

Top quark physics and Top-Higgs interplay

Li Lin Yang
Peking University

14th Workshop on TeV Physics
at Nanjing Normal University

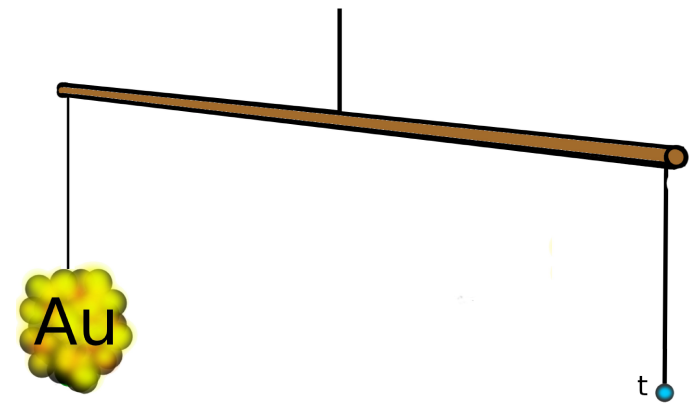
Outline

- * Introduction
- * Top quark pair production
- * Top-Higgs interplay
 - * Higgs production associated with a top quark pair
 - * Top quarks inside loops for Higgs physics
- * Single top quark production



Basic facts about the top quark

Large mass $m_t \approx 173 \text{ GeV}$



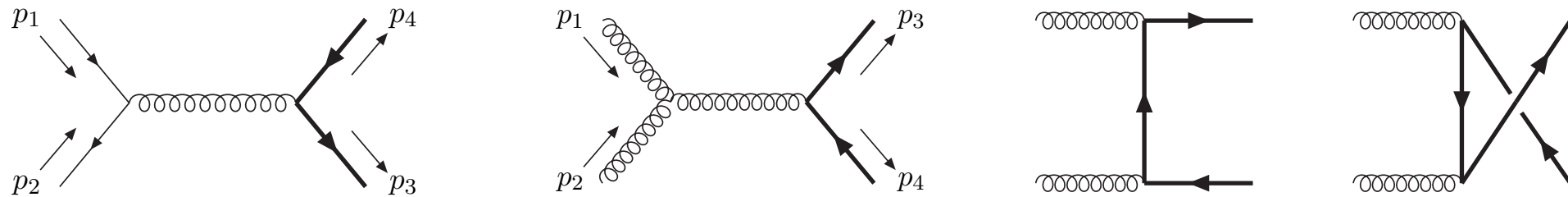
Strong Yukawa coupling $y_t \sim 1$

- Fermion mass origin
- Hierarchy problem
- Vacuum stability

Short lifetime $\tau \sim 5 \times 10^{-25} \text{ s}$

Decays before hadronization: pQCD dominates!

Top quark pair production



A standard candle for the LHC and future colliders

- * Main production mechanism for top quarks
- * Test of the Standard Model at the energy frontier
- * Possible signals of new physics
- * Major background to many searches

State-of-the-art predictions

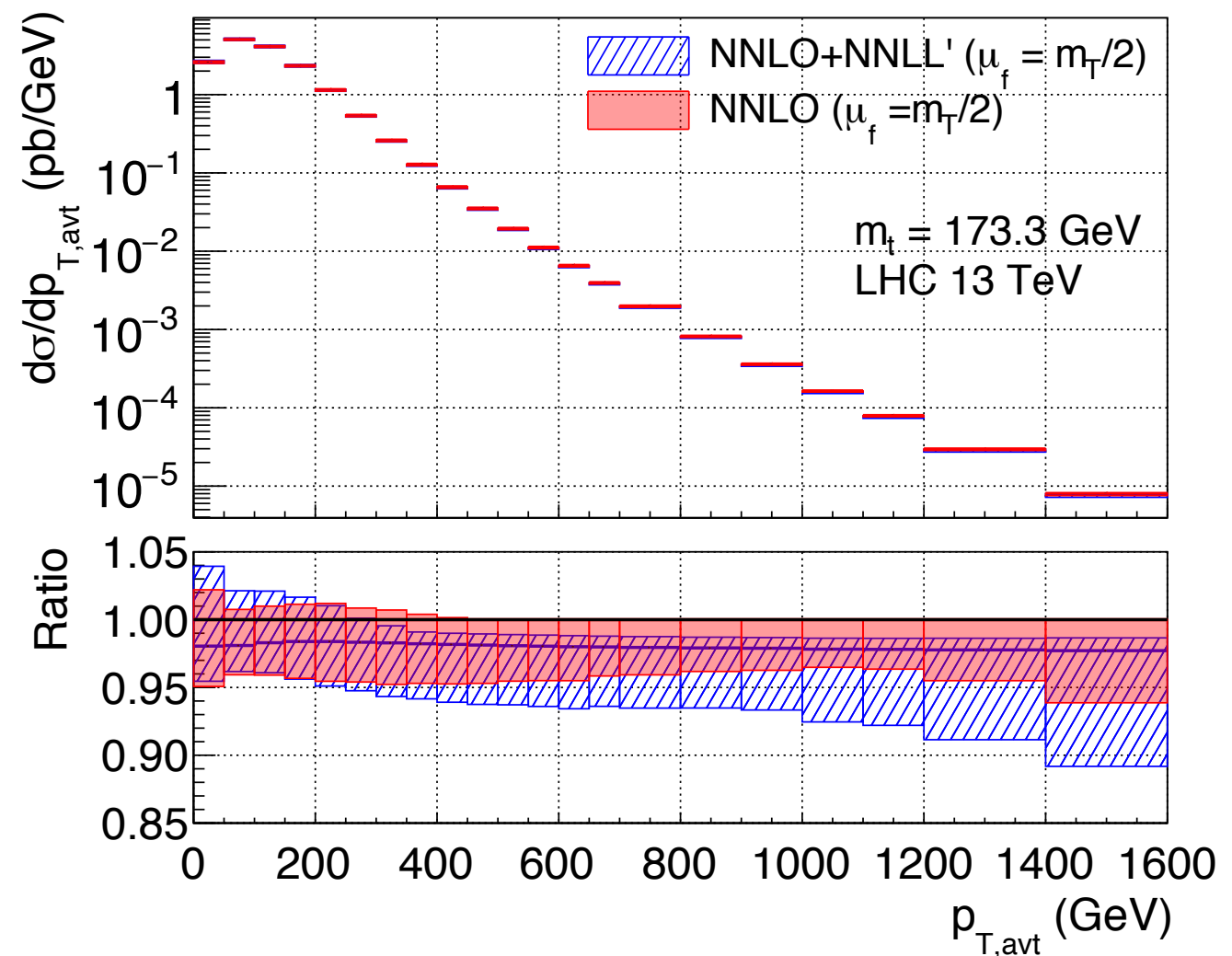
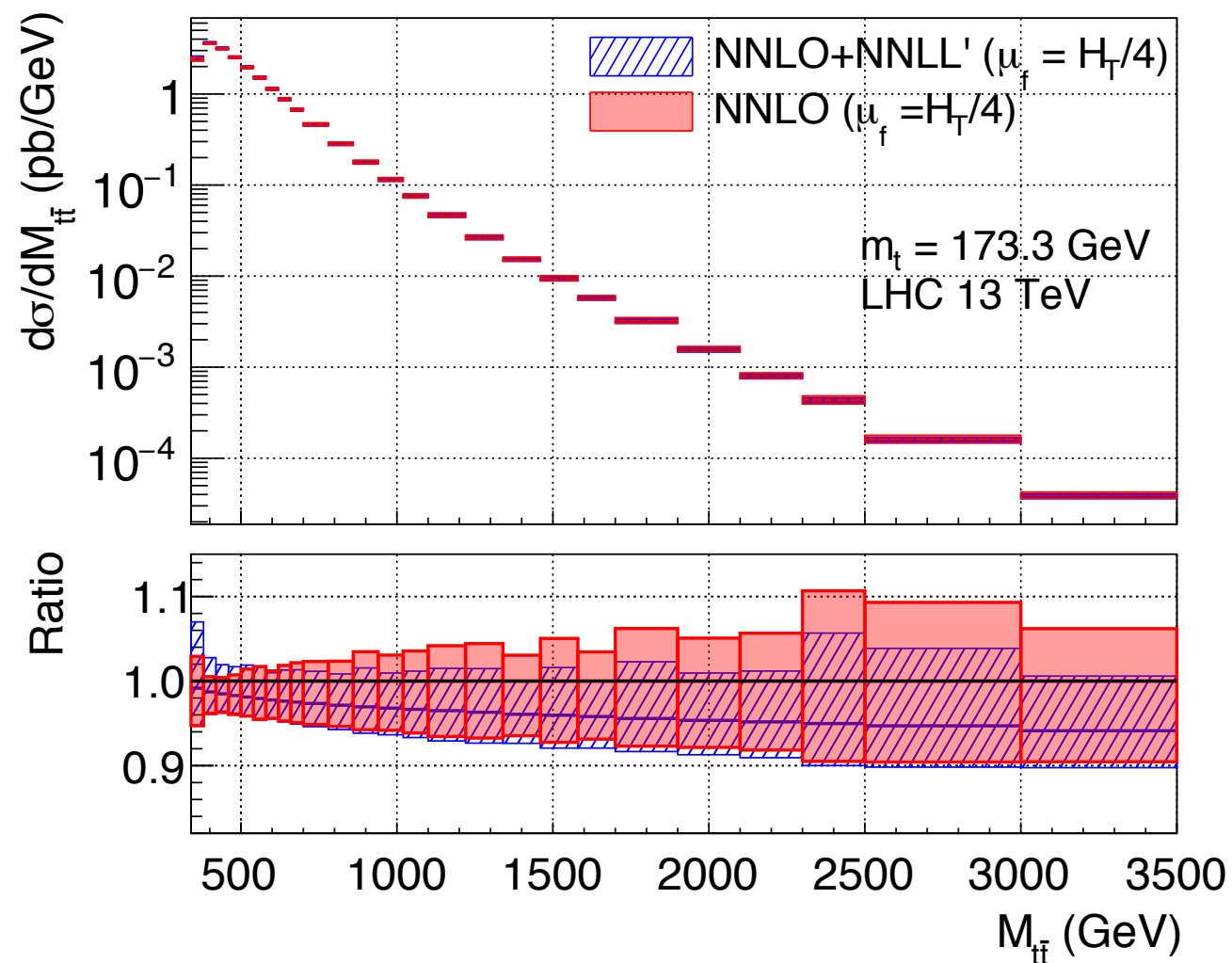
NNLO+NNLL' in QCD

Pecjak, Scott, Wang, **LLY**: 1601.07020

Czakon, Heymes, Mitov: 1606.03350

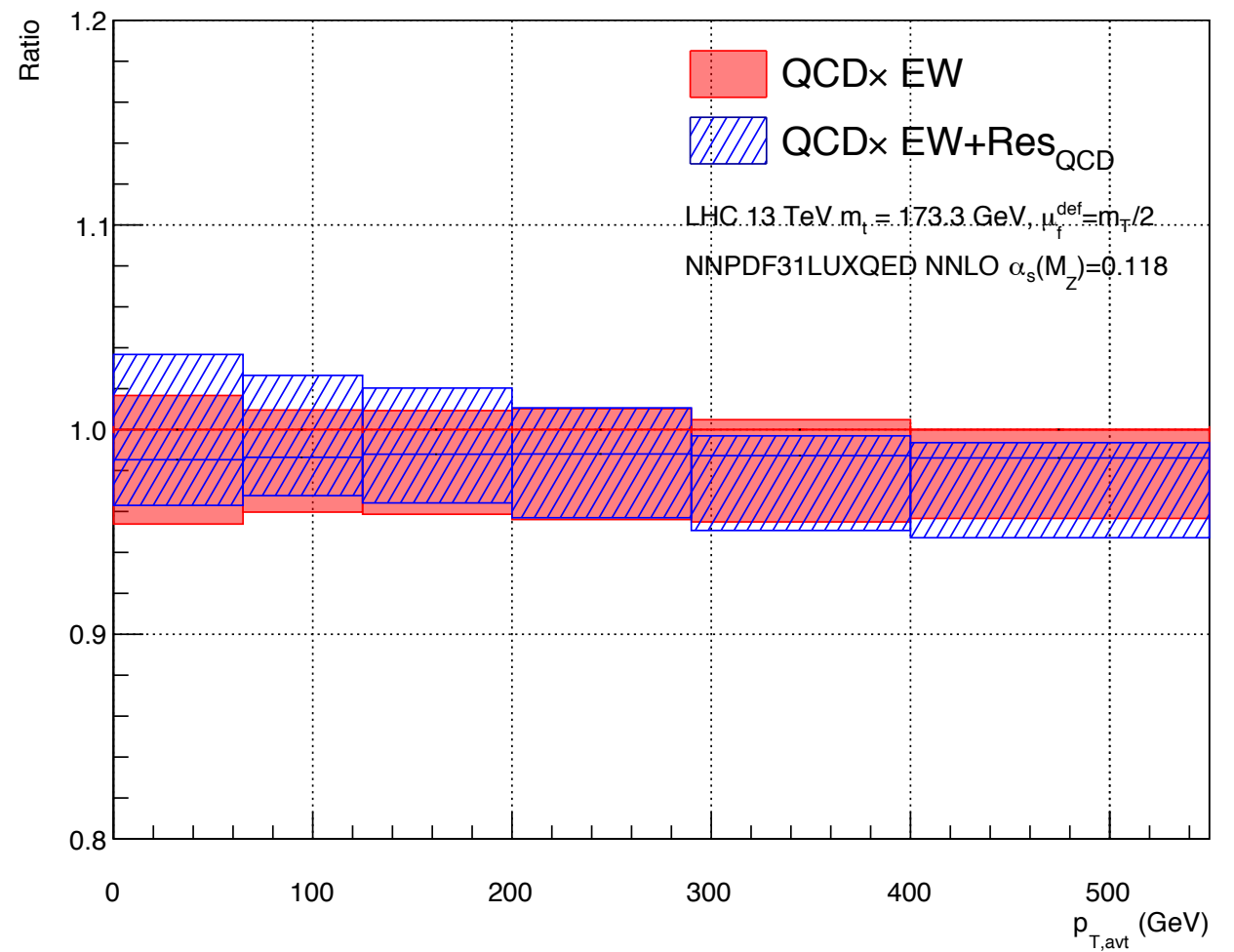
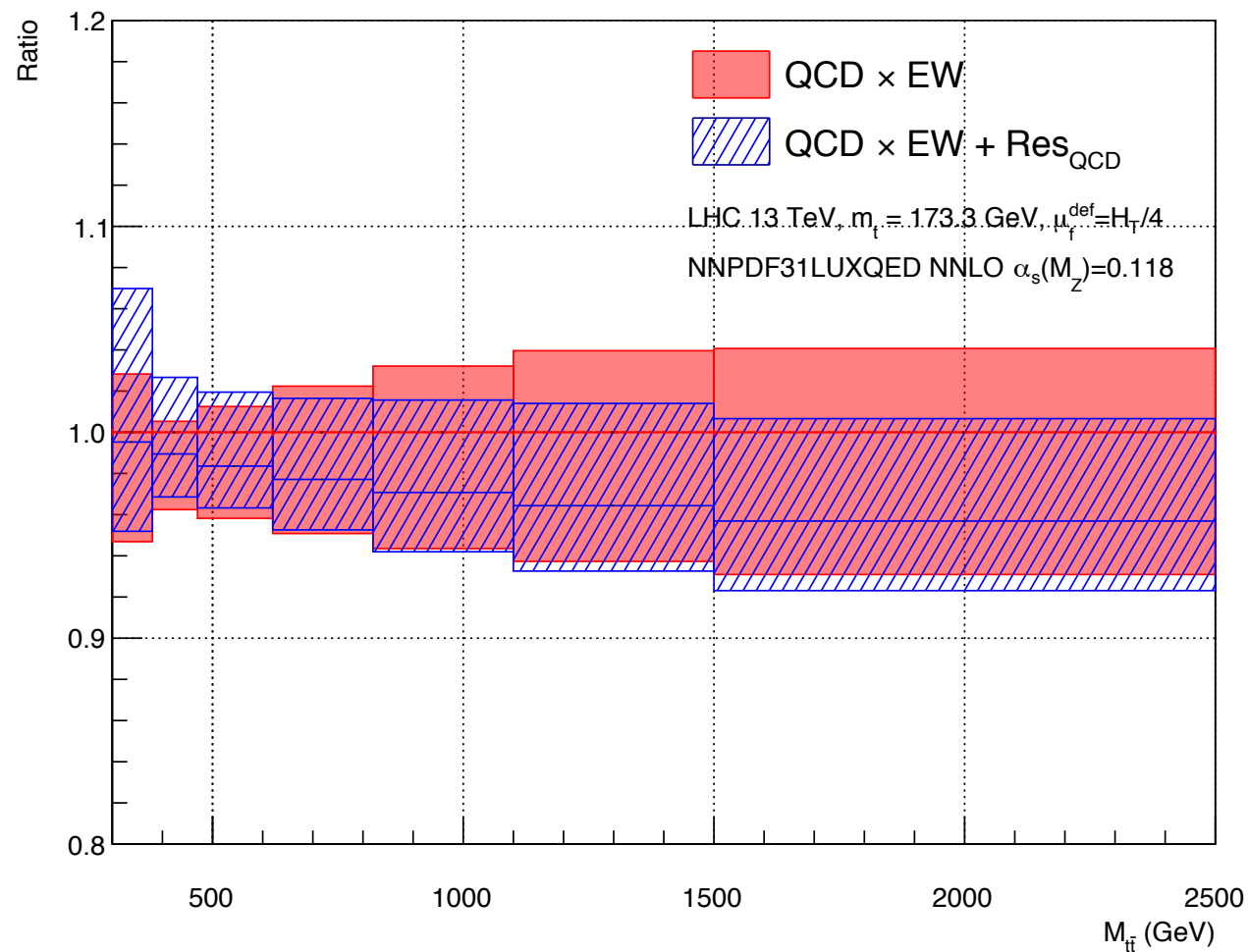
Czakon, Ferroglia, Heymes, Mitov, Pecjak,
Scott, Wang, **LLY**: 1803.07623

Pecjak, Scott, Wang, **LLY**: 1811.10527



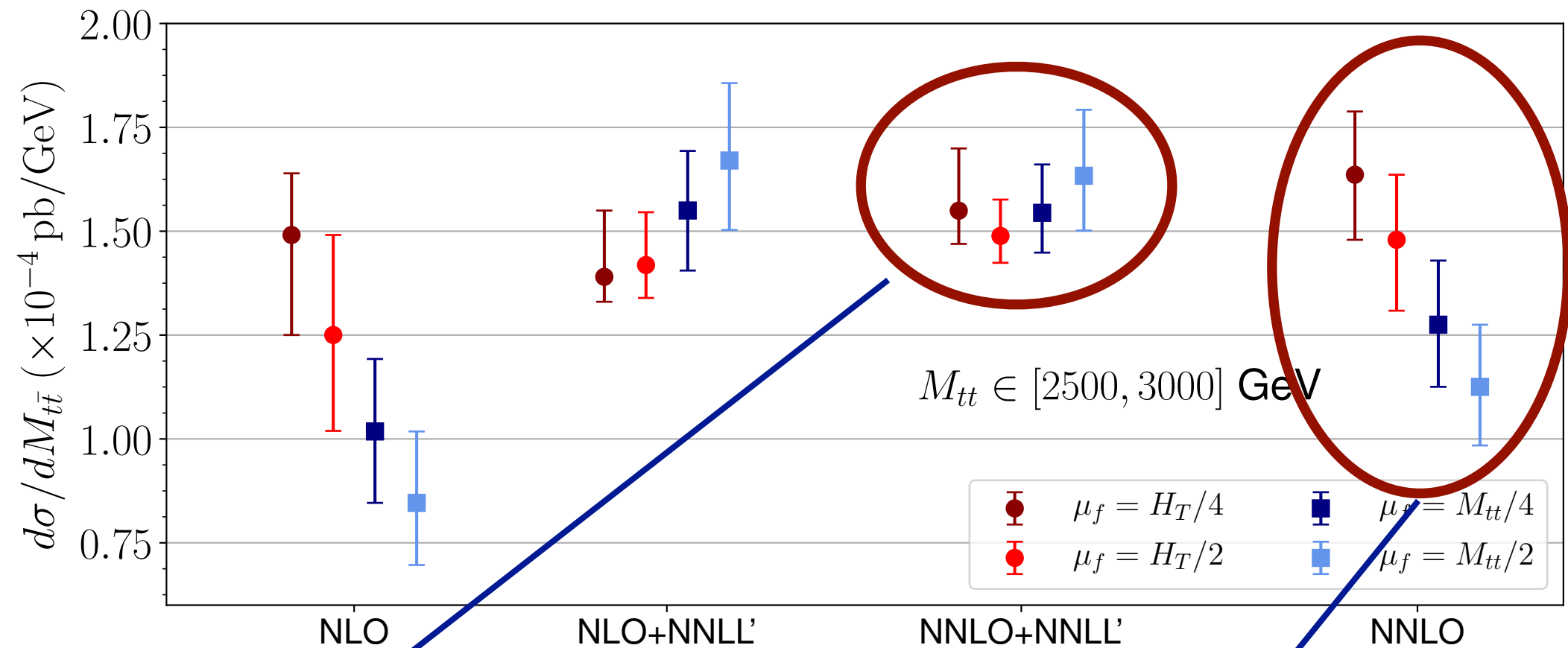
State-of-the-art predictions

Combined with NLO electroweak corrections



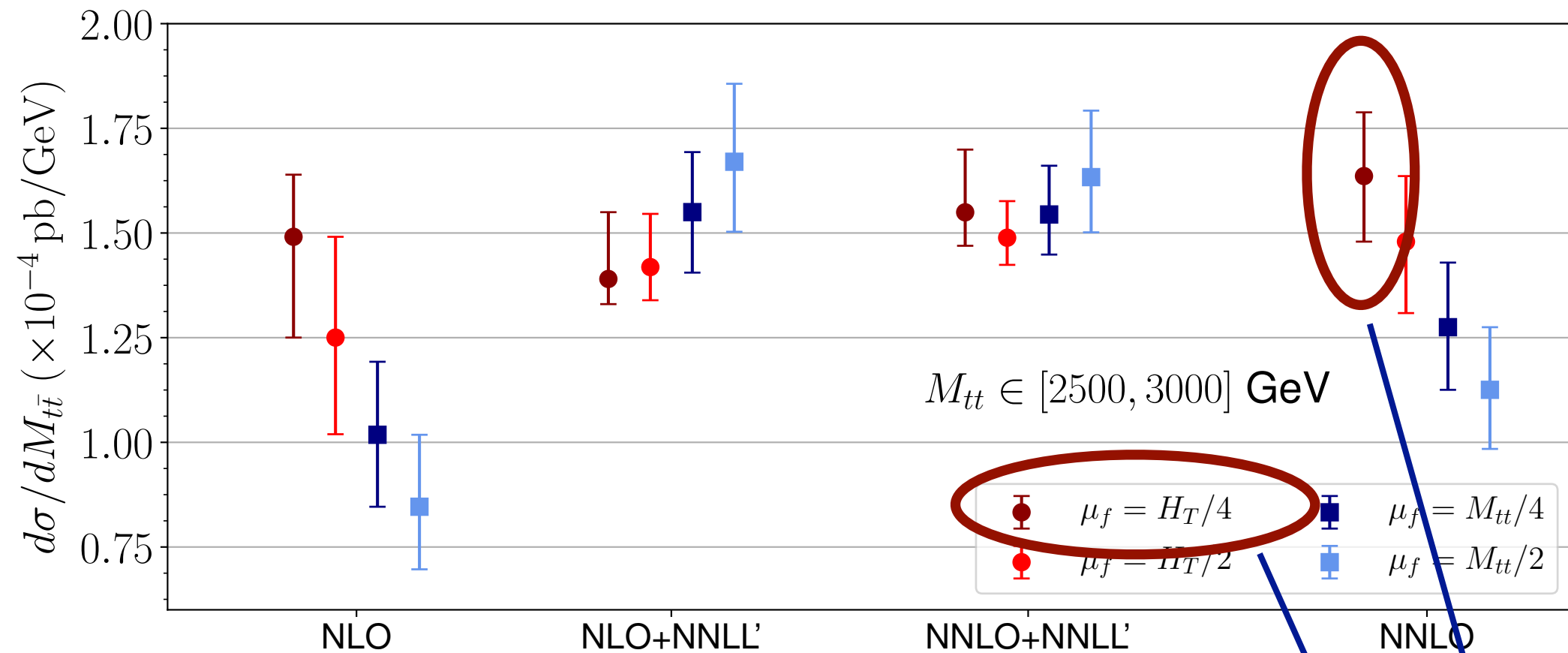
Czakon, Ferroglia, Mitov, Pagani, Papanastasiou, Pecjak,
Scott, Tsinikos, Wang, **LLY**, Zaro: 1901.08281

Czakon, Ferroglia, Heymes, Mitov, Pecjak,
Scott, Wang, **LLY: 1803.07623**



NNLL' resummation stabilizes scale ambiguity compared to NNLO

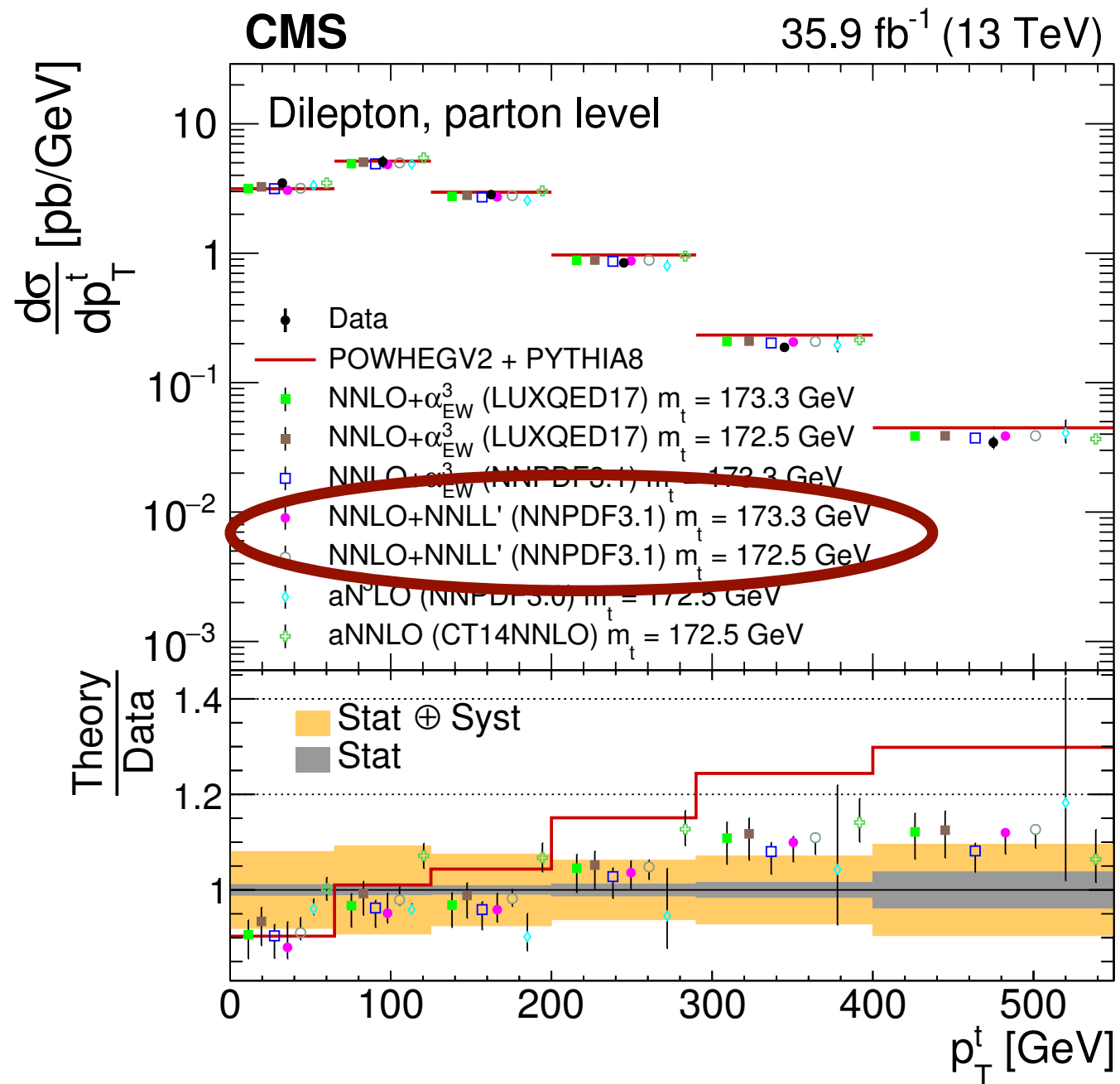
Czakon, Ferroglia, Heymes, Mitov, Pecjak,
Scott, Wang, **LLY: 1803.07623**



**And confirms optimal scale choice
for fixed order simulations**

Theory confronting data

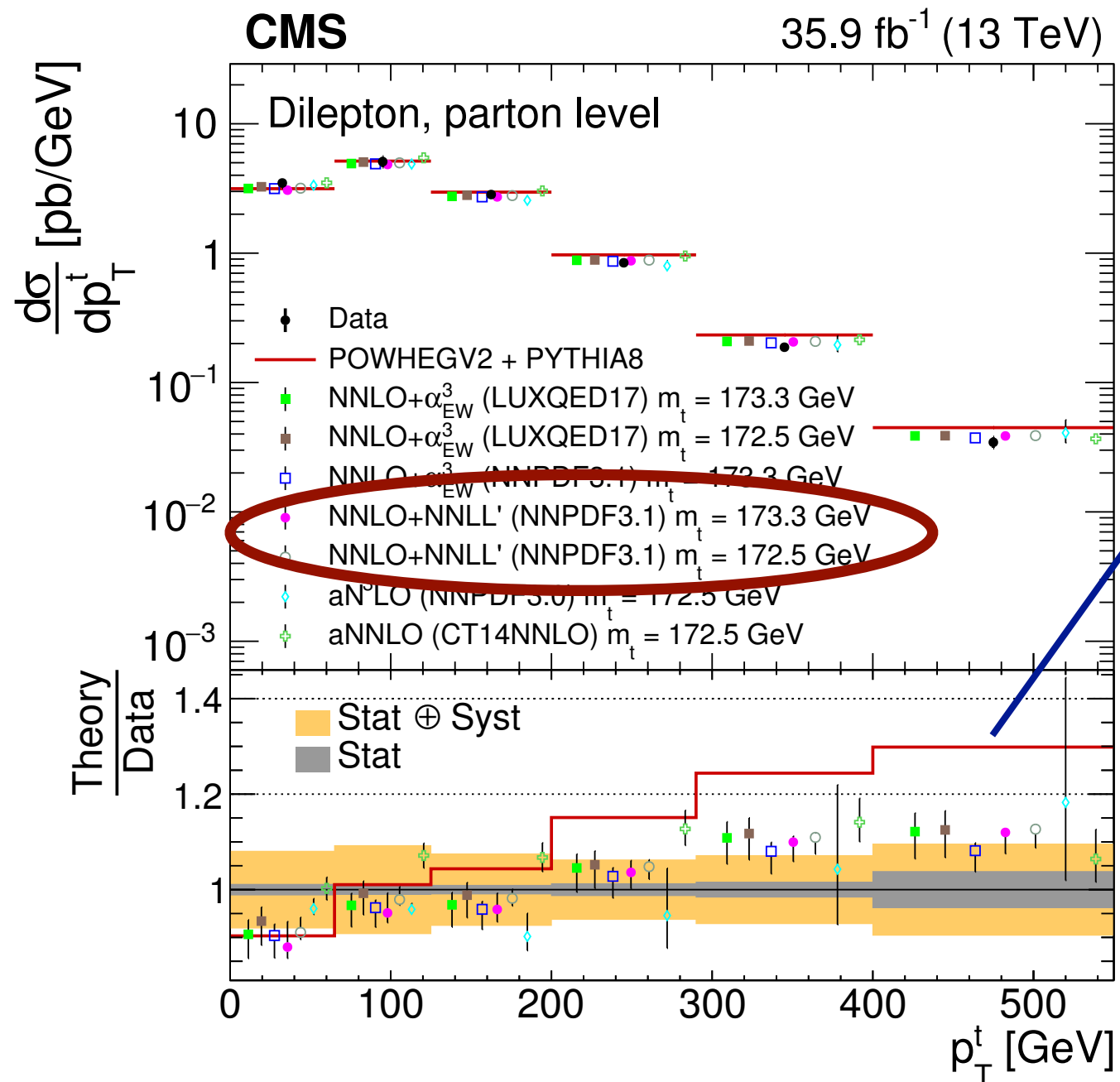
CMS collaboration: 1811.06625



Transverse momentum

Theory confronting data

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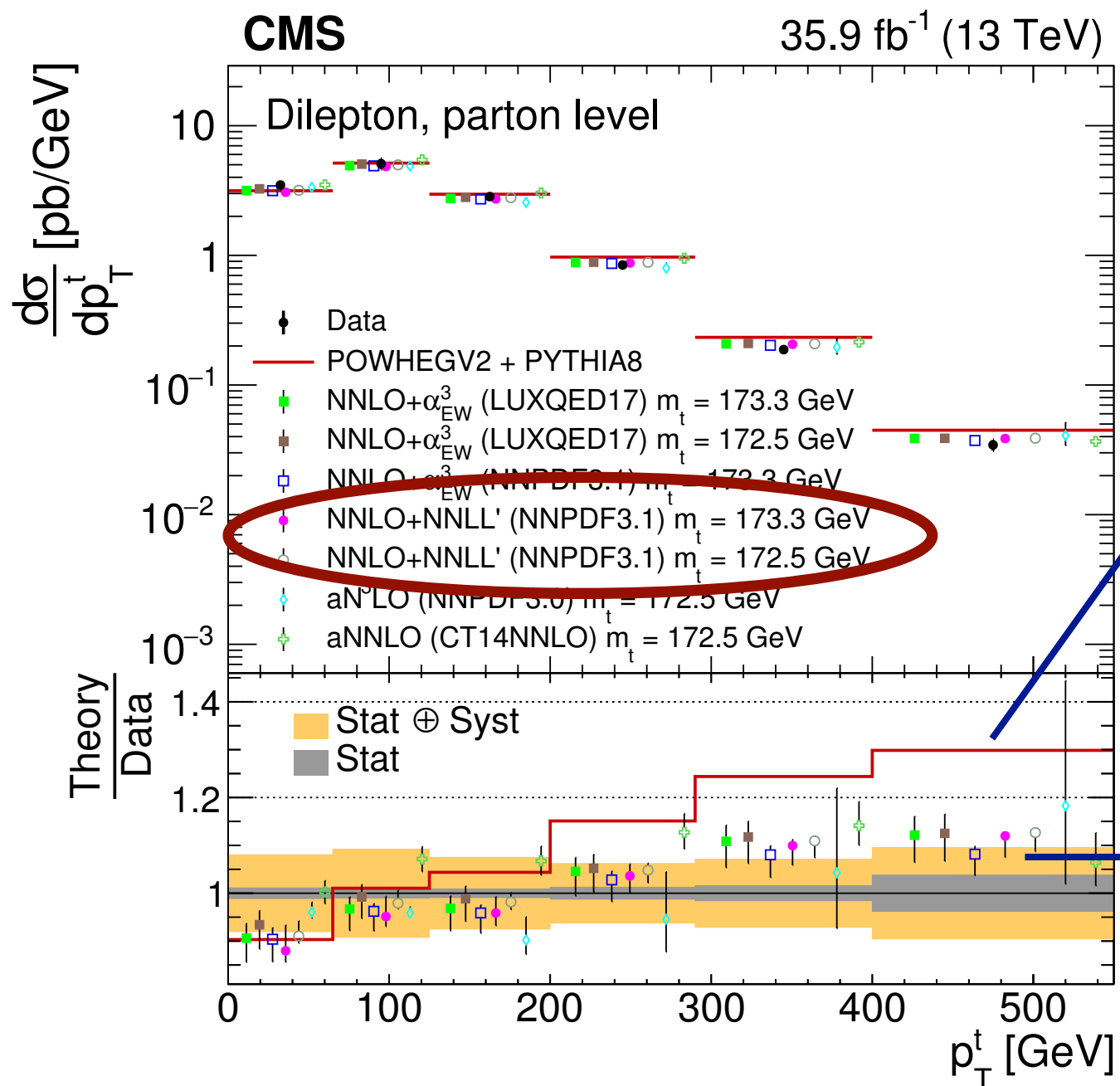


**NLO + parton shower
cannot describe the shape!**

Transverse momentum

Theory confronting data

CMS collaboration: 1811.06625



**NLO + parton shower
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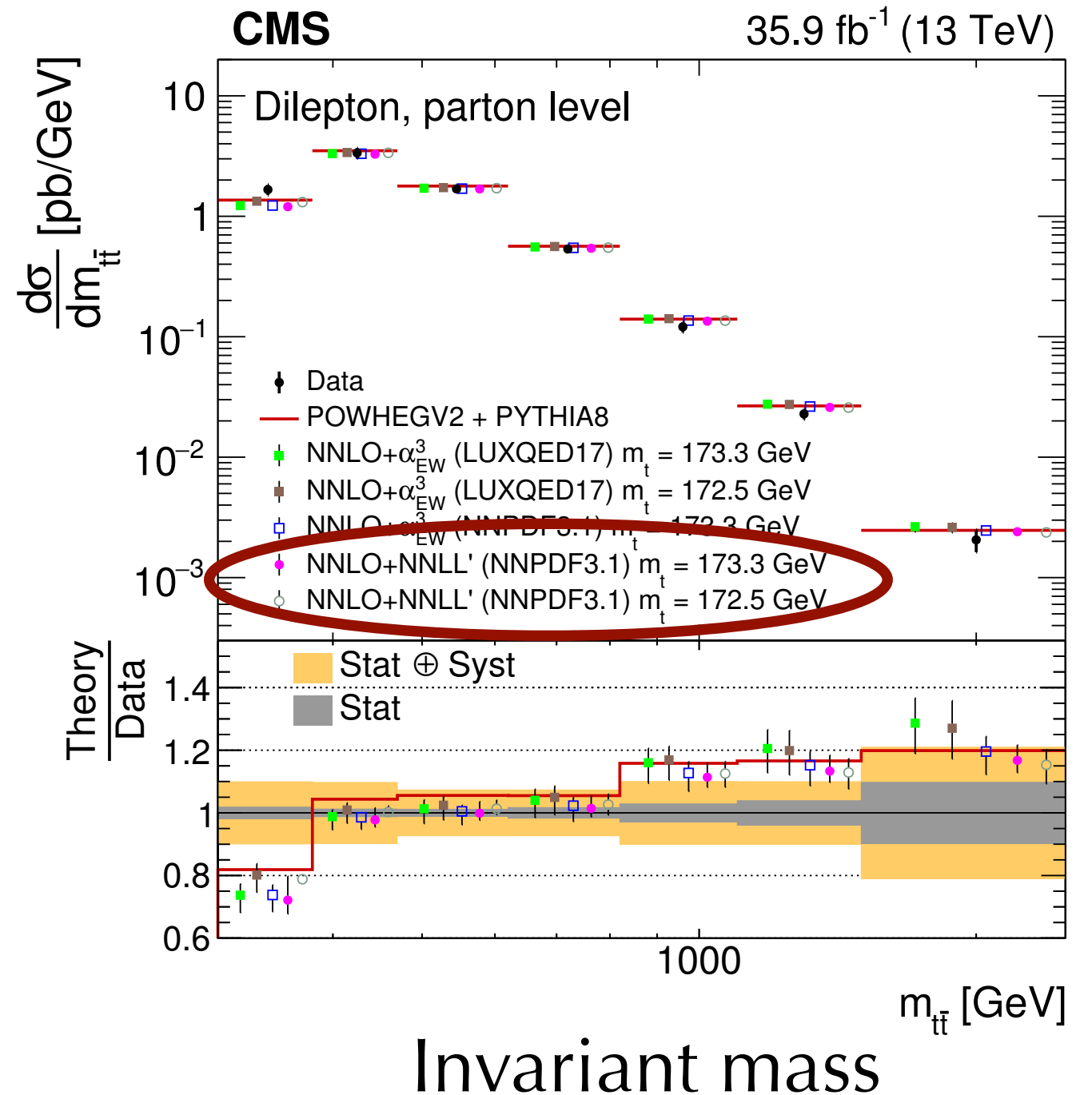
**Higher order
calculations bring
together theory
and experiment**

Transverse momentum

Theory confronting data

CMS collaboration: 1811.06625

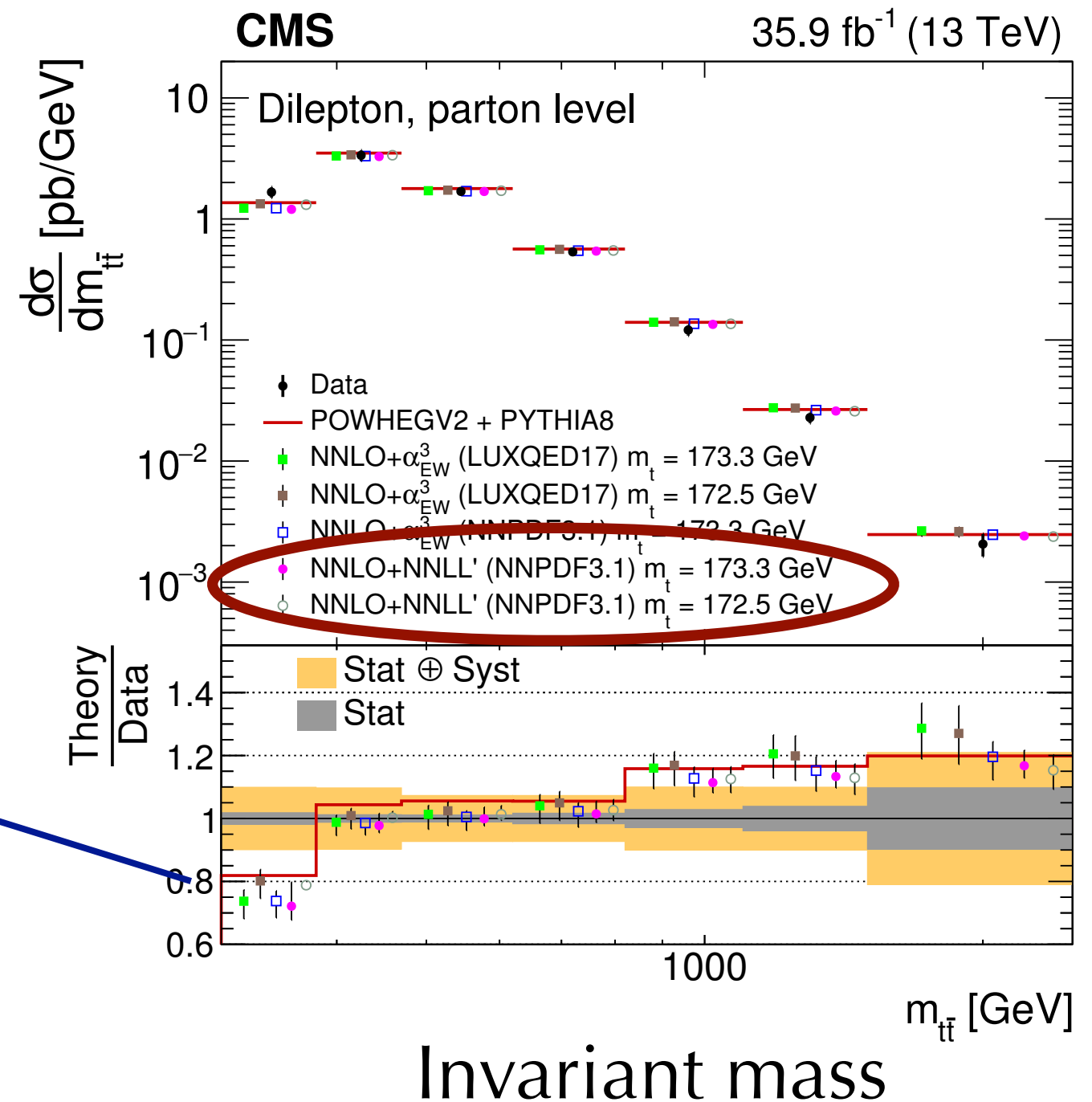
Overall good agreement



Theory confronting data

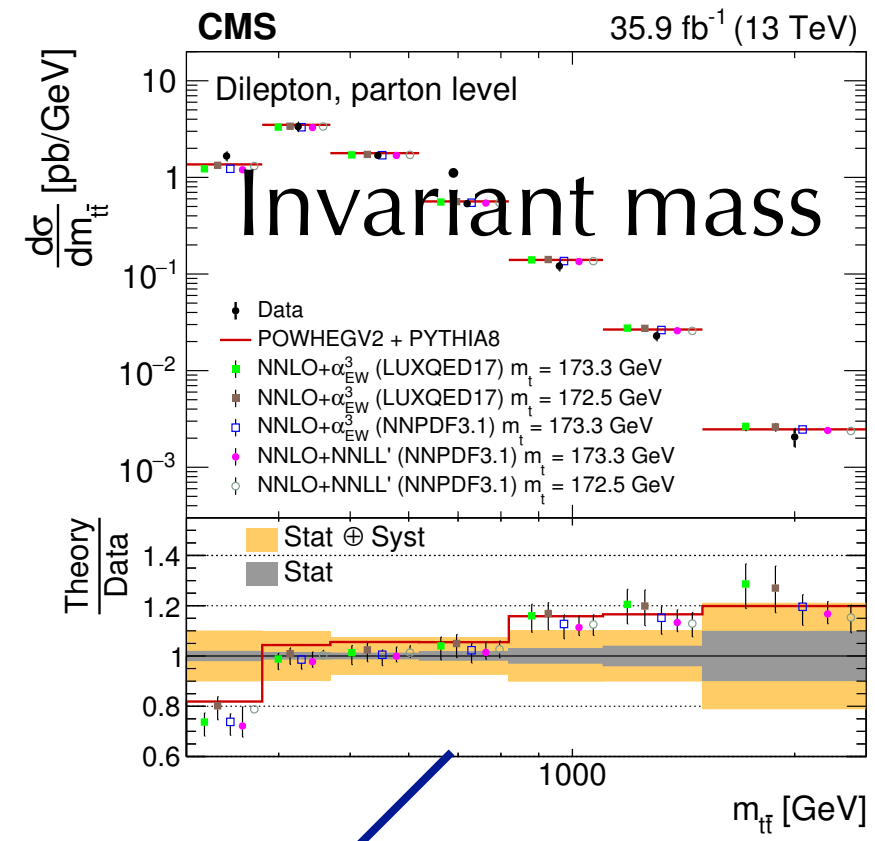
CMS collaboration: 1811.06625

Overall good agreement



Except the first bin

Inside the calculations



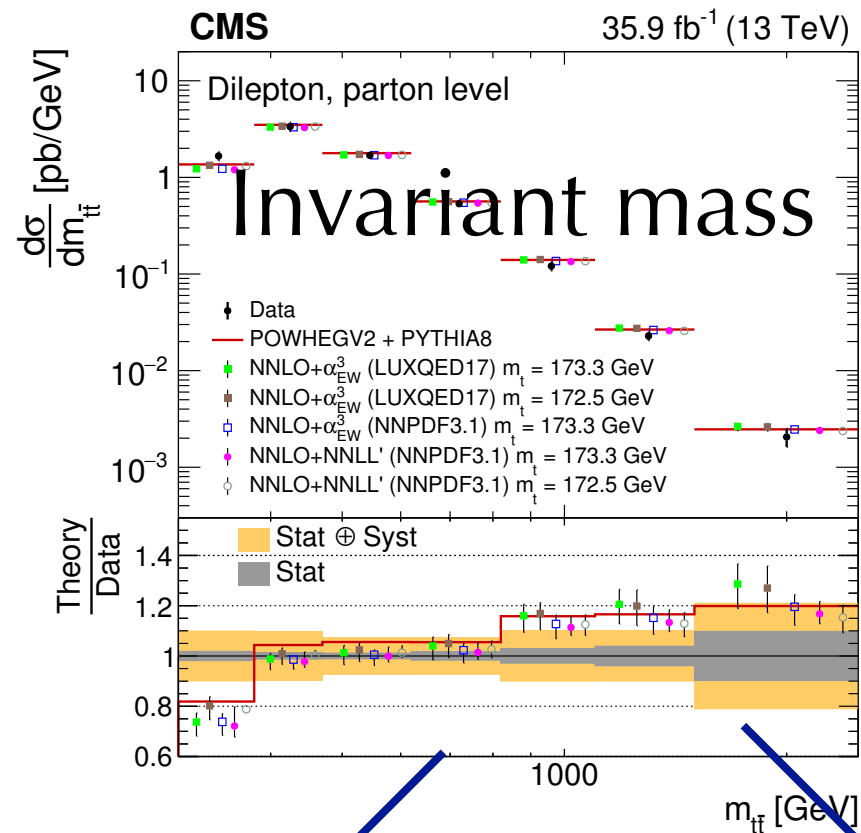
Whole region

soft emissions to all orders

Ahrens, Ferroglia, Neubert, Pecjak, **LLY**: 1003.5827

$$\ln \frac{\hat{s} - M_{t\bar{t}}^2}{M_{t\bar{t}}^2}$$

Inside the calculations



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Boosted region

soft+quasi-collinear
emissions to all orders

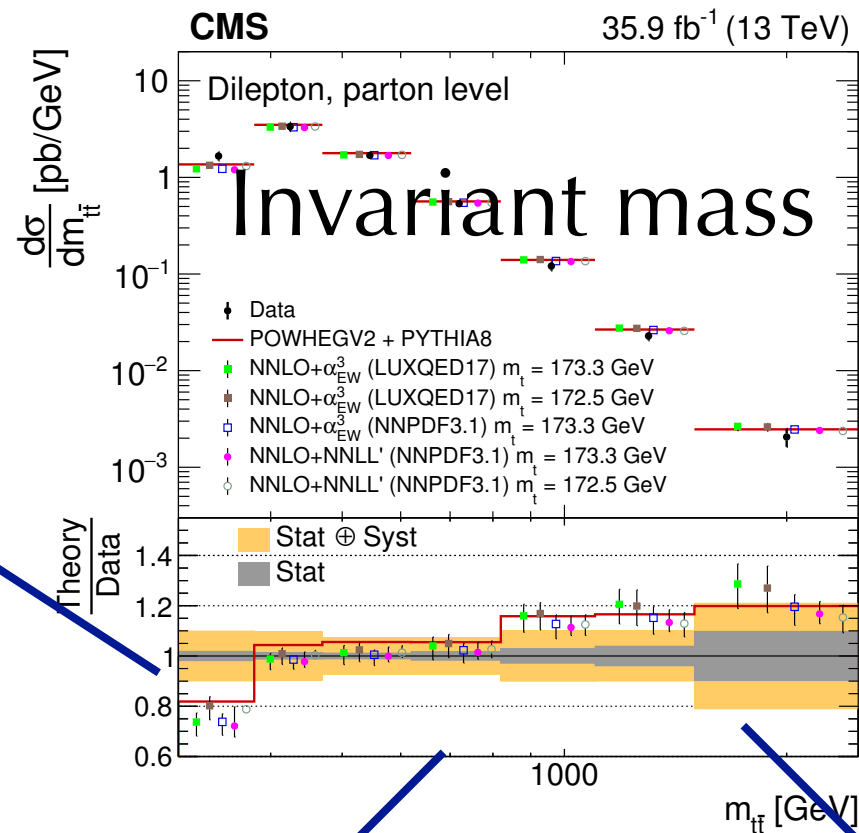
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$$\ln \frac{\hat{s} - M_{t\bar{t}}^2}{M_{t\bar{t}}^2}$$

$$\ln \frac{m_t^2}{M_{t\bar{t}}^2}$$

Inside the calculations

Threshold region
soft+Coulomb?



$$\ln \frac{\hat{s} - M_{t\bar{t}}^2}{M_{t\bar{t}}^2}$$

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Coulomb corrections for total cross section

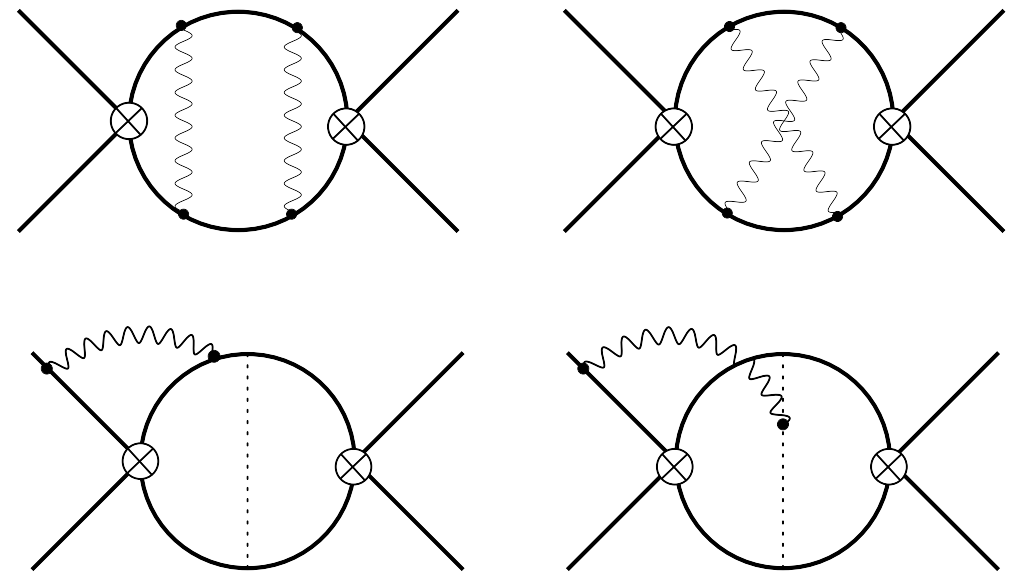
Coulomb corrections for total cross section have been considered in, e.g.:

Beneke, Czakon, Falgari, Mitov, Schwinn: 0911.5166

Beneke, Falgari, Schwinn: 1007.5414

Threshold limit: $\sqrt{\hat{s}} \rightarrow 2m_t$

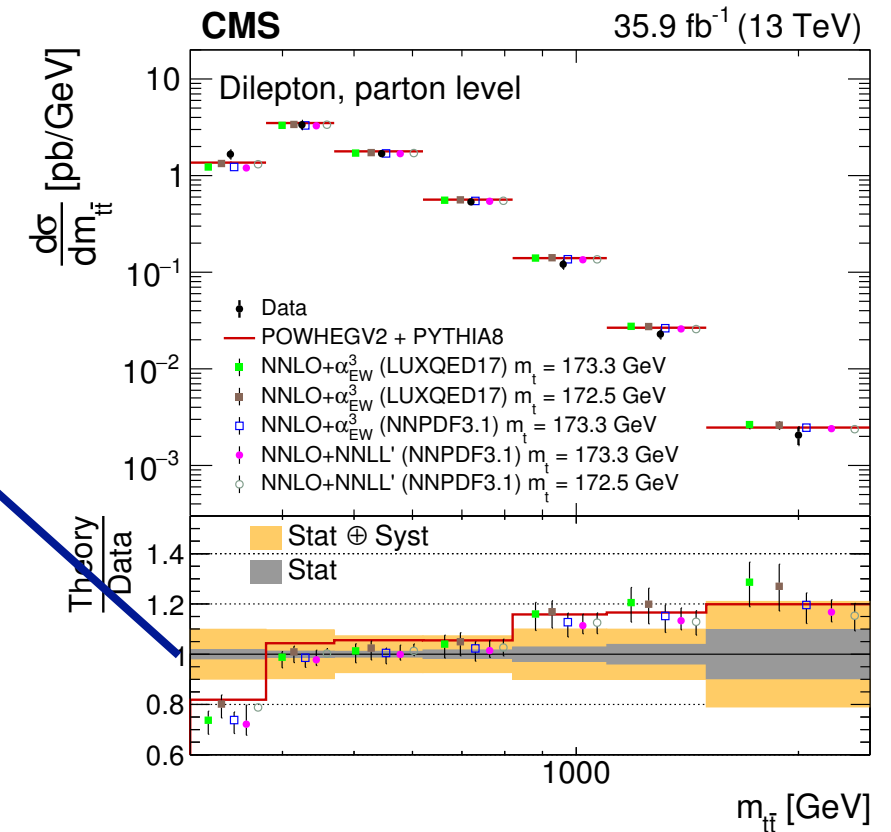
SCET+NRQCD



Remark: top quark physics is a good place to study NRQCD since mv^2 is (very often) a perturbative scale

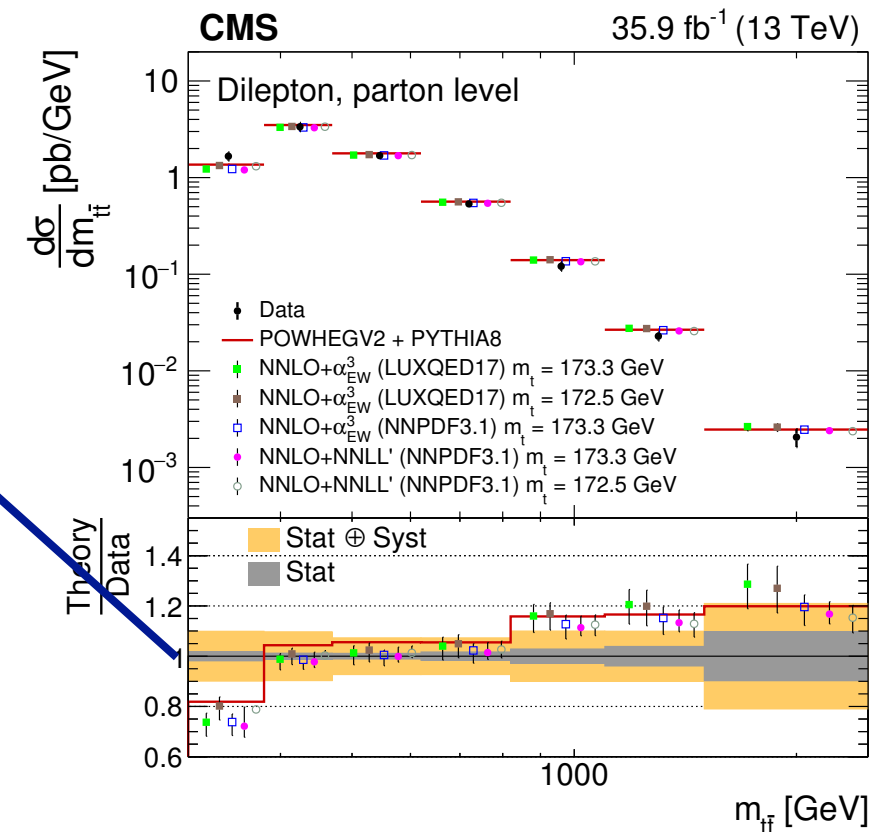
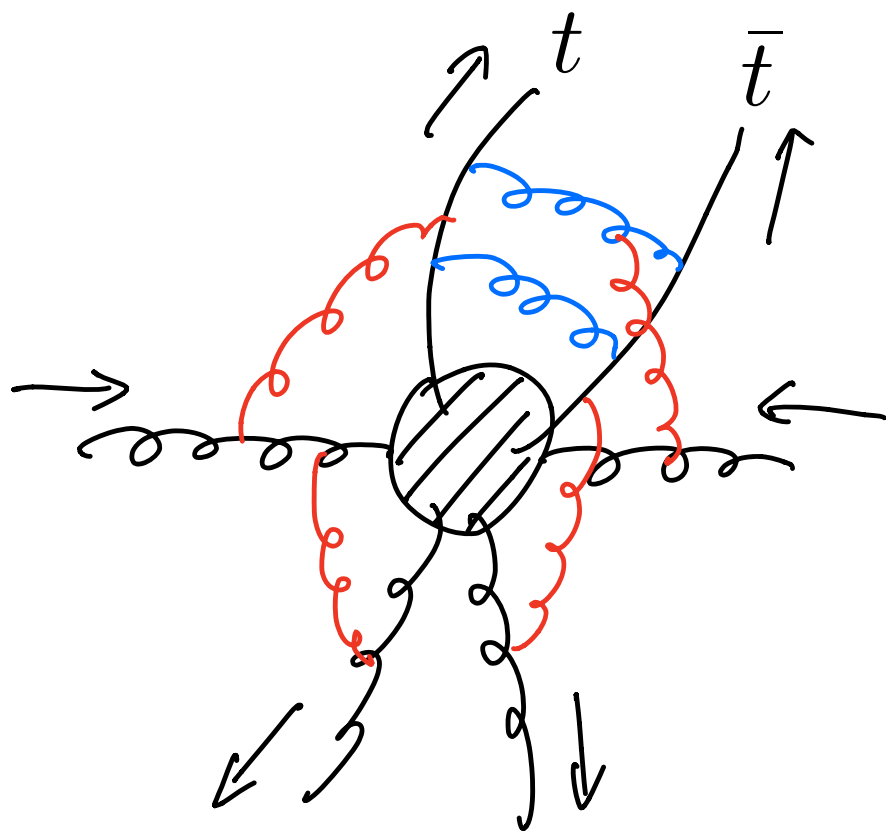
Coulomb corrections for invariant mass distribution

$\sqrt{\hat{s}} \rightarrow 2m_t$ is not the same as $M_{t\bar{t}} \rightarrow 2m_t$



Coulomb corrections for invariant mass distribution

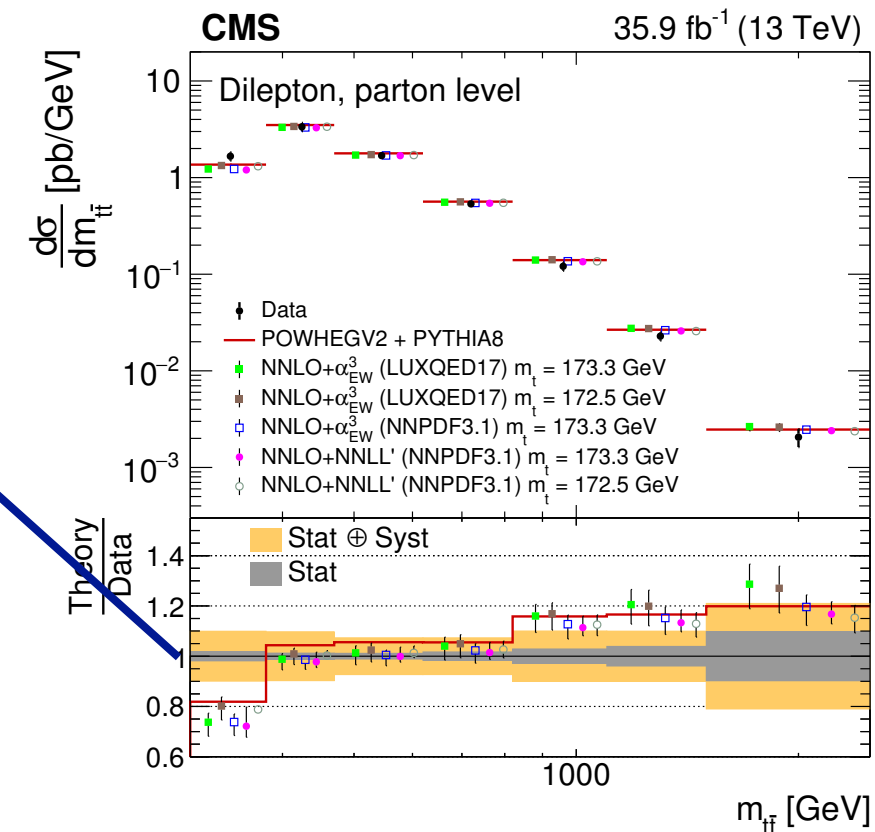
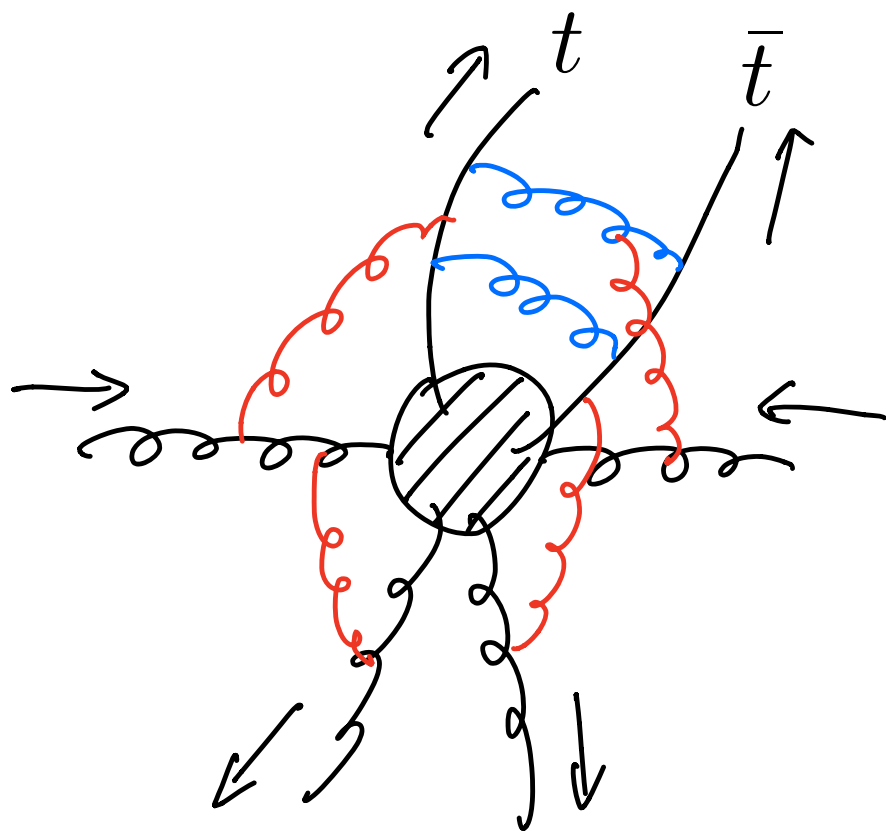
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The top quark pair can be recoiled by extra emissions

Coulomb corrections for invariant mass distribution

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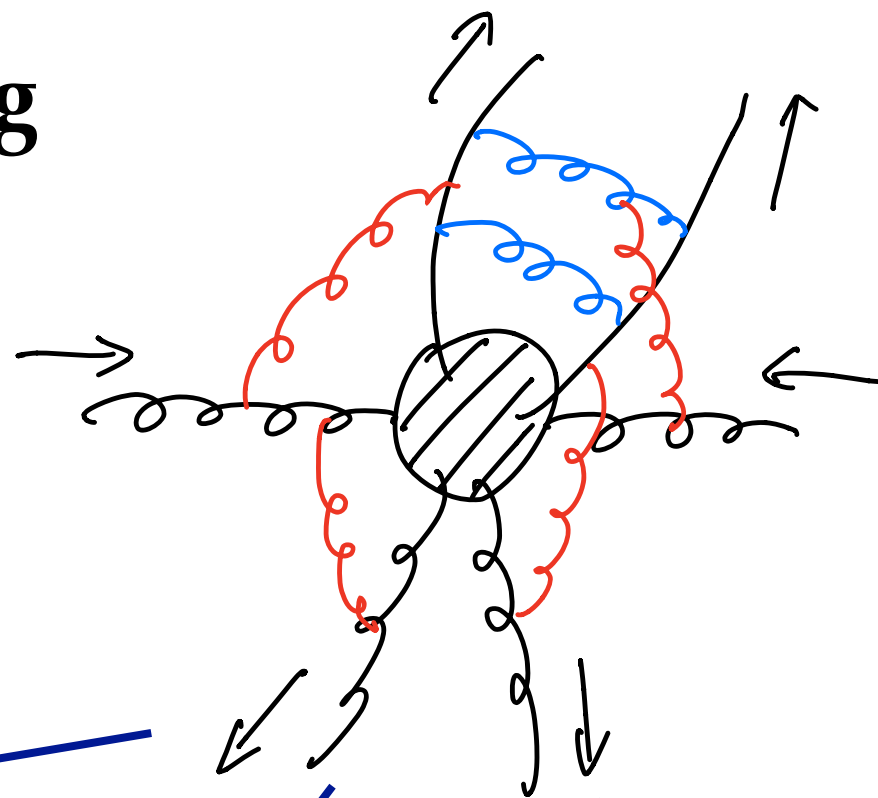
More complicated interplay among collinear, soft and Coulomb gluons

Ju, Wang, Xu, **LLY**: in progress

The top quark pair can be recoiled by extra emissions

**The resummation framework
depends on the power-counting
of extra emissions!**

$E \sim$ binding energy of
top quark pair



$E_g \sim E$
ultrasoft

$E_g \sim \sqrt{m_t E}$
soft

$E_g \sim m_t$
hard

Same as $\sqrt{\hat{s}} \rightarrow 2m_t$

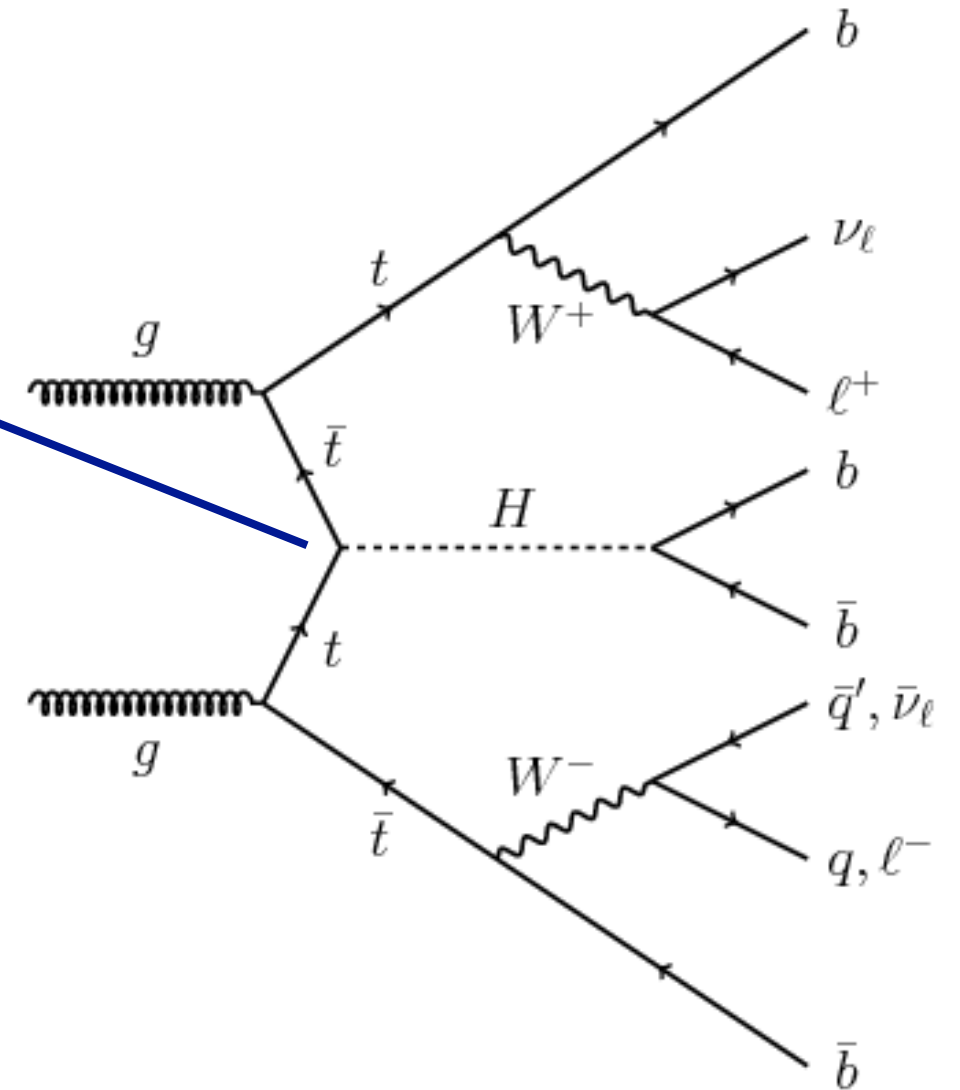
A warm-up: $t\bar{t}H$ production

Probing the Yukawa coupling of the top quark (origin of large mass)

Just observed at the LHC

CMS collaboration: 1804.02610

ATLAS collaboration: 1806.00425



Also sensitive to possible CP violation in top quark sector

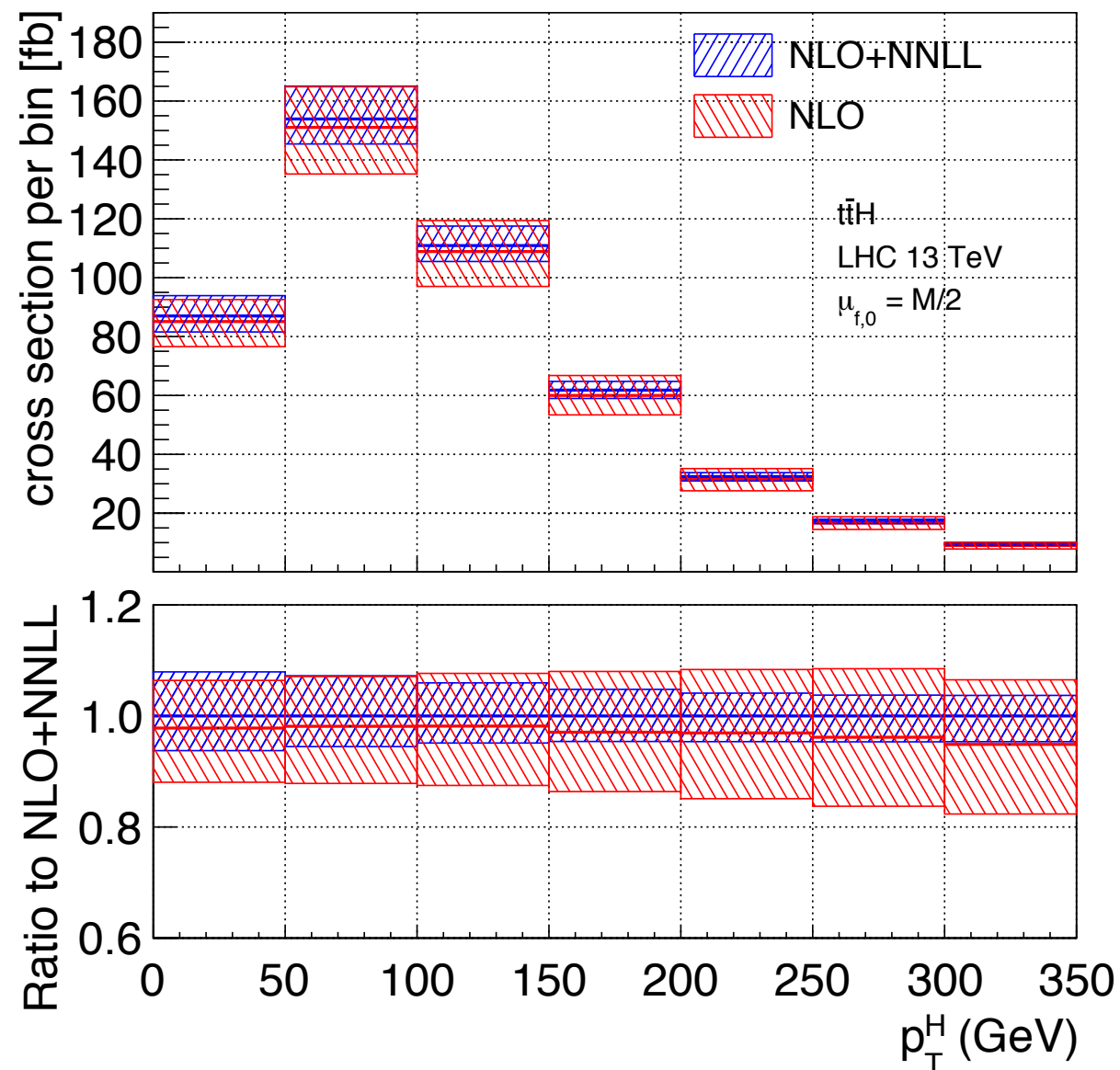
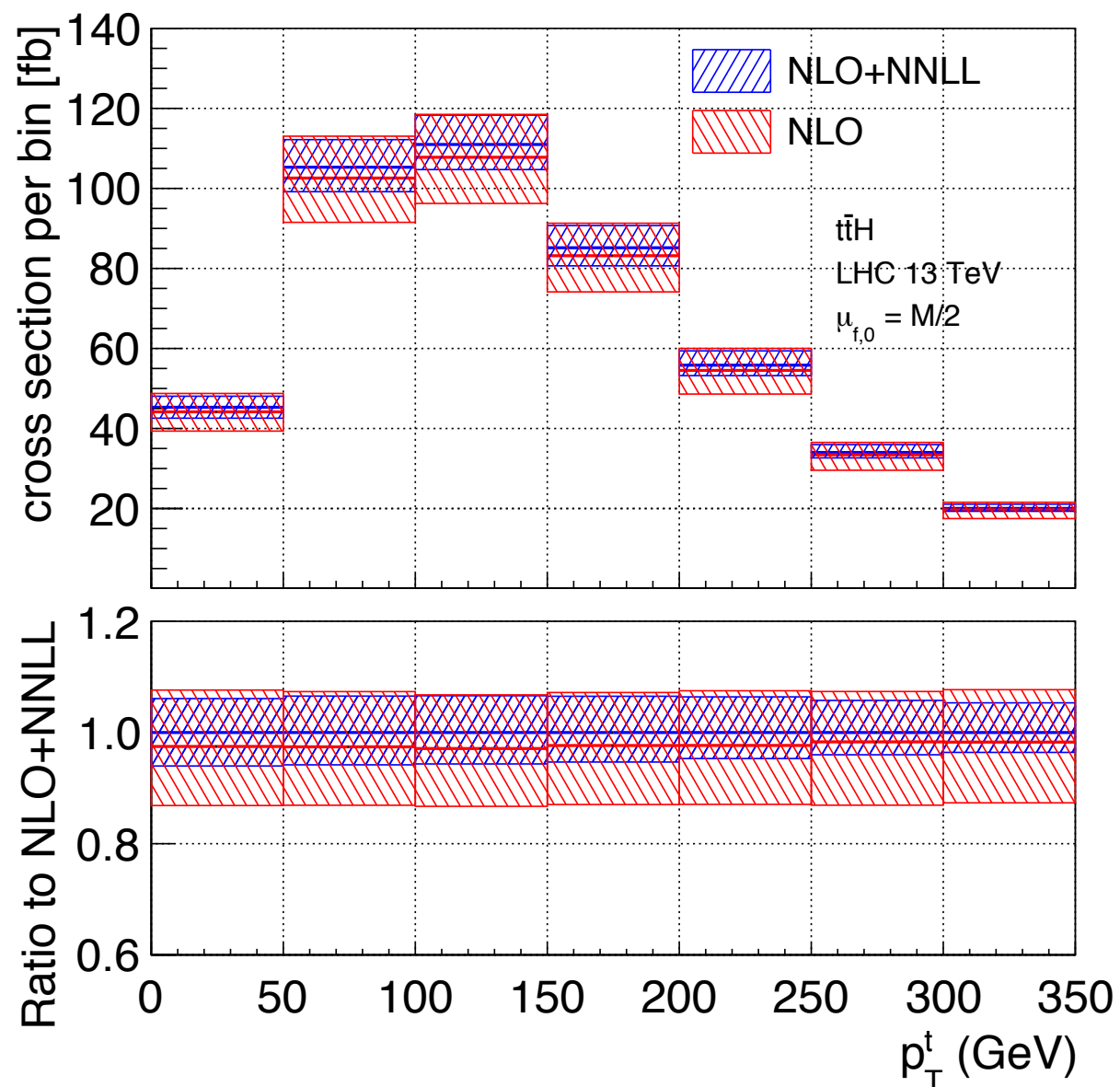
See talk by Prof. Qing-Hong Cao

Differential cross sections

Broggio, Ferroglia, Pecjak, [LLY: 1611.00049](#)

Kulesza, Motyka, Stebel, Theeuwes: [1704.03363](#)

Soft gluon resummation for $\sqrt{\hat{s}} \rightarrow M_{t\bar{t}H}$



State-of-the-art QCD calculation

Total cross section at threshold

Ju, LLY: 1904.08744

See also Kulesza et al.: 1509.02780

Threshold limit for total cross section

$$\sqrt{\hat{s}} \rightarrow 2m_t + m_H \quad \beta = \sqrt{1 - \frac{(2m_t + m_H)^2}{s}} \rightarrow 0$$

Typical 3-velocity of
final-state particles

Total cross section at threshold

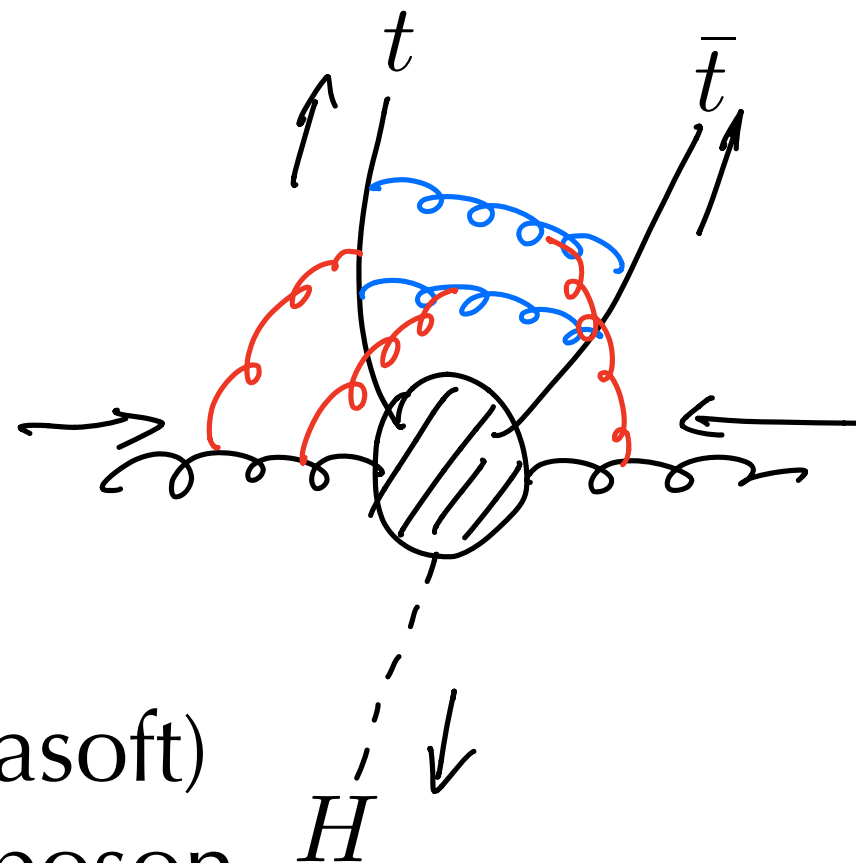
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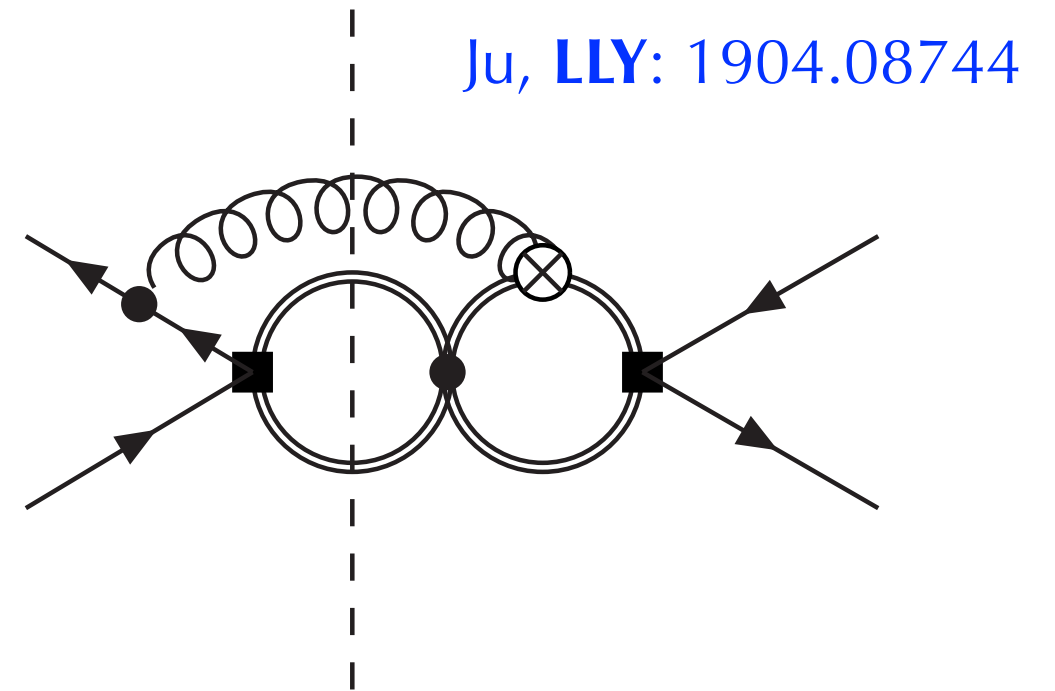
Typical 3-velocity of
final-state particles



Recoiled by soft (NOT ultrasoft)
3-momentum of the Higgs boson

Factorization near threshold

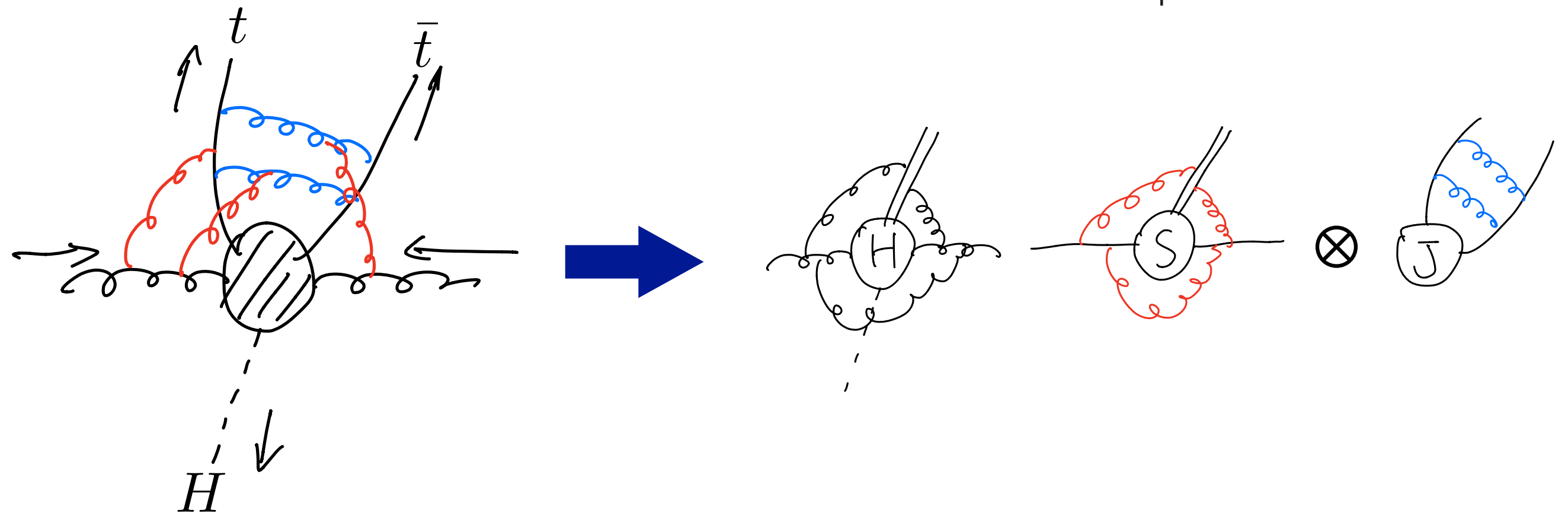
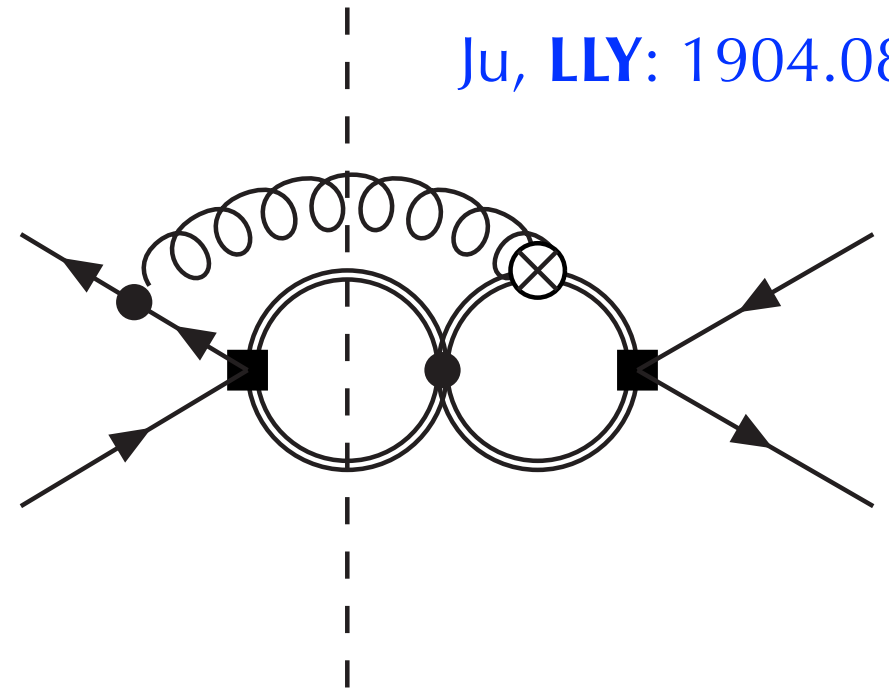
Non-trivial cancellation
of ultrasoft interactions at
next-to-leading power



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Resummation of soft and Coulomb corrections

Ju, LLY: 1904.08744

	13 TeV LHC (pb)
NLO	$0.493^{+5.8\%}_{-9.2\%}$
NLL'+NLO	$0.521^{+1.9\%}_{-2.6\%}$
<i>K</i> -factor	1.06

6% effect

Big reduction of scale dependence

Resummation of soft and Coulomb corrections

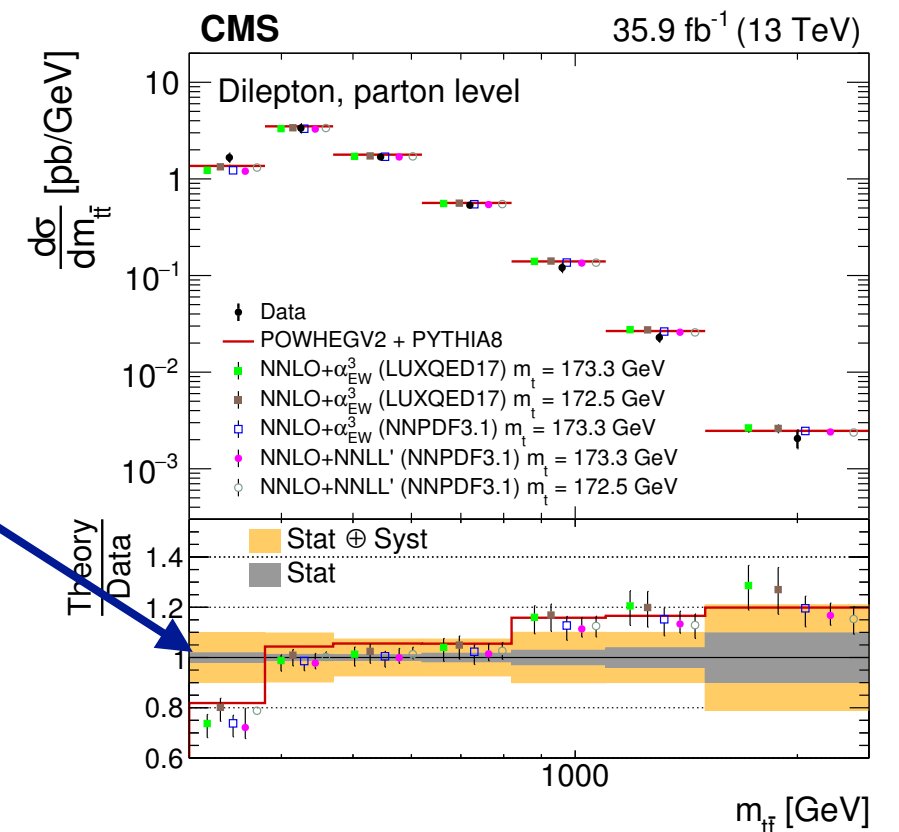
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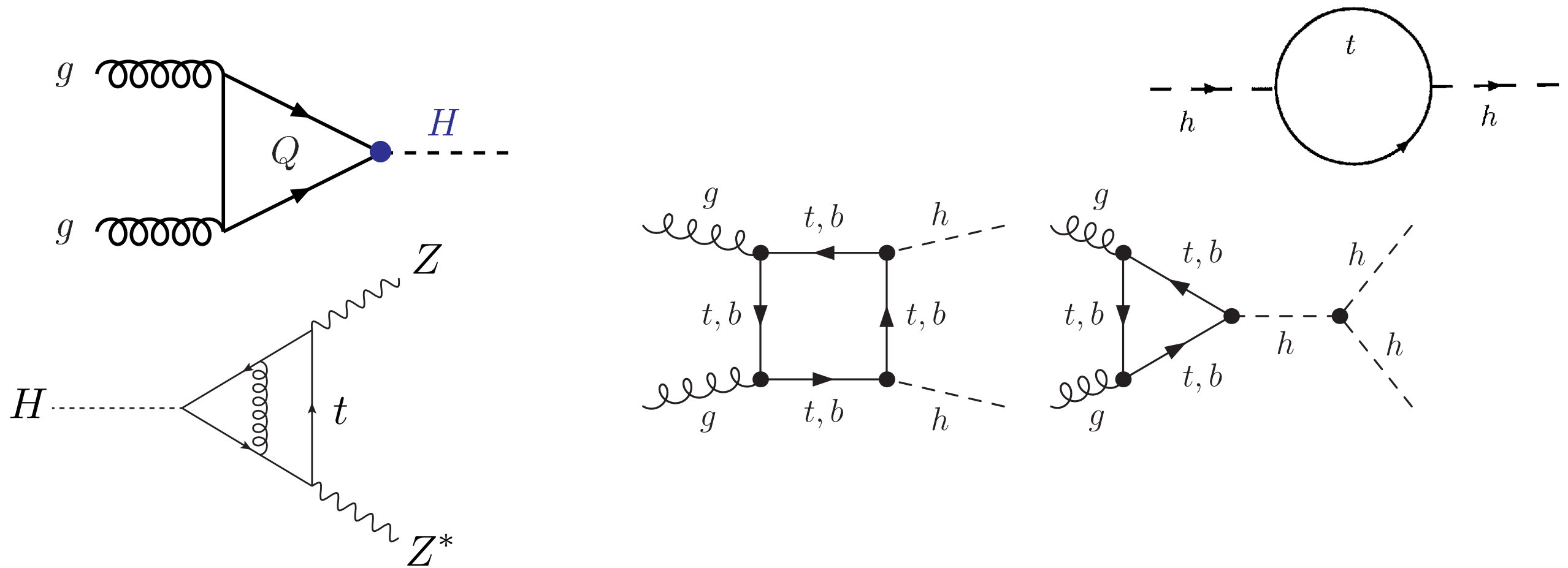
Big reduction of scale dependence

May be generalized to



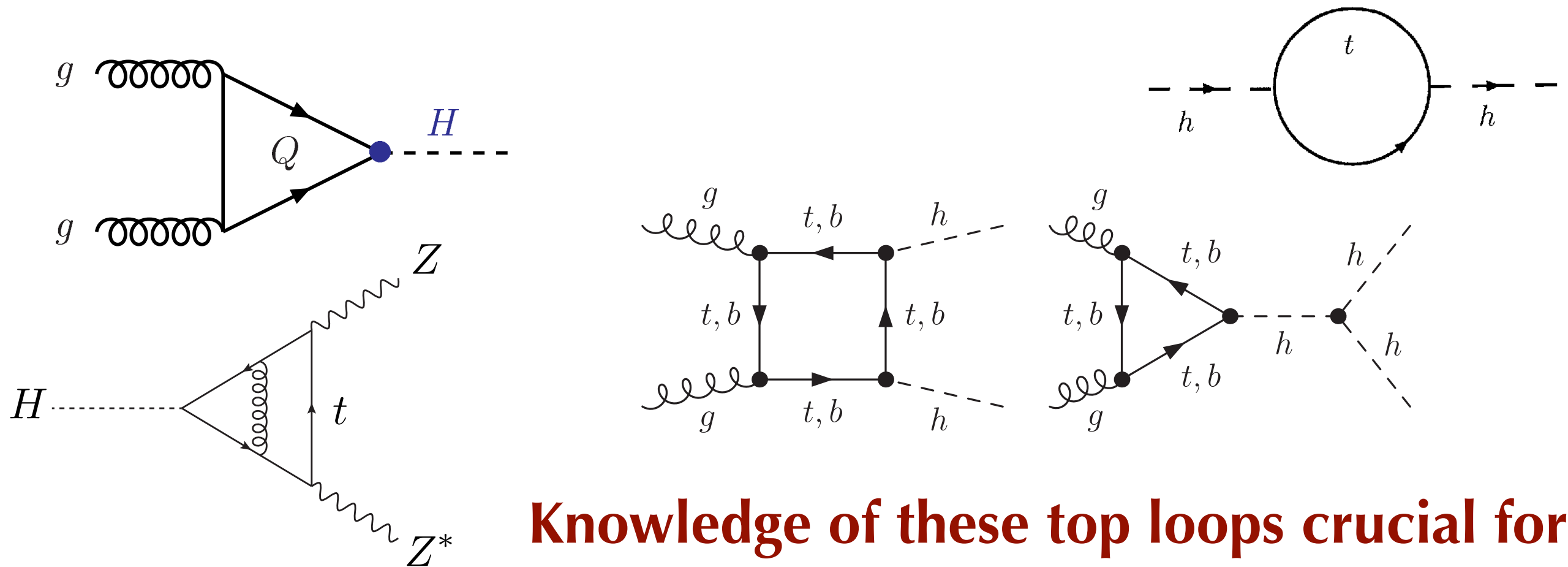
Top quarks in loops (for Higgs)

Virtual top quarks are everywhere in Higgs physics
(due to the large Yukawa coupling)



Top quarks in loops (for Higgs)

Virtual top quarks are everywhere in Higgs physics
(due to the large Yukawa coupling)



Knowledge of these top loops crucial for extracting interesting information

e.g., anomalous Hgg , HZZ , HHH couplings

ZH production at CEPC

Gong, Li, Xu, **LLY**, Zhao: 1609.03955

Sun, Feng, Jia, Sang: 1609.03995

See also talk by Prof. Yu Jia

NNLO mixed QCD-EW corrections



Two-loop integrals with 4 scales

**Purely numeric evaluation (sector decomposition)
highly resource-demanding!**

Large top mass expansion

Gong, Li, Xu, **LLY**, Zhao: 1609.03955

Taylor series in $\frac{s, m_H^2, m_Z^2}{m_t^2}$

$$\begin{aligned} \sigma^{\alpha\alpha_s}(\sqrt{s}, m_H, m_Z, m_t) &= m_t^2 c_2(\sqrt{s}, m_H, m_Z) \\ &+ m_t^0 c_0(\sqrt{s}, m_H, m_Z) \\ &+ m_t^{-2} c_{-2}(\sqrt{s}, m_H, m_Z) \\ &+ \dots \end{aligned}$$

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Simple analytic expressions!

Blazingly fast numeric evaluation

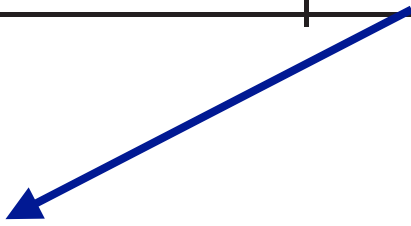
Easy to be implemented in an event generator

Convergence of the expansion

Gong, Li, Xu, LLY, Zhao: 1609.03955

Good convergence for optimal energies of Higgs factories!

\sqrt{s} (GeV)	$\mathcal{O}(m_t^2)$	$\mathcal{O}(m_t^0)$	$\mathcal{O}(m_t^{-2})$	$\mathcal{O}(m_t^{-4})$
240	81.8%	16.2%	1.4%	0.4%
250	81.7%	16.1%	1.5%	0.5%

$$\frac{m_t^2 c_2}{\sigma^{\alpha\alpha_s}}$$


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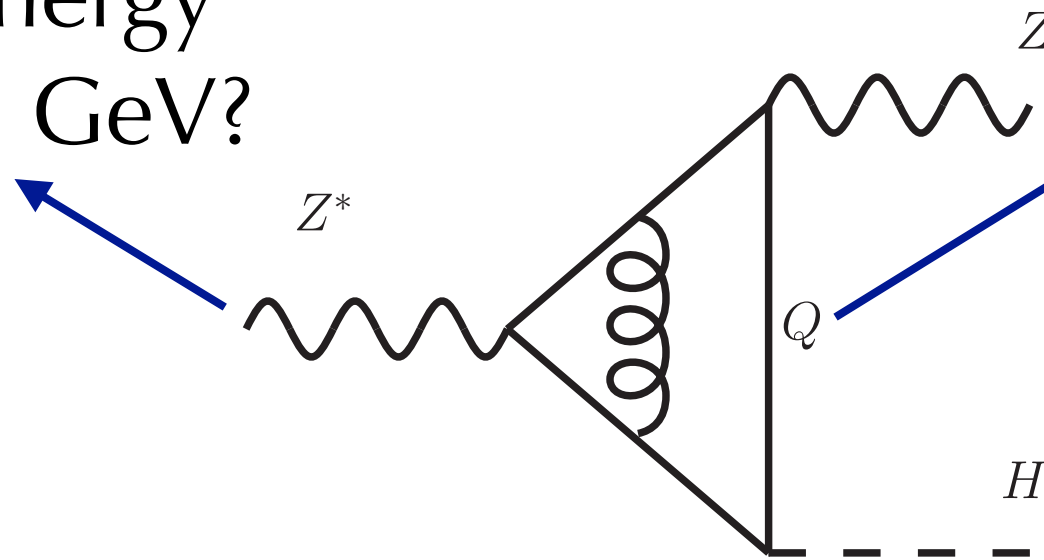
\sqrt{s} (GeV)	σ_{LO} (fb)	σ_{NLO} (fb)	σ_{NNLO} (fb)	$\sigma_{\text{NNLO}}^{\text{exp.}}$ (fb)
240	252.0	228.6	231.5	231.5
250	252.0	227.9	230.8	230.8

No difference between exact and expanded results (4 digits)

Exact analytic solution

Wang, Xu, **LLY**: 1904.xxxxx

What if energy
above 346 GeV?

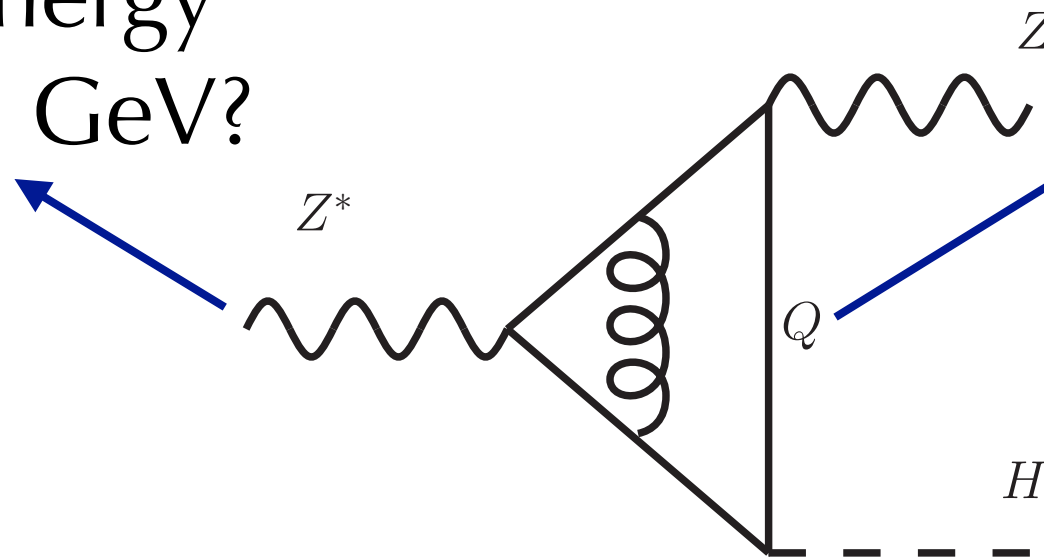


What if bottom quarks
are included?

Exact analytic solution

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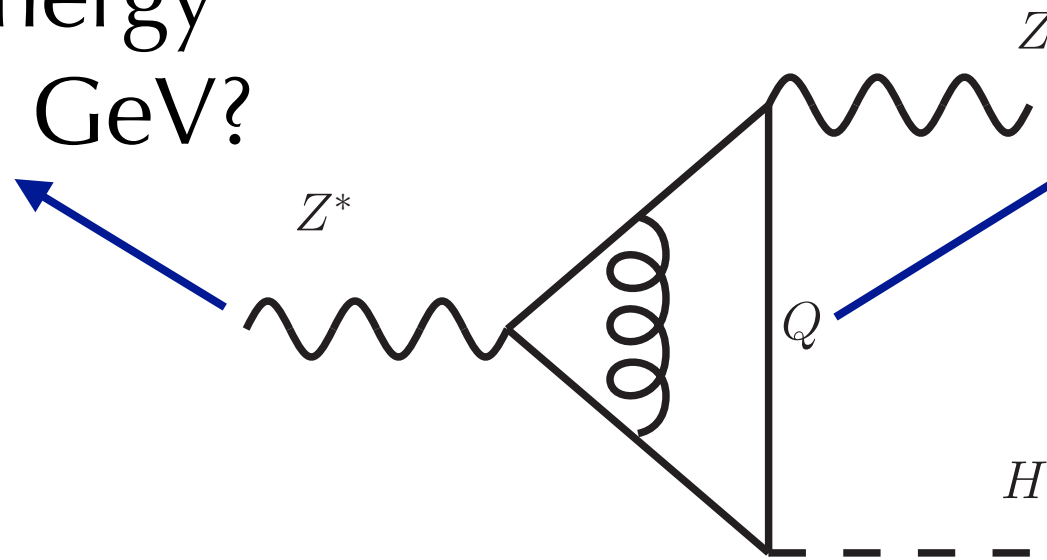
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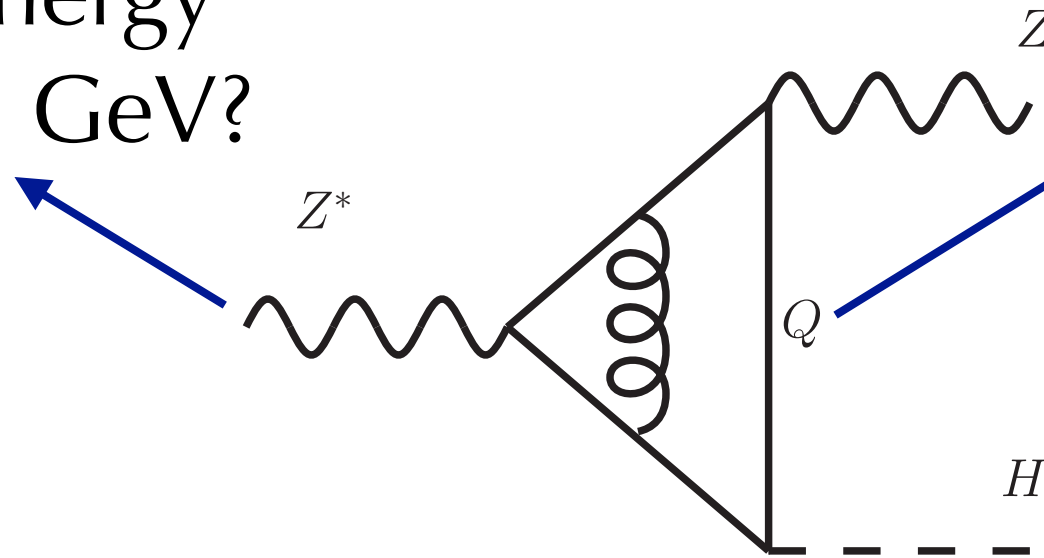
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Sector decomposition very slow!

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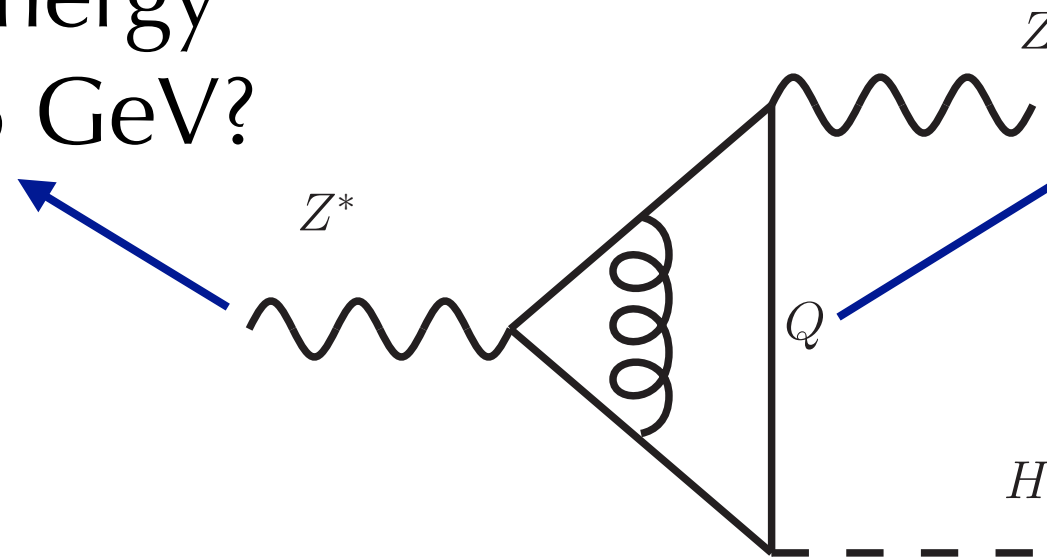
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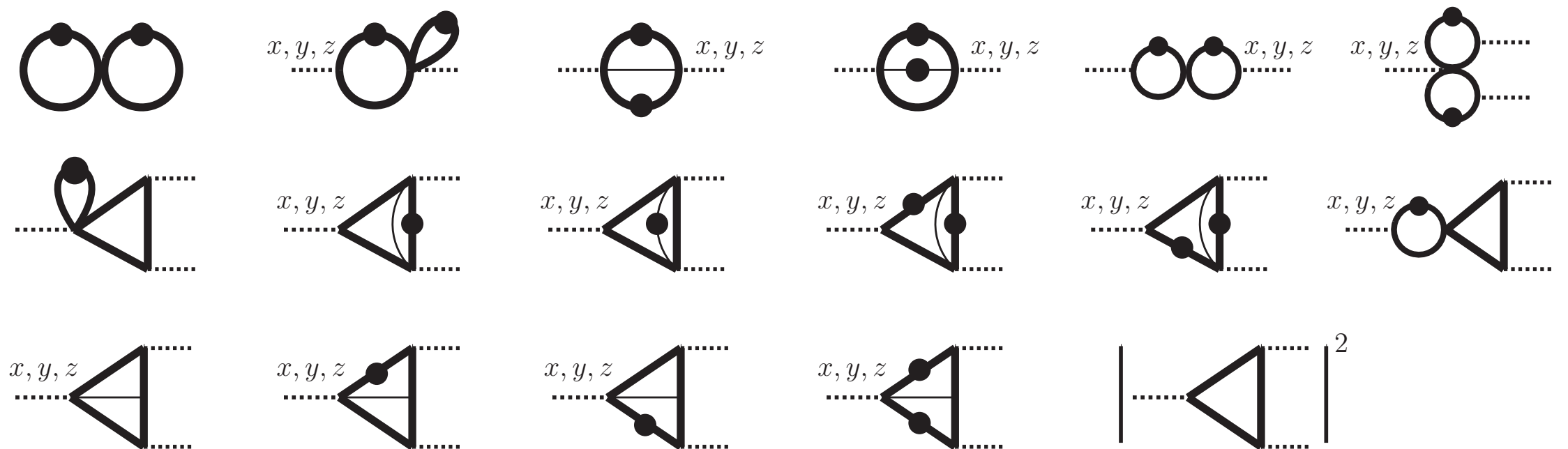
Exact analytic solution needed...

Also theoretically interesting: few massive two-loop multiple-scale integrals are known analytically

Exact analytic solution

Wang, Xu, LLY: 1904.xxxxx

Solve 41 master integrals using differential equations and symbol techniques

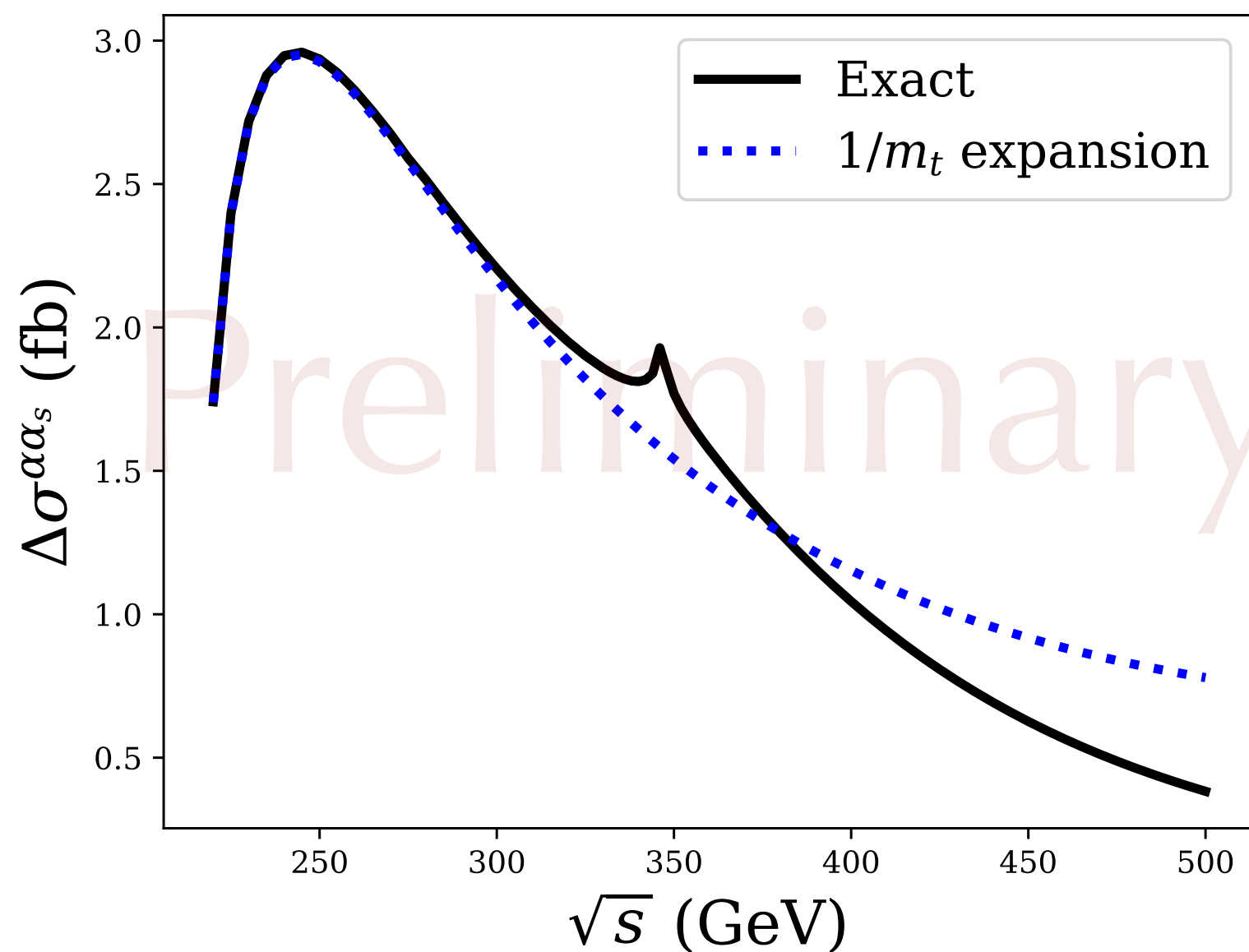


Functions of 3 dimensionless variables

$$x = -\frac{q^2}{4m_Q^2}, \quad y = -\frac{p_Z^2}{4m_Q^2}, \quad z = -\frac{p_H^2}{4m_Q^2}$$

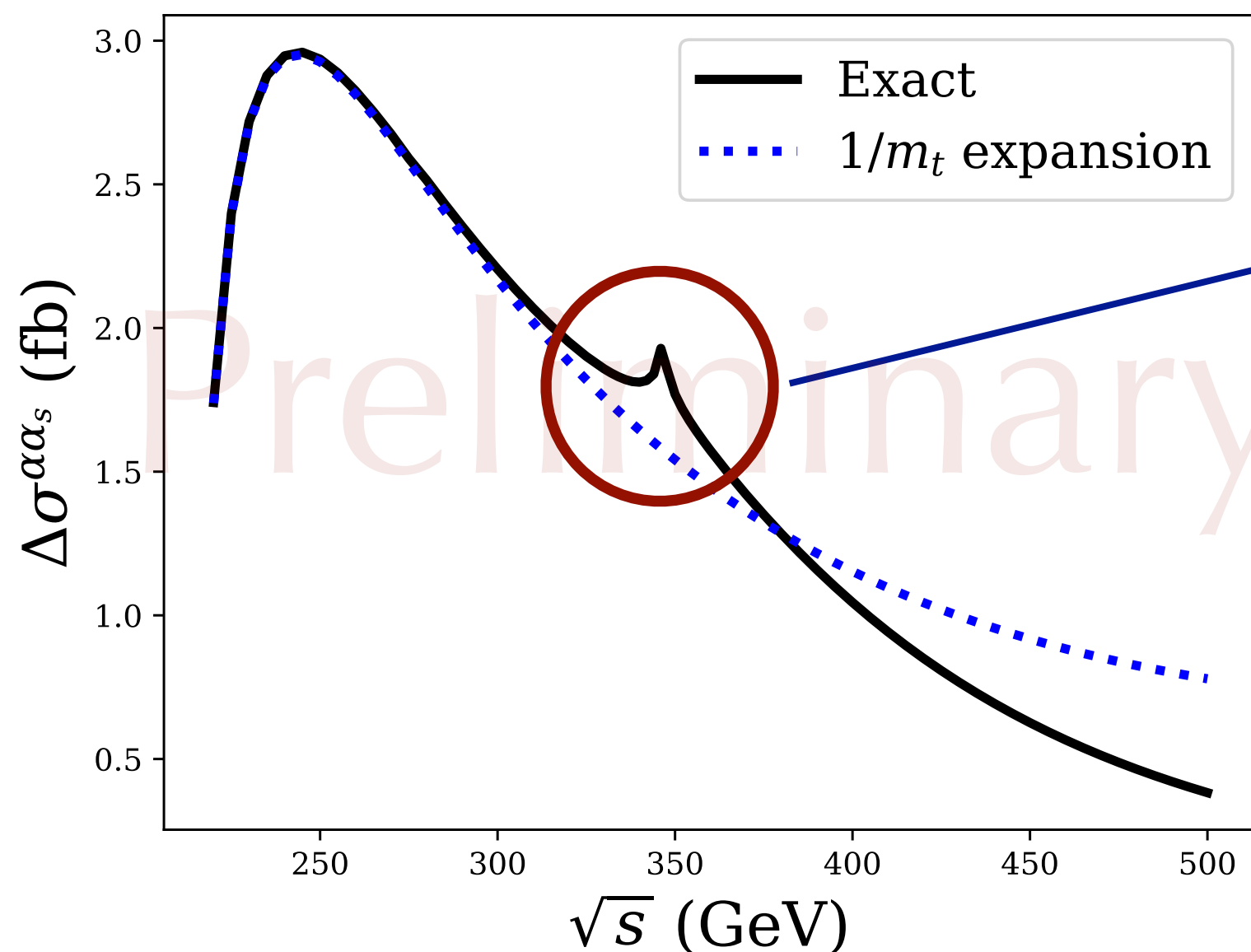
The analytic solution allows us to perform numeric studies efficiently

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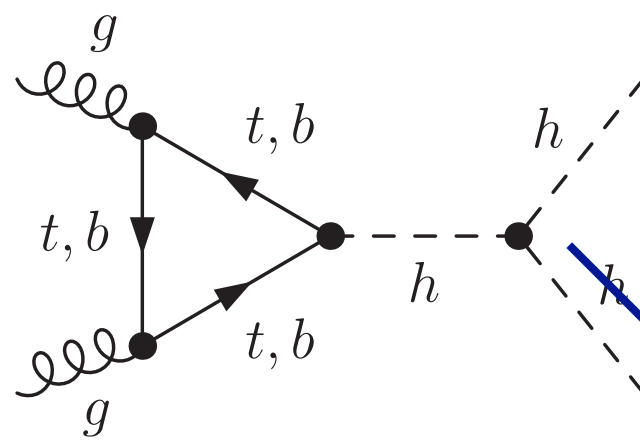
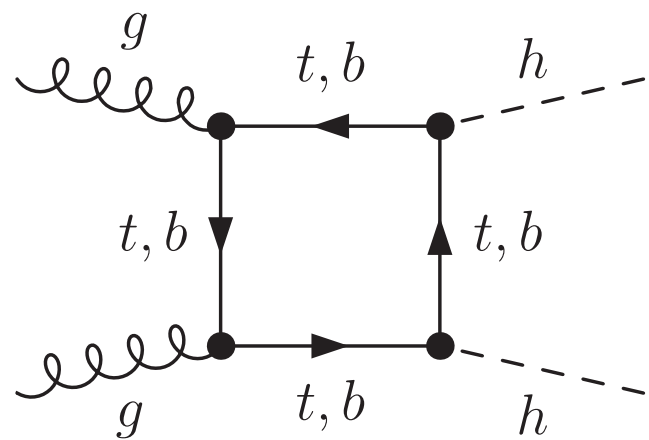


$t\bar{t}$ threshold

Difficult for sector decomposition

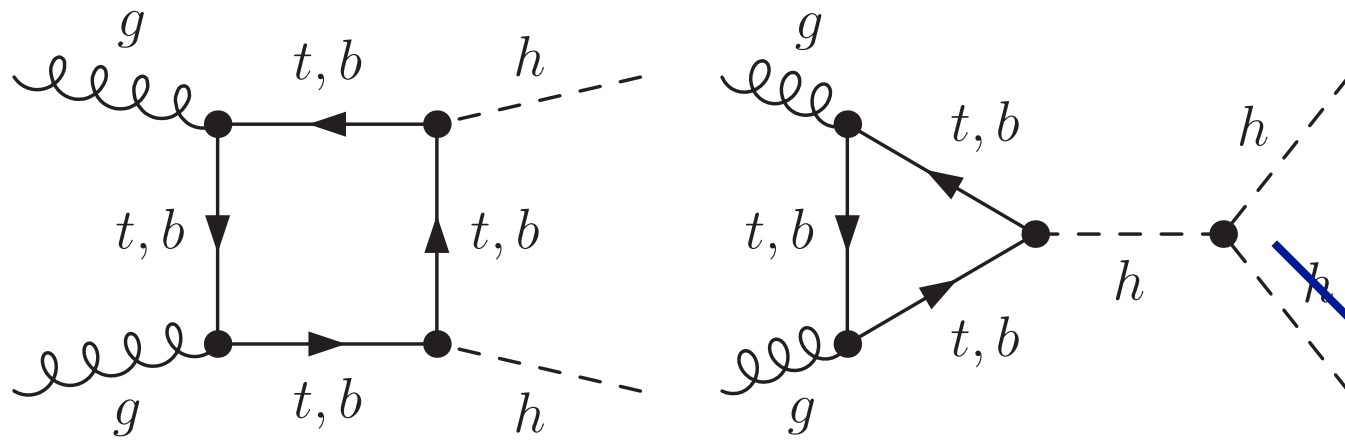
Easy with analytic solution

A more complicated case



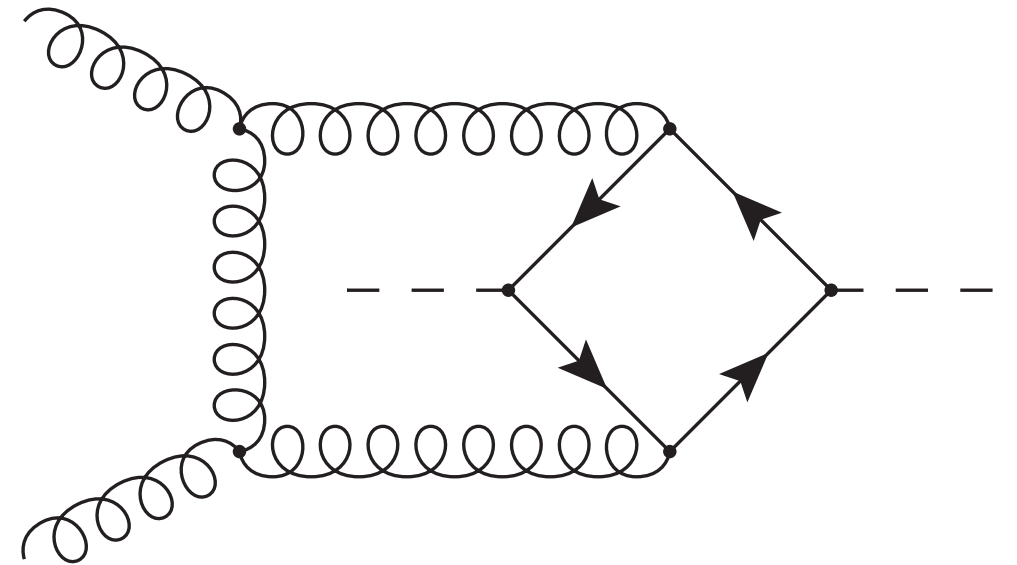
Probe Higgs self-coupling

A more complicated case

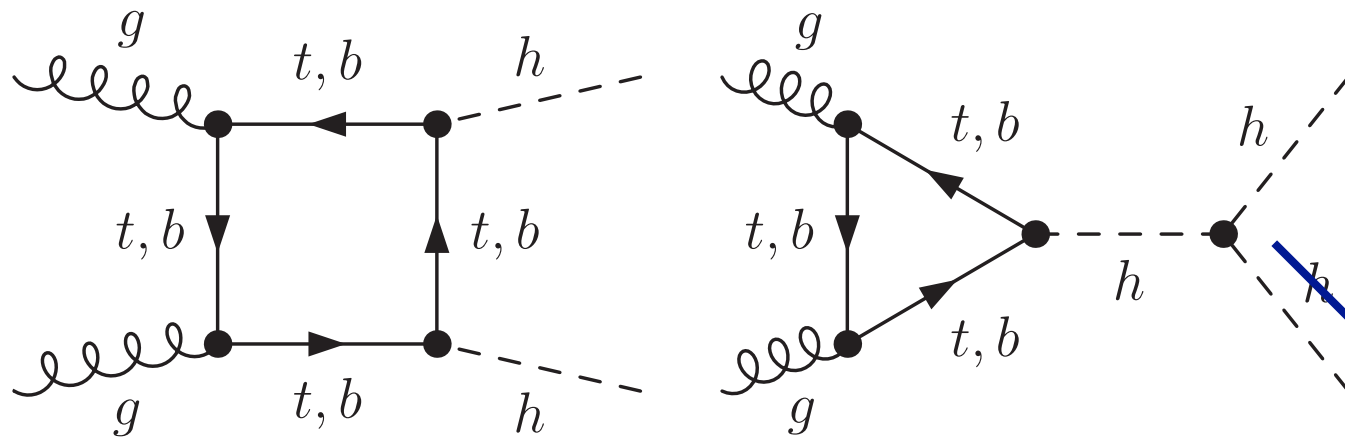


Probe Higgs self-coupling

Loop induced, NLO QCD already
difficult two-loop integrals
involving massive top quark
propagators

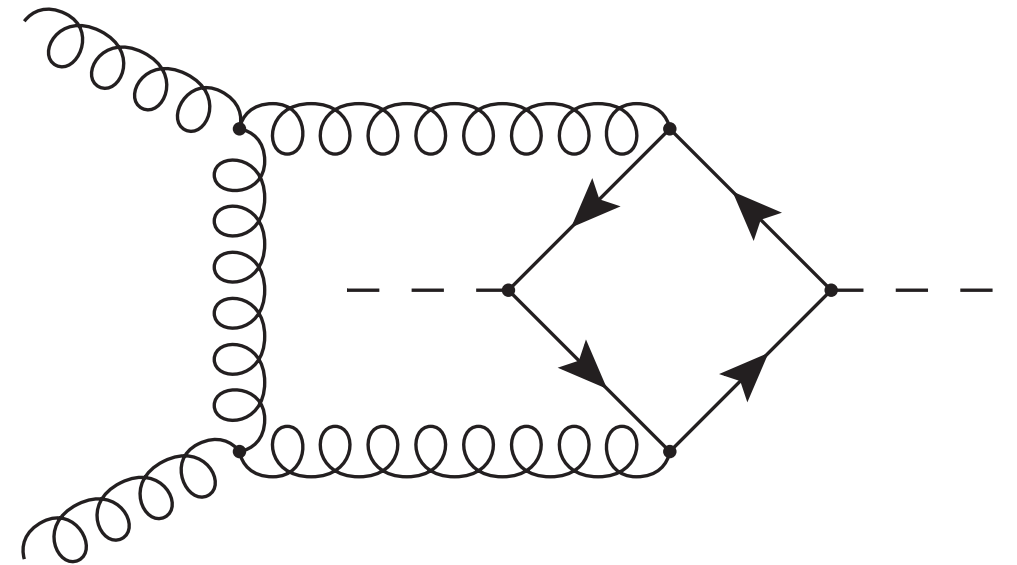


A more complicated case



Probe Higgs self-coupling

Loop induced, NLO QCD already
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propagators



Extremely resource-demanding using conventional methods

A new approximation method

Xu, **LLY**: 1810.12002

Taylor expansion in the $m_h \rightarrow 0$ limit

$$I(s, t, m_t^2, m_h^2, \epsilon) = \sum_{n=0}^{\infty} \frac{m_h^{2n}}{n!} I^{(n)}(s, t, m_t^2, \epsilon)$$

A new approximation method

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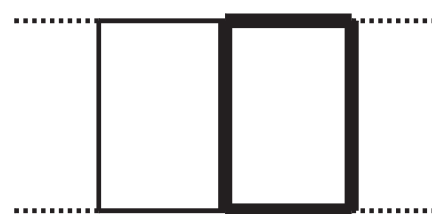
Taylor expansion in the $m_h \rightarrow 0$ limit

$$I(s, t, m_t^2, m_h^2, \epsilon) = \sum_{n=0}^{\infty} \frac{m_h^{2n}}{n!} I^{(n)}(s, t, m_t^2, \epsilon)$$

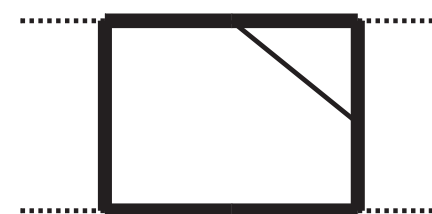
Still complicated integrals



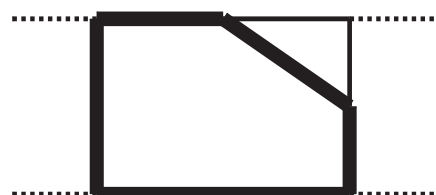
(A)



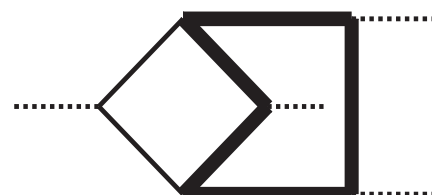
(B)



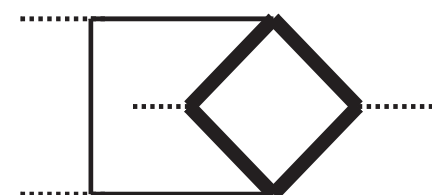
(C)



(D)



(E)

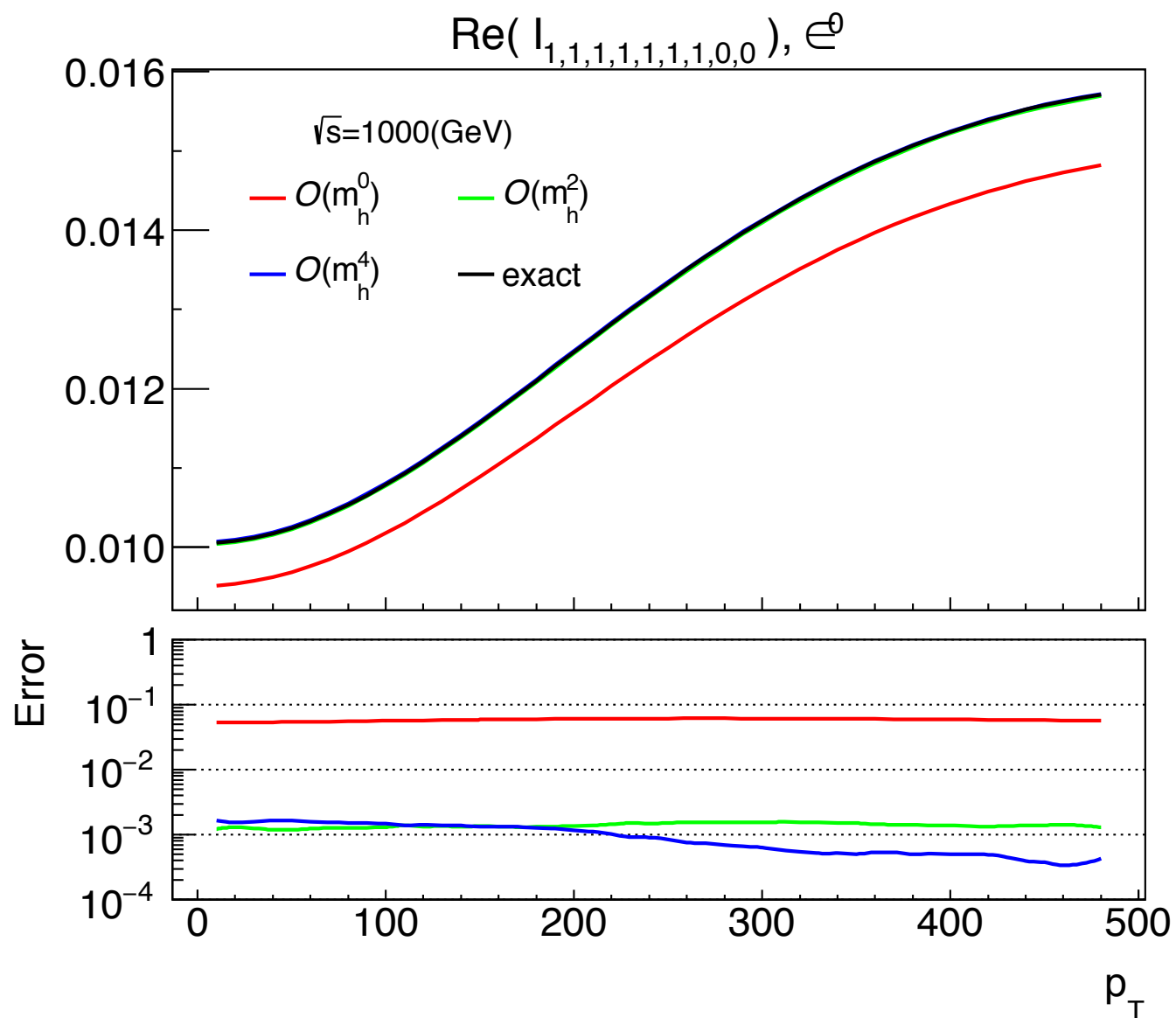


(F)

A new approximation method

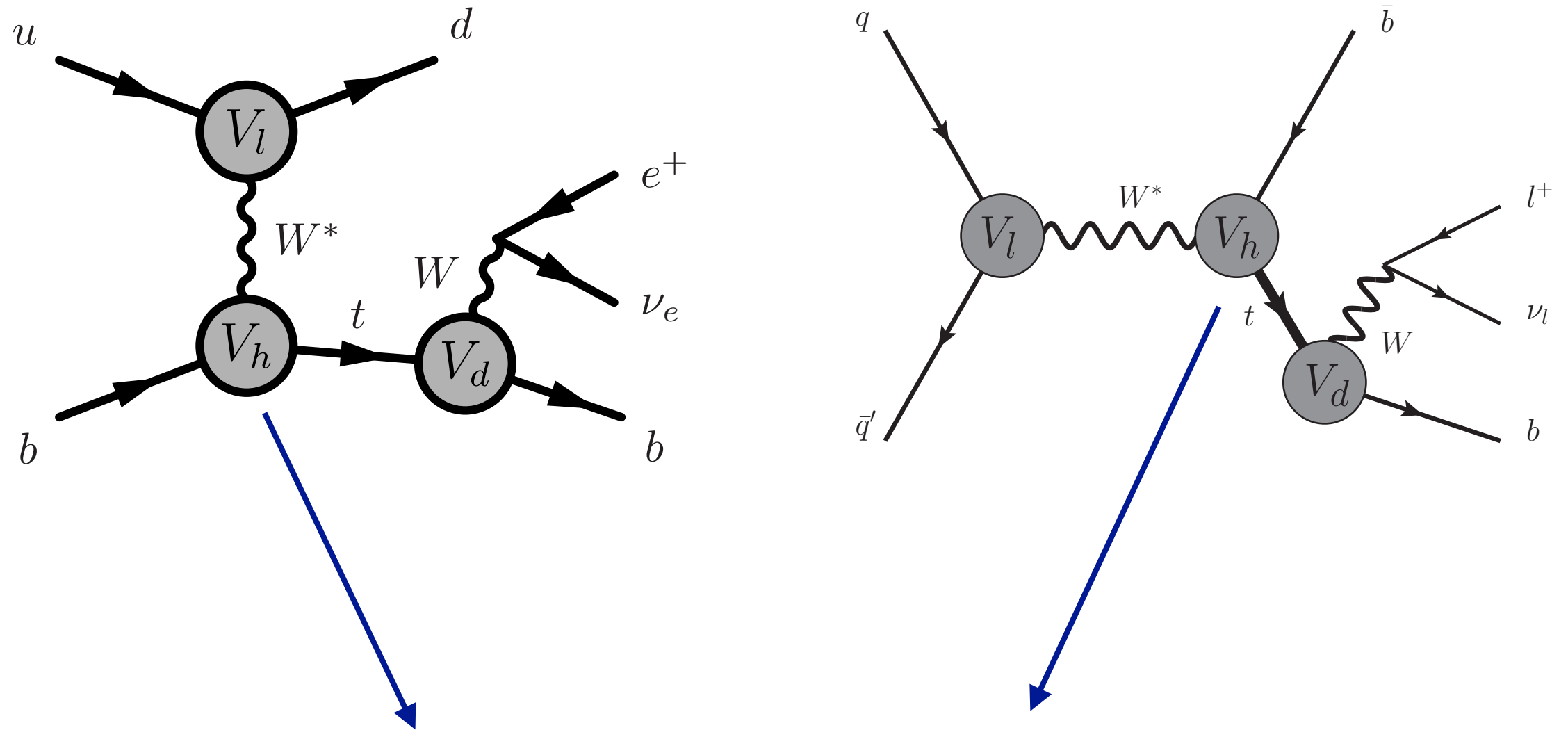
Good convergence for master integrals

Xu, **LLY**: 1810.12002



Towards the full amplitude Wang, Xu, **LLY**: in preparation

Single top quark production



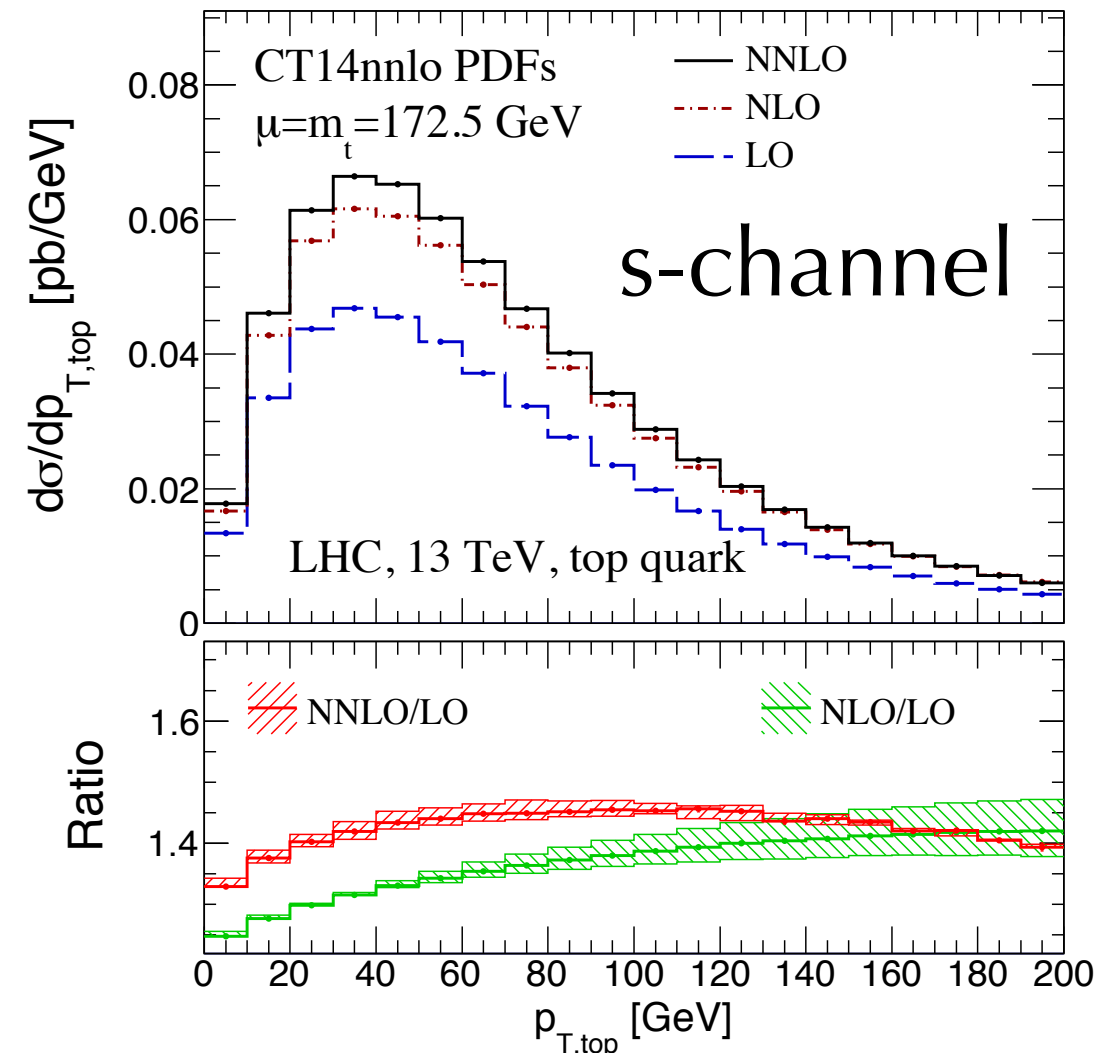
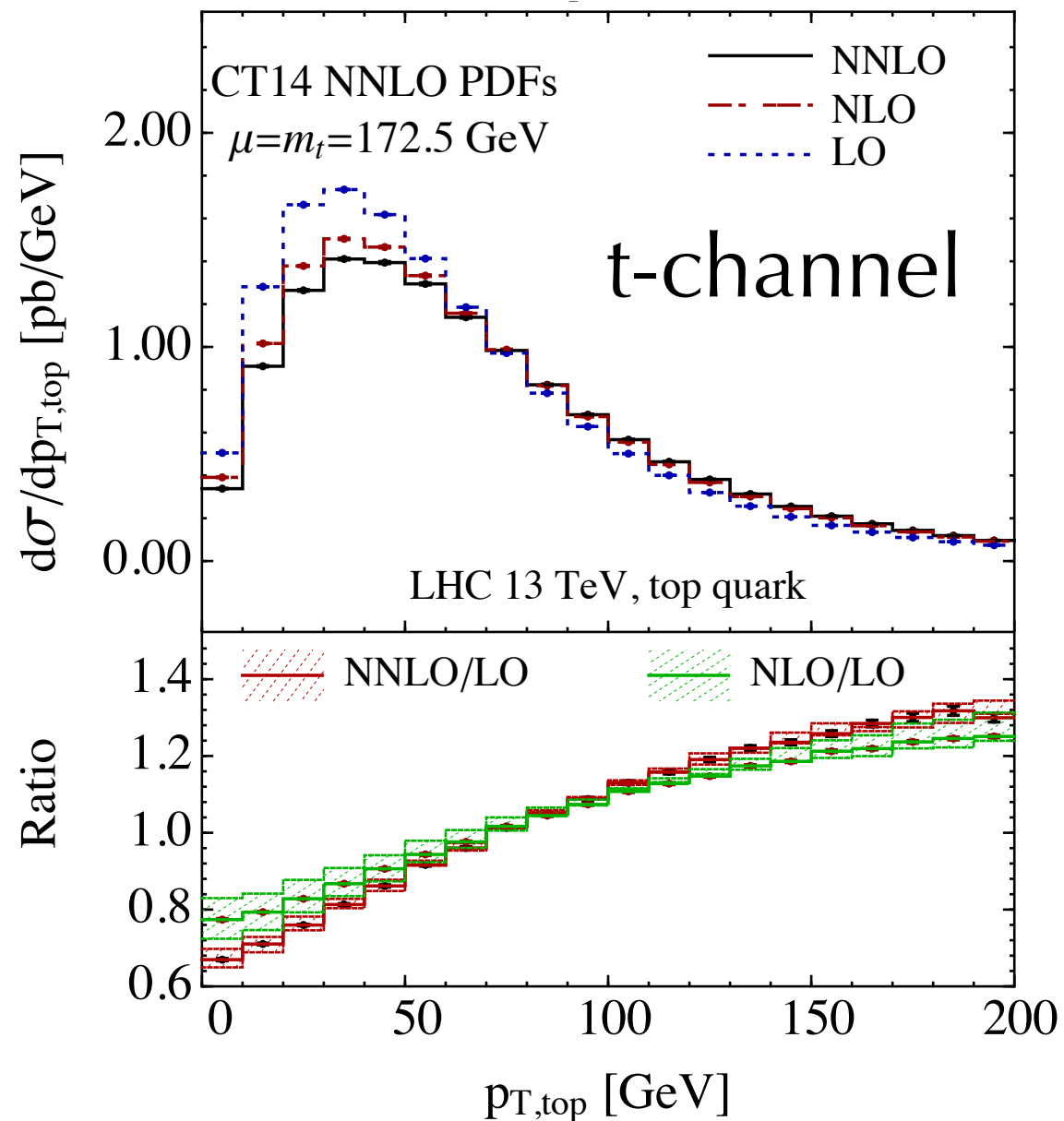
Probe weak interactions of the top quark
 In particular, the CKM matrix element V_{tb}

Single top production and decay at NNLO

Berger, Gao, Yuan, Zhu: 1606.08463

Berger, Gao, Zhu: 1708.09405

Liu, Gao: 1807.03835



Shape change in distributions

TOP2019 Workshop

Hosted at IHEP in Beijing this September



12th International Workshop on Top Quark Physics (TOP2019)

22-27 September 2019
Beijing
Asia/Shanghai timezone

<https://indico.cern.ch/e/top2019>



Overview

Timetable

Registration

Participant List

Transportation

Accommodation

Visa to China

Social Events

About Beijing

Online Payment

Welcome to the 12th International Workshop on Top Quark Physics (TOP2019)

The 12th International Workshop on Top Quark Physics (TOP 2019) will be held at **Institute of High Energy Physics (IHEP), Beijing, China**, from **September 22nd to 27th**.

Following the long tradition of the workshop series, the 2019 edition will be dedicated to an overview of the most up-to-date experimental measurements at the Large Hadron Collider (LHC) and latest theoretical developments on top quark physics. Special focus on theoretical developments related to physics beyond the standard model will be given in a Mini-Workshop with the name "Top Meets New Physics" that will take place on Thursday, September 26th. There will also be a session on top quark physics at future facilities such as the High Luminosity LHC and CEPC/SppC.

We are looking forward to meeting you in Beijing this coming September.

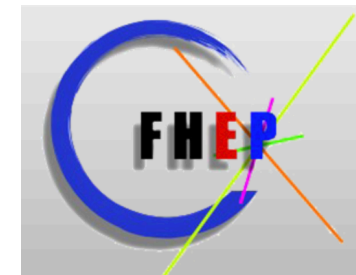
12TH INTERNATIONAL WORKSHOP ON TOP QUARK PHYSICS

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2019

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中国科学院高能物理研究所
Institute of High Energy Physics Chinese Academy of Sciences



22 - 27
September 2019
Beijing

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Roberto Tenchini, INFN Pisa
Wolfgang Wagner, Wuppertal (chair)
Malgorzata Worek, Aachen

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<https://indico.cern.ch/event/792576/>

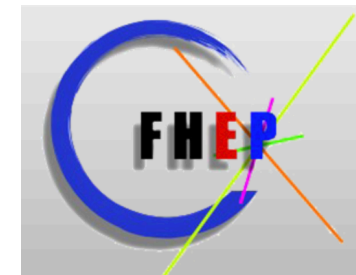
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Thank you!