

New spectrum of negative-parity doubly charmed baryons

Mao-Jun Yan

Institute of Theoretical Physics, CAS
School of Physics, BUAA

Collaborators: Xiao-Hai Liu, Feng-Kun Guo, Sergi Gonzalez-Solis,
C. Hanhart, U.-G. Meißner & B.S. Zou.

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Doubly charmed baryon in observation

First observation of Ξ_{cc}^+ in $\Xi_{cc}^+ \rightarrow \Lambda_c^+ K^- \pi^+$

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Confirmation of $\Xi_{cc}^+(3520)$ via its decay to pD^+K^-

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Lattice calculation: $\Xi_{cc}(3610)(23)(22)$.

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Observation of $\Xi_{cc}^{++}(3621)$ in $\Lambda_c^+ K^- \pi^+ \pi^+$ mass spectrum

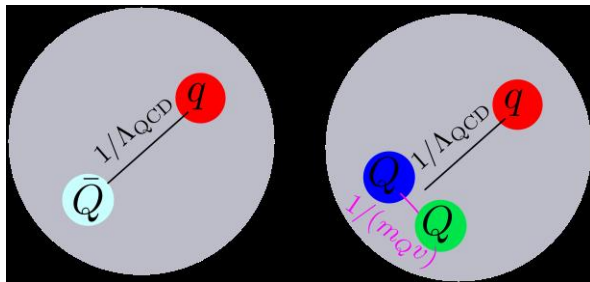
LHCb, PRL119(2017)

Heavy anti-quark-diquark symmetry

heavy quark is a static color (anti-)triplet in heavy meson.

$m_{QV} \gg \Lambda_{QCD}$, heavy diquark serves as a point-like color anti-triplet source, like a heavy anti-quark in heavy meson.

It relates doubly-heavy baryons to anti-heavy mesons.



Doubly charmed baryon with $J^P = \frac{1}{2}^-$

Following heavy anti-quark-diquark symmetry, there is a bridge between charmed mesons and doubly charmed baryons.

$D_{s0}^*(2317)$

$D_{s0}^*(2317)$ is understood as DK bound state mainly.

T. Barnes et al PRD68(2003); E.E. Kolomeitsev et al PLB582(2004) ; A. Faessler et al PRD76(2007); D. Gamermann et al PRD76(2007) ;F.K. Guo et al PLB(641)(2006), EPJ.A40(2009), PR D87 (2013); L.S. Geng et al PRD89(2014);

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Extended to doubly charmed baryon,

Prediction: $\Omega_{cc}(1/2^-)$ with mass $m_{\Xi_{cc}} + m_{D_{s0}^*(2317)} - m_D \approx 4.1\text{GeV}$.

While SU(3) multiplet calculated for GBs scattering off ground states of doubly charmed baryons.

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Does inner structure of heavy diquark contribute to spectrum?

Doubly charmed baryon with $J^P = \frac{1}{2}^-$

Size of doubly charmed baryon

$$r_d \approx 1/(m_Q v_Q) \approx 0.25 \text{ fm with } m_Q v_Q \approx 800 \text{ MeV}$$

$$r_q \approx 1/\Lambda_{QCD} \approx 0.8 \text{ fm with } \Lambda_{QCD} \approx 250 \text{ MeV.}$$

$$\frac{r_d}{r_q} \approx 0.3$$

Value of $m_Q v_Q$ is given in [J. Hu and T. Mehen PRD73,054003\(2006\)](#)

Spin structure in heavy diquark

$$\vec{J}_{QQ} = \vec{S}_{QQ} + \vec{L}_{QQ},$$

$$S_{QQ} = 1, L_{QQ} = 0 \text{ in ground state, } \mathcal{P}(+)$$

$$S_{QQ} = 0, L_{QQ} = 1 \text{ in P-wave excitation. } \mathcal{P}(-)$$

Doubly charmed baryon with $J^P = \frac{1}{2}^-$

Potential of P-wave excitation in heavy diquark:

$V^P(cc) = \frac{1}{2} V^P(c\bar{c})$ is predicted in quark model.

$$M_{\psi_{cc}^P} - M_{\psi_{cc}} \approx (M_{h_c} - M_{J/\psi})/2 = 214 \text{ MeV}.$$

T.Mehen PRD96 (2017)

Something new?

1. 214 MeV = $\mathcal{O}(m_\pi, m_K, m_\eta)$, P-wave excitation in heavy diquark should be a degree of freedom in spectrum of doubly charmed baryon. (s- and u- channel)
2. How to take these P-wave excitations in heavy diquark into consideration?

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$\psi_{cc}^P(\frac{1}{2}^-)$ couples to $\psi_{cc}\phi$ in S-wave

$$\mathcal{L}_P = \lambda \bar{\psi}_{cc}^P \gamma^\mu u_\mu \psi_{cc} + h.c.$$

This term breaks HQSS and λ is expected to be

$$\mathcal{O}(\Lambda_{QCD}/m_c) = \mathcal{O}(0.2) \ll 1 \quad \text{T. Mehen et al PRD73,054003(2006), PRD96,094028(2017)}$$

Doubly charmed baryon with $J^P = \frac{1}{2}^-$

$$V_s = \frac{2\lambda^2}{F^2} C^{(s)} \bar{u}^f(p_3, \sigma^f) \not{p}_4 \frac{1}{\not{p} - M_{\psi_{cc}^P}} \not{p}_2 u^i(p_1, \sigma^i),$$

Born terms in s-channels are considered and the contribution from u-channel Born terms is small.

$$\left(\begin{array}{cc} 2 & -\frac{2}{\sqrt{3}} \\ -\frac{2}{\sqrt{3}} & \frac{2}{3} \end{array} \right)_{I=0}, \quad \left(\begin{array}{ccc} \frac{3}{2} & \frac{1}{2} & \frac{\sqrt{6}}{2} \\ \frac{1}{2} & \frac{1}{6} & \frac{1}{\sqrt{6}} \\ \frac{\sqrt{6}}{2} & \frac{1}{\sqrt{6}} & 1 \end{array} \right)_{I=1/2}$$

$$I = 0: \Xi_{cc}\bar{K} - \Omega_{cc}\eta; \quad I = 1/2: \Xi_{cc}\pi - \Xi_{cc}\eta - \Omega_{cc}K$$

Doubly charmed baryon with $J^P = \frac{1}{2}^-$

The interactions in LO ChPT contain Weinberg-Tomozawa terms and Born terms with ground state of doubly charmed baryons exchanging.

$$\mathcal{L}_{LO} = \bar{\psi}_{cc}(\not{D} - m_0 + \frac{g_A}{2}\gamma^\mu\gamma_5 u_\mu)\psi_{cc}.$$

with

$$D_\mu = \partial_\mu + \frac{1}{2} \left[u^\dagger \partial_\mu u + u \partial_\mu u^\dagger \right], \quad u_\mu = iu^\dagger D_\mu U u^\dagger$$

The axial coupling constant g_A is estimated as, $|g_A| = 0.2$

Doubly charmed baryon with $J^P = \frac{1}{2}^-$

The ground-state doubly charmed baryons are expected to form a flavor triplet of matter fields,

$$\psi_{cc} = \begin{pmatrix} \Xi_{cc}^{++} \\ \Xi_{cc}^+ \\ \Omega_{cc}^+ \end{pmatrix}$$

The light pseudoscalar mesons (π, K, η) are the Goldstone bosons of QCD,

$$U = u^2 = e^{i\frac{\sqrt{2}\Phi}{F}}$$

with

$$\Phi = \begin{pmatrix} \frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta & \pi^+ & K^+ \\ \pi^- & -\frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta & K^0 \\ K^- & \bar{K}^0 & \frac{-2}{\sqrt{6}}\eta \end{pmatrix}$$

Doubly charmed baryon with $J^P = \frac{1}{2}^-$

NLO terms in ChPT:

$$V^{(2)}(s, t, u) = \frac{4C_0}{F^2}h_0 + \frac{2C_1}{F^2}h_1 - \frac{2C_{24}}{F^2} + \frac{2C_{35}}{F^2}H_{35}(s, t, u)$$

$$c_i = \frac{h_i}{2\bar{M}_D}, \quad i = 0, 1, 24, 35,$$

where $C_{24} = C_2 + C'_4$, $C_{35} = C_3 + C'_5$, $C'_4 = C_4\bar{M}_{\psi_{cc}}^2$ and $C'_5 = C_5\bar{M}_{\psi_{cc}}^2$. \bar{M}_D and $\bar{M}_{\psi_{cc}}$ are the averaged masses of the ground state charmed mesons and doubly charmed baryons, respectively.

Values of h_i have been fixed from fitting results of lattice calculation.

L. Liu et al PRD 87,014508(2013)

Bethe-Salpeter equation with on-shell approximation

$$T = (1 - V \cdot G)^{-1} V,$$

where $V = V_{WT} + V_s + V^{(2)}$. V_s is contribution from baryon exchanging with P-wave excitation in heavy diquark.

Neglecting u-channels in Born terms of ground states and excitation states exchanging, contribution of which has been checked and is small.

F-K Guo et al PLB641,278(2006); D.-L. Yao et al EPJC78,310(2018)

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$$M_{\Xi_{cc}^{++}} = 3621.4 \text{ MeV}$$

$$M_{\Omega_{cc}^+} - M_{\Xi_{cc}^+} = M_{D_s^+} - M_{D^+}$$

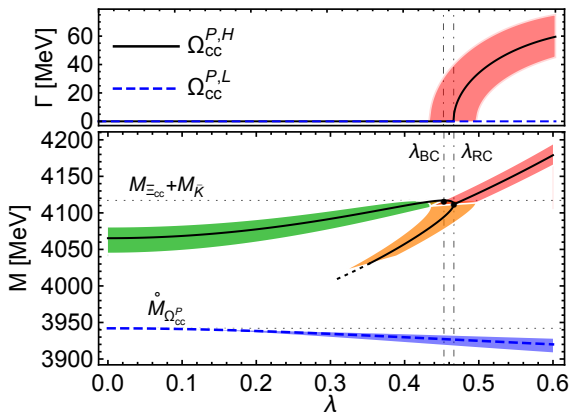
$$M_{\Xi_{cc}^P} = 3838 \text{ MeV, bare pole } (\frac{1}{2}^-) \text{ in quark model.}$$

D.Ebert et al PRD 66,014008(2002)

$$M_{\Omega_{cc}^P} \approx M_{\Omega_{cc}} + 217 \text{ MeV} \approx 3942 \text{ MeV.}$$

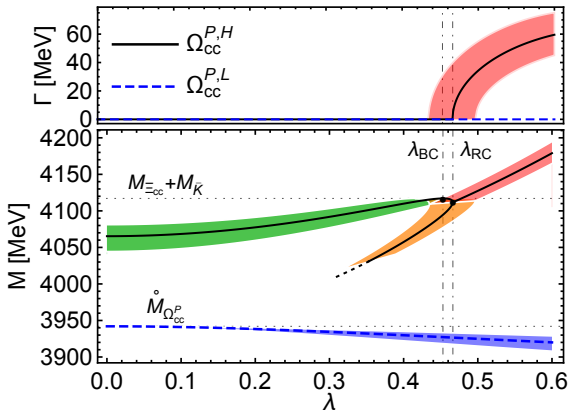
Doubly charmed baryon with $J^P = \frac{1}{2}^-$

Sector $I=0, S=-1$, $\Xi_{cc}\bar{K}-\Omega_{cc}\eta$. Thresholds: 4120 MeV and 4273 MeV.



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Sector $I=0, S=-1$, $\Xi_{cc}\bar{K}-\Omega_{cc}\eta$. Thresholds: 4120 MeV and 4273 MeV.



Compositeness: $P = -g^2 \frac{\partial G}{\partial s} \Big|_{s=M_{pole}^2}$.

The higher pole contains 55-80 % of $\Xi_{cc}\bar{K}$.

Doubly charmed baryon with $J^P = \frac{1}{2}^-$

Study on isospin violated decay width is a good way to understand hadronic structure. Mass differences of intermediate particles in loops in particle basis and $\pi^0 - \eta$ mixing contribute to decay width.

$\pi^0 - \eta$ mixing

$$\begin{aligned}\tilde{\pi}^0 &= \pi^0 \cos\epsilon_{\pi^0\eta} + \eta \sin\epsilon_{\pi^0\eta}, \\ \tilde{\eta} &= -\pi^0 \sin\epsilon_{\pi^0\eta} + \eta \cos\epsilon_{\pi^0\eta}.\end{aligned}$$

where

$$\epsilon_{\pi^0\eta} = \frac{\sqrt{3}}{4} \frac{m_d - m_u}{m_s - \hat{m}}$$

with $\hat{m} = (m_u + m_d)/2$, $\frac{m_d - m_u}{m_s - \hat{m}} = 0.012 \pm 0.001$

F.K. Guo et al PLB66(2008)

Sector $I=0, S=-1$, $\Xi_{cc}\bar{K}-\Omega_{cc}\eta-\Omega_{cc}\pi^0$

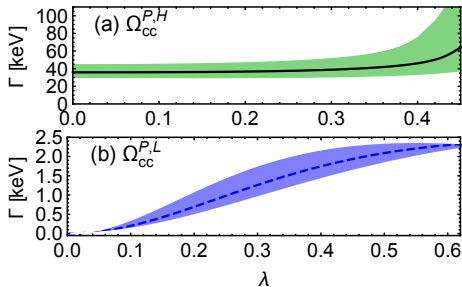


Figure: Decay width of Isospin violated process

Decay width of the lower pole is a few keV and the one of the higher pole is larger than 30 keV.

Doubly charmed baryon with $J^P = \frac{1}{2}^-$

Sector $I=1/2, S=0, \Xi_{cc}\pi - \Xi_{cc}\eta - \Omega_{cc}K$

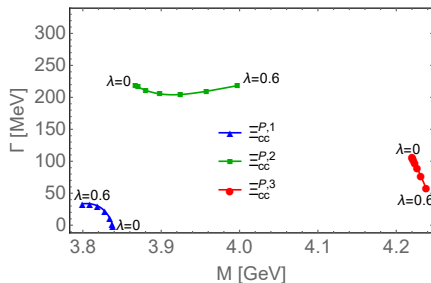


Figure: Trajectories of the three resonant poles in the $(S, I) = (0, 1/2)$ channel vary with λ value. Central values of LECs and $a^{\psi_{cc}\phi}$ are adopted, and $M_{\Xi_{cc}^P} = 3838$ MeV is used.

Thresholds: 3762 MeV, 4176 MeV and 4222 MeV.

- Analogue of DK hadronic molecule $D_{s0}^*(2317)$: Possibility of two narrow doubly charmed baryons with $J^P = \frac{1}{2}^-$, the lower one corresponds to the normal ccs baryon, while the higher pole to the $\Xi_{cc}\bar{K}$ hadronic molecule.
- The LECs up to NLO are correlated to those for heavy meson-GBs interactions via HADS, the latter ones have been widely studied and fixed by lattice simulation.
- Difference: there is an additional s-channel pole contribution.
- Other analogues: $J^P = \frac{1}{2}^-$, $\frac{3}{2}^-$ doubly heavy baryons.

Thanks

NLO terms in chiral Lagrangian and low energy constants read

$$T^{(2)}(s, t, u) = \frac{4C_0}{F^2} h_0 + \frac{2C_1}{F^2} h_1 - \frac{2C_{24}}{F^2} + \frac{2C_{35}}{F^2} H_{35}(s, t, u) \quad (1)$$

with

$$H_{24}(s, t, u) = 2h_2 p_2 \cdot p_4 + h_4(p_1 \cdot p_2 p_3 \cdot p_4 + p_1 \cdot p_4 p_2 \cdot p_3) \quad (2)$$

$$H_{35}(s, t, u) = h_3 p_2 \cdot p_4 + h_5(p_1 \cdot p_2 p_3 \cdot p_4 + p_1 \cdot p_4 p_2 \cdot p_3) \quad (3)$$

G contains a subtraction, $a(1\text{GeV}) = -2.79_{-0.05}^{+0.04}$.

Matching the value of G at threshold with a regularization of three momentum cut-off, $q_{\max} \approx m_\rho$.

Here one makes an analogy to the case of $D_{s0}^*(2317)$ bounded from DK. But the contributions from $m_d - m_u$ and electromagnetic term (virtual photons) go in opposite directions.

$D_s(2317)$

$$(M_{D^+} - M_{D^0})^{strong} = (2.67 \pm 0.30) \text{ MeV},$$

$$(M_{D^+} - M_{D^0})^{em} = (2.10 \pm 0.32) \text{ MeV}$$

Ξ_{cc}

$$(M_{\Xi_{cc}^{++}} - M_{\Xi_{cc}^+})^{strong} = (-2.7 \pm 1.5) \text{ MeV},$$

$$(M_{\Xi_{cc}^{++}} - M_{\Xi_{cc}^+})^{em} = (4.2 \pm 2.30) \text{ MeV}$$