



RUB

# Investigation of $h_c$ Decay Patterns at BESIII

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**BESIII Charmonium Group Meeting**

# Brief Introduction

- Studying  $h_c$  via production process  $\psi' \rightarrow \pi^0 h_c$
- Production using XYZ data via  $X \rightarrow \pi^+ \pi^- h_c$  not suitable due to smaller reconstruction efficiency and lower production rate

## Data Sets

**Beam data:**  $448.1 \cdot 10^6$   $\psi'$  events

**inclusive MC:**  $506 \cdot 10^6$  events

**Signal MC:**  $1 \cdot 10^6$  events per final state

**Boss Version:** 664p03

# Final States Analyzed

## 3-body final states

- $h_c \rightarrow K^+K^-\pi^0, K_S^0K^\pm\pi^\mp$

- $h_c \rightarrow K^+K^-\eta$

## 5-body final states

- $h_c \rightarrow K^+K^-\pi^+\pi^-\pi^0, K_S^0K^\pm\pi^\mp\pi^+\pi^-$

- $h_c \rightarrow K^+K^-\pi^+\pi^-\eta$

- $h_c \rightarrow 2(K^+K^-\pi^0)$

## 4-body final states

- $h_c \rightarrow \pi^+\pi^-\pi^0\eta$

- $h_c \rightarrow K^+K^-\pi^0\eta$

- $h_c \rightarrow \bar{p}p\pi^0\pi^0$

Branching fractions have been determined

Upper limits have been determined

# Questions and Remarks within the Last Talk

1. Using different models in order to parameterize the resolution distribution  
➔ additional source of systematic uncertainty
2. Generating Signal MC with HELAMP model instead of PHSP model
3. Investigate background from  $\phi \rightarrow \pi^+\pi^-\pi^0$  in the final state  $h_c \rightarrow K_S^0 K^\pm \pi^\mp \pi^+ \pi^-$

# 1. Using different models in order to parameterize the resolution distribution

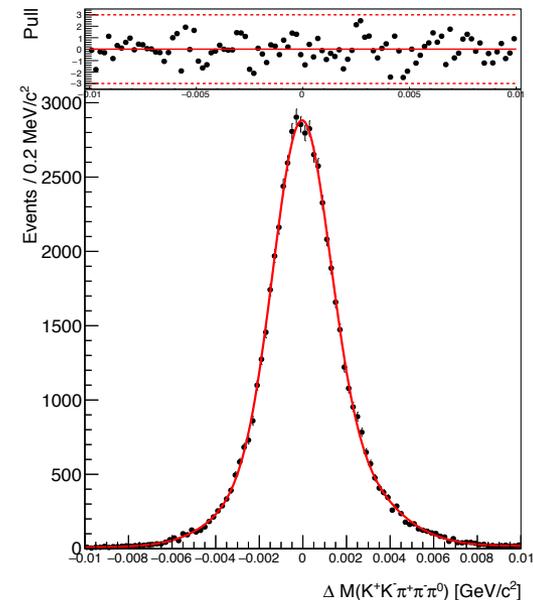
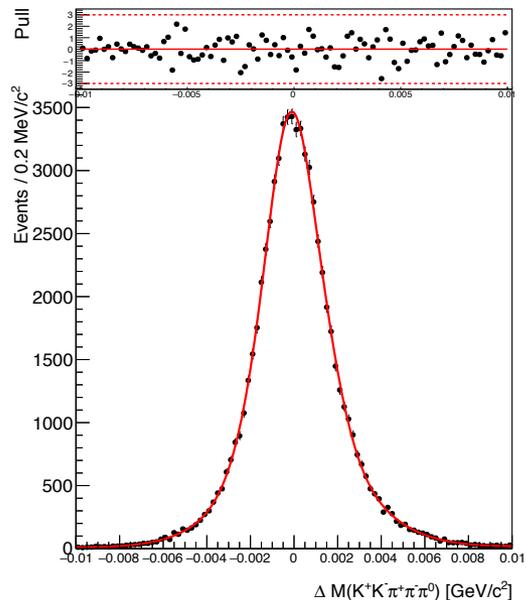
- Consider the final state  $h_c \rightarrow K^+K^-\pi^+\pi^-\pi^0$

So far Resolution is described by:

$$= \begin{cases} e^{\frac{\sigma_L^2}{2} + \sigma_L \left(\frac{m-\mu}{\sigma}\right)^2}, & \frac{m-\mu}{\sigma} \leq -\sigma_L \\ e^{-\frac{1}{2} \left(\frac{m-\mu}{\sigma}\right)^2}, & -\sigma_L < \frac{m-\mu}{\sigma} \leq \sigma_H \\ e^{\frac{\sigma_H^2}{2} - \sigma_H \left(\frac{m-\mu}{\sigma}\right)^2}, & \sigma_H < \frac{m-\mu}{\sigma} \end{cases} + 3 \text{ Gaussian}$$

Another valid parameterization but worse fit stability:

Crystal Ball + 4 Gaussian



- results in difference of 2.2% for the determined branching fraction (2-3% for other final states)
- taken as additional systematic uncertainty

## 2. Generating Signal MC with HELAMP model instead of PHSP model

*Before*

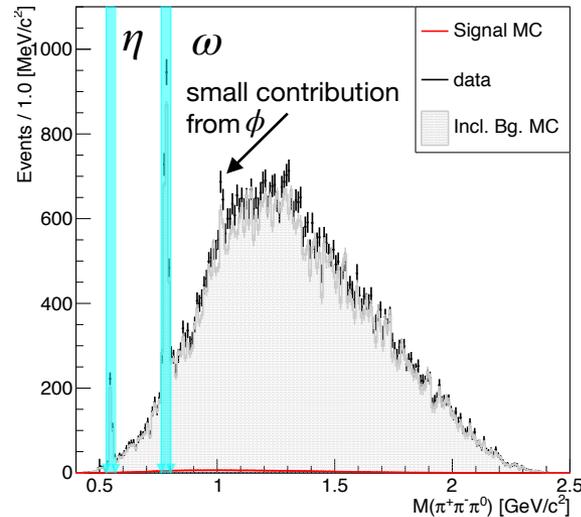
```
#  
Decay psi(2S)  
1.0000 pi0 h_c PHSP;  
Enddecay
```

*Now*

```
#  
Decay psi(2S)  
1.0000 pi0 h_c HELAMP 0 0 1 0 0 0;  
Enddecay
```

- ➔ difference in efficiency of at most 0.8% for all final states
- HELAMP model will be used from now on
- ➔ PHSP model will be taken into account within systematic error

### 3. Investigate background from $\phi \rightarrow \pi^+\pi^-\pi^0$ in the final state $h_c \rightarrow K_S^0 K^\pm \pi^\mp \pi^+ \pi^-$



- Background is visible in the system of the  $\pi^0$  from  $\psi' \rightarrow \pi^0 h_c$
- and charged pions from  $h_c$  decay
- Background from  $\phi$  contributes with only  $\sim 1\%$  to all background events
- Cut on  $\phi$  affects signal efficiency by 1%!
- ➔ not sufficient to reduce this background

# Summary

- In total 10 final states have been analyzed which have never been measured before - hints for 3 new decay modes of the  $h_c$  have been found
- Changes to last talk:
  1. Additional systematic uncertainties have been determined for the parametrization of the resolution distribution
  2. Different generator model has been used for signal MC (HELAMP instead of PHSP)
- Results change slightly:

| final state                   | BF( $h_c \rightarrow X$ )                     |
|-------------------------------|---|
| $K^+K^-\pi^+\pi^-\pi^0$       | $(3.3 \pm 0.4 \pm 0.4 \pm 0.5) \cdot 10^{-3}$ |
| $K_S^0K^\pm\pi^\mp\pi^+\pi^-$ | $(7.6 \pm 1.7 \pm 1.0 \pm 1.1) \cdot 10^{-3}$ |
| $\pi^+\pi^-\pi^0\eta$         | $(7.3 \pm 1.9 \pm 0.8 \pm 1.1) \cdot 10^{-3}$ |
| $2(K^+K^-)\pi^0$              | $< 2.0 \cdot 10^{-4}$                         |
| $K^+K^-\pi^0$                 | $< 5.7 \cdot 10^{-4}$                         |
| $K^+K^-\eta$                  | $< 9.2 \cdot 10^{-4}$                         |
| $K^+K^-\pi^0\eta$             | $< 2.2 \cdot 10^{-3}$                         |
| $K^+K^-\pi^+\pi^-\eta$        | $< 2.5 \cdot 10^{-3}$                         |
| $K_S^0K^\pm\pi^\mp$           | $< 6.4 \cdot 10^{-4}$                         |
| $p\bar{p}\pi^0\pi^0$          | $< 5.7 \cdot 10^{-4}$                         |

- Looking forward to taking further steps!



*Thank You!*

# Backup

# General selection criteria

## Good charged track criteria

Poca:  $R_{xy} < 1 \text{ cm}$  ,  $R_z < 10 \text{ cm}$

Polar angle:  $|\cos \theta| < 0.93$

## PID criteria

using  $dE/dx$  information from MDC and TOF information

p-Value:  $P(X) > 10^{-3}$ ,

$P(X) > P(Y)$ ,  $X \neq Y$

## Good photon criteria

Separation from tracks:  $\Delta\Omega > 10^\circ$

EMC time info:  $t < 700 \text{ ns}$

Barrel:  $E_\gamma > 25 \text{ MeV}$ ,

$|\cos \theta| < 0.8$

Endcaps:  $E_\gamma > 50 \text{ MeV}$ ,

$0.86 < |\cos \theta| < 0.92$

## Reconstruction of $\pi^0$ candidates

$|M(\gamma\gamma) - M(\pi^0)| < 30 \text{ MeV}/c^2$

mass constrained fit

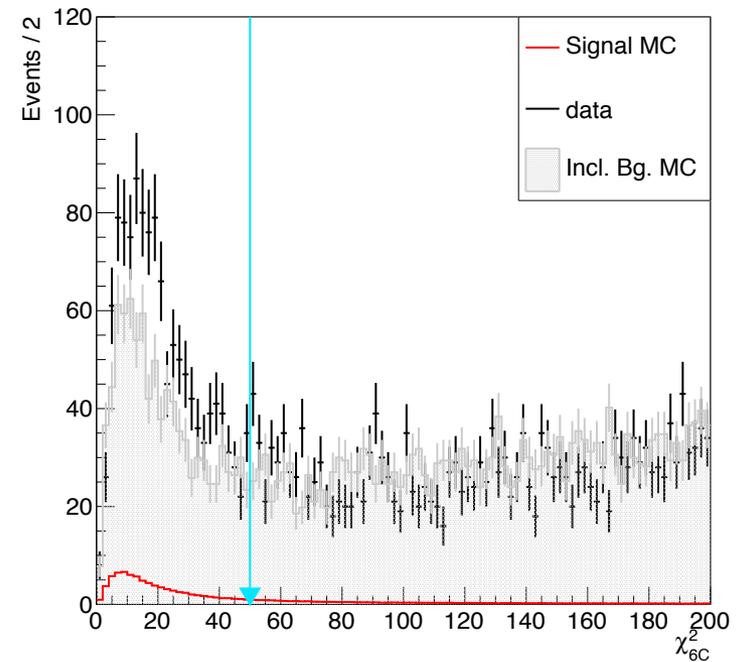
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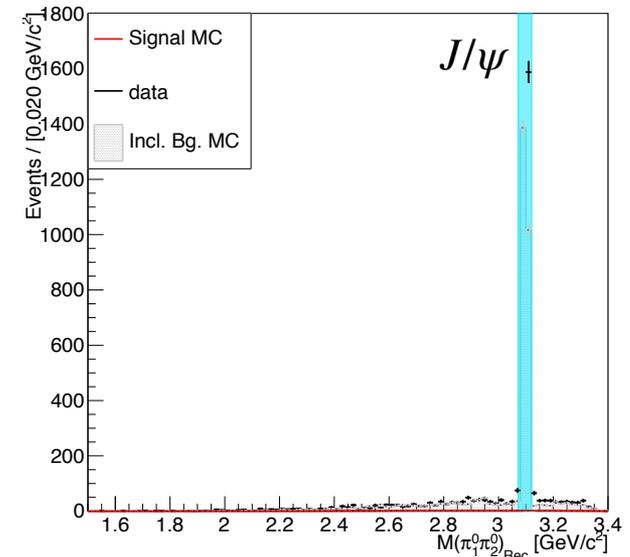
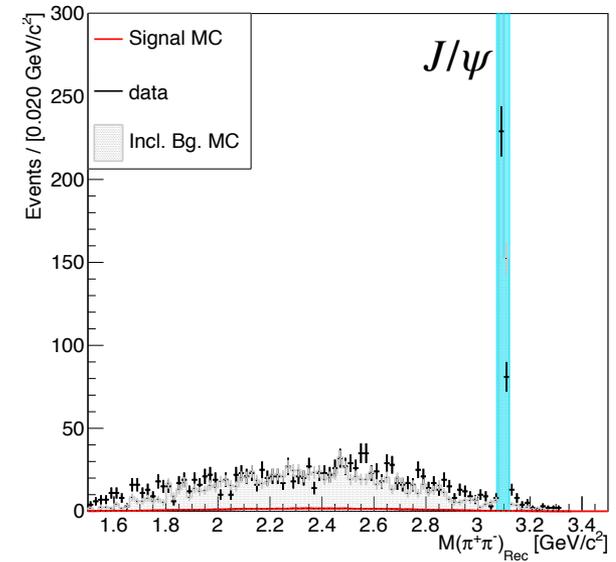
# Analysis of $h_c \rightarrow K^+K^-\pi^+\pi^-\pi^0$

- Common vertex ensured by converged vertex fit
- $N_\pi = 2$ ,  $N_K = 2$ ,  $N_\gamma \geq 4$
- Limit goodness of 6C Fit:  $\chi_{6C}^2 < 50$



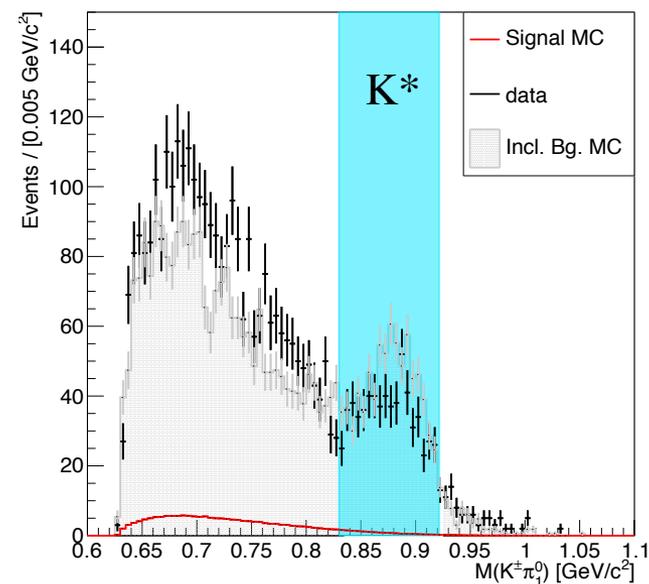
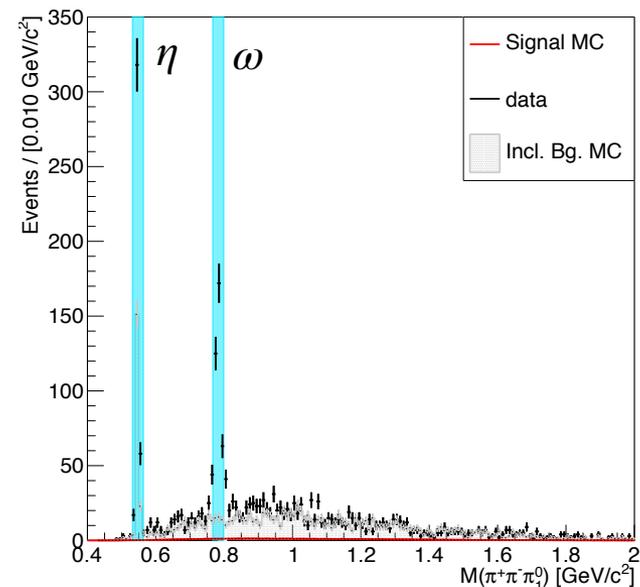
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- additional 4C fit under hypothesis  $3\gamma K^+K^-\pi^+\pi^-$  to veto background from
  - $\psi' \rightarrow \gamma\chi_{cJ} : \chi_{4C}^2 < \chi_{3\gamma}^2$
- reject background from  $\psi' \rightarrow \pi^+\pi^-J/\psi$ ,  $\pi^0\pi^0J/\psi$  :
  - $|M(\pi^+\pi^-)_{Rec} - M(J/\psi)| > 25 \text{ MeV}/c^2$
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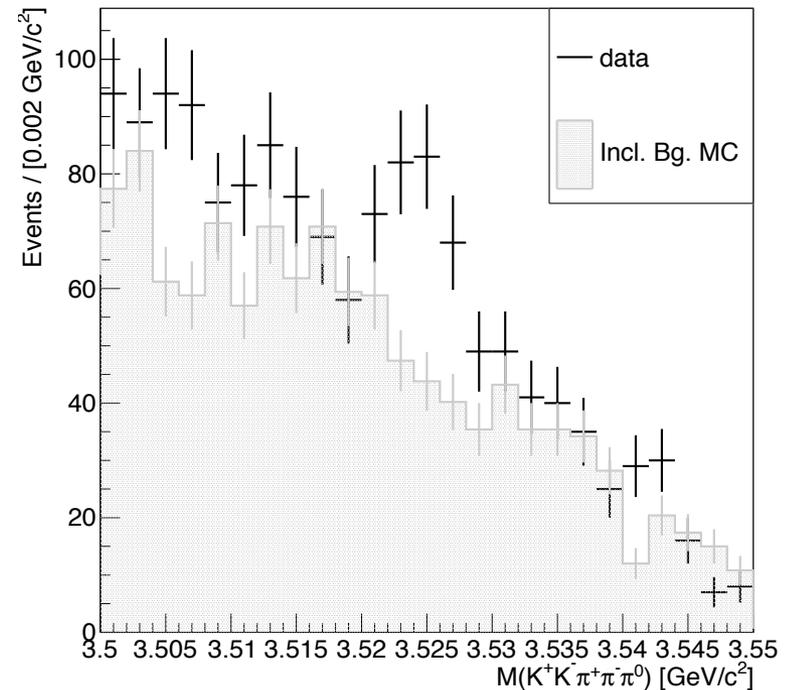
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  - $|M(\pi^+\pi^-\pi^0) - M(\eta)| > 16 \text{ MeV}/c^2$
  - $|M(\pi^+\pi^-\pi^0) - M(\omega)| > 20 \text{ MeV}/c^2$
  - $0.82 \text{ GeV}/c^2 \leq M(K^\pm\pi_1^0) \leq 0.92 \text{ GeV}/c^2$



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➔ **obtained efficiency 6.5%**



# Background studies

- Non-resonant contribution dominates (99%)

| process                           | $N_{\text{rem}}$ |
|-----------------------------------|------------------|
| $K^{*0} K^{*\pm} \pi^{\mp} \pi^0$ | 437              |
| $K^{*\pm} K^{*\mp} \pi^+ \pi^-$   | 230              |
| $K^{*0} K^{*\pm} \rho^{\mp}$      | 185              |
| $K^{*+} K^{*-} \rho^0$            | 25               |

- Study of peaking background caused by radiative decays:

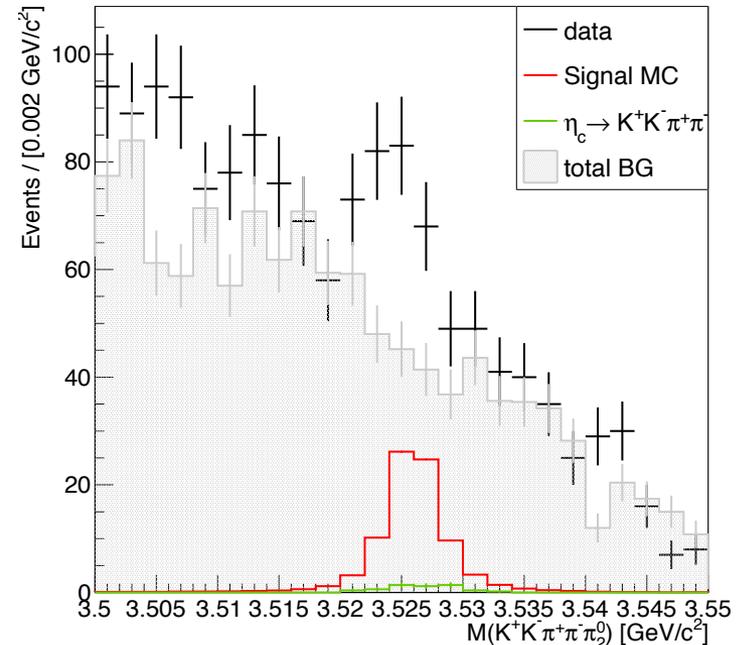
- $h_c \rightarrow \gamma \eta_c, \gamma \chi_{c1}, \gamma \chi_{c0}$

- ✗ Problem: decay modes mostly unknown, explicit search limited by statistics and dominated by background

→ But theoretical predictions exist, used to estimate:

- $\text{BF}(h_c \rightarrow \gamma \chi_{c1}) \sim 3.4 \cdot 10^{-7}$  (suppressed by PHSP)
  - $\text{BF}(h_c \rightarrow \gamma \chi_{c1}) \sim 8.6 \cdot 10^{-4}$  [Phys. Rev. D 89 11 (2014)]

→ remaining peaking background taken into account within fit



- known decay modes scaled to PDG value
- unknown decay modes generated using LUND Model
- additional sets similar to final state have been generated (see next slide)

# Background studies

List of explicitly generated final states

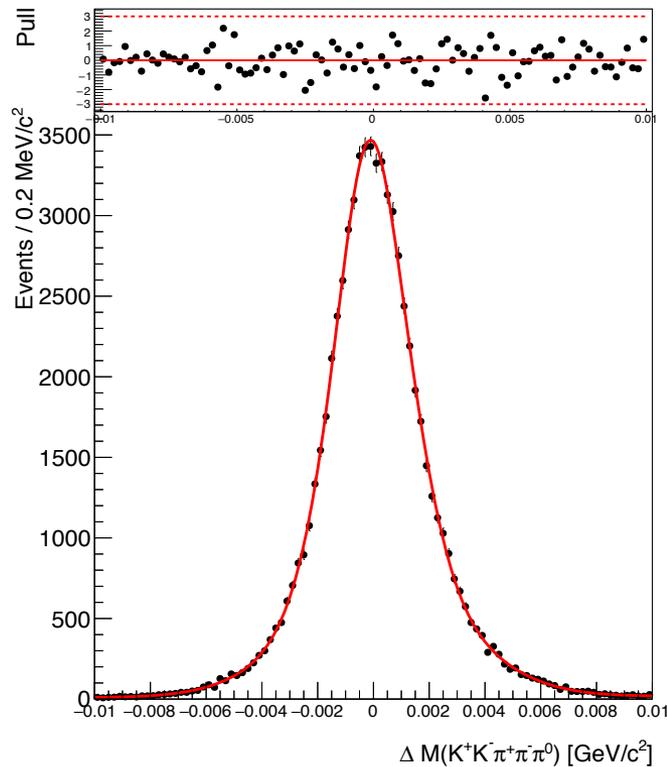
| process $h_c \rightarrow \gamma X$                   | intermediate states         | $N_{\text{rem}}$ | $N_{\text{expected}}$ |
|--|-----------------------------|------------------|-----------------------|
| $\eta_c \rightarrow K^+ K^- \pi^+ \pi^-$             | $K^{*0} K^{*\pm} \pi^\mp$   | 12               | 3                     |
| $\eta_c \rightarrow K^+ K^- \pi^+ \pi^-$             | PSHP                        | 10               | 2                     |
| $\eta_c \rightarrow K^+ K^- \pi^+ \pi^- \pi^0 \pi^0$ | PHSP                        | 2                | 0                     |
| $\eta_c \rightarrow K^+ K^- \pi^+ \pi^- \pi^0 \pi^0$ | $K^{*+} K^{*-} \pi^0 \pi^0$ | 1                | 0                     |
| $\eta_c \rightarrow K^+ K^- \pi^+ \pi^- \pi^0 \eta$  | PHSP                        | 0                | 0                     |
| $\eta_c \rightarrow K^+ K^- \pi^+ \pi^- \pi^0 \eta$  | $K^{*+} K^{*-} \pi^0 \eta$  | 0                | 0                     |
| $\eta_c \rightarrow K^+ K^- \pi^+ \pi^- \eta \eta$   | PHSP                        | 0                | 0                     |
| $\chi_{c0}$  | PHSP                        | 5                | 0                     |
| $\chi_{c1}$  | PHSP                        | 0                | 0                     |

**No background process identified,  
which could describe the complete observed structure**

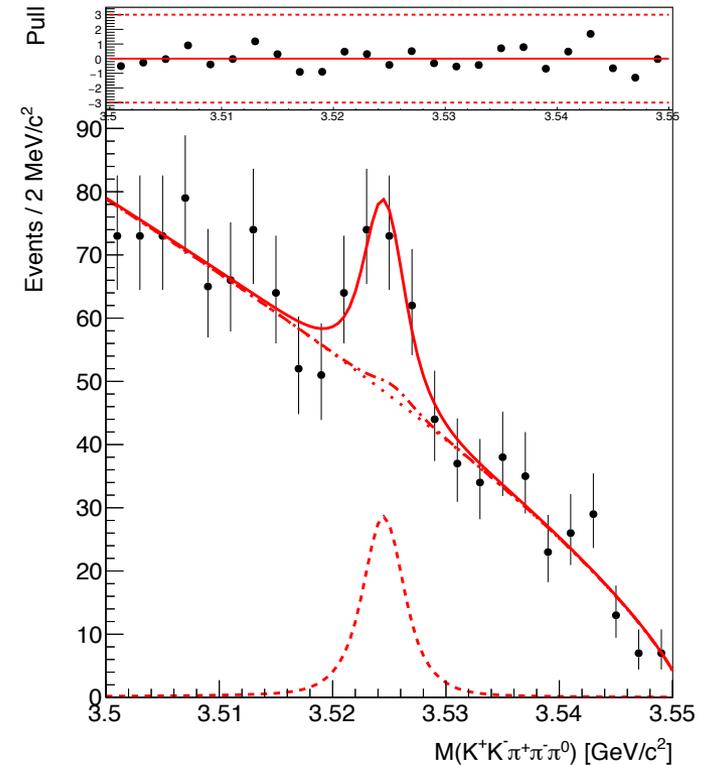
# Determination of branching fraction of $h_c \rightarrow K^+K^-\pi^+\pi^-\pi^0$

## Resolution

$$= \begin{cases} e^{-\frac{\sigma_L^2}{2} + \sigma_L \left(\frac{m-\mu}{\sigma}\right)^2}, & \frac{m-\mu}{\sigma} \leq -\sigma_L \\ e^{-\frac{1}{2} \left(\frac{m-\mu}{\sigma}\right)^2}, & -\sigma_L < \frac{m-\mu}{\sigma} \leq \sigma_H \\ e^{-\frac{\sigma_H^2}{2} - \sigma_H \left(\frac{m-\mu}{\sigma}\right)^2}, & \sigma_H < \frac{m-\mu}{\sigma} \end{cases} + 3 \text{ Gaussian}$$



## Breit-Wigner $\otimes$ Resolution + Argus



Significance calculated to  $6.0\sigma$

$$M(h_c) = 3524.9 \pm 0.6 \text{ MeV}/c^2$$

$$\Gamma(h_c) = 0.8 \pm 0.5 \text{ MeV}$$

$$BF(h_c \rightarrow K^+K^-\pi^+\pi^-\pi^0)$$

$$= (3.0 \pm 0.4 \pm 0.4 \pm 0.6) \cdot 10^{-3}$$

# Systematic studies

## Selection procedure

- variation of selection criteria

| cut   | nominal value | range | step size | uncertainty |
|---|---------------|-------|-----------|-------------|
| $\chi_{6C}^2$   | 50            | 30-70 | 1         | 2.8 %       |
| $ M(\pi^+\pi^-)_{Rec} - M(J/\psi) $ [MeV/c <sup>2</sup> ] | 25            | 10-40 | 1         | 0.5 %       |
| $ M(\pi^0\pi^0)_{Rec} - M(J/\psi) $ [MeV/c <sup>2</sup> ] | 25            | 10-40 | 1         | 1.4 %       |
| $ M(\pi^0 K^\pm) - M(K^{*\pm}) $ [MeV/c <sup>2</sup> ]    | 30            | 10-50 | 1         | 3.8 %       |
| $ M(\pi^+\pi^-\pi^0) - M(\eta) $ [MeV/c <sup>2</sup> ]    | 16            | 6-26  | 1         | 1.3 %       |
| $ M(\pi^+\pi^-\pi^0) - M(\omega) $ [MeV/c <sup>2</sup> ]  | 20            | 10-30 | 1         | 2.5 %       |

- Kinematic fit using helix correction method: 1.5%

## Generator model

- including intermediate resonances to generator model leads efficiency difference of at most **5.1%**

## Fit model

- Describing background by Chebychev polynomial instead of Argus function: **1.2%**
- Different parametrization of resolution: **2.2%**
- Fitting range: **0.9%**

## Tracking

- 1% per track  $\Rightarrow$  4%

## Photon reconstruction

- 1% per photon  $\Rightarrow$  4%

## PID

- 1% per track  $\Rightarrow$  4%

## $\pi^0$ reconstruction

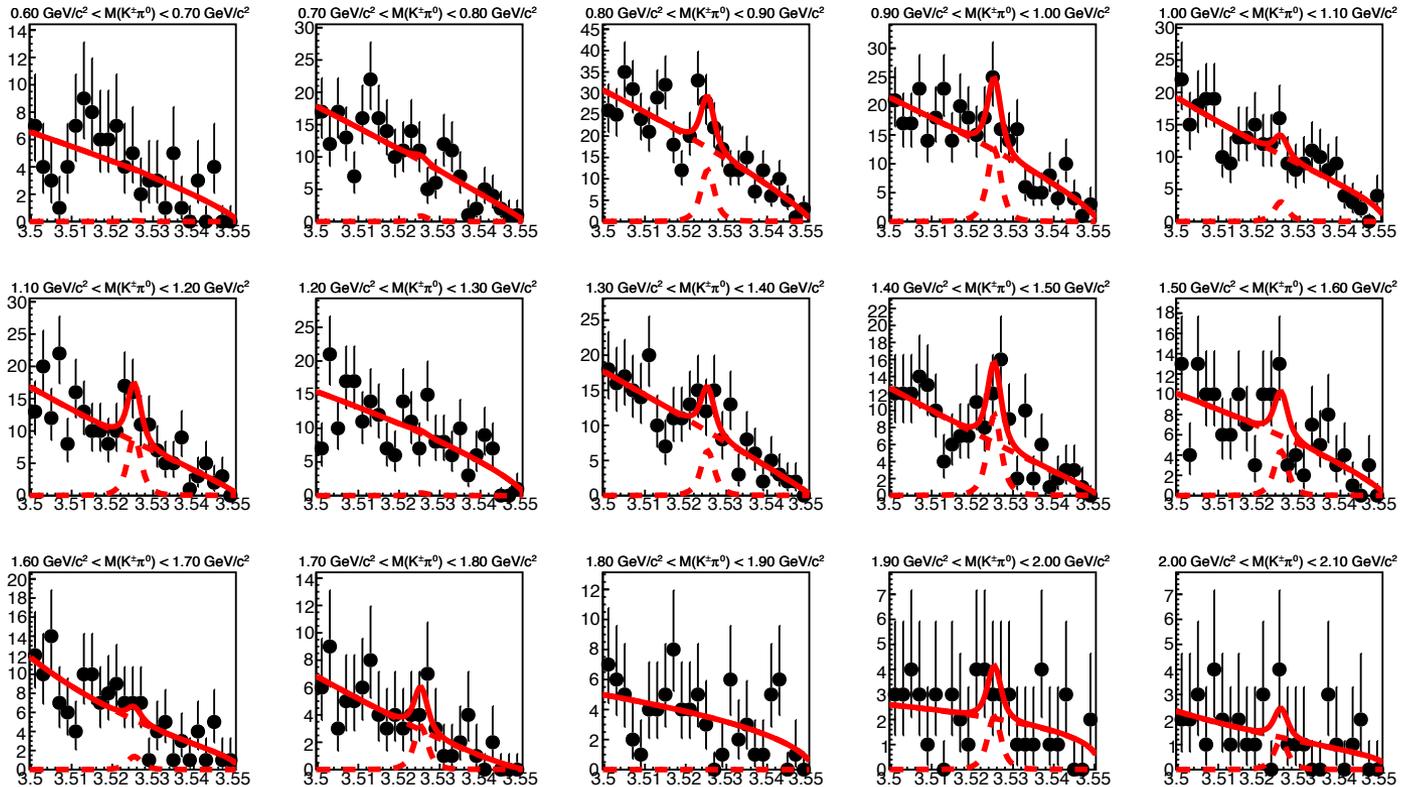
- 1% per  $\pi^0$   $\Rightarrow$  2%

**total 10.7% + 15.1% caused by involved branching fractions!**

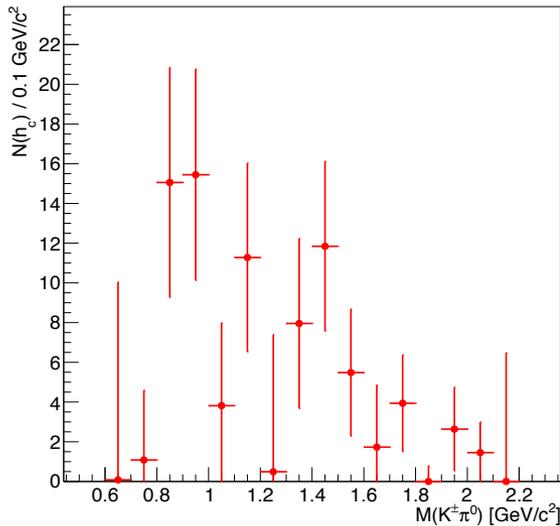
# Study of intermediate resonances

- **Problem:** Background dominated process, sideband subtraction not suitable
- **Idea:** Extracting signal yield in slices of subsystems
- same fitting procedure used as before in subregions

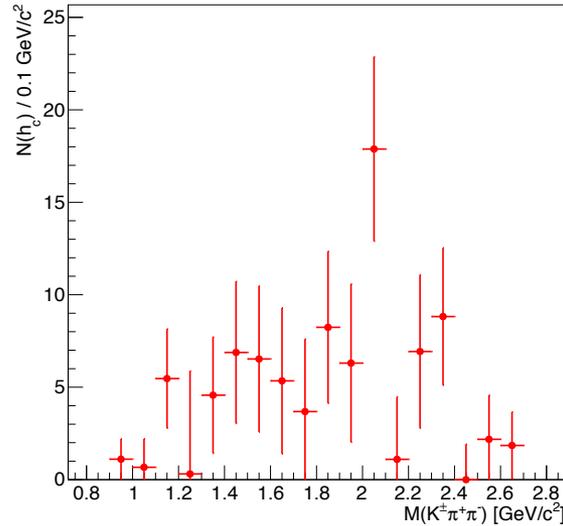
For example fit in slices of  $K\pi$  mass



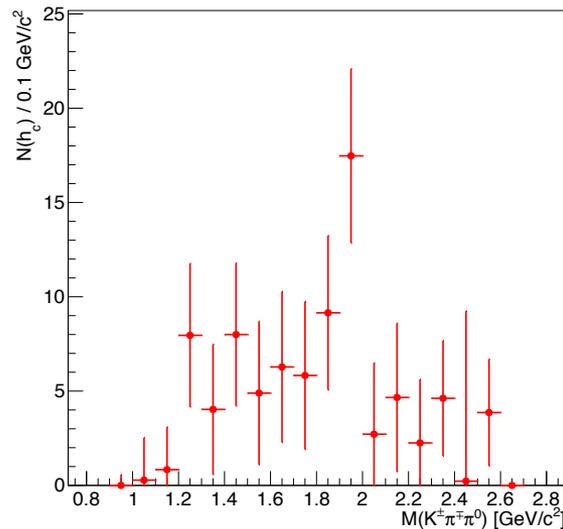
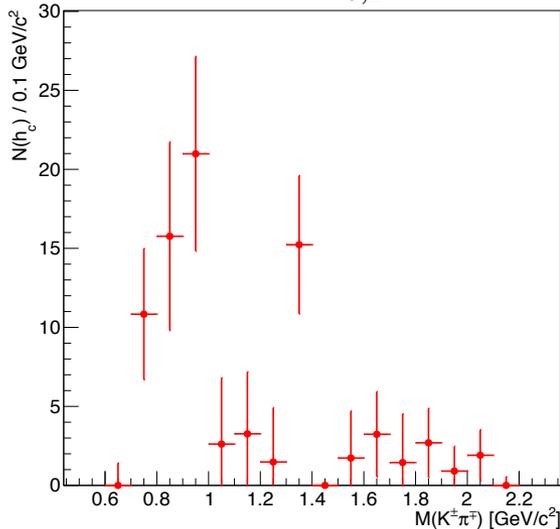
# Study of intermediate resonances



$K^*(892)$ ,  $K_{0,2}^*(1430)$



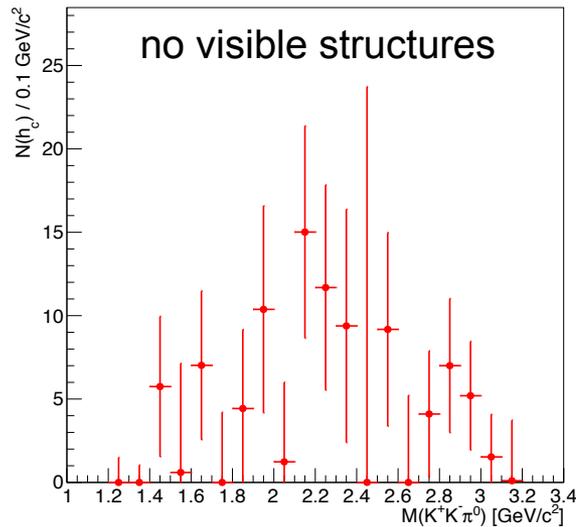
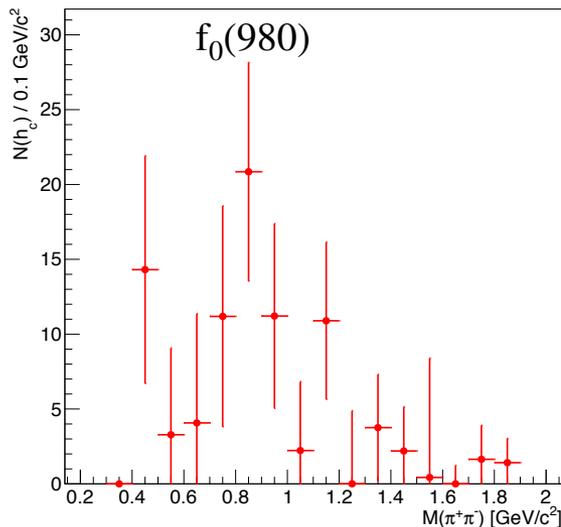
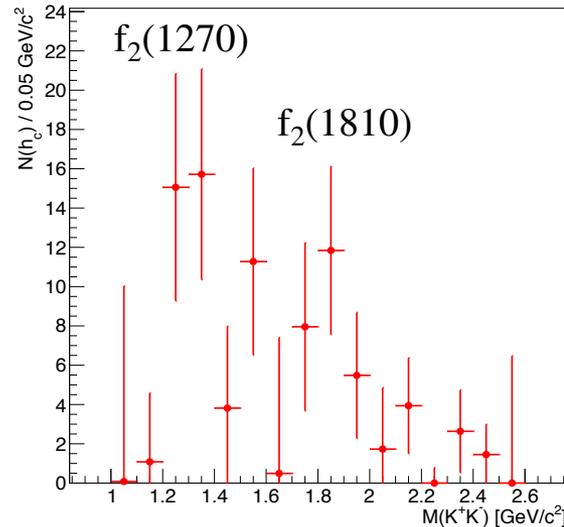
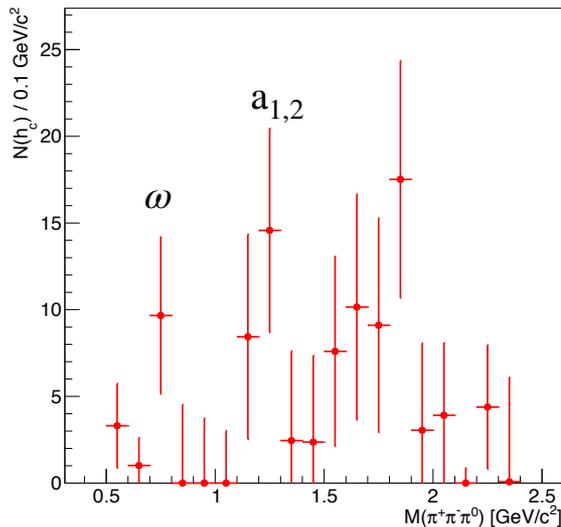
$K_2(1820)$ ,  $K_2^*(1980)$



- shown error bars are statistical only
- similar structures in charged and neutral mode
- indication for intermediate reactions like:

$$h_c \rightarrow \left( K^*(892)/K_{0,2}^*(1430) \right) \\ \left( K_2(1820)/K_2^*(1980) \right)$$

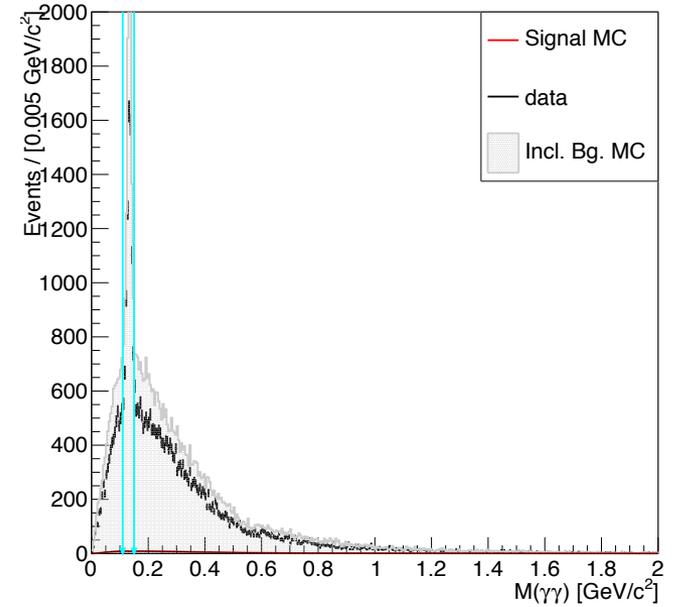
# Study of intermediate resonances



- $h_c \rightarrow (\pi^+ \pi^- \pi^0)(K^+ K^-)$  seems to be more favored than  $h_c \rightarrow (\pi^+ \pi^-)(\pi^0 K^+ K^-)$
- Correlations between subsystems have been investigated by generating the supposed intermediate reactions

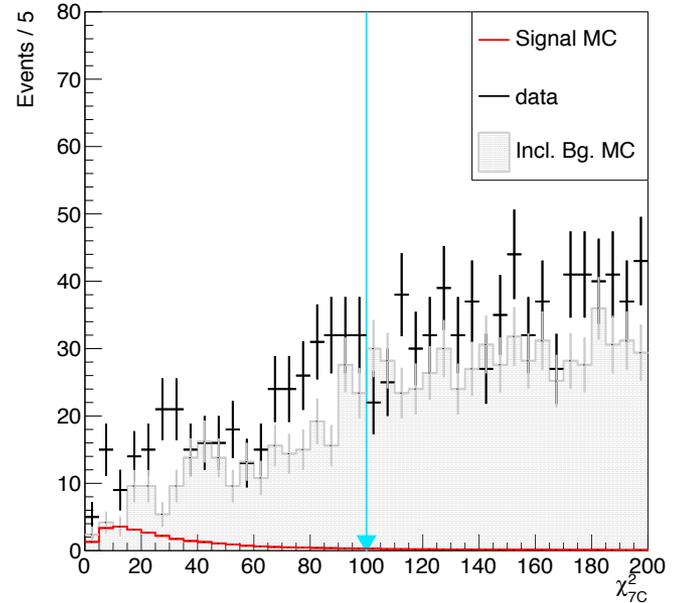
# Analysis of $h_c \rightarrow \pi^+ \pi^- \pi^0 \eta$

- Common vertex ensured by converged vertex fit
- $N_\pi = 2, N_\gamma \geq 6$
- no pair of photons from different particles should form a  $\pi^0$ :
  - $|M(\gamma\gamma) - M(\pi^0)| > 15 \text{ MeV}/c^2$



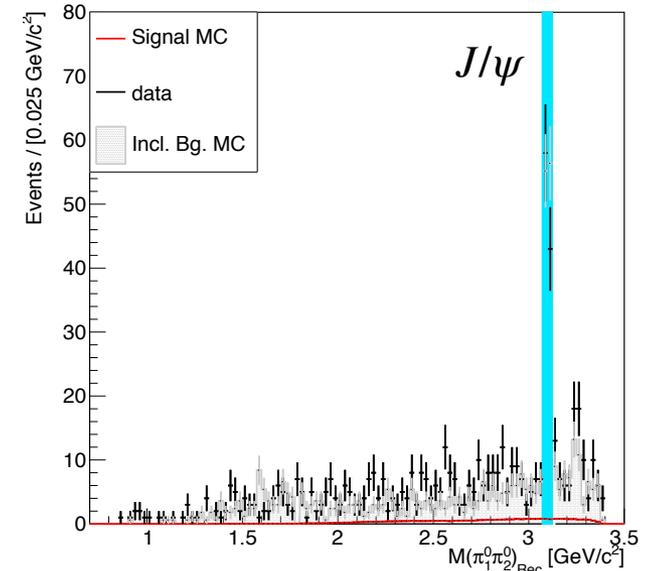
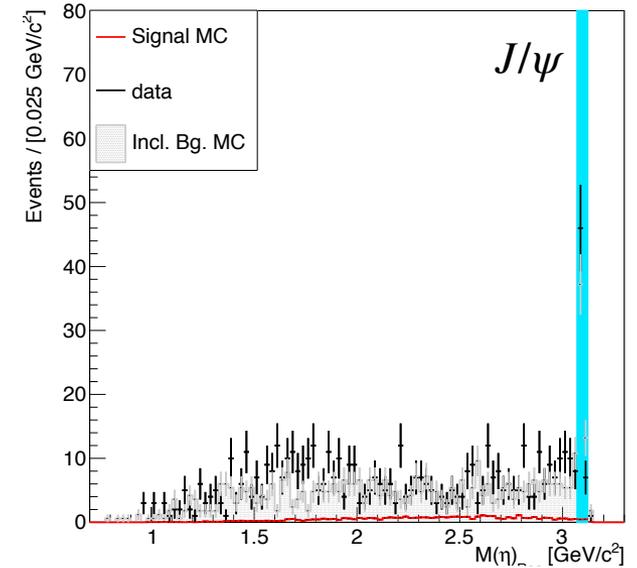
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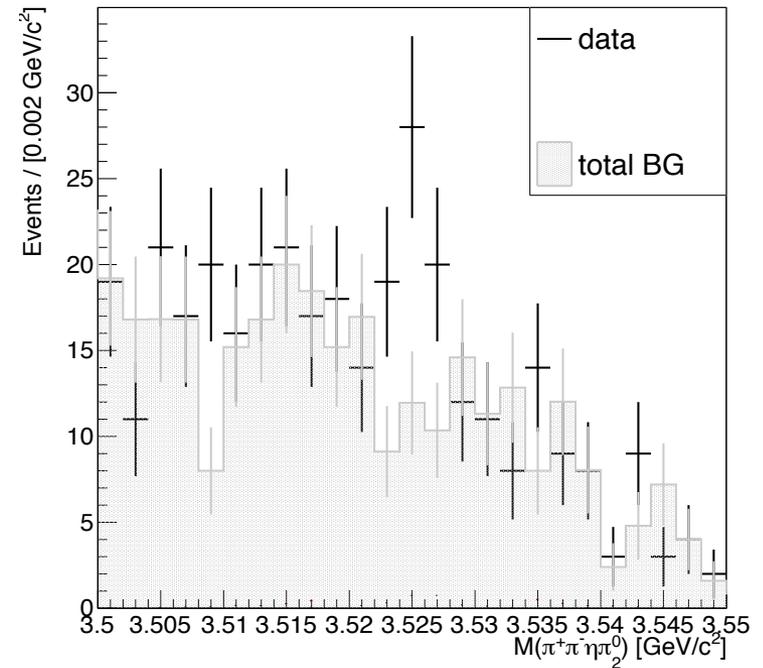
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  - $|M(\pi^+ \pi^- \pi^0) - M(\omega)| > 20 \text{ MeV}/c^2$
- reject background from  $\psi' \rightarrow \pi^0 \pi^0 J/\psi, \eta J/\psi$  :
  - $|M(\pi^0 \pi^0)_{\text{Rec}} - M(J/\psi)| > 30 \text{ MeV}/c^2$
  - $|M(\eta)_{\text{Rec}} - M(J/\psi)| > 30 \text{ MeV}/c^2$



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  - $|M(\eta)_{Rec} - M(J/\psi)| > 30 \text{ MeV}/c^2$

➔ obtained efficiency 3.9 %

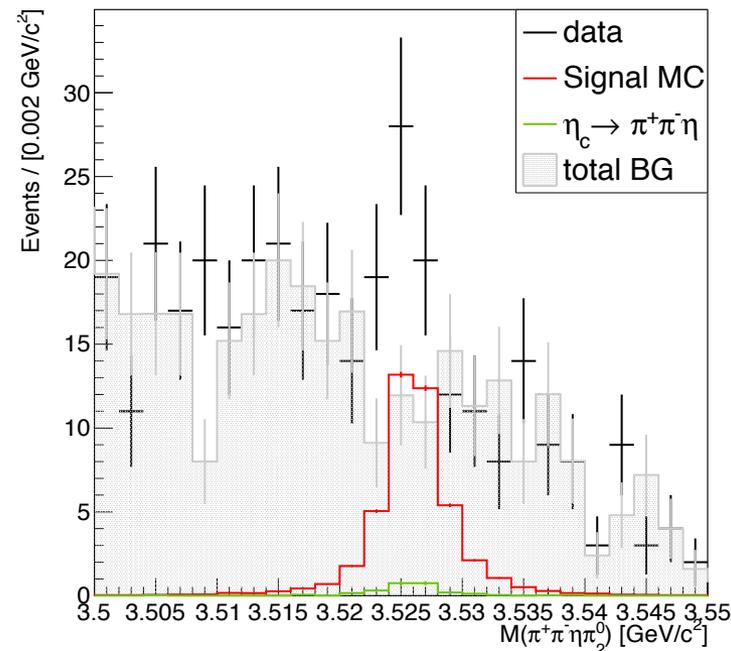


# Background studies

- Dominating contribution from  $e^+e^- \rightarrow 4\gamma\pi^+\pi^-\eta$
- Study of peaking background caused by radiative decays:
  - $h_c \rightarrow \gamma\chi_{c1}, \gamma\chi_{c0}$
  - ➔ negligible contribution
- $h_c \rightarrow \gamma\eta_c$

| process                                   | $N_{\text{rem}}$ | $N_{\text{expected}}$ |
|---|------------------|-----------------------|
| $\eta_c \rightarrow \pi^+\pi^-\pi^0$      | 16               | 3                     |
| $\eta_c \rightarrow \pi^+\pi^-\pi^0\pi^0$ | 7                | 1                     |

- ➔ peaking background is taken into account within the fit to determine the effective signal yield

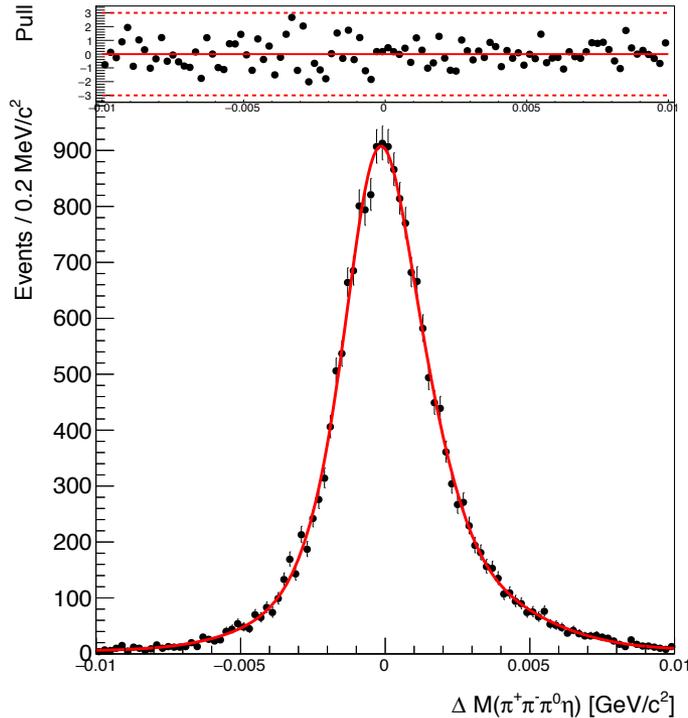


- known decay modes scaled to PDG value
- unknown decay modes generated using LUND Model

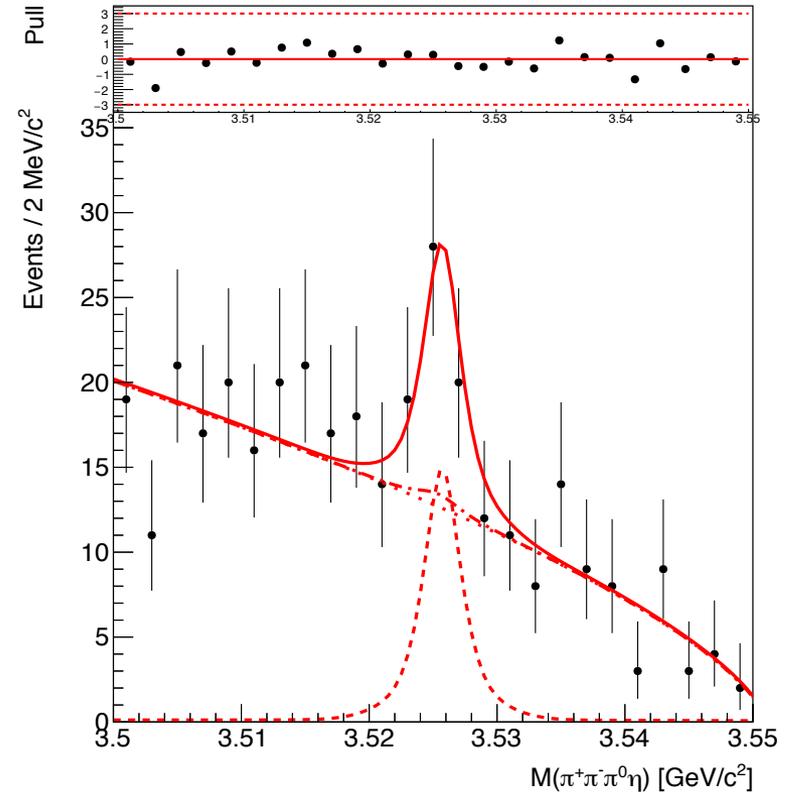
# Determination of branching fraction of $h_c \rightarrow \pi^+ \pi^- \pi^0 \eta$

## Resolution

$$= \begin{cases} e^{\frac{\sigma_L^2}{2} + \sigma_L \left(\frac{m-\mu}{\sigma}\right)^2}, & \frac{m-\mu}{\sigma} \leq -\sigma_L \\ e^{-\frac{1}{2} \left(\frac{m-\mu}{\sigma}\right)^2}, & -\sigma_L < \frac{m-\mu}{\sigma} \leq \sigma_H \\ e^{\frac{\sigma_H^2}{2} - \sigma_H \left(\frac{m-\mu}{\sigma}\right)^2}, & \sigma_H < \frac{m-\mu}{\sigma} \end{cases} + 3 \text{ Gaussian}$$



## Breit-Wigner ⊗ Resolution + Argus



$$\text{BF}(h_c \rightarrow \pi^+ \pi^- \pi^0 \eta)$$

$$= (9.9 \pm 1.6 \pm 1.2 \pm 1.5) \cdot 10^{-3}$$

Significance calculated to  $3.8\sigma$

# Systematic studies

## Selection procedure

- variation of selection criteria

| cut  | nominal value | range  | step size | uncertainty |
|--|---------------|--------|-----------|-------------|
| $\chi^2_{7C}$  | 100           | 80-120 | 1         | 3.1         |
| $ M(\eta)_{\text{Rec}} - M(J/\psi) $ [MeV/c <sup>2</sup> ]       | 30            | 15-45  | 1         | 1.3         |
| $ M(\pi^0\pi^0)_{\text{Rec}} - M(J/\psi) $ [MeV/c <sup>2</sup> ] | 30            | 20-40  | 1         | 1.5         |
| $ M(\gamma\gamma) - M(\pi^0) $ [MeV/c <sup>2</sup> ]             | 15            | 5-25   | 1         | 2.8         |
| $ M(\pi^+\pi^-\pi^0) - M(\eta) $ [MeV/c <sup>2</sup> ]           | 16            | 6-26   | 1         | 1.6         |
| $ M(\pi^+\pi^-\pi^0) - M(\omega) $ [MeV/c <sup>2</sup> ]         | 20            | 10-30  | 1         | 2.2         |

- Kinematic fit using helix correction method: 2.1%

## Generator model

- including intermediate resonances to generator model leads efficiency difference of at most 6.3%

## Fit model

- Describing background by Chebychev polynomial instead of Argus function: 2.1%
- Fitting range: 1.1%

## Tracking

## Photon reconstruction

## PID

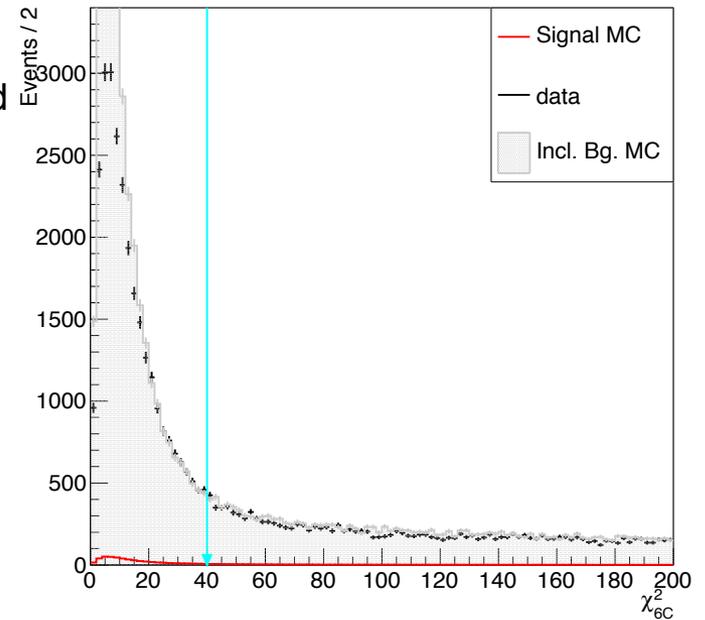
## $\pi^0$ , $\eta$ reconstruction

- 1% per track  $\Rightarrow$  2%
- 1% per photon  $\Rightarrow$  6%
- 1% per track  $\Rightarrow$  2%
- 1% per  $\pi^0$  or  $\eta$   $\Rightarrow$  3%

**total 11.5% + 15.1% caused by involved branching fractions!**

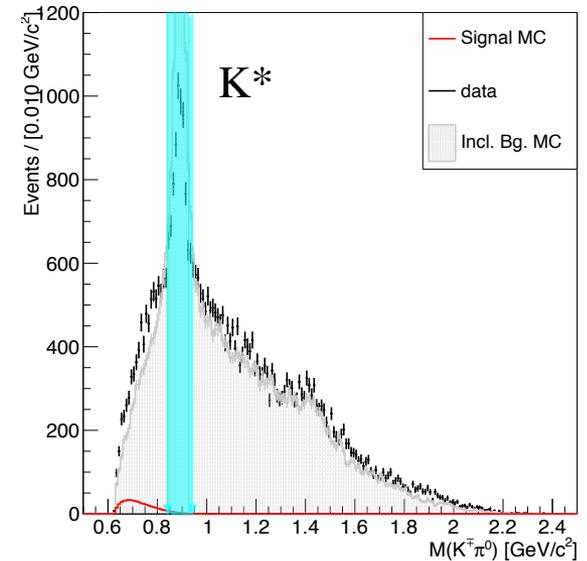
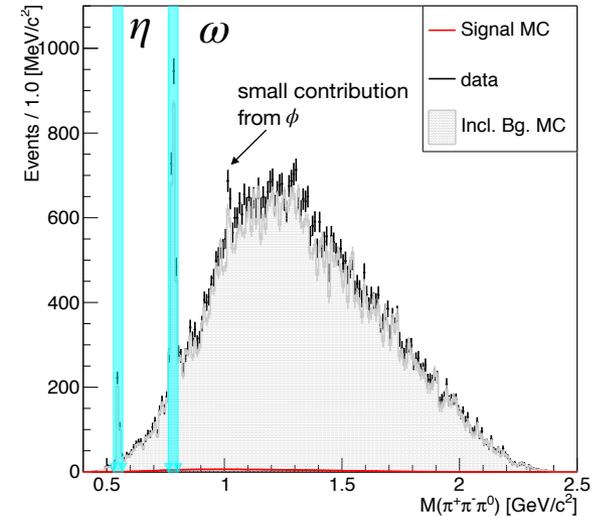
# Analysis of $h_c \rightarrow K_S^0 K^\pm \pi^\mp \pi^+ \pi^-$

- $N_\pi = 5, N_K = 1, N_\gamma \geq 2$
- $K_S^0$  reconstruction:
  - Limit decay length and error determined by secondary vertex fit:  $\lambda/\Delta\lambda < 2$
  - $0.487 \text{ MeV}/c^2 \leq M(\pi^+\pi^-) \leq 0.511 \text{ MeV}/c^2$
- Common vertex ensured by converged vertex fit for all charged particles
- Limit goodness of 6C-Fit:  $\chi_{6C}^2 < 40$



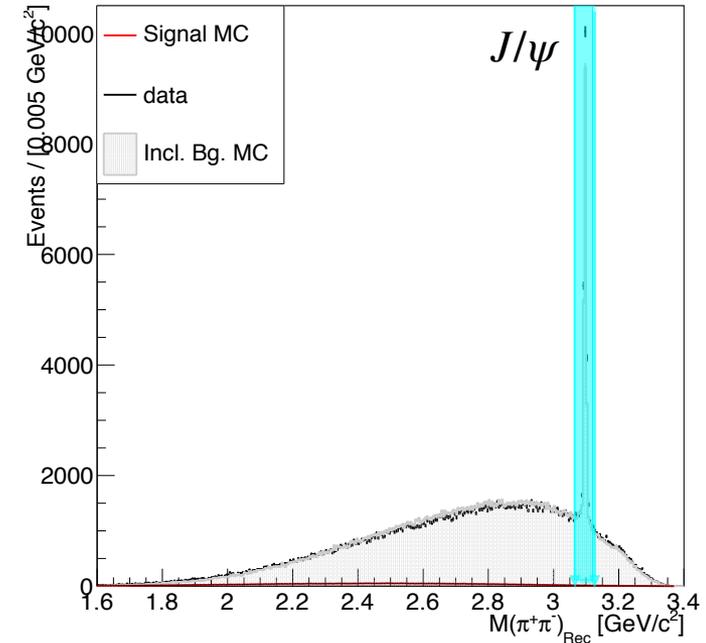
# Analysis of $h_c \rightarrow K_S^0 K^\pm \pi^\mp \pi^+ \pi^-$

- $N_\pi = 5, N_K = 1, N_\gamma \geq 2$
- $K_S^0$  reconstruction:
  - Limit decay length and error determined by secondary vertex fit:  $\lambda/\Delta\lambda < 2$
  - $0.487 \text{ MeV}/c^2 \leq M(\pi^+\pi^-) \leq 0.511 \text{ MeV}/c^2$
- Common vertex ensured by converged vertex fit for all charged particles
- Limit goodness of 6C-Fit:  $\chi_{6C}^2 < 40$
- $\pi^0$  from  $\psi'$  decay should not from other resonances:
  - $|M(\pi^+\pi^-\pi^0) - M(\eta)| > 20 \text{ MeV}/c^2$
  - $|M(\pi^+\pi^-\pi^0) - M(\omega)| > 20 \text{ MeV}/c^2$
- No  $K\pi$  system should form a  $K^*$  meson thus:
  - $|M(K^\pm\pi^0) - M(K^*)| > 50 \text{ MeV}/c^2$
  - $|M(K_S^0\pi^0) - M(K^*)| > 50 \text{ MeV}/c^2$



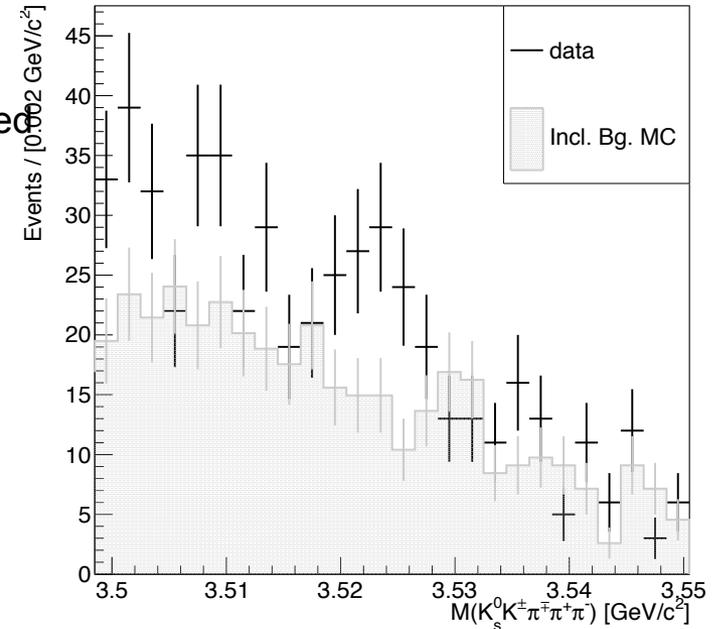
# Analysis of $h_c \rightarrow K_S^0 K^\pm \pi^\mp \pi^+ \pi^-$

- $N_\pi = 5, N_K = 1, N_\gamma \geq 2$
- $K_S^0$  reconstruction:
  - Limit decay length and error determined by secondary vertex fit:  $\lambda/\Delta\lambda < 2$
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  - $|M(\pi^+\pi^-\pi^0) - M(\omega)| > 20 \text{ MeV}/c^2$
- No  $K\pi$  system should form a  $K^*$  meson thus:
  - $|M(K^\pm\pi^0) - M(K^*)| > 50 \text{ MeV}/c^2$
  - $|M(K_S^0\pi^0) - M(K^*)| > 50 \text{ MeV}/c^2$
- No  $\pi^+\pi^-$  pair not resulting from the  $K_S^0$  decay should form a  $K_S^0$ :
  - $|M(\pi^+\pi^-) - M(K_S^0)| > 20 \text{ MeV}/c^2$
- Background from  $\psi' \rightarrow \pi^+\pi^- J/\psi$  is suppressed by:
  - $|M(\pi^+\pi^-)_{Rec} - M(J/\psi)| > 30 \text{ MeV}/c^2$



# Analysis of $h_c \rightarrow K_S^0 K^\pm \pi^\mp \pi^+ \pi^-$

- $N_\pi = 5, N_K = 1, N_\gamma \geq 2$
- $K_S^0$  reconstruction:
  - Limit decay length and error determined by secondary vertex fit:  $\lambda/\Delta\lambda < 2$
  - $0.487 \text{ MeV}/c^2 \leq M(\pi^+\pi^-) \leq 0.511 \text{ MeV}/c^2$
- Common vertex ensured by converged vertex fit for all charged particles
- Limit goodness of 6C-Fit:  $\chi_{6C}^2 < 40$
- $\pi^0$  from  $\psi'$  decay should not from other resonances:
  - $|M(\pi^+\pi^-\pi^0) - M(\eta)| > 20 \text{ MeV}/c^2$
  - $|M(\pi^+\pi^-\pi^0) - M(\omega)| > 20 \text{ MeV}/c^2$
- No  $K\pi$  system should form a  $K^*$  meson thus:
  - $|M(K^\pm\pi^0) - M(K^*)| > 50 \text{ MeV}/c^2$
  - $|M(K_S^0\pi^0) - M(K^*)| > 50 \text{ MeV}/c^2$
- No  $\pi^+\pi^-$  pair not resulting from the  $K_S^0$  decay should form a  $K_S^0$ :
  - $|M(\pi^+\pi^-) - M(K_S^0)| > 20 \text{ MeV}/c^2$
- Background from  $\psi' \rightarrow \pi^+\pi^- J/\psi$  is suppressed by:
  - $|M(\pi^+\pi^-)_{Rec} - M(J/\psi)| > 30 \text{ MeV}/c^2$

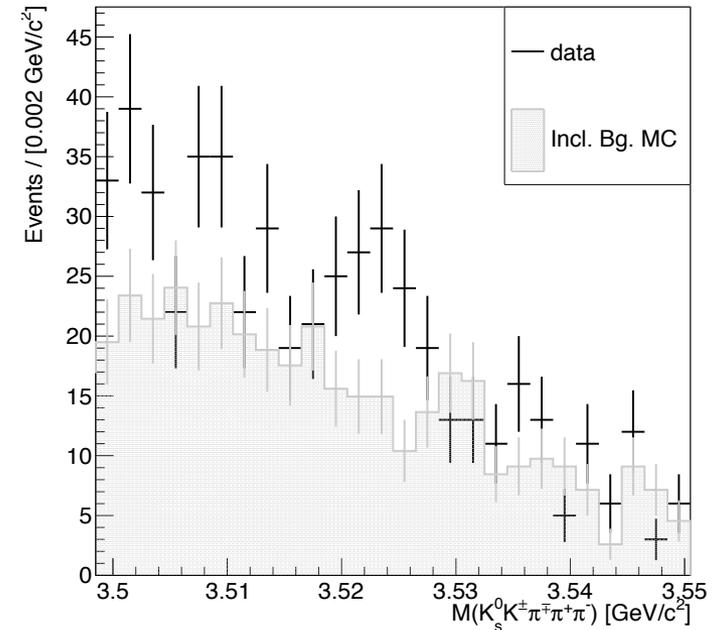


- ➔ obtained efficiency 6.4%
- ➔ structure as expected due to  $h_c \rightarrow K^+ K^- \pi^+ \pi^- \pi^0$  channel but smaller yield

# Background studies

- Here no peaking background can result from  $h_c \rightarrow \gamma \eta_c$  due to misidentification of a  $\pi^0$
- Main background contributions are:

| process                             | final state                             | $N_{\text{rem}}$ | $N_{\text{expected}}$ |
|-------------------------------------|---|------------------|-----------------------|
| $K^{*+}K^{*-}\pi^+\pi^-$            | $K_S^0 K^\pm \pi^\mp \pi^+ \pi^- \pi^0$ | 114              | 35 %                  |
| $K^{*0}\overline{K^{*0}}\pi^+\pi^-$ | $K_S^0 K^\pm \pi^\mp \pi^+ \pi^- \pi^0$ | 98               | 30 %                  |
| $K^{*0}K^{*\pm}\pi^\mp\pi^0$        | $K_S^0 K^\pm \pi^\mp \pi^+ \pi^- \pi^0$ | 92               | 28 %                  |

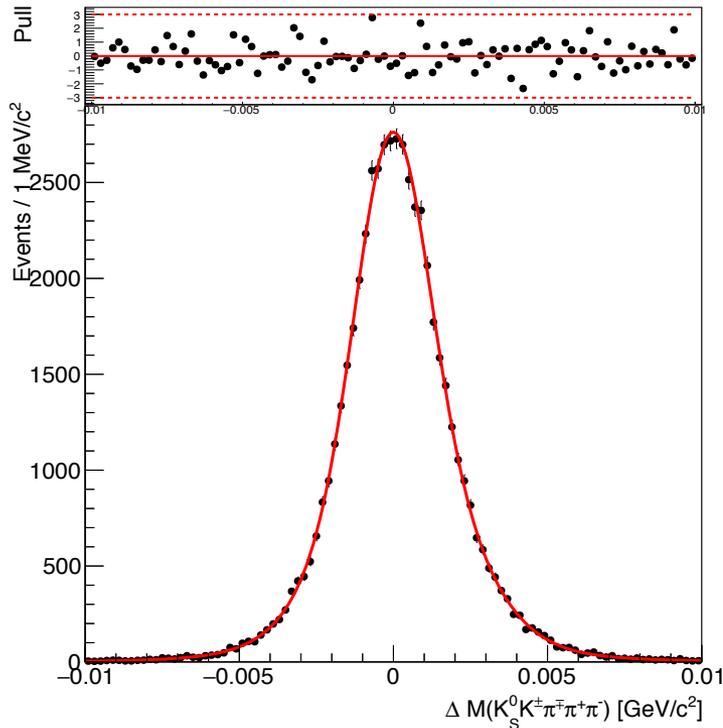


- despite the criterion to reduce  $K^*$  resonances, events in which the  $\pi^0$  meson contributes to a  $K^*$ , remain

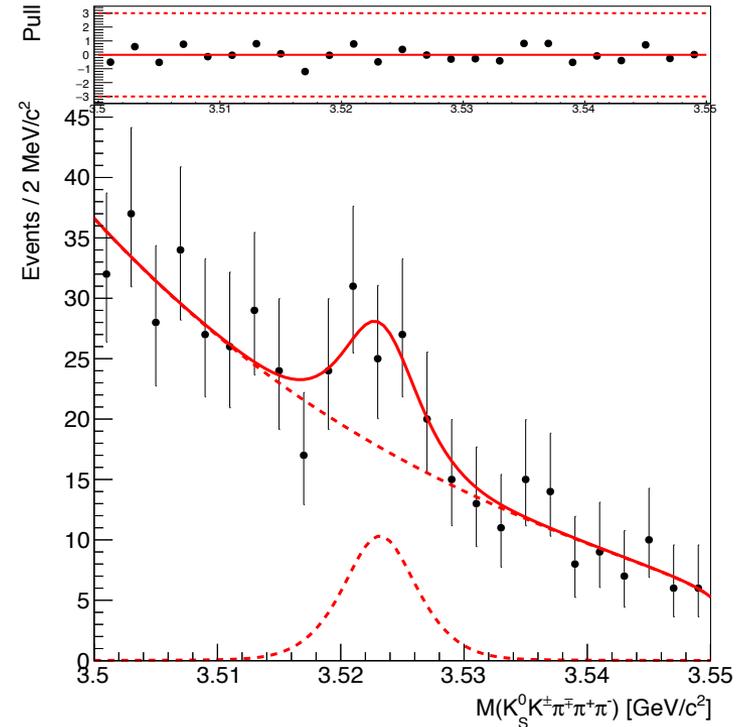
# Determination of branching fraction of $h_c \rightarrow K_S^0 K^\pm \pi^\mp \pi^+ \pi^-$

## Resolution

$$= \begin{cases} e^{-\frac{\sigma_L^2}{2} + \sigma_L \left(\frac{m-\mu}{\sigma}\right)^2}, & \frac{m-\mu}{\sigma} \leq -\sigma_L \\ e^{-\frac{1}{2} \left(\frac{m-\mu}{\sigma}\right)^2}, & -\sigma_L < \frac{m-\mu}{\sigma} \leq \sigma_H \\ e^{-\frac{\sigma_H^2}{2} - \sigma_H \left(\frac{m-\mu}{\sigma}\right)^2}, & \sigma_H < \frac{m-\mu}{\sigma} \end{cases} + 2 \text{ Gaussian}$$



## Breit-Wigner $\otimes$ Resolution + Argus



$$\text{BF}(h_c \rightarrow K_S^0 K^\pm \pi^\mp \pi^+ \pi^-)$$

$$= (7.6 \pm 1.7 \pm 0.9 \pm 1.1) \cdot 10^{-3}$$

Significance calculated to  $3.2\sigma$

# Overview of Selection Criteria

| final state                       | $\chi_{\text{NC}}^2$ | $M(\pi_1^0 \pi_2^0)_{\text{Rec}}$ | J/ $\psi$ Veto on             |                        | Veto on |            |            | $\pi^0$ Veto on |                   |
|-----------------------------------|----------------------|-----------------------------------|-------------------------------|------------------------|---------|------------|------------|-----------------|-------------------|
|                                   |                      |                                   | $M(\pi^+ \pi^-)_{\text{Rec}}$ | $M(\eta)_{\text{Rec}}$ | $\eta$  | $\omega$   | $K^{*\pm}$ | $K_S^0$         | $M(\gamma\gamma)$ |
| $K^+ K^- \pi^+ \pi^- \pi^0$       | ✓                    | ✓                                 | ✓                             |                        | ✓       | ✓          | ✓          |                 |                   |
| $K_S^0 K^\pm \pi^\mp \pi^+ \pi^-$ | ✓                    |                                   | ✓                             |                        | ✓       | ✓          | ✓          | ✓               |                   |
| $\pi^+ \pi^- \pi^0 \eta$          | ✓                    | ✓                                 |                               | ✓                      | ✓       |            |            |                 | ✓                 |
| $2(K^+ K^-) \pi^0$                | ✓                    | ✓                                 |                               |                        |         |            | ✓          |                 |                   |
| $K^+ K^- \pi^0$                   | ✓                    | ✓                                 |                               |                        |         |            | ✓          |                 |                   |
| $K^+ K^- \eta$                    | ✓                    |                                   |                               |                        |         |            |            |                 | ✓                 |
| $K^+ K^- \pi^0 \eta$              | ✓                    | ✓                                 |                               | ✓                      |         |            |            |                 |                   |
| $K^+ K^- \pi^+ \pi^- \eta$        | ✓                    |                                   | ✓                             | ✓                      |         |            | ✓          |                 | ✓                 |
| $K_S^0 K^\pm \pi^\mp$             | ✓                    |                                   | ✓                             |                        |         |            | ✓          |                 |                   |
|                                   |                      |                                   |                               |                        | $\eta$  | $\Delta^+$ | $\Sigma^+$ |                 |                   |
| $p\bar{p} \pi^0 \pi^0$            | ✓                    | ✓                                 |                               |                        | ✓       | ✓          | ✓          |                 | ✓                 |

- Limit Goodness of kinematic fit to suppress background
- Veto  $J/\psi$  in recoil systems
- $\pi^0$  from  $\psi'$  decay should not from other resonances
- avoid fake  $\pi^0$

# Overview of Selection Criteria

| final state                       | $\chi_{\text{NC}}^2$ | J/ $\psi$ Veto on                 |                               | Veto on                |        |            | $\pi^0$ Veto on |         |
|-----------------------------------|----------------------|-----------------------------------|-------------------------------|------------------------|--------|------------|-----------------|---------|
|                                   |                      | $M(\pi_1^0 \pi_2^0)_{\text{Rec}}$ | $M(\pi^+ \pi^-)_{\text{Rec}}$ | $M(\eta)_{\text{Rec}}$ | $\eta$ | $\omega$   | $K^{*\pm}$      | $K_S^0$ |
| $K^+ K^- \pi^+ \pi^- \pi^0$       | ✓                    | ✓                                 | ✓                             |                        | ✓      | ✓          | ✓               |         |
| $K_S^0 K^\pm \pi^\mp \pi^+ \pi^-$ | ✓                    |                                   | ✓                             |                        | ✓      | ✓          | ✓               |         |
| $\pi^+ \pi^- \pi^0 \eta$          | ✓                    | ✓                                 |                               | ✓                      | ✓      |            |                 | ✓       |
| $2(K^+ K^-) \pi^0$                | ✓                    | ✓                                 |                               |                        |        |            | ✓               |         |
| $K^+ K^- \pi^0$                   | ✓                    | ✓                                 |                               |                        |        |            | ✓               |         |
| $K^+ K^- \eta$                    | ✓                    |                                   |                               |                        |        |            |                 | ✓       |
| $K^+ K^- \pi^0 \eta$              | ✓                    | ✓                                 |                               | ✓                      |        |            |                 |         |
| $K^+ K^- \pi^+ \pi^- \eta$        | ✓                    |                                   | ✓                             | ✓                      |        |            | ✓               | ✓       |
| $K_S^0 K^\pm \pi^\mp$             | ✓                    |                                   | ✓                             |                        |        |            | ✓               |         |
|                                   |                      |                                   |                               |                        | $\eta$ | $\Delta^+$ | $\Sigma^+$      |         |
| $p\bar{p} \pi^0 \pi^0$            | ✓                    | ✓                                 |                               |                        | ✓      | ✓          | ✓               | ✓       |

- Limit Goodness of kinematic fit to suppress background
- Veto  $J/\psi$  in recoil systems
- $\pi^0$  from  $\psi'$  decay should not from other resonances
- avoid fake  $\pi^0$

# Overview of Selection Criteria

| final state                       | $\chi_{\text{NC}}^2$ | J/ $\psi$ Veto on                 |                               |                        | Veto on |            |            | $\pi^0$ Veto on |                   |
|-----------------------------------|----------------------|-----------------------------------|-------------------------------|------------------------|---------|------------|------------|-----------------|-------------------|
|                                   |                      | $M(\pi_1^0 \pi_2^0)_{\text{Rec}}$ | $M(\pi^+ \pi^-)_{\text{Rec}}$ | $M(\eta)_{\text{Rec}}$ | $\eta$  | $\omega$   | $K^{*\pm}$ | $K_S^0$         | $M(\gamma\gamma)$ |
| $K^+ K^- \pi^+ \pi^- \pi^0$       | ✓                    | ✓                                 | ✓                             |                        | ✓       | ✓          | ✓          |                 |                   |
| $K_S^0 K^\pm \pi^\mp \pi^+ \pi^-$ | ✓                    |                                   | ✓                             |                        | ✓       | ✓          | ✓          | ✓               |                   |
| $\pi^+ \pi^- \pi^0 \eta$          | ✓                    | ✓                                 |                               | ✓                      | ✓       |            |            |                 | ✓                 |
| $2(K^+ K^-) \pi^0$                | ✓                    | ✓                                 |                               |                        |         |            | ✓          |                 |                   |
| $K^+ K^- \pi^0$                   | ✓                    | ✓                                 |                               |                        |         |            | ✓          |                 |                   |
| $K^+ K^- \eta$                    | ✓                    |                                   |                               |                        |         |            |            |                 | ✓                 |
| $K^+ K^- \pi^0 \eta$              | ✓                    | ✓                                 |                               | ✓                      |         |            |            |                 |                   |
| $K^+ K^- \pi^+ \pi^- \eta$        | ✓                    |                                   | ✓                             | ✓                      |         |            | ✓          |                 | ✓                 |
| $K_S^0 K^\pm \pi^\mp$             | ✓                    |                                   | ✓                             |                        |         |            | ✓          |                 |                   |
|                                   |                      |                                   |                               |                        | $\eta$  | $\Delta^+$ | $\Sigma^+$ |                 |                   |
| $p\bar{p} \pi^0 \pi^0$            | ✓                    | ✓                                 |                               |                        | ✓       | ✓          | ✓          |                 | ✓                 |

- Limit Goodness of kinematic fit to suppress background
- Veto  $J/\psi$  in recoil systems
- $\pi^0$  from  $\psi'$  decay should not from other resonances
- avoid fake  $\pi^0$

# Overview of Selection Criteria

| final state  | $\chi_{\text{NC}}^2$ | J/ $\psi$ Veto on                     |                                   |                            | Veto on |            |                                |                             | $\pi^0$ Veto on<br>M( $\gamma\gamma$ ) |
|--|----------------------|---------------------------------------|-----------------------------------|----------------------------|---------|------------|--------------------------------|-----------------------------|--|
|  |                      | M( $\pi_1^0 \pi_2^0$ ) <sub>Rec</sub> | M( $\pi^+ \pi^-$ ) <sub>Rec</sub> | M( $\eta$ ) <sub>Rec</sub> | $\eta$  | $\omega$   | K <sup>*<math>\pm</math></sup> | K <sub>S</sub> <sup>0</sup> |  |
| K <sup>+</sup> K <sup>-</sup> $\pi^+ \pi^- \pi^0$                | ✓                    | ✓                                     | ✓                                 |                            | ✓       | ✓          | ✓                              |                             |  |
| K <sub>S</sub> <sup>0</sup> K <sup>±</sup> $\pi^\mp \pi^+ \pi^-$ | ✓                    |                                       | ✓                                 |                            | ✓       | ✓          | ✓                              | ✓                           |  |
| $\pi^+ \pi^- \pi^0 \eta$   | ✓                    | ✓                                     |                                   | ✓                          | ✓       |            |                                |                             | ✓                                      |
| 2(K <sup>+</sup> K <sup>-</sup> ) $\pi^0$                        | ✓                    | ✓                                     |                                   |                            |         |            | ✓                              |                             |  |
| K <sup>+</sup> K <sup>-</sup> $\pi^0$                            | ✓                    | ✓                                     |                                   |                            |         |            | ✓                              |                             |  |
| K <sup>+</sup> K <sup>-</sup> $\eta$                             | ✓                    |                                       |                                   |                            |         |            |                                |                             | ✓                                      |
| K <sup>+</sup> K <sup>-</sup> $\pi^0 \eta$                       | ✓                    | ✓                                     |                                   | ✓                          |         |            |                                |                             |  |
| K <sup>+</sup> K <sup>-</sup> $\pi^+ \pi^- \eta$                 | ✓                    |                                       | ✓                                 | ✓                          |         |            | ✓                              |                             | ✓                                      |
| K <sub>S</sub> <sup>0</sup> K <sup>±</sup> $\pi^\mp$             | ✓                    |                                       | ✓                                 |                            |         |            | ✓                              |                             |  |
|  |                      |                                       |                                   |                            | $\eta$  | $\Delta^+$ | $\Sigma^+$                     |                             |  |
| p $\bar{p} \pi^0 \pi^0$  | ✓                    | ✓                                     |                                   |                            | ✓       | ✓          | ✓                              |                             | ✓                                      |

- Limit Goodness of kinematic fit to suppress background
- Veto  $J/\psi$  in recoil systems
- $\pi^0$  from  $\psi'$  decay should not from other resonances
- avoid fake  $\pi^0$

# Overview of Selection Criteria

| final state                       | $\chi_{\text{NC}}^2$ | J/ $\psi$ Veto on                 |                               |                        | Veto on |            |            |         | $\pi^0$ Veto on   |
|-----------------------------------|----------------------|-----------------------------------|-------------------------------|------------------------|---------|------------|------------|---------|-------------------|
|                                   |                      | $M(\pi_1^0 \pi_2^0)_{\text{Rec}}$ | $M(\pi^+ \pi^-)_{\text{Rec}}$ | $M(\eta)_{\text{Rec}}$ | $\eta$  | $\omega$   | $K^{*\pm}$ | $K_S^0$ | $M(\gamma\gamma)$ |
| $K^+ K^- \pi^+ \pi^- \pi^0$       | ✓                    | ✓                                 | ✓                             |                        | ✓       | ✓          | ✓          |         |                   |
| $K_S^0 K^\pm \pi^\mp \pi^+ \pi^-$ | ✓                    |                                   | ✓                             |                        | ✓       | ✓          | ✓          | ✓       |                   |
| $\pi^+ \pi^- \pi^0 \eta$          | ✓                    | ✓                                 |                               | ✓                      | ✓       |            |            |         | ✓                 |
| $2(K^+ K^-) \pi^0$                | ✓                    | ✓                                 |                               |                        |         |            | ✓          |         |                   |
| $K^+ K^- \pi^0$                   | ✓                    | ✓                                 |                               |                        |         |            | ✓          |         |                   |
| $K^+ K^- \eta$                    | ✓                    |                                   |                               |                        |         |            |            |         | ✓                 |
| $K^+ K^- \pi^0 \eta$              | ✓                    | ✓                                 |                               | ✓                      |         |            |            |         |                   |
| $K^+ K^- \pi^+ \pi^- \eta$        | ✓                    |                                   | ✓                             | ✓                      |         |            | ✓          |         | ✓                 |
| $K_S^0 K^\pm \pi^\mp$             | ✓                    |                                   | ✓                             |                        |         |            | ✓          |         |                   |
|                                   |                      |                                   |                               |                        | $\eta$  | $\Delta^+$ | $\Sigma^+$ |         |                   |
| $p\bar{p} \pi^0 \pi^0$            | ✓                    | ✓                                 |                               |                        | ✓       | ✓          | ✓          |         | ✓                 |

- Limit Goodness of kinematic fit to suppress background
- Veto  $J/\psi$  in recoil systems
- $\pi^0$  from  $\psi'$  decay should not from other resonances
- avoid fake  $\pi^0$

# Determination of Upper Limits

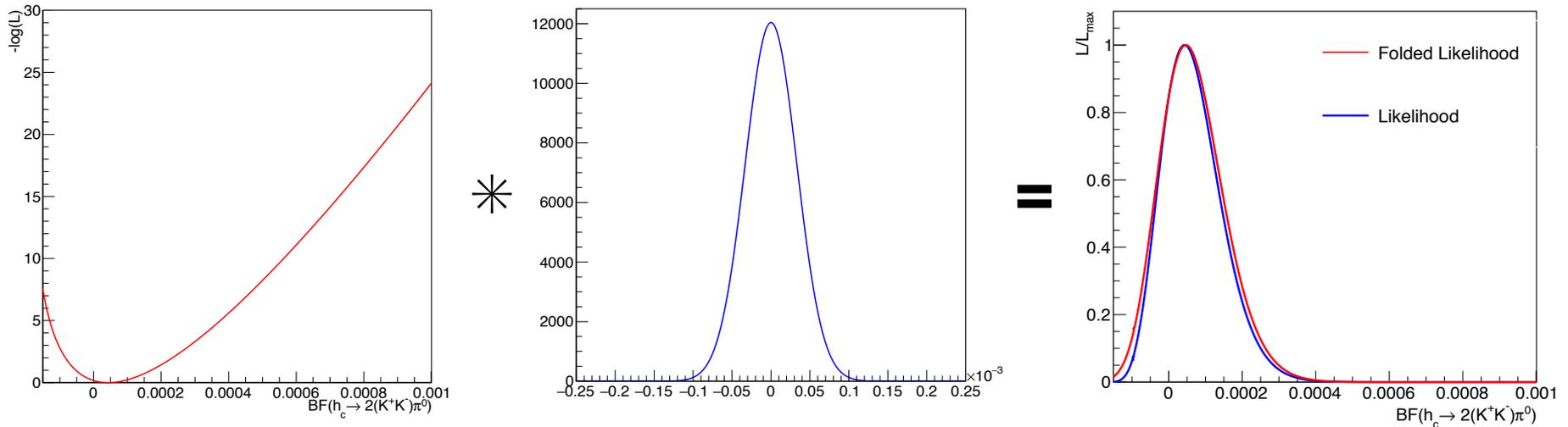
- Using Bayesian method:

$$0.9 = \sum_{\theta_0 \leq \theta_{up}} d\theta_0 \mathbb{P}(\theta = \theta_0 | x) = \frac{\int_{\theta_0 \leq \theta_{up}} d\theta_0 \mathcal{L}(x|\theta_0) \mathbb{P}(\theta = \theta_0)}{\int_{\theta' \in \Theta} d\theta' \mathcal{L}(x|\theta') \mathbb{P}(\theta = \theta')}$$

- Taking systematic uncertainties into account by folding the likelihood with a gaussian distribution

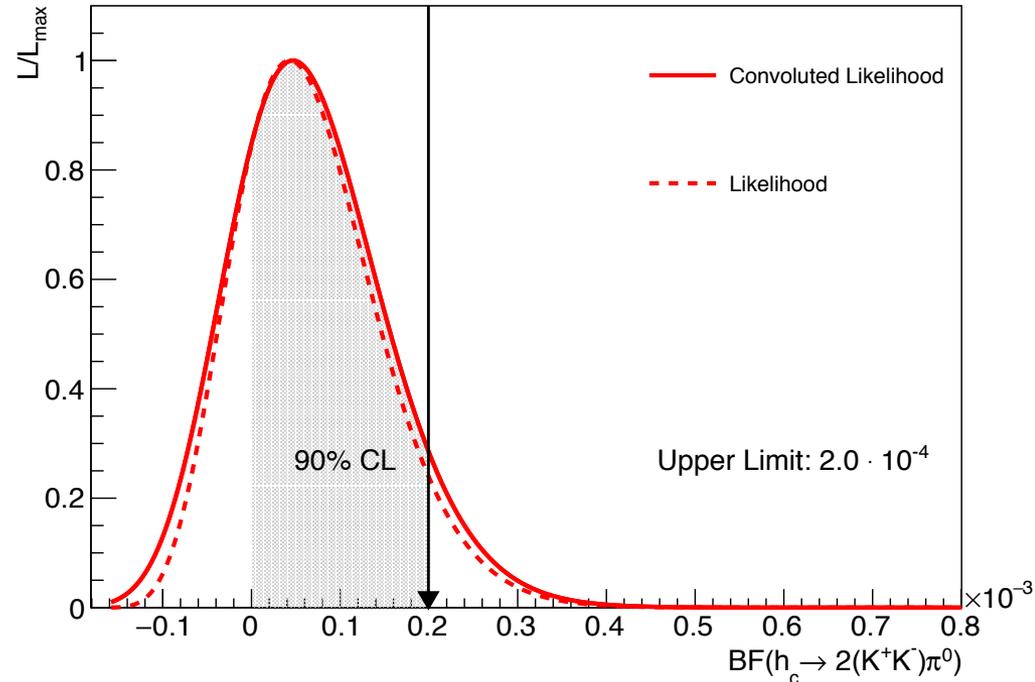
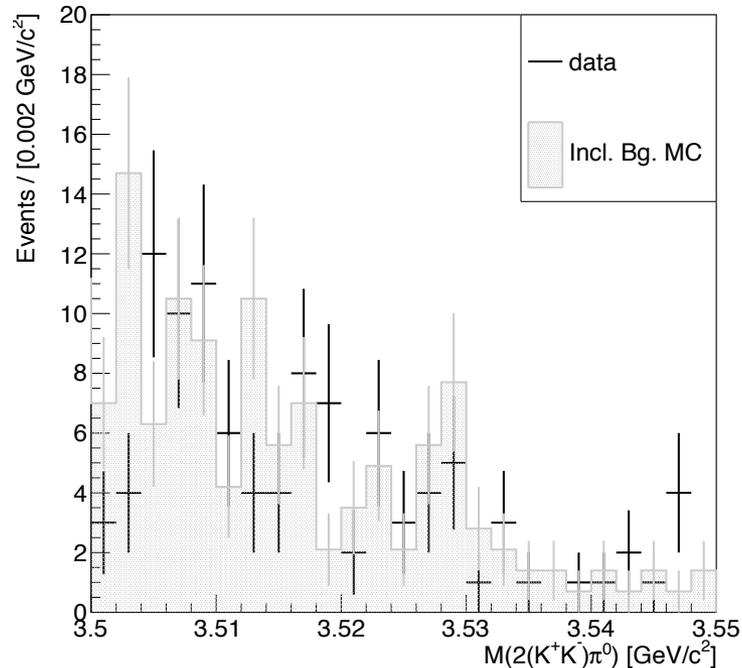
Replace  $\mathcal{L}(x|\theta)$  by

$$\mathcal{L}_{sys}(x|\theta) = \int dx'_i \mathcal{L}(x_1, x_2, \dots, x'_i, \dots, x_k | \theta) \cdot G(x_i - x'_i, \mu_i, \Delta x_i), \quad x_i \text{ fehlerbehaftete Gr\u00f6\u00dfe mit Fehler } \Delta x_i$$



# At the Example of $h_c \rightarrow 2(K^+K^-)\pi^0$

- After applying all selection criteria, no evidence for a signal contribution is visible!

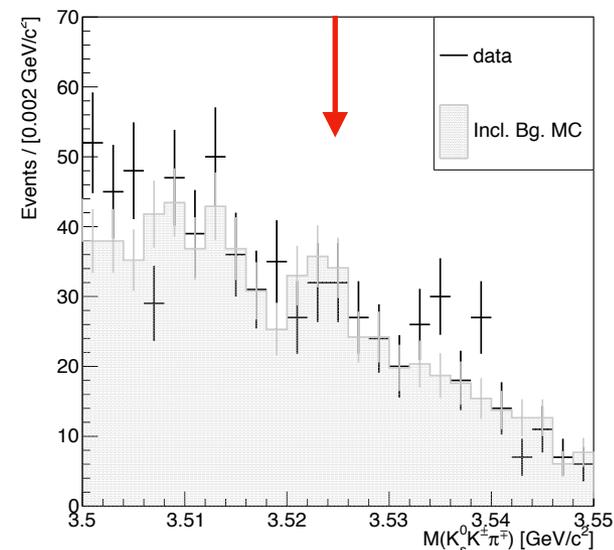
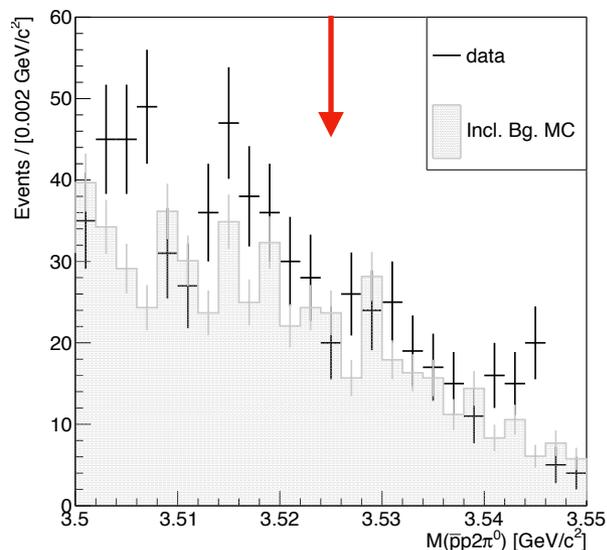
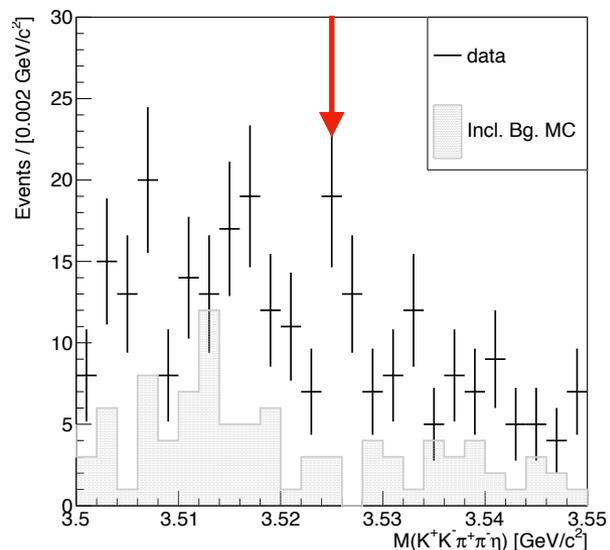
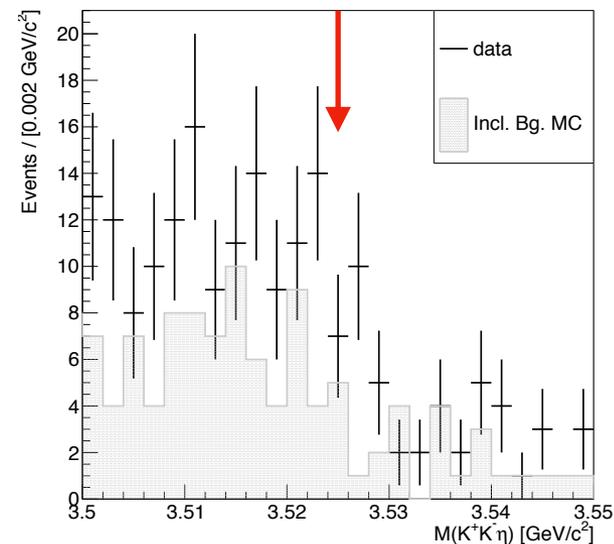
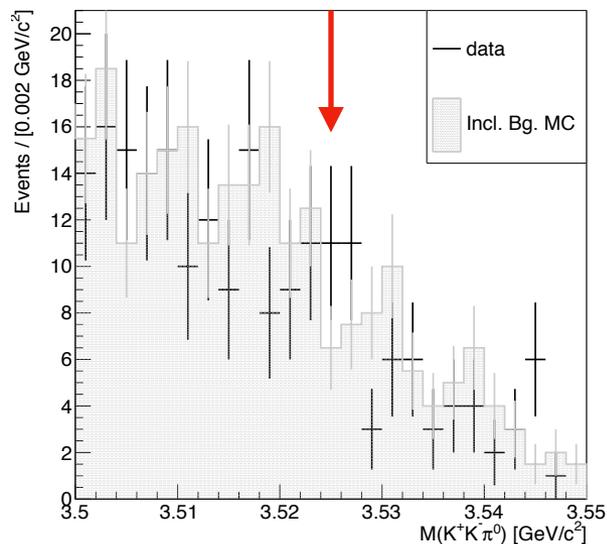
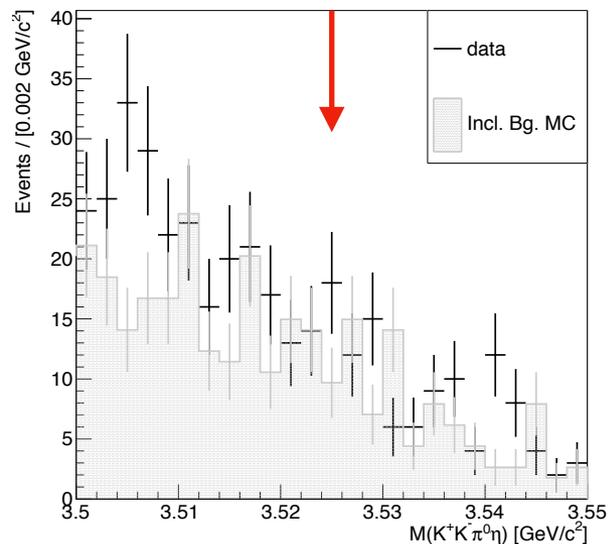


→ determine an upper limit

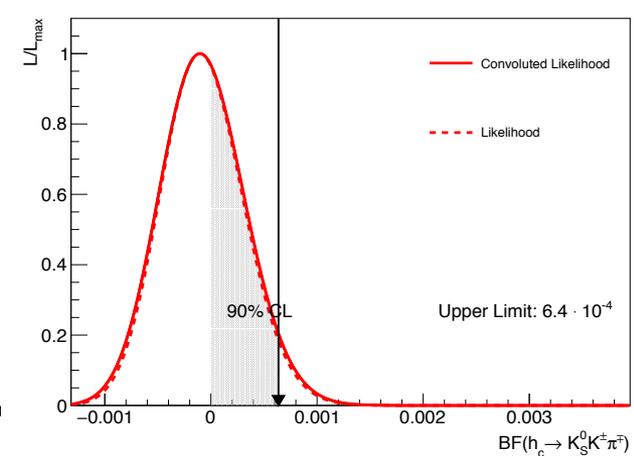
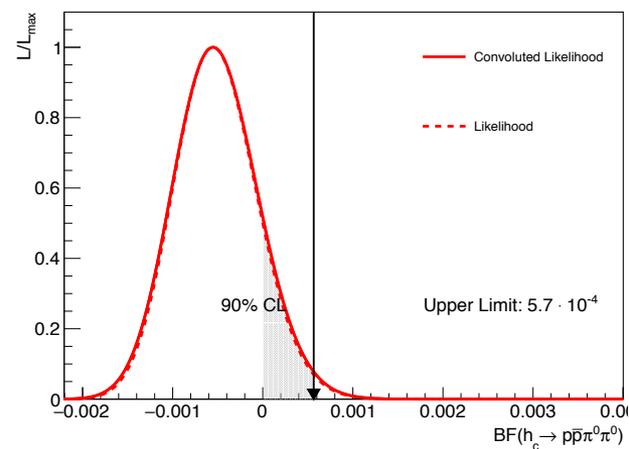
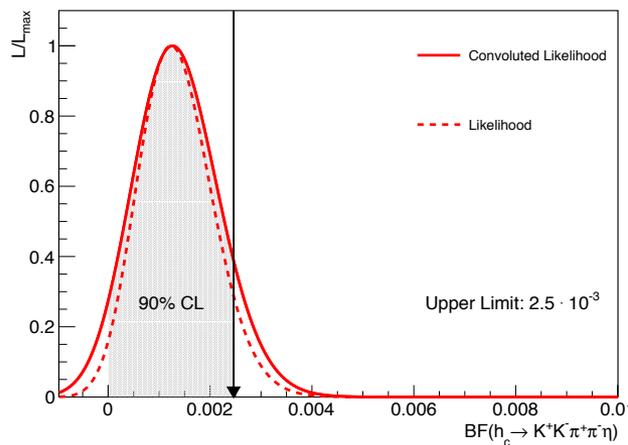
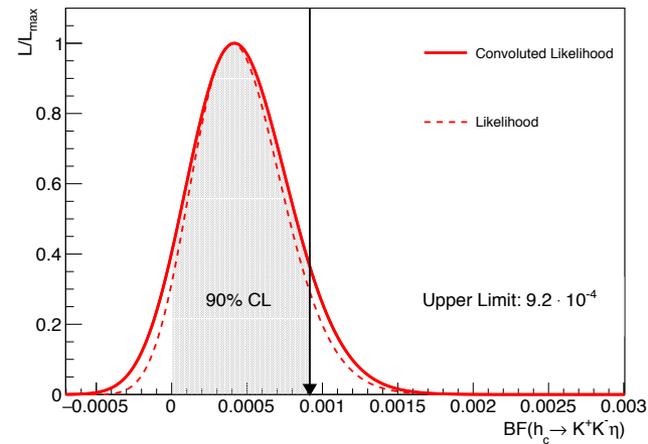
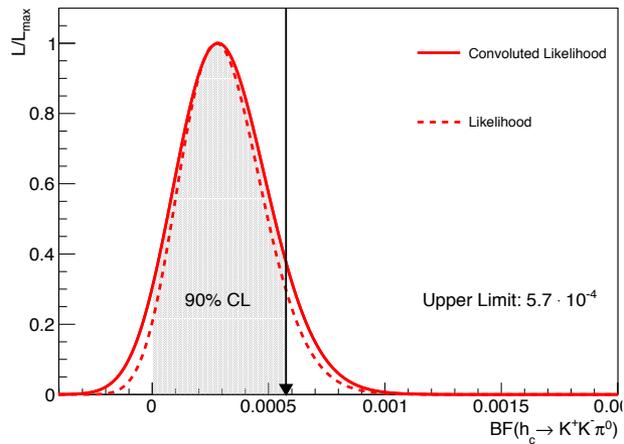
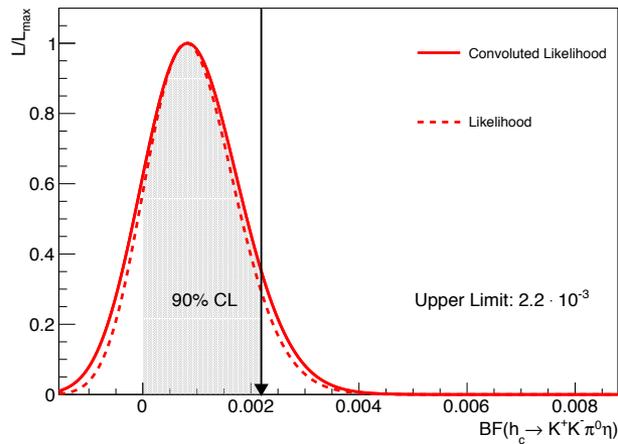
$$\text{BF}(h_c \rightarrow 2(K^+K^-)\pi^0) < 2.0 \cdot 10^{-4}$$

- systematic uncertainty of 18.5% taken into account

# Same Procedure for other Final States



# Same Procedure for other Final States



# Summary and Outlook

- In total 10 final states have been analyzed which have never been measured before
- It was possible to find hints for 3 new decay modes of the  $h_c$
- Furthermore indications for contributing intermediate resonances have been found for  $h_c \rightarrow K^+K^-\pi^+\pi^-\pi^0$
- For all other final states upper limits have been determined
- Comprehensive systematic studies have been performed for all final states

| final state                   | BF( $h_c \rightarrow X$ )                     |
|-------------------------------|---|
| $K^+K^-\pi^+\pi^-\pi^0$       | $(3.3 \pm 0.4 \pm 0.3 \pm 0.5) \cdot 10^{-3}$ |
| $K_S^0K^\pm\pi^\mp\pi^+\pi^-$ | $(7.6 \pm 1.7 \pm 0.9 \pm 1.1) \cdot 10^{-3}$ |
| $\pi^+\pi^-\pi^0\eta$         | $(7.3 \pm 1.9 \pm 0.8 \pm 1.1) \cdot 10^{-3}$ |
| $2(K^+K^-\pi^0)$              | $< 2.0 \cdot 10^{-4}$                         |
| $K^+K^-\pi^0$                 | $< 5.7 \cdot 10^{-4}$                         |
| $K^+K^-\eta$                  | $< 9.2 \cdot 10^{-4}$                         |
| $K^+K^-\pi^0\eta$             | $< 2.2 \cdot 10^{-3}$                         |
| $K^+K^-\pi^+\pi^-\eta$        | $< 2.5 \cdot 10^{-3}$                         |
| $K_S^0K^\pm\pi^\mp$           | $< 6.4 \cdot 10^{-4}$                         |
| $p\bar{p}\pi^0\pi^0$          | $< 5.7 \cdot 10^{-4}$                         |

- Looking forward to taking further steps!



*Thank You!*

# Overview of Systematic Uncertainties

| final state                   | PID and reconstruction | selection | kinematic fit | efficiency | fit | BF   | $\sqrt{\sum \Delta_i^2}$ |
|-------------------------------|------------------------|-----------|---------------|------------|-----|------|--------------------------|
| $K^+K^-\pi^+\pi^-\pi^0$       | 7.2                    | 5.7       | 1.5           | 5.1        | 2.7 | 15.1 | 18.7                     |
| $\pi^+\pi^-\pi^0\eta$         | 7.3                    | 5.4       | 2.1           | 6.3        | 2.8 | 15.1 | 19                       |
| $2(K^+K^-\pi^0)$              | 7.2                    | 4.7       | 2.3           | 5.2        | 3.7 | 15.1 | 18.7                     |
| $K^+K^-\pi^0$                 | 5.3                    | 4.2       | 1.9           | 4.1        | 3.8 | 15.1 | 17.6                     |
| $K^+K^-\eta$                  | 5.3                    | 3.5       | 1.9           | 3.7        | 3.4 | 15.1 | 17.2                     |
| $K^+K^-\pi^0\eta$             | 7.3                    | 3.9       | 2             | 4.5        | 4   | 15.1 | 18.4                     |
| $K^+K^-\pi^+\pi^-\eta$        | 7.2                    | 5         | 1.6           | 3.4        | 4.7 | 15.1 | 18.5                     |
| $K_S^0K^\pm\pi^\mp$           | 6.4                    | 4.4       | 2.1           | 4          | 3.4 | 15.1 | 17.9                     |
| $K_S^0K^\pm\pi^\mp\pi^+\pi^-$ | 9                      | 4.5       | 3.9           | 5.3        | 4   | 15.1 | 19.7                     |
| $p\bar{p}\pi^0\pi^0$          | 7.3                    | 6.1       | 2.7           | 4.9        | 3.3 | 15.1 | 19                       |