The EicC project in China

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On behalf of the EicC Discussion Group

08/20/2019, Hadron 2019 Guilin, China

Outline

Introduction

polarized Electron ion collider in China (EicC)

> Physics programs in EicC

PDFs, TMDs, GPDs, Proton Mass,

pi/K structure function, Hadron Spectroscopy

Current status



Introduction

 QCD is successful (in general). More than 90% of visible matter in nature governed by strong interaction QCD.



• Exploring the internal structure of the nucleon is one path.

Introduction

- How to explore the internal structure of the nucleon?
 - spin of nucleon
 - > 3D structure

> ...

mass of nucleon



 Electron Ion Collider (EIC), regarded as a "super electron microscope", can provide the clearest image inside the nucleon.



Facilities Landscape



High Intensity heavy-ion Accelerator Facility (HIAF)



EicC accelerator complex overview



Machine Kinematics



EicC, Vs : 15 ~ 20 GeV

- Focus on nuclear physics
- B-quark hadron production



Location of HIAF and EicC



2004年11月

Spin of the Proton



1980s

1



Only ~30% of the proton spin from the quark spin, based on experiments.



now

$$\frac{1}{2} = S_q + L_q + S_g + L_g \qquad S_q \sim 30\% S_p \ ^{[1]} \quad L_q < 70\% S_p \ ^{[2,3]}$$
$$S_q (Q^2) = \frac{1}{2} \int_0^1 \Delta \Sigma(x, Q^2) dx \equiv \frac{1}{2} \int_0^1 \left(\Delta u + \Delta \bar{u} + \Delta d + \Delta \bar{d} + \Delta s + \Delta \bar{s} \right) (x, Q^2) dx$$

[1] EMC, J. Ashman et al., Phys. Lett. B206, 364 (1988).
 [2] Lattice: P. Hagler, Phys. Rept. 490, 49 (2010)
 [3] Lattice: Yi-Bo Yang, R. Sufian, et. A., PRL118, 042001(2017)
 [4] EPJA52, 268 (2016), arXiv: 1212.1701
 [5] D. Florian, PRL 113, 012001 (2014)

- [6] STAR NPA932, 500(2014),1404.5134
- [7] PHENIX PRD90, 012007(2014), 1402.6296
- [8] COMPASS PLB690, 466(2010), 1001.4654
- [9] X. Ji, J. Zhang, and Y. Zhao, PRL111 112002 (2013)

The Longitudinal Spin of the Nucleon



The Longitudinal Spin of the Nucleon



3D Structure of Nucleons – TMDs & GPDs

In Quantum Dynamics, a known particle's full state is $\psi(\vec{x}, \vec{k}, t)$. In particle physics, the spatial dimension along the energy transfer direction (i.e., Z-axis) is ignored due to the relativistic effect. Also at t=0, it is a 5D space.



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Transverse Momentum Dependent Functions (TMDs)



A.Kotzinian, Nucl. Phys. B441, 234 (1995). Bacchetta, Diehl, Goeke, Metz, Mulders and Schlegel JHEP 0702:093 (2007)

SIDIS Observables



SIDIS: Detect scattered electrons and produced single-hadron in the final state.

Measuring different hadrons, as flavor-tagger to probe the internal quark structure of nucleons.

- perform multidimensional
 analyses to disentangle all the
 relevant kinematical dependencies
- provide hadron identification to access the parton flavor
- Iarge and uniform acceptance
- with high luminosity.

EicC projections on Sivers



Generalized Parton Distributions (GPDs)



> GPDs encode information about the spatial distribution of partons inside a hadron,

correlated with their distribution in longitudinal momentum.

> GPD is related to quark angular momentum.

Ji's sum rule ^[1]
$$J^{f}(Q^{2}) = \frac{1}{2} \lim_{t \to 0} \int_{-1}^{1} dx \ x \left[H^{f}(x,\xi,t,Q^{2}) + E^{f}(x,\xi,t,Q^{2}) \right],$$

> Exclusive reactions, such as DVCS or DVMP, can get access to GPDs.

[1] X.-D. Ji, Phys. Rev. Lett. 78 (1997) 610.

Probe GPD via DVCS

- > Detect the scattered electron, real photon and nucleon.
- Absolute Cross Section:

$$\frac{d\sigma}{dQ^2 dx_B dt d\phi} \propto \left| \tau_{DVCS} \right|^2 + I + \left| \tau_{BH} \right|^2$$

$$\tau_{DVCS} \propto \int_{-1}^{+1} \frac{H(x,\xi,t)}{x\pm\xi\mp i\varepsilon} dx = P \int_{-1}^{+1} \frac{H(x,\xi,t)}{x\pm\xi} dx - i\pi H(\pm\xi,\xi,t),$$

Asymmetries with polarized target and/or polarized beam:

$$A = \frac{I}{|\tau_{DVCS}|^{2} + I + |\tau_{BH}|^{2}} = \frac{\sigma^{+} - \sigma^{-}}{\sigma^{+} + \sigma^{-}}$$

 $\sigma^{+/-}$: Beam or/and Target Polarization.



Polarization	Asymmetries	CFFs	
Longitudinal Beam	A _{LU}	$Im\{\boldsymbol{\mathcal{H}}_{p}, \widetilde{\mathcal{H}}_{p}, \mathcal{E}_{p}\}$ $Im\{\boldsymbol{\mathcal{H}}_{n}, \widetilde{\mathcal{H}}_{n}, \mathcal{E}_{n}\}$	
Longitudinal Target	A _{UL}	$Im\{\boldsymbol{\mathcal{H}}_{p}, \boldsymbol{\widetilde{\mathcal{H}}}_{p}, \}$ $Im\{\boldsymbol{\mathcal{H}}_{n}, \boldsymbol{\mathcal{E}}_{n}, \boldsymbol{\tilde{\mathcal{E}}}_{n}\}$	
Long. Beam + Long. Target	A _{LL}	$Re\{\boldsymbol{\mathcal{H}}_{p}, \boldsymbol{\widetilde{\mathcal{H}}}_{p}, \}$ $Re\{\boldsymbol{\mathcal{H}}_{n}, \boldsymbol{\mathcal{E}}_{n}, \boldsymbol{\widetilde{\mathcal{E}}}_{n}\}$	
Transverse Target	A _{UT}	$Im\{\boldsymbol{\mathcal{H}}_{p}, \boldsymbol{\mathcal{E}}_{p}\}$ $Im\{\boldsymbol{\mathcal{H}}_{n}\}$	
Long. Beam +Trans.Targt	A _{LT}	$Re\{\boldsymbol{\mathcal{H}}_{p}, \boldsymbol{\mathcal{E}}_{p}\}$ $Re\{\boldsymbol{\mathcal{H}}_{n}\}$	

GPD -- EicC Projections



Proton Mass



b: related to quarkonium-proton scattering amplitude $M_{\psi p}$ near-threshold

[1] X. Ji, PRL 74, 1071 (1995) & PRD 52, 271 (1995)

Other interesting topics



EicC detector conceptual design



EicC Status









4 pre-Collaboration meetings up to now.

Discussions on: physics programs, simulations accelerator, detector.

EicC white paper

- 1. Chinese Version by the end of 2019,
- 2. English Version by the middle of 2020.

Electron Ion Collider in China

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Summary

- **EicC** has been proposed based on the HIAF facility.
 - -- polarized electron beam (3.5 GeV)
 - -- polarized proton beam (20 GeV)/ion beam (20 GeV/u)
- High precision measurements for 1D (helicity), 3D (TMDs/GPDs) nucleon structure study with flavor separation in the valence and sea quark dominated region.
- > Other interesting physics topics will be delivered as well, not mentioned here in details.

Welcome to join us! EicC@impcas.ac.cn

Thank You

EicC detector requirements



~ 8 charged + ~ 8 neutrals

Scattering electron distributions



Final state hadrons



EicC detector requirements



3D Structure of Nucleons

> Probe TMD using SIDIS

Leading Twist TMDs		Quark Polarization			тм	Ds	Quark Polarization			
		Unpolarized (U)	Longitudinally Polarized (L)	Transversely Polarized (T)	^{via} SIDIS		Unpolarized (U)	Longitudinally Polarized (L)	Transversely Polarized (T)	
-	υ	$f_1(x,k_T^2)$ • Unpolarized		$h_1^{\perp}(x,k_T^2)$ Boer-Mulders	_	υ	$\begin{array}{c} F_{UU} \\ \propto f_1 \otimes D_1 \\ \\ \text{Unpolarized} \end{array}$		$F_{UU}^{\cos(2\phi_h)} \propto h_1^{\perp} \bigotimes H_1^{\perp}$ Boer-Mulders	
Nucleon Polarizatior	L		$g_1(x,k_T^2) \xrightarrow[Helicity]{ \bullet \bullet$	$h_{1L}^{\perp}(x,k_T^2) \xrightarrow[Long-Transversity]{} \cdot \cdot$	larizatior	L		$A_{LL} \propto g_1 \bigotimes D_1$ Helicity	$A_{UL}^{\sin(2\phi_h)} \propto h_{1L}^{\perp} \otimes H_1^{\perp}$ Long-Transversity	
	т	$f_{1T}^{\perp}(x,k_T^2)$ $f_{1T}(x,k_T^2)$ $f_{1T}(x,k_T^2)$ $f_{1T}(x,k_T^2)$ $f_{1T}(x,k_T^2)$	$g_{1T}(x,k_T^2)$ - d Trans-Helicity	$h_{1}(x,k_{T}^{2}) \textcircled{\bullet}_{Transversity}^{\bullet} - \underbrace{\bullet}_{Transversity}^{\bullet}$ $h_{1T}^{\perp}(x,k_{T}^{2}) \textcircled{\bullet}_{Pretzelosity}^{\bullet} - \underbrace{\bullet}_{Pretzelosity}^{\bullet}$	Nucleon Po	т	$\begin{array}{c} A_{UT}^{\sin(\phi_h - \phi_S)} \\ \propto f_{1T}^{\perp} \otimes D_1 \\ \\ \text{Sivers} \end{array}$	$A_{LT}^{\cos(\phi_h-\phi_S)} \propto g_{1T} \otimes D_1$ Trans-Helicity	$\begin{array}{l} A_{UT}^{\sin(\phi_{h}+\phi_{S})} \propto h_{1} \otimes H_{1}^{\perp} \\ & Transversity \\ A_{UT}^{\sin(3\phi_{h}-\phi_{S})} \propto h_{1T}^{\perp} \otimes H_{1}^{\perp} \\ & Pretzelosity \end{array}$	

> Fragmentation Functions (FF):
 D₁→Unpolarized FF, H[⊥]₁ → Collins FF
 < Describe the process of the struck quark fragmenting into a hadron
 < Can be obtained from (e + e⁻ → h[±] + X) data (e.g., BELLE)

Present status of TMDs extraction



Transverse Momentum Dependent Parton Distributions

$$\frac{d\sigma}{dxdydzd_{2r}^{2}d\phi_{n}d\psi} = \left[\frac{\alpha}{x_{2}Q^{2}} \frac{y^{2}}{2(1-\varepsilon)} \left(1+\frac{y^{2}}{2x}\right)\right] \times \left(F_{UU,T} + \varepsilon F_{UU,L}\right) \times \left(\frac{1+\cos\varphi_{h} \times \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\sin\varphi_{h}} + \cos(2\varphi_{h}) \times \varepsilon A_{UU}^{\cos(2\varphi_{h})} + A_{UU}^{\sin(2\varphi_{h})}\right) + \frac{1+\varepsilon}{2\varepsilon(1-\varepsilon)} A_{UU}^{\sin\varphi_{h}} + \frac{1+\varepsilon}{2\varepsilon(1-\varepsilon)} + \frac{1+\varepsilon}{2\varepsilon(1-\varepsilon)} A_{UU}^{\sin\varphi_{h}} + \frac{1+\varepsilon}{2\varepsilon(1-\varepsilon)} + \frac{1+\varepsilon}{$$

A.Kotzinian, Nucl. Phys. B441, 234 (1995). Bacchetta, Diehl, Goeke, Metz, Mulders and Schlegel JHEP 0702:093 (2007)

With recent progresses in [5, 6] it is possible to calculate the TMD parton distributions with Lattice QCD.

Transverse Momentum Dependent Parton Distributions



Generalized Parton Distributions (GPDs)

Eight GPDs for quarks or gluons



- $x \rightarrow$ Longitudinal quark momentum fraction (not experimental accessible)
- $\xi \rightarrow$ Longitudinal momentum transfer. In Bjorken limit: $\xi = x_B/(2-x_B)$ ٠
- $t \rightarrow$ Total squared momentum transfer to the nucleon: $t = (P-P')^2$ ٠ mentum

$$J^{q} = \frac{1}{2} \int dx \, x \left[H^{q}(x,\xi,t=0) + E^{q}(x,\xi,t=0) \right]$$

X.-D. Ji, Phys. Rev. Lett. 78 (1997) 610.



The plot shows the kinematic coverage of DVCS measurement on US-EIC and that on EicC. EicC would be a perfect machine to coverage the sea quark domain.

The projection of relative statistic uncertainties at different bins of high Q^2 on EicC, with the integrated luminosity = 50 fb⁻¹. HERMES data are shown with the relative statistical errors divided by a factor of 10.



The invariant kinematical variable distribution of DVCS+BH on EicC. The binning strategy is shown in the figures below.



The projection of relative statistic uncertainties at different bins on EicC, with the integrated luminosity = 50 fb⁻¹.



HIAF Timetable



EicC 总体规划



20 GeV, C: 1347 m Polarized proton

德国-HERA: 国际首台 EIC 装置



		Lepton	Proton
Energy	GeV	27.5	920
Intensities	mA	60	180x10 ¹¹
Magnetic field	Т	0.15	1.5
Acc. voltage	MV	130	2
e-polarization	%	50 to 70	

Final luminosity (1.5 to 5)x10³¹ cm⁻²s⁻¹

A Ring-Ring (polarized) Lepton-Proton collider with 320 GeV CM energy

- 1981 Proposal
- 1984 Start construction
- 1991 Commissioning, first Collisions
- 1992 Start Operations for H1 and ZEUS,
- →1st exciting results with low luminosity
 1994 Install East Spin Rotators
- → Longitudinal polarized leptons for HERMES
 1996 Install 4th Interaction region for HERA-B
 1999 High Luminosity Run with electrons
 2000 High efficient luminosity production:100 /pb/y
 2001 Install luminosity upgrade, Spin Rotators for H1 and ZEUS
 2003 Longitudinal polarization in high energy collisions
 2007 End of a highly successful program



美国-BNL: eRHIC





		1.0.1	Diele Balaissatien			
	Nominal Design			Risk Mitigation		
	(with cooling)			(no cooling)		
Species	р	e		р	E	
Bunch frequency [MHz]	11	2.6		56.	3	
Bunch intensity [10^11]	0.6 1.5			1.05	3.0	
Number of bunches	13	20		660)	
Beam current [A]	1	2.5		0.87	2.5	
Rms norm. emit. h/v [um]	2.7/0.38	391/20		4.1/2.5	391/95	
Rms emittance h/v [nm]	9.2/1.3	20/1		13.9/8.5	20/4.9	
β* h/v [cm]	90/4	42/5		90/5.9	63/10.4	
IP rms beam size h/v [um]	91,	7.2		112/22.5		
IR rms angular spread h/v [urad]	Ingular spread h/v [urad] 101/179 219/143 ameter (/IP) h/v 0.013/0.007 0.064/0.099 nch length [cm] 5 1.9 ergy spread, 10^-4 4.6 5.5 ace charge parameter 0.004 neglig.			124/380	179/216	
b-b parameter (/IP) h/v			0.015/0.005		0.1/0.083	
Rms bunch length [cm]				7	1.9	
Rms energy spread, 10^-4				6.6	5.5	
Max space charge parameter				0.001	neglig.	
IBS growth time tr/long, h	2.1/2.0			9.2/10.1		
Polarization, %	80	70		80	70	
Hourglass and crab crossing factor	0.87			0.85		
Peak luminosity [10^33 cm-2s-1]	10.1			4.4		
Integrated luminosity/week, fb ⁻¹	4.51			1.12		

电子环方案: ERL, NS-FFAG 质心能量: 255GeV/p + 15.9GeV/e √S=126GeV 设计亮度: 4.4×10³³ cm⁻²s⁻¹ - 无冷却 1.0×10³⁴ cm⁻²s⁻¹-冷却 工程计划: 2022-2025之间开建

美国-JLab: JLEIC



美国-JLab: JLEIC



Present baseline: Ring-Ring

- Energy: 3-12 GeV e on 20-100 GeV p or up 40 GeV/u ion
- Polarized light ions (p, d, ³He), unpolarized ions up to A=200 (Au, Pb)
- New ion complex & two collider rings
- Up to 3 interaction points
- High polarization for both beams
- Conventional electron cooling
- Upgradable to 20 GeV electron, 250 GeV proton or 100 GeV/u ion

电子环方案: "8"字型环
质心能量: 60-100GeV p + 3-12 GeV e
设计亮度: 5.6×10 ³³ cm ⁻² s ⁻¹ 1.4×10 ³⁴ cm ⁻² s ⁻¹
工程计划: 2022-2025方案设计

CERN: LHeC



10 ³⁴ cm ⁻² s ⁻¹ Luminosity reach		PROTONS	ELECTRONS
Beam Energy	GeV	7000	60
Luminosity	10 ³³ cm ⁻² s ⁻¹	16	16
Normalized emittance ge _{x,y}	mm	2.5	20
Beta Funtion b [*] _{x,y}	m	0.05	0.10
rms Beam size s [*] _{x,y}	mm	4	4
Beam Current	mA	1112	25
Bunch Spacing	Ns	25	25
Bunch Population	10 ⁹	2.2*10 ¹¹	4*10 ⁹
Bunch charge	nC	35	0.64

电子环方案: ERL circulator Ring 质心能量: 7 TeV p + 60 GeV e 设计亮度: 1.6×10³⁴ cm⁻²s⁻¹ 工程计划: 2025-2035 方案设计

国际EIC研究目标



The Longitudinal Spin of the Nucleon



Lattice: P. Hagler, Phys. Rept. 490, 49 (2010), arXiv:0912.5483.

$$T^{\mu\nu} = \frac{1}{2}\bar{\psi}i\overleftrightarrow{D}^{(\mu}\gamma^{\nu)}\psi + \frac{1}{4}g^{\mu\nu}F^2 - F^{\mu\alpha}F^{\nu}_{\ \alpha},$$

First of all, let me decompose the $T^{\mu\nu}$ into traceless and trace parts,

$$T^{\mu\nu} = \bar{T}^{\mu\nu} + \hat{T}^{\mu\nu},\tag{7}$$

where $\bar{T}^{\mu\nu}$ is traceless. According to Eq. (4), I have,

$$\langle P|\bar{T}^{\mu\nu}|P\rangle = (P^{\mu}P^{\mu} - \frac{1}{4}M^2g^{\mu\nu})/M,$$
(8)

$$\langle P|\hat{T}^{\mu\nu}|P\rangle = \frac{1}{4}g^{\mu\nu}M.$$
(9)

Combining Eq. (6) with the above three equations, I get,

$$\langle \bar{T}^{00} \rangle = \frac{3}{4}M,\tag{10}$$

$$\langle \hat{T}^{00} \rangle = \frac{1}{4} M. \tag{11}$$

Thus 3/4 of the nucleon mass comes from the traceless part of the energy-momentum tensor and 1/4 from the trace part. The magic number 4 is just the space-time dimension. This

The traceless part of the energy-momentum tensor can be decomposed into the contribution from the quark and gluon parts,

$$\bar{T}_{q}^{\mu\nu} = \bar{T}_{q}^{\mu\nu} + \bar{T}_{g}^{\mu\nu}, \qquad (12)$$
$$\bar{T}_{q}^{00} = \frac{3}{4} a(\mu^{2}) M, \\\bar{T}_{g}^{00} = \frac{3}{4} (1 - a(\mu^{2})) M.$$

Finally, I turn to the trace part of the energy-momentum tensor $\hat{T}^{\mu\nu}$. According to Eq. (5), I decompose it into $\hat{T}^{\mu\nu}_{m}$ and $\hat{T}^{\mu\nu}_{a}$, the mass term and trace anomaly term, respectively. Both operators are finite and scale independent. If I define,

$$b = 4 \langle \hat{T}_m^{00} \rangle / M, \tag{20}$$

then according to Eq. (11), the anomaly part contributes,

$$\langle \hat{T}_{a}^{00} \rangle = \frac{1}{4} (1-b) M.$$
 (21)

Thus, the energy-momentum tensor $T^{\mu\nu}$ can be separated into four gauge-invariant parts, $\bar{T}_{q}^{\mu\nu}$, $\bar{T}_{g}^{\mu\nu}$, $\hat{T}_{m}^{\mu\nu}$, and $\hat{T}_{a}^{\mu\nu}$. They contribute, respectively, 3a/4, 3(1-a)/4, b/4, and (1-b)/4 fractions of the nucleon mass. The corresponding breakdown for the hamiltonian is, $H_{\rm QCD} = H'_q + H_g + H'_m + H_a$, with

$$\begin{split} H'_q &= \int d^3 \vec{x} \; \left[\bar{\psi} (-i \mathbf{D} \cdot \alpha) \psi + \frac{3}{4} \bar{\psi} m \psi \right], \\ H_g &= \int d^3 \vec{x} \; \frac{1}{2} (\mathbf{E}^2 + \mathbf{B}^2), \\ H'_m &= \int d^3 \vec{x} \; \frac{1}{4} \bar{\psi} m \psi, \\ H_a &= \int d^3 \vec{x} \; \frac{9 \alpha_s}{16 \pi} (\mathbf{E}^2 - \mathbf{B}^2). \end{split}$$

$$H_q = \int d^3 \vec{x} \ \bar{\psi}(-i\mathbf{D} \cdot \alpha)\psi,$$
$$H_m = \int d^3 \vec{x} \ \bar{\psi}m\psi,$$

then the QCD hamiltonian becomes,

$$H_{\rm QCD} = H_q + H_m + H_g + H_a.$$

Here H_q (Eq. (26)) represents the quark and antiquark kinetic and potential energies and contributes 3(a - b)/4 fraction of the nucleon mass. H_m (Eq. (27)) is the quark mass term and contributes b fraction of the mass. H_g (Eq. (23)) is the normal part of the gluon energy and contributes 3(1 - a)/4 fraction of the mass. Finally, H_a (Eq. (25)) is the gluon energy from the trace anomaly. It contributes (1 - b)/4 fraction of the mass.

$$\begin{aligned} \frac{d\sigma}{dx \, dy \, d\psi \, dz \, d\phi_h \, dP_{h\perp}^2} & \text{TMD} \\ &= \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2}\right) \\ &\times \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos \phi_h F_{UU}^{\cos \phi_h} + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} \right. \\ &+ \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin \phi_h F_{LU}^{\sin \phi_h} + S_{\parallel} \left[\sqrt{2\varepsilon(1+\varepsilon)} \sin \phi_h F_{UL}^{\sin \phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] \\ &+ S_{\parallel} \lambda_e \left[\sqrt{1-\varepsilon^2} F_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \phi_h F_{LL}^{\cos \phi_h} \right] \\ &+ |S_{\perp}| \left[\sin(\phi_h - \phi_S) \left(F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} \right. \\ &+ \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} + \sqrt{2\varepsilon(1+\varepsilon)} \sin \phi_S F_{UT}^{\sin \phi_S} \\ &+ \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \phi_S F_{LT}^{\cos \phi_S} \\ &+ \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \right\}, \end{aligned}$$

One particular example is the quark bution will be azimuthally asymmetric in the Sivers function $f_{1T}^{\perp q}$ which describes the transverse momentum space in a transversely transverse momentum distribution corre- polarized nucleon. Figure 2.13 demonstrates lated with the transverse polarization vector the deformations of the up and down quark of the nucleon. As a result, the quark distri- distributions. There is strong evidence of the

change of (infinitely many) gluons between cess can be measured at RHIC. the active struck quark and the remnants of

Sivers effect in the DIS experiments observed the target, which is referred to as final state by the HERMES, COMPASS, and JLab Hall interaction effects in DIS. On the other hand. A collaborations [71, [72, [73]. An important for the Drell-Yan lepton pair production proaspect of the Sivers functions that has been cess, it is due to the initial state interaction revealed theoretically in last few years is the effects. As a consequence, the quark Sivers process dependence and the color gauge in- and Boer-Mulders functions differ by a sign variance [74, [75, [76], [77]. Together with the in these two processes. This non-universality Boer-Mulders function, they are denoted as is a fundamental prediction from the gauge naive time-reversal odd (T-odd) functions. invariance of QCD [75]. The experimental In SIDIS, where a leading hadron is detected check of this sign change is currently one of in coincidence with the scattered lepton, the the outstanding topics in hadronic physics, quark Sivers function arises due to the ex- and Sivers functions from the Drell-Yan pro-



The Longitudinal Spin of the Nucleon

$$\frac{1}{2} = S_q + L_q + S_g + L_g$$

$$\Delta f(x, Q^2) \equiv f^+(x, Q^2) - f^-(x, Q^2) \qquad f = u, d, s, \bar{u}, \bar{d}, \bar{s}, g$$

$$S_q(Q^2) = \frac{1}{2} \int_0^1 \Delta \Sigma(x, Q^2) dx \equiv \frac{1}{2} \int_0^1 (\Delta u + \Delta \bar{u} + \Delta d + \Delta \bar{d} + \Delta s + \Delta \bar{s}) (x, Q^2) dx$$

$$\frac{1}{2} \left[\frac{d^2 \sigma^{\neq 2}}{dx \, dQ^2} - \frac{d^2 \sigma^{\neq}}{dx \, dQ^2} \right] \simeq \frac{4\pi \, \alpha^2}{Q^4} y (2 - y) \, g_1(x, Q^2)$$

$$g_1(x, Q^2) = \frac{1}{2} \sum e_q^2 \left[\Delta q(x, Q^2) + \Delta \bar{q}(x, Q^2) \right]$$

Lattice: P. Hagler, Phys. Rept. 490, 49 (2010), arXiv:0912.5483.

10

 Q^2 (GeV²)

 10^{2}

