

Study of $e^+e^- \rightarrow \phi\eta'$

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- ② Data sample and software version
- ③ Event selection
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- ⑤ Systematic uncertainties
- ⑥ Upper limit for $e^+e^- \rightarrow Y(4260) \rightarrow \phi\eta'$
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Motivation

- Several hadronic transitions about $\Upsilon(4260)$ states have been found in these experiments, such as:
 $\pi^+\pi^-J/\psi^1$, K^+K^-J/ψ^2 and $\pi^+\pi^-\psi(2S)^3$, but no light hadron decay modes have been found.
- Different interpretations were proposed to explain $\Upsilon(4260)$ structure, the natures of the $\Upsilon(4260)$ are still unclear.
- Utilize the newest data, we search for $e^+e^- \rightarrow \phi\eta'$ to study the line-shape with improved precision then better understanding of the structure, and check the energy dependence feature of $\Upsilon(4260)$ particles.

¹[Phys.Rev.Lett.95.142001](#)

²[PhysRevD.77.011105](#)

³[PhysRevLett.99.142002](#)

Data sample and software version

- Boss version: 7.0.3
- Exclusive MC: 10K for each energy point
- Inclusive MC: with the same integrated luminosity as data at 4.23 GeV.
- Data Sets
 - The search of $e^+e^- \rightarrow \phi\eta'$ based on data samples collected with the BESIII detector at center-of-mass energy $\sqrt{s} > 4$ GeV.

Data Sets	\sqrt{s} (GeV)	Luminosity(pb^{-1})
1	4.009	481.96
2	4.180	3194.50
3	4.190	522.50
4	4.200	524.60
5	4.210	518.10
6	4.220	514.30
7	4.230	1047.34
8	4.237	530.60
9	4.246	537.40
10	4.260	825.67
11	4.270	529.70
12	4.280	175.50
13	4.360	539.84
14	4.420	1028.89
15	4.600	566.93

- Decay chain

- $e^+e^- \rightarrow \phi\eta'$ VVS_PWAVE
- $\phi \rightarrow K^+K^-$ VSS
- $\eta' \rightarrow \eta\pi^+\pi^-$ PHSP
- $\eta \rightarrow \gamma\gamma$ PHSP
- $\eta' \rightarrow \gamma\pi^+\pi^-$ PHSP

Selections

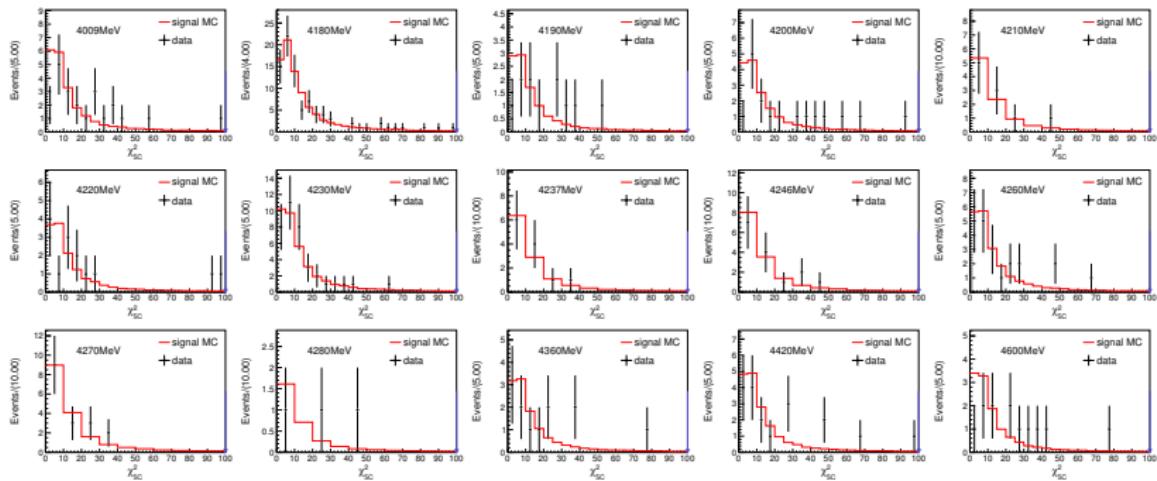
- Charged track selection
 - $|\cos \theta| < 0.93$, $|R_z| < 10.0$ cm, $|R_{xy}| < 1.0$ cm
 - $N_{charged} = 4$
- Particle identification
 - pion, $\text{prob}(\pi) > \text{prob}(K)$, $\text{prob}(\pi) > 0$
 - kaon, $\text{prob}(K) > \text{prob}(\pi)$, $\text{prob}(K) > 0$
- Good photon selection
 - $0 \leq t_{TDC} \leq 14$ ($\times 50$ ns)
 - photon from barrel ($|\cos \theta| < 0.8$) : $E > 0.025$ GeV
 - photon from endcap ($0.86 < |\cos \theta| < 0.92$): $E > 0.05$ GeV
 - angle between any charged track is greater than 10°
 - $N_\gamma \geq 2$
- η reconstruction:
 - mass window: $0.40 \leq M_{\gamma\gamma} \leq 0.67$ GeV/c²
 - mass constraint kinematic fit with $\chi^2 < 100$
- 5C kinematic fit
 - choose the photons with least χ^2
 - $M(\gamma\gamma)$ is constrained to M_η
 - $\chi^2_{5C} < 100$

Event selection

$$e^+ e^- \rightarrow \phi\eta', \eta' \rightarrow \eta\pi^+\pi^-, \eta \rightarrow \gamma\gamma$$

Event selection

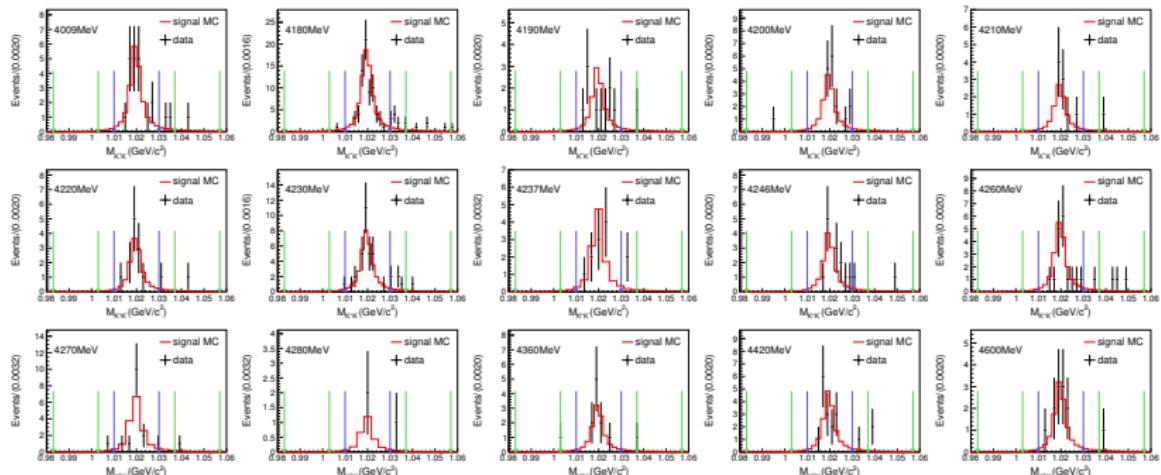
χ^2_{5C} distribution



- $\chi^2_{5C} < 100$

Event selection

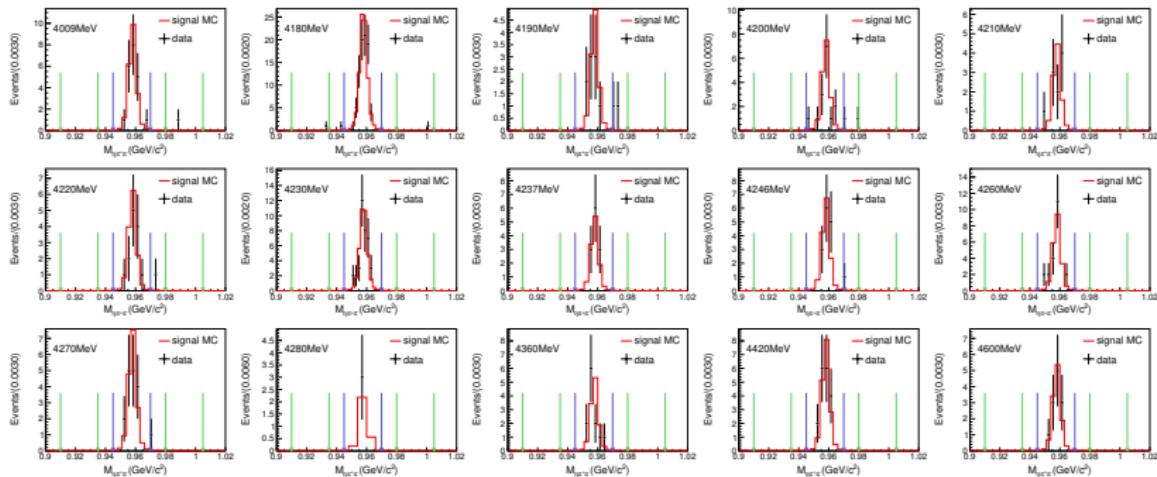
the distribution of invariant mass of ϕ



- signal region: $M_{K^+K^-} \in (1.010, 1.030) \text{ GeV}/c^2$
- sideband: $M_{K^+K^-} \in (0.983, 1.003) \cup (1.037, 1.057) \text{ GeV}/c^2$

Event selection

the distribution of invariant mass of η'



- signal region: $M_{\eta\pi^+\pi^-} \in (0.945, 0.970) \text{ GeV}/c^2$
- sideband: $M_{\eta\pi^+\pi^-} \in (0.910, 0.935) \cup (0.980, 1.005) \text{ GeV}/c^2$

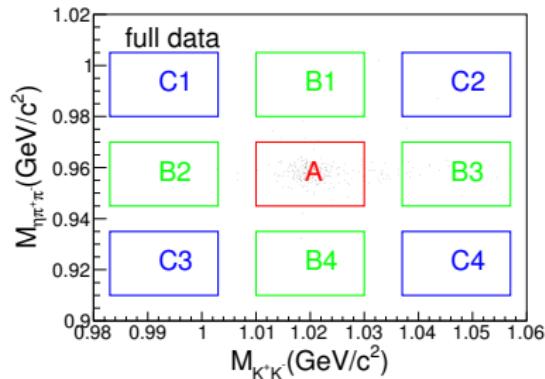
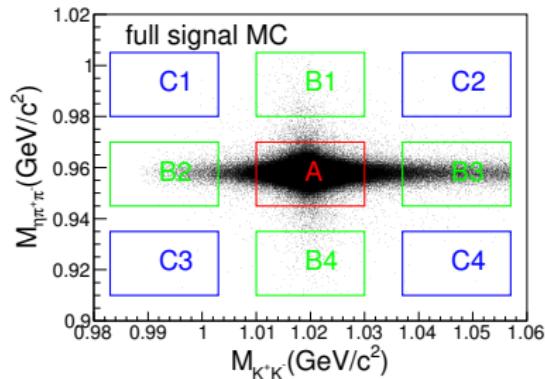
Background check from Inclusive MC

- Signal observable is defined as the invariant mass of ϕ and η' , which all in their signal region
- No peak background exist in signal region
- After all selections, there is no events in Inclusive MC

cut: $M_\phi \in (0.983, 1.057) \text{ GeV}/c^2 \cap M_{\eta'} \in (0.910, 1.005) \text{ GeV}/c^2 \cap \chi^2_{5C} < 100$

Event selection

2D scatter



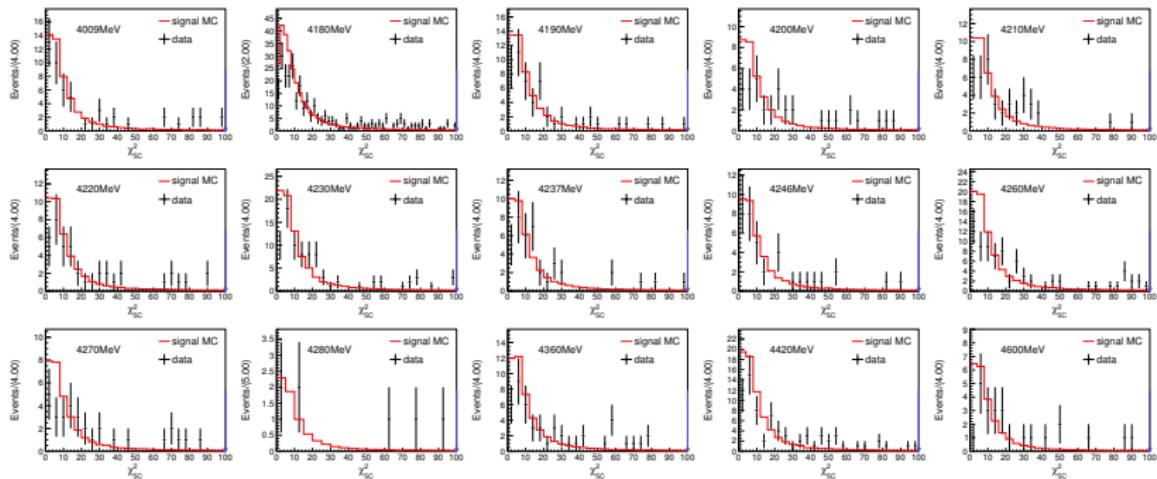
- A: $\phi \eta' + \phi \text{ non-}\eta' + \text{non-}\phi \eta' + \text{non-}\phi \text{ non-}\eta'$
- B_1, B_4 : $\phi \text{ non-}\eta' + \text{non-}\phi \text{ non-}\eta'$
- B_2, B_3 : $\text{non-}\phi \eta' + \text{non-}\phi \text{ non-}\eta'$
- C_1, C_2, C_3, C_4 : $\text{non-}\phi \text{ non-}\eta'$

$$N^{sig} = N_A - 0.5N_B + 0.25N_C$$

$$e^+ e^- \rightarrow \phi\eta', \eta' \rightarrow \gamma\pi^+\pi^-$$

Event selection

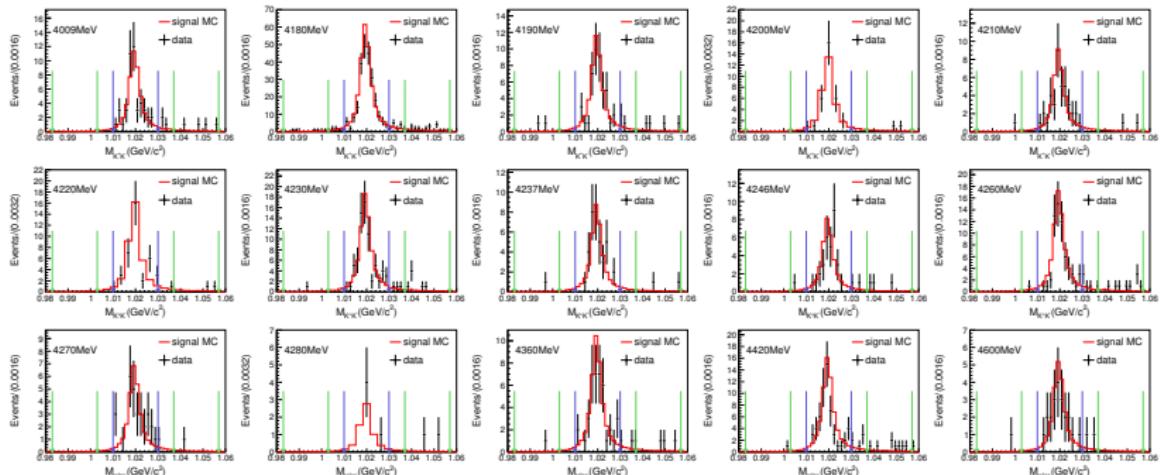
χ^2_{5C} distribution



- $\chi^2_{5C} < 100$

Event selection

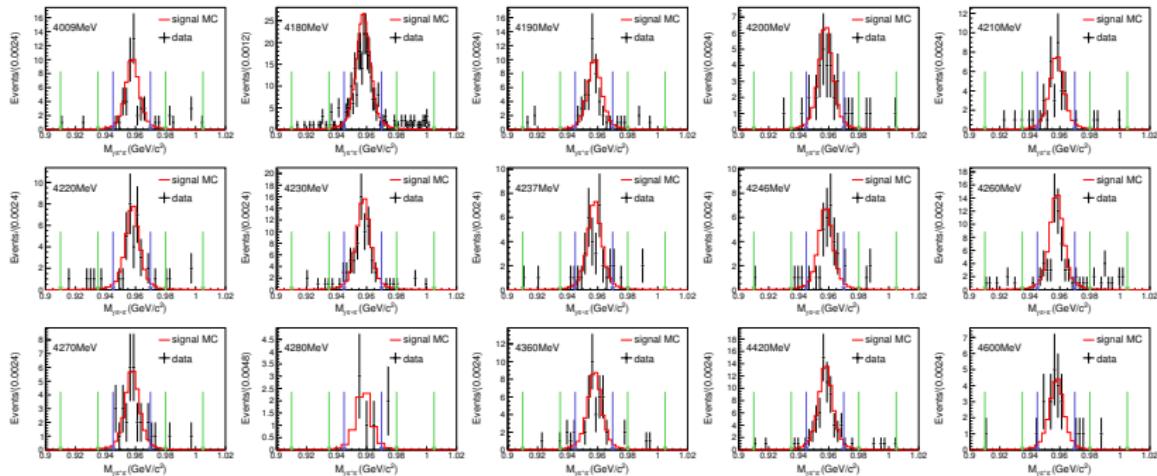
the distribution of invariant mass of ϕ



- signal region: $M_{K^+K^-} \in (1.010, 1.030) \text{ GeV}/c^2$
- sideband: $M_{K^+K^-} \in (0.983, 1.003) \cup (1.037, 1.057) \text{ GeV}/c^2$

Event selection

the distribution of invariant mass of η'



- signal region: $M_{\gamma\pi^+\pi^-} \in (0.945, 0.970) \text{ GeV}/c^2$
- sideband: $M_{\gamma\pi^+\pi^-} \in (0.910, 0.935) \cup (0.980, 1.005) \text{ GeV}/c^2$

Background check from Inclusive MC

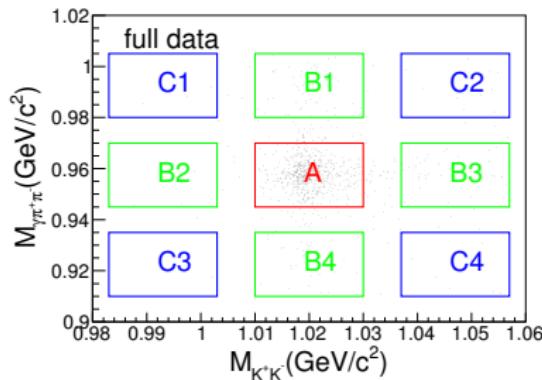
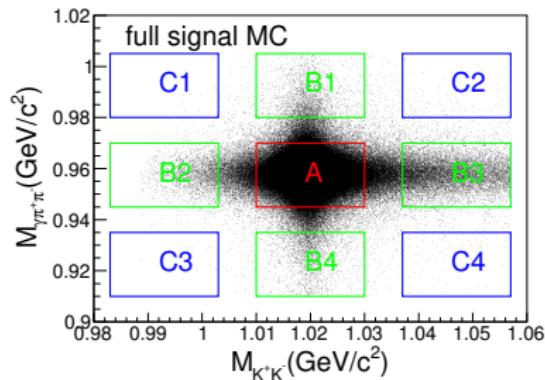
No.	Decay Chain	Final States	Event Number
0	$e^+e^- \rightarrow \eta' K^+ K^-, \eta' \rightarrow \rho^0 \gamma, \rho^0 \rightarrow \pi^+ \pi^-$	$K^- \pi^- \gamma \pi^+ K^+$	1
1	$e^+e^- \rightarrow \eta' K^+ K^-, \eta' \rightarrow \rho^0 \gamma, \rho^0 \rightarrow \pi^+ \pi^-$	$K^- \pi^- \gamma \pi^+ K^+$	1
2	$e^+e^- \rightarrow \eta' K^+ K^-, \eta' \rightarrow \rho^0 \gamma, \rho^0 \rightarrow \pi^+ \pi^-$	$K^- \pi^- \gamma \pi^+ K^+$	1
3	$e^+e^- \rightarrow K^+ \rho^0 \pi^0 K^-, \rho^0 \rightarrow \pi^+ \pi^-, \pi^0 \rightarrow \gamma\gamma$	$K^- \pi^- \gamma \gamma \pi^+ K^+$	1
4	$e^+e^- \rightarrow K^+ \pi^+ \pi^0 \pi^- K^-, \pi^0 \rightarrow \gamma\gamma$	$K^- \pi^- \gamma \gamma \pi^+ K^+$	1
5	$e^+e^- \rightarrow K^+ \pi^+ \rho^- K^-, \rho^- \rightarrow \pi^0 \pi^-, \pi^0 \rightarrow \gamma\gamma$	$K^- \pi^- \gamma \gamma \pi^+ K^+$	1
6	$e^+e^- \rightarrow K^{*0} \pi^+ \pi^0 K^-, K^{*0} \rightarrow K^+ \pi^-, \pi^0 \rightarrow \gamma\gamma$	$K^- \pi^- \gamma \gamma \pi^+ K^+$	1
7	$e^+e^- \rightarrow K^+ \pi^+ \rho^- K^-, \rho^- \rightarrow \pi^0 \pi^-, \pi^0 \rightarrow \gamma\gamma$	$K^- \pi^- \gamma \gamma \pi^+ K^+$	1

- Signal observable is defined as the invariant mass of ϕ and η' , which all in their signal region
- No peak background in signal region
- After all selections, the background level is very low

cut: $M_\phi \in (0.983, 1.057) \text{ GeV}/c^2 \cap M_{\eta'} \in (0.910, 1.005) \text{ GeV}/c^2 \cap \chi^2_{5C} < 100$

Event selection

2D scatter



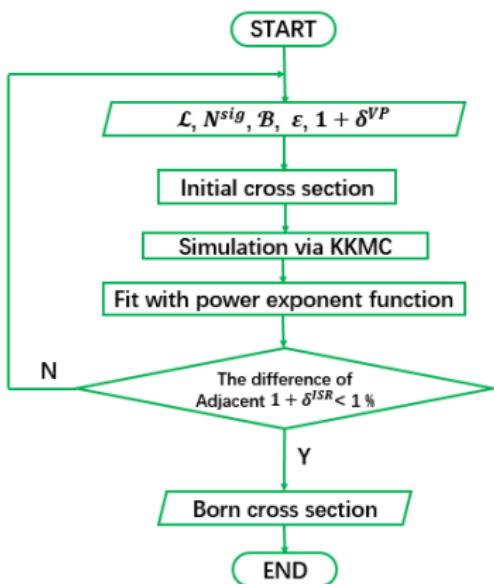
- A: $\phi\eta' + \phi$ non- η' + non- ϕ $\eta' +$ non- ϕ non- η'
- B_1, B_4 : ϕ non- η' + non- ϕ non- η'
- B_2, B_3 : non- ϕ $\eta' +$ non- ϕ non- η'
- C_1, C_2, C_3, C_4 : non- ϕ non- η'

$$N^{sig} = N_A - 0.5N_B + 0.25N_C$$

Cross section of $e^+e^- \rightarrow \phi\eta'$

$$\sigma_B(e^+e^- \rightarrow \phi\eta') =$$

$$\frac{N_1^{sig} + N_2^{sig}}{L_{int} \cdot (1 + \delta^{ISR}) \cdot (1 + \delta^{VP}) \cdot B(\phi \rightarrow K^+K^-) \cdot [B(\eta' \rightarrow \eta\pi^+\pi^-) \cdot B(\eta \rightarrow \gamma\gamma) \cdot \epsilon_1 + B(\eta' \rightarrow \gamma\pi^+\pi^-) \cdot \epsilon_2]} *$$



- N_1^{sig}, N_2^{sig} : obtained from data scatter plot counting
- L_{int} : determined from Bhabha events
- ϵ_1, ϵ_2 : obtained from exclusive MC scatter plot counting
- $B(\phi \rightarrow K^+K^-)$: 48.9% (PDG)
- $B(\eta' \rightarrow \eta\pi^+\pi^-)$: 42.6% (PDG)
- $B(\eta' \rightarrow \gamma\pi^+\pi^-)$: 28.9% (PDG)
- $B(\eta \rightarrow \gamma\gamma)$: 39.41% (PDG)
- $1 + \delta^{VP}$: based on Fred Jegerlehner's alphaQED
- $1 + \delta^{ISR}$: obtained from cross section iteration via KKMC

* Values with subscripts 1 and 2 are corresponding value for $\eta' \rightarrow \eta\pi^+\pi^-$ and $\eta' \rightarrow \gamma\pi^+\pi^-$ respectively

Cross section of $e^+e^- \rightarrow \phi\eta'$

\sqrt{s} (GeV)	ϵ_1 (%)	ϵ_2 (%)	N_1^{signal}	N_2^{signal}	$1 + \delta^{ISR}$	$1 + \delta^{VP}$	σ_B (pb)
4.009	17.67	20.58	19.3 ± 4.4	32.0 ± 6.2	0.901	1.0441	$2.59 \pm 0.53 \pm 0.17$
4.180	16.38	19.03	66.5 ± 8.5	168.3 ± 14.2	0.951	1.0545	$1.82 \pm 0.17 \pm 0.12$
4.190	16.12	19.01	9.0 ± 3.0	35.0 ± 6.3	0.955	1.0562	$2.08 \pm 0.44 \pm 0.14$
4.200	16.37	18.97	13.5 ± 3.8	25.5 ± 5.2	0.955	1.0570	$1.83 \pm 0.42 \pm 0.12$
4.210	15.91	18.47	8.5 ± 3.0	28.3 ± 5.7	0.956	1.0569	$1.79 \pm 0.43 \pm 0.12$
4.220	15.97	18.61	10.5 ± 3.4	25.3 ± 5.6	0.958	1.0566	$1.74 \pm 0.43 \pm 0.11$
4.230	16.22	18.96	32.5 ± 5.8	48.8 ± 7.7	0.961	1.0566	$1.90 \pm 0.32 \pm 0.12$
4.237	16.07	18.79	10.0 ± 3.2	25.8 ± 5.4	0.958	1.0557	$1.68 \pm 0.40 \pm 0.11$
4.246	16.08	18.74	12.5 ± 3.6	26.5 ± 5.3	0.960	1.0558	$1.80 \pm 0.41 \pm 0.12$
4.260	16.21	19.01	15.5 ± 4.2	41.5 ± 7.1	0.967	1.0537	$1.69 \pm 0.34 \pm 0.11$
4.270	16.10	18.34	13.5 ± 3.8	23.5 ± 5.1	0.969	1.0534	$1.75 \pm 0.42 \pm 0.11$
4.280	15.75	18.04	2.0 ± 1.4	2.0 ± 1.9	0.972	1.0532	$0.58 \pm 0.48 \pm 0.04$
4.360	15.44	18.25	9.5 ± 3.2	29.0 ± 5.8	0.987	1.0514	$1.79 \pm 0.42 \pm 0.12$
4.420	15.26	17.93	14.0 ± 3.9	47.0 ± 7.4	0.992	1.0527	$1.50 \pm 0.28 \pm 0.10$
4.600	14.53	16.73	10.5 ± 3.4	13.5 ± 4.0	1.026	1.0549	$1.10 \pm 0.34 \pm 0.07$

Systematic uncertainties (I)

- Luminosity(BAM-157 and BAM-218)
 - 1% for luminosity
 - we consider these values to be uncorrelated between the energies
- Tracking efficiency¹²
 - 1% for every charged track reconstructed → 4%
- PID¹²
 - 1% for every charged track PID → 4%
- Photon efficiency³
 - 1% for per photon reconstructed

¹https://docbes3.ihep.ac.cn/charmoniumgroup/images/8/89/PID_for_kaon.pdf

²https://docbes3.ihep.ac.cn/charmoniumgroup/images/c/ce/Liujie_track_and_pid_efficiency.pdf

³BESIII Collaboration, M. Ablikim et al., Phys. Rev. D81 (2010) 052005

Systematic uncertainties (II)

- η reconstruction³
 - 1% for the reconstruction of η from the two photons mode \rightarrow 1%
- Kinematic fit
 - To correct the track helix parameters to check the difference between data and MC, we take the difference before and after this correction as systematic uncertainties
- ISR
 - As we use recursion method to get the value of ISR factor, and the finish condition of the recursion is that the changes of the Born cross section is smaller than 1.0% between two recursions, 1.0% is taken as the systematical uncertainty from the evaluation of ISR factor

³BESIII Collaboration, M. Ablikim et al., Phys. Rev. D81 (2010) 052005

Systematic uncertainties (III)

- VP factor
 - The uncertainty of the $(1 + \delta^{VP})$ is smaller than 0.1% and can be ignored
- Mass window selection
 - Varying signal mass window of ϕ , η' and sideband mass window, the difference between before and after this change is taken as systematic uncertainty

Summary of systematic uncertainties

- Since the main uncertainties comes from the statistical uncertainty, we assign **identical error for all energy points** about the corresponding item of systematic uncertainties, i.e., the largest data sample at 4.180 GeV. The total systematic uncertainty is the sum of them in quadrature.

sources	Relative error(%)	
	$\eta' \rightarrow \eta\pi^+\pi^-$	$\eta' \rightarrow \gamma\pi^+\pi^-$
Luminosity(pb^{-1})	1.0	1.0
Tracking	4.0	4.0
PID	4.0	4.0
Photon	2.0	1.0
Kinematic fit	0.7	1.8
ISR factor	1.0	1.0
η reconstruction	1.0	-
Mass window of ϕ	0.3	0.3
Mass window of η'	0.6	0.7
Sideband	0.5	0.7
$B_r(\phi \rightarrow K^+K^-)$	1.0	1.0
$B_r(\eta' \rightarrow \eta\pi^+\pi^-)$	1.6	-
$B_r(\eta' \rightarrow \gamma\pi^+\pi^-)$	-	1.7
$B_r(\eta \rightarrow \gamma\gamma)$	0.5	-
Total	6.6	6.6

Combining systematic uncertainties (I)

- Covariance matrix $V(\mathbf{Y})$: $V(\mathbf{Y}) = S V(\mathbf{X}) S^T$, where

$$S = \begin{pmatrix} \frac{\partial Y_1}{\partial X_1} & \frac{\partial Y_1}{\partial X_2} & \cdots & \frac{\partial Y_1}{\partial X_n} \\ \frac{\partial Y_2}{\partial X_1} & \frac{\partial Y_2}{\partial X_2} & \cdots & \frac{\partial Y_2}{\partial X_n} \\ \vdots & \vdots & & \vdots \\ \frac{\partial Y_m}{\partial X_1} & \frac{\partial Y_m}{\partial X_2} & \cdots & \frac{\partial Y_m}{\partial X_n} \end{pmatrix}$$

- Born cross section $\sigma_B = \frac{N_1^{sig} + N_2^{sig}}{A \cdot (w_1 + w_2)}$
 - A: common coefficient
 - the weight factor of systematic uncertainty: w_1 and w_2
 - $w_1: B(\eta' \rightarrow \eta \pi^+ \pi^-) \cdot B(\eta \rightarrow \gamma \gamma) \cdot \epsilon_1$
 - $w_2: B(\eta' \rightarrow \gamma \pi^+ \pi^-) \cdot \epsilon_2$
- $N_1^{sig} = A \cdot w_1 \cdot \sigma_1^B, N_2^{sig} = A \cdot w_2 \cdot \sigma_2^B$
- the total cross section can be written as: $\frac{w_1 \cdot \sigma_1^B + w_2 \cdot \sigma_2^B}{w_1 + w_2}$

Combining systematic uncertainties (II)

- the i th systematic uncertainties δ_{sum}^i are combined by:

$$(\delta_{sum}^i)^2 = \begin{pmatrix} \frac{w_1}{w_1+w_2} & \frac{w_2}{w_1+w_2} \\ V_{21}^i & V_{22}^i \end{pmatrix} \begin{pmatrix} V_{11}^i & V_{12}^i \\ V_{21}^i & V_{22}^i \end{pmatrix} \begin{pmatrix} \frac{w_1}{w_1+w_2} \\ \frac{w_2}{w_1+w_2} \end{pmatrix} = w_1^2 V_{11}^i + w_2^2 V_{22}^i + 2w_1 w_2 V_{12}^i$$

$$\delta_{sum}^i = \frac{\sqrt{(w_1 \delta_1^i)^2 + (w_2 \delta_2^i)^2 + 2w_1 w_2 \rho_{12}^i \delta_1^i \delta_2^i}}{w_1 + w_2}$$

- $V_{km}^i = \rho_{km}^i \delta_k^i \delta_m^i$
- ρ_{km}^i : the correlation coefficient for the i th item system systematic uncertainties
- δ_k^i or δ_m^i : the k th or m th column raw systematic uncertainty
- For luminosity, tracking, PID, photon, kinematic fit, ISR factor, ϕ mass window, the $\rho_{12}^i = 1$, and the others is 0
- Finally, the combined systematic uncertainty δ_{sum} is :

$$\delta_{sum} = \sqrt{\sum (\delta_{sum}^i)^2}$$

The summary of combined systematic uncertainties

sources	Relative error(%)	Energy dependence
Luminosity(pb^{-1})	1.0	Yes
Tracking	4.0	No
PID	4.0	No
Photon	1.3	No
Kinematic fit	1.4	No
ISR factor	1.0	Yes
η reconstruction	0.3	No
Mass window of ϕ	0.3	No
Mass window of η'	0.5	No
Sideband	0.5	No
$B_r(\phi \rightarrow K^+ K^-)$	1.0	No
$B_r(\eta' \rightarrow \eta \pi^+ \pi^-)$	0.5	No
$B_r(\eta' \rightarrow \gamma \pi^+ \pi^-)$	1.1	No
$B_r(\eta \rightarrow \gamma \gamma)$	0.2	No
Total	6.4	-

Upper limit for $e^+e^- \rightarrow Y(4260) \rightarrow \phi\eta'$ (I)

- the least square method
- likelihood ratio ordering method
- unbiased χ^2 estimator for linear function fit involving correlated data
 - δ_c : the common part of the relative systematical uncertainty of Born cross section
 - δ_i : the individual part of the total uncertainty of Born cross section at each energy point

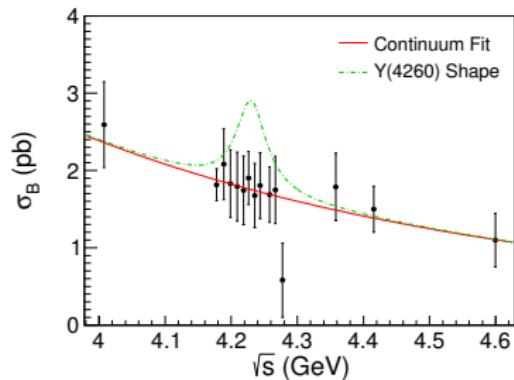
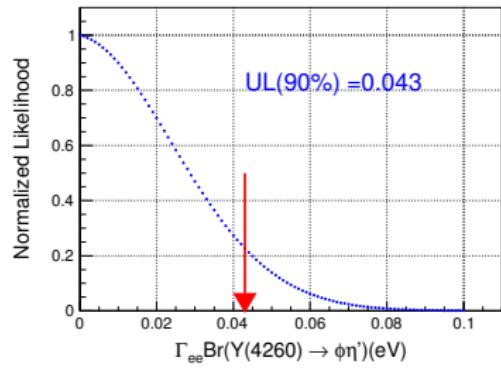
$$Q^2 = \sum_i \frac{(\sigma_{B_i} - h \cdot \sigma_{B_i}^{fit})^2}{\delta_i^2} + \frac{(h - 1)^2}{\delta_c^2}$$

- $L = e^{-0.5Q^2}$
- model of flat continuum and relativistic Breit-Wigner:
 - $\Gamma_{tot}\Gamma_{ee} \times \mathcal{B}(Y(4260) \rightarrow \phi\eta')$ treated as one parameter

$$\sigma_{e^+e^- \rightarrow \phi\eta'}(\sqrt{s}) = c_0 \cdot \sigma_{cont}(\sqrt{s}) + 12\pi \frac{\Gamma_{tot}\Gamma_{ee} \times \mathcal{B}(Y(4260) \rightarrow \phi\eta')}{(s - m_0^2)^2 + m_0^2\Gamma_{tot}^2}$$

- continuum process: $\sigma_{cont}(\sqrt{s}) = \frac{p_0}{\sqrt{s}^{p_1}}$

Upper limit for $e^+e^- \rightarrow Y(4260) \rightarrow \phi\eta'$ (II)



- The largest one from these upper limit results correspond to different $Y(4260)$ mass and width combinations is taken as the final upper limit
- $p_0 = (4.94 \pm 14.70) \times 10^3 (\text{pb})(\text{GeV})^{p_1}$, $p_1 = 5.51 \pm 2.06$
- green dash-dotted lines are the MC shape of the $Y(4260)$ with an arbitrary scale factor

$$\Gamma_{ee} \times \mathcal{B}(Y(4260) \rightarrow \phi\eta') < 0.04 \text{ eV @ 90\% (C.L.)}$$

Summary

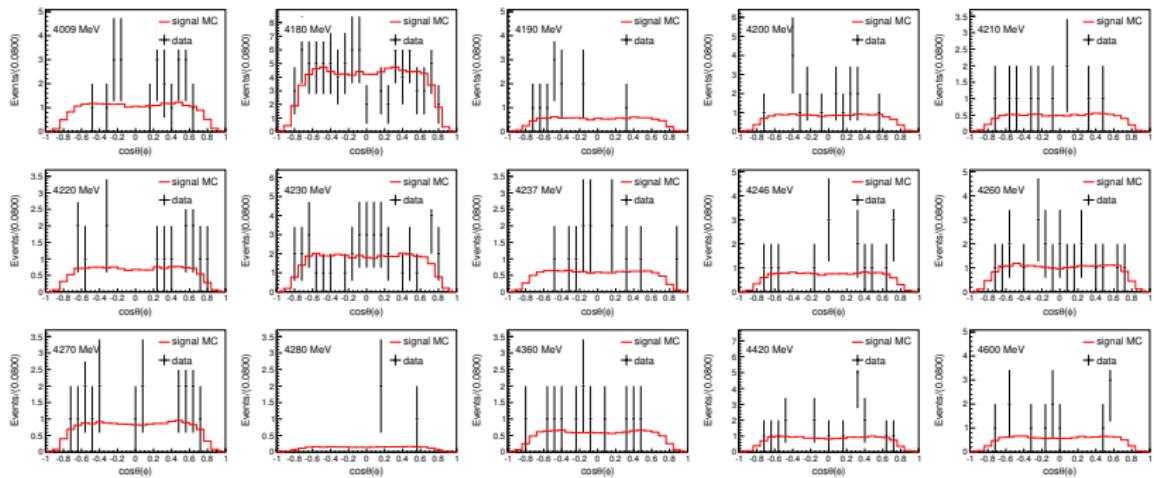
- We measured the cross sections line shape of $e^+e^- \rightarrow \phi\eta'$ in the region of energies above 4.0 GeV;
- An upper limit on $\Gamma_{ee} \times \mathcal{B}(Y(4260) \rightarrow \phi\eta')$ has determined to be 0.04 eV at the 90% confidence level;
- Memo is being revised.

Thanks for your attention!

Backup

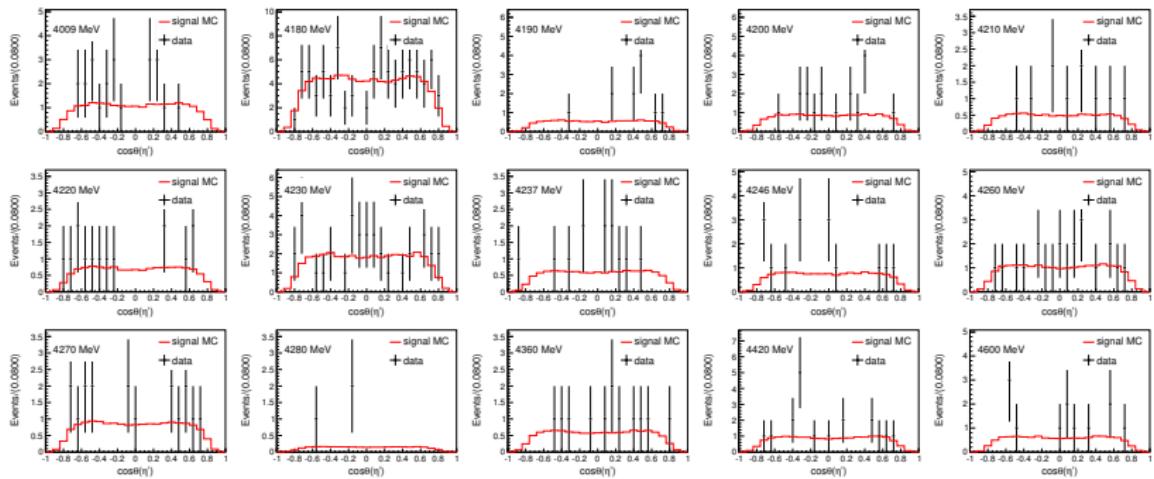
Angular distribution of ϕ

$$\eta' \rightarrow \eta\pi^+\pi^-$$



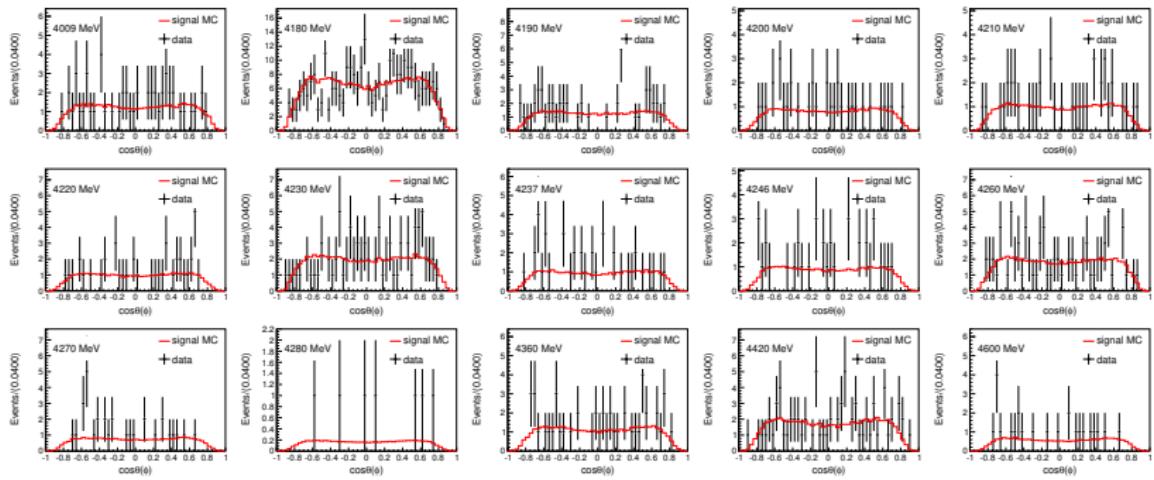
Angular distribution of η'

$$\eta' \rightarrow \eta\pi^+\pi^-$$



Angular distribution of ϕ

$$\eta' \rightarrow \gamma\pi^+\pi^-$$



Angular distribution of η'

$$\eta' \rightarrow \gamma\pi^+\pi^-$$

