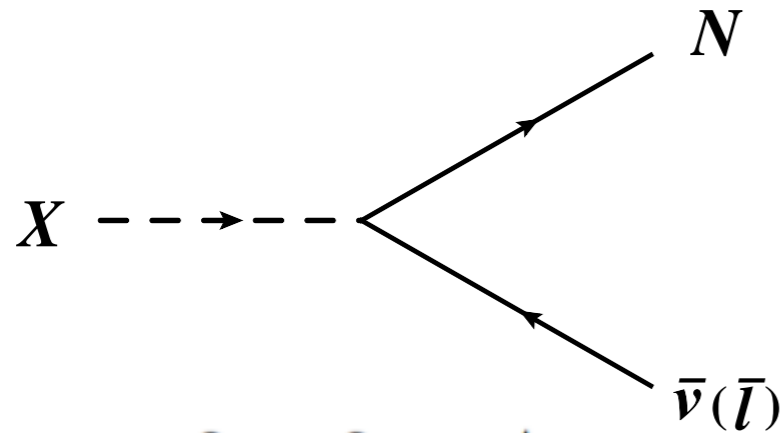
$$\mathbf{M}^2 = \begin{pmatrix} 2\mu_S^2 + v^2 \lambda_{s\phi} & v\mu_{\text{soft}} & 0 \\ v\mu_{\text{soft}} & \mu_\eta^2 + v^2 \lambda_L & 0 \\ 0 & 0 & \mu_\eta^2 + v^2 \lambda_S \end{pmatrix}$$



# PT patterns and dynamical thermal masses

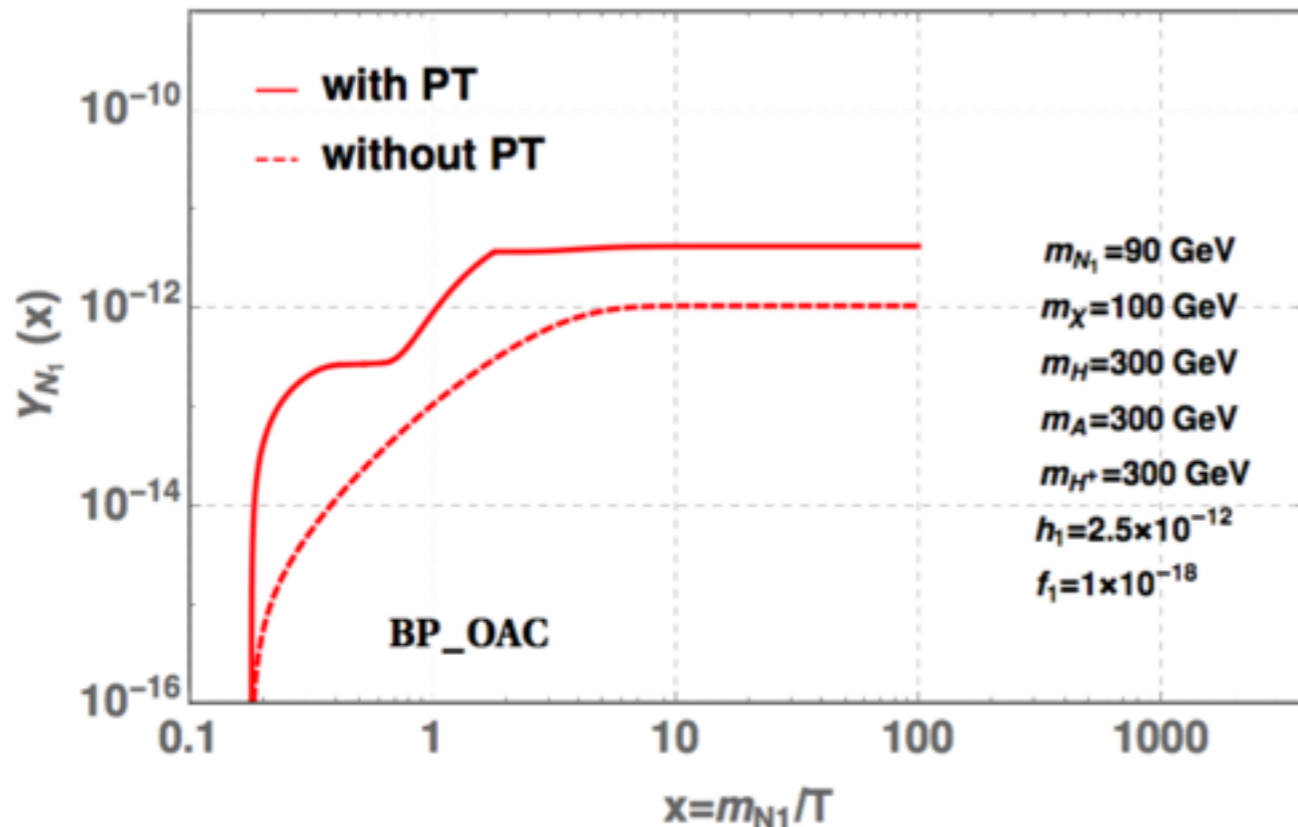
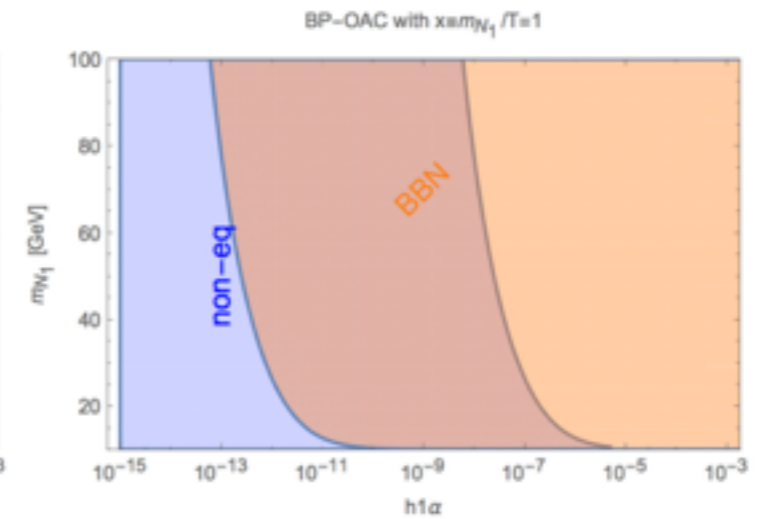
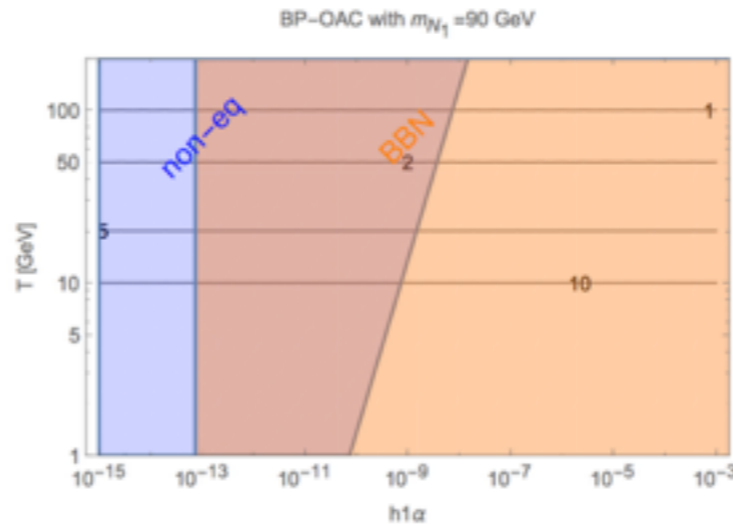


# OAC pattern PT DDM



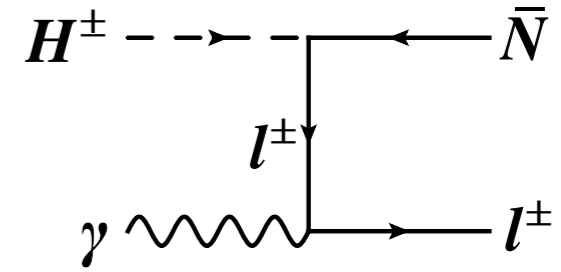
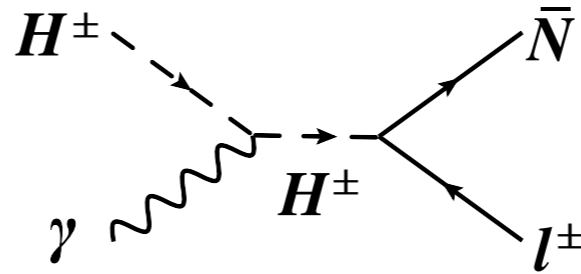
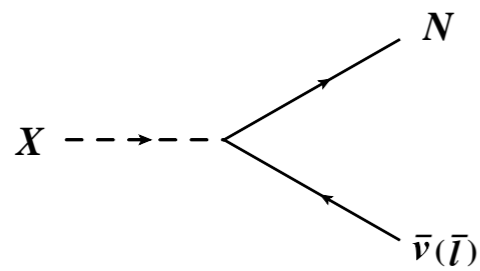
$$X = H^0, A^0, H^\pm, \chi$$

$X$  lives in bath



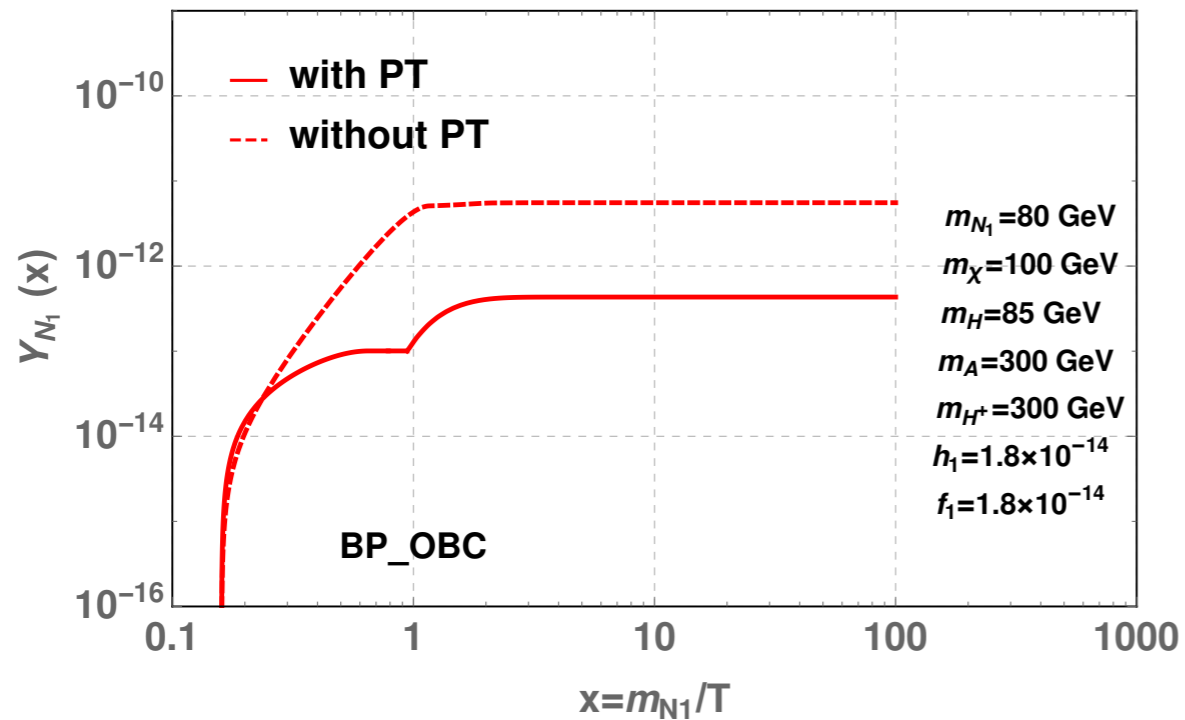
Amplified effects:  
 larger thermal masses before PT  
 temporarily open of decay channel

# OBC pattern PT DDM



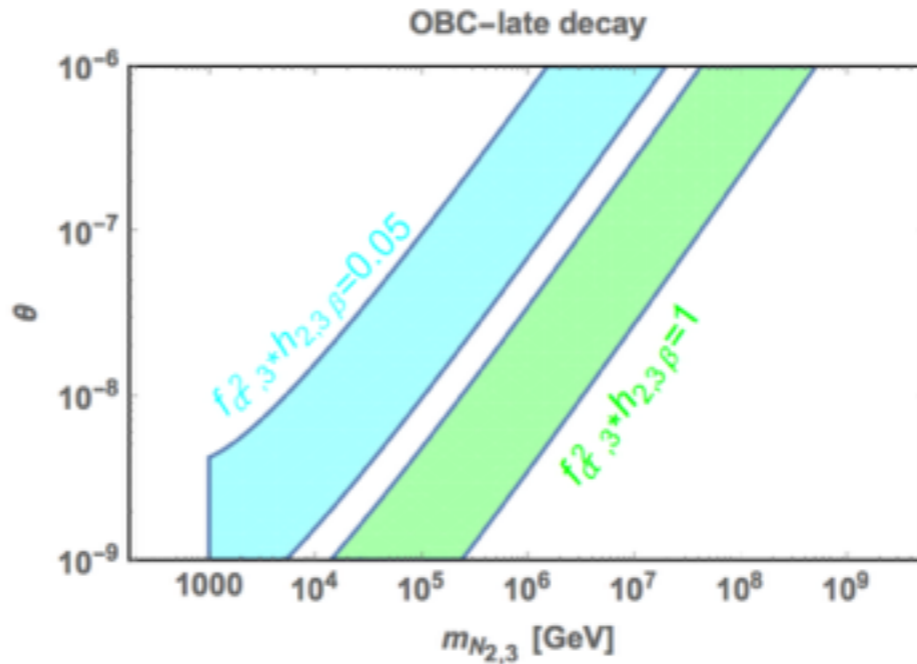
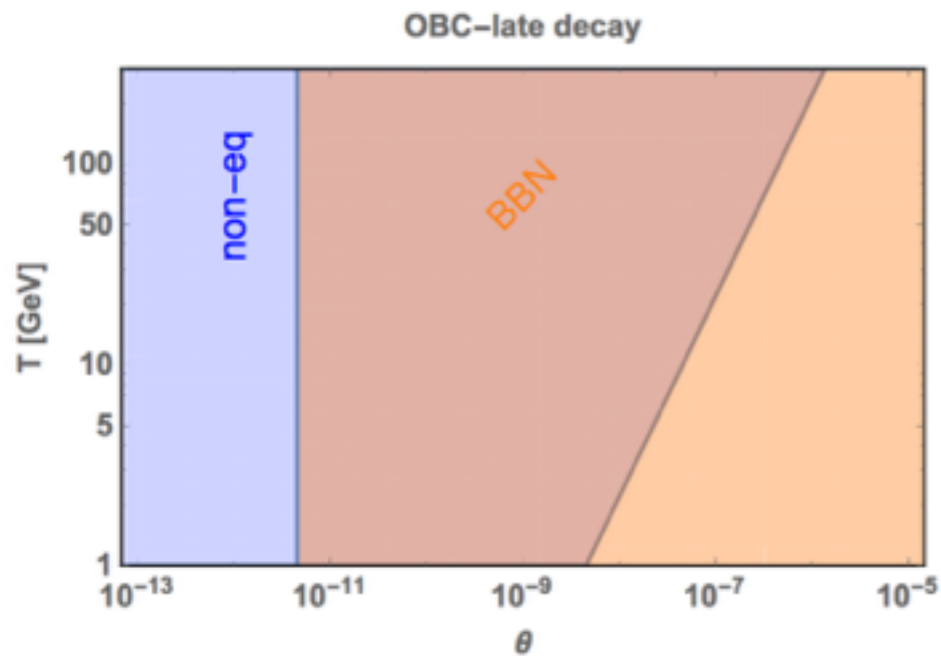
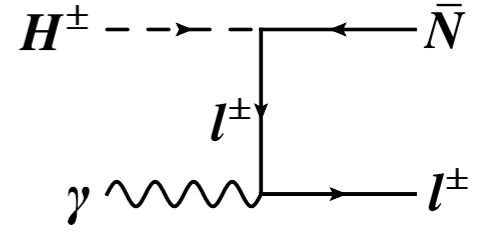
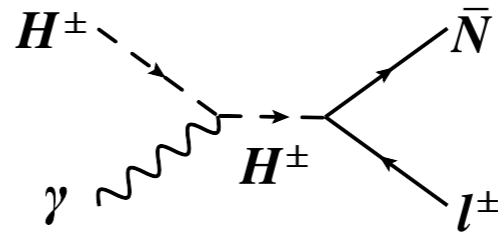
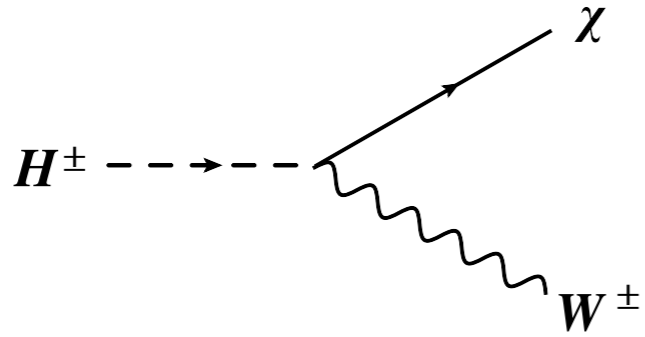
$$X = H^0, A^0, H^\pm, \chi$$

X lives in bath

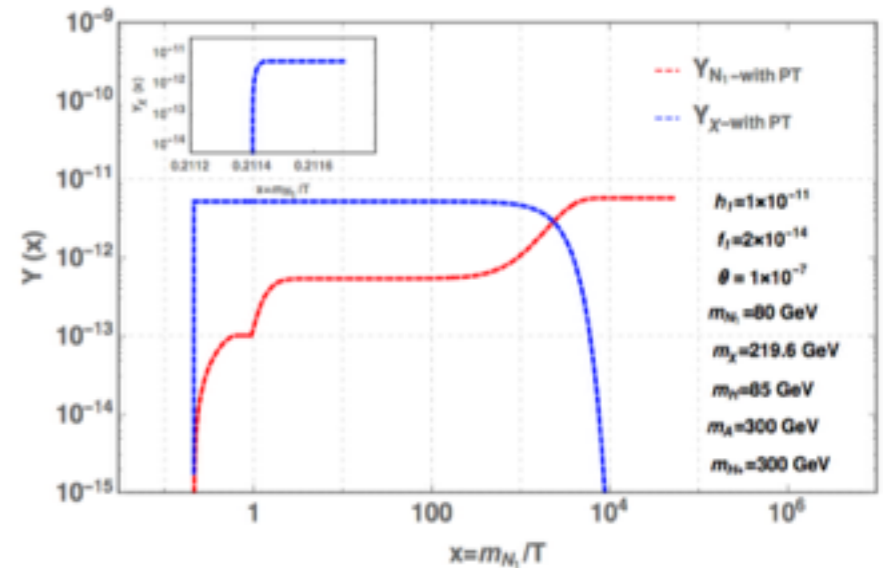
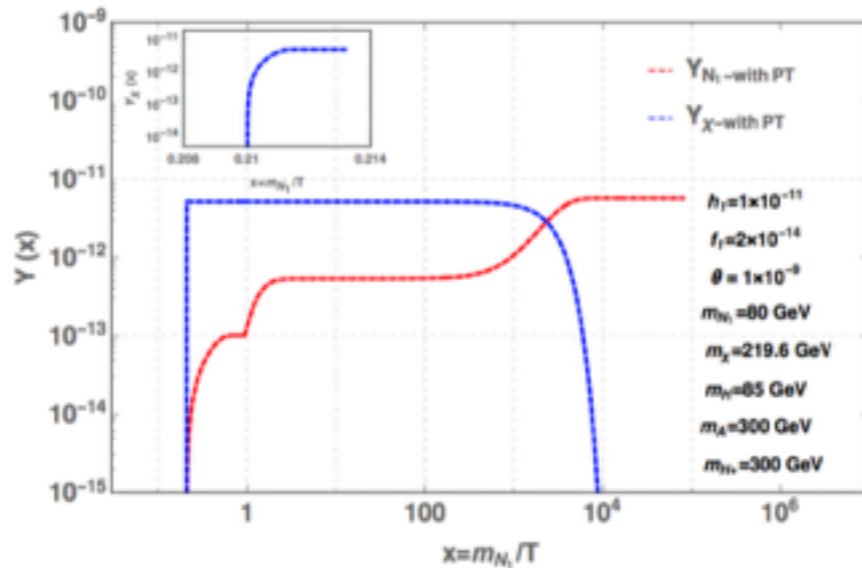
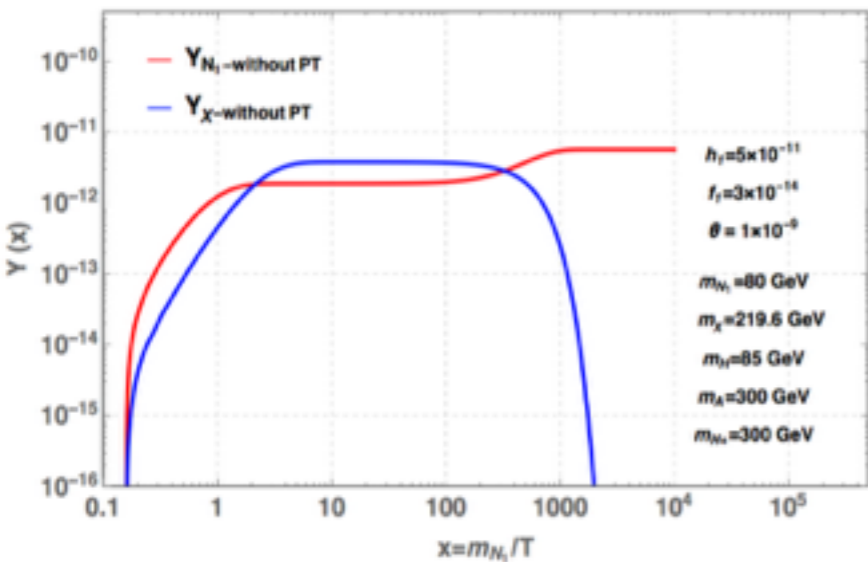


reduction effects:  
smaller thermal  
masses before PT  
temporarily open of  
decay channel

# OBC pattern PT DDM-late decay

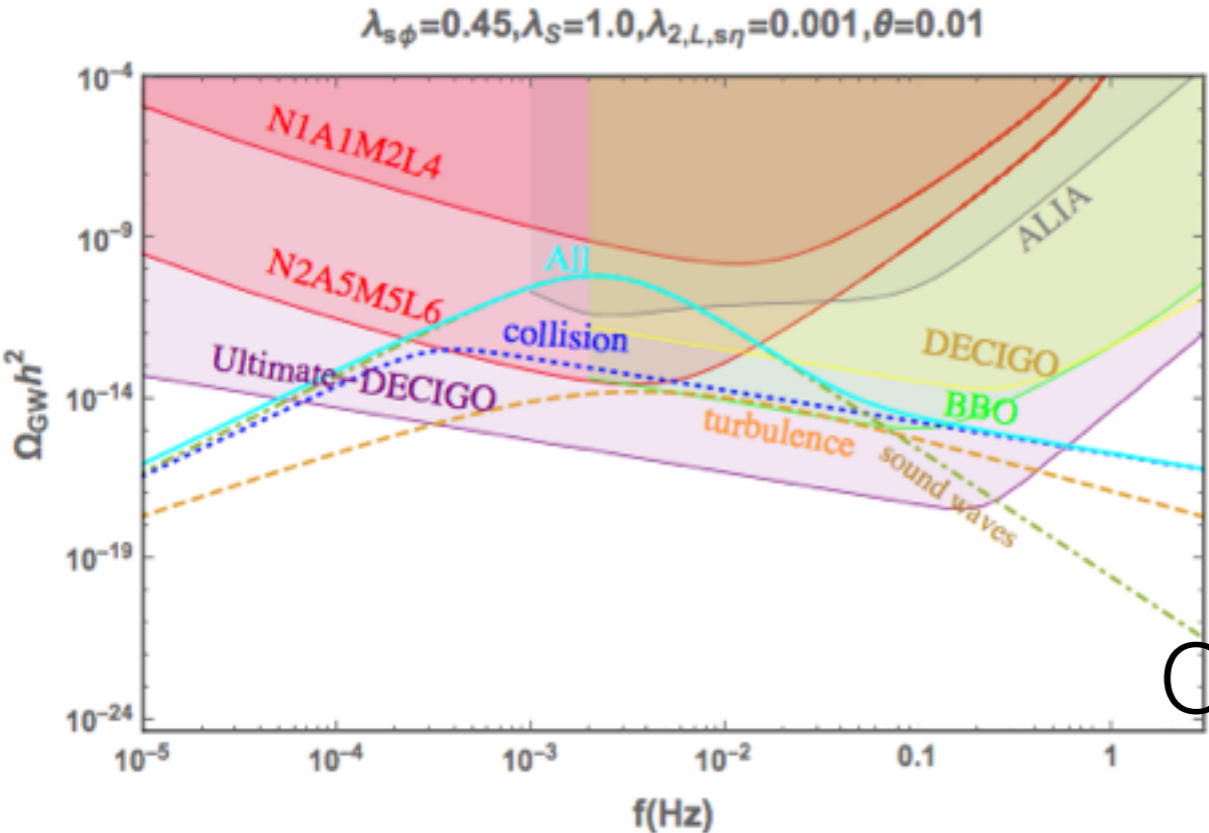


reduction effects:  
smaller thermal masses before PT  
temporarily open of decay channel at high  $T$

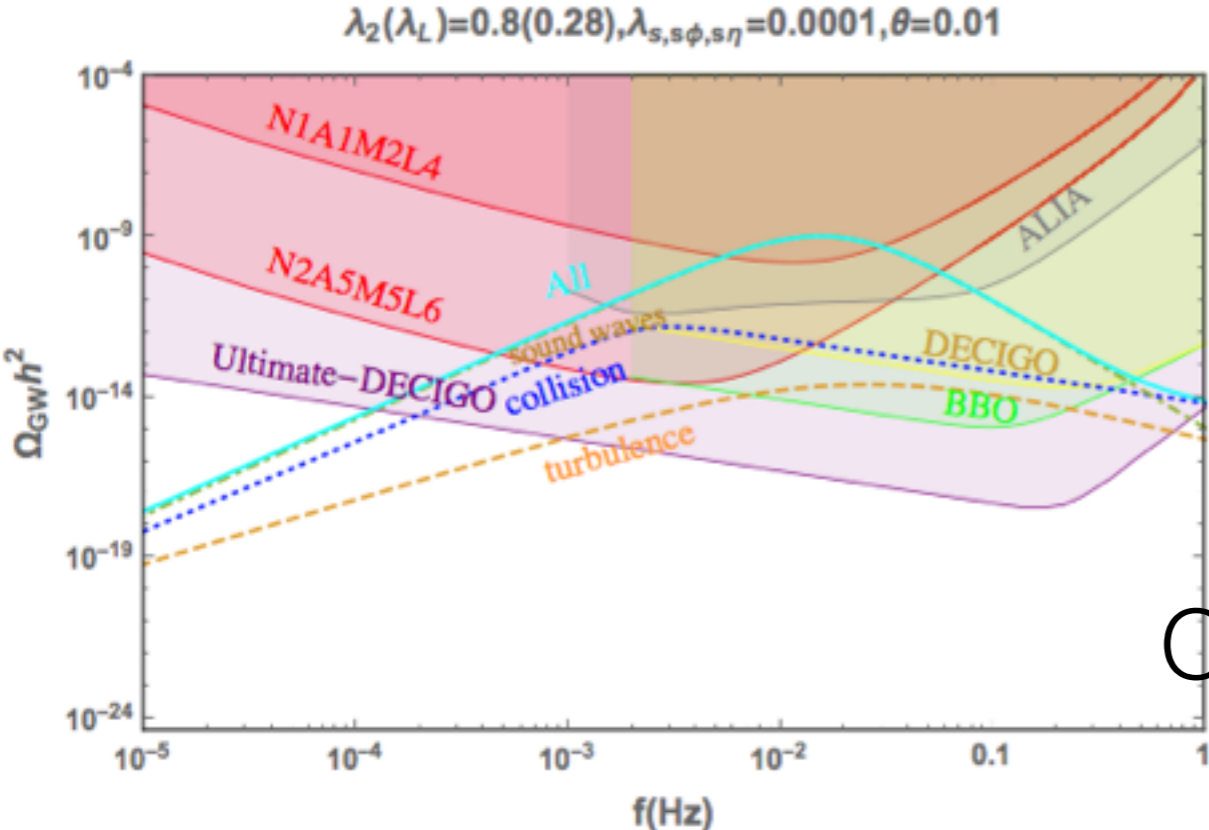
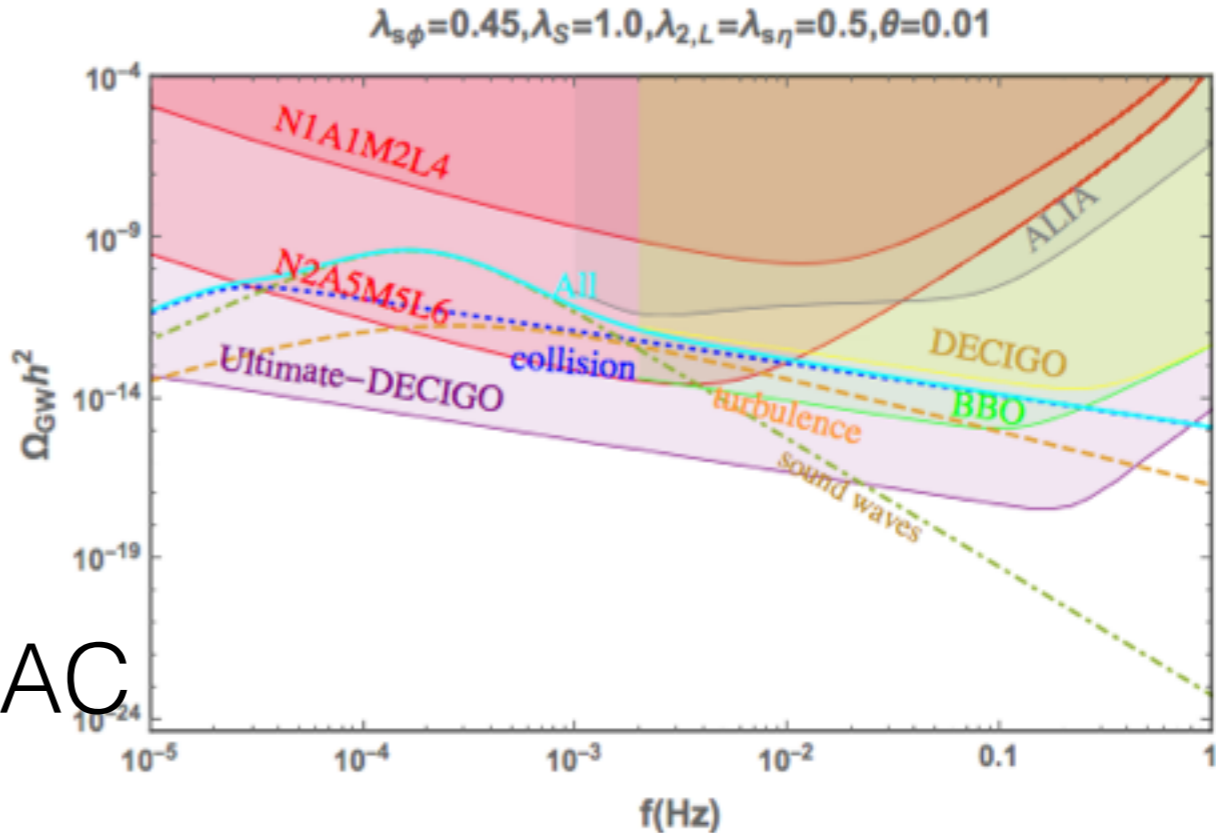




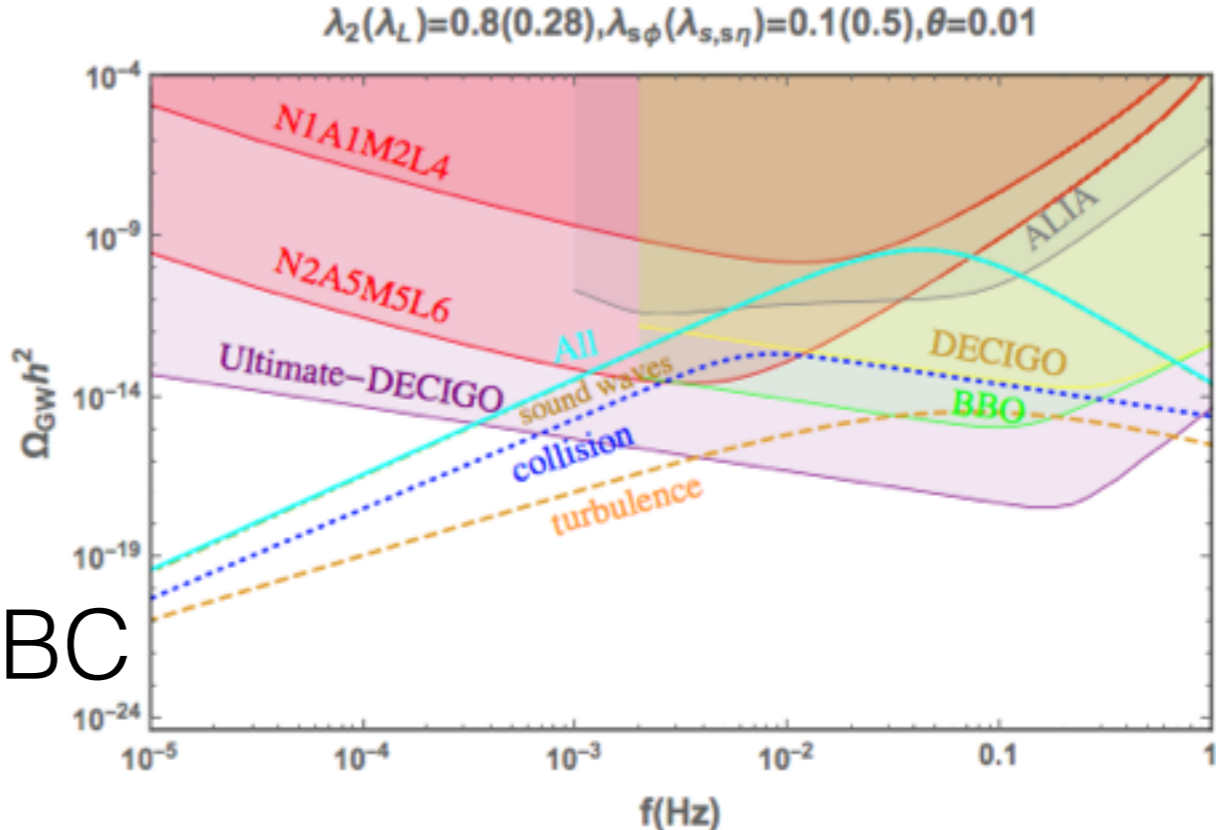
# GWs from 1st EWPT



OAC



OBC



# GWs

$$\alpha \sim \frac{\text{latent heat}}{\text{radiation energy}} \sim \frac{T \partial_T V(T)}{a g_* T^4}$$

$$v_b \simeq \frac{1/\sqrt{3} + \sqrt{\alpha^2 + 2\alpha/3}}{1 + \alpha}, \quad \kappa \simeq \frac{0.715\alpha + \frac{4}{27}\sqrt{3\alpha/2}}{1 + 0.715\alpha}$$

Bubble size  $\langle R \rangle \sim v_b \tau \sim \frac{v_b}{\beta}$        $\frac{\beta}{H_*} = T_* \frac{d}{dT} \left( \frac{S_3}{T} \right) \Big|_{T_*}$

β reflect the duration of the phase transition

$$\Omega_{\text{col}} h^2 = 1.67 \times 10^{-5} \left( \frac{H_*}{\beta} \right)^2 \left( \frac{\kappa \alpha}{1 + \alpha} \right)^2 \left( \frac{100}{g_*} \right)^{1/3} \left( \frac{0.11 v_b^3}{0.42 + v_b^2} \right) \frac{3.8 (f/f_{\text{env}})^{2.8}}{1 + 2.8 (f/f_{\text{env}})^{3.8}}$$

envelop approximation

$$f_{\text{env}} = 16.5 \times 10^{-6} \left( \frac{f_*}{H_*} \right) \left( \frac{T_*}{100 \text{ GeV}} \right) \left( \frac{g_*}{100} \right)^{1/6} \text{ Hz}$$

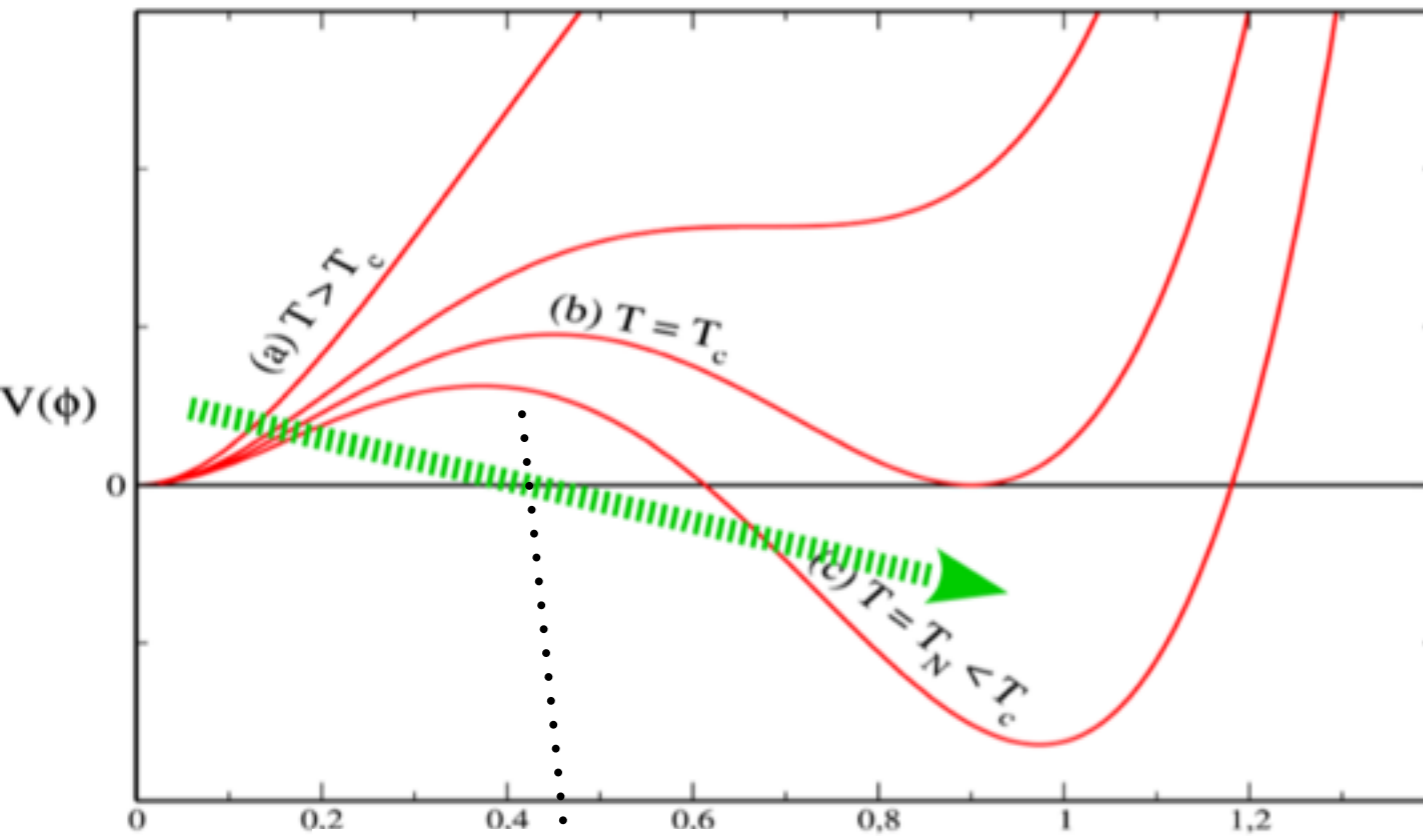
$$\Omega_{\text{sw}} h^2 = 2.65 \times 10^{-6} \left( \frac{H_*}{\beta} \right) \left( \frac{\kappa_v \alpha}{1 + \alpha} \right)^2 \left( \frac{100}{g_*} \right)^{1/3} v_b \left( \frac{f}{f_{\text{sw}}} \right)^3 \left( \frac{7}{4 + 3(f/f_{\text{sw}})^2} \right)^{7/2} \quad (5.6)$$

$$\Omega_{\text{turb}} h^2 = 3.35 \times 10^{-4} \left( \frac{H_*}{\beta} \right) \left( \frac{\kappa_{\text{turb}} \alpha}{1 + \alpha} \right)^{3/2} \left( \frac{100}{g_*} \right)^{1/3} v_b \frac{(f/f_{\text{turb}})^3}{[1 + (f/f_{\text{turb}})]^{11/3} (1 + 8\pi f/\hbar_*)} \quad (5.7)$$

$$\kappa_v \approx \alpha(0.73 + 0.083\sqrt{\alpha} + \alpha)^{-1} \text{ and } \kappa_{\text{turb}} \approx 0.1\kappa_v f_{\text{sw}} = 1.9 \times 10^{-5} \frac{1}{v_b} \left( \frac{\beta}{H_*} \right) \left( \frac{T_*}{100 \text{ GeV}} \right) \left( \frac{g_*}{100} \right)^{1/6} \text{ Hz},$$

κ<sub>v</sub>, κ<sub>turb</sub>: the fraction of latent heat transformed into the bulk motion of the fluid for sound waves and MHD

$$f_{\text{turb}} = 2.7 \times 10^{-5} \frac{1}{v_b} \left( \frac{\beta}{H_*} \right) \left( \frac{T_*}{100 \text{ GeV}} \right) \left( \frac{g_*}{100} \right)^{1/6} \text{ Hz}$$

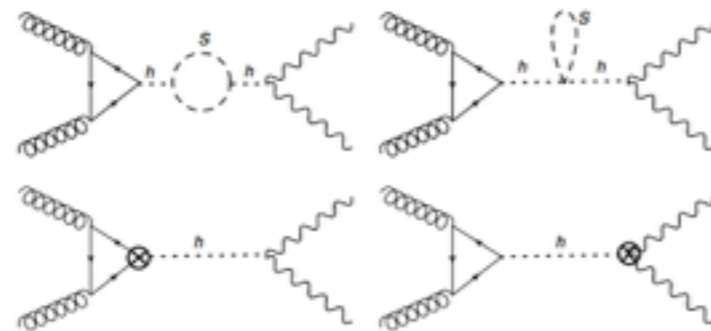


# 1st Phase transition and the collider search



$e^+ e^- \rightarrow Z hh$   
 $pp \rightarrow hh$

- N. Arkani-Hamed, T. Han, M. Mangano and L. T. Wang, Phys. Rept. 652, 1 (2016)
- D. Curtin, P. Meade and C. T. Yu, JHEP 1411, 127 (2014)

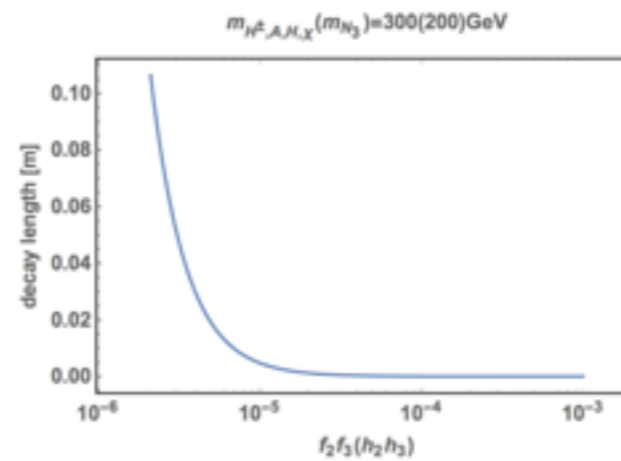


$pp \rightarrow ZZ$

- D. Goncalves, T. Han and S. Mukhopadhyay, Phys. Rev. Lett. 120, no. 11, 111801 (2018)

$$\Gamma'_1(N_3 \rightarrow N_2 \bar{\ell}_\alpha \ell_\beta) = \frac{m_{N_3}^5}{6144 \pi^3 m_{H^\pm, H, A}^4} (|f_{\alpha 2}|^2 |f_{\beta 3}|^2 + |f_{\beta 3}|^2 |f_{\alpha 2}|^2)$$

$$\Gamma'_2(N_3 \rightarrow N_2 \bar{\ell}_\alpha \ell_\beta) = \frac{m_{N_3}^5}{6144 \pi^3 m_\chi^4} (|h_{\alpha 2}|^2 |h_{\beta 3}|^2 + |h_{\beta 3}|^2 |h_{\alpha 2}|^2)$$



1611.09540

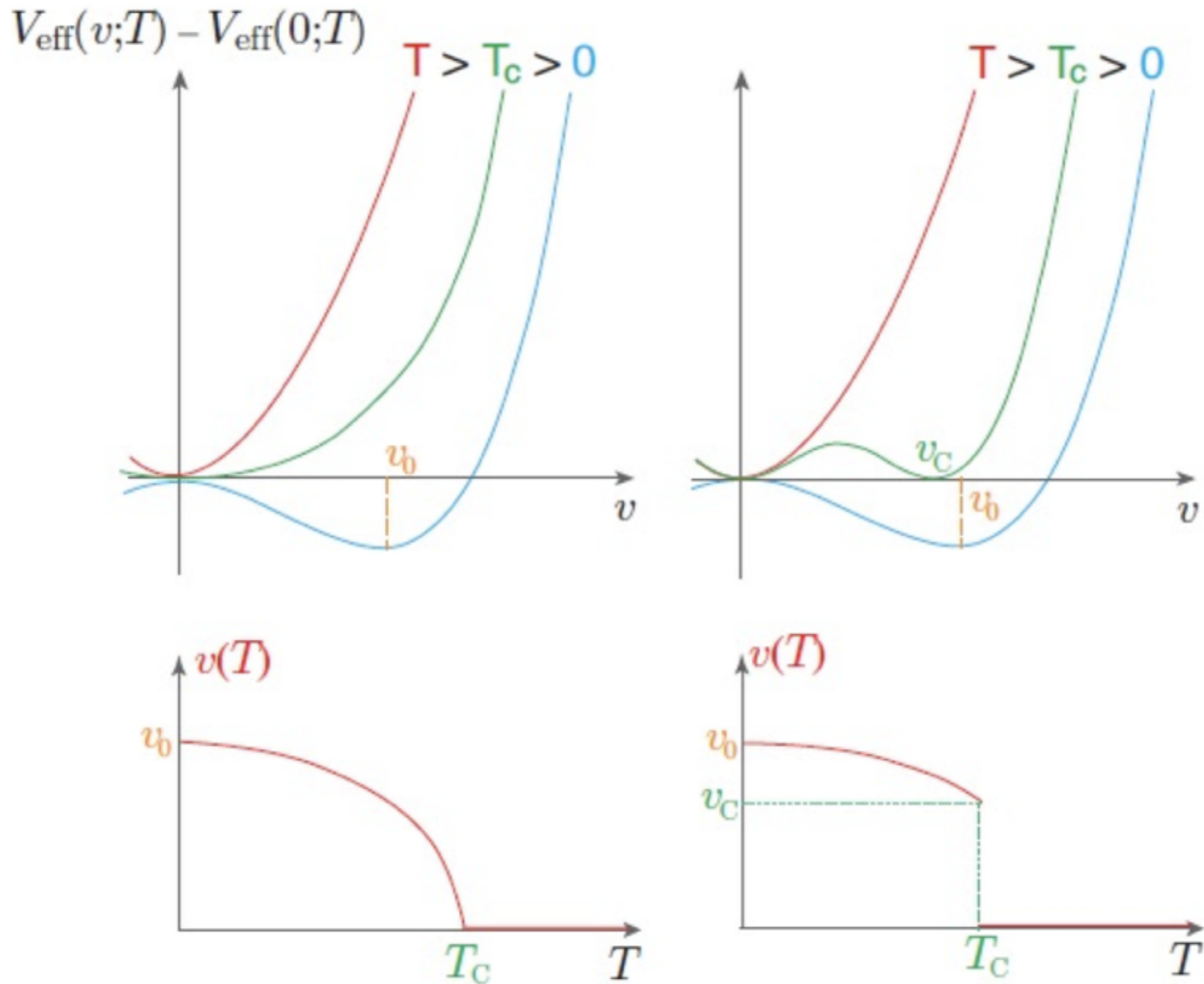


*Thanks*





# First or second order



Cross over/ 2nd order PT

1st order PT

# Backup slides

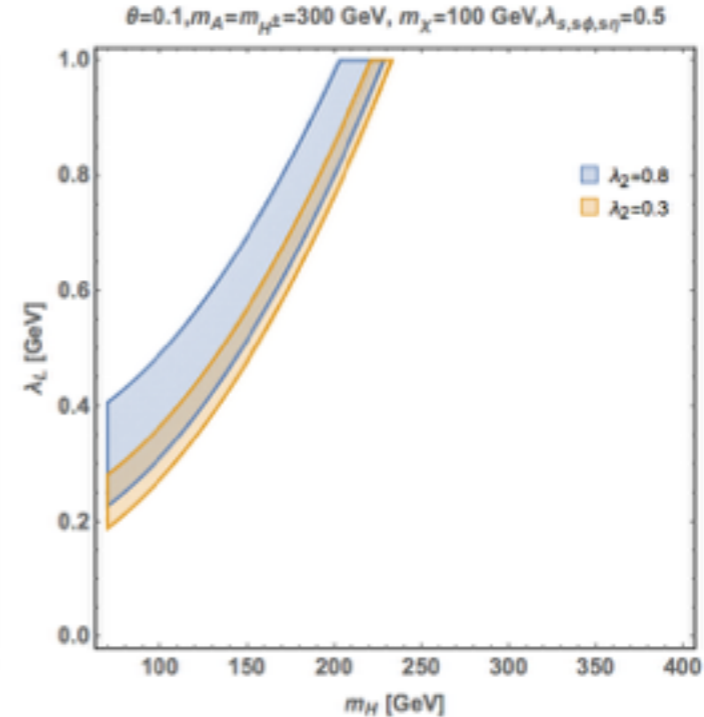
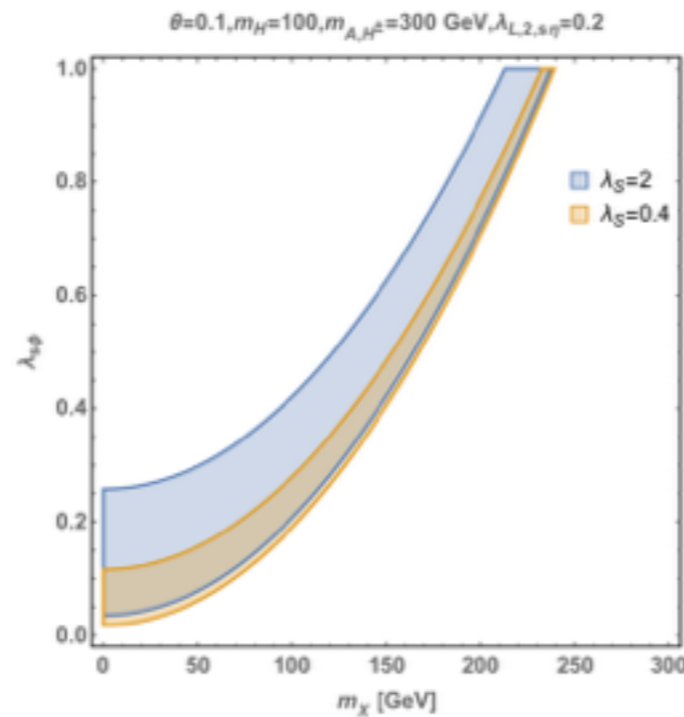
$$V_0(h, H, S) = \frac{\mu_\Phi^2}{2} h^2 + \frac{\mu_\eta^2}{2} H_0^2 + \frac{\mu_S^2}{2} S^2 + \frac{\lambda_1}{4} h^4 + \frac{1}{4} (\lambda_3 + \lambda_4 + \lambda_5) h^2 H_0^2 + \frac{\lambda_2}{4} H_0^4$$

$$+ \frac{1}{2} \lambda_{s\phi} h^2 S^2 + \frac{1}{2} \lambda_{s\eta} H_0^2 S^2 + \frac{\lambda_S}{4} S^4 + \mu_{soft} h H_0 S ,$$

$$\mu_\Phi^2(T) = \mu_\Phi^2 + c_\Phi T^2, \quad c_\Phi = \frac{6\lambda_1 + 2\lambda_3 + \lambda_4 + \lambda_{s\phi}}{12} + \frac{3g^2 + g'^2}{16} + \frac{y_t^2}{4}$$

$$\mu_\eta^2(T) = \mu_\eta^2 + c_\eta T^2, \quad c_\eta = \frac{6\lambda_2 + 2\lambda_3 + \lambda_4 + \lambda_{s\eta}}{12} + \frac{3g^2 + g'^2}{16}$$

$$\mu_S^2(T) = \mu_S^2 + c_S T^2, \quad c_S = \frac{\lambda_S}{4} + \frac{\lambda_{s\phi} + \lambda_{s\eta}}{12} .$$



$$\begin{aligned}
M_h^2 &= \begin{pmatrix} 3\lambda_1 h^2 + \lambda_L H_0^2 + \lambda_{s\phi} S^2 + \mu_\phi^2 & 2\lambda_L h H_0 + \mu_{soft} S & 2\lambda_{s\phi} h S + \mu_{soft} H_0 \\ 2\lambda_L h H_0 + \mu_{soft} S & \lambda_L h^2 + 3\lambda_2 H_0^2 + \lambda_{s\eta} S^2 + \mu_\eta^2 & 2\lambda_{s\eta} H_0 S + \mu_{soft} h \\ 2\lambda_{s\phi} h S + \mu_{soft} H_0 & 2\lambda_{s\eta} H_0 S + \mu_{soft} h & \lambda_{s\phi} h^2 + 3\lambda_s S^2 + \lambda_{s\eta} H_0^2 + \mu_s^2 \end{pmatrix}, & \mu_i^2 \rightarrow \mu_i^2(T) \\
M_A^2 &= \begin{pmatrix} \lambda_1 h^2 + \lambda_L H_0^2 + \lambda_{s\phi} S^2 + \mu_\phi^2 & \lambda_5 h H_0 + \mu_{soft} S \\ \lambda_5 h H_0 + \mu_{soft} S & \lambda_S h^2 + \lambda_2 H_0^2 + \lambda_{s\eta} S^2 + \mu_\eta^2 \end{pmatrix}, \\
M_{H^\pm}^2 &= \begin{pmatrix} \lambda_1 h^2 + \frac{\lambda_3}{2} H_0^2 + \lambda_{s\phi} S^2 + \mu_\phi^2 & \frac{\lambda_4 + \lambda_5}{2} h H_0 + \mu_{soft} S \\ \frac{\lambda_4 + \lambda_5}{2} h H_0 + \mu_{soft} S & \frac{\lambda_3}{2} h^2 + \lambda_2 H_0^2 + \lambda_{s\eta} S^2 + \mu_\eta^2 \end{pmatrix}. & (C.1)
\end{aligned}$$

Symmetry phase

$$M_h^{sys}(T) = M_h(T) |_{\langle h, H_0, S \rangle \rightarrow 0},$$

$$M_A^{sys}(T) = M_A(T) |_{\langle h, H_0, S \rangle \rightarrow 0},$$

$$M_{H^\pm}^{sys}(T) = M_{H^\pm} |_{\langle h, H_0, S \rangle \rightarrow 0}.$$

Z2 broken phase

$$M_h^{\mathbb{Z}_2}(T) = M_h(T) |_{\langle h \rangle \rightarrow 0, \langle H_0 \text{ or } S \rangle \rightarrow v_H(T) \text{ or } v_s(T)},$$

$$M_A^{\mathbb{Z}_2}(T) = M_A(T) |_{\langle h \rangle \rightarrow 0, \langle H_0 \text{ or } S \rangle \rightarrow v_H(T) \text{ or } v_s(T)},$$

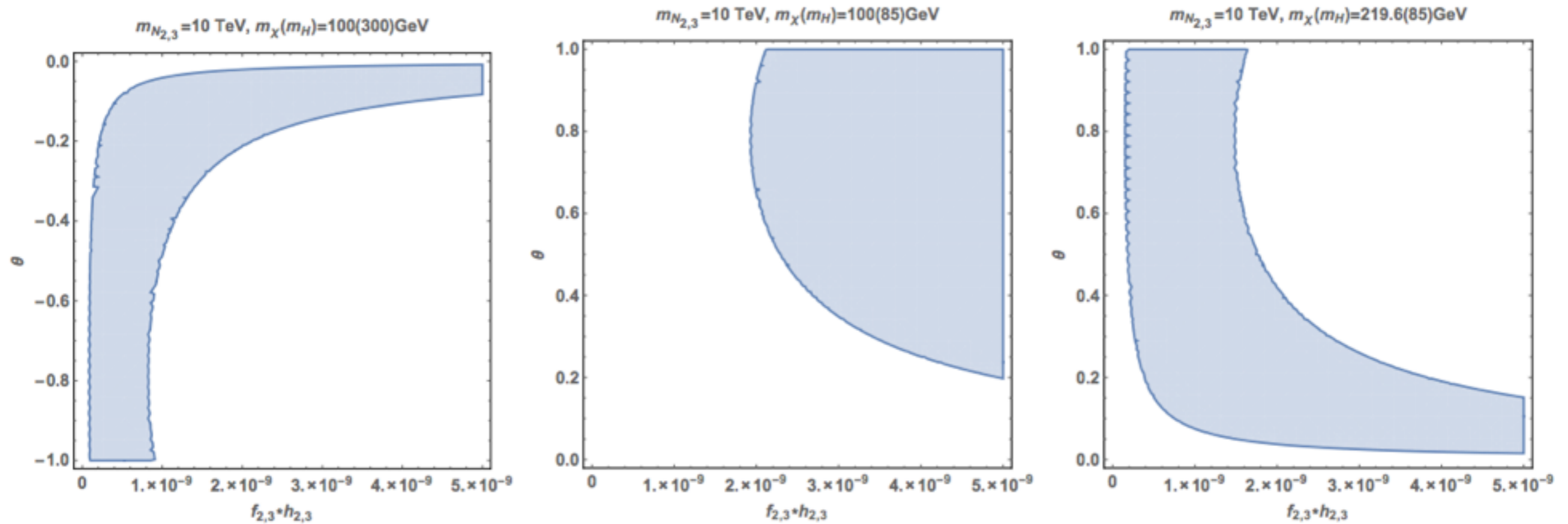
$$M_{H^\pm}^{\mathbb{Z}_2}(T) = M_{H^\pm} |_{\langle h \rangle \rightarrow 0, \langle H_0 \text{ or } S \rangle \rightarrow v_H(T) \text{ or } v_s(T)},$$

EW broken phase

$$M_h^{EW}(T) = M_h(T) |_{\langle h \rangle \rightarrow v(T), \langle H_0, S \rangle \rightarrow 0},$$

$$M_A^{EW}(T) = M_A(T) |_{\langle h \rangle \rightarrow v(T), \langle H_0, S \rangle \rightarrow 0},$$

$$M_{H^\pm}^{EW}(T) = M_{H^\pm} |_{\langle h \rangle \rightarrow v(T), \langle H_0, S \rangle \rightarrow 0}.$$



The neutrino mass bounds on mixing angle  $\theta$  and the multiplication of Yukawa  $f$  and  $h$  for OAC(left), OBC (middle), OBC with late decay (right).