



university of
 groningen

faculty of science
 and engineering

van swinderen institute for
 particle physics and gravity

cLFV in Meson Decays

– at high energy colliders –



中國科學院高能物理研究所
Institute of High Energy Physics
Chinese Academy of Sciences

Gerco Onderwater

International School on cLFV 2019 – IHEP Beijing

Who am I?

1993-1998 : VU/NIKHEF Amsterdam

Hadron group at the AmPS facility

1998-2004 : Univ. of Illinois at Urbana-Champaign

Precision Physics Group

Several low-energy “precision” experiments,
incl. muon $g-2$, EDM & lifetime @ BNL & PSI

2004-now : Univ. of Groningen

Van Swinderen Institute for Particle Physics & Gravity

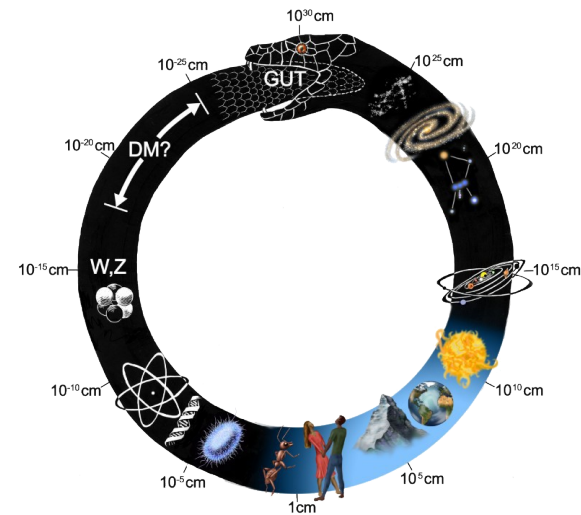
Experimental Particle Physics Group

C, P, & T: EDM (μ, p, d, Ra, Xe), Ra^+APV , β -decay, SrF

LIV : ^{20}Na & Λ -decay, $d\tau/d\Omega$

LFV : $B_{(s)} \rightarrow e\mu$, $\Lambda_b \rightarrow \Lambda e\mu$

LU : Muon $g-2$



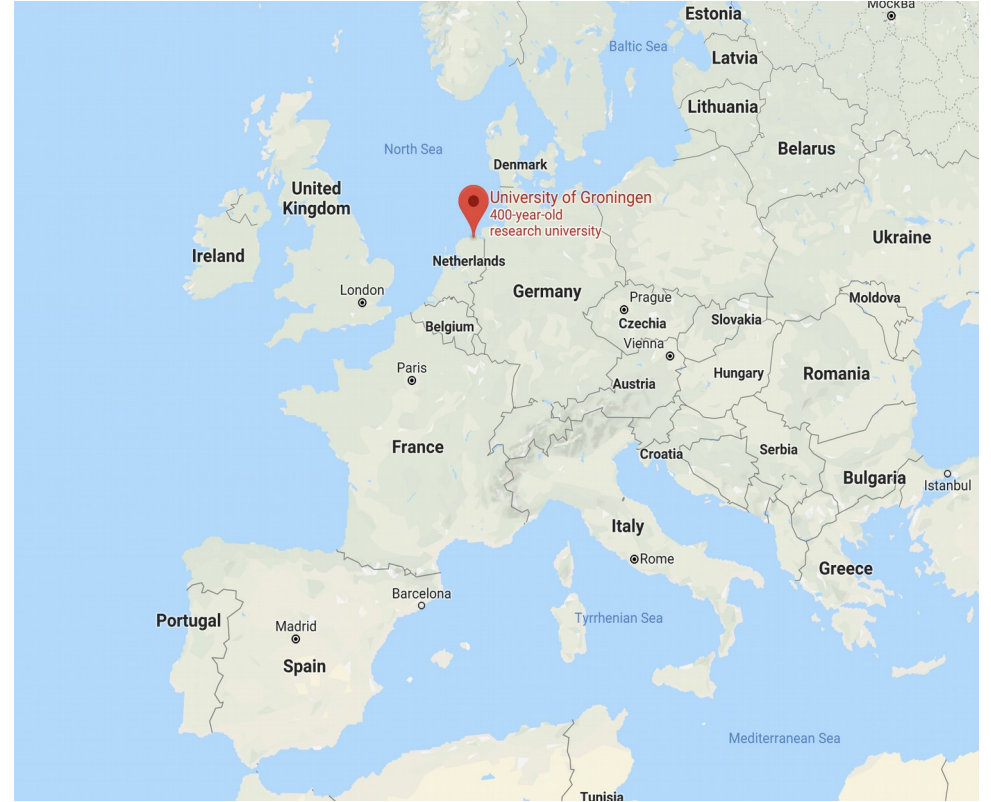
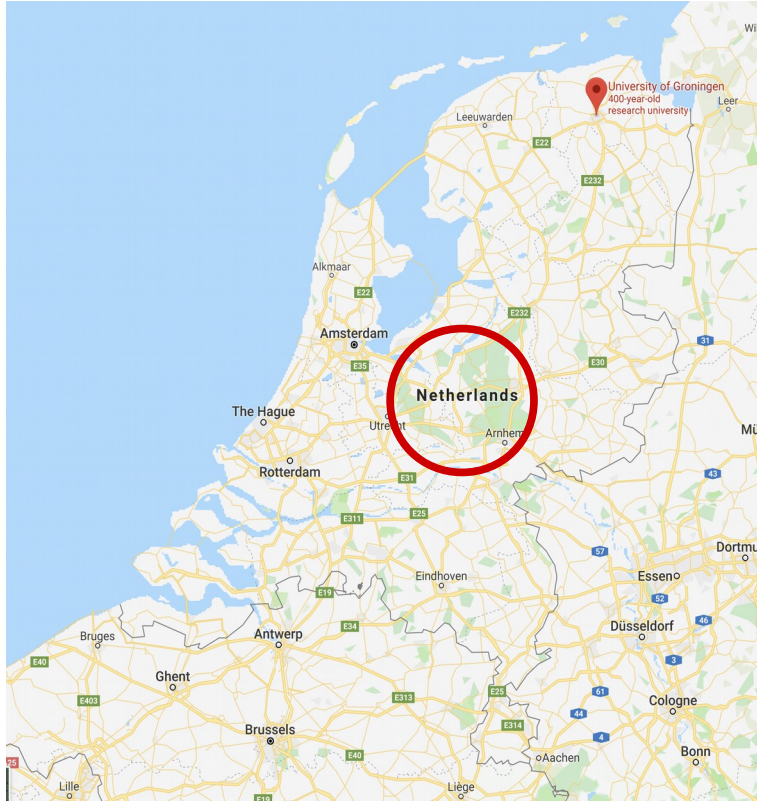
My research



University of Groningen



Groningen, the Netherlands



Outline

Goal

by the end of my lectures, you can formulate how cLFV appears in meson decays, what the essential steps are in the experimental searches, and how to interpret the result in relation to other cLFV searches

Topics to cover

cLFV in meson & baryon decay

Sensitivity & Selectivity

Hadron production

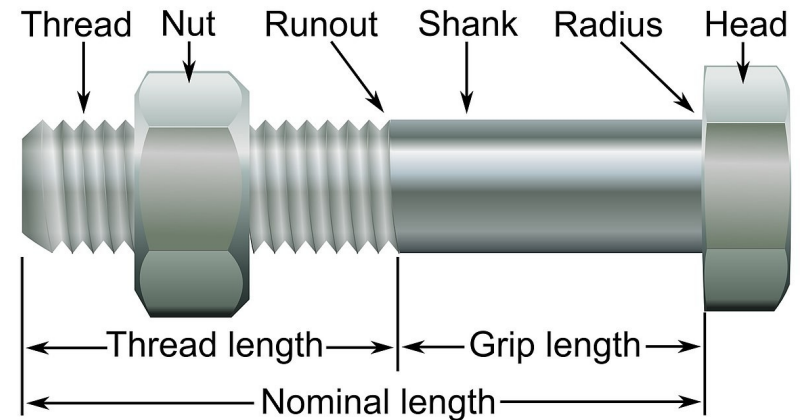
Particle identification

Signal & background: invariant mass spectrum

Normalisation

Efficiency

Interpretation



cLFV in hadron decay

Convention

e

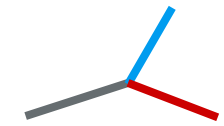
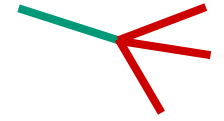
μ

T

Towards studying (c)LFV

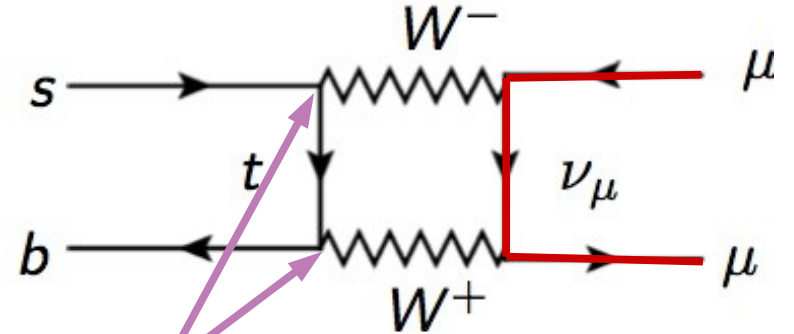
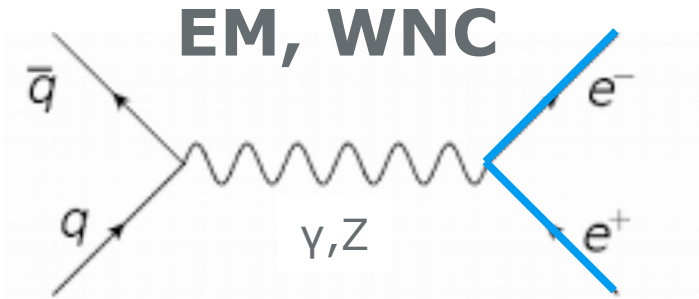
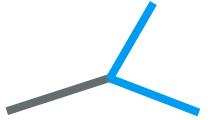
----- Lorenzo Calibbi -----

| | |
|-------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Decay | <i>Angela Papa Kiyoshi Hayasaka</i> $\mu \rightarrow e\gamma, \mu \rightarrow eee, \tau \rightarrow \mu\mu\mu, \tau \rightarrow \mu hh, \dots$ |
| Conversion | $\mu A \rightarrow eA$ <i>David Hitlin</i> |
| Production | $B_s \rightarrow e\mu, B \rightarrow Ke\mu, \Lambda_b \rightarrow \Lambda e\mu, h^0 \rightarrow \mu\tau, \dots$ |
| Oscillation | $\nu_e \leftrightarrow \nu_\mu \leftrightarrow \nu_\tau, M(\mu^+e^-) \leftrightarrow \bar{M}(\mu^-e^+)$ |
| Number violation | $0\nu 2\beta, B^- \rightarrow \pi^+ \mu^- \mu^-, \dots$ |
| Non-Universality | $\bar{B}^0 \rightarrow D^{*+} \tau^- \bar{\nu}_\tau$ vs $\bar{B}^0 \rightarrow D^{*+} \mu^- \bar{\nu}_\mu, g_e$ vs g_μ, \dots <i>Sébastien Descotes-Genon Tsutomu Mibe</i> |

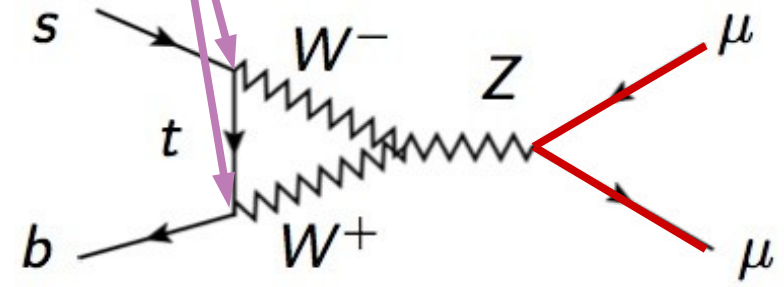
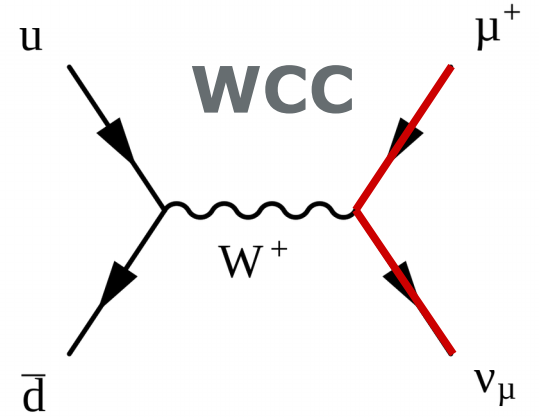


(charges dropped, unless relevant)

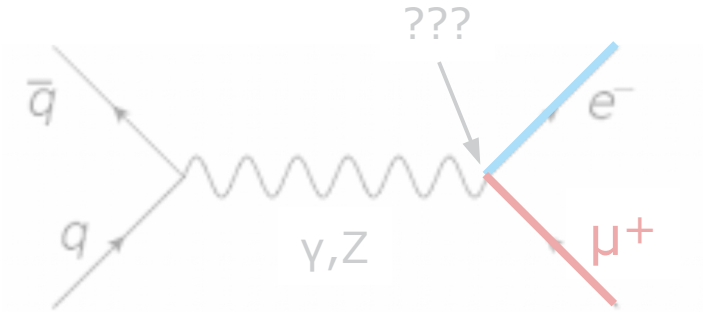
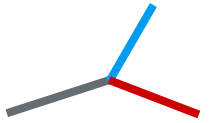
Leptonic meson decay in SM



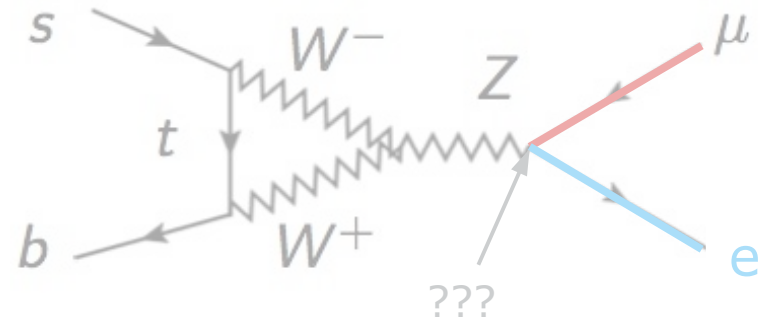
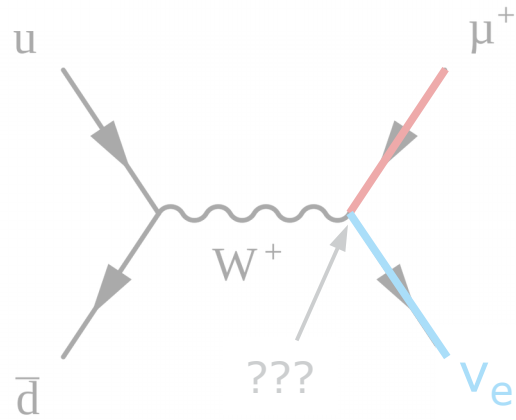
CKM "FCNC"



Leptonic meson decay in SM



PMNS



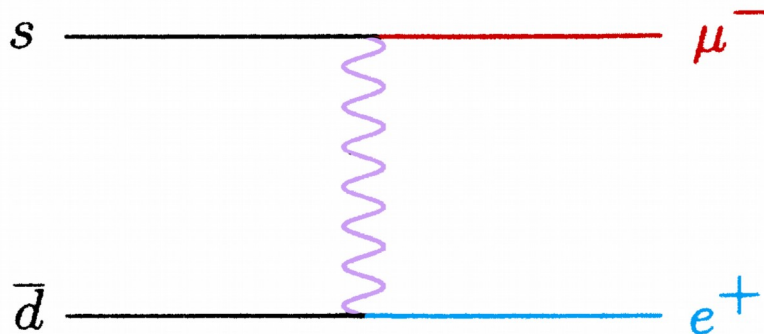
Leptonic meson decay post-SM

Standard Model cLFV

Only possible via neutrino oscillations
 Unmeasureably small

Beyond Standard Model Physics

(Too) many well-motivated possibilities
 Many produce results within reach of experiment
 Experiments put stringents limits on them
E.g., **quark-lepton unification*** with lepto-quarks:



THERE ARE KNOWN KNOWNNS
 THERE ARE THINGS THAT WE KNOW THAT WE KNOW, THERE ARE
KNOWN UNKNOWNNS
 THAT IS TO SAY, THERE ARE
 THINGS THAT WE NOW KNOW WE DON'T KNOW
 BUT THERE ARE ALSO
UNKNOWN UNKNOWNNS
 THERE ARE THINGS
WE DO NOT KNOW
WE DON'T KNOW
 AND EACH YEAR WE DISCOVER
 A FEW MORE OF THOSE
UNKNOWN
UNKNOWNNS

*<https://doi.org/10.1103/PhysRevD.50.6843>

Sensitivity & Selectivity

Some definitions

In designing an experiment two properties to be considered:

Sensitivity

Also known as *true positive rate*, *probability of detection*, or *efficiency*

“If the process occurs, what fraction of events do we actually see?”

In other words, your ability to identify and measure the signal

Selectivity

Also known as *specificity*, or *true negative rate*

“If another process occurs, what fractions of events are labeled as such?”

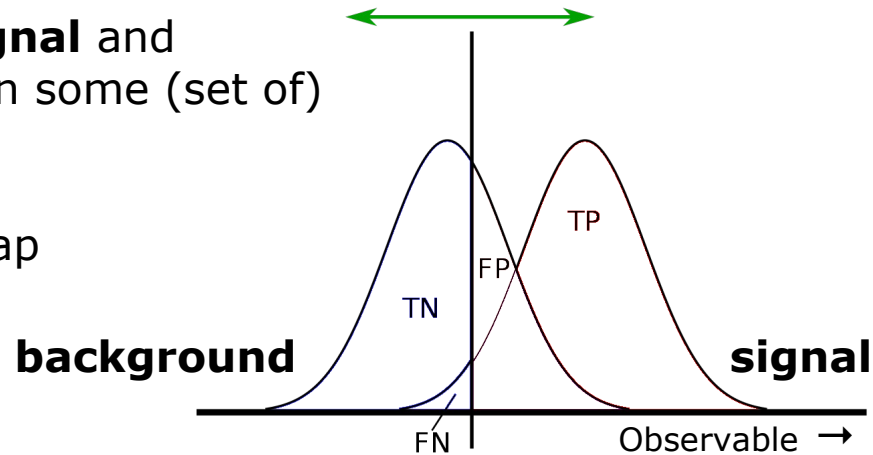
In other words, your ability to identify and eliminate background

Typically **sensitivity** and **selectivity** are mutually exclusive

Contingency table and ROC curve

Need to distinguish **signal** and **background**, based on some (set of) observable(s)

Signatures often overlap



Contingency table and ROC curve

Need to distinguish **signal** and **background**, based on some (set of) observable(s)

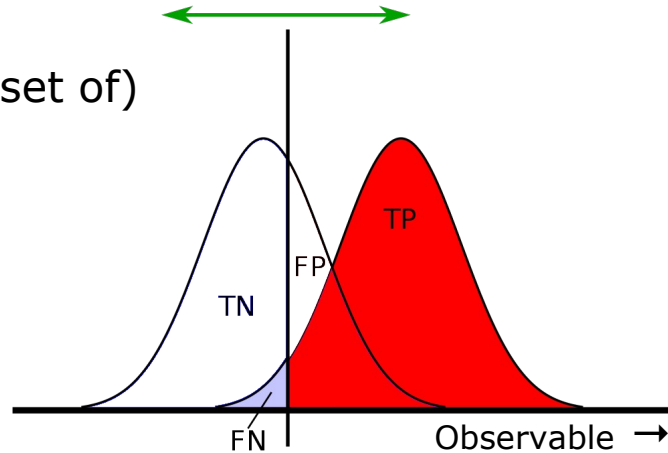
Signatures often overlap

Goal

Maximize **TRUE POSITIVE η**

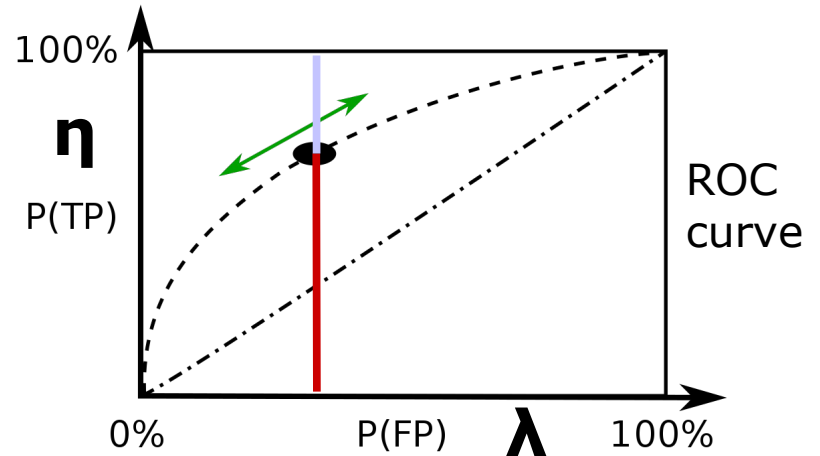
Side effect

Reduced efficiency (**FALSE NEGATIVE**)



| | |
|----|----|
| TP | FP |
| FN | TN |

contingency table



ROC curve

Contingency table and ROC curve

Need to distinguish **signal** and **background**, based on some (set of) observable(s)

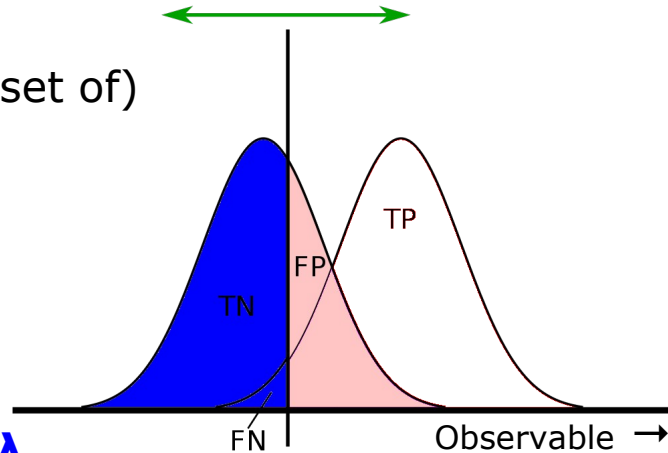
Signatures often overlap

Goal

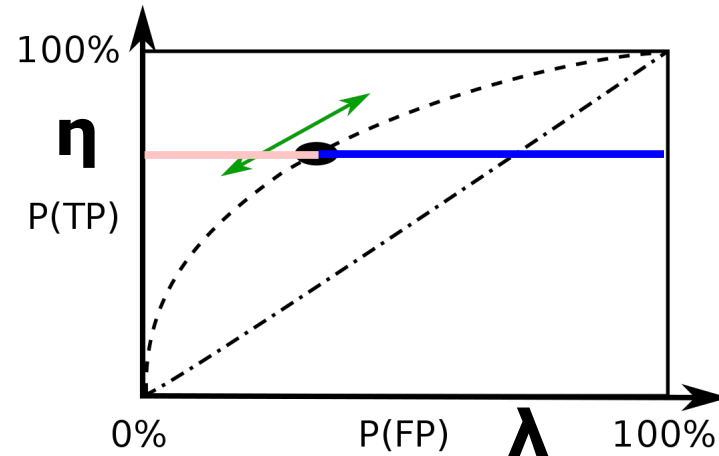
Maximize **TRUE POSITIVE η**
 Maximize **TRUE NEGATIVE $1-\lambda$**

Side effect

Reduced efficiency (**FALSE NEGATIVE**)
 Noise leakage (**FALSE POSITIVE**)



| | |
|----|----|
| TP | FP |
| FN | TN |



Contingency table and ROC curve

Need to distinguish **signal** and **background**, based on some (set of) observables

Signatures often overlap

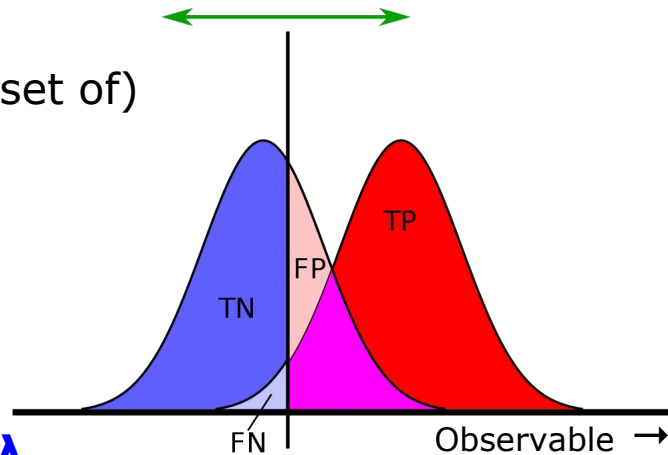
Goal

Maximize **TRUE POSITIVE η**
 Maximize **TRUE NEGATIVE $1-\lambda$**

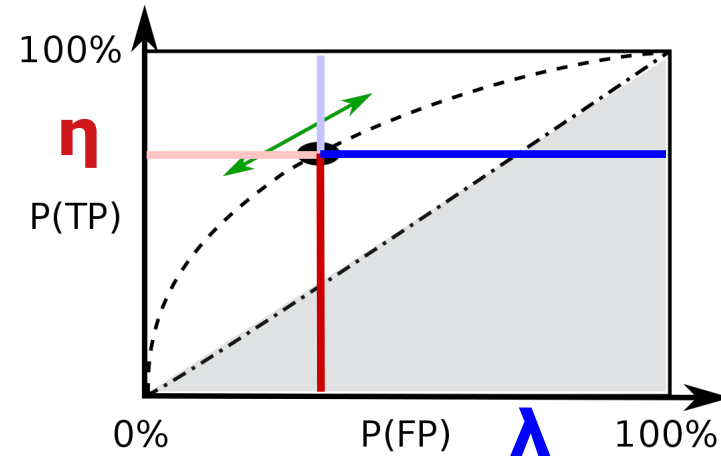
Side effect

Reduced efficiency (**FALSE NEGATIVE**)
 Noise leakage (**FALSE POSITIVE**)

Need sophisticated optimization



| | |
|------------|------------|
| TP | FP |
| FN | TN |
| $\Sigma=1$ | $\Sigma=1$ |



Contingency table and ROC curve

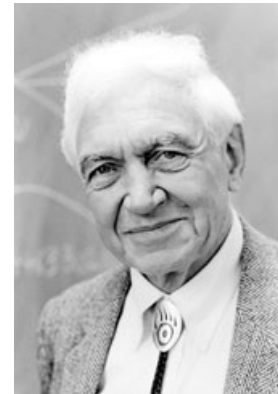
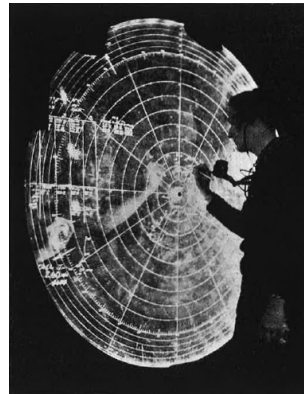
Quiz 1

What does "ROC" stand for?

Answer: ROC = **R**eceiver **O**perating **C**haracteristic

Quiz 2

What does this have to do with cLFV? Where does this name come from?



Expected significance

Signal estimation : S

Within signal window number of counts is measured

$$: N_S = \eta \cdot S + \lambda \cdot B$$

In an independent window the background is estimated

$$: N_B = k \cdot \lambda \cdot B$$

From these two together, the signal is estimated

$$: S = (N_S - N_B/k)/\eta$$

Error estimation : σ

$$\text{Uncertainty} : \eta^2 \sigma^2(S) = \sigma^2(N_S) + \sigma^2(N_B)/k^2$$

$$= N_S + N_B/k^2$$

$$= (\eta \cdot S + \lambda \cdot B) + (\lambda \cdot B/k)$$

$$= \eta \cdot S + k' \cdot \lambda \cdot B$$

$$k' = 1 + 1/k$$

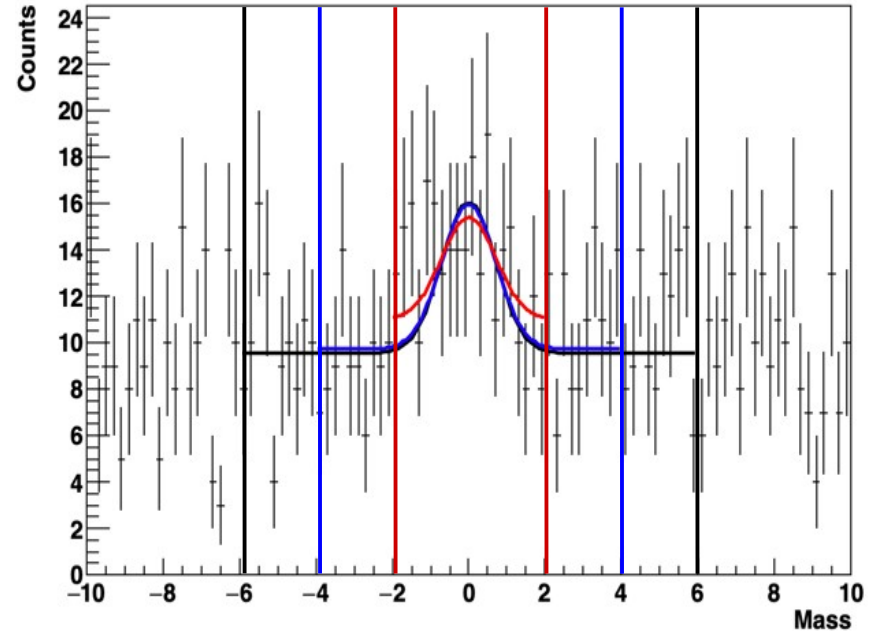
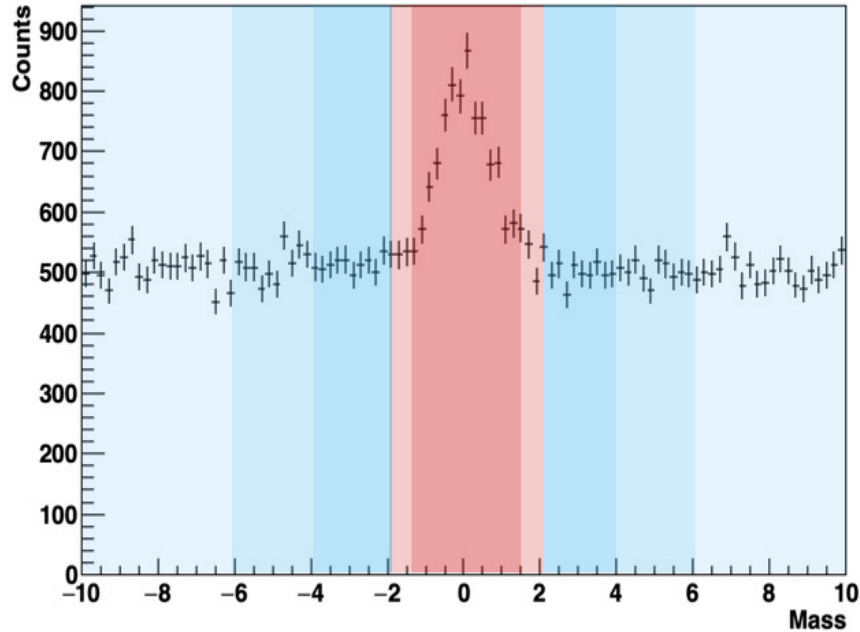
$$\sigma^2(S) = S/\eta + k' \cdot \lambda/\eta^2 \cdot B$$

Significance : ρ

$$\rho \equiv S/\sigma(S) = \eta S/\sqrt{(\eta S + k' \cdot \lambda \cdot B)} \stackrel{S \ll B}{\approx} \eta S/\sqrt{(k' \cdot \lambda \cdot B)} \stackrel{S \leq 1}{\approx} \eta/\sqrt{(k' \cdot \lambda \cdot B)}$$

So, need η large, λ small, k large, small B

Expected significance



Branching fractions *etc.*

Branching fraction \mathcal{B} defined and measured as

$$\begin{aligned}
 \mathcal{B}(M \rightarrow X) &= \Gamma(M \rightarrow X) / \Gamma(M \rightarrow \text{anything}) \\
 &= \int \Gamma(M \rightarrow X) \cdot dt / \int \Gamma(M \rightarrow \text{anything}) \cdot dt \\
 &= N(M \rightarrow X) / N(M \rightarrow \text{anything}) \\
 &= N(M \rightarrow X) / N(M) \\
 &= N(M \rightarrow X) / [N(\text{collisions}) \cdot f(\text{collision} \rightarrow M)] \\
 &= N(M \rightarrow X) / [\int \mathcal{L} \cdot dt \cdot \sigma(\text{collision} \rightarrow M)]
 \end{aligned}$$

Beware: could produce multiple M's per collision!

\mathcal{L} : luminosity
 σ : cross section

Also for other particles

$$\mathcal{B}(P \rightarrow Y) = N(P \rightarrow Y) / [\int \mathcal{L} \cdot dt \cdot \sigma(\text{collision} \rightarrow P)]$$

Combining two reactions gives

$$\mathcal{B}(M \rightarrow X) = \mathcal{B}(P \rightarrow Y) \cdot N(M \rightarrow X) / N(P \rightarrow Y) \cdot \sigma(\text{collision} \rightarrow P) / \sigma(\text{collision} \rightarrow M)$$

Need high $\int \mathcal{L} \cdot dt$, large $\sigma(\text{collision} \rightarrow M, P)$, known $\mathcal{B}(P \rightarrow Y)$ & $f(P)/f(M)$

Hadron production

High Energy Machines (2000–)

Electron-positron colliders

LEP, BEPC (II), CESR(-c), VEPP(-4M,5, 2000), DAΦNE, PEP-II, (Super)KEKB

$\mathcal{E} =$ 104 4.63 6 6 0.7 9+3.1 7+4 GeV

Electron-Proton colliders

HERA (27.5+920GeV)

Proton-Antiproton colliders

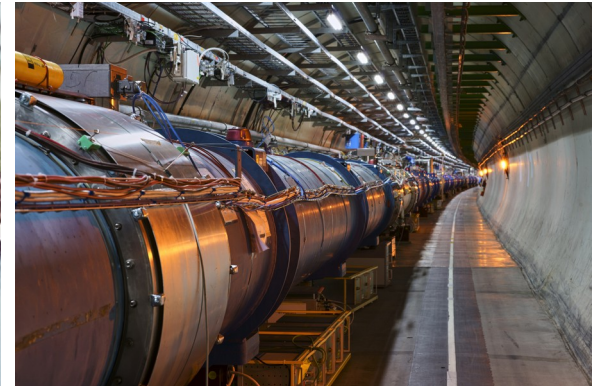
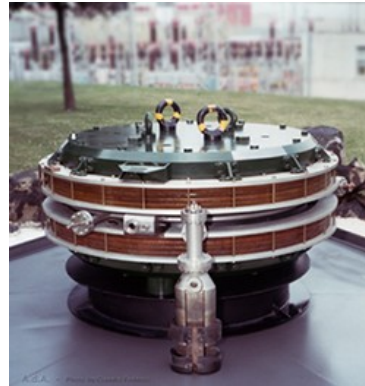
Tevatron (980GeV)

Proton-Proton colliders

RHIC (255GeV), LHC (6.5TeV)

Fixed target machines

LANL, PSI, AGS, J-PARC



Electron-Positron Colliders

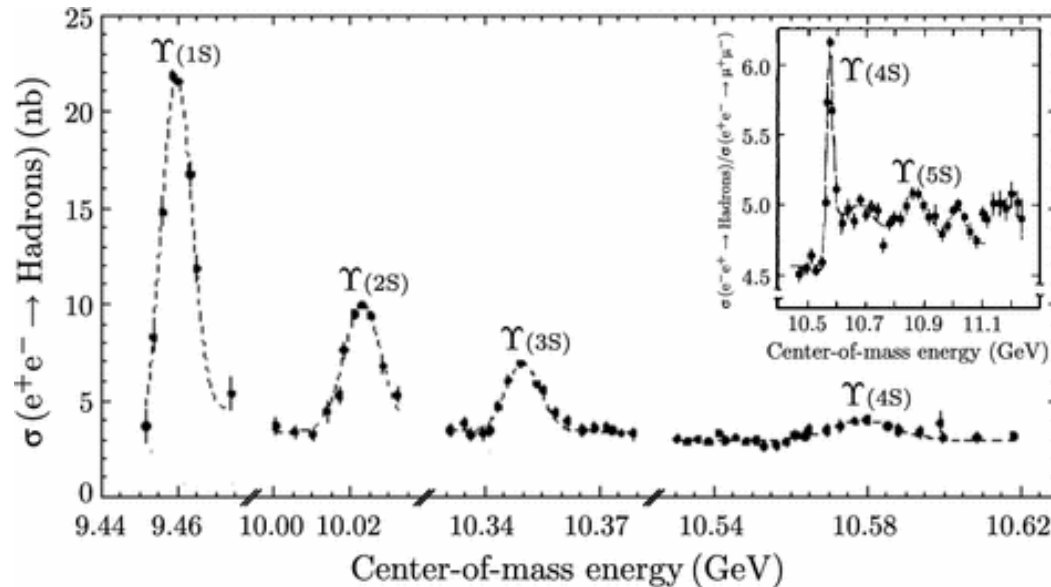
Some scan their energy, but mostly fixed

Resonant production, e.g. via $e^+e^- \rightarrow J/\psi \rightarrow M\bar{M}$

Only $\Upsilon(4S)$ decays into $B\bar{B}$ ($\mathcal{B} > 96\%$)

Most are symmetric, so $J/\psi(c\bar{c})$ or $\Upsilon(b\bar{b})$ is at rest

Often referred to as **B-factories**, or **tau-charm factories**
(depending on most abundant production channel)



$$\sigma(e^+e^- \rightarrow \Upsilon(4S)) \sim 5 \text{ nb} \\ = 5 \cdot 10^{-33} \text{ cm}^2$$

Electron-Positron Colliders

KEKB

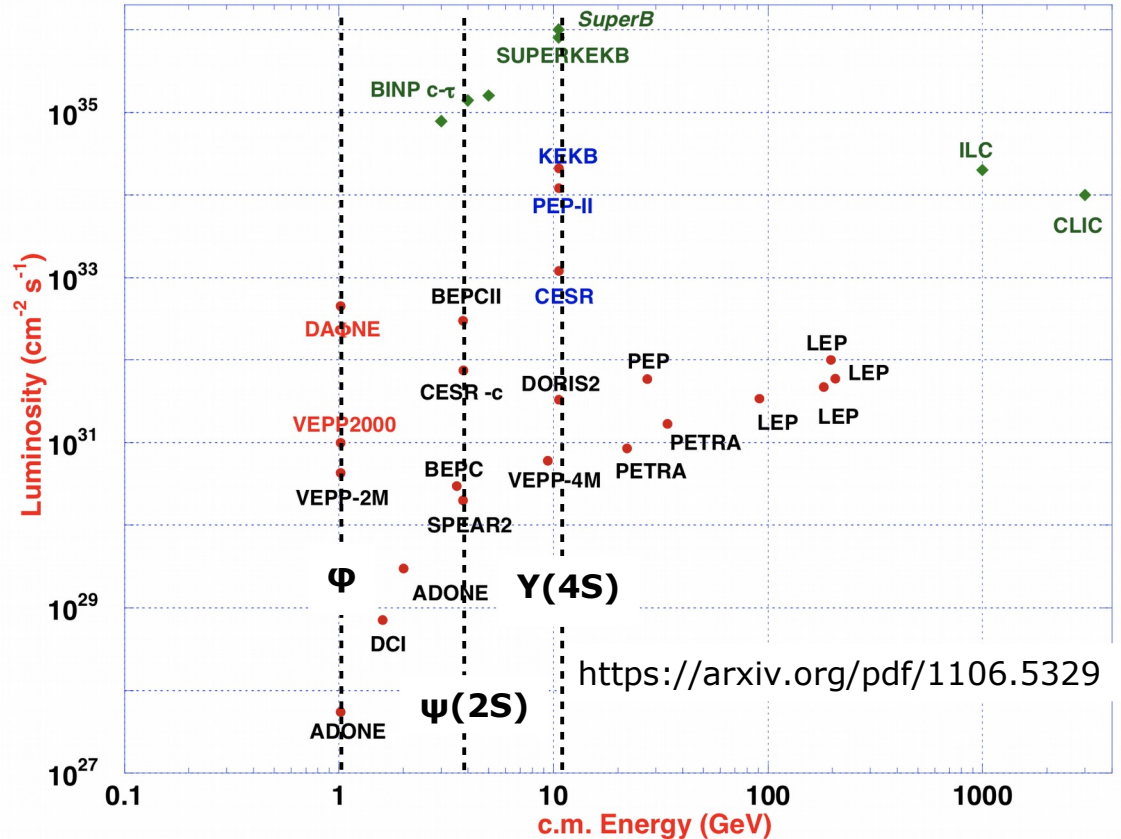
Luminosity of $10^{34} \text{ cm}^{-2} \cdot \text{s}^{-1}$
 Production rate of $\sim 50 \text{ Y} \cdot \text{s}^{-1}$
 Annually $\sim 5 \cdot 10^8 \text{ BB}$

SuperKEKB

Annually $\sim 5 \cdot 10^9 \text{ BB}$

BEPC

Annually $\sim 3 \cdot 10^9 \text{ } \Psi(2S)$



DOI:10.1063/PT.6.1.20180516a

Figure 1. Peak luminosity and energy of the past, present and future (diamonds) electron-positron colliders.

Large Hadron Collider

Proton on proton collision

Enormous energy: 6.5 TeV + 6.5 TeV

Single collision produces many particles (100's)

LHCb (2015-2018)

Average luminosity $\langle L \rangle \sim 50 \mu\text{b}^{-1}\cdot\text{s}^{-1}$

$B\bar{B}$ production in acceptance $\sigma(pp \rightarrow b\bar{b}X) \sim 150 \mu\text{b}$

Production rate $B\bar{B} \sim 7500 \text{ s}^{-1}$

Integrated luminosity: 6 fb^{-1}

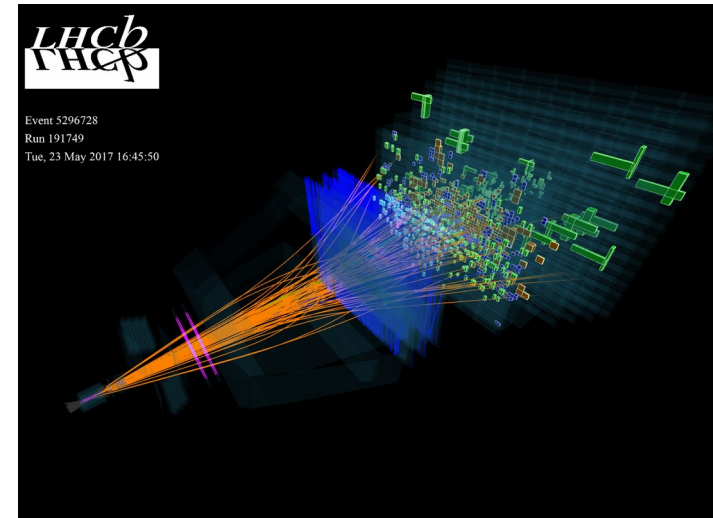
Total production: $\sim 10^{12} B\bar{B}$

ATLAS (2015-2018)

Integrated luminosity: 160 fb^{-1}

$B\bar{B}$ production in acceptance $\sigma(pp \rightarrow b\bar{b}X) \sim 500 \mu\text{b}$

Total production: $\sim 10^{14} B\bar{B}$



Particle identification

LHC

CMS

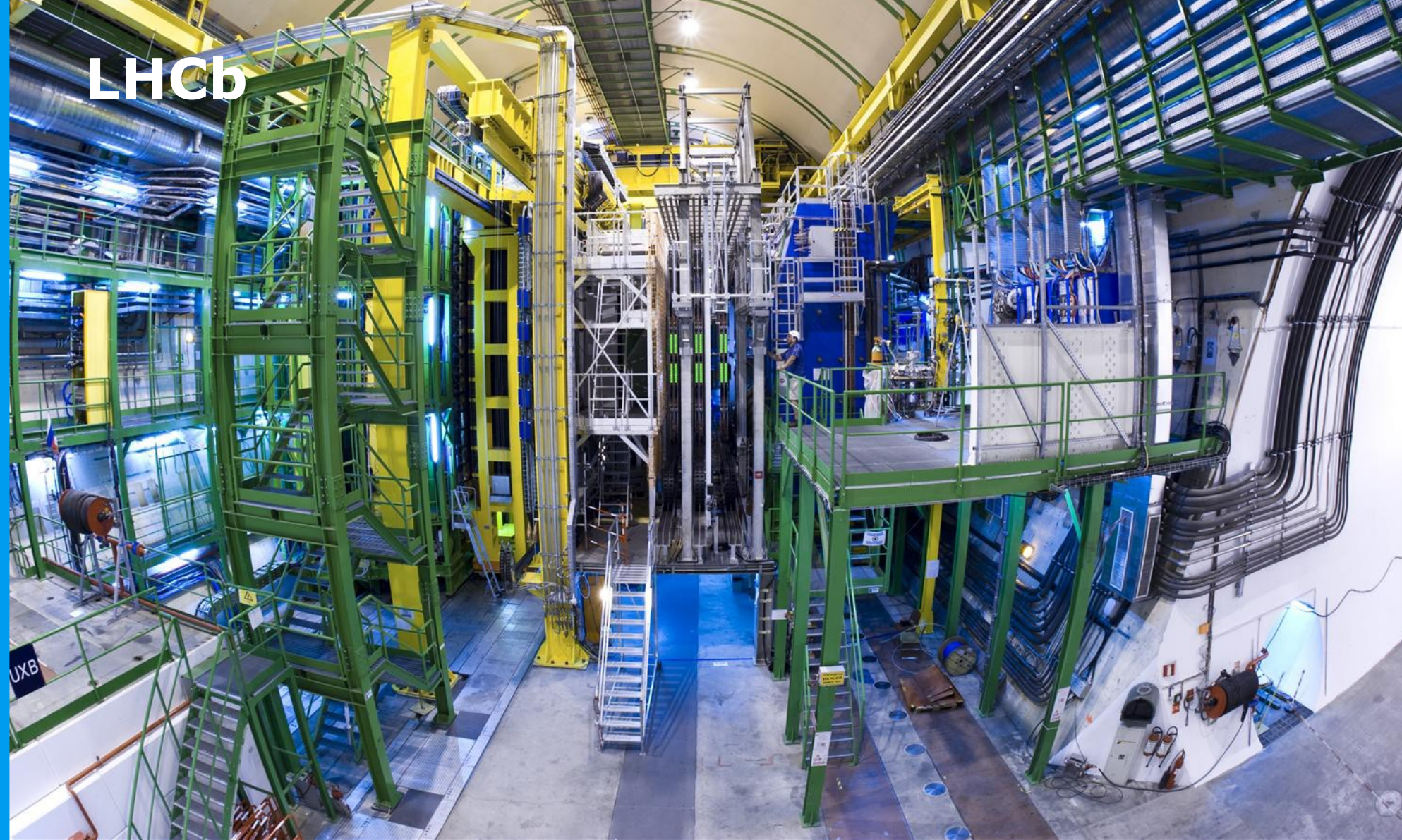
LHCb

ALICE

ATLAS



LHCb



LHCb



LHCb

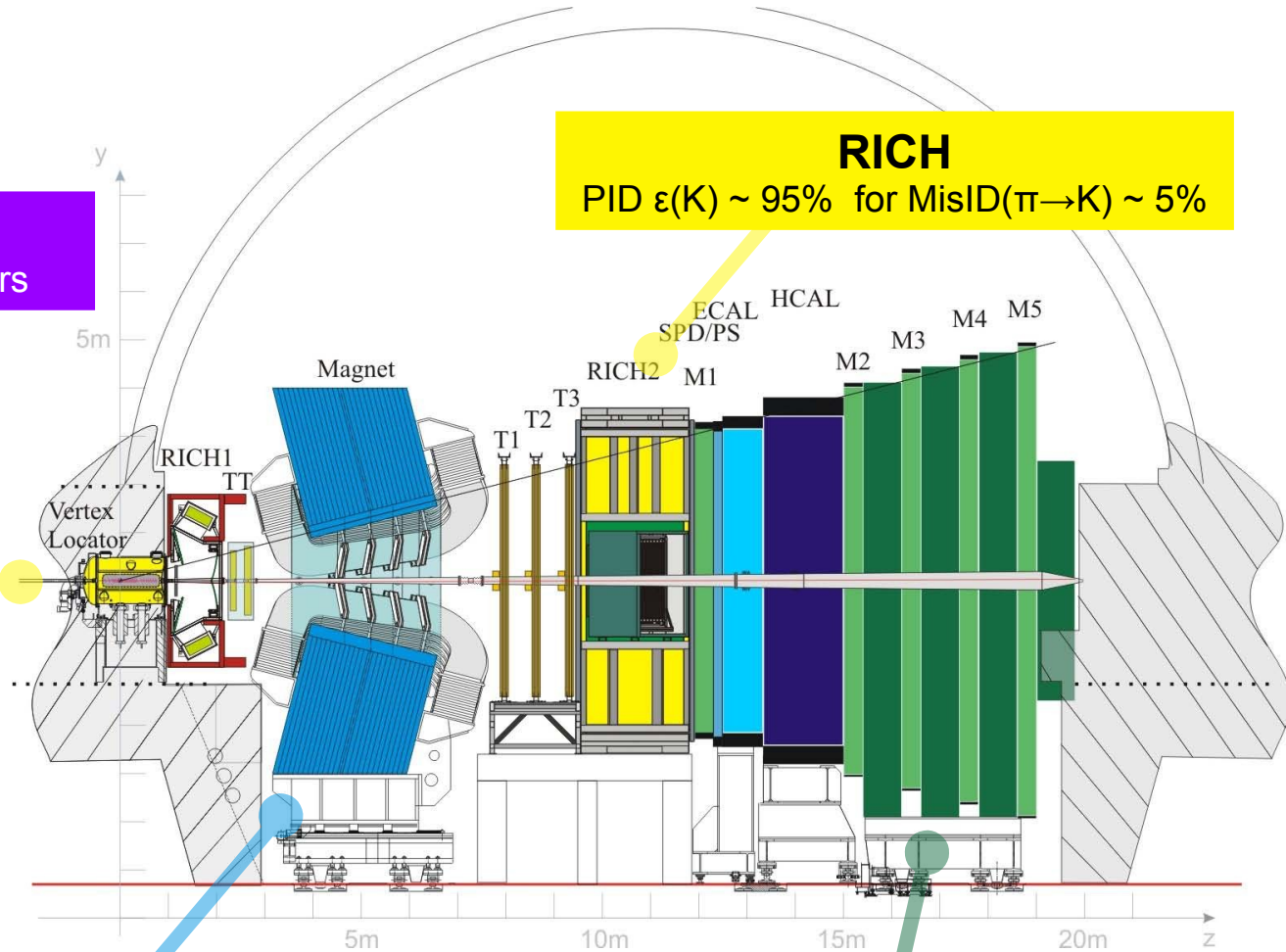
Trigger
high efficiency esp. muon triggers

VELO
IP resolution $15+29/(p_T/\text{GeV}) \mu\text{m}$

Tracking $\Delta p/p$
 $0.4\% @ 5 \text{ GeV}/c - 1.0\% @ 200 \text{ GeV}/c$

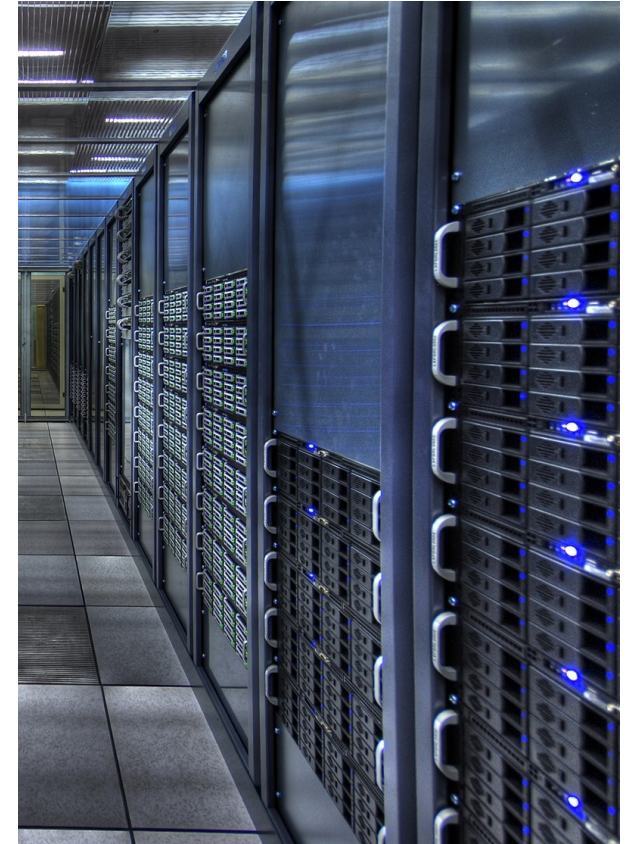
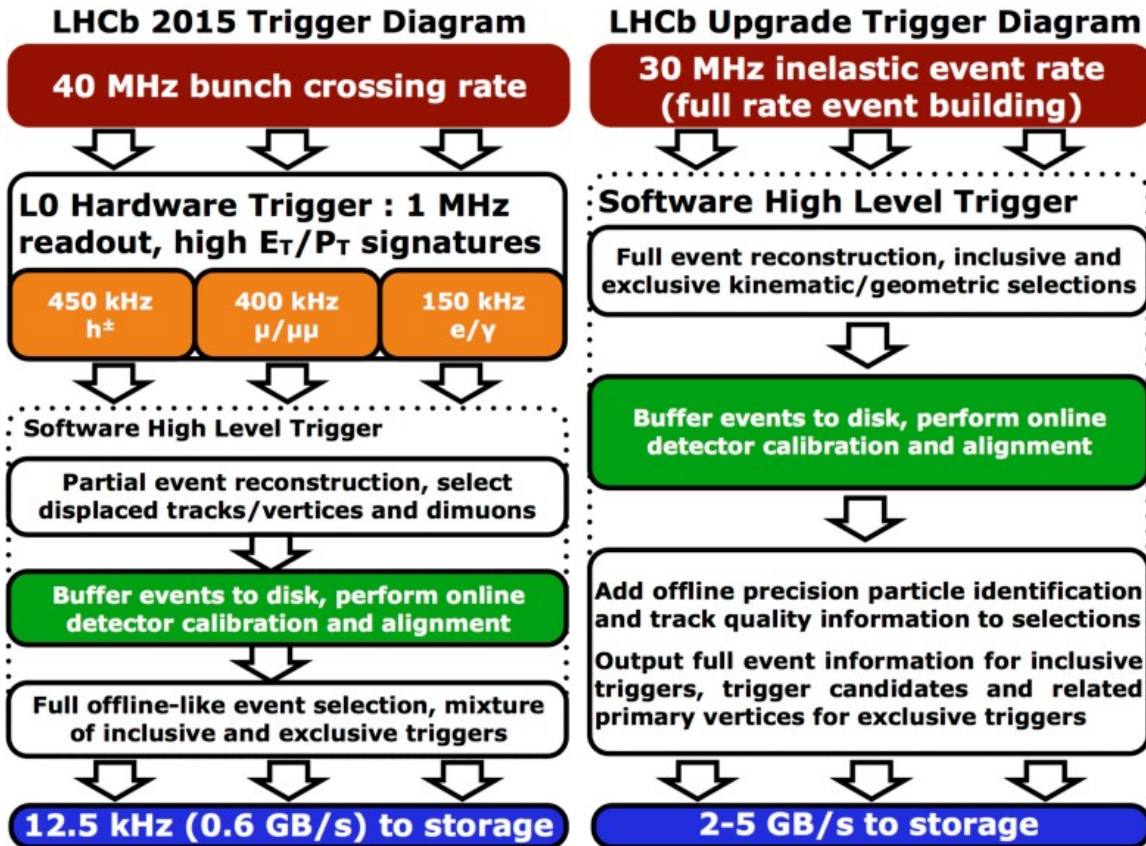
RICH
PID $\epsilon(K) \sim 95\%$ for MisID($\pi \rightarrow K$) $\sim 5\%$

Muon ID
identification $\epsilon \sim 97\%$ misID $\sim 2\%$



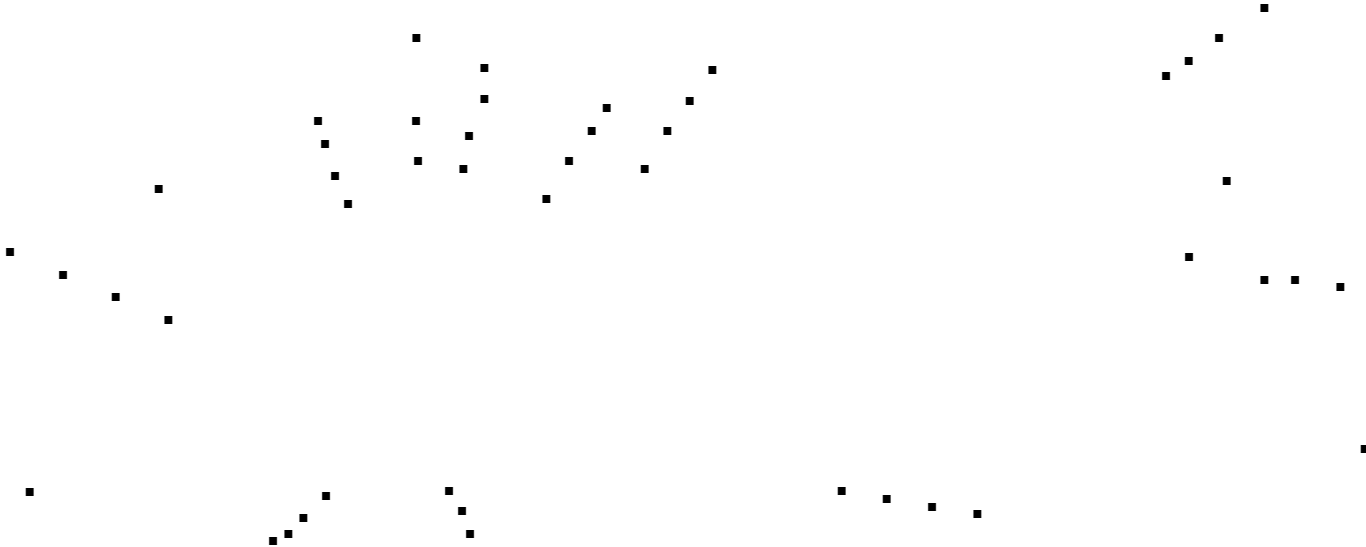
Triggering

Most collision events are un-interesting → event selection / triggering



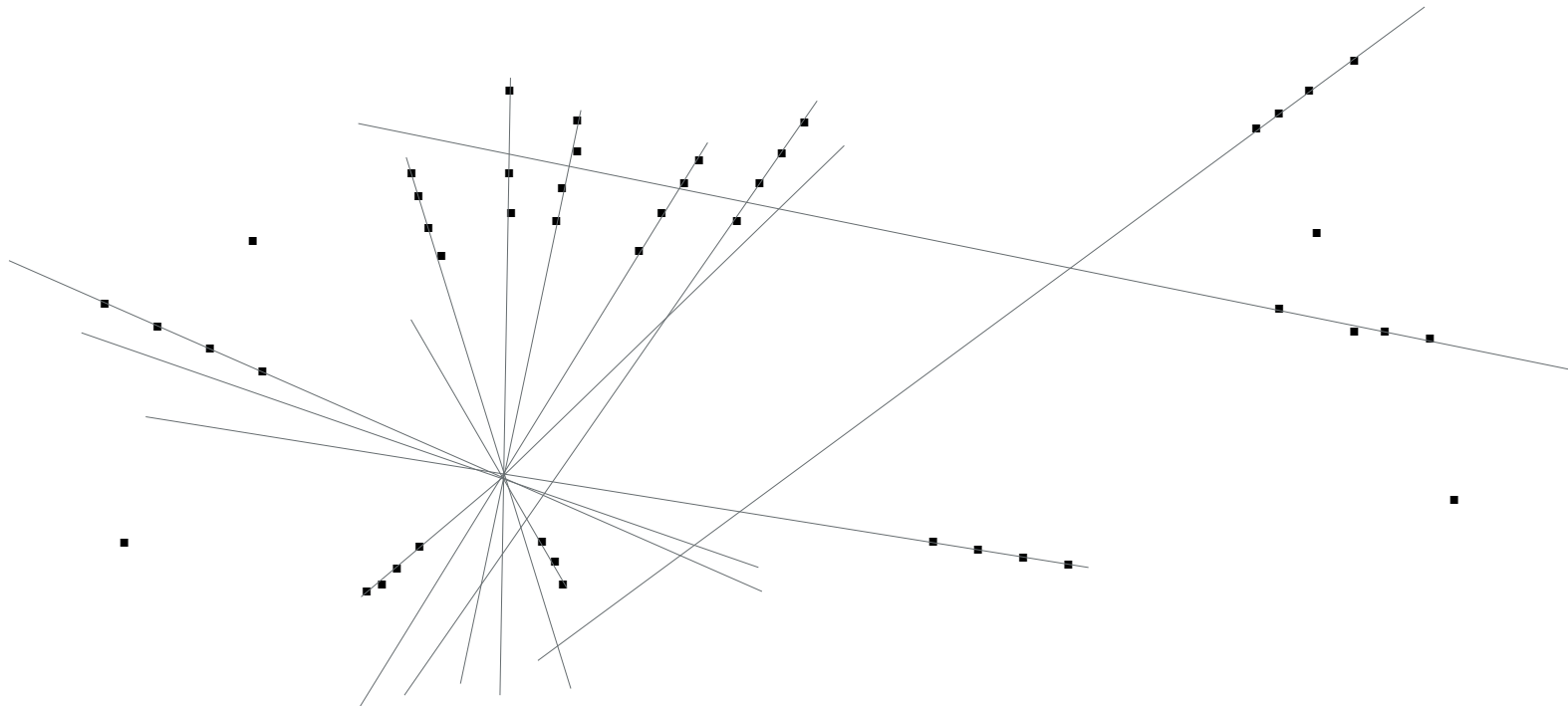
Reconstruction

Tracking : connecting **hits**



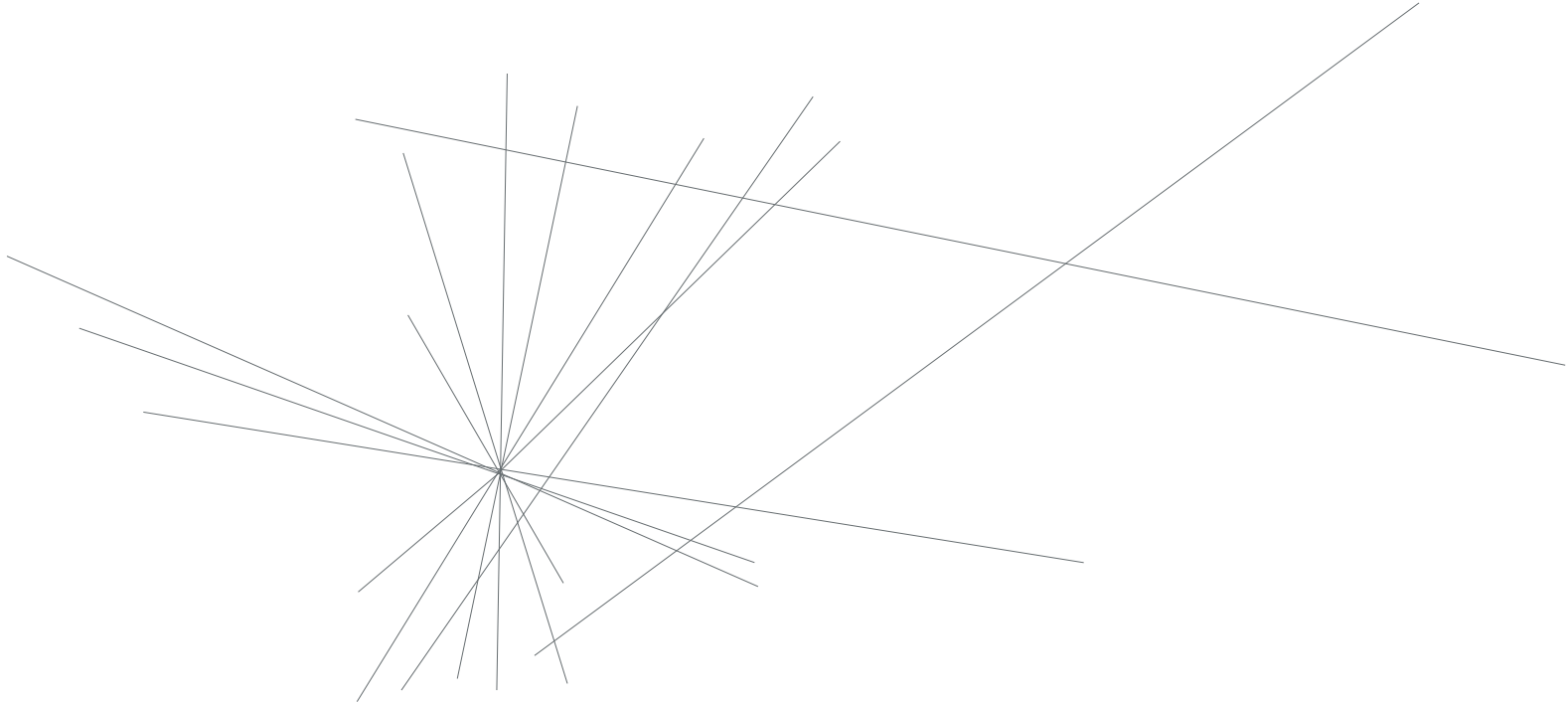
Reconstruction

Tracking : connecting hits to form **tracks**



Reconstruction

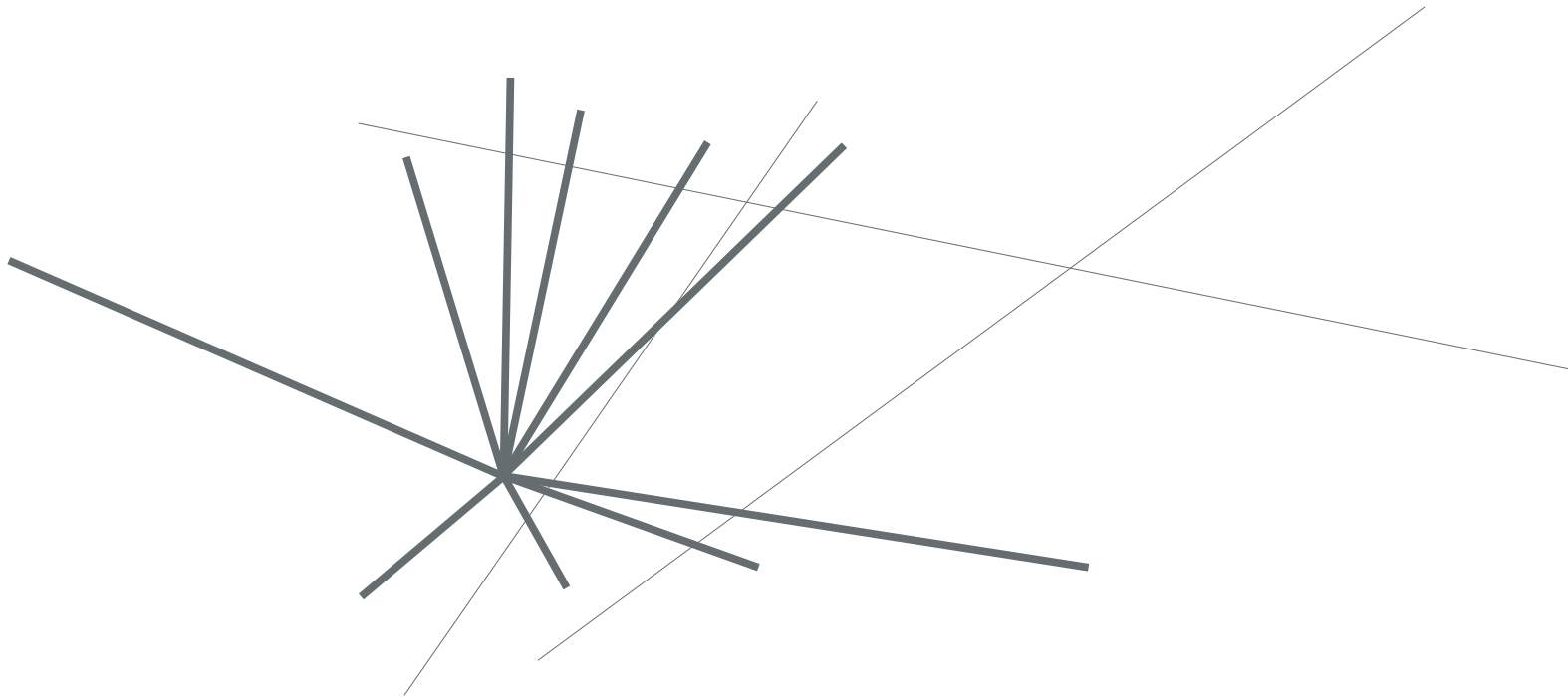
Tracking : connecting hits to form tracks
and determine *charge* and *momentum* from bending in magnetic field



Reconstruction

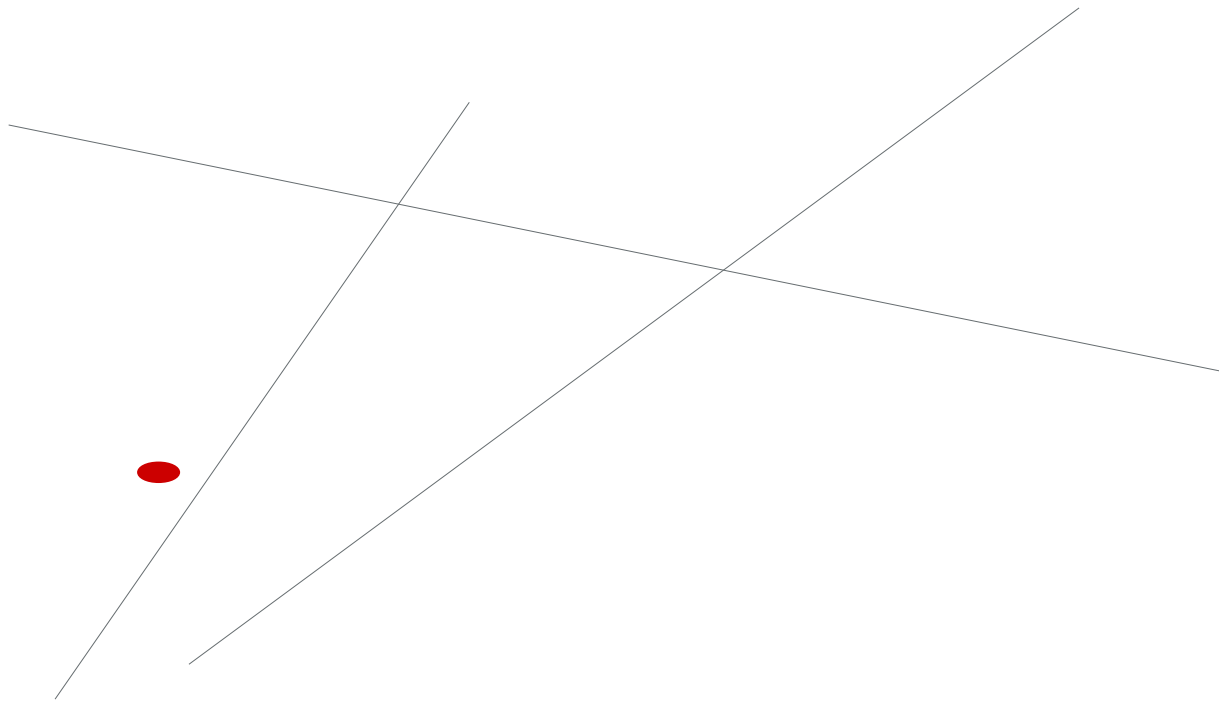
Find the **primary vertex** = collision point of two protons

Many tracks will originate from a common location close to the beam



Reconstruction

Find the **primary vertex**

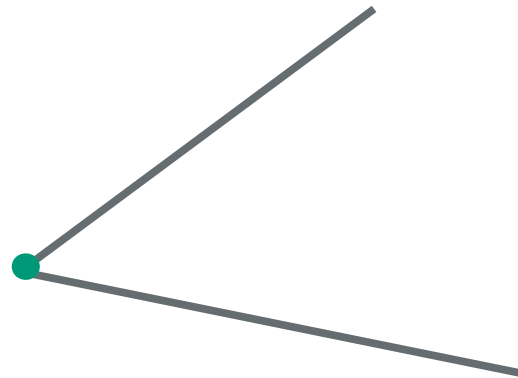
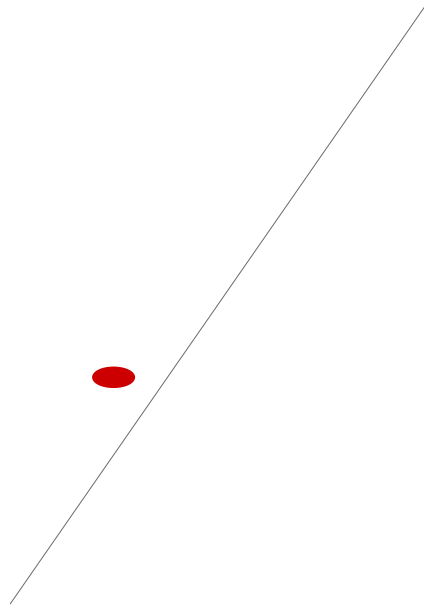


Reconstruction

Find **secondary vertex**

= location in space where two (or more tracks) converge

WARNING: probability that 2 lines in 3D space cross = zero, so use "best" point

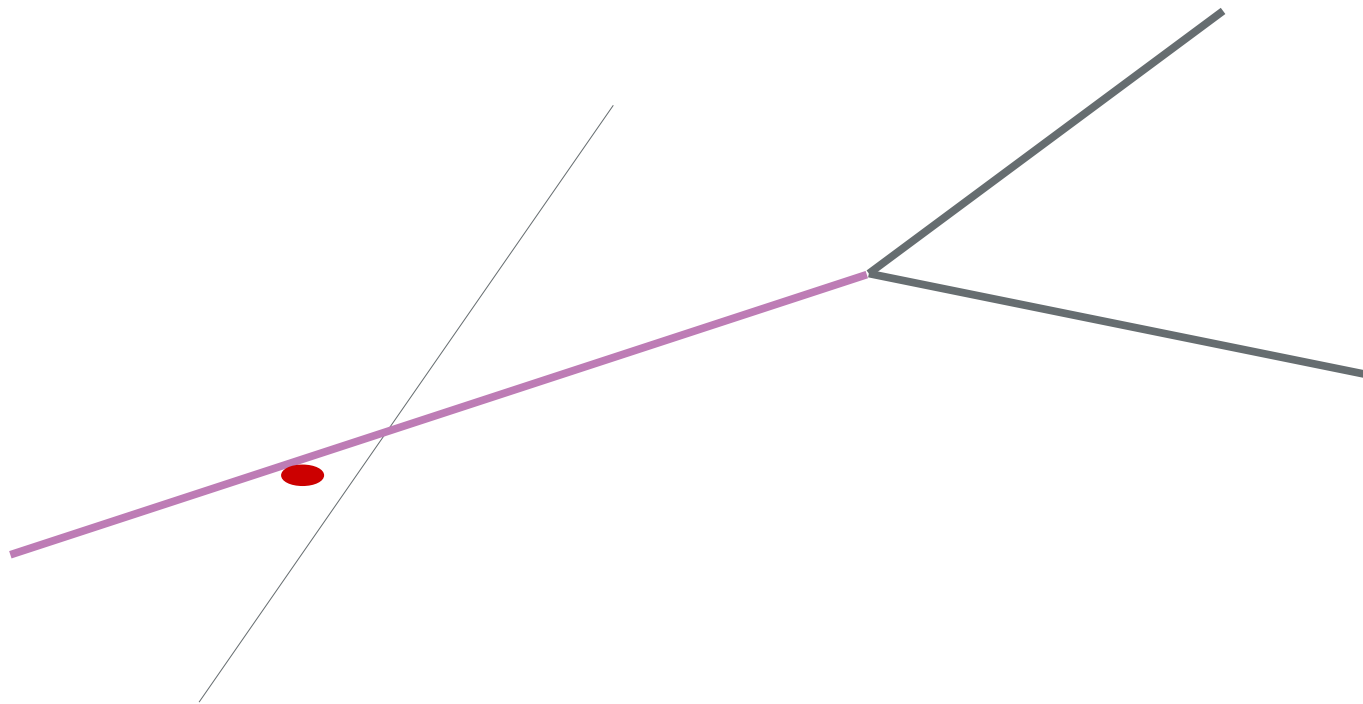


Reconstruction

Find **secondary vertex**, reconstuct **parent track**

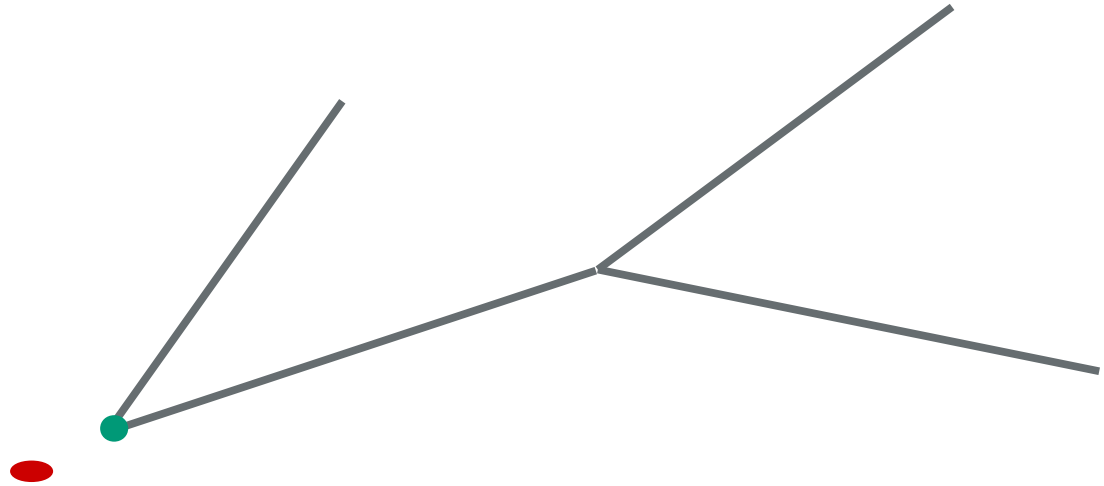
Combing 3-momenta gives parent 3-momentum, and direction of track

POSSIBLE IMPROVEMENT: refit tracks with perfect secondary vertex



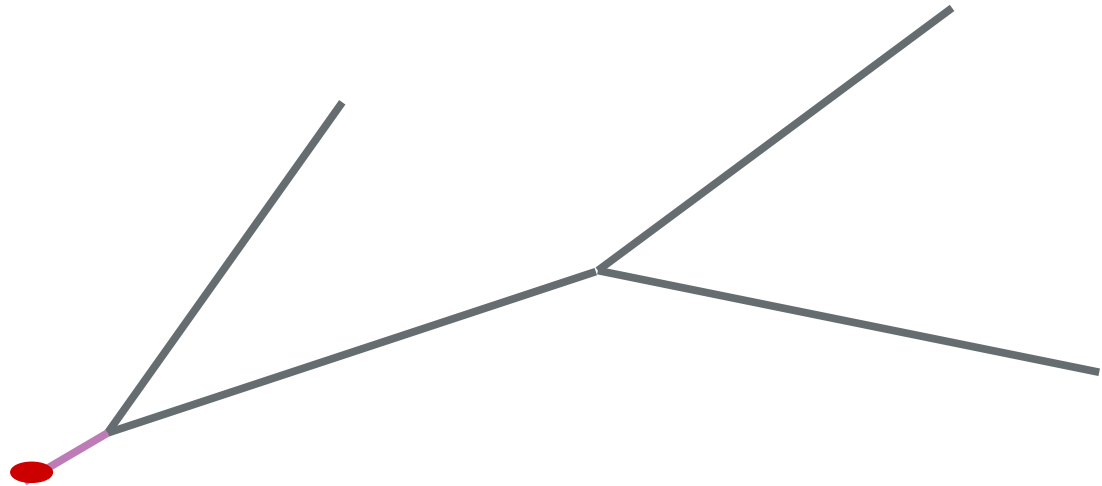
Reconstruction

Find **secondary vertex**, reconstitute **parent track**, and repeat



Reconstruction

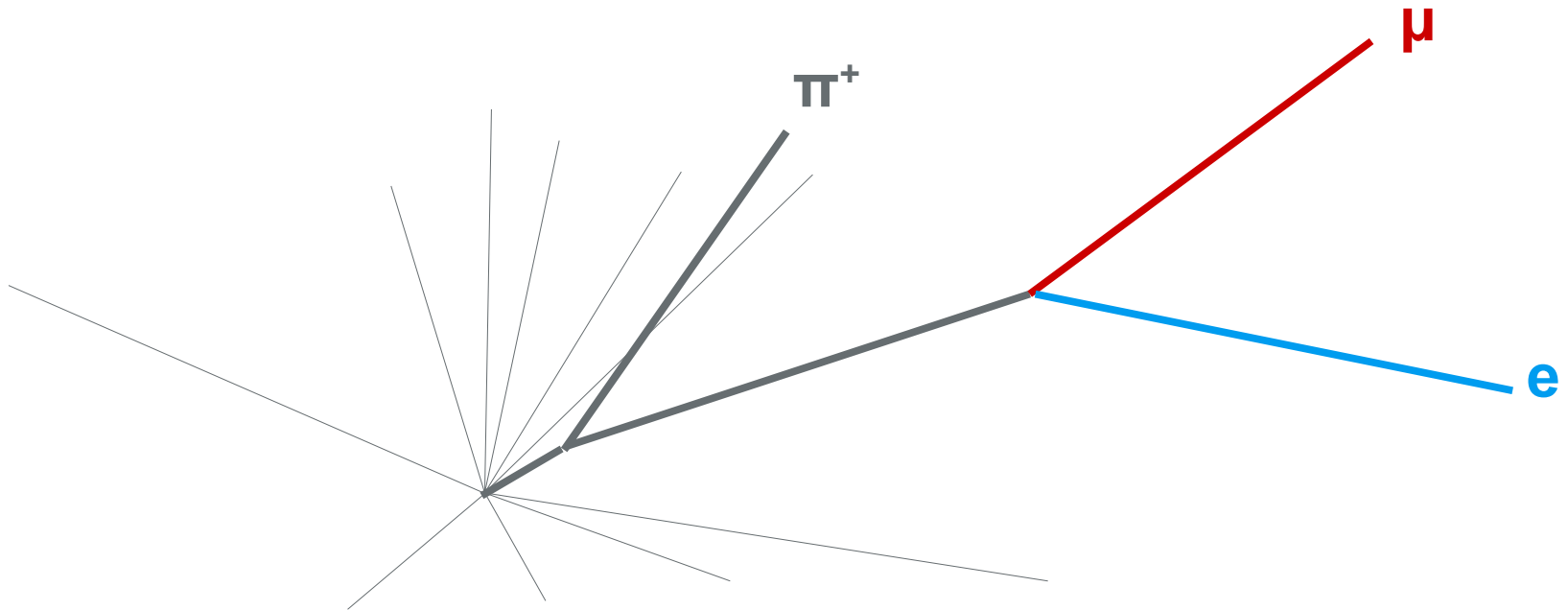
Find **secondary vertex**, reconstitute **parent track**, and repeat until last parent tracks comes from primary vertex



Reconstruction

Identify detected particles

WARNING: cannot be done uniquely, assume *most likely* identity

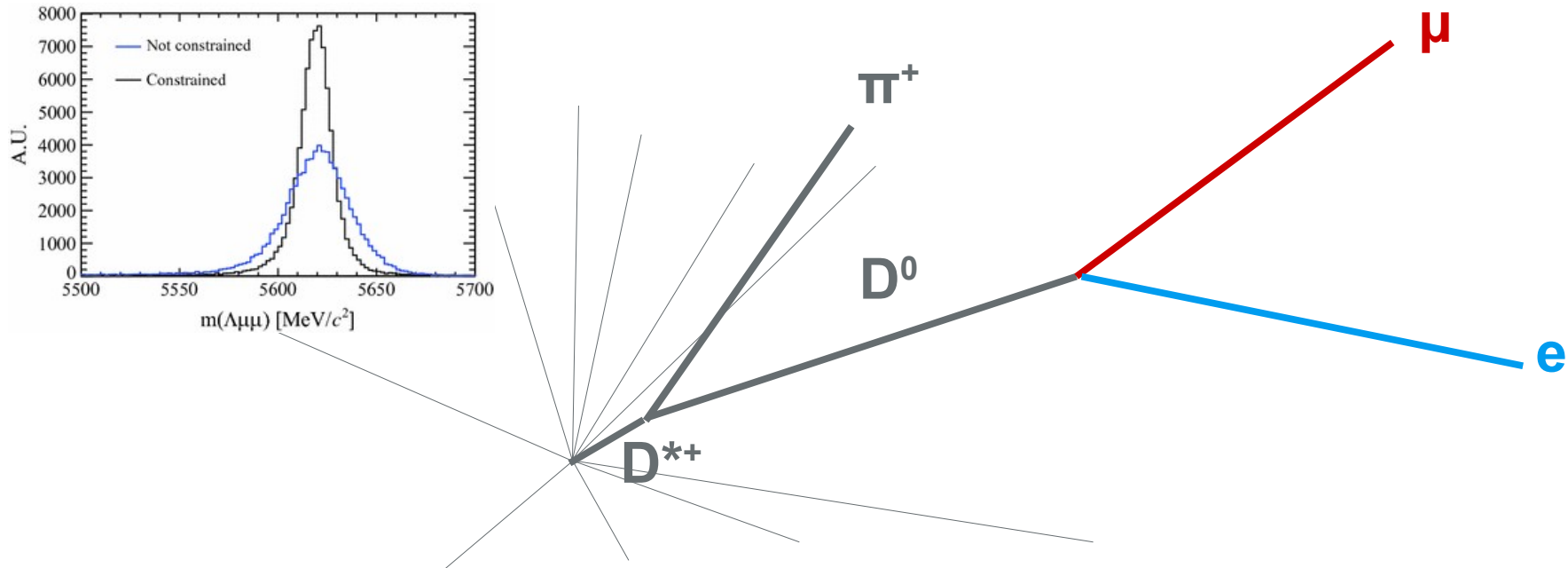


Reconstruction

Identify invisible particles

Construct four-momenta of parents, calculate invariant mass, and identify

POSSIBLE IMPROVEMENT: refit tracks with perfect vertices and/or parent mass



Challenge #1 : Particle (mis-)ID

At LHCb all light particles (γ, e, μ, n, K, p) ultra-relativistic, $p \leq 200 \text{ GeV}/c$

Photons and electron cause similar shower (mostly) in EM calorimeter (**ECAL**)

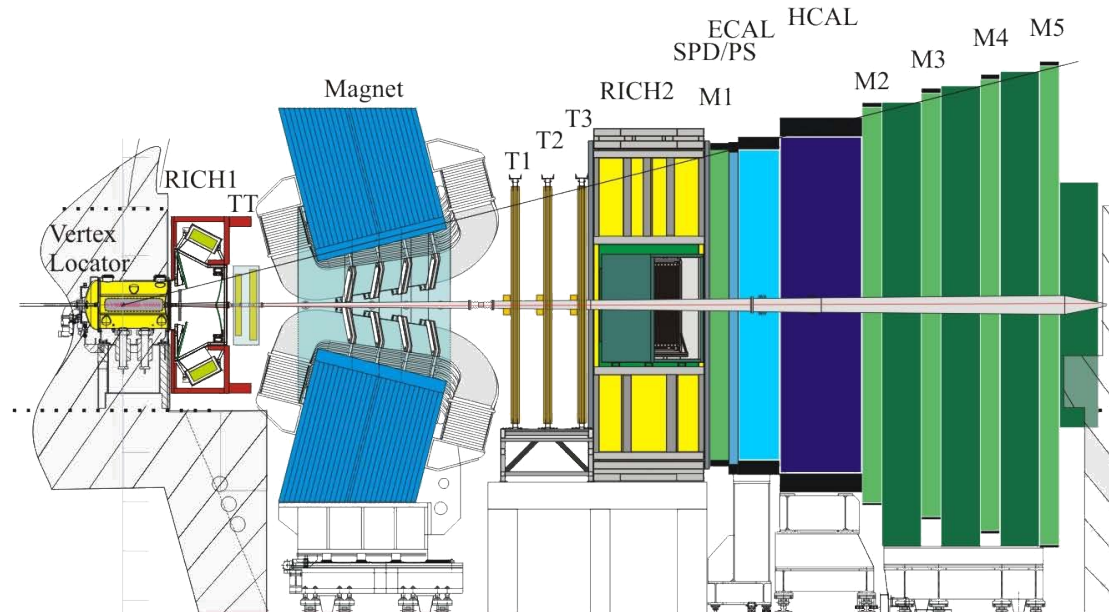
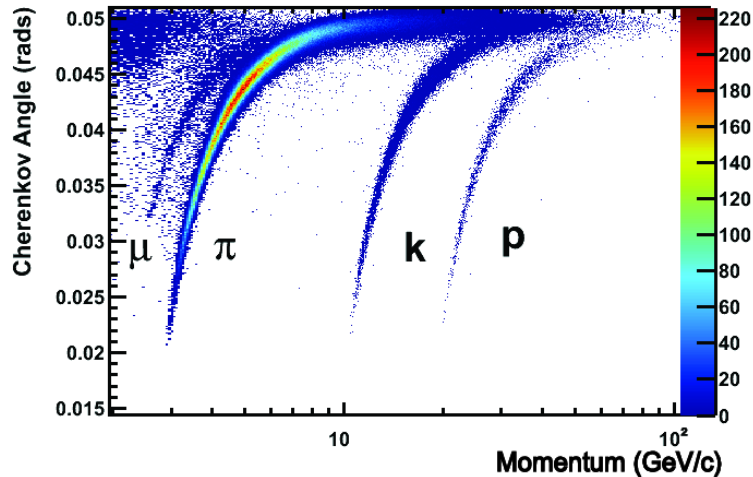
Photons leave no/little signal in pre-shower detector (**PS**) and trackers (**TT-T3**)

(Essentially) only muons make it to the muon chambers (**M1-M5**)

Hadrons (mostly) stop in hadronic calorimeter (**HCAL**)

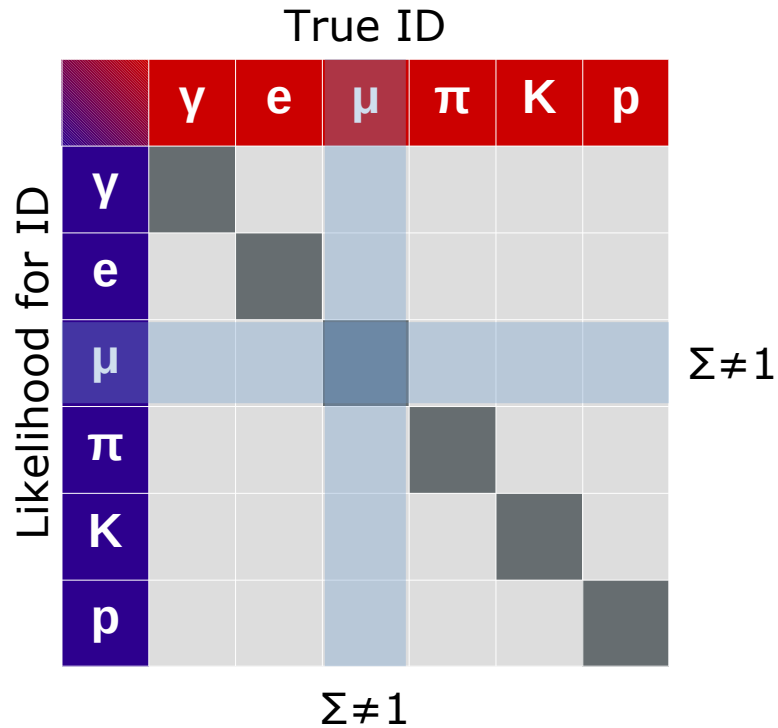
Ring-imaging Cherenkov Detector (**RICH**) distinguishes velocity

All rather energy dependent



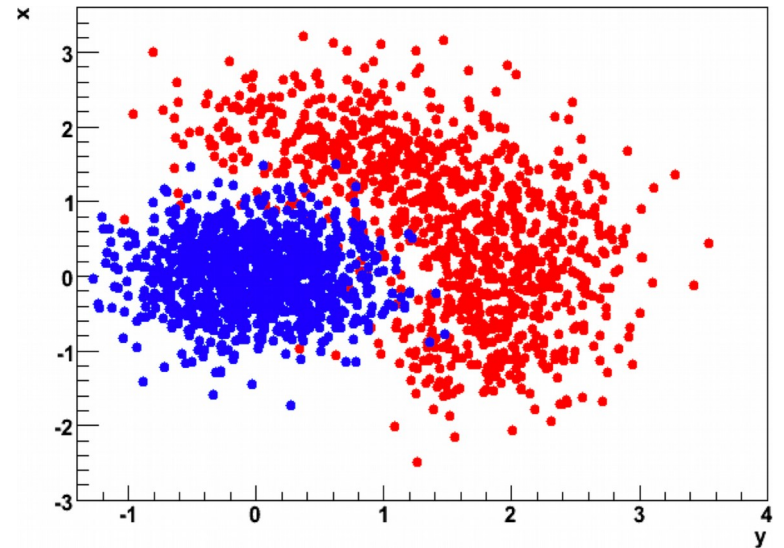
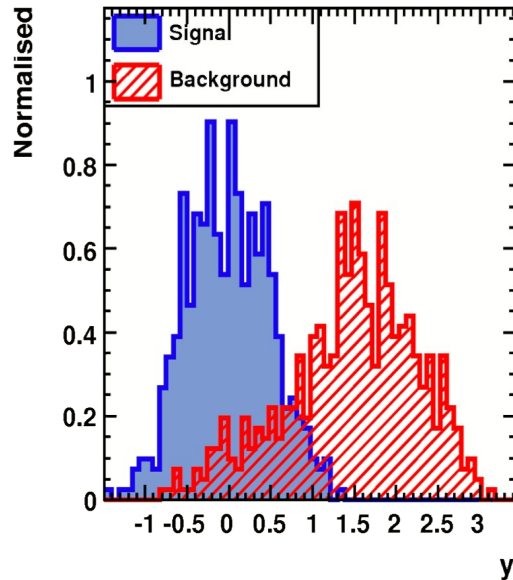
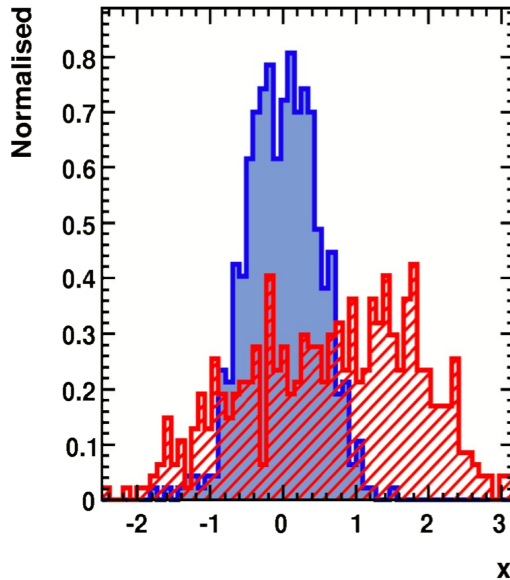
Challenge #1 : Particle (mis-)ID

Particle not uniquely ID'ed
 Likelihood per species



(Boosted) decision trees

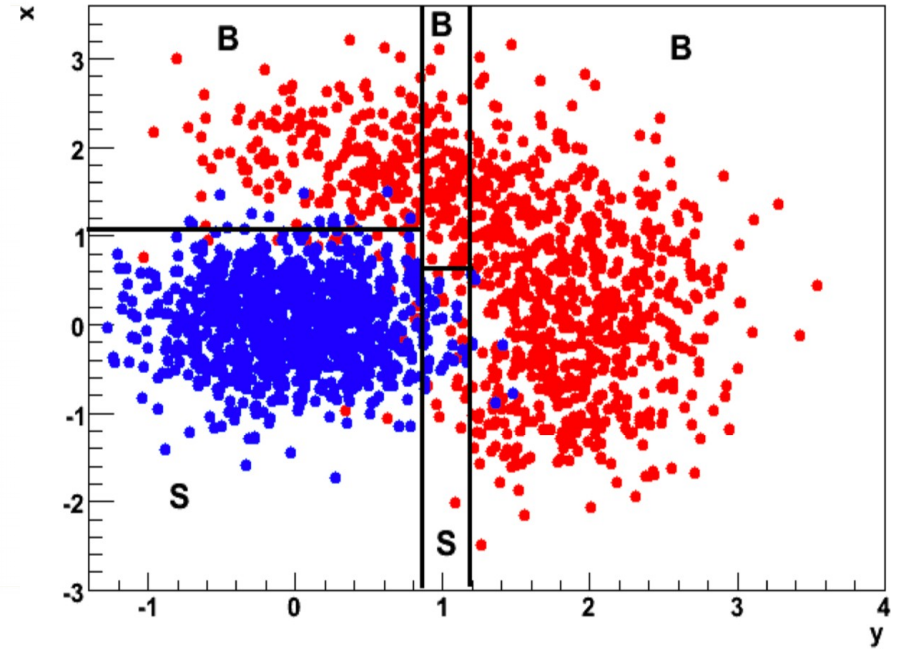
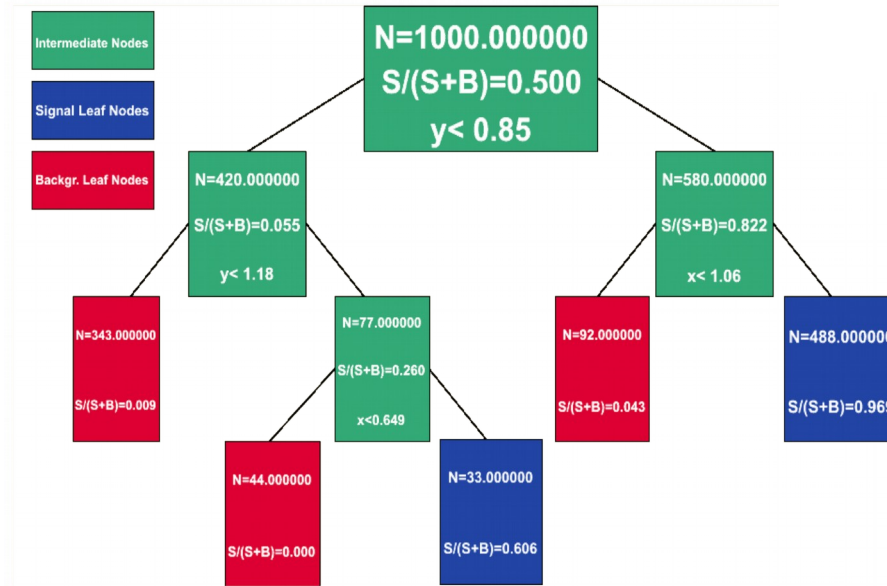
Example: **signal** and **background** measured in 2 detectors **X** and **Y**



Signal windows has lots of background → (automatically) optimize selection?

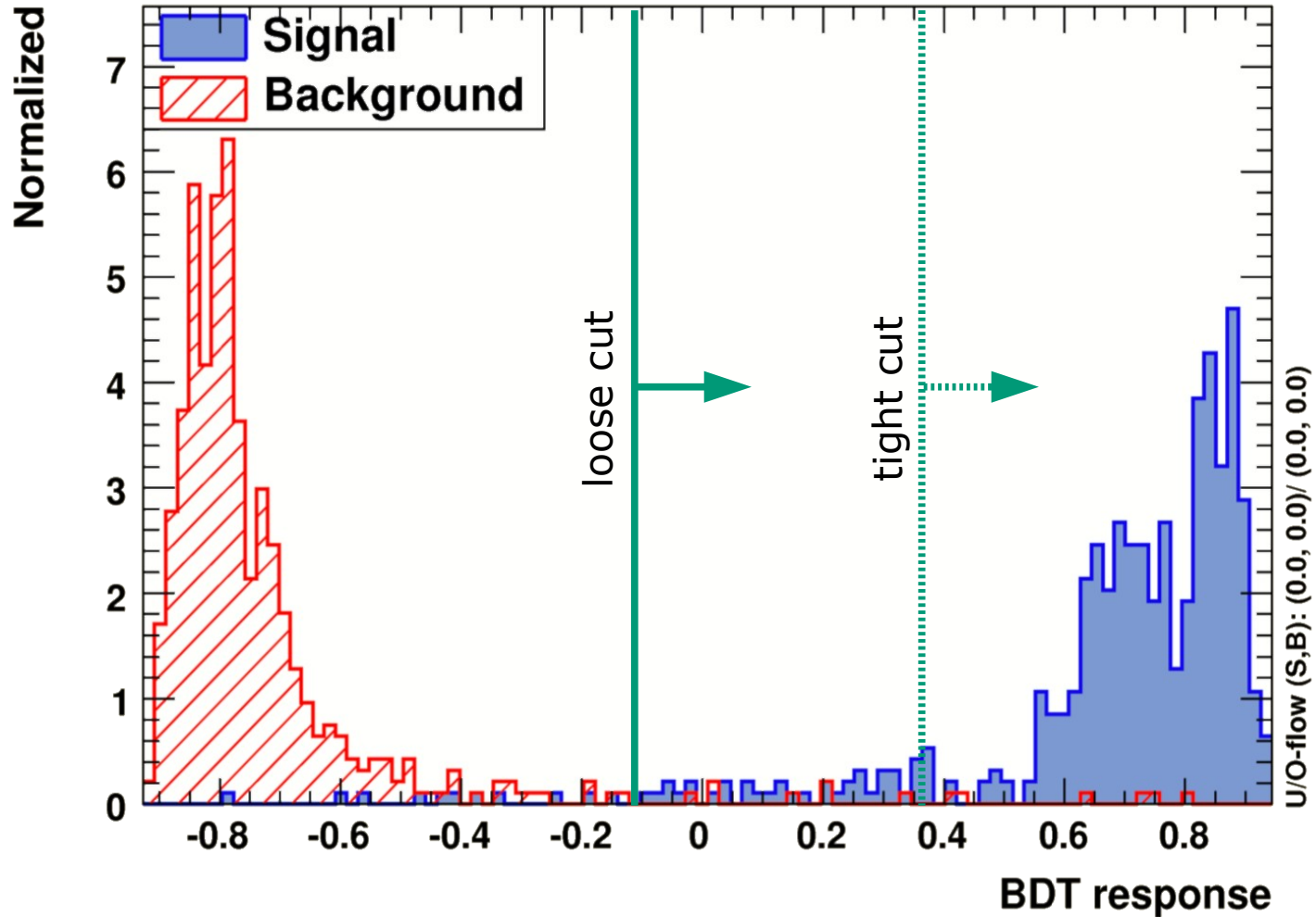
(Boosted) decision trees

Repeatedly split data in **X** or **Y** to optimize **signal-significance**



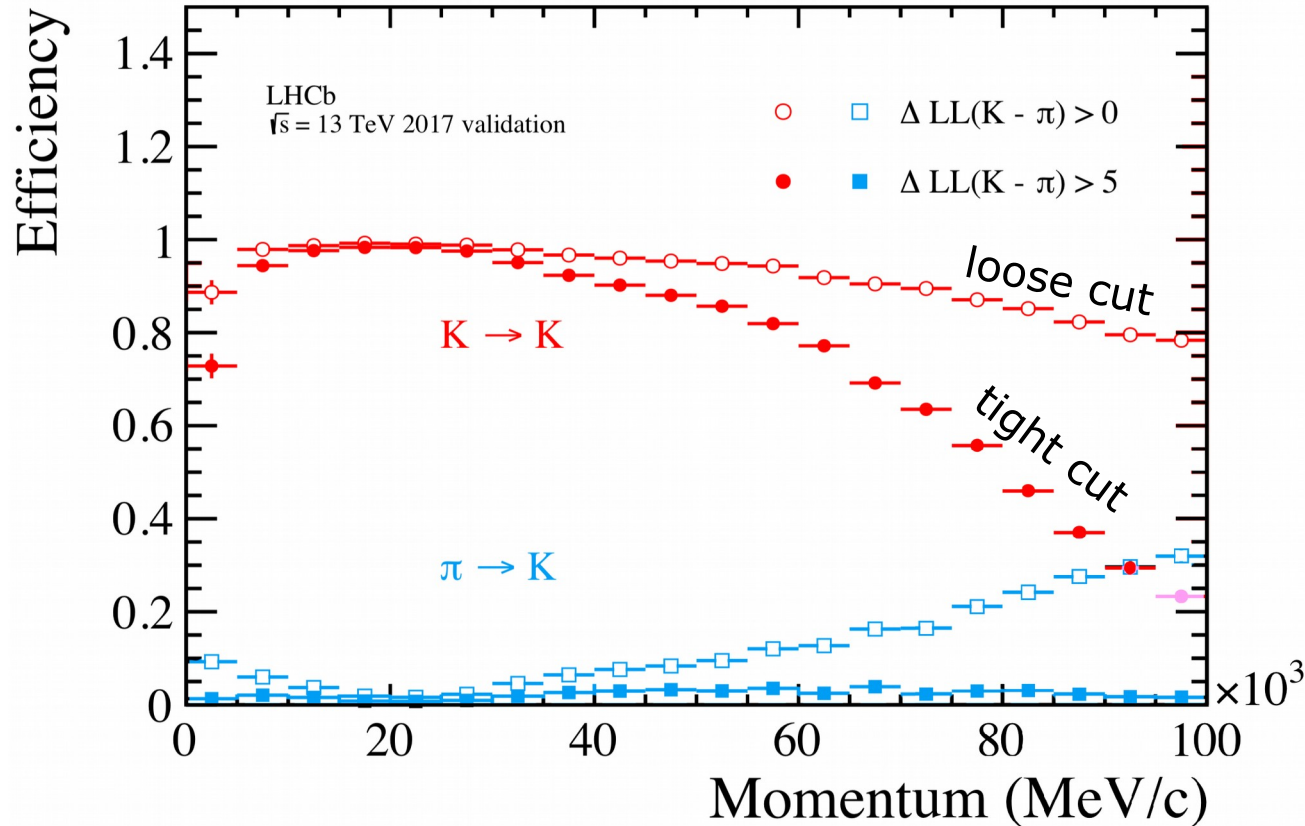
Boosting: take output of DT and re-weight training data for next DT

(Boosted) decision trees



Particle (mis-)ID

Incorrect inclusion/rejection of event for further analysis
 Leads to mis-reconstruction of parent mass



Challenge #2 : Bremsstrahlung

Charged particles deflected by other particles (nuclei) emit radiation

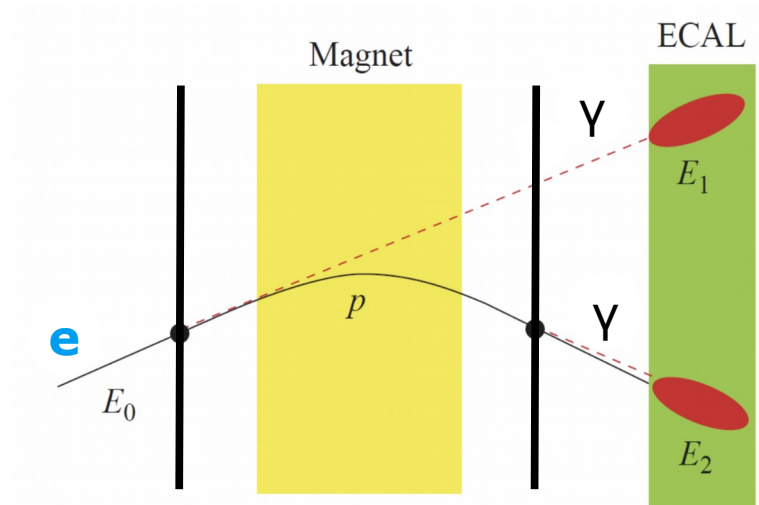
Bremsstrahlung is proportional to γ^6 .

Especially important for **electrons**

Photons emitted predominantly along direction of motion

Main effect : change in *magnitude* of momentum, less so in *direction*

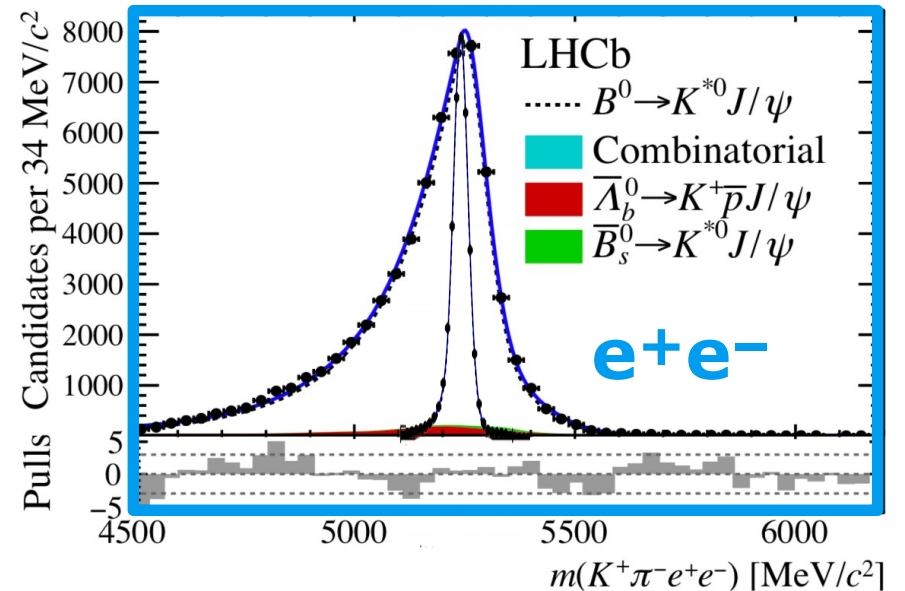
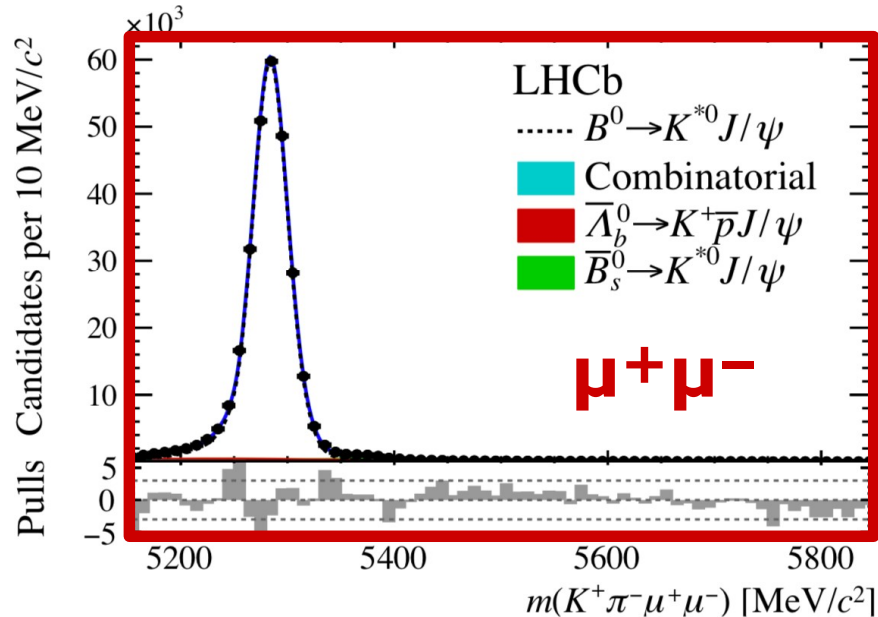
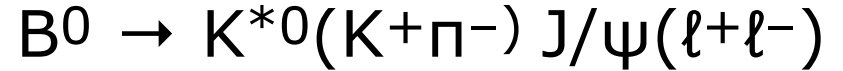
In part automatically recovered, in part to be done by-hand



Challenge #2 : Bremsstrahlung

Reconstructed parent mass less precise

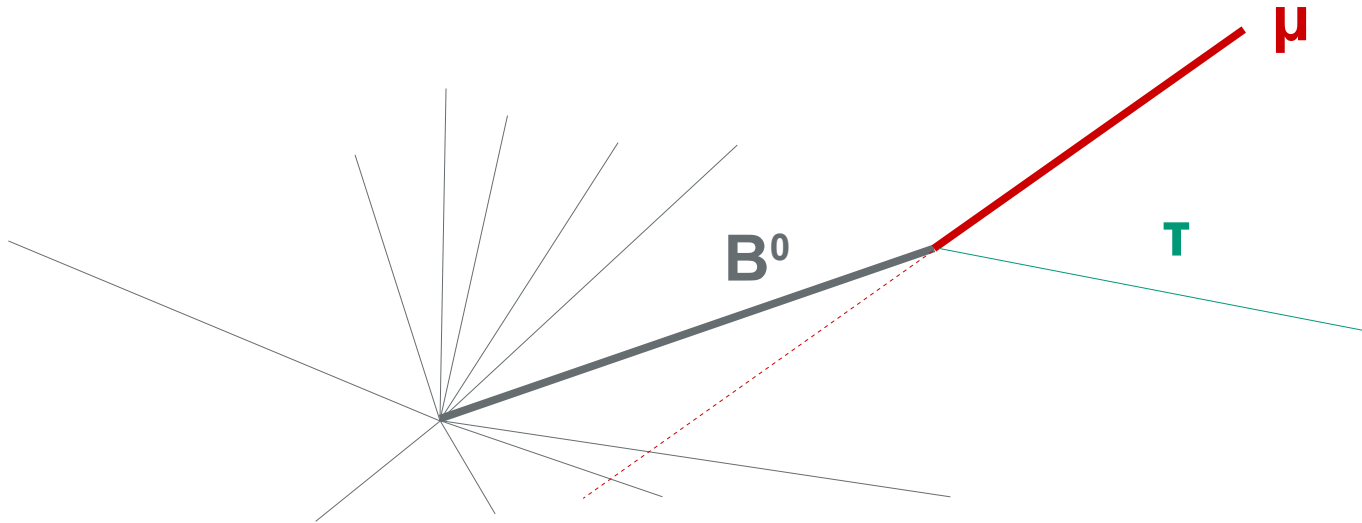
- wider signal region
- more background
- lower signal significance
- weaker limit



Challenge #3 : Tau-decay

Tau lifetime is 0.29 ps ($c\tau = 87 \mu\text{m}$)

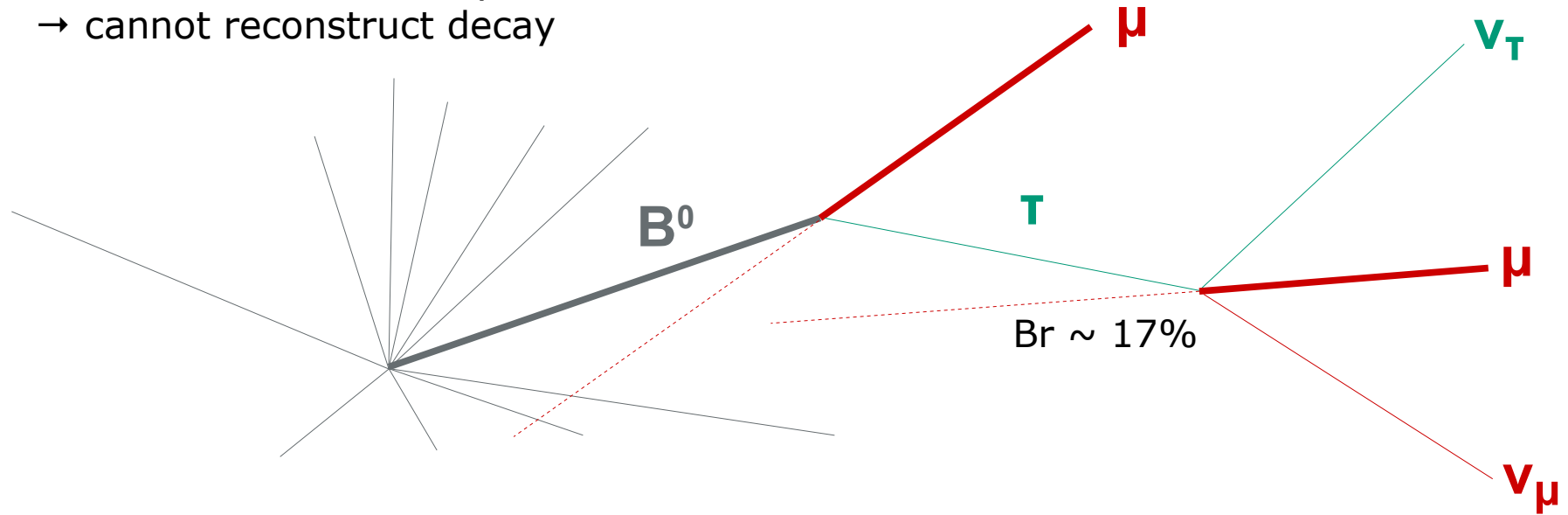
So **tau** cannot be detected itself



Challenge #3 : Tau-decay

Can only detect charged decay products, not neutrinos

- always missing tau-neutrino, if leptonic decay also second one
- missing p and E
- cannot find secondary vertex
- cannot reconstruct decay



Challenge #3 : Tau-decay

Hadronic decay : only a single missing neutrino

Several charged pions : can reconstruct **tau** decay vertex

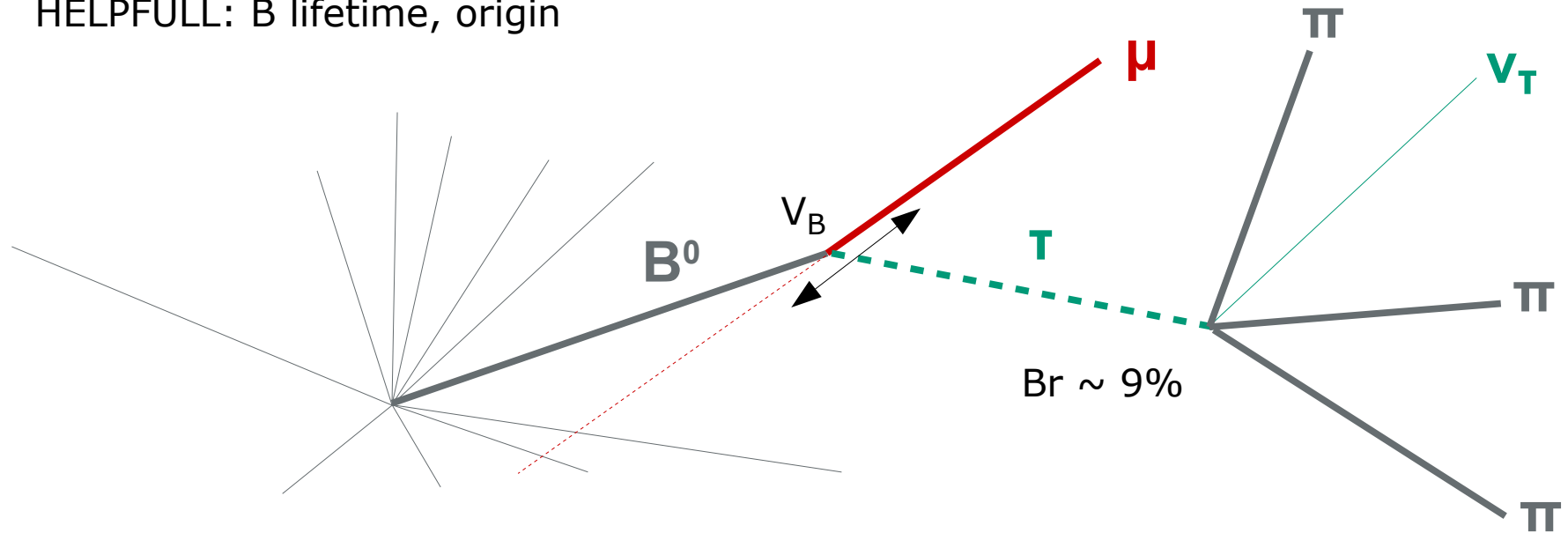
PROBLEM: B decay vertex along **μ** track unknown

HELPFULL: B lifetime, origin

$$p_{\perp}(\mathbf{v}) \text{ along } \mathbf{p}_{\mu} \times \mathbf{p}_{\tau}$$

$$p_{\parallel}(\mathbf{v}) \text{ along } \mathbf{p}_{\tau}$$

$$p_{\perp}(\mathbf{v}) \text{ 3}^{\text{rd}} \text{ term } \perp \mathbf{p}_{\tau}$$



Can reconstruct B decay vertex if **tau** & B^0 mass/origin assumed

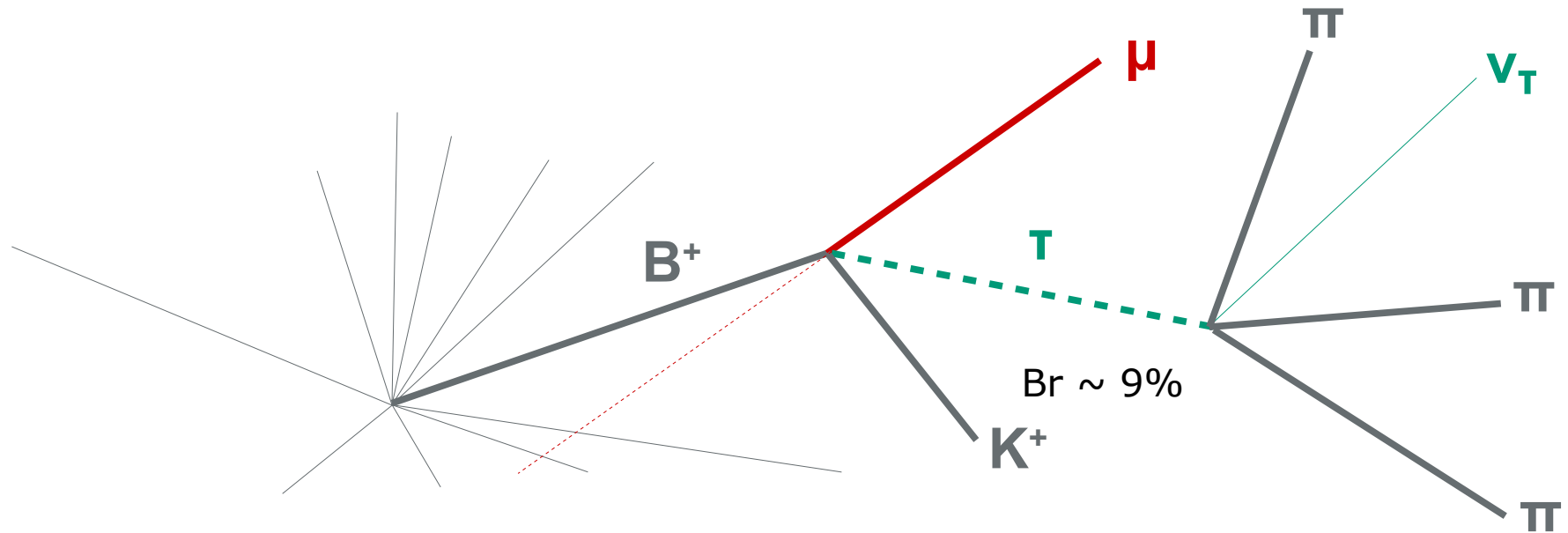
always: $p_{\perp}(\mathbf{v}) = -p_{\perp}(\mathbf{3n})$, for given V_B : $p_{\perp}(\mathbf{v}) = -p_{\perp}(\mathbf{3n})$, $p_{\parallel}(\mathbf{v})$ fixed by masses

Challenge #3 : Tau-decay

Adding an extra charged meson fixes B decay vertex

“Tags” the presence of the parent meson

CHALLENGE: need to detect 5 particles



$p_{\perp}(\mathbf{v})$ and $p_{\parallel}(\mathbf{v})$ determined by $p(\mathbf{3}\pi)$, but still need to find $p_{\parallel}(\mathbf{v})$

SOLUTION: could fix **tau** mass and check B mass or v.v.