

# Flow and non-flow response in Pb-Pb, p-Pb collisions at 5.02 TeV

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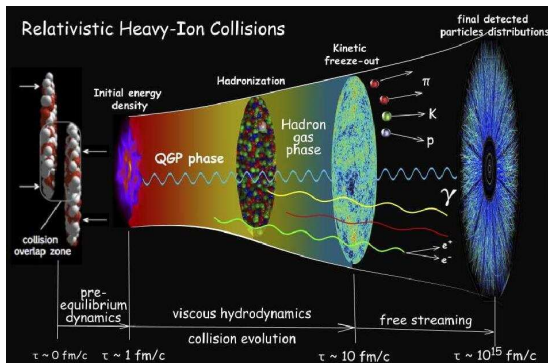
Guangxi University of Science and Technology

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Aug. 16-20, 2019

- ① Introduction
- ② Response theory
- ③ Flow and non-flow response: Large and small systems
- ④ Summary

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# I. Introduction

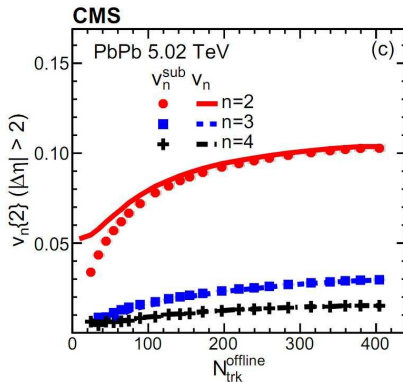
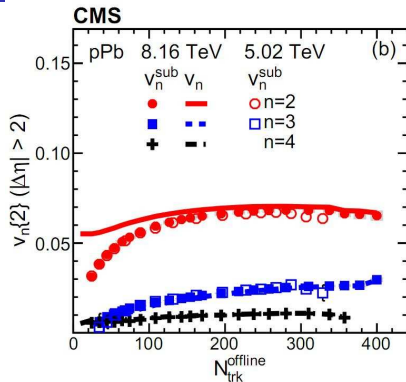


**What happen?**

**Detector**

- 1 In heavy-ion collisions(HIC), final flow induced from initial fluctuate geometry.
- 2 However, we know little about the initial states without a directly experimental data.

# I. Introduction

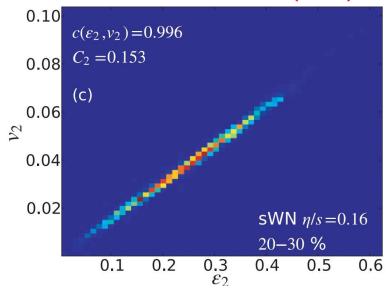


- 1 Similarly multiplicity dependent  $v_2$  for Pb-Pb and p-Pb system<sup>[1]</sup>.
- 2 Initial fluctuations-driven both flow and non-flow on small system, especially for low multiplicity. How about the real flow can be seen in small system?  
(Talks by: Q. H. Xu, J. Y. Jiang, G. L. Ma, Z. Chen, ...)

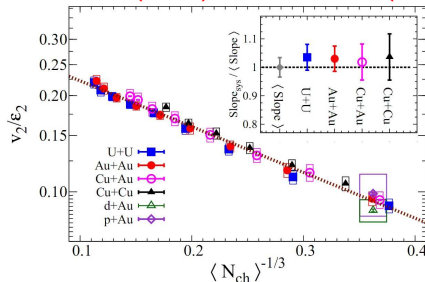
[1]. A. M. Sirunyan et al.(CMS), PRL 120,092301 (2018)

# I. Introduction

H. Niemi et al., PRC 87,054901(2013)



J. Adam et al.(STAR), PRL 122,172301(2019)



- 1 The  $v_2$  are determined by linear response to  $\epsilon_2$  without initial fluctuations.
- 2 A linear relation,  $v_2/\epsilon_2$ , from large system to small system. A sizable uncertainties for the pA systems at low multiplicity where estimates for residual non-flow contributions.

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## II. Response theory

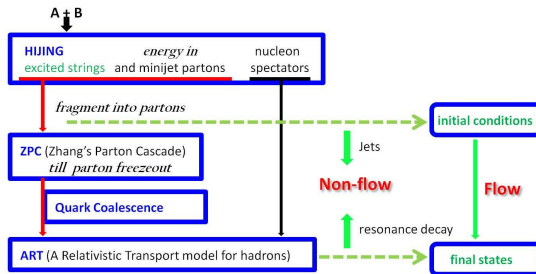


FIG. Structure of the AMPT model with string melting

AMPT is a hybrid model, which has composed of four main stages:

- 1 **Initial conditions:** Heavy Ion Jet Interaction Generator(HIJING ).
- 2 **Parton cascades:** ZPC, describe partons interaction as two-body elastic scattering.
- 3 **Hadronizations:** partons are formed into hadrons via a coalescence model.
- 4 **Hadronic rescatterings:** ART, included hadrons rescatterings and resonance decays.

Z. Lin et al., PRC 72, 064901 (2005)



## II. Response theory

The azimuthal distribution of particles:

$$\text{Initial states : } E_n \equiv \varepsilon_n e^{in\Phi_n} = -\frac{\int r^n e^{in\phi} \epsilon(r, \phi) r dr d\phi}{\int r^n \epsilon(r, \phi) r dr d\phi}. \quad (1)$$

$$\text{Final states : } V_n \equiv v_n e^{in\Psi_n} = \frac{\int e^{in\varphi} h(\varphi) d\varphi}{\int h(\varphi) d\varphi}. \quad (2)$$

where  $\Phi_n$ ,  $\Psi_n$  named Participant Plane and Event Plane, respectively.

**A simple theory is the response relation between the initial states and final states, as<sup>[1]</sup>**

$$v_n e^{in\Psi_n} = \kappa_n \varepsilon_n e^{in\Phi_n} + \kappa'_n \varepsilon'_n e^{in\Phi_n} + \kappa''_n \varepsilon''_n e^{in\Phi_n} + \dots + \delta_n \quad (3)$$

where  $\varepsilon'_n = \varepsilon_2^2 \varepsilon_n$ ,  $\varepsilon''_n = \varepsilon_3^2 \varepsilon_n$ .

One solves of the first two order for  $\kappa_2$  and  $\kappa'_2$  (named **USNF**):

$$\begin{aligned} \kappa_2 &= \frac{\text{Re}(\langle \varepsilon_2^6 \rangle \langle V_2 E_2^* \rangle - \langle \varepsilon_2^4 \rangle \langle V_2 E_2^* \varepsilon_2^2 \rangle)}{\langle \varepsilon_2^6 \rangle \langle \varepsilon_2^2 \rangle - \langle \varepsilon_2^4 \rangle^2} \\ \kappa'_2 &= \frac{\text{Re}(-\langle \varepsilon_2^4 \rangle \langle V_2 E_2^* \rangle + \langle \varepsilon_2^2 \rangle \langle V_2 E_2^* | \varepsilon_2 |^2 \rangle)}{\langle \varepsilon_2^6 \rangle \langle \varepsilon_2^2 \rangle - \langle \varepsilon_2^4 \rangle^2}, \end{aligned} \quad (4)$$

[1]. **DXW**, X. Huang and L. Yan, PRC 98, 044908 (2018)

## II. Response theory

To subtract the non-flow effect, one by the cumulants method<sup>[1]</sup>

$$v_2\{2, |\Delta\eta|\} = \kappa_2 \varepsilon_2\{2\} \left[ 1 + \frac{\kappa_2'}{\kappa_2} \frac{\langle \varepsilon_2^4 \rangle}{\langle \varepsilon_2^2 \rangle} \right]. \quad (5)$$

$$v_2\{4\} = \kappa_2 \varepsilon_2\{4\} \left[ 1 + \frac{\kappa_2'}{\kappa_2} \frac{2\langle \varepsilon_2^2 \rangle \langle \varepsilon_2^4 \rangle - \langle \varepsilon_2^6 \rangle}{2\langle \varepsilon_2^2 \rangle^2 - \langle \varepsilon_2^4 \rangle} \right]. \quad (6)$$

$v_2\{2\}$  is obtained from two-particle correlations using a pseudorapidity gap with  $|\Delta\eta| > 1.0$ . And the solution is (named **SNF**)

$$\kappa_2 = \frac{v_2\{2, |\Delta\eta|\} \cdot B - v_2\{4\} \cdot A}{\varepsilon_2\{2\} \cdot B - \varepsilon_2\{4\} \cdot A}, \quad (7)$$

$$\kappa_2' = \frac{-(v_2\{2, |\Delta\eta|\} \varepsilon_2\{4\} - v_2\{4\} \varepsilon_2\{2\})}{\varepsilon_2\{2\} \cdot B - \varepsilon_2\{4\} \cdot A}. \quad (8)$$

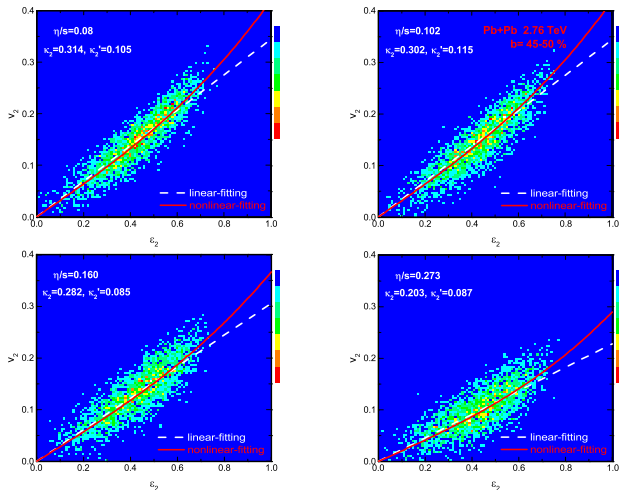
where

$$A = \frac{\langle \varepsilon_2^4 \rangle}{\langle \varepsilon_2^2 \rangle} \cdot \varepsilon_2\{2\}, \quad B = \frac{2\langle \varepsilon_2^2 \rangle \langle \varepsilon_2^4 \rangle - \langle \varepsilon_2^6 \rangle}{2\langle \varepsilon_2^2 \rangle^2 - \langle \varepsilon_2^4 \rangle} \cdot \varepsilon_2\{4\}. \quad (9)$$

[1]. **DXW**, X. Huang and L. Yan, PRC 98, 044908 (2018)

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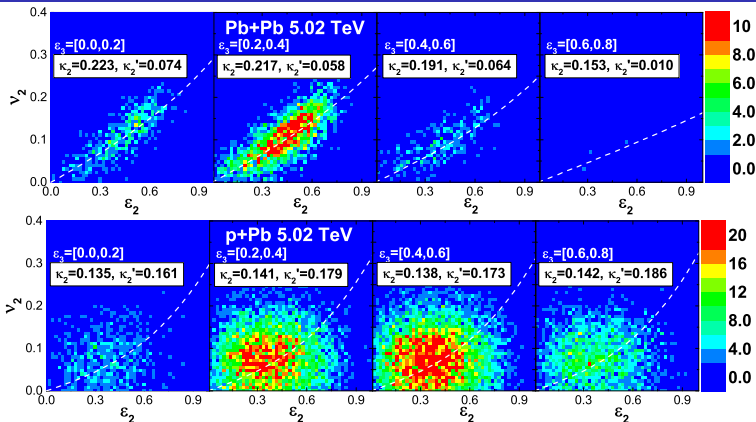
# III. Flow and non-flow response: Large and small systems



DXW, X. Huang and L. Yan, PRC 98, 044908 (2018)

- ① Both  $\kappa_n$  and  $\kappa_n'$  are sensitive to the specific viscosity  $\eta/s$ .

### III. Flow and non-flow response: Large and small systems

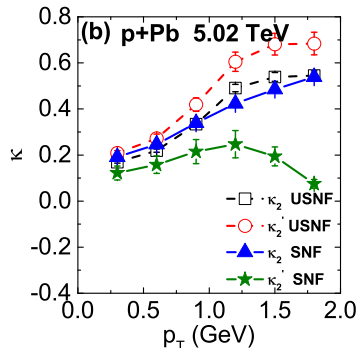
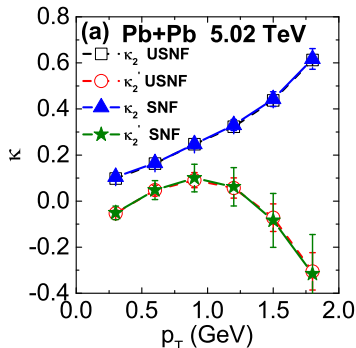


- 1 Dissimilarly 2D-response distribution for Pb-Pb and p-Pb system.
- 2 A weaker Pearson correlation result observed on p-Pb system. For p-Pb system, flow is not only come from the initial geometry but also come from the medium expanding and/or hadrons cascade, similarly results seen in Ref.[1 – 2] (also calculated by AMPT).

[1]. M. Nie, L. Yi, J. Jia and G. Ma, arXiv:1906.01422

[2]. Z. Lin, PRC 90,014904(2014)

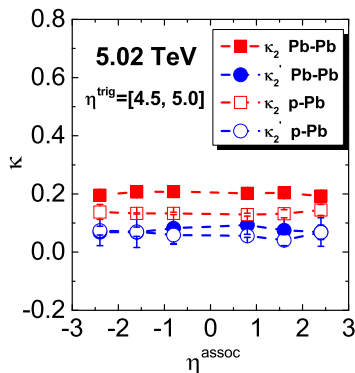
# III. Flow and non-flow response: Large and small systems



- 1 A non-negligible non-flow effects of response relations shown on p-Pb system, but hydrodynamic response for Pb-Pb system.
- 2 Similarly  $p_T$  dependent distribution within SNF for Pb-Pb and p-Pb system.
- 3 A specific viscosity  $\eta/s$ -driven response relation within both the two systems. Similarly results can be seen in STAR<sup>[1]</sup>.

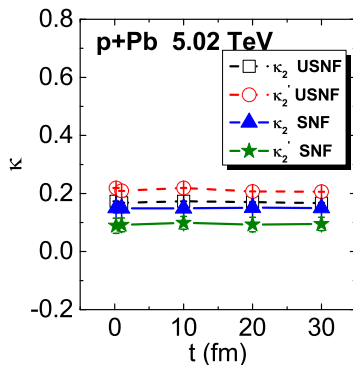
[1]. J. Adam et al.(STAR), PRL 122, 172301 (2019)

### III. Flow and non-flow response: Large and small systems



- 1 Similarly  $\eta$  dependent distribution within SNF for Pb-Pb and p-Pb system.  
(Talks by: L. Yan)
- 2 Similarly longitudinal dynamics, provides information on the initial states and the expanding medium for both the two systems.

### III. Flow and non-flow response: Large and small systems



- 1 Response relations are not sensitive to the hadron evolution times.
- 2 A dominated contribution to response relation of non-flow effect is from the early time of the expanding medium.



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## IV. Summary

- ① Dissimilarly 2D-response distribution for Pb-Pb and p-Pb system. For small system, flow is not only come from the initial fluctuate geometry but also from the medium expanding.
- ② A non-negligible non-flow effects of response coefficients shown on p-Pb system where unlike on Pb-Pb system, and these non-flow effects mainly come from the early time of the expanding medium.
- ③ Response coefficients also dependence on  $p_T$  and  $\eta$ .

Thank you!