

Semileptonic and leptonic charm decays at BESIII

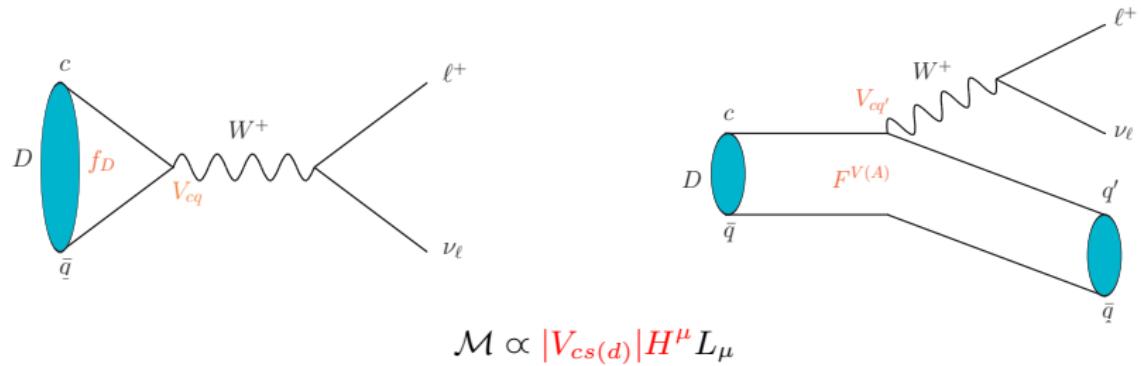
Yue Wang (on behalf of the BESIII collaboration)

University of Science and Technology of China

HADRON 2019, Guilin, China, August 16-21, 2019



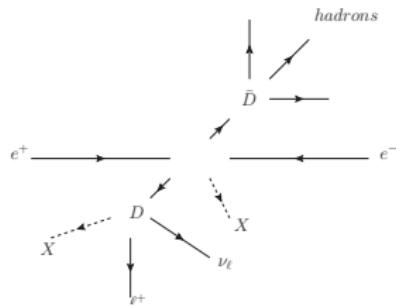
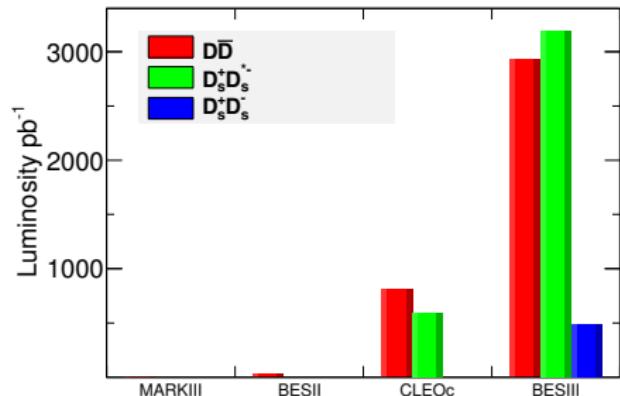
Motivation



- test the unitarity of quark mixing matrix and search for new physics.
- test the theoretical calculation on decay constants and form factors, especially LQCD.
- test the lepton flavor universality.
- help to understand the internal structure of light scalar mesons.
- measure the semileptonic Λ_c^+ decays.

$D^0(+)$ _(@3.773 GeV) and D_s^+ _(@4.18 and 4.01 GeV) data set at BESIII

Pair production at threshold, high efficiency and very low background.



The number of signal events is determined by examining the kinematic variables of the missing neutrino

$$\mathcal{B}_{sig} = \frac{N_{DT}^i}{N_{ST}^i \epsilon_{DT}^i / \epsilon_{ST}^i}$$

$\epsilon_{ST/DT}^i$: The efficiency of ST/DT

$\mathcal{B}_{ST/DT}^i$: The BF of ST/DT

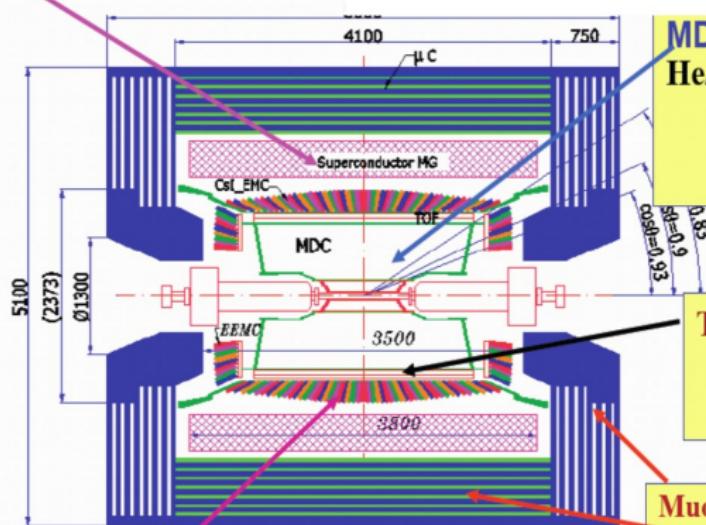
$$U_{\text{miss}} = E_{\text{miss}} - |\vec{p}|_{\text{miss}}$$

$$M_{\text{miss}}^2 = E_{\text{miss}}^2 - |\vec{p}|_{\text{miss}}^2$$

BESIII

Nucl. Instr. Meth. A614, 345 (2010)

Magnet: 1 T Super conducting



EMC: CsI crystal, 28 cm
 $\Delta E/E = 2.5\% @ 1 \text{ GeV}$
 $\sigma_z = 0.6 \text{ cm}/\sqrt{\text{E}}$

Data Acquisition:
Event rate = 4 kHz
Total data volume ~ 50 MB/s

MDC: small cell & Gas:
He/C₃H₈ (60/40), 43 layers
 $\sigma_{xy} = 130 \mu\text{m}$
 $\sigma_p/p = 0.5\% @ 1 \text{ GeV}$
 $dE/dx = 6\%$

TOF:
 $\sigma_t = 100 \text{ ps}$ Barrel
 110 ps Endcap

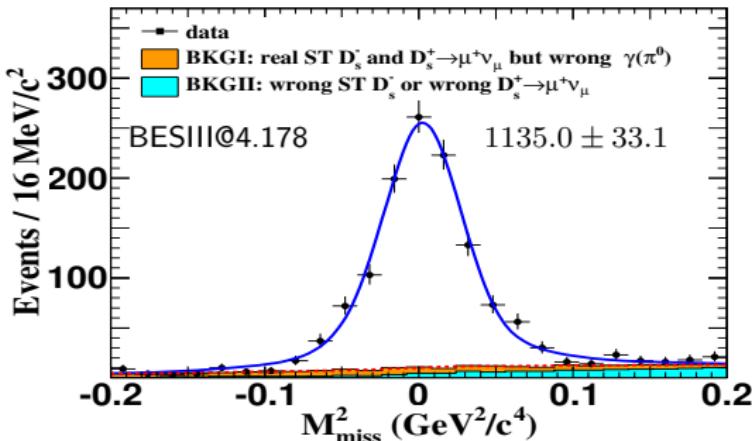
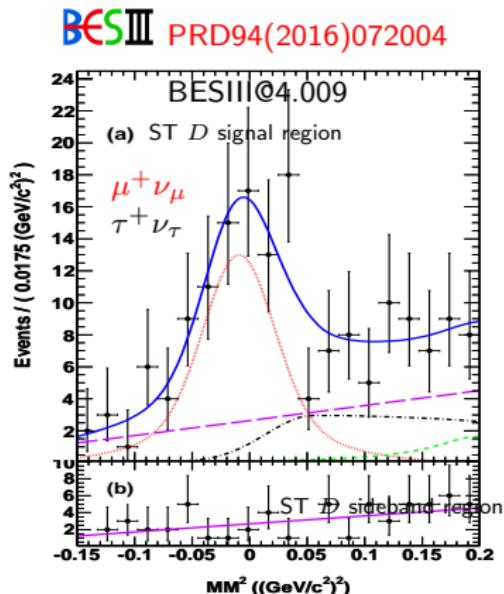
Muon ID: 9 layers RPC
8 layers for endcap

60 ps for ETOF after
upgraded in 2015

D_s^+ leptonic decays

$$\Gamma(D_s^+ \rightarrow \ell^+ \nu_\ell) = \frac{G_F^2}{8\pi} |V_{cs}|^2 f_{D_s^+}^2 m_\ell^2 m_{D_s^+} (1 - \frac{m_\ell^2}{m_{D_s^+}^2})^2$$

BESIII PRL122(2019)071802



$$\mathcal{B}(D_s^+ \rightarrow \mu^+ \nu_\mu) = (5.49 \pm 0.16 \pm 0.15) \times 10^{-3}$$

$$f_{D_s^+} |V_{cs}| = 246.2 \pm 3.6 \pm 3.5 \text{ MeV}$$

$$R_{D_s^+} = \frac{\Gamma(D_s^+ \rightarrow \tau^+ \nu_\tau)}{\Gamma(D_s^+ \rightarrow \mu^+ \nu_\mu)} = 9.98 \pm 0.52$$

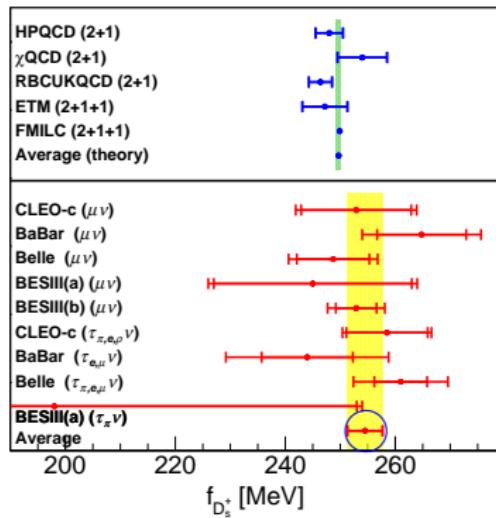
SM prediction 9.74 ± 0.01 .

Comparison of $|V_{cs}|$ and $f_{D_s^+}$

Inputs:

PDG2018 from CKM unitarity:

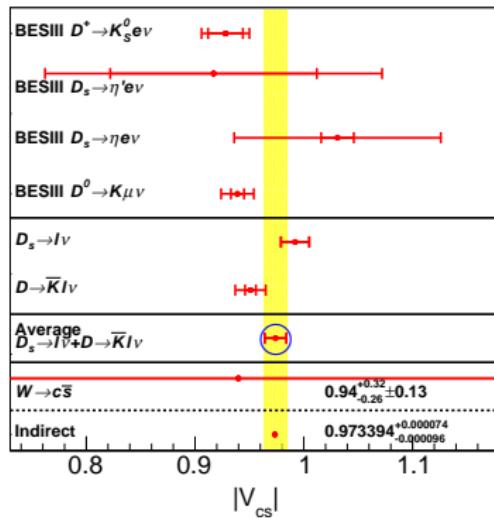
$$|V_{cs}| = 0.97359^{+0.00010}_{-0.00011}$$



LQCD average:

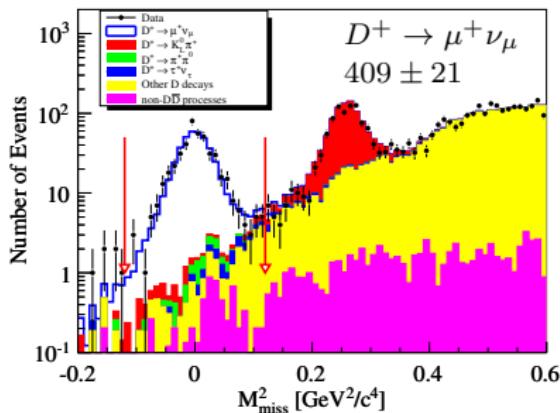
$$f_{D_s^+}^{\text{LQCD}} = 249.7 \pm 0.4 \text{ MeV}$$

$$f_+^{D \rightarrow K(0)} \text{LQCD} = 0.760 \pm 0.011$$



D^+ leptonic decays

BESIII PRD89(2014)051104

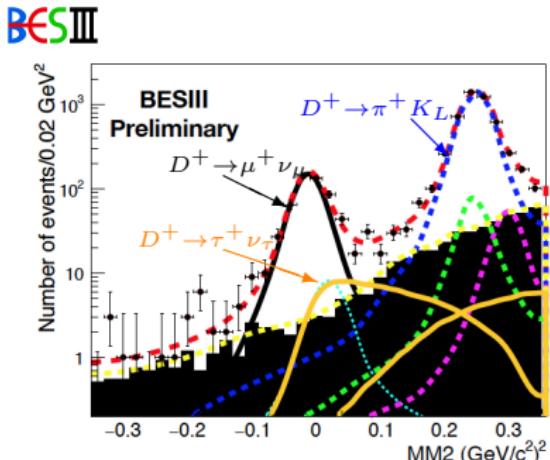


$$\mathcal{B}(D^+ \rightarrow \mu^+ \nu_\mu) = (3.71 \pm 0.19 \pm 0.06) \times 10^{-4}$$

$$f_{D^+} |V_{cd}| = 45.75 \pm 1.20 \pm 0.39 \text{ MeV}$$

$$R_{D^+} = \frac{\Gamma(D^+ \rightarrow \tau^+ \nu_\tau)}{\Gamma(D^+ \rightarrow \mu^+ \nu_\mu)} = 3.21 \pm 0.64$$

Consistent



$$\mathcal{B}(D^+ \rightarrow \tau^+ \nu_\tau) = (1.20 \pm 0.24_{\text{stat}}) \times 10^{-3}$$

$$f_{D^+} |V_{cd}| = 50.4 \pm 5.0_{\text{stat}} \text{ MeV}$$

First evidence with 4σ statistical significance.

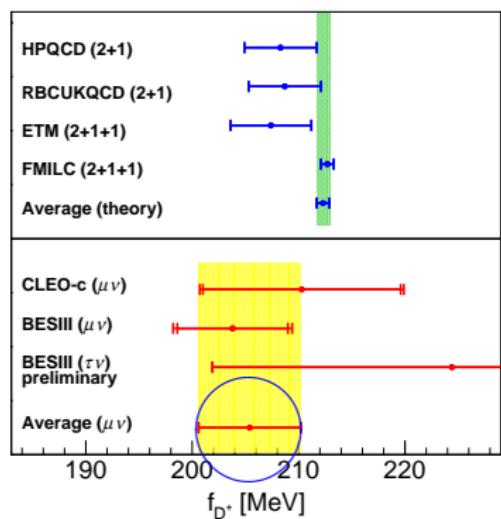
SM prediction 2.66 ± 0.01 .

Comparison of $|V_{cd}|$ and f_{D^+}

Inputs:

PDG2018 from CKM unitarity:

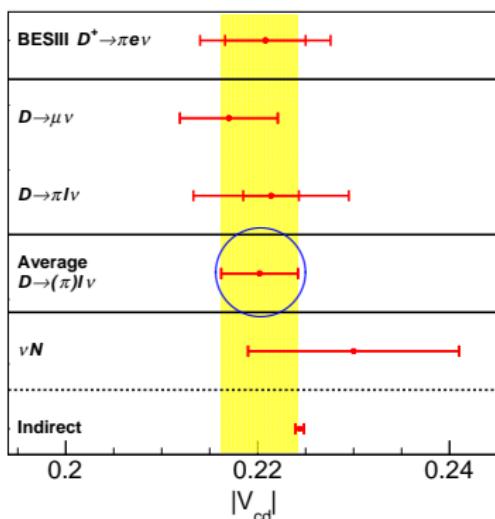
$$|V_{cd}| = 0.22438 \pm 0.00044$$



LQCD average:

$$f_{D^+}^{\text{LQCD}} = 212.3 \pm 0.6 \text{ MeV}$$

$$f_+^{D \rightarrow \pi}(0)^{\text{LQCD}} = 0.634 \pm 0.015$$



Dynamic study of $D^0 \rightarrow K^-(\pi^-)e^+\nu_e$

$$\langle P(p_2)|V^\mu|D(p_1)\rangle = f_+(q^2)[P^\mu - \frac{M_1^2 - M_2^2}{q^2}q^\mu] + f_0(q^2)\frac{M_1^2 - M_2^2}{q^2}q^\mu \quad q^\mu L_\mu \rightarrow 0 \text{ when } m_\ell \rightarrow 0$$

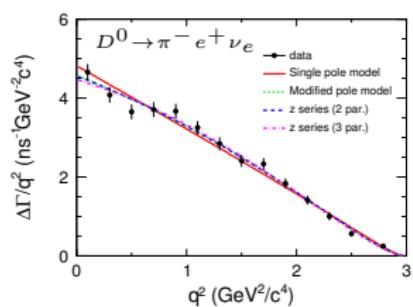
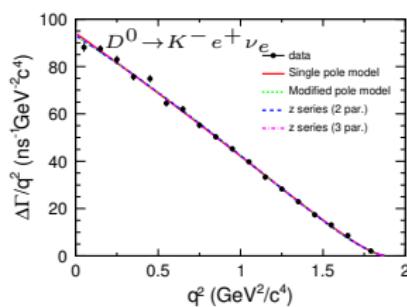
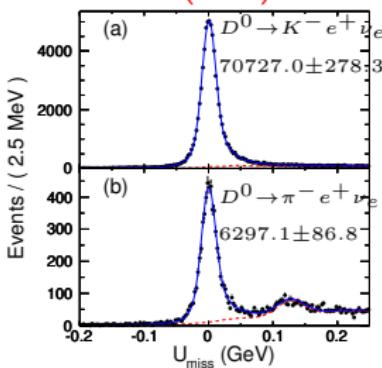
Single pole model: $f_+(q^2) = \frac{f_+(0)}{1 - \frac{q^2}{M_{\text{pole}}^2}}$

Modified pole mode: $f_+(q^2) = \frac{f_+(0)}{(1 - \frac{q^2}{M_{\text{pole}}^2})(1 - \alpha \frac{q^2}{M_{\text{pole}}^2})}$

z series(2 par): $f_+(t) = \frac{1}{P(t)\Phi(t,t_0)} a_0(t_0) \times (1 + r_1(t_0)[z(t,t_0)])$

z series(3 par): $f_+(t) = \frac{1}{P(t)\Phi(t,t_0)} a_0(t_0) \times (1 + r_1(t_0)[z(t,t_0)] + r_2(t_0)[z(t,t_0)]^2)$

BESIII PRD92(2015)072012



$$\mathcal{B}(D^0 \rightarrow K^- e^+ \nu_e) \quad (3.505 \pm 0.014 \pm 0.033)\%$$

$$\mathcal{B}(D^0 \rightarrow \pi^- e^+ \nu_e) \quad (0.295 \pm 0.004 \pm 0.003)\%$$

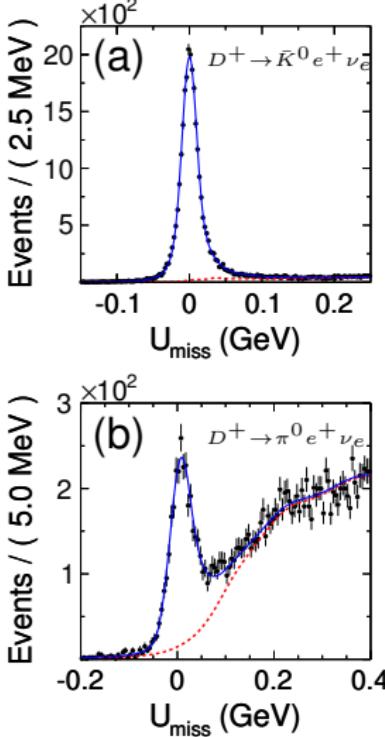
$$f_+^{D \rightarrow K}(0)|V_{cs}| \quad 0.7172 \pm 0.0025 \pm 0.0035$$

$$f_+^{D \rightarrow \pi}(0)|V_{cd}| \quad 0.1435 \pm 0.0018 \pm 0.0009$$

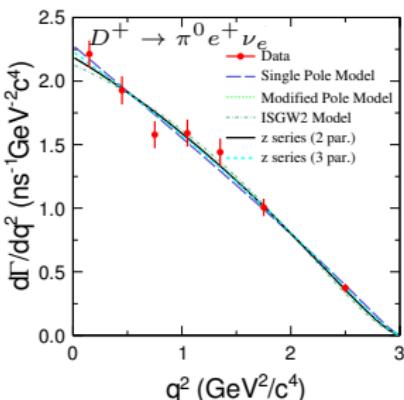
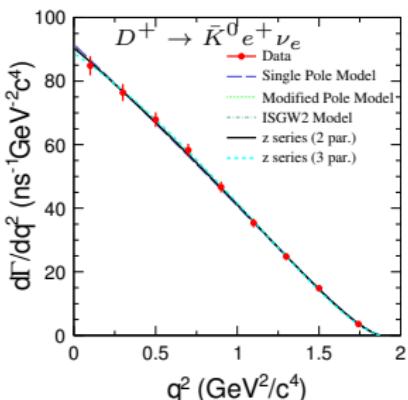
Dynamic study of $D^+ \rightarrow \bar{K}^0(\pi^0)e^+\nu_e$

BES III

PRD96(2017)012002

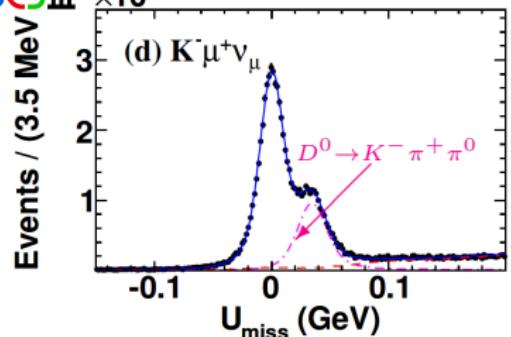


$\mathcal{B}(D^+ \rightarrow \bar{K}^0 e^+ \nu_e)$ (via K_S^0)	$(8.60 \pm 0.06 \pm 0.15)\%$
$f_+^{D \rightarrow K}(0) V_{cs} $	$0.7053 \pm 0.0040 \pm 0.0112$
$\mathcal{B}(D^+ \rightarrow \pi^0 e^+ \nu_e)$	$(0.363 \pm 0.008 \pm 0.005)\%$
$f_+^{D \rightarrow \pi}(0) V_{cd} $	$0.1400 \pm 0.0026 \pm 0.0007$

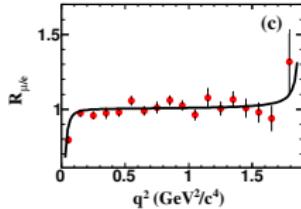
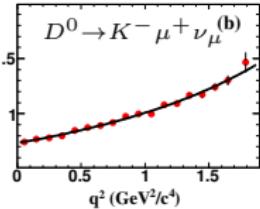
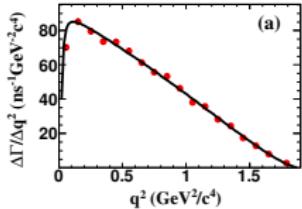
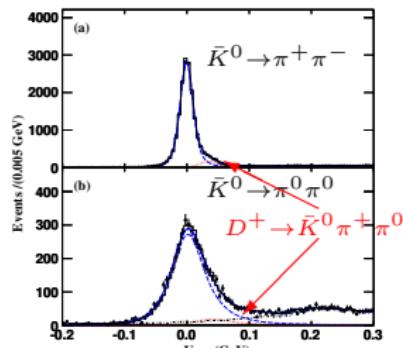


Dynamic study and LFU test with $D \rightarrow \bar{K}\mu^+\nu_\mu$

BESIII $\times 10^3$ PRL122(2019)011804



BESIII EPJC76(2016)369



$$\frac{\Gamma(D^0 \rightarrow K^-\mu^+\nu_\mu)}{\Gamma(D^0 \rightarrow K^-e^+\nu_e)}$$

$$0.974 \pm 0.014$$

$$\frac{\Gamma(D^+ \rightarrow \bar{K}^0\mu^+\nu_\mu)}{\Gamma(D^+ \rightarrow \bar{K}^0e^+\nu_e)}$$

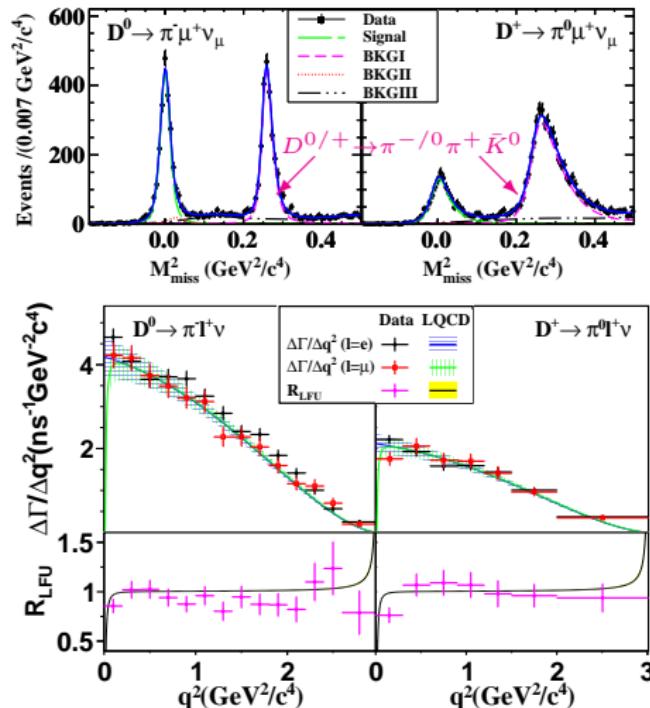
$$0.988 \pm 0.033$$

Expected: 0.975 ± 0.001
 Consistent

$\mathcal{B}(D^0 \rightarrow K^-\mu^+\nu_\mu)$	$(3.431 \pm 0.019 \pm 0.035)\%$
$f_+^{D \rightarrow K}(0) V_{cs} $	$0.7133 \pm 0.0038 \pm 0.0030$
$\mathcal{B}(D^+ \rightarrow \bar{K}^0\mu^+\nu_\mu)$	$(8.72 \pm 0.07 \pm 0.18)\%$

Test of LFU with $D \rightarrow \pi\mu^+\nu_\mu$

BESIII PRL121(2018)171803



$$\mathcal{B}(D^0 \rightarrow \pi^- \mu^+ \nu_\mu) = (0.272 \pm 0.008 \pm 0.006)\%$$

$$\mathcal{B}(D^+ \rightarrow \pi^0 \mu^+ \nu_\mu) = (0.350 \pm 0.011 \pm 0.010)\%$$

$$\frac{\Gamma(D^0 \rightarrow \pi^- \mu^+ \nu_\mu)}{\Gamma(D^0 \rightarrow \pi^- e^+ \nu_e)} = 0.922 \pm 0.037$$

$$\frac{\Gamma(D^+ \rightarrow \pi^0 \mu^+ \nu_\mu)}{\Gamma(D^+ \rightarrow \pi^0 e^+ \nu_e)} = 0.964 \pm 0.045$$

The LQCD calculations are taken from ETM's results published in PRD96(2017)054514, with

$$\frac{\Gamma(D \rightarrow \pi \mu^+ \nu_\mu)}{\Gamma(D \rightarrow \pi e^+ \nu_e)} = 0.985 \pm 0.002$$

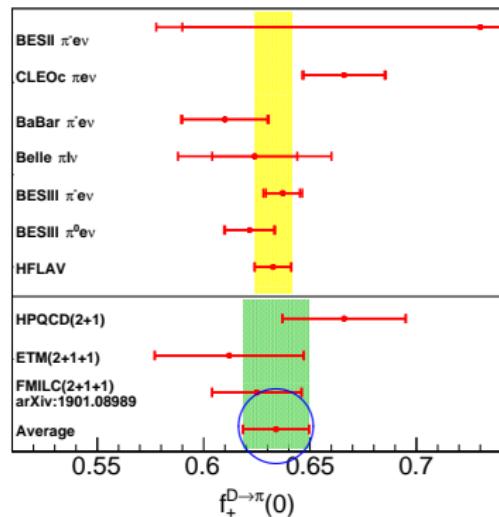
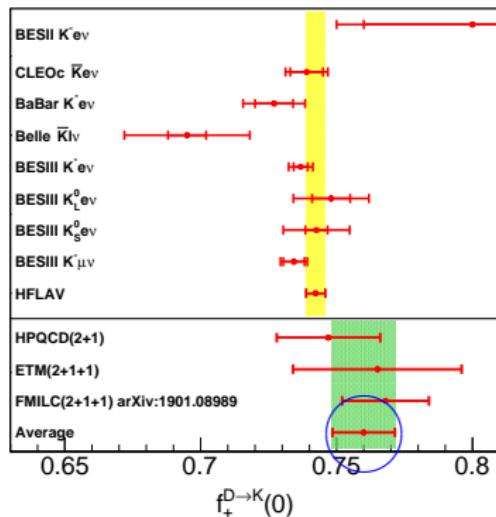
Comparison of $f_+^{D \rightarrow K}(0)$ and $f_+^{D \rightarrow \pi}(0)$

Inputs:

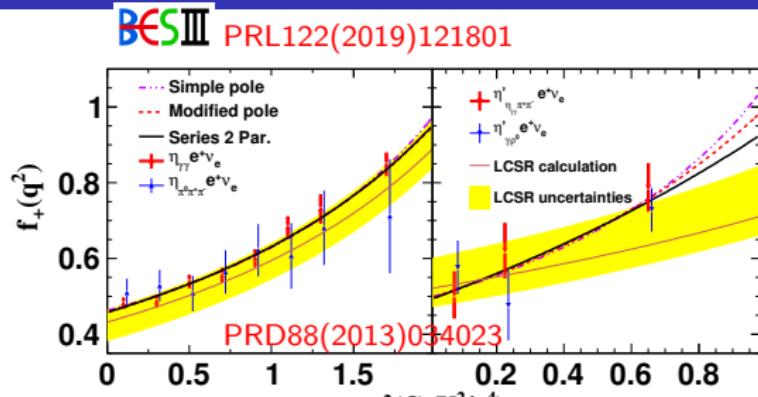
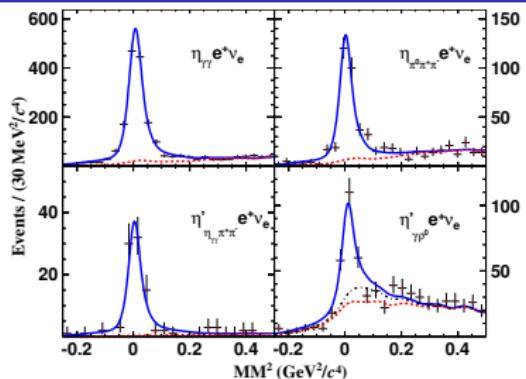
PDG2018 from CKM unitarity:

$$|V_{cs}| = 0.97359^{+0.00010}_{-0.00011}$$

$$|V_{cd}| = 0.22438 \pm 0.00044$$



First measurement of FFs of $D_s^+ \rightarrow \eta^{(\prime)} e^+ \nu_e$

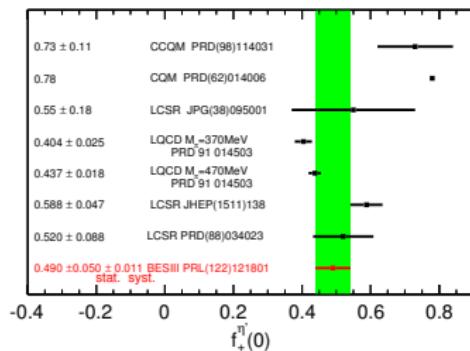
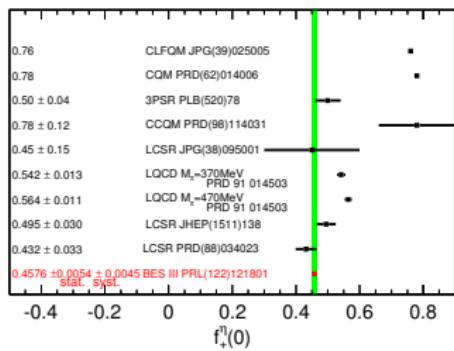


$$\mathcal{B}(D_s^+ \rightarrow \eta e^+ \nu_e) = (2.323 \pm 0.063 \pm 0.063)\%$$

$$\mathcal{B}(D_s^+ \rightarrow \eta' e^+ \nu_e) = (0.824 \pm 0.073 \pm 0.027)\%$$

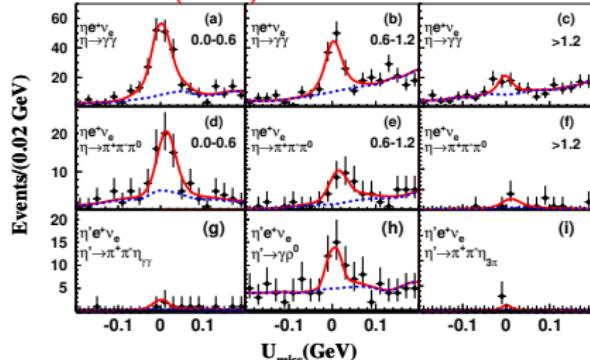
$$f_+^{D_s^+ \rightarrow \eta}(0)|V_{cs}| = 0.4455 \pm 0.0053 \pm 0.0044$$

$$f_+^{D_s^+ \rightarrow \eta'}(0)|V_{cs}| = 0.477 \pm 0.049 \pm 0.011$$



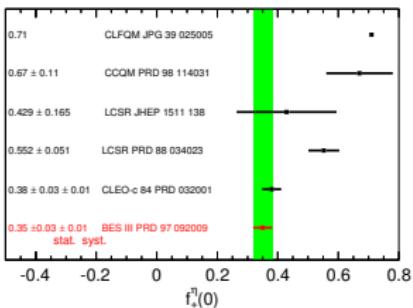
Measurement of $D^+ \rightarrow \eta^{(\prime)} e^+ \nu_e$, FF, $\eta - \eta'$ mixing angle

BESIII PRD97(2018)092009



$$\mathcal{B}(D^+ \rightarrow \eta e^+ \nu_e) = (10.74 \pm 0.81 \pm 0.51) \times 10^{-4}$$

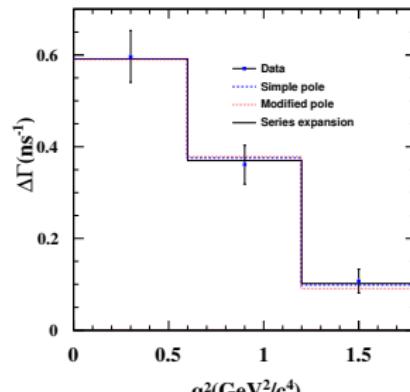
$$\mathcal{B}(D^+ \rightarrow \eta' e^+ \nu_e) = (1.91 \pm 0.51 \pm 0.13)^{-4}$$



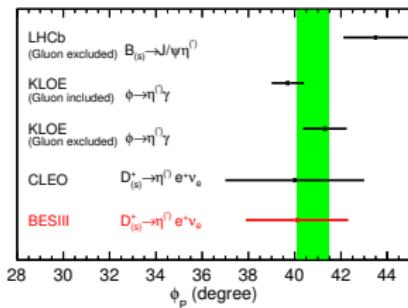
Model independent determination of $\eta - \eta'$ mixing angle.

$$\frac{\Gamma(D_s^+ \rightarrow \eta' e^+ \nu_e) / \Gamma(D_s^+ \rightarrow \eta e^+ \nu_e)}{\Gamma(D^+ \rightarrow \eta' e^+ \nu_e) / \Gamma(D^+ \rightarrow \eta e^+ \nu_e)} \simeq \cot^4 \Phi_P$$

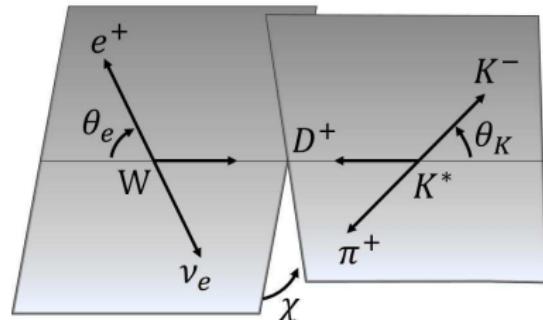
$$\Phi_P = (40.1 \pm 2.1 \pm 0.7)^\circ$$



$$f_+^{D^+\rightarrow\eta}(0)|V_{cd}| = (7.86 \pm 0.64 \pm 0.21) \times 10^{-2}$$



First measurement of FFs of $D^0 \rightarrow \bar{K}^0\pi^-e^+\nu_e$

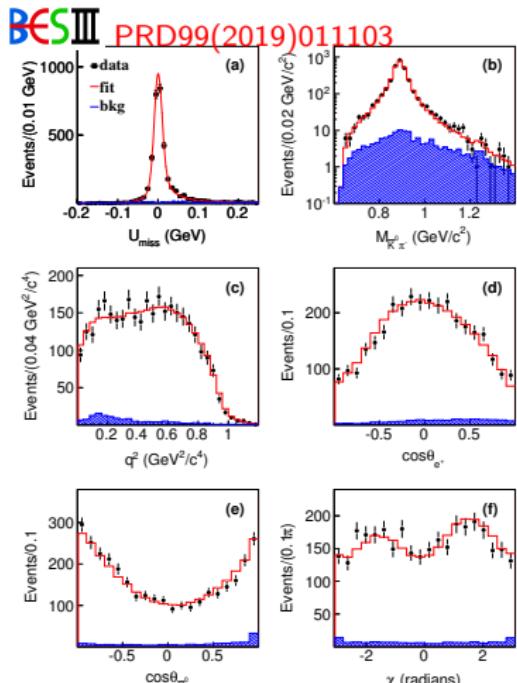


$$\begin{aligned} & < V(p_2, \epsilon_2) | V^\mu - A^\mu | D(p_1) > = \\ & - (M_1 + M_2) \epsilon_2^{*\mu} A_1(q^2) + \frac{\epsilon_2^{*q}}{M_1 + M_2} P^\mu A_2(q^2) + \\ & 2M_2 \frac{\epsilon_2^{*q}}{q^2} q^\mu [A_3(q^2) - A_0(q^2)] + \frac{2i\epsilon_{\mu\nu\rho\sigma}\epsilon^{*\nu} p_1^\rho p_2^\sigma}{M_1 + M_2} V(q^2) \end{aligned}$$

$q^\mu L_\mu \rightarrow 0$ when $m_\ell \rightarrow 0$

$$r_V = \frac{V(0)}{A_1(0)} \quad r_2 = \frac{A_2(0)}{A_1(0)}$$

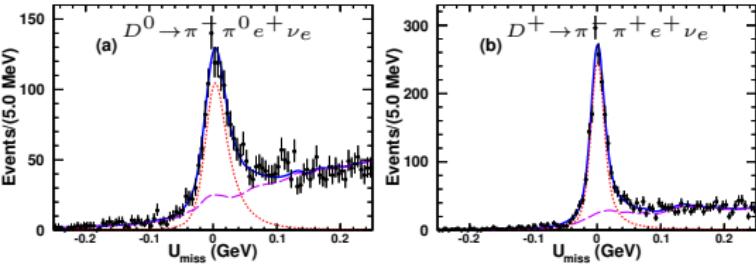
$S((K^0\pi)_{S\text{-wave}})$	$(7.90 \pm 1.40 \pm 0.91) \times 10^{-4}$	$P(K^*(892)^-)$	$(1.355 \pm 0.031 \pm 0.032)\%$
r_V	$1.46 \pm 0.07 \pm 0.02$	r_2	$0.67 \pm 0.06 \pm 0.01$



$$D^0 \rightarrow \bar{K}^0\pi^-e^+\nu_e$$

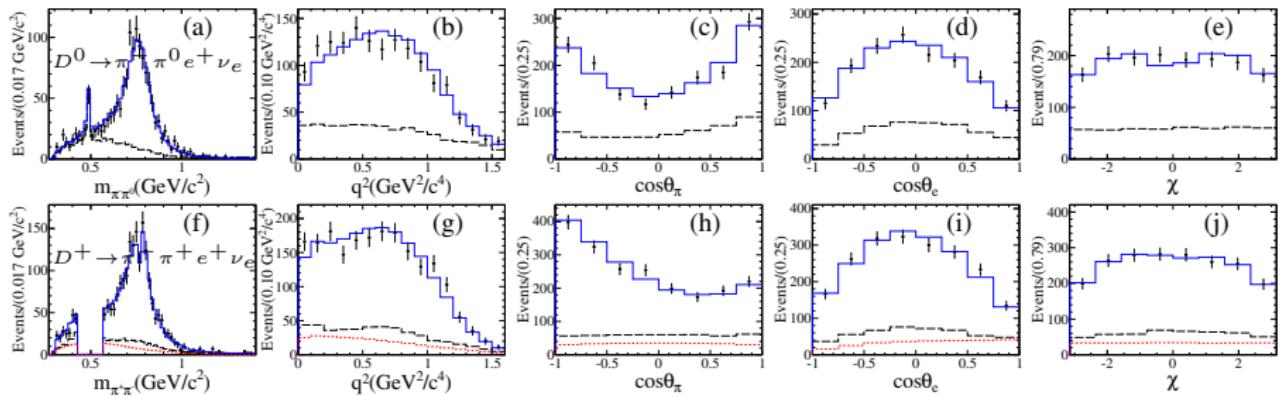
Observation of $D \rightarrow \pi\pi e^+ \nu_e$ (S wave)

BESIII PRL122(2019)062001



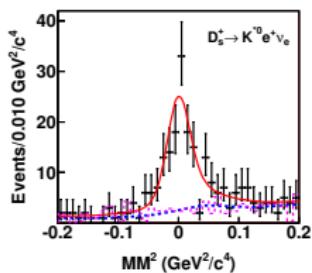
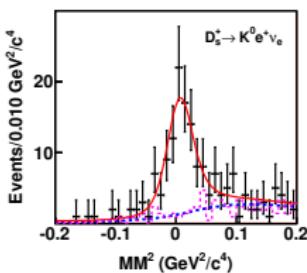
Signal mode	BF ($\times 10^{-3}$)
$D^0 \rightarrow \pi^- \pi^0 e^+ \nu_e$	$1.445 \pm 0.058 \pm 0.039$
$D^0 \rightarrow \rho^- e^+ \nu_e$	$1.445 \pm 0.048 \pm 0.039$
$D^+ \rightarrow \pi^- \pi^+ e^+ \nu_e$	$2.449 \pm 0.074 \pm 0.073$
$D^+ \rightarrow \rho^0 e^+ \nu_e$	$1.860 \pm 0.070 \pm 0.061$
$D^+ \rightarrow \omega e^+ \nu_e$	$2.05 \pm 0.66 \pm 0.30$
$D^+ \rightarrow f_0(500) e^+ \nu_e$	$0.630 \pm 0.043 \pm 0.032$
$f_0(500) \rightarrow \pi^+ \pi^-$	
$D^+ \rightarrow f_0(980) e^+ \nu_e$	
$f_0(980) \rightarrow \pi^+ \pi^-$	< 0.028

$$r_V = 1.695 \pm 0.083 \pm 0.051 \quad r_2 = 0.845 \pm 0.056 \pm 0.039$$



First measurement of FFs of $D_s^+ \rightarrow K^{(*)0} e^+ \nu_e$

BESIII PRL122(2019)061801



$$\mathcal{B}(D_s^+ \rightarrow K^0 e^+ \nu_e) = (3.25 \pm 0.38 \pm 0.16) \times 10^{-3}$$

$$f_+^{D_s^+ \rightarrow K^0}(0) |V_{cd}| = 0.162 \pm 0.019 \pm 0.003$$

$$\mathcal{B}(D_s^+ \rightarrow K^{*0} e^+ \nu_e) = (2.37 \pm 0.26 \pm 0.20) \times 10^{-3}$$

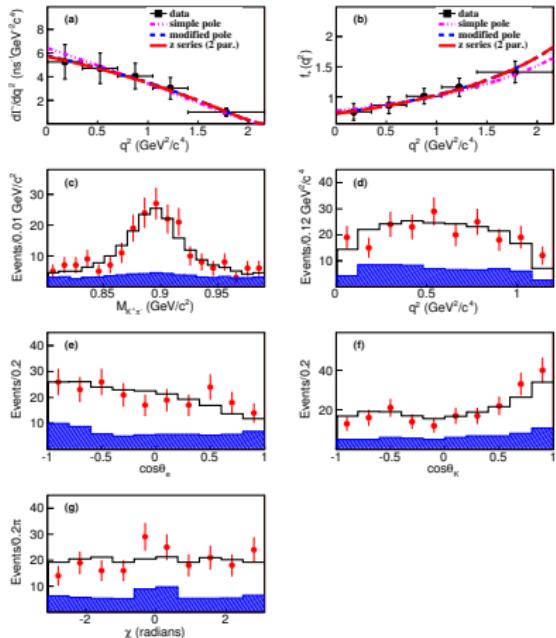
$$r_V = 1.67 \pm 0.34 \pm 0.16$$

$$r_2 = 0.77 \pm 0.28 \pm 0.07$$

$$f_+^{D_s^+ \rightarrow K^0}(0) / f_+^{D^+ \rightarrow \pi^0}(0) = 1.16 \pm 0.14 \pm 0.02$$

$$r_V^{D_s^+ \rightarrow K^{*0}} / r_V^{D^+ \rightarrow \rho^0} = 1.13 \pm 0.26 \pm 0.11$$

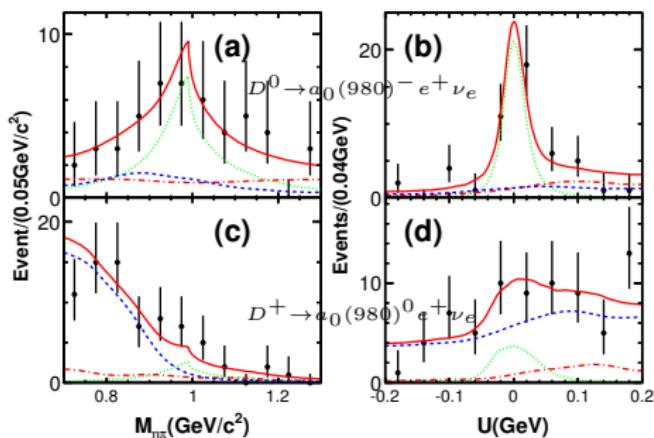
$$r_2^{D_s^+ \rightarrow K^{*0}} / r_2^{D^+ \rightarrow \rho^0} = 0.93 \pm 0.36 \pm 0.10$$



Agrees with U-spin ($d \leftrightarrow s$) symmetry.

Observation of $D \rightarrow a_0(980)e^+\nu_e$

BESIII PRL121(2018)081802



A model-independent way to study the nature of light scalar mesons proposed by PRD82(2016)034016

$$R = \frac{\mathcal{B}(D^+ \rightarrow f_0(980)e^+\nu_e) + \mathcal{B}(D^+ \rightarrow f_0(500)e^+\nu_e)}{\mathcal{B}(D^+ \rightarrow a_0(980)^0 e^+\nu_e)}$$

$R = 1.0 \pm 0.3$ for two-quark description;
 $R = 3.0 \pm 0.9$ for tetraquark description.

We have $R > 2.7$ @90% C.L. at BESIII
Which favors the tetraquark description.

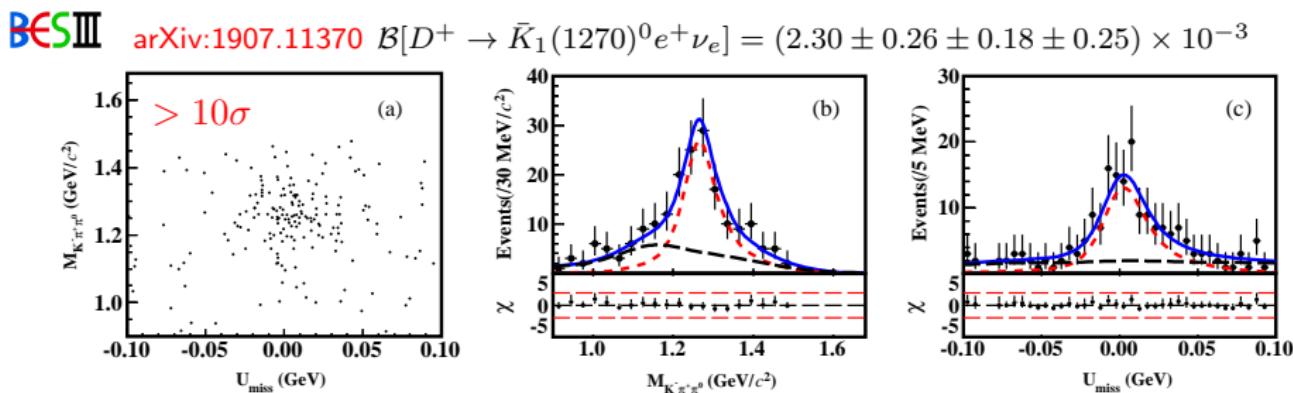
Decay	BF ($\times 10^{-4}$)	Significance
$D^0 \rightarrow a_0(980)^- e^+ \nu_e, a_0(980)^- \rightarrow \eta\pi^-$	$1.33^{+0.33}_{-0.29} \pm 0.09$	6.4σ
$D^+ \rightarrow a_0(980)^0 e^+ \nu_e, a_0(980)^0 \rightarrow \eta\pi^0$	$1.66^{+0.81}_{-0.66} \pm 0.11$ < 3.0 (90% C.L.)	2.9σ

Observation of $D^+ \rightarrow \bar{K}_1(1270)^0 e^+ \nu_e$

Semileptonic D transitions into axial vector meson were predicted 30 years ago, but not experimentally confirmed yet.

In theory, the predicted BFs are sensitive to K_1 mixing angle(θ_{K_1}) and its sign

[PRD79(2009)036004, EPJC77(2017)369].

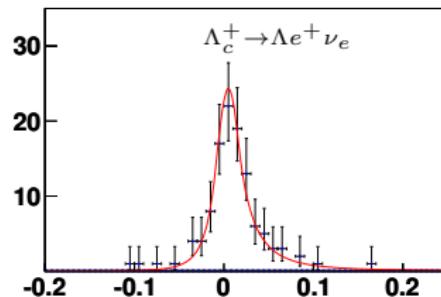


Our result indicates $\theta_{K_1} \sim 33^\circ$ or 57° and opens up opportunity to precisely study nature of $\bar{K}_1(1270)$.

Absolute branching fraction of $\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e$

0.567 fb^{-1} data @4.6 GeV

BESIII PRL115(2015)221805



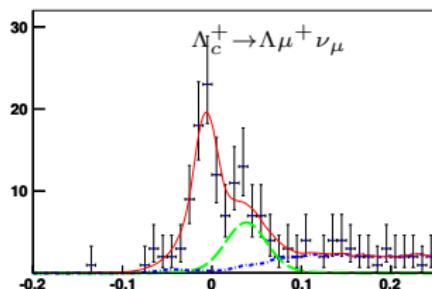
Previously expected: 1.4% \rightarrow 9.2%.

$$\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e) = (3.63 \pm 0.38 \pm 0.20)\%$$

$$\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda \mu^+ \nu_\mu) = (3.49 \pm 0.46 \pm 0.26)\%$$

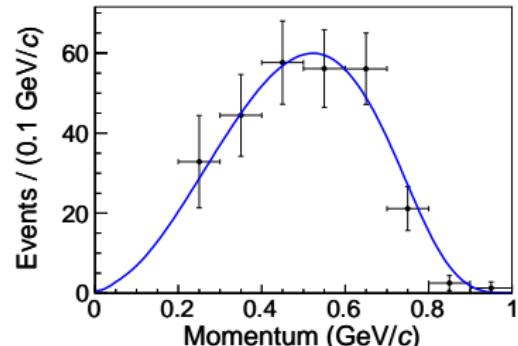
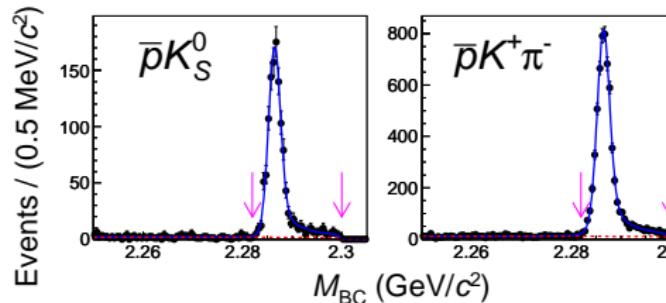
$$\frac{\Gamma(\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e)}{\Gamma(\Lambda_c^+ \rightarrow \Lambda \mu^+ \nu_\mu)} = 0.96 \pm 0.16 \pm 0.04$$

BESIII PLB767(2017)42



Absolute BF of inclusive decay $\Lambda_c^+ \rightarrow X e^+ \nu_e$

BESIII PRL121(2018)251801



Decay channel	\mathcal{B} (%)	Model
$\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e$	3.63 ± 0.43	$F_1^V(q^2) = \frac{2.52}{5.09 - q^2}$
$\Lambda_c^+ \rightarrow \Lambda(1405)e^+ \nu_e$	0.38 ± 0.38	PYTHIA
$\Lambda_c^+ \rightarrow n e^+ \nu_e$	0.27 ± 0.27	PYTHIA

$$\mathcal{B}(\Lambda_c^+ \rightarrow X e^+ \nu_e) = (3.95 \pm 0.34 \pm 0.09)\%$$

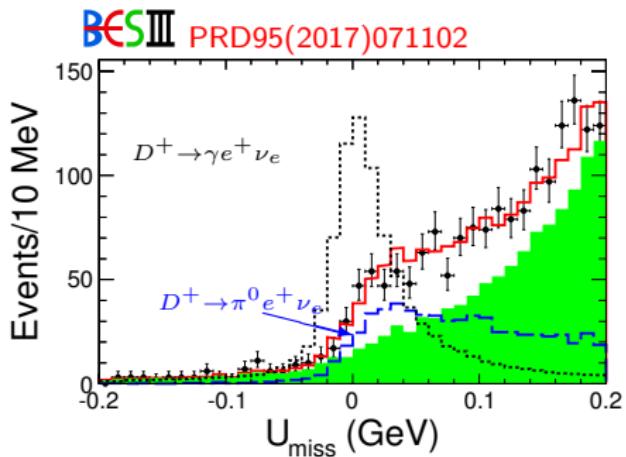
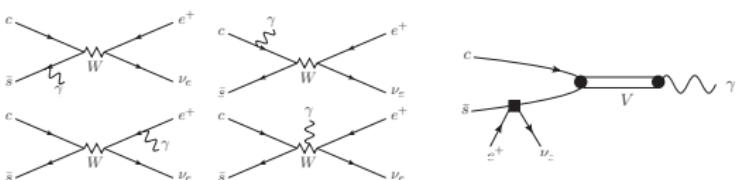
$$\frac{\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e)}{\mathcal{B}(\Lambda_c^+ \rightarrow X e^+ \nu_e)} = (91.9 \pm 12.5 \pm 5.4)\%$$

Result	$\Lambda_c^+ \rightarrow X e^+ \nu_e$	$\frac{\Gamma(\Lambda_c^+ \rightarrow X e^+ \nu_e)}{\Gamma(D \rightarrow X e^+ \nu_e)}$
BESIII	3.95 ± 0.35	1.26 ± 0.12
MARK II	4.5 ± 1.7	1.44 ± 0.54

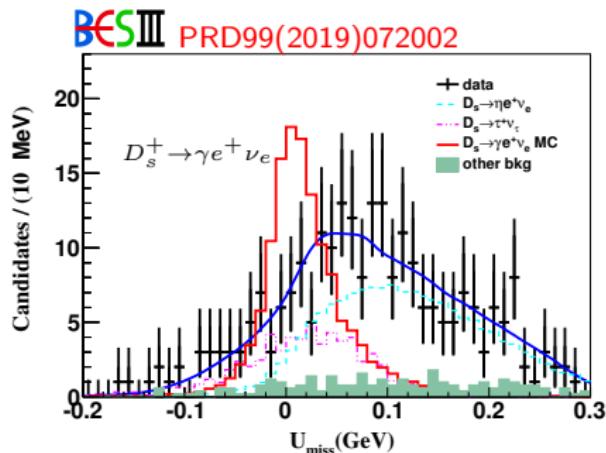
This ratio is predicted to be 1.67 using an effective-quark theory calculation
1.2 based on a calculation using the heavy-quark expansion.

Search for radiative semileptonic decay $D \rightarrow \gamma e^+ \nu_e$

Not subject to helicity suppression.
Only photon energy larger than 10 MeV are considered.
The BFs are predicted to be $10^{-5} \rightarrow 10^{-3}$ in various models.



$$\mathcal{B}(D^+ \rightarrow \gamma e^+ \nu_e) < 3.0 \times 10^{-5} \text{ @90% C.L.}$$



$$\mathcal{B}(D_s^+ \rightarrow \gamma e^+ \nu_e) < 1.3 \times 10^{-4} \text{ @90% C.L.}$$

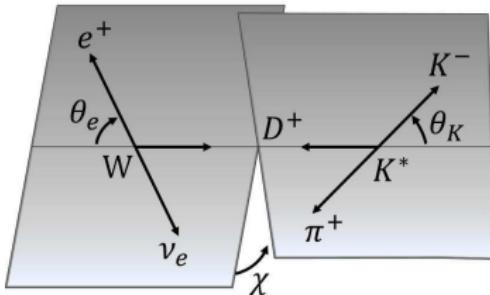
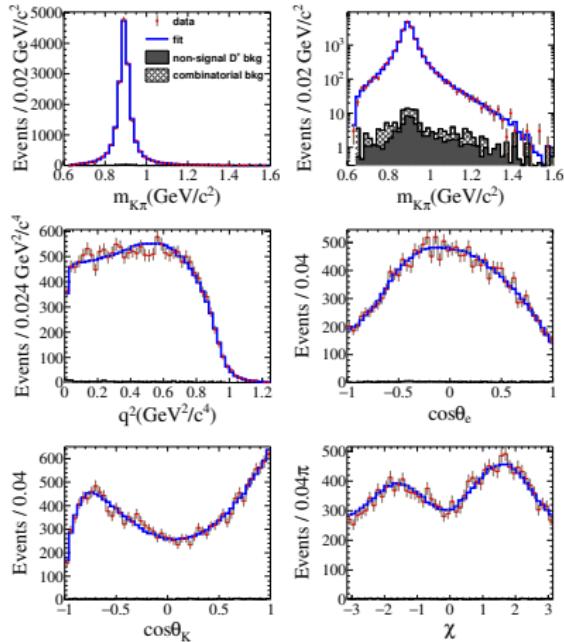
Summary

- ① Precise measurement of decay constants, form factors and quark mixing matrix elements → precision improved with BESIII measurement.
 - $f_{D^+}|V_{cd}| \sim 2.8\%$
 - $f_{D_s^+}|V_{cs}| \sim 2.0\%$
 - $f_+^{D \rightarrow K}(0)|V_{cs}| \sim 0.6\%$
 - $f_+^{D \rightarrow \pi}(0)|V_{cd}| \sim 1.4\%$
- ② Lepton flavor universality test → no evidence of violation found in the charm sector at the precision of 1.5% for CF decays and 4% for SCS decays.
- ③ The results of $(a_0(980)e^+\nu, f_0(500)e^+\nu)$ favor the tetraquark description.
- ④ First measurement of absolute branching fractions of semileptonic Λ_c^+ decays.
- ⑤ Upcoming data at BESIII → more results to be expected.

Back up

$$D^+ \rightarrow K^- \pi^+ e^+ \nu_e$$

BESIII PRD94(2016)032001



$$r_V = V(0)/A_1(0) = 1.411 \pm 0.058 \pm 0.007$$

$$r_2 = A_2(0)/A_1(0) = 0.788 \pm 0.042 \pm 0.008$$

$$A_1(0) = 0.589 \pm 0.010 \pm 0.012$$

Not included in the nominal fit:

$$\mathcal{B}(D^+ \rightarrow \bar{K}^*(1410)^0 e^+ \nu_e) \quad (0 \pm 0.009 \pm 0.008)\% \\ < 0.028\% \text{ (90\% C.L.)}$$

$$\mathcal{B}(D^+ \rightarrow \bar{K}_2^*(1430)^0 e^+ \nu_e) \quad (0.011 \pm 0.003 \pm 0.007)\% \\ < 0.023\% \text{ (90\% C.L.)}$$

$$\mathsf{P}(\bar{K}^*(892)^0)$$

$$\begin{aligned} &\text{Simple Pole plus} \\ &\text{BW with mass-dependent width} \\ &\text{LASS plus} \\ &\text{BW with mass-dependent width} \end{aligned}$$

$$(3.54 \pm 0.03 \pm 0.08)\%$$

$$\mathsf{S}(\bar{K}_0^*(1430)^0 \text{ and non-resonant part})$$

$$(0.228 \pm 0.008 \pm 0.008)\%$$