

# Flavor Changing Neutral Current transitions in Warped Extra Dimension

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October 19, 2018



# Outline

- ① Motivations
- ② Introduction to the RS model and its variants
- ③ Wrong sign  $b \rightarrow ss\bar{d}$  and  $b \rightarrow dd\bar{s}$  transitions
- ④  $\overline{B}^0 \rightarrow K^+ \pi^-$  decay in the RS models
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- ⑥ Summary

## Motivations I

- Need to go beyond the SM
- Hierarchies
  - ★ Gauge hierarchy problem :  $M_{\text{EW}} \ll M_{\text{Pl}}$
  - ★ SM flavor puzzle :  $m_e \ll m_t$
- The Randall-Sundrum model is among few proposals which can solve both issues.
- Interesting solutions by considering fifth dimension and a warped metric (warped extra dimension).
- Search for the Warped Extra Dimension
- Direct Search: Find KK resonances
- Indirect Search: Flavor Phenomenology of the RS model



Tree level FCNCs

## Motivations II

- Rare  $B$ -meson and  $\Lambda_b$ -baryon decays induced by FCNC transitions.
- Radiative and semi-leptonic  $B$ -meson decays in RS model.

[Burdman, 2004; Agashe *et al.*, 2005; Casagrande *et al.*, 2008; Blanke *et al.*, 2009;  
Bauer *et al.*, 2010; Blanke *et al.*, 2012; Biancofiore *et al.*, 2014]
- Alternative approach: Highly suppressed wrong-sign Kaon decays.

[Huitu, Lü, Singer, Zhang, Phys. Rev. Lett. 81, 4313 (1998)]
- Wrong-sign Kaon decays are  $\Delta S = -1(b \rightarrow d\bar{d}s)$  and  $\Delta S = +2(b \rightarrow s\bar{s}\bar{d})$  transitions in the SM which are highly suppressed compared to the Right-sign Kaon decays which are  $\Delta S = 0$  and  $\Delta S = +1$  transitions.
- Inclusive  $b \rightarrow d\bar{d}s$  and  $b \rightarrow s\bar{s}\bar{d}$  decays studies in different beyond SM scenarios.

[Huitu *et al.*, 1999; Wu *et al.*, 2004; Cai *et al.*, 2004; Fajfer *et al.*, 2006]
- Exclusive doubly weak decays studies in various NP models.

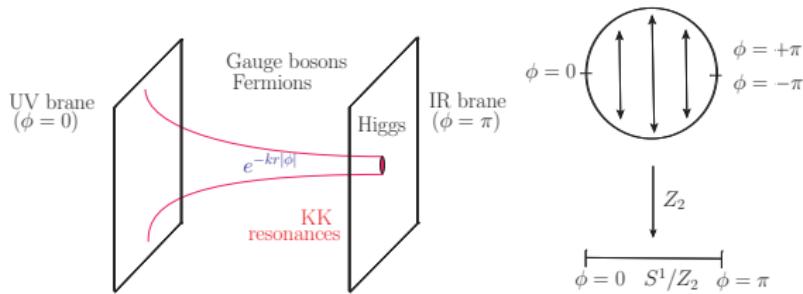
[Fajfer *et al.*, 2000; Fajfer *et al.*, 2001; Chun *et al.*, 2003; Fajfer *et al.*, 2006; Pirjol *et al.*, 2010]
- Only three body modes are searched in the experiments. Two body exclusive decays never suggested before. Why?
- $\overline{B}^0 \rightarrow K^+ \pi^-$  decay never studied before. Experimentally measurable by observing deviations in the  $B^0$ - $\overline{B}^0$  mixing oscillation curve in the study of time dependent decay of  $B^0 \rightarrow K^+ \pi^-$  with large experimental data.
- Impact of RS model with tree level FCNCs on the doubly weak rare hadronic  $B$ -meson decays and on semi-leptonic  $\Lambda_b$ -baryon decays.

# Introduction to the Randall-Sundrum model

- 5D spacetime with **warped** metric

$$ds^2 = e^{-2kr|\phi|} \eta_{\mu\nu} dx^\mu dx^\nu - r^2 d\phi^2, \quad \phi \in [-\pi, \pi]$$

[Randall, Sundrum, Phys. Rev. Lett. 83, 3370 (1999)]



- The fundamental scale is  $M_{\text{Pl}}$ , and the effective 4D electroweak scale emerges through the **warped factor**

$$M_{\text{EW}} \sim e^{-kr\pi} M_{\text{Pl}} \sim \text{TeV}$$

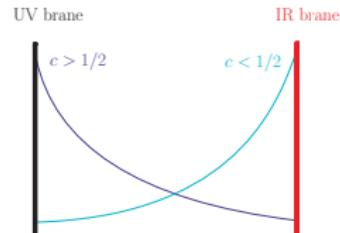
- natural explanation of **gauge hierarchy** problem.
- **Kaluza-Klein (KK) excitations** live close to the IR brane.

# Solution to the flavor problem and flavor implications

- The profiles of zero mode fermions depend heavily on bulk mass parameter  $c$

$$f^{(0)}(y, c) \propto e^{(\frac{1}{2}-c)ky}$$

$c > 1/2$ : Localized near UV brane  
 $c < 1/2$ : Localized near IR brane



- Hierarchical structure can be naturally generated.

- Light fermions live close to UV brane.
- Third generation localized closest to the IR brane.

$$m_{ij} \propto v(Y_{u,d}^{(5D)})_{ij} f(c_{Q_i}) f(c_{u_j, d_j})$$

- Warped extra dimension with bulk fields have explanation for fermion masses and CKM hierarchies.
- Couplings involve overlap integrals of profiles, so different SM fermion profiles lead to flavour non-universal couplings of KK gauge bosons.
- Rotation to the fermion mass basis generates tree level FCNCs.
- New tree level FCNC effects strongly suppressed for light SM fermions by RS-GIM mechanism.

# The RS model with Custodial protection

- The RS<sub>c</sub> model is based on a single **warped extra dimension** with the bulk gauge group

$$SU(3)_c \times SU(2)_L \times SU(2)_R \times U(1)_X \times P_{LR}$$

- The Only free parameter coming from space-time geometry

$$M_{KK} \equiv k e^{-k\pi r} \sim \mathcal{O}(\text{TeV})$$

- SM matter fields and gauge bosons are allowed to propagate in the bulk while the Higgs sector is localized on the **IR brane**.
- Discrete  $P_{LR}$  symmetry interchanging the two  $SU(2)_{L,R}$  provide the custodial protection of  $Z b_L \bar{b}_L$  coupling.
- The mass of the lowest **Kaluza-Klein (KK)** states is  $M_{g^{(1)}} \approx 2.45 M_{KK}$ .
- The mixing among zero modes and higher KK modes of neutral gauge bosons give rise to new heavy electroweak  $Z_H$  and  $Z'$  gauge bosons.

## The bulk-Higgs RS model

- The bulk-Higgs RS model is based on a single **warped extra dimension** with the bulk gauge group

$$SU(3)_c \times SU(2)_V \times U(1)_Y$$

- All the fields in SM including matter fields, gauge bosons as well as Higgs boson are allowed to propagate in the 5D spacetime.
- We consider the summation over the contributions from the **entire KK towers**, with the lightest KK states having mass  $M_{g^{(1)}} \approx 2.45 M_{\text{KK}}$ .
- Mixing among the Goldstone bosons  $\varphi^\pm, \varphi^3$  and the fifth components of the gauge fields give rise to additional KK towers of physical scalars known as the **extended scalar sector**.

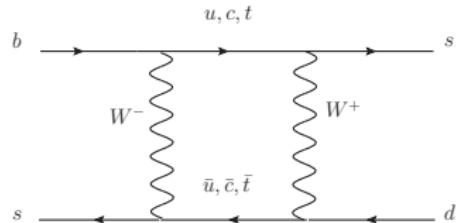
## $b \rightarrow ss\bar{d}$ and $b \rightarrow dd\bar{s}$ transitions in the SM

- Local  $\Delta S = 2$  SM effective Hamiltonian for  $b \rightarrow ss\bar{d}$  transition

$$\mathcal{H}_{\text{eff}}^{\Delta S=2} = \frac{G_F^2 m_W^2}{4\pi^2} \left( V_{td} V_{ts}^* V_{tb} V_{ts}^* S_0 \left( \frac{m_t^2}{m_W^2} \right) + V_{cd} V_{cs}^* V_{tb} V_{ts}^* S_0 \left( \frac{m_t^2}{m_W^2}, \frac{m_b^2}{m_W^2} \right) \right) [(\bar{s}_L^i \gamma^\mu b_L^i)(\bar{s}_L^j \gamma_\mu d_L^j)]$$

- Local  $\Delta S = -1$  SM effective Hamiltonian for  $b \rightarrow dd\bar{s}$  transition  $s \leftrightarrow d$

$$\mathcal{B}(b \rightarrow ss\bar{d})_{\text{SM}} = (2.19 \pm 0.38) \times 10^{-12}$$
$$\mathcal{B}(b \rightarrow dd\bar{s})_{\text{SM}} = (2.24 \pm 0.41) \times 10^{-14}$$



- $b \rightarrow ss\bar{d}$  and  $b \rightarrow dd\bar{s}$  decays with very small strengths in the SM serve as a sensitive probe for new physics searches.

$$\mathcal{B}(B^+ \rightarrow K^+ K^+ \pi^-) < 1.1 \times 10^{-8}$$

$$\mathcal{B}(B^+ \rightarrow \pi^+ \pi^+ K^-) < 4.6 \times 10^{-8}$$

[R. Aaij *et al.* (LHCb), Phys. Lett. B765, 307 (2017)]

## $b \rightarrow ss\bar{d}$ decay in the RS<sub>c</sub> model

- $b \rightarrow ss\bar{d}$  decay receives **tree level contributions** from the Kaluza-Klein (KK) gluons, the heavy KK photons, new heavy electroweak (EW) gauge bosons  $Z_H$  and  $Z'$ , and in principle the  $Z$  boson.

$$M_{G^{(1)}} = M_{Z_H} = M_{Z'} = M_{A^{(1)}} \equiv M_{g^{(1)}} \approx 2.45 \text{ } M_{\text{KK}}$$

- Custodial protection of the  $Z b_L \bar{b}_L$  coupling through the discrete  $P_{LR}$  symmetry renders tree-level  $Z$  contributions negligible.
- The effective Hamiltonian for the  $\Delta S = 2$   $b \rightarrow ss\bar{d}$  decay with the Wilson coefficients corresponding to  $\mu = \mathcal{O}(M_{g^{(1)}})$

$$\begin{aligned} [\mathcal{H}_{\text{eff}}^{\Delta S=2}]_{\text{KK}} &= \frac{1}{(M_{g^{(1)}})^2} [C_1^{VLL} \mathcal{Q}_1^{VLL} + C_1^{VRR} \mathcal{Q}_1^{VRR} \\ &\quad + C_1^{LR} \mathcal{Q}_1^{LR} + C_2^{LR} \mathcal{Q}_2^{LR} + C_1^{RL} \mathcal{Q}_1^{RL} + C_2^{RL} \mathcal{Q}_2^{RL}]. \end{aligned}$$

$$\mathcal{Q}_1^{VLL} = (\bar{s}\gamma_\mu P_L b)(\bar{s}\gamma^\mu P_L d),$$

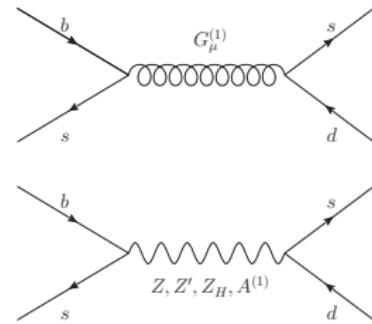
$$\mathcal{Q}_1^{LR} = (\bar{s}\gamma_\mu P_L b)(\bar{s}\gamma^\mu P_R d),$$

$$\mathcal{Q}_2^{LR} = (\bar{s}P_L b)(\bar{s}P_R d),$$

$$\mathcal{Q}_1^{VRR} = (\bar{s}\gamma_\mu P_R b)(\bar{s}\gamma^\mu P_R d),$$

$$\mathcal{Q}_1^{RL} = (\bar{s}\gamma_\mu P_R b)(\bar{s}\gamma^\mu P_L d),$$

$$\mathcal{Q}_2^{RL} = (\bar{s}P_R b)(\bar{s}P_L d).$$



# $b \rightarrow ss\bar{d}$ decay in the RS<sub>c</sub> model

$$\begin{aligned} [C_1^{VLL}(M_{g(1)})]^{\mathcal{G}^{(1)}} &= 1/3[\Delta_L^{sb}(\mathcal{G}^{(1)})][\Delta_L^{sd}(\mathcal{G}^{(1)})], \\ [C_1^{VRR}(M_{g(1)})]^{\mathcal{G}^{(1)}} &= 1/3[\Delta_R^{sb}(\mathcal{G}^{(1)})][\Delta_R^{sd}(\mathcal{G}^{(1)})], \\ [C_1^{LR}(M_{g(1)})]^{\mathcal{G}^{(1)}} &= -1/6[\Delta_L^{sb}(\mathcal{G}^{(1)})][\Delta_R^{sd}(\mathcal{G}^{(1)})], \\ [C_2^{LR}(M_{g(1)})]^{\mathcal{G}^{(1)}} &= -[\Delta_L^{sb}(\mathcal{G}^{(1)})][\Delta_R^{sd}(\mathcal{G}^{(1)})], \\ [C_1^{RL}(M_{g(1)})]^{\mathcal{G}^{(1)}} &= -1/6[\Delta_R^{sb}(\mathcal{G}^{(1)})][\Delta_L^{sd}(\mathcal{G}^{(1)})], \\ [C_2^{RL}(M_{g(1)})]^{\mathcal{G}^{(1)}} &= -[\Delta_R^{sb}(\mathcal{G}^{(1)})][\Delta_L^{sd}(\mathcal{G}^{(1)})], \end{aligned}$$

$$\begin{aligned} [\Delta C_1^{VLL}(M_{g(1)})]^{A^{(1)}} &= [\Delta_L^{sb}(A^{(1)})][\Delta_L^{sd}(A^{(1)})], \\ [\Delta C_1^{VRR}(M_{g(1)})]^{A^{(1)}} &= [\Delta_R^{sb}(A^{(1)})][\Delta_R^{sd}(A^{(1)})], \\ [\Delta C_1^{LR}(M_{g(1)})]^{A^{(1)}} &= [\Delta_L^{sb}(A^{(1)})][\Delta_R^{sd}(A^{(1)})], \\ [\Delta C_1^{RL}(M_{g(1)})]^{A^{(1)}} &= [\Delta_R^{sb}(A^{(1)})][\Delta_L^{sd}(A^{(1)})], \end{aligned}$$

$$\begin{aligned} [\Delta C_1^{VLL}(M_{g(1)})]^{Z_H, Z'} &= [\Delta_L^{sb}(Z^{(1)})\Delta_L^{sd}(Z^{(1)}) + \Delta_L^{sb}(Z_X^{(1)})\Delta_L^{sd}(Z_X^{(1)})], \\ [\Delta C_1^{VRR}(M_{g(1)})]^{Z_H, Z'} &= [\Delta_R^{sb}(Z^{(1)})\Delta_R^{sd}(Z^{(1)}) + \Delta_R^{sb}(Z_X^{(1)})\Delta_R^{sd}(Z_X^{(1)})], \\ [\Delta C_1^{LR}(M_{g(1)})]^{Z_H, Z'} &= [\Delta_L^{sb}(Z^{(1)})\Delta_R^{sd}(Z^{(1)}) + \Delta_L^{sb}(Z_X^{(1)})\Delta_R^{sd}(Z_X^{(1)})], \\ [\Delta C_1^{RL}(M_{g(1)})]^{Z_H, Z'} &= [\Delta_R^{sb}(Z^{(1)})\Delta_L^{sd}(Z^{(1)}) + \Delta_R^{sb}(Z_X^{(1)})\Delta_L^{sd}(Z_X^{(1)})], \end{aligned}$$

## $b \rightarrow ss\bar{d}$ decay in the RS<sub>c</sub> model

$$C_1^{VLL}(M_{g^{(1)}}) = [0.333 + 0.01 + 0.28]\tilde{\Delta}_L^{sb}\tilde{\Delta}_L^{sd} = 0.623\tilde{\Delta}_L^{sb}\tilde{\Delta}_L^{sd},$$

$$C_1^{VRR}(M_{g^{(1)}}) = [0.333 + 0.01 + 0.49]\tilde{\Delta}_R^{sb}\tilde{\Delta}_R^{sd} = 0.833\tilde{\Delta}_R^{sb}\tilde{\Delta}_R^{sd},$$

$$C_1^{LR}(M_{g^{(1)}}) = [-0.167 + 0.01 + 0.28]\tilde{\Delta}_L^{sb}\tilde{\Delta}_R^{sd} = 0.123\tilde{\Delta}_L^{sb}\tilde{\Delta}_R^{sd},$$

$$C_1^{RL}(M_{g^{(1)}}) = [-0.167 + 0.01 + 0.28]\tilde{\Delta}_R^{sb}\tilde{\Delta}_L^{sd} = 0.123\tilde{\Delta}_R^{sb}\tilde{\Delta}_L^{sd},$$

- After **renormalization group** running of the Wilson coefficients to a low energy scale  $\mu_b = 4.6 \text{ GeV}$ , the decay width in the RS<sub>c</sub> model

$$\begin{aligned}\Gamma_{\text{RS}_c} = & \frac{m_b^5}{3072(2\pi)^3(M_{g^{(1)}})^4}[16(|C_1^{VLL}(\mu_b)|^2 + |C_1^{VRR}(\mu_b)|^2) \\ & + 12(|C_1^{LR}(\mu_b)|^2 + |C_1^{RL}(\mu_b)|^2) + 3(|C_2^{LR}(\mu_b)|^2 + |C_2^{RL}(\mu_b)|^2) \\ & - 2\Re(C_1^{LR}(\mu_b)C_2^{*LR}(\mu_b) + C_2^{LR}(\mu_b)C_1^{*LR}(\mu_b)) \\ & + C_1^{RL}(\mu_b)C_2^{*RL}(\mu_b) + C_2^{RL}(\mu_b)C_1^{*RL}(\mu_b))].\end{aligned}$$

# $b \rightarrow ss\bar{d}$ decay in the bulk-Higgs RS model

- We start with the effective Hamiltonian

$$[\mathcal{H}_{\text{eff}}^{\Delta S=2}]_{KK} = \sum_{n=1}^5 [C_n \mathcal{O}_n + \tilde{C}_n \tilde{\mathcal{O}}_n],$$

$$\begin{aligned}\mathcal{O}_1 &= (\bar{s}_L \gamma_\mu b_L)(\bar{s}_L \gamma^\mu d_L), & \mathcal{O}_4 &= (\bar{s}_R b_L)(\bar{s}_L d_R), \\ \mathcal{O}_2 &= (\bar{s}_R b_L)(\bar{s}_R d_L), & \mathcal{O}_5 &= (\bar{s}_R^\alpha b_L^\beta)(\bar{s}_L^\beta d_R^\alpha). \\ \mathcal{O}_3 &= (\bar{s}_R^\alpha b_L^\beta)(\bar{s}_R^\beta d_L^\alpha),\end{aligned}$$

$$C_1 = \frac{4\pi L}{M_{KK}^2} (\tilde{\Delta}_D)_{23} \otimes (\tilde{\Delta}_D)_{21} \left[ \frac{\alpha_s}{2} \left(1 - \frac{1}{N_c}\right) + \alpha Q_d^2 + \frac{\alpha}{s_w^2 c_w^2} (T_3^d - Q_d s_w^2)^2 \right],$$

$$\tilde{C}_1 = \frac{4\pi L}{M_{KK}^2} (\tilde{\Delta}_d)_{23} \otimes (\tilde{\Delta}_d)_{21} \left[ \frac{\alpha_s}{2} \left(1 - \frac{1}{N_c}\right) + \alpha Q_d^2 + \frac{\alpha}{s_w^2 c_w^2} (-Q_d s_w^2)^2 \right],$$

$$C_4 = -\frac{4\pi L \alpha_s}{M_{KK}^2} (\tilde{\Delta}_D)_{23} \otimes (\tilde{\Delta}_d)_{21} - \frac{L}{\pi \beta M_{KK}^2} (\tilde{\Omega}_d)_{23} \otimes (\tilde{\Omega}_D)_{21},$$

$$\tilde{C}_4 = -\frac{4\pi L \alpha_s}{M_{KK}^2} (\tilde{\Delta}_d)_{23} \otimes (\tilde{\Delta}_D)_{21} - \frac{L}{\pi \beta M_{KK}^2} (\tilde{\Omega}_D)_{23} \otimes (\tilde{\Omega}_d)_{21},$$

$$C_5 = \frac{4\pi L}{M_{KK}^2} (\tilde{\Delta}_D)_{23} \otimes (\tilde{\Delta}_d)_{21} \left[ \frac{\alpha_s}{N_c} - 2\alpha Q_d^2 + \frac{2\alpha}{s_w^2 c_w^2} (T_3^d - Q_d s_w^2)(Q_d s_w^2) \right],$$

$$\tilde{C}_5 = \frac{4\pi L}{M_{KK}^2} (\tilde{\Delta}_d)_{23} \otimes (\tilde{\Delta}_D)_{21} \left[ \frac{\alpha_s}{N_c} - 2\alpha Q_d^2 + \frac{2\alpha}{s_w^2 c_w^2} (T_3^d - Q_d s_w^2)(Q_d s_w^2) \right].$$

# $b \rightarrow ss\bar{d}$ decay in the bulk-Higgs RS model

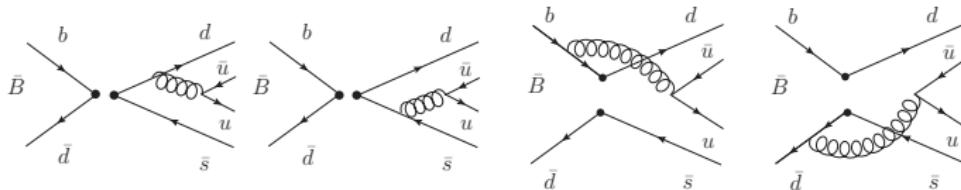
$$\begin{aligned} (\widetilde{\Delta}_D)_{23} \otimes (\widetilde{\Delta}_d)_{21} &\rightarrow (U_d^\dagger)_{2i}(U_d)_{i3}(\widetilde{\Delta}_{Dd})_{ij}(W_d^\dagger)_{2j}(W_d)_{j1}, \\ (\widetilde{\Delta}_{Dd})_{ij} &= \frac{F^2(c_{Q_i})}{3 + 2c_{Q_i}} \frac{3 + c_{Q_i} + c_{d_j}}{2(2 + c_{Q_i} + c_{d_j})} \frac{F^2(c_{d_j})}{3 + 2c_{d_j}}, \\ (\widetilde{\Omega}_D)_{23} \otimes (\widetilde{\Omega}_d)_{21} &\rightarrow (U_d^\dagger)_{2i}(W_d)_{j3}(\widetilde{\Omega}_{Dd})_{ijkl}(W_d^\dagger)_{2k}(U_d)_{l1}, \\ (\widetilde{\Omega}_{Dd})_{ijkl} &= \frac{\pi(1 + \beta)}{4L} \frac{F(c_{Q_i})F(c_{d_j})}{2 + \beta + c_{Q_i} + c_{d_j}} \frac{(Y_d)_{ij}(Y_d^\dagger)_{kl}}{1} \\ &\times \frac{(4 + 2\beta + c_{Q_i} + c_{d_j} + c_{d_k} + c_{Q_l})}{4 + c_{Q_i} + c_{d_j} + c_{d_k} + c_{Q_l}} \frac{F(c_{d_k})F(c_{Q_l})}{2 + \beta + c_{d_k} + c_{Q_l}}. \end{aligned}$$

- The decay width in the bulk-Higgs RS model

$$\begin{aligned} \Gamma_{KK} = & \frac{m_b^5}{3072(2\pi)^3} [64(|C_1(\mu_b)|^2 + |\tilde{C}_1(\mu_b)|^2) \\ & + 12(|C_4(\mu_b)|^2 + |\tilde{C}_4(\mu_b)|^2 + |C_5(\mu_b)|^2 + |\tilde{C}_5(\mu_b)|^2) \\ & + 4\mathcal{R}e(C_4(\mu_b)C_5^*(\mu_b) + C_4^*(\mu_b)C_5(\mu_b) \\ & + \tilde{C}_4(\mu_b)\tilde{C}_5^*(\mu_b) + \tilde{C}_4^*(\mu_b)\tilde{C}_5(\mu_b))]. \end{aligned}$$

# $\overline{B}^0 \rightarrow K^+ \pi^-$ decay in the Standard Model

$$\mathcal{H}^{\text{SM}} = C^{\text{SM}} [(\bar{d}_L^\alpha \gamma^\mu b_L^\alpha)(\bar{d}_L^\beta \gamma_\mu s_L^\beta)],$$



$$\mathcal{A}^{\text{SM}} = F_{a1} \left[ \frac{4}{3} C^{\text{SM}} \right] + \mathcal{M}_{a1} [C^{\text{SM}}],$$

$$F_{a1} = 4\pi C_F m_B^2 f_B \int_0^1 dx_2 dx_3 \int_0^\infty b_2 db_2 b_3 db_3 \left[ \left\{ x_3 \phi_K^A(x_2) \phi_\pi^A(x_3) + 2r_\pi r_K \phi_K^P(x_2) \left[ (\phi_\pi^P(x_3) - \phi_\pi^T(x_3)) \right. \right. \right. \\ \left. \left. \left. + x_3 (\phi_\pi^P(x_3) + \phi_\pi^T(x_3)) \right] \right\} E_a(t_a) h_a(x_2, x_3, b_2, b_3) S_t(x_3) - \left\{ (1-x_2) \phi_K^A(x_2) \phi_\pi^A(x_3) + 4r_\pi r_K \phi_K^P(x_2) \phi_\pi^P(x_3) \right. \\ \left. - 2r_\pi r_K x_2 \phi_\pi^P(x_3) (\phi_K^P(x_2) - \phi_K^T(x_2)) \right\} E_a(t_b) h_b(x_2, x_3, b_2, b_3) S_t(x_2) \right],$$

$$\mathcal{M}_{a1} = 8\pi C_F \frac{\sqrt{2N_c}}{N_c} m_B^2 \int_0^1 dx_1 dx_2 dx_3 \int_0^\infty b_1 db_1 b_3 db_3 \phi_B \left[ \left\{ (1-x_2) \phi_K^A(x_2) \phi_\pi^A(x_3) + r_\pi r_K \left[ (1-x_2) (\phi_K^P(x_2) - \phi_K^T(x_2)) \right. \right. \right. \\ \times (\phi_\pi^P(x_3) + \phi_\pi^T(x_3)) + x_3 (\phi_K^P(x_2) + \phi_K^T(x_2)) (\phi_\pi^P(x_3) - \phi_\pi^T(x_3)) \left. \right\} E'_a(t_c) h_c(x_1, x_2, x_3, b_1, b_3) \\ - \left\{ x_3 \phi_K^A(x_2) \phi_\pi^A(x_3) + r_\pi r_K \left[ 4\phi_K^P(x_2) \phi_\pi^P(x_3) - (1-x_3) (\phi_K^P(x_2) - \phi_K^T(x_2)) (\phi_\pi^P(x_3) + \phi_\pi^T(x_3)) \right. \right. \\ \left. \left. - x_2 (\phi_K^P(x_2) + \phi_K^T(x_2)) (\phi_\pi^P(x_3) - \phi_\pi^T(x_3)) \right] \right\} E'_a(t_d) h_d(x_1, x_2, x_3, b_1, b_3) \right],$$

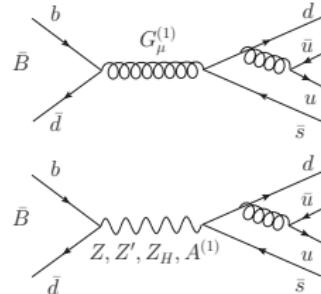
$$\mathcal{B}(\overline{B}^0 \rightarrow K^+ \pi^-)^{\text{SM}} = 1.0 \times 10^{-19}$$

# $\overline{B}^0 \rightarrow K^+ \pi^-$ decay in the RS<sub>c</sub> model

$$[\mathcal{H}_{\text{eff}}]_{\text{RS}_c} = \frac{1}{[M_{g(1)}]^2} [C_1^{VLL} \mathcal{O}_1 + C_1^{VRR} \tilde{\mathcal{O}}_1 + C_4^{LR} \mathcal{O}_4 + C_4^{RL} \tilde{\mathcal{O}}_4 + C_5^{LR} \mathcal{O}_5 + C_5^{RL} \tilde{\mathcal{O}}_5].$$

$$\begin{aligned}\mathcal{O}_1 &= (\bar{d}_L \gamma_\mu b_L)(\bar{d}_L \gamma^\mu s_L), \\ \mathcal{O}_4 &= (\bar{d}_R b_L)(\bar{d}_L s_R), \\ \mathcal{O}_5 &= (\bar{d}_R^\alpha b_L^\beta)(\bar{d}_L^\beta s_R^\alpha).\end{aligned}$$

$$\begin{aligned}[C_1^{VLL}(M_{g(1)})]^{\mathcal{G}^{(1)}} &= 1/3 p_{UV}^2 \Delta_L^{db} \Delta_L^{ds}, \\ [C_1^{VRR}(M_{g(1)})]^{\mathcal{G}^{(1)}} &= 1/3 p_{UV}^2 \Delta_R^{db} \Delta_R^{ds}, \\ [C_4^{LR}(M_{g(1)})]^{\mathcal{G}^{(1)}} &= -p_{UV}^2 \Delta_L^{db} \Delta_R^{ds}, \\ [C_4^{RL}(M_{g(1)})]^{\mathcal{G}^{(1)}} &= -p_{UV}^2 \Delta_R^{db} \Delta_L^{ds}, \\ [C_5^{LR}(M_{g(1)})]^{\mathcal{G}^{(1)}} &= 1/3 p_{UV}^2 \Delta_L^{db} \Delta_R^{ds}, \\ [C_5^{RL}(M_{g(1)})]^{\mathcal{G}^{(1)}} &= 1/3 p_{UV}^2 \Delta_R^{db} \Delta_L^{ds},\end{aligned}$$



$$\begin{aligned}[\Delta C_1^{VLL}(M_{g(1)})]^{A^{(1)}} &= [\Delta_L^{db}(A^{(1)})][\Delta_L^{ds}(A^{(1)})], \\ [\Delta C_1^{VRR}(M_{g(1)})]^{A^{(1)}} &= [\Delta_R^{db}(A^{(1)})][\Delta_R^{ds}(A^{(1)})], \\ [\Delta C_5^{LR}(M_{g(1)})]^{A^{(1)}} &= -2[\Delta_L^{db}(A^{(1)})][\Delta_R^{ds}(A^{(1)})], \\ [\Delta C_5^{RL}(M_{g(1)})]^{A^{(1)}} &= -2[\Delta_R^{db}(A^{(1)})][\Delta_L^{ds}(A^{(1)})].\end{aligned}$$

$$\begin{aligned}[\Delta C_1^{VLL}(M_{g(1)})]^{Z_H, Z'} &= [\Delta_L^{db}(Z^{(1)}) \Delta_L^{ds}(Z^{(1)}) + \Delta_L^{db}(Z_X^{(1)}) \Delta_L^{ds}(Z_X^{(1)})], \\ [\Delta C_1^{VRR}(M_{g(1)})]^{Z_H, Z'} &= [\Delta_R^{db}(Z^{(1)}) \Delta_R^{ds}(Z^{(1)}) + \Delta_R^{db}(Z_X^{(1)}) \Delta_R^{ds}(Z_X^{(1)})], \\ [\Delta C_5^{LR}(M_{g(1)})]^{Z_H, Z'} &= -2[\Delta_L^{db}(Z^{(1)}) \Delta_R^{ds}(Z^{(1)}) + \Delta_L^{db}(Z_X^{(1)}) \Delta_R^{ds}(Z_X^{(1)})], \\ [\Delta C_5^{RL}(M_{g(1)})]^{Z_H, Z'} &= -2[\Delta_R^{db}(Z^{(1)}) \Delta_L^{ds}(Z^{(1)}) + \Delta_R^{db}(Z_X^{(1)}) \Delta_L^{ds}(Z_X^{(1)})],\end{aligned}$$

$$\begin{aligned}\mathcal{A} &= \frac{1}{[M_{g(1)}]^2} \left[ F_{a1} \left[ \frac{4}{3} (C_1^{VLL} + C_1^{VRR}) \right] + F_{a4} \left[ \frac{4}{3} (C_4^{LR} + C_4^{RL}) \right] + F_{a5} \left[ \frac{4}{3} (C_5^{LR} + C_5^{RL}) \right] \right. \\ &\quad \left. + \mathcal{M}_{a1} \left[ C_1^{VLL} - C_1^{VRR} \right] + \mathcal{M}_{a4} \left[ C_4^{LR} - C_4^{RL} \right] + \mathcal{M}_{a5} \left[ C_5^{LR} - C_5^{RL} \right] \right].\end{aligned}$$

# $\overline{B}^0 \rightarrow K^+ \pi^-$ decay in the bulk-Higgs RS model

- We start with the effective Hamiltonian

$$[\mathcal{H}_{\text{eff}}^{\Delta S = -1}]_{KK} = \sum_{n=1}^5 [C_n \mathcal{O}_n + \tilde{C}_n \tilde{\mathcal{O}}_n],$$

$$\begin{aligned}\mathcal{O}_1 &= (\bar{d}_L \gamma_\mu b_L)(\bar{d}_L \gamma^\mu s_L), & \mathcal{O}_4 &= (\bar{d}_R b_L)(\bar{d}_L s_R), \\ \mathcal{O}_2 &= (\bar{d}_R b_L)(\bar{d}_R s_L), & \mathcal{O}_5 &= (\bar{d}_R^\alpha b_L^\beta)(\bar{d}_L^\beta s_R^\alpha), \\ \mathcal{O}_3 &= (\bar{d}_R^\alpha b_L^\beta)(\bar{d}_R^\beta s_L^\alpha),\end{aligned}$$

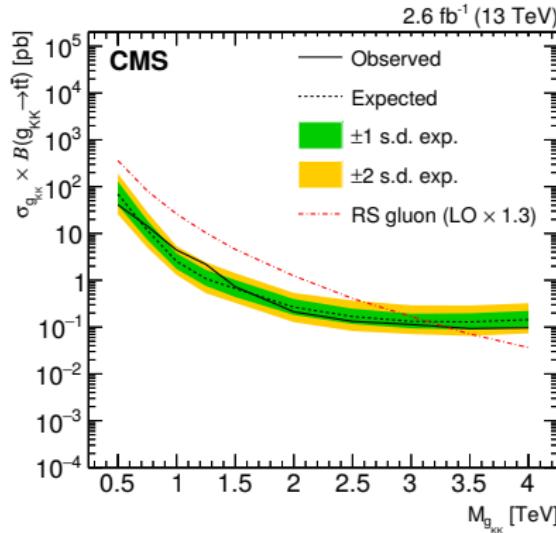
$$\begin{aligned}\mathcal{A} = F_{a1} &\left[ \frac{4}{3}(C_1 + \tilde{C}_1) \right] + F_{a4} \left[ \frac{4}{3}(C_4 + \tilde{C}_4) \right] + F_{a5} \left[ \frac{4}{3}(C_5 + \tilde{C}_5) \right] \\ &+ \mathcal{M}_{a1} \left[ C_1 - \tilde{C}_1 \right] + \mathcal{M}_{a4} \left[ C_4 - \tilde{C}_4 \right] + \mathcal{M}_{a5} \left[ C_5 - \tilde{C}_5 \right],\end{aligned}$$

$$\Gamma = \frac{m_B^3}{64\pi} |\mathcal{A}|^2.$$

# Constraints on the RS Parameter space

- Direct Searches

[A. M. Sirunyan *et al.* (CMS), JHEP 07 (2017) 001]



$$M_{g^{(1)}} > 3.3 \text{ TeV} \quad (95\% \text{ CL}).$$

# More Constraints

- The RS<sub>c</sub> model

- Constraint from tree-level analysis of the **S** and **T** parameters

[Malm, Neubert, Novotny, Schmell, JHEP 01 (2014) 173]

$$M_{g(1)} > 4.8 \text{ TeV} \quad (95\% \text{ CL}).$$

- The bulk-Higgs RS model

$$S = \frac{2\pi v^2}{M_{KK}^2} \left( 1 - \frac{1}{(2 + \beta)^2} - \frac{1}{2L} \right)$$

$$T = \frac{\pi v^2}{2c_W^2 M_{KK}^2} \frac{2L(1 + \beta)^2}{(2 + \beta)(3 + 2\beta)}$$

$$U = 0.$$

[M. Baak *et al.* (Gfitter), Eur. Phys. J. C74 (2014) 3046]

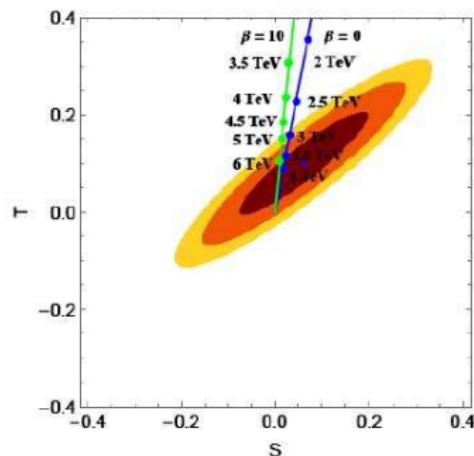
$$S = 0.06 \pm 0.09$$

$$T = 0.10 \pm 0.07$$

$$U = 0.$$

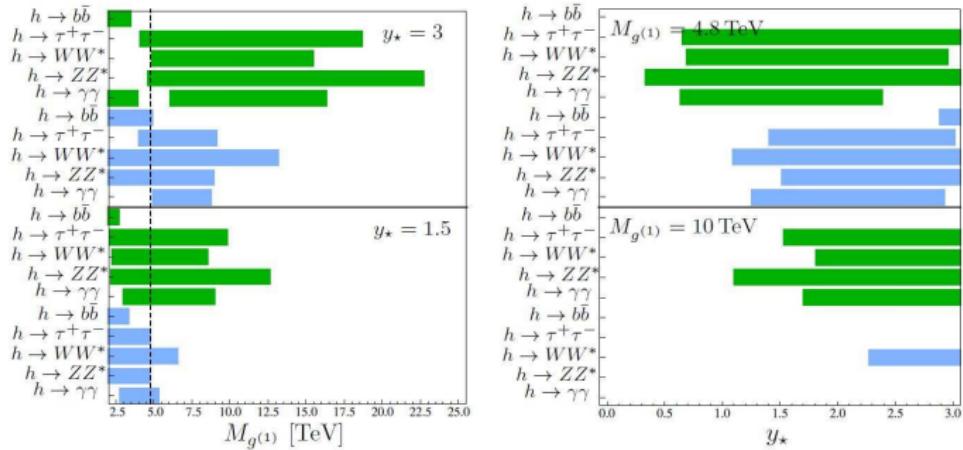
$M_{KK} > 5 \text{ TeV}$ , with  $\beta = 10$

$M_{KK} > 3 \text{ TeV}$ , with  $\beta = 0$



## More Constraints

- The RS<sub>c</sub> model



[Malm, Neubert, Schmell, JHEP 02 (2015) 008]

- Stringent bounds emerge from the signal rates for  $pp \rightarrow h \rightarrow ZZ^*, WW^*$ , at 95% CL

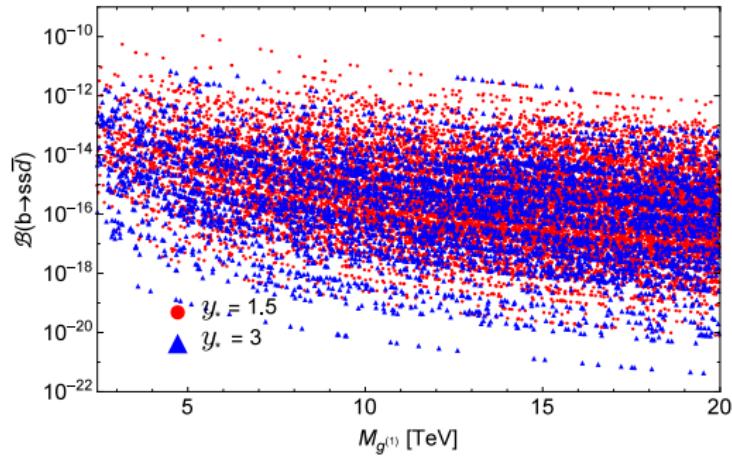
$$M_{g(1)}|_{\text{brane-Higgs}}^{\text{custodial RS}} > 22.7 \text{ TeV} \times \left(\frac{y^*}{3}\right), \quad M_{g(1)}|_{\text{Higgs}}^{\text{narrow custodial RS}} > 13.2 \text{ TeV} \times \left(\frac{y^*}{3}\right)$$

# Branching ratio of $b \rightarrow ss\bar{d}$ in the RS<sub>c</sub> model

$\Delta M_K$ ,  $\epsilon_K$  and  $\Delta M_{B_s}$  constraints

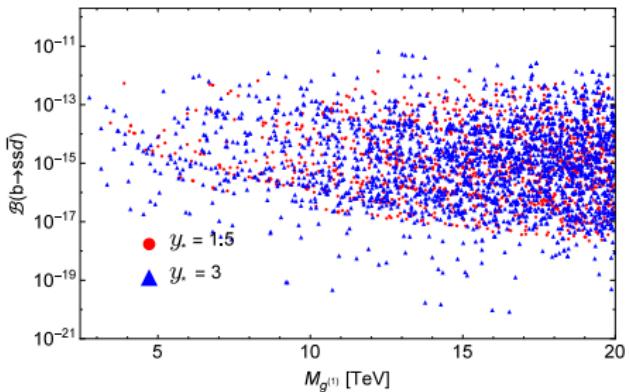
KK gluons dominant

Comparable  $Z_H$  and  $Z'$  contributions



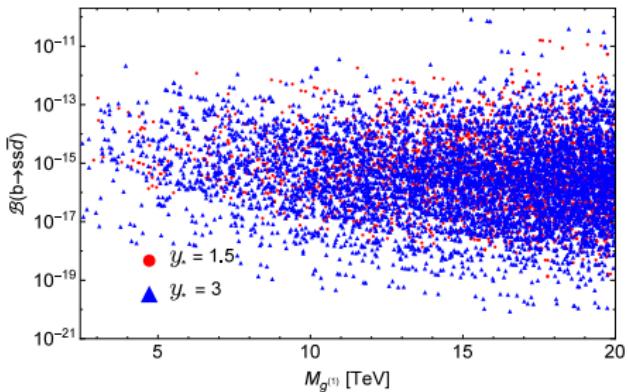
# Branching ratio of $b \rightarrow ss\bar{d}$ in the bulk-Higgs RS model

broad Higgs profile



$$\beta = 1$$

narrow Higgs profile

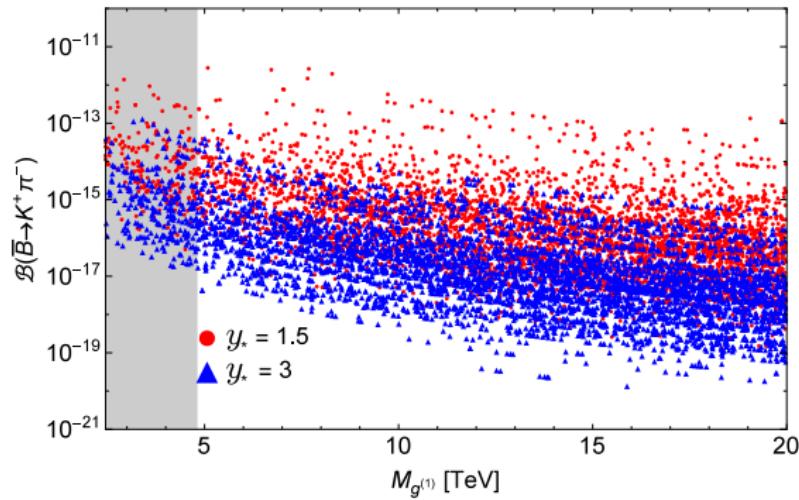


$$\beta = 10$$

# Branching ratio of $\bar{B}^0 \rightarrow K^+ \pi^-$ decay in the RS<sub>c</sub> model

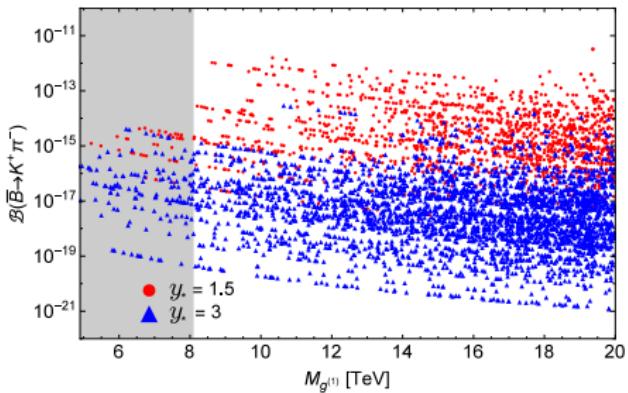
$\Delta M_K$ ,  $\epsilon_K$  and  $\Delta M_{B_d}$   
constraints

KK gluons dominant



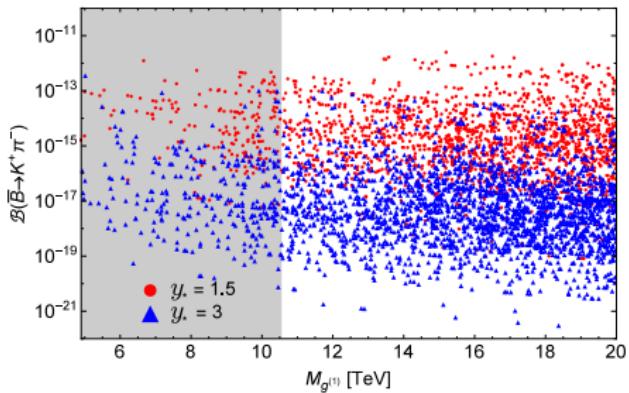
# Branching ratio in the bulk-Higgs RS model

broad Higgs profile



$$\beta = 1$$

narrow Higgs profile



$$\beta = 10$$

# Model Independent Analysis of $\bar{B}^0 \rightarrow K^+ \pi^-$ decay

- Assuming new physics contribution only to local operator  $\mathcal{O}_1$

$$[\mathcal{H}_{\text{eff}}^{\Delta S=-1}] = C_1^{dd\bar{s}} (\bar{d}_L \gamma_\mu b_L) (\bar{d}_L \gamma^\mu s_L),$$

$$[\mathcal{H}_{\text{eff}}^{\Delta S=2}] = C_1^K (\bar{d}_L \gamma_\mu s_L) (\bar{d}_L \gamma^\mu s_L), \quad C_1^{dd\bar{s}} \sim \sqrt{C_1^K C_1^{B_d}}$$

$$[\mathcal{H}_{\text{eff}}^{\Delta B=2}] = C_1^{B_d} (\bar{d}_L \gamma_\mu b_L) (\bar{d}_L \gamma^\mu b_L).$$

- Assuming NP contributions come from non standard model chiralities

$$\begin{aligned} \mathcal{A}_j(\bar{B}^0 \rightarrow K^+ \pi^-) &= F_{aj} \left[ \frac{4}{3} C_j^{dd\bar{s}} \right] + \mathcal{M}_{aj} \left[ C_j^{dd\bar{s}} \right] \\ \tilde{\mathcal{A}}_j(\bar{B}^0 \rightarrow K^+ \pi^-) &= F_{aj} \left[ \frac{4}{3} \tilde{C}_j^{dd\bar{s}} \right] + \mathcal{M}_{aj} \left[ -\tilde{C}_j^{dd\bar{s}} \right] \end{aligned}$$

$$R \equiv \frac{\mathcal{B}(\bar{B}^0 \rightarrow K^+ \pi^-)}{\mathcal{B}(\bar{B}^0 \rightarrow K^- \pi^+)}$$

- For an experimental precision of  $R < 0.001$

Parameter	Allowed range ( $\text{GeV}^{-2}$ )	Parameter	Allowed range ( $\text{GeV}^{-2}$ )
		$\tilde{C}_1$	$< 1.1 \times 10^{-7}$
$C_2$	$< 6.3 \times 10^{-9}$	$\tilde{C}_2$	$< 6.8 \times 10^{-9}$
$C_3$	$< 5.1 \times 10^{-8}$	$\tilde{C}_3$	$< 5.3 \times 10^{-8}$
$C_4$	$< 4.9 \times 10^{-9}$	$\tilde{C}_4$	$< 4.2 \times 10^{-9}$
$C_5$	$< 1.6 \times 10^{-6}$	$\tilde{C}_5$	$< 7.3 \times 10^{-7}$

# New Physics with Conserved Charge

- NP Lagrangian of a generic form

$$\mathcal{L}_{\text{flavor}} = g_{b \rightarrow d} (\bar{d} \Gamma b) X + g_{d \rightarrow b} (\bar{b} \Gamma d) X + g_{s \rightarrow d} (\bar{d} \Gamma s) X + g_{d \rightarrow s} (\bar{s} \Gamma d) X + \text{h.c.},$$

$$\begin{aligned}\mathcal{L}_{\text{eff}} = & \frac{1}{M_X^2} \left[ g_{s \rightarrow d} g_{d \rightarrow s}^* (\bar{d} \Gamma s) (\bar{d} \bar{\Gamma} s) + g_{b \rightarrow d} g_{d \rightarrow b}^* (\bar{d} \Gamma b) (\bar{d} \bar{\Gamma} b) \right. \\ & \left. + g_{b \rightarrow d} g_{d \rightarrow s}^* (\bar{d} \Gamma b) (\bar{d} \bar{\Gamma} s) + g_{s \rightarrow d} g_{d \rightarrow b}^* (\bar{d} \bar{\Gamma} b) (\bar{d} \Gamma s) \right].\end{aligned}$$

- $K^0 - \overline{K}^0$  and  $B^0 - \overline{B}^0$  mixing bounds

$$\frac{|g_{s \rightarrow d} g_{d \rightarrow s}^*|}{M_X^2} < \frac{1}{(\Lambda_j^K)^2}, \quad \frac{|g_{b \rightarrow d} g_{d \rightarrow b}^*|}{M_X^2} < \frac{1}{(\Lambda_j^B)^2}.$$

Scenarios	$R_X$				$R_{\text{SM}}$
	$M_X$ (TeV)	Case-I	$M_X$ (TeV)	Case-II	
S1	1.0	0.085	10	$8.5 \times 10^{-6}$	$6.8 \times 10^{-15}$
S2		0.074		$7.3 \times 10^{-6}$	
S3		55		0.005	
S4		0.002		$1.9 \times 10^{-7}$	

# $\Lambda_b \rightarrow \Lambda(\rightarrow p\pi^-)\mu^+\mu^-$ decay in the RS<sub>c</sub> model

- The effective weak Hamiltonian for  $b \rightarrow s\mu^+\mu^-$  transition in the RS<sub>c</sub> model

$$H_{\text{eff}}^{\text{RS}_c} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left[ C_7^{\text{RS}_c} O_7 + C_7'^{\text{RS}_c} O'_7 + C_9^{\text{RS}_c} O_9 + C_9'^{\text{RS}_c} O'_9 + C_{10}^{\text{RS}_c} O_{10} + C_{10}'^{\text{RS}_c} O'_{10} \right],$$

$$O_7 = \frac{e}{16\pi^2} m_b (\bar{s}_{L\alpha} \sigma^{\mu\nu} b_{R\alpha}) F_{\mu\nu}, \quad O'_7 = \frac{e}{16\pi^2} m_b (\bar{s}_{R\alpha} \sigma^{\mu\nu} b_{L\alpha}) F_{\mu\nu},$$

$$O_9 = \frac{e^2}{16\pi^2} (\bar{s}_{L\alpha} \gamma^\mu b_{L\alpha}) \bar{\mu} \gamma_\mu \mu, \quad O'_9 = \frac{e^2}{16\pi^2} (\bar{s}_{R\alpha} \gamma^\mu b_{R\alpha}) \bar{\mu} \gamma_\mu \mu,$$

$$O_{10} = \frac{e^2}{16\pi^2} (\bar{s}_{L\alpha} \gamma^\mu b_{L\alpha}) \bar{\mu} \gamma_\mu \gamma_5 \mu, \quad O'_{10} = \frac{e^2}{16\pi^2} (\bar{s}_{R\alpha} \gamma^\mu b_{R\alpha}) \bar{\mu} \gamma_\mu \gamma_5 \mu.$$

$$C_i^{(\prime)\text{RS}_c} = C_i^{(\prime)\text{SM}} + \Delta C_i^{(\prime)},$$

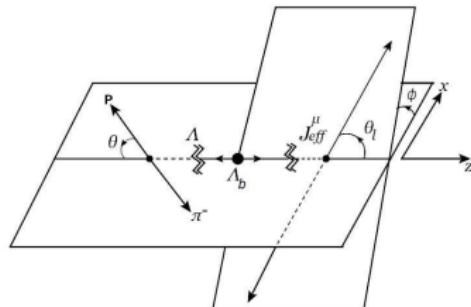
$$\Delta C_9 = \frac{\Delta Y_s}{\sin^2 \theta_W} - 4\Delta Z_s, \quad \Delta Y_s = -\frac{1}{V_{tb} V_{ts}^*} \sum_X \frac{\Delta_L^{\mu\mu}(X) - \Delta_R^{\mu\mu}(X)}{4M_X^2 g_{SM}^2} \Delta_L^{bs}(X),$$

$$\Delta C'_9 = \frac{\Delta Y'_s}{\sin^2 \theta_W} - 4\Delta Z'_s, \quad \Delta Y'_s = -\frac{1}{V_{tb} V_{ts}^*} \sum_X \frac{\Delta_L^{\mu\mu}(X) - \Delta_R^{\mu\mu}(X)}{4M_X^2 g_{SM}^2} \Delta_R^{bs}(X),$$

$$\Delta C_{10} = -\frac{\Delta Y_s}{\sin^2 \theta_W}, \quad \Delta Z_s = \frac{1}{V_{tb} V_{ts}^*} \sum_X \frac{\Delta_R^{\mu\mu}(X)}{8M_X^2 g_{SM}^2 \sin^2 \theta_W} \Delta_L^{bs}(X),$$

$$\Delta C'_{10} = \frac{\Delta Y'_s}{\sin^2 \theta_W}, \quad \Delta Z'_s = \frac{1}{V_{tb} V_{ts}^*} \sum_X \frac{\Delta_R^{\mu\mu}(X)}{8M_X^2 g_{SM}^2 \sin^2 \theta_W} \Delta_R^{bs}(X).$$

# Angular distributions



- $\theta = \theta_\Lambda$  : angle of emission between  $\Lambda$  and  $p$  in di-meson rest frame
- $\theta_l = \theta_\mu$  : angle of emission between  $\mu^-$  and  $z$ -axis in di-muon rest frame
- $\phi$  : angle between the two planes
- $q^2 = s$  : di-muon invariant mass squared

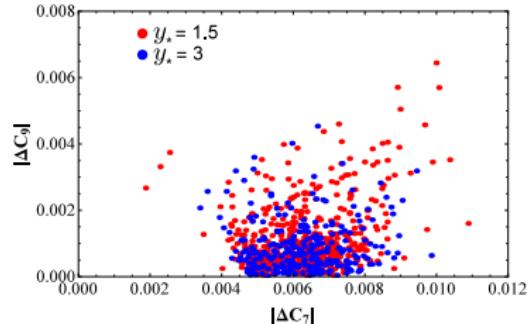
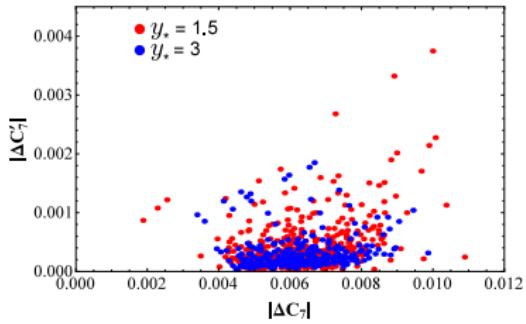
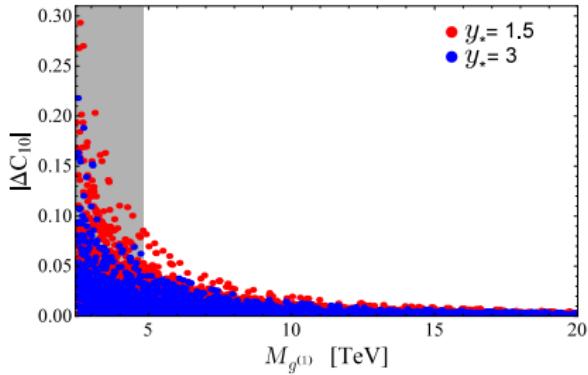
- The angular decay distribution of the four-fold decay  $\Lambda_b \rightarrow \Lambda(\rightarrow p\pi)\mu^+\mu^-$

$$\frac{d^4\Gamma}{ds d\cos\theta_\Lambda d\cos\theta_l d\phi} = \frac{3}{8\pi} \left[ K_{1ss} \sin^2\theta_l + K_{1cc} \cos^2\theta_l + K_{1c} \cos\theta_l + (K_{2ss} \sin^2\theta_l + K_{2cc} \cos^2\theta_l + K_{2c} \cos\theta_l) \cos\theta_\Lambda + (K_{3sc} \sin\theta_l \cos\theta_l + K_{3s} \sin\theta_l) \sin\theta_\Lambda \sin\phi + (K_{4sc} \sin\theta_l \cos\theta_l + K_{4s} \sin\theta_l) \sin\theta_\Lambda \cos\phi \right].$$

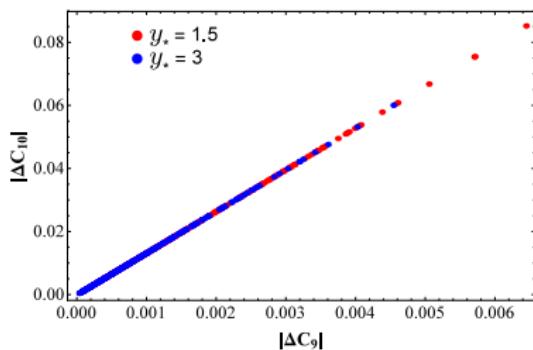
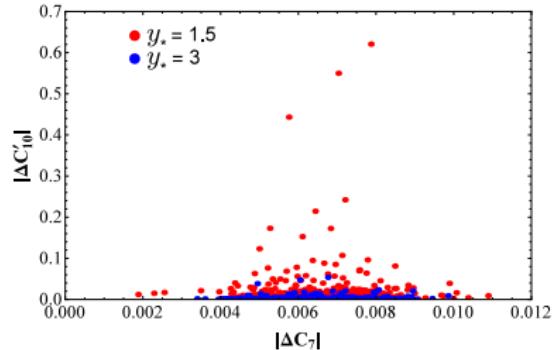
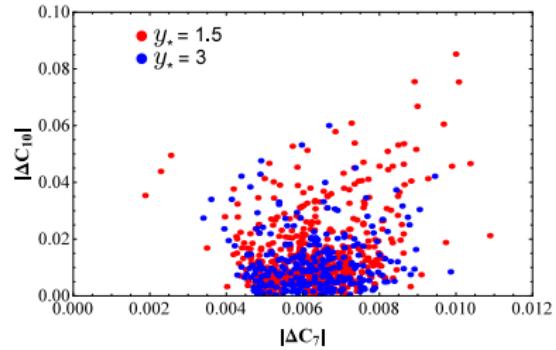
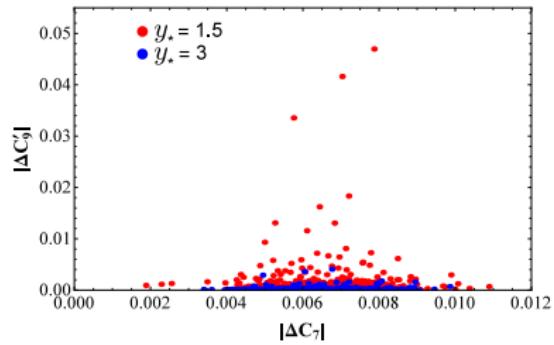
$$\frac{d\Gamma}{ds} = 2K_{1ss} + K_{1cc}, \quad F_L = \frac{2K_{1ss} - K_{1cc}}{2K_{1ss} + K_{1cc}}, \quad A_{FB}^l = \frac{3K_{1c}}{4K_{1ss} + 2K_{1cc}},$$

$$A_{FB}^\Lambda = \frac{2K_{2ss} + K_{2cc}}{4K_{1ss} + 2K_{1cc}}, \quad A_{FB}^{l\Lambda} = \frac{3K_{2c}}{8K_{1ss} + 4K_{1cc}}.$$

## Wilson coefficients



# Correlations plots between the Wilson coefficients



# Numerical Results

	$\left\langle \frac{d\mathcal{B}}{ds} \times 10^{-7} \right\rangle$	$\langle F_L \rangle$	$\langle A_{FB}^\ell \rangle$	$\langle A_{FB}^A \rangle$	$\langle A_{FB}^{IA} \rangle$	
$[0.1, 2]$	SM	$0.238^{+0.230}_{-0.230}$	$0.535^{+0.065}_{-0.078}$	$0.097^{+0.006}_{-0.007}$	$-0.310^{+0.015}_{-0.008}$	$-0.031^{+0.003}_{-0.002}$
	$RS_c _{M_g^{(1)}} = 4.8$	$0.219^{+0.218}_{-0.217}$	$0.552^{+0.069}_{-0.084}$	$0.093^{+0.005}_{-0.006}$	$-0.313^{+0.013}_{-0.004}$	$-0.030^{+0.003}_{-0.002}$
	$RS_c _{M_g^{(1)}} = 10$	$0.233^{+0.228}_{-0.225}$	$0.539^{+0.066}_{-0.080}$	$0.096^{+0.006}_{-0.007}$	$-0.311^{+0.015}_{-0.007}$	$-0.031^{+0.003}_{-0.002}$
	LHCb	$0.36^{+0.122}_{-0.112}$	$0.56^{+0.244}_{-0.566}$	$0.37^{+0.371}_{-0.481}$	$-0.12^{+0.344}_{-0.318}$	—
$[2, 4]$	SM	$0.180^{+0.123}_{-0.123}$	$0.855^{+0.008}_{-0.012}$	$0.054^{+0.037}_{-0.030}$	$-0.306^{+0.022}_{-0.012}$	$-0.016^{+0.008}_{-0.009}$
	$RS_c _{M_g^{(1)}} = 4.8$	$0.171^{+0.118}_{-0.117}$	$0.860^{+0.008}_{-0.006}$	$0.040^{+0.035}_{-0.026}$	$-0.311^{+0.016}_{-0.005}$	$-0.013^{+0.009}_{-0.010}$
	$RS_c _{M_g^{(1)}} = 10$	$0.177^{+0.120}_{-0.120}$	$0.857^{+0.008}_{-0.011}$	$0.051^{+0.037}_{-0.030}$	$-0.309^{+0.021}_{-0.010}$	$-0.016^{+0.008}_{-0.009}$
	LHCb	$0.11^{+0.120}_{-0.091}$	—	—	—	—
$[4, 6]$	SM	$0.232^{+0.110}_{-0.110}$	$0.807^{+0.018}_{-0.012}$	$-0.063^{+0.038}_{-0.026}$	$-0.311^{+0.014}_{-0.008}$	$0.021^{+0.007}_{-0.009}$
	$RS_c _{M_g^{(1)}} = 4.8$	$0.224^{+0.108}_{-0.108}$	$0.806^{+0.021}_{-0.016}$	$-0.078^{+0.034}_{-0.021}$	$-0.314^{+0.008}_{-0.002}$	$0.024^{+0.008}_{-0.009}$
	$RS_c _{M_g^{(1)}} = 10$	$0.230^{+0.110}_{-0.110}$	$0.807^{+0.019}_{-0.013}$	$-0.067^{+0.037}_{-0.025}$	$-0.313^{+0.013}_{-0.006}$	$0.022^{+0.007}_{-0.009}$
	LHCb	$0.02^{+0.091}_{-0.010}$	—	—	—	—
$[6, 8]$	SM	$0.312^{+0.094}_{-0.094}$	$0.724^{+0.025}_{-0.014}$	$-0.162^{+0.025}_{-0.017}$	$-0.317^{+0.007}_{-0.004}$	$0.052^{+0.005}_{-0.007}$
	$RS_c _{M_g^{(1)}} = 4.8$	$0.306^{+0.094}_{-0.093}$	$0.720^{+0.026}_{-0.016}$	$-0.174^{+0.021}_{-0.013}$	$-0.314^{+0.002}_{-0.001}$	$0.054^{+0.005}_{-0.007}$
	$RS_c _{M_g^{(1)}} = 10$	$0.310^{+0.094}_{-0.094}$	$0.723^{+0.025}_{-0.014}$	$-0.165^{+0.024}_{-0.016}$	$-0.317^{+0.006}_{-0.003}$	$0.053^{+0.006}_{-0.007}$
	LHCb	$0.25^{+0.120}_{-0.111}$	—	—	—	—
$[1.1, 6]$	SM	$0.199^{+0.120}_{-0.120}$	$0.818^{+0.011}_{-0.011}$	$0.009^{+0.027}_{-0.018}$	$-0.309^{+0.018}_{-0.010}$	$-0.002^{+0.004}_{-0.005}$
	$RS_c _{M_g^{(1)}} = 4.8$	$0.190^{+0.120}_{-0.119}$	$0.824^{+0.010}_{-0.007}$	$-0.005^{+0.025}_{-0.014}$	$-0.312^{+0.012}_{-0.004}$	$0.001^{+0.005}_{-0.006}$
	$RS_c _{M_g^{(1)}} = 10$	$0.197^{+0.120}_{-0.120}$	$0.819^{+0.011}_{-0.011}$	$0.006^{+0.026}_{-0.017}$	$-0.311^{+0.017}_{-0.008}$	$-0.001^{+0.004}_{-0.005}$
	LHCb	$0.09^{+0.061}_{-0.051}$	—	—	—	—

# Numerical Results

	$\left\langle \frac{d\beta}{ds} \times 10^{-7} \right\rangle$	$\langle F_L \rangle$	$\langle A_{FB}^\ell \rangle$	$\langle A_{FB}^\Lambda \rangle$	$\langle A_{FB}^{l\Lambda} \rangle$	
[15, 16]	SM	$0.798^{+0.073}_{-0.073}$	$0.454^{+0.032}_{-0.017}$	$-0.382^{+0.017}_{-0.008}$	$-0.307^{+0.002}_{-0.004}$	$0.131^{+0.004}_{-0.008}$
	$RS_c _{M_g^{(1)}} = 4.8$	$0.832^{+0.073}_{-0.073}$	$0.447^{+0.033}_{-0.017}$	$-0.365^{+0.014}_{-0.006}$	$-0.287^{+0.003}_{-0.005}$	$0.132^{+0.004}_{-0.008}$
	$RS_c _{M_g^{(1)}} = 10$	$0.804^{+0.074}_{-0.074}$	$0.452^{+0.032}_{-0.017}$	$-0.378^{+0.016}_{-0.008}$	$-0.304^{+0.002}_{-0.004}$	$0.132^{+0.004}_{-0.008}$
	LHCb	$1.12^{+0.197}_{-0.187}$	$0.49^{+0.304}_{-0.304}$	$-0.10^{+0.183}_{-0.163}$	$-0.19^{+0.143}_{-0.163}$	—
[16, 18]	SM	$0.825^{+0.075}_{-0.075}$	$0.418^{+0.033}_{-0.017}$	$-0.381^{+0.013}_{-0.006}$	$-0.289^{+0.005}_{-0.006}$	$0.141^{+0.004}_{-0.008}$
	$RS_c _{M_g^{(1)}} = 4.8$	$0.877^{+0.075}_{-0.075}$	$0.411^{+0.033}_{-0.017}$	$-0.356^{+0.010}_{-0.004}$	$-0.265^{+0.005}_{-0.006}$	$0.140^{+0.004}_{-0.009}$
	$RS_c _{M_g^{(1)}} = 10$	$0.835^{+0.075}_{-0.075}$	$0.416^{+0.033}_{-0.017}$	$-0.376^{+0.012}_{-0.006}$	$-0.284^{+0.005}_{-0.006}$	$0.141^{+0.004}_{-0.008}$
	LHCb	$1.22^{+0.143}_{-0.152}$	$0.68^{+0.158}_{-0.216}$	$-0.07^{+0.136}_{-0.127}$	$-0.44^{+0.104}_{-0.058}$	—
[18, 20]	SM	$0.658^{+0.066}_{-0.066}$	$0.371^{+0.034}_{-0.019}$	$-0.317^{+0.010}_{-0.010}$	$-0.227^{+0.011}_{-0.011}$	$0.153^{+0.005}_{-0.009}$
	$RS_c _{M_g^{(1)}} = 4.8$	$0.726^{+0.066}_{-0.066}$	$0.367^{+0.034}_{-0.020}$	$-0.286^{+0.010}_{-0.010}$	$-0.201^{+0.010}_{-0.010}$	$0.151^{+0.005}_{-0.009}$
	$RS_c _{M_g^{(1)}} = 10$	$0.672^{+0.066}_{-0.066}$	$0.370^{+0.034}_{-0.019}$	$-0.309^{+0.010}_{-0.010}$	$-0.221^{+0.011}_{-0.011}$	$0.153^{+0.005}_{-0.009}$
	LHCb	$1.24^{+0.152}_{-0.149}$	$0.62^{+0.243}_{-0.273}$	$0.01^{+0.155}_{-0.146}$	$-0.13^{+0.095}_{-0.124}$	—
[15, 20]	SM	$0.753^{+0.069}_{-0.069}$	$0.409^{+0.033}_{-0.018}$	$-0.358^{+0.012}_{-0.007}$	$-0.271^{+0.011}_{-0.011}$	$0.143^{+0.005}_{-0.008}$
	$RS_c _{M_g^{(1)}} = 4.8$	$0.807^{+0.069}_{-0.069}$	$0.403^{+0.034}_{-0.019}$	$-0.332^{+0.008}_{-0.009}$	$-0.247^{+0.011}_{-0.011}$	$0.142^{+0.005}_{-0.009}$
	$RS_c _{M_g^{(1)}} = 10$	$0.764^{+0.069}_{-0.069}$	$0.407^{+0.033}_{-0.019}$	$-0.353^{+0.011}_{-0.007}$	$-0.266^{+0.011}_{-0.011}$	$0.143^{+0.005}_{-0.008}$
	LHCb	$1.20^{+0.092}_{-0.099}$	$0.61^{+0.114}_{-0.143}$	$-0.05^{+0.095}_{-0.095}$	$-0.29^{+0.076}_{-0.081}$	—

## Summary

- In both models, main contributions to the branching ratios of the inclusive  $b \rightarrow ss\bar{d}$ ,  $b \rightarrow dd\bar{s}$  and the exclusive  $\bar{B}^0 \rightarrow K^+\pi^-$  decay come from the KK gluons exchange.
- For the inclusive  $b \rightarrow ss\bar{d}$  and  $b \rightarrow dd\bar{s}$  decays in the  $RS_c$  model, contributions of EW gauge bosons  $Z_H$  and  $Z'$  are equally important to that of the KK gluons.
- The  $RS_c$  model enhances the branching ratio, such that compared to the SM result, a maximum enhancement of two and six orders of magnitude for  $b \rightarrow ss\bar{d}$  and  $\bar{B}^0 \rightarrow K^+\pi^-$  decay, respectively is possible for few points in the parameter space with  $y_* = 1.5$  case.
- In the bulk-Higgs RS model, branching ratio of the  $b \rightarrow ss\bar{d}$  gets a maximum increase of one order of magnitude for  $y_* = 1.5$  value with  $\beta = 10$  scenario, while for the exclusive  $\bar{B}^0 \rightarrow K^+\pi^-$  decay, maximum possible enhancement of five to six orders of magnitude is probable for both cases of  $y_*$  within broad and narrow Higgs profile cases.
- In the model independent analysis of  $\bar{B}^0 \rightarrow K^+\pi^-$  decay, it is possible to constrain the Wilson coefficients of different dimension-6 operators for a specific experimental precision for the observable  $R$ .
- The current constraints on the parameters of  $RS_c$  model are too strict to explain the discrepancies in various observables predicted by LHCb measurements in  $\Lambda_b$  decays.

- This talk is based on, arXiv:1807.05350, 1805.01393, 1607.07713, the work done under the supervision of Prof. Lü Cai-Dian and in collaboration with Ying Li, M. Jamil Aslam and Qin Qin.

**THANK YOU!**