

Determine the magnitude of the magnetic field at freeze-out

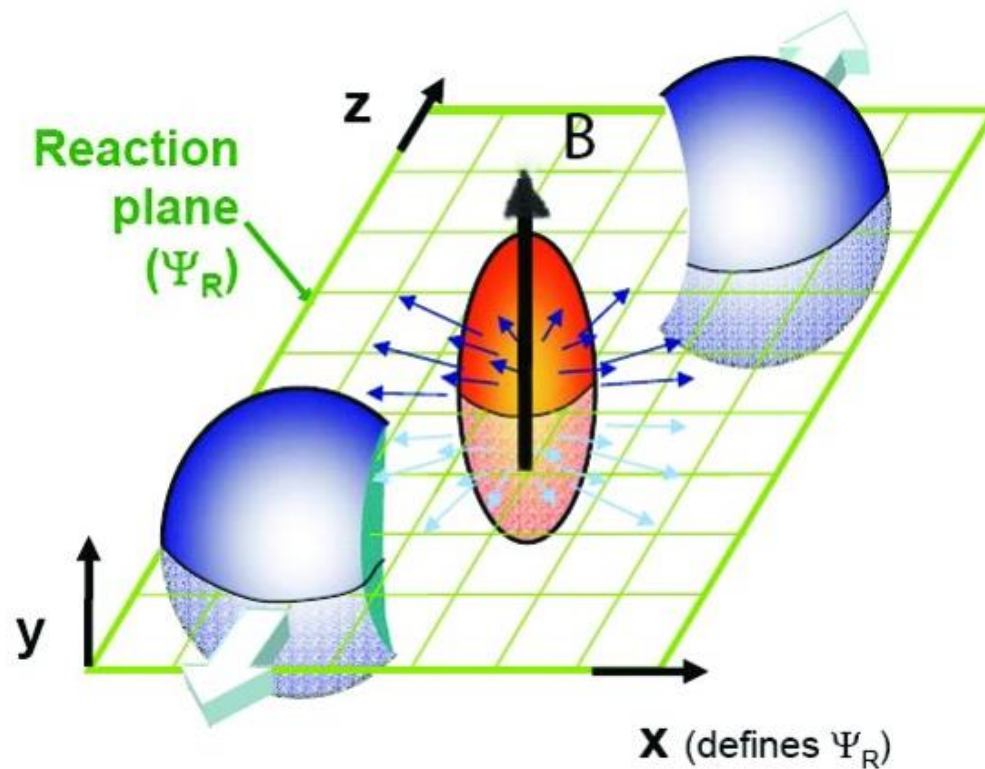
Paper in preparation...

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第十三届QCD相变与相对论重离子物理研讨会

Introduction

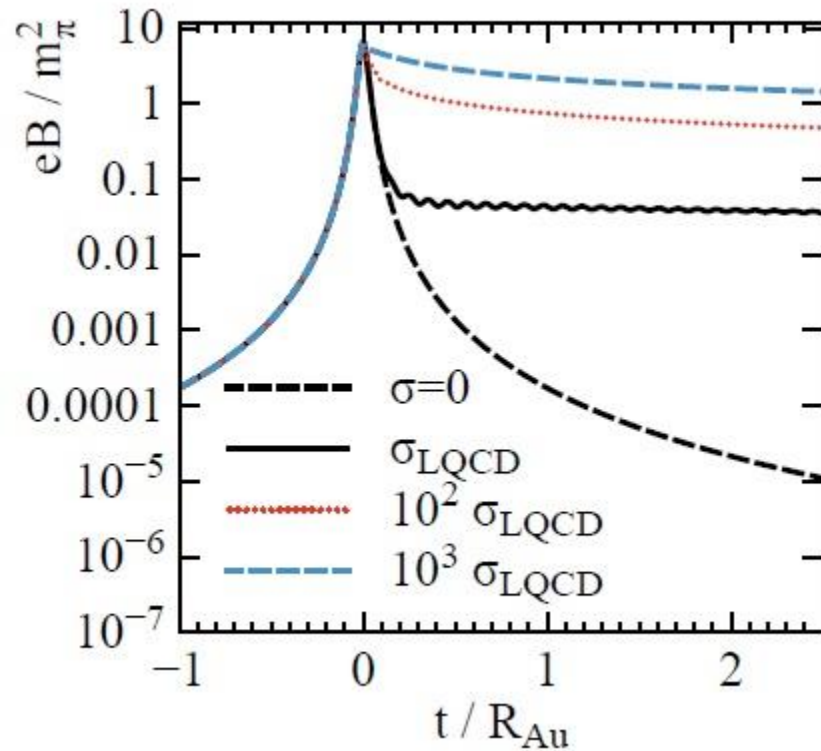


Question:

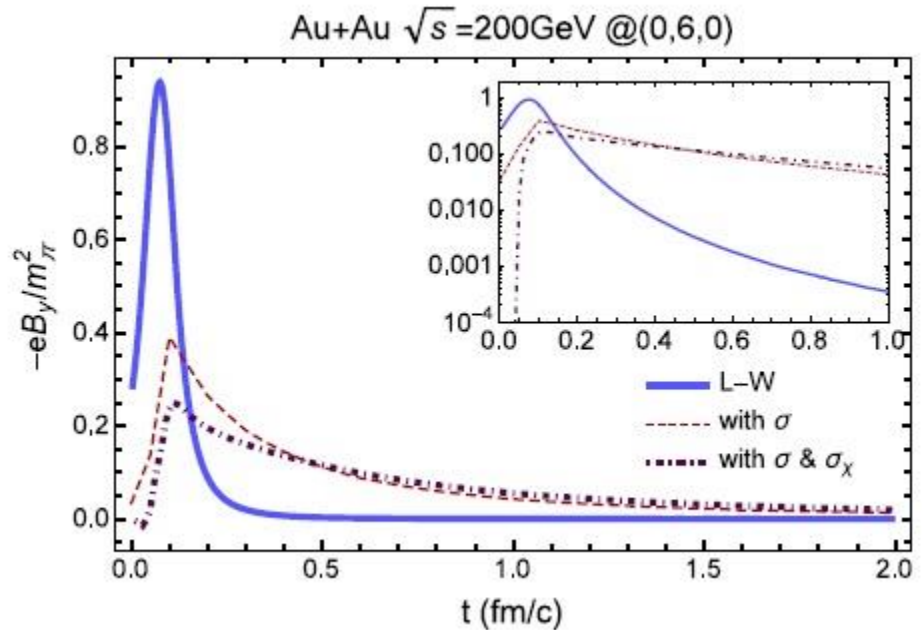
How does the magnetic field evolve?

How large the magnitude of the magnetic field remains at freeze-out?

Dynamical evolution

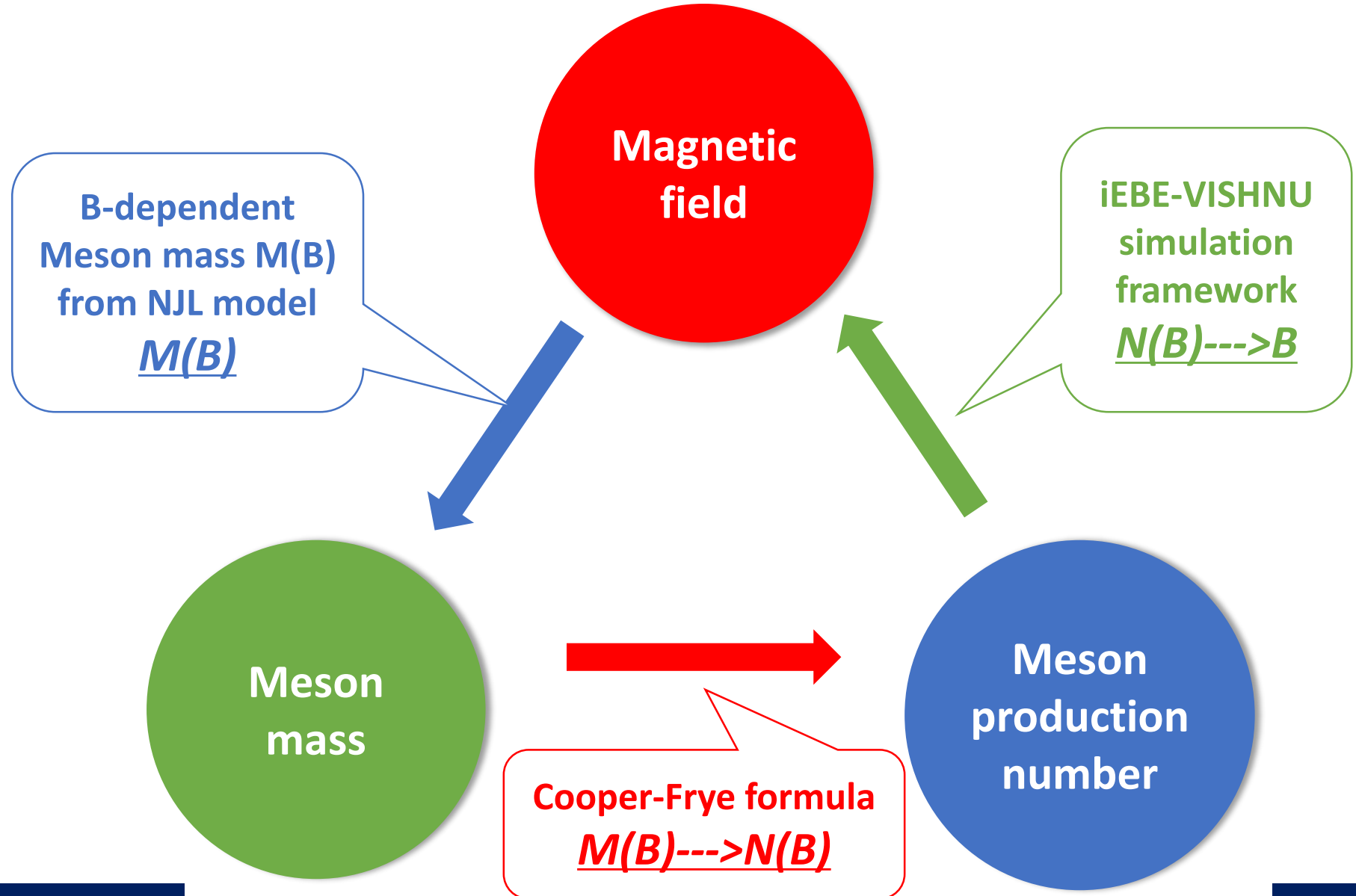


L. McLerran, V. Skokov 1305.0774



Hui Li, Xin-li Sheng, and Qun Wang 1602.02223

Motivation



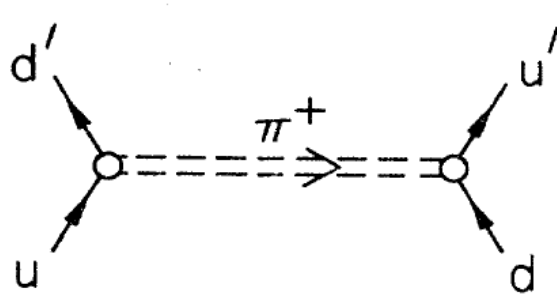
Lagrangian density of NJL model

$$\begin{aligned}\mathcal{L} = & \bar{\psi}(i\gamma^\mu D_\mu - m_0)\psi + G_S[(\bar{\psi}\psi)^2 + (\bar{\psi}i\gamma^5\vec{\tau}\psi)^2] \\ & - G_V[(\bar{\psi}\gamma^\mu\tau^a\psi)^2 + (\bar{\psi}\gamma^\mu\gamma^5\tau^a\psi)^2] \\ & + \frac{1}{4}F_{\mu\nu}F^{\mu\nu},\end{aligned}$$

Where $D_\mu = \partial_\mu - iq_f A_\mu^{\text{ext}}$

$$F_{\mu\nu} = \partial_\mu A_\nu^{\text{ext}} - \partial_\nu A_\mu^{\text{ext}}, \quad A_\mu^{\text{ext}} = \{0, 0, Bz, 0\}$$

Meson mass in NJL model



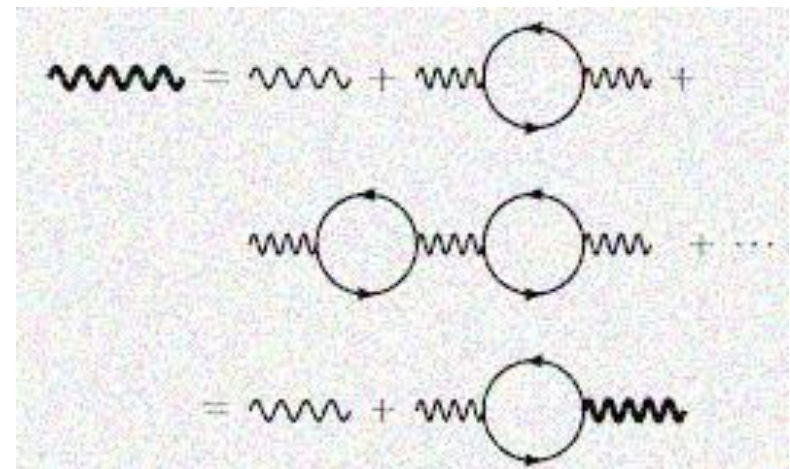
[1408.1318, Hao Liu, Lang Yu, Mei Huang]

[1507.05809, Lang Yu, Hao Liu, Mei Huang]

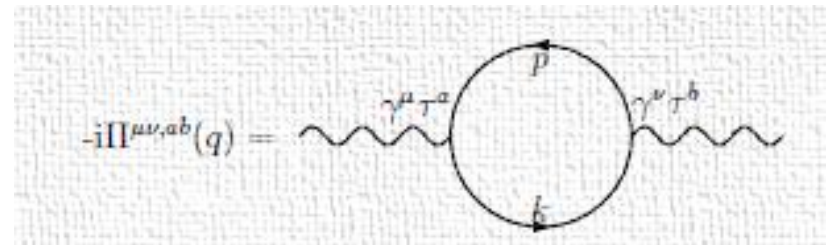
Full propagator in random phase approximation

Schwinger-Dyson equation

$$[-iD_{ab}^{\mu\nu}] = [-2iG_V\delta_{ab}g^{\mu\nu}] + [-2iG_V\delta_{ac}g^{\mu\lambda}] [-i\Pi_{\lambda\sigma,cd}] [-iD_{db}^{\sigma\nu}]$$



One-loop polarization function

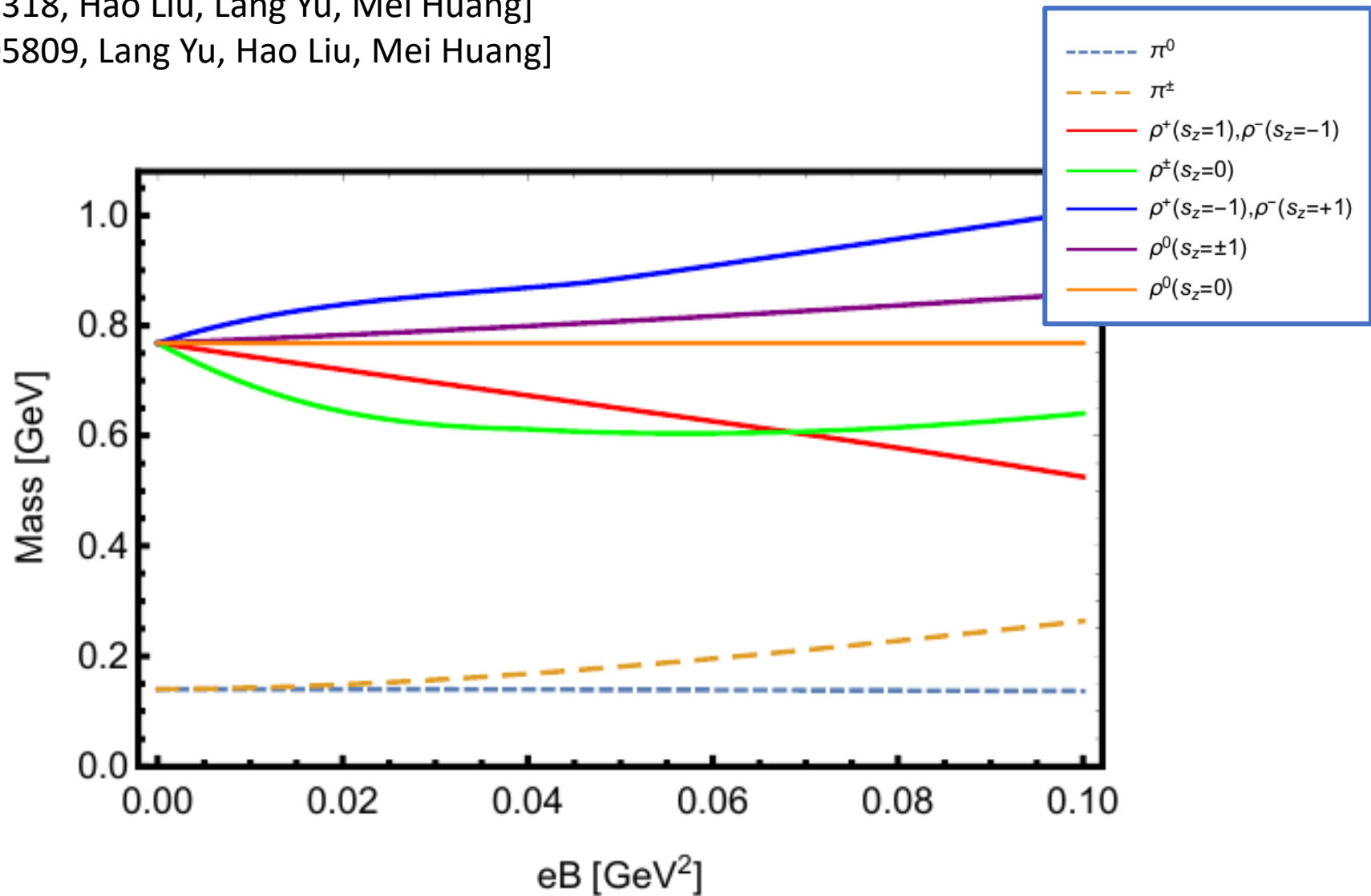


$$D(q^2) = \frac{2G}{1+2G\Pi(q^2)}, \quad 1 + 2G\Pi(q^2)=0$$

Meson mass and magnetic field

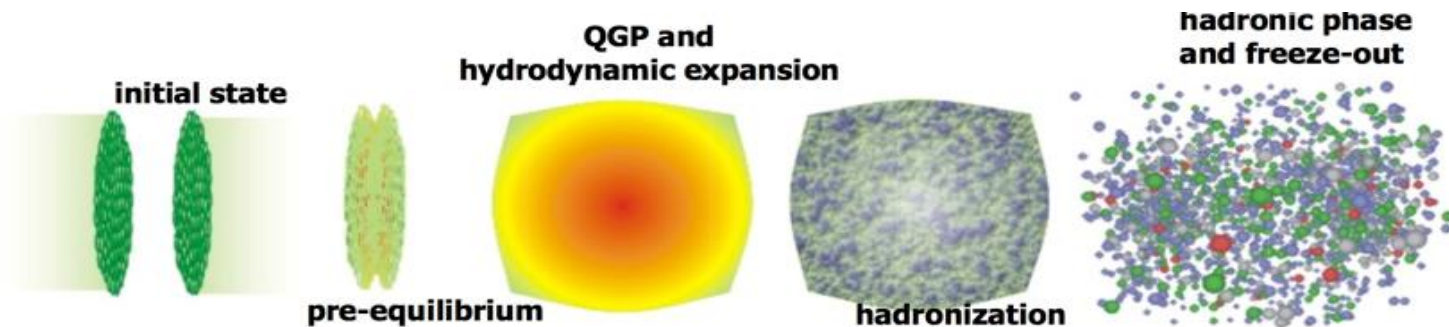
[1408.1318, Hao Liu, Lang Yu, Mei Huang]

[1507.05809, Lang Yu, Hao Liu, Mei Huang]



Evolution: Hydro->freeze-out->decay

1、Dynamical evolution of energy-momentum:



2、Chemical freeze-out. Cooper-Frye formula: [F. Cooper, G. Frye, 1974]

$$\frac{dN}{dy p_T dp_T d\phi} = \frac{g_i}{(2\pi)^3} \int_{\Sigma} p^{\mu} d\sigma_{\mu} \left[f_0 + f_0(1 \mp f_0) \frac{p^{\mu} p^{\nu} \pi_{\mu\nu}}{2T^2(e + P)} \right]$$

$$\text{where } f_0 = \frac{1}{\exp((p \cdot V)/T \pm 1)}$$

$$N \sim f(m)$$

B dependent mass

3、Hadron resonance decay:

$$\rho^{\pm} \rightarrow \pi^{\pm} + \pi^0, \rho^0 \rightarrow \pi^{+} + \pi^{-}$$

**Measurement of
production number**

Collision condition:

Au-Au collision, 200GeV, 30%-40% centrality

Assumptions:

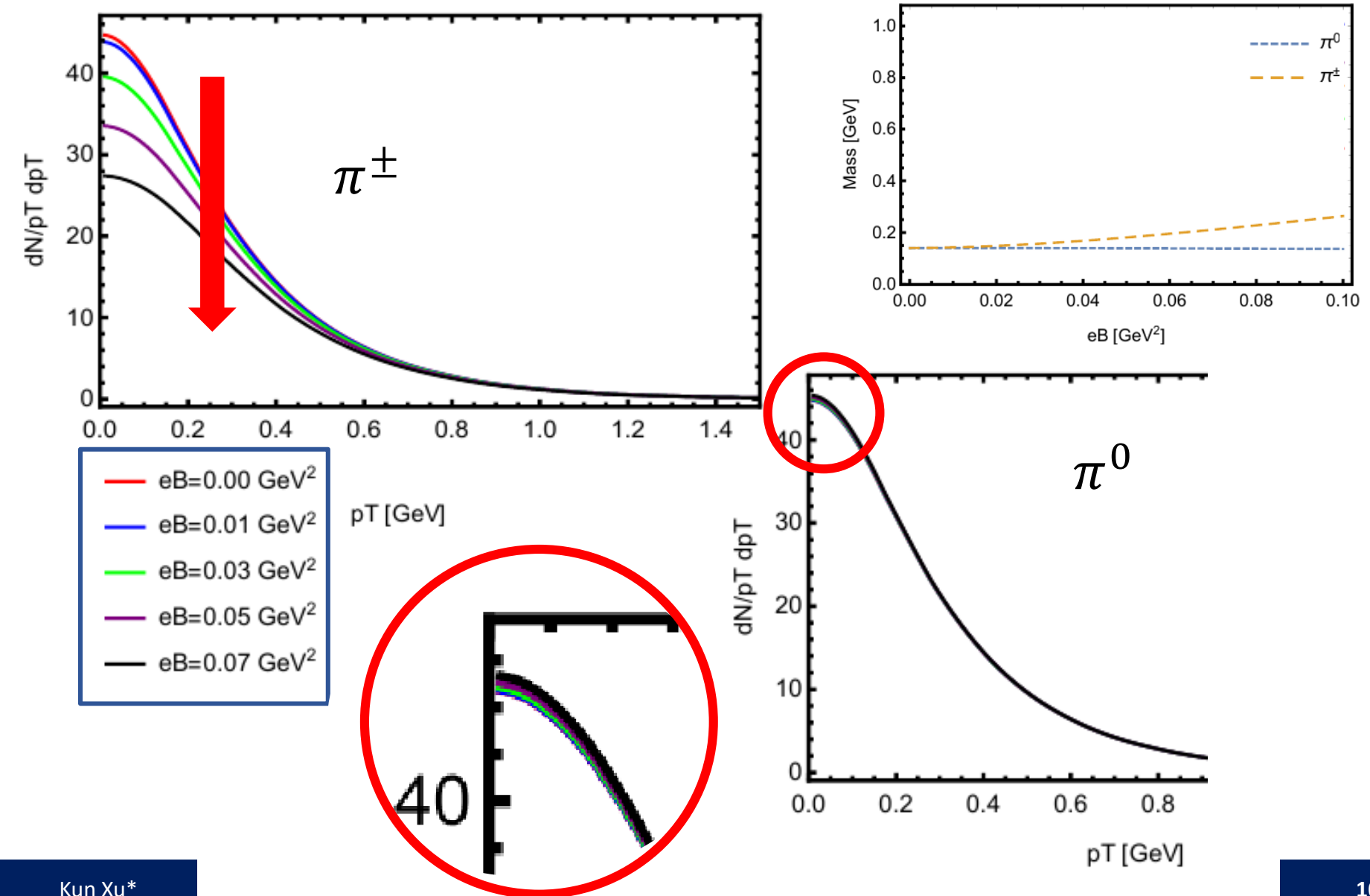
- 1、 only pion and rho are considered;
- 2、 "averaged freeze out time" τ_{ave} ;

$$\tau_{ave} = \frac{\int (dN/d\tau) \tau d\tau}{\int (dN/d\tau) d\tau}$$

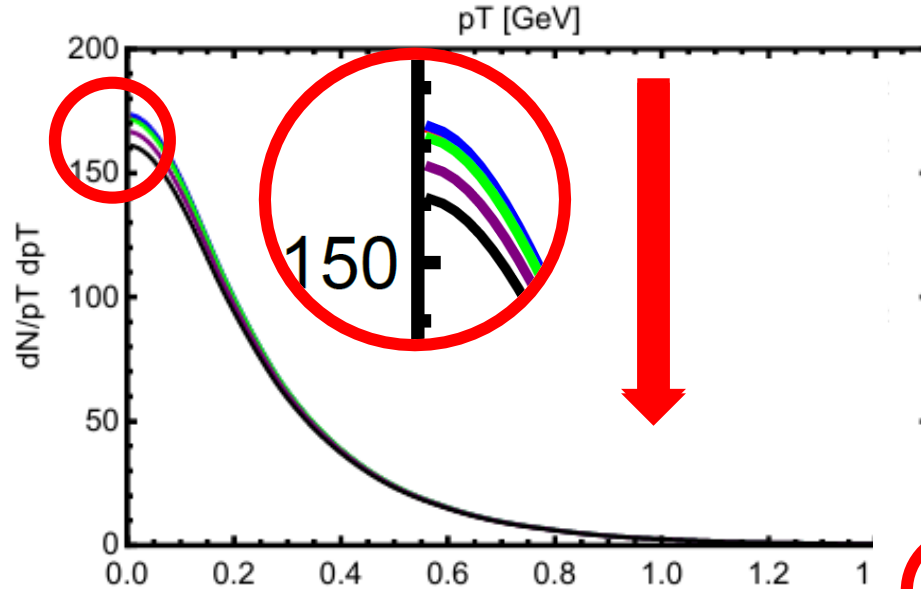
dN: number of hadrons freeze out at $\tau \rightarrow \tau + d\tau$

- 3、 no magnetic field at hadron resonance decay stage.

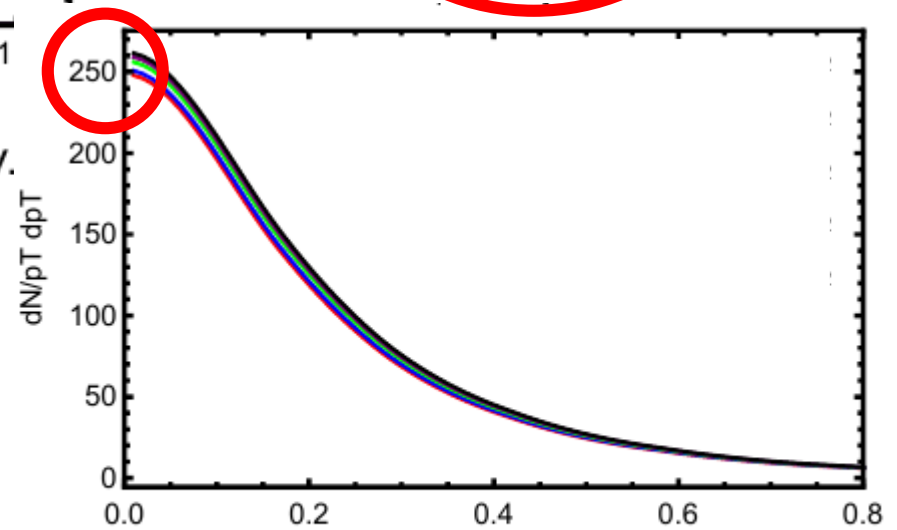
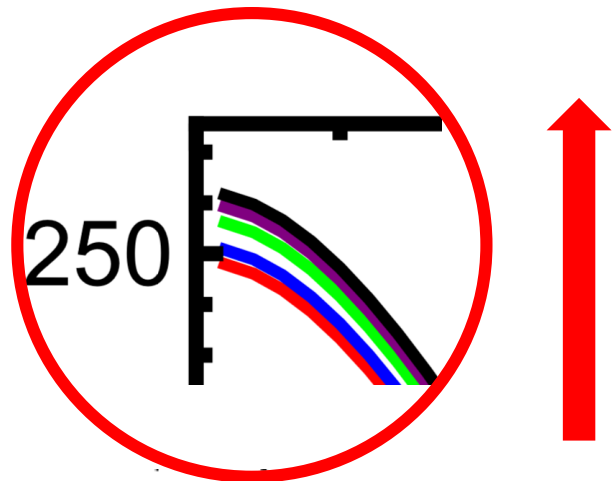
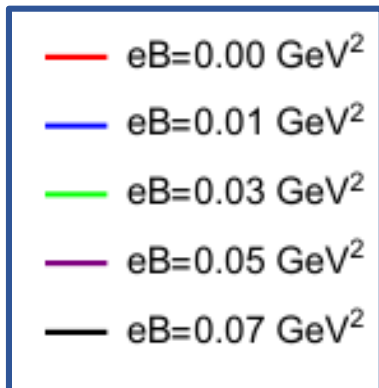
(Momentum distribution) Pion from chemical freeze out



(Momentum distribution) Pion after hadron resonance decay stage

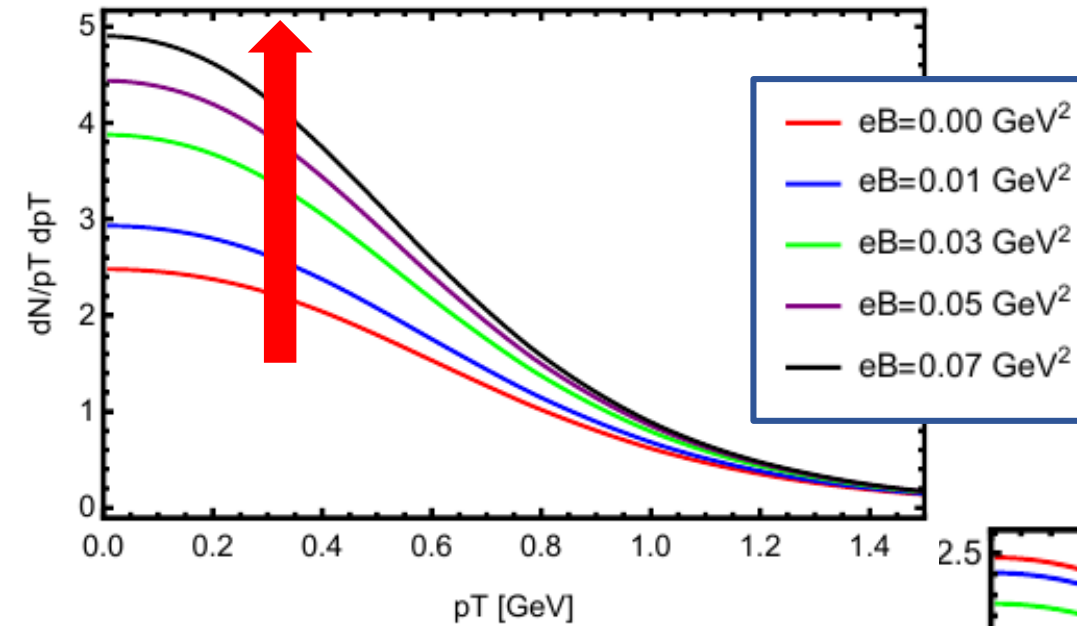


π^\pm , hadron resonance decay.



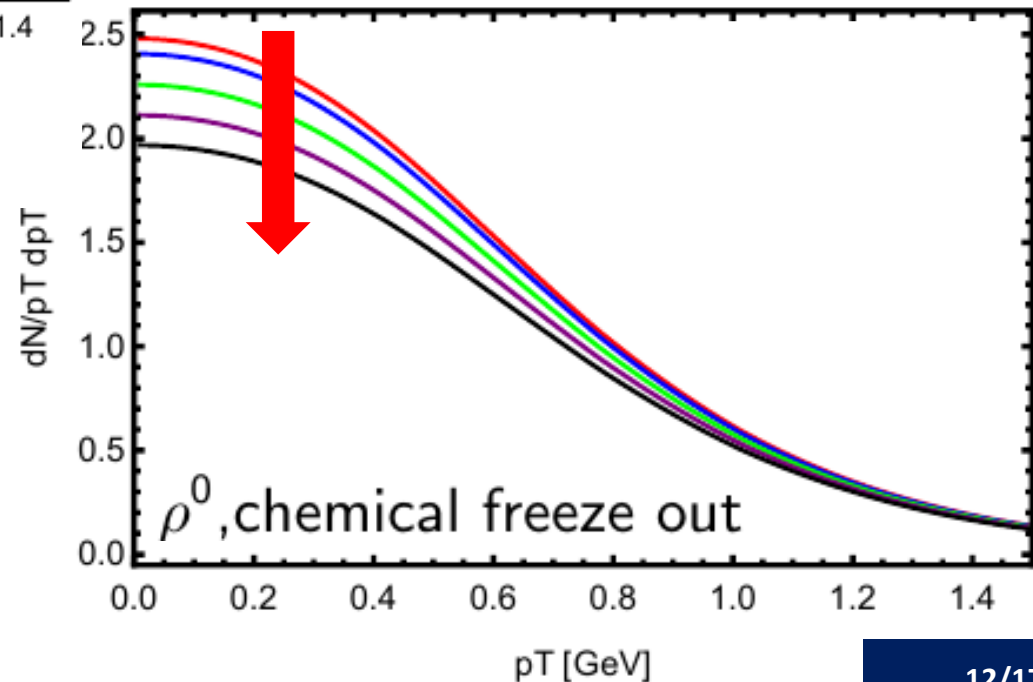
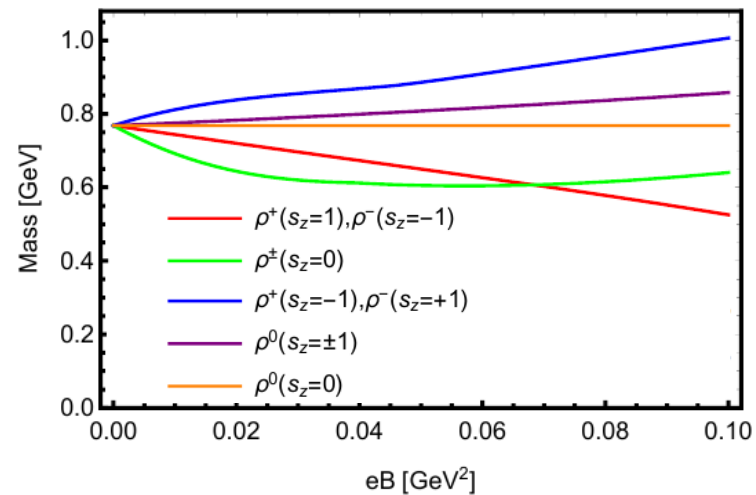
π^0 , hadron resonance decay.

(Momentum distribution) Rho from chemical freeze out



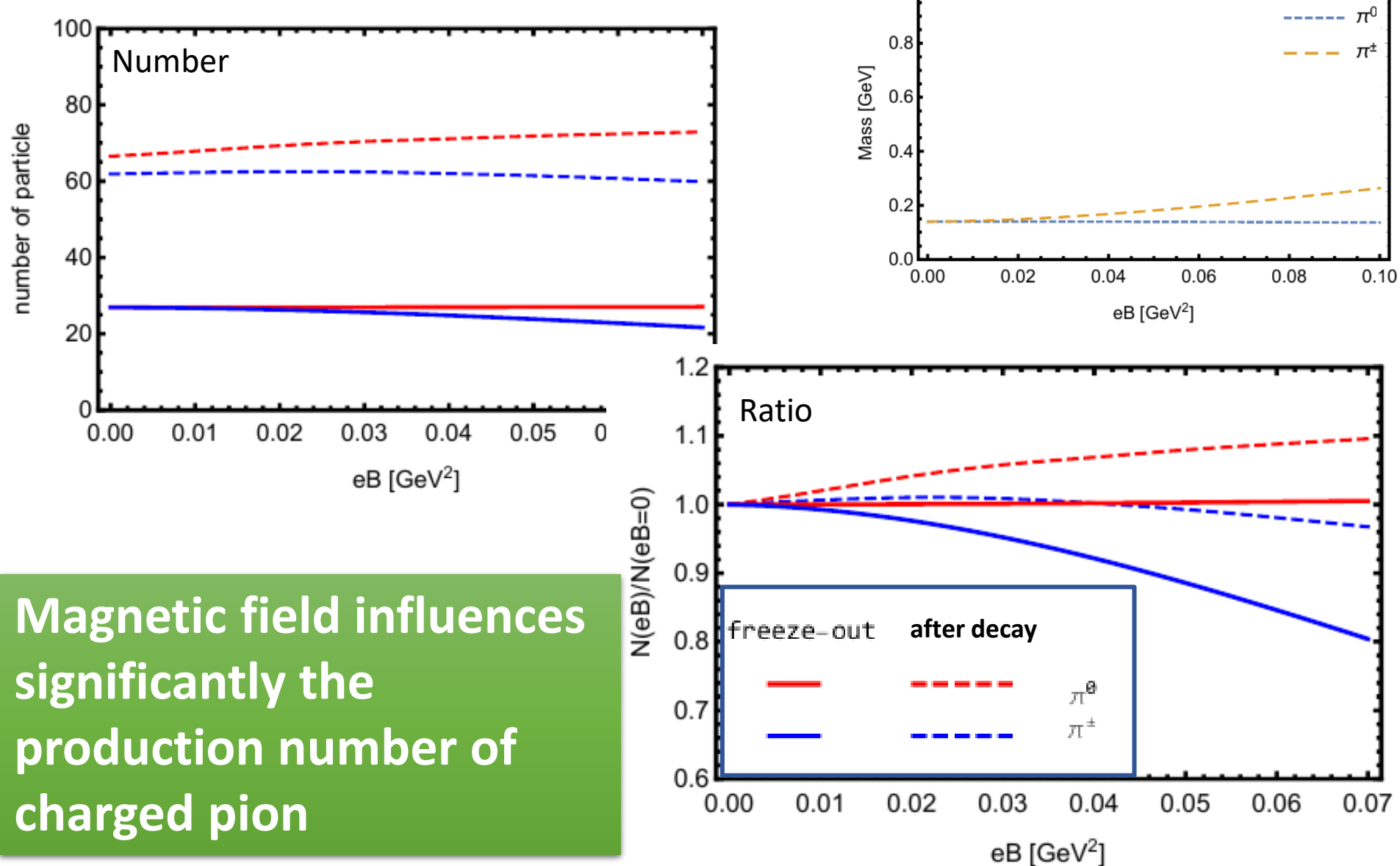
ρ^\pm , chemical freeze out

$$\rho^\pm \rightarrow \pi^\pm + \pi^0, \rho^0 \rightarrow \pi^+ + \pi^-$$



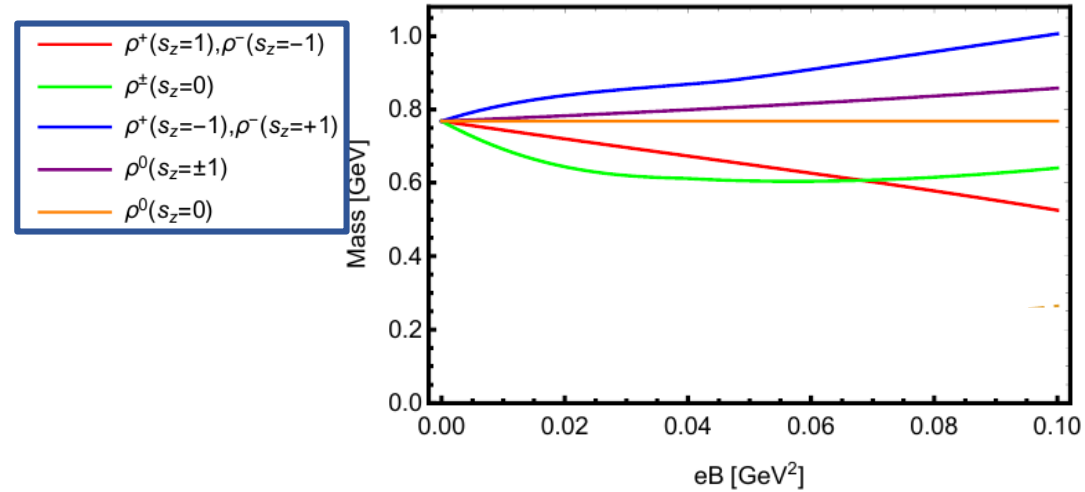
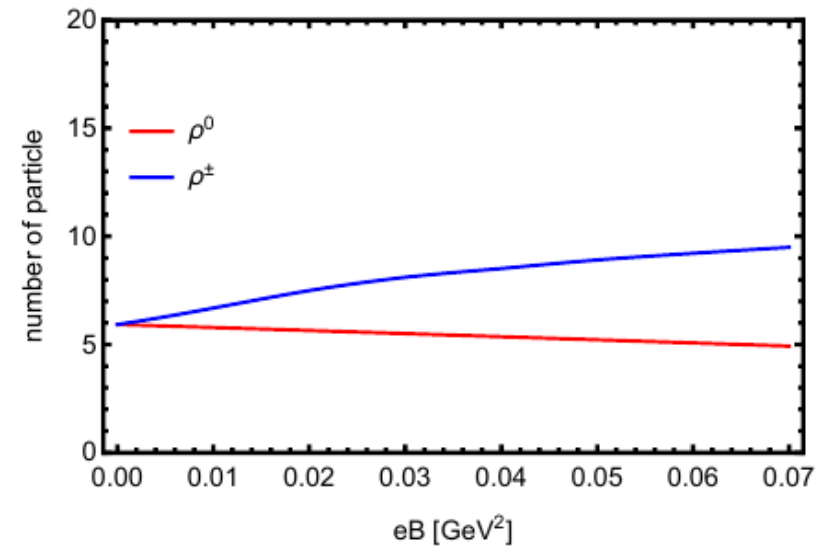
ρ^0 , chemical freeze out

Production number of pion ($0.15\text{GeV} < p_t < 2\text{GeV}$)

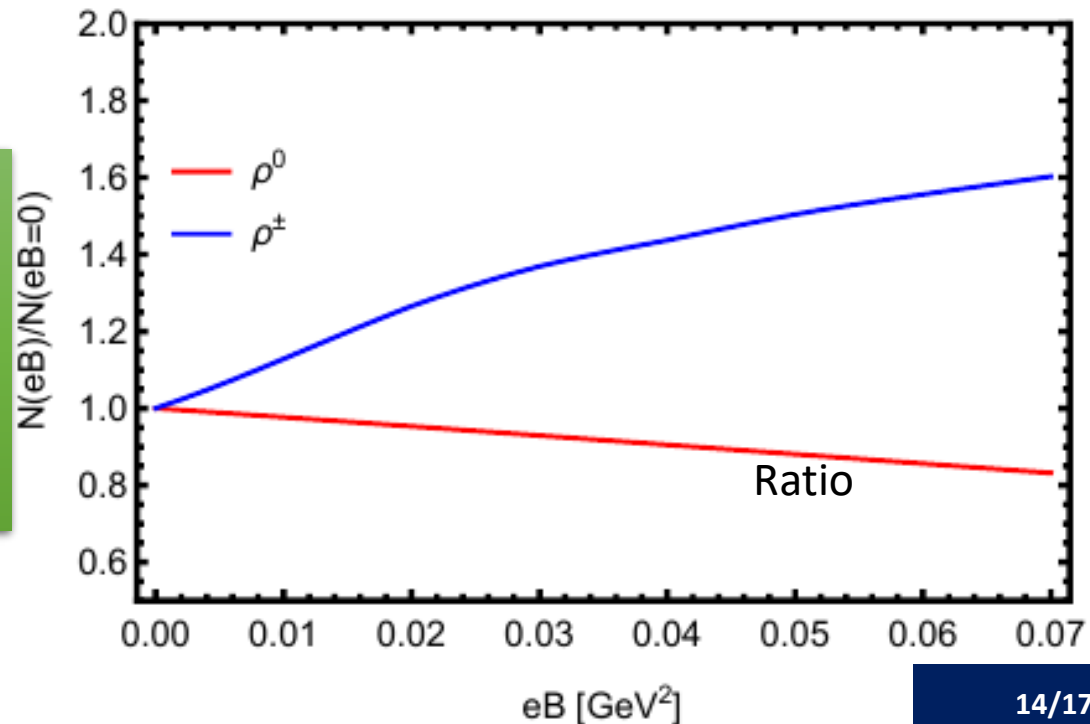


Magnetic field influences significantly the production number of charged pion

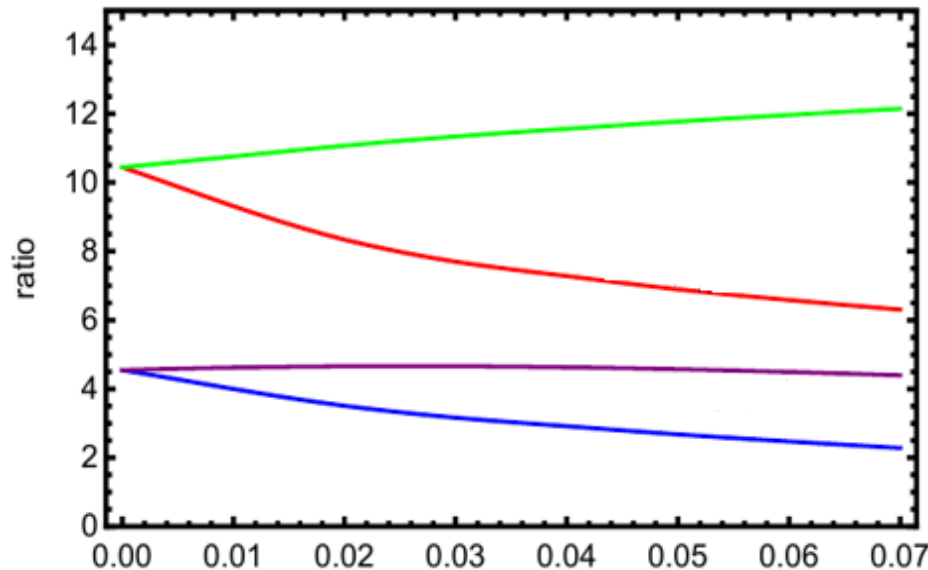
Production number of rho ($0.15\text{GeV} < p_t < 2\text{GeV}$)



Magnetic field influences significantly the production number of charged rho

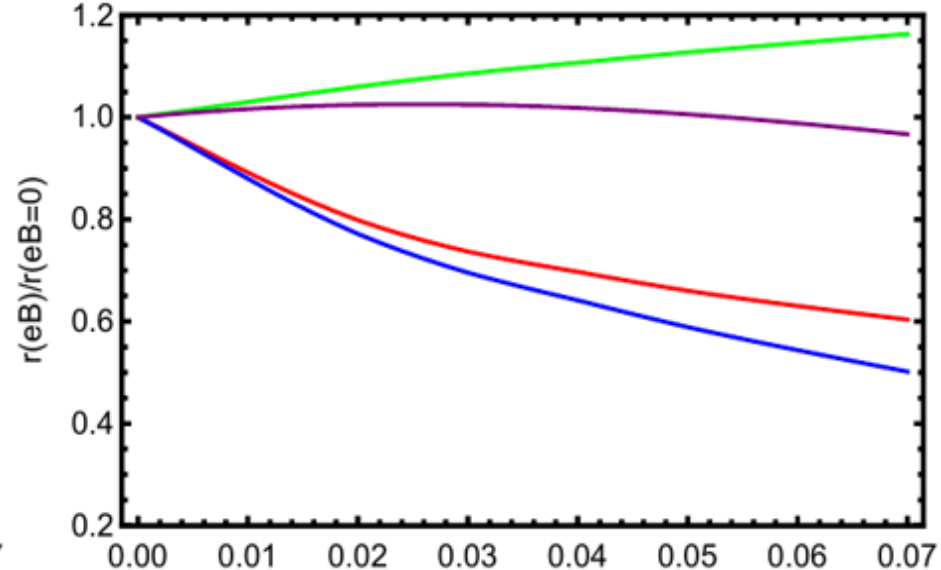


Ratio of pion number over rho number



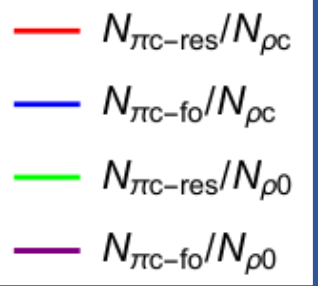
eB [GeV²]

(a)



eB [GeV²]

(b)



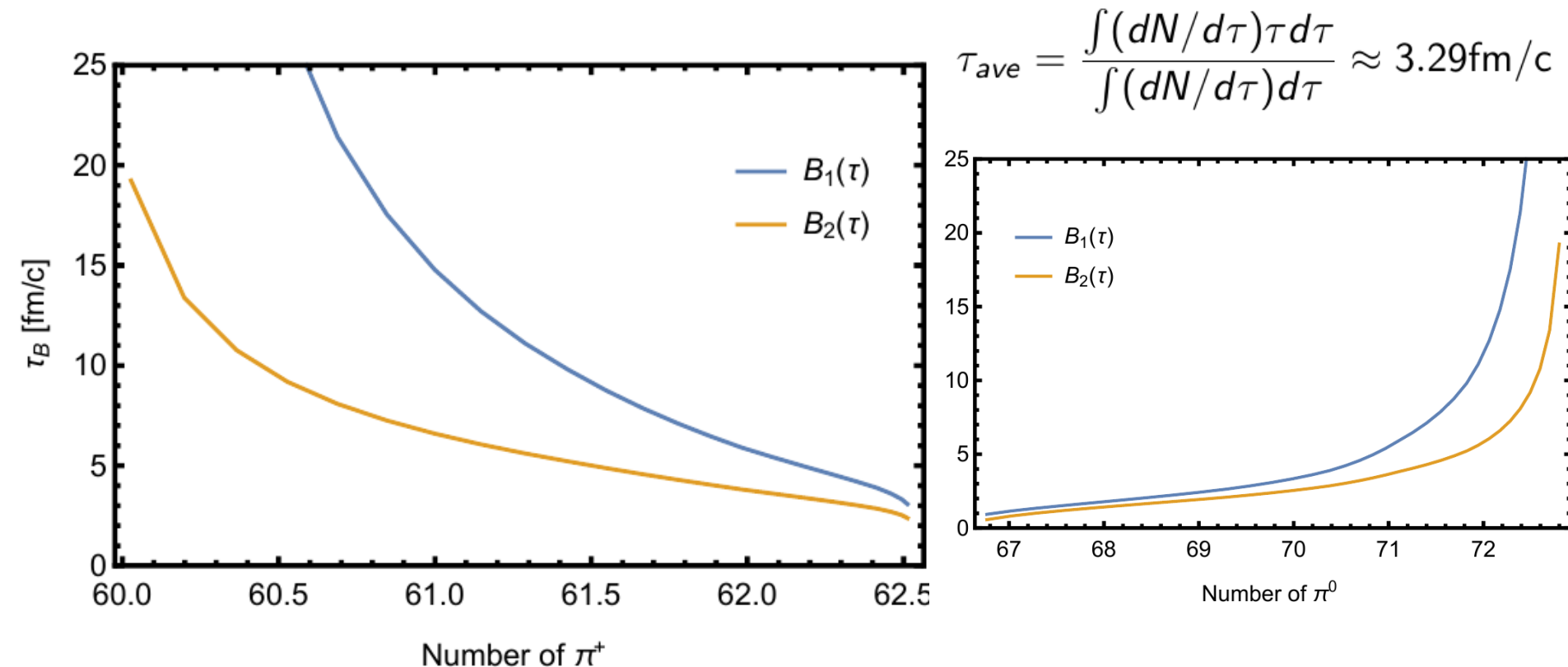
Magnetic field influences the ratio of the number of charged pion over the number of charged rho significantly.

Assumed evolution function

[Yin Jiang, Shuzhe Shi, Yi Yin, Jinfeng Liao] 1611.04586

[Shuzhe Shi, Yin Jiang, Elias Lilleskov, Jinfeng Liao] 1711.02496

$$B_1(\tau) = B_0 e^{-\frac{\tau}{\tau_{1,B}}}, \quad B_2(\tau) = \frac{B_0}{1 + (\tau/\tau_{2,B})^2}, \quad eB_0 = 0.07 \text{ GeV}^2$$



tau_B can be determined by the production number of pion;
tau_B is sensitive to the production number of pion

Summary

- Magnetic field influences the production number of rho and pion, significantly for charged rho and charged pion;
- Magnetic field influences the ratio of the production number of pion over the production number of rho, significantly for charged pion over charged rho;
- τ_B can be determined by the production number of pion;
- τ_B is sensitive to the production number of pion

FUTURE:

- realistic freeze out;
- magnetic field evolution;
- temperature dependence

THANKS