



university of  
 groningen

faculty of science  
 and engineering

van swinderen institute for  
 particle physics and gravity

# cLFV in Meson Decays

– at high energy colliders –



中國科學院高能物理研究所  
*Institute of High Energy Physics*  
*Chinese Academy of Sciences*

Gerco Onderwater

International School on cLFV 2019 – IHEP Beijing

# Who am I?

**1993-1998 : VU/NIKHEF Amsterdam**

Hadron group at the AmPS facility

**1998-2004 : Univ. of Illinois at Urbana-Champaign**

Precision Physics Group

Several low-energy “precision” experiments,  
incl. muon  $g-2$ , EDM & lifetime @ BNL & PSI

**2004-now : Univ. of Groningen**

**Van Swinderen Institute for Particle Physics & Gravity**

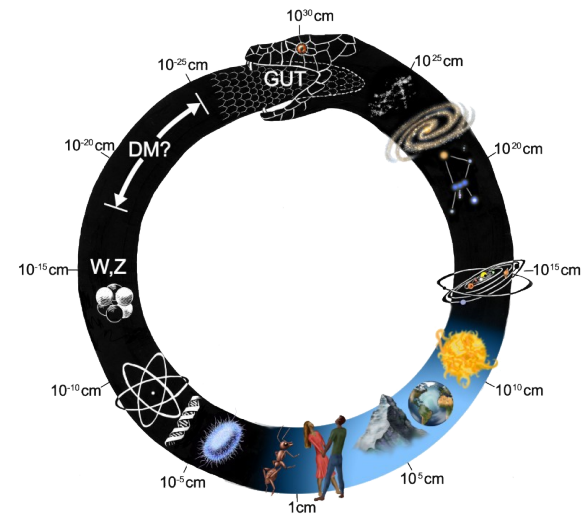
Experimental Particle Physics Group

**C, P, & T**: EDM ( $\mu, p, d, Ra, Xe$ ),  $Ra^+APV$ ,  $\beta$ -decay, SrF

**LIV** :  $^{20}Na$  &  $\Lambda$ -decay,  $d\tau/d\Omega$

**LFV** :  $B_{(s)} \rightarrow e\mu$ ,  $\Lambda_b \rightarrow \Lambda e\mu$

**LU** : Muon  $g-2$





# My research



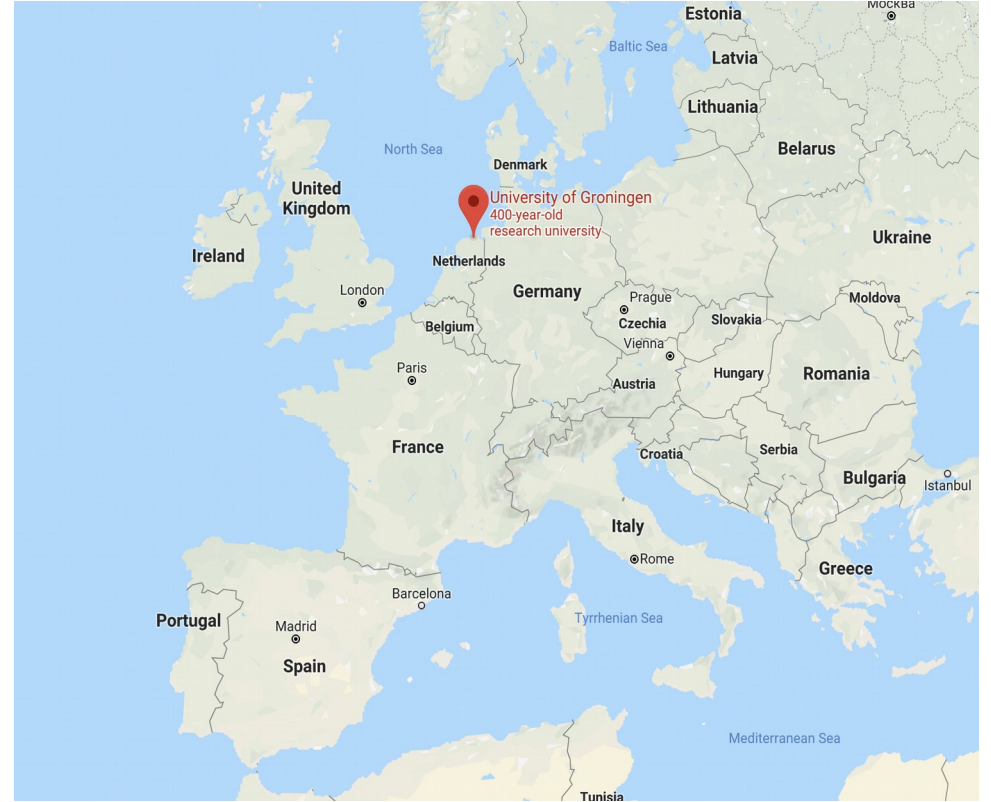
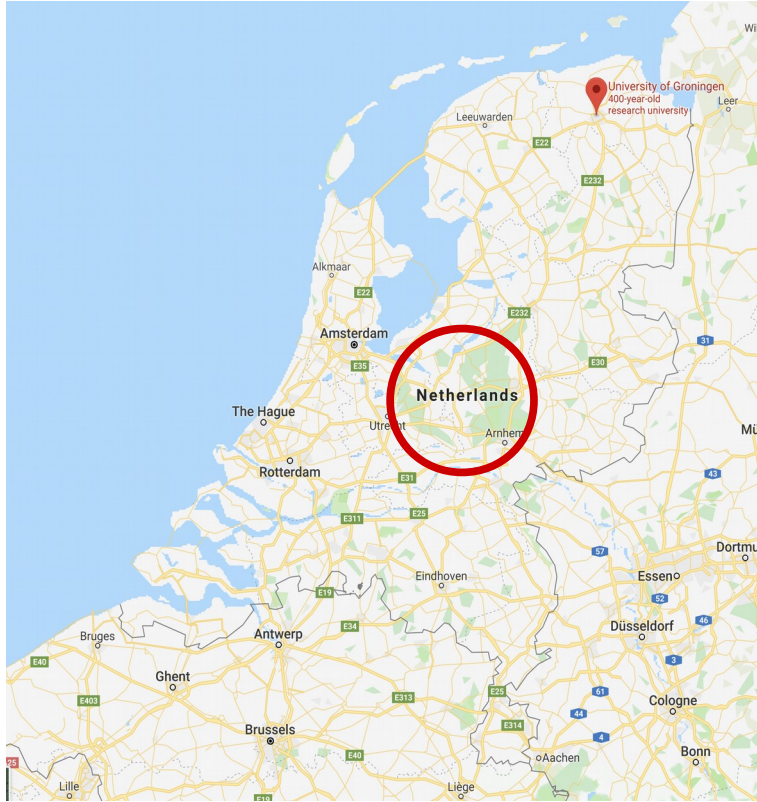


# University of Groningen





# Groningen, the Netherlands



# Outline

## Goal

by the end of my lectures, you can formulate how cLFV appears in meson decays, what the essential steps are in the experimental searches, and how to interpret the result in relation to other cLFV searches

## Topics to cover

cLFV in meson & baryon decay

Sensitivity & Selectivity

Hadron production

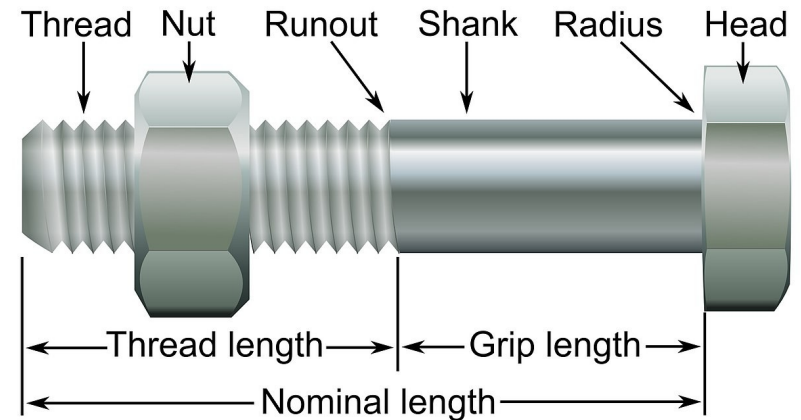
Particle identification

Signal & background: invariant mass spectrum

Normalisation

Efficiency

Interpretation





# cLFV in hadron decay

# Convention

e

$\mu$

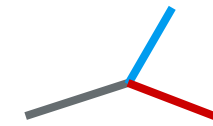
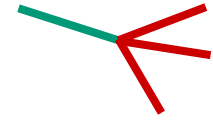
T



# Towards studying (c)LFV

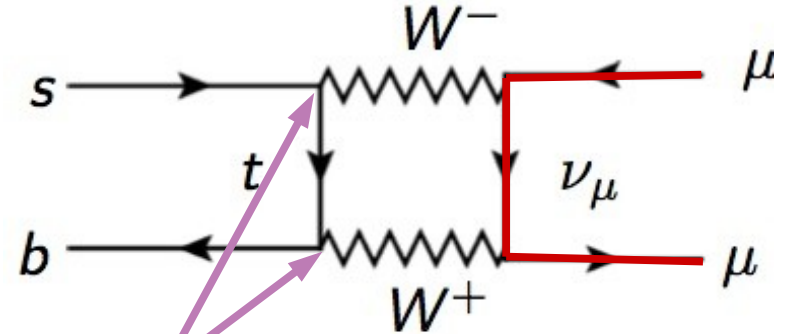
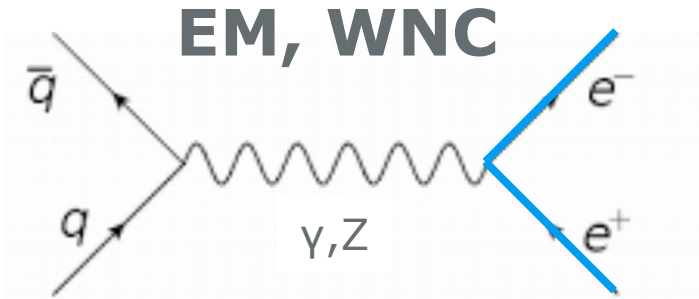
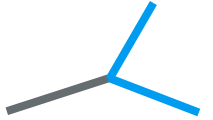
----- Lorenzo Calibbi -----

<b>Decay</b>	<i>Angela Papa Kiyoshi Hayasaka</i> $\mu \rightarrow e\gamma, \mu \rightarrow eee, \tau \rightarrow \mu\mu\mu, \tau \rightarrow \mu hh, \dots$
<b>Conversion</b>	$\mu A \rightarrow eA$ <i>David Hitlin</i>
<b>Production</b>	$B_s \rightarrow e\mu, B \rightarrow Ke\mu, \Lambda_b \rightarrow \Lambda e\mu, h^0 \rightarrow \mu\tau, \dots$
<b>Oscillation</b>	$\nu_e \leftrightarrow \nu_\mu \leftrightarrow \nu_\tau, M(\mu^+e^-) \leftrightarrow \bar{M}(\mu^-e^+)$
<b>Number violation</b>	$0\nu 2\beta, B^- \rightarrow \pi^+ \mu^- \mu^-, \dots$
<b>Non-Universality</b>	$\bar{B}^0 \rightarrow D^{*+} \tau^- \bar{\nu}_\tau$ vs $\bar{B}^0 \rightarrow D^{*+} \mu^- \bar{\nu}_\mu, g_e$ vs $g_\mu, \dots$ <i>Sébastien Descotes-Genon Tsutomu Mibe</i>

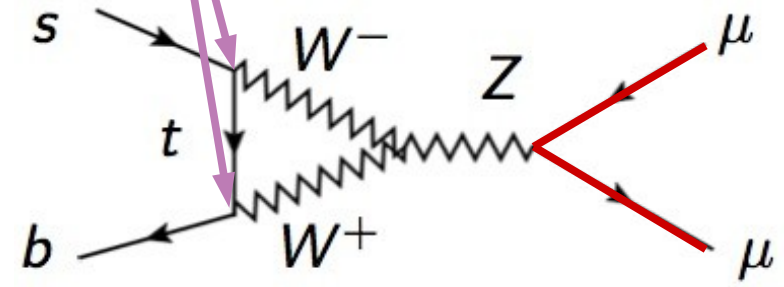
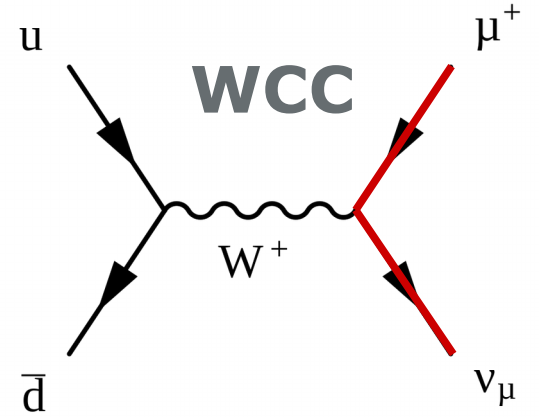


(charges dropped, unless relevant)

# Leptonic meson decay in SM

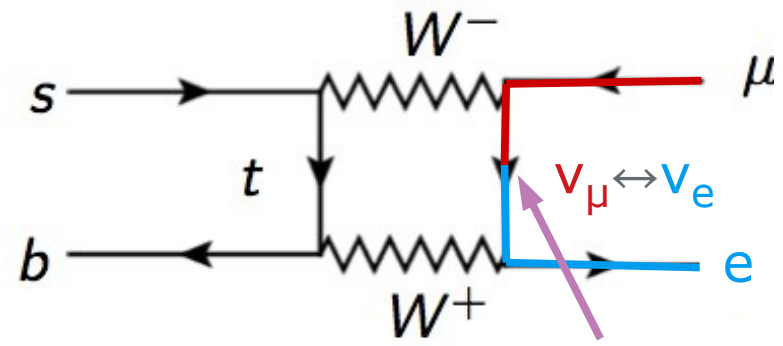
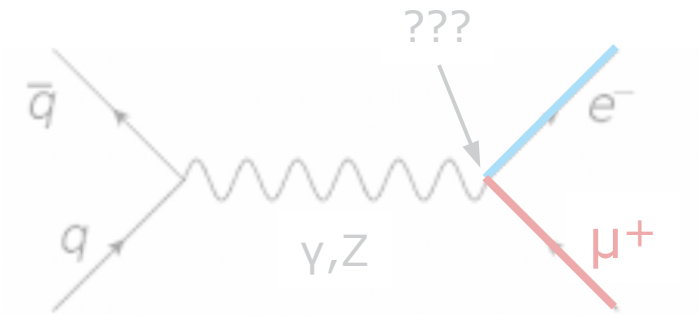
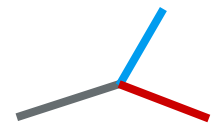


**CKM "FCNC"**

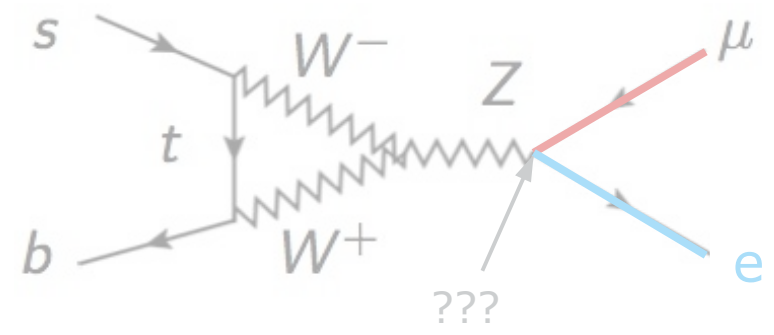
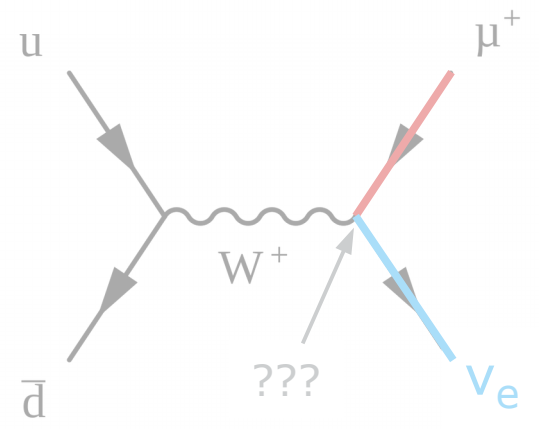




# Leptonic meson decay in SM



**PMNS**



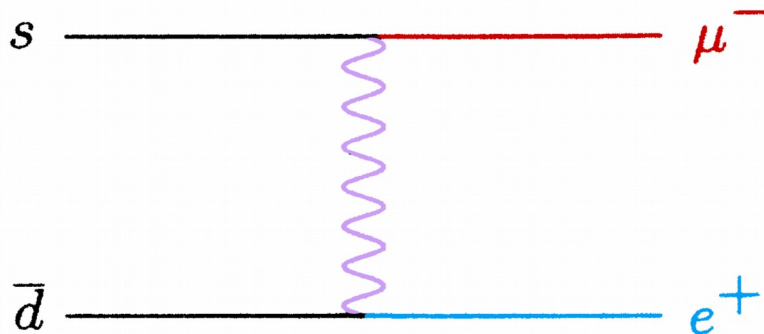
# Leptonic meson decay post-SM

## Standard Model cLFV

Only possible via neutrino oscillations  
 Unmeasureably small

## Beyond Standard Model Physics

(Too) many well-motivated possibilities  
 Many produce results within reach of experiment  
 Experiments put stringents limits on them  
*E.g.*, **quark-lepton unification**\* with lepto-quarks:



THERE ARE KNOWN KNOWNNS  
 THERE ARE THINGS THAT WE KNOW THAT WE KNOW, THERE ARE  
**KNOWN UNKNOWNNS**  
 THAT IS TO SAY, THERE ARE  
 THINGS THAT WE NOW KNOW WE DON'T KNOW  
 BUT THERE ARE ALSO  
**UNKNOWN UNKNOWNNS**  
 THERE ARE THINGS  
**WE DO NOT KNOW**  
**WE DON'T KNOW**  
 AND EACH YEAR WE DISCOVER  
 A FEW MORE OF THOSE  
**UNKNOWN**  
**UNKNOWNNS**

\*<https://doi.org/10.1103/PhysRevD.50.6843>

# Sensitivity & Selectivity

# Some definitions

In designing an experiment two properties to be considered:

## **Sensitivity**

Also known as *true positive rate*, *probability of detection*, or *efficiency*

“If the process occurs, what fraction of events do we actually see?”

In other words, your ability to identify and measure the signal

## **Selectivity**

Also known as *specificity*, or *true negative rate*

“If another process occurs, what fractions of events are labeled as such?”

In other words, your ability to identify and eliminate background

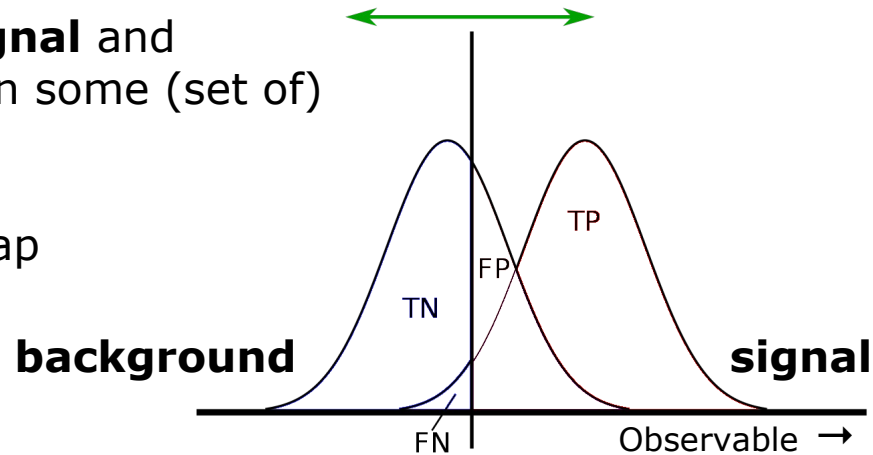
Typically **sensitivity** and **selectivity** are mutually exclusive



# Contingency table and ROC curve

Need to distinguish **signal** and **background**, based on some (set of) observable(s)

Signatures often overlap



# Contingency table and ROC curve

Need to distinguish **signal** and **background**, based on some (set of) observable(s)

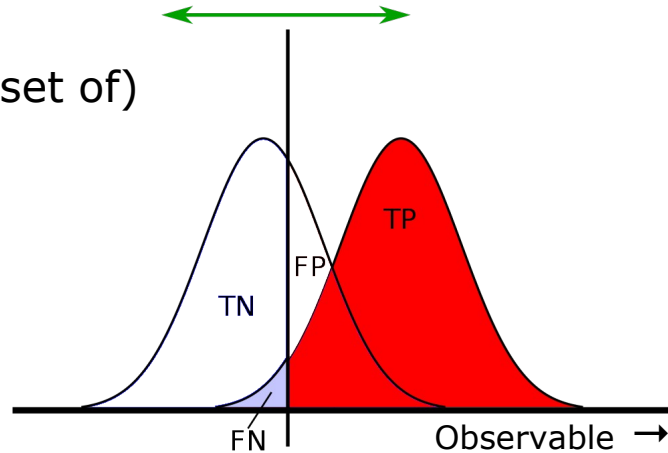
Signatures often overlap

**Goal**

Maximize **TRUE POSITIVE  $\eta$**

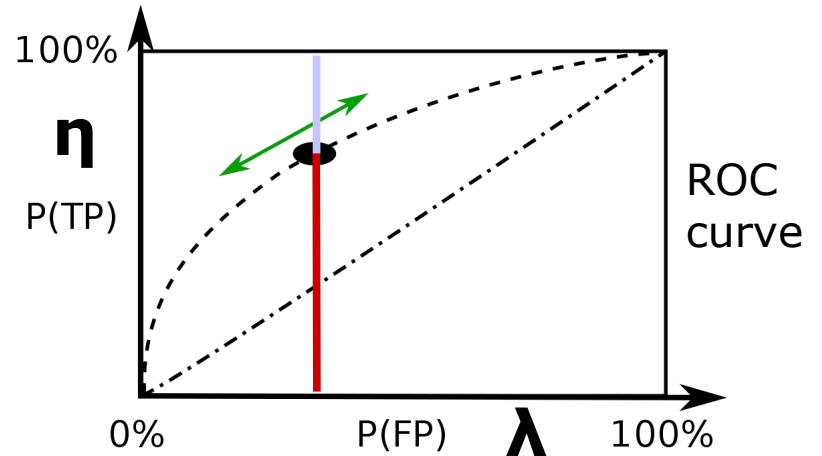
**Side effect**

Reduced efficiency (**FALSE NEGATIVE**)



TP	FP
FN	TN

contingency table



# Contingency table and ROC curve

Need to distinguish **signal** and **background**, based on some (set of) observable(s)

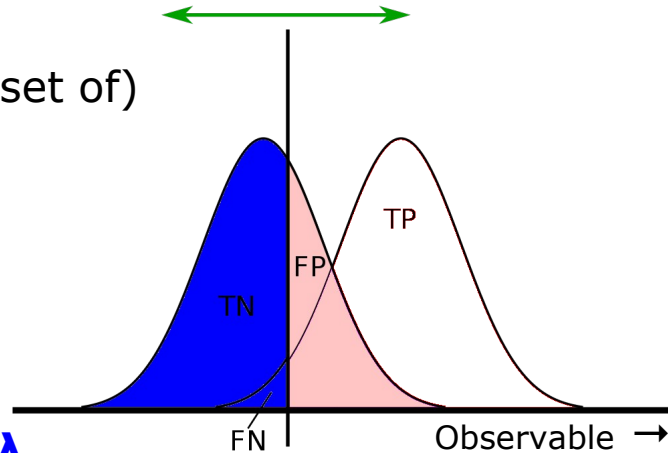
Signatures often overlap

## Goal

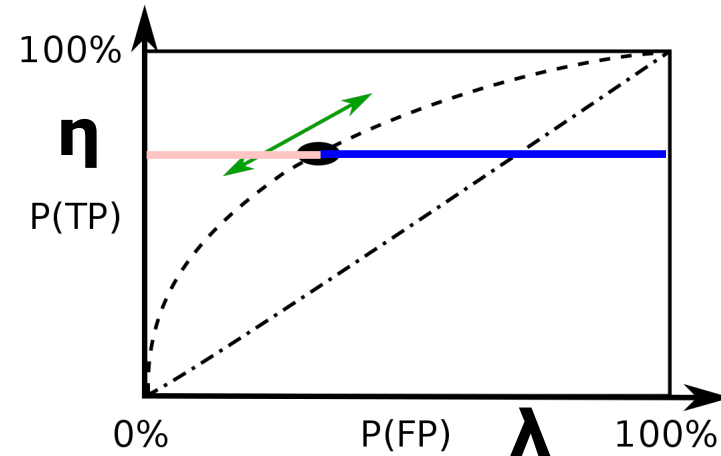
Maximize **TRUE POSITIVE  $\eta$**   
 Maximize **TRUE NEGATIVE  $1-\lambda$**

## Side effect

Reduced efficiency (**FALSE NEGATIVE**)  
 Noise leakage (**FALSE POSITIVE**)



TP	FP
FN	TN



# Contingency table and ROC curve

Need to distinguish **signal** and **background**, based on some (set of) observables

Signatures often overlap

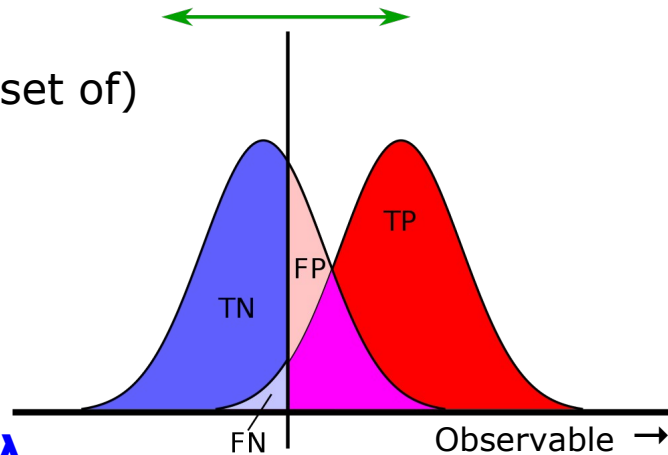
## Goal

Maximize **TRUE POSITIVE  $\eta$**   
 Maximize **TRUE NEGATIVE  $1-\lambda$**

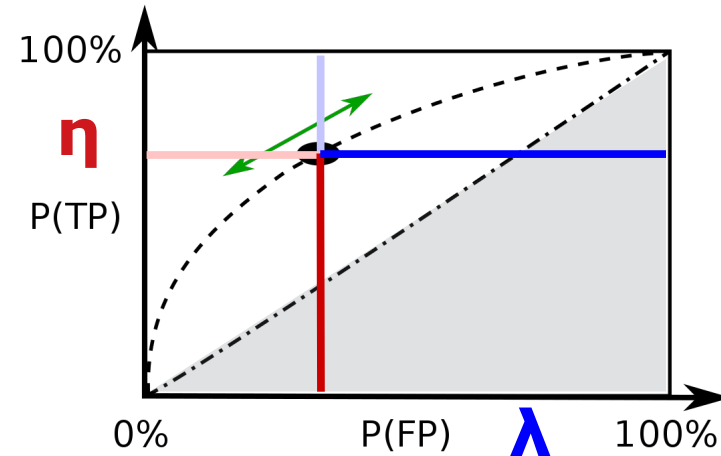
## Side effect

Reduced efficiency (**FALSE NEGATIVE**)  
 Noise leakage (**FALSE POSITIVE**)

**Need sophisticated optimization**



TP	FP
FN	TN
$\Sigma=1$	$\Sigma=1$





# Contingency table and ROC curve

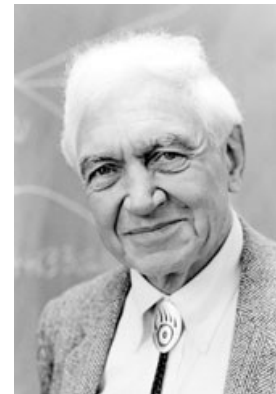
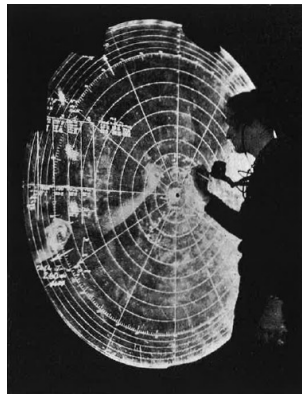
## Quiz 1

What does "ROC" stand for?

Answer: ROC = **R**eceiver **O**perating **C**haracteristic

## Quiz 2

What does this have to do with cLFV? Where does this name come from?



# Expected significance

## Signal estimation : $S$

Within signal window number of counts is measured

$$: N_S = \eta \cdot S + \lambda \cdot B$$

In an independent window the background is estimated

$$: N_B = k \cdot \lambda \cdot B$$

From these two together, the signal is estimated

$$: S = (N_S - N_B/k)/\eta$$

## Error estimation : $\sigma$

$$\text{Uncertainty} : \eta^2 \sigma^2(S) = \sigma^2(N_S) + \sigma^2(N_B)/k^2$$

$$= N_S + N_B/k^2$$

$$= (\eta \cdot S + \lambda \cdot B) + (\lambda \cdot B/k)$$

$$= \eta \cdot S + k' \cdot \lambda \cdot B$$

$$k' = 1 + 1/k$$

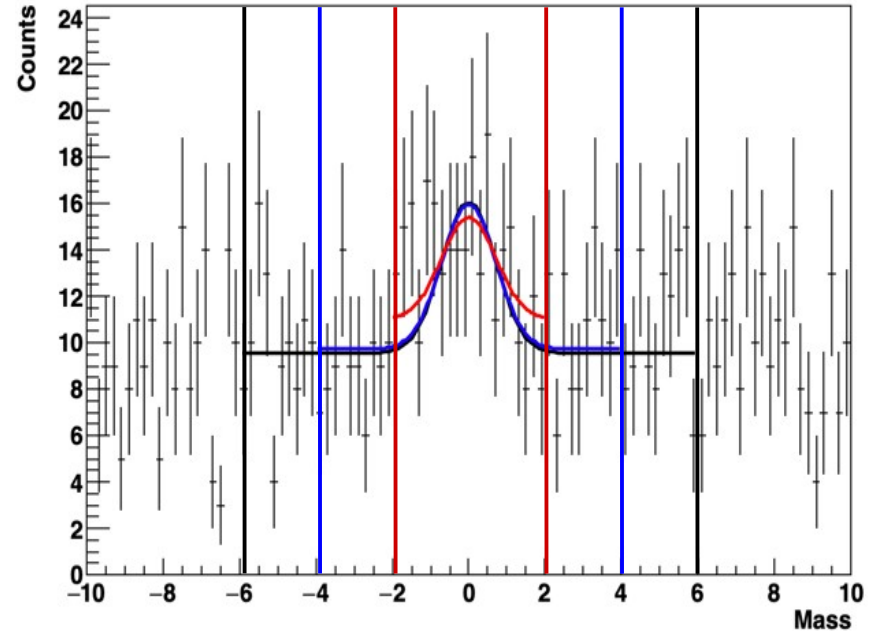
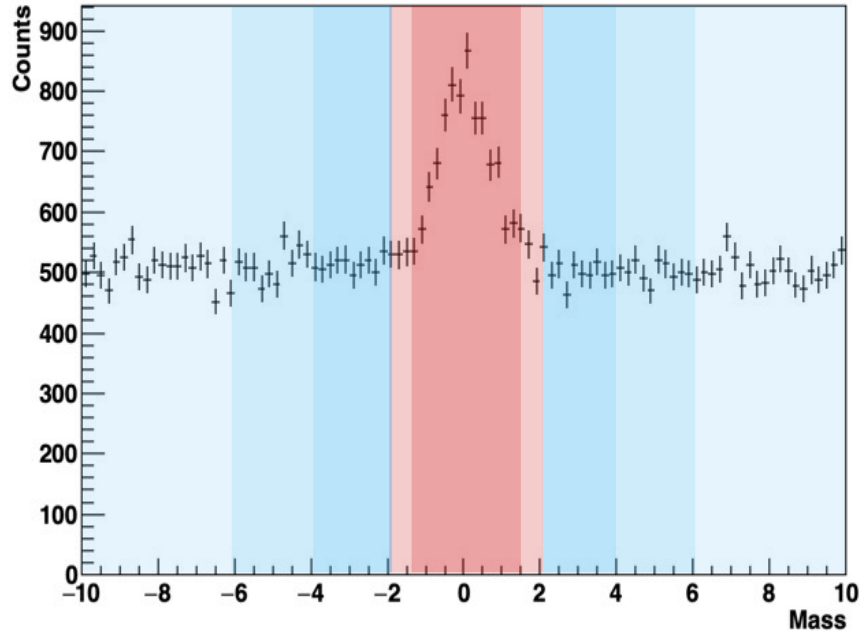
$$\sigma^2(S) = S/\eta + k' \cdot \lambda/\eta^2 \cdot B$$

## Significance : $\rho$

$$\rho \equiv S/\sigma(S) = \eta S/\sqrt{(\eta S + k' \cdot \lambda \cdot B)} \stackrel{S \ll B}{\approx} \eta S/\sqrt{(k' \cdot \lambda \cdot B)} \stackrel{S \leq 1}{\approx} \eta/\sqrt{(k' \cdot \lambda \cdot B)}$$

**So, need  $\eta$  large,  $\lambda$  small,  $k$  large, small  $B$**

# Expected significance



# Branching fractions *etc.*

**Branching fraction  $\mathcal{B}$  defined and measured as**

$$\begin{aligned}
 \mathcal{B}(M \rightarrow X) &= \Gamma(M \rightarrow X) / \Gamma(M \rightarrow \text{anything}) \\
 &= \int \Gamma(M \rightarrow X) \cdot dt / \int \Gamma(M \rightarrow \text{anything}) \cdot dt \\
 &= N(M \rightarrow X) / N(M \rightarrow \text{anything}) \\
 &= N(M \rightarrow X) / N(M) \\
 &= N(M \rightarrow X) / [ N(\text{collisions}) \cdot f(\text{collision} \rightarrow M) ] \\
 &= N(M \rightarrow X) / [ \int \mathcal{L} \cdot dt \cdot \sigma(\text{collision} \rightarrow M) ]
 \end{aligned}$$

**Beware:** could produce multiple M's per collision!

$\mathcal{L}$ : luminosity  
 $\sigma$ : cross section

**Also for other particles**

$$\mathcal{B}(P \rightarrow Y) = N(P \rightarrow Y) / [ \int \mathcal{L} \cdot dt \cdot \sigma(\text{collision} \rightarrow P) ]$$

**Combining two reactions gives**

$$\mathcal{B}(M \rightarrow X) = \mathcal{B}(P \rightarrow Y) \cdot N(M \rightarrow X) / N(P \rightarrow Y) \cdot \sigma(\text{collision} \rightarrow P) / \sigma(\text{collision} \rightarrow M)$$

**Need high  $\int \mathcal{L} \cdot dt$ , large  $\sigma(\text{collision} \rightarrow M, P)$ , known  $\mathcal{B}(P \rightarrow Y)$  &  $f(P)/f(M)$**



# Hadron production

# High Energy Machines (2000–)

## Electron-positron colliders

LEP, BEPC (II), CESR(-c), VEPP(-4M,5, 2000), DAΦNE, PEP-II, (Super)KEKB

$\mathcal{E} =$  104    4.63    6    6    0.7    9+3.1    7+4 GeV

## Electron-Proton colliders

HERA (27.5+920GeV)

## Proton-Antiproton colliders

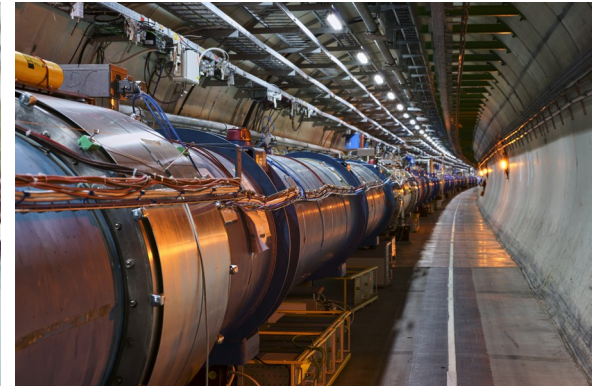
Tevatron (980GeV)

## Proton-Proton colliders

RHIC (255GeV), LHC (6.5TeV)

## Fixed target machines

LANL, PSI, BNL, J-PARC



# Electron-Positron Colliders

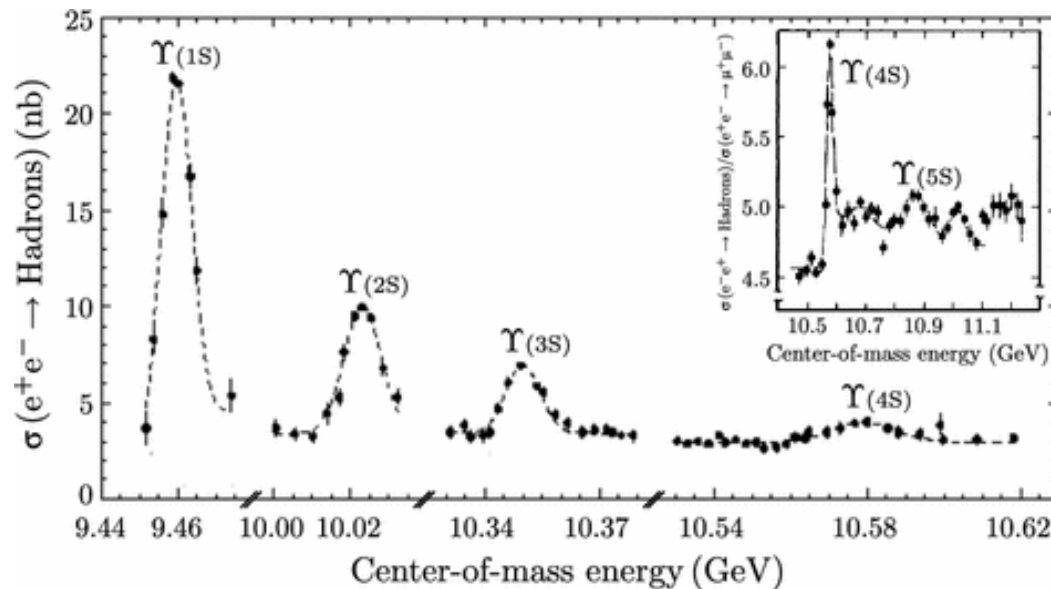
Some scan their energy, but mostly fixed

Resonant production, e.g. via  $e^+e^- \rightarrow J/\psi \rightarrow M\bar{M}$

Only  $\Upsilon(4S)$  decays into  $B\bar{B}$  ( $\mathcal{B} > 96\%$ )

Most are symmetric, so  $J/\psi(c\bar{c})$  or  $\Upsilon(b\bar{b})$  is at rest

Often referred to as **B-factories**, or **tau-charm factories**  
(depending on most abundant production channel)



**At  $E_{cm} = m(\Upsilon(4S))$ :**

$$\begin{aligned} \sigma(e^+e^- \rightarrow \text{hadron}) &\sim 5 \text{ nb} \\ &= 5 \cdot 10^{-33} \text{ cm}^2 \end{aligned}$$

# Electron-Positron Colliders

## KEKB

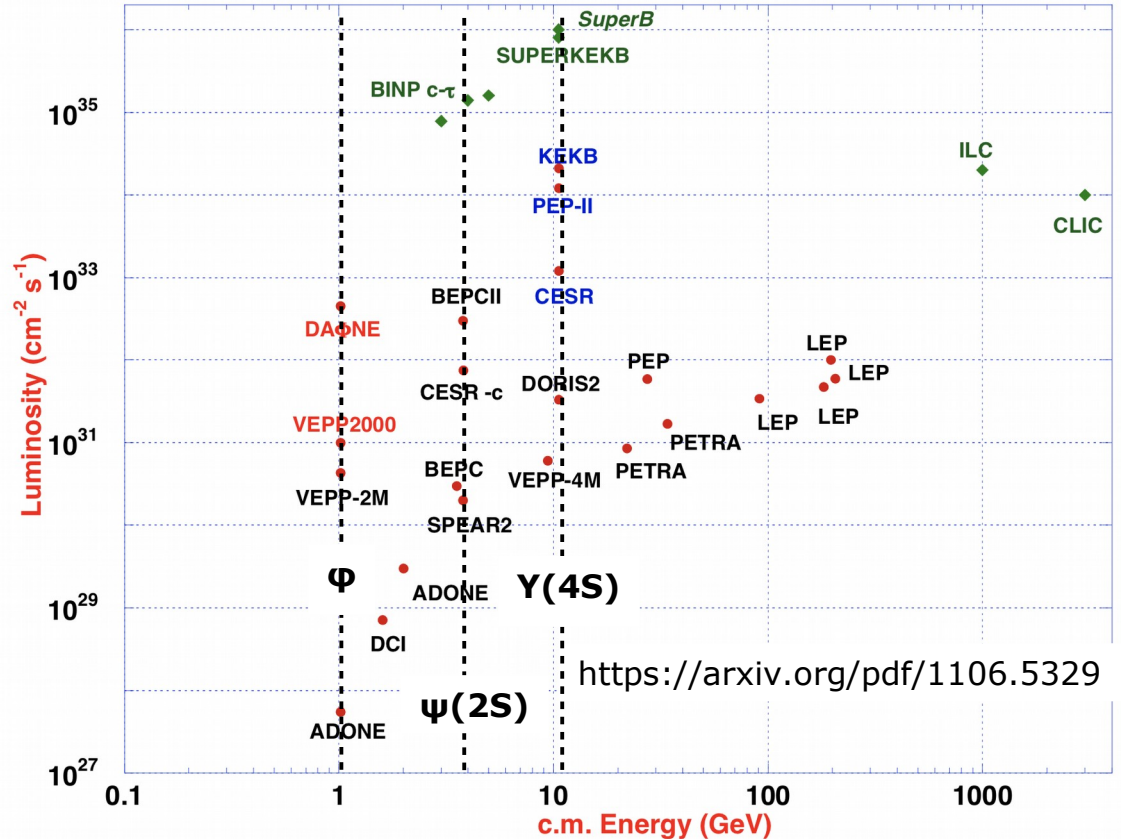
Luminosity of  $10^{34} \text{ cm}^{-2} \cdot \text{s}^{-1}$   
 Production rate of  $\sim 50 \text{ Y} \cdot \text{s}^{-1}$   
 Annually  $\sim 5 \cdot 10^8 \text{ BB}$

## SuperKEKB

Annually  $\sim 5 \cdot 10^9 \text{ BB}$

## BEPC

Annually  $\sim 3 \cdot 10^9 \text{ } \Psi(2S)$



DOI:10.1063/PT.6.1.20180516a

Figure 1. Peak luminosity and energy of the past, present and future (diamonds) electron-positron colliders.



# Large Hadron Collider

Proton on proton collision

Enormous energy: 6.5 TeV + 6.5 TeV

Single collision produces many particles (100's)

## LHCb (2015-2018)

Average luminosity  $\langle L \rangle \sim 50 \mu\text{b}^{-1}\cdot\text{s}^{-1}$

$B\bar{B}$  production in acceptance  $\sigma(pp \rightarrow b\bar{b}X) \sim 150 \mu\text{b}$

Production rate  $B\bar{B} \sim 7500 \text{ s}^{-1}$

Integrated luminosity:  $6 \text{ fb}^{-1}$

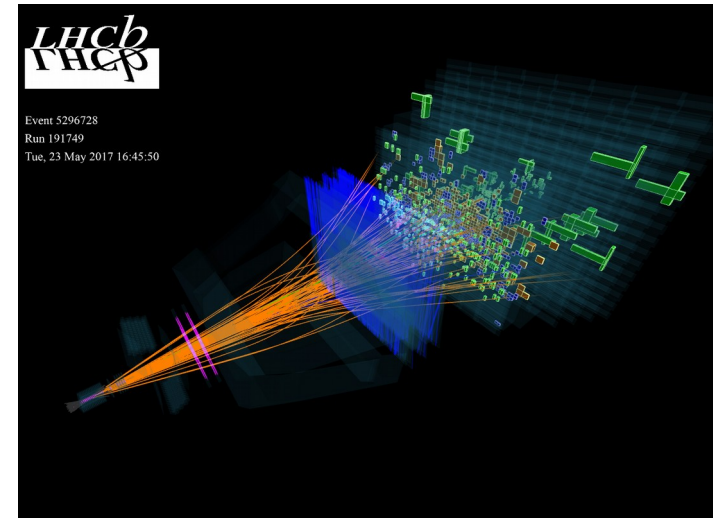
Total production:  $\sim 10^{12} B\bar{B}$

## ATLAS (2015-2018)

Integrated luminosity:  $160 \text{ fb}^{-1}$

$B\bar{B}$  production in acceptance  $\sigma(pp \rightarrow b\bar{b}X) \sim 500 \mu\text{b}$

Total production:  $\sim 10^{14} B\bar{B}$



# Particle identification



LHC

CMS

LHCb

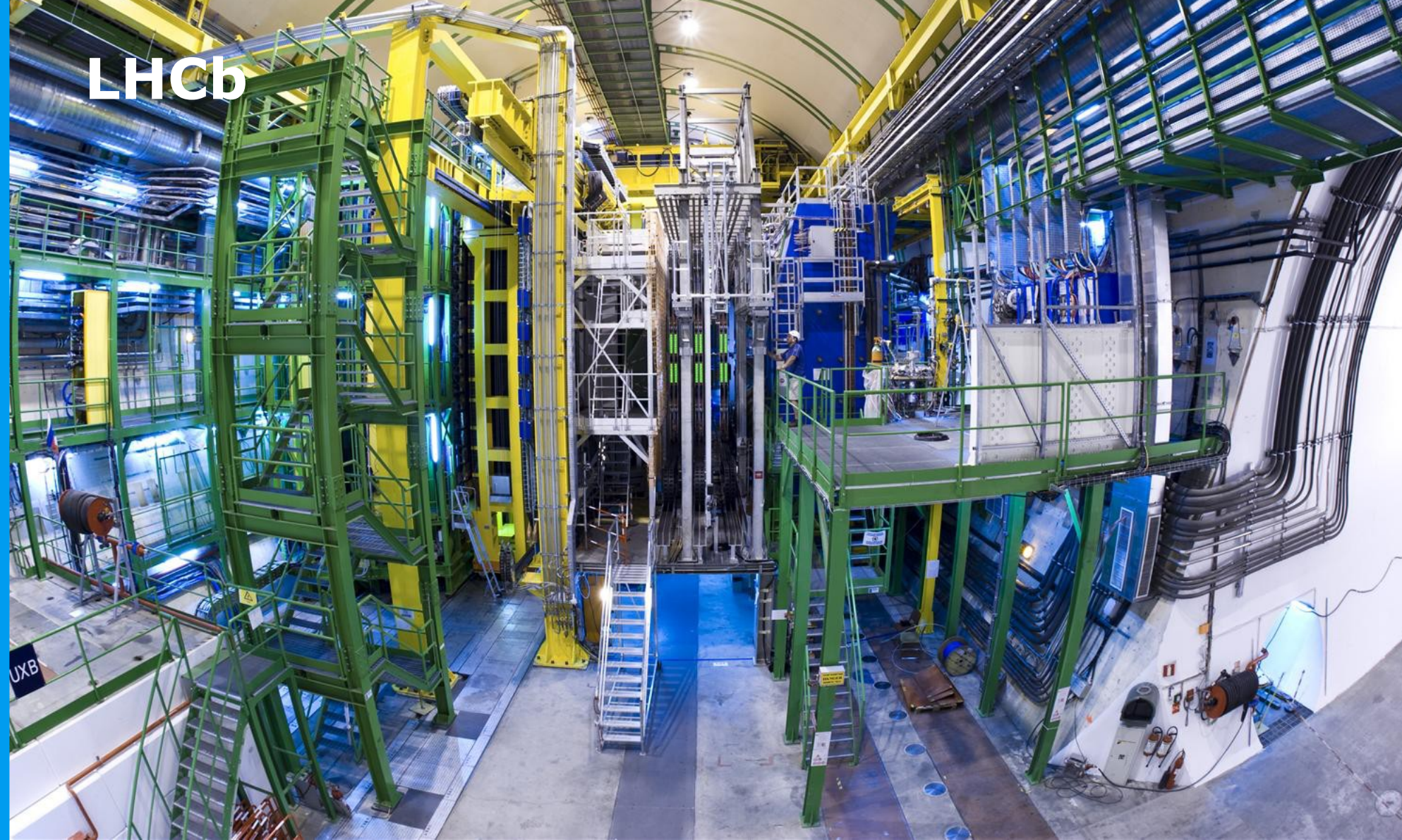
ALICE

ATLAS





LHCb





# LHCb



# LHCb

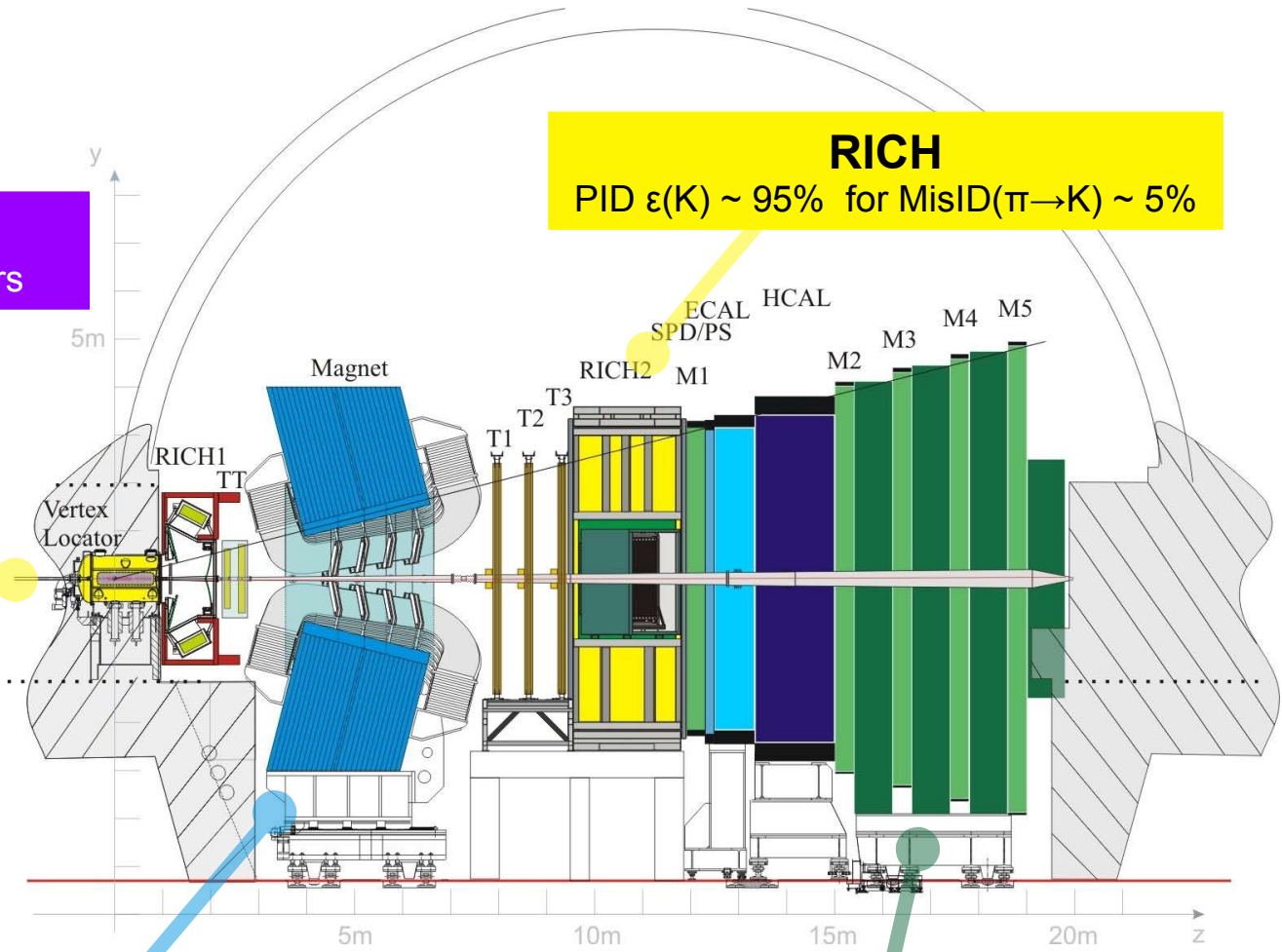
**Trigger**  
high efficiency esp. muon triggers

**VELO**  
IP resolution  $15+29/(p_T/\text{GeV}) \mu\text{m}$

**Tracking  $\Delta p/p$**   
 $0.4\% @ 5 \text{ GeV}/c - 1.0\% @ 200 \text{ GeV}/c$

**RICH**  
PID  $\epsilon(K) \sim 95\%$  for MisID( $\pi \rightarrow K$ )  $\sim 5\%$

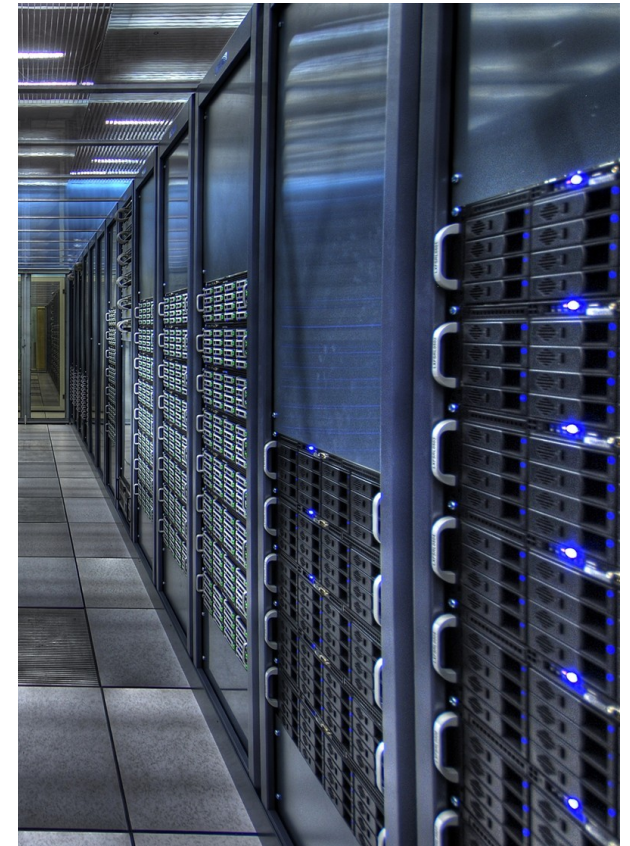
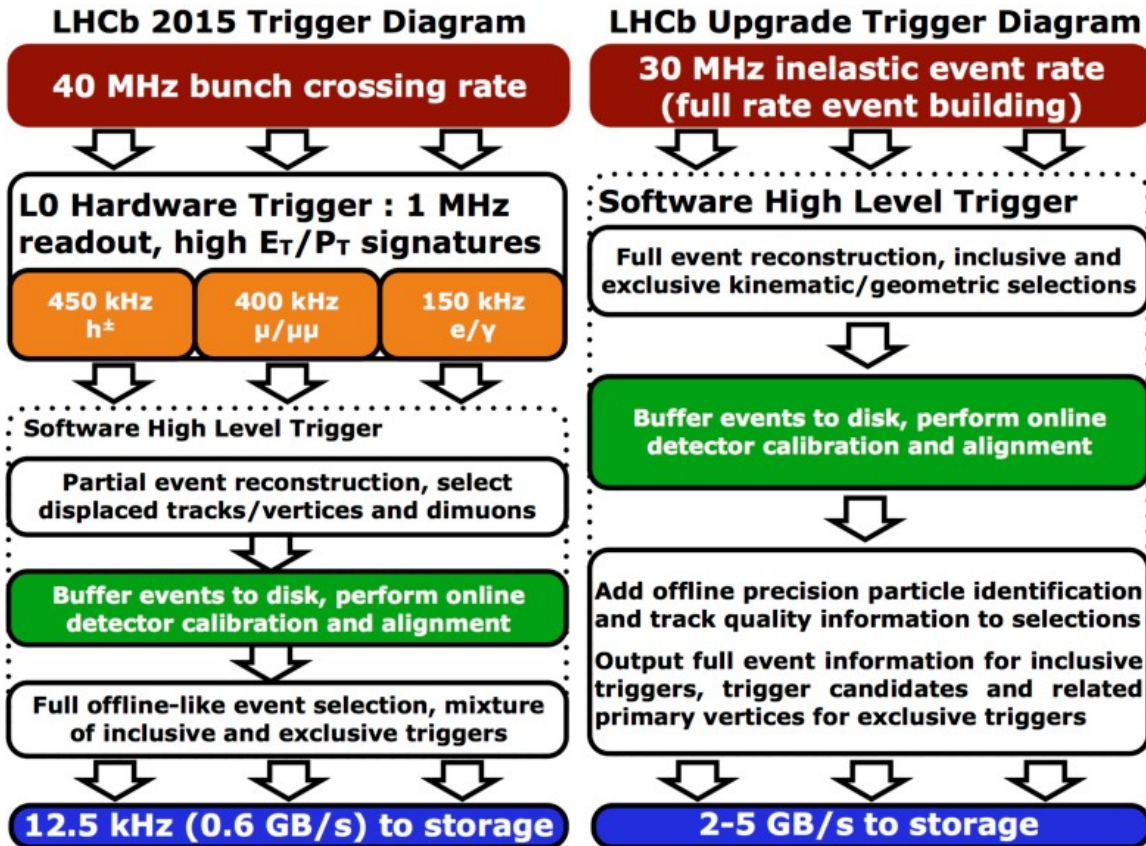
**Muon ID**  
identification  $\epsilon \sim 97\%$  misID  $\sim 2\%$





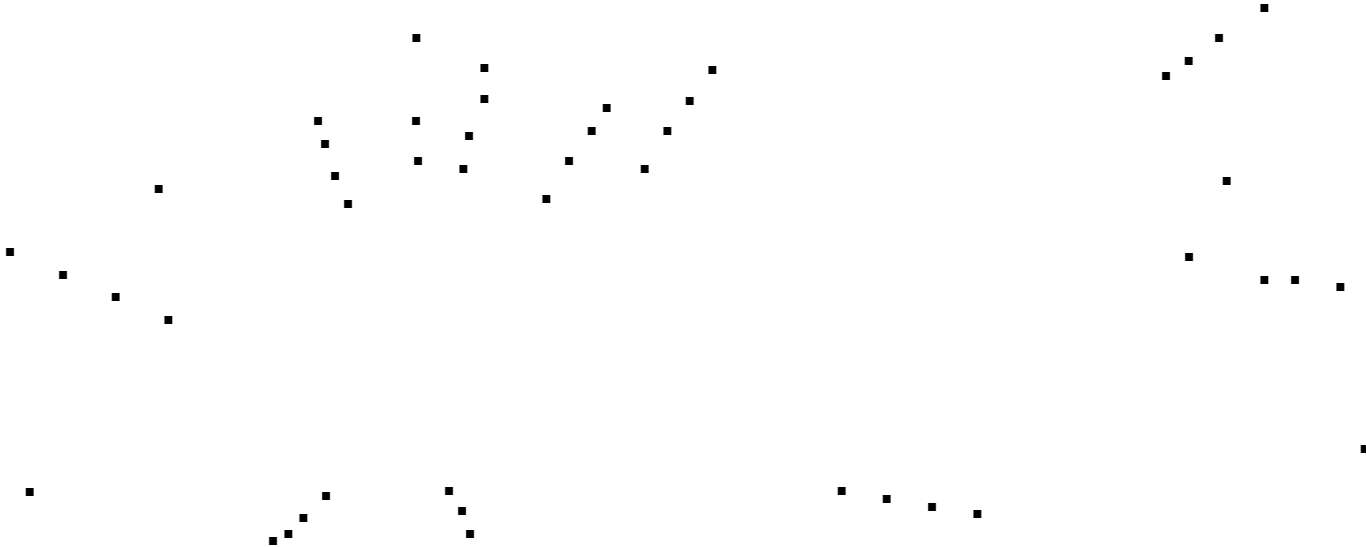
# Triggering

Most collision events are un-interesting → event selection / triggering



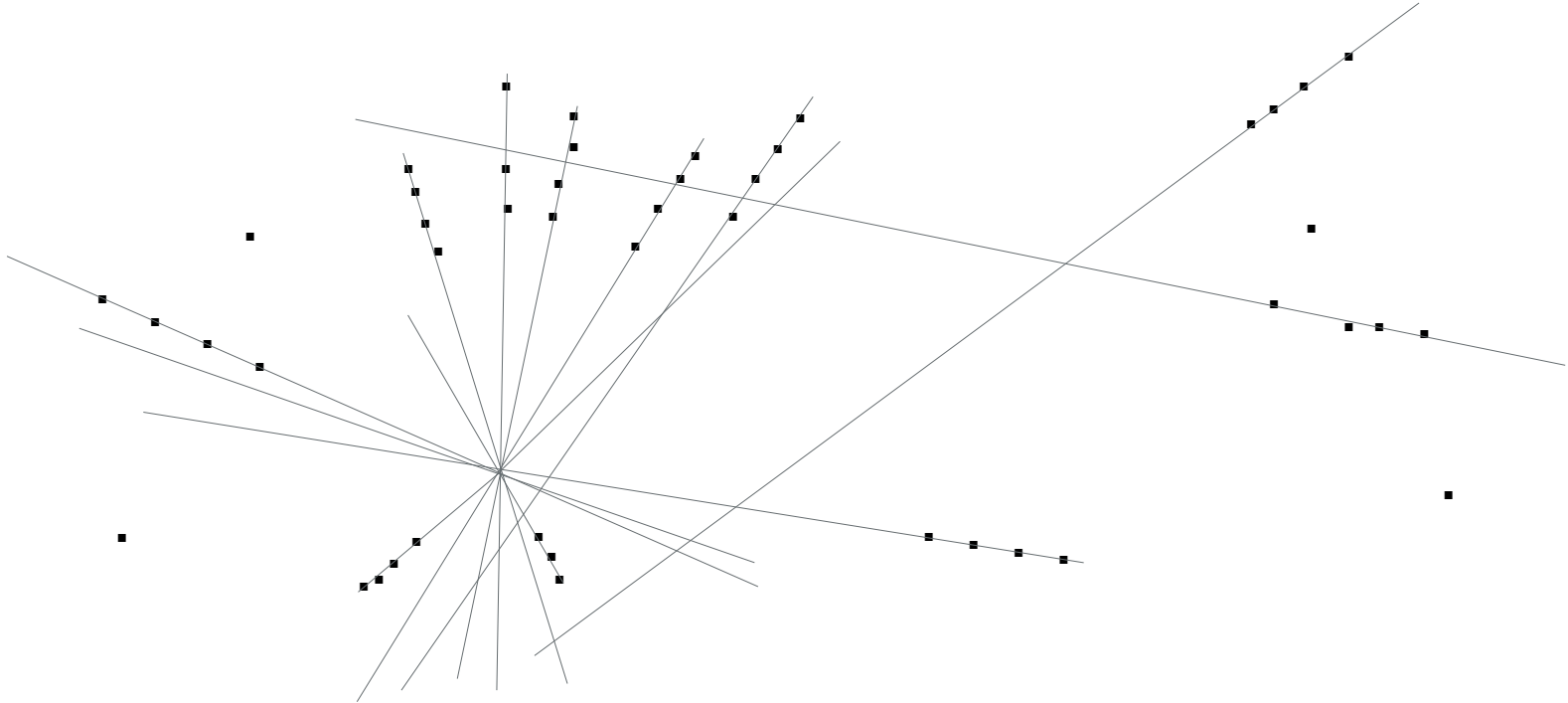
# Reconstruction

Tracking : connecting **hits**



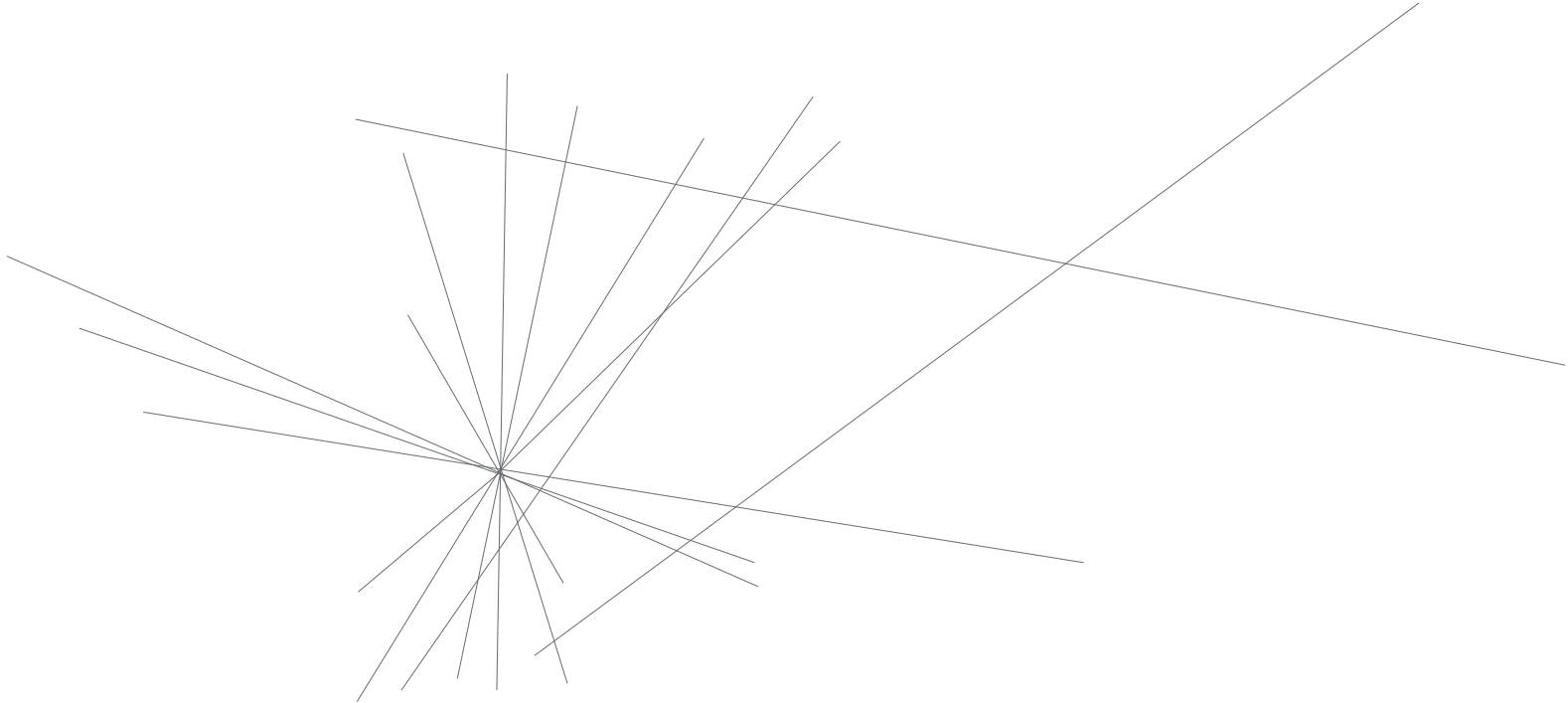
# Reconstruction

Tracking : connecting hits to form **tracks**



# Reconstruction

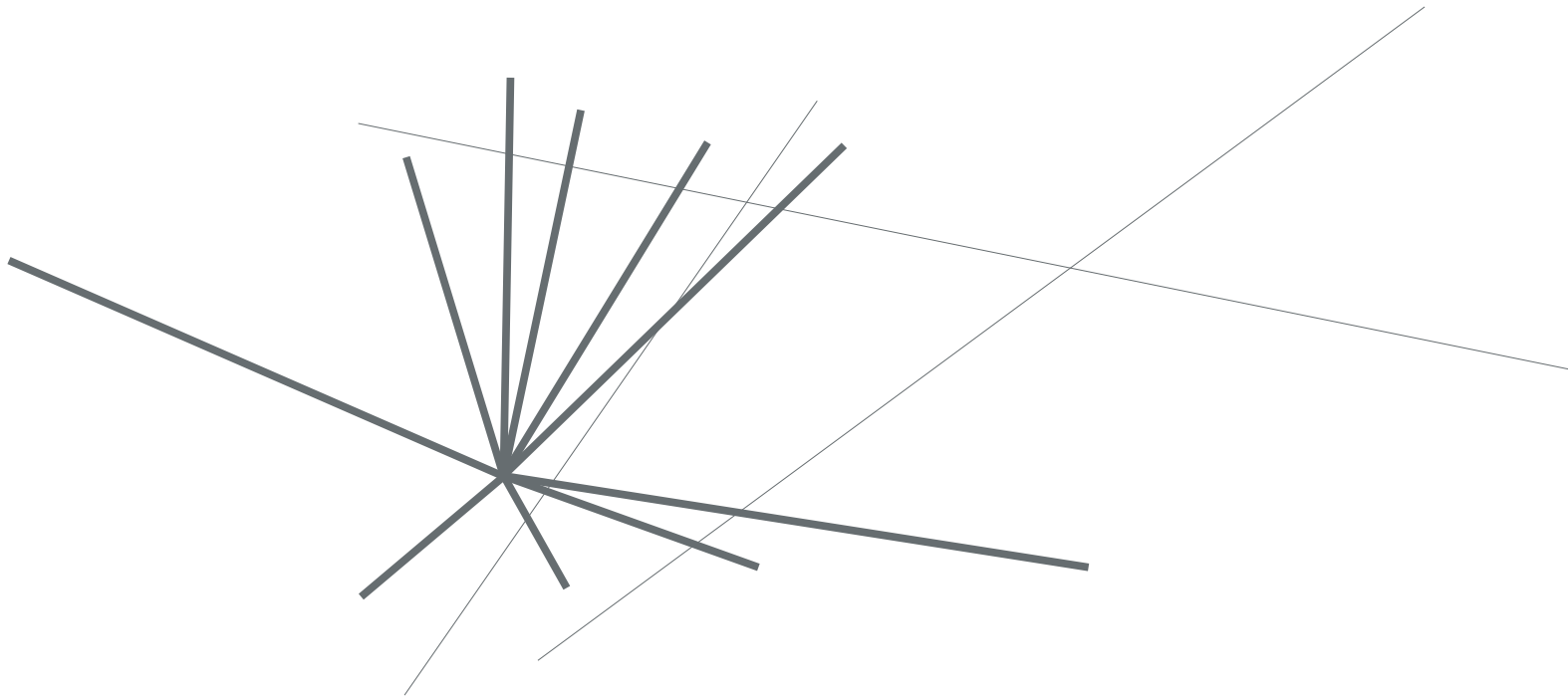
**Tracking : connecting hits to form tracks**  
and determine *charge* and *momentum* from bending in magnetic field



# Reconstruction

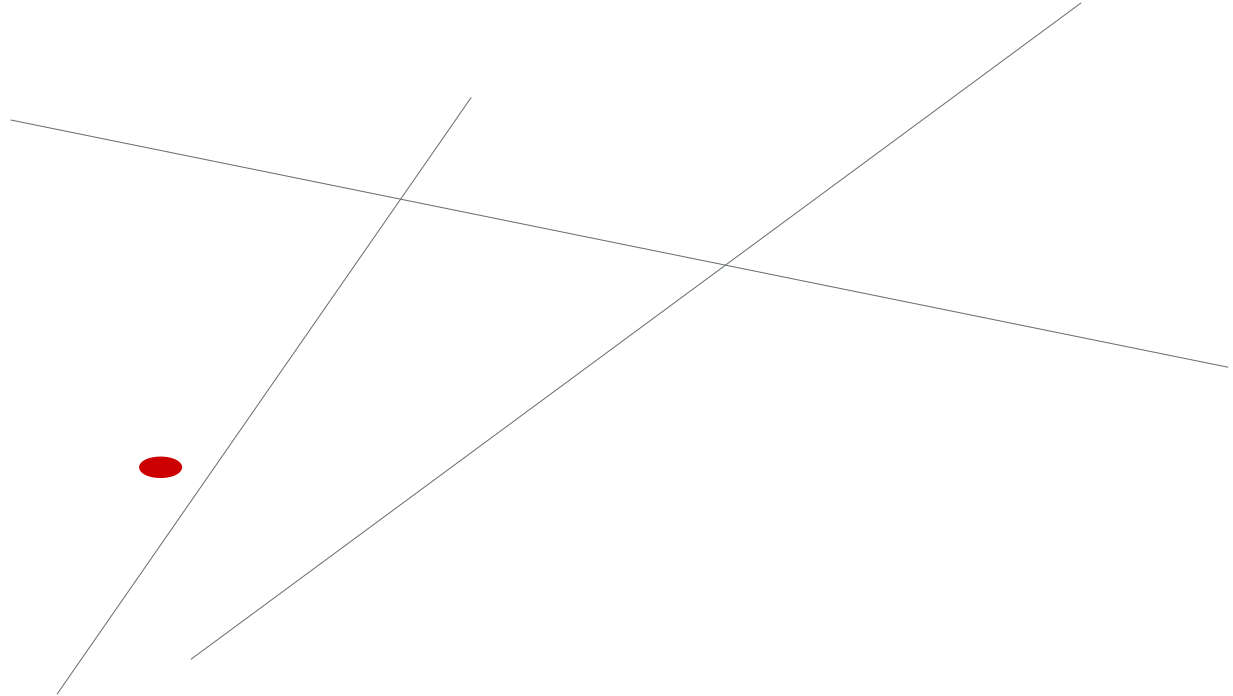
Find the **primary vertex** = collision point of two protons

Many tracks will originate from a common location close to the beam



# Reconstruction

Find the **primary vertex**



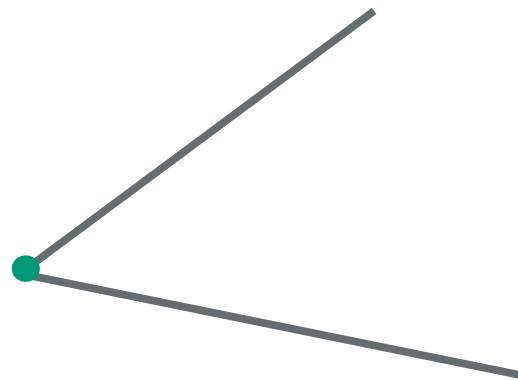
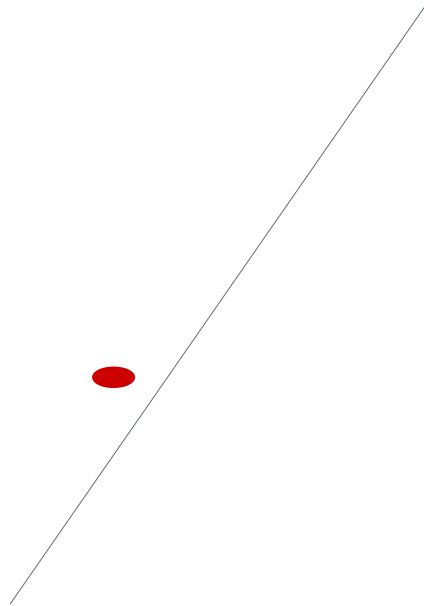


# Reconstruction

## Find **secondary vertex**

= location in space where two (or more tracks) converge

WARNING: probability that 2 lines in 3D space cross = zero, so use "best" point

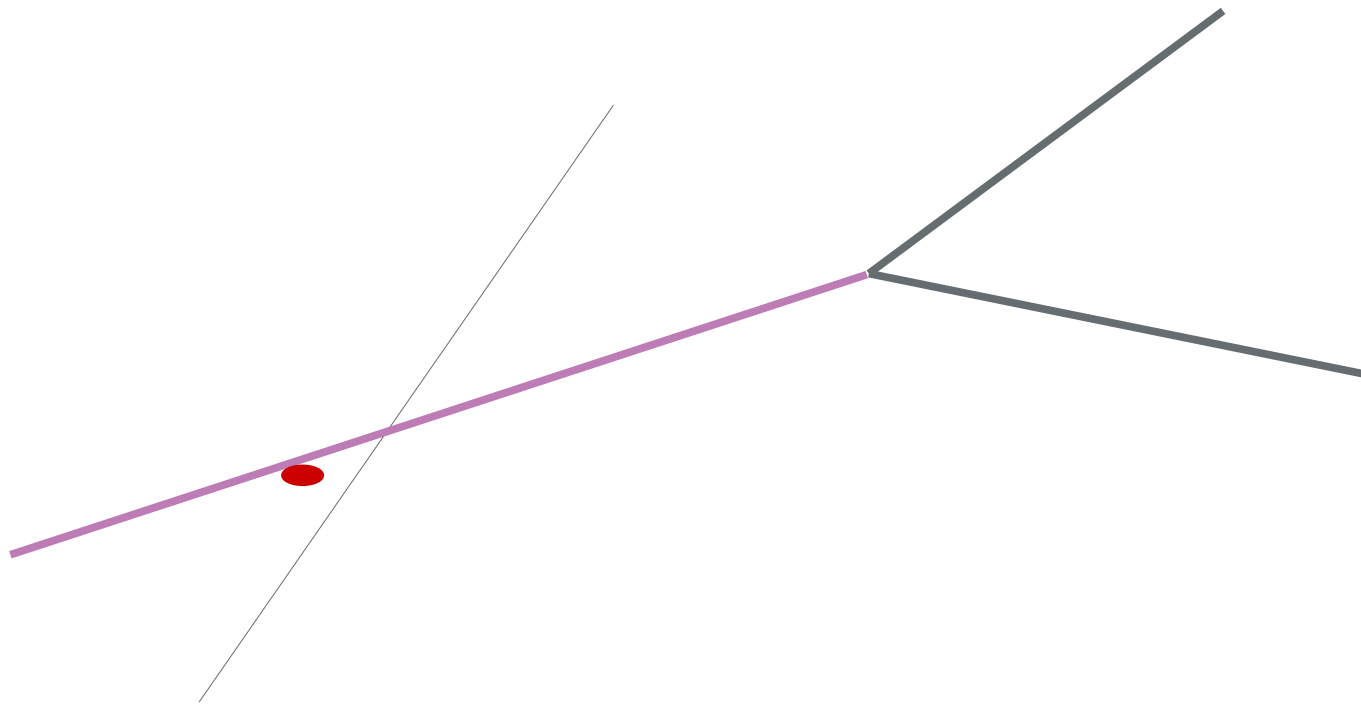


# Reconstruction

Find **secondary vertex**, reconstuct **parent track**

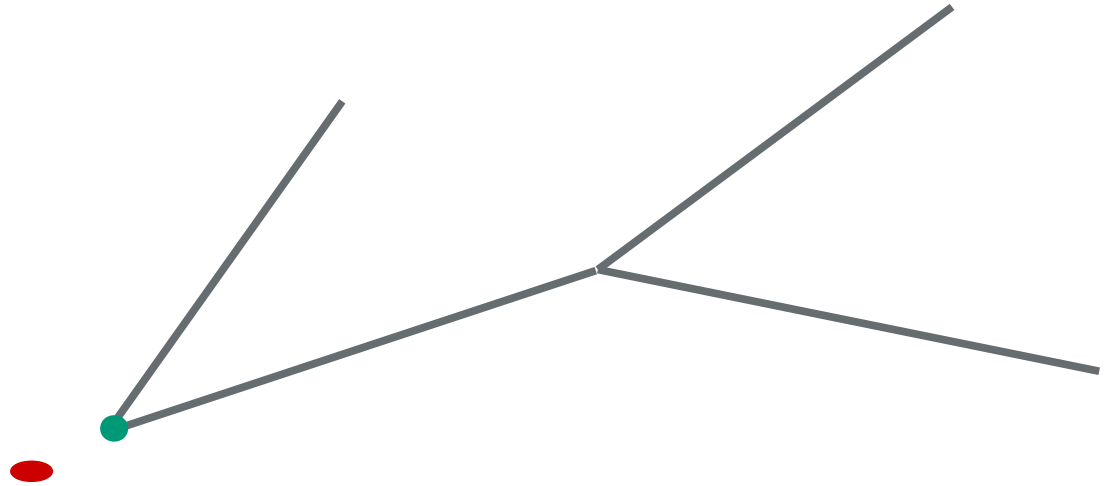
Combing 3-momenta gives parent 3-momentum, and direction of track

POSSIBLE IMPROVEMENT: refit tracks with perfect secondary vertex



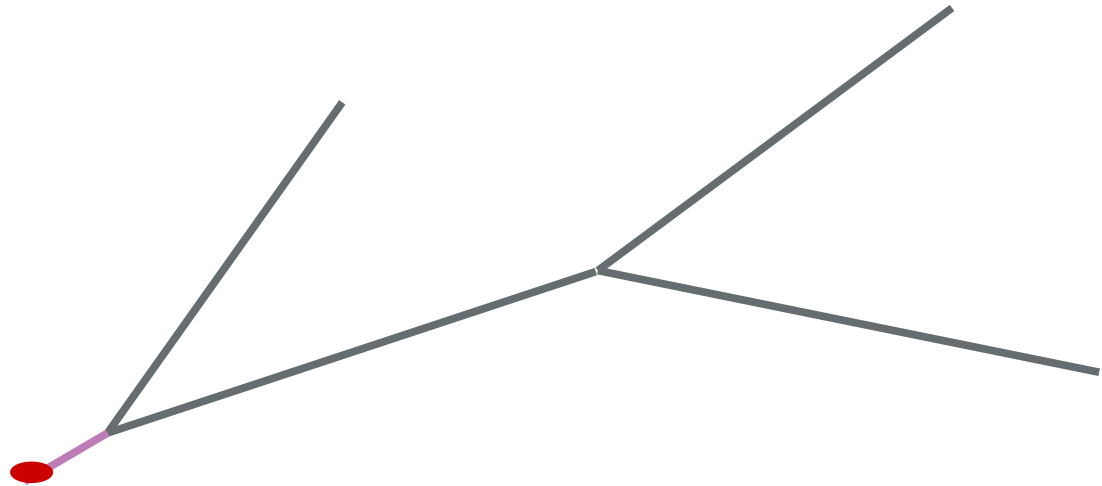
# Reconstruction

Find **secondary vertex**, reconstuct **parent track**, and repeat



# Reconstruction

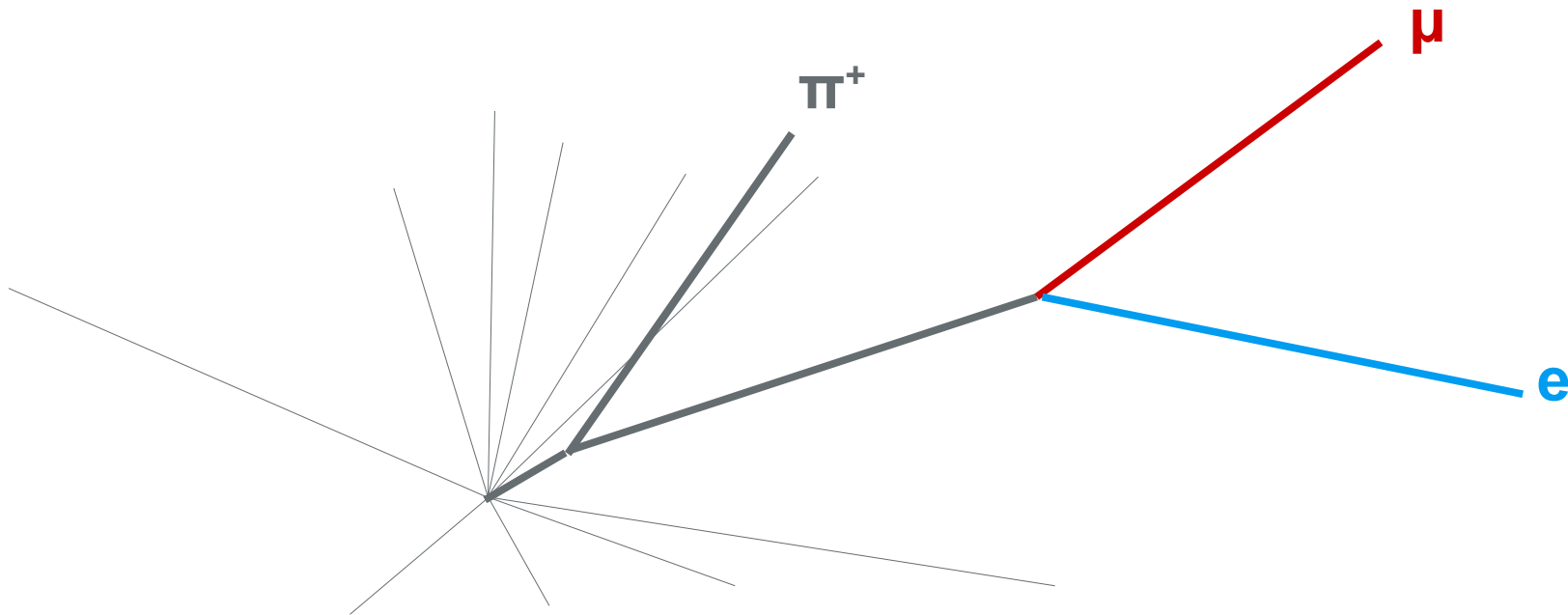
Find **secondary vertex**, reconstitute **parent track**, and repeat until last parent track comes from primary vertex



# Reconstruction

## Identify detected particles

WARNING: cannot be done uniquely, assume *most likely* identity

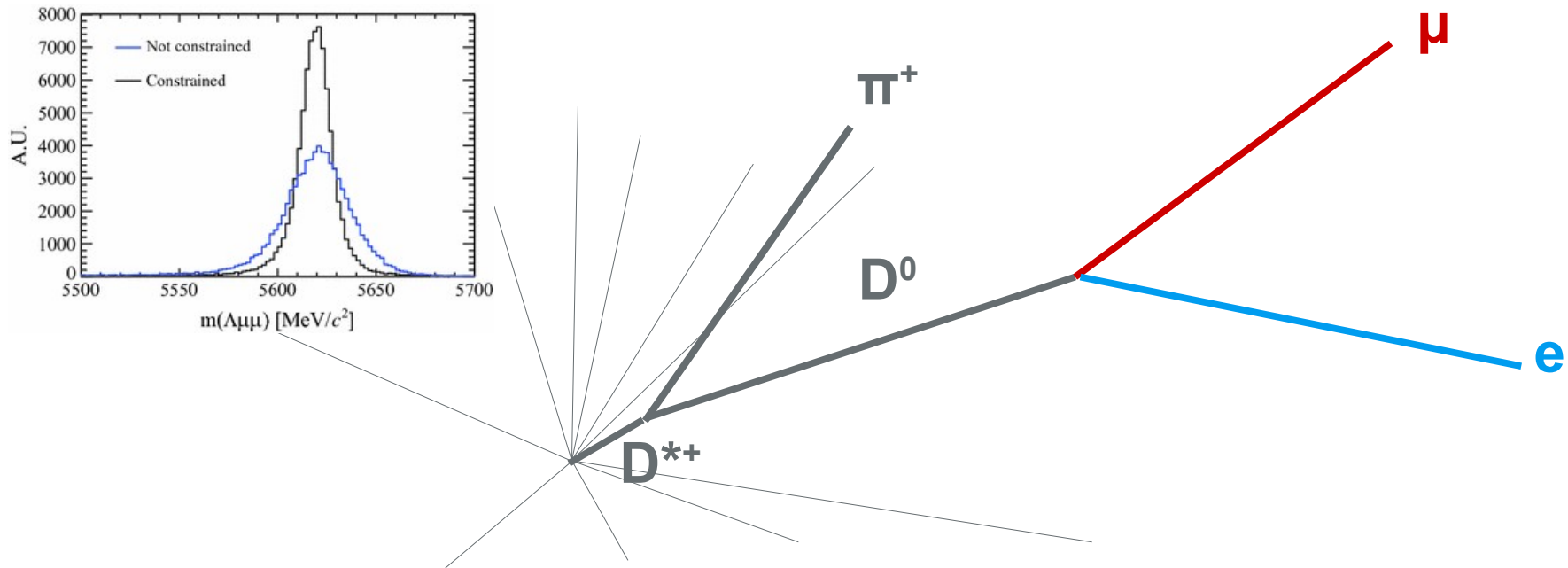


# Reconstruction

## Identify invisible particles

Construct four-momenta of parents, calculate invariant mass, and identify

POSSIBLE IMPROVEMENT: refit tracks with perfect vertices and/or parent mass





# Challenge #1 : Particle (mis-)ID

At LHCb all light particles ( $\gamma, e, \mu, n, K, p$ ) ultra-relativistic,  $p \leq 200 \text{ GeV}/c$

Photons and electron cause similar shower (mostly) in EM calorimeter (**ECAL**)

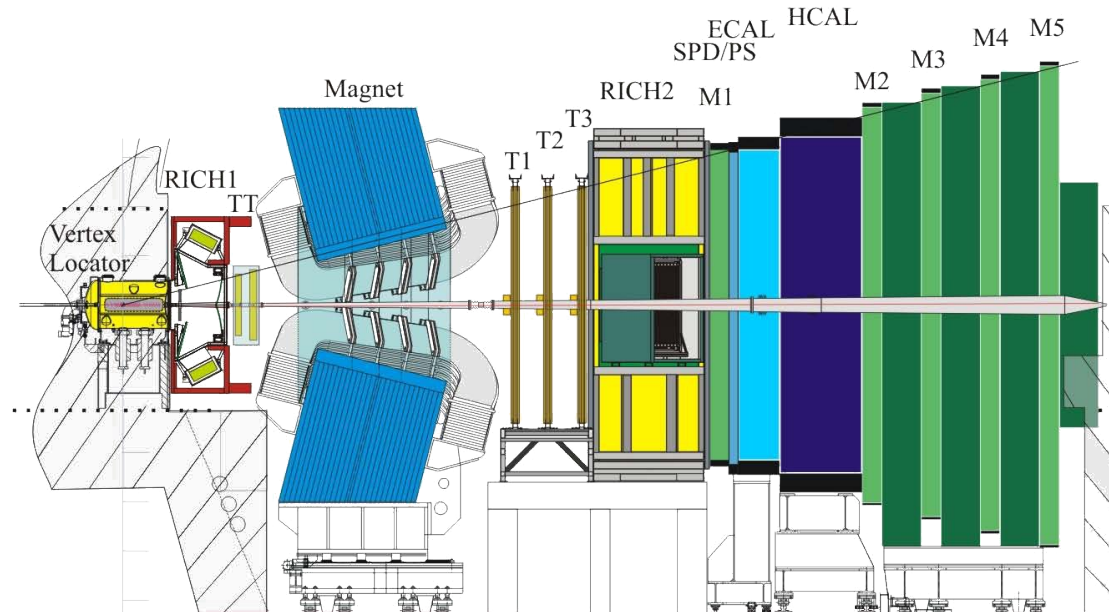
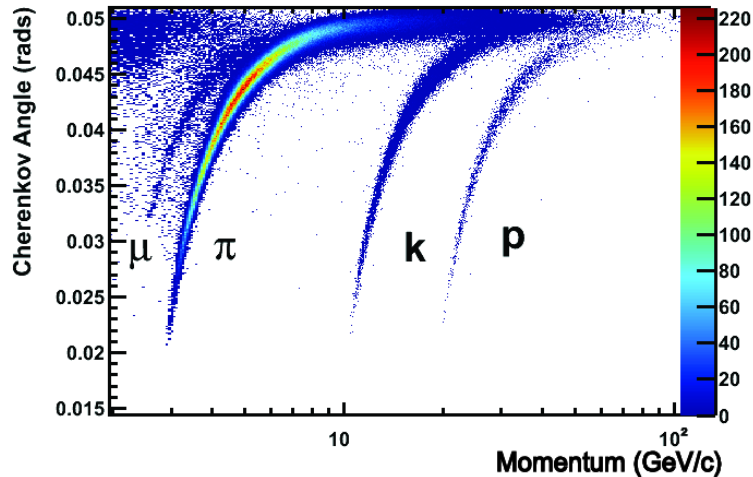
Photons leave no/little signal in pre-shower detector (**PS**) and trackers (**TT-T3**)

(Essentially) only muons make it to the muon chambers (**M1-M5**)

Hadrons (mostly) stop in hadronic calorimeter (**HCAL**)

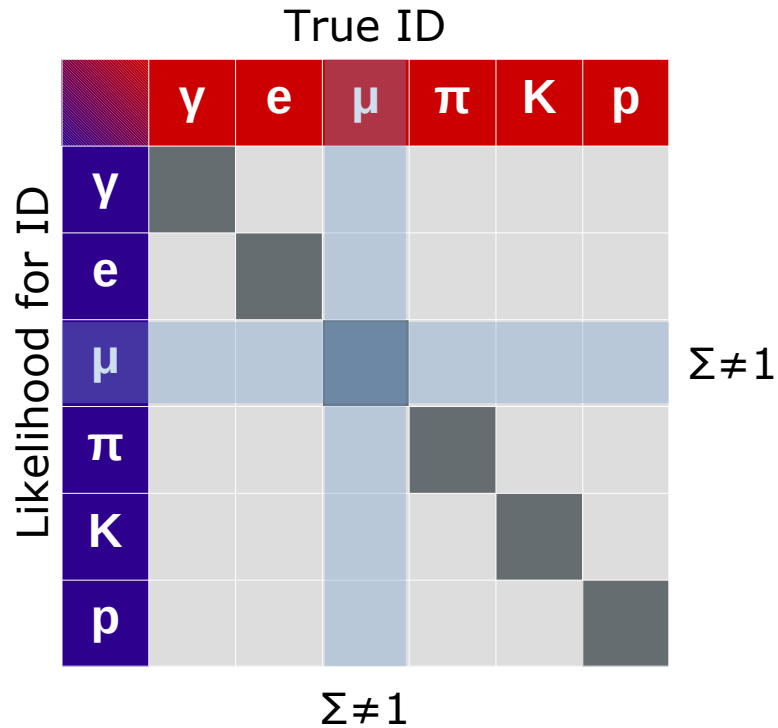
Ring-imaging Cherenkov Detector (**RICH**) distinguishes velocity

**All rather energy dependent**



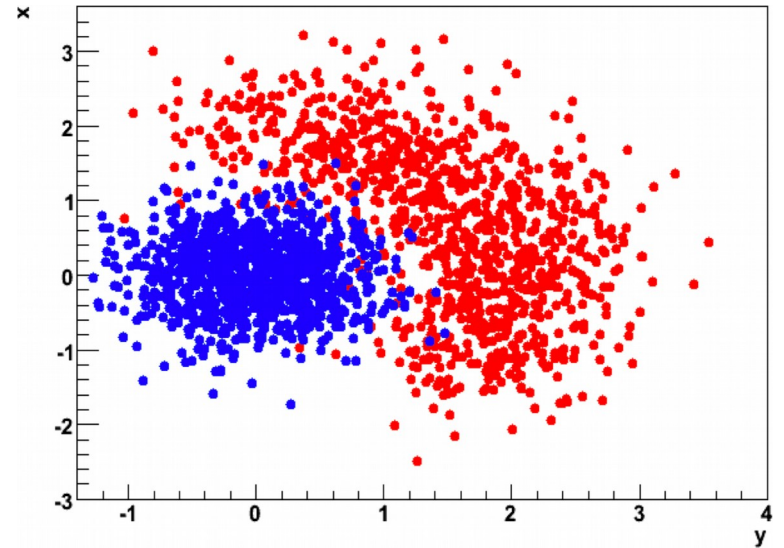
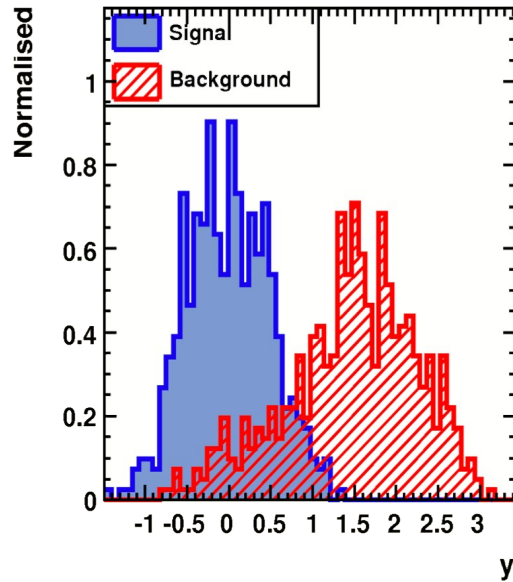
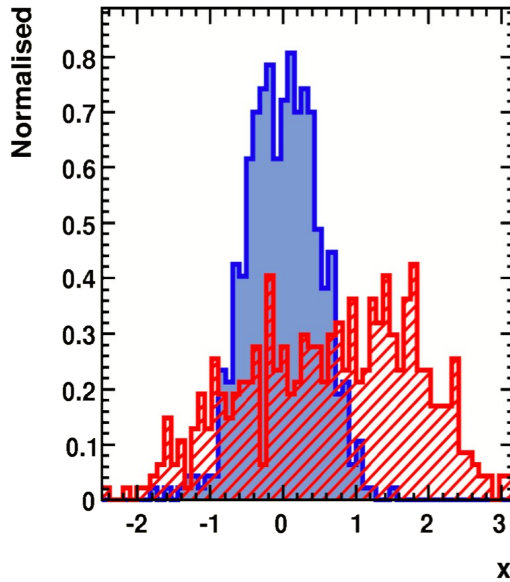
# Challenge #1 : Particle (mis-)ID

Particle not uniquely ID'ed  
 Likelihood per species



# (Boosted) decision trees

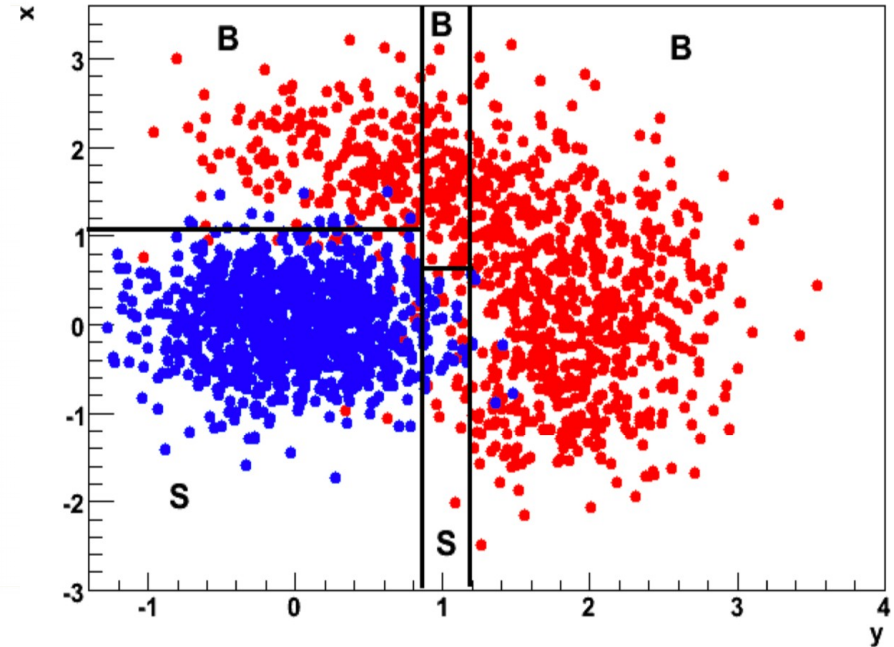
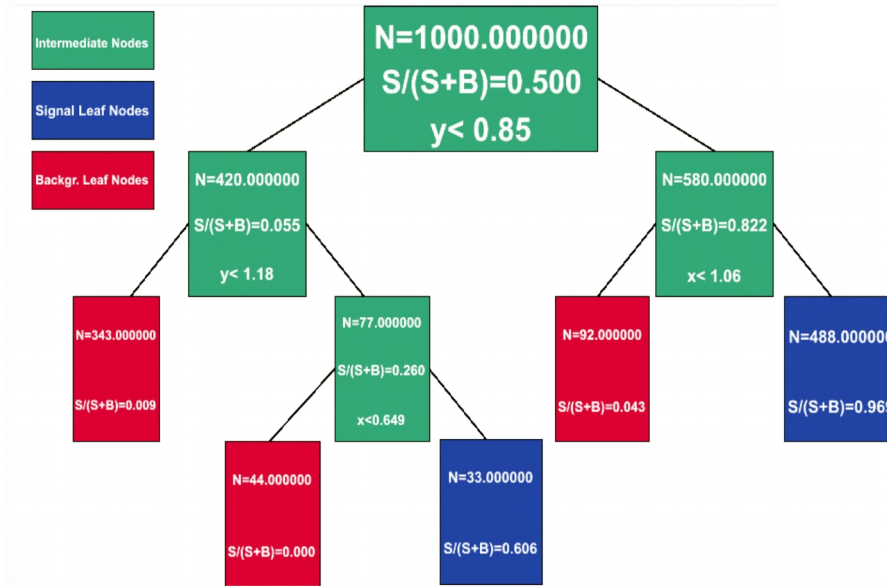
Example: **signal** and **background** measured in 2 detectors **X** and **Y**



Signal windows has lots of background → (automatically) optimize selection?

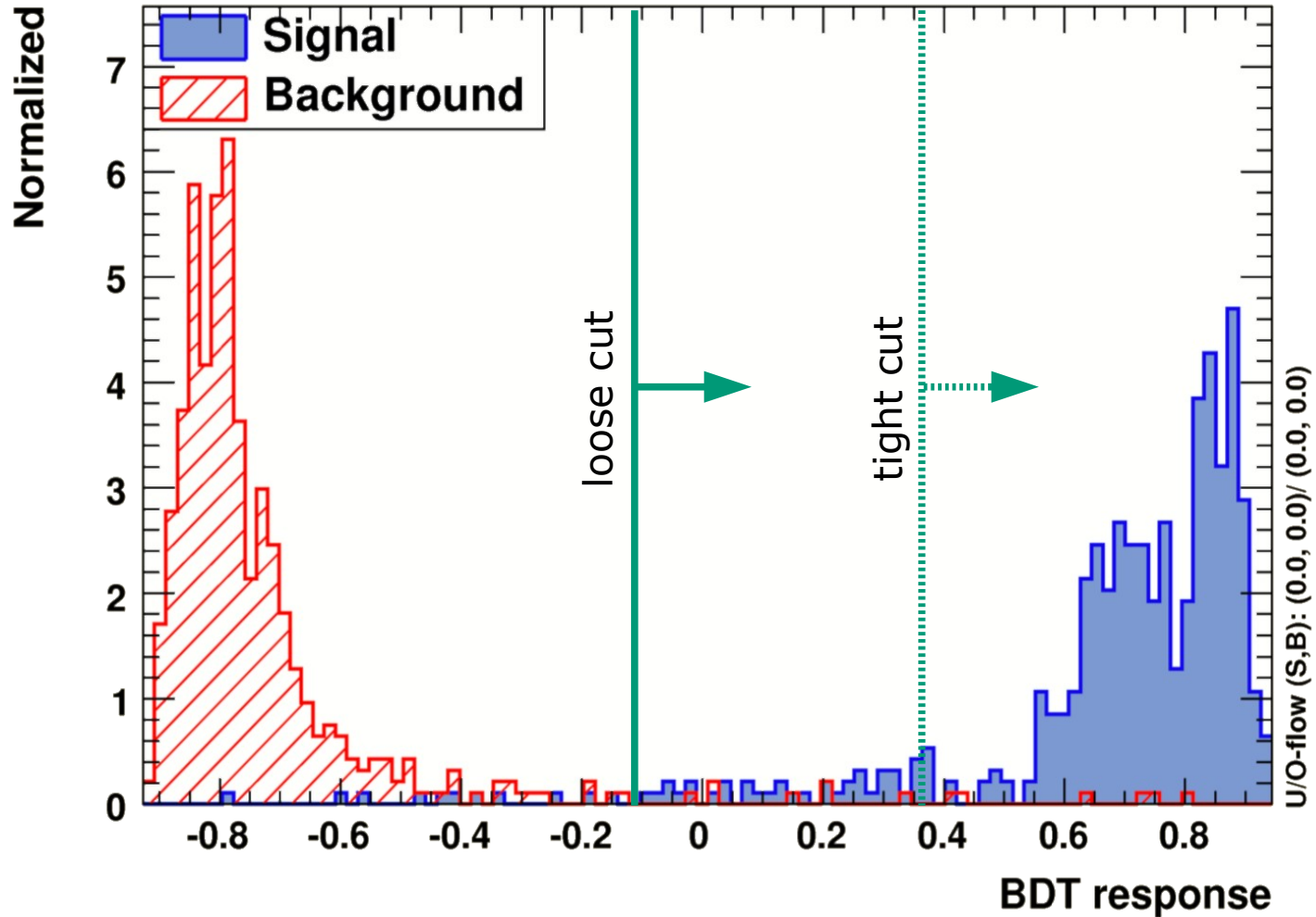
# (Boosted) decision trees

Repeatedly split data in **X** or **Y** to optimize **signal-significance**



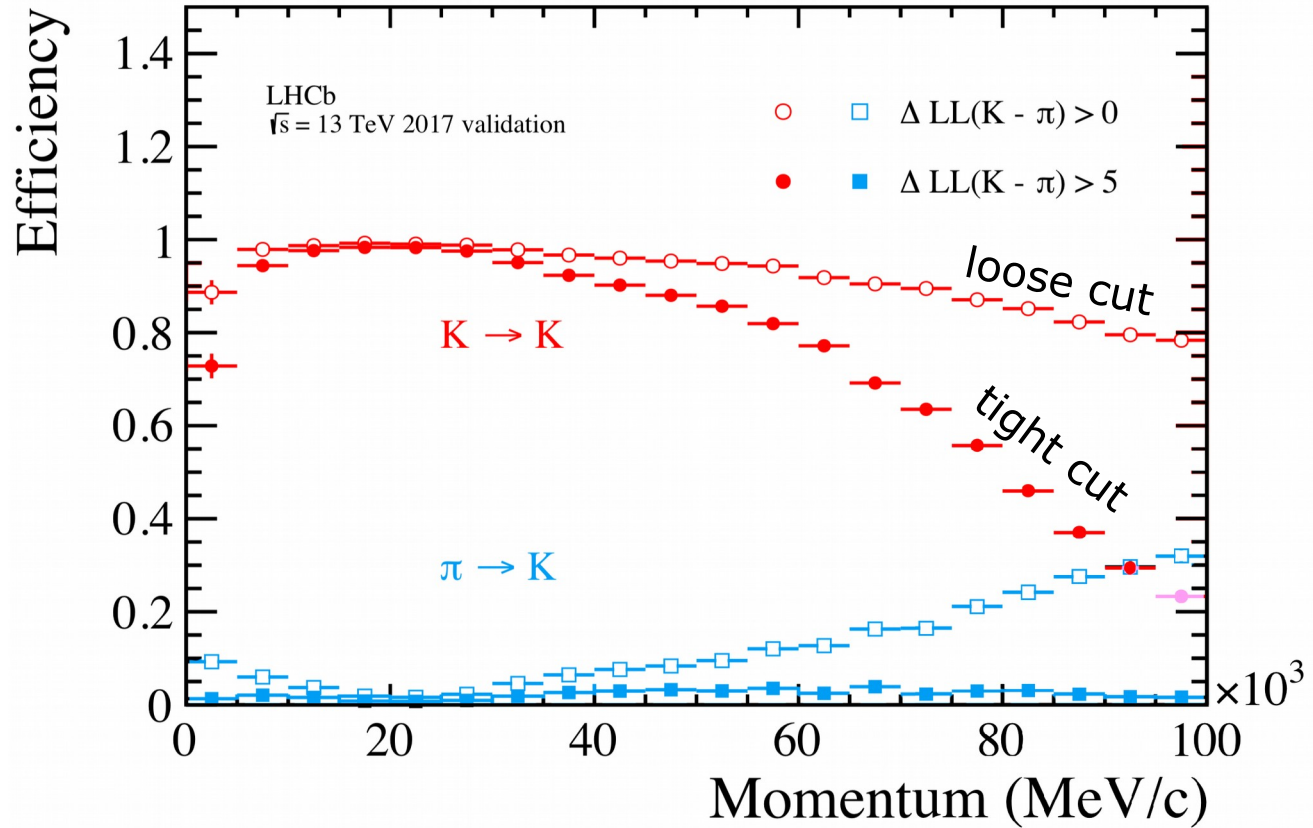
Boosting: take output of DT and re-weight training data for next DT

# (Boosted) decision trees



# Particle (mis-)ID

Incorrect inclusion/rejection of event for further analysis  $\rightarrow \eta, \lambda$   
 Leads to mis-reconstruction of parent mass





# Challenge #2 : Bremsstrahlung

**Charged particles deflected by other particles (nuclei) emit radiation**

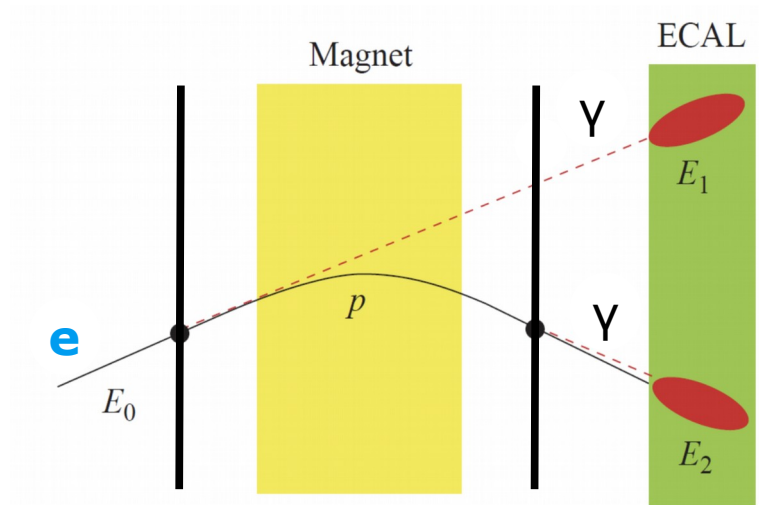
Bremsstrahlung is proportional to  $\gamma^6$ .

Especially important for **electrons**

Photons emitted predominantly along direction of motion

**Main effect** : change in *magnitude* of momentum, less so in *direction*

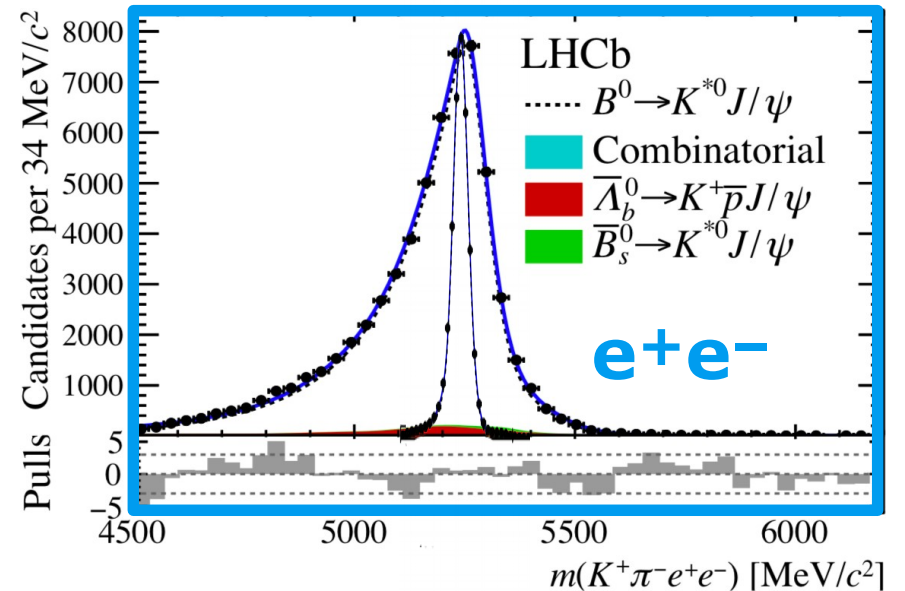
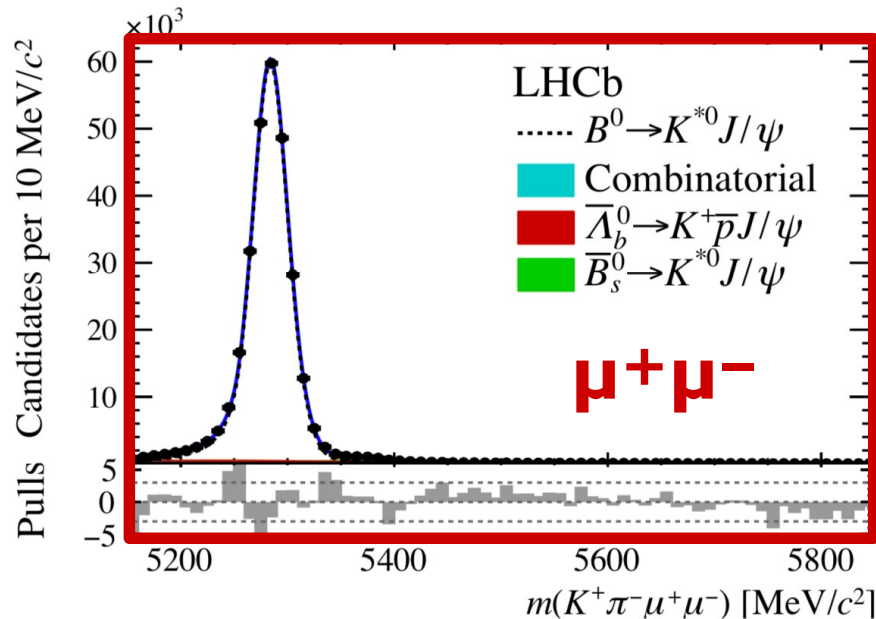
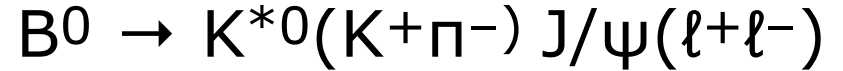
In part automatically recovered, in part to be done by-hand



# Challenge #2 : Bremsstrahlung

## Reconstructed parent mass less precise

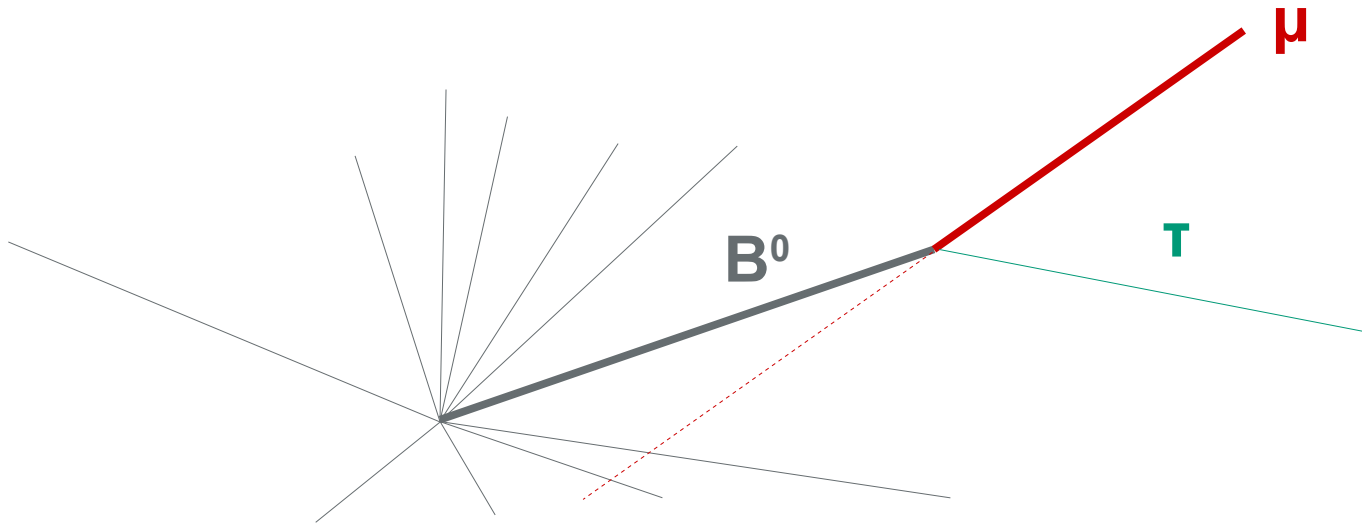
- wider signal region
- more background
- lower signal significance
- weaker limit



# Challenge #3 : Tau-decay

**Tau** lifetime is 0.29 ps ( $c\tau = 87 \mu\text{m}$ )

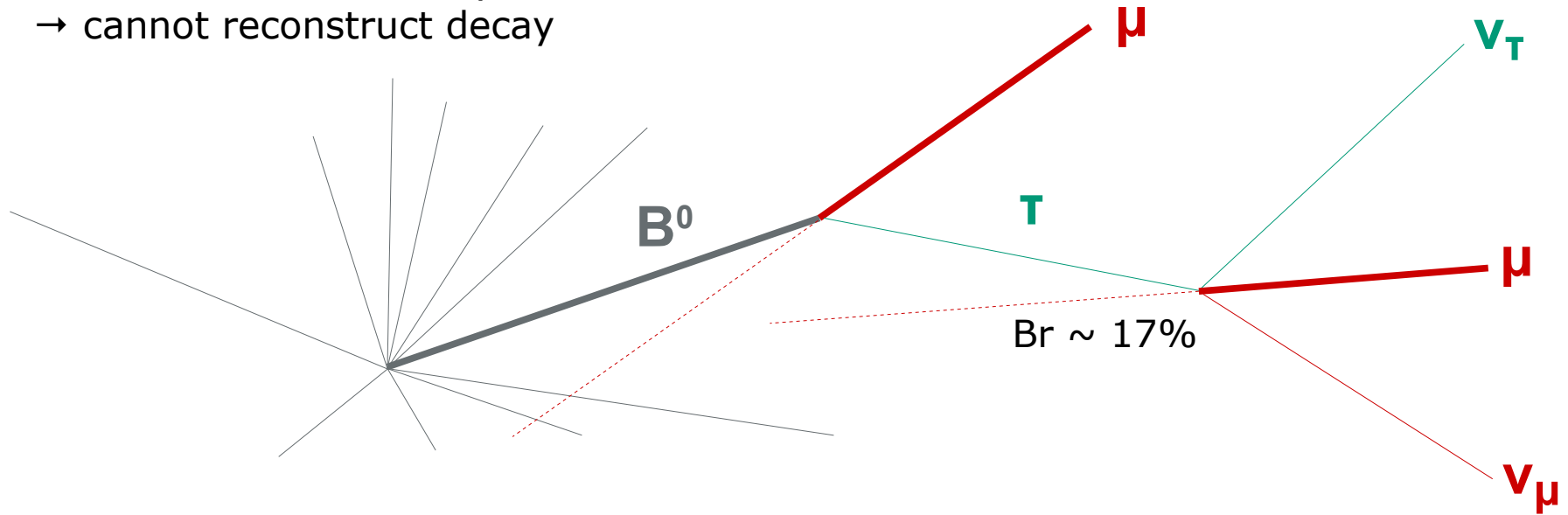
So **tau** cannot be detected itself



# Challenge #3 : Tau-decay

**Can only detect charged decay products, not neutrinos**

- always missing tau-neutrino, if leptonic decay also second one
- missing p and E
- cannot find secondary vertex
- cannot reconstruct decay



# Challenge #3 : Tau-decay

**Hadronic decay : only a single missing neutrino**

Several charged pions : can reconstruct **tau** decay vertex

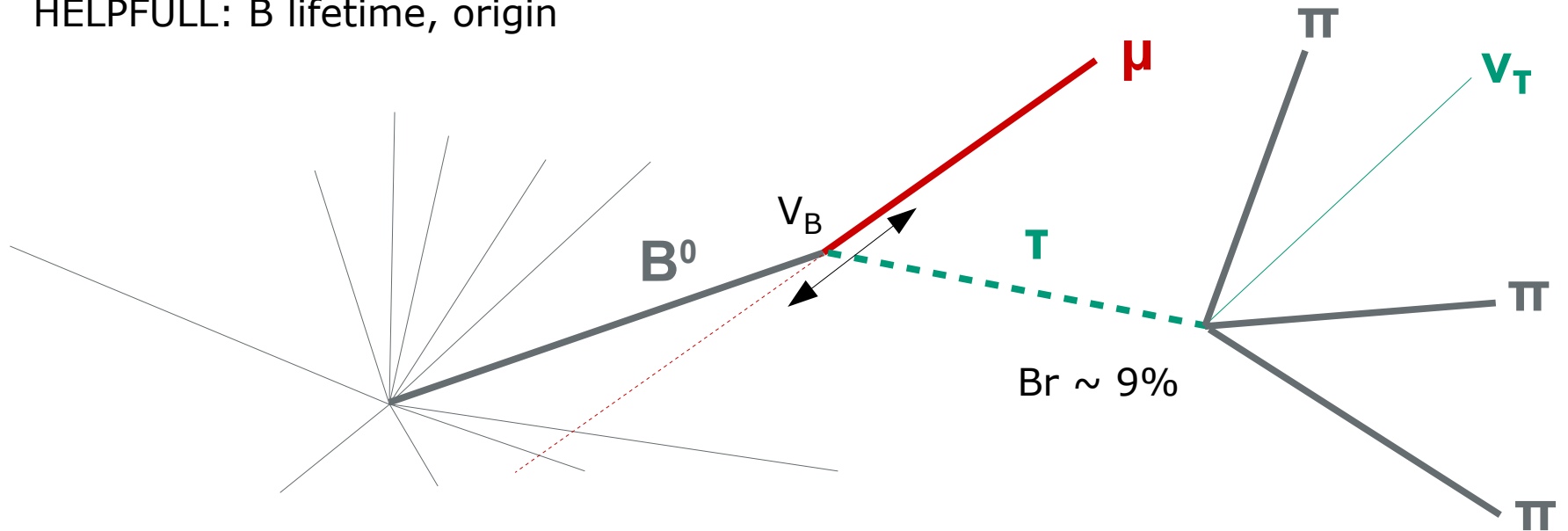
PROBLEM: B decay vertex along **μ** track unknown

HELPFULL: B lifetime, origin

$$p_{\perp}(\mathbf{v}) \text{ along } \mathbf{p}_{\mu} \times \mathbf{p}_{\tau}$$

$$p_{\parallel}(\mathbf{v}) \text{ along } \mathbf{p}_{\tau}$$

$$p_{\perp}(\mathbf{v}) \text{ 3}^{\text{rd}} \text{ term } \perp \mathbf{p}_{\tau}$$



Can reconstruct B decay vertex if **tau** &  $B^0$  mass/origin assumed

always:  $p_{\perp}(\mathbf{v}) = -p_{\perp}(\mathbf{3n})$ , for given  $V_B$ :  $p_{\perp}(\mathbf{v}) = -p_{\perp}(\mathbf{3n})$ ,  $p_{\parallel}(\mathbf{v})$  fixed by masses

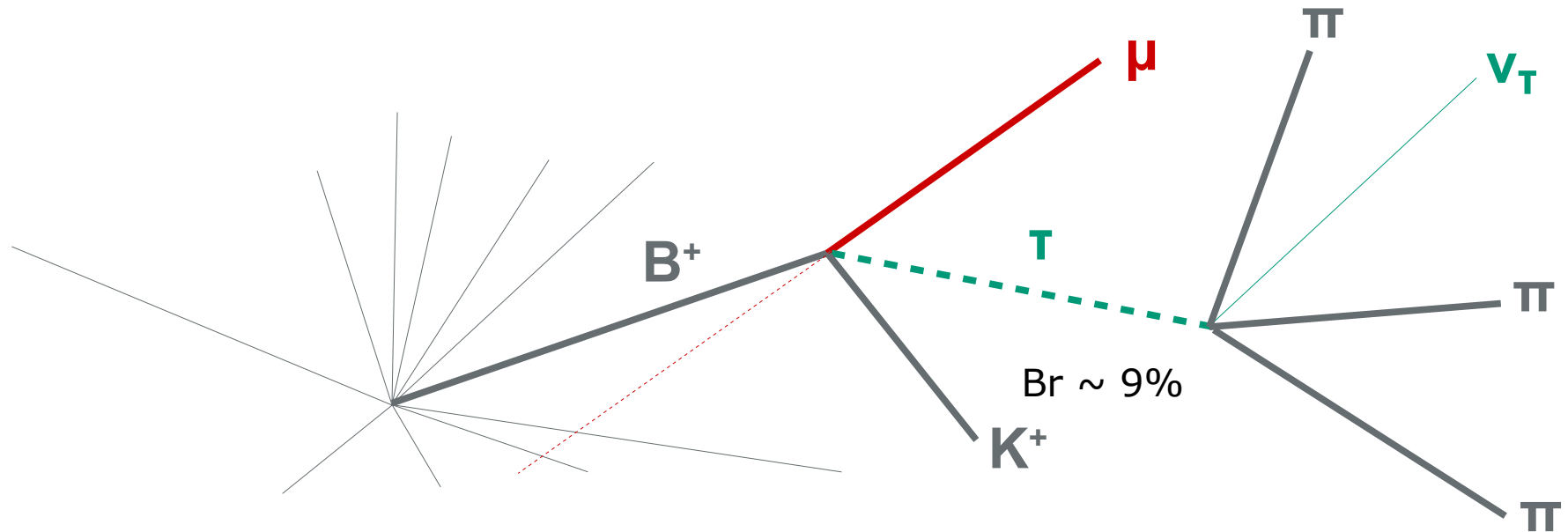


# Challenge #3 : Tau-decay

**Adding an extra charged meson fixes B decay vertex**

“Tags” the presence of the parent meson

CHALLENGE: need to detect 5 particles



$p_{\perp}(\mathbf{v})$  and  $p_{\parallel}(\mathbf{v})$  determined by  $p(\mathbf{3}\pi)$ , but still need to find  $p_{\parallel}(\mathbf{v})$

SOLUTION: could fix **tau** mass and check B mass or v.v.

# Signal & Background

# Signal

## Important S vs B selection criterium : Invariant Mass of Parent

Reconstructed from directly detected particles

**Reminder:** signal significance

$$\rho \equiv S/\sigma(S) = \eta S/\sqrt{(\eta S + \mathbf{k}' \cdot \boldsymbol{\lambda} \cdot B)} \approx \eta S/\sqrt{(\mathbf{k}' \cdot \boldsymbol{\lambda} \cdot B)} \approx \eta/\sqrt{(\mathbf{k}' \cdot \boldsymbol{\lambda} \cdot B)}$$

### Some observations

Narrower window has less background B

→ work hard to get best possible resolution

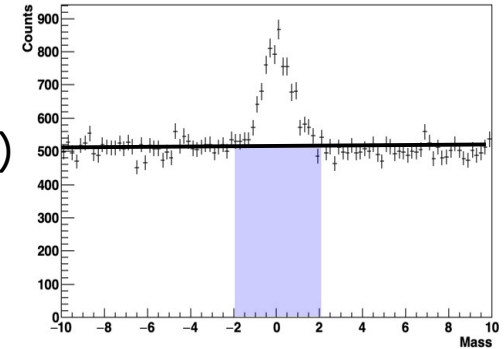
Signal window or fitting range depends on *peak shape*

Shape not trivial, *i.e.* not Gaussian

→ *relative* momentum resolution is mostly constant

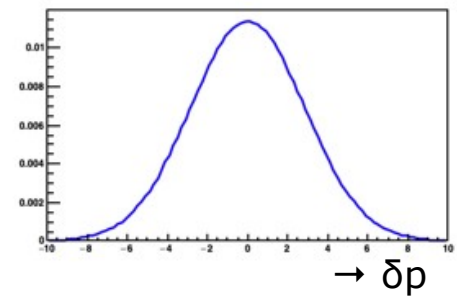
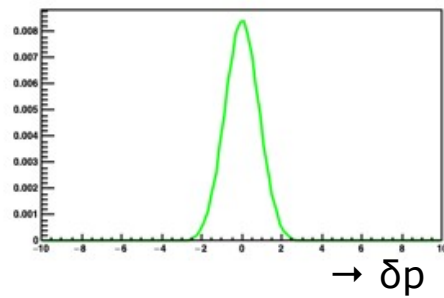
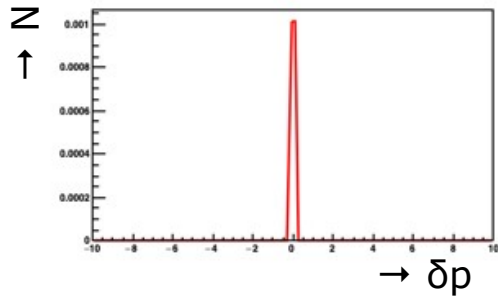
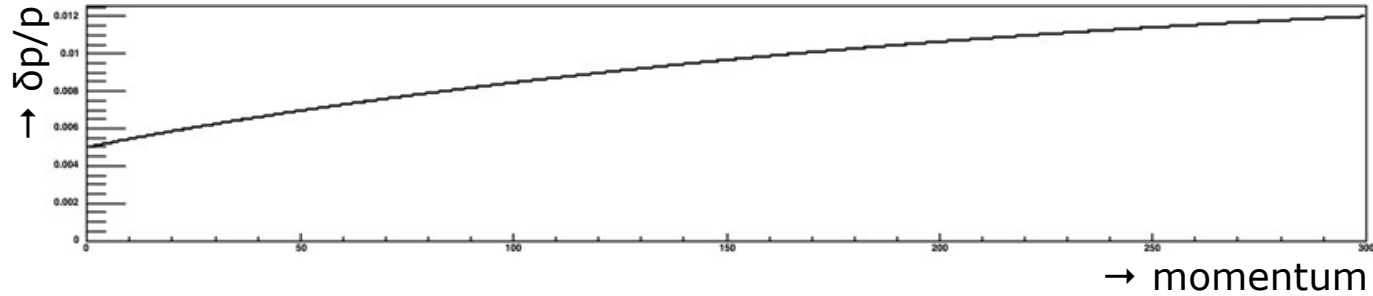
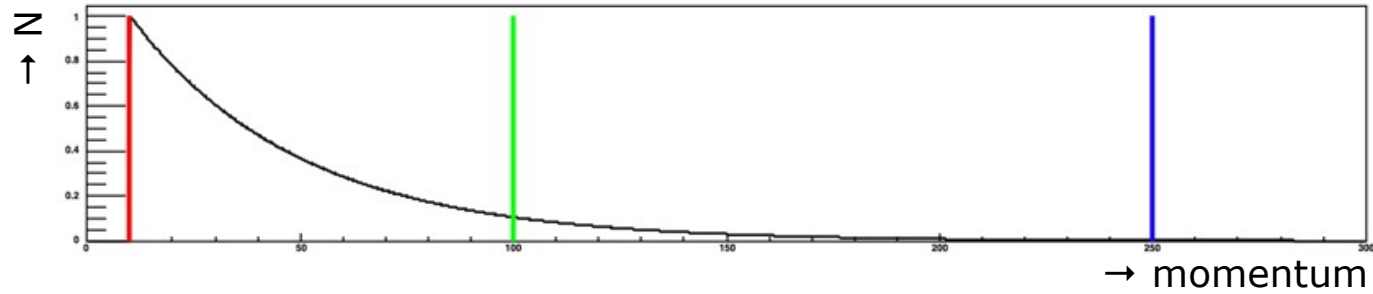
cLFV has no visible peak that can be fit

→ need to determine shape beforehand



**Fix signal shape and fit amplitude to set limit**

# Signal Peak Shape



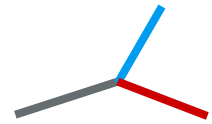
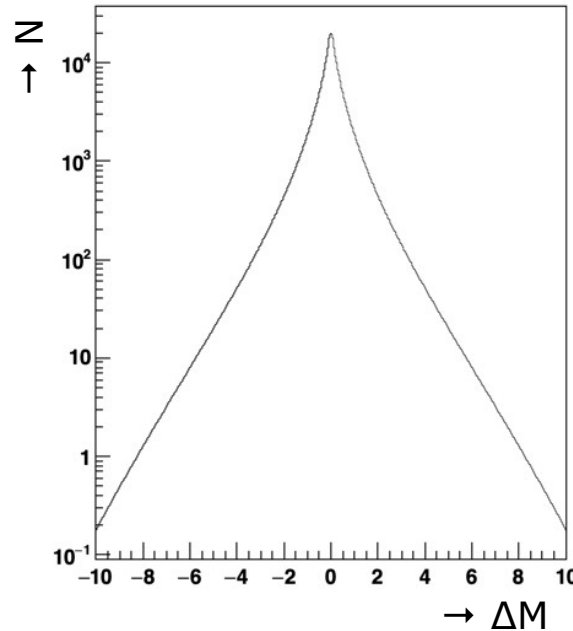
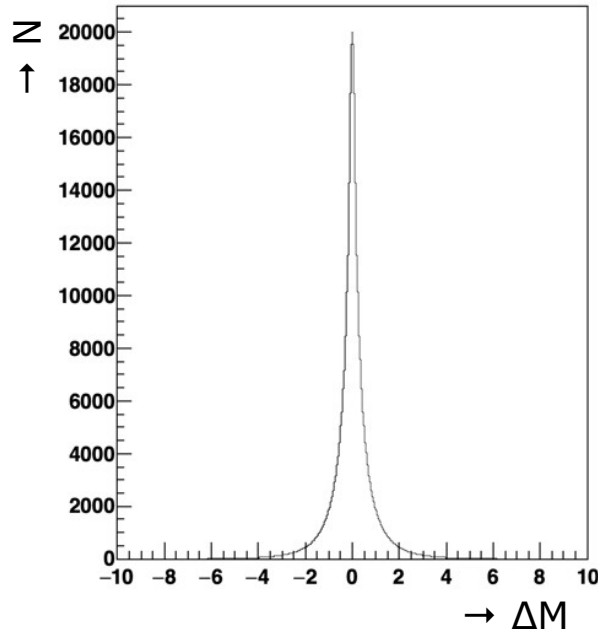
# Signal Peak Shape

**Resulting invariant mass distribution = sum of Gaussians**

Shape depends on (distribution of) momenta of child-particles

Shape depends on (distribution of) angles between momenta

Shape depends on (illuminated part of) detector acceptance





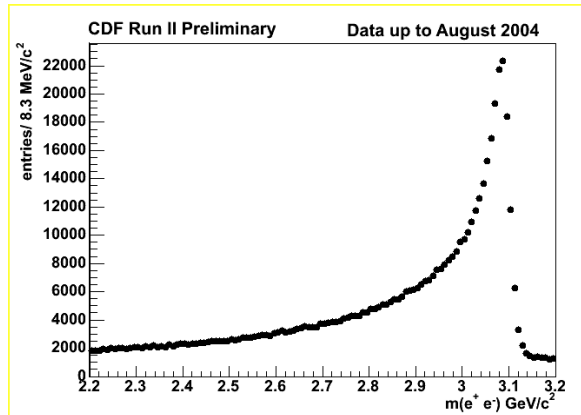
# Signal Peak Shape

## Dealing with Bremsstrahlung

- Incorporate energy lost via photon
- Requires photon energy distribution
- material traversed by electron
- physics behind bremsstrahlung
- via modelling or calibration channel

## Crystal Ball function

- Parametrizes lossy processes
- Nasty to fit



The Crystal Ball function is given by:

$$f(x; \alpha, n, \bar{x}, \sigma) = N \cdot \begin{cases} \exp\left(-\frac{(x-\bar{x})^2}{2\sigma^2}\right), & \text{for } \frac{x-\bar{x}}{\sigma} > -\alpha \\ A \cdot \left(B - \frac{x-\bar{x}}{\sigma}\right)^{-n}, & \text{for } \frac{x-\bar{x}}{\sigma} \leq -\alpha \end{cases}$$

where

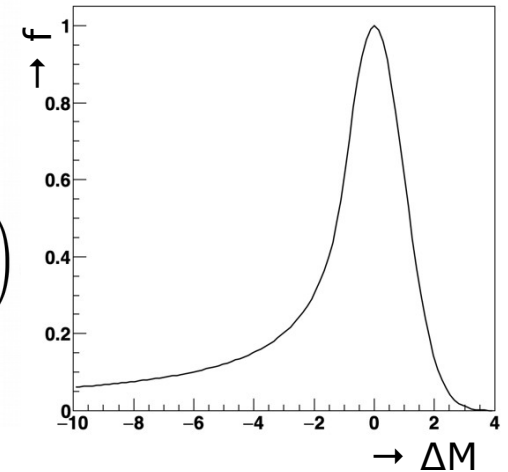
$$A = \left(\frac{n}{|\alpha|}\right)^n \cdot \exp\left(-\frac{|\alpha|^2}{2}\right),$$

$$B = \frac{n}{|\alpha|} - |\alpha|,$$

$$N = \frac{1}{\sigma(C + D)},$$

$$C = \frac{n}{|\alpha|} \cdot \frac{1}{n-1} \cdot \exp\left(-\frac{|\alpha|^2}{2}\right)$$

$$D = \sqrt{\frac{\pi}{2}} \left(1 + \operatorname{erf}\left(\frac{|\alpha|}{\sqrt{2}}\right)\right).$$



# Signal Peak Shape

## Photon recovery

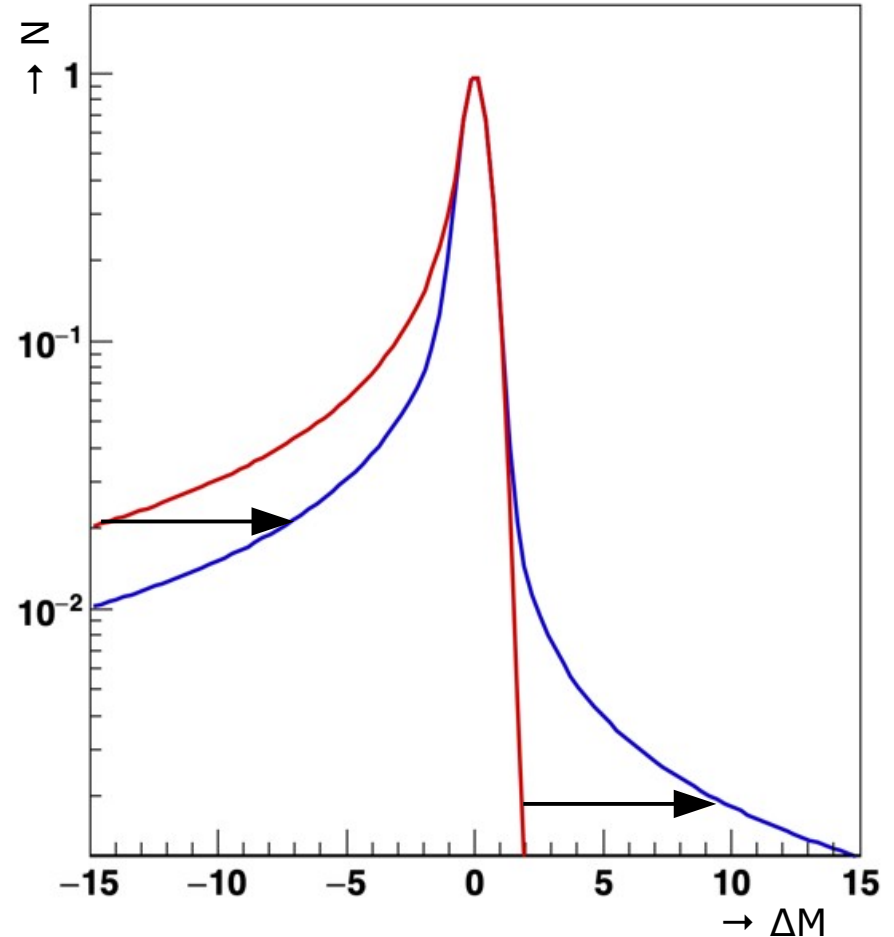
Reduces low-end tail

→ when photon correctly added

Introduces high-end tail

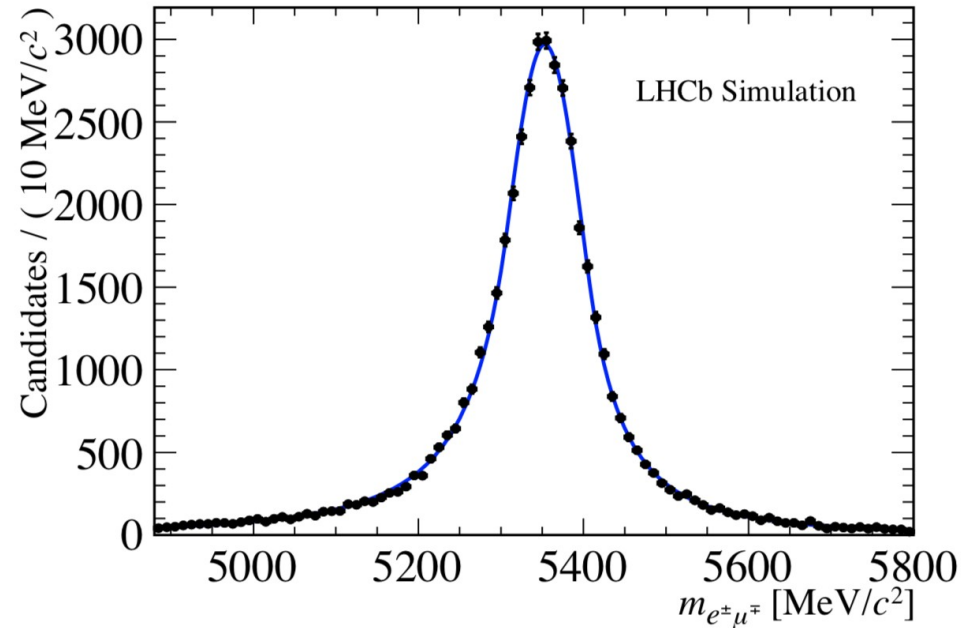
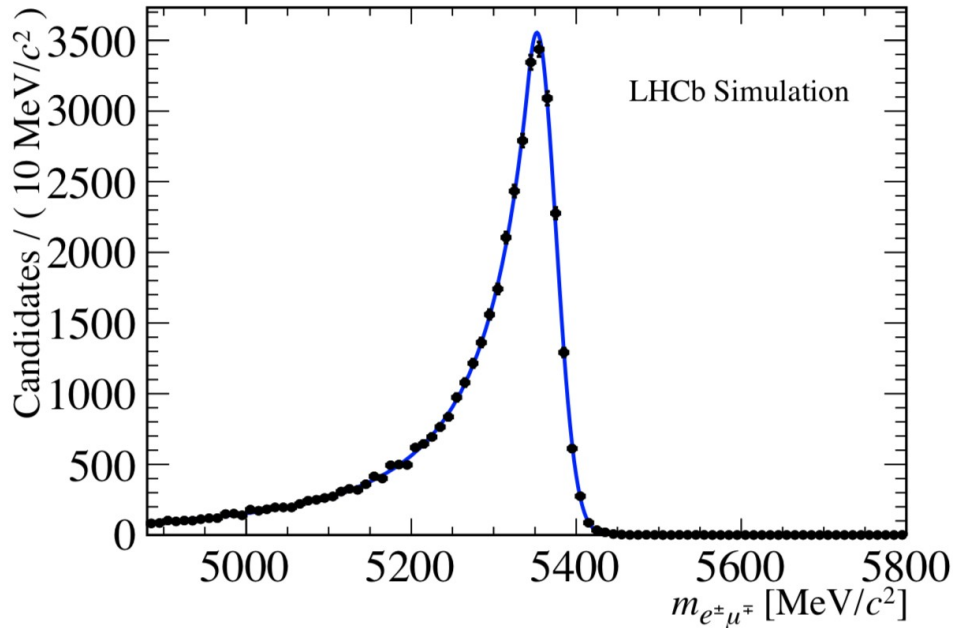
→ when photon incorrectly added

**Overall width decreases**



# Signal Peak Shape

Simulation of  $B_s \rightarrow e\mu$



# Background

## Important S vs B selection criterium : Invariant Mass of Parent

Reconstructed from directly detected particles

**Reminder:** signal significance

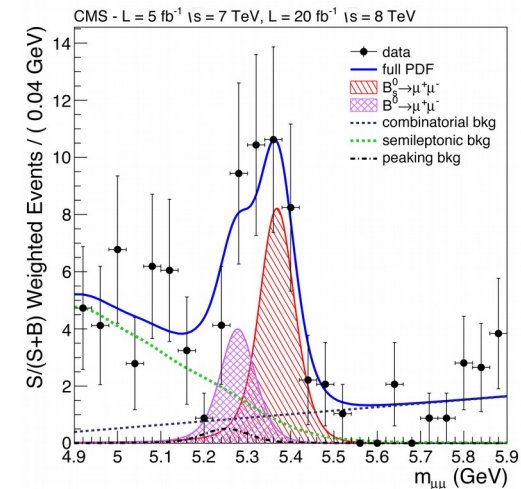
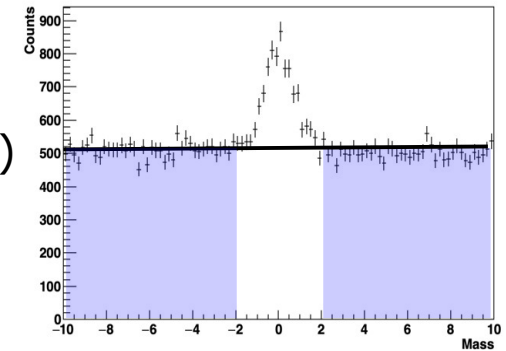
$$\rho \equiv S/\sigma(S) = \eta S/\sqrt{(\eta S + \mathbf{k}' \cdot \boldsymbol{\lambda} \cdot B)} \approx \eta S/\sqrt{(\mathbf{k}' \cdot \boldsymbol{\lambda} \cdot B)} \approx \eta/\sqrt{(\mathbf{k}' \cdot \boldsymbol{\lambda} \cdot B)}$$

### Some observations

Independent determination of B requires "room in tails"  
 → need to understand background shape

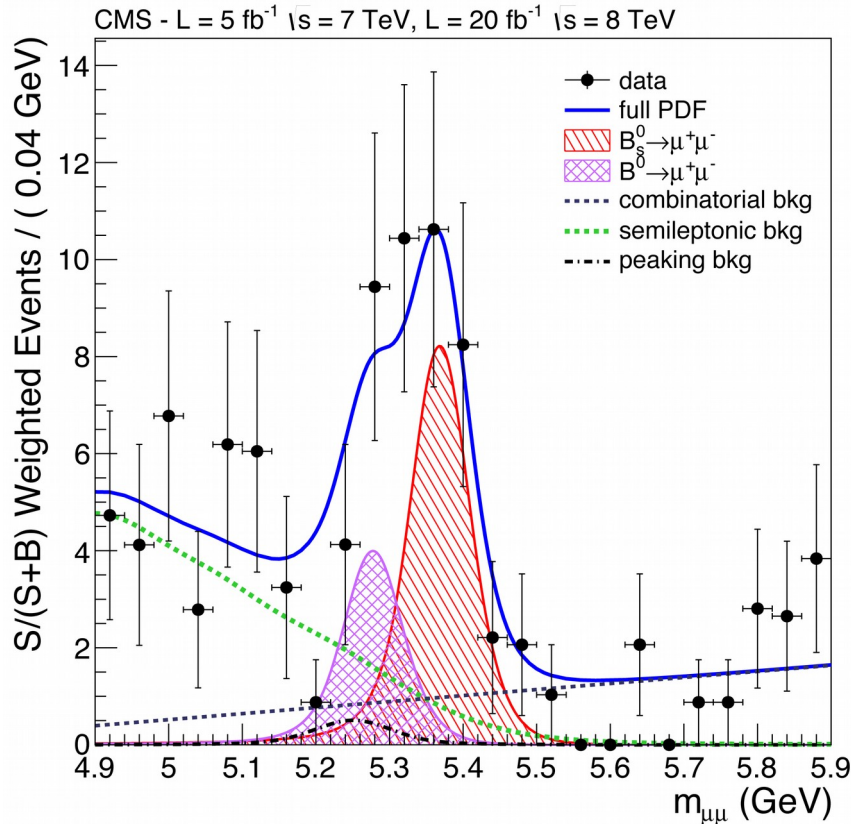
### Types of background

- ▶ Peaking
- ▶ Semi-peaking
- ▶ Smooth



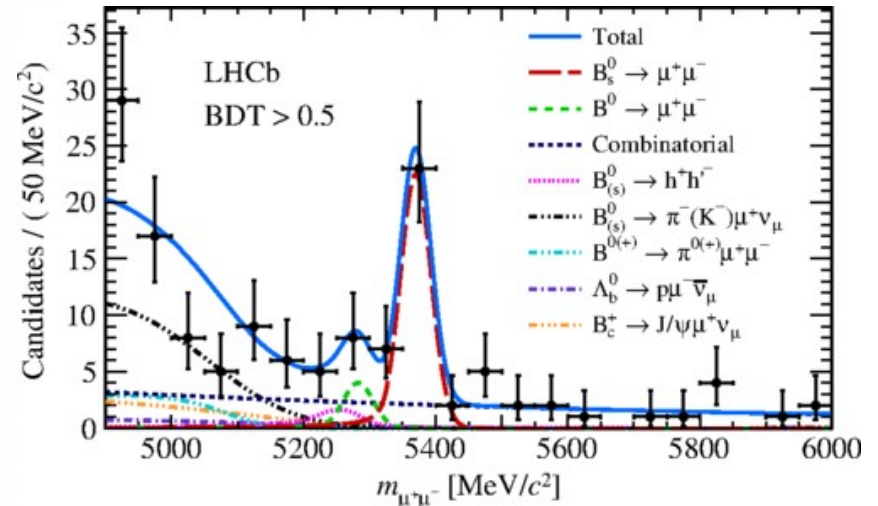
# Peaking Background

Due to another parent with similar mass



**Example:**

$B^0 \rightarrow \mu\mu$   $m(B^0) = 5280 \text{ MeV}$   
 $B_S^0 \rightarrow \mu\mu$   $m(B_S^0) = 5367 \text{ MeV}$



# Peaking Background

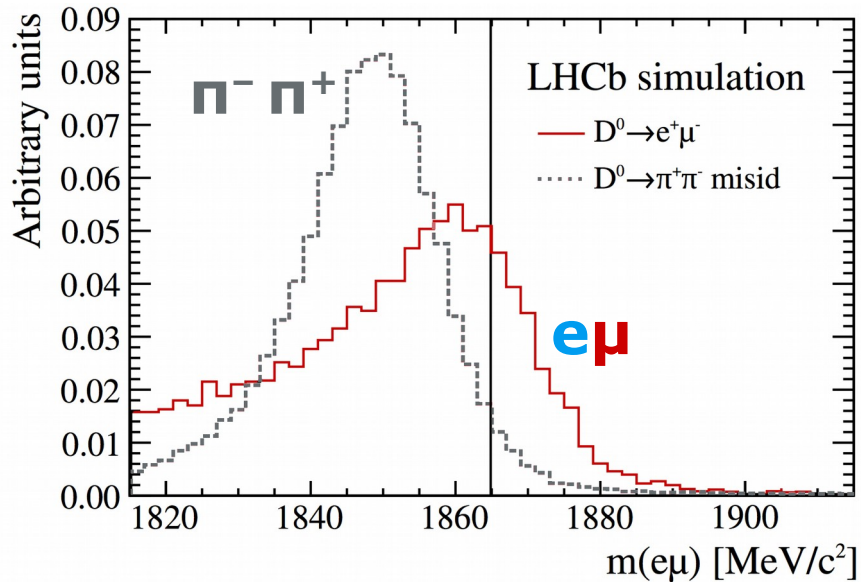
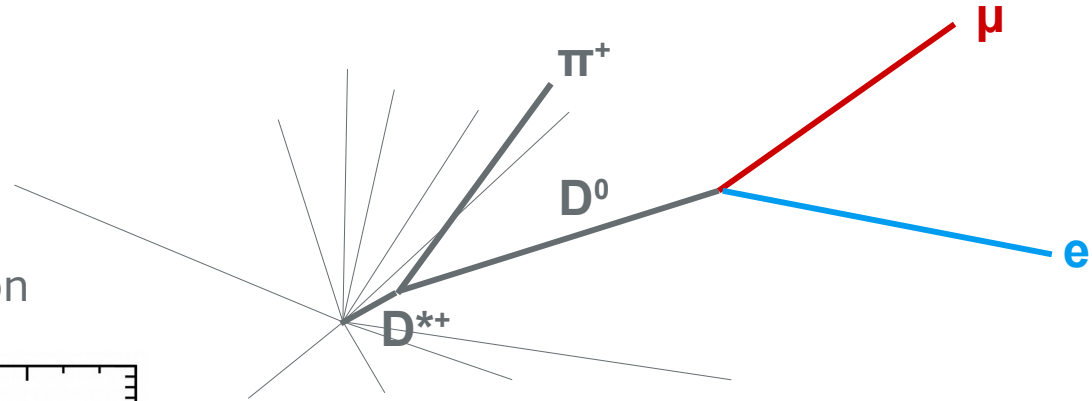
Due to mis-ID

## Example

$$D^{*+} \rightarrow D^0 \pi^+$$

↳  $D^0 \rightarrow e\mu$  Signal

↳  $D^0 \rightarrow K^- \pi^+$  Normalization



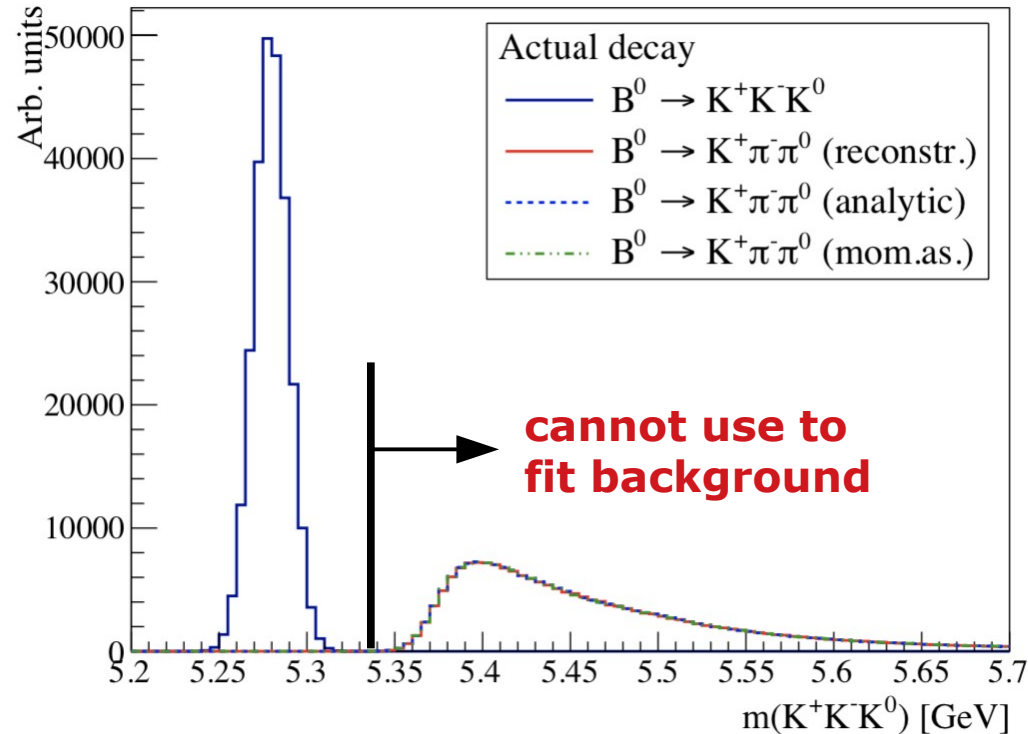
Probability for  
 $\pi^+ \pi^- \rightarrow e\mu$  mis-ID  
 $\sim (1-2) \times 10^{-8}$



# (Semi-)Peaking Background

**Mis-ID events mostly shift away from peak**

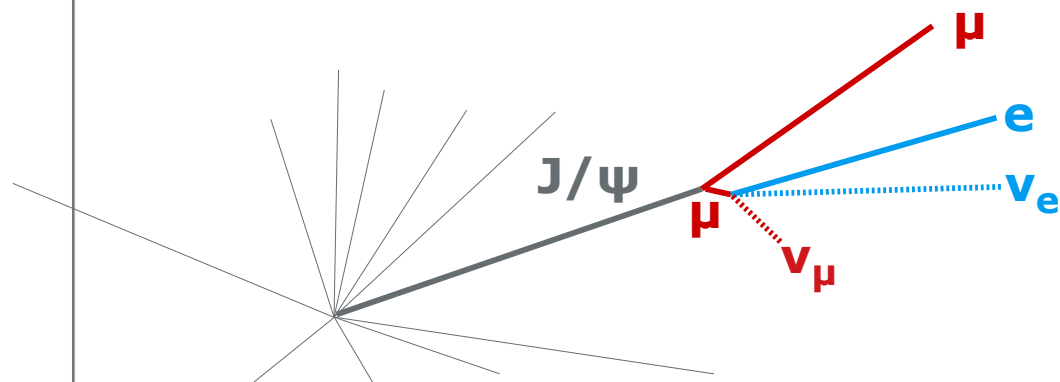
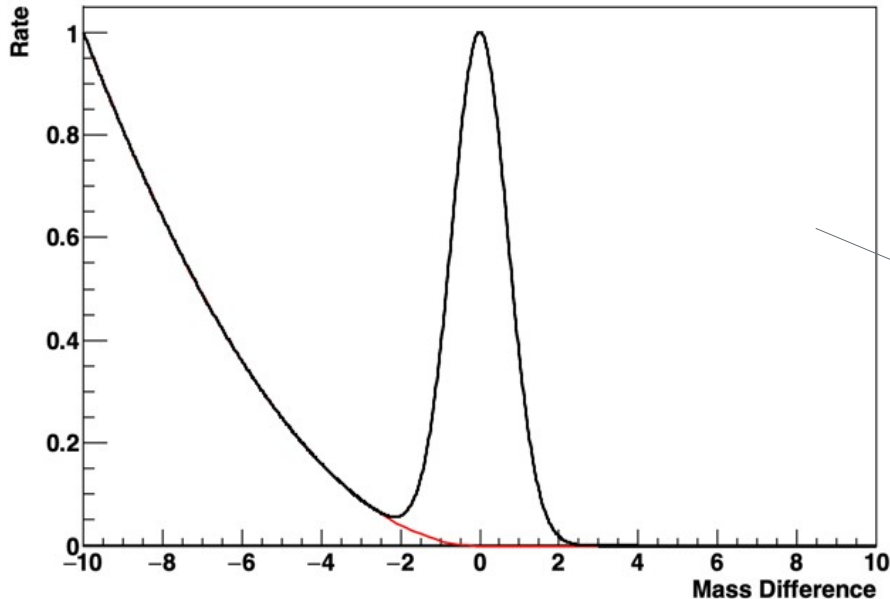
Cannot use high-mass side for background determination  
i.e. without knowing/fitting the shape



# Semi-Peaking Background

Typically due to reaction with one or more missing particles

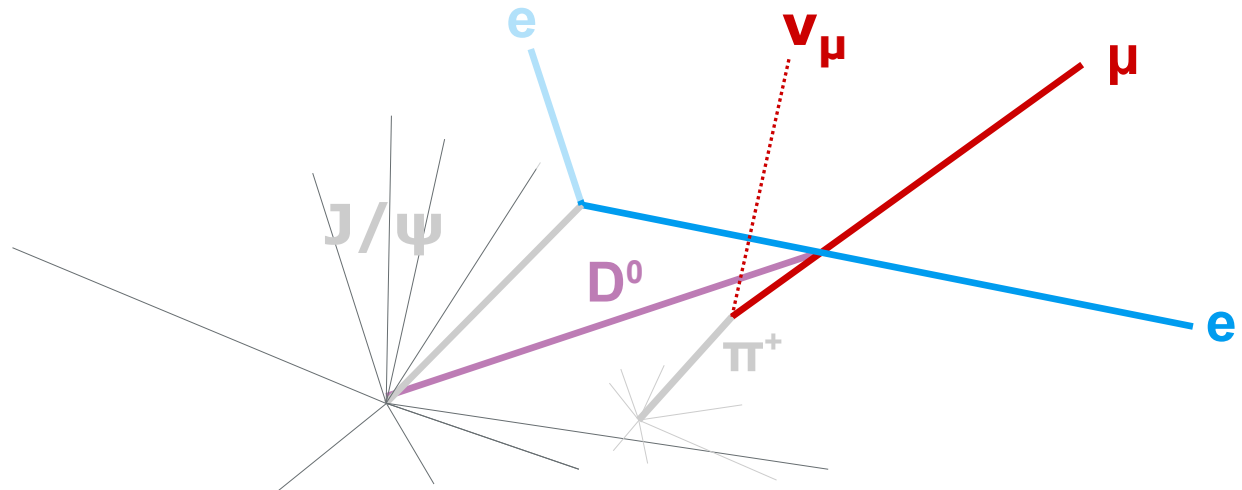
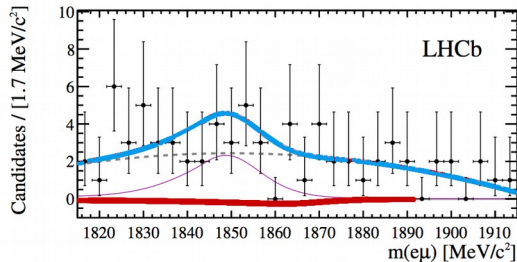
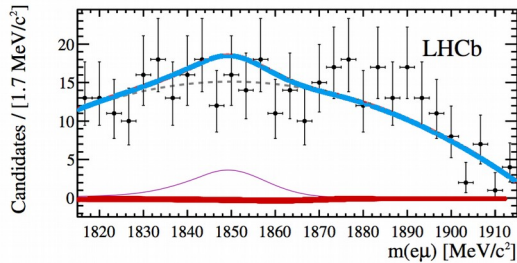
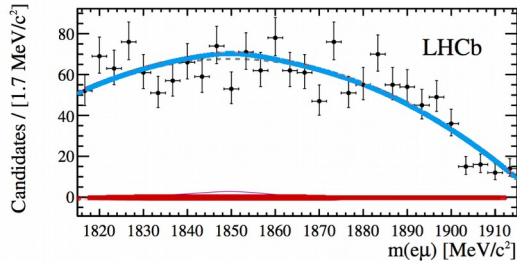
## Example



# Smooth Background

Mainly due to combinatorial background

Particles have no kinematics relation and happen to cross "by accident"  
 Resulting invariant mass distribution featureless  
 More probable in crowded environment  
 Challenging @ LHC, much better @  $e^+e^-$



# Normalisation



# Efficiency



# Interpretation



# LFV Results (2009-2019)

## LHCb

$\tau \rightarrow \mu\mu\mu$	$4.6 \times 10^{-8}$	JHEP 02 (2015) 121
$D^0 \rightarrow e\mu$	$1.3 \times 10^{-8}$	PLB 754 (2016) 167
$B^0_{(s)} \rightarrow e\mu$	$1.0/5.4 \times 10^{-9}$	JHEP 03 (2018) 078
$B^0_{(s)} \rightarrow \mu\tau$	$1.2/3.4 \times 10^{-5}$	arXiv:1905.06614
$h^0 \rightarrow \mu\tau$		EPJ C78 (2018) 1008

## ATLAS / CMS

$Z^0 \rightarrow \mu\tau$	$1.7 \times 10^{-5}$	Eur. Phys. J. C 77 (2017) 70
$H \rightarrow e/\mu\tau$	$6/3 \times 10^{-3}$	JHEP 06 (2018) 001

## BES

$J/\psi \rightarrow e\mu$	$1.6 \times 10^{-7}$	PRD 87 (2013) 112007
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## BaBar

$Y(nS) \rightarrow e/\mu\tau$	$\sim 3 \times 10^{-6}$	PRL 104 (2010) 151802
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## VEPP

$\phi \rightarrow e\mu$	$2 \times 10^{-6}$	PRD 81 (2010) 057102
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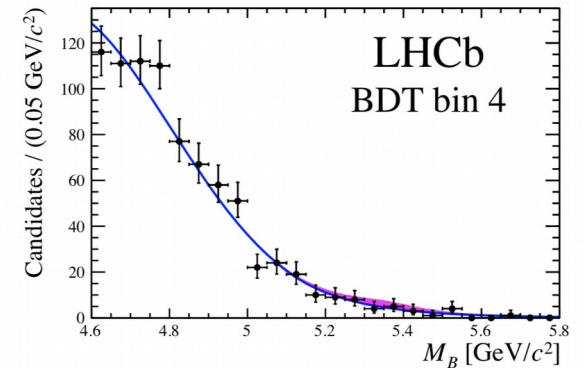
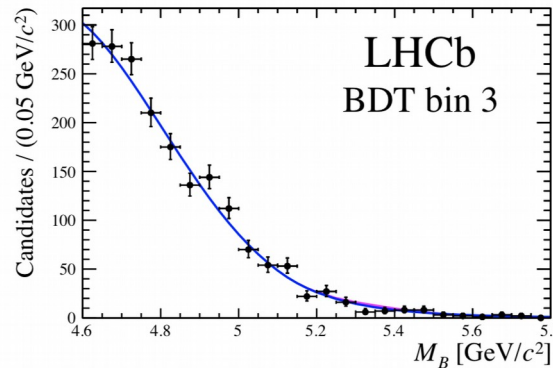
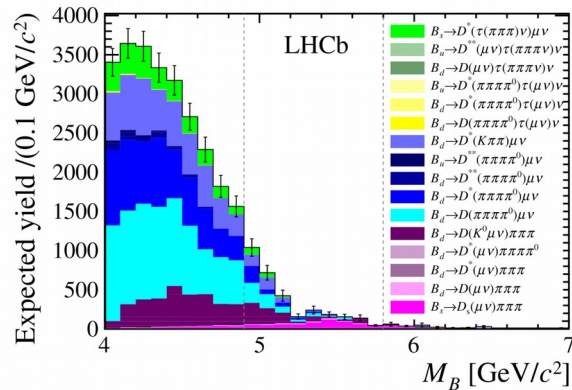
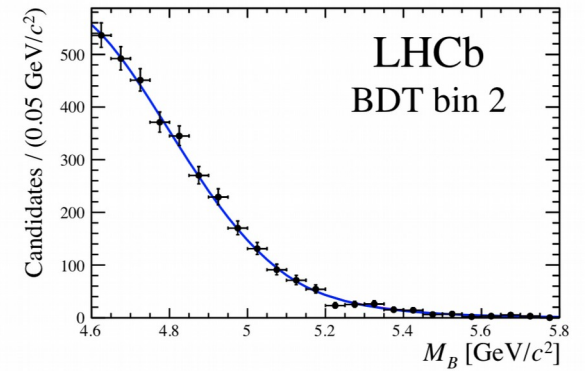
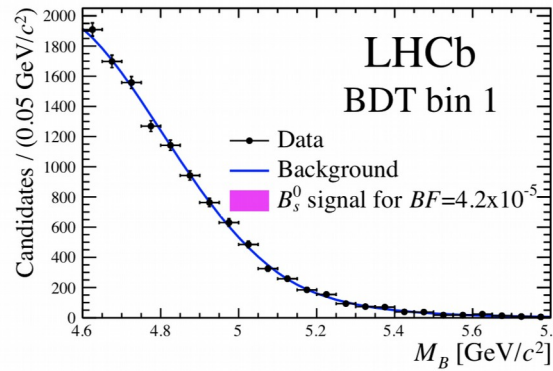
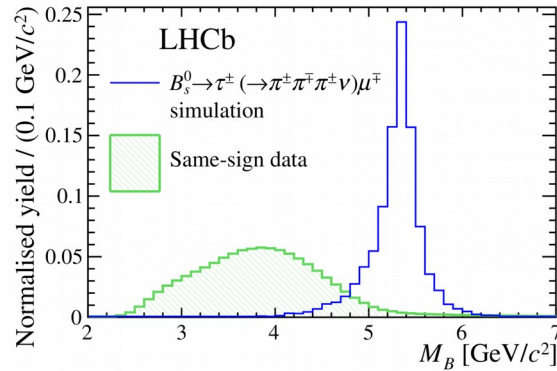
# Latest LFV Result (LHCb)



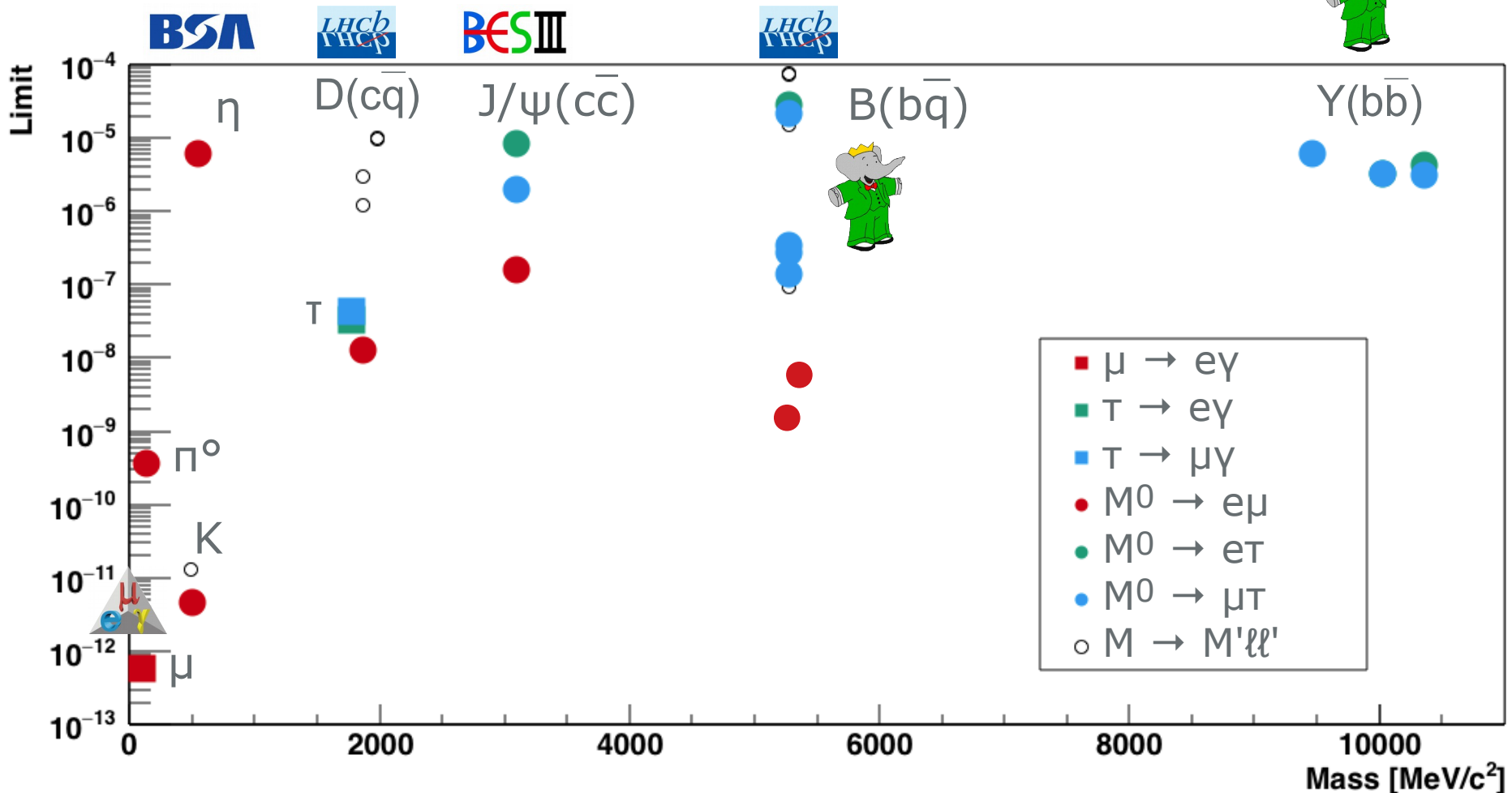
ArXiv:1905.06614

$\text{Br}(B^0_{(s)} \rightarrow \mu\tau) < 1.4/4.2 \times 10^{-5}$  (95% C.L.)

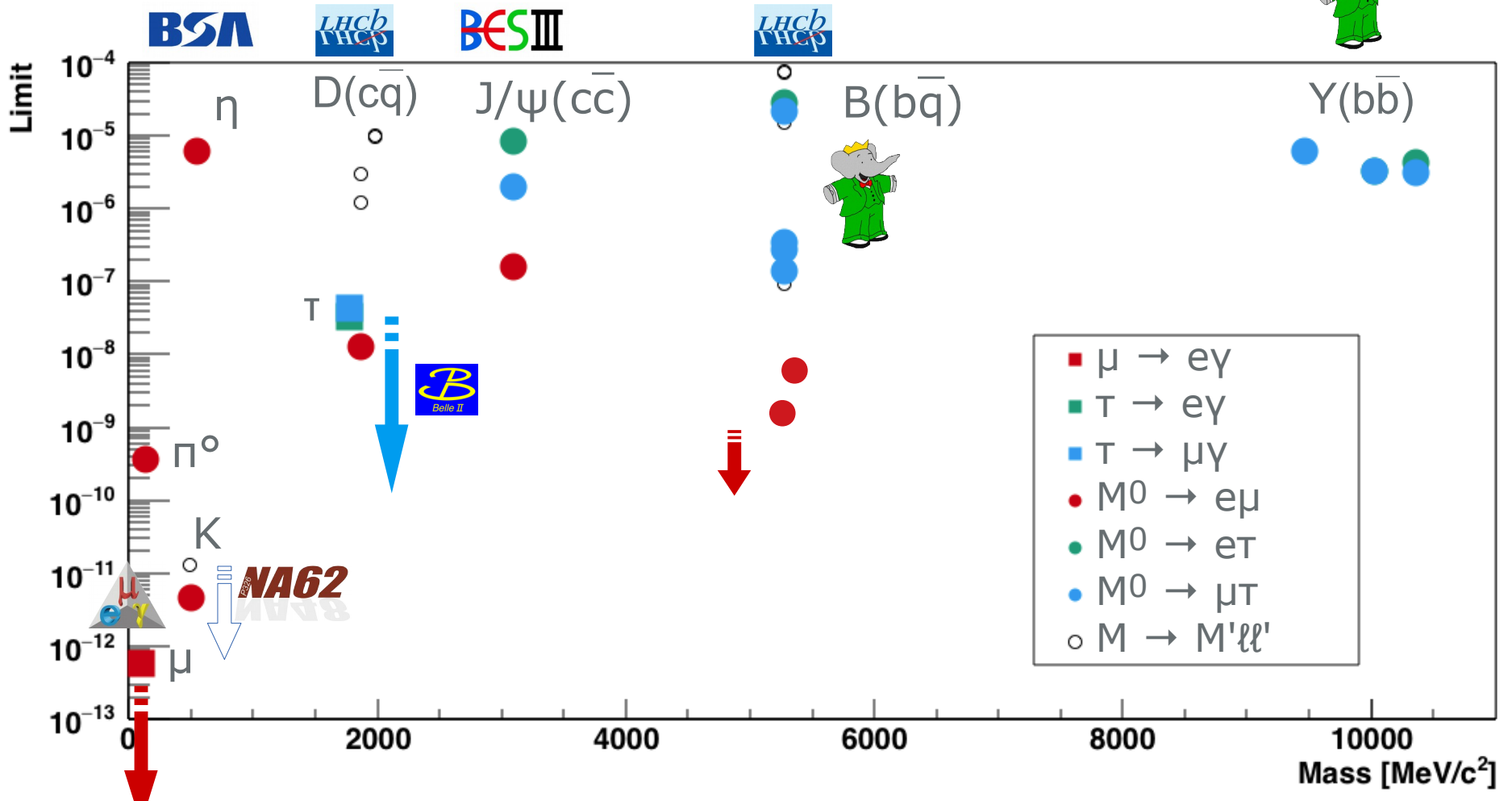
Previous :  $\text{Br}(B^0 \rightarrow \mu\tau) < 3.8 \times 10^{-5}$  (90% C.L.) @ CLEO



# LFV frontier



# LFV frontier (prospects)

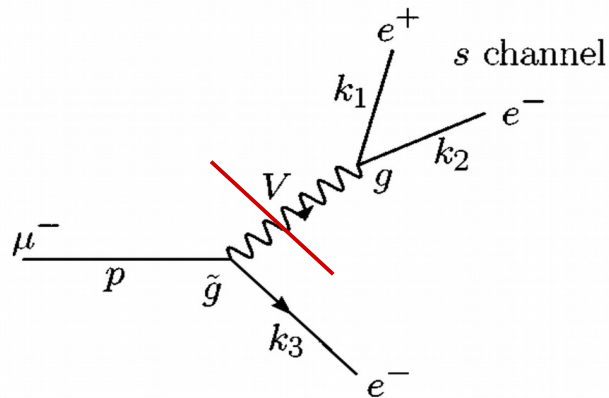


# LFV frontier (intermezzo)

## Unitarity puts rather strong constraints on two-body LFV processes

For example:  $\text{Br}[\tau \rightarrow e \mu \mu] > \text{Br}[\tau \rightarrow e \phi] \cdot \text{Br}[\phi \rightarrow \mu \mu] \approx 3 \cdot 10^{-4} \cdot \text{Br}[\tau \rightarrow e \phi]$

Thus (stringent) bound on  $\text{Br}[\tau \rightarrow e \mu \mu]$  produces a limit on  $\text{Br}[\tau \rightarrow e \phi]$



$$\text{Br}[\mu \rightarrow e e e] < 10^{-12}$$

$$\blacktriangleright \text{Br}[\phi \rightarrow e \mu] < 4 \cdot 10^{-17}$$

$$\blacktriangleright \text{Br}[J/\psi \rightarrow e \mu] < 4 \cdot 10^{-13}$$

$$\blacktriangleright \text{Br}[\Upsilon \rightarrow e \mu] < 2 \cdot 10^{-9}$$

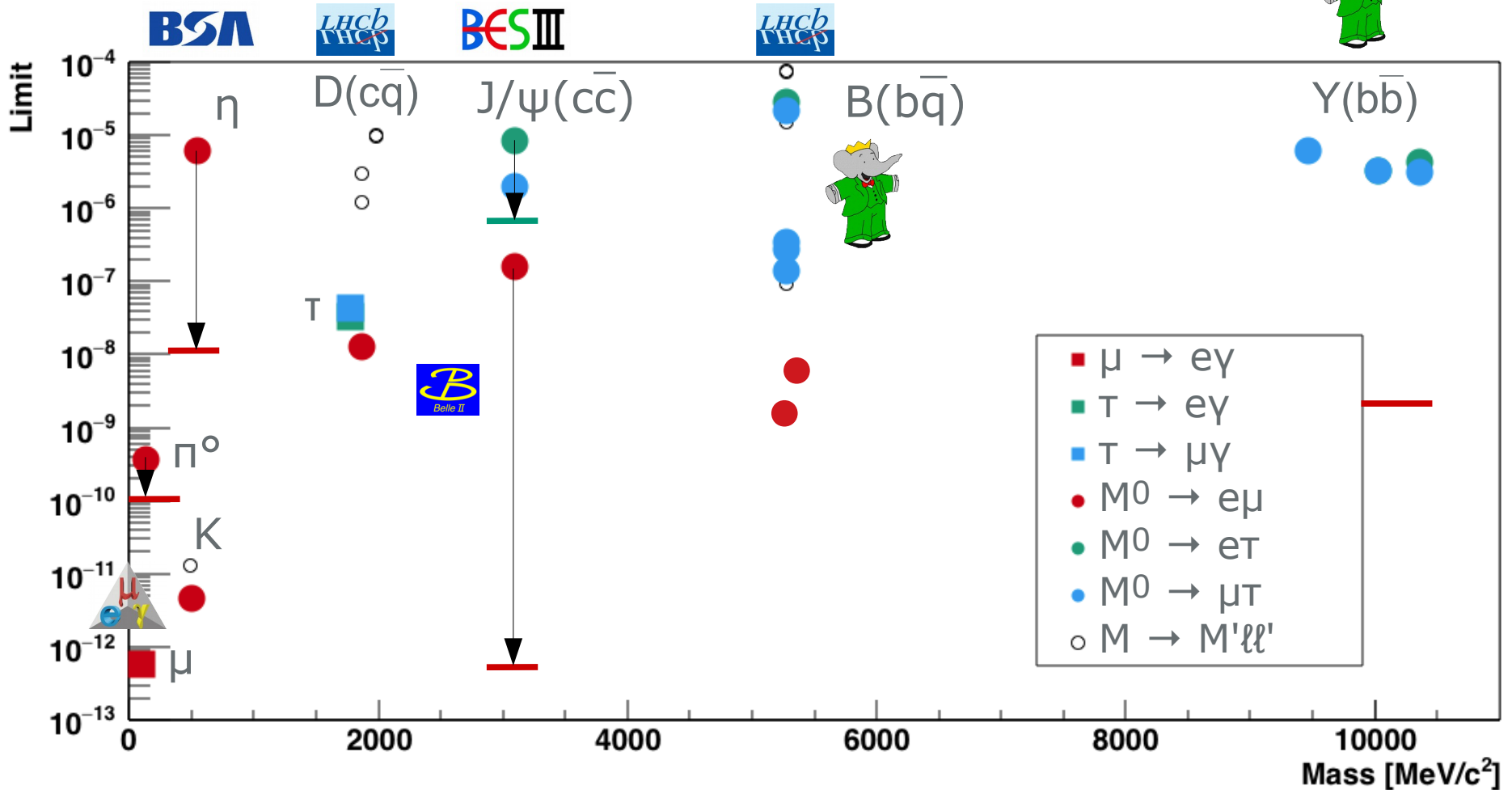
$$\text{Br}[\mu \rightarrow e \gamma \gamma] < 10^{-10}$$

$$\blacktriangleright \text{Br}[\pi^0 \rightarrow e \mu] < 10^{-10}$$

$$\blacktriangleright \text{Br}[\eta \rightarrow e \mu] < 10^{-8}$$

CAVEAT: indirect bounds (somewhat) model dependent; also other relations

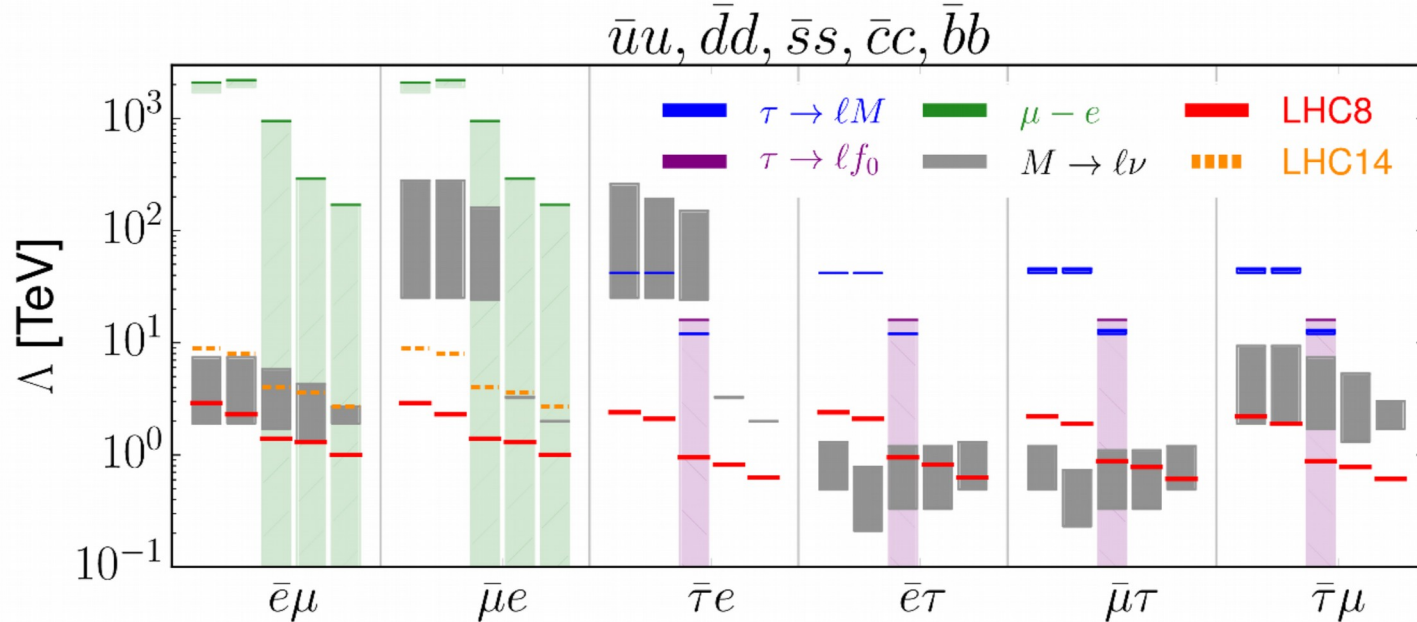
# LFV frontier (directions)





# LHC & low energy

**Ten different gauge invariant operators with 2 quarks and 2 leptons**  
 Quote limits in terms of cutoff scale  $\Lambda$  of effective operators



**Figure 5.** Summary plots of most stringent limits from precision experiments and the LHC. See the text for a detailed explanation.

# LHC & low energy

## Ten different gauge invariant operators with 2 quarks and 2 leptons

Quote limits in terms of cutoff scale  $\Lambda$  of effective operators

### 7 Conclusions

From the comprehensive case study in this work, we see that precision measurements and the LHC study are indeed complementary. Which experiment gives the best reach depends on both the quark flavour and the lepton pair in the operator. For light quarks  $u$ ,  $d$  and  $s$ , precision measurements clearly outperform the LHC irrespective of the charged lepton flavour. However, the LHC becomes competitive for heavier quarks,  $c$  and  $b$ , and there is an interesting interplay between the two approaches to obtain limits on LFV operators with two quarks and two leptons. Operators with  $e\mu$  are still highly constrained by precision measurements, particularly  $\mu$ - $e$  conversion in nuclei, but the LHC competes for LFV operators with right-handed  $\tau$  leptons and can set limits independent of the phase of the Wilson coefficient. We set a lower limit of 600–800 GeV on the cutoff scale of all these operators.

# Personal outlook

## Charm

$$D_{(s)} \rightarrow e\mu$$

will improve 10-100x @ LHCb

$$D_{(s)} \rightarrow e\mu\gamma$$

lifts helicity suppression, costs  $\alpha$ , need  $E_\gamma$  threshold

$$D^+ \rightarrow K^+ e\mu$$

lower efficiency, tighter mass-peak?

## Bottom

$$B_{(s)} \rightarrow e\mu$$

will improve 10-100x @ LHCb

$$B_{(s)} \rightarrow \mu\tau$$

will improve 10x @ LHCb

$$B_{(s)} \rightarrow e\mu\gamma$$

lifts helicity suppression, costs  $\alpha$ , need  $E_\gamma$  threshold

$$B_{(s)} \rightarrow K^{*0}(K^+\pi^-) e/\mu/\tau(3\pi) \text{ for least unconstrained tau decay}$$

$$B_{(c)}^+ \rightarrow (K/D)^+ e/\mu/\tau \text{ heaviest open-flavour meson}$$

## Baryons

$$\Lambda_b \rightarrow \Lambda(p\pi) e\mu$$

production cross section  $\sigma(\Lambda_b)/\sigma(B) \sim 0.1 - 1$

# Final words

**Search for cLFV @ colliders is certainly possible**

**Experiment design an art, with many subtleties to take into account**

**Can benefit from developments in hadronic + SM research**

**Relation between low-E and high-E cLFV results exist**

**Such relations are model-dependent**

**Just do it!**