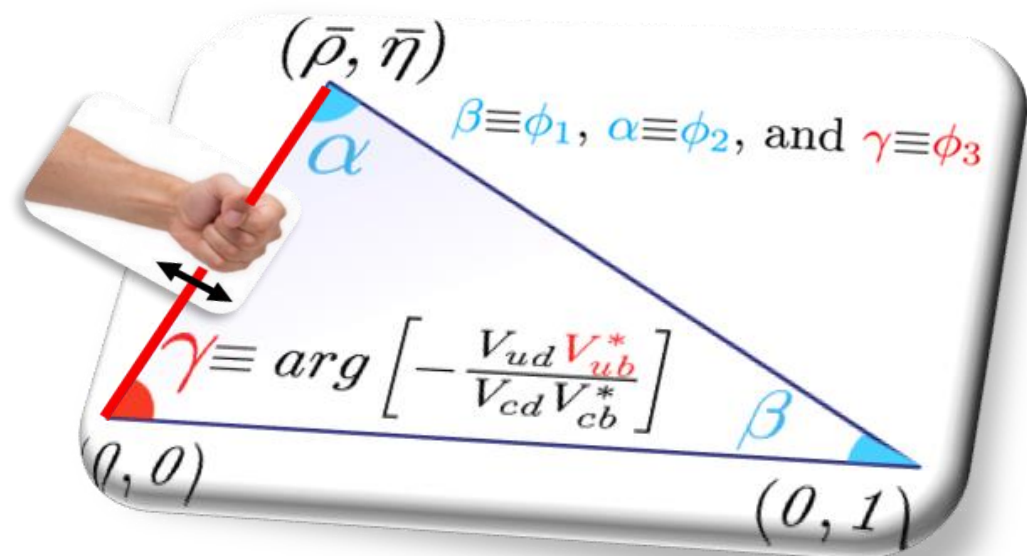
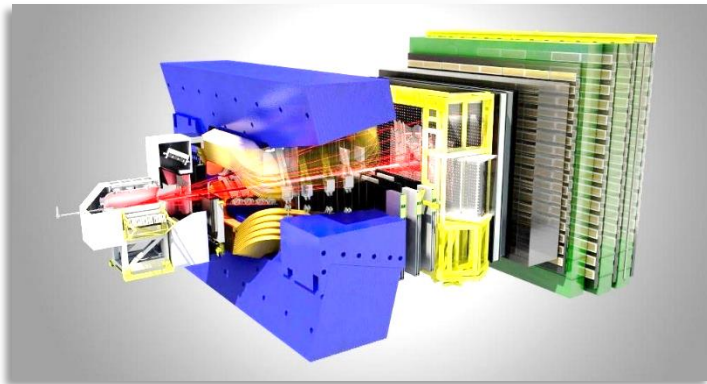


# Recent results on the CKM angle $\gamma$ with open charm B decays at LHCb

V. Tisserand (CKMfitter/LHCb), LPC-Clermont Ferrand, France  
IHEP Beijing Nov 21<sup>st</sup> 2018

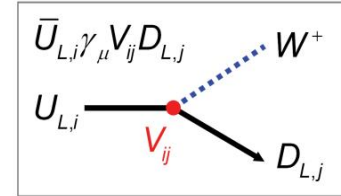


# The Standard Model (SM) & the Unitary CKM Matrix

→ mixing of the 3 quarks families & CP violation

- the Higgs boson gives mass to elementary bosons & fermions (quarks, leptons) through Yukawa couplings, but there is not only that ! :

$$\mathcal{L}_{cc}^{\text{quarks}} = \frac{g}{2\sqrt{2}} W_{\mu}^{\dagger} \left[ \sum_{ij} \bar{u}_i(q_2) \gamma^{\mu} (1 - \gamma^5) V_{ij} d_j \right] + \text{h.c}$$



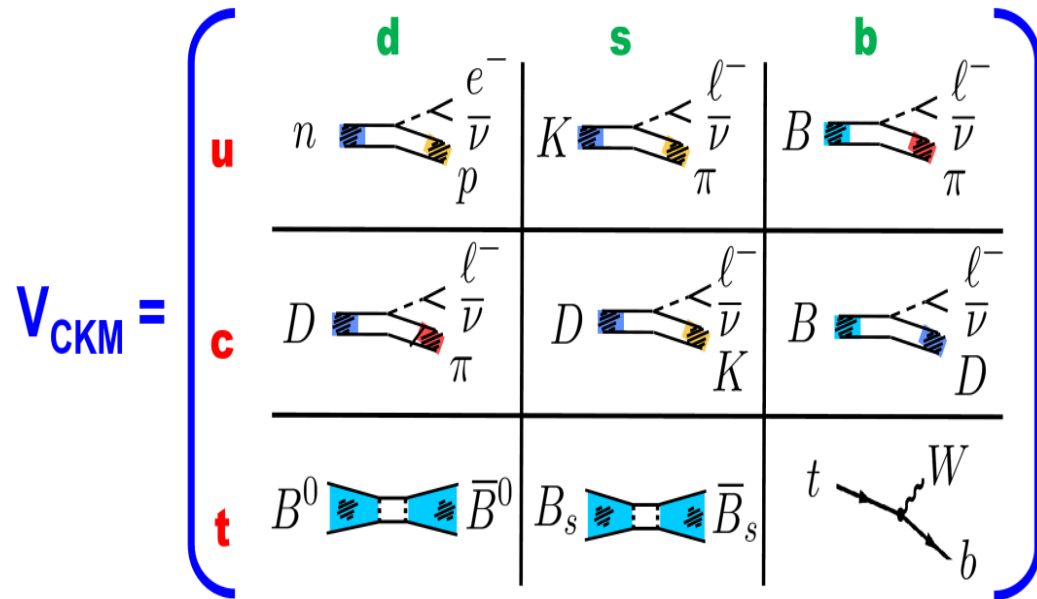
charged currents (EW) imply transitions between quark families : quarks decays [there are no neutral current changing flavour (FCNC) at tree level (i.e. GIM mechanism )].

$$V_{\text{CKM}} = \begin{pmatrix} \text{u} & \text{d} & \text{s} & \text{b} \\ 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ \text{c} & -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ \text{t} & A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4) \quad (\mathbf{V}\mathbf{V}^{\dagger} = \mathbf{1})$$

- strong hierarchy** in EW  $V_{ij}$  couplings for the 3 families (wrt diagonal couplings  $\propto \lambda^N \approx (0.225)^N$  : → **Cabibbo angle**).

- KM** (Kobayashi-Maskawa) mechanism : **3 generations** → **4 parameters**:  $A, \lambda, \rho$  & **1 complex part  $\eta$  which phase** is the unique source of CPV in SM.

# The CKM Matrix : the unitary triangle & the very rich phenomenology of quark flavors



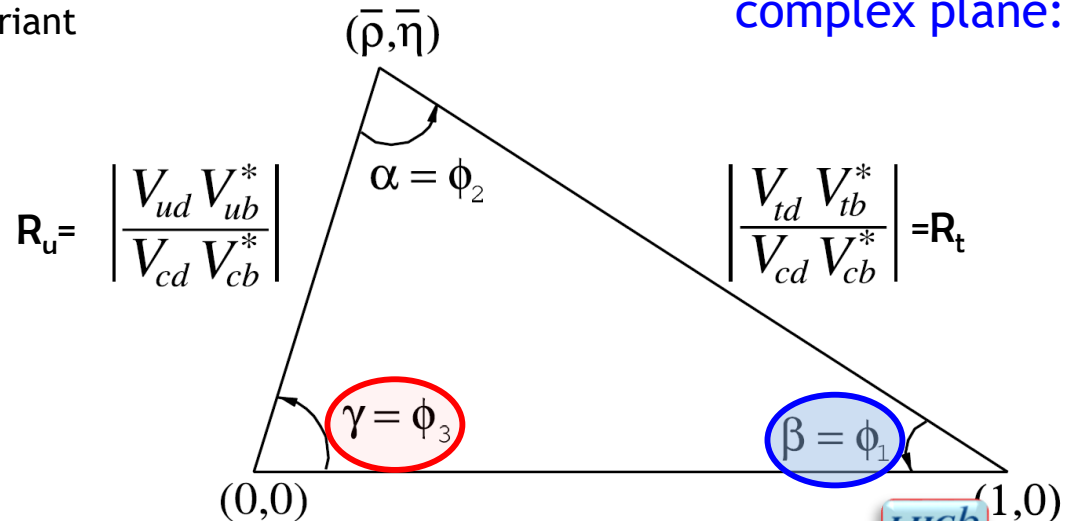
→ 4 parameters ( $A, \lambda, \rho$  &  $\eta$ ) to be obtained/tested wrt data: nucleons, K, D,  $B_{(s)}$  & top quark physics.

→ unitarity relation in  $B_d$  system (1<sup>st</sup> line/3<sup>rd</sup> column):

$$\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} + 1 + \frac{V_{td} V_{tb}^*}{V_{cd} V_{cb}^*} = 0$$

$$O(1) + O(1) + O(1)$$

Unitarity triangle in the  $(\bar{\rho}, \bar{\eta})$  complex plane:



Parametrisation « à la Wolfenstein » phase invariant & valid at any orders in  $\lambda$  @ CKMfitter

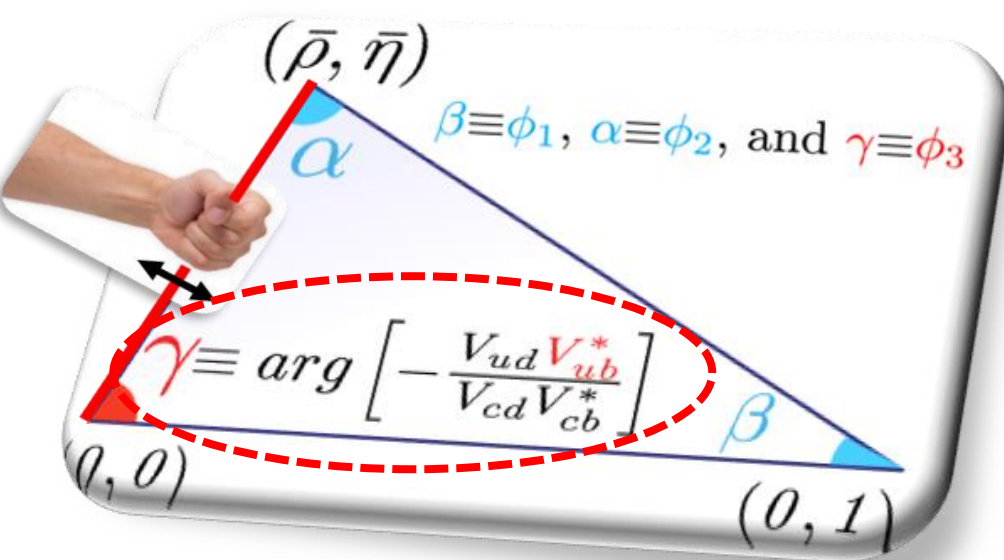
(EPJ C41, 1-131, 2005):

$$\bar{\rho} + i\bar{\eta} = -\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*}$$

$$\lambda^2 = \frac{|V_{us}|^2}{|V_{ud}|^2 + |V_{us}|^2}$$

$$A^2 \lambda^4 = \frac{|V_{cb}|^2}{|V_{ud}|^2 + |V_{us}|^2}$$

→ The CKM angle  $\gamma$  is a fundamental parameter of the SM related to the complex phase in the KM mechanism responsible for CP violation in quark sector



Already 10 years ago after the B factories BaBar@SLAC and Belle@KEK we knew that



Kobayashi et Masakawa, Nobel prize of physics 2008

The KM mechanism is the main source of CPV at EW scale (i.e. @  $m_{W/Z}$ )

→ So why do we still care about the CKM angle  $\gamma$  ?

$$\gamma[\text{combined@2008}] = (70^{+27}_{-29})^\circ$$






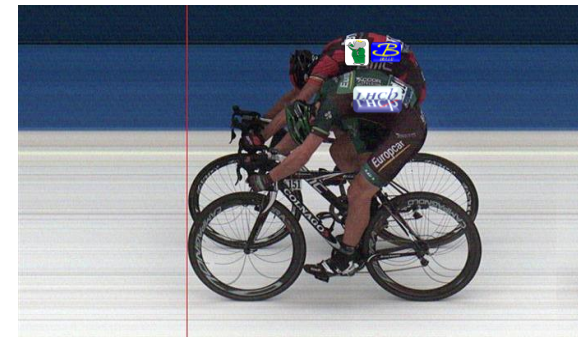


# 5 years after: the CKM angle $\gamma$ after LHC run1 in 2013

$$\gamma \equiv \arg \left[ -\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} \right]$$

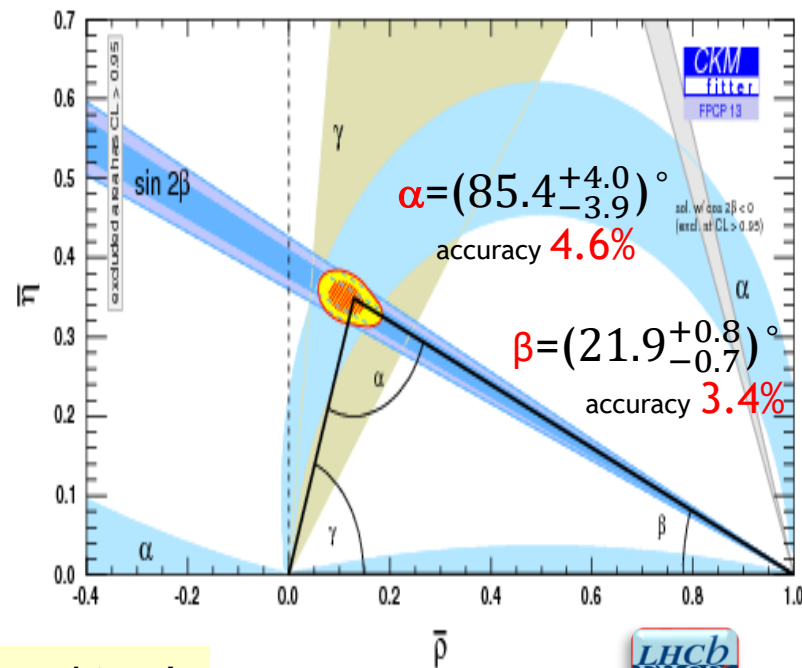
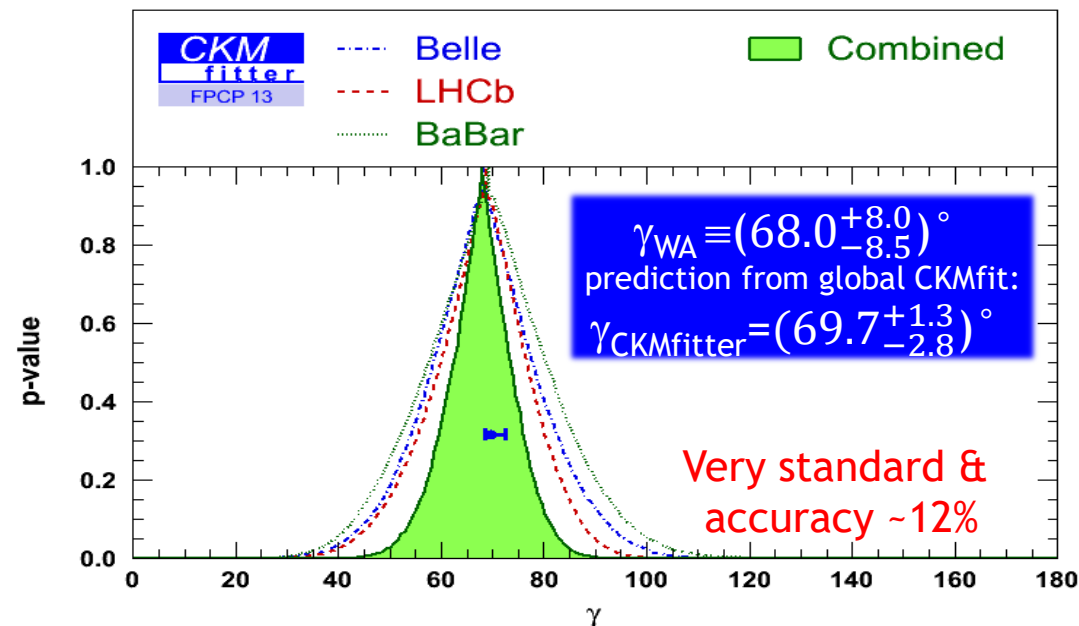
→ Astonishing/impressive overall consistency:

- $(69^{+17}_{-16})^\circ$   PRD 87(2013)052015
  - $(68^{+15}_{-14})^\circ$   arXiv:1301.2033
  - $(67 \pm 12)^\circ$   PLB 726(2013)151  
LHCb-CONF-2013-006
- } B-factories:  $(67 \pm 11)^\circ$   
PBF book



→ Many DK like modes combined, observables are predictable!

→ M. Karbach (RIP) : "We understand what we're doing!"



LHCb was already competitive with only 2 years of data taking !

# The theoretical usefulness of measuring accurately the CKM angle $\gamma$ in 2018 and beyond

Angle  $\gamma$  is the least well known CKM constraint (although now only just (i.e. similar to  $\alpha$ )) and remains a unique CPV parameter:

- SM benchmark or standard candle - only CKM angle accessible at tree level
- Determination from tree  $B \rightarrow DK$  decay theoretically extremely clean :

[arXiv:1308.5663]

$$\delta\gamma/\gamma \sim \mathcal{O}(10^{-7})$$

Only one caveat: New physics at tree level in Wilson coeff of interfering amplitudes  $C_1$  and  $C_2$  can cause sizeable (up to  $5^\circ$ ) shifts in  $\gamma$ , however quite academic speculation, type of possible NP model very unclear and yet unmotivated [arXiv:1412.1446]

- Probes NP scales extremely far beyond direct searches in ((N)M)FV NP scenarios:

[arXiv:1101.0134]

$$\Lambda_{NP}^\gamma \sim \mathcal{O}(10^3 \text{ TeV})$$

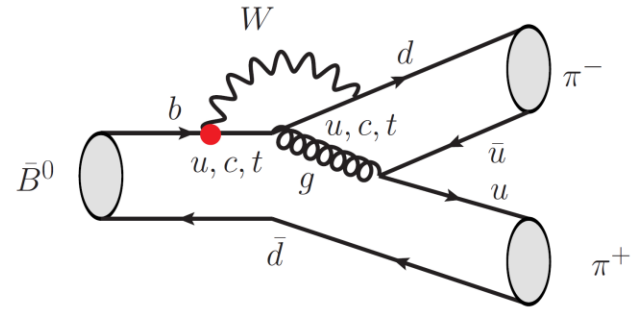
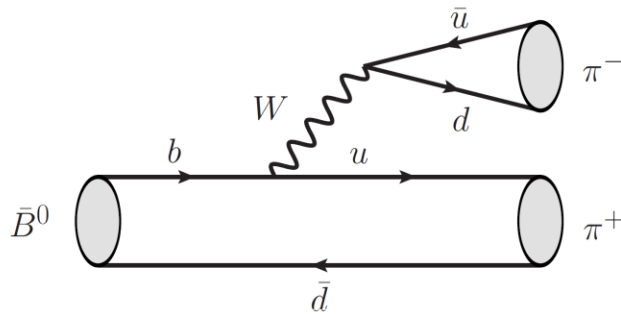
➔ Use for “direct” vs “indirect” (i.e. “tree” vs “loop” processes) disagreement in global CKM fit consistency test :

- Tree level decays test the SM and are robust to New Physics (“standard candle for the SM KM coherence tests”):  $\perp$  constraint to  $\sin(2\beta)$ , need ideally precision of about  $\sim 1^\circ$  and below
- Loops (B to charmless decays) test for physics beyond the SM but require a clean measurement as input & precise understanding of theory assumptions (SU(3) breaking, U-spin...).

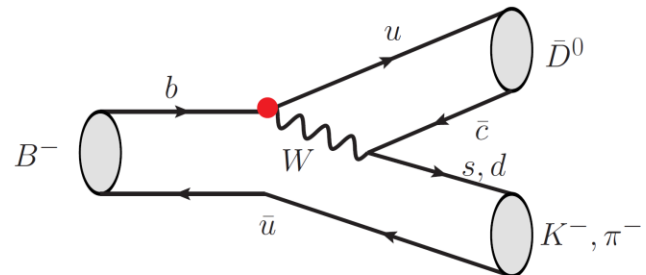
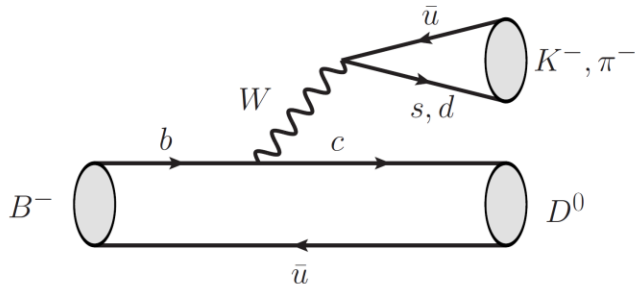


# CKM angle $\gamma$ in loops and trees

- From  $B \rightarrow \pi\pi$  determine  $\alpha = \pi - \beta - \gamma$  [Gronau, London 1990]
- Use  $B \rightarrow \pi\pi$  and  $B_s \rightarrow KK$  to extract  $\gamma$  [Fleischer 1999]



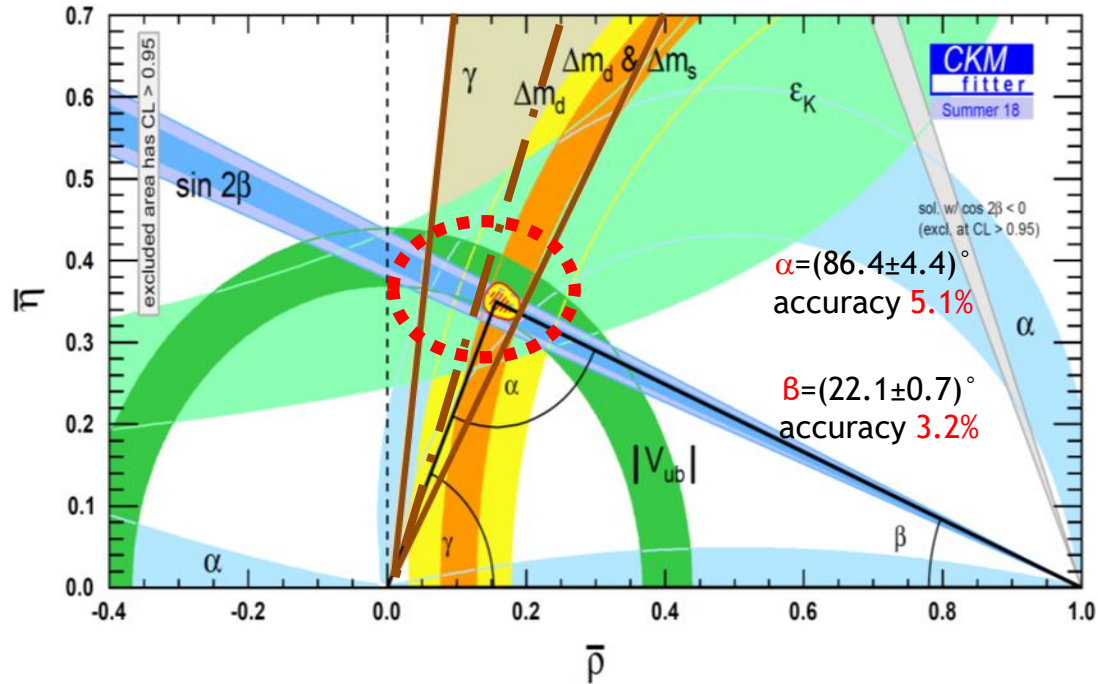
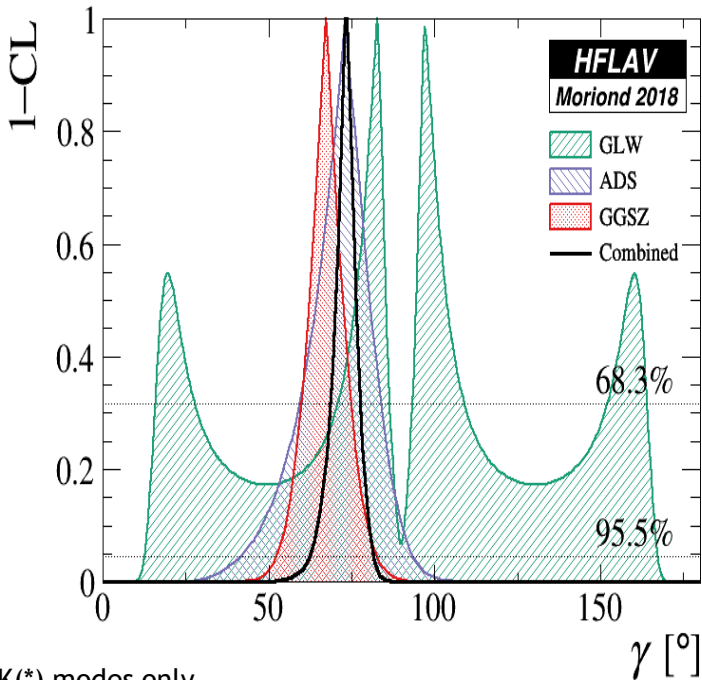
- Compare to  $\gamma$  from tree-level  $B \rightarrow DK$  [Bigi, Sanda 1981]



I will come back later on it...

# The early 2018 state of play

The current world average (HFLAV), LHCb combination and indirect determination (CKMfitter) on  $\gamma$



D(\*)K(\*) modes only

$$\gamma_{WA} = (73.5^{+4.2}_{-5.1})^\circ \quad \gamma_{LHCb} = (75.8^{+5.1}_{-5.7})^\circ$$

$$\gamma_{CKMfitter} = (65.6^{+1.0}_{-3.4})^\circ$$

LHCb dominates WA

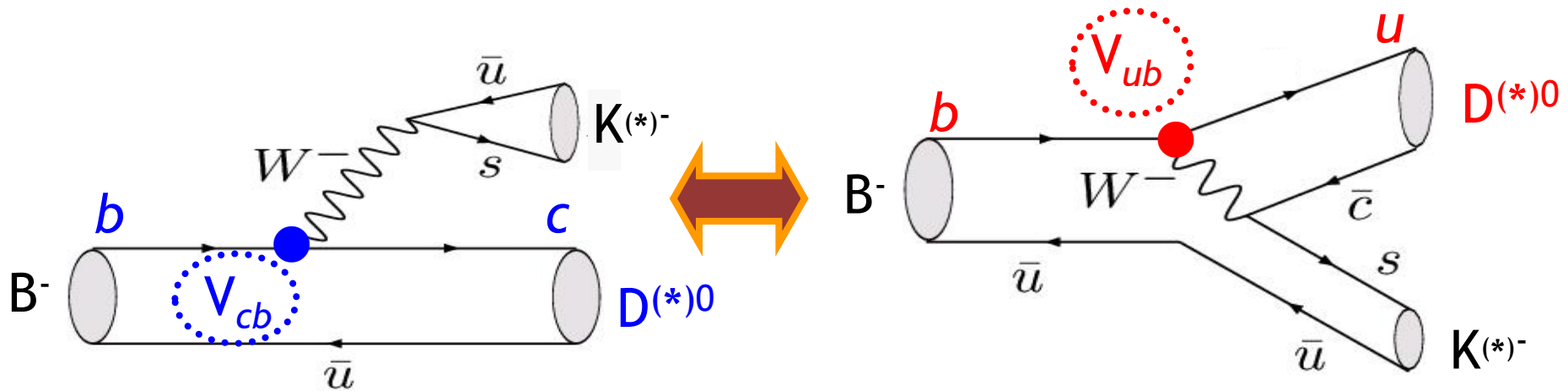
**1.5 $\sigma$  shift / WA**  
Need to measure at **< 1° accuracy**  
→ test  $\Lambda_{NP} > 17$  TeV (model indep.)

We entered yet the **sub 5° (6%) precision era** → **but still not enough!**



$$\gamma \text{ in } B^- \rightarrow \tilde{D}^{(*)0} K^{*-}$$

Same final state  $\tilde{D}^0 \equiv [D^0/D^0]$

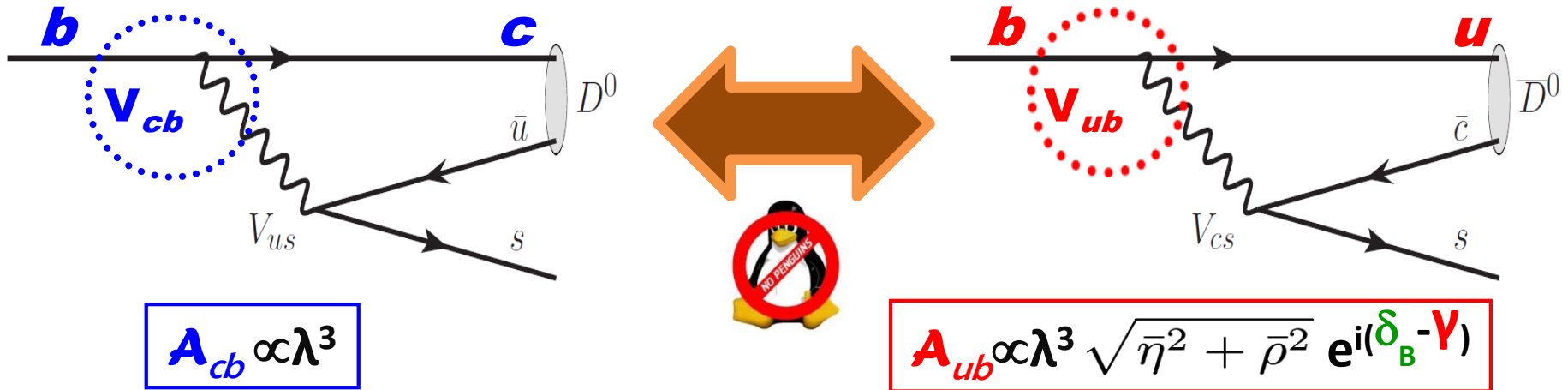


$$\gamma \equiv \arg \left[ - \frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} \right]$$



# Obtaining $\gamma$ : use interference between $b \rightarrow c\bar{u}s$ and $b \rightarrow u\bar{c}s$

Gronau, Wyler (91); Gronau, London (90)



→ Take any spectator(s) you like. Color-allowed diagrams are also possible for certain spectators. For **color-suppressed  $V_{ub}$  decays**:

$$A_{tot} = A + \bar{A}$$

CPV asymmetry size depends upon the critical parameter :

$r_B \equiv |A/\bar{A}| \sim 5-30\%$  color/Cabibbo suppression

PLB 557(2003)198

if  $r_B$  small  $\Rightarrow$  small experim. sensitivity to  $\gamma$  (precision as  $1/r_B$ )

same  $D \equiv [D^0/\bar{D}^0]$  final state

→ Experimentally unfold  $\gamma$ ,  $\delta_B$ , and  $r_B$  from ratios of BFs and B vs  $\bar{B}$  asymmetries observables

→ Hadronic nuisance parameters can be determined from data directly or from external inputs



# Experimental aspects of $\gamma$ measurements

→ **measuring  $\gamma$  at tree level is difficult** (typical BFs  $<10^{-6}$  and less, reconst. & selection efficiencies below % ):

- **STATISTICS is THE NAME OF THE GAME**  $\Rightarrow$  efficient detection/selection/ PID/tracking/vertexing and even neutrals
- **combining many measurements/methods + inputs** from charm factories (D parameters + mixing & CPV)

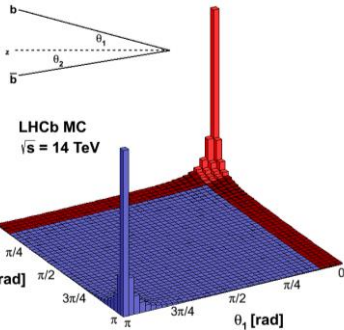
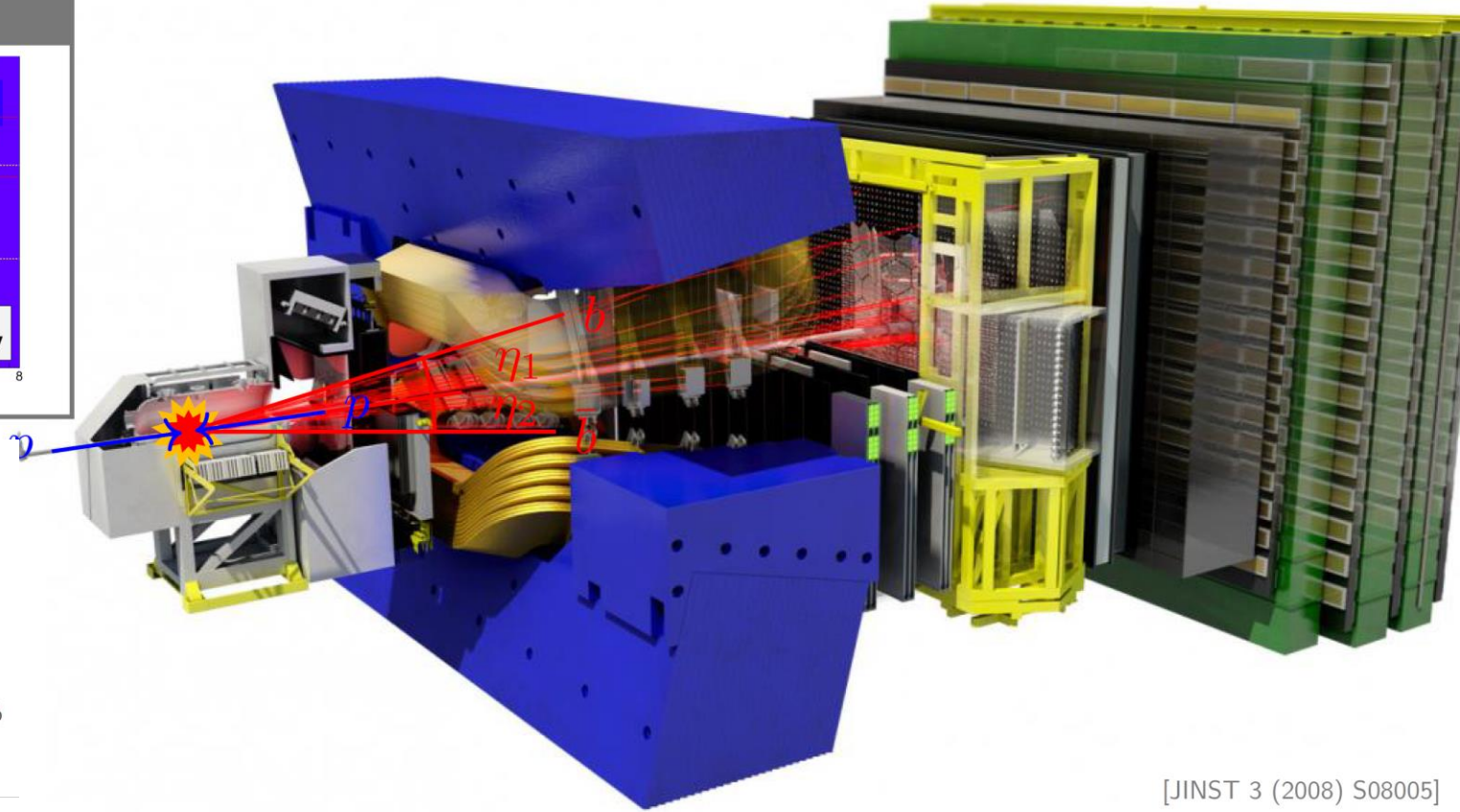
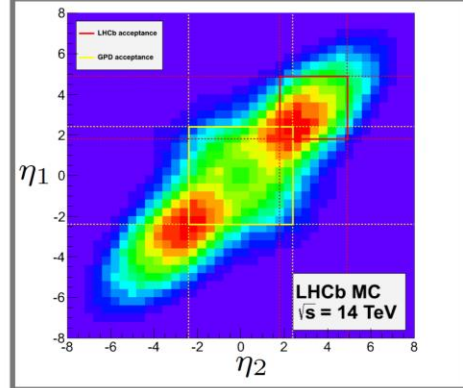
→ **Many methods/modes to combine** for optimal & redundant determination of  $\gamma$  (and rigorous statistical treatment possibly matters !)

→ **various charmed modes in  $B^0$ ,  $B^+$ ,  $B^0_s$ ,  $\Lambda^0_b$ ,  $B^+_c$  decays** are useful to understand/confirm possible sensitivity to BSM physics and its nature

*The LHCb experiment at LHC is designed to accomplish all of the above !*

# LHCb: Optimized for precision flavour measurements

$b\bar{b}$  production



[JINST 3 (2008) S08005]

[IJMPA 30 (2015) 1530022]

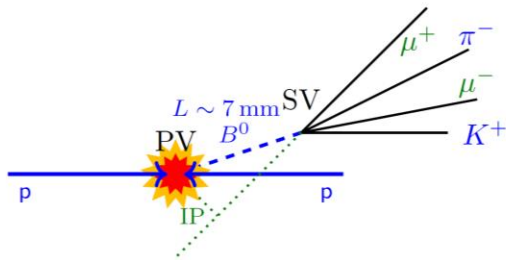
- $b\bar{b}$  produced in forward/backward direction  $\rightarrow$  Optimized acceptance  $2 < \eta < 5$
- Huge production cross-sections in LHCb acceptance  
 $1.4 \times 10^{11}$   $b\bar{b}$ -pairs per  $\text{fb}^{-1}$  (Run 2)
- All beauty, charm and strange hadrons produced  
 $B_s^0, \Lambda_b^0, B_c^+, D_s^+, \Lambda_c^+, \Sigma, \Xi, \dots$

	$\sqrt{s} = 7 \text{ TeV}$	$\sqrt{s} = 13 \text{ TeV}$
$\sigma_{b\bar{b}}^{\text{acc.}} [\mu\text{b}]$	$75.3 \pm 14.1$	$144 \pm 1 \pm 21$
$\sigma_{c\bar{c}}^{\text{acc.}} [\mu\text{b}]$	$1419 \pm 134$	$2940 \pm 241$
Refs.	[PLB 694:209 (2010)] [NPB 871 (2013) 1-20]	[PRL 118 (2017) 052002] [JHEP 03 (2016) 159]

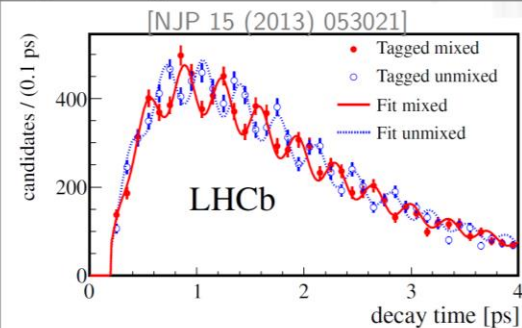


# LHCb: Optimized for precision flavour measurements

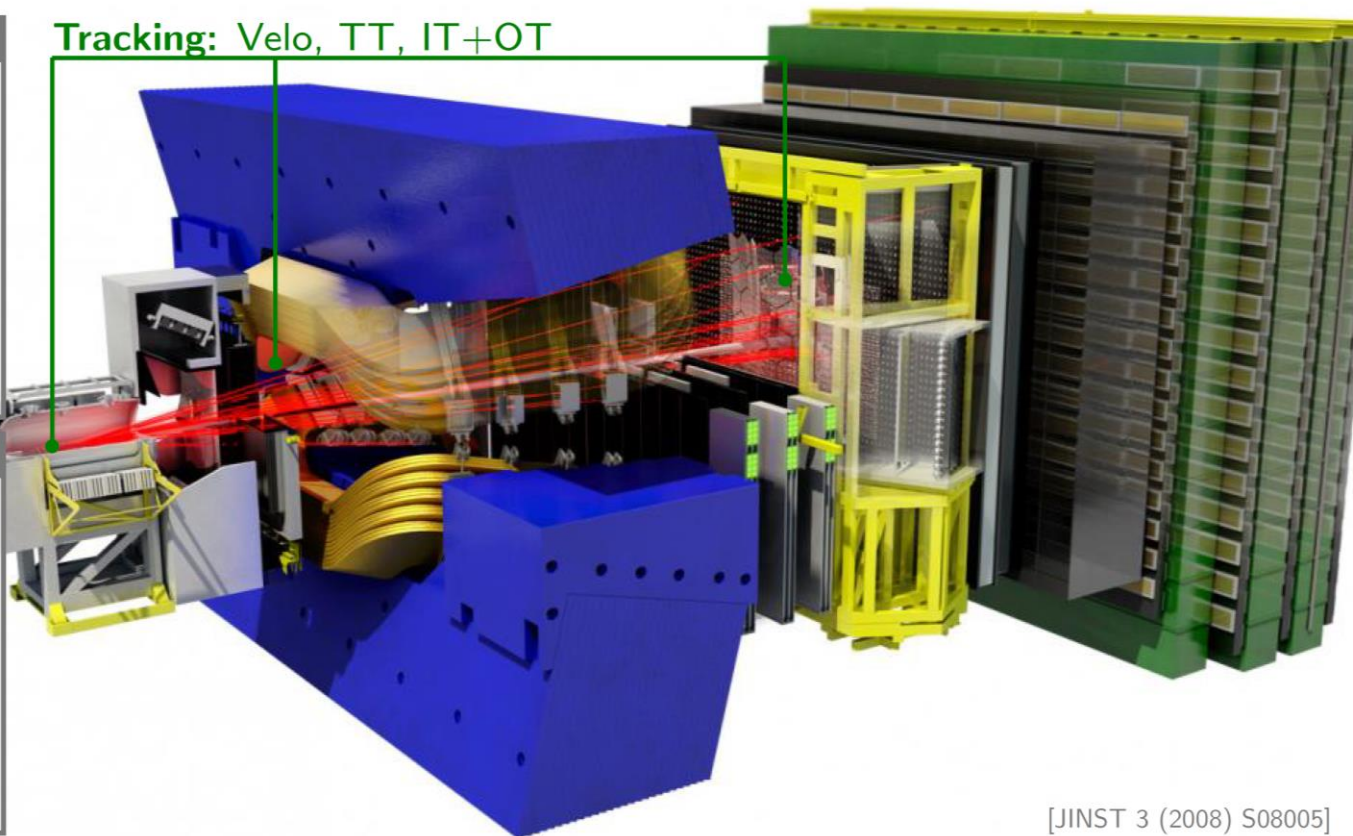
## Heavy flavour signature



## $B_s^0$ mixing



## Tracking: Velo, TT, IT+OT



[JINST 3 (2008) S08005]

[IJMPA 30 (2015) 1530022]

- Excellent IP resolution  $\sim 20 \mu\text{m}$  to identify  $B$  decay vertices
- Decay time resolution  $\sim 45 \text{ fs}$
- Resolutions  $\sigma(p)/p = 0.5 - 1\%$ ,  $\sigma(m) \sim 22 \text{ MeV}$  for two-body  $B$ -decays  
→ Low combinatorial backgrounds







# LHCb: Optimized for precision flavour measurements

## LHCb Run 2 trigger

40 MHz bunch crossing rate

L0 Hardware Trigger : 1 MHz readout, high  $E_T/P_T$  signatures

450 kHz  $h^\pm$

400 kHz  $\mu/\mu\mu$

150 kHz  $e/\gamma$

Software High Level Trigger

Partial event reconstruction, select displaced tracks/vertices and dimuons

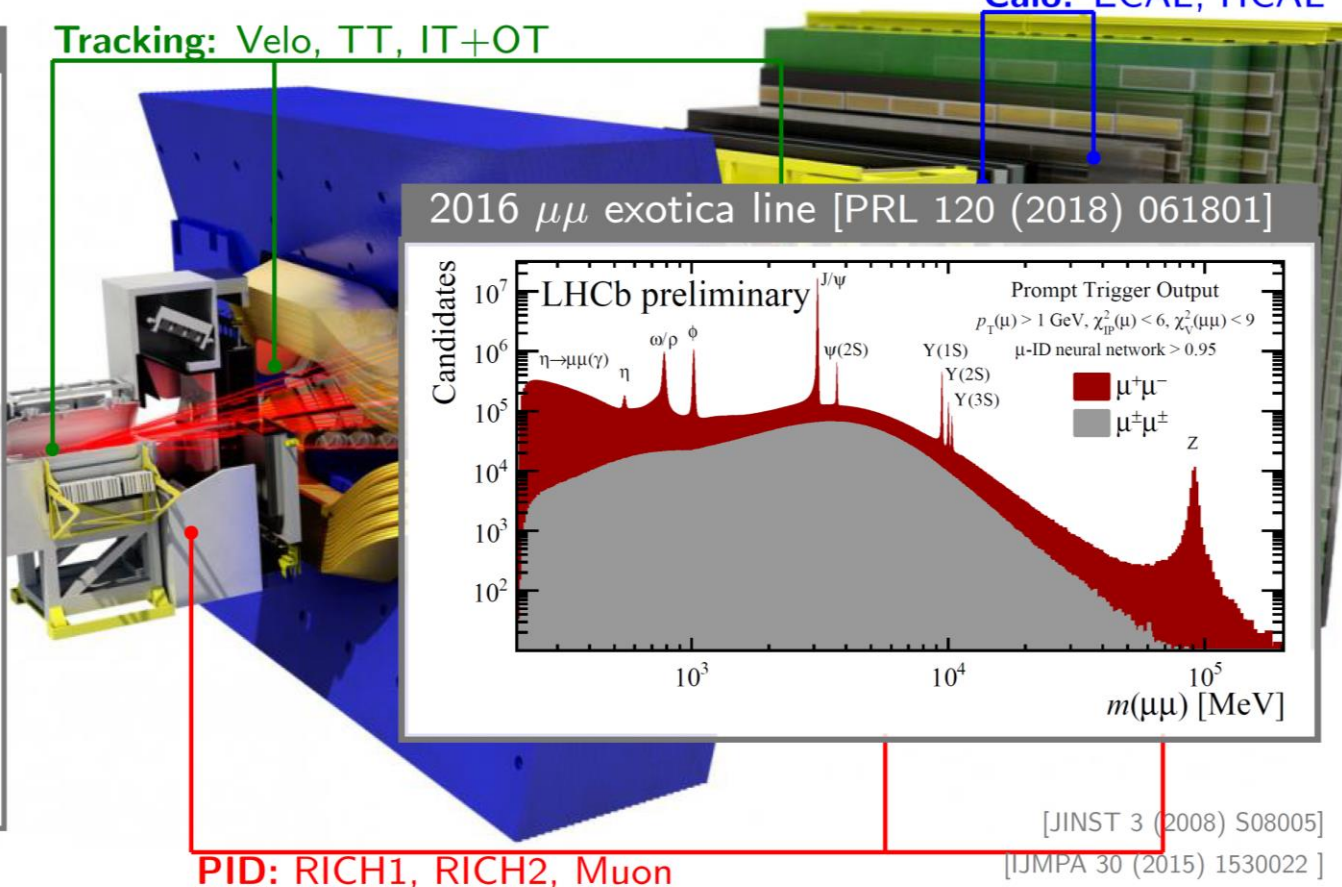
Buffer events to disk, perform online detector calibration and alignment

Full offline-like event selection, mixture of inclusive and exclusive triggers

12.5 kHz (0.6 GB/s) to storage

Tracking: Velo, TT, IT+OT

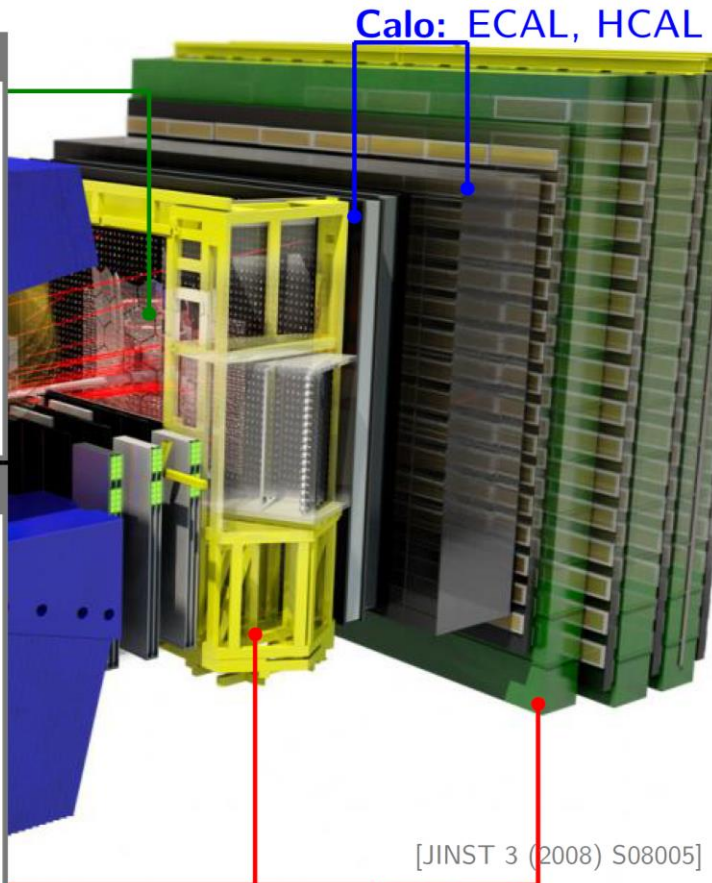
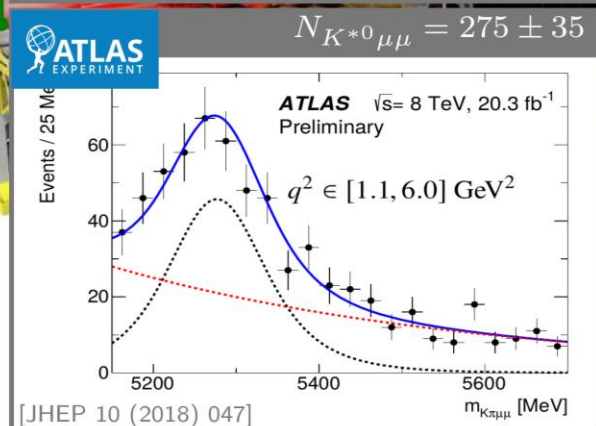
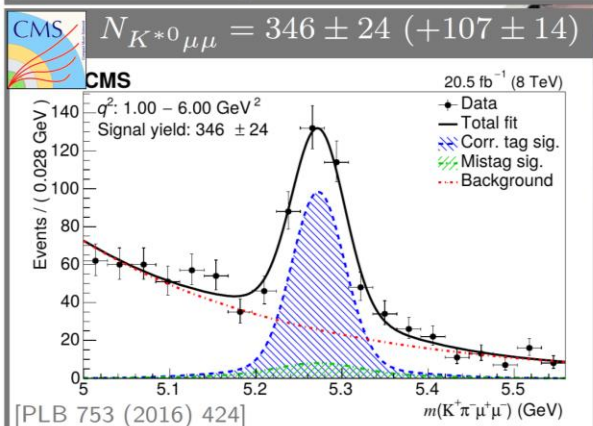
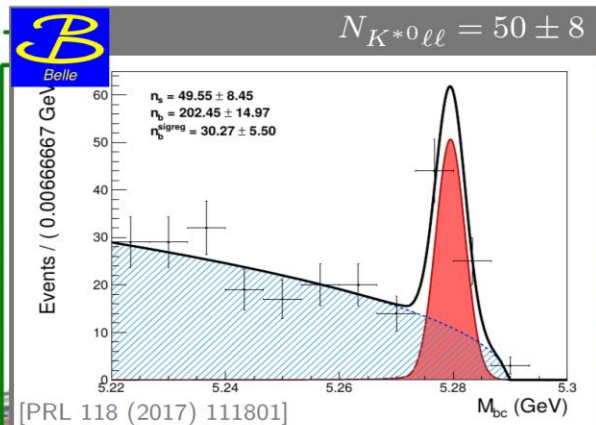
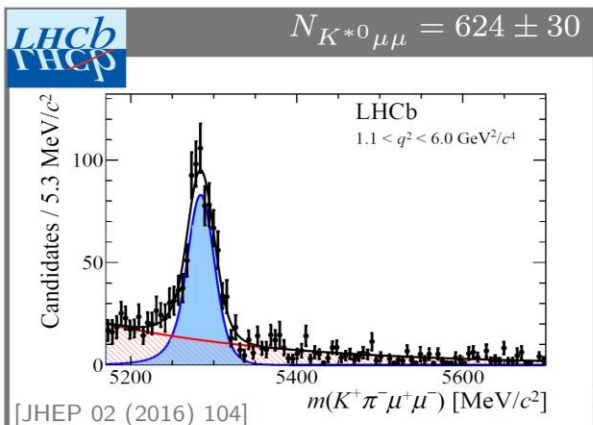
Calo: ECAL, HCAL



- Flexible trigger system with low thresholds:  $p_T(\mu) > 1.8 \text{ GeV}$ ,  $E_T(e) > 3.0 \text{ GeV}$
- High efficiencies, e.g.  $\epsilon_{\text{trigger}}(B \rightarrow J/\psi X) \sim 90\%$
- Since Run 2: Online calibration and alignment, allows use of PID in trigger
- Allows low  $p_T$  physics: charm, strange, exotica, ...

→ L0 HW trigger to be removed during LHC LS2

# LHCb: Optimized for precision flavour measurements



PID: RICH1, RICH2, Muon

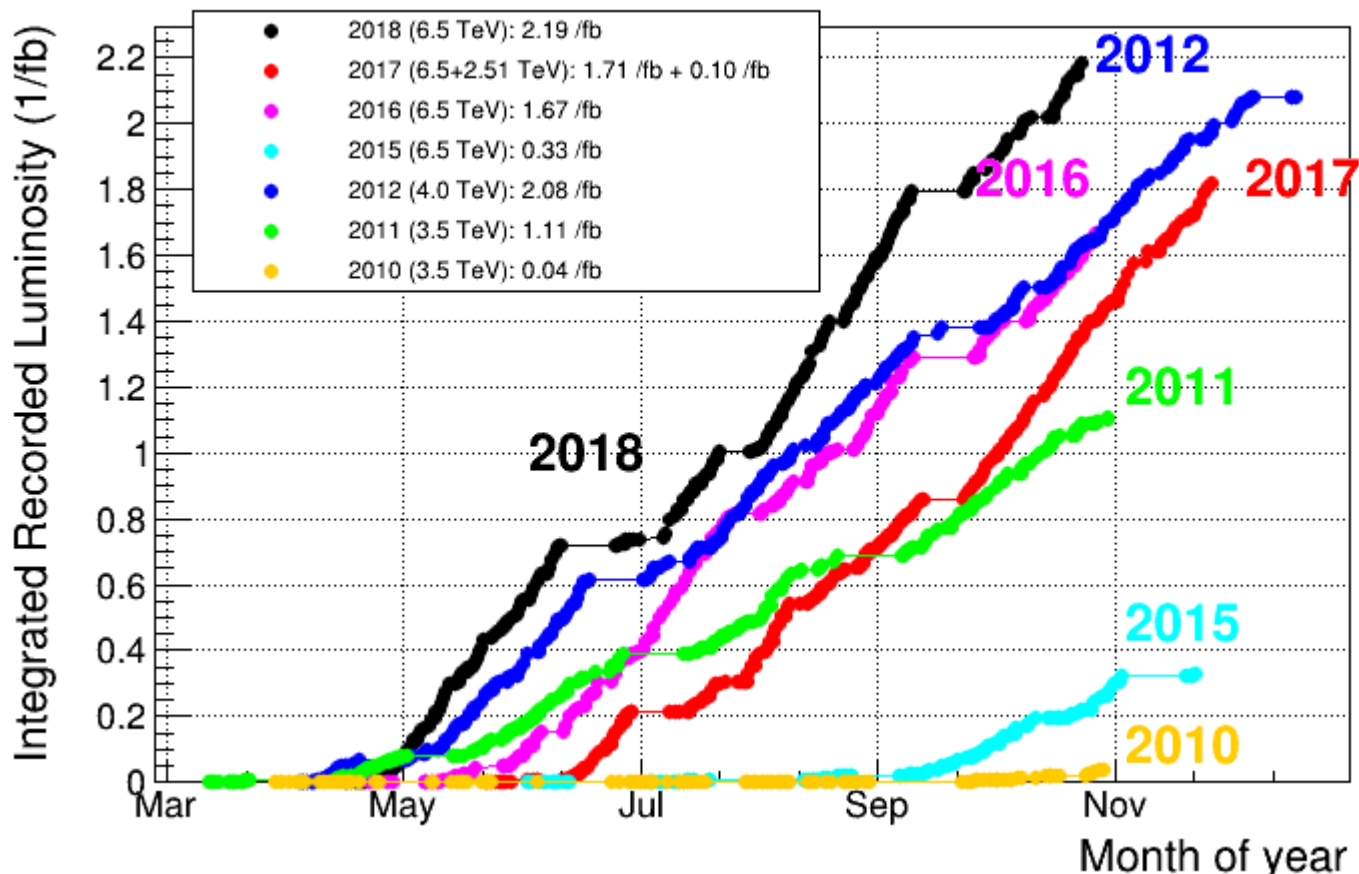
- Performance comparison using  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$  Run 1 results as example
- LHCb compares very favourably
  - Largest yields ( $b\bar{b}$  cross-section, large acceptance and high trigger efficiencies)
  - Excellent mass resolution and low combinatorial backgrounds
  - Negligible peaking backgrounds due to powerful particle identification



# LHCb: so far accumulated statistics in LHC Run 1&2

- Instantaneous luminosity was from  $3.3$  to  $4.4 \times 10^{32} \text{ cm}^{-2} \cdot \text{s}^{-1}$
- the heavy-flavour cross-section is  $\sim$ twice at 13 TeV compared to 7 TeV

LHCb Integrated Recorded Luminosity in pp, 2010-2018

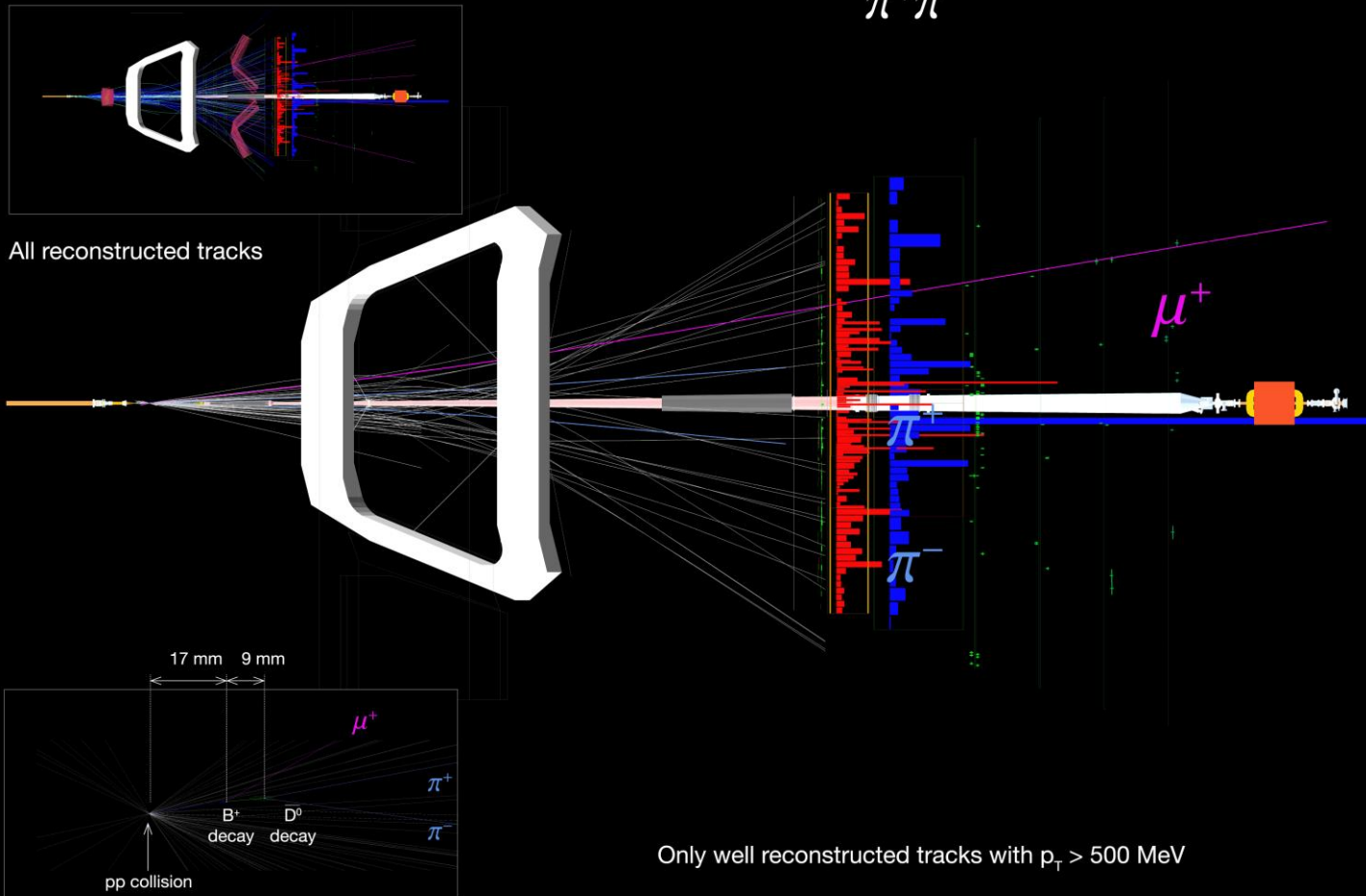
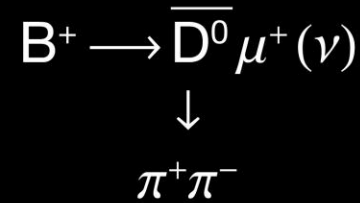


- Most published results use part of LHC Run 1 (<2013) + Run 2 (>2014) data
- Total number of b-hadrons is Run 1+Run 2 is about 5 times that of Run 1



# LHCb: Optimized for precision flavour measurements

Very similar event display  
as for  $B \rightarrow D_{CP^+} K$  events

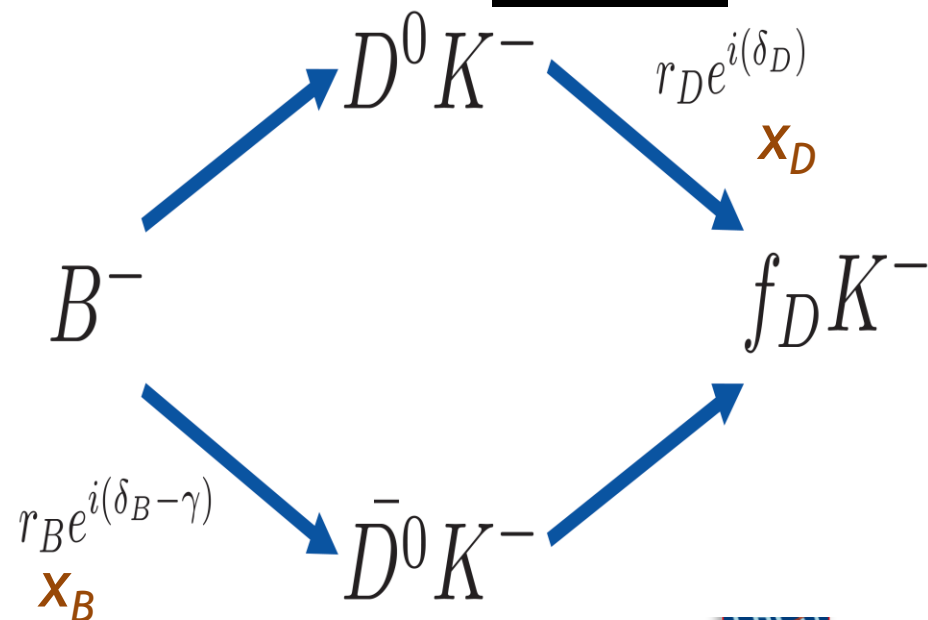


# Experimental aspects of $\gamma$ measurements

- Theoretically straightforward, experimentally more challenging
  - Branching fractions ( $\sim 10^{-7}$ ) and interference effects tend to be small ( $\sim 10\%$ )
  - Triggering on fully hadronic final states is not trivial (LHCb Trigger upgrade after LHCb LS2)
  - Many decay modes feature  $K_S^0$  or  $\pi^0$  mesons - lower efficiencies at LHCb
  - Statistically challenging - many decay modes, observables and hadronic parameters
  - External inputs required for several beauty and charm parameters

CLEO-c BESIII  
HFLAV

- The golden mode  $B^- \rightarrow DK^-$ 
  - Sensitivity from interference of  $b \rightarrow c$  and  $b \rightarrow u$  amplitudes
  - Weak phase difference  $\gamma$  the same for all D meson decay final states





# Measuring $\gamma$ : several methods and approaches depending on the D meson decays

→ Time-integrated “well known” methods that need a lot of B mesons  
 → counting direct CPV,  $N(B)$  vs  $N(\bar{B})$ :

- **GLW**:  $D \equiv CP$ -eigenstate: many modes, but small asymmetry. PLB253(1991)483; PLB265(1991)172
- **ADS**:  $D \equiv$  Doubly-Cabibbo suppressed decays (DCSD)  $D^0 \rightarrow K^+ \pi^-$  OS to  $B^-$  decays: large asymmetry, but very few events. PRL78(1997)3257; PRD63(2001)036005
- **GGSZ**:  $D \equiv$  Dalitz: better than a mixture of ADS+GLW  $\Rightarrow$  large asymmetry in some regions, but strong phases varying other the Dalitz plane (model dep. vs indep.) PRL78(1997)3257; PRD68(2003)054018
- **GLS** (Grossman-Ligeti-Soffer): “Less well known” ADS variant  $D \equiv$  Singly-Cabibbo suppressed decays (SCSD) both OS and SS decays comparable in size  $\Rightarrow$  4 amplitudes: 3-body  $KK^0_s \pi$  dominated by coherent  $KK^*$  PRD-RC 67(2003)071301



→ Largest effects due to:

- Charm mixing
  - Charm CPV
- Can't be ignored/neglected any more with improved sensitivity (especially for  $D\pi$ ). Ways exist to account for it, when unfolding  $\gamma$  from modified observables (was PRD-RC72(2005)031501; PRD 67(2003)071301; PLB 649(2007)61; PRD82(2010)034033). A lot of papers + HFAG: PRD89(2014)014021; PRD 87(2013)074002; EPJC73(2013)2476; PRD87(2013)034005; PRL 110(2013)061802 ...

→ Different B-decays ( $DK, D^*K, DK^* \dots$ )  $\Rightarrow$  different hadronic nuisance factors ( $r_B, \delta_B$ ) for each

→ Many more modes explored at LHCb and B-factories (see next slide)



# Measuring $\gamma$ : some other methods/examples (non-exhaustive list)

- Many-body B final states:

- $B^+ \rightarrow DK^+\pi^0$ ,  $B^+ \rightarrow DK^+\pi^+\pi^-$ ,  $B^0 \rightarrow D\pi^-K^+$ ,  $DK_s\pi$
- $B_s \rightarrow DK^+K^-$

Aleksan, Petersen, Soffer (02), Gershon (08), Gershon, Williams (09), Gershon, Poluektov (09, 10), Gronau, London (91), Gronau et al. (04, 07), London, Nandi (12)

- Use  $D^{*0}$  in addition to  $D^0$  Bondar, Gershon (04)

- Use self tagging  $D^{0**}$ ,  $D^{2*-}$  Sinha (04), Gershon (08)

- Use  $DK^*$  & also  $DK^*_{0,2}$  Wang (11)

- Other neutral B decays:

- time dependent CPV (i.e. tagging & vertexing) :  $B_s (B_s) \rightarrow D_s^\mp K^\pm$  or  $D_s^\mp K^\pm \pi \pi$  ( $\sin(2\beta_s + \gamma)$ ) or  $B_d (B_d) \rightarrow D^{(*)\mp} \rho^\pm/\pi^\pm$  ( $\sin(2\beta + \gamma)$ )
- time-integrated, self-tag:  $B_d \rightarrow DK^{*0}$

Aleksan, Dunietz, Kayser(92), Kayser, London (00), Atwood, Soni (03), Fleischer(03), Gronau et al. (04)

- Use beauty baryons:  $\Lambda_b^0 \rightarrow DpK^-$

- Use other b-hadrons:  $B_c^+ \rightarrow D_s^+ D$  &  $B_s \rightarrow D^{(*)0} \phi$



# Measuring $\gamma$ : what LHCb actually has published

Latest update is [LHCb-CONF-2018-002](#) (ICHEP18) last was for [EPS 2017](#)

In Feb 2018 [Joint BESIII-LHCb workshop in IHEP](#)

$B$ decay	$D$ decay	Method	Ref.	Dataset <sup>†</sup>	Status since last combination [3]
$B^+ \rightarrow DK^+$	$D \rightarrow h^+h^-$	GLW	[14]	Run 1 & 2	Minor update
$B^+ \rightarrow DK^+$	$D \rightarrow h^+h^-$	ADS	[15]	Run 1	As before
$B^+ \rightarrow DK^+$	$D \rightarrow h^+\pi^-\pi^+\pi^-$	GLW/ADS	[15]	Run 1	As before
$B^+ \rightarrow DK^+$	$D \rightarrow h^+h^-\pi^0$	GLW/ADS	[16]	Run 1	As before
$B^+ \rightarrow DK^+$	$D \rightarrow K_s^0 h^+ h^-$	GGSZ	[17]	Run 1	As before
$B^+ \rightarrow DK^+$	$D \rightarrow K_s^0 h^+ h^-$	GGSZ	[18]	Run 2	New
$B^+ \rightarrow DK^+$	$D \rightarrow K_s^0 K^+ \pi^-$	GLS	[19]	Run 1	As before
$B^+ \rightarrow D^* K^+$	$D \rightarrow h^+ h^-$	GLW	[14]	Run 1 & 2	Minor update
$B^+ \rightarrow DK^{*+}$	$D \rightarrow h^+ h^-$	GLW/ADS	[20]	Run 1 & 2	Updated results
$B^+ \rightarrow DK^{*+}$	$D \rightarrow h^+ \pi^- \pi^+ \pi^-$	GLW/ADS	[20]	Run 1 & 2	New
$B^+ \rightarrow DK^+ \pi^+ \pi^-$	$D \rightarrow h^+ h^-$	GLW/ADS	[21]	Run 1	As before
$B^0 \rightarrow DK^{*0}$	$D \rightarrow K^+ \pi^-$	ADS	[22]	Run 1	As before
$B^0 \rightarrow DK^+ \pi^-$	$D \rightarrow h^+ h^-$	GLW-Dalitz	[23]	Run 1	As before
$B^0 \rightarrow DK^{*0}$	$D \rightarrow K_s^0 \pi^+ \pi^-$	GGSZ	[24]	Run 1	As before
$B_s^0 \rightarrow D_s^\mp K^\pm$	$D_s^+ \rightarrow h^+ h^- \pi^+$	TD	[25]	Run 1	Updated results
$B^0 \rightarrow D^\mp \pi^\pm$	$D^+ \rightarrow K^+ \pi^- \pi^+$	TD	[26]	Run 1	New

98 observables,  
40 free params.

- [15] PLB **760** (2016) 117
- [16] PRD **91** (2016) 112014
- [17] JHEP **10** (2014) 097
- [19] PLB **773** (2014) 36
- [20] JHEP **11** (2017) 156
- [21] PRD **92** (2015) 112005
- [22] PRD **90** (2014) 112002
- [23] PRD **93** (2016) 112018
- [24] JHEP **08** (2016) 137
- [25] JHEP **03** (2018) 059
- [26] LHCb-PAPER-2018-009

<sup>†</sup> Run 1 corresponds to an integrated luminosity of  $3 \text{ fb}^{-1}$  taken at centre-of-mass energies of 7 and 8 TeV. Run 2 corresponds to an integrated luminosity of  $2 \text{ fb}^{-1}$  taken at a centre-of-mass energy of 13 TeV.

Most are Run1 based or partial Run2, many more to come soon.



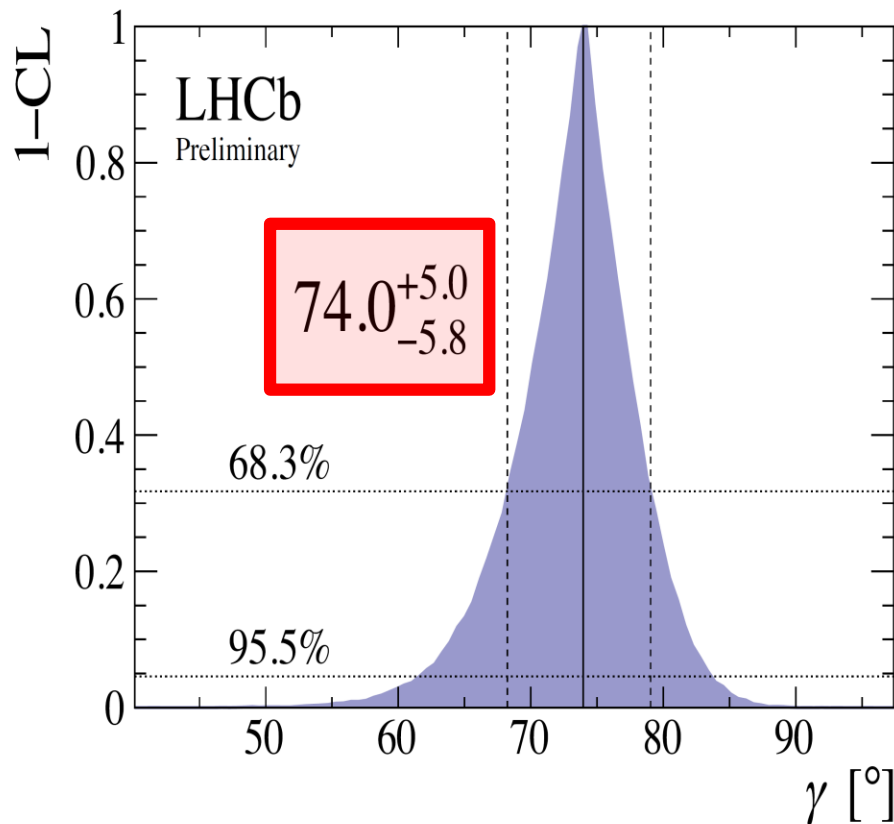
# Measuring $\gamma$ : the latest LHCb average

Latest update is [LHCb-CONF-2018-002](#) (ICHEP18) last was for [EPS 2018](#)

In Feb 2018 [Joint BESIII-LHCb workshop in IHEP](#)

• We now have 98 observables and 40 free parameters

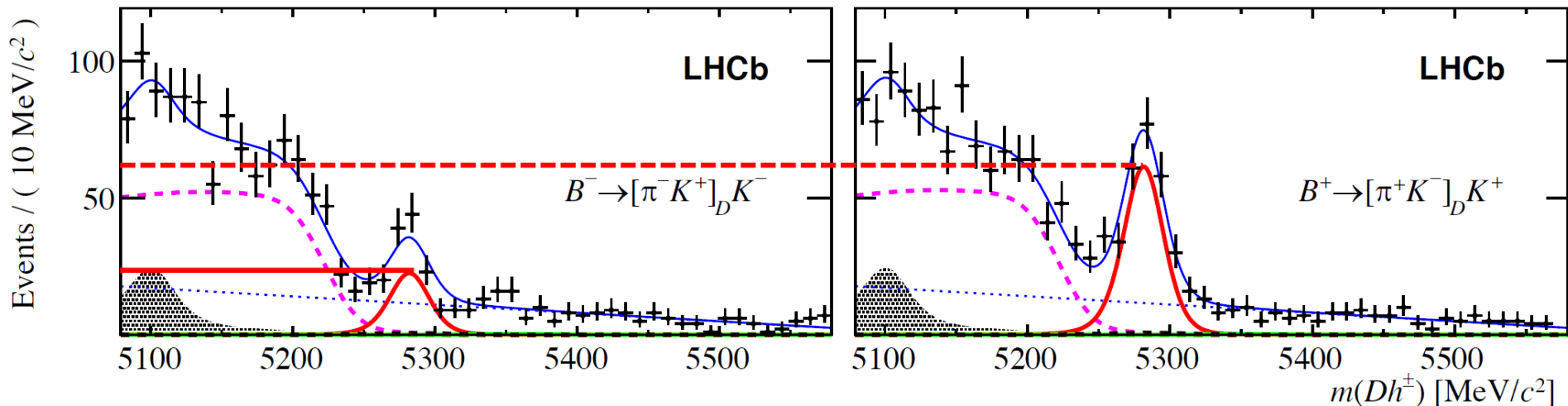
[LHCb-CONF-2018-002]



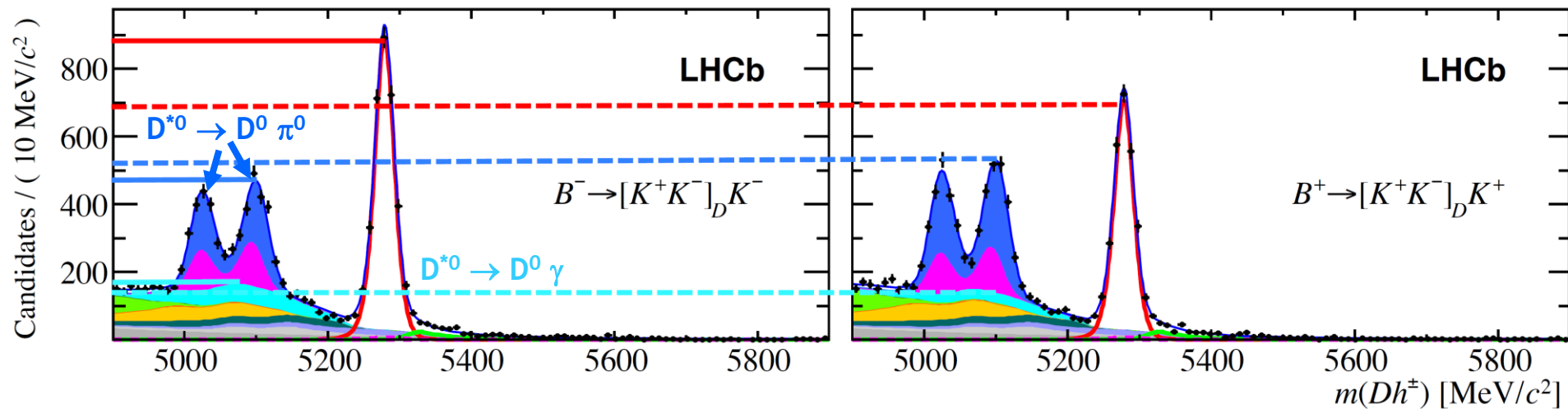
Quantity	Value	68.3% CL	95.5% CL
$\gamma$ [°]	74.0	[68.2, 79.0]	[61.6, 83.7]
$r_B^{DK}$	0.0989	[0.0939, 0.1040]	[0.0891, 0.1087]
$\delta_B^{DK}$ [°]	131.2	[125.3, 136.3]	[118.3, 140.9]
$r_B^{D^*K^+}$	0.191	[0.153, 0.236]	[0.121, 0.287]
$\delta_B^{D^*K^+}$ [°]	331.6	[321.4, 339.8]	[309, 346]
$r_B^{DK^{*+}}$	0.092	[0.059, 0.110]	[0.034, 0.126]
$\delta_B^{DK^{*+}}$ [°]	40	[20, 132]	[5, 155]
$r_B^{DK^{*0}}$	0.221	[0.174, 0.265]	[0.123, 0.309]
$\delta_B^{DK^{*0}}$ [°]	187	[167, 210]	[148, 239]
$r_B^{DK\pi\pi}$	0.081	[0.054, 0.106]	[0.000, 0.125]
$\delta_B^{DK\pi\pi}$ [°]	351.4	[314.0, 359.8]	[180, 360]
$r_B^{D_s^\mp K^\pm}$	0.301	[0.215, 0.391]	[0.14, 0.49]
$\delta_B^{D_s^\mp K^\pm}$ [°]	355	[339, 372]	[321, 390]
$\delta_B^{D_s^\mp \pi^\pm}$ [°]	17	[0, 46]	[0, 76]

# Measuring $\gamma$ : ADS DK & GLW D(\*)K

ADS textbook like [arXiv:1603.08993] -40% asymmetry! (only Run1)



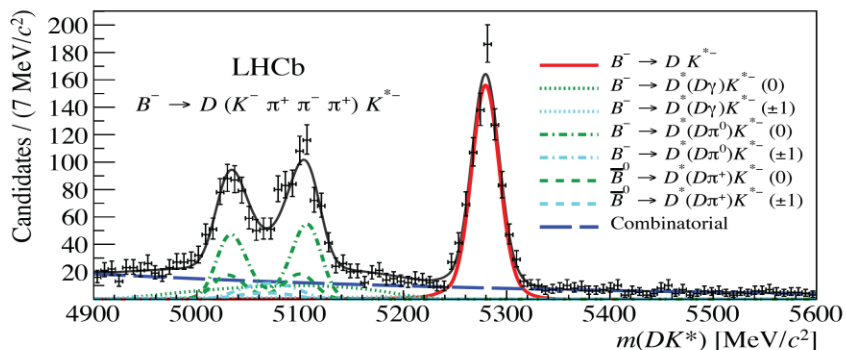
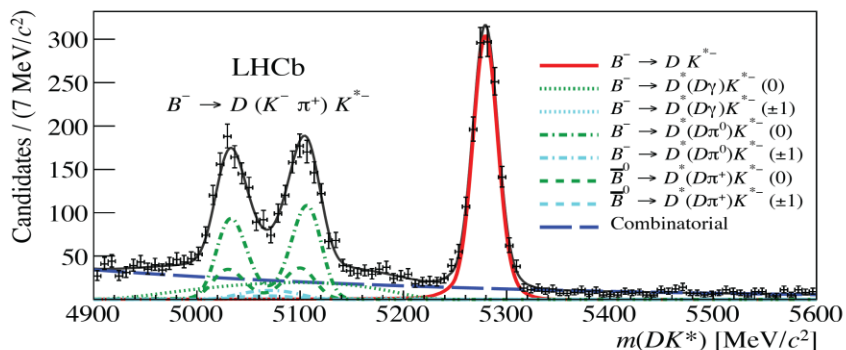
GLW DK and partial D\*K [arXiv:1708.06370] (Run1& "Run2")





# Measuring $\gamma$ : ADS/GLW $DK^*$ -

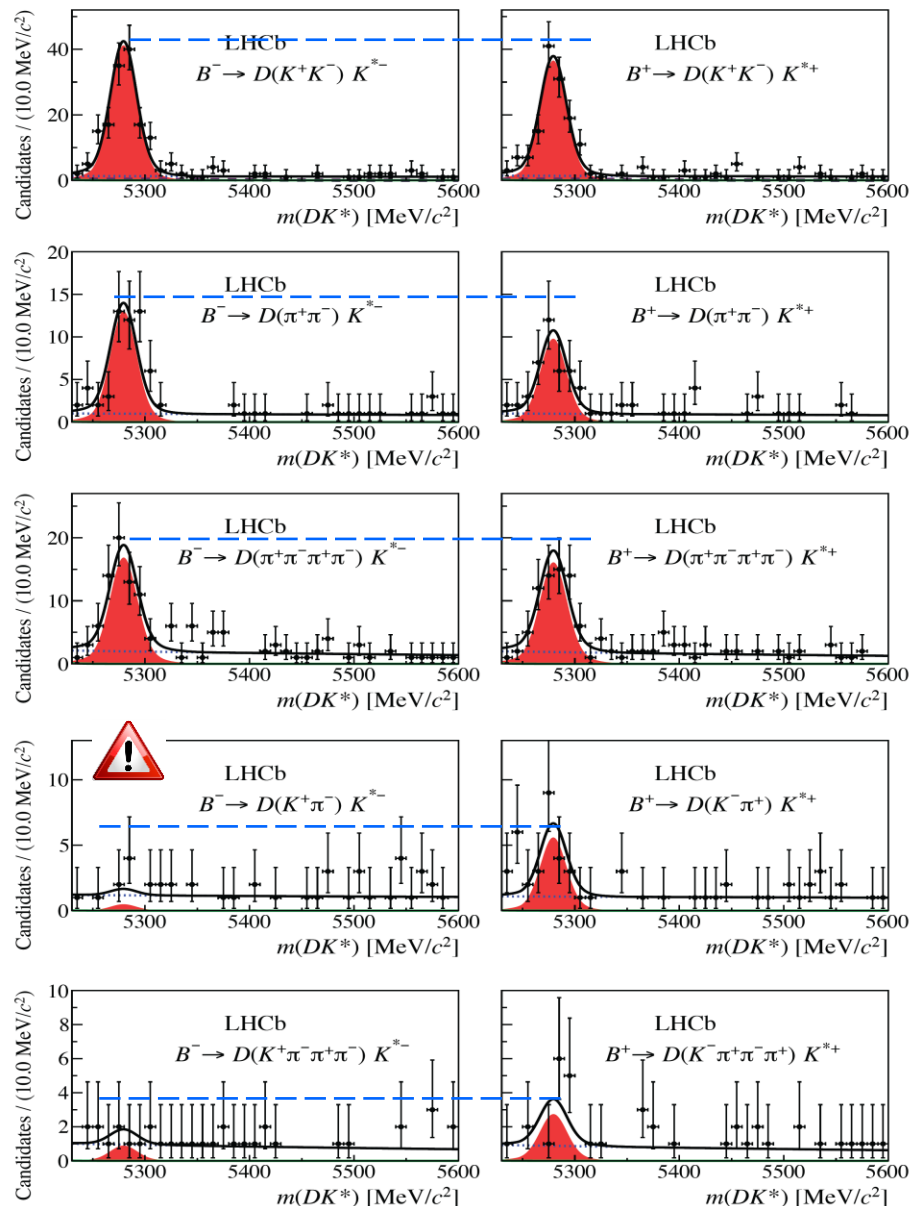
A fit to the favoured decays  
in an extended range fixes  
signal and background models.



Simultaneous fit to 56 subsamples:  
yields of favoured modes and  
 $CP$  observables.

JHEP 11(2017) 156  
(Run1& "Run2")

$K^*$  in  $K_S \pi^-$  and  $K \pi^0$  is underway



# Measuring $\gamma$ : ADS/GLW DK\*-

JHEP 11(2017) 156

$$A_{CP+} = 0.08 \pm 0.06 \pm 0.01$$

$$R_{CP+} = 1.18 \pm 0.08 \pm 0.01$$

$$R_{ADS}^{K\pi} = 0.011 \pm 0.004 \pm 0.001$$

$$A_{ADS}^{K\pi} = -0.81 \pm 0.17 \pm 0.04$$

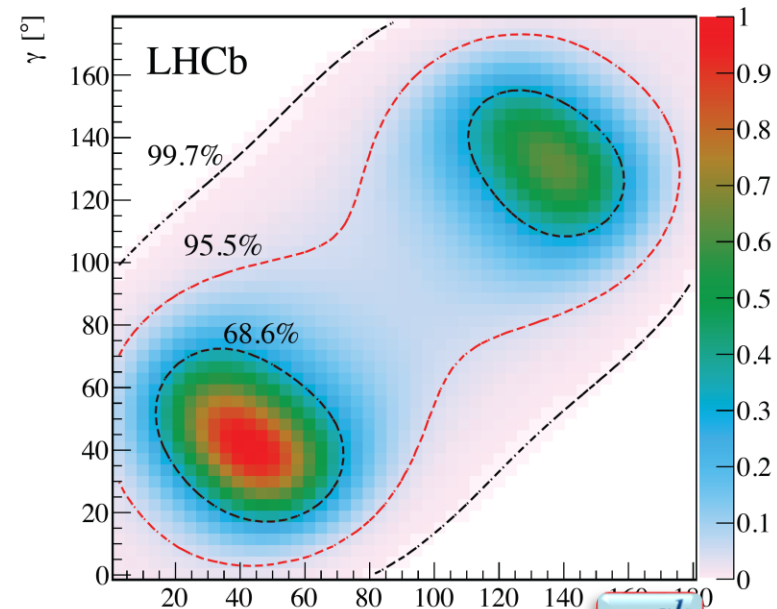
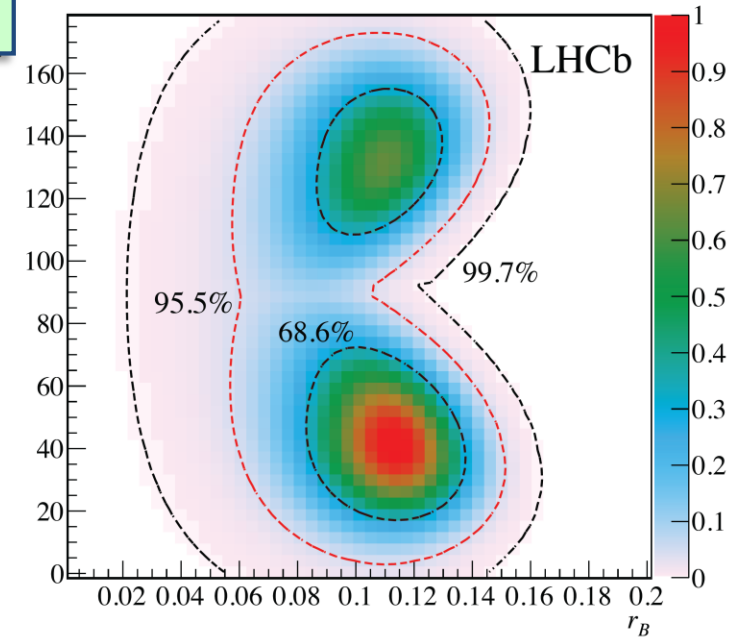
 Huge asymmetry in ADS

$$A_{ADS}^{K\pi\pi\pi} = -0.45 \pm 0.21 \pm 0.14$$

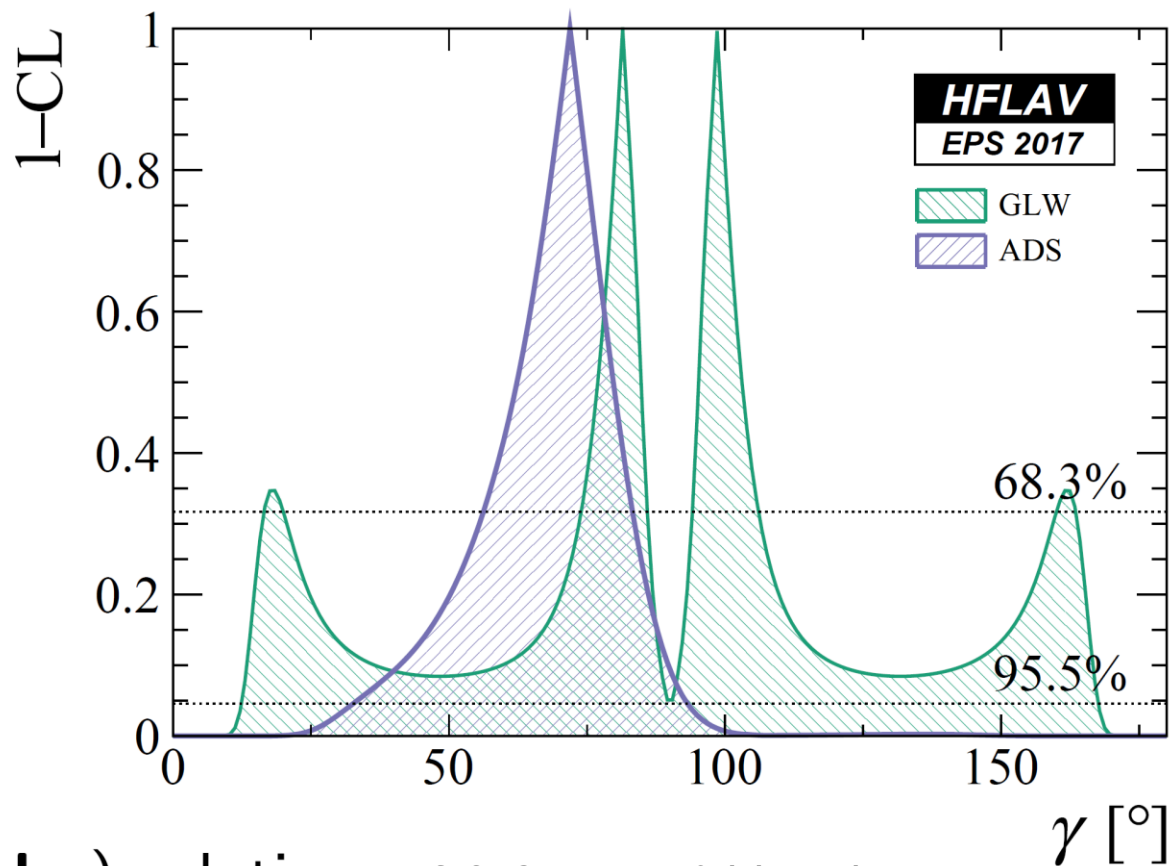
$$R_{ADS}^{K\pi\pi\pi} = 0.011 \pm 0.005 \pm 0.003$$

Values are inputs to the  
 $\gamma$  combination

(Run1& "Run2")



# Measuring $\gamma$ : ADS DK and GLW D(\*)K



- ▶ A single (**yet broader**) solution (ADS & GLW is 4-folds ambiguous)
- ▶ Require knowledge of  $r_D$ ,  $\delta_D$ ,  $\kappa_D$  from charm friends

**CLEO-c**  
**HFLAV**

**BESIII**



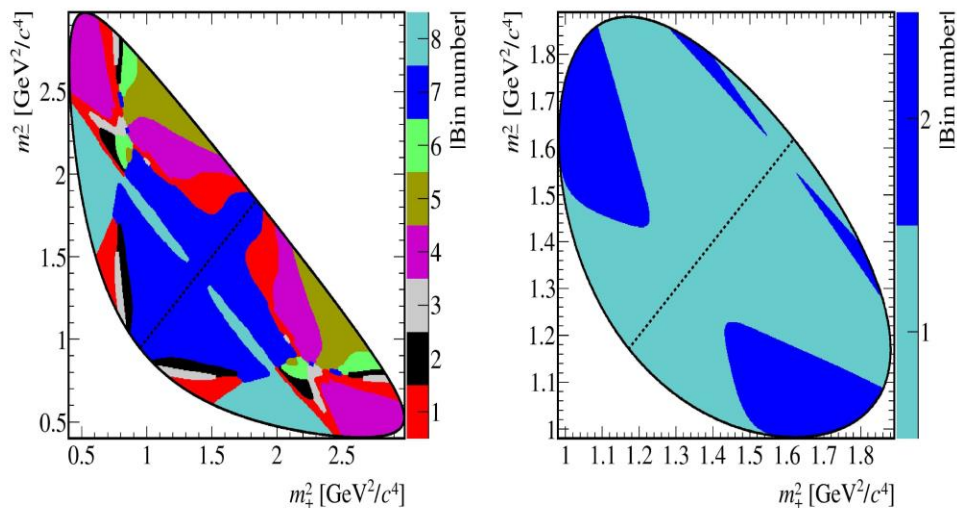
# The most precise measurement of $\gamma$ :

## GGSZ DK and $D \rightarrow K_S \pi \pi$ & $K_S K K$

### Model Independent Method (MIM)

- GGSZ method for 3 body decays like  $D \rightarrow K_S^0 \pi^+ \pi^-$  [Phys. Rev. D68 (2003) 054018]
  - Strong phase variation across the D Dalitz plot required as an input
  - Model independent - take inputs from quantum correlated  $D^0 \bar{D}^0$  decays (CLEO-c)
  - Model dependent - perform an amplitude analysis to the D Dalitz plot
- LHCb Run II analysis with  $B^- \rightarrow D(K_S^0 \pi^+ \pi^-, K_S^0 K^+ K^-) K^-$ 
  - New analysis with Run II data
  - Take strong phase information from CLEO-c in bins of the D Dalitz plot
  - Bins optimised for best sensitivity to  $\gamma$ , strong phase is  $\sim$ constant across each bin

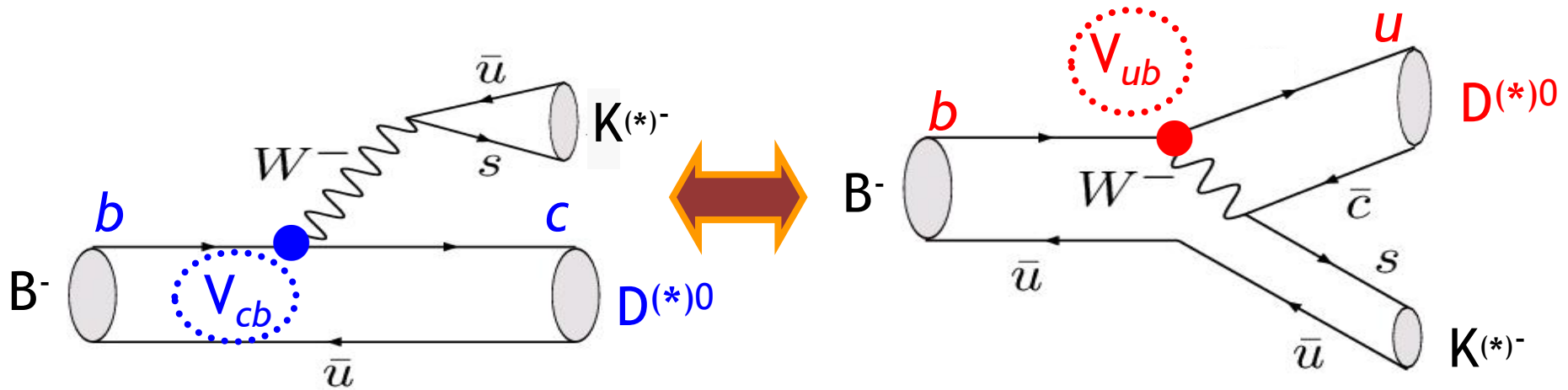
[LHCb-PAPER-2018-017]



- $B \rightarrow D^{*\pm} \mu^\mp \nu_\mu X$ ,  $B^\pm \rightarrow D \pi^\pm$ : control channels

$$\gamma \text{ in } B^- \rightarrow \tilde{D}^{(*)0} K^{(*)-}$$

Same final state  $\tilde{D}^0 \equiv [D^0/D^0]$



$$\gamma \equiv \arg \left[ - \frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} \right]$$



# How does this GGSZ MIM work ?

- The amplitude for  $B^- \rightarrow [K_S^0 h^+ h^-]_D K^-$  :

$$A_{B^-} \propto A_D(m_-^2, m_+^2) + r_B e^{i(\delta_B - \gamma)} A_{\bar{D}}(m_-^2, m_+^2)$$

- The Dalitz plot density :

$$\frac{d\Gamma}{dm_-^2 dm_+^2} = A_D^2(m_-^2, m_+^2) + r_B^2 A_D^2(m_+^2, m_-^2) +$$

$$2r_B \operatorname{Re}[A_D(m_-^2, m_+^2) A_D^*(m_+^2, m_-^2) e^{-i(\delta_B - \gamma)}]$$

symmetric w.r.t

$$m_+ = m_-, \\ m_{\pm} \equiv m(K_S^0 h^{\pm})$$

- Measure the yields in each of the bins of the Dalitz plot

[LHCb-PAPER-2018-017]

$$N_{\pm i}^+ = h_{B^+} (F_{\mp i} + (x_+^2 + y_+^2) F_{\pm i} + 2\sqrt{F_i F_{-i}} (x_+ c_{\pm i} + y_+ s_{\pm i}))$$

$$N_{\pm i}^- = h_{B^-} (F_{\pm i} + (x_-^2 + y_-^2) F_{\mp i} + 2\sqrt{F_i F_{-i}} (x_- c_{\pm i} + y_- s_{\pm i}))$$

- Fraction of  $D^0$  and  $\bar{D}^0$  in each bin (from semileptonic control sample)
- Strong phase measurements from CLEO-c measurements of QC  $D^0 \bar{D}^0$  decays
- The parameters of interest!

$$x_{\pm} = r_B \cos(\delta_B \pm \gamma) \quad y_{\pm} = r_B \sin(\delta_B \pm \gamma)$$

Ratio of B decay amplitudes

Strong phase difference of B decay amplitudes

# Eagerly waiting for this to be combined/deployed !

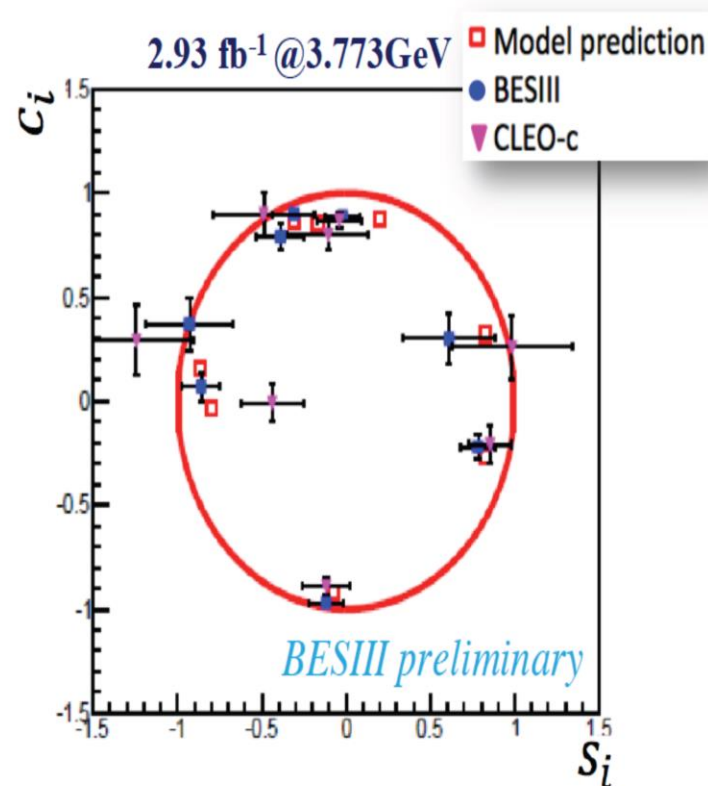
## We need BESIII for this and other D decays strong inputs



- $D^0 \rightarrow K_S \pi \pi^+$  strong phase differences  $c_i$  and  $s_i$

Bins	$c_i$		$s_i$	
	BES-III	CLEO-c	BES-III	CLEO-c
1	$0.066 \pm 0.066$	$-0.009 \pm 0.088$	$-0.843 \pm 0.119$	$-0.438 \pm 0.184$
2	$0.796 \pm 0.061$	$0.900 \pm 0.106$	$-0.357 \pm 0.148$	$-0.490 \pm 0.295$
3	$0.361 \pm 0.125$	$0.292 \pm 0.168$	$-0.962 \pm 0.258$	$-1.243 \pm 0.341$
4	$-0.985 \pm 0.017$	$-0.890 \pm 0.041$	$-0.090 \pm 0.093$	$-0.119 \pm 0.141$
5	$-0.278 \pm 0.056$	$-0.208 \pm 0.085$	$0.778 \pm 0.092$	$0.853 \pm 0.123$
6	$0.267 \pm 0.119$	$0.258 \pm 0.155$	$0.635 \pm 0.293$	$0.984 \pm 0.357$
7	$0.902 \pm 0.017$	$0.869 \pm 0.034$	$-0.018 \pm 0.103$	$-0.041 \pm 0.132$
8	$0.888 \pm 0.036$	$0.798 \pm 0.070$	$-0.301 \pm 0.140$	$-0.107 \pm 0.240$

CLEO-c results can be found in Phys.Rev. D82 (2010) 112006



Dan Ambrose, APS 2014

**This (CLEO-c) limits the systematics on  $\gamma$  GGSZ: 4° (strong phase map) wrt to 2° (LHCb exp.)**

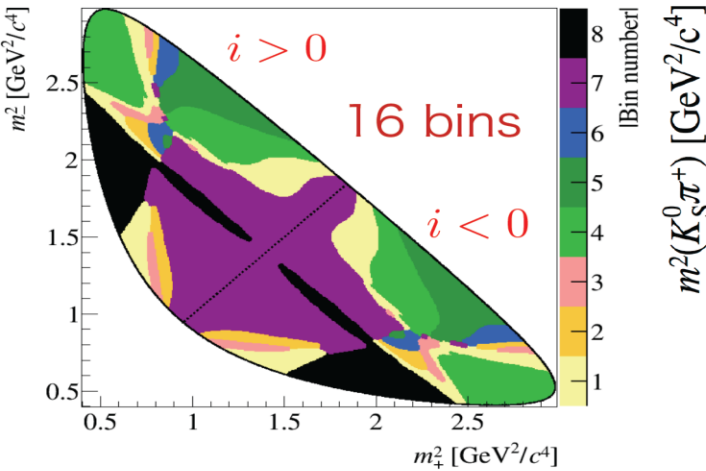
2° achievable, see arXiv:1712.07853

(Craik, Gershon, Poluektov:  $B^0 \rightarrow DK^+ \pi^-$ ,  $D \rightarrow K^0_S \pi^+ \pi^-$  double Dalitz plot analysis)

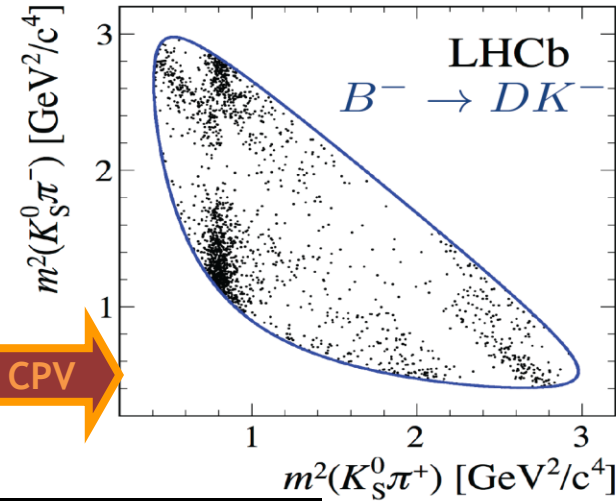
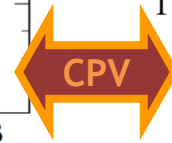
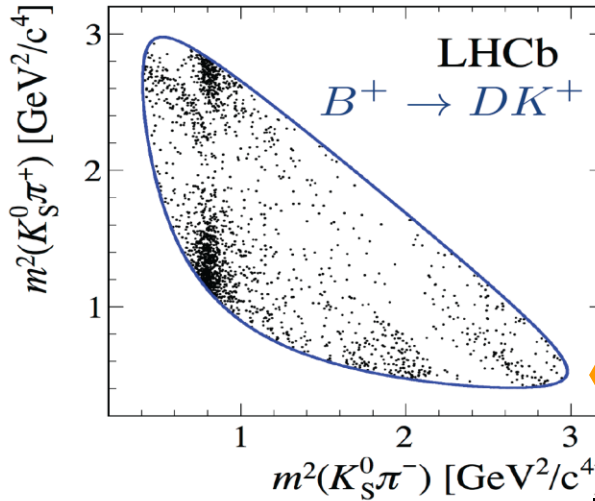


# Following the B-mass fits perform the CP fit for Extract yields in each bin of the Dalitz plot

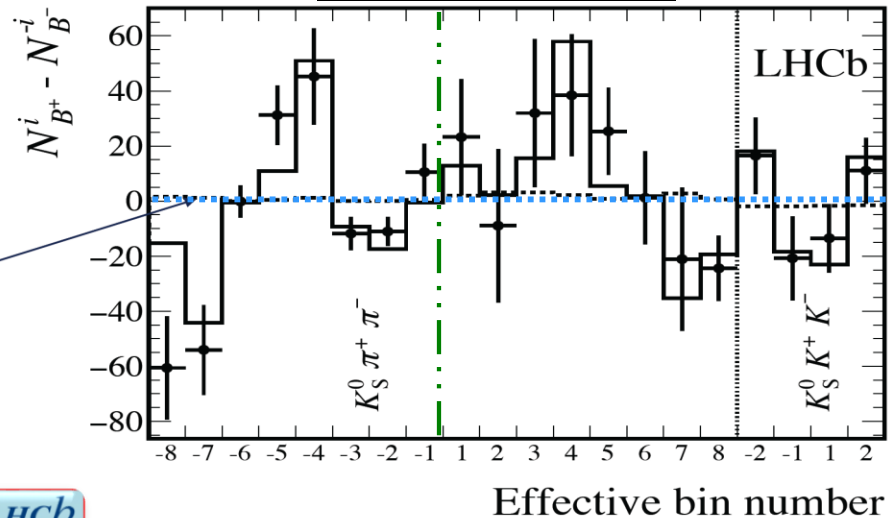
(“Run2”)



$D \rightarrow K_S^0 \pi^+ \pi^-$  ( $\sim 3.8K$   $B^\pm$  candidates)



Asymmetry in bins



- $B^\pm \rightarrow DK^\pm$  yields determined independently as a cross-check, and compared to the nominal fit

- data fitted assuming no CPV  
 $x_+ = x_- \equiv x_0, \quad y_+ = y_- \equiv y_0$

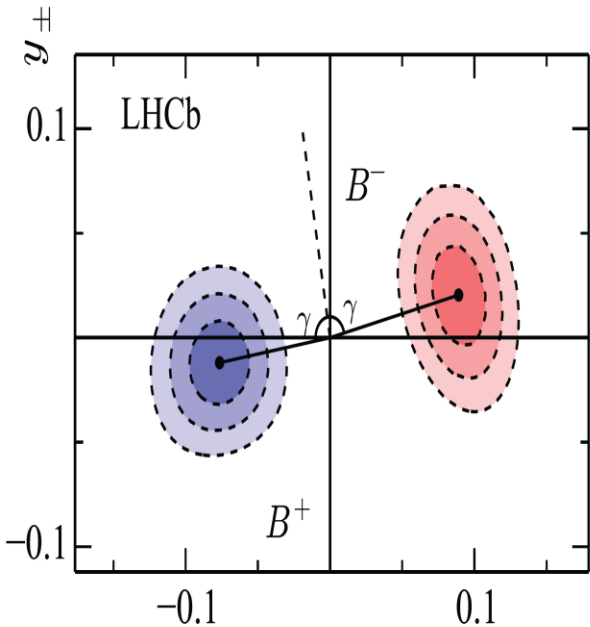
- p-value of  $2 \times 10^{-6}$  disfavors CP-conserving hypothesis



# GGSZ MIM Run2 & 1+2

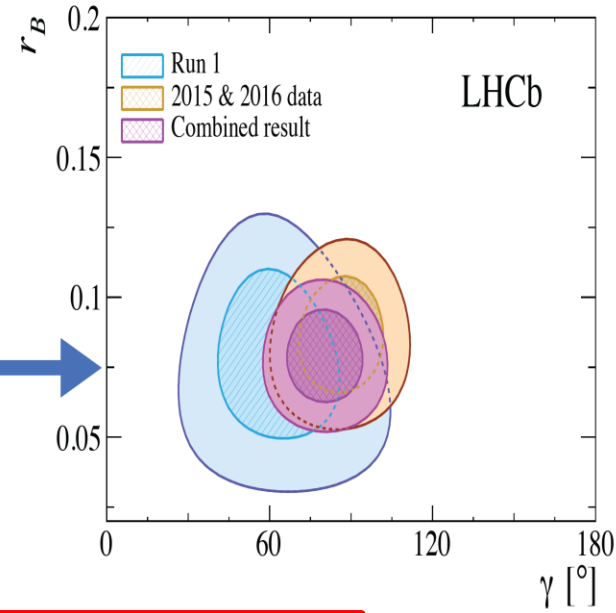
[LHCb-PAPER-2018-017]

• Following the mass fits perform the CP fit for  $x_{\pm}, y_{\pm}$



Run II results

Run I + II combination



stat+syst+Cleo-c strong phase  $x_{\pm}$

$$x_{-} = (9.0 \pm 1.7 \pm 0.7 \pm 0.4) \times 10^{-2}$$

$$y_{-} = (2.1 \pm 2.2 \pm 0.5 \pm 1.1) \times 10^{-2}$$

$$x_{+} = (-7.7 \pm 1.9 \pm 0.7 \pm 0.4) \times 10^{-2}$$

$$y_{+} = (-1.0 \pm 1.9 \pm 0.4 \pm 0.9) \times 10^{-2}$$

$$|(x_{+}, y_{+}) - (x_{-}, y_{-})| = (17.0 \pm 2.7) \times 10^{-2}$$

6.4σ : first observation of CPV in  $B^{\pm} \rightarrow DK^{\pm}$  with  $D^0 \rightarrow K_S^0 h^+ h^-$

Run1+2

$$\gamma = 80^{\circ} \begin{matrix} +10^{\circ} \\ -9^{\circ} \end{matrix} \begin{matrix} (+19^{\circ}) \\ (-18^{\circ}) \end{matrix}$$

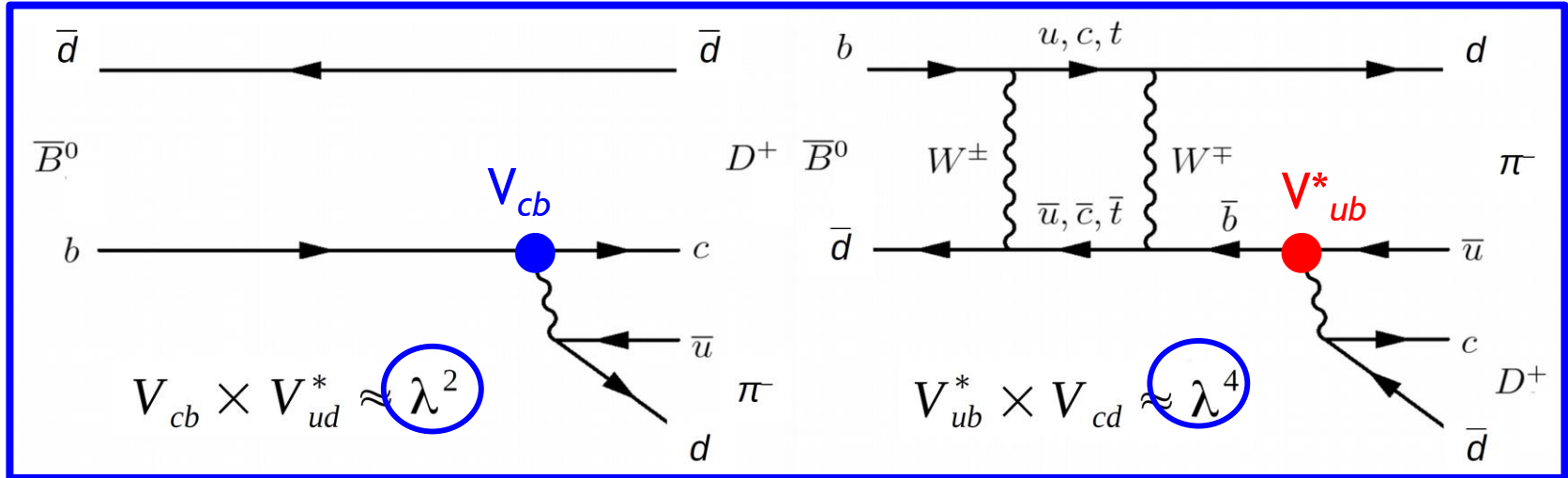
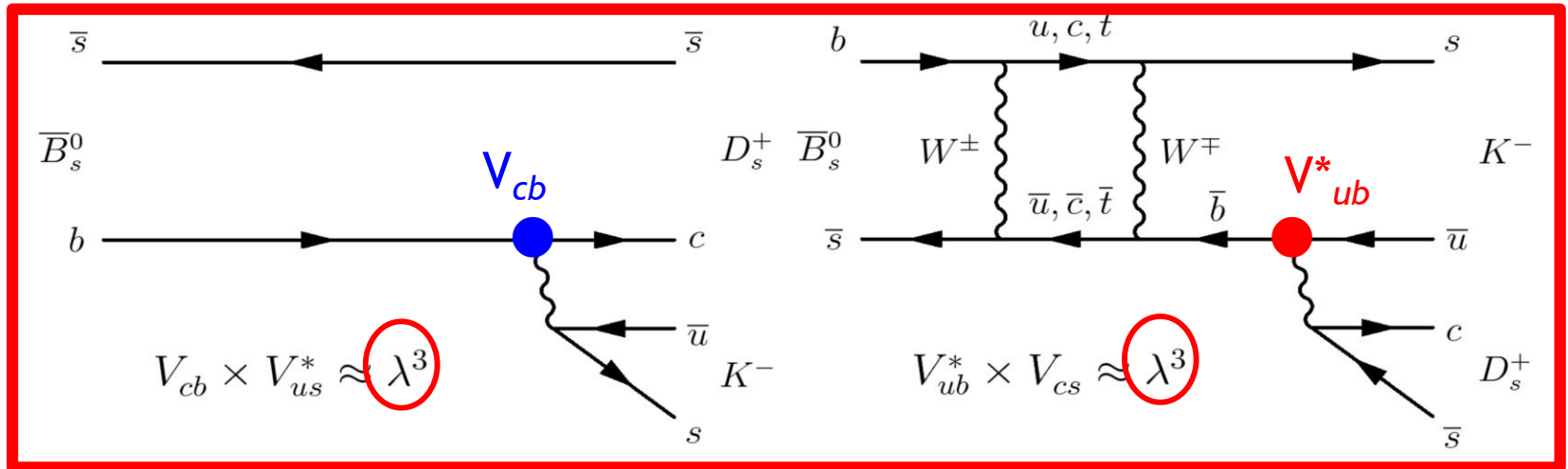
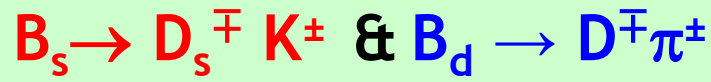
$$r_B = 0.080 \begin{matrix} +0.011 \\ -0.011 \end{matrix} \begin{matrix} (+0.022) \\ (-0.023) \end{matrix}$$

$$\delta_B = 110^{\circ} \begin{matrix} +10^{\circ} \\ -10^{\circ} \end{matrix} \begin{matrix} (+19^{\circ}) \\ (-20^{\circ}) \end{matrix}$$

68, 95% CL



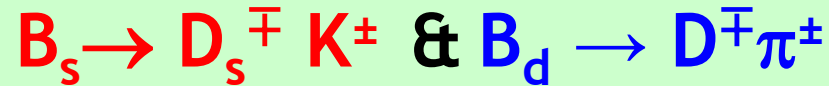
# Time dependent CPV measurements



→ Sensitive to  $\gamma - 2\beta_s$  ( $B_s \rightarrow D_s K$ ) or  $\gamma + 2\beta$  ( $B_0 \rightarrow D \pi$ ), i.e. not Trees !!!!  
 Know  $B_{(s)}$  independently → sensitivity to  $\gamma$  [or vice versa]



# Time dependent CPV measurements



PROS & CONS

$B_s \rightarrow D_s K$  (LHCb golden mode:  
vertexing/PID/trigger)

- Smaller yields
  - background challenges
  - control samples available
- Fast oscillations
- Non-zero  $\Delta\Gamma$ s
  - extra observables
- Large interference effects

$B^0 \rightarrow D\pi$  (challenging but  
excellent LHCb sensitivity)

- Huge yields
  - little background
  - control sample challenges
- Slow oscillations
- Negligible  $\Delta\Gamma$ d
  - fewer observables
- Small interference effects

(Run1)

# TD CPV $B_s \rightarrow D_s \bar{F} K^\pm$

$$\frac{d\Gamma_{B_s^0 \rightarrow f}(t)}{dt} = \frac{1}{2} |A_f|^2 (1 + |\lambda_f|^2) e^{-\Gamma_s t} \left[ \cosh\left(\frac{\Delta\Gamma_s t}{2}\right) + \underline{A_f^{\Delta\Gamma}} \sinh\left(\frac{\Delta\Gamma_s t}{2}\right) \right. \\ \left. + \underline{C_f} \cos(\Delta m_s t) - \underline{S_f} \sin(\Delta m_s t) \right],$$

$$\frac{d\Gamma_{\bar{B}_s^0 \rightarrow f}(t)}{dt} = \frac{1}{2} |A_f|^2 \left| \frac{p}{q} \right|^2 (1 + |\lambda_f|^2) e^{-\Gamma_s t} \left[ \cosh\left(\frac{\Delta\Gamma_s t}{2}\right) + \underline{A_f^{\Delta\Gamma}} \sinh\left(\frac{\Delta\Gamma_s t}{2}\right) \right. \\ \left. - \underline{C_f} \cos(\Delta m_s t) + \underline{S_f} \sin(\Delta m_s t) \right],$$

Five observables  
for three unknowns  
→ measure  $\gamma - 2\beta_s$   
(up to ambiguity)

... and similar equations for  $\bar{f}$  (e.g.  $f = D_s^- K^+$ ,  $\bar{f} = D_s^+ K^-$ )

$$C_f = \frac{1 - r_{D_s K}^2}{1 + r_{D_s K}^2},$$

Also determine strong  
phase difference  $\delta$

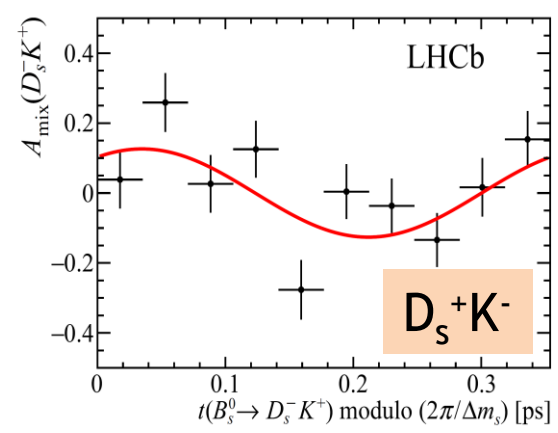
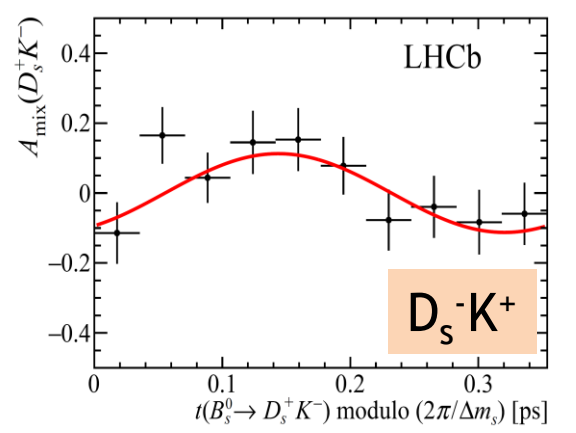
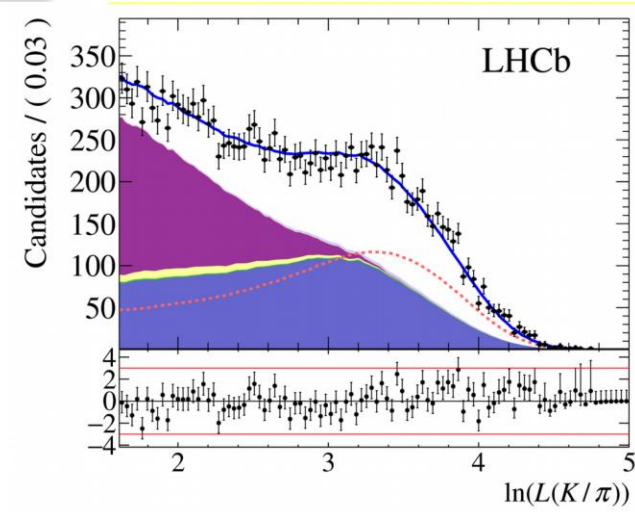
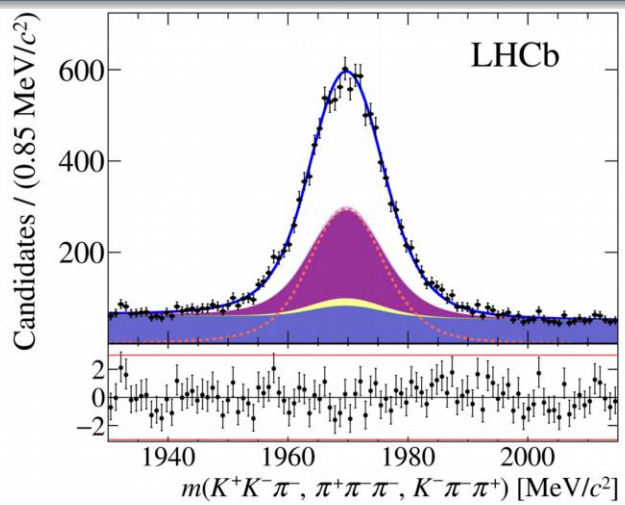
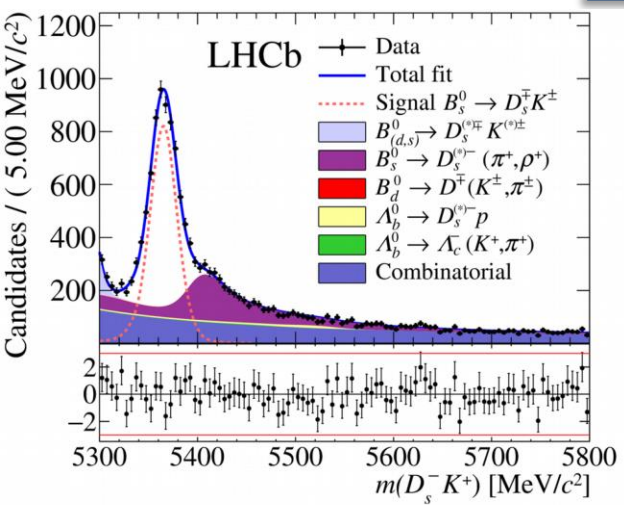
$$A_f^{\Delta\Gamma} = \frac{-2r_{D_s K} \cos(\delta - (\gamma - 2\beta_s))}{1 + r_{D_s K}^2}, \quad A_{\bar{f}}^{\Delta\Gamma} = \frac{-2r_{D_s K} \cos(\delta + (\gamma - 2\beta_s))}{1 + r_{D_s K}^2},$$

$$S_f = \frac{2r_{D_s K} \sin(\delta - (\gamma - 2\beta_s))}{1 + r_{D_s K}^2}, \quad S_{\bar{f}} = \frac{-2r_{D_s K} \sin(\delta + (\gamma - 2\beta_s))}{1 + r_{D_s K}^2}.$$

5955±90 signal events

**TD CPV  $B_s \rightarrow D_s^\mp K^\pm$**

efficient flavour tagging  
 $\epsilon_{\text{eff}} = (5.80 \pm 0.25)\%$



Parameter	Value
$C_f$	$0.730 \pm 0.142 \pm 0.045$
$A_f^{\Delta\Gamma}$	$0.387 \pm 0.277 \pm 0.153$
$A_{\bar{f}}^{\Delta\Gamma}$	$0.308 \pm 0.275 \pm 0.152$
$S_f$	$-0.519 \pm 0.202 \pm 0.070$
$S_{\bar{f}}$	$-0.489 \pm 0.196 \pm 0.068$

$$\gamma = (128^{+17}_{-22})^\circ$$

$$\delta = (358^{+13}_{-14})^\circ$$

$$r_{D_s K} = 0.37^{+0.10}_{-0.09}$$

**3.8σ evidence for CP violation**  
 2.3σ compatibility wrt LHCb@2016 average



(Run1)

# TD CPV $B_d \rightarrow D^{\mp} \pi^{\pm}$

$$\Gamma_{B^0 \rightarrow f}(t) \propto e^{-\Gamma t} [1 + \underline{C_f} \cos(\Delta m t) - \underline{S_f} \sin(\Delta m t)]$$

$$\Gamma_{B^0 \rightarrow \bar{f}}(t) \propto e^{-\Gamma t} [1 + \underline{C_{\bar{f}}} \cos(\Delta m t) - \underline{S_{\bar{f}}} \sin(\Delta m t)]$$

...and similar Eqs. for  $B^{\bar{0}}$  (e.g.  $f = D^{\bar{0}} \pi^+$ ,  $\bar{f} = D^+ \pi^{\bar{0}}$ )

$$C_f = \frac{1 - r_{D\pi}^2}{1 + r_{D\pi}^2} = -C_{\bar{f}},$$

But  $r_{D\pi}$  is about 2% so C is very close to 1 !

$$S_f = -\frac{2r_{D\pi} \sin[\delta - (2\beta + \gamma)]}{1 + r_{D\pi}^2},$$

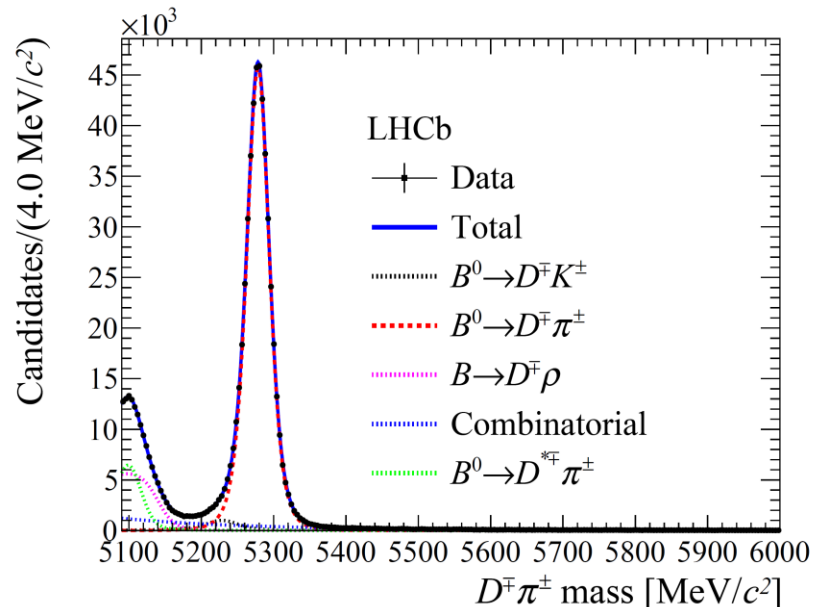
$$S_{\bar{f}} = \frac{2r_{D\pi} \sin[\delta + (2\beta + \gamma)]}{1 + r_{D\pi}^2},$$

So we have only 2 observables  
for three unknowns

➔ need external input to measure  $\gamma+2\beta$

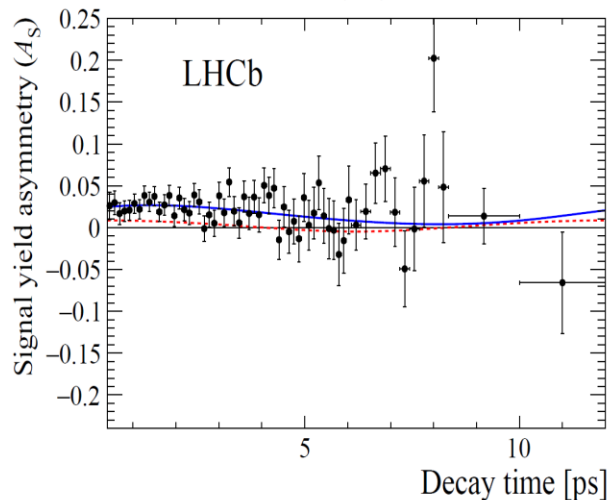
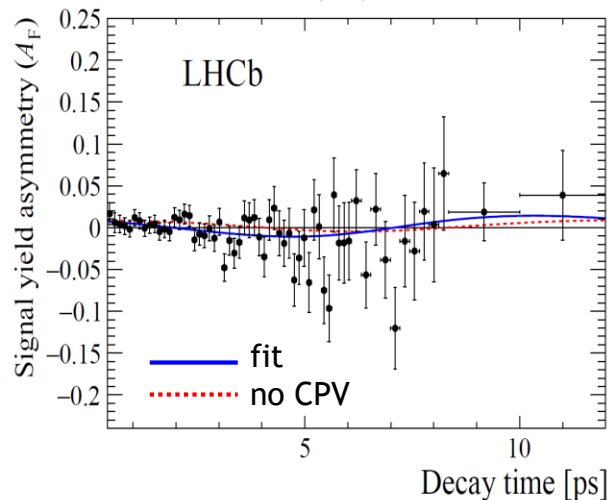
Signal yield of  $479\,000 \pm 700$  !!!  
Against  $34\,400 \pm 300$  bkgd

Flavour Tagging  $\varepsilon_{\text{eff}} = (5.59 \pm 0.01)\%$



(Run1)

# TD CPV $B_d \rightarrow D^{\mp} \pi^{\pm}$

favoured (F)  $\bar{b} \rightarrow \bar{c} u \bar{d}$ suppressed (S)  $\bar{b} \rightarrow \bar{u} c \bar{d}$ 

$$A_F = \frac{\Gamma_{B^0 \rightarrow f}(t) - \Gamma_{\bar{B}^0 \rightarrow \bar{f}}(t)}{\Gamma_{B^0 \rightarrow f}(t) + \Gamma_{\bar{B}^0 \rightarrow \bar{f}}(t)}$$

$$A_S = \frac{\Gamma_{\bar{B}^0 \rightarrow f}(t) - \Gamma_{B^0 \rightarrow \bar{f}}(t)}{\Gamma_{\bar{B}^0 \rightarrow f}(t) + \Gamma_{B^0 \rightarrow \bar{f}}(t)}$$

$$S_f = 0.058 \pm 0.020 \text{ (stat)} \pm 0.011 \text{ (syst)}$$

$$S_{\bar{f}} = 0.038 \pm 0.020 \text{ (stat)} \pm 0.007 \text{ (syst)}$$

correlations of 60% (-41%) for  
statistical (systematic) uncertainties

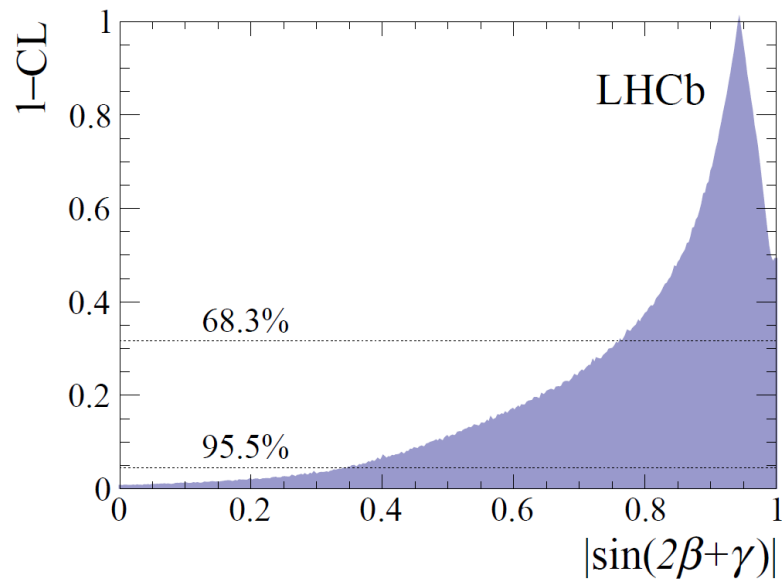
→  $r_{D\pi}$  from external inputs (PDG, LQCD, CKMfitter):

$$r_{D\pi} = \tan \theta_c \frac{f_{D^+}}{f_{D_s}} \sqrt{\frac{\mathcal{B}(B^0 \rightarrow D_s^+ \pi^-)}{\mathcal{B}(B^0 \rightarrow D^- \pi^+)}}$$

$$= (1.82 \pm 0.12 \pm 0.36)\% \text{ (includes 20\% SU(2) breaking)}$$

→ HFLAV  $B=(22.2 \pm 0.7)\%$ , bings to CPV@2.7  $\sigma$ :

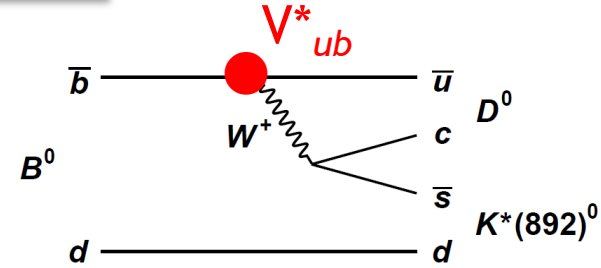
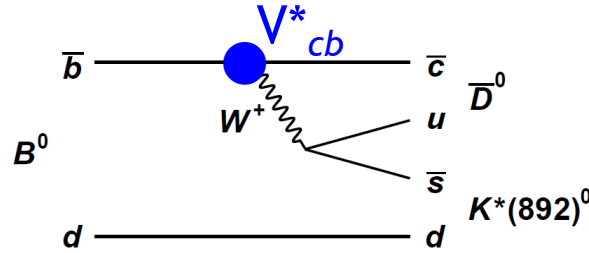
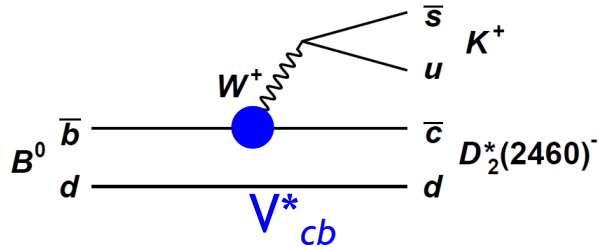
$$\gamma \in [5, 86]^\circ \cup [185, 266]^\circ \text{ @68\% CL}$$



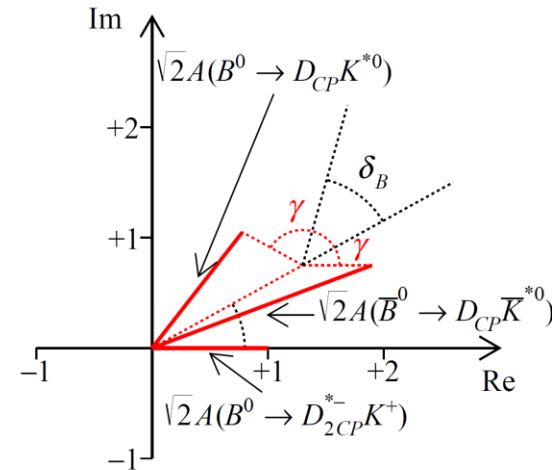
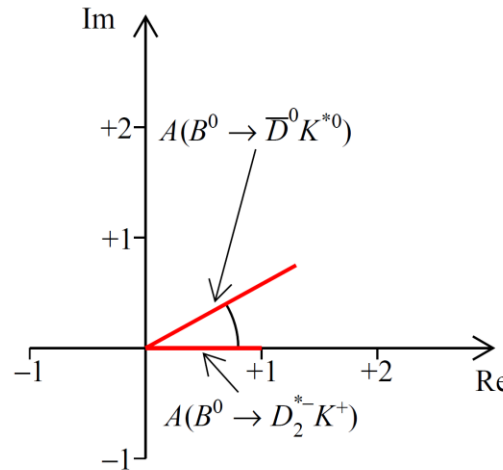


(Run1)

# 3-body decay $B^0 \rightarrow D\pi^-K^+$



→ 1<sup>st</sup> idea Gershon, Williams (2009):  
use Dalitz structure of B decays



$B^0 \rightarrow D\pi^-K^+$  [Phys. Rev. D80 (2009) 092002]

→ Get multiple interfering resonances which increase sensitivity to  
 $D^*_0(2400)^-, D^*_2(2460)^-, K^*(892)^0, K^*(1410)^0, K^*_2(1430)^0$

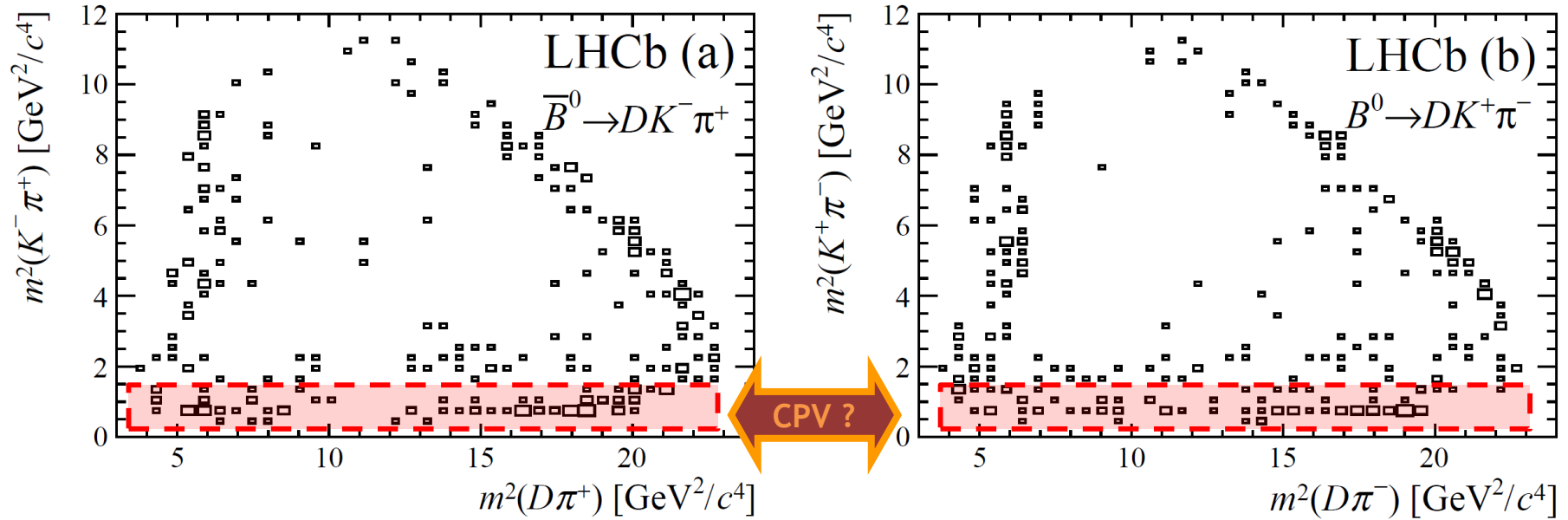
→ Fit B decay Dalitz Plot for cartesian parameters  
(similar to GGSZ except for the B not the D)

- $D_{CP+} \rightarrow K^+K^-, \pi^+\pi^-$  - GLW-Dalitz (done by LHCb - [arXiv:1602.03455]) HERE !
- $D \rightarrow K\pi$  - ADS-Dalitz (difficult due to backgrounds from  $B^0_s \rightarrow D^{(*)0}K^+\pi^-$ )
- $D \rightarrow K^0_S \pi^+\pi^-$  - GGSZ-Dalitz (double Dalitz!)



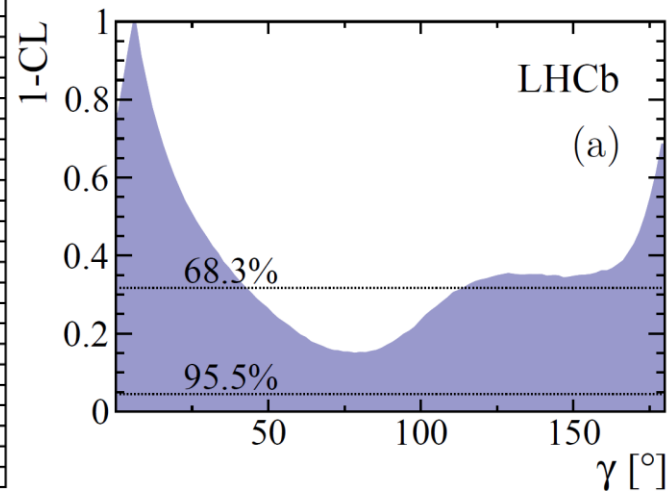
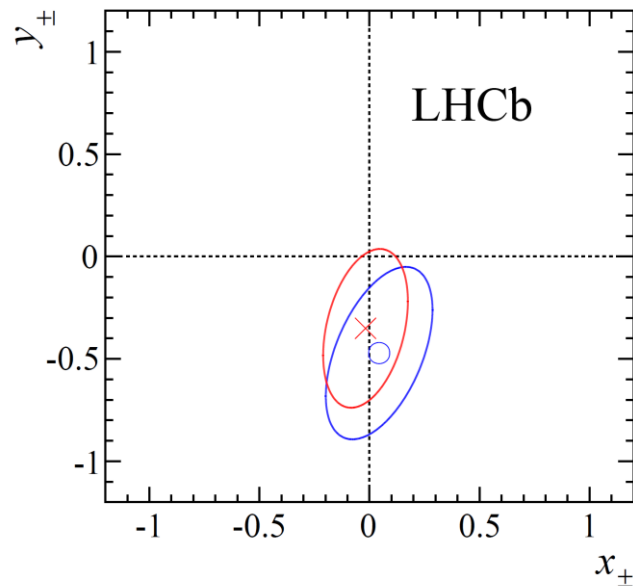
(Run1)

# 3-body decay $B^0 \rightarrow D\pi^-K^+$



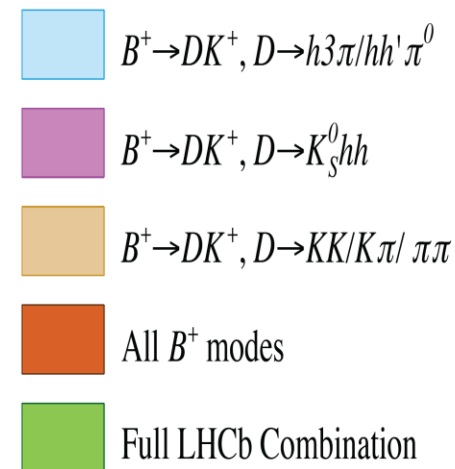
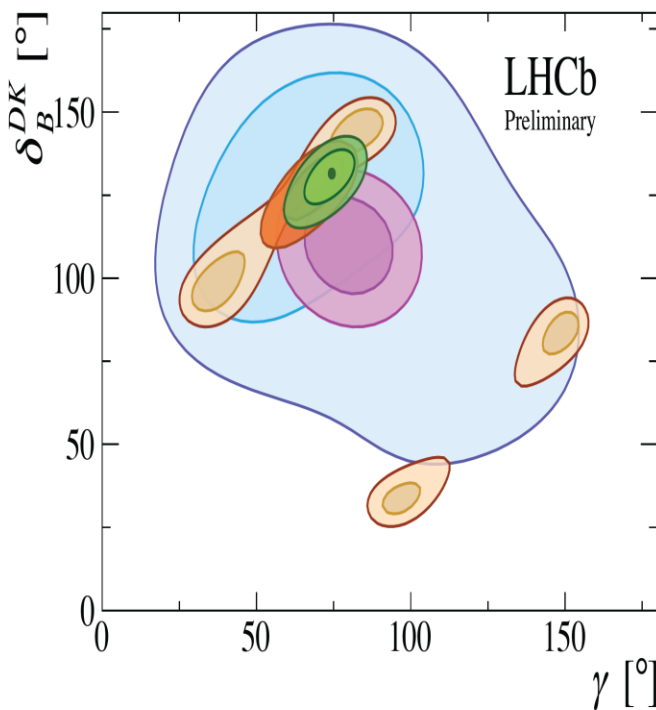
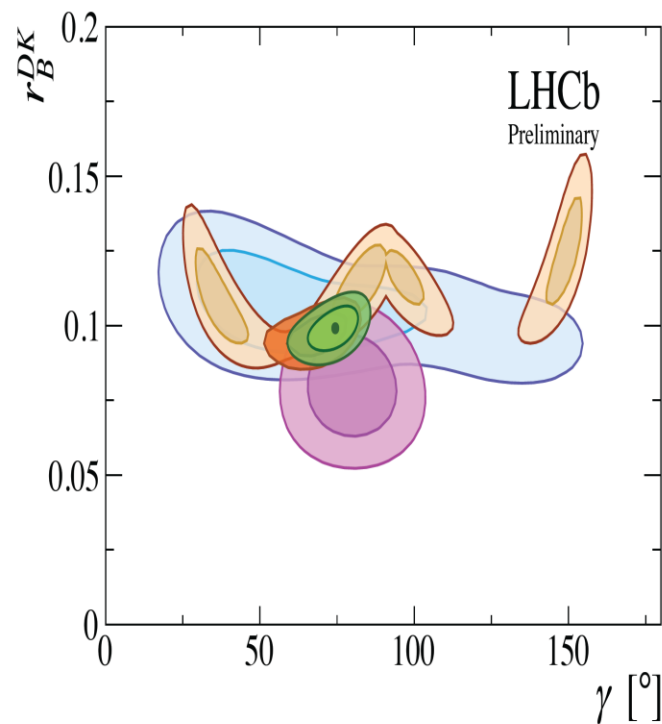
For the first time in the  $B^0 \rightarrow DK^*(892)^0$  decay

- @68% CL
- no CPV  $\equiv (0,0)$
- yet weak constraint
- proof of feasibility



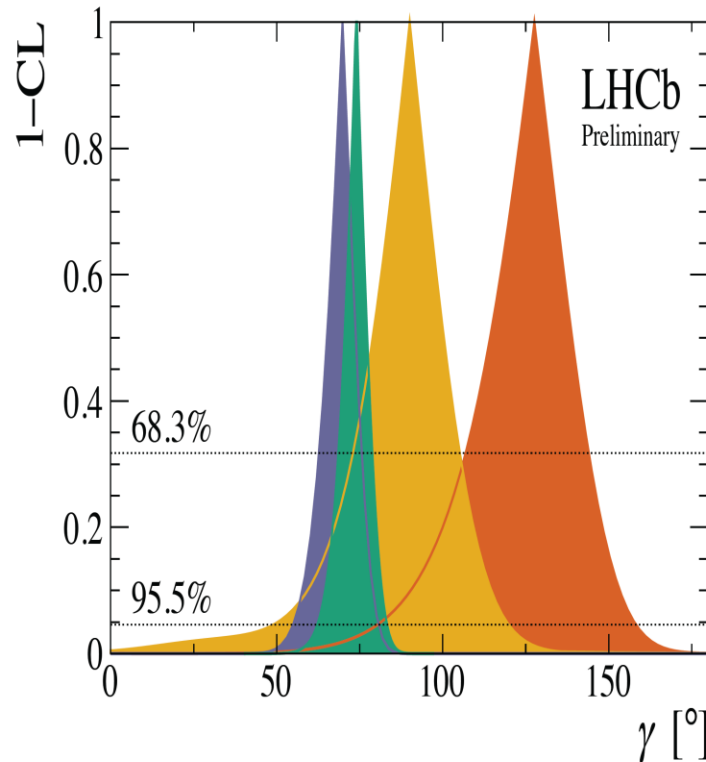
# The new LHCb combination

- Breakdown the results by methods - the power of the combination
  - For example look at inputs from  $B^+$  decays
  - Methods vary in precision and number of solutions



# The new LHCb combination

- Breakdown the results by B meson type
  - Everything consistent at the 2 sigma level currently
  - In the SM they should be the same - if NP appears it could affect the different species differently due to differing decay topologies



$B_s^0$  decays

$B^0$  decays

$B^+$  decays

Combination

$$\gamma = (74.0^{+5.0}_{-5.8})^\circ$$

# Beauty baryon $\Lambda_b^0/\Xi_b^0$ decays to $D^0 p h^-$ final states

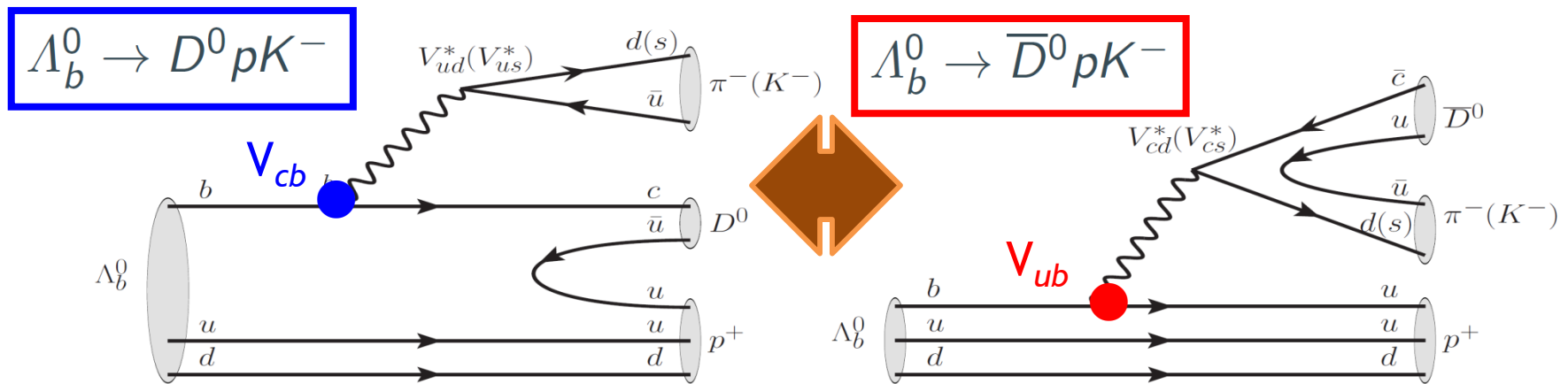
1 fb<sup>-1</sup>  
(2011)

PRD 89(2014)03 (arXiv:1311.4823)

→ Beauty baryon sector remains largely unexplored ⇒ this is LHCb game field

→ Decays such as  $\Lambda_b \rightarrow D^0 \Lambda$  and  $\Lambda_b \rightarrow D^0 p K^-$  can be used to measure  $\gamma$

Z. Phys. C56(1992)129; Mod. Phys. Lett. A 14(1999)63; PRD 65(2002)073029



→ LHCb has studied beauty baryon decays to  $D^0 p h^-$  and  $\Lambda_c^+ h^-$  final states, using 1 fb<sup>-1</sup> of data:

- The Cabibbo favored final states  $D^0 \rightarrow K^- \pi^+$  and  $\Lambda_c^+ \rightarrow p K^- \pi^+$  are used. The Common  $p K^- \pi^+$  final states is used to reduce systematic uncertainties.
- $\Lambda_b \rightarrow D^0 p \pi^-$  seen with  $3\,383 \pm 94$  ! See also Amp. Analysis: [arXiv:1701.07873]





# Beauty baryon $\Lambda_b^0/\Xi_b^0$ decays to $D^0 p K^-$ final states

1 fb<sup>-1</sup>  
(2011)

PRD 89(2014)03 (arXiv:1311.4823)

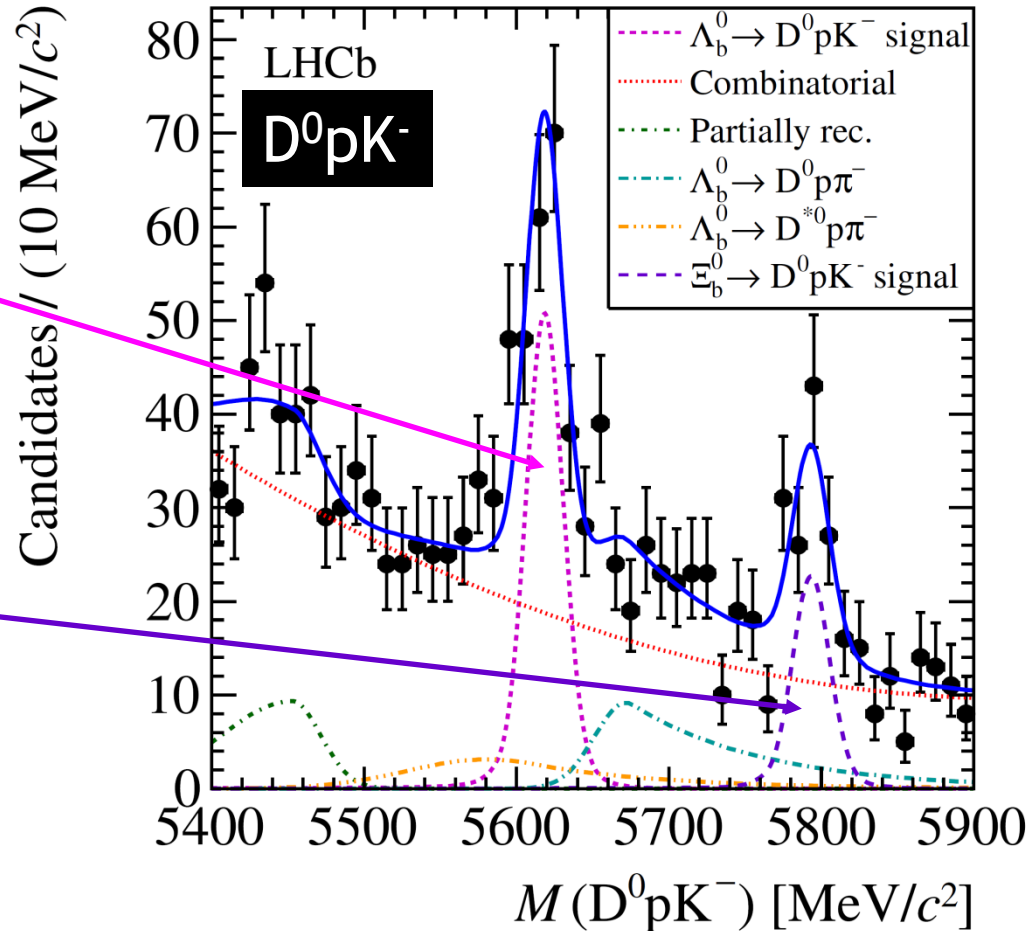
→ Observation of (signif incl. syst.):

$\Lambda_b^0 \rightarrow D^0 p K^-$  @ 9.0 $\sigma$  :  $R_{\Lambda_b^0 \rightarrow D^0 p K^-}$

$$\frac{\mathcal{B}(\Lambda_b^0 \rightarrow D^0 p K^-)}{\mathcal{B}(\Lambda_b^0 \rightarrow D^0 p \pi^-)} = (7.3 \pm 0.8^{+0.5}_{-0.6})\%$$

$\Xi_b^0 \rightarrow D^0 p K^-$  @ 5.9 $\sigma$  :  $R_{\Xi_b^0 \rightarrow D^0 p K^-}$

$$\frac{f_{\Xi_b^0} \times \mathcal{B}(\Xi_b^0 \rightarrow D^0 p K^-)}{f_{\Lambda_b^0} \times \mathcal{B}(\Lambda_b^0 \rightarrow D^0 p K^-)} = (44 \pm 9 \pm 6)\%$$



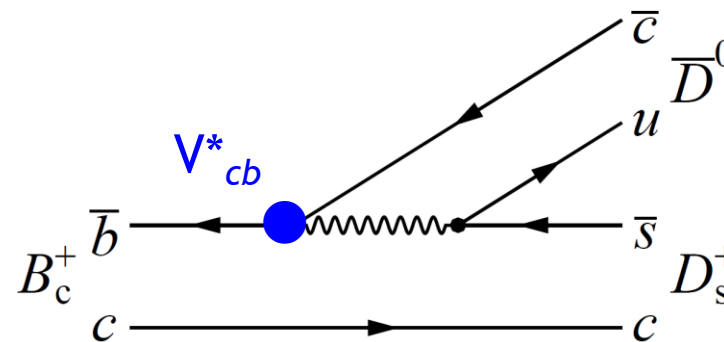
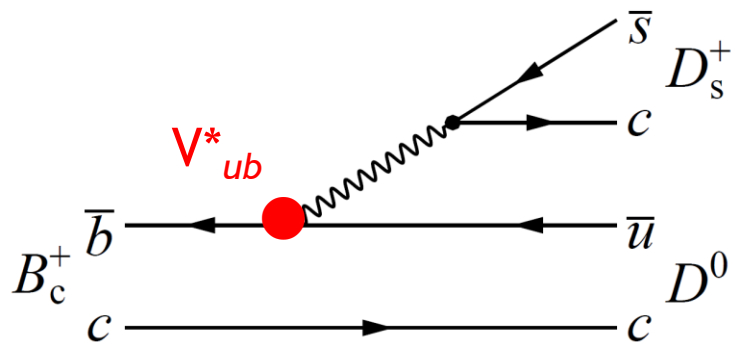
A lot of events already  $\Rightarrow$  high time to move to CP analyses  
LHCb has almost 15 times this is hands (ADS underway)



# $\gamma$ measurements in $B_c^+$ decays ?

[arXiv:1712.04702]  
(Run1)

- Massive sample of  $B_c^+$  produced in LHCb:  $\sim 30K B_c^+ \rightarrow J/\psi \pi^+$  with Run1+Run2
- Branching fraction of  $B_c^+ \rightarrow J/\psi \pi^+$  :  $(0.6-2.9) \times 10^{-3}$   
PRD 49 (1994) 3399, PRD 68 (2003) 094020, PRD 89 (2014) 034008
- Able to access  $B_c^+$  decays with Branching Fractions of  $10^{-5}-10^{-6}$
- $B_c^+ \rightarrow D^+_{(s)} D^0$  decays sensitive to  $\gamma$  with  $r_{D_s} \sim 1$  and  $r_D \sim 0.1$

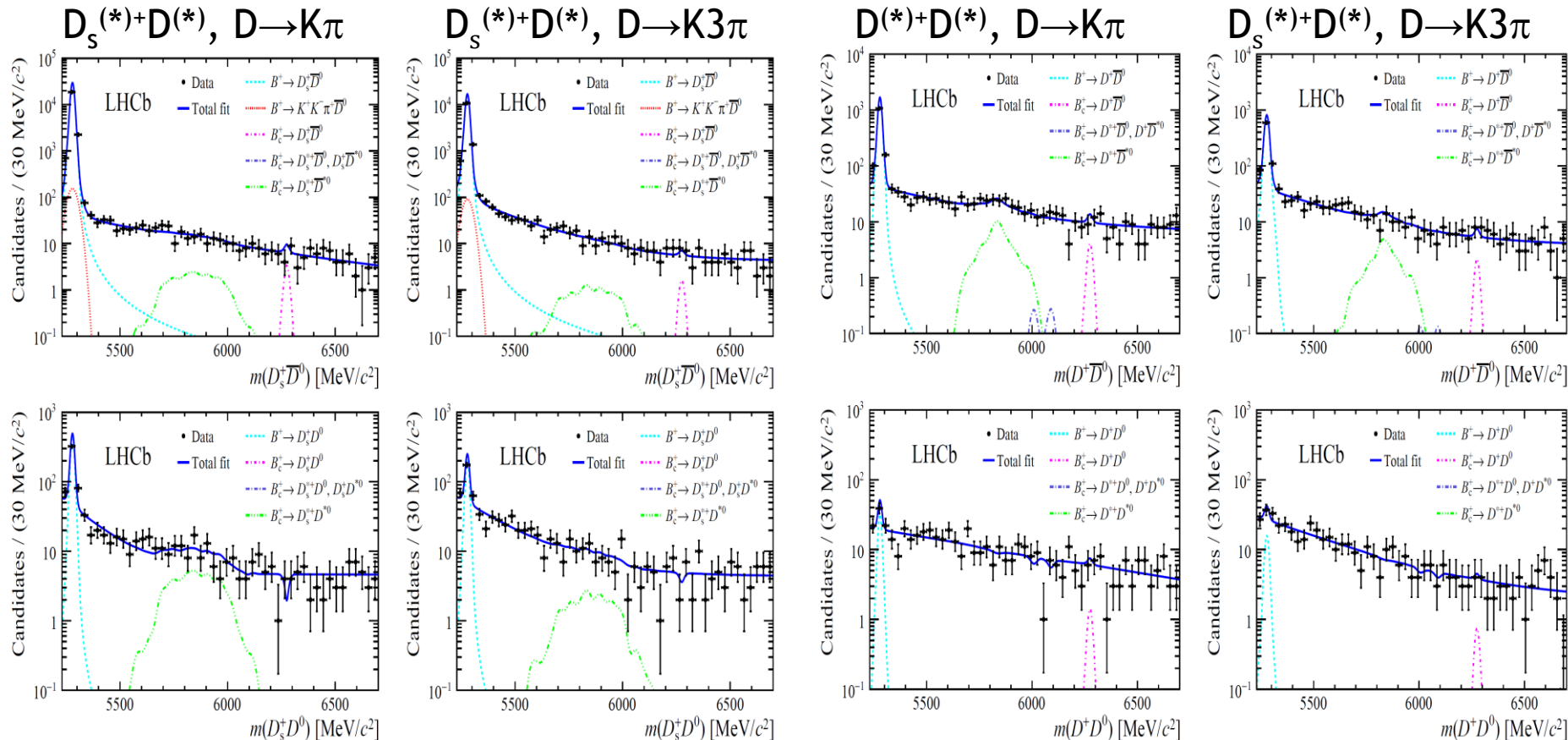


- The branching fractions are predicted to be:

Channel	Prediction for the branching fraction [ $10^{-6}$ ]			
	Ref. [9]	Ref. [10]	Ref. [11]	Ref. [12]
$B_c^+ \rightarrow D_s^+ \bar{D}^0$	$2.3 \pm 0.5$	4.8	1.7	2.1
$B_c^+ \rightarrow D_s^+ D^0$	$3.0 \pm 0.5$	6.6	2.5	7.4
$B_c^+ \rightarrow D^+ \bar{D}^0$	$32 \pm 7$	53	32	33
$B_c^+ \rightarrow D^+ D^0$	$0.10 \pm 0.02$	0.32	0.11	0.32

# Results of $B_c^+ \rightarrow D_{(s)}^*(*) + D^{(*)0}$ searches

[arXiv:1712.04702]  
(Run1)

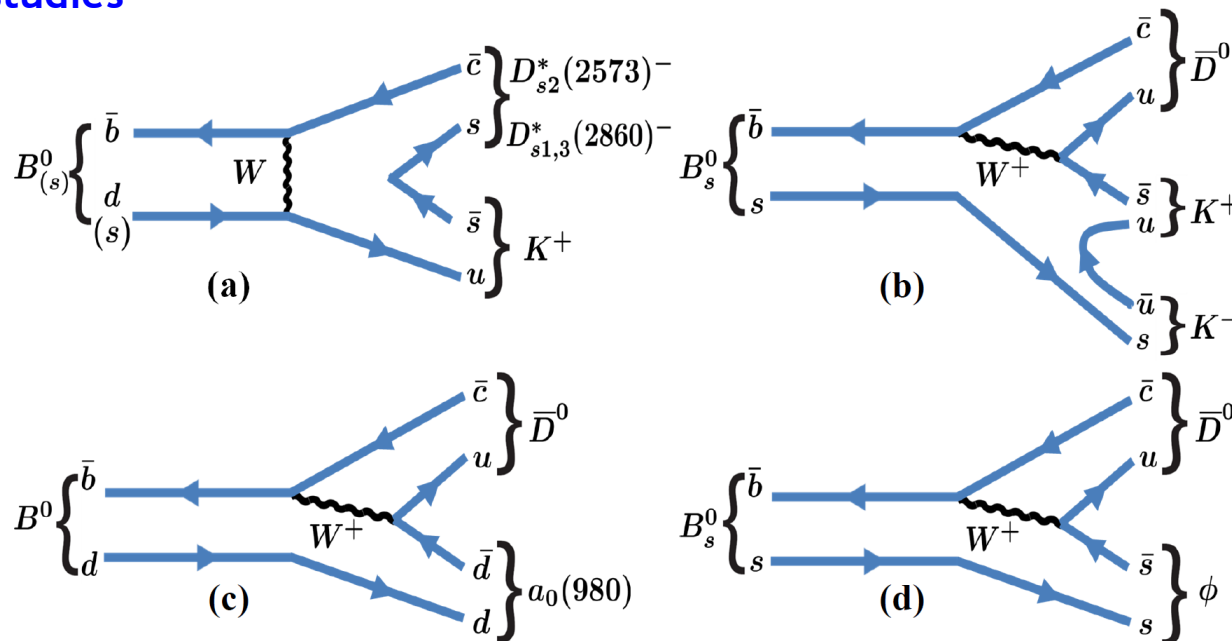


- Nothing observed and upper limits set on these decays
- Absolute Branching fraction upper limits at level of  $10^{-4}$ – $10^{-3}$ , consistent with expectations in previous slide
- Decays with  $D(s)^*$  and  $D^*$  are searched without reconstructing  $\gamma/\pi^0$

# Physics with/of $B^0_{(s)} \rightarrow \bar{D}^0 K^+ K^-$ decays

✓ **Time-Dependent Dalitz analyses** can be used to access CKM angles  $\gamma$  and to obtain clean (i.e. tree decays) determination of  $\beta_{(s)}$  in  $B_{(s)} - \bar{B}_{(s)}$  mixing (Phys. Rev D85 (2012) 114015)

✓ **Rich phenomenology of Dalitz structures** are interesting for excited  $D_s^{**}$  charmed B-decays spectroscopy studies



## First steps:

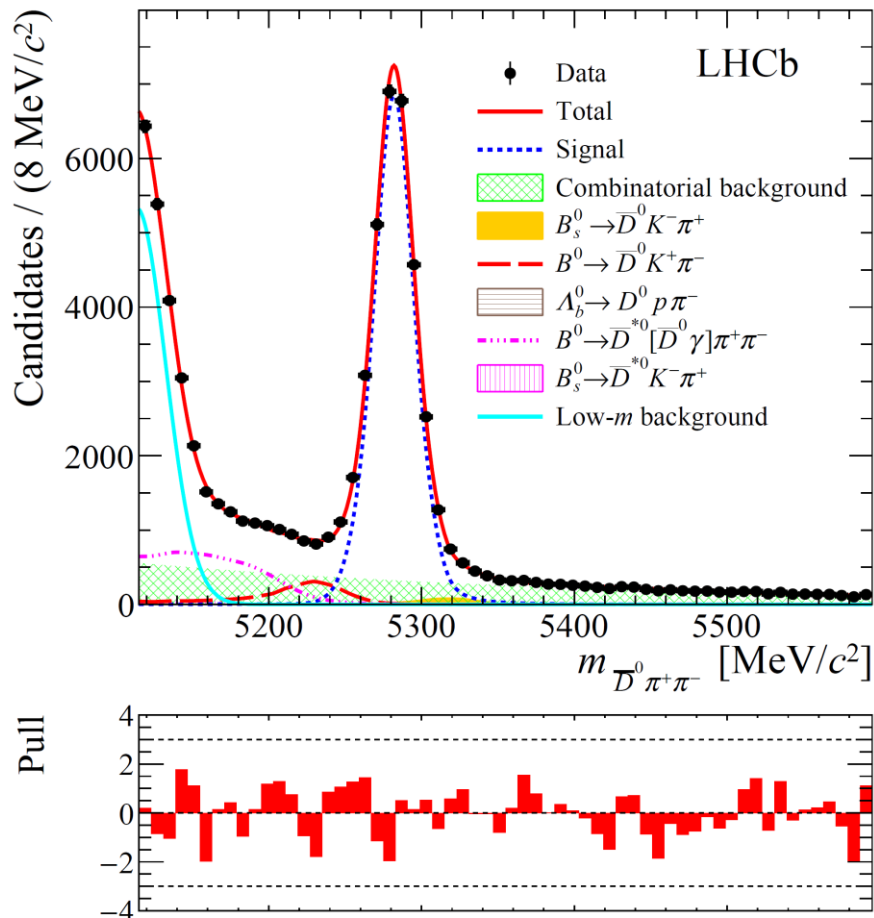
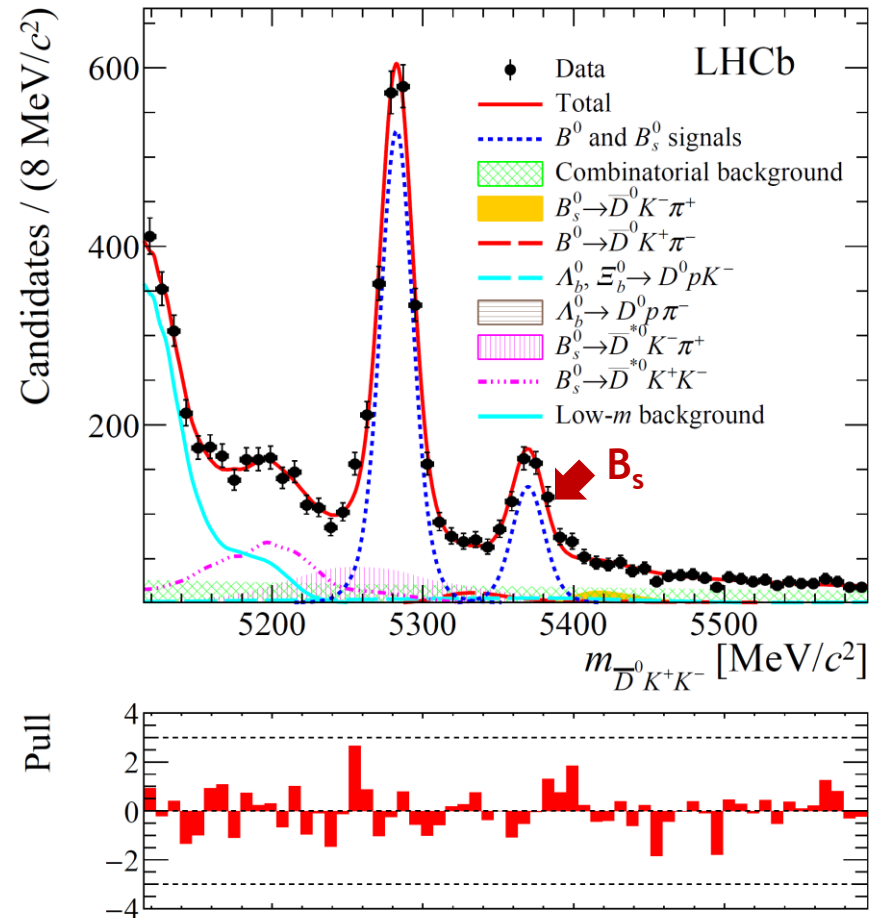
✓ Analysis already performed with early LHCb dataset (0.6/fb) : observation of  $B^0$  channel and only evidence for  $B^0_s$  mode (Phys. Rev. Lett. 109 (2012) 131801)

✓ Updated measurements performed with 3/fb (Run1: 2011+2012)  $\rightarrow$  new analysis

- Improved background treatment (e.g. :  $B^0_{(s)} \rightarrow \bar{D}^0 K^+ \pi^-$  and  $\Lambda_b \rightarrow D^0 p K^-$ )
- control/norm. mode:  $B^0 \rightarrow D^0 \pi^+ \pi^-$

Future developments in collaboration with UCAS/Tsinghua colleagues

# invariant mass fit of $B^0_{(s)} \rightarrow \bar{D}^0 h^+ h^-$ decays

 $B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$ 

 $29\,943 \pm 243$ 
 $B^0_{(s)} \rightarrow \bar{D}^0 K^+ K^-$ 


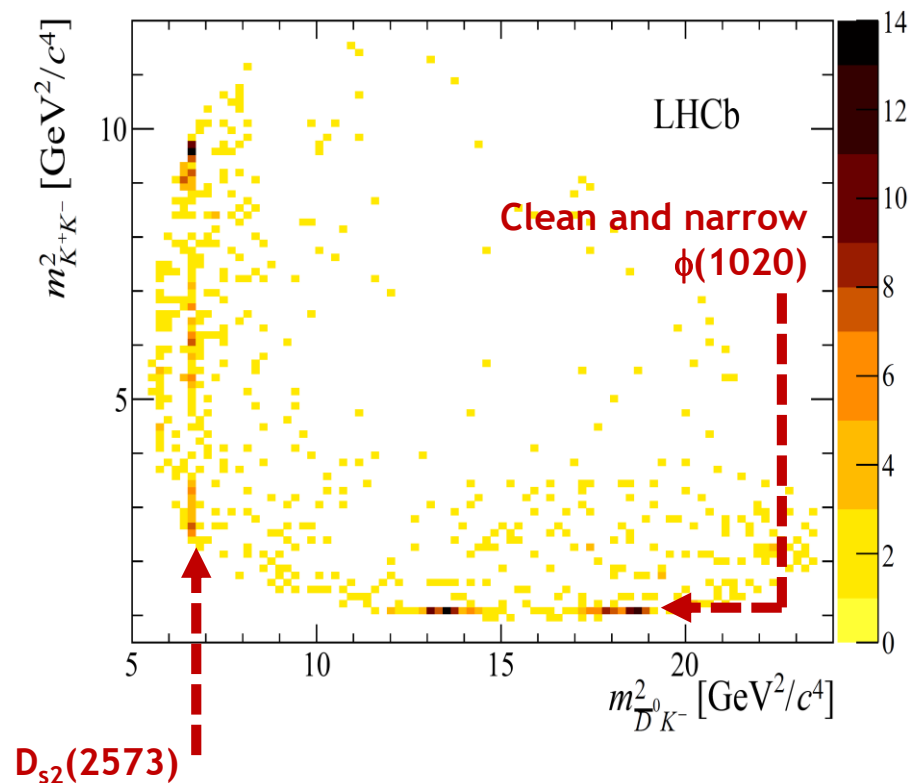
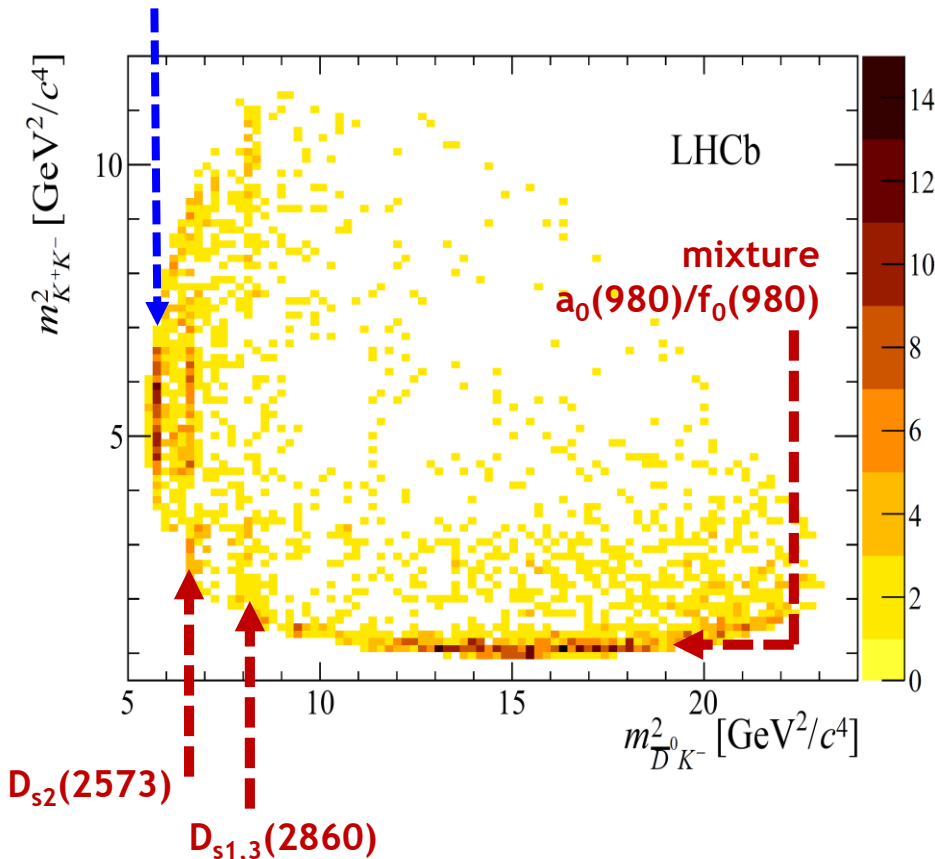
$1918 \pm 74 B^0$  & NEW  $\rightarrow 473 \pm 33 B^0_s$   
Observed for the 1<sup>st</sup> time!

ratio of yields  $\mathcal{R}_{B_s^0/B^0} = (24.7 \pm 1.7)\%$





# Inspection of Dalitz plot

 $B^0 \rightarrow \bar{D}^0 K^+ K^-$ 
(in [5240,5320] MeV/c<sup>2</sup>)
 $B_s^0 \rightarrow \bar{D}^0 K^+ K^-$ 
(in [5340,5400] MeV/c<sup>2</sup>)non subtracted background  $D_{s1}(2536)$ 

→ Performed only with LHC Run1 : motivates amplitude analysis with additional LHCb data

Future developments in collaboration with UCAS/Tsinghua colleagues

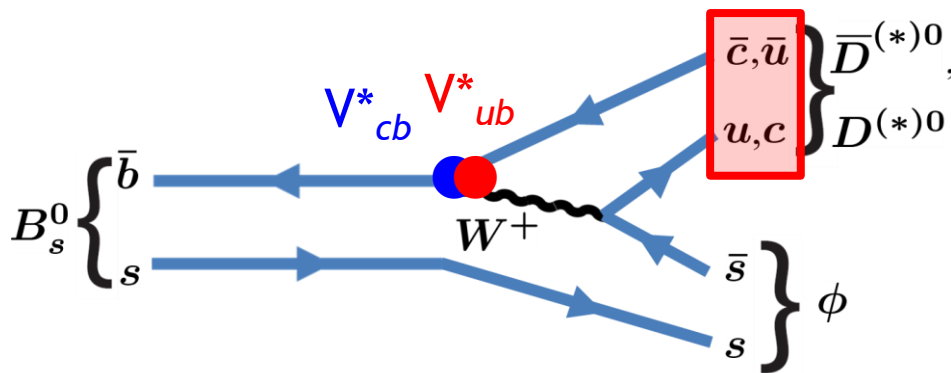


# Studies of $B^0_{(s)} \rightarrow \bar{D}^{(*)0} \phi$

✓ The  $\phi(1020)$  is a narrow resonance and using the selected candidates in  $B^0_{(s)} \rightarrow \bar{D}^0 K^+ K^-$  of 1807.01891 permits studies on  $B^0_{(s)} \rightarrow \bar{D}^{(*)0} \phi$

✓ Significant sensitivity to the CKM angle  $\gamma$  for  $B^0_s \rightarrow \bar{D}^{(*)0} \phi$  decays:  
(Phys. Lett. B253 (1991) 483 & LHCb-PUB-2010-005)

- Precision on CKM angle  $\gamma$  still limited (i.e. around  $5^\circ \rightarrow$  see talk by Alberto Correa dos Reis) to indirectly constraint BSM physics  
 $\rightarrow$  alternate methods welcome
- $b \rightarrow c$  and  $b \rightarrow u$  interfering transition of about same size:  $r_B \approx 30-50\%$  ( $B^0_s \rightarrow D^+ K^-$  JHEP 03 (2018) 059)
- For the  $D^{*0}$  decay (VV) the reconstruction can be partial, if  $f_L$  known, to almost double the  $B^0_s$  dataset (i.e. omit  $\gamma/\pi^0$  (Phys. Lett. B777 (2017) 16))

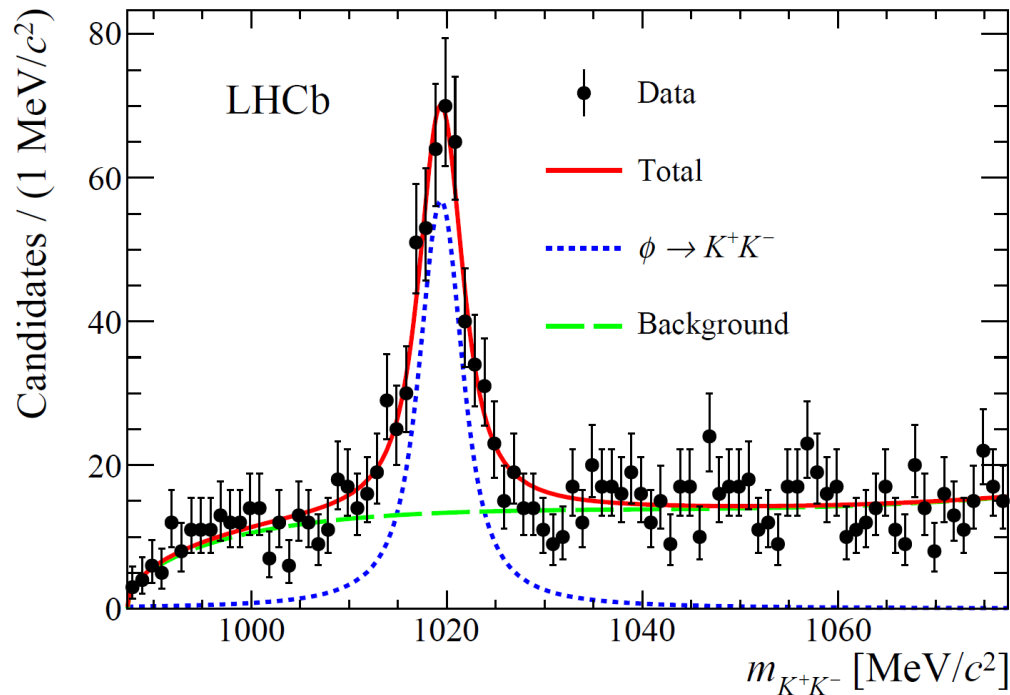


✓  $\mathcal{B}(B_s^0 \rightarrow \bar{D}^0 \phi)$  is  $(3.0 \pm 0.8) \times 10^{-5}$  as measured with LHCb 1/fb with a specific selection normalised to  $\mathcal{B}(B_s^0 \rightarrow \bar{D}^0 \bar{K}^{*0})$  (Phys. Lett. B727 (2013) 403)

✓  $B_s^0 \rightarrow \bar{D}^{*0} \phi$  is still unobserved

# The $\phi \rightarrow K^+K^-$ spectrum of $B^0_{(s)} \rightarrow \bar{D}^{(*)0}K^+K^-$

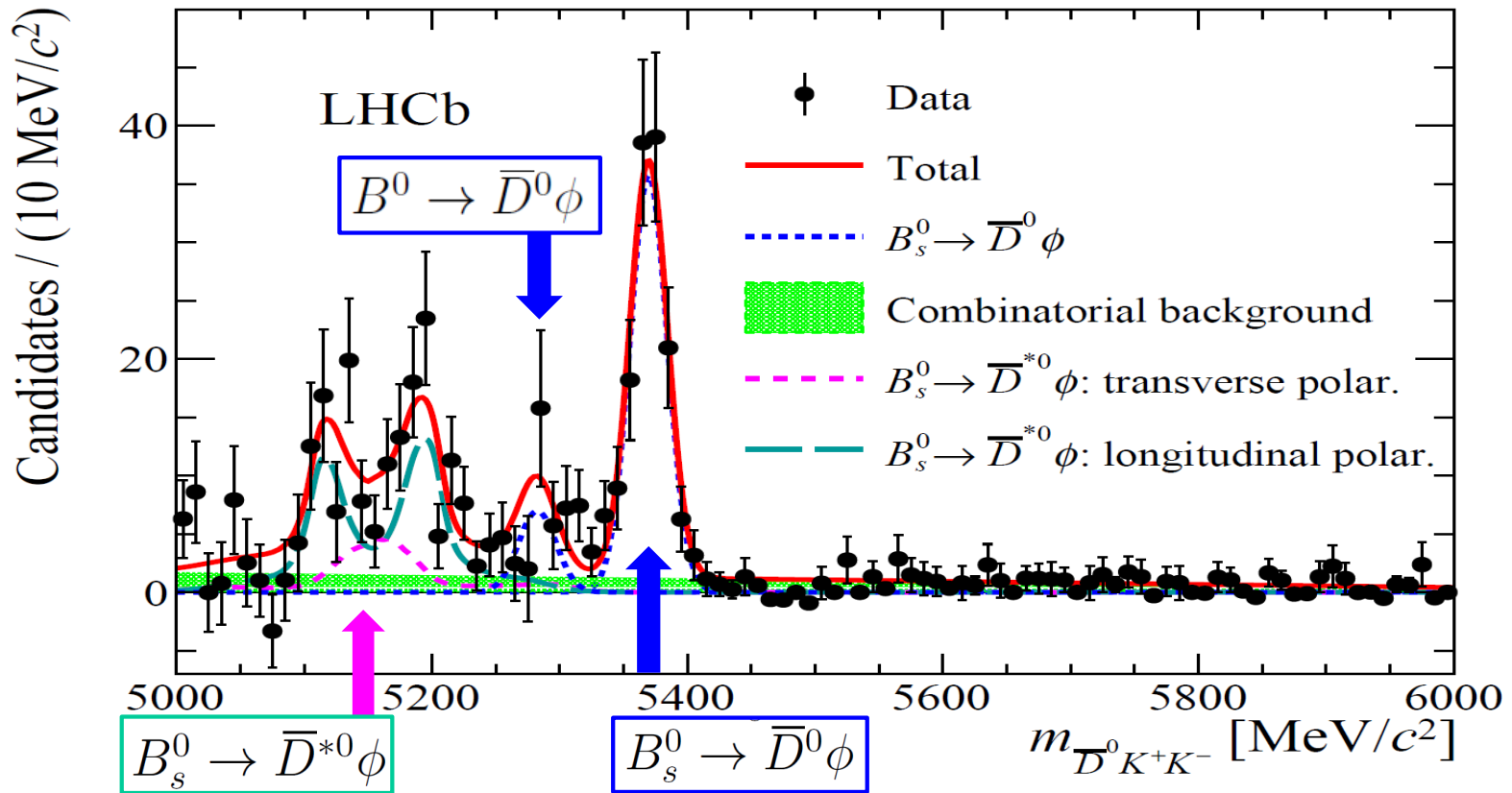
- ✓ Using selected  $B^0_{(s)}$  candidates ([see slide on invariant mass fit](#)) in the window  $m_{DKK} \in [5000, 6000] \text{ GeV}/c^2$  obtain the following  $m_{KK}$  spectrum:



$427 \pm 30$   $\phi$  signal candidates  
 $1152 \pm 41$   $K^+K^-$  background

- ✓ Fit signal with relativistic Breit-Wigner PDF and background with threshold PDF proportional to  $(p \times q) \cdot (1 + ax + b(2x^2 - 1))$ , where  $p$  &  $q$  are the momentum of the K in the KK rest frame and  $D$  in DKK rest frame and  $x = 2(m_{K^+K^-} - 2m_K)/90 \text{ MeV}/c^2 - 1$
- ✓ Fit used to obtain sPlot-projected mass spectrum  $m_{\bar{D}^0 K^+ K^-}$  (correlations with  $m_{KK}$  less than 6%)

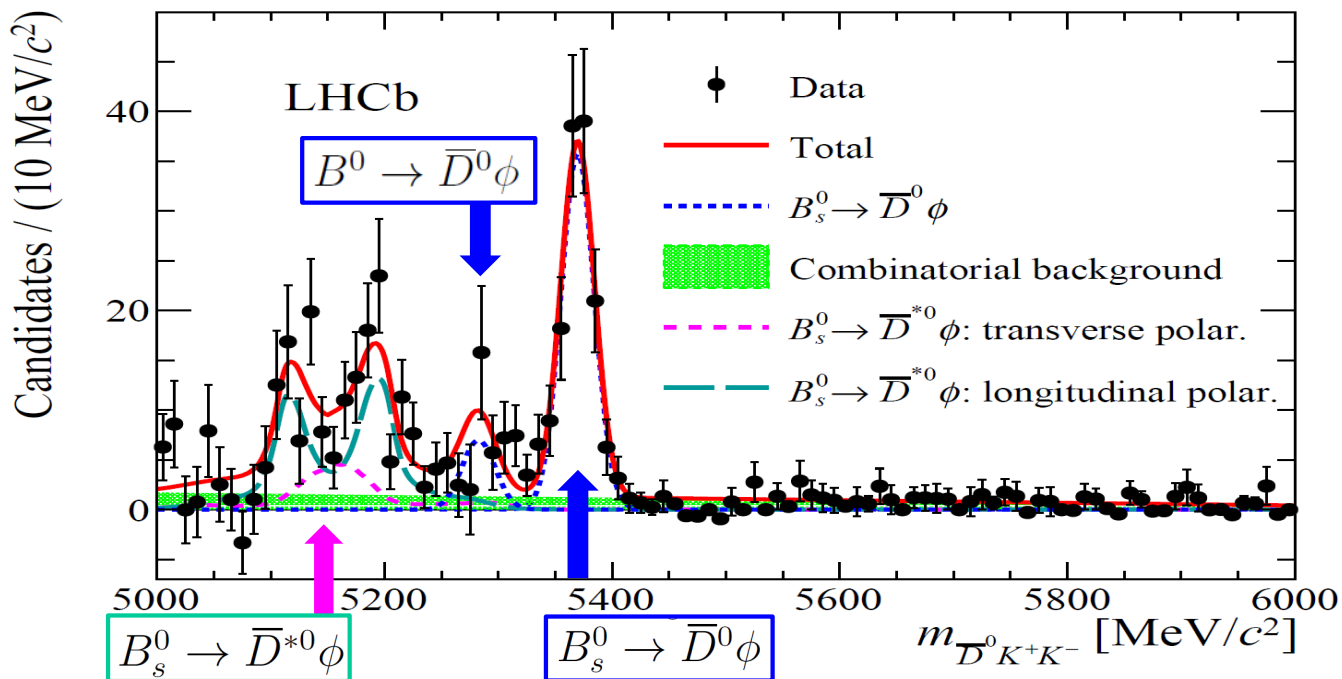
# The projected mass spectrum of $B^0_{(s)} \rightarrow \bar{D}^{(*)0} \phi$



## Invariant mass fit:

- ✓ Shape of  $B^0$  and  $B_s^0$  decaying to  $\bar{D}^0 \phi$  modelled by Gaussian functions (mass difference fixed to PDG2018).
- ✓ Shape of  $B_s^0$  decaying to  $\bar{D}^{*0} \phi$  determined from simulation : sum of 2 PDFs with fully longitudinal/transverse polarisation ( $f_L=1$  or 0) and relative branching fraction  $D^{*0}$  to  $D^0 \gamma / D^0 \pi^0$  fixed to PDG2018 value.
- ✓ Remaining combinatorial background modelled by straight line.

# Fit results for $B^0_{(s)} \rightarrow \bar{D}^{(*)0} \phi$



$$N_{B_s^0 \rightarrow \bar{D}^0 \phi} = 132 \pm 13, N_{B^0 \rightarrow \bar{D}^0 \phi} = 26 \pm 11, \text{ and } N_{B_s^0 \rightarrow \bar{D}^{*0} \phi} = 163 \pm 19, \text{ with } f_L = (73 \pm 15)\%.$$

**Observation of  $B_s^0 \rightarrow \bar{D}^{*0} \phi$  with more than 7 standard deviations !**

The whole procedure was repeated with various  $m_{KK}$  background fit parameters obtained from various regions to evaluate possible biases due to  $K^+K^-$  S-Waves under the  $\phi$  resonance.

Future developments in collaboration with UCAS/Tsinghua colleagues



# Measuring $\gamma$ in $B_s^0 \rightarrow \bar{D}^{(*)0} \phi$ decays

Based on Phys. Lett. B253 (1991) 483 & LHCb-PUB-2010-005 one can define in a **time integrated manner** with D Cabibbo-favoured (CF) or doubly-Cabibbo suppressed decays (DCS) decays merged the observables (normalised rates):

D  $\rightarrow$  K $\pi$ , K3 $\pi$ , K $\pi\pi^0$  flavour specific

$$R_{K\pi}^- = \frac{\Gamma(D(K^-\pi^+)\phi)}{\Gamma(D(K^-\pi^+)\phi) + \Gamma(D(K^+\pi^-)\phi)}$$

$$R_{K\pi}^+ = \frac{\Gamma(D(K^+\pi^-)\phi)}{\Gamma(D(K^-\pi^+)\phi) + \Gamma(D(K^+\pi^-)\phi)}$$

$$R_{K3\pi}^- = \frac{\Gamma(D(K^-3\pi)\phi)}{\Gamma(D(K^-\pi^+)\phi) + \Gamma(D(K^+\pi^-)\phi)}$$

$$R_{K3\pi}^+ = \frac{\Gamma(D(K^+3\pi)\phi)}{\Gamma(D(K^-\pi^+)\phi) + \Gamma(D(K^+\pi^-)\phi)}$$

$$R_{K\pi\pi^0}^- = \frac{\Gamma(D(K^-\pi^+\pi^0)\phi)}{\Gamma(D(K^-\pi^+)\phi) + \Gamma(D(K^+\pi^-)\phi)}$$

$$R_{K\pi\pi^0}^+ = \frac{\Gamma(D(K^+\pi^-\pi^0)\phi)}{\Gamma(D(K^-\pi^+)\phi) + \Gamma(D(K^+\pi^-)\phi)}$$

D  $\rightarrow$  KK &  $\pi\pi$  CP+ eigenstates

$$R_{KK} = \frac{\Gamma(D(K^+K^-)\phi)}{\Gamma(D(K^-\pi^+)\phi) + \Gamma(D(K^+\pi^-)\phi)}$$

$$R_{\pi\pi} = \frac{\Gamma(D(\pi^+\pi^-)\phi)}{\Gamma(D(K^-\pi^+)\phi) + \Gamma(D(K^+\pi^-)\phi)}$$

or D  $\rightarrow$  Ks $\pi\pi$  KsKK with lower rates and more challenging

$\rightarrow$  Precision Counting  $B_s \rightarrow D^{(*)0} \phi$  signal rates in those modes allows to access to  $\gamma$  and  $(r_{B_s}^{(*)}, \delta_{B_s}^{(*)})$  parameters : 8x3 observables and 3 unknowns

$\rightarrow$  with external inputs on strong D decays +  $B_s$  decay time & mixing parameters  $y = \Delta\Gamma_s/2\Gamma_s$  &  $B_s$

HFLAV

CLEO-c

BESIII

Future developments in collaboration with UCAS/Tsinghua colleagues



# Measuring $\gamma$ in $B^0_s \rightarrow \bar{D}^{(*)0} \phi$ decays

Based on Phys. Lett. B253 (1991) 483 & LHCb-PUB-2010-005 one can define in a **time integrated manner** with D Cabibbo-favoured (CF) or doubly-Cabibbo suppressed (DCS) decays merged the observables (normalised rates):

$$R_{K\pi}^- = \frac{(1+r_B^2)(1+(r_D^{K\pi})^2) + 4r_B r_D^{K\pi} \cos \delta_B \cos(\delta_{K\pi} + \gamma) - 2yr_B \cos(2\beta_s + \delta_B - \gamma)}{2 \left[ (1+r_B^2)(1+(r_D^{K\pi})^2) + 4r_B r_D^{K\pi} \cos \delta_B \cos \delta_{K\pi} \cos \gamma - 2yr_B \cos(2\beta_s - \gamma) \cos \delta_B \right]}$$

$$R_{K\pi}^+ = \frac{(1+r_B^2)(1+(r_D^{K\pi})^2) + 4r_B r_D^{K\pi} \cos \delta_B \cos(\delta_{K\pi} - \gamma) - 2yr_B \cos(2\beta_s - \delta_B - \gamma)}{2 \left[ (1+r_B^2)(1+(r_D^{K\pi})^2) + 4r_B r_D^{K\pi} \cos \delta_B \cos \delta_{K\pi} \cos \gamma - 2yr_B \cos(2\beta_s - \gamma) \cos \delta_B \right]}$$

$$R_{KK} = F_{KK} \frac{4 \left[ 1+r_B^2 + 2r_B \cos \delta_B \cos \gamma - 2y \sqrt{1+2r_B^2 + 4r_B \cos \delta_B \cos \gamma} \cos \left( 2\beta_s + \tan^{-1} \left( \frac{r_B \sin(\delta_B - \gamma)}{1+r_B \cos(\delta_B - \gamma)} \right) - \tan^{-1} \left( \frac{r_B \sin(\delta_B + \gamma)}{1+r_B \cos(\delta_B + \gamma)} \right) \right]}{2 \left[ (1+r_B^2)(1+(r_D^{K\pi})^2) + 4r_B r_D^{K\pi} \cos \delta_B \cos \delta_{K\pi} \cos \gamma - 2yr_B \cos(2\beta_s - \gamma) \cos \delta_B \right]}$$

$$\text{avec } F_{KK} = \frac{\varepsilon(D \rightarrow KK) Br(D^0 \rightarrow KK)}{\varepsilon(D \rightarrow K\pi) [Br(D^0 \rightarrow K^-\pi^+) + Br(D^0 \rightarrow K^+\pi^-)]}$$

$$R_{\pi\pi} = F_{\pi\pi} \frac{4 \left[ 1+r_B^2 + 2r_B \cos \delta_B \cos \gamma - 2y \sqrt{1+2r_B^2 + 4r_B \cos \delta_B \cos \gamma} \cos \left( 2\beta_s + \tan^{-1} \left( \frac{r_B \sin(\delta_B - \gamma)}{1+r_B \cos(\delta_B - \gamma)} \right) - \tan^{-1} \left( \frac{r_B \sin(\delta_B + \gamma)}{1+r_B \cos(\delta_B + \gamma)} \right) \right]}{2 \left[ (1+r_B^2)(1+(r_D^{K\pi})^2) + 4r_B r_D^{K\pi} \cos \delta_B \cos \delta_{K\pi} \cos \gamma - 2yr_B \cos(2\beta_s - \gamma) \cos \delta_B \right]}$$

$$\text{avec } F_{\pi\pi} = \frac{\varepsilon(D \rightarrow \pi\pi) Br(D^0 \rightarrow \pi\pi)}{\varepsilon(D \rightarrow K\pi) [Br(D^0 \rightarrow K^-\pi^+) + Br(D^0 \rightarrow K^+\pi^-)]}$$

➔ Efficiencies must accounts decay time acceptance

$$R_{K3\pi}^- = F_{K3\pi}^- \frac{\left[ (1+r_B^2)(1+(r_D^{K3\pi})^2) + 4r_B R_{K3\pi} r_D^{K3\pi} \cos \delta_B \cos(\delta_{K3\pi} + \gamma) - 2yr_B \cos(2\beta_s + \delta_B - \gamma) \right]}{2 \left[ (1+r_B^2)(1+(r_D^{K\pi})^2) + 4r_B r_D^{K\pi} \cos \delta_B \cos \delta_{K\pi} \cos \gamma - 2yr_B \cos(2\beta_s - \gamma) \cos \delta_B \right]}$$

$$\text{avec } F_{K3\pi}^- = \frac{\varepsilon(D \rightarrow K3\pi) [Br(D^0 \rightarrow K^-3\pi) + Br(\bar{D}^0 \rightarrow K^-3\pi)]}{\varepsilon(D \rightarrow K\pi) [Br(D^0 \rightarrow K^-\pi^+) + Br(D^0 \rightarrow K^+\pi^-)]}$$

$$R_{K3\pi}^+ = F_{K3\pi}^+ \frac{\left[ (1+r_B^2)(1+(r_D^{K3\pi})^2) + 4r_B R_{K3\pi} r_D^{K3\pi} \cos \delta_B \cos(\delta_{K3\pi} - \gamma) - 2yr_B \cos(2\beta_s - \delta_B - \gamma) \right]}{2 \left[ (1+r_B^2)(1+(r_D^{K\pi})^2) + 4r_B r_D^{K\pi} \cos \delta_B \cos \delta_{K\pi} \cos \gamma - 2yr_B \cos(2\beta_s - \gamma) \cos \delta_B \right]}$$

$$\text{avec } F_{K3\pi}^+ = \frac{\varepsilon(D \rightarrow K3\pi) [Br(D^0 \rightarrow K^+3\pi) + Br(\bar{D}^0 \rightarrow K^+3\pi)]}{\varepsilon(D \rightarrow K\pi) [Br(D^0 \rightarrow K^-\pi^+) + Br(D^0 \rightarrow K^+\pi^-)]}$$

$$R_{K\pi\pi^0}^- = F_{K\pi\pi^0}^- \frac{\left[ (1+r_B^2)(1+(r_D^{K\pi\pi^0})^2) + 4r_B R_{K\pi\pi^0} r_D^{K\pi\pi^0} \cos \delta_B \cos(\delta_{K\pi\pi^0} + \gamma) - 2yr_B \cos(2\beta_s + \delta_B - \gamma) \right]}{2 \left[ (1+r_B^2)(1+(r_D^{K\pi})^2) + 4r_B r_D^{K\pi} \cos \delta_B \cos \delta_{K\pi} \cos \gamma - 2yr_B \cos(2\beta_s - \gamma) \cos \delta_B \right]}$$

$$\text{avec } F_{K\pi\pi^0}^- = \frac{\varepsilon(D \rightarrow K\pi\pi^0) [Br(D^0 \rightarrow K^-\pi\pi^0) + Br(\bar{D}^0 \rightarrow K^-\pi\pi^0)]}{\varepsilon(D \rightarrow K\pi) [Br(D^0 \rightarrow K^-\pi^+) + Br(D^0 \rightarrow K^+\pi^-)]}$$

$$R_{K\pi\pi^0}^+ = F_{K\pi\pi^0}^+ \frac{\left[ (1+r_B^2)(1+(r_D^{K\pi\pi^0})^2) + 4r_B R_{K\pi\pi^0} r_D^{K\pi\pi^0} \cos \delta_B \cos(\delta_{K\pi\pi^0} - \gamma) - 2yr_B \cos(2\beta_s - \delta_B - \gamma) \right]}{2 \left[ (1+r_B^2)(1+(r_D^{K\pi})^2) + 4r_B r_D^{K\pi} \cos \delta_B \cos \delta_{K\pi} \cos \gamma - 2yr_B \cos(2\beta_s - \gamma) \cos \delta_B \right]}$$

$$\text{avec } F_{K\pi\pi^0}^+ = \frac{\varepsilon(D \rightarrow K\pi\pi^0) [Br(D^0 \rightarrow K^+\pi\pi^0) + Br(\bar{D}^0 \rightarrow K^+\pi\pi^0)]}{\varepsilon(D \rightarrow K\pi) [Br(D^0 \rightarrow K^-\pi^+) + Br(D^0 \rightarrow K^+\pi^-)]}$$

Future developments in collaboration with UCAS/Tsinghua colleagues



# Sensitivity to $\gamma$ in $B_s^0 \rightarrow \bar{D}^{(*)0} \phi$ decays

An educated but rough estimate of LHCb Run1+Run2 data number of quasi pure  $B_s \rightarrow D^{(*)0} \phi$  candidates (with only B to  $D^* \phi$  events with  $f_L=1$ , for a defined CP eigen-state):

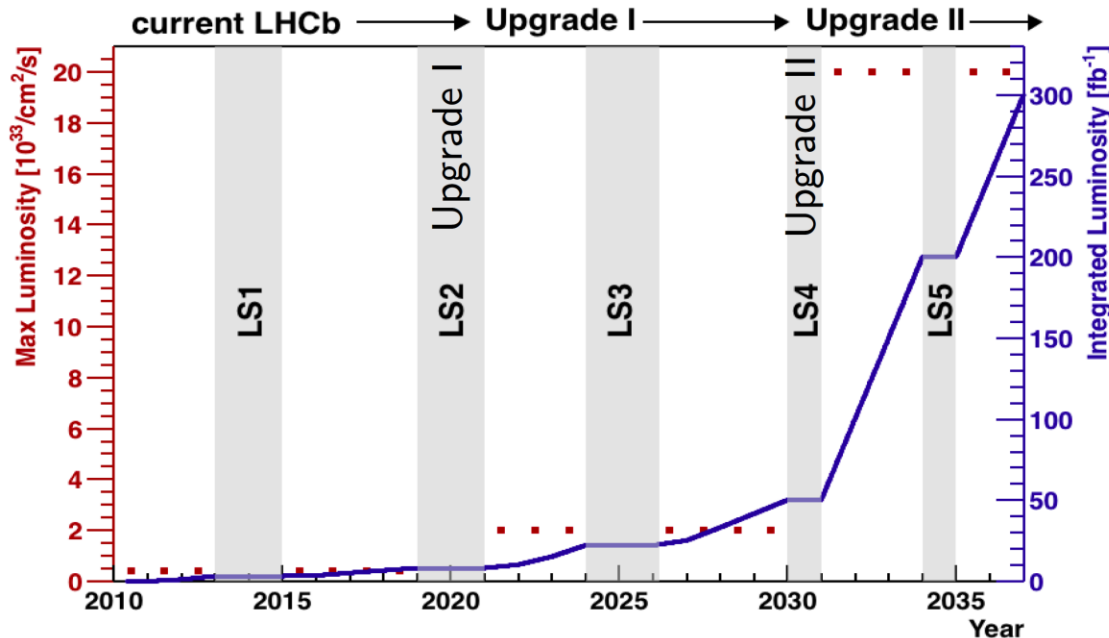
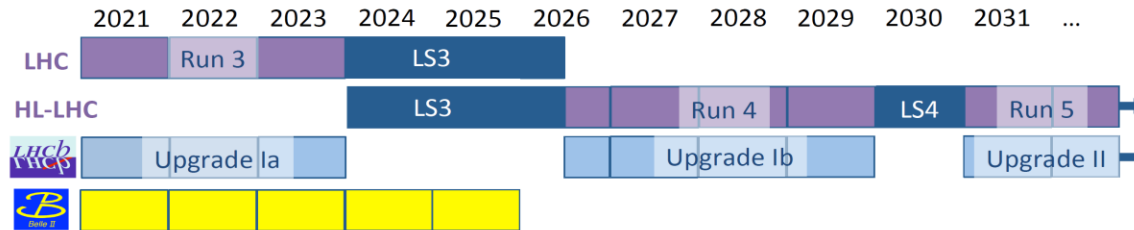
decay	$K\pi$	$K3\pi$	$K^+K^-$	$\pi^+\pi^-$	$K\pi\pi^0$	$K_s^0\pi^+\pi^-$	$K_s^0K^+K^-$
$D\phi$	629	240	82	25	31	52	7-8
$D^*(D\pi^0)\phi$	375	145	50	15	19	-	-
$D^*(D\gamma)\phi$	201	76	27	8	10	-	-

**VERY PRELIMINARY:**

**Expect a statistical sensitivity to the angle  $\gamma$  at the level of  $<10-15^\circ$**

Detailed sensitivity study underway with UCAS/Tsinghua LHCb colleagues

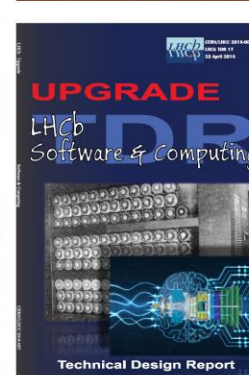
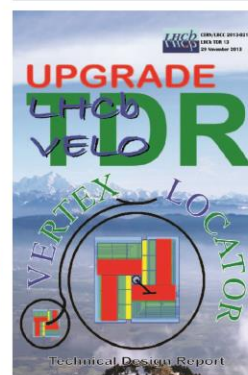
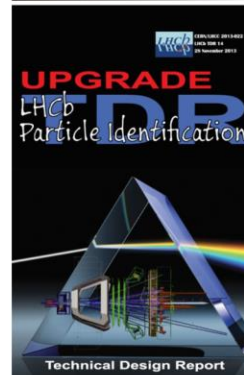
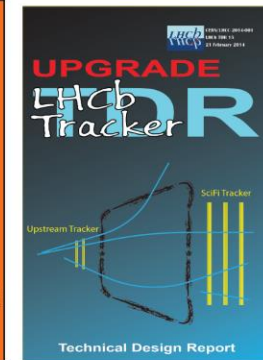
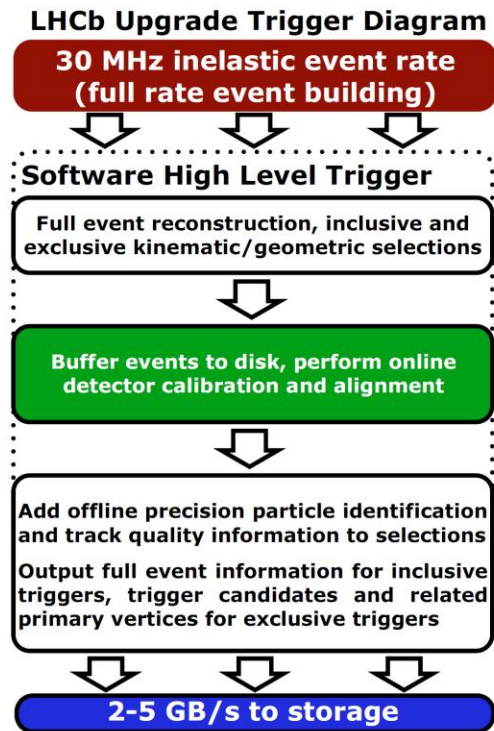
# LHCb upgrade schedule towards 50/fb and 300/fb in 12 and 20 years !



- Upgrade I a+b:  $50 \text{ fb}^{-1}$  after Run 3+4 at  $\mathcal{L} = 2 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$
- Upgrade II:  $300 \text{ fb}^{-1}$  after Run 5+6 at  $\mathcal{L} = 2 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$
- Full Belle 2 detector data taking starting 2019,  $50 \text{ ab}^{-1}$  sample 2025

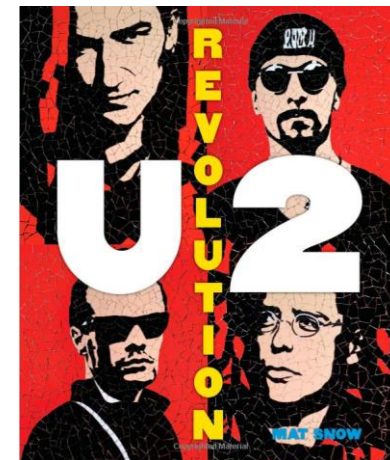


# LHCb: Trigger/detector upgrade phase 1 for Run 3 starting in 2021



- Removal of L0 bottleneck and move to full software trigger will increase efficiencies, by a factor of  $\sim 2$  for hadronic modes
- Upgrade I replaces frontend electronics: readout at inelastic 30 MHz rate
- Far reaching detector upgrades to improve occupancy, radiation hardness  
Vertex Locator  $\rightarrow$  Pixel; Main trackers  $\rightarrow$  SciFi Tracker, UT; RICH photodetectors





## Physics case for an LHCb Upgrade II Opportunities in flavour physics, and beyond, in the HL-LHC era

The LHCb collaboration

### Abstract

The LHCb Upgrade II will fully exploit the flavour-physics opportunities of the HL-LHC, and study additional physics topics that take advantage of the forward acceptance of the LHCb spectrometer. The LHCb Upgrade I will begin operation in 2020. Consolidation will occur, and modest enhancements of the Upgrade I detector will be installed, in Long Shutdown 3 of the LHC (2025) and these are discussed here. The main Upgrade II detector will be installed in long shutdown 4 of the LHC (2030) and will build on the strengths of the current LHCb experiment and the Upgrade I. It will operate at a luminosity up to  $2 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ , ten times that of the Upgrade I detector. New detector components will improve the intrinsic performance of the experiment in certain key areas. An Expression Of Interest proposing Upgrade II was submitted in February 2017. The physics case for the Upgrade II is presented here in more depth. *CP*-violating phases will be measured with precisions unattainable at any other envisaged facility. The experiment will probe  $b \rightarrow s\ell^+\ell^-$  and  $b \rightarrow d\ell^+\ell^-$  transitions in both muon and electron decays in modes not accessible at Upgrade I. Minimal flavour violation will be tested with a precision measurement of the ratio of  $\mathcal{B}(B^0 \rightarrow \mu^+\mu^-)/\mathcal{B}(B_s^0 \rightarrow \mu^+\mu^-)$ . Probing charm *CP* violation at the  $10^{-5}$  level may result in its long sought discovery. Major advances in hadron spectroscopy will be possible, which will be powerful probes of low energy QCD. Upgrade II potentially will have the highest sensitivity of all the LHC experiments on the Higgs to charm-quark couplings. Generically, the new physics mass scale probed, for fixed couplings, will almost double compared with the pre-HL-LHC era; this extended reach for flavour physics is similar to that which would be achieved by the HE-LHC proposal for the energy frontier.

# Looking forwards : LHCb upgrade & gains on $\gamma$ precision

Exciting times - measurements of  $\gamma$  are reaching a high precision era:

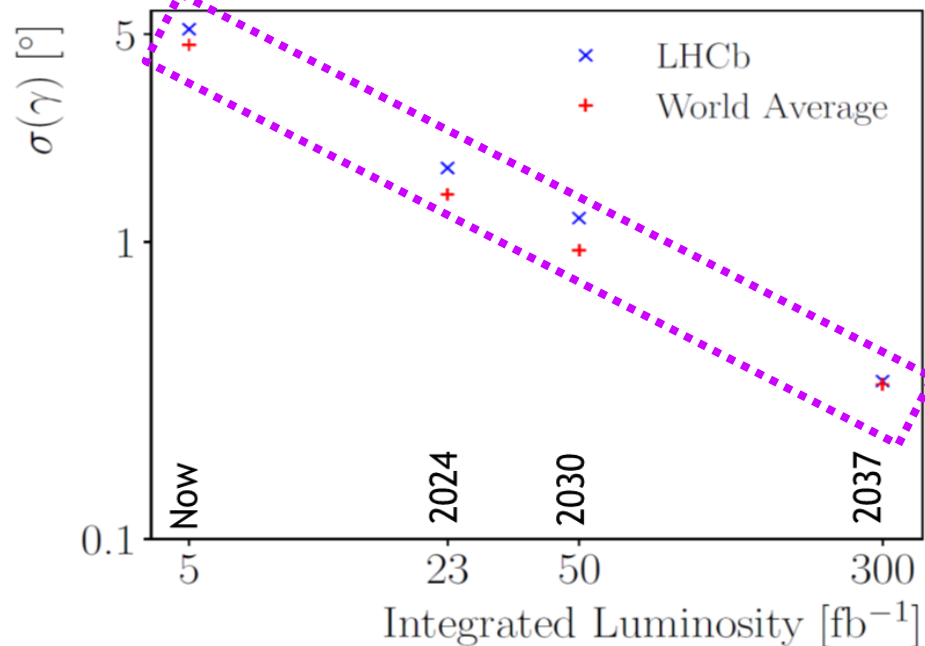
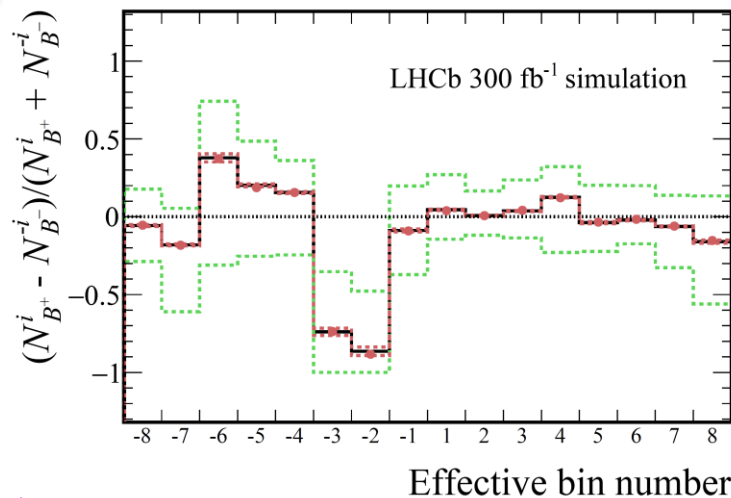
- We look forward to collaboration and competition from Belle-II

- With  $50 \text{ ab}^{-1}$  at Belle-II and a possible  $300 \text{ fb}^{-1}$  sample at LHCb:  $\sigma(\gamma) < 0.35^\circ$  to tackle BSM physics in CKM global fit well above a few 10 TeVs

- New ideas can help us go even further (some of them shown in this seminar)

- Will require new charm inputs from BES-III, LHCb and Belle-II

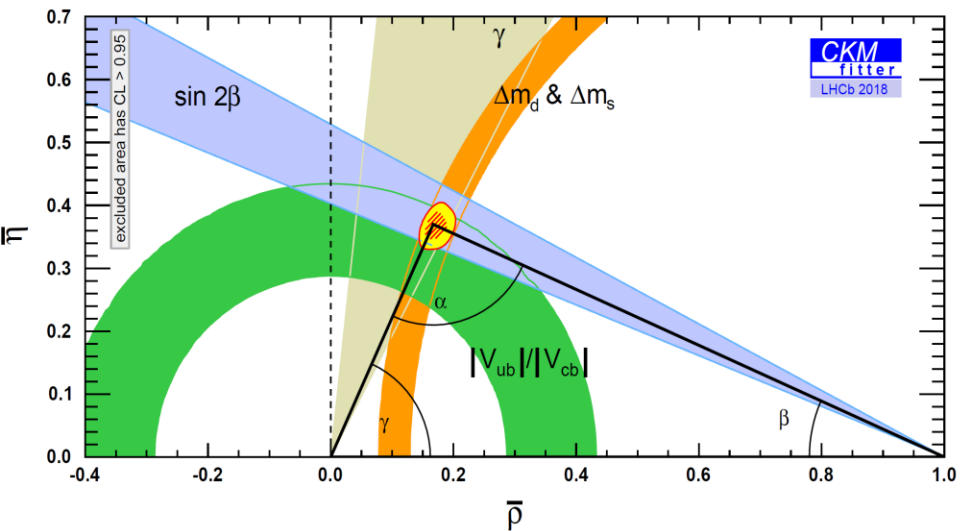
Physics case for an LHCb Upgrade II  
arXiv:1808.08865



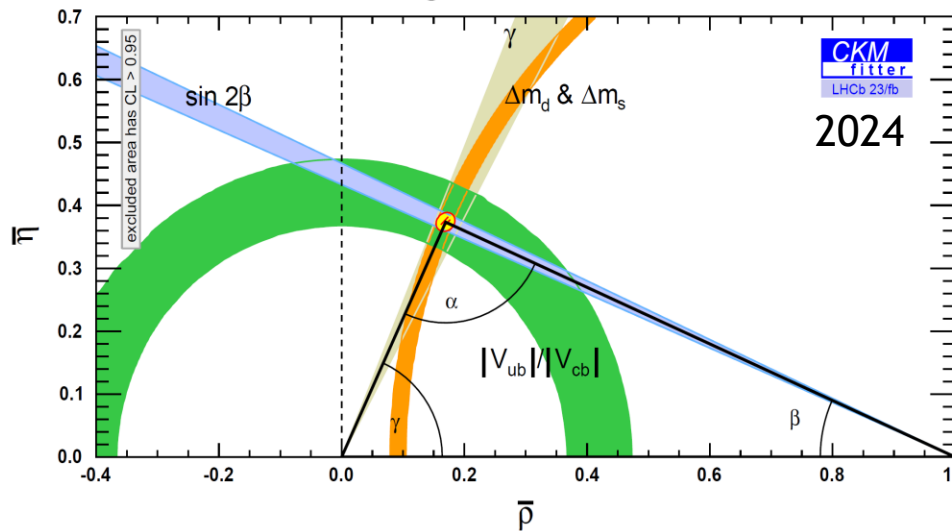
# Prospects for CKM fit : LHCb upgrade

Physics case for an LHCb Upgrade II  
arXiv:1808.08865

LHCb now



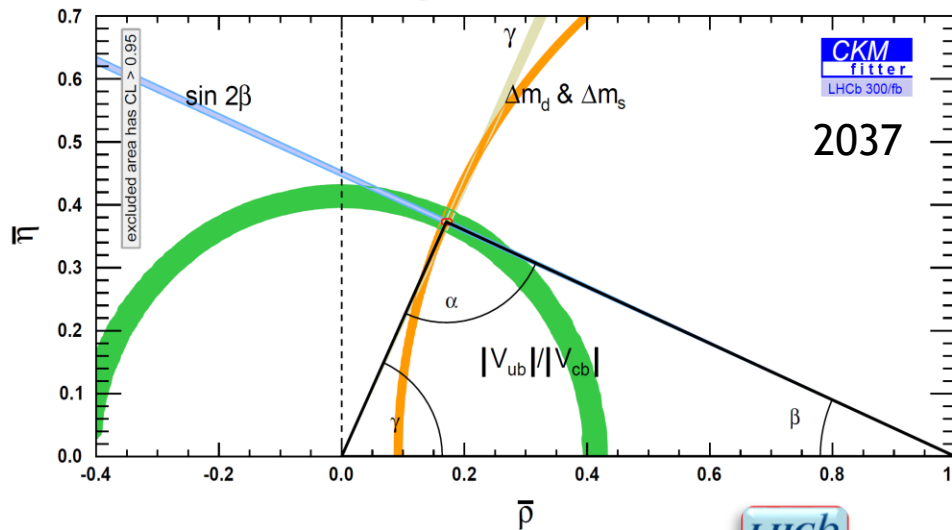
LHCb Upgrade Ia 23 fb<sup>-1</sup>



Inputs

	LHCb (now)	LHCb 23 fb <sup>-1</sup>	LHCb 300 fb <sup>-1</sup>
CKM inputs (LHCb)			
$\sin 2\beta$	$0.760 \pm 0.034$	$0.7480 \pm 0.0095$	$0.7480 \pm 0.0024$
$\gamma$ rad	$1.296^{+0.087}_{-0.101}$	$1.136 \pm 0.025$	$1.136 \pm 0.005$
$ V_{ub} / V_{cb} $	15%	6%	1%
$\Delta m_d$ (ps <sup>-1</sup> )	$0.5065 \pm 0.0020$	same	same
$\Delta m_s$ (ps <sup>-1</sup> )	$17.757 \pm 0.021$	same	same
Hadronic input (LQCD)			
$\xi = \frac{f_{B_d} \sqrt{B_{B_d}}}{f_{B_s} \sqrt{B_{B_s}}}$	2.0%	0.6%	0.2%

LHCb Upgrade II 300 fb<sup>-1</sup>



LHCb “alone”



Observable	Current LHCb	LHCb 2025	Belle II	Upgrade II	ATLAS & CMS
<b>EW Penguins</b>					
$R_K$ ( $1 < q^2 < 6 \text{ GeV}^2 c^4$ )	0.1 [274]	0.025	0.036	0.007	–
$R_{K^*}$ ( $1 < q^2 < 6 \text{ GeV}^2 c^4$ )	0.1 [275]	0.031	0.032	0.008	–
$R_\phi, R_{pK}, R_\pi$	–	0.08, 0.06, 0.18	–	0.02, 0.02, 0.05	–
<b>CKM tests</b>					
$\gamma$ , with $B_s^0 \rightarrow D_s^+ K^-$	$(\begin{smallmatrix} +17 \\ -22 \end{smallmatrix})^\circ$ [136]	$4^\circ$	–	$1^\circ$	–
$\gamma$ , all modes	$(\begin{smallmatrix} +5.0 \\ -5.8 \end{smallmatrix})^\circ$ [167]	$1.5^\circ$	$1.5^\circ$	$0.35^\circ$	–
$\sin 2\beta$ , with $B^0 \rightarrow J/\psi K_s^0$	0.04 [609]	0.011	0.005	0.003	–
$\phi_s$ , with $B_s^0 \rightarrow J/\psi \phi$	49 mrad [44]	14 mrad	–	4 mrad	22 mrad [610]
$\phi_s$ , with $B_s^0 \rightarrow D_s^+ D_s^-$	170 mrad [49]	35 mrad	–	9 mrad	–
$\phi_s^{\bar{s}s}$ , with $B_s^0 \rightarrow \phi \phi$	154 mrad [94]	39 mrad	–	11 mrad	Under study [611]
$a_{\text{sl}}^s$	$33 \times 10^{-4}$ [211]	$10 \times 10^{-4}$	–	$3 \times 10^{-4}$	–
$ V_{ub} / V_{cb} $	6% [201]	3%	1%	1%	–
<b><math>B_s^0, B^0 \rightarrow \mu^+ \mu^-</math></b>					
$\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-)/\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)$	90% [264]	34%	–	10%	21% [612]
$\tau_{B_s^0 \rightarrow \mu^+ \mu^-}$	22% [264]	8%	–	2%	–
$S_{\mu\mu}$	–	–	–	0.2	–
<b><math>b \rightarrow c \ell^- \bar{\nu}_\ell</math> LUV studies</b>					
$R(D^*)$	0.026 [215, 217]	0.0072	0.005	0.002	–
$R(J/\psi)$	0.24 [220]	0.071	–	0.02	–
<b>Charm</b>					
$\Delta A_{CP}(KK - \pi\pi)$	$8.5 \times 10^{-4}$ [613]	$1.7 \times 10^{-4}$	$5.4 \times 10^{-4}$	$3.0 \times 10^{-5}$	–
$A_\Gamma (\approx x \sin \phi)$	$2.8 \times 10^{-4}$ [240]	$4.3 \times 10^{-5}$	$3.5 \times 10^{-4}$	$1.0 \times 10^{-5}$	–
$x \sin \phi$ from $D^0 \rightarrow K^+ \pi^-$	$13 \times 10^{-4}$ [228]	$3.2 \times 10^{-4}$	$4.6 \times 10^{-4}$	$8.0 \times 10^{-5}$	–
$x \sin \phi$ from multibody decays	–	( $K3\pi$ ) $4.0 \times 10^{-5}$	( $K_s^0 \pi \pi$ ) $1.2 \times 10^{-4}$	( $K3\pi$ ) $8.0 \times 10^{-6}$	–

# Conclusions

- Excellent progress from LHCb over the last few years
  - As shown today we are currently exploiting our beautiful Run-II data sample
  - The Run-II precision will be around 3 or 4 degrees

- Latest combination gives

$$\gamma_{\text{LHCb}} = (74.0^{+5.0}_{-5.8})^\circ$$

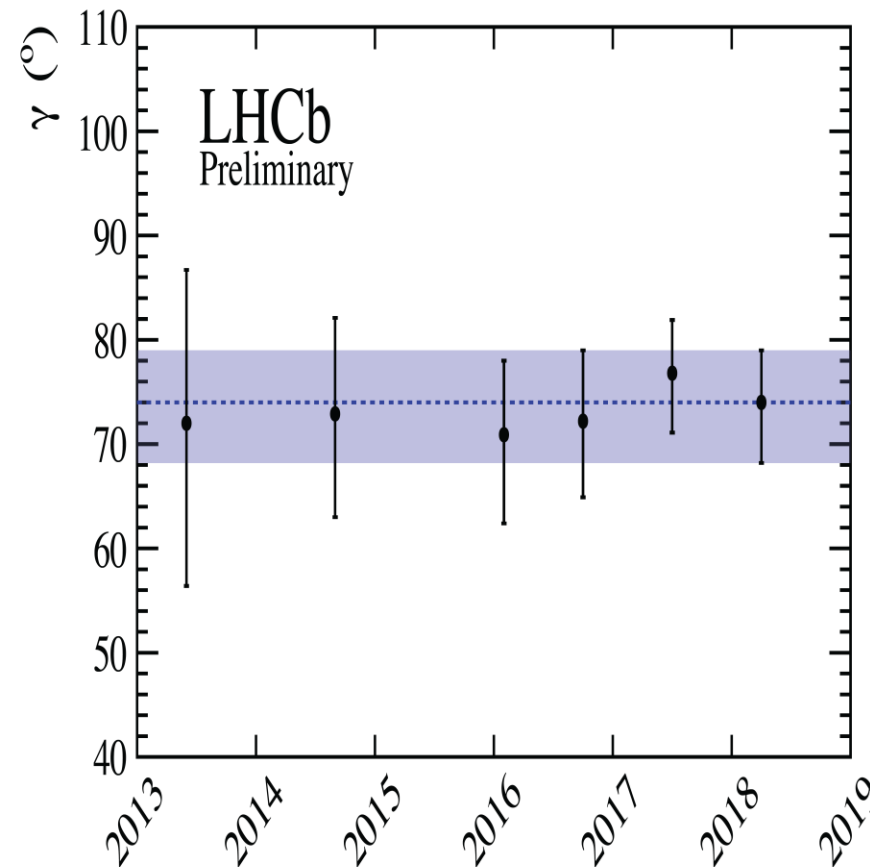
- Indirect measurements

$$\gamma_{\text{CKMfitter}} = (65.6^{+1.0}_{-3.4})^\circ$$

1.7 $\sigma$   
shift

- Watch this space...

- Lots more to come from LHCb, LHCb upgrade(s) and Belle-II!





# BACKUP Slides

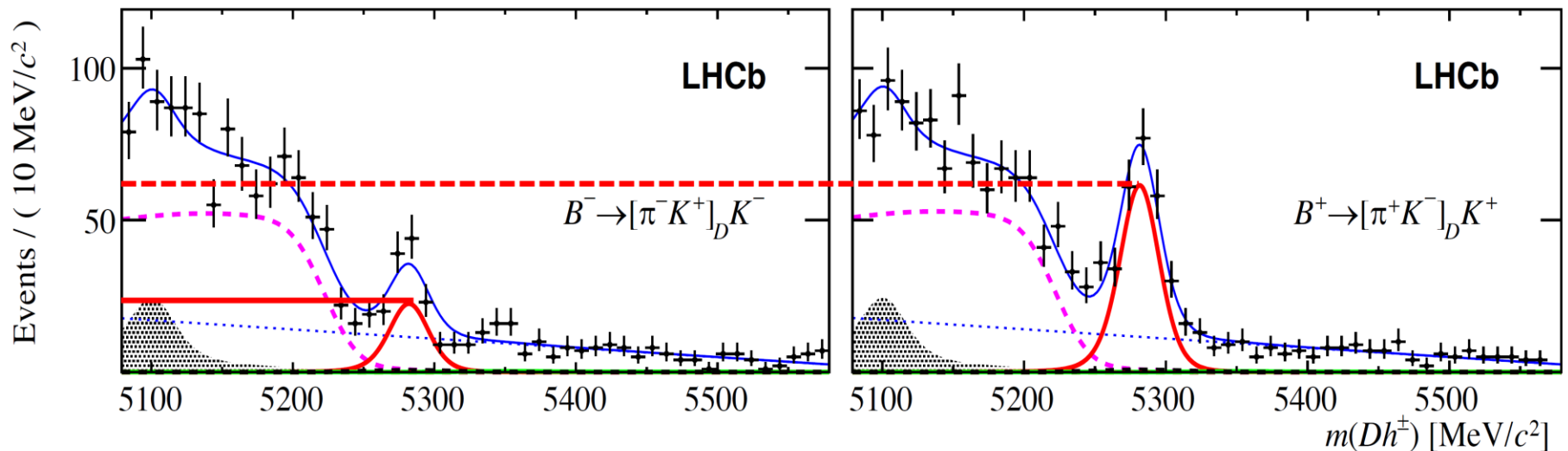


# Measuring $\gamma$ : ADS DK

## ADS observables

$$A_{ADS} = \frac{\Gamma(B^- \rightarrow [K^+\pi^-]_D K^-) - \Gamma(B^+ \rightarrow [K^-\pi^+]_D K^+)}{\Gamma(B^- \rightarrow [K^+\pi^-]_D K^-) + \Gamma(B^+ \rightarrow [K^-\pi^+]_D K^+)} = \frac{2r_B r_D \kappa_D \sin(\delta_B + \delta_D) \sin(\gamma)}{r_B^2 + r_D^2 + 2r_B r_D \kappa_D \cos(\delta_B + \delta_D) \cos(\gamma)} \quad (3)$$

$$R_{ADS} = \frac{\Gamma(B^- \rightarrow [K^+\pi^-]_D K^-) + \Gamma(B^+ \rightarrow [K^-\pi^+]_D K^+)}{\Gamma(B^- \rightarrow [K^-\pi^+]_D K^-) + \Gamma(B^+ \rightarrow [K^+\pi^-]_D K^+)} = r_B^2 + r_D^2 + 2r_B r_D \kappa_D \cos(\delta_B + \delta_D) \cos(\gamma) \quad (4)$$



- Much harder to extract partially reconstructed observables because of  $B_s^0 \rightarrow D^{(*)0} K^+ \pi^-$  backgrounds.

# Measuring $\gamma$ : GLW $D(^*)K$

The  $B^\mp \rightarrow D(^*) h^\mp$  signals

- a positive  $CP$  asymmetry observed in  $B^\pm \rightarrow D_{CP} K^\pm$

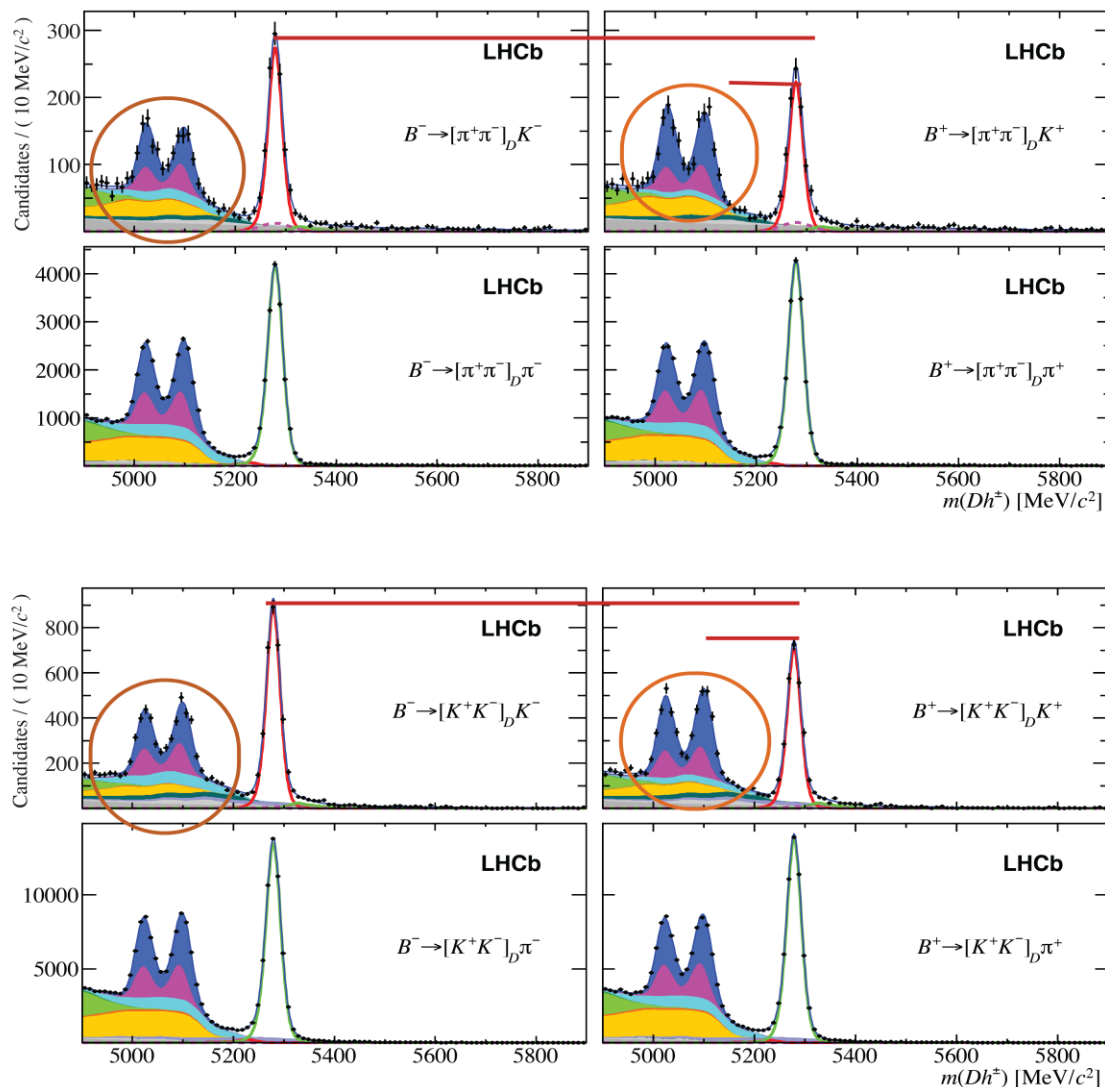
- $B^- \rightarrow D^* K^-$ ,  $D^* \rightarrow D\pi^0$  :  

$$D = D^0 + r_B e^{i(\delta_B - \gamma)} \bar{D}^0$$

- $B^- \rightarrow D^* K^-$ ,  $D^* \rightarrow D\gamma$  :  

$$D = D^0 + r_B e^{i(\delta_B + \pi - \gamma)} \bar{D}^0$$
  
 PRD **70**, 091503

$CP$  asymmetries from  
 $D^* \rightarrow D\pi^0$  and  $D^* \rightarrow D\gamma$   
 have opposite signs



PLB **777** (1028) 16



# Measuring $\gamma$ : GLW D(\*)K

Defining

$$R_{K/\pi}^{K\pi} \equiv \frac{\Gamma(B^- \rightarrow [K^- \pi^+]_D K^-) + \Gamma(B^+ \rightarrow [K^+ \pi^-]_D K^+)}{\Gamma(B^- \rightarrow [K^- \pi^+]_D \pi^-) + \Gamma(B^+ \rightarrow [K^+ \pi^-]_D \pi^+)} \approx \frac{\mathcal{B}(B^- \rightarrow D^0 K^-)}{\mathcal{B}(B^- \rightarrow D^0 \pi^-)}$$

and averaging  $R_{KK}$ ,  $R_{\pi\pi}$  and  $A_{CP}^{KK}$ ,  $A_{CP}^{\pi\pi}$  :

$$R_{CP+} = \frac{\Gamma(B^- \rightarrow D_{CP} K^-) + \Gamma(B^+ \rightarrow D_{CP} K^+)}{\Gamma(B^- \rightarrow D_{CP} \pi^-) + \Gamma(B^+ \rightarrow D_{CP} \pi^+)} \times \frac{1}{R_{K/\pi}^{K\pi}}$$

$$= 1 + (r_B^{DK})^2 + 2r_B^{DK} \cos \delta_B^{DK} \cos \gamma$$

$$A_{CP+} = \frac{2r_B^{DK} \sin \delta_B^{DK} \sin \gamma}{1 + (r_B^{DK})^2 + 2r_B^{DK} \cos \delta_B^{DK} \cos \gamma}$$

$$R_{CP+} = 0.989 \pm 0.013 \pm 0.010$$

$$A_{CP+} = 0.124 \pm 0.012 \pm 0.002$$

PLB **777** (1028) 16

Values of these and the other observables to be used in the  $\gamma$  combination

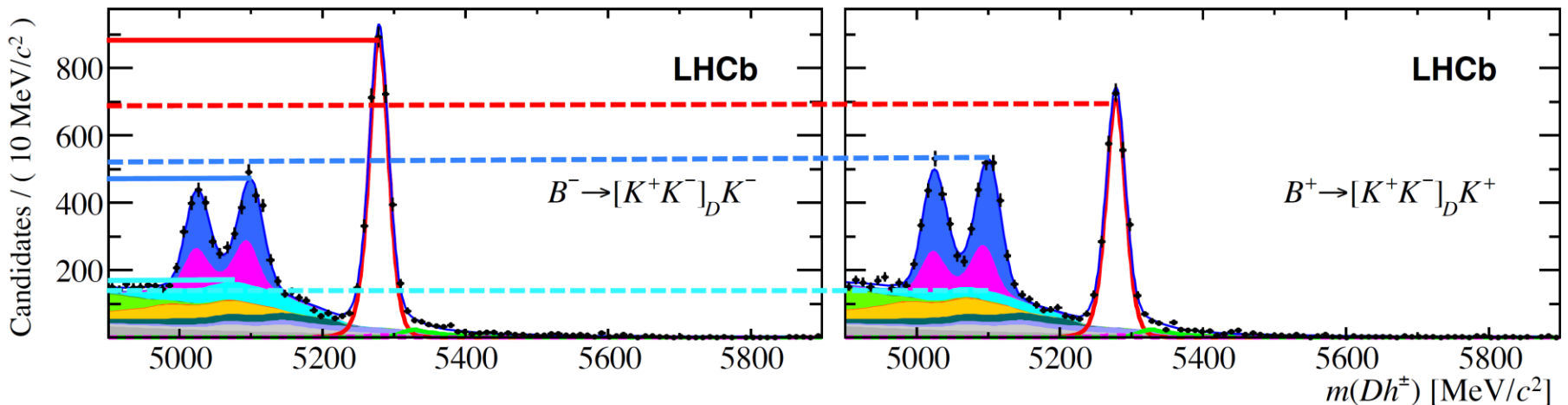
# Measuring $\gamma$ : GLW $D(^*)K$

- ▶ CP eigenstates e.g.  $D \rightarrow KK$ ,  $D \rightarrow K_S^0 \pi^0$  ▶ [Phys. Lett. B253 (1991) 483]
- ▶ Gronau, London, Wyler (1991) ▶ [Phys. Lett. B265 (1991) 172]

## GLW observables

$$A_{CP} = \frac{\Gamma(B^- \rightarrow D_{CP}^0 K^-) - \Gamma(B^+ \rightarrow D_{CP}^0 K^+)}{\Gamma(B^- \rightarrow D_{CP}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP}^0 K^+)} = \frac{\pm 2r_B(2F^+ + 1) \sin(\delta_B) \sin(\gamma)}{1 + r_B^2 \pm 2r_B(2F^+ + 1) \cos(\delta_B) \cos(\gamma)} \quad (1)$$

$$R_{CP} = \frac{\Gamma(B^- \rightarrow D_{CP}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP}^0 K^+)}{\Gamma(B^- \rightarrow D^0 K^-) + \Gamma(B^+ \rightarrow D^0 K^+)} = 1 + r_B^2 \pm 2r_B(2F^+ + 1) \cos(\delta_B) \cos(\gamma) \quad (2)$$



- ▶ LHCb has recently extracted GLW observables from partially reconstructed  $B^- \rightarrow D^{*0} K^-$  in the same fit - [Phys. Lett. B777 (2018) 16]
- ▶ Can extend to quasi-CP-eigenstates ( $D^0 \rightarrow KK\pi^0$ ) if fraction of CP content,  $F^+$ , is known

$F^+=0$  in Eq (1) & (2) for  $KK$  and  $\pi\pi$

Measurement of  $CP$  observables in  $B^\pm \rightarrow DK^{*\pm}$  decays  
 using two- and four-body  $D$  final states JHEP 11(2017) 156

12  $CP$  observables from  $B^- \rightarrow D(\rightarrow f)K^*(892)^-$ ,  $K^*(892)^- \rightarrow K_S^0\pi^-$   
 $f = K^-K^+$ ,  $\pi^-\pi^+$ ,  $K^\mp\pi^\pm$ ,  $\pi^+\pi^-\pi^+\pi^-$ ,  $K^\mp\pi^\pm\pi^+\pi^-$

$$A_{CP}^f = \frac{\Gamma(B^- \rightarrow D(\rightarrow f)K^{*-}) - \Gamma(B^+ \rightarrow D(\rightarrow \bar{f})K^{*+})}{\Gamma(B^- \rightarrow D(\rightarrow f)K^{*-}) + \Gamma(B^+ \rightarrow D(\rightarrow \bar{f})K^{*+})} \quad (A_{CP} = A_{\text{raw}} - A_{\text{prod}} - A_{\text{det}})$$

$$R_f = \frac{\Gamma(B^- \rightarrow D(\rightarrow f)K^{*-}) + \Gamma(B^+ \rightarrow D(\rightarrow \bar{f})K^{*+})}{\Gamma(B^- \rightarrow D_{\text{fav}}K^{*-}) + \Gamma(B^+ \rightarrow D_{\text{fav}}K^{*+})} \times \frac{\mathcal{B}(D_{\text{fav}}^0)}{\mathcal{B}(D^0 \rightarrow f)}$$

Neglecting  $CPV$  and  
 mixing in  $D$  decays:

$$A_{CP}^{KK} = A_{CP}^{\pi\pi} = A_{CP+}$$

$$R_{KK} = R_{\pi\pi} = R_{CP+}$$

The ADS modes:

$$B^- \rightarrow [K^+\pi^-]_D K^{*-}$$

$$B^- \rightarrow [K^+\pi^-\pi^+\pi^-]_D K^{*-}$$

No  $CPV$  expected in  
 favoured decays  $D_{\text{fav}}$

$$B^- \rightarrow [K^-\pi^+]_D K^{*-}$$

$$B^- \rightarrow [K^-\pi^+\pi^+\pi^-]_D K^{*-}$$



## The relation between $CP$ observables and physics parameters:

$$A_{CP+} = \frac{2\kappa r_B \sin \delta_B \sin \gamma}{1 + r_B^2 + 2\kappa r_B \cos \delta_B \cos \gamma}, \quad R_{CP+} = 1 + r_B^2 + 2\kappa r_B \cos \delta_B \cos \gamma,$$

$\kappa$  accounts for  $K_S^0 \pi$  not from  $K^*$  ( $\kappa=1$ : pure  $K^*$ )

$\kappa = 0.95 \pm 0.06$ ,  
from simulations

$$A_{\pi\pi\pi\pi} = \frac{2\kappa (2F_{4\pi} - 1) r_B \sin \delta_B \sin \gamma}{1 + r_B^2 + 2\kappa (2F_{4\pi} - 1) r_B \cos \delta_B \cos \gamma}, \quad F_{4\pi} (\sim 0.75) : \pi^- \pi^+ \pi^- \pi^+ \text{ is not a pure } CP \text{ eigenstate}$$

$$R_{\pi\pi\pi\pi} = 1 + r_B^2 + 2\kappa (2F_{4\pi} - 1) r_B \cos \delta_B \cos \gamma,$$

PLB **747** (2015) 9

## ADS decays need additional external inputs

$$R_{K\pi}^{\pm} = \frac{r_B^2 + (r_D^{K\pi})^2 + 2\kappa r_B r_D^{K\pi} \cos(\delta_B + \delta_D^{K\pi} \pm \gamma)}{1 + r_B^2 (r_D^{K\pi})^2 + 2\kappa r_B r_D^{K\pi} \cos(\delta_B - \delta_D^{K\pi} \pm \gamma)},$$

$r_D^{K\pi}, \delta_D^{K\pi}$

HFLAV, arXiv:1612.07233

$$R_{K\pi\pi\pi}^{\pm} = \frac{r_B^2 + (r_D^{K3\pi})^2 + 2\kappa r_B \kappa_{K3\pi} r_D^{K3\pi} \cos(\delta_B + \delta_D^{K3\pi} \pm \gamma)}{1 + (r_B r_D^{K3\pi})^2 + 2\kappa r_B \kappa_{K3\pi} r_D^{K3\pi} \cos(\delta_B - \delta_D^{K3\pi} \pm \gamma)}.$$

$r_D^{K3\pi}, \delta_D^{K3\pi}, \kappa_{K3\pi}$

PRL **116** (2016) 241801

PLB **757** (2016) 520



# Measure strong phases

e.g. probe strong-phase distribution of multibody decays...

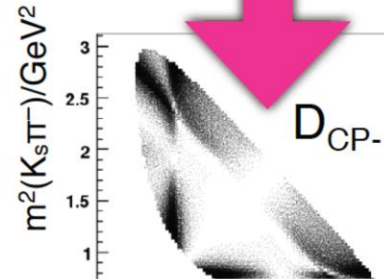
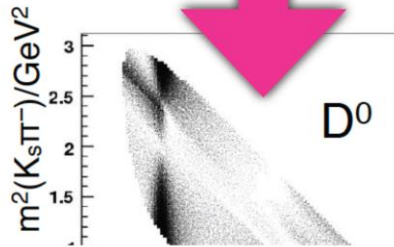
$$D^{*+} \rightarrow D^0 \pi^+ \text{ or } D^0 \rightarrow K_l \nu$$

$$D^0 \rightarrow K_s \pi^+ \pi^-$$

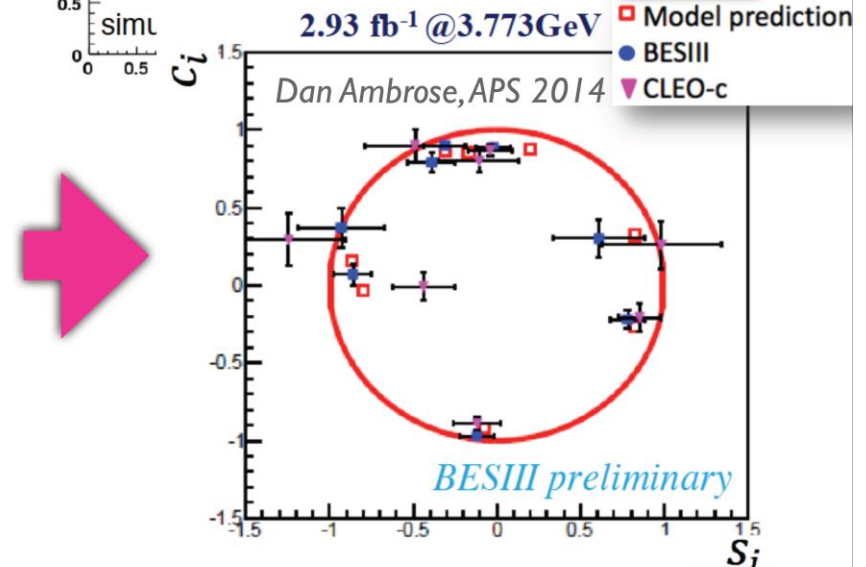
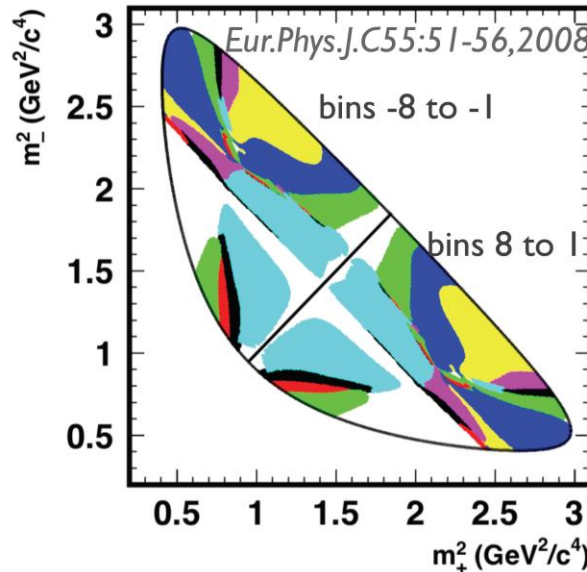
$$\psi'' \rightarrow D_a D_b \rightarrow D_a \rightarrow KK \text{ eg. CP+}$$

$$D_b \rightarrow K_s \pi^+ \pi^-$$

Flavour tagged  
Distribution  $\sim$   
 $|D^0|^2$  or  $|\bar{D}^0|^2$



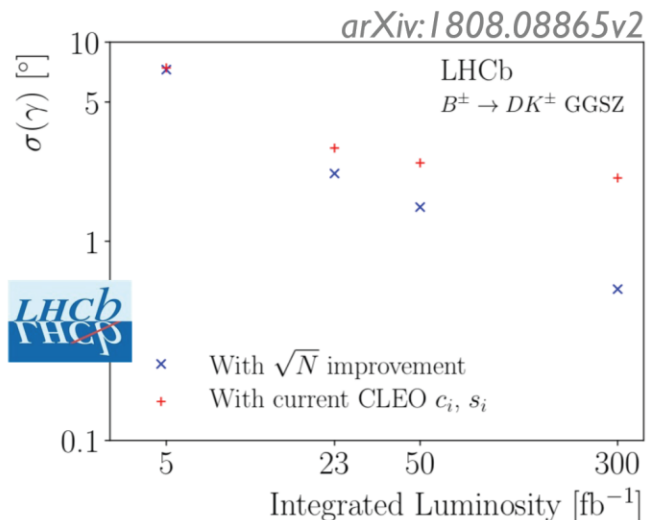
CP-tagged  $\sim$   
 $|D^0|^2 + |\bar{D}^0|^2 \pm$   
 $2 |D^0 \bar{D}^0| \cos \delta$



- Most precise determination of  $\gamma$  from a single channel from  $B \rightarrow DK$  with  $D \rightarrow K_{shh}$

$$\gamma = (80.0^{+10.0}_{-9.0})^\circ \quad JHEP 08 176$$

- Uncertainty due to strong-phase inputs (CLEO-c)  $4^\circ >$  uncertainty due to experimental systematic effects  $2^\circ$



$3^\circ$  with  $50 \text{ ab}^{-1}$  at BELLEII

P. Krishnan, FPCP2018

- Input important for  $B \rightarrow DK\pi$  with  $D \rightarrow K_{shh}$ , precision of  $2^\circ$  achievable after the upgrade *Craik et al., arXiv:1712.0853*

# How does this GGSZ Model Indep. Method works ?

- The Dalitz plot is divided into  $2n$  bins, from  $i = -n$  to  $i = +n$ . The populations of bins  $\pm i$  are

$$N_{\pm i}^+ = h_{B^+} \left[ F_{\mp i} + (x_+^2 + y_+^2) F_{\pm i} + 2\sqrt{F_i F_{-i}} (x_+ c_{\pm i} - y_+ s_{\pm i}) \right]$$

$$N_{\pm i}^- = h_{B^-} \left[ F_{\pm i} + (x_-^2 + y_-^2) F_{\mp i} + 2\sqrt{F_i F_{-i}} (x_- c_{\pm i} + y_- s_{\pm i}) \right]$$

normalization  
factors

fraction of  
decays in bins  $\pm i$

strong phases  
from CLEO-c

$$F_i = \frac{\int_i dm_-^2 dm_+^2 |A_D(m_-^2, m_+^2)|^2 \eta(m_-^2, m_+^2)}{\sum_j \int_j dm_-^2 dm_+^2 |A_D(m_-^2, m_+^2)|^2 \eta(m_-^2, m_+^2)}$$

from  $B \rightarrow D^{*\pm} \mu^\mp \nu_\mu X$  with  
 $D^{*+} \rightarrow D^0 \pi^+$ ,  $D^0 \rightarrow K_S^0 \pi^+ \pi^+$

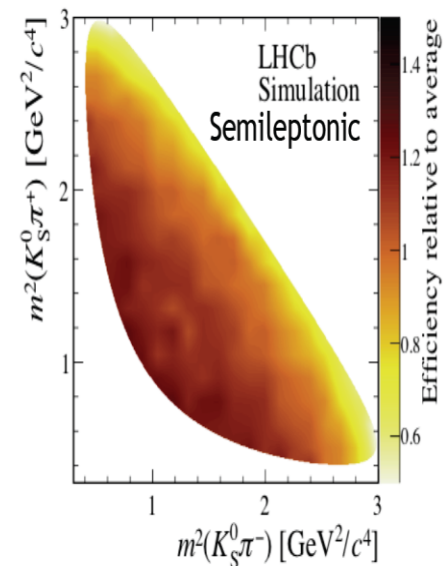
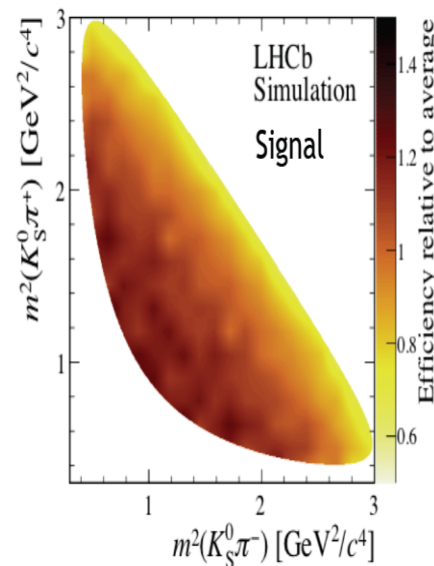
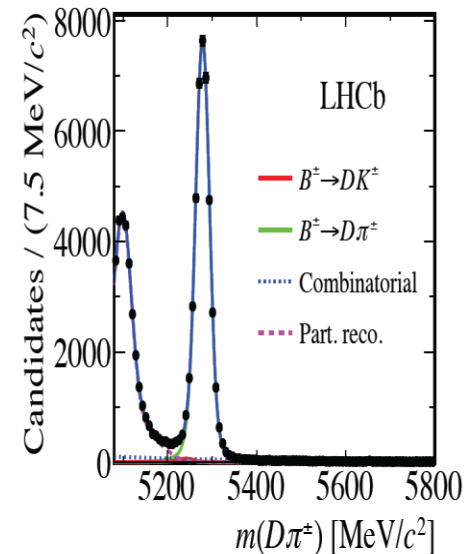
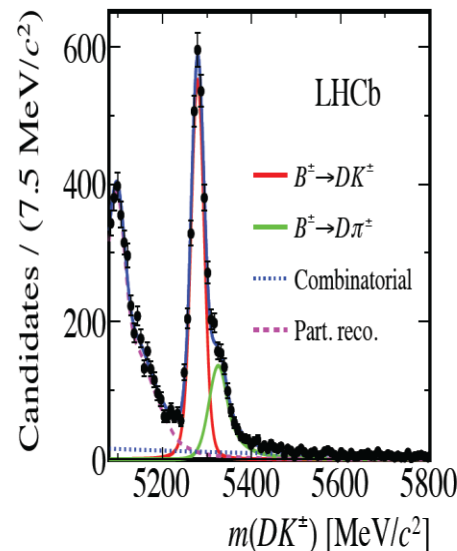
$$c_i \equiv \frac{\int_i dm_-^2 dm_+^2 |A_D(m_-^2, m_+^2)| |A_D(m_+^2, m_-^2)| \cos[\delta_D(m_-^2, m_+^2) - \delta_D(m_+^2, m_-^2)]}{\sqrt{\int_i dm_-^2 dm_+^2 |A_D(m_-^2, m_+^2)|^2 \int_i dm_-^2 dm_+^2 |A_D(m_+^2, m_-^2)|^2}}$$

$\gamma$ ,  $r_B$ ,  $\delta_B$  translated into  $x_\pm \equiv r_B \cos(\delta_B \pm \gamma)$ ,  $y_\pm \equiv r_B \sin(\delta_B \pm \gamma)$

# How does this GGSZ Model Indep. Method works ?

- Fitting the invariant mass distribution
  - Cross-feeds from  $\pi \rightarrow K$  misid taken from control mode  $B^- \rightarrow D\pi^-$
- Efficiencies over the D Dalitz plot
  - Taken from simulation with data driven corrections
  - Smoothly varying
  - Account for differences between the signal decays and semileptonic control sample used to described the fraction of  $D^0 \bar{D}^0$  in each bin

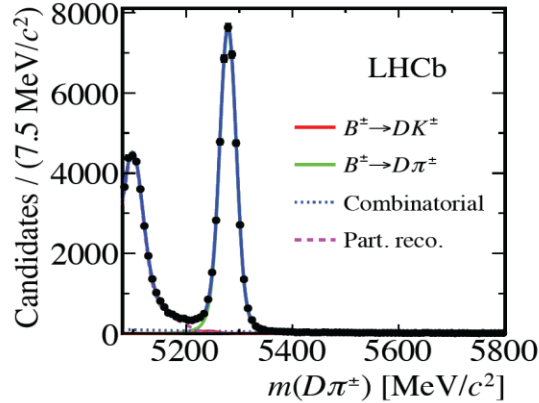
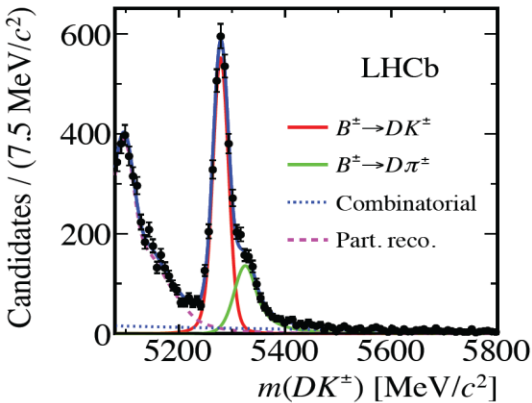
[LHCb-PAPER-2018-017]



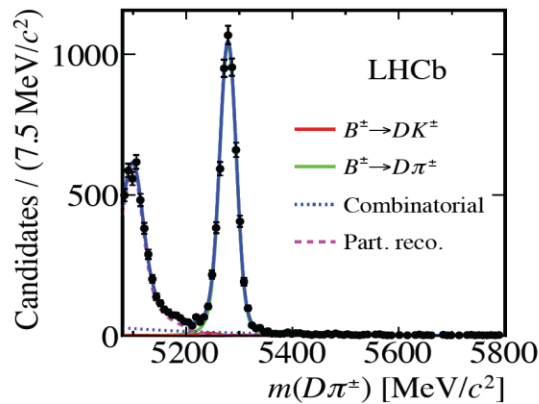
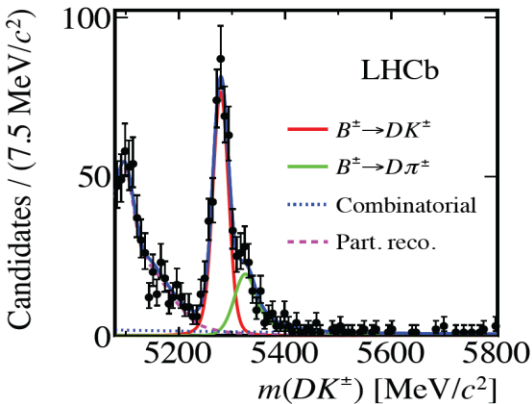


# How does this GGSZ Model Indep. Method works ?

$$D^0 \rightarrow K_S^0 \pi^+ \pi^- \quad \text{JHEP 08, 176}$$



$$D^0 \rightarrow K_S^0 K^+ K^-$$



$B^- \rightarrow D\pi^-$  used to estimate contamination in  $B^- \rightarrow DK^-$  sample due to  $\pi - K$  misID

A fit to the 8  $B^\pm \rightarrow Dh^\pm$  subsamples, integrated over the DP, fix the shapes of signal and bkg.

yields/bin of  $B^\pm \rightarrow D\pi^\pm$  :  
direct  $B^\pm$  mass fit

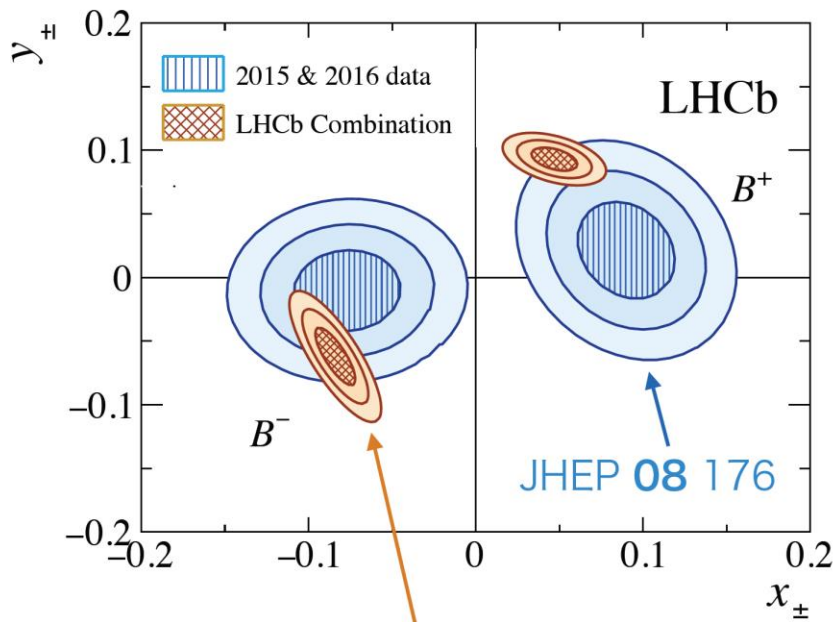
yields/bin of  $B^\pm \rightarrow DK^\pm$  :

$$S_i^\pm = N_{\text{tot}}(DK) \times \frac{N_i^\pm}{\sum_{-n}^{+n} N_i^\pm}$$

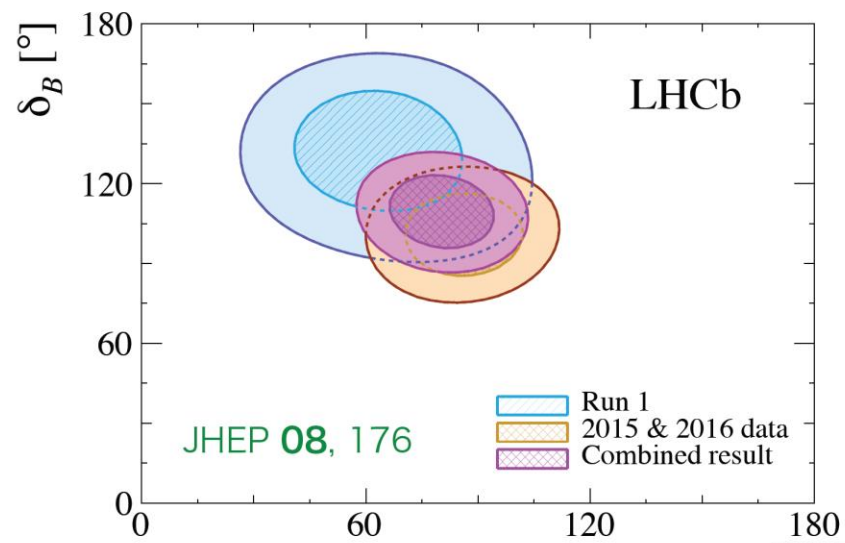
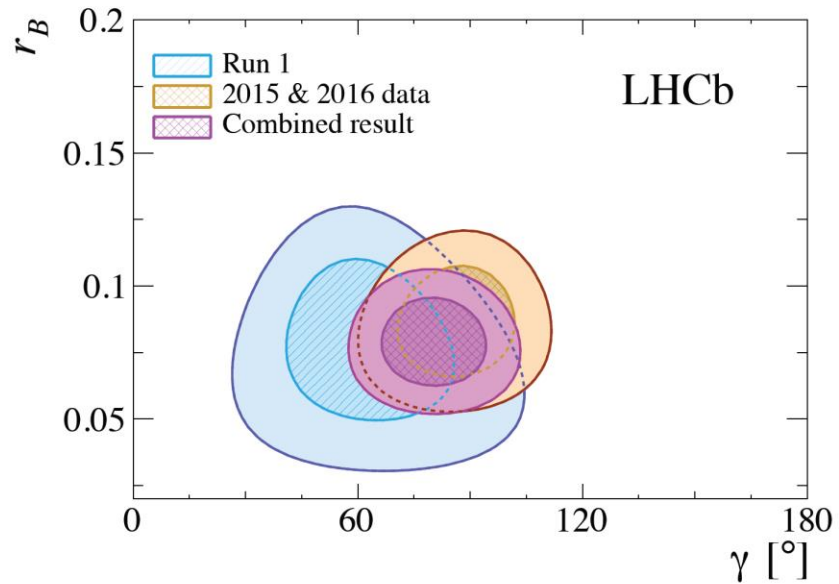
$$N_{\pm i}^+ = h_{B^+} \left[ F_{\mp i} + (x_+^2 + y_+^2) F_\pm + 2\sqrt{F_i F_{-i}} (x_+ c_{\pm i} - y_+ s_{\pm i}) \right]$$



# GGSZ Model Indep. Method Run1/2



LHCb-CONF-2017-004



## Dalitz structure of other multibody D modes

- ▶ We have a good model for the GGSZ modes ( $D \rightarrow K_S^0 \pi \pi$  and  $D \rightarrow K_S^0 K K$ ) but development of others (e.g. the 4-body charm decays) could prove very useful.
- ▶ Recent measurements of  $D^0 \rightarrow K^+ \pi^- \pi^+ \pi^-$  amplitude model at LHCb - [\[arXiv:1712.08609\]](#)
  - ▶ Indeed equivalent knowledge of  $c_i$  and  $s_i$  for this and related modes allows for binned Dalitz analyses in  $\gamma$  (see Tim Evans talk later)
- ▶ For some modes (e.g.  $D \rightarrow K K \pi^0$  and  $D^0 \rightarrow 4\pi$ ) there is a low  $F^+$  value suggesting a Dalitz analysis could offer considerable improvement
- ▶ Many recent developments in  $D^0 \rightarrow \pi^+ \pi^- \pi^+ \pi^-$  and  $D^0 \rightarrow K^+ K^- \pi^+ \pi^-$  Dalitz models with CLEO data - [\[JHEP 05 \(2017\) 143\]](#)
- ▶ Can one define optimal binning schemes for various  $D^0 \rightarrow 4h$  and  $D^0 \rightarrow hh\pi^0$  from which  $c_i$  and  $s_i$  equivalents can be extracted?

# TDCPV $B_s \rightarrow D_s^\mp K^\pm$

$$\frac{d\Gamma_{B_s^0 \rightarrow f}(t)}{dt} = \frac{1}{2} |A_f|^2 (1 + |\lambda_f|^2) e^{-\Gamma_s t} \left[ \cosh\left(\frac{\Delta\Gamma_s t}{2}\right) + \underline{A_f^{\Delta\Gamma}} \sinh\left(\frac{\Delta\Gamma_s t}{2}\right) + \underline{C_f} \cos(\Delta m_s t) - \underline{S_f} \sin(\Delta m_s t) \right],$$

$$\frac{d\Gamma_{\bar{B}_s^0 \rightarrow f}(t)}{dt} = \frac{1}{2} |A_f|^2 \left| \frac{p}{q} \right|^2 (1 + |\lambda_f|^2) e^{-\Gamma_s t} \left[ \cosh\left(\frac{\Delta\Gamma_s t}{2}\right) + \underline{A_f^{\Delta\Gamma}} \sinh\left(\frac{\Delta\Gamma_s t}{2}\right) - \underline{C_f} \cos(\Delta m_s t) + \underline{S_f} \sin(\Delta m_s t) \right],$$

... and similar equations for  $\bar{f}$  (e.g.  $f = D_s^- K^+$ ,  $\bar{f} = D_s^+ K^-$ )

Five independent observables assuming no CP violation in mixing or in decay

$$C_f = \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2} = -C_{\bar{f}} = -\frac{1 - |\lambda_{\bar{f}}|^2}{1 + |\lambda_{\bar{f}}|^2},$$

$$\lambda_f = \frac{q}{p} \frac{\bar{A}_f}{A_f}$$

$$S_f = \frac{2\mathcal{I}m(\lambda_f)}{1 + |\lambda_f|^2}, \quad A_f^{\Delta\Gamma} = \frac{-2\mathcal{R}e(\lambda_f)}{1 + |\lambda_f|^2},$$

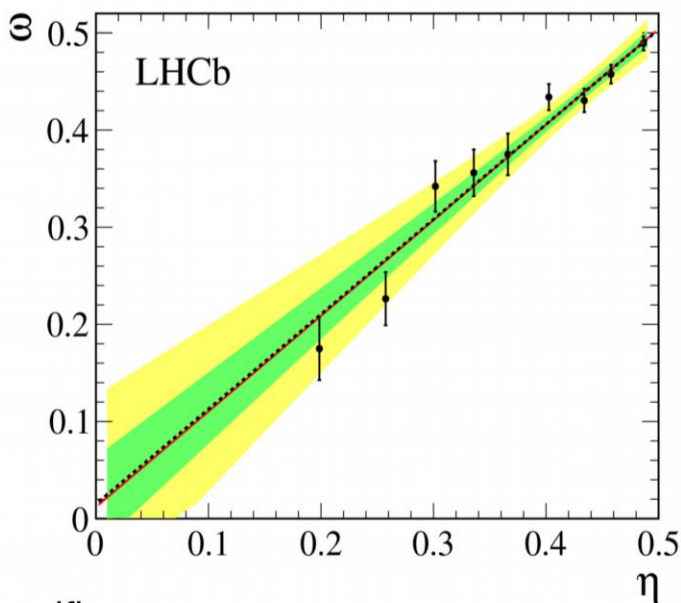
$$|\lambda_f| = |\lambda_{\bar{f}}| \equiv r_{D_s K} \sim 0.4$$

$$S_{\bar{f}} = \frac{2\mathcal{I}m(\lambda_{\bar{f}})}{1 + |\lambda_{\bar{f}}|^2}, \quad A_{\bar{f}}^{\Delta\Gamma} = \frac{-2\mathcal{R}e(\lambda_{\bar{f}})}{1 + |\lambda_{\bar{f}}|^2}.$$

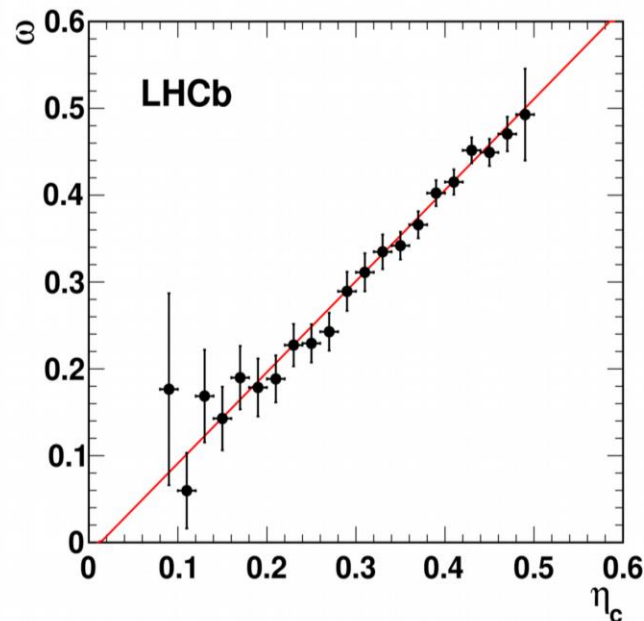


# Tagging $B_s \rightarrow D_s^- K^\pm$

Same side kaon  
LHCb-PAPER-2015-056  
JINST 11 (2016) P05010



Opposite side taggers  
LHCb-PAPER-2011-027  
EPJ C72 (2012) 2022



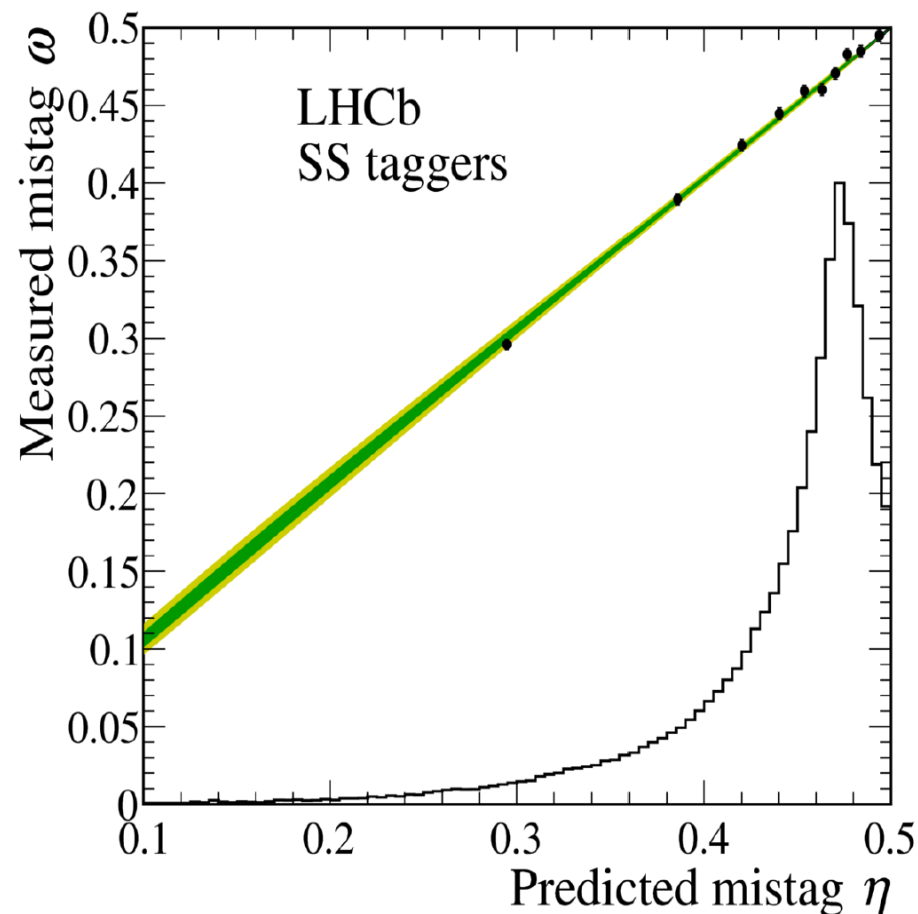
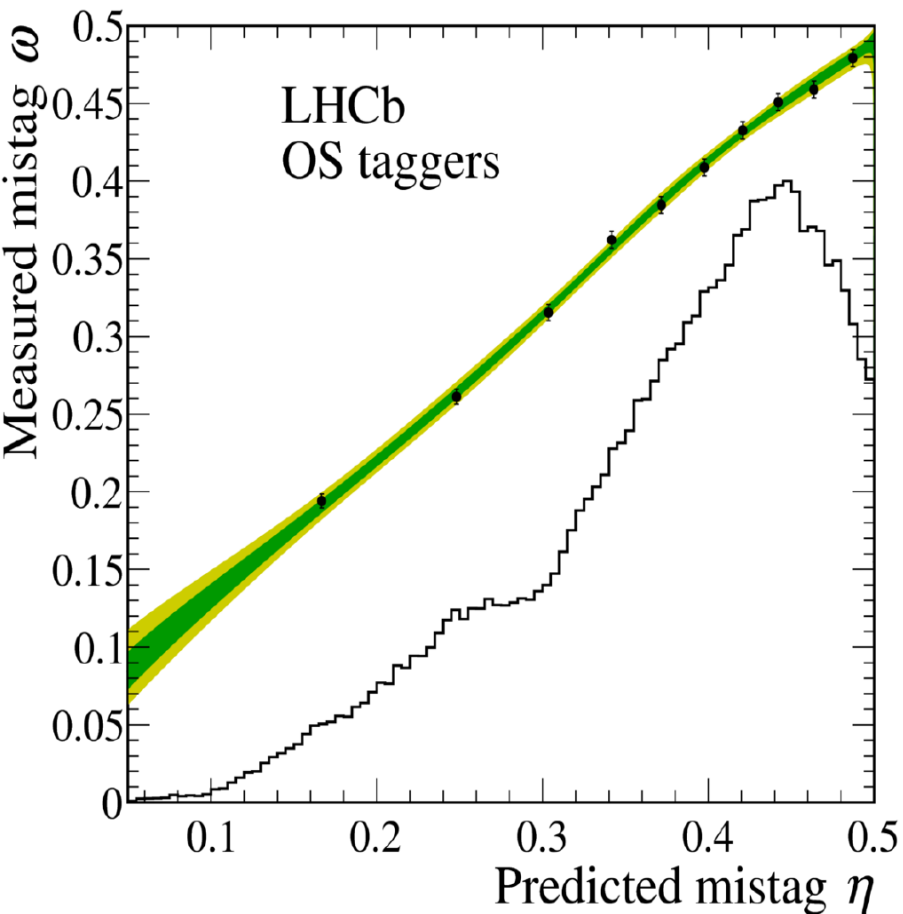
Analysis-specific  
calibration:

$B_s^0 \rightarrow D_s^- \pi^+$	$\epsilon_{\text{tag}} [\%]$	$\epsilon_{\text{eff}} [\%]$
OS only	$12.94 \pm 0.11$	$1.41 \pm 0.11$
SS only	$39.70 \pm 0.16$	$1.29 \pm 0.13$
Both OS and SS	$24.21 \pm 0.14$	$3.10 \pm 0.18$
Total	$76.85 \pm 0.24$	$5.80 \pm 0.25$

LHCb-PAPER-2017-047, 3 fb<sup>-1</sup>  
JHEP 03 (2018) 059

$$\epsilon_{\text{eff}} = \epsilon_{\text{tag}} (1 - 2\langle \omega \rangle)^2$$

# Tagging $B_d \rightarrow D^{\mp} \pi^{\pm}$

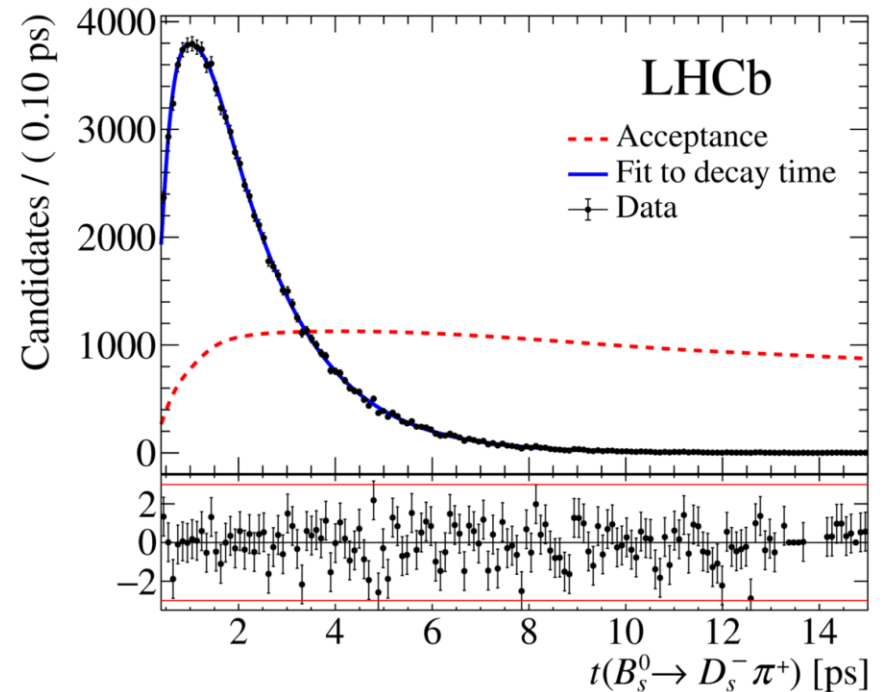
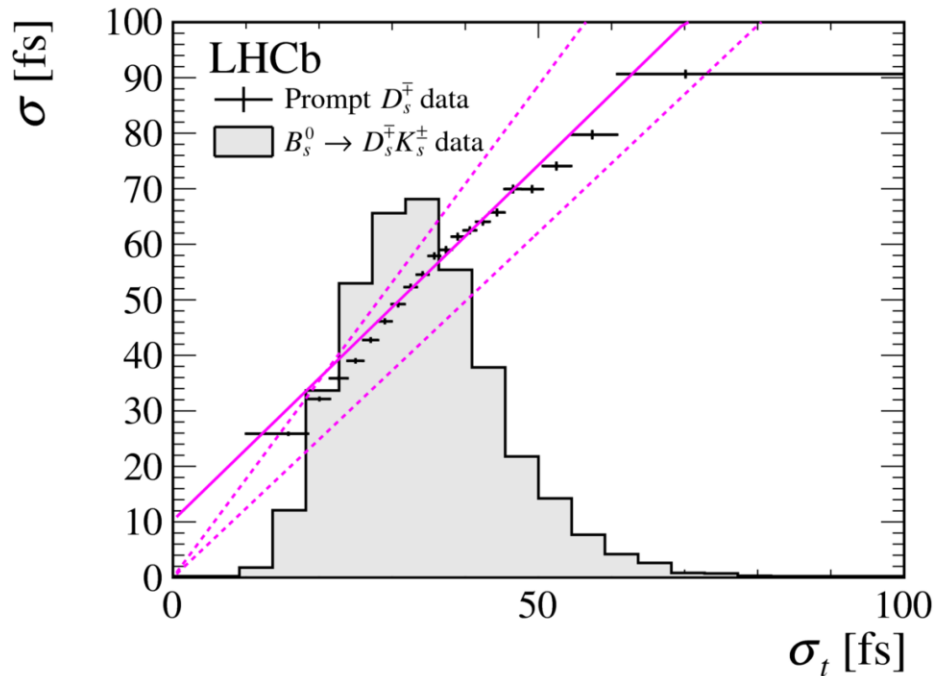


Exploit fact that  $|C|=1$  to calibrate tagging with signal channel

$$\varepsilon_{\text{eff}} = (5.59 \pm 0.01)\%$$



# Decay time resolution and acceptance $B_s \rightarrow D_s^\mp K^\pm$



- Candidate-by-candidate resolution used to improve sensitivity
  - Vertex fit gives good estimate ( $\sigma_t$ ); calibrated with prompt  $D_s$  mesons
- Known lifetime of  $B_s \rightarrow D_s \pi$  used to obtain acceptance function
  - Corrections for  $B_s \rightarrow D_s K / B_s \rightarrow D_s \pi$  differences obtained from MC
  - Important source of systematic uncertainty on  $A^{\Delta\Gamma}$  observables



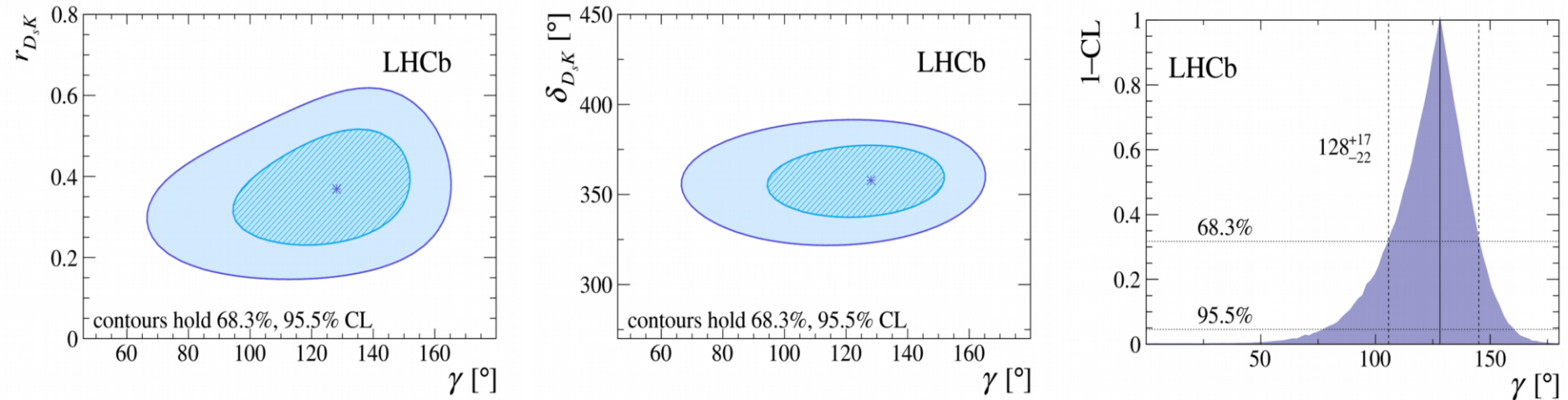
# Systematics $B_s \rightarrow D_s^\mp K^\pm$

Quoted relative to the statistical uncertainty

Source	$C_f$	$A_f^{\Delta\Gamma}$	$A_{\bar{f}}^{\Delta\Gamma}$	$S_f$	$S_{\bar{f}}$
Detection asymmetry	0.02	0.28	0.29	0.02	0.02
$\Delta m_s$	0.11	0.02	0.02	0.20	0.20
Tagging and scale factor	0.18	0.02	0.02	0.16	0.18
Tagging asymmetry	0.02	0.00	0.00	0.02	0.02
Correlation among observables	0.20	0.38	0.38	0.20	0.18
Closure test	0.13	0.19	0.19	0.12	0.12
Acceptance, simulation ratio	0.01	0.10	0.10	0.01	0.01
Acceptance data fit, $\Gamma_s$ , $\Delta\Gamma_s$	0.01	0.18	0.17	0.00	0.00
Total	0.32	0.55	0.55	0.35	0.35

Mainly from control samples – will scale with statistics  
Others also appear reducible

# Constraint on $\gamma$ : $B_s \rightarrow D_s^\mp K^\pm$



Measurements of five observables converted to constraints on three parameters using *GammaCombo* (LHCb-PAPER-2016-032, LHCb-CONF-2018-002)

$\gamma - 2\beta_s$  converted to  $\gamma$  using  
 $-\beta_s$  from  $B_s \rightarrow J/\psi\phi$

$$\gamma = (128^{+17}_{-22})^\circ,$$

$$\delta = (358^{+13}_{-14})^\circ,$$

$$r_{D_s K} = 0.37^{+0.10}_{-0.09},$$

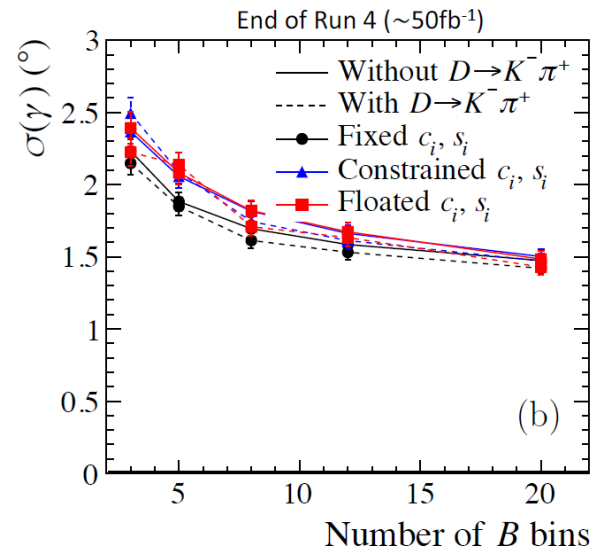
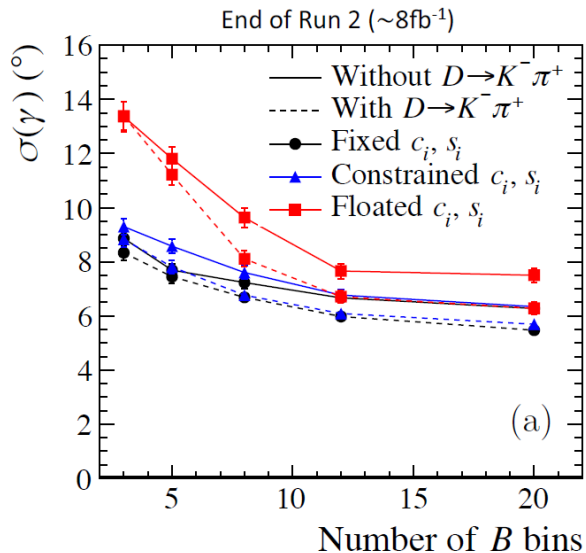
**3.8 $\sigma$  evidence  
 for CP violation**

# 3-body decay $B^0 \rightarrow D\pi^-K^+$

- ▶ Some studies of future prospects of the  $B$  Dalitz method with GGSZ modes in [\[arXiv:1712.07853\]](#)
- ▶ Can include GLW, ADS and GGSZ modes in single framework to improve constraints on  $B$  Dalitz bins,  $\varkappa_j$  and  $\sigma_j$
- ▶ The double Dalitz method has **sufficient information** (large number of bins) to extract  $c_i$  and  $s_i$

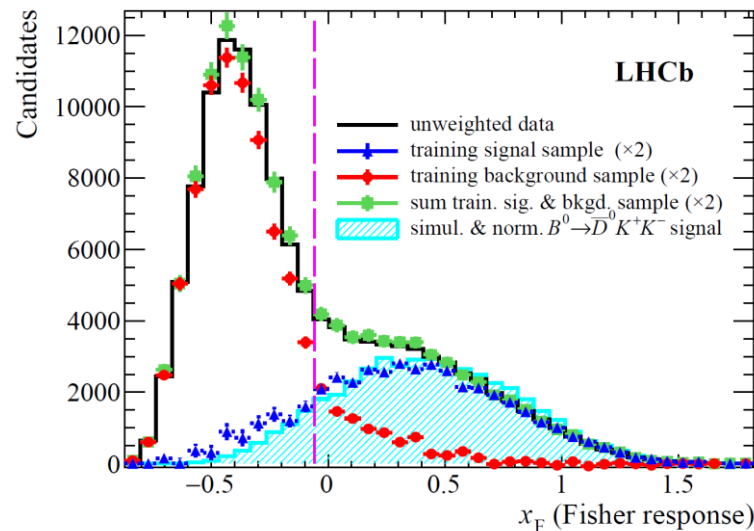
## Double Dalitz observables (partial rate as function of both Dalitz positions)

$$|A|^2 = |A_B|^2 |A_D|^2 + |\bar{A}_B|^2 |\bar{A}_D|^2 + 2|A_B| |A_D| |\bar{A}_B| |\bar{A}_D| [(\varkappa c - \sigma s) \cos(\gamma) - (\varkappa s + \sigma c) \sin(\gamma)]$$



# Selection of $B^0_{(s)} \rightarrow \bar{D}^0 K^+ K^-$ decays

- ✓  $\bar{D}^0$  reconstructed in  $K^+ \pi^-$  decay
- ✓ Kinematic and topological discriminating variables
- ✓ Charmless B decays rejected by requiring the D meson vertex to be downstream of the B meson vertex
- ✓ Veto of  $B^0 \rightarrow D^*(2010)^- \pi^+$ ,  $D^*(2010)^- \rightarrow \bar{D}^0 \pi^-$
- ✓ Combinatorial background rejected with robust MVA Fisher discriminant optimised on data with  $B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$  using sPlot technique



- ✓ Selections for  $B^0_{(s)} \rightarrow \bar{D}^0 K^+ K^-$  signal and  $B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$  normalisation modes differ only on the PID of the  $h^+ h^-$  pair (use of RICHs)
- ✓ One candidate/event only

# invariant mass fit of $B^0_{(s)} \rightarrow \bar{D}^0 h^+ h^-$ decays

- ✓ Signals modelled with 2 Crystal Ball functions (tails params. fixed from simulation) and mass difference between  $B^0$  and  $B^0_s$  for  $DK^+K^-$  fixed to PDG2018 value (87.35 MeV/c<sup>2</sup>)
- ✓ Surviving combinatorial background modelled with exponential function
- ✓ Mis-identified and partially reconstructed b-hadron decays modelled from simulation with corrections to match data
- ✓ Specific treatment of  $\Lambda_b \rightarrow D^0 p \pi^-$ ,  $\Lambda_b \rightarrow D^0 p K^-$  and  $\Xi_b \rightarrow D^0 p K^-$  backgrounds constrained from data

Likelihood function:

$$\mathcal{L}_{\bar{D}^0 h^+ h^-} = \frac{v^n}{n!} e^{-v} \prod_{i=1}^n \mathcal{P}_{\theta}^{\text{tot}}(m_{i, \bar{D}^0 h^+ h^-})$$

$v$  is the sum of the yields and  $n$  the number of observed candidates

- $B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$  (7 background components):

$$\mathcal{P}_{\theta}^{\text{tot}}(m_{\bar{D}^0 \pi^+ \pi^-}) = N_{\bar{D}^0 \pi^+ \pi^-} \times \mathcal{P}_{\text{sig}}^{B^0}(m_{\bar{D}^0 \pi^+ \pi^-}) + \sum_{j=1}^7 N_{j, \text{bkg}} \times \mathcal{P}_{j, \text{bkg}}(m_{\bar{D}^0 \pi^+ \pi^-})$$

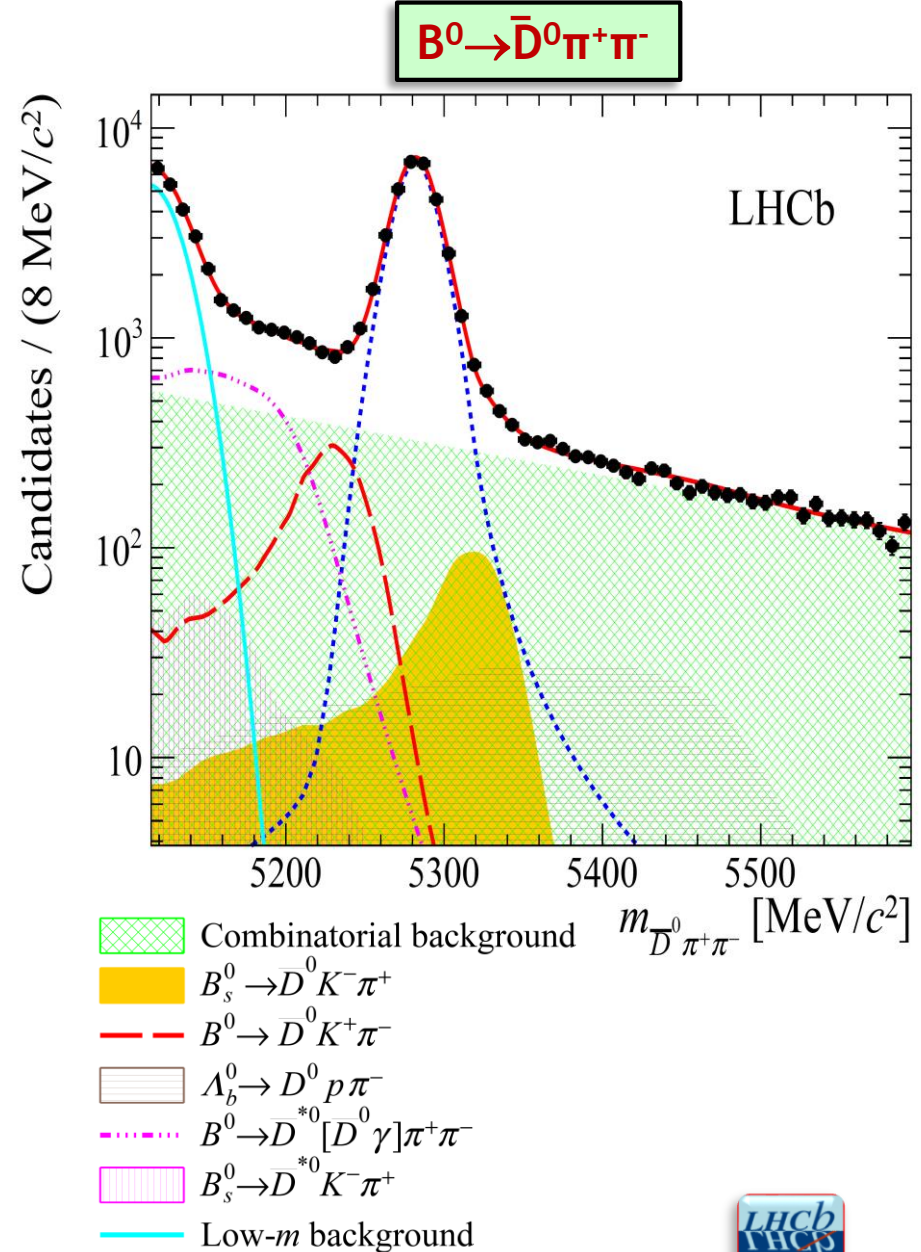
- $B^0_{(s)} \rightarrow \bar{D}^0 K^+ K^-$  (2 signal + 9 background components):

$$\begin{aligned} \mathcal{P}_{\theta}^{\text{tot}}(m_{\bar{D}^0 K^+ K^-}) &= N_{B^0 \rightarrow \bar{D}^0 K^+ K^-} \times \mathcal{P}_{\text{sig}}^{B^0}(m_{\bar{D}^0 K^+ K^-}) \\ &+ N_{B^0_s \rightarrow \bar{D}^0 K^+ K^-} \times \mathcal{P}_{\text{sig}}^{B^0_s}(m_{\bar{D}^0 K^+ K^-}) \\ &+ \sum_{j=1}^9 N_{j, \text{bkg}} \times \mathcal{P}_{j, \text{bkg}}(m_{\bar{D}^0 K^+ K^-}). \end{aligned}$$

invariant mass fit of  $B^0_{(s)} \rightarrow \bar{D}^0 h^+ h^-$  decays

## Fit output details

Parameter	$B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$	$B^0_{(s)} \rightarrow \bar{D}^0 K^+ K^-$
$m_0$ [MeV/ $c^2$ ]	$5282.0 \pm 0.1$	$5282.6 \pm 0.3$
$\sigma_1$ [MeV/ $c^2$ ]	$9.7 \pm 1.0$	fixed at 9.7
$\sigma_2$ [MeV/ $c^2$ ]	$16.2 \pm 0.8$	fixed at 16.2
$f_{CB}$	$0.3 \pm 0.1$	$0.6 \pm 0.1$
$a_{\text{comb.}}$ [ $10^{-3} \times (\text{MeV}/c^2)^{-1}$ ]	$-3.2 \pm 0.1$	$-1.3 \pm 0.4$
$N_{B^0 \rightarrow \bar{D}^0 h^+ h^-}$	$29\,943 \pm 243$	$1918 \pm 74$
$N_{B^0_{(s)} \rightarrow \bar{D}^0 h^+ h^-}$	–	$473 \pm 33$
$N_{\text{comb.}}$	$20\,266 \pm 463$	$1720 \pm 231$
$N_{B^0_{(s)} \rightarrow \bar{D}^0 K^- \pi^+}$	$923 \pm 191$	$151 \pm 47$
$N_{B^0 \rightarrow \bar{D}^0 K^+ \pi^-}$	$2450 \pm 211$	$131 \pm 65$
$N_{\Lambda_b^0 \rightarrow D^0 p K^-}$ (constrained)	–	$197 \pm 44$
$N_{\Xi_b^0 \rightarrow D^0 p K^-}$ (constrained)	–	$57 \pm 20$
$N_{\Lambda_b^0 \rightarrow D^0 p \pi^-}$ (constrained)	$1016 \pm 136$	$74 \pm 32$
$N_{B^0_{(s)} \rightarrow \bar{D}^{*0} K^- \pi^+}$	540 (fixed)	$833 \pm 185$
$N_{B^0_{(s)} \rightarrow \bar{D}^{*0} K^+ K^-}$	–	$775 \pm 100$
$N_{B^0 \rightarrow \bar{D}^{*0} [\bar{D}^0 \gamma] \pi^+ \pi^-}$	$7697 \pm 325$	–
$N_{\text{Low-}m}$	$14\,914 \pm 222$	$1632 \pm 68$
$\chi^2/\text{ndf}$ ( $p$ -value)	52/46 (25%)	43/46 (60%)

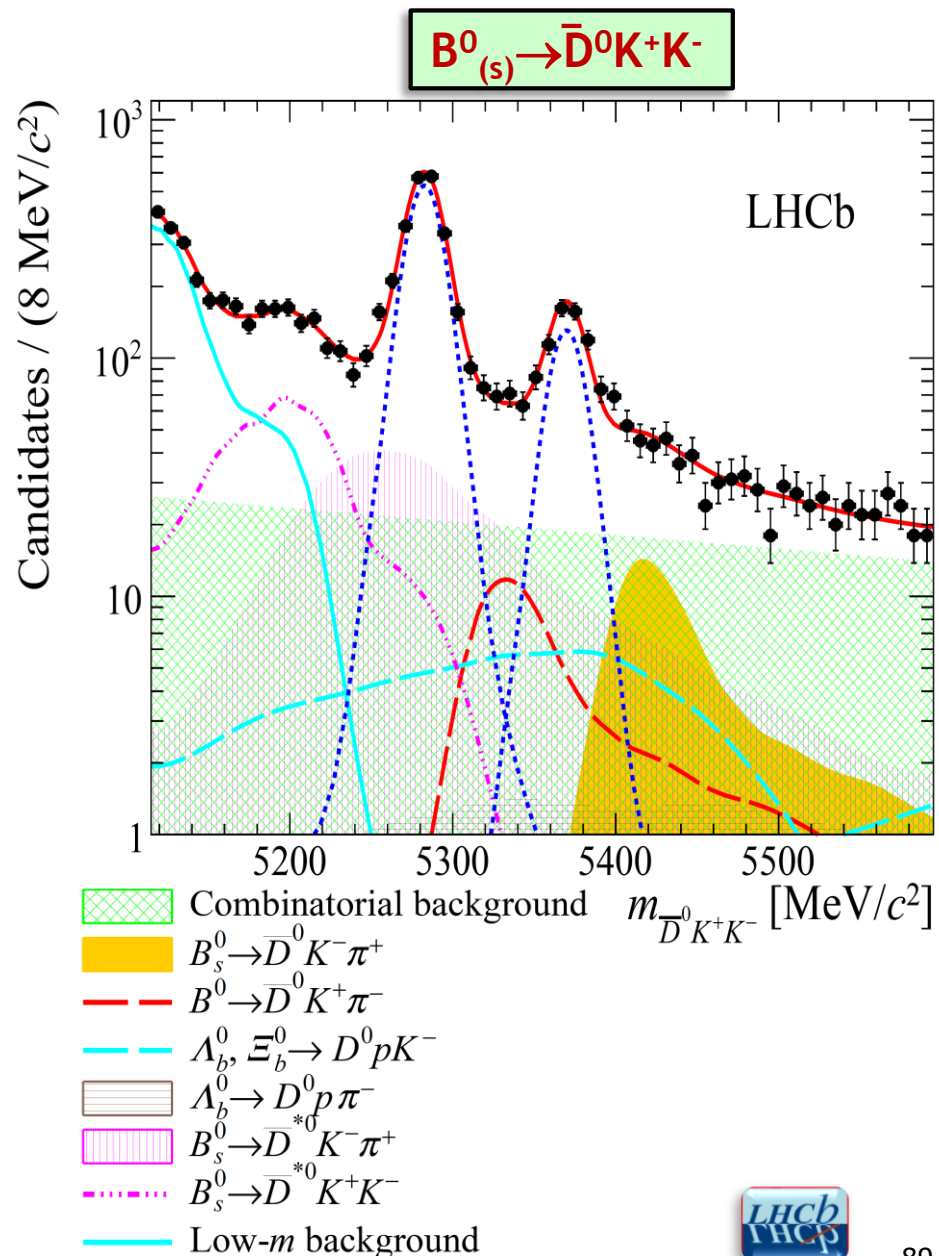




invariant mass fit of  $B^0_{(s)} \rightarrow \bar{D}^0 h^+ h^-$  decays

## Fit output details

Parameter	$B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$	$B^0_{(s)} \rightarrow \bar{D}^0 K^+ K^-$
$m_0$ [MeV/c <sup>2</sup> ]	$5282.0 \pm 0.1$	$5282.6 \pm 0.3$
$\sigma_1$ [MeV/c <sup>2</sup> ]	$9.7 \pm 1.0$	fixed at 9.7
$\sigma_2$ [MeV/c <sup>2</sup> ]	$16.2 \pm 0.8$	fixed at 16.2
$f_{CB}$	$0.3 \pm 0.1$	$0.6 \pm 0.1$
$a_{\text{comb.}}$ [ $10^{-3} \times (\text{MeV}/c^2)^{-1}$ ]	$-3.2 \pm 0.1$	$-1.3 \pm 0.4$
$N_{B^0 \rightarrow \bar{D}^0 h^+ h^-}$	$29\,943 \pm 243$	$1918 \pm 74$
$N_{B^0_s \rightarrow \bar{D}^0 h^+ h^-}$	–	$473 \pm 33$
$N_{\text{comb.}}$	$20\,266 \pm 463$	$1720 \pm 231$
$N_{B^0_s \rightarrow \bar{D}^0 K^- \pi^+}$	$923 \pm 191$	$151 \pm 47$
$N_{B^0 \rightarrow \bar{D}^0 K^+ \pi^-}$	$2450 \pm 211$	$131 \pm 65$
$N_{\Lambda_b^0 \rightarrow D^0 p K^-}$ (constrained)	–	$197 \pm 44$
$N_{\Xi_b^0 \rightarrow D^0 p K^-}$ (constrained)	–	$57 \pm 20$
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$N_{B^0_s \rightarrow \bar{D}^{*0} K^- \pi^+}$	540 (fixed)	$833 \pm 185$
$N_{B^0_s \rightarrow \bar{D}^{*0} K^+ K^-}$	–	$775 \pm 100$
$N_{B^0 \rightarrow \bar{D}^{*0} [\bar{D}^0 \gamma] \pi^+ \pi^-}$	$7697 \pm 325$	–
$N_{\text{Low-}m}$	$14\,914 \pm 222$	$1632 \pm 68$
$\chi^2/\text{ndf}$ ( $p$ -value)	52/46 (25%)	43/46 (60%)



# Ratios of branching fractions & efficiencies

## ✓ Compute ratios of branching fractions:

$$\frac{\mathcal{B}(B^0 \rightarrow \bar{D}^0 K^+ K^-)}{\mathcal{B}(B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-)} = \frac{N_{B^0 \rightarrow \bar{D}^0 K^+ K^-}}{N_{B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-}} \times \frac{\varepsilon_{B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-}}{\varepsilon_{B^0 \rightarrow \bar{D}^0 K^+ K^-}}$$

$$\frac{\mathcal{B}(B_s^0 \rightarrow \bar{D}^0 K^+ K^-)}{\mathcal{B}(B^0 \rightarrow \bar{D}^0 K^+ K^-)} = r_{B_s^0/B^0} \times \frac{\varepsilon_{B^0 \rightarrow \bar{D}^0 K^+ K^-}}{\varepsilon_{B_s^0 \rightarrow \bar{D}^0 K^+ K^-}} \times \frac{1}{f_s/f_d}$$

✓  $\mathcal{B}(B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-)$  from PDG2018 (including Phys. Rev. D 92 (2015) 032002)

✓  $f_s/f_d$  from LHCb (JHEP 04 (2003) 001 & LHCb-CONF-2013-011)

✓ **Efficiencies** account for acceptance/reconstruction, hardware L0 /software HLT1/2 triggering, PID and selections (including Fisher discriminant).

- Mostly computed with simulation, but PID/tracking simulation corrected with data control samples.
- Hardware L0 trigger part determined from calibration data samples.
- Global efficiency corrected for phase-space effects in  $B^0_{(s)} \rightarrow \bar{D}^0 h^+ h^-$  multi-body decays on event-by-event basis using sPlot technique (i.e. sWeights).

# Systematic uncertainties

- ✓ Many sources of systematic uncertainty cancel in the ratios of branching fractions
- ✓ Other non-vanishing sources:
  - Hardware L0 trigger (signal specific part).
  - PID difference in the  $h^+h^-$  selection for  $B^0_{(s)} \rightarrow \bar{D}^0 K^+ K^-$  signal and  $B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$  normalisation mode.
  - Signal and background modelling in the invariant mass fit.

Source [%]	$\mathcal{R}_{\bar{D}^0 K^+ K^- / \bar{D}^0 \pi^+ \pi^-}$	$\mathcal{R}_{B_s^0 / B^0}$
HW trigger efficiency	2.0	—
PID efficiency	2.0	—
PDF modelling	3.2	4.5
$f_s / f_d$	—	5.8
Total [%]	4.3	7.3

Where:

$$\mathcal{R}_{\bar{D}^0 K^+ K^- / \bar{D}^0 \pi^+ \pi^-} \equiv \mathcal{B}(B^0 \rightarrow \bar{D}^0 K^+ K^-) / \mathcal{B}(B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-)$$

$$\mathcal{R}_{B_s^0 / B^0} \equiv \mathcal{B}(B_s^0 \rightarrow \bar{D}^0 K^+ K^-) / \mathcal{B}(B^0 \rightarrow \bar{D}^0 K^+ K^-)$$

# Results 3/fb

$$\frac{\mathcal{B}(B^0 \rightarrow \bar{D}^0 K^+ K^-)}{\mathcal{B}(B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-)} = (6.9 \pm 0.4 \pm 0.3)\%$$

stat.      syst.

$$\mathcal{B}(B^0 \rightarrow \bar{D}^0 K^+ K^-) = (6.1 \pm 0.4 \pm 0.3 \pm 0.3) \times 10^{-5}$$

stat.      syst.      normalis.

(was  $(4.7 \pm 0.9 \pm 0.6 \pm 0.5) \times 10^{-5}$  with 0.6/fb \*)

$$\frac{\mathcal{B}(B_s^0 \rightarrow \bar{D}^0 K^+ K^-)}{\mathcal{B}(B^0 \rightarrow \bar{D}^0 K^+ K^-)} = (93.0 \pm 8.9 \pm 6.9)\%$$

stat.      syst.

$$\mathcal{B}(B_s^0 \rightarrow \bar{D}^0 K^+ K^-) = (5.7 \pm 0.5 \pm 0.4 \pm 0.5) \times 10^{-5}$$

stat.      syst.      normalis.

**Observed !**

(was  $(4.2 \pm 1.3 \pm 0.9 \pm 1.1) \times 10^{-5}$  with 0.6/fb \*)

# Branching fractions of $B^0_{(s)} \rightarrow \bar{D}^{(*)0} \phi$

$$\frac{\mathcal{B}(B^0_{(s)} \rightarrow \bar{D}^{(*)0} \phi)}{\mathcal{B}(B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-)} = \frac{N_{B^0_{(s)} \rightarrow \bar{D}^{(*)0} \phi} \times \varepsilon(B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-)}{N_{B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-} \times \varepsilon(B^0_{(s)} \rightarrow \bar{D}^{(*)0} \phi)} \times \frac{\mathcal{F}}{\mathcal{B}(\phi \rightarrow K^+ K^-)},$$

where  $\mathcal{F}$  is 1 for  $B^0$  decays and  $f_d/f_s$  for  $B^0_s$  decays.

- ✓ **Efficiencies** computed as for 1807.01891.
- ✓ Various sources of **systematic uncertainties** considered [%]:

Source	$\frac{\mathcal{B}(B^0_s \rightarrow \bar{D}^0 \phi)}{\mathcal{B}(B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-)}$	$\frac{\mathcal{B}(B^0 \rightarrow \bar{D}^0 \phi)}{\mathcal{B}(B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-)}$	$\frac{\mathcal{B}(B^0_s \rightarrow \bar{D}^{*0} \phi)}{\mathcal{B}(B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-)}$	$\frac{\mathcal{B}(B^0_s \rightarrow \bar{D}^{*0} \phi)}{\mathcal{B}(B^0_s \rightarrow \bar{D}^0 \phi)}$	$f_L$
$N_{B^0_{(s)} \rightarrow \bar{D}^{(*)0} \phi}$	1.5	27.0	4.8	4.9	4.1
$N_{B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-}$	2.0	2.0	2.0	—	—
$\epsilon_{\text{PID}}$	2.0	2.0	2.0	—	—
$\epsilon_{\text{trigger}}$	2.0	2.0	2.0	—	—
$\mathcal{B}(\phi \rightarrow K^+ K^-)^*$	1.0	1.0	1.0	—	—
$f_s/f_d^{**}$	5.8	—	5.8	—	—
Lifetime <sup>***</sup>	0.8	—	0.8	1.6	1.6
Total	7.0	27.1	8.4	5.2	4.4

\* PDG2018

\*\* JHEP 04 (2003) 001 &amp; LHCb-CONF-2013-011

\*\*\* See: Phys. Rev. D 86 (2012) 014027

# Results for Branching fractions of $B_s^0 \rightarrow \bar{D}^{(*)0} \phi$

$$\frac{\mathcal{B}(B_s^0 \rightarrow \bar{D}^0 \phi)}{\mathcal{B}(B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-)} = (3.4 \pm 0.4 \pm 0.2)\% \begin{matrix} \text{stat.} \\ \text{syst.} \end{matrix}$$

$$\mathcal{B}(B_s^0 \rightarrow \bar{D}^0 \phi) = (3.0 \pm 0.3 \pm 0.2 \pm 0.2) \times 10^{-5} \begin{matrix} \text{stat.} \\ \text{syst.} \\ \text{normalis.} \end{matrix}$$

Compatible and twice as accurate as Phys. Lett. B727 (2013) 403

$$\frac{\mathcal{B}(B_s^0 \rightarrow \bar{D}^{*0} \phi)}{\mathcal{B}(B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-)} = (4.2 \pm 0.5 \pm 0.4)\% \begin{matrix} \text{stat.} \\ \text{syst.} \end{matrix}$$

Observation with more than 7 standard deviations !

$$\mathcal{B}(B_s^0 \rightarrow \bar{D}^{*0} \phi) = (3.7 \pm 0.5 \pm 0.3 \pm 0.2) \times 10^{-5} \begin{matrix} \text{stat.} \\ \text{syst.} \\ \text{normalis.} \end{matrix}$$

$$\frac{\mathcal{B}(B_s^0 \rightarrow \bar{D}^{*0} \phi)}{\mathcal{B}(B_s^0 \rightarrow \bar{D}^0 \phi)} = 1.23 \pm 0.20 \pm 0.06 \begin{matrix} \text{stat.} \\ \text{syst.} \end{matrix}$$

Fraction of longitudinal polarisation:

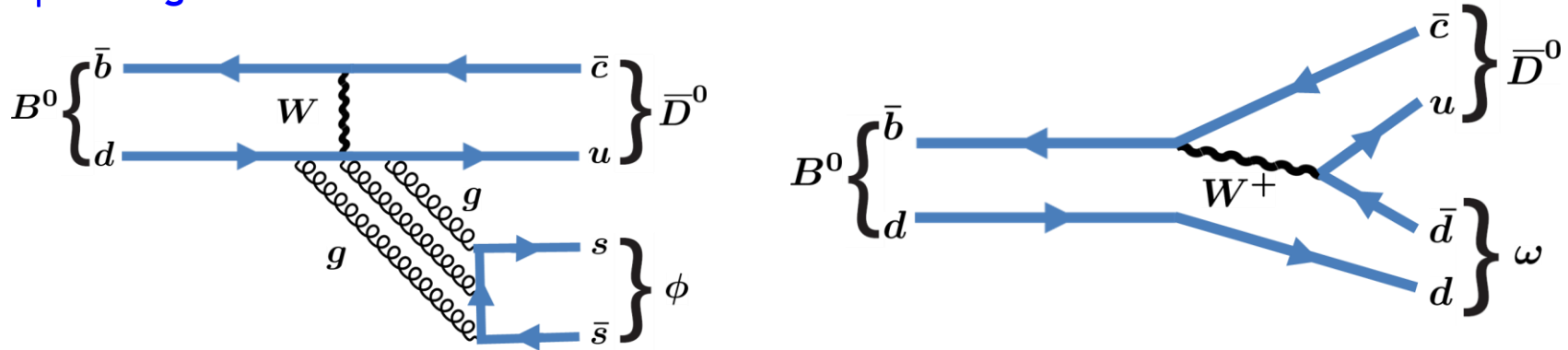
$$f_L = (73 \pm 15 \pm 3)\% \begin{matrix} \text{stat.} \\ \text{syst.} \end{matrix}$$

- ✓  $f_L < 90\%$ , compatible with colour-suppressed VV open charm  $B^0$ -decays (e.g. BaBar: Phys. Rev D 84 (2011) 112007 or Belle: Phys. Rev. D 92 (2015) 012013 )
- ✓ About the same number of fully longitudinally polarised  $B_s \rightarrow D^* \phi$  wrt  $B_s \rightarrow D \phi$  :  $1.23 \times 0.73 = 0.9$   
 → Yet another mode for CKM angle  $\gamma$  !



# Search for the $B^0 \rightarrow \bar{D}^0 \phi$ decay

→ Occurs through **W-exchange diagram + Okubo-Zweig-Iizuka (OZI) suppression** or through  **$\omega$ - $\phi$  mixing**



→ Yet **non-significant  $B^0 \rightarrow \bar{D}^0 \phi$  signal** ( $\sim 2\sigma$ ), interpreted as:

$$\frac{\mathcal{B}(B^0 \rightarrow \bar{D}^0 \phi)}{\mathcal{B}(B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-)} = (1.2 \pm 0.7 \pm 0.3) \times 10^{-3}$$

stat.    syst.

$$\mathcal{B}(B^0 \rightarrow \bar{D}^0 \phi) = (1.1 \pm 0.6 \pm 0.3 \pm 0.1) \times 10^{-6}$$

stat.    syst.    normalis.

Adapted prediction from Phys. Lett. B 666 (2008) 185 + BaBar  
Phys. Rev. D 84 (2011) 112007:  $(1.6 \pm 0.1) \times 10^{-6}$

→ **Upper limits** set on **both branching fraction and mixing angle** (i.e. ideally mixed states\*)  
assuming that the contribution from  $\omega$ - $\phi$  mixing dominates (@ 90% (95%) of CL):

$$\mathcal{B}(B^0 \rightarrow \bar{D}^0 \phi) < 2.0 \text{ (2.2)} \times 10^{-6} \quad \Rightarrow \quad |\delta| < 5.2^\circ \text{ (5.5}^\circ)$$

**Factor 6 better improvement** wrt BaBar

(Phys. Rev. D76 (2007) 051103)

$$* \quad \omega^I \equiv (u\bar{u} + d\bar{d})/\sqrt{2} \text{ and } \phi^I \equiv s\bar{s} \quad \begin{pmatrix} \omega \\ \phi \end{pmatrix} = \begin{pmatrix} \cos \delta & \sin \delta \\ -\sin \delta & \cos \delta \end{pmatrix} \begin{pmatrix} \omega^I \\ \phi^I \end{pmatrix}$$