

# PrimEx Final Result: Neutral Pion Lifetime

**Liping Gan**

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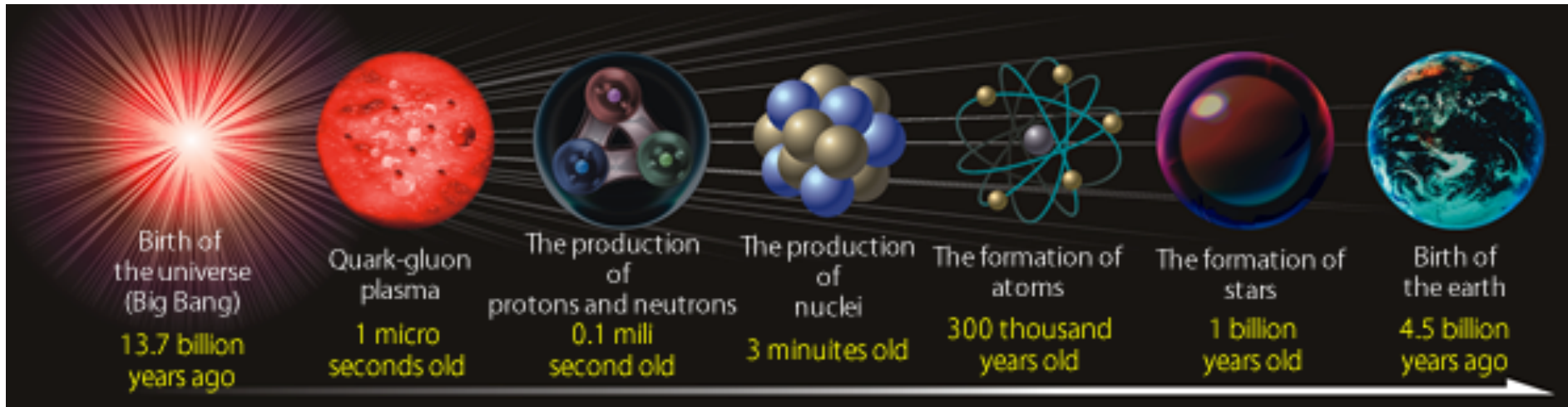
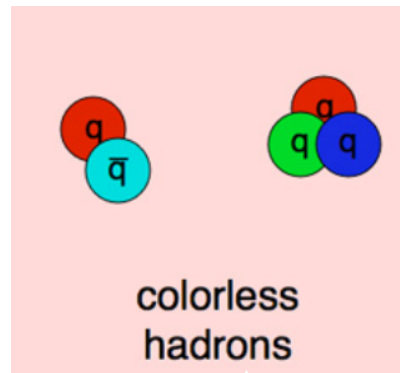
**(On behalf of the PrimEx Collaboration)**

## Outline

- Low-energy QCD symmetries and the  $\pi^0$  lifetime
- The PrimEx experiments and final result
- Summary

# Challenge: QCD Confinement

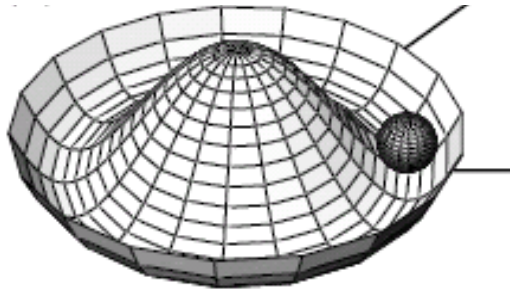
- QCD confinement is the last frontier for the standard model
- $\pi^0 \rightarrow \gamma\gamma$  offers a sensitive probe: **chiral symmetry and anomaly**



# Spontaneous Chiral Symmetry Breaking Gives Rise to $\pi^0$

In the massless quark limit

$$SU_L(3) \times SU_R(3) \rightarrow SU(3)$$



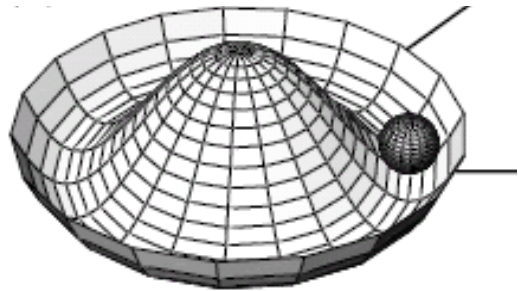
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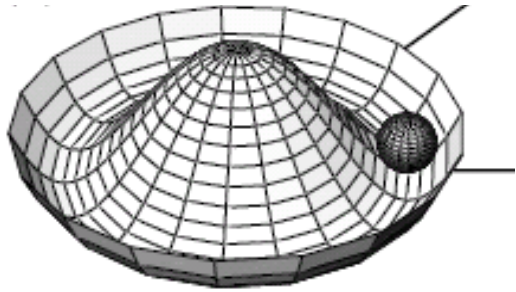
$SU_L(3) \times SU_R(3)$  and  $SU(3)$  are explicitly breaking due to non-zero quark masses and quark mass differences:

- Goldstone bosons are massive
- Mixing of  $\pi^0, \eta, \eta'$

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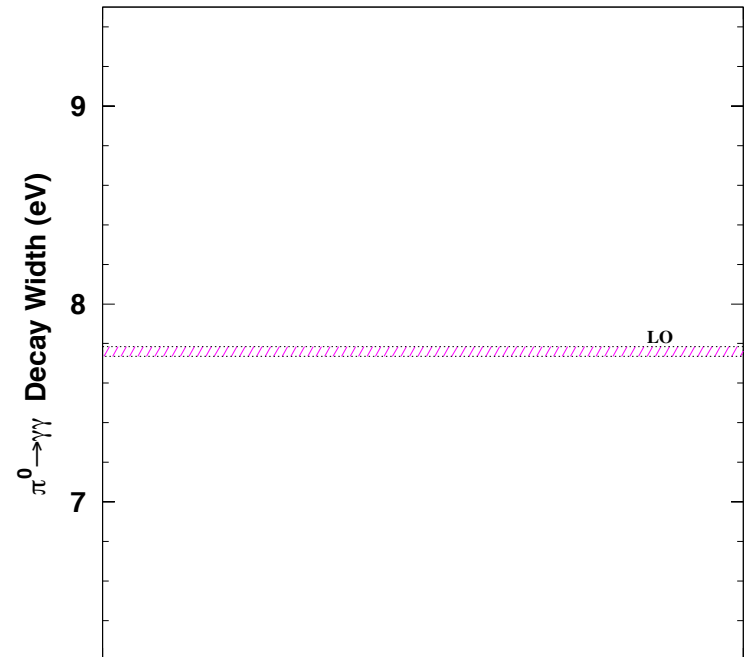
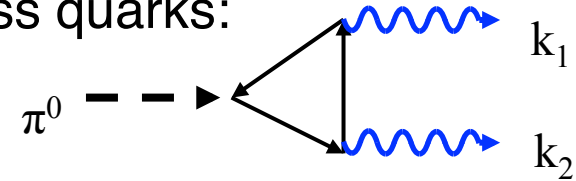
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As the lightest hadron in nature, these corrections to  $\pi^0$  are small.

# Axial Anomaly Determines $\pi^0$ Lifetime

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- ◆ The chiral anomaly prediction **is exact** for massless quarks:

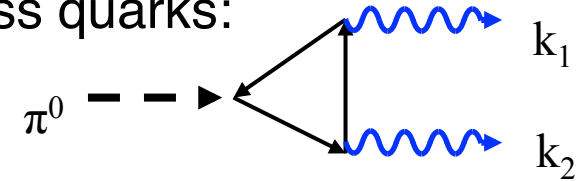
$$\Gamma(\pi^0 \rightarrow \gamma\gamma) = \frac{\alpha^2 N_c^2 m_\pi^3}{576 \pi^3 F_\pi^2} = 7.750 \pm 0.016 \text{ eV}$$



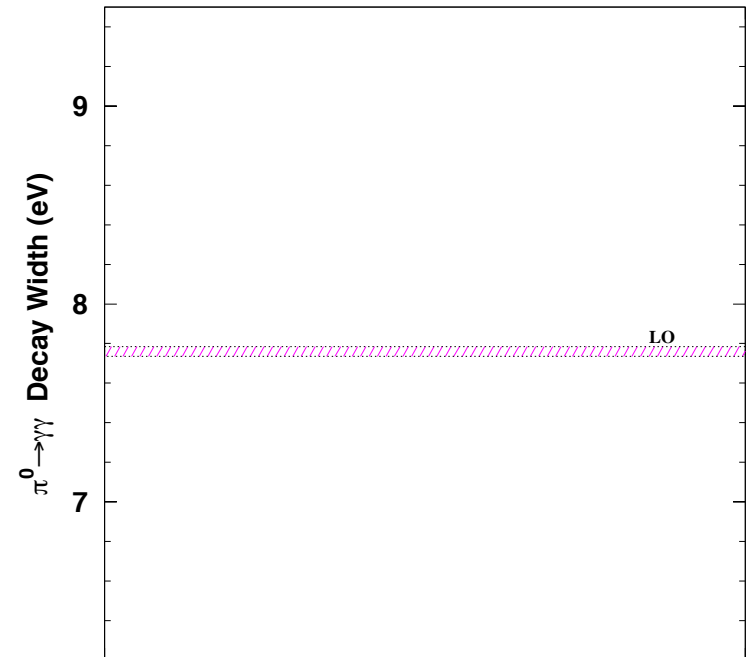
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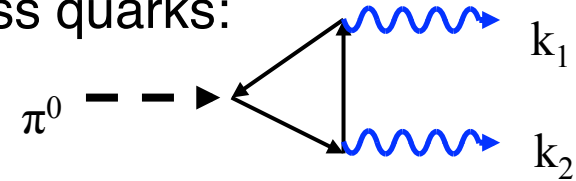
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## ➤ Corrections to the chiral anomaly prediction:

Calculations in NLO ChPT:

□  $\Gamma(\pi^0 \rightarrow \gamma\gamma) = 8.10 \text{ eV} \pm 1.0\%$

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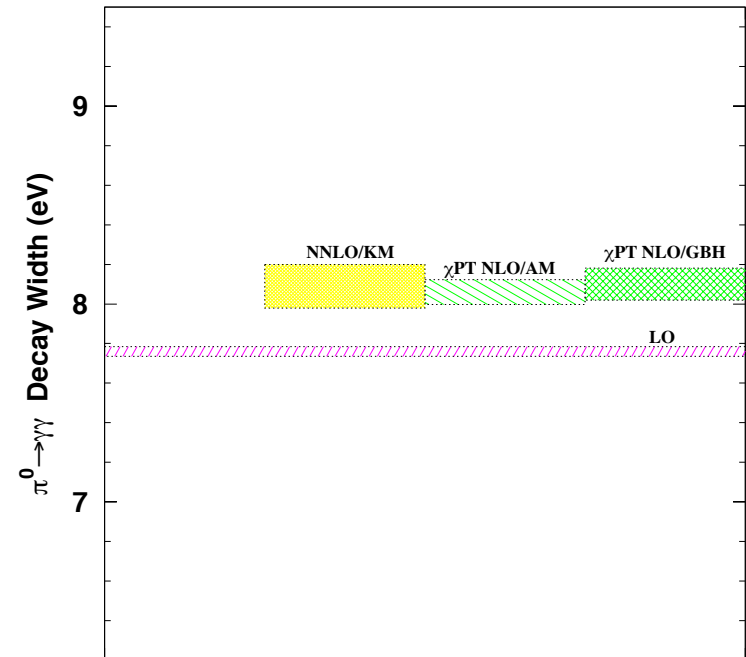
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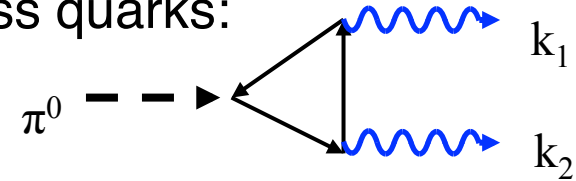




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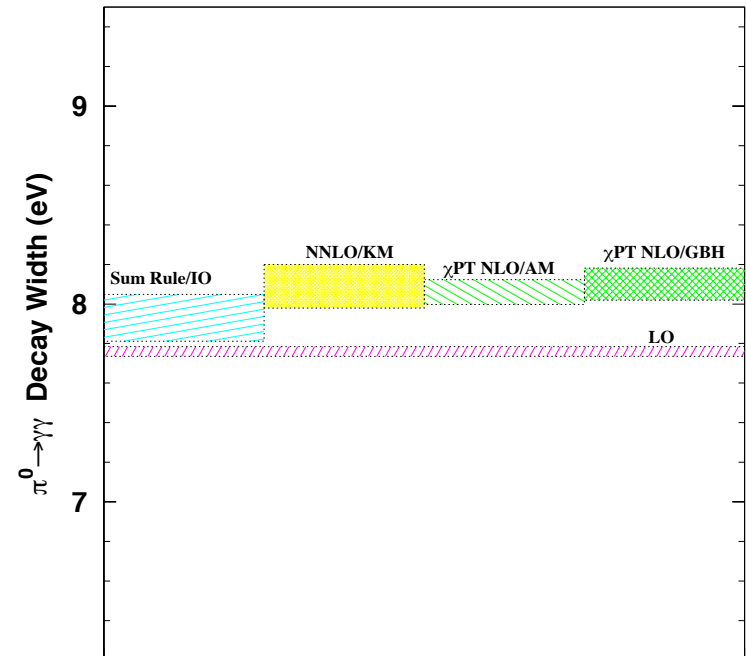
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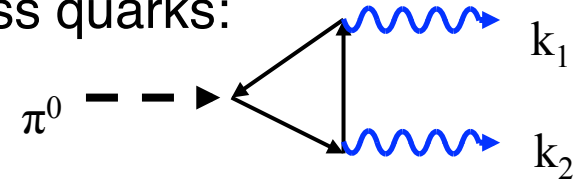
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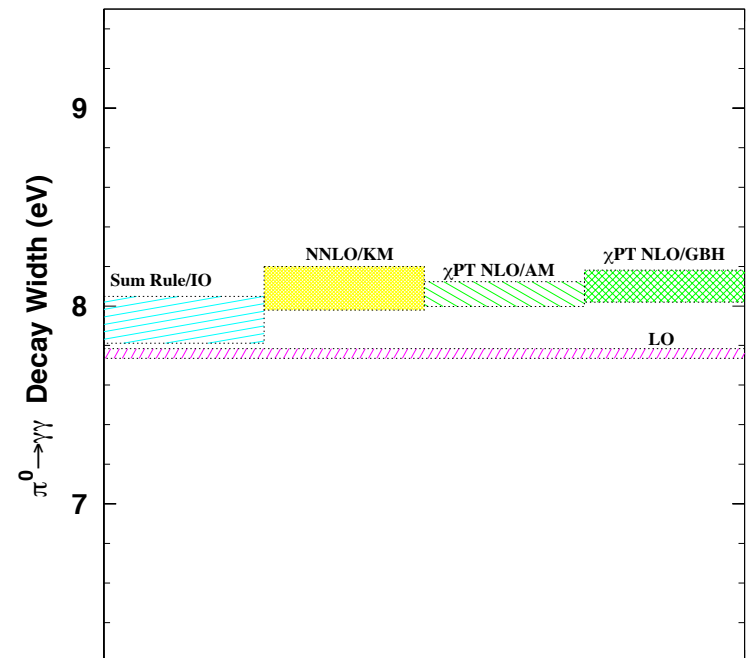
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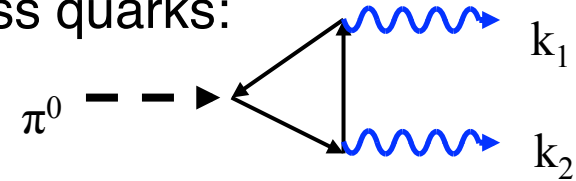


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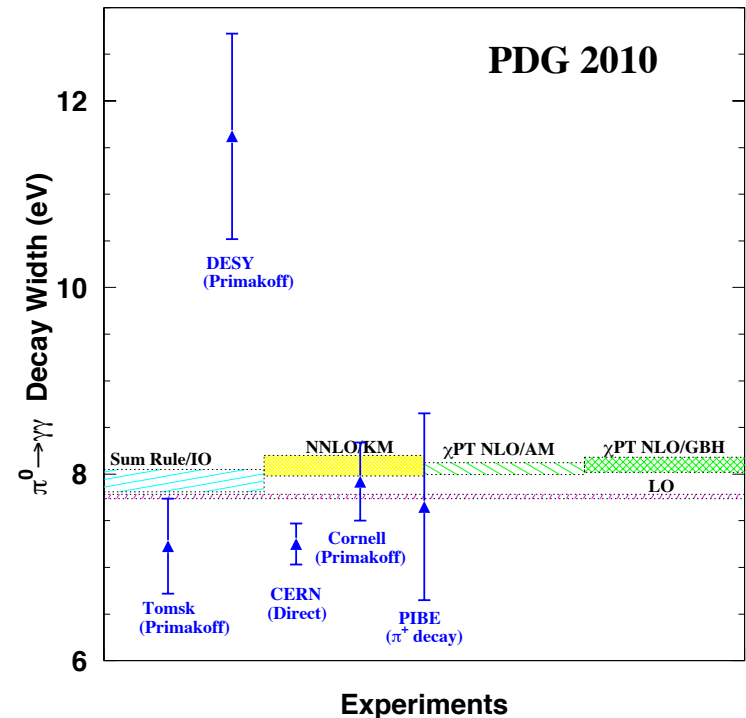
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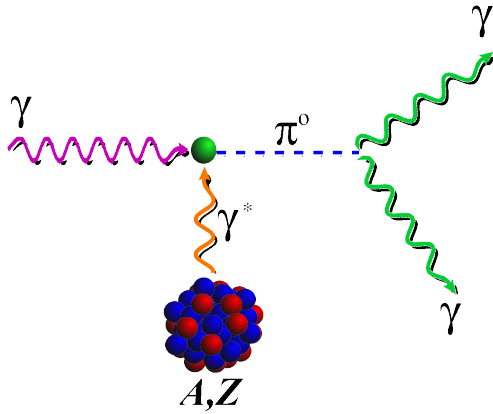
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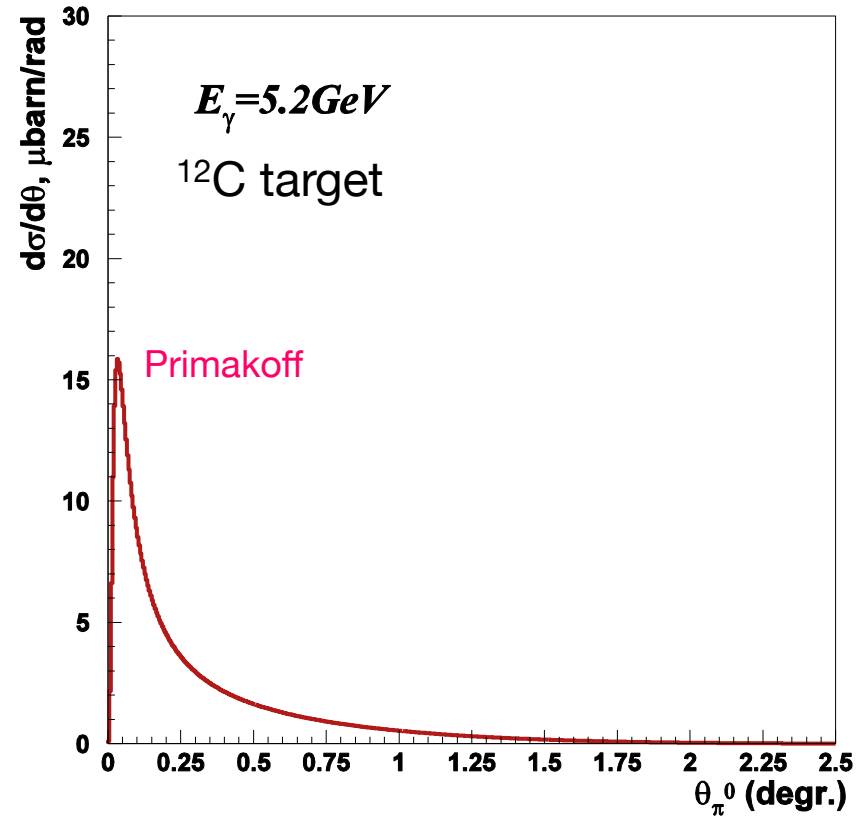


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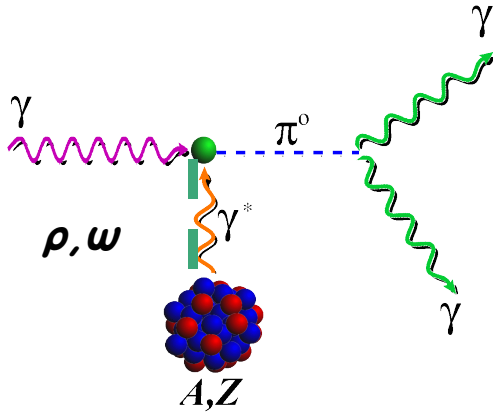
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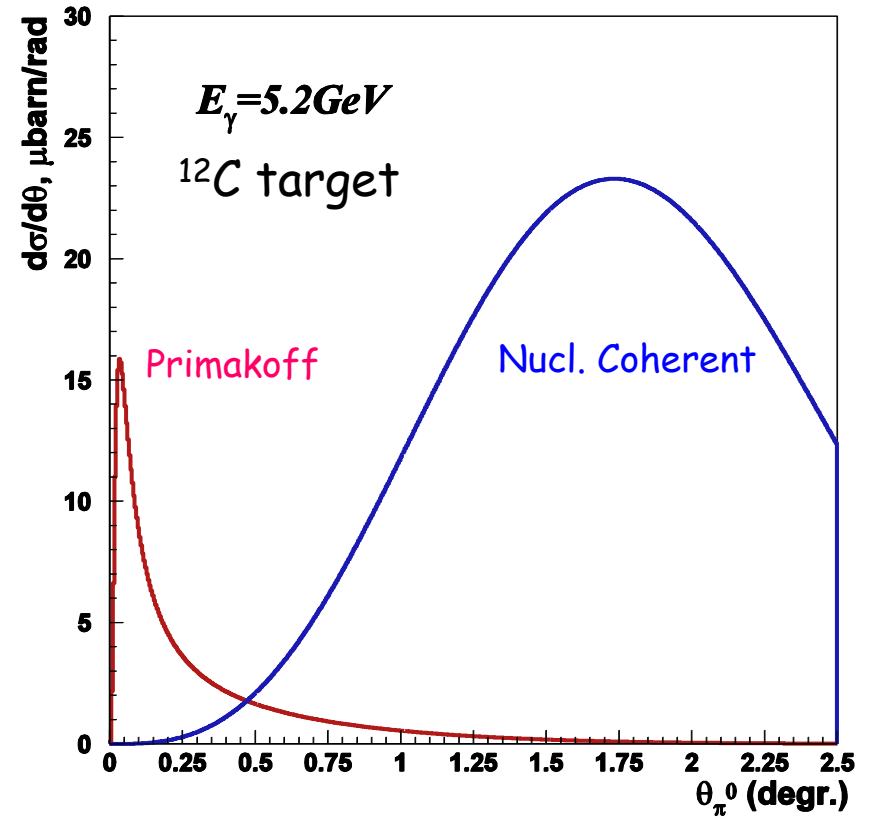
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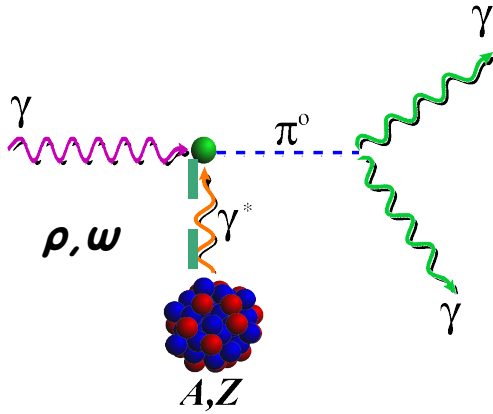
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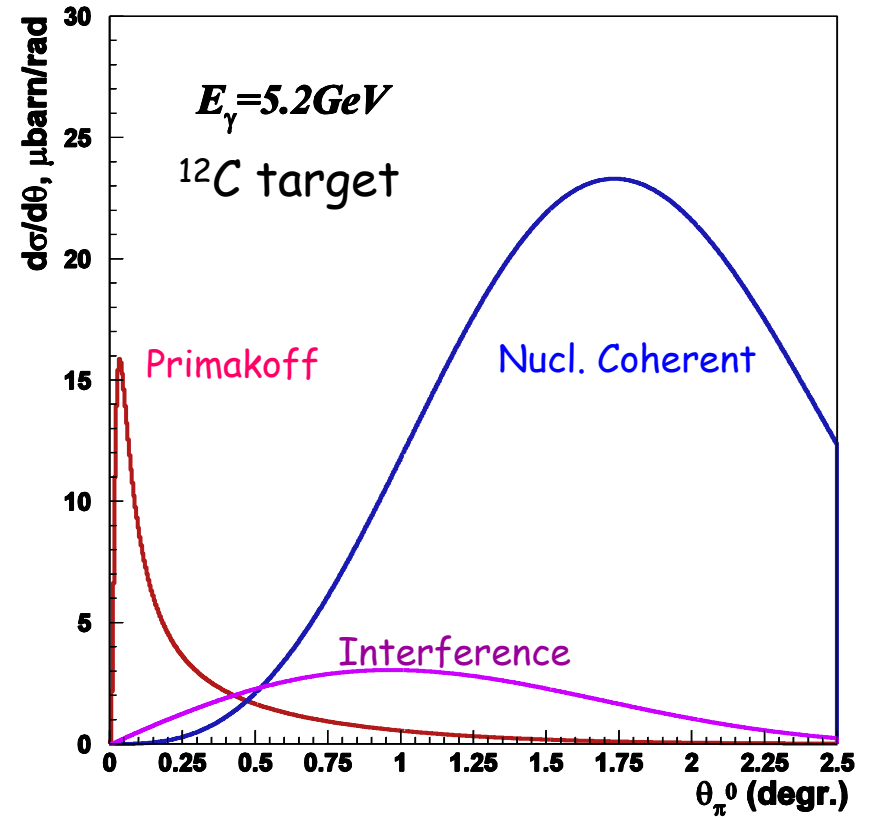
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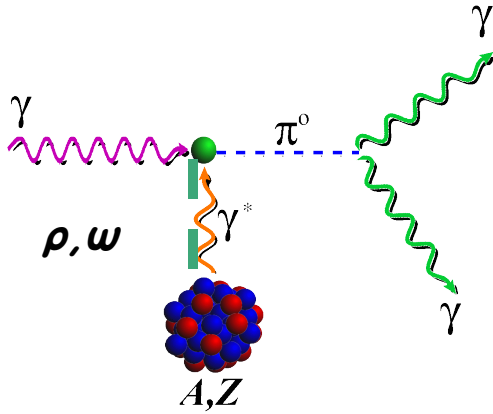
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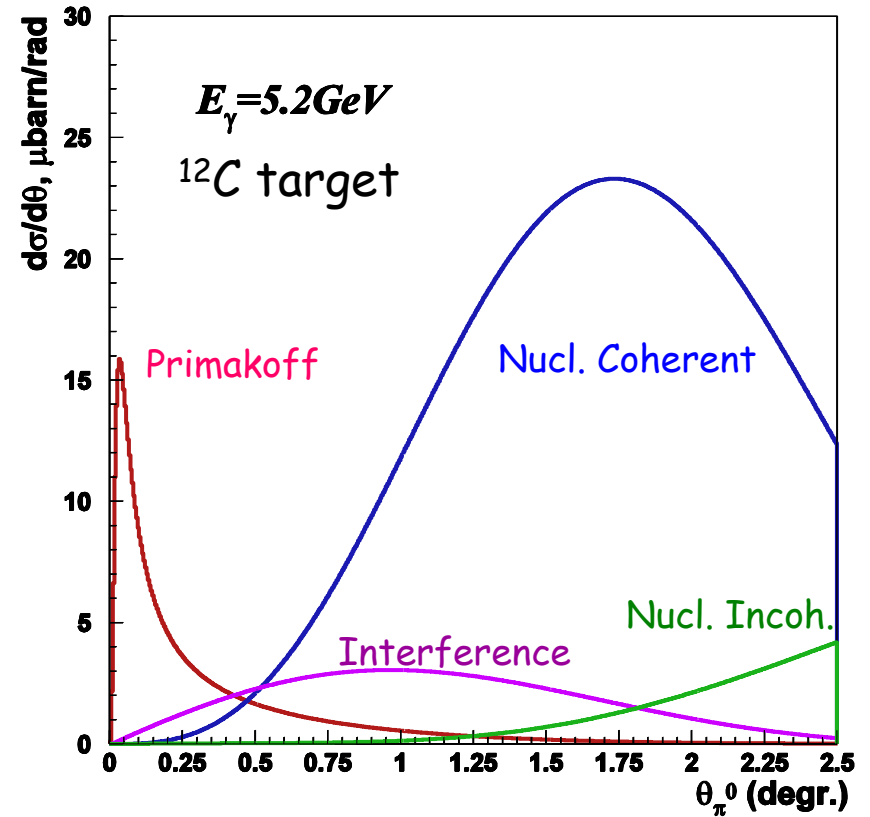
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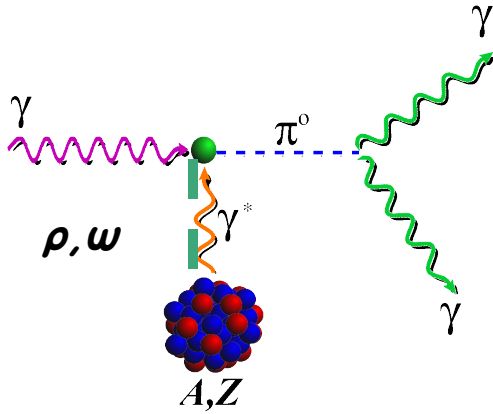
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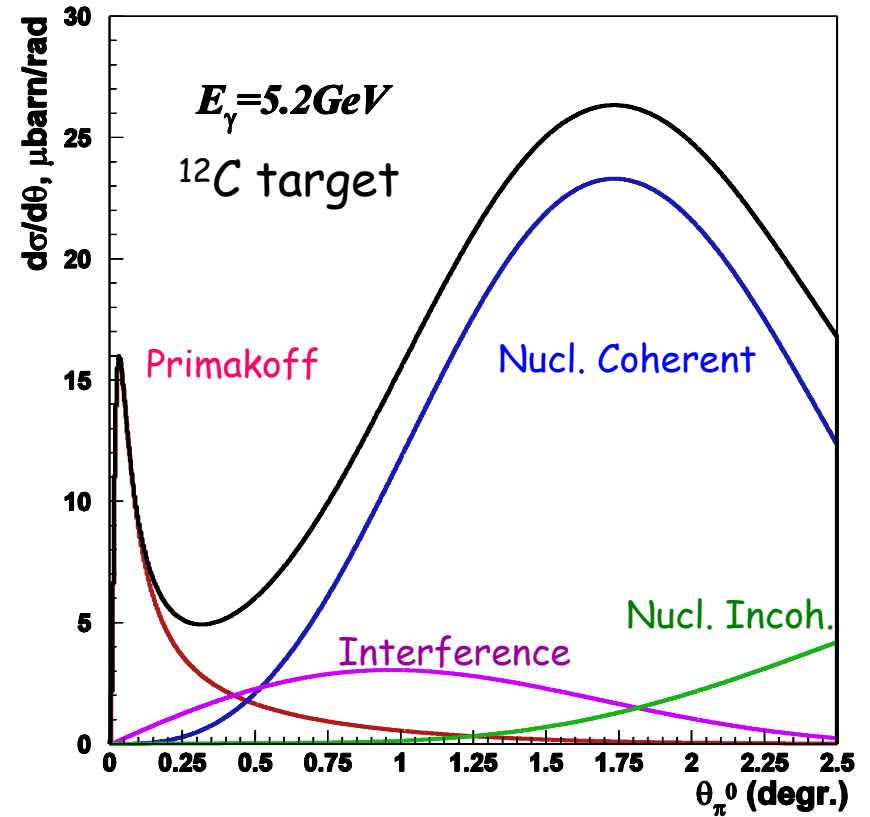
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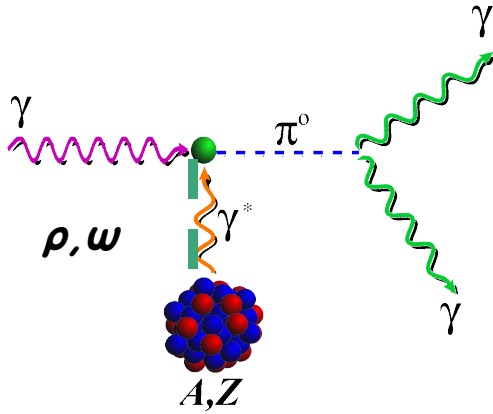
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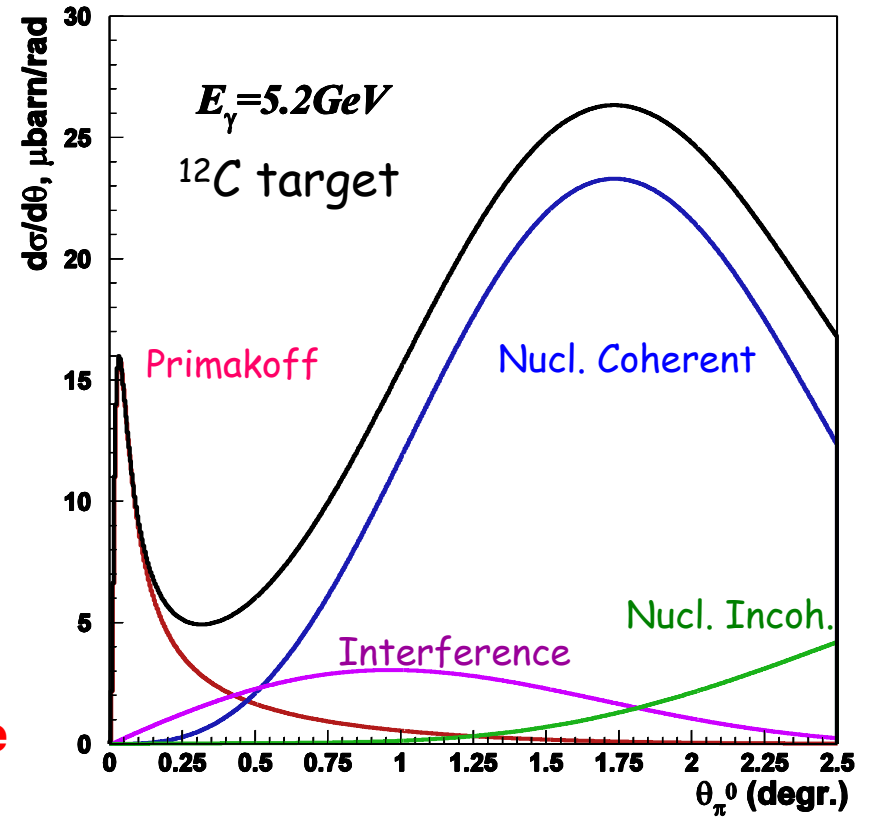


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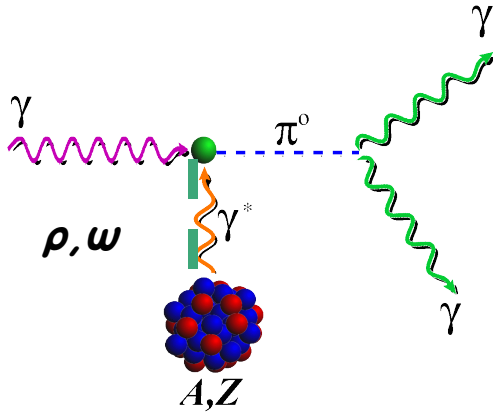
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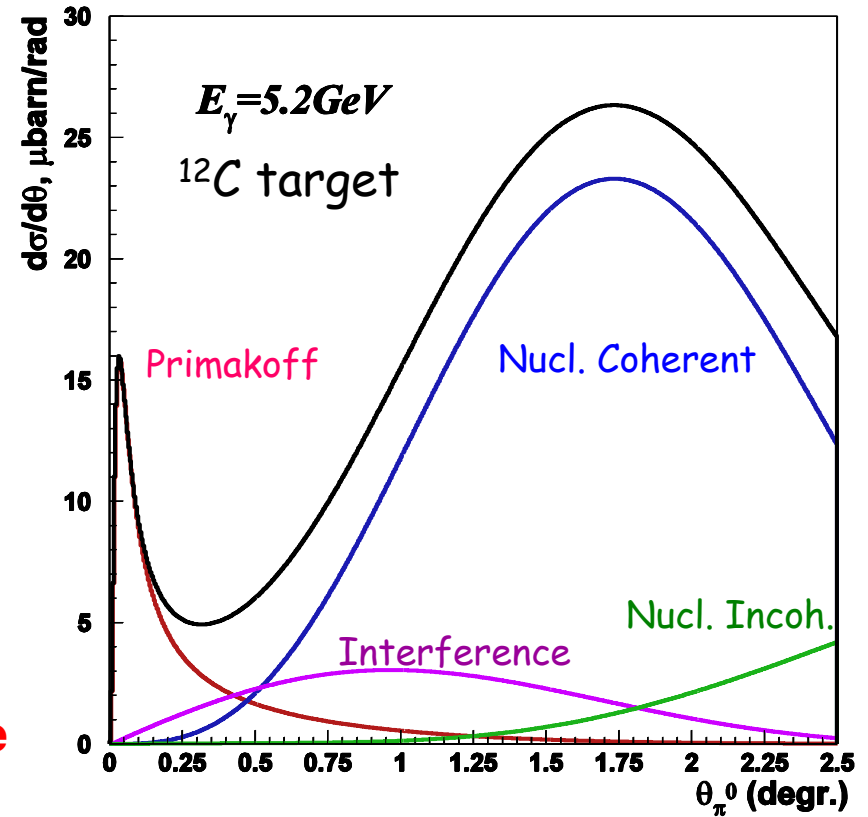
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## Requirement:

- Photon flux
- Beam energy
- $\pi^0$  production angle resolution
- Compact nuclear target

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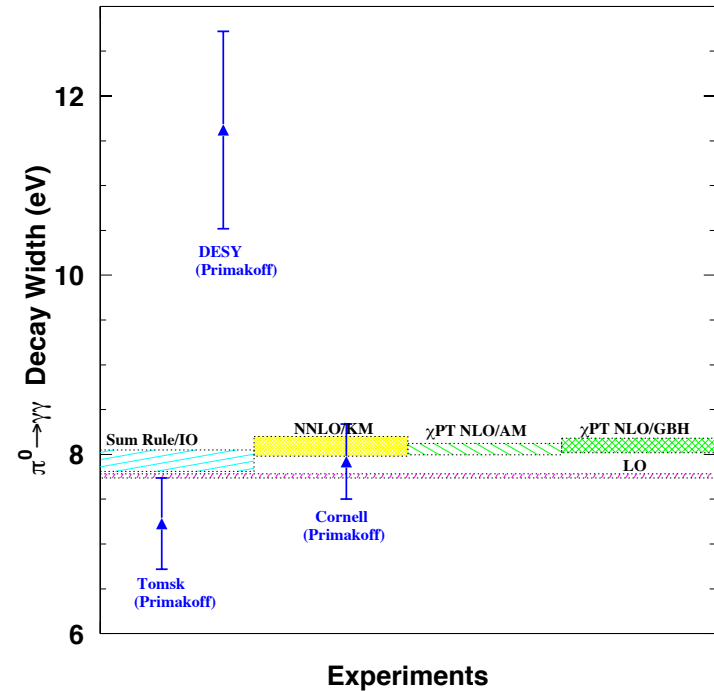
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# Previous Primakoff Experiments

- ◆ DESY (1970) (N.C.,66A,243)  
 Untagged bremsstrahlung beam,  
 $E_\gamma$ : about 1.5 and 2.5 GeV  
 Targets: C, Zn, Al, Pb  
 Result:  $\Gamma(\pi^0 \rightarrow \gamma\gamma) = (11.7 \pm 1.2)$  eV  
 (10%)
- ◆ Tomsk (1970) (Sov.Phys.JETP,30, 1037)  
 Untagged bremsstrahlung beam  
 $E_\gamma \sim 1.1$  GeV  
 target: Pb  
 Result:  $\Gamma(\pi^0 \rightarrow \gamma\gamma) = (7.23 \pm 0.51)$  eV  
 (7.1%)
- ◆ Cornell (1974) (PRL,33,1400)  
 Untagged bremsstrahlung  $\gamma$  beam  
 $E_\gamma$ : about 4 and 6 GeV  
 targets: Be, Al, Cu, Ag, U  
 Result:  $\Gamma(\pi^0 \rightarrow \gamma\gamma) = (7.92 \pm 0.42)$  eV  
 (5.3%)

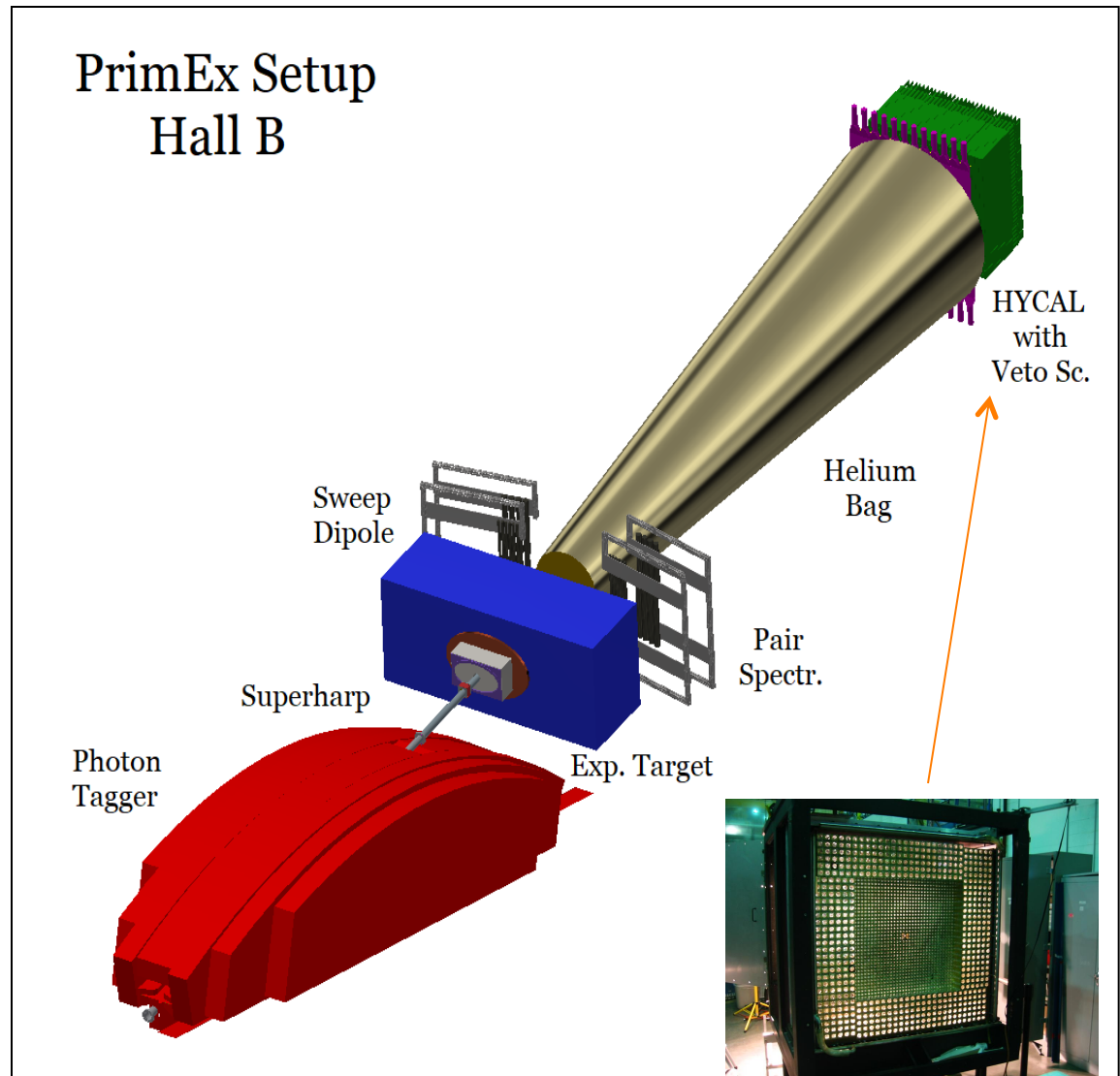


All these experiments used

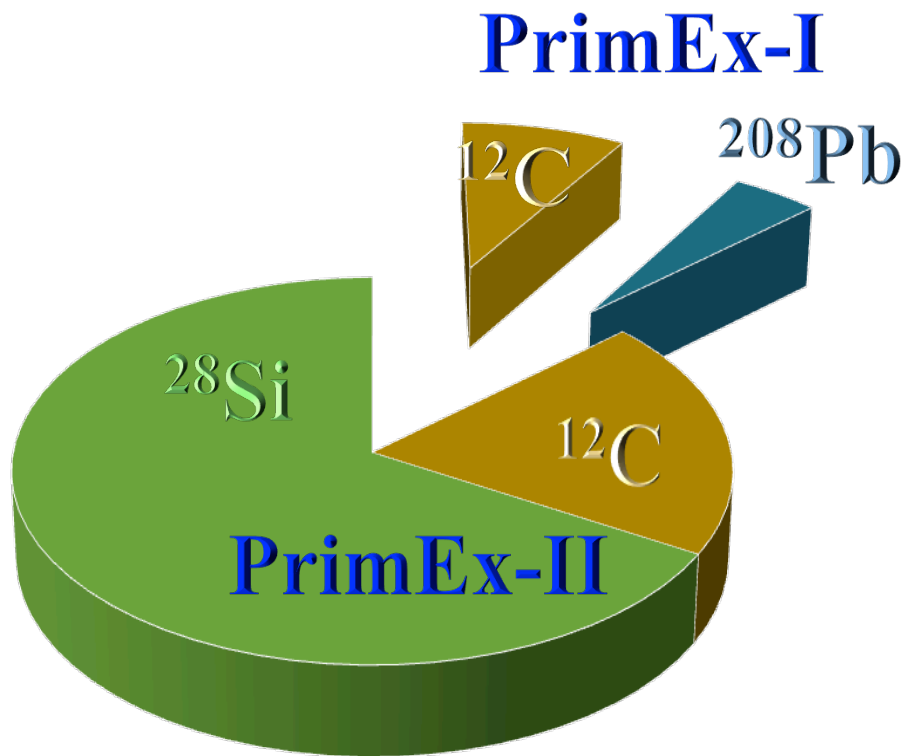
1. Untagged bremsstrahlung photon beam
2. Conventional Pb-glass calorimeter
3. Earlier theoretical calculations

# PrimEx Experimental Setup

- ❑ Hall B high resolution, high intensity photon tagging facility
- ❑ A pair spectrometer for photon flux control at high beam intensities
- ❑ New high resolution hybrid multi-channel calorimeter (HyCal)



# Two Experiments: PrimEx I and II



- PrimEx I was performed on  $^{12}\text{C}$  and  $^{208}\text{Pb}$  targets with  $E_\gamma=4.9\text{-}5.5$  GeV, and the result was published in 2011.

PRL 106, 162303 (2011)

- PrimEx II was performed on  $^{12}\text{C}$  and  $^{28}\text{Si}$  targets with  $E_\gamma=4.4\text{-}5.3$  GeV. The result is recently finalized

# Improvements for PrimEx-II

## Systematics

- Better control of Background:
  - ✓ Add timing information in HyCal (~500 chan.)
  - ✓ Improve photon beam line
  - ✓ Improve PID in HyCal (add horizontal veto counters to have both x and y detectors)
  - ✓ More empty target data
- Measure HyCal detection efficiency
- New  $^{28}\text{Si}$  target

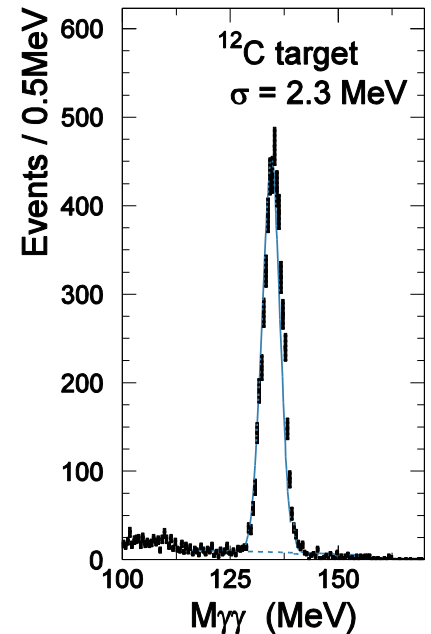
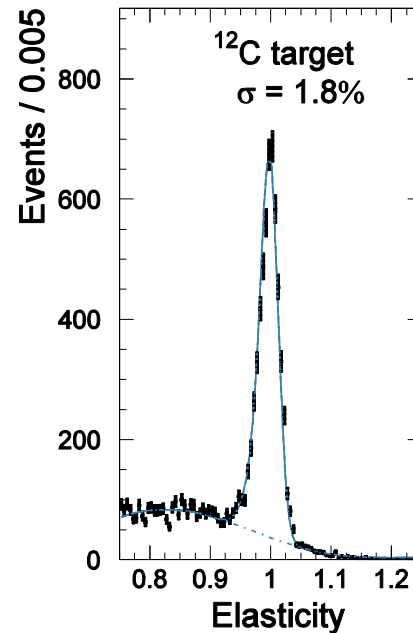
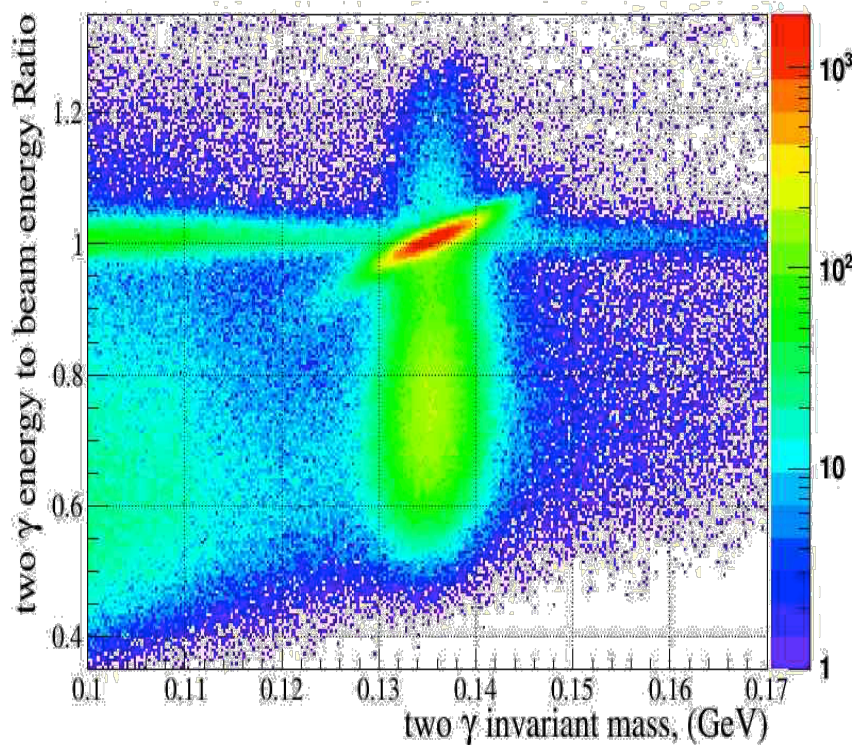
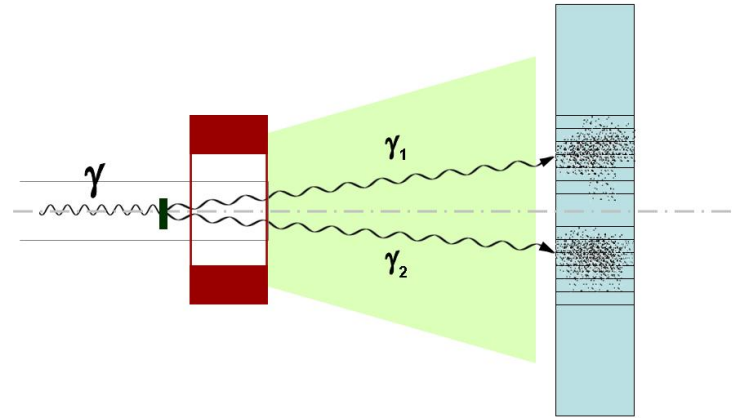
## Statistics

- ✓ Double target thickness (factor of 2 gain)
- ✓ Hall B DAQ with 5 kHz rate, (factor of 5 gain)
- ✓ increase photon beam energy interval by 50% in the trigger

# $\pi^0$ Event selection

We measure:

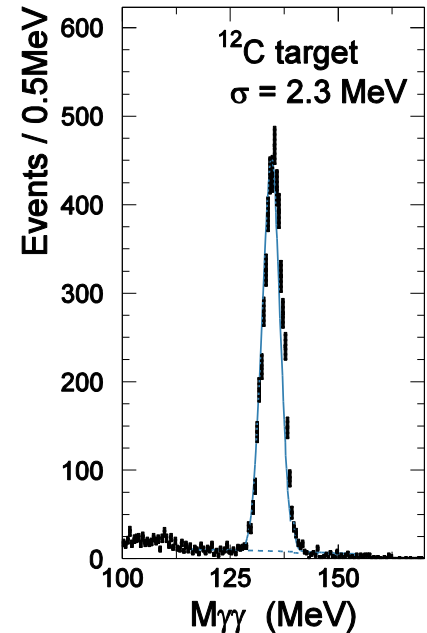
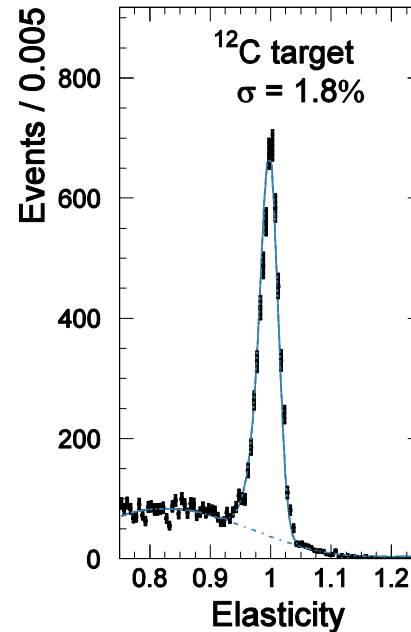
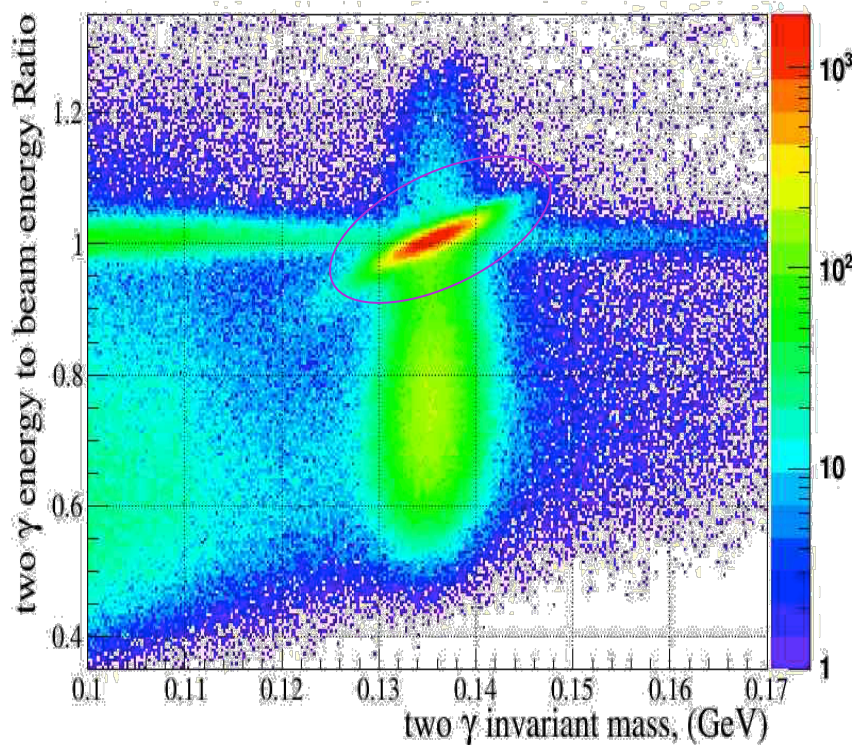
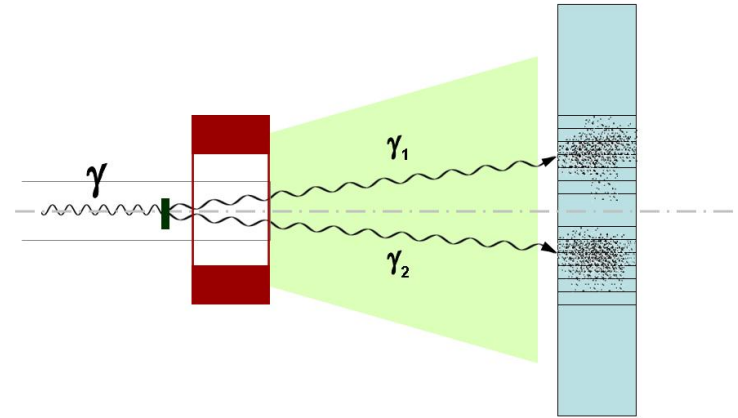
- incident photon:  $E_\gamma$  and time
- two decay photons:  $E_{\gamma_1}$ ,  $E_{\gamma_2}$  and time
- X,Y positions of decay photons



# $\pi^0$ Event selection

We measure:

- incident photon:  $E_\gamma$  and time
- two decay photons:  $E_{\gamma_1}$ ,  $E_{\gamma_2}$  and time
- X,Y positions of decay photons

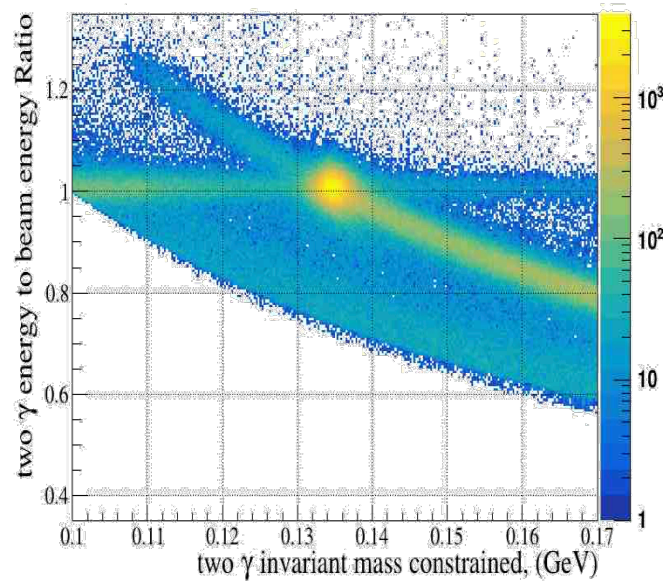




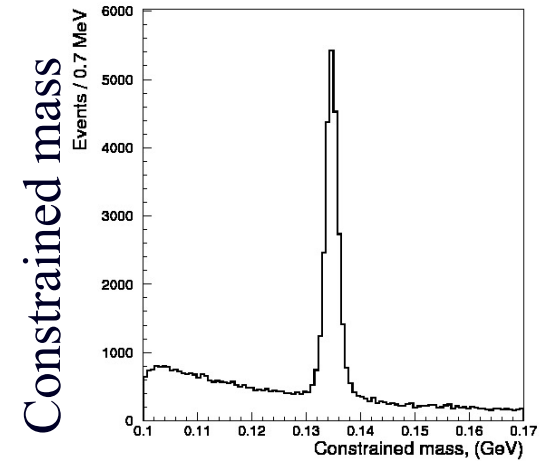
# Two Methods for $\pi^0$ yield extraction

- **Energy Constrained mass analysis (C)**

by I. Larin, Umass

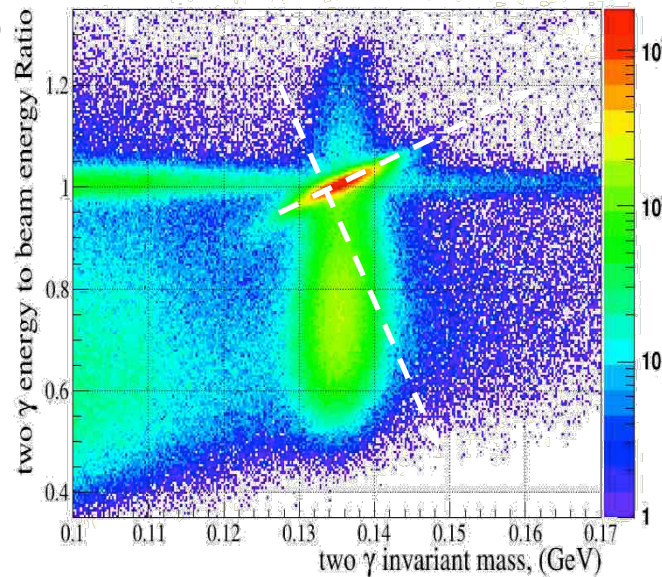


C-analysis

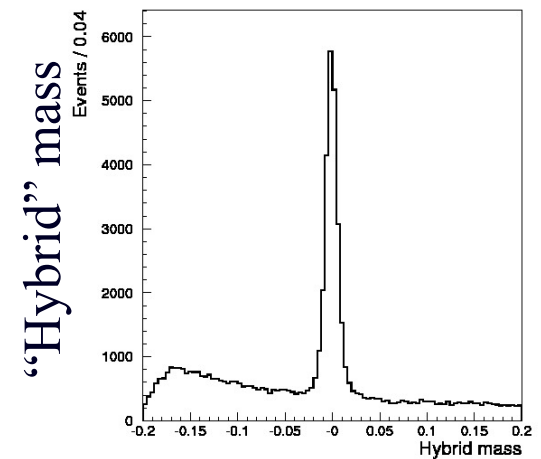


- **Hybrid mass analysis (H)**

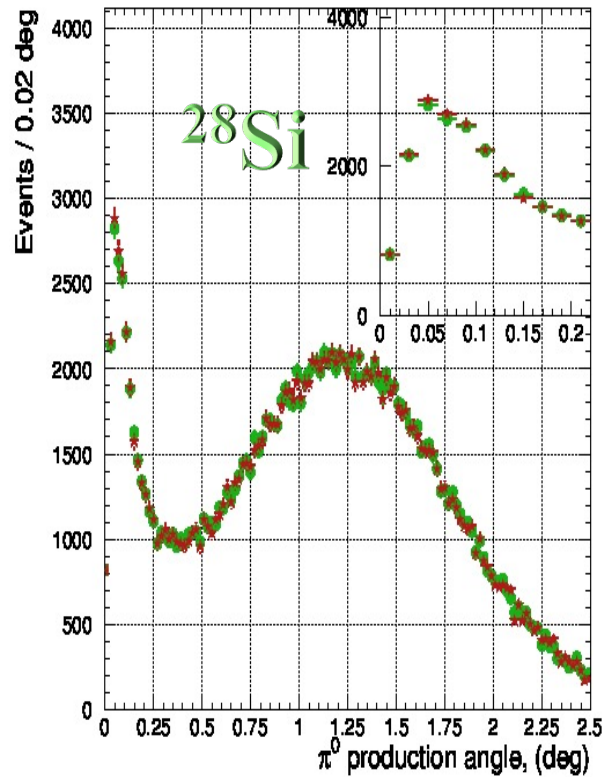
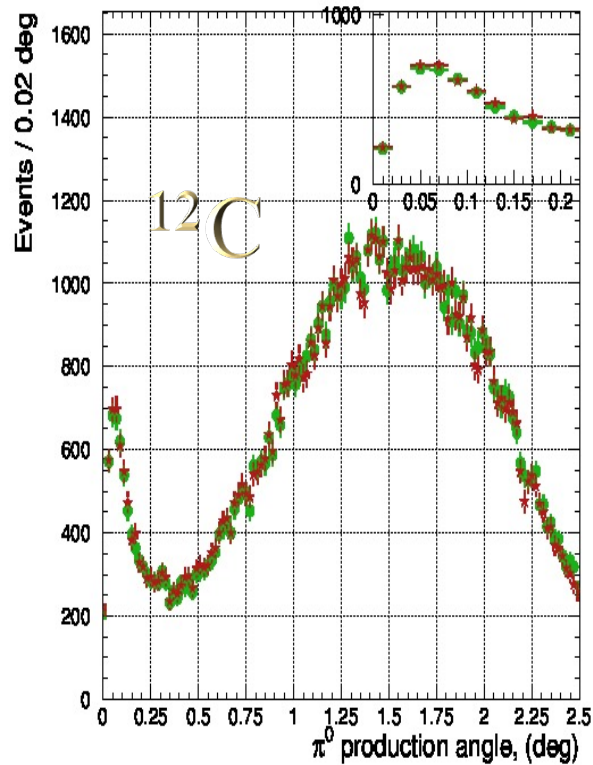
by Y. Zhang, Duke Univ.



H-analysis



# Comparison of yield extraction methods (PrimEx-II)

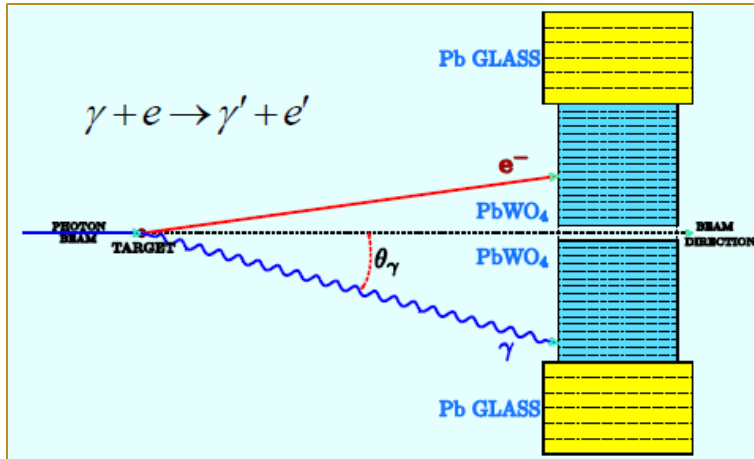


- ★ H-analysis
- C-analysis

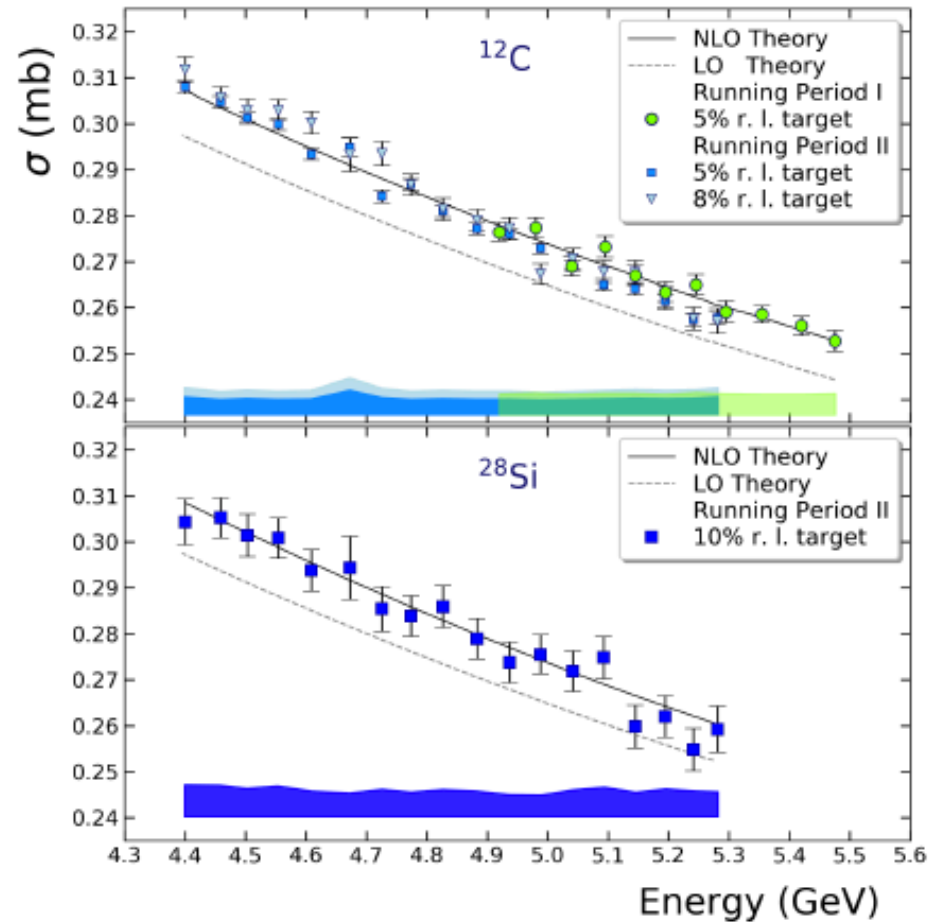
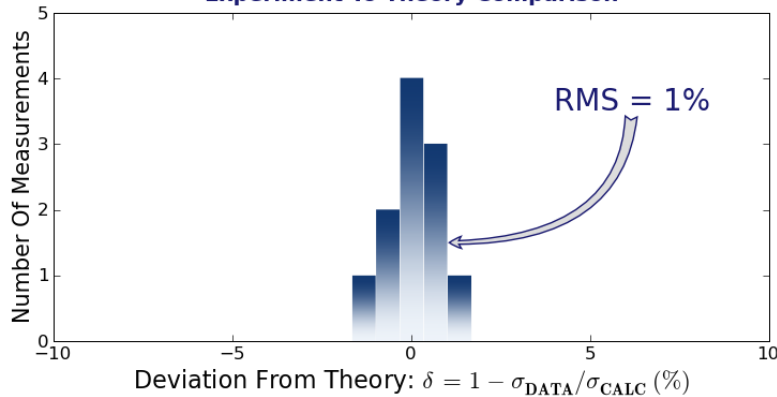
Method	$^{12}\text{C}$	$^{28}\text{Si}$
Hybrid mass	83,751	165,329
Constr. mass	84,015	165,736

Extracted  $\pi^0$  yield up to 2.5 deg.

# Verification of Overall Experimental Systematics with Compton Scattering

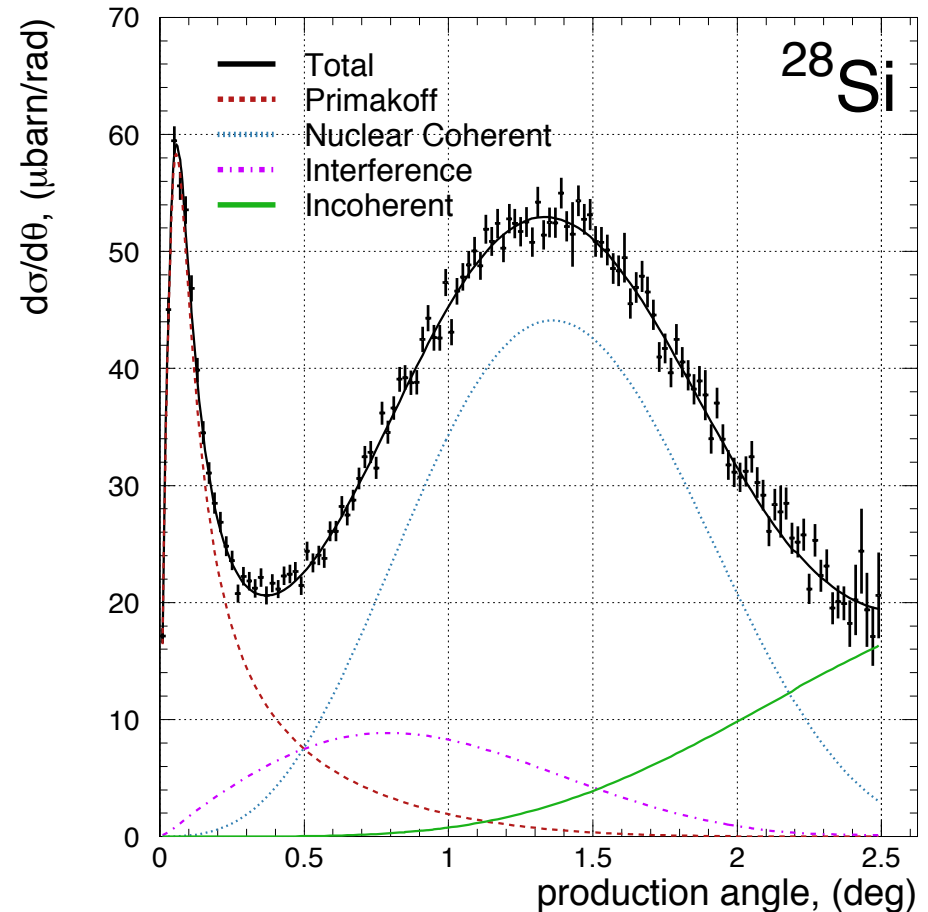
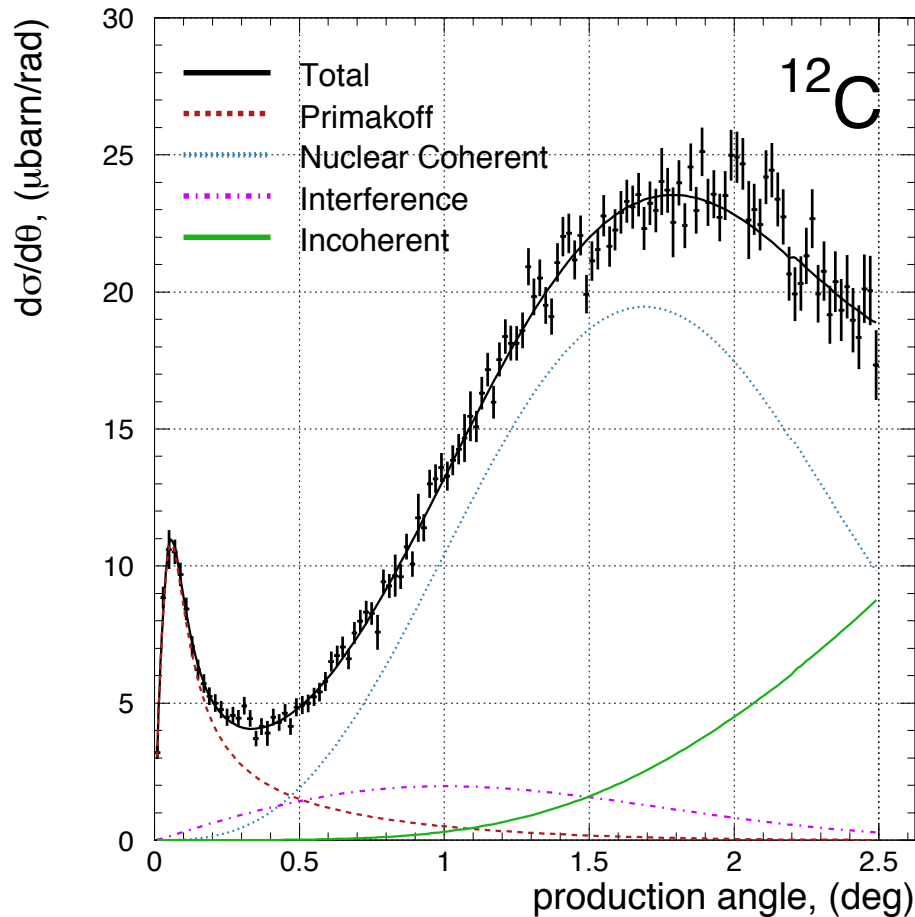
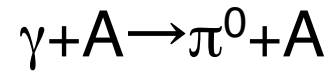


Experiment To Theory Comparison



Systematic uncertainties of measured cross section are controlled at 1.5%

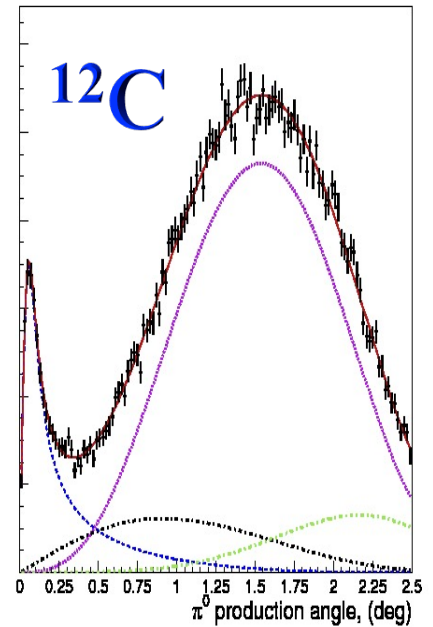
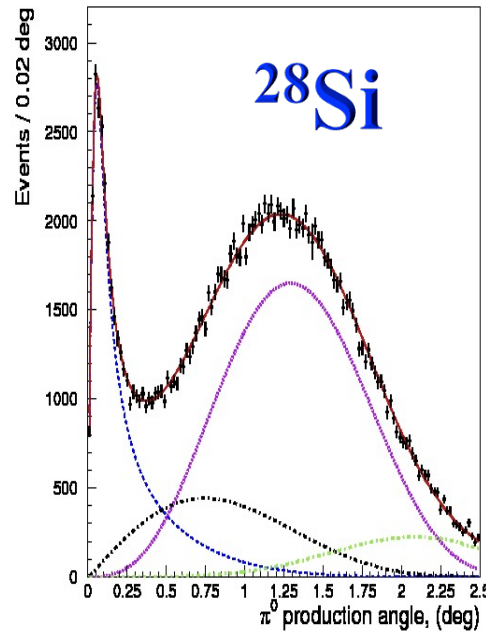
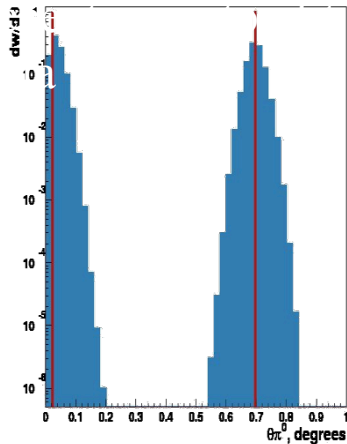
# Measured Differential Cross Sections



# Extraction of $\Gamma(\pi^0 \rightarrow \gamma\gamma)$

- Theoretical angular distributions smeared with experimental resolutions
- Fit the experimental yield (normalized with the luminosity and the detection efficiency) to extract  $\Gamma(\pi^0 \rightarrow \gamma\gamma)$

$$\left(\frac{d\sigma}{d\Omega}\right)_{Pr} = \boxed{\Gamma_{\gamma\gamma}} \frac{8\alpha Z^2}{m_\pi^3} \frac{\beta^3 E^4}{Q^4} |F_{em}(Q)|^2 \sin^2 \theta_\pi$$

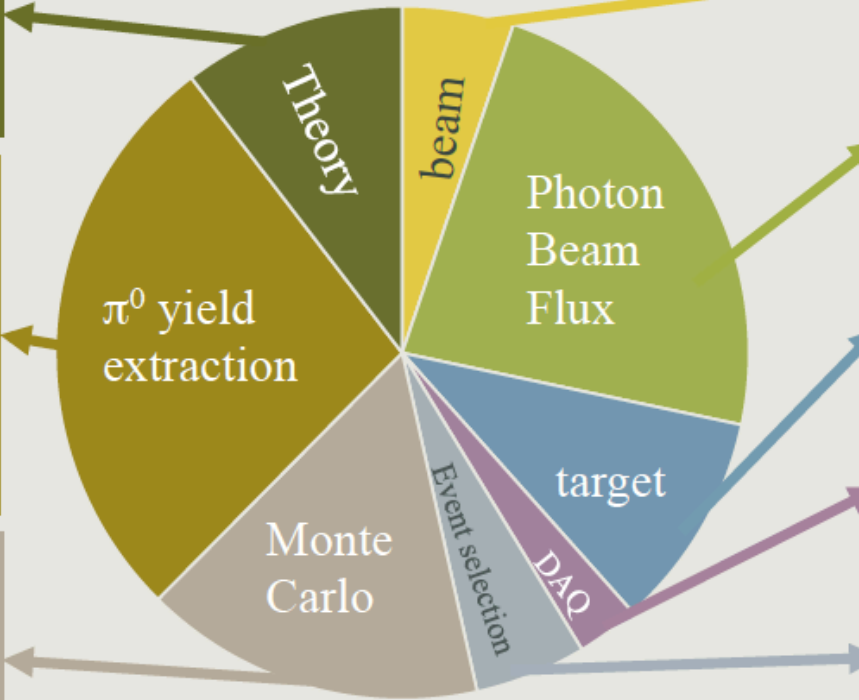


# PrimEx-II $\Gamma(\pi^0 \rightarrow \gamma\gamma)$ systematic breakdown for $^{28}\text{Si}$

$\pi\text{N}$ cross section	0.1%
Shadowing effect amplitude	0.31%
Nuclear coherent parameterization	0.08%
Incoherent model	0.08%
Non-zero spin admixture	$\leq 0.1\%$
Nuclear strong vs EM radius	0.20%
Total	0.40%

Background shape	0.4%
Fitting range	0.4%
Empty target subtraction	0.2%
Fit parameter uncertainty	0.5%
Signal accounting	0.55%
Omega/rho background subtraction	0.09%
Bin migration at zero angle	0.2%
$dN/d\theta$ binning $0.01^\circ, 0.02^\circ, 0.03^\circ$	0.12%
Extraction from MC test	0.2%
Total	0.93%

Target absorption	0.24%
Pi0 angular resolution	0.17%
Pi0 two gamma decay branching	0.034%
Calorimeter geometry	0.05%
Calorimeter energy response	0.45%
Limited statistics	0.02%
Total	0.54%



Energy	0.14%
Position	0.05%
Slope	0.09%
Width	0.12%
Total	0.24%

Absolute tagging ratio	0.37%
Electron counting	0.55%
Beam collimation	0.18%
Relative tagging ratio	0.4%
Total	0.80%

Density	0.35%
Thickness	0.03%
Purity	$< 0.01\%$
Total	0.35%

Trigger efficiency	$< 0.1\%$
ADC errors	$< 0.1\%$
Dead channels	$< 0.1\%$
Total	0.1%

Gamma energy cut	0.1%
Pion energy cut	$< 0.1\%$
Time window	0.05%
Wrong beam candidate	0.10%
Total	0.18%

from I. Larin

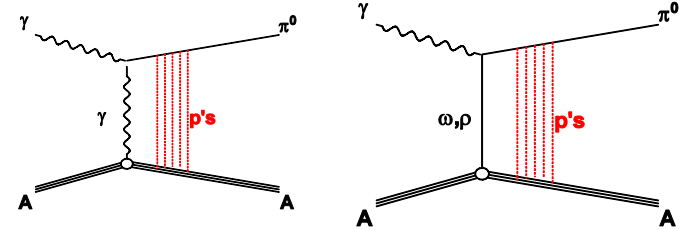
# Theoretical Calculations

## Coherent Production $\gamma + A \rightarrow \pi^0 + A$

□ 1964, G. Morpurgo, *Neuovo Cimento*, 31, 569

- ✓ Strong absorption for outgoing pion in uniform nuclear density

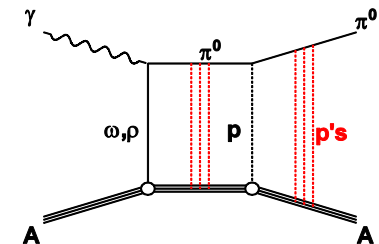
Used for Tomsk and DESY Primakoff Exp.



□ 1972, G. Faldt, *Nucl. Phys.* B43, 591

- ✓ Strong absorption in a nucleus for both incident and produced particles
- ✓ final state pion re-scattering in nucleus
- ✓ corrections for light nuclei

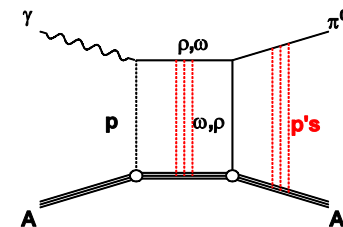
Used for Cornell exp.



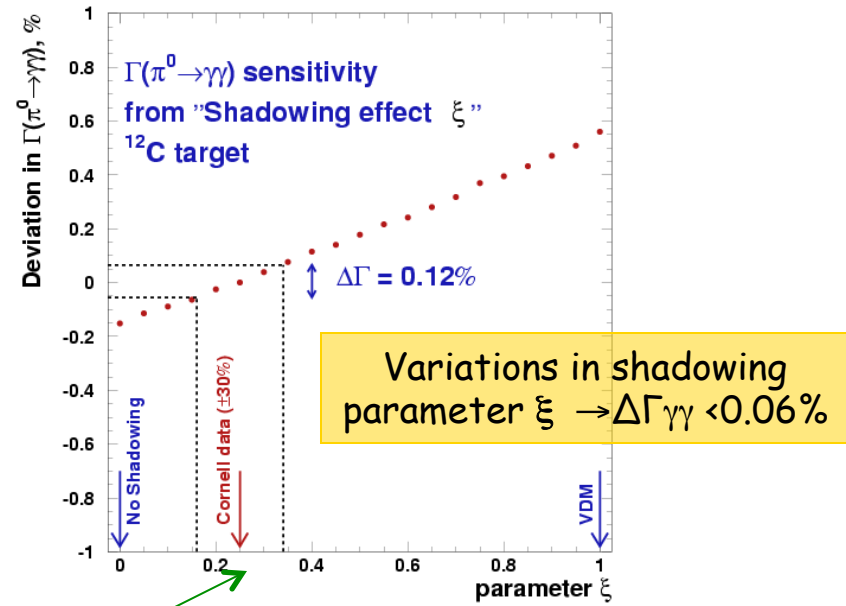
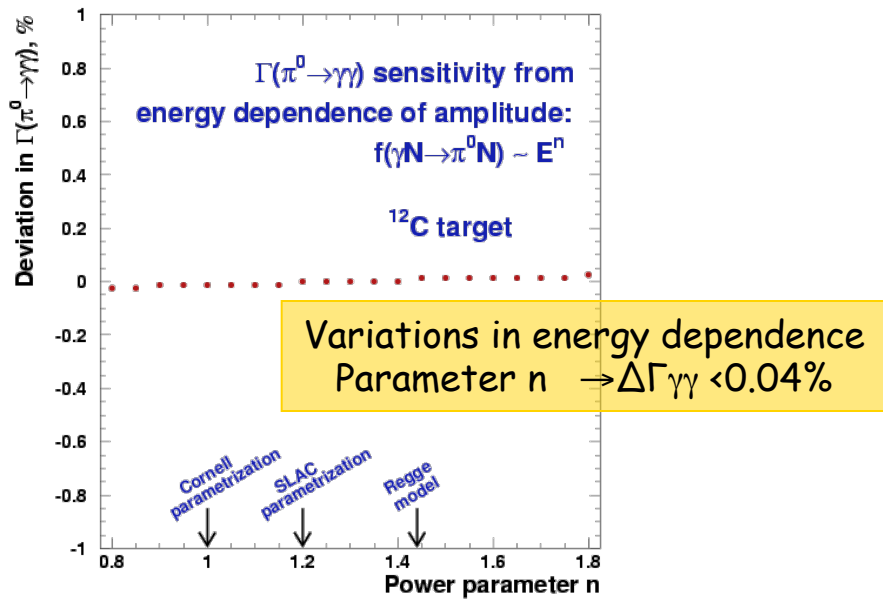
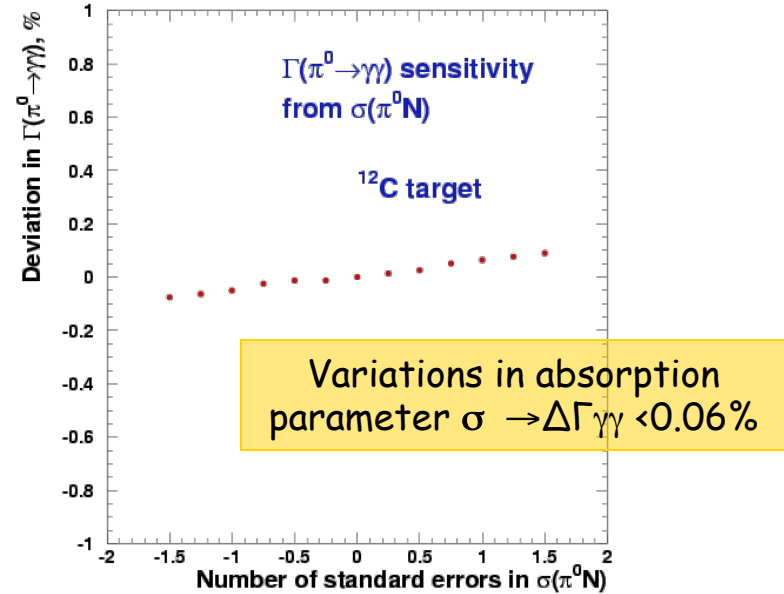
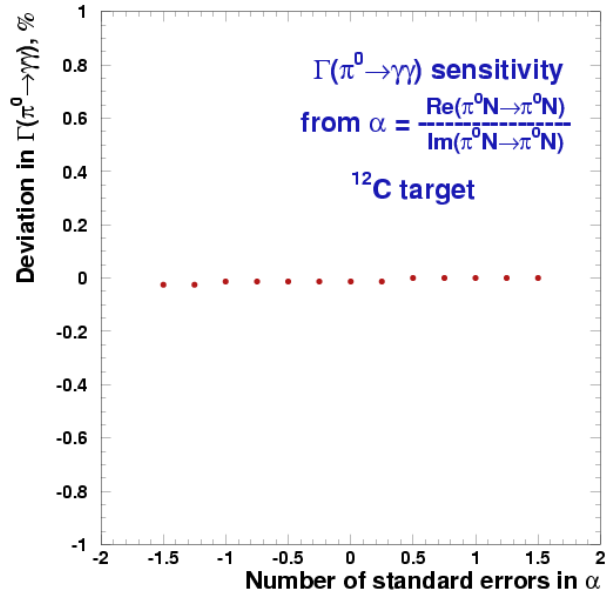
□ 2009, S. Gevorkyan *et. al.*, *Phys.Rev.* C80, 055201, PrimEx note #85

- ✓ Strong absorption in a nucleus for initial and final states
- ✓ the final state pion re-scattering in nucleus
- ✓ corrections for light nuclei
- ✓ photon shadowing effect
- ✓ Pion form factor

Used for PrmEx



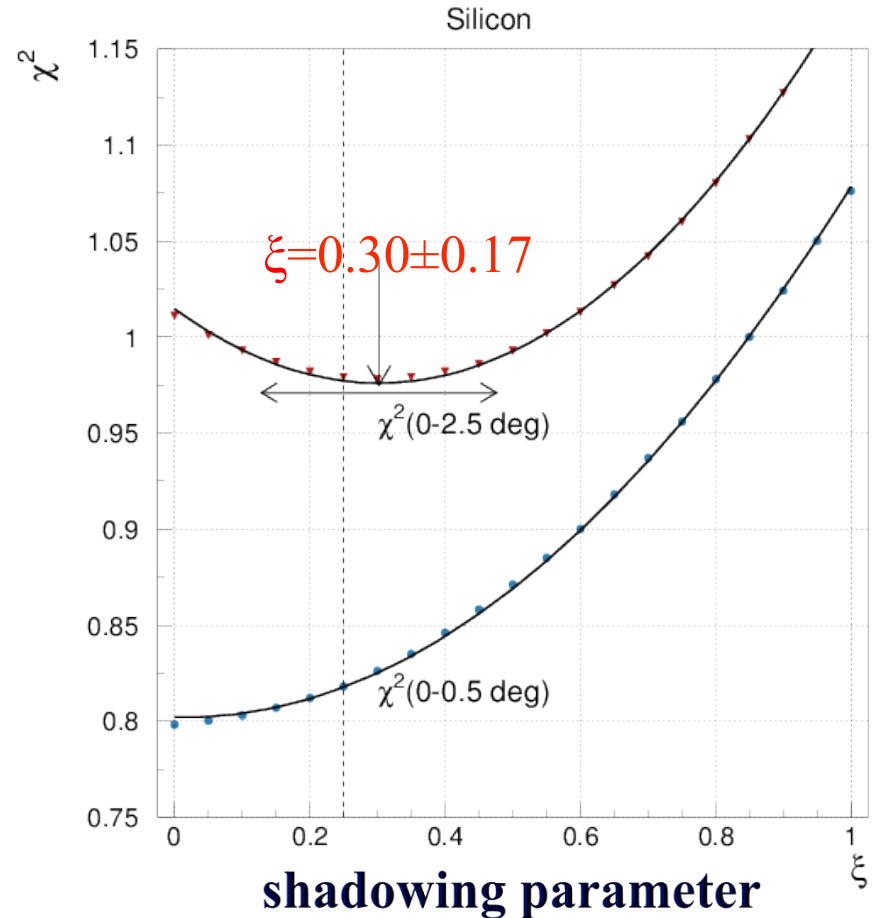
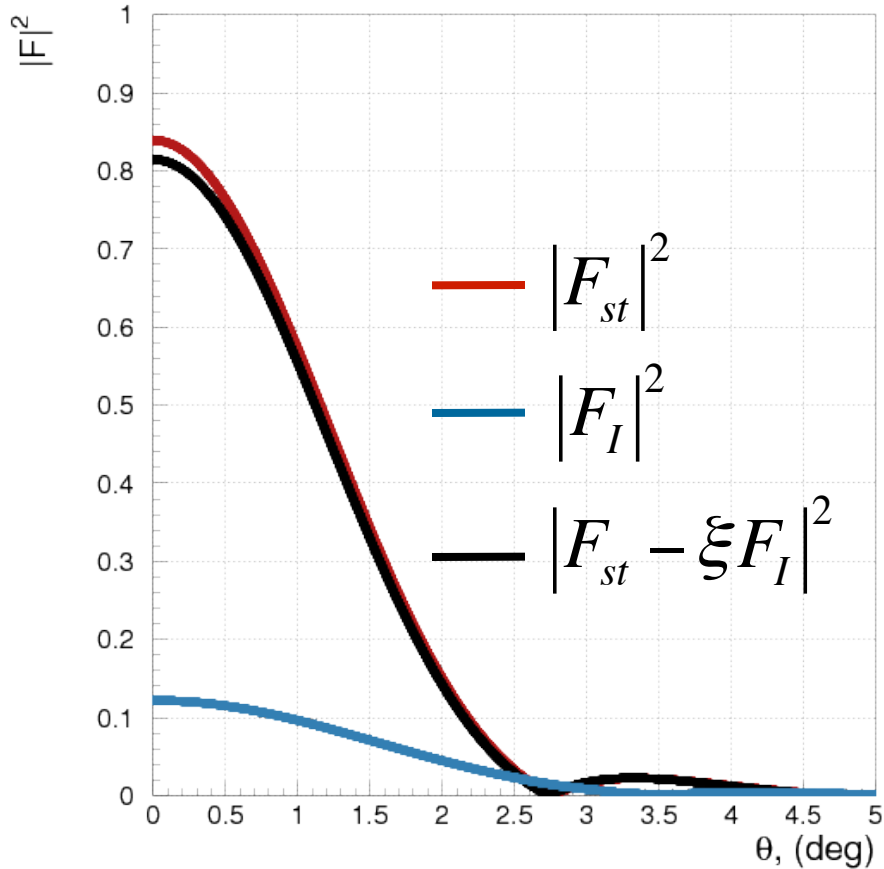
# $\Gamma(\pi^0 \rightarrow \gamma\gamma)$ dependence on model parameters



*Phys. Rev. Lett.* 28, 1344 (1972)



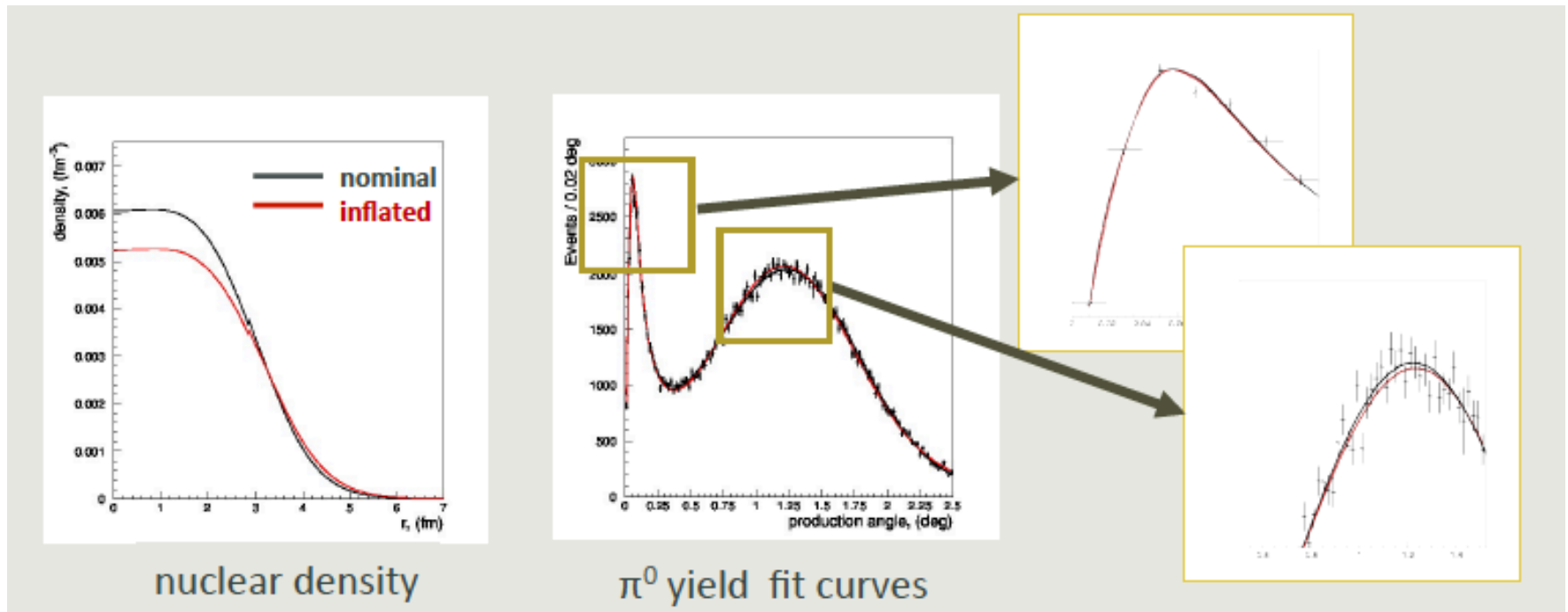
# Shadowing parameter from PrimEx-II Data



The measured value of  $\xi=0.25^*$  from the previous experiment is used in PrimEx analysis

\* *W. Meyer et al., Phys. Rev. Lett. 28, 1344 (1972);*  
*A. M. Boyarski et al., Phys. Rev. Lett. 23, 1343 (1969)*

# Effects of nuclear density models



Three nuclear density models are compared

- Harmonic Oscillator,
- 3 parameter Fermi,
- Fourier-Bessel,

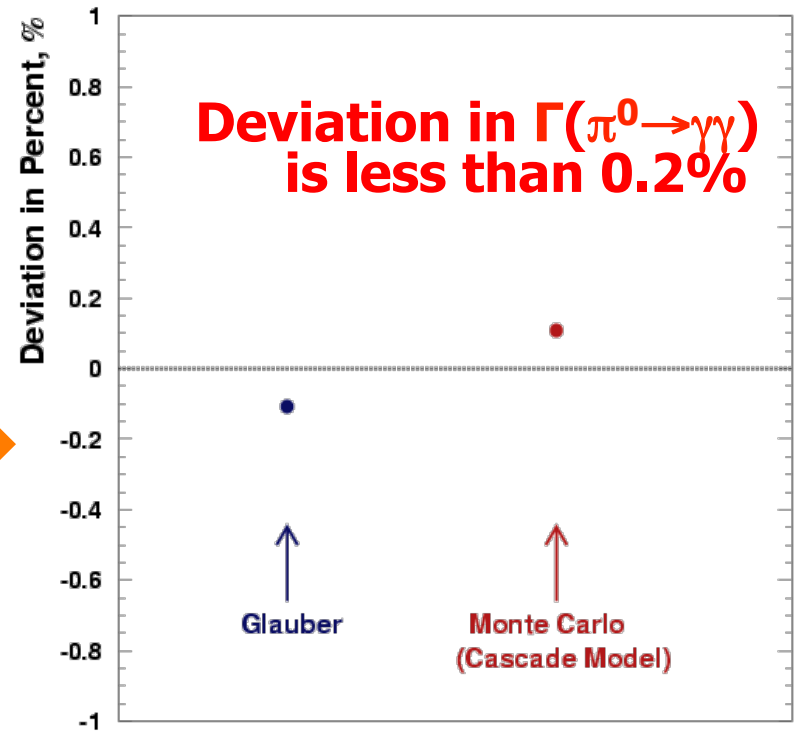
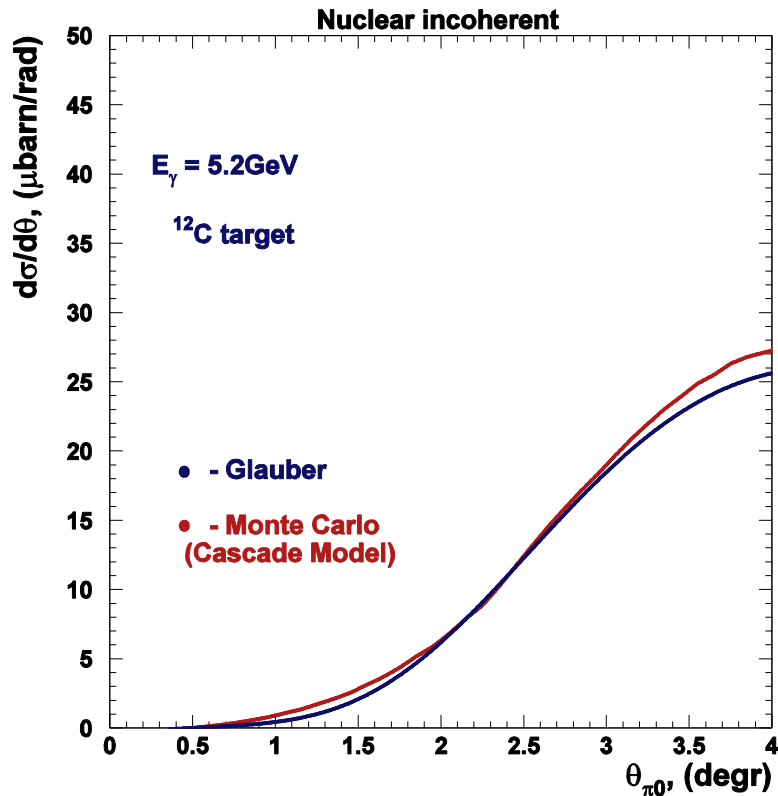
← Best for describing PrimEx data

# Theoretical Calculation (cont.)

Incoherent Production  $\gamma+A\rightarrow\pi^0+A'$

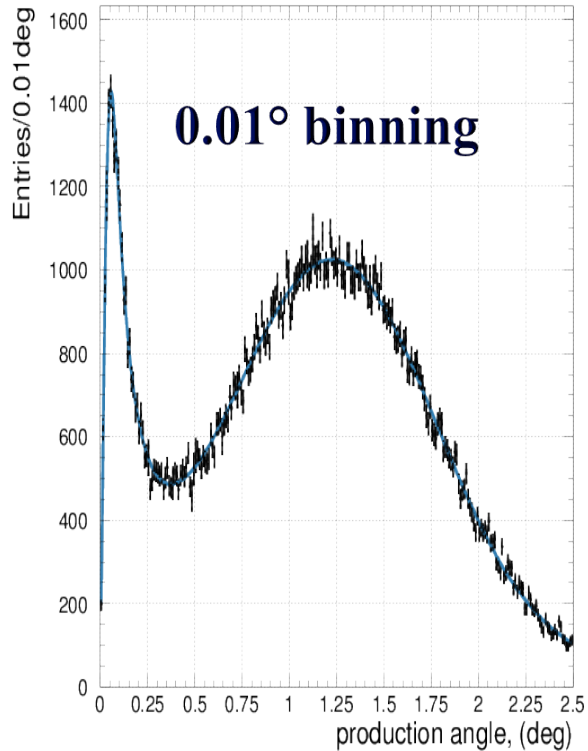
Two independent approaches:

- Glauber theory, *Phys.Part.Nucl.Lett.*,9,3 (2012)
- Cascade Model, *Phys.Rev.Lett.*,101, 012301 (2008)

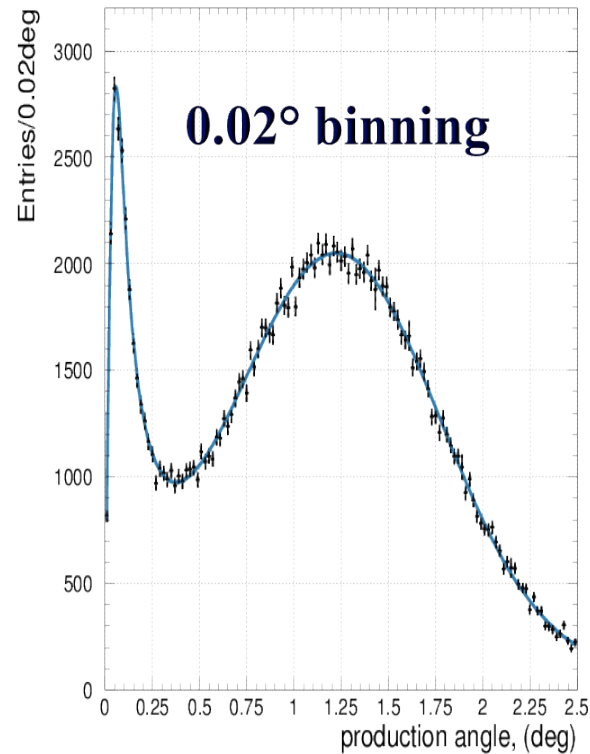


# Uncertainty due to angular binning

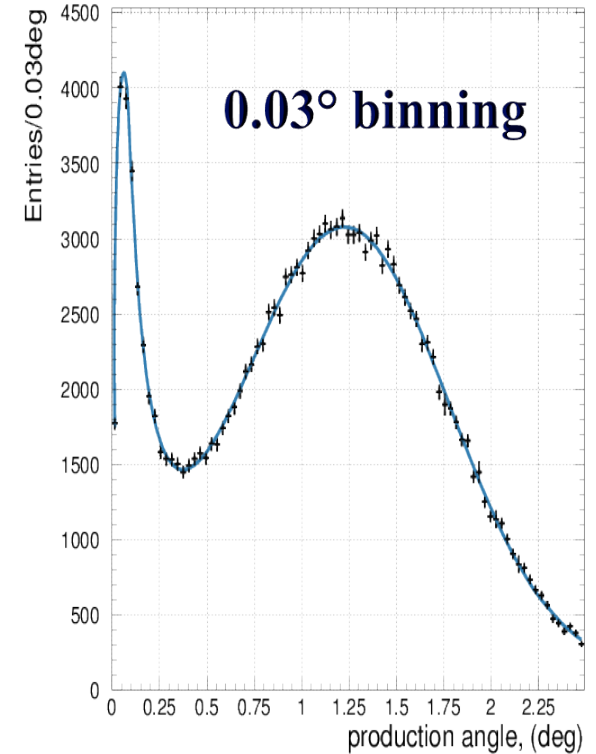
**$^{28}\text{Si}$**  target



$$\Gamma = 7.769 \pm 0.066 \text{ eV}$$
$$\chi^2/\text{Ndf} = 0.956$$



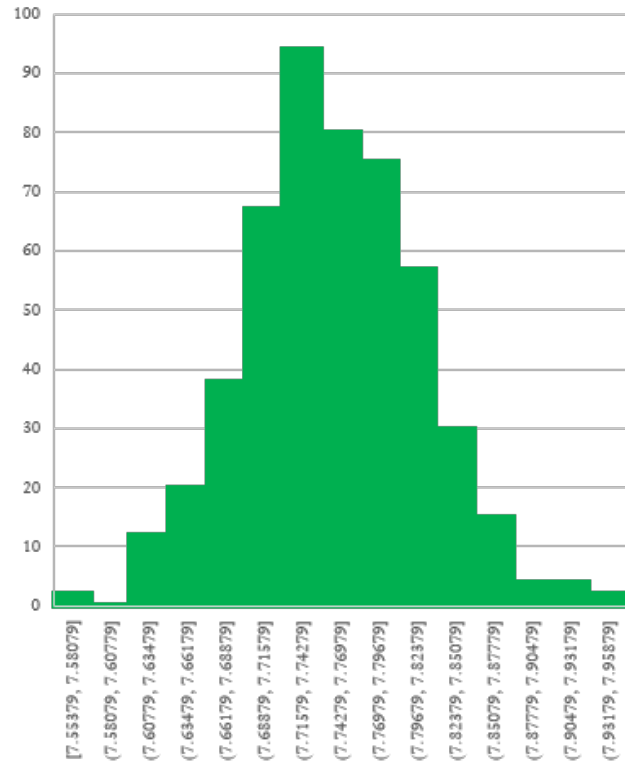
$$\Gamma = 7.769 \pm 0.064 \text{ eV}$$
$$\chi^2/\text{Ndf} = 1.225$$



$$\Gamma = 7.776 \pm 0.064 \text{ eV}$$
$$\chi^2/\text{Ndf} = 1.052$$

# Uncertainty due to fitting procedure

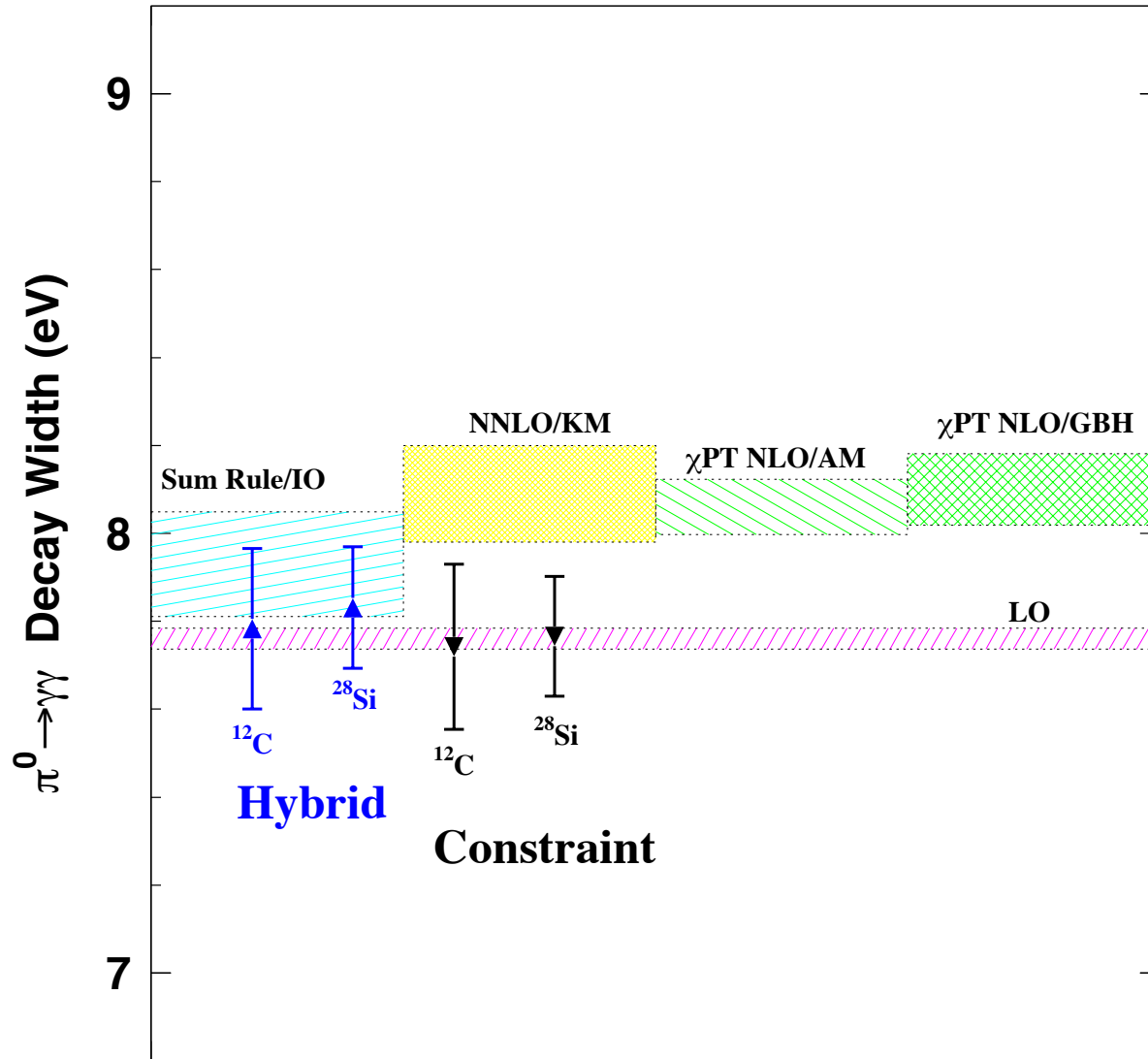
- 500 sets of Monte-Carlo data sample with predefined parameters ( $\Gamma$ , nuclear coherent, interference, and incoherent amplitudes)
- Each MC data set has the same statistics as the experimental data
- Add the background from experimental data
- $\Gamma(\pi^0 \rightarrow \gamma\gamma)$  is extracted by fitting these MC samples



Uncertainty due to fitting procedure:

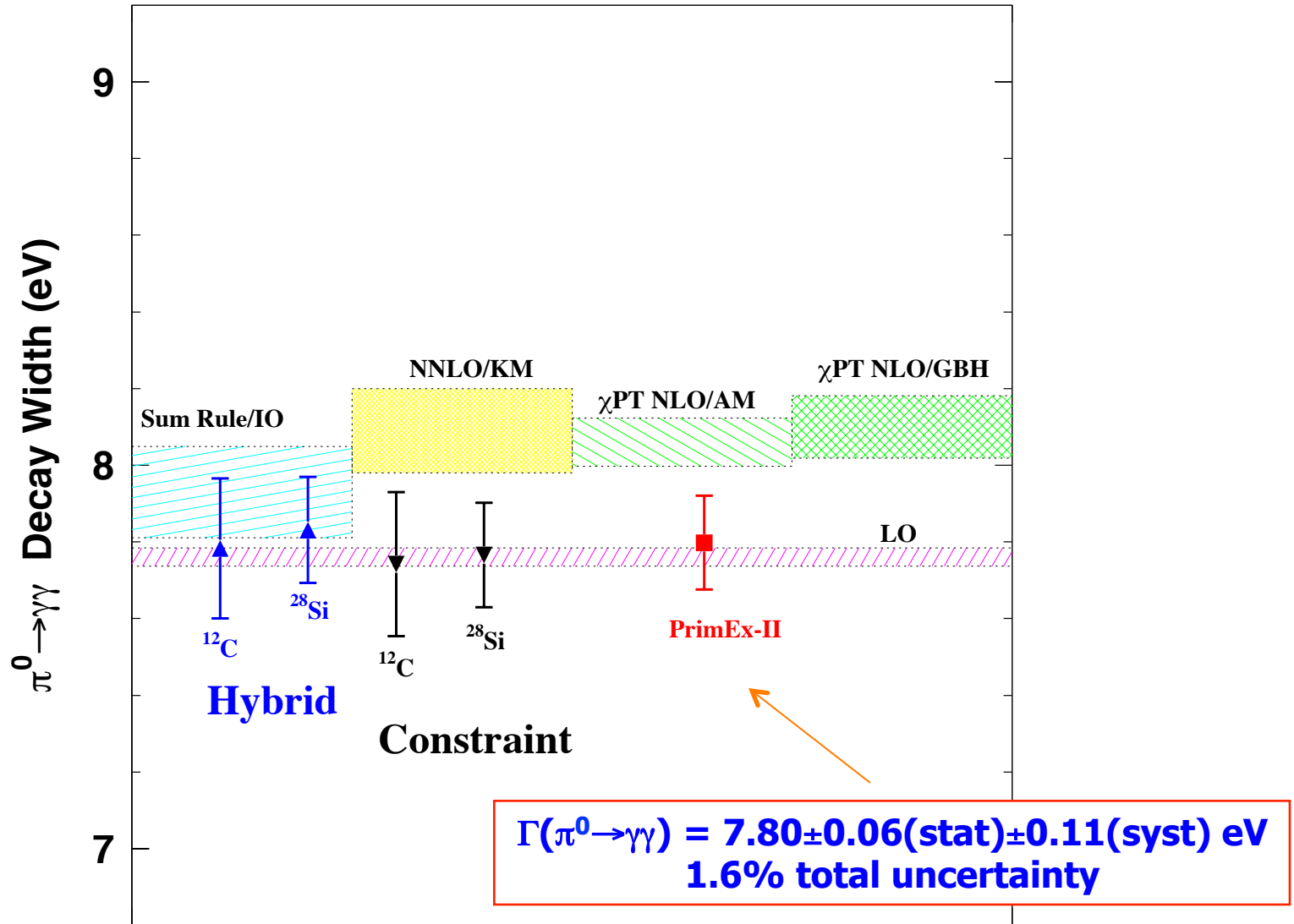
Analysis	C-analysis	H-analysis
Uncertainty	0.2%	0.65%

# PrimEx-II Analyses



Analysis Results

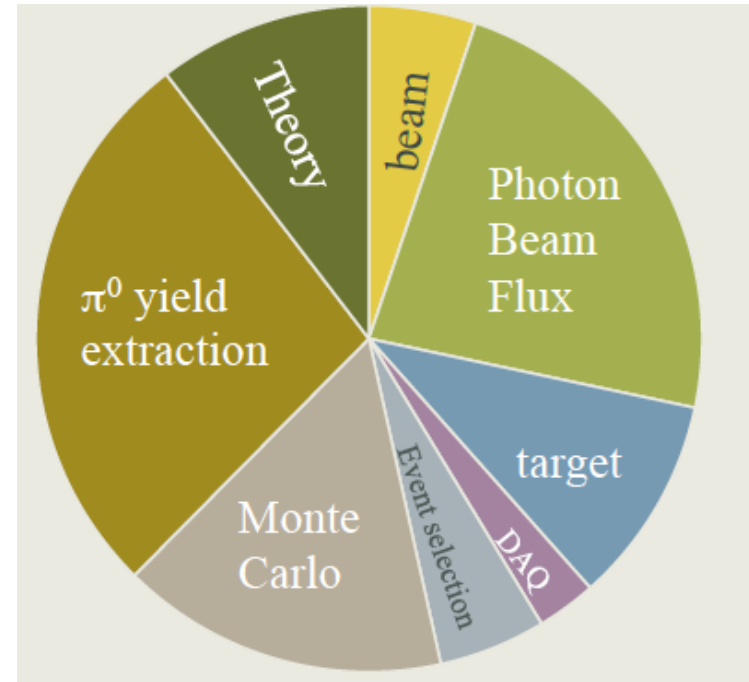
# PrimEx-II Result



Analysis Results

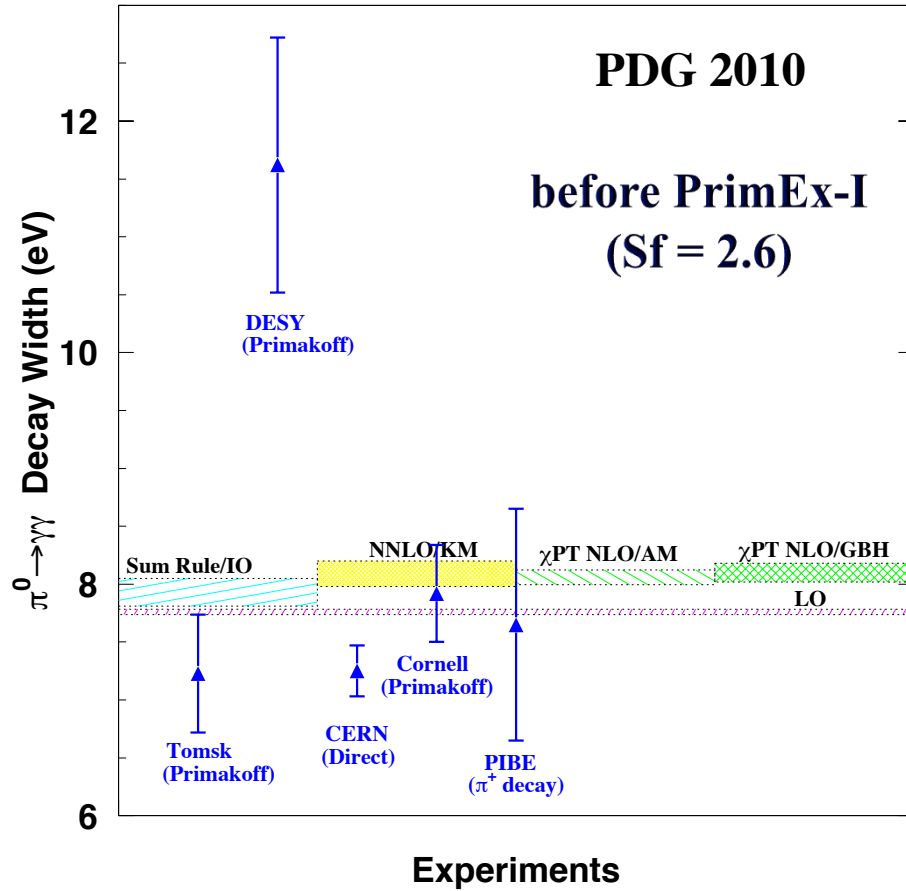
# Uncertainties of $\Gamma(\pi^0 \rightarrow \gamma\gamma)$

Item	PrimEx-II
Beam parameters	0.2%
Photon flux	0.8%
Target	0.3%
DAQ	0.1%
Event selection	0.2%
Monte-Carlo simulation	0.6%
Yield extraction	1.0%
Photoproduction theory parameters	0.4%
<b>Systematics</b>	<b>1.5%</b>
Statistical	0.7%
<b>Total</b>	<b>1.6%</b>

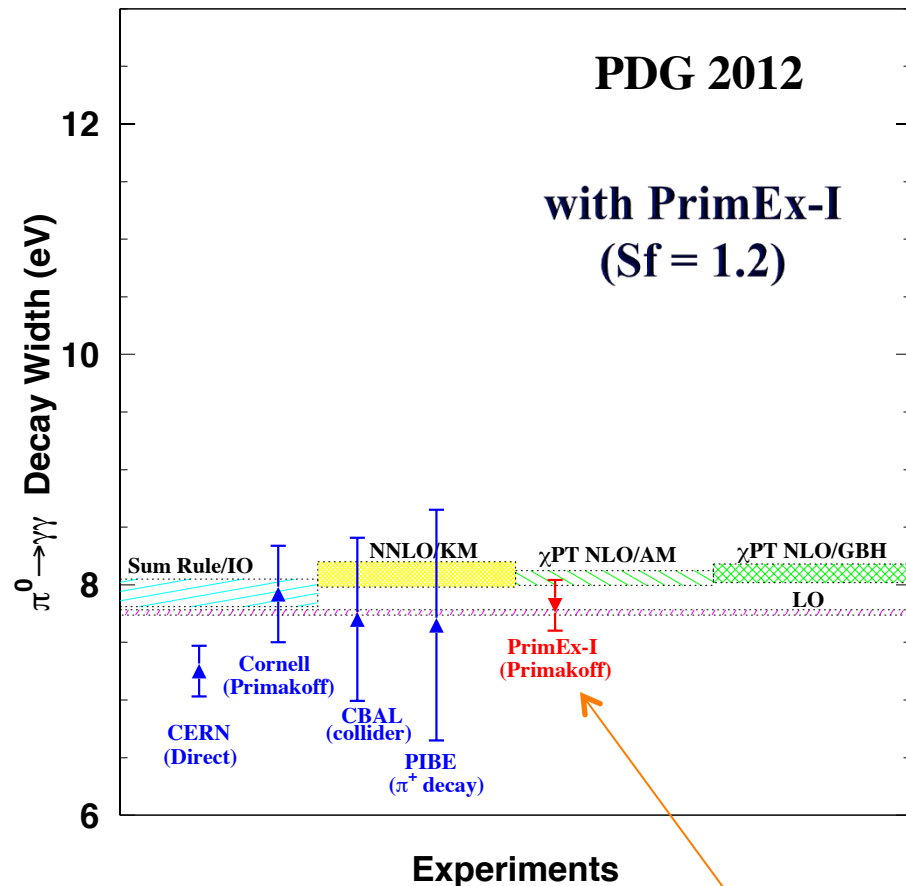
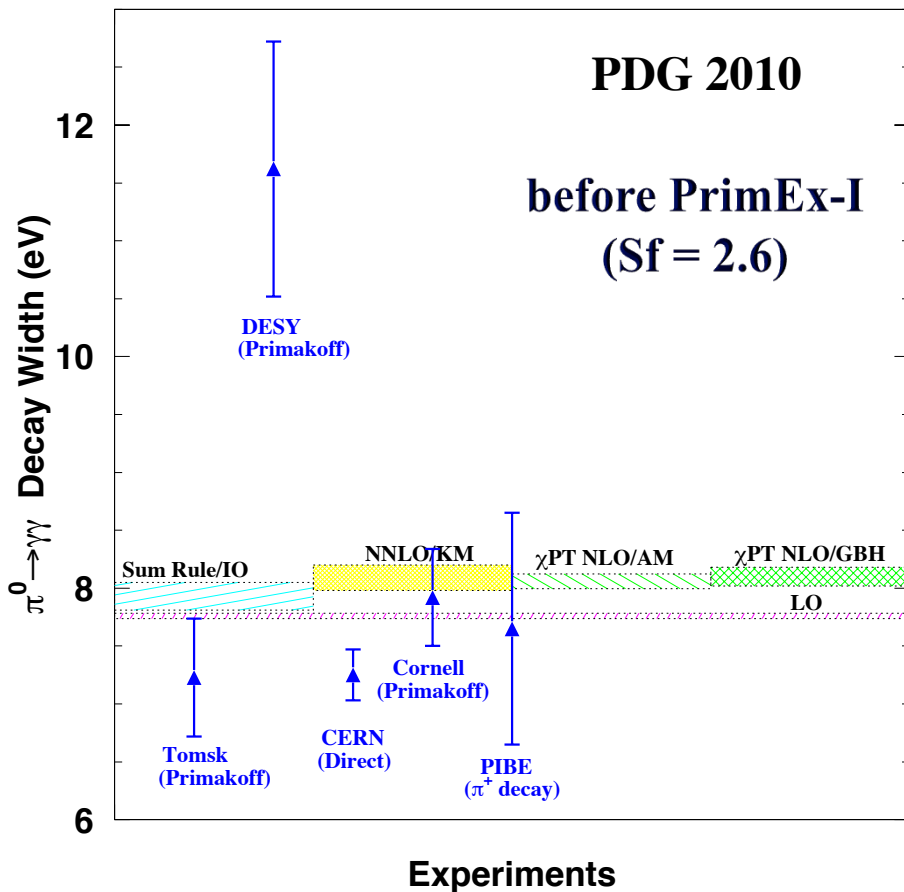




# Impact of PrimEx result



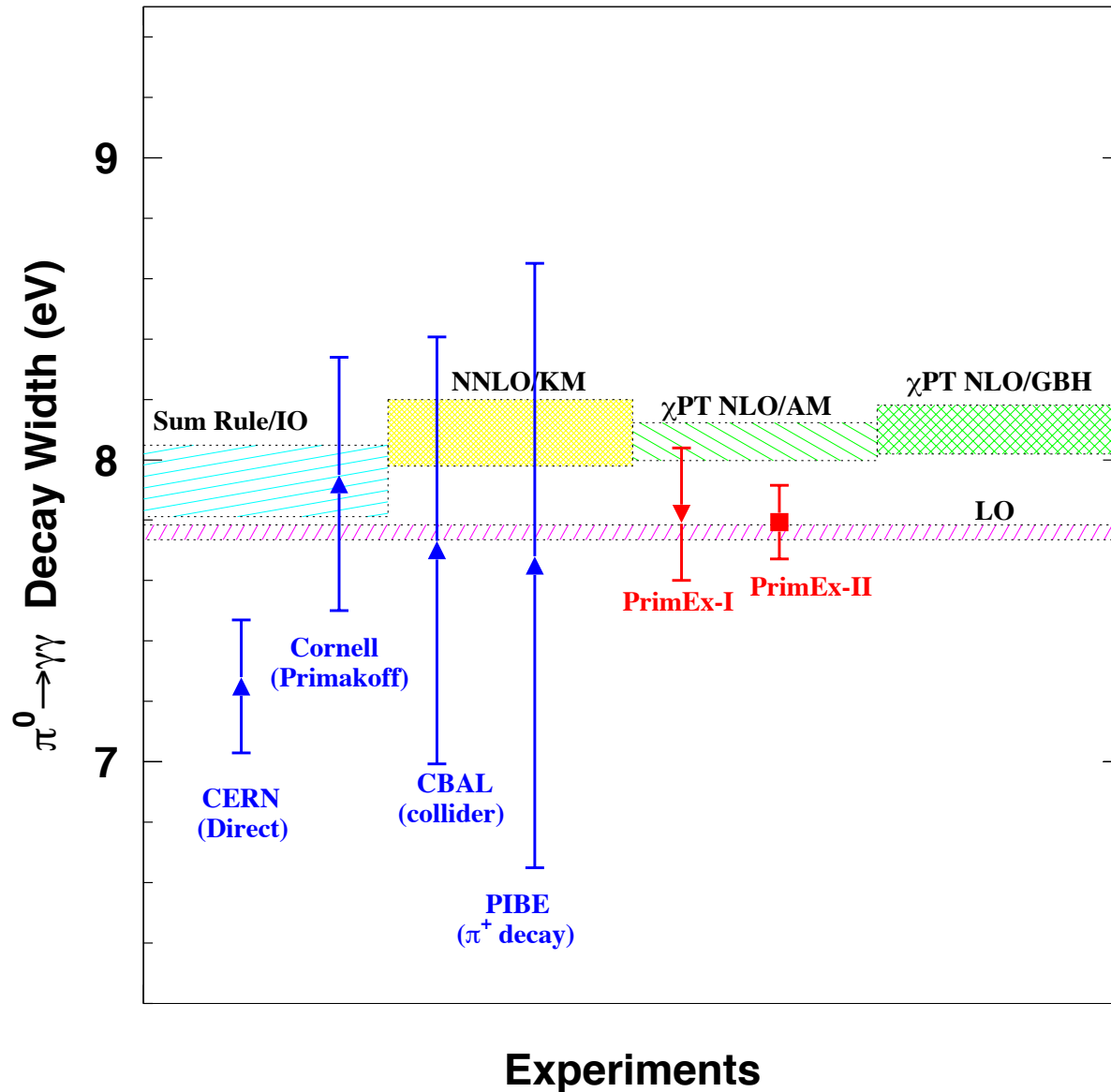
# Impact of PrimEx result



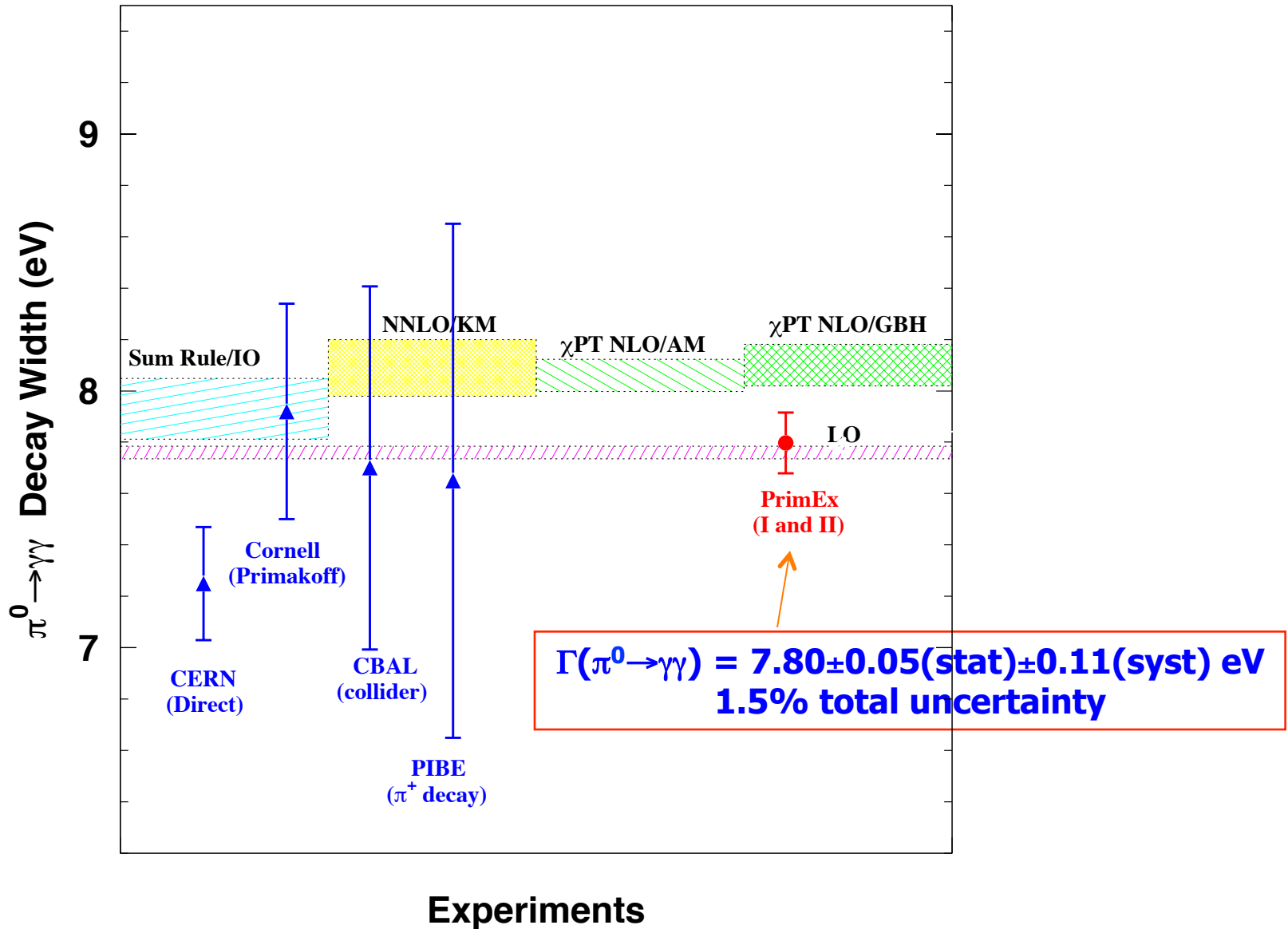
$\Gamma(\pi^0 \rightarrow \gamma\gamma) = 7.82 \pm 0.14(\text{stat}) \pm 0.17(\text{syst}) \text{ eV}$   
2.8% total uncertainty

PRL 106, 162303 (2011)

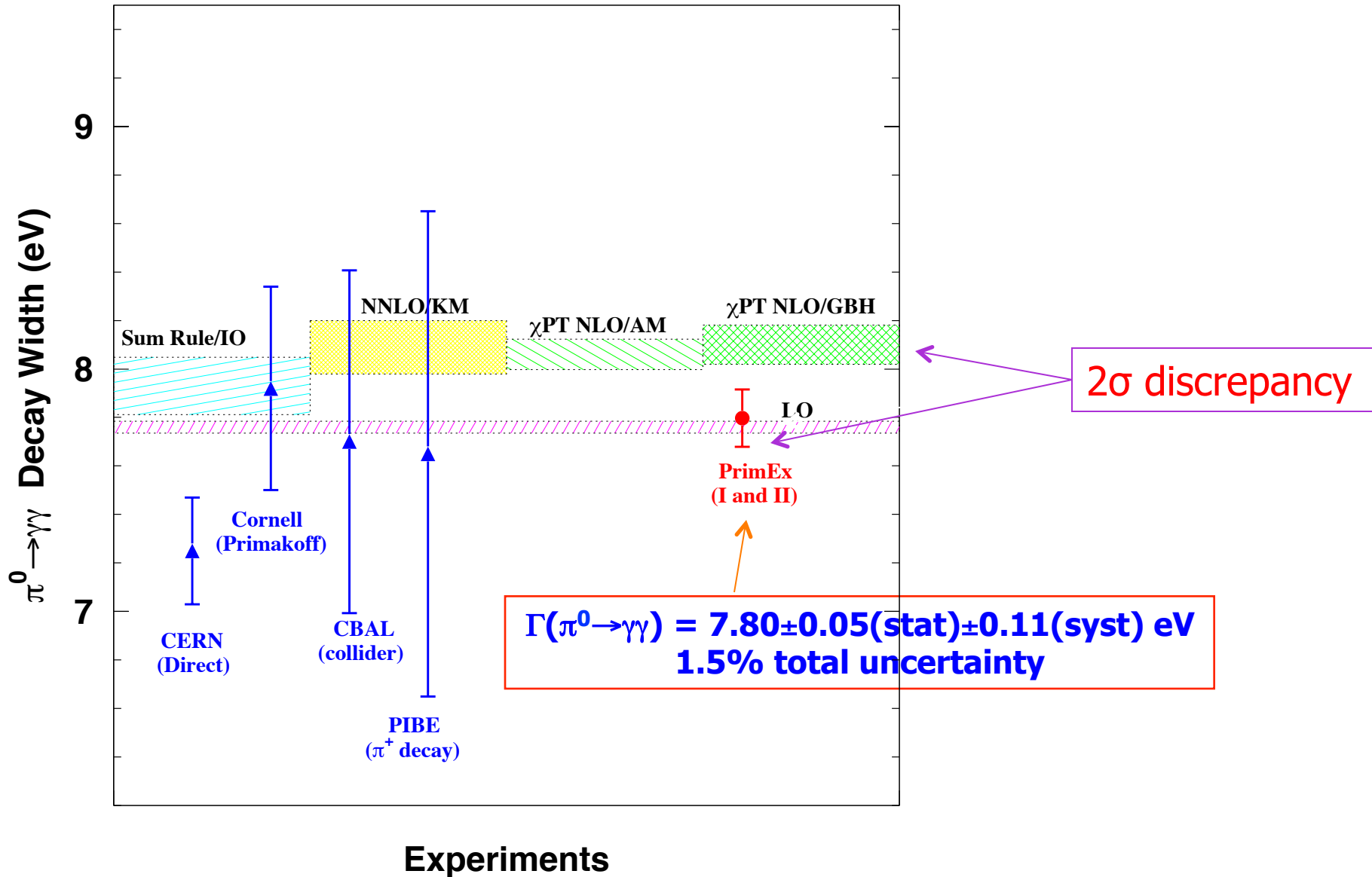
# Impact of PrimEx Result Cont.



# PrimEx Final Result



# PrimEx Final Result

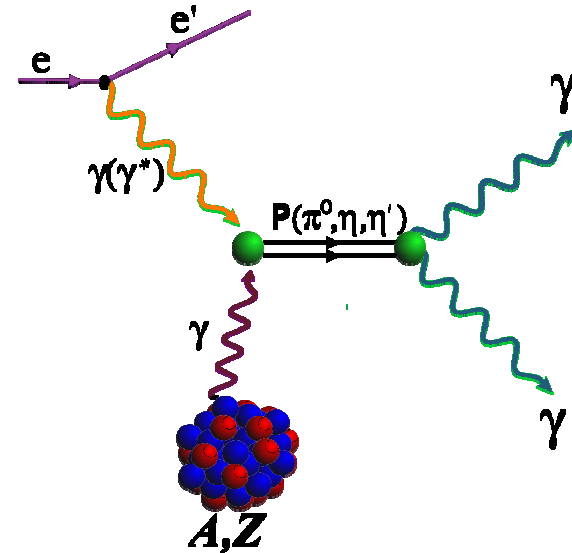


# Summary

- ❑ The PrimEx collaboration developed a state-of-the-art experimental setup to perform a high precision measurement of  $\Gamma(\pi^0 \rightarrow \gamma\gamma)$  via the Primakoff effect.
- ❑ The final PrimEx result is:  
$$\Gamma(\pi^0 \rightarrow \gamma\gamma) = 7.80 \pm 0.05 \text{ (stat.)} \pm 0.11 \text{ (syst.) eV} \quad (1.5\% \text{ total})$$
- ❑ Our result is consistent with the leading order chiral anomaly calculation and  $\sim 2\sigma$  below the high order QCD predictions.

# Primakoff Program at Jlab

Precision measurements of electromagnetic properties of  $\pi^0$ ,  $\eta$ ,  $\eta'$  via Primakoff effect.



## a) Two-Photon Decay Widths:

- 1)  $\Gamma(\pi^0 \rightarrow \gamma\gamma)$  @ 6 GeV
- 2)  $\Gamma(\eta \rightarrow \gamma\gamma)$
- 3)  $\Gamma(\eta' \rightarrow \gamma\gamma)$

### Input to Physics:

- precision tests of Chiral symmetry and anomalies
- determination of light quark mass ratio
- $\eta$ - $\eta'$  mixing angle

## b) Transition Form Factors at low

$Q^2$  (0.001-0.5  $\text{GeV}^2/c^2$ ):

$F(\gamma\gamma^* \rightarrow \pi^0)$ ,  $F(\gamma\gamma^* \rightarrow \eta)$ ,  $F(\gamma\gamma^* \rightarrow \eta')$

### Input to Physics:

- $\pi^0, \eta$  and  $\eta'$  electromagnetic interaction radii
- is the  $\eta'$  an approximate Goldstone boson?
- inputs to  $a_\mu$  (HLbL) calculations

# The $\pi^0$ Meson

- ◆  $\pi^0$  is the lightest hadron:  
 $m_\pi = 134.9770 \pm 0.0005 \text{ MeV}$ ,  $\pi^0 = (u\bar{u} - d\bar{d}) / \sqrt{2}$
- ◆  $\pi^0$  is unstable:  
 $\pi^0 \rightarrow \gamma\gamma$ ,  $\text{BR}(\pi^0 \rightarrow \gamma\gamma) = (98.823 \pm 0.034)\%$
- ◆ Lifetime and radiative decay width  $\Gamma(\pi^0 \rightarrow \gamma\gamma)$ :  
 $\tau = \text{B.R.}(\pi^0 \rightarrow \gamma\gamma) / \Gamma(\pi^0 \rightarrow \gamma\gamma)$   
 $\sim (8.52 \pm 0.18) \times 10^{-17} \text{ s}$
- ◆  $\pi^0 \rightarrow \gamma\gamma$  is associated to two fundamental symmetry properties of QCD: chiral symmetry and anomaly.



# Extracted $\Gamma(\pi^0 \rightarrow \gamma\gamma)$ vs. Nuclear Matter Radius

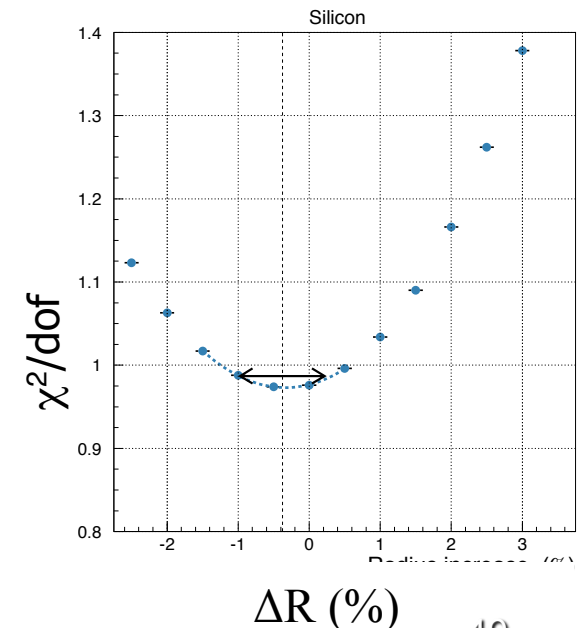
Slope $a_p$ (fm <sup>2</sup> )	Target	Radius $\Delta R^{**}$	$\Gamma(\pi^0 \rightarrow \gamma\gamma)$ (eV)
0.4*	<sup>28</sup> Si	-0.33% ± 0.6% (stat)	7.78 (±0.17% sys)
	<sup>12</sup> C	-1.4% ± 1.8% (stat)	7.74 (±0.52% sys)
0.24	<sup>28</sup> Si	2.2% ± 0.4% (stat)	7.77 (±0.14% sys)
	<sup>12</sup> C	2.5% ± 1.4% (stat)	7.75 (±0.39% sys)

$$\frac{d\sigma(\gamma N \rightarrow \pi^0 N)}{dt} = |f_N(0)|^2 e^{-a_p q^2}$$

Extracted  $\Gamma(\pi^0 \rightarrow \gamma\gamma)$  is not sensitive to parameters of nuclear radius and slope of  $\sigma(\gamma N \rightarrow \pi^0 N)$

\* ArXiv:1806.08414; J.Eur.Phys., A41,71

\*\* Changes of matter radius relative to the nuclear charge radius listed in Atom.Nucl.Tab.(1987) from the electron scattering exp.



# Challenges to theory colleagues

1. Calculation from Light-Front Holography
2. Lattice calculation
3. Exam the input parameters in ChPT calculations
  - $F_\pi$
  - $m_u - m_d$
  - Meson mixing
  - LEC's
4. Other possibilities?

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1. Calculation from Light-Front Holography
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  - $F_\pi$  ← Possible non-standard electroweak coupling contribution in  $\pi^+ \rightarrow \nu_\mu \mu^+$ ? JHEP 01 (2008) 015
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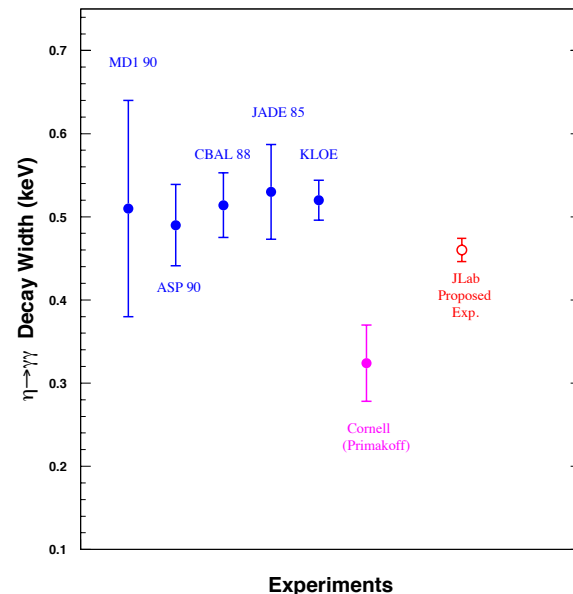
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- $m_u - m_d$

- Meson mixing

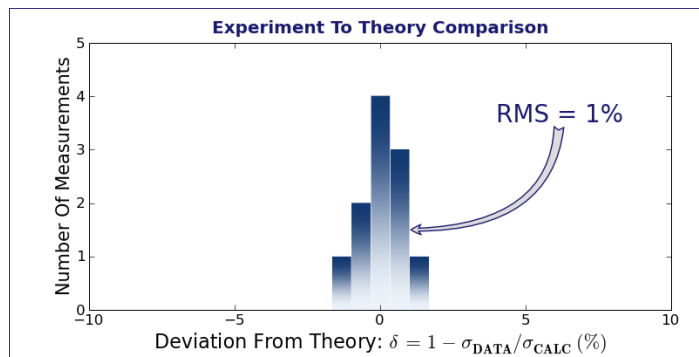
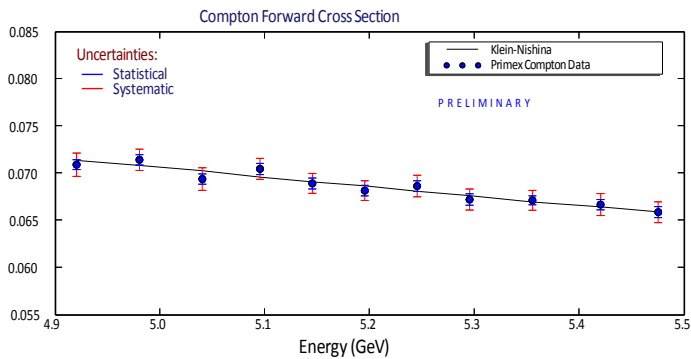
- LEC's

4. Other possibilities?

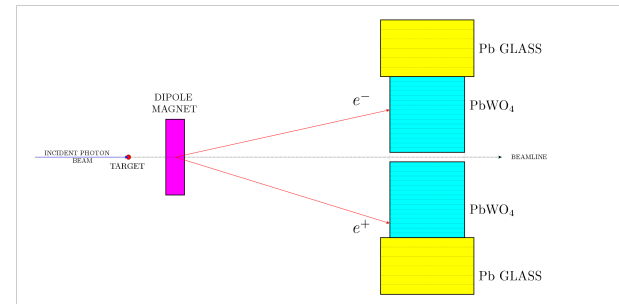
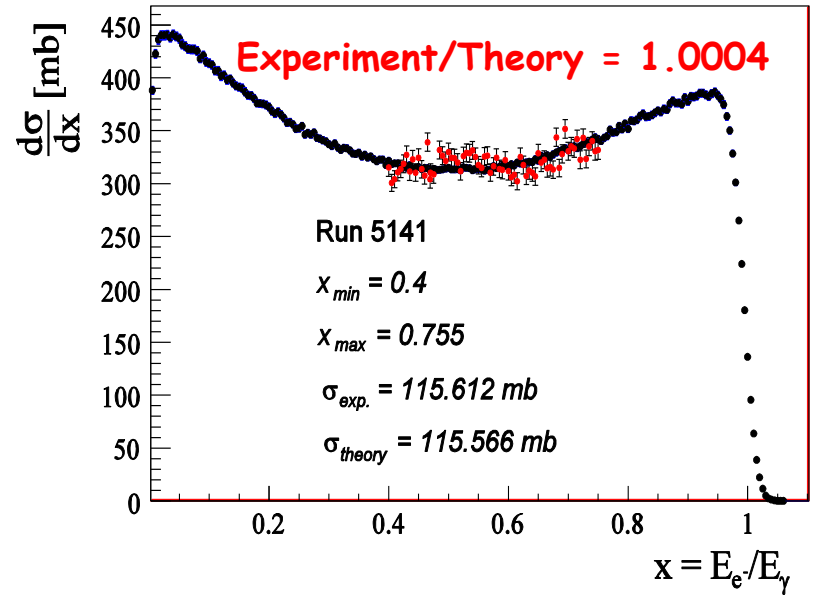


# Verification of Overall Systematical Uncertainties

☐  $\gamma + e \rightarrow \gamma + e$  Compton cross section measurement



☐  $e^+e^-$  pair-production cross section measurement:



Systematic uncertainties on cross section are controlled better than 1.5%

# Low-Energy QCD Symmetries and Light Mesons

- QCD Lagrangian in Chiral limit ( $m_q \rightarrow 0$ ) is invariant under:

$$SU_L(3) \times SU_R(3) \times U_A(1) \times U_B(1)$$

- Chiral symmetry  $SU_L(3) \times SU_R(3)$  spontaneously breaks to  $SU(3)$

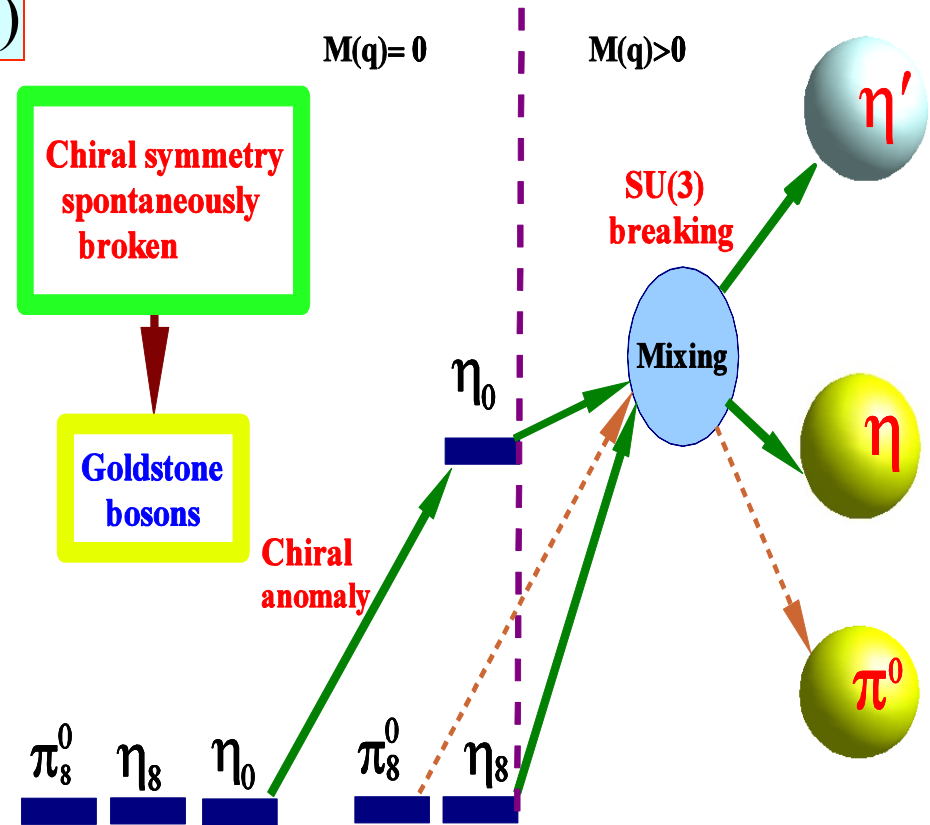
- 8 Goldstone Bosons (GB)

- $U_A(1)$  is explicitly broken: (Chiral anomalies)

- $\Gamma(\pi^0 \rightarrow \gamma\gamma)$ ,  $\Gamma(\eta \rightarrow \gamma\gamma)$ ,  $\Gamma(\eta' \rightarrow \gamma\gamma)$
- Mass of  $\eta_0$

- $SU_L(3) \times SU_R(3)$  and  $SU(3)$  are explicitly broken:

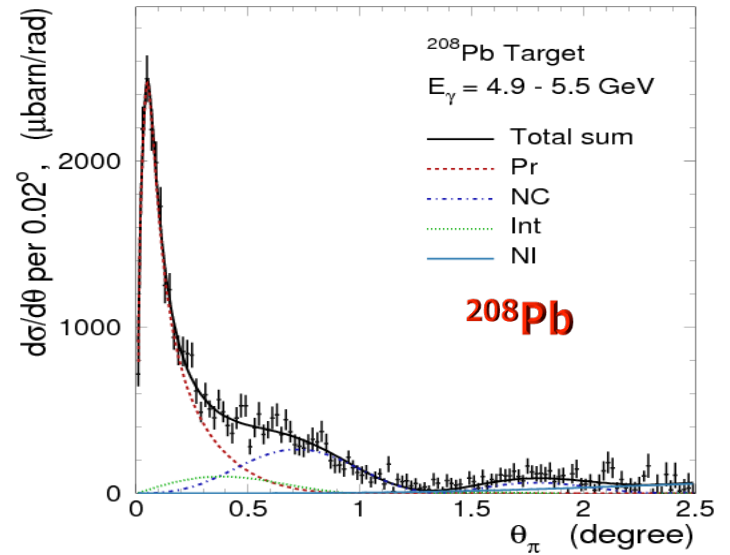
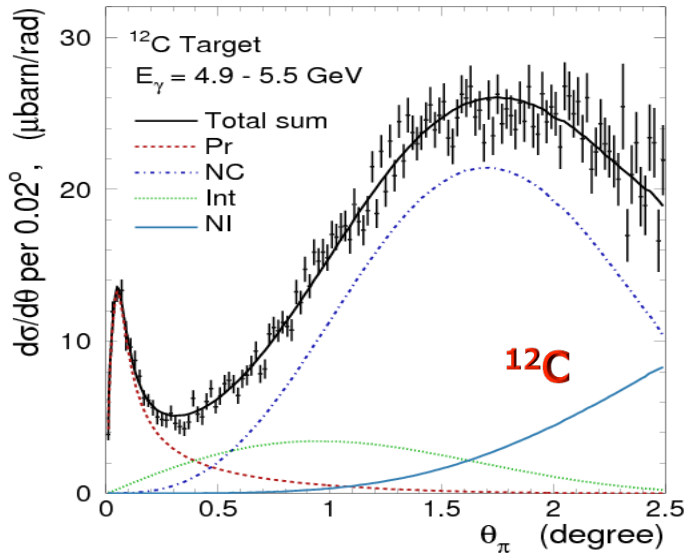
- GB are massive
- Mixing of  $\pi^0$ ,  $\eta$ ,  $\eta'$



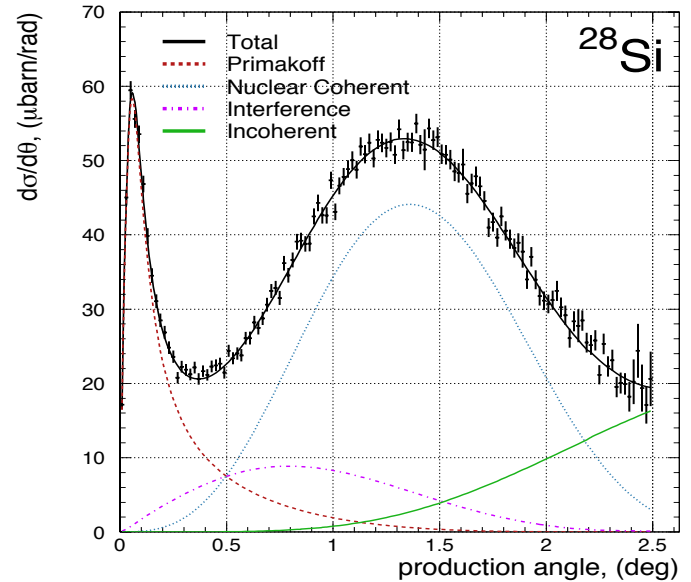
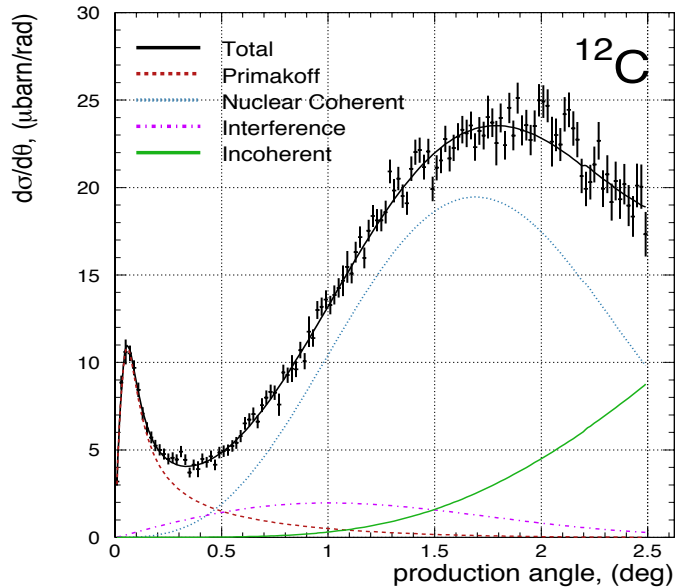
The  $\pi^0$ ,  $\eta$ ,  $\eta'$  system provides a rich laboratory to study the symmetry structure of QCD at low energies.

# Differential Cross Sections

PrimEx I:

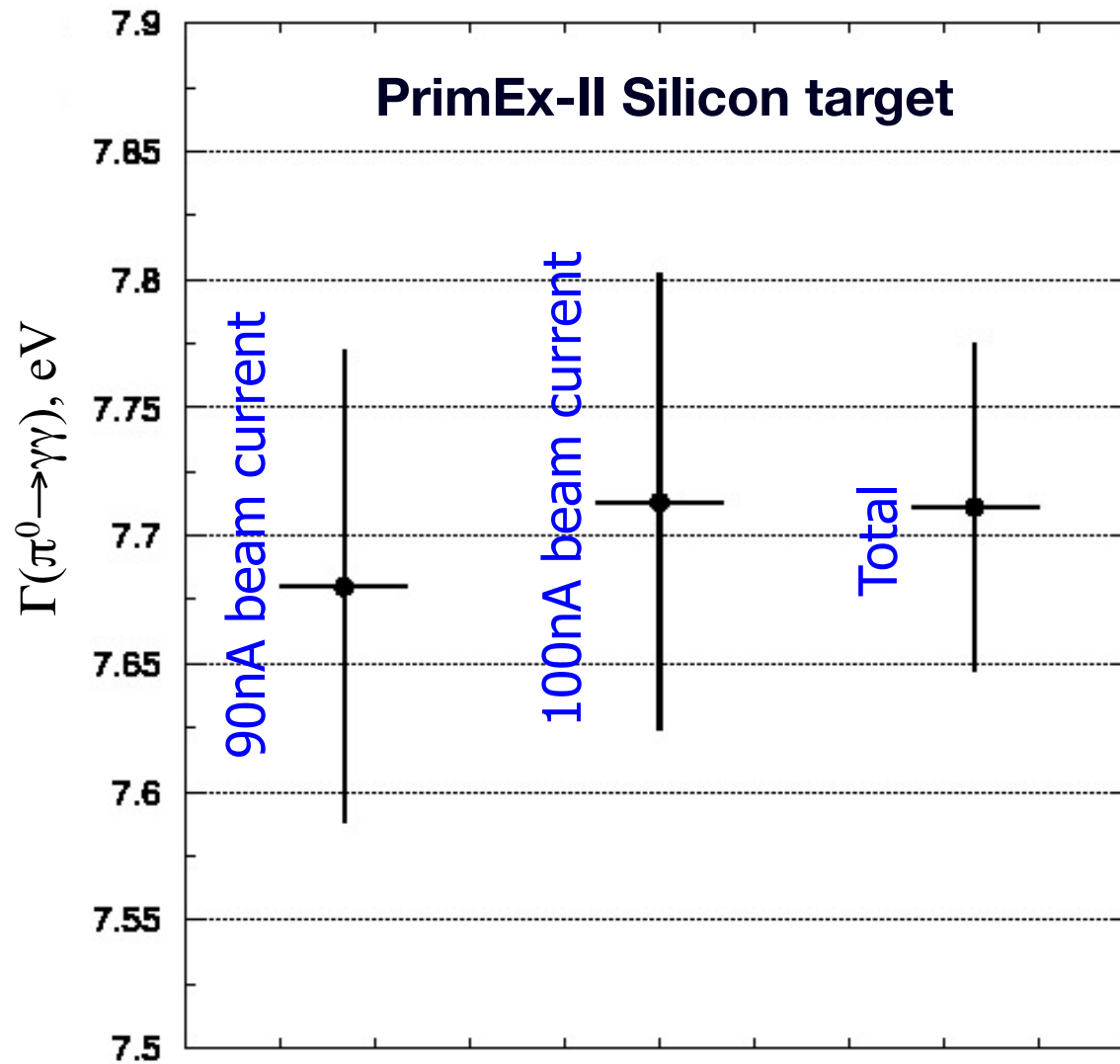


PrimEx II:

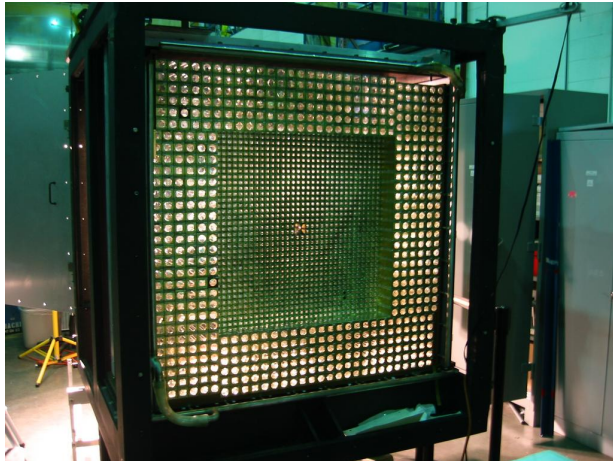
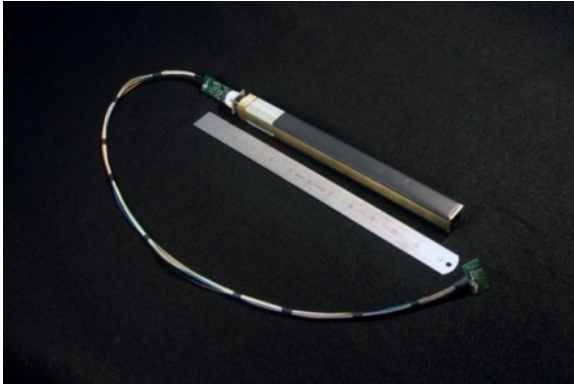




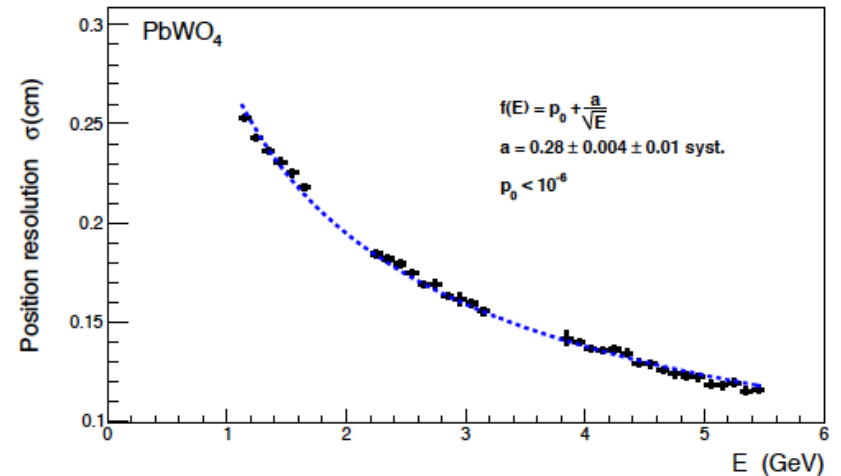
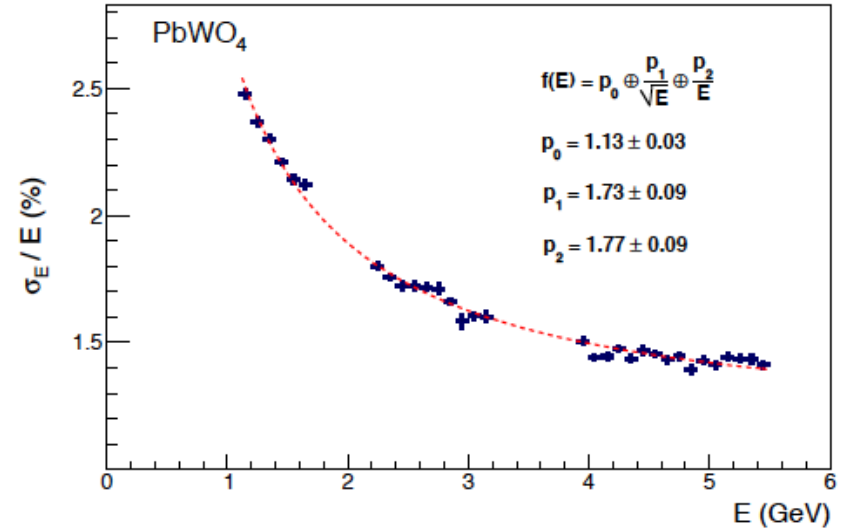
# Time and Run Condition Dependence



# PrimEx Hybrid Calorimeter - HyCal



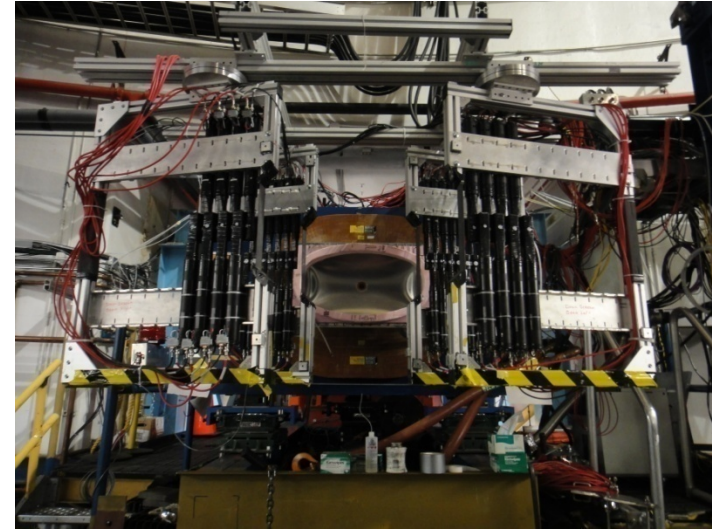
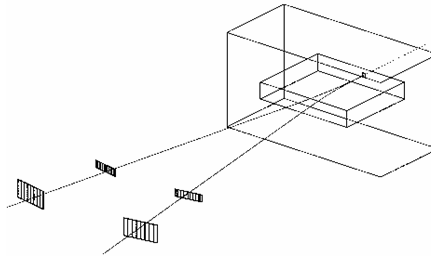
1152 PbWO<sub>4</sub> crystal detectors  
576 Pb-glass Cherenkov detectors



# Photon Flux Control

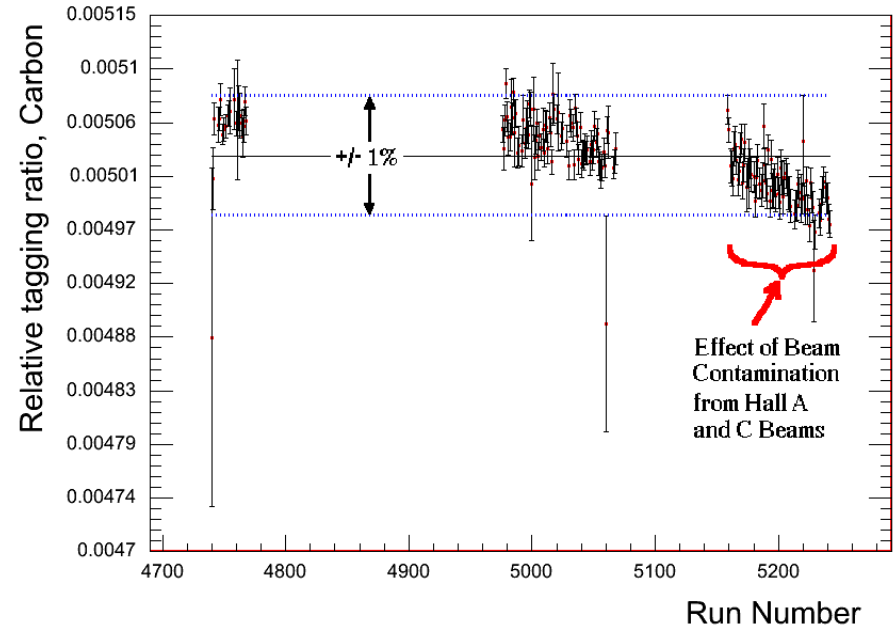
- ❑ Combination of:
  - 16 KGxM dipole magnet
  - 2 telescopes of 2x8 scintillating detectors

Pair Spectrometer



Measured in experiment:

- ❑ absolute tagging ratios
  - TAC measurements at low intensities
- ❑ relative tagging ratios:
  - pair production measured by pair spectrometer at low and high intensities
- ❑ Uncertainty of photon flux has been controlled at 1%
- ❑ Verified by measuring two well-known QED processes:
  - Compton scattering
  - $e^+e^-$  pair production



# Decay Length Measurements (Direct Method)

Measure  $\pi^0$  decay length

$$\tau_\pi \sim 8.5 \times 10^{-17} \text{ s} \Rightarrow c\tau_\pi \sim 25 \text{ nm}$$

too short to measure!

Solution: create energetic  $\pi^0$

$$L = v_\pi \gamma \tau_\pi \quad \gamma = 1 / \sqrt{1 - v_\pi^2 / c^2}$$

for  $E_\pi = 450 \text{ GeV}$ ,  $L_{\text{mean}} \sim 50 \mu\text{m}$

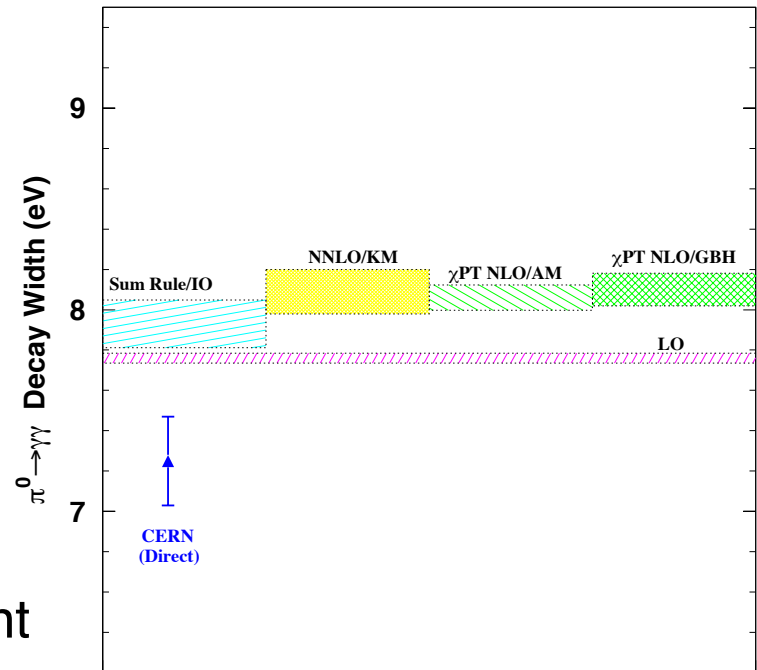
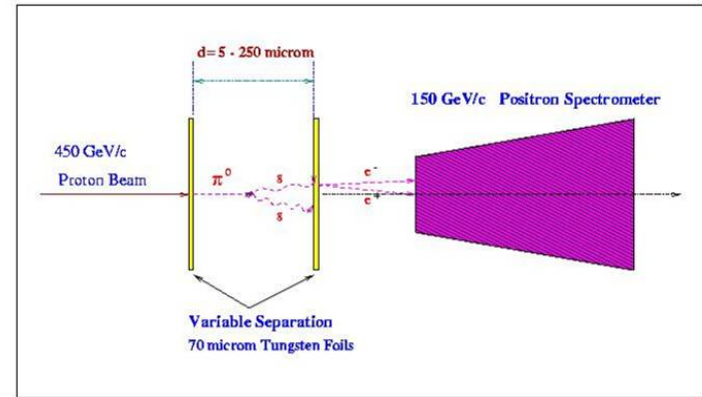
1984 CERN experiment (Phys.Lett.,158B,81):  
 P=450 GeV proton beam  
 Two variable separation (5-250 $\mu\text{m}$ ) foils

Result:

$$\Gamma(\pi^0 \rightarrow \gamma\gamma) = 7.25 \pm 0.18 \pm 0.11 \text{ eV (3\%)}$$

Major limitations of method:

1. needs higher energies for improvement
2. unknown  $P_{\pi^0}$  spectrum



Experiments

# The $e^+e^-$ Collision Method

CBAL @ DESY (1988)

Phy.Rev.,D38,1365

$$e^+e^- \rightarrow e^+e^-\gamma^*\gamma^* \rightarrow e^+e^-\pi^0 \rightarrow e^+e^-\gamma\gamma$$

$e^+$ ,  $e^-$  scattered at small angles (not detected)

only  $\gamma\gamma$  detected

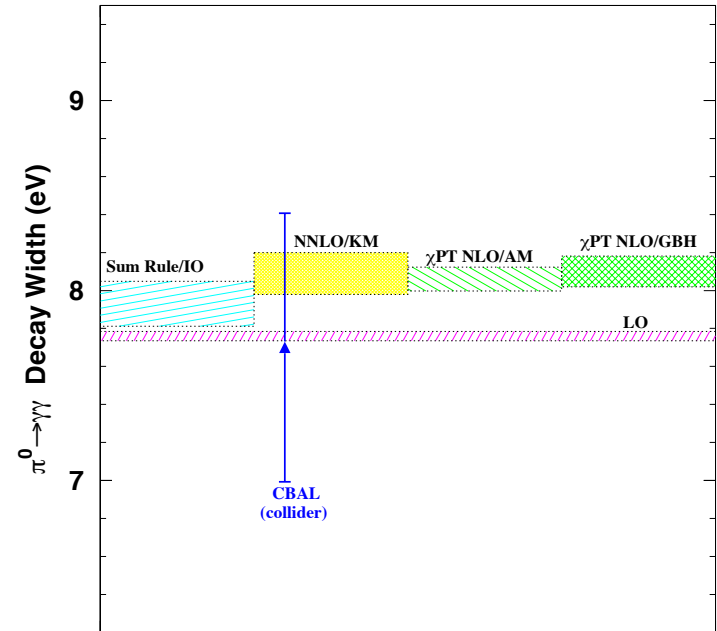
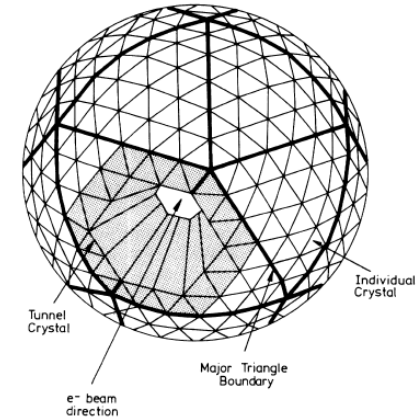
Results:

$$\Gamma(\pi^0 \rightarrow \gamma\gamma) = 7.7 \pm 0.5 \pm 0.5 \text{ eV (9.2\%)}$$

Not included in PDG until 2012

Major limitations of method

1. knowledge of luminosity
2. unknown  $q^2$  for  $\gamma^*\gamma^*$



Experiments

# Pion Beta Decay Method

## PIBETA @ PSI, 2009

Phys.Rev.Lett.,103,051802

◆ Measure  $\pi^+ \rightarrow e^+ \nu_e \gamma$  at rest to extract weak form factors  $F_V$  and  $F_A$

◆ Assume conserved vector current and isospin invariance, then

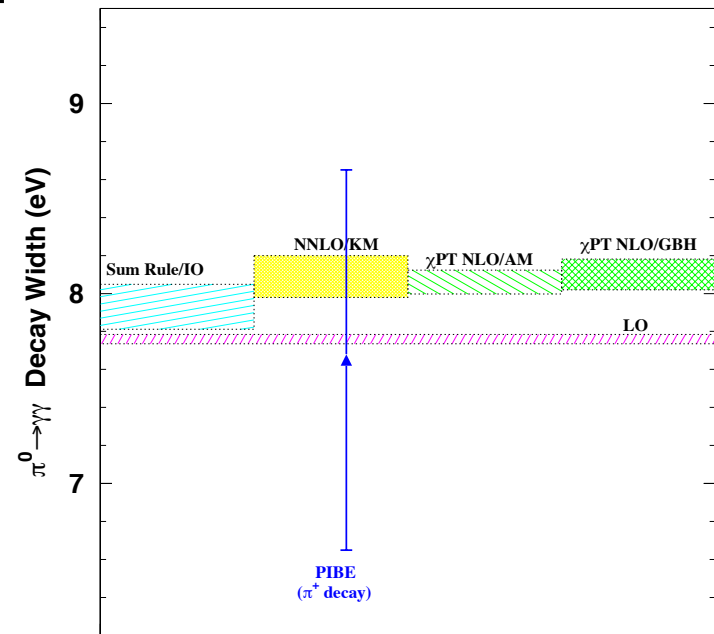
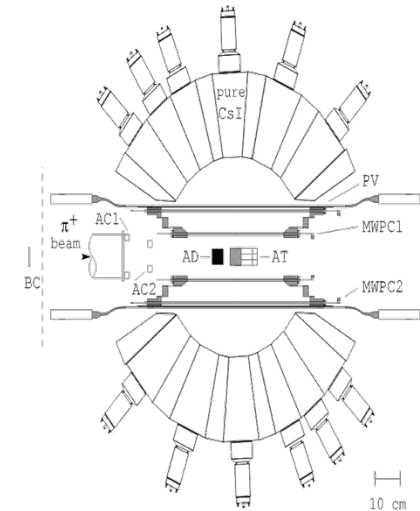
$$\Gamma(\pi \rightarrow \gamma\gamma) = \pi m_\pi \alpha^2 |F_V(0)|^2 / 2$$

Results:

$$\Gamma(\pi^0 \rightarrow \gamma\gamma) = 7.7 \pm 1.0 \text{ eV (13\%)}$$

### Major limitations of method

1. Isospin violation effect
2. Rare decay



Experiments