

Curious Link of Exclusive & Inclusive CPV in Charmless 3-body B^+ Decays

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National Taiwan University

17 August 2019, Hadron 2019, Guilin, China



臺灣大學

National Taiwan University



I. The Striking Plot, and a Curiosity

LHCb 1408.5373 (PRD)

II. FSI: elastic vs inelastic

III. FSI: soft vs hard

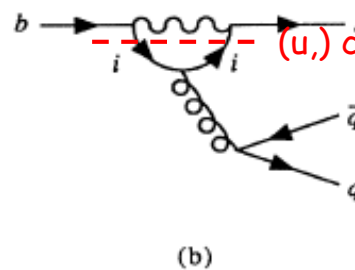
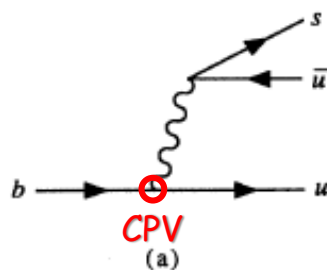
- CPT and inelastic hadron scattering
- a Critique

IV. Unitarity/ CPT at Quark Level: a 30-yr “Sum Rule”

V. Conclusion

Gérard and WSH, PRL'89
PRD'91

I. The Striking Plot, and a Curiosity



Bander, Silverman, Soni, PRL'79

Measurements of CP violation in the three-body phase space of charmless B^\pm decays

R. Aaij *et al.**

(LHCb Collaboration)

(Received 25 August 2014; published 11 December 2014)

The charmless three-body decay modes $B^\pm \rightarrow K^\pm \pi^+ \pi^-$, $B^\pm \rightarrow K^\pm K^+ K^-$, $B^\pm \rightarrow \pi^\pm K^+ K^-$ and $B^\pm \rightarrow \pi^\pm \pi^+ \pi^-$ are reconstructed using data, corresponding to an integrated luminosity of 3.0 fb^{-1} , collected by the LHCb detector. The inclusive CP asymmetries of these modes are measured to be

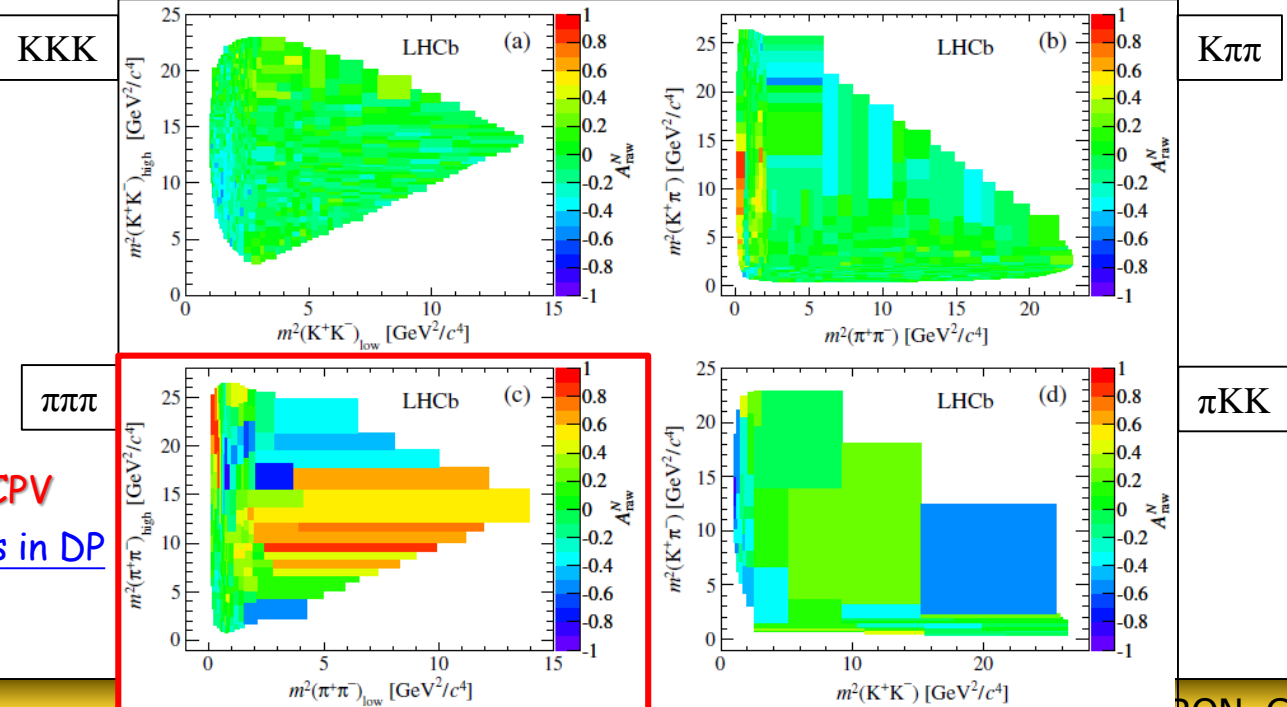
$$A_{CP}(B^\pm \rightarrow K^\pm \pi^+ \pi^-) = +0.025 \pm 0.004 \pm 0.004 \pm 0.007,$$

$$A_{CP}(B^\pm \rightarrow K^\pm K^+ K^-) = -0.036 \pm 0.004 \pm 0.002 \pm 0.007,$$

$$A_{CP}(B^\pm \rightarrow \pi^\pm \pi^+ \pi^-) = +0.058 \pm 0.008 \pm 0.009 \pm 0.007,$$

$$A_{CP}(B^\pm \rightarrow \pi^\pm K^+ K^-) = -0.123 \pm 0.017 \pm 0.012 \pm 0.007,$$

where the first uncertainty is statistical, the second systematic, and the third is due to the CP asymmetry of the $B^\pm \rightarrow J/\psi K^\pm$ reference mode. The distributions of these asymmetries are also studied as functions of position in the Dalitz plot and suggest contributions from rescattering and resonance interference



- strikingly large CPV
- strong variations in DP

KKK
181k

$K\pi\pi$
109k

$\pi\pi\pi$
25k

πKK
6k

KKK

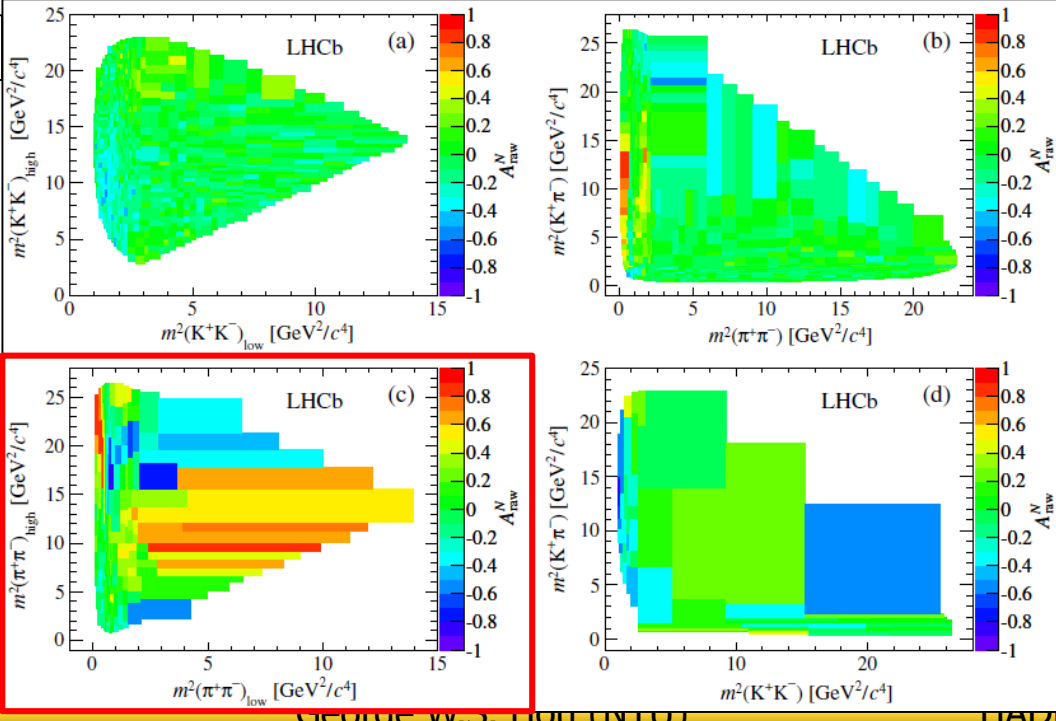
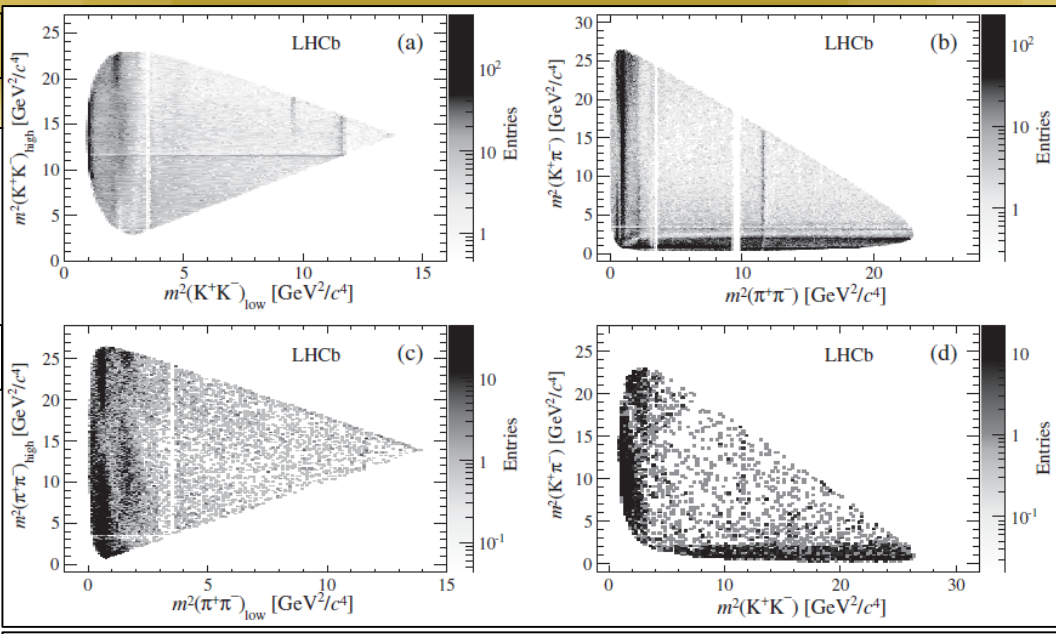
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incl. DCPV



bins w/ same # evts

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BR (10^{-5})

5.1	$A_{CP}(B^\pm \rightarrow K^\pm \pi^+ \pi^-) = +0.025 \pm 0.004 \pm 0.004 \pm 0.007,$	$+2.7 \pm 0.8\%$
3.4	$A_{CP}(B^\pm \rightarrow K^\pm K^+ K^-) = -0.036 \pm 0.004 \pm 0.002 \pm 0.007,$	$-3.3 \pm 0.8\%$
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(PDG)

a Curiosity

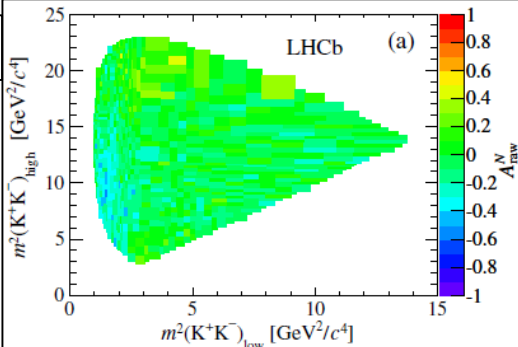
0.3% ($b \rightarrow s$)

1.1% ($b \rightarrow d$)

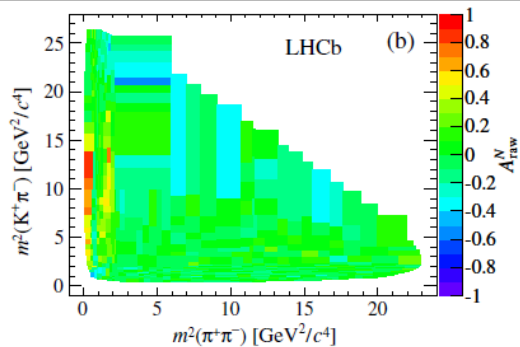
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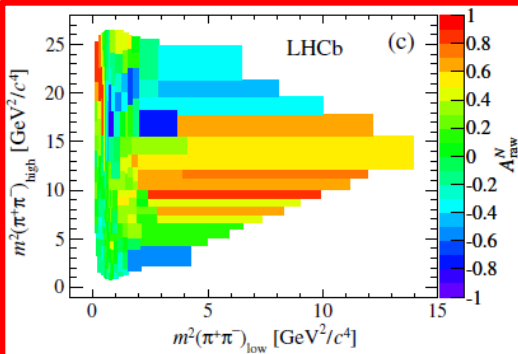
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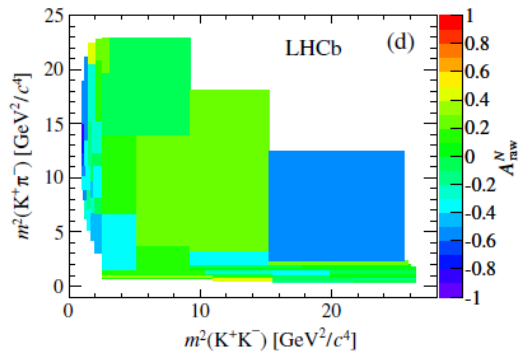
Kpi



pi pi



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bins w/ same # evts

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LHCb 1408.5373 (PRD)

PHYSICAL REVIEW D 90, 112004 (2014) Measurements of CP violation in the three-body phase space of charmless B^\pm decays

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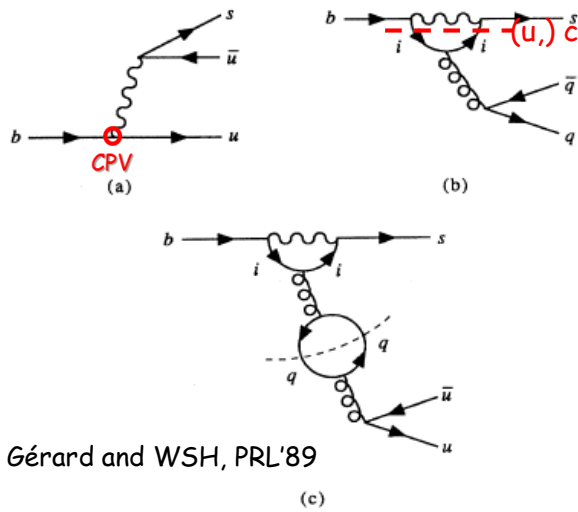
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181k
109k
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6k



Gérard and WSH, PRL'89

TABLE I. (Semi-)inclusive branching ratio B and asymmetries for $b \rightarrow s$ and $b \rightarrow d$ processes for $\rho = -0.5$, $\eta = 0.15$, and $m_t = M_W$. a_0 is with Figs. 1(a) and 1(b) only, while a is the result with Fig. 1(c) taken into account. The entry "0.0" stands for a very small positive number.

	B (%)	a_0 (%)	a (%)
$b \rightarrow su\bar{u}$	0.46	1.2	0.0
$b \rightarrow sd\bar{d} + ss\bar{s}$	0.54	0.5	0.5
<u>Total $b \rightarrow s$ (no charm)</u>	1.19	0.7	0.2
$b \rightarrow du\bar{u}$	0.71	-0.7	-0.0
$b \rightarrow dd\bar{d} + ds\bar{s}$	0.07	-4.2	-4.2
<u>Total $b \rightarrow d$ (no charm)</u>	0.80	-1.0	-0.4

$\sim 0.12, 0.35$

Gérard and WSH, PRD'91

II. FSI: elastic vs inelastic

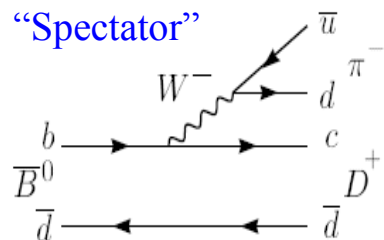
Experiment-driven take on Final State Interactions

Observation of the Color-Suppressed Decay $\bar{B}^0 \rightarrow D^0 \pi^0$

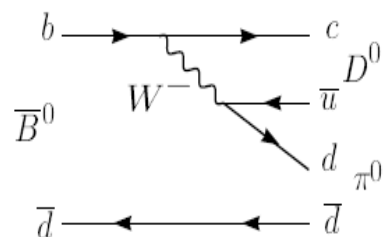
Belle, PRL'02

Mode	Signal Yield	Σ	$B\bar{B}$ bg	$D^{*0}h^0$	$q\bar{q}$ bg	$\epsilon(\%)$	$\mathcal{B} (\times 10^{-4})$	UL ($\times 10^{-4}$)	Th ($\times 10^{-4}$)
$D^0 \pi^0$	$126.2^{+16.1+7.2}_{-15.5-5.2}$	9.3	26.7	1.3	145.6	1.79	$3.1 \pm 0.4 \pm 0.5$	—	0.7
$D^{*0} \pi^0$	$26.4^{+7.7+1.6}_{-7.1-2.2}$	4.1	5.9	—	10.4	0.42	$2.7^{+0.8+0.5}_{-0.7-0.6}$	—	1.0
$D^0 \eta^*$	$22.1^{+7.0+2.0}_{-6.3-1.8}$	4.2	3.4	0.7	19.1	0.67	$1.4^{+0.5}_{-0.4} \pm 0.3$	—	0.5
$D^{*0} \eta$	$7.8^{+3.6}_{-3.0} \pm 0.7$	3.3	1.4	—	1.5	0.17	$2.0^{+0.9}_{-0.8} \pm 0.4$	4.6	0.6
$D^0 \omega$	$32.5^{+9.4+4.0}_{-8.6-3.1}$	4.4	$5.3(2.3)^\dagger$	1.4	58.5	0.80	$1.8 \pm 0.5^{+0.4}_{-0.3}$	—	0.7
$D^{*0} \omega$	$16.1^{+6.8}_{-6.0} \pm 2.4$	3.0	$5.3(1.5)^\dagger$	—	13.8	0.23	$3.1^{+1.3}_{-1.1} \pm 0.8$	7.9	1.7

“Spectator”



Color-suppressed



PHYSICAL REVIEW D, VOLUME 65, 096007

Final state rescattering and color-suppressed $\bar{B}^0 \rightarrow D^{(*)0} h^0$ decays

Chun-Khiang Chua* and Wei-Shu Hou

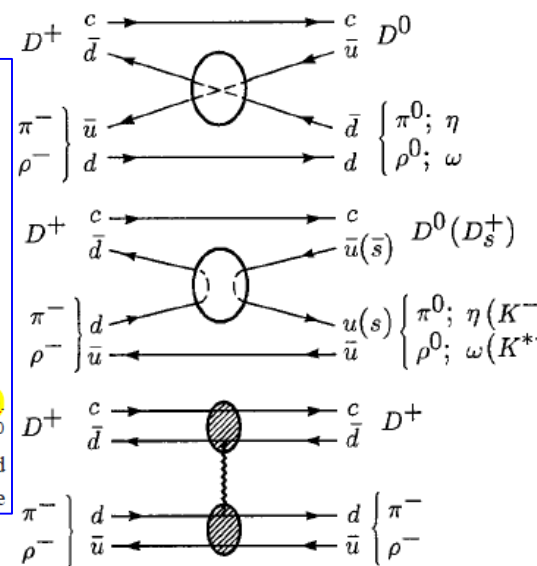
Physics Department, National Taiwan University, Taipei, Taiwan 10764, Republic of China

Kwei-Chou Yang

Physics Department, Chung Yuan Christian University, Chung-Li, Taiwan 32023, Republic of China

(Received 11 December 2001; published 7 May 2002)

The color-suppressed $B^0 \rightarrow D^{(*)0} \pi^0$, $D^{(*)0} \eta$, $D^0 \omega$ decay modes have just been **observed for the first time**. The rates are all larger than expected, hinting at the presence of **final state interactions**. Considering the $B^0 \rightarrow D^{(*)0} \pi^0$ mode alone, an **elastic $D^{(*)} \pi \rightarrow D^{(*)} \pi$ rescattering** phase difference $\delta \equiv \delta_{1/2} - \delta_{3/2} \sim 30^\circ$ would suffice, but the $\bar{B}^0 \rightarrow D^{(*)0} \eta$, $D^0 \omega$ modes compel one to extend the elastic formalism to SU(3) symmetry. We



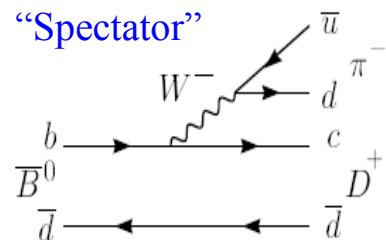
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Belle, PRL'02

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PHYSICAL REVIEW D 71, 014030 (2005)

Final state interactions in hadronic B decays

Hai-Yang Cheng,¹ Chun-Khiang Chua,¹ and Amarjit Soni²

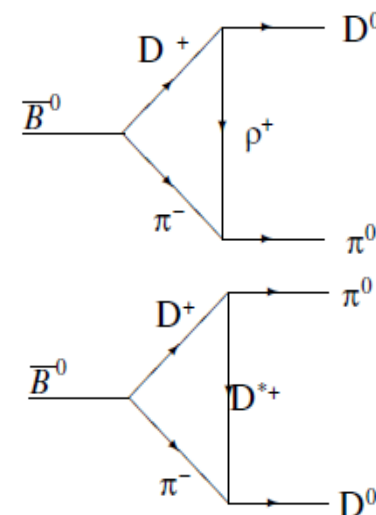
¹*Institute of Physics, Academia Sinica, Taipei, Taiwan 115, Republic of China*

²*Physics Department, Brookhaven National Laboratory, Upton, New York 11973, USA*

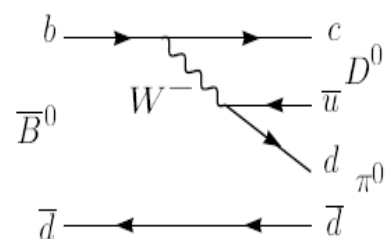
(Received 5 October 2004; published 26 January 2005)

There exist many experimental indications that final-state interactions (FSIs) may play a prominent role not only in charmful B decays but also in charmless B ones. We examine the final-state rescattering effects on the hadronic B decay rates and their impact on direct CP violation. The color-suppressed neutral modes such as $B^0 \rightarrow D^0 \pi^0, \pi^0 \pi^0, \rho^0 \pi^0, K^0 \pi^0$ can be substantially enhanced by long-distance rescattering effects. The direct CP-violating partial rate asymmetries in charmless B decays to $\pi\pi/\pi K$ and $\rho\pi$ are significantly affected by final-state rescattering, and their signs are generally different from that predicted by the short-distance (SD) approach. For example, direct CP asymmetry in $B^0 \rightarrow \rho^0 \pi^0$ is increased to

- Meson loops: how does it work when far off-shell?
- Went on to **Inelastic**, for sake of “charmless” (e.g. $K\pi$)
→ diagrammatics is cherry-picking and arbitrary.



Color-suppressed



I'm not at all adverse to Final State Interactions

CLEO Era

- “Prospects for direct CP violation in exclusive and inclusive **charmless B decays**”
He, WSH, Yang, PRL'98
- “Electroweak Penguins, FSI Phases, and CP Violation in **$B \rightarrow K\pi$** Decays”
Deshpande, He, WSH, Pakvasa, PRL'99
- “Possibility of Large Final State Interaction Phases in Light of **$B \rightarrow K\pi, \pi\pi$** Decays”
WSH, Yang, PRL'00

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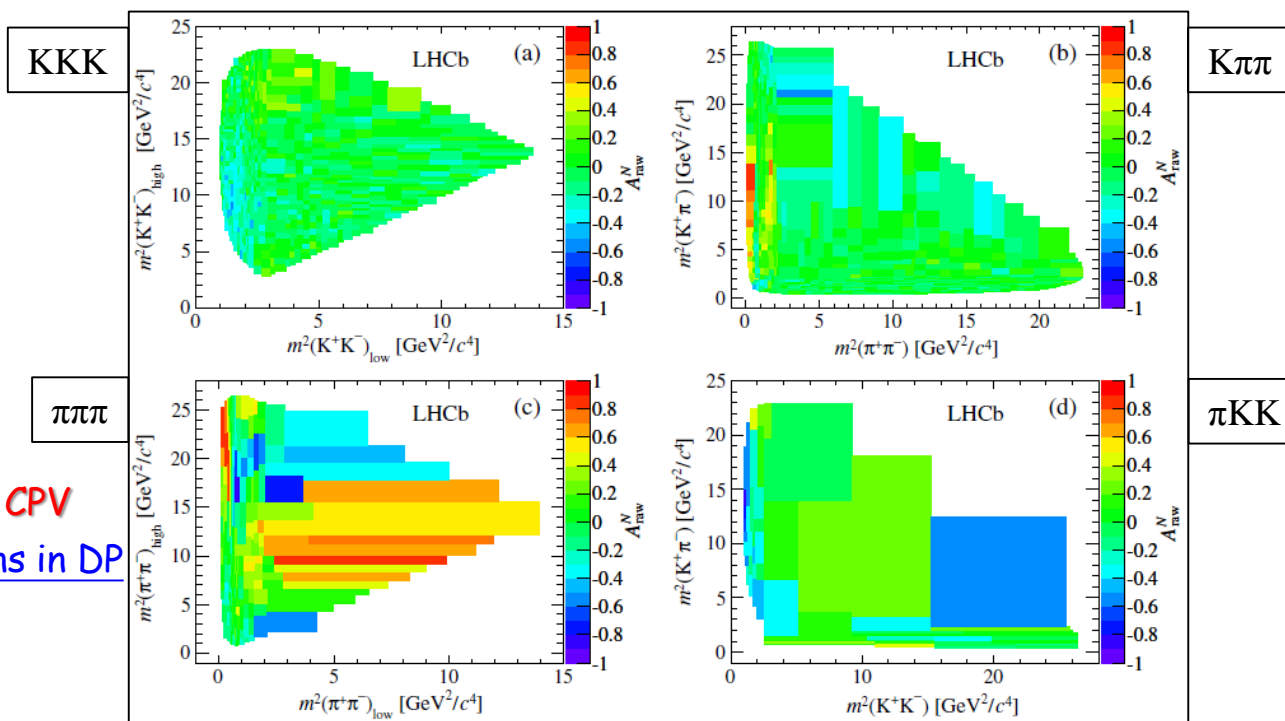
- “Indication for Large Rescatterings in Charmless Rare B Decays”
Chua, WSH, Yang, MPLA'03

→ 2004: DCPV in B Observed!

Belle*
BaBar

III. FSI: soft vs hard

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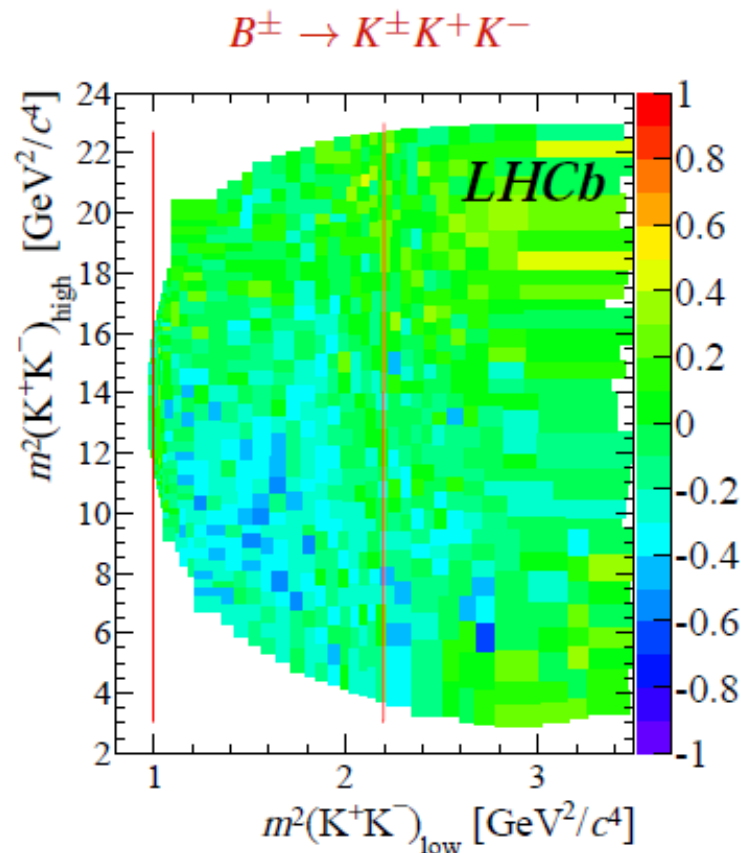
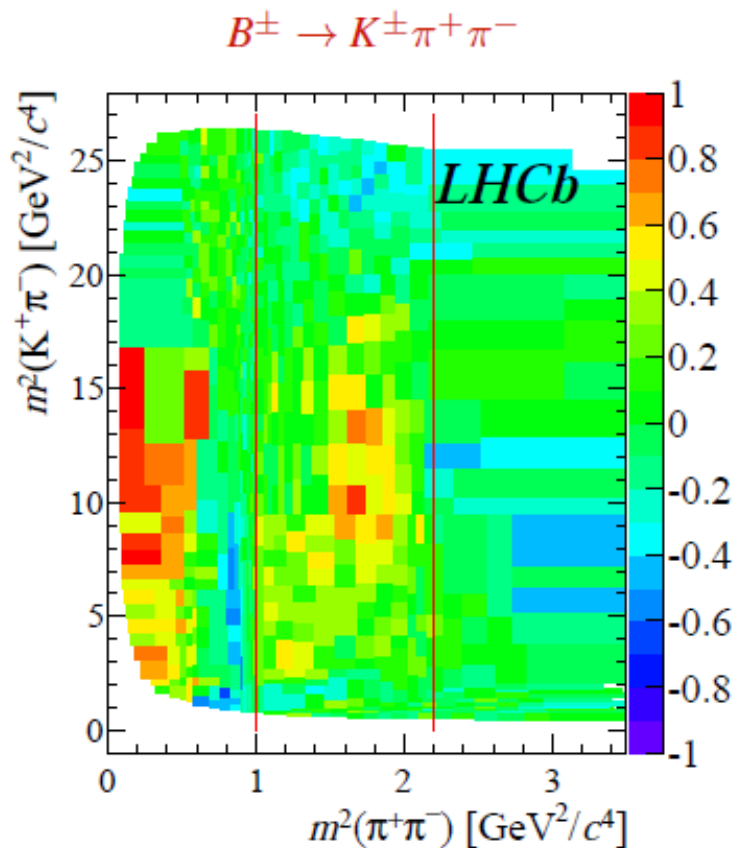


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“All the inelasticity of the $\pi\pi$ interaction goes into the KK channel”?

Not Quite.

$B^\pm \rightarrow K^\pm h^+ h^-$ charge asymmetries: a zoom at low $\pi^+\pi^-/K^+K^-$ mass



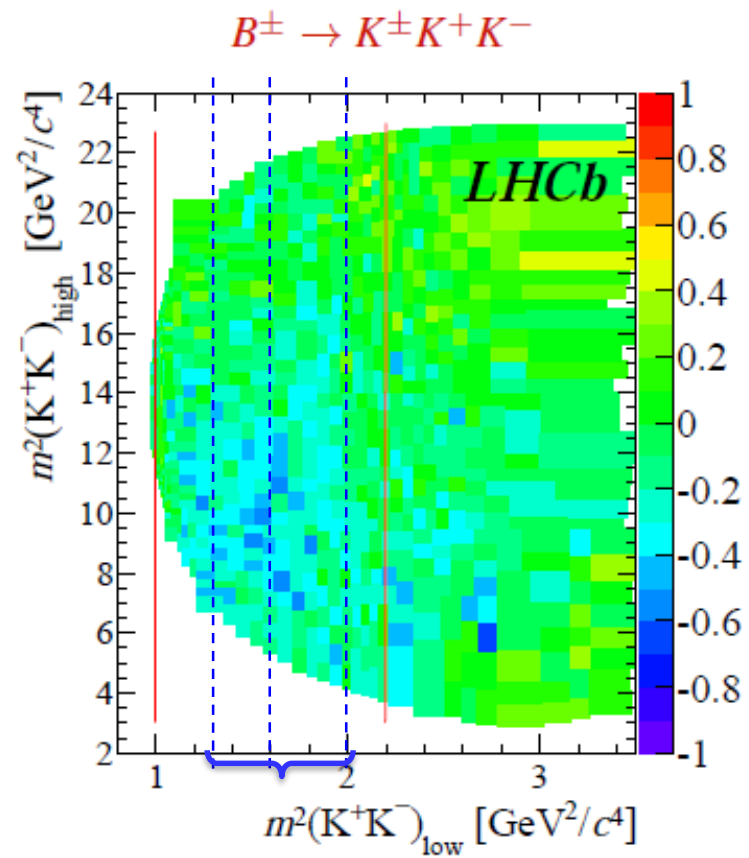
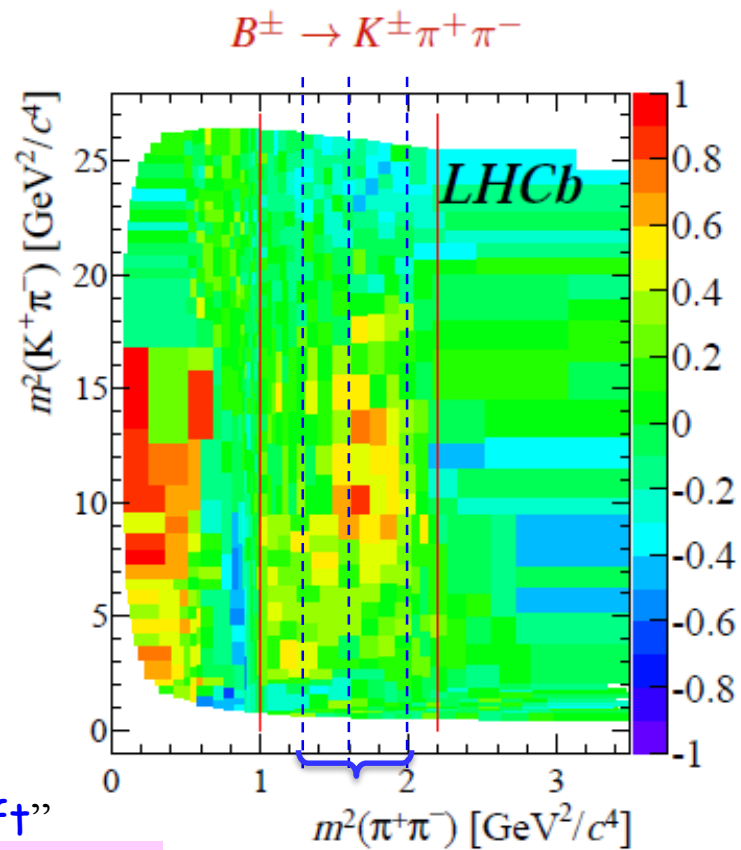
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Strong phase difference would come from $\pi\pi \rightleftharpoons KK$ rescattering.

Alberto dos Reis
@ Hadron 2015

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“soft”

KKnπ thresholds
 $n = 0, 1, 2, 3$

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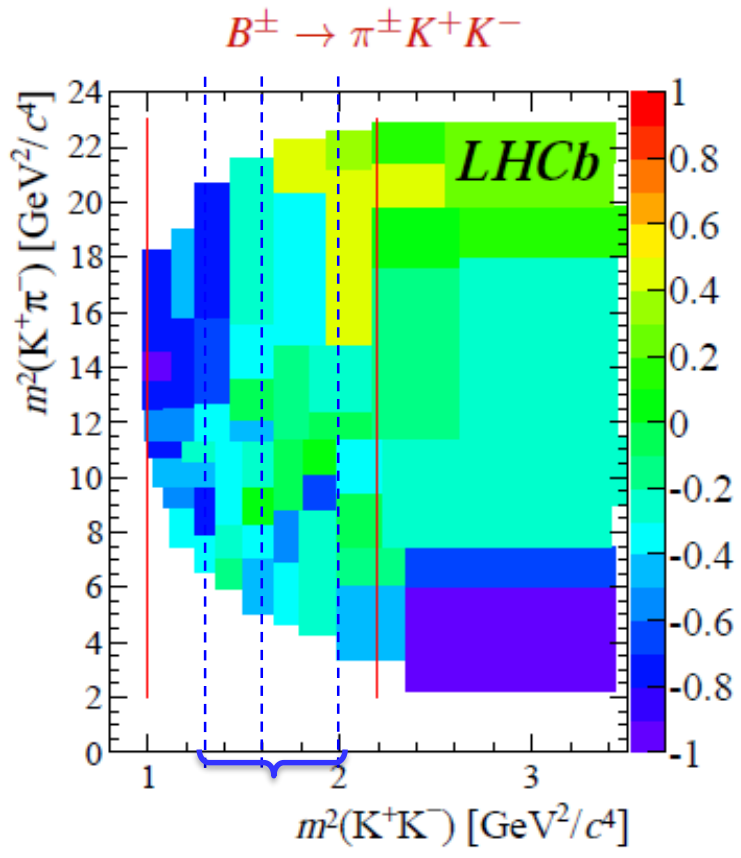
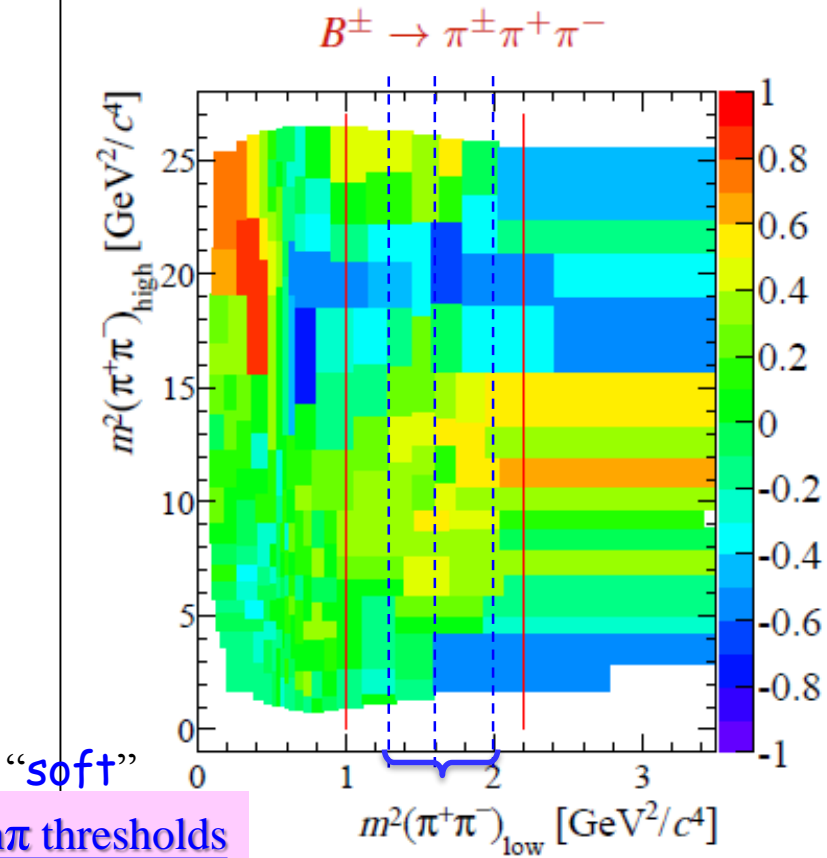
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10/27



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Similar effect in $B^\pm \rightarrow \pi^\pm h^+ h^-$ (more evident in $B^\pm \rightarrow \pi^\pm K^+ K^-$).

Alberto dos Reis
@ Hadron 2015

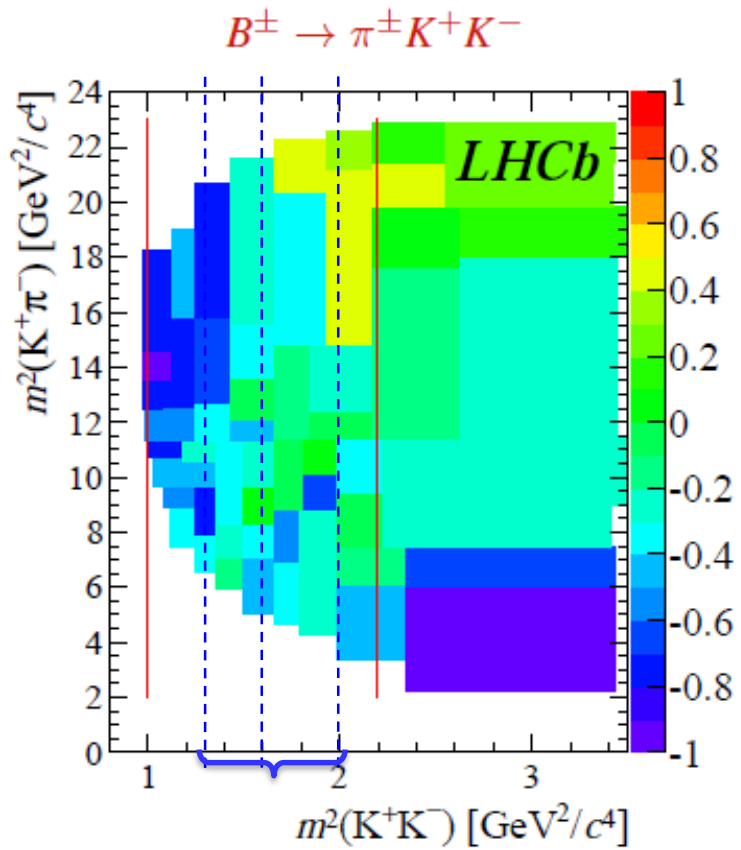
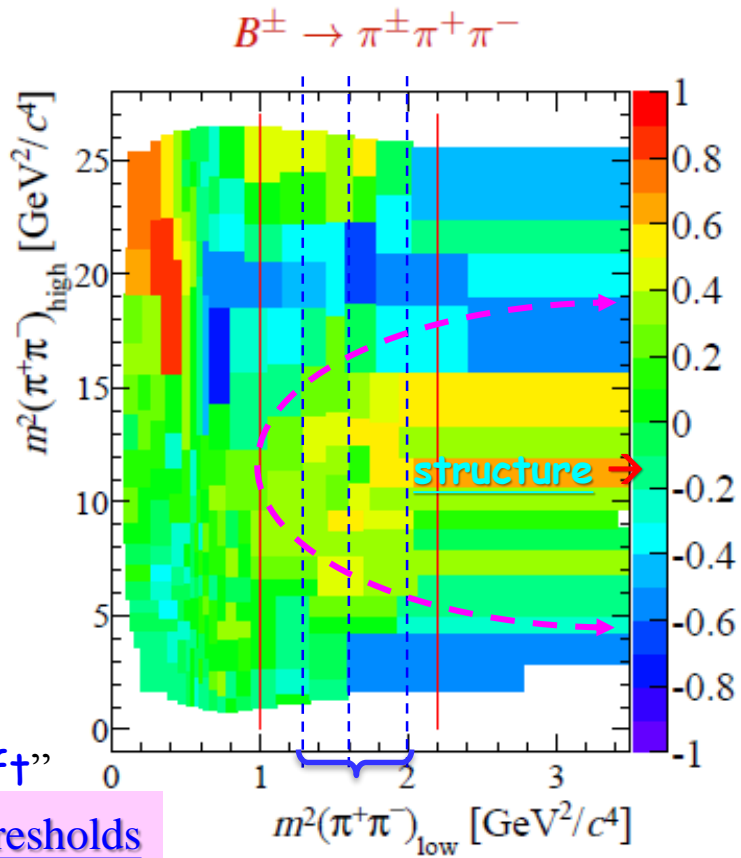
1/27

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structure \rightarrow



“soft”

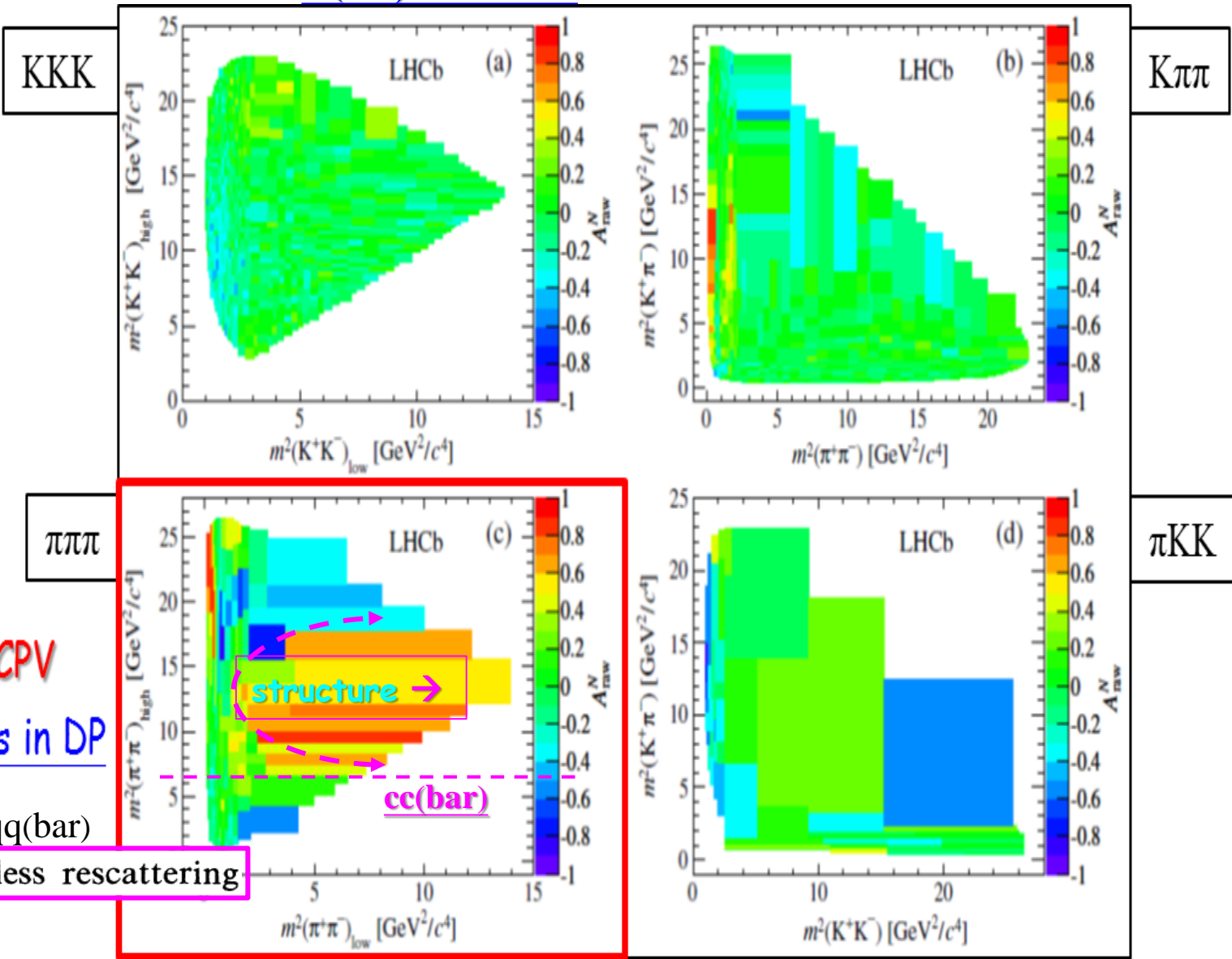
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“soft”: $K + n\pi \rightarrow K + n\pi$ rescattering
hard : $(D\bar{D} + X) \rightarrow$ charmless rescattering
cc(bar) – annihilate

LHCb 1408.5373 (PRD)



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hard: cc(bar) to qq(bar)
 $(D\bar{D} + X) \rightarrow$ charmless rescattering

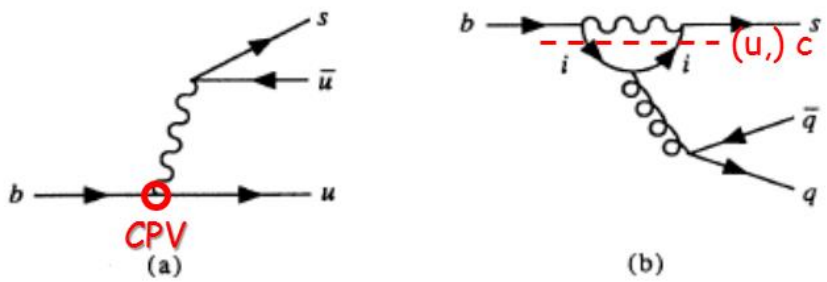
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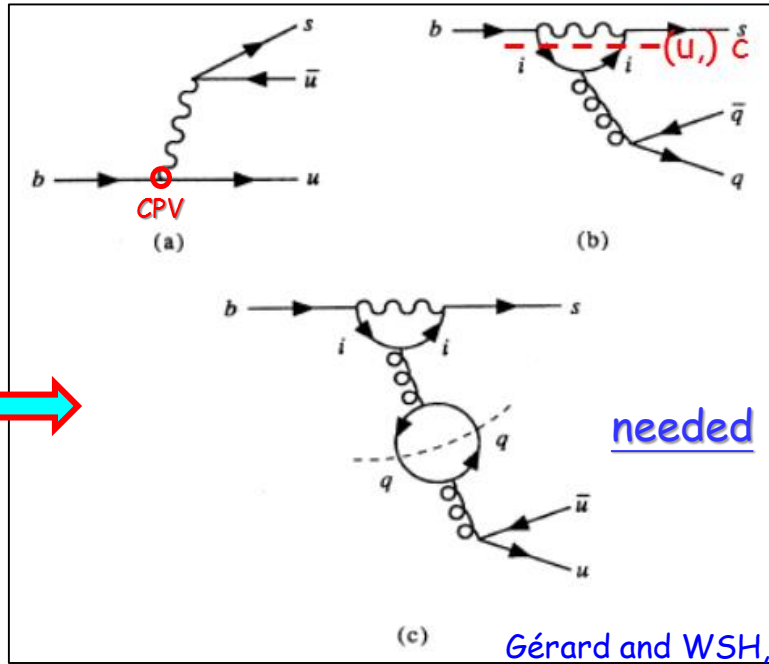
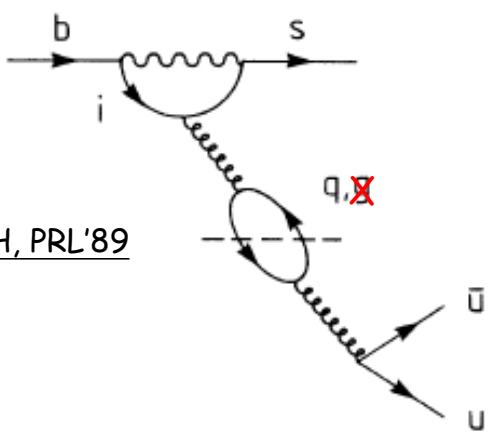
Unitarity/CPT at Quark Level



Bander, Silverman, Soni, PRL'79



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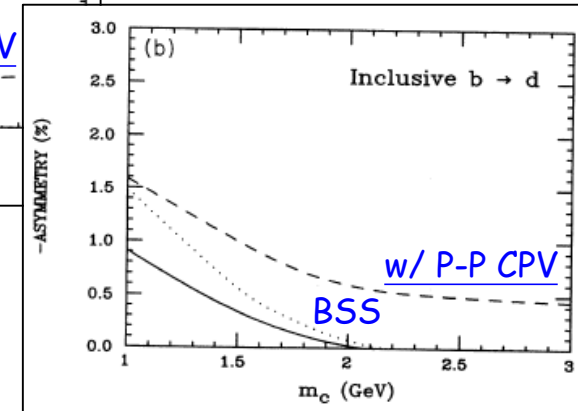
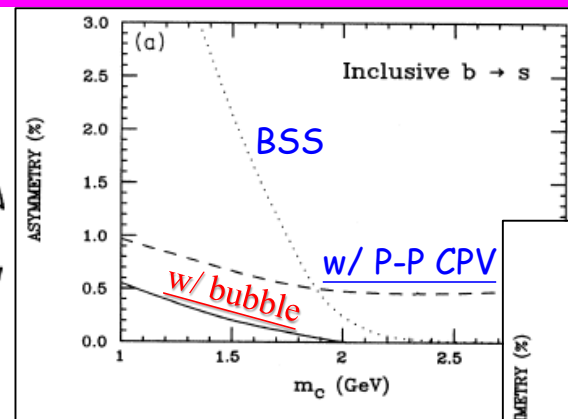
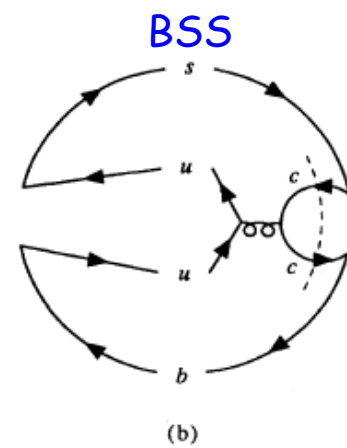
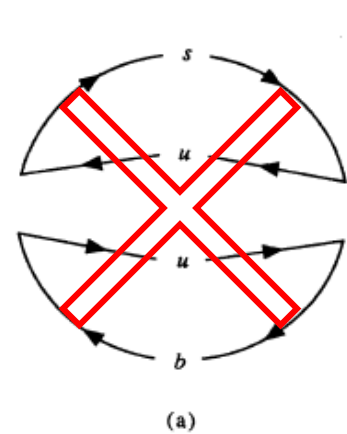
TABLE I. (Semi-)inclusive branching ratio B and asymmetries for $b \rightarrow s$ and $b \rightarrow d$ processes for $\rho = -0.5$, $\eta = 0.15$, and $m_t = M_W$. a_0 is with Figs. 1(a) and 1(b) only, while a is the result with Fig. 1(c) taken into account. The entry "0.0" stands for a very small positive number.

	B (%)	a_0 (%)	a (%)
$b \rightarrow su\bar{u}$	0.46	1.2	0.0
$b \rightarrow sd\bar{d} + ss\bar{s}$	0.54	0.5	0.5
<u>Total $b \rightarrow s$ (no charm)</u>	1.19	0.7	0.2
$b \rightarrow du\bar{u}$	0.71	-0.7	-0.0
$b \rightarrow dd\bar{d} + ds\bar{s}$	0.07	-4.2	-4.2
<u>Total $b \rightarrow d$ (no charm)</u>	0.80	-1.0	-0.4

Unitarity/CPT at Quark Level



inclusive $b \rightarrow s/d$ CPV should vanish for $2m_c > m_b$



Gérard and WSH, PRD'91

Purposed
Pure-P DCPV



CPT/Unitarity

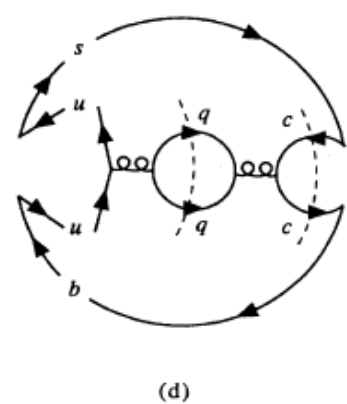
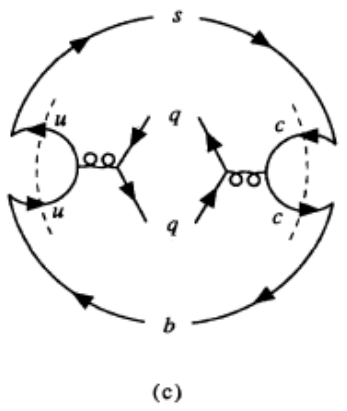


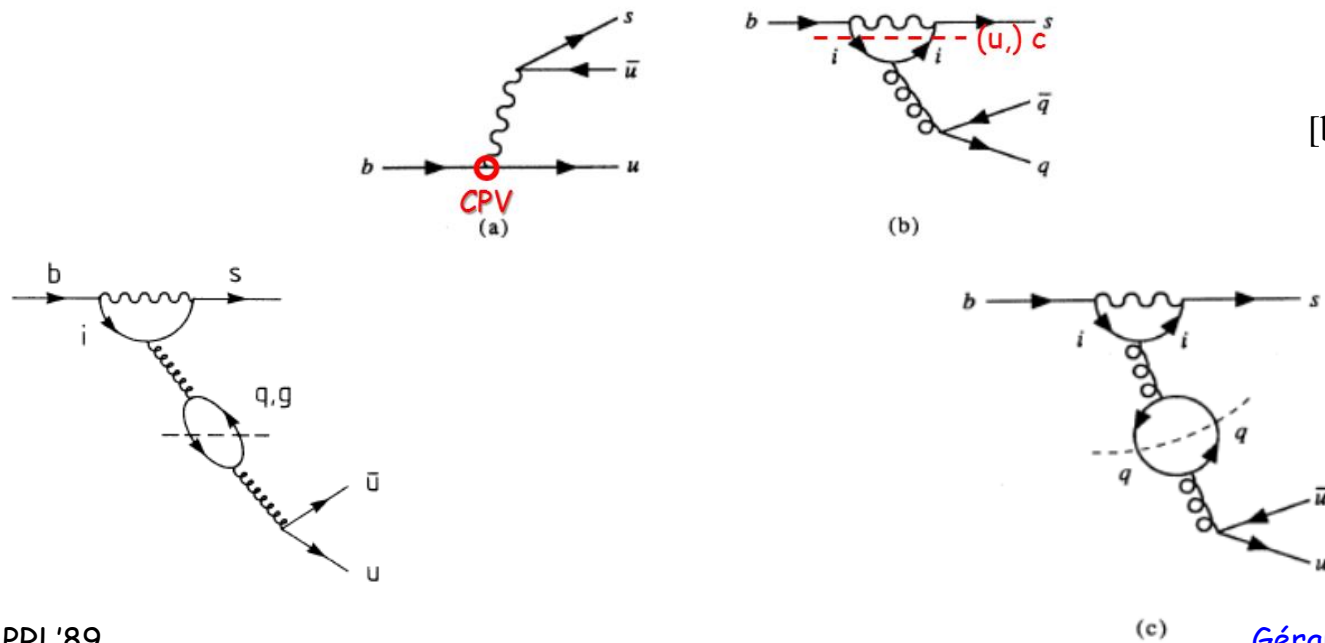
FIG. 3. Amplitude squared term-by-term analysis for BSS mechanism: (a) tree-tree interference ($b \rightarrow su\bar{u}$); (b) tree-penguin interference ($b \rightarrow su\bar{u}$); (c) penguin-penguin interference ($b \rightarrow sq\bar{q}$); and (d) tree-double-penguin interference.

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a 30-yr "Sum Rule"

inclusive $b \rightarrow s/d$ CPV sub-%: $2m_c$ threshold-suppress



[$b \rightarrow sgg$ absent]

Gérard and WSH, PRL'89

Gérard and WSH, PRD'91

TABLE I. Inclusive branching ratios (BR) and asymmetries for $b \rightarrow s$ and $b \rightarrow d$ processes for $\rho = -0.6$, $\eta = 0.25$, and $m_t = 60$ GeV. a_0 is with Fig. 1 only, while a is the result with Fig. 2 taken into account.

	BR (%)	a_0 (%)	a (%)
$b \rightarrow su\bar{u}$	0.53	1.8	-1.7
$b \rightarrow sd\bar{d} + ss\bar{s} + sgg$	1.44	0.8	0.8
Total $b \rightarrow s$ (no charm)	2.12	1.0	0.1
$b \rightarrow du\bar{u}$	1.23	-0.8	0.7
$b \rightarrow dd\bar{d} + ds\bar{s} + dgg$	0.19	-6.0	-6.0
Total $b \rightarrow d$ (no charm)	1.45	-1.5	-0.2

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Total $b \rightarrow s$ (no charm)	1.19	0.7	0.2
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LHCb 1408.5373 (PRD)

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Measurements of CP violation in the three-body phase space of charmless B^\pm decays

R. Aaij *et al.*^{*}
(LHCb Collaboration)
(Received 25 August 2014; published 11 December 2014)

The charmless three-body decay modes $B^\pm \rightarrow K^\pm \pi^+ \pi^-$, $B^\pm \rightarrow K^\pm K^+ K^-$, $B^\pm \rightarrow \pi^\pm K^+ K^-$ and $B^\pm \rightarrow \pi^\pm \pi^+ \pi^-$ are reconstructed using data, corresponding to an integrated luminosity of 3.0 fb^{-1} , collected by the LHCb detector. The inclusive CP asymmetries of these modes are measured to be

$A_{CP}(B^\pm \rightarrow K^\pm \pi^+ \pi^-) = +0.025 \pm 0.004 \pm 0.004 \pm 0.007,$	$+ 2.7 \pm 0.8\%$	} (PDG)
$A_{CP}(B^\pm \rightarrow K^\pm K^+ K^-) = -0.036 \pm 0.004 \pm 0.002 \pm 0.007,$	$- 3.3 \pm 0.8\%$	
$A_{CP}(B^\pm \rightarrow \pi^\pm \pi^+ \pi^-) = +0.058 \pm 0.008 \pm 0.009 \pm 0.007,$	$+ 5.7 \pm 1.3\%$	
$A_{CP}(B^\pm \rightarrow \pi^\pm K^+ K^-) = -0.123 \pm 0.017 \pm 0.012 \pm 0.007,$	$-12.2 \pm 2.1\%$	

where the first uncertainty is statistical, the second systematic, and the third is due to the CP asymmetry of the $B^\pm \rightarrow J/\psi K^\pm$ reference mode. The distributions of these asymmetries are also studied as functions of position in the Dalitz plot and suggest contributions from rescattering and resonance interference

$\left\{ \begin{array}{l} s \text{ } u\bar{d} \text{ } u\bar{d} \\ s \text{ } u\bar{s} \text{ } u\bar{s} \end{array} \right\}$
 $\left\{ \begin{array}{l} d \text{ } u\bar{d} \text{ } u\bar{d} \\ d \text{ } u\bar{s} \text{ } u\bar{s} \end{array} \right\}$

a Curiosity
0.3% ($b \rightarrow s$)
1.1% ($b \rightarrow d$)
sub-percent

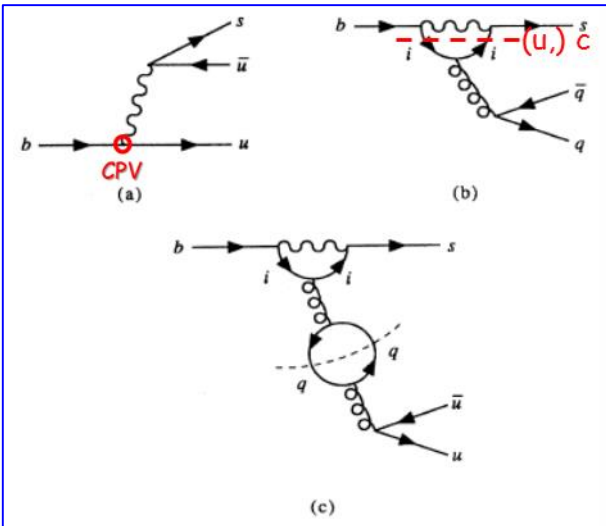


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Total $b \rightarrow d$ (no charm)	0.80	-1.0	-0.4

$\sim 0.12, 0.35$

Gérard and WSH, PRD'91

Improving the Inclusive DCPV Theory



- Interested theorists can try (a bit muddled/complicated).
- Need to consider $b \rightarrow sg$, known to be $\sim 0.5\%$ ($b \rightarrow sqq(\text{bar}) \sim 1\%$).
 - But “on-shell” gluon does not give much absorptive parts, how to incorporate?
 - In what part of “ $h^+h^-h^+$ ” Dalitz Plot does $b \rightarrow sg$ interfere with $b \rightarrow sqq(\text{bar})$?
- Near cancellation guaranteed by the strength of absorptive part of Penguin.
Interesting to see experimental development and further affirmation.

Greub and Linniger, PLB'00, PRD'01

WSH, NPB'88

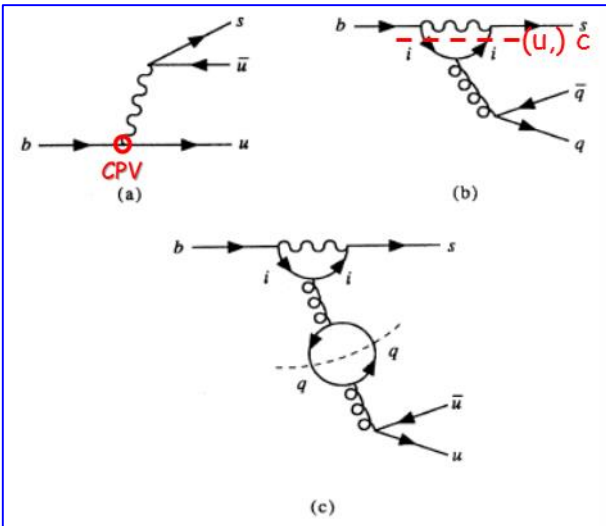


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Gérard and WSH, PRD'91

V. Conclusion



- From “CP violation in inclusive and exclusive charmless B decays”

sistently, we found the surprising result that $O(\alpha_s^2)$ contributions are as important as $O(\alpha_s)$ effects for individual semi-inclusive modes such as $b \rightarrow su\bar{u}$. These unexpected results were uncovered because we chose to study the rates and asymmetries of semi-inclusive charmless B decays, and we therefore had to pay better attention to general conditions such as unitarity and CPT.

Gérard and WSH, PRD'91

The upshot of our results is that the total inclusive charmless $b \rightarrow s$ and $b \rightarrow d$ decay asymmetries are rather suppressed. Nature seems to prefer hiding away the effects of CP violation, by one form of cancellation or another. In our case it is indeed a subtle one. The situa-

- LHCb'14 Observation of $B^+ \rightarrow h'^+ h^- h^+$ 3-body DCPV

- **Large CPV**, strongly varying across Darlitz Plot
- **Inclusive CPV** for $B^+ \rightarrow K^+ h^- h^+$ and $B^+ \rightarrow \pi^+ h^- h^+$ @ **sub%**



LHCb has affirmed 30-yr DCPV “Sum Rule”
and affirmed quark-hadron duality in
charmless 3-body B^+ decay CPV

