

Dense nuclear matter based on a chiral model with parity doublet structure

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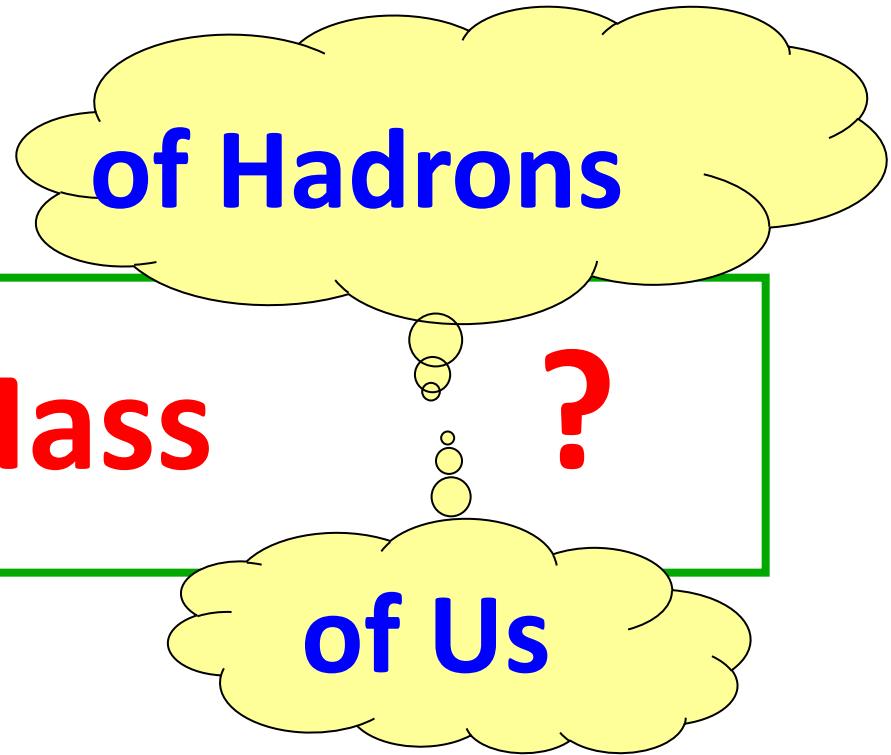
@ The 18th International Conference on Hadron Spectroscopy
and Structure (HADRON2019) (August 18, 2019)

Based on

- T. Yamazaki and M. Harada, Phys. Rev. C 100, 025205 (2019).
- T. Yamazaki and M. Harada, Phys. Rev. D 99, 034012 (2018).

Introduction

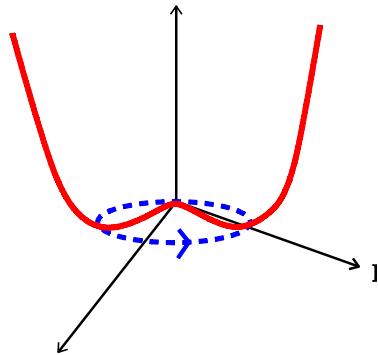
Origin of Mass



II

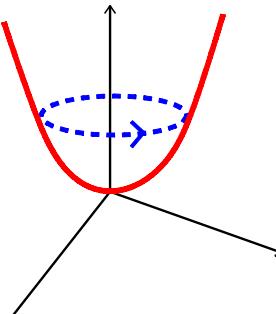
One of the Interesting problems of QCD

spontaneous chiral symmetry breaking



chiral symmetry
broken phase at
vacuum

$$\langle \bar{q}q \rangle \neq 0 \text{ (chiral condensate)}$$



chiral symmetric
phase at high T
and/or density

$$\langle \bar{q}q \rangle = 0$$

- The spontaneous chiral symmetry breaking is expected to generate a part of hadron masses.
- It causes mass difference between chiral partners.

- How much mass of nucleon is from the spontaneous chiral symmetry breaking ?
- What is the chiral partner of the nucleon ?

Parity Doublet models for nucleons

- How much mass of nucleon is from the spontaneous chiral symmetry breaking ?
- What is the chiral partner of nucleon ?
- A Parity doublet model for light baryons
 - In [C.DeTar, T.Kunihiro, PRD39, 2805 (1989)],
N*(1535) is regarded as the chiral partner to the
N(939) having the chiral invariant mass.

$$m_N = m_0 + m_{\langle \bar{q}q \rangle}$$

chiral invariant mass spontaneous chiral symmetry breaking



- This model can be extended to include different excited nucleons.

- We constructed an extended parity doublet model including four light nucleons N(939), N(1440), N(1535) and N(1650).
- We showed that the chiral invariant masses are constrained by the saturation properties of nuclear matter and neutron star properties.
 - T. Yamazaki and M. Harada, Phys. Rev. C 100, 025205 (2019).
 - T. Yamazaki and M. Harada, Phys. Rev. D 99, 034012 (2018).

Outline

1. Introduction
2. An Extended Parity Doublet Model for Nucleons:
Constraints to chiral invariant masses at vacuum
3. Constraints from Nuclear Matter and Neutron Star Properties
4. Summary

2. An Extended Parity Doublet Model for Nucleons: Constraints to chiral invariant masses at vacuum

T. Yamazaki and M. Harada, Phys. Rev. D 99, 034012 (2018).

chiral representation of baryons

- representation of quark under $SU(2)_R \times SU(2)_L$

$$q \sim q_r + q_l \sim (2,1) \oplus (1,2)$$

- representation of baryon under $SU(2)_R \times SU(2)_L$

$$\psi \sim q \otimes q \otimes q \sim [(2,1) \oplus (1,2)]^3$$

$$= 5[(2,1) \oplus (1,2)] \oplus 3[(3,2) \oplus (2,3)] \oplus [(4,1) \oplus (1,4)]$$

Chiral symmetry is broken and the isospin symmetry remains

$$I = \frac{1}{2} \text{ baryons}$$

$$I = \frac{3}{2} \text{ baryons}$$

Parity Doublet models with $[(2,1) \oplus (1,2)]$ nucleons

C.DeTar, T.Kunihiro, PRD39, 2805 (1989)

D.Jido, M.Oka, A.Hosaka, PTP106, 873 (2001)

S. Gallas, F. Giacosa, D. Rischke, PRD82, 014004 (2010)

- An excited nucleon with negative parity such as **N(1535)** is regarded as **the chiral partner** to the N(939).
- N(939) and N(1535) have a chiral invariant mass:
 - $m_0[\bar{\psi}_1\gamma_5\psi_2 - \bar{\psi}_2\gamma_5\psi_1]$
- Spontaneous chiral symmetry breaking generates the mass difference between chiral partners.
 - $-g_1[\bar{\psi}_{1l}M\psi_{1r} + \bar{\psi}_{1r}M^\dagger\psi_{1l}] - g_2[\bar{\psi}_{2r}M\psi_{2l} + \bar{\psi}_{2l}M^\dagger\psi_{2r}]$



- $M = \sigma + i \vec{\tau} \cdot \vec{\pi}$ transforms $M \rightarrow g_L M g_R^\dagger$
- $\langle M \rangle = \bar{\sigma} \neq 0$ causes the spontaneous chiral symmetry breaking.

$$m_\pm = \frac{1}{2} \left[\sqrt{(g_1 + g_2)^2 \bar{\sigma}^2 + 4m_0^2} \mp (g_2 - g_1) \bar{\sigma} \right]$$

$$\begin{aligned} m_+ &= m(N(939)) \\ m_- &= m(N(1535)) \end{aligned}$$

A model with $[(1,2) \oplus (2,1)]$ and $[(2,3) \oplus (3,2)]$ representations

T. Yamazaki and M. Harada, Phys. Rev. D99, 034012 (2018)

- We include two representations, $\psi \in [(1,2) \oplus (2,1)]$ and $\eta \in [(2,3) \oplus (3,2)]$ to study N(939), N(1440), N(1535), N(1650).
- There are 2 chiral invariant masses.
 - $-m_0^{(1)}[\bar{\psi}_1 \gamma_5 \psi_2 - \bar{\psi}_2 \gamma_5 \psi_1] - m_0^{(2)}[\bar{\eta}_1 \gamma_5 \eta_2 - \bar{\eta}_2 \gamma_5 \eta_1]$
- 6 Yukawa Interactions
 - $-g_1[\bar{\psi}_{1l} M \psi_{1r} + \bar{\psi}_{1r} M^\dagger \psi_{1l}] - g_2[\bar{\psi}_{2r} M \psi_{2l} + \bar{\psi}_{2l} M^\dagger \psi_{2r}]$
etc.
- We also have 4 terms with one derivative.
 - $a_1[\bar{\psi}_{1l} \gamma^\mu \partial_\mu M \psi_{2l} - \bar{\psi}_{1r} \gamma^\mu \partial_\mu M^\dagger \psi_{2r}]$ etc

Physical inputs

We first fix the values of the chiral invariant masses $m_0^{(1)}$ and $m_0^{(2)}$ to some constants, and use the following 10 physical inputs to determine 10 parameters (10 couplings).

Masses $m_{N(939)} = 939\text{MeV}$ $m_{N(1440)} = 1430\text{MeV}$
 $m_{N(1535)} = 1535\text{MeV}$ $m_{N(1650)} = 1650\text{MeV}$

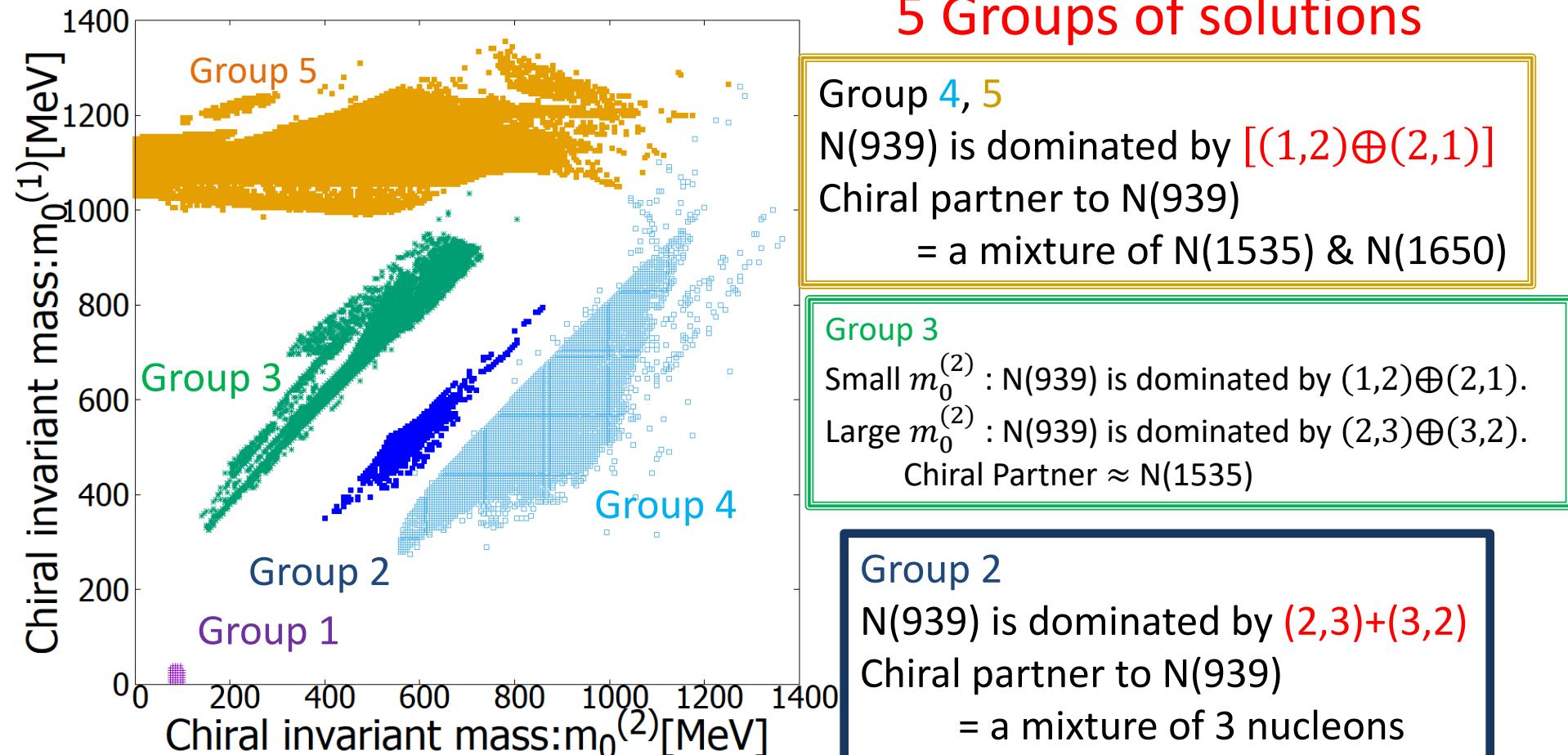
Decay widths $\Gamma(N(1440) \rightarrow N(939) + \pi) = 228\text{MeV}$
 $\Gamma(N(1535) \rightarrow N(939) + \pi) = 68\text{MeV}$
 $\Gamma(N(1650) \rightarrow N(939) + \pi) = 84\text{MeV}$
 $\Gamma(N(1650) \rightarrow N(1440) + \pi) = 22\text{MeV}$

Axial charges $g_A(N(939)) = 1.27$
 $g_A(N(1650)) = 0.55$ (Lattice analysis [T.T.Takahashi, T.Kunihiro, PRD78 (2008)])

Constraint $-0.25 \leq g_A(N(1535)) \leq 0.25$

2019/8/1 (Lattice analysis [T.T.Takahashi, T.Kunihiro, PRD78 (2008)] shows $g_A \sim O(0.1)$.)

Chiral invariant masses & Chiral partner structure



Group 1

N(939) is dominated by $(2,3)+(3,2)$ representation.
Chiral partner to n(939) = N(1440)

Prediction - Axial charges -

- In our model the following relation is satisfied:
 - $\sum_{i=1}^4 g_A(N_i) = 0$

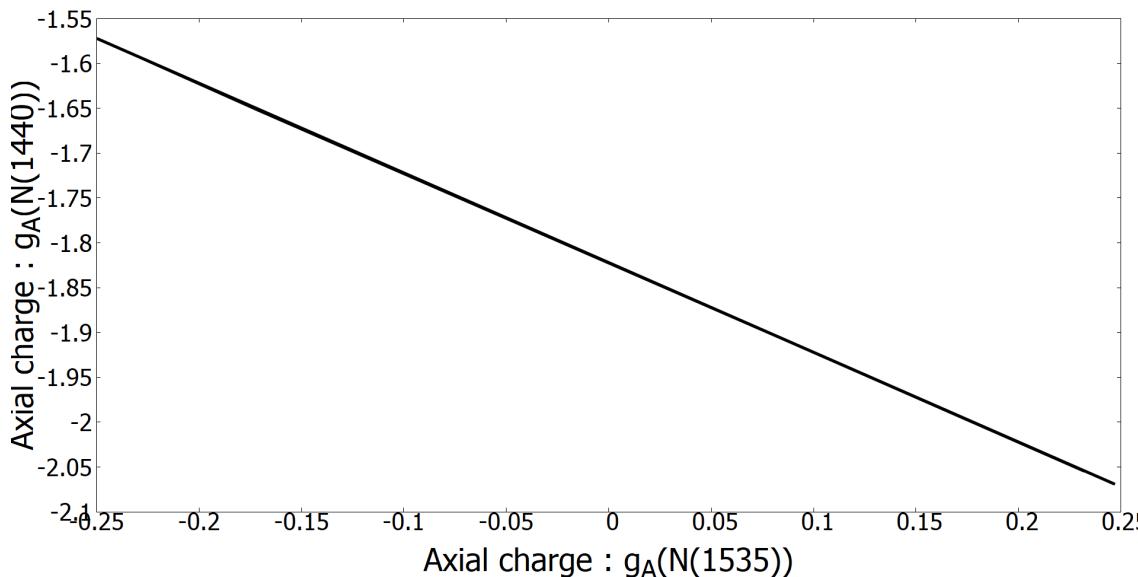
Constraint

$$-0.25 \leq g_A(N(1535)) \leq 0.25$$

Input

$$g_A(N(939)) = 1.27$$
$$g_A(N(1650)) = 0.55$$

$$-2.07 \leq g_A(N(1440)) \leq -1.57$$



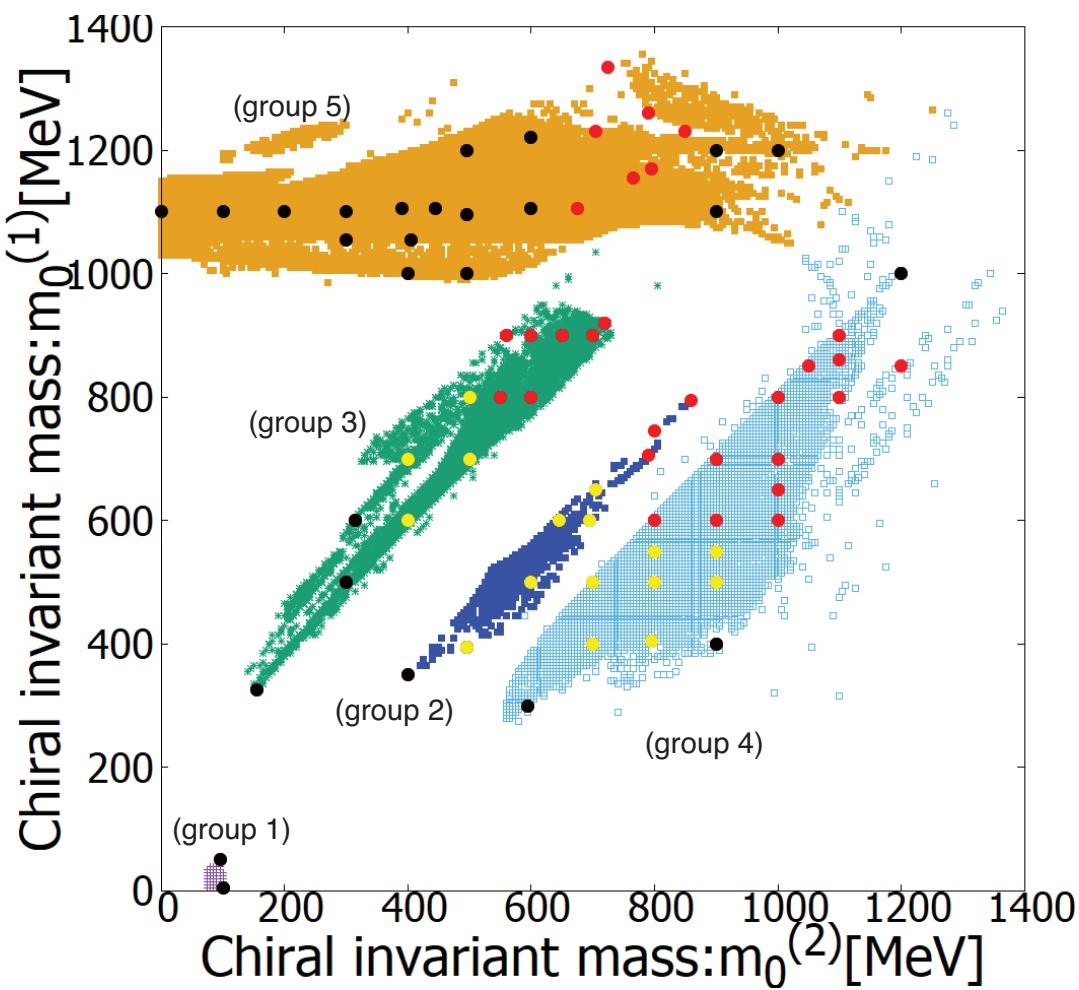
3. Constraints from Nuclear Matter and Neutron Star Properties

T. Yamazaki and M. Harada, Phys. Rev. C 100, 025205 (2019)

Construction of Nuclear Matter

- We include the **omega** and **rho** mesons into our model using the hidden local symmetry.
- We calculate the thermodynamic potential in the nuclear medium in our model, using **the mean field approximation**.
- Then, we adjust model parameters to reproduce the following physical inputs for given values of the chiral invariant masses $m_0^{(1)}$ and $m_0^{(2)}$.
- **Nuclear saturation density**
 - $\rho(\mu_B^* = 923\text{MeV}) = \rho_0 = 0.16\text{fm}^{-3}$
- **Binding energy at normal nuclear density**
 - $\left[\frac{E}{A} - m(939) \right]_{\rho_0} = \left[\frac{\varepsilon}{\rho_B} - m(939) \right]_{\rho_0} = -16\text{MeV}$
- **Incompressibility**
 - $K = 9\rho_0^2 \left. \frac{\partial^2(E/A)}{\partial \rho^2} \right|_{\rho_0} = 9\rho_0 \left. \frac{\partial \mu_B}{\partial \rho} \right|_{\rho_0} = 240\text{MeV}$
- **Symmetry energy**
 - $E_{\text{sym}}(\rho_0) = 31 \text{ MeV}$

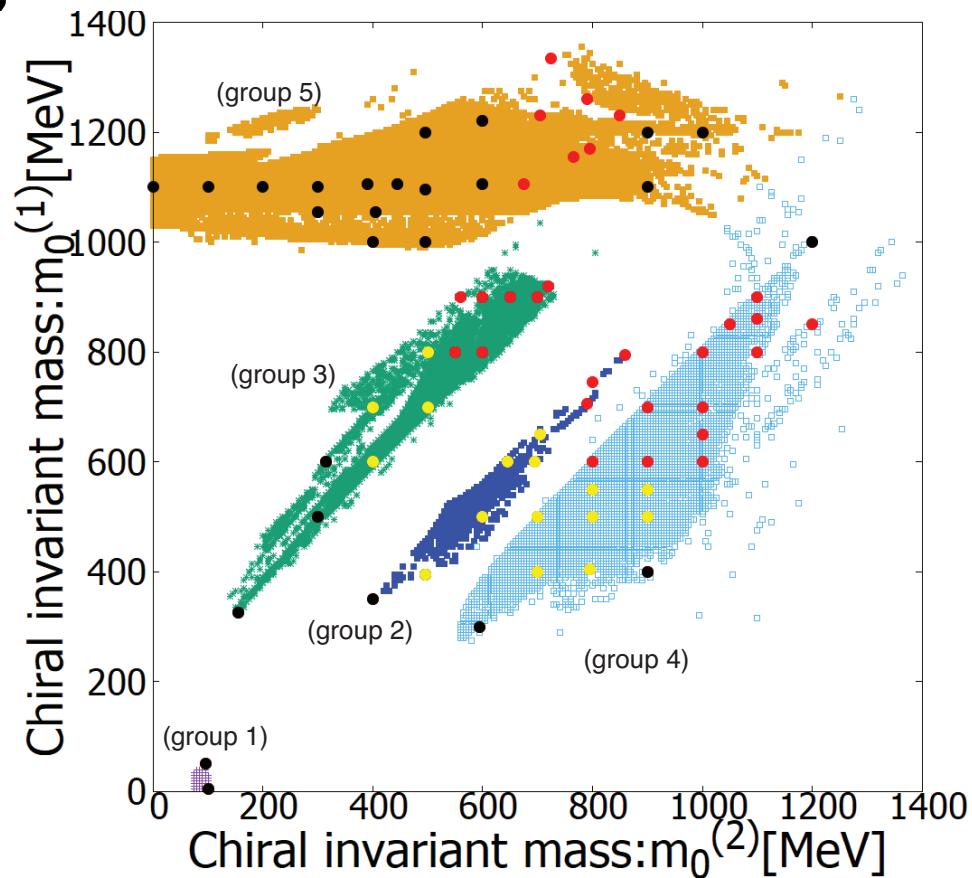
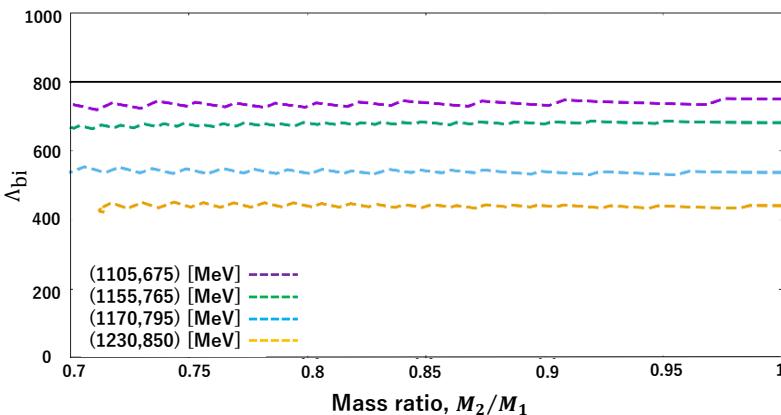
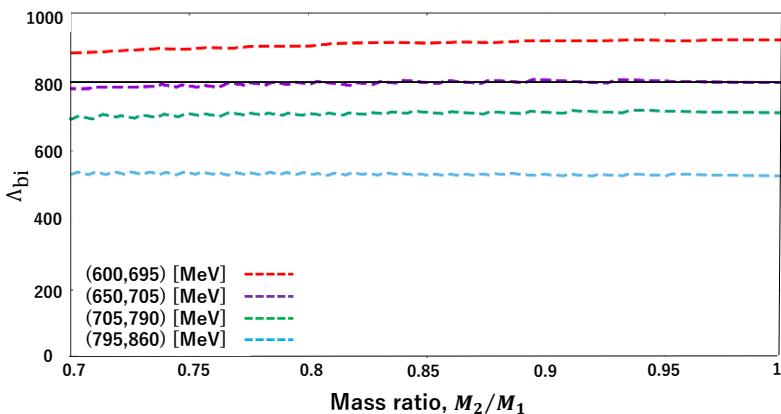
Constraint to model parameters



- We checked whether the saturation properties are satisfied for the parameter choices indicated by • marks.
- We found that, for the parameter choices indicated by • marks, the saturation properties are **NOT** satisfied.
- So, these parameter choices are excluded.
- In particular, please note that the parameter choices in **Group 1** are all excluded.

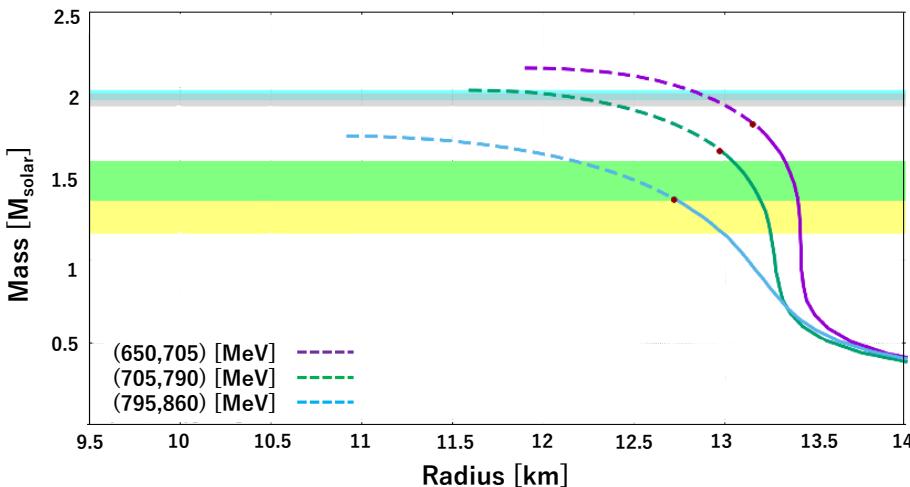
Constraint from Neutron Star Properties

- We obtained constraint to the chiral invariant masses from the tidal deformability of Neutron Stars.
 - Tidal deformability: $\tilde{\Lambda} \leq 800$ with $M_{\text{chirp}} = 1.188 M_{\odot}$
- • (yellow dots) are excluded, and • (red dots) are allowed

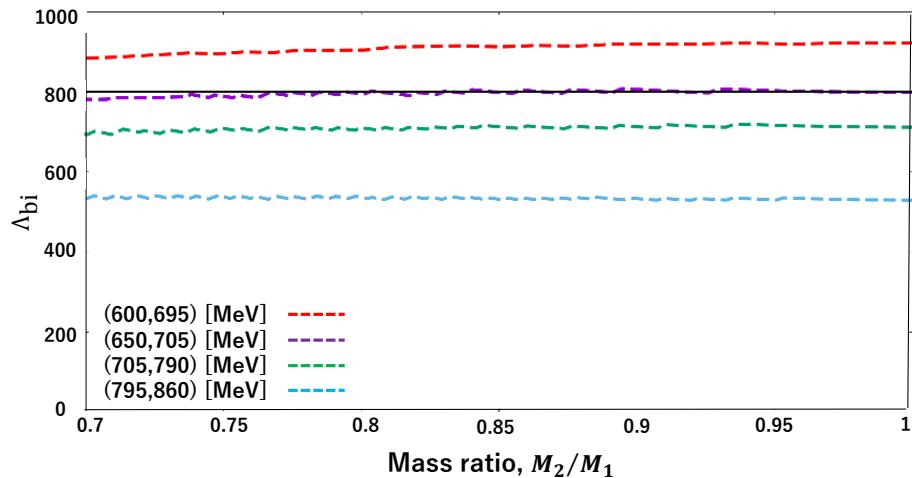


Mass-Radius Relation

- M-R relation



- Tidal deformability



The reason why smaller chiral invariant masses are excluded.

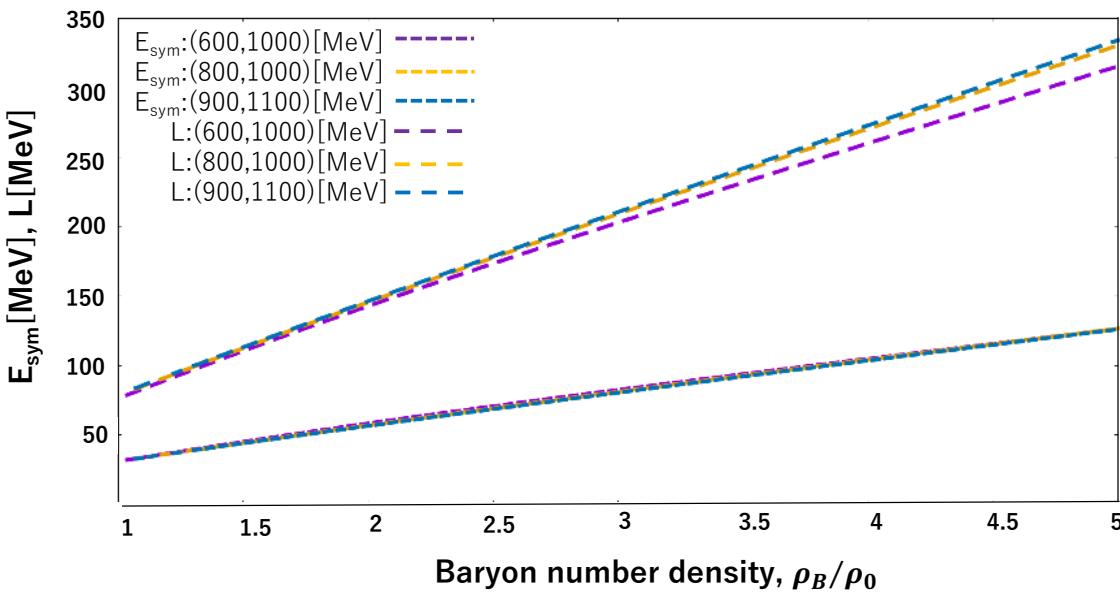
- The attractive force mediated by sigma contribution is larger for smaller chiral invariant masses. $m_{\pm} = \frac{1}{2} \sqrt{(g_1 + g_2)^2 \bar{\sigma}^2 + 4m_0^2 \mp (g_2 - g_1)\bar{\sigma}}$
- The repulsive force mediated by omega contribution is then larger for larger sigma contribution to satisfy the saturation properties of normal nuclear matter.
- The attractive force by the sigma contribution becomes smaller for larger density, while the repulsive force by the omega contribution becomes larger.
- The larger repulsive force make the radius and tidal deformability larger.
- As a result, the smaller chiral invariant masses cause the larger tidal deformability.

Symmetry energy and Slope parameter

- We include ρ meson into the model and obtain the symmetry energy and the slope parameter.

$$\begin{aligned} - E_{\text{sym}} &= \frac{\rho_B}{8} \left(\frac{2\pi^2}{\sum_{N,j} k_{FN}^{(i)} E_{FN}^{(i)}} + \frac{g_{\rho NN}^2}{m_\rho^2} \right) ; \quad E_{FN}^{(i)} = \sqrt{\left(k_{FN}^{(i)} \right)^2 + \left(m_*^{(I)} \right)^2} \\ - L &= 3\rho_B \left[\frac{1}{8} \left(\frac{2\pi^2}{kE} + \frac{g_{\rho NN}^2}{m_\rho^2} \right) + \frac{\rho_B}{8} \frac{\pi^2}{2k^2} \left(-\frac{2\pi^2}{k^2 E} - \frac{2\pi^2}{E^3} \right) \right] \end{aligned}$$

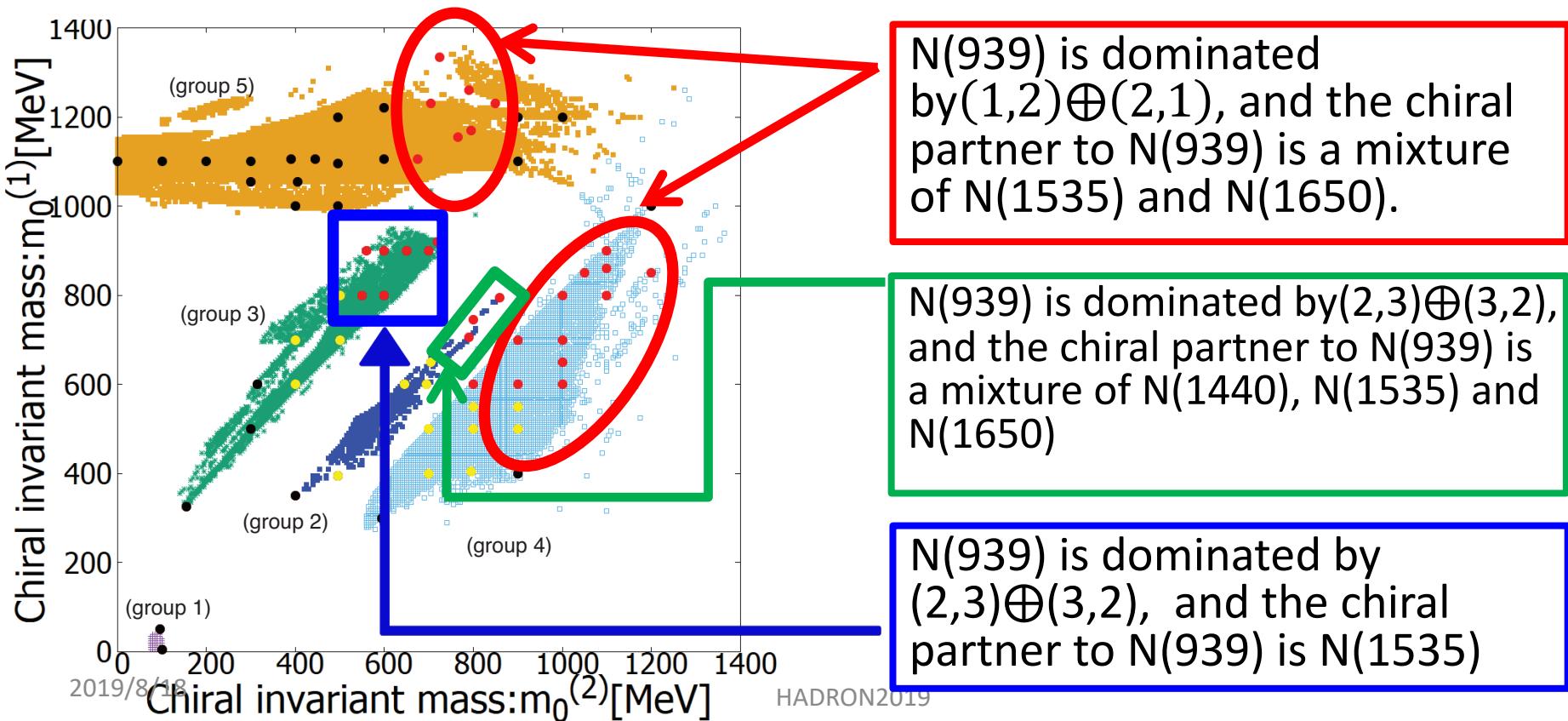
Predictions of the model



- The slope parameter has very little dependence on the chiral invariant mass.
- The symmetry energy does not depend on the choice of chiral invariant masses.
- Both increase linearly with density.

4. Summary

- We constructed an extended parity doublet model including two representations, $\psi \in [(1,2) \oplus (2,1)]$ and $\eta \in [(2,3) \oplus (3,2)]$ to study N(939), N(1440), N(1535), N(1650).
- We use masses, decay widths and axial charges to constrain 2 chiral invariant masses, and found that possible combinations are categorized into 5 groups.
- We exclude some values of the chiral invariant masses by requiring the saturation properties of normal nuclear matter indicated by black dots.
- We further obtain more constraints from the tidal deformability determined by the observation of the gravitational waves from neutron star merger GW170817

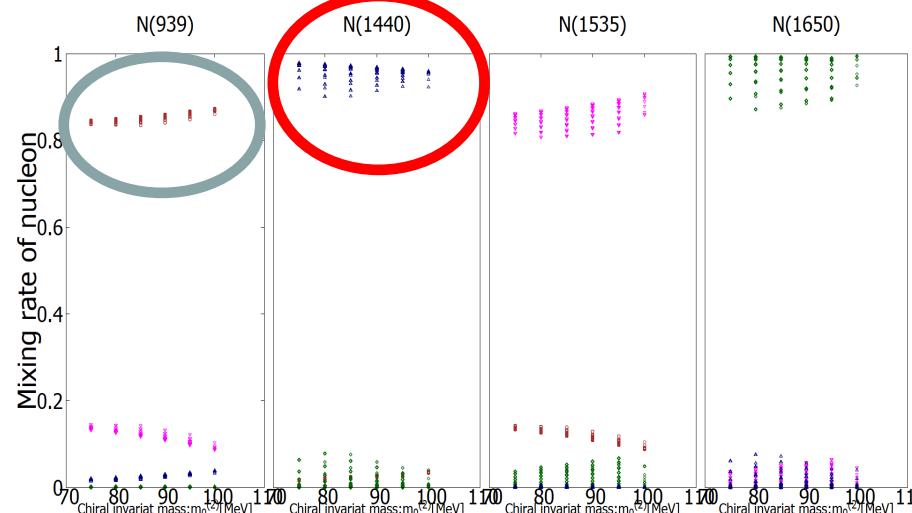


The End

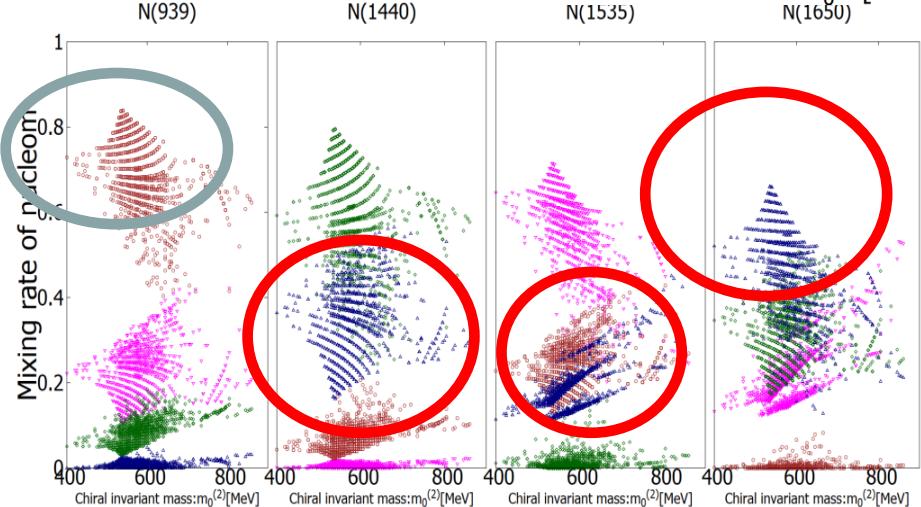
Mixing Rates of Nucleons

$(1,2) \oplus (2,1)$: ψ_1 ψ_2
 $(2,3) \oplus (3,2)$: η_1 η_2

Group 1



Group 2



N(939) is dominated by $[(2,3) \oplus (3,2)]$ representation.

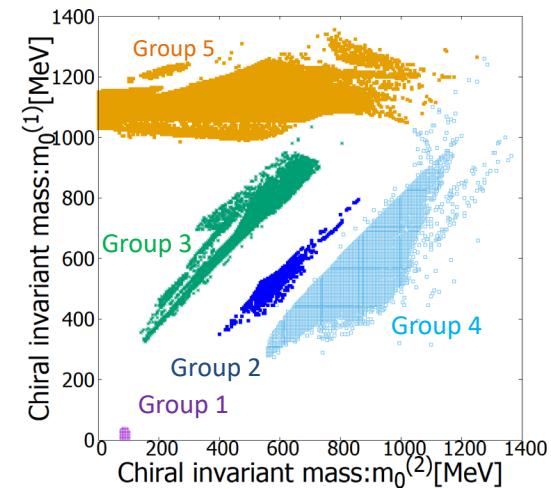
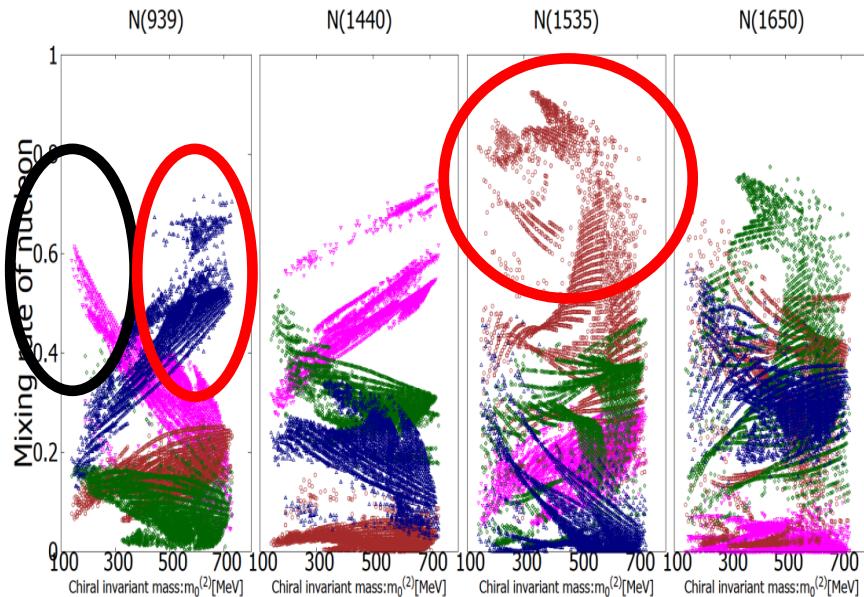
N(1440) is also dominated
by $[(2,3) \oplus (3,2)]$ representation. [> 80 %]
 \Rightarrow Chiral partner to N(939) = N(1440)

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N(1440) includes large amount of $(1,2)+(2,1)$
representation. [$[(2,3) \oplus (3,2)] < 60\%$]
 \Rightarrow Chiral partner to N(939) =
mixture of N(1440) + N(1535) + N(1650)

Mixing Rate of Nucleons NO.2

Group 3

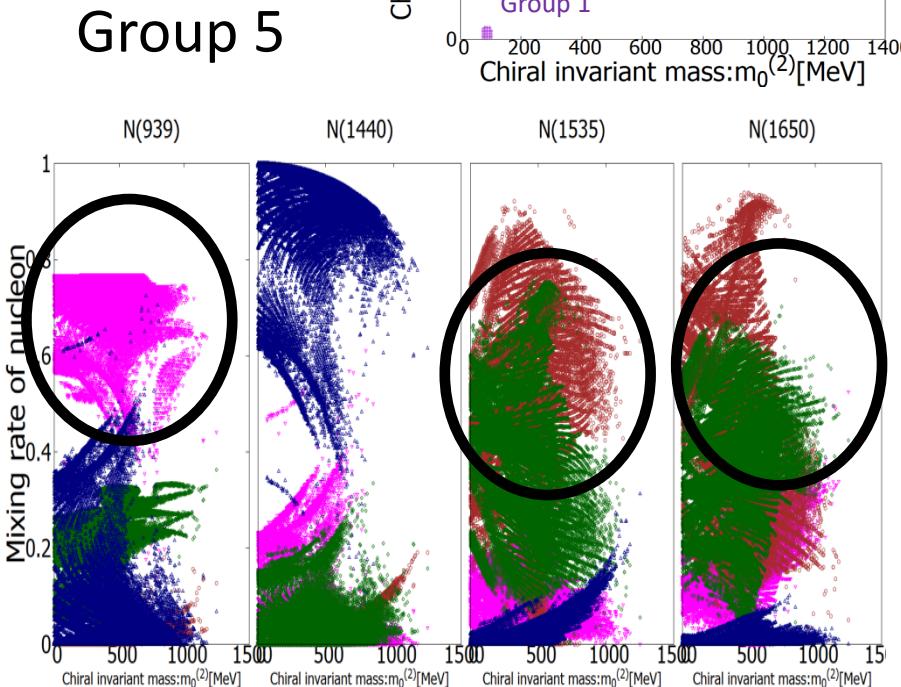
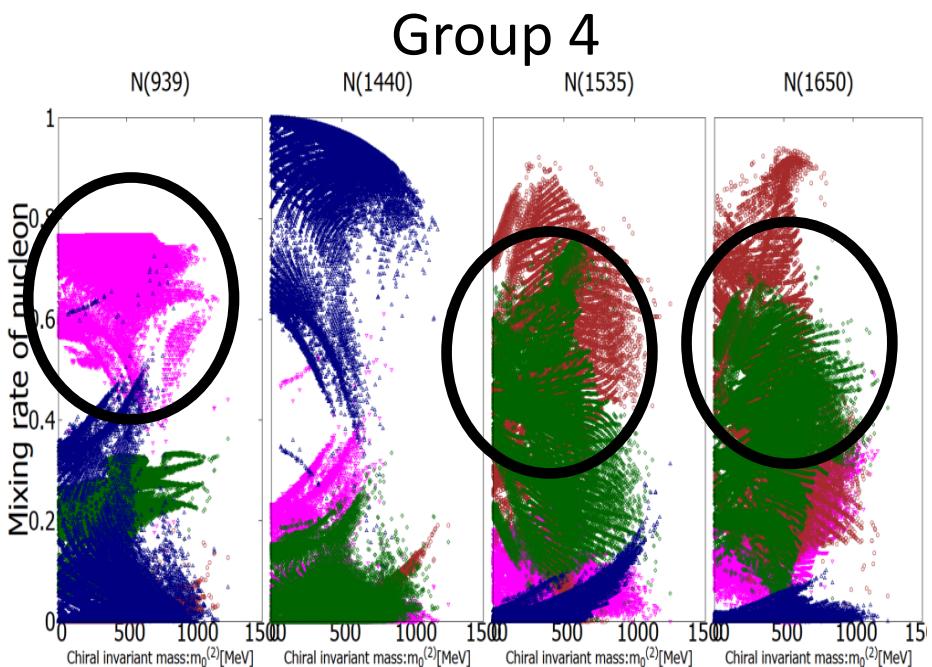


$$\begin{aligned}
 (1,2)\oplus(2,1) : & \psi_1 \text{ } \nabla \quad \psi_2 \text{ } \diamond \\
 (2,3)\oplus(3,2) : & \eta_1 \text{ } \circ \quad \eta_2 \text{ } \triangle
 \end{aligned}$$

- Small $m_0^{(2)}$: N(939) is dominated by $(1,2)\oplus(2,1)$.
- Large $m_0^{(2)}$: N(939) is dominated by $(2,3)\oplus(3,2)$.
 - Chiral Partner \approx N(1535)

Mixing Rate of Nucleons NO.3

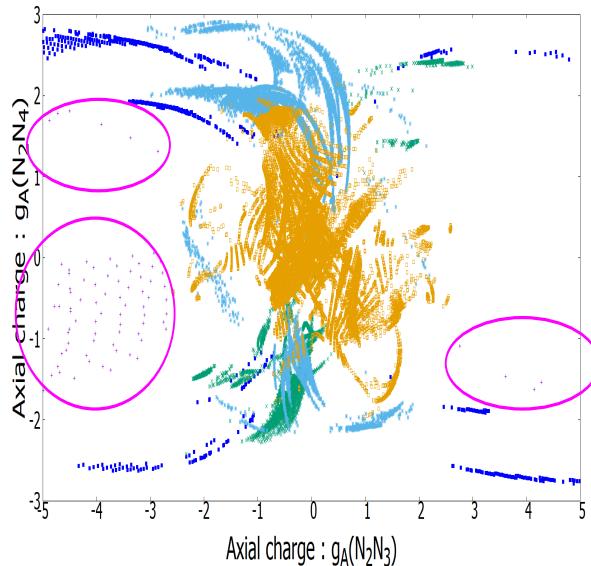
$(1,2) \oplus (2,1)$: ψ_1  ψ_2 
 $(2,3) \oplus (3,2)$: η_1  η_2 



- N(939) is dominated by $(1,2) \oplus (2,1)$.
 - Chiral Partner \approx a mixture of N(1535) and N(1650)

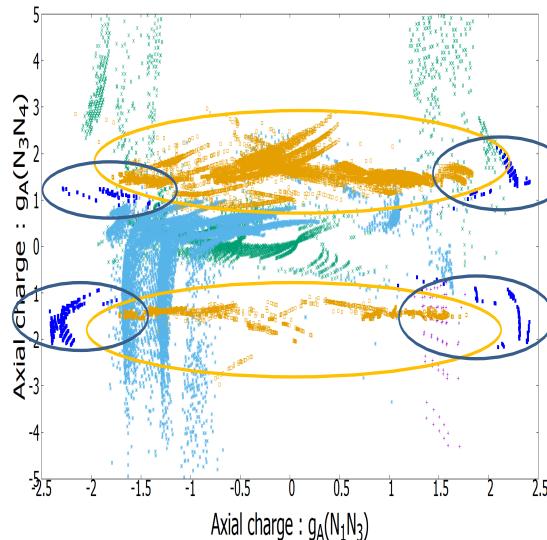
Transition Axial-Charges

- We calculated transition axial-charges:
 - $g_A(N_2(1440) - N_3(1535))$, $g_A(N_2(1440) - N_4(1650))$,
 - $g_A(N_1(939) - N_3(1535))$, $g_A(N_3(1535) - N_4(1650))$,
 - $g_A(N_1(939) - N_4(1650))$, $g_A(N_1(939) - N_2(1440))$,
- We find some features.

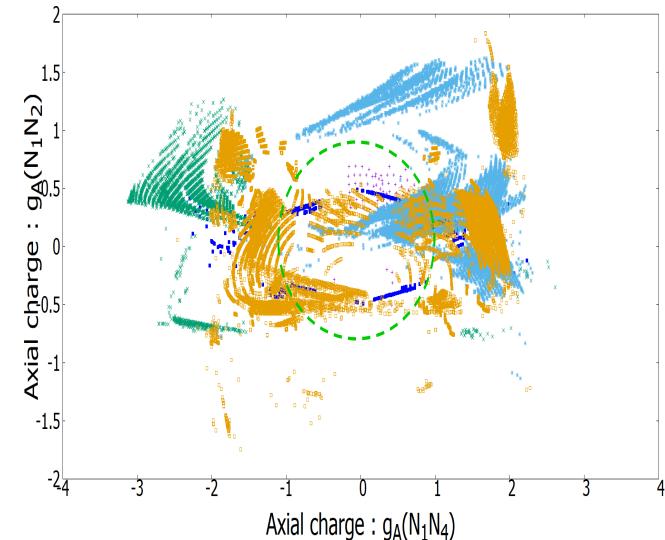


Predictions of Group 1
are separated from those
from other groups.

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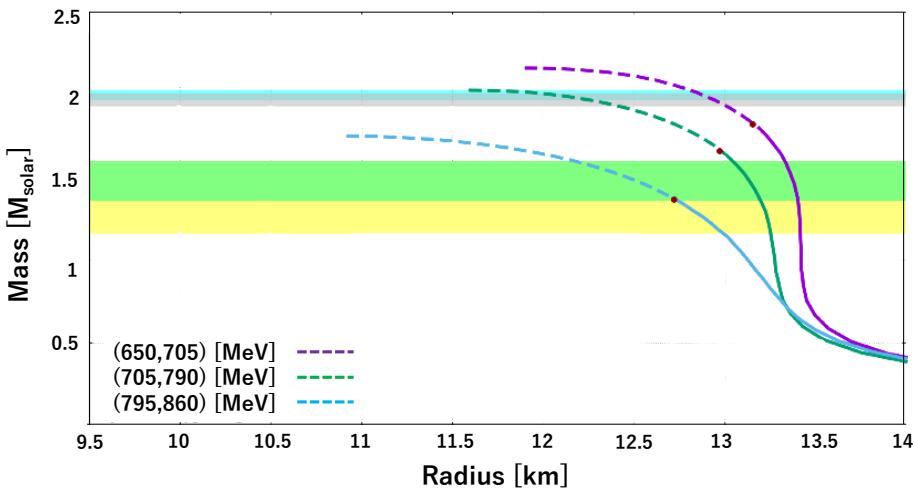
$g_A(N_3N_4)$ [for Group 2
and Group 5] ≈ 2
 $g_A(N_1N_3)$ for Group 2 is
large.



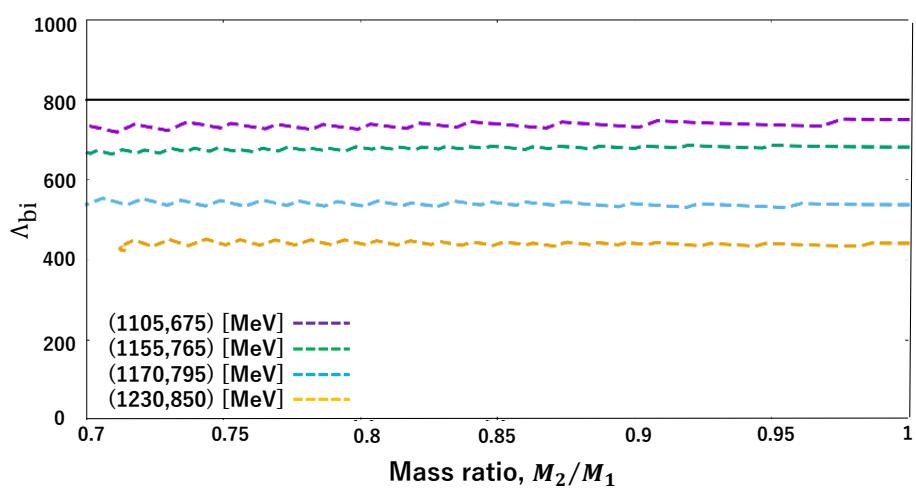
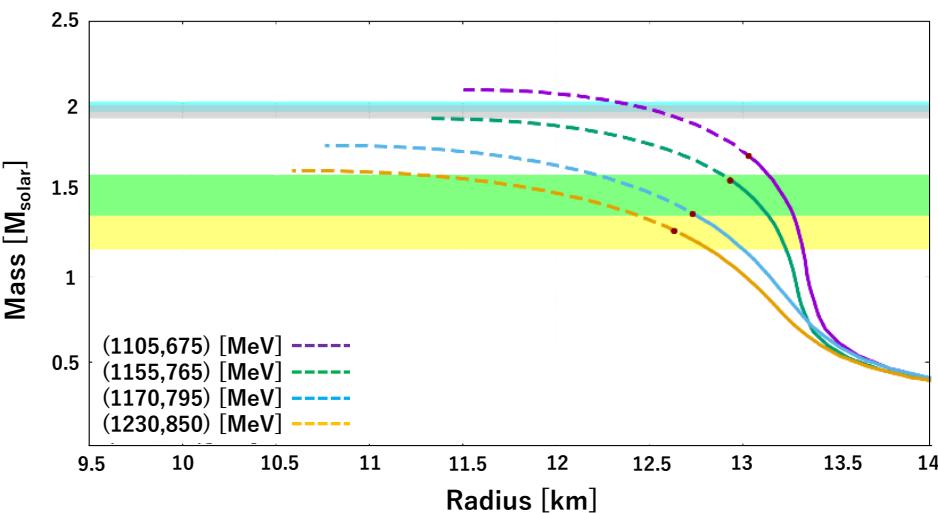
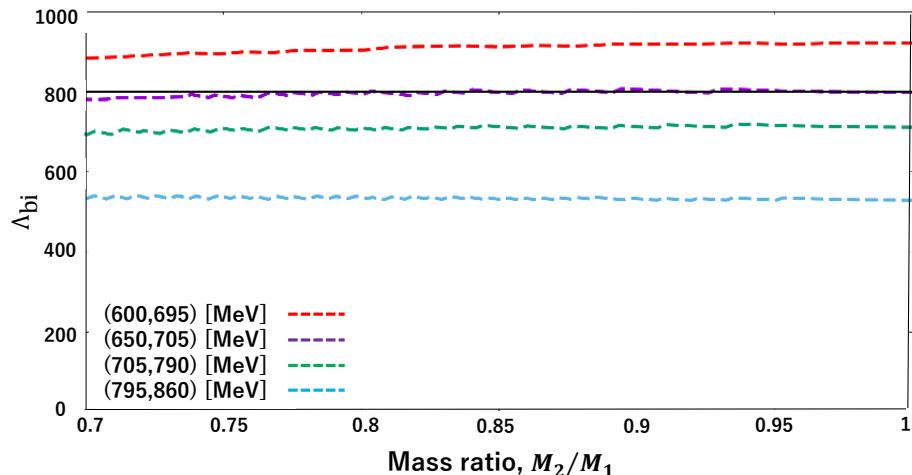
No Group 3 inside

Neutron Star Properties

- M-R relation

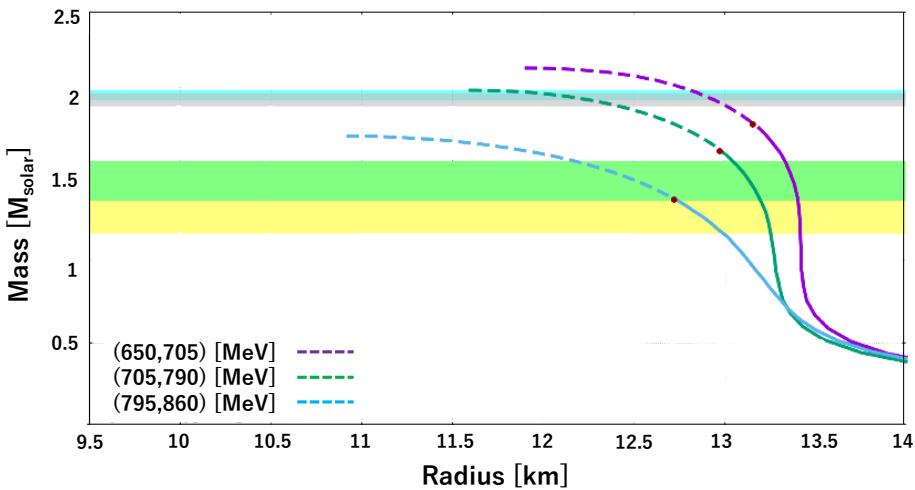


- Tidal deformability



Neutron Star Properties 2

- M-R relation



- Central density

