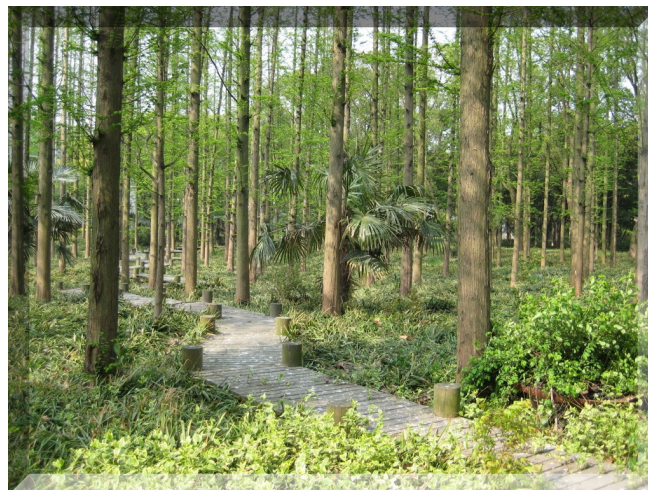


# $\alpha$ -clustering nuclei effect in relativistic heavy ion collisions by AMPT model

Song Zhang (张松)

Fudan University (复旦大学)



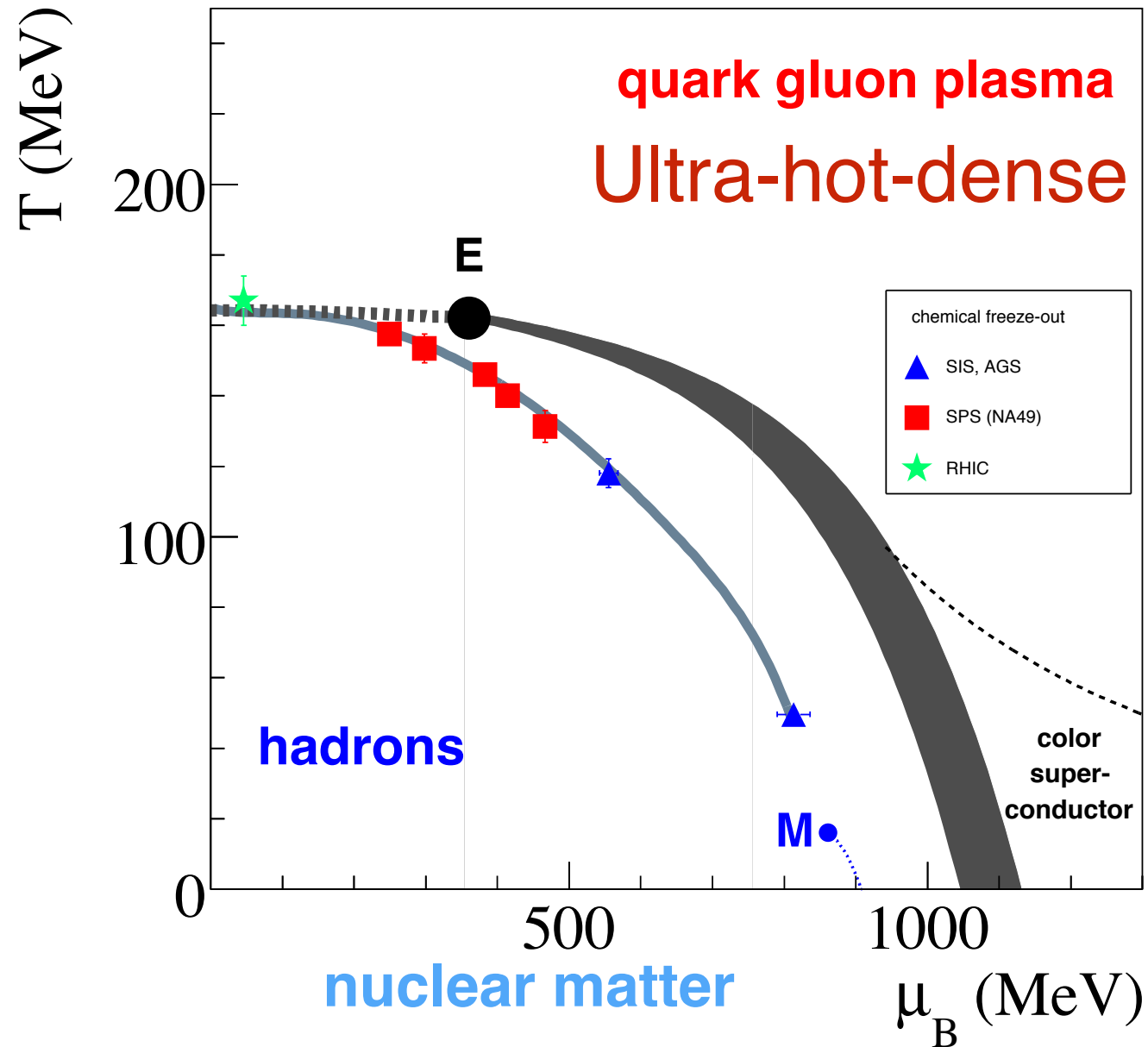


# Outline

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- Introduction to RHIC
- Initial geometry distribution/fluctuation and  $\alpha$ -clustered nuclei
- Model and  $\alpha$ -cluster nuclei effect
- Summary

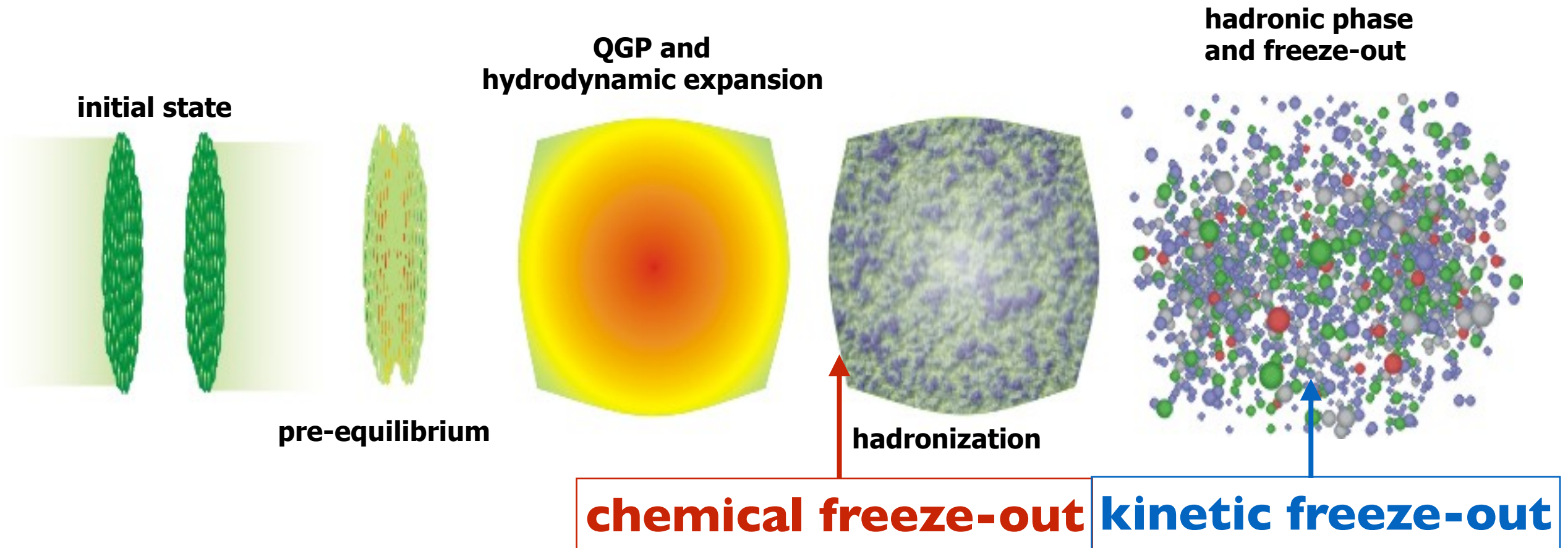
# Nuclear matter & History of universe



- ✓ QCD, quark-gluon plasma (QGP)
- ✓ Early stage of universe, relativistic heavy-ion collisions at laboratory

# High energy nucleus-nucleus collisions

## Micro-bangs in A+A collisions at laboratory



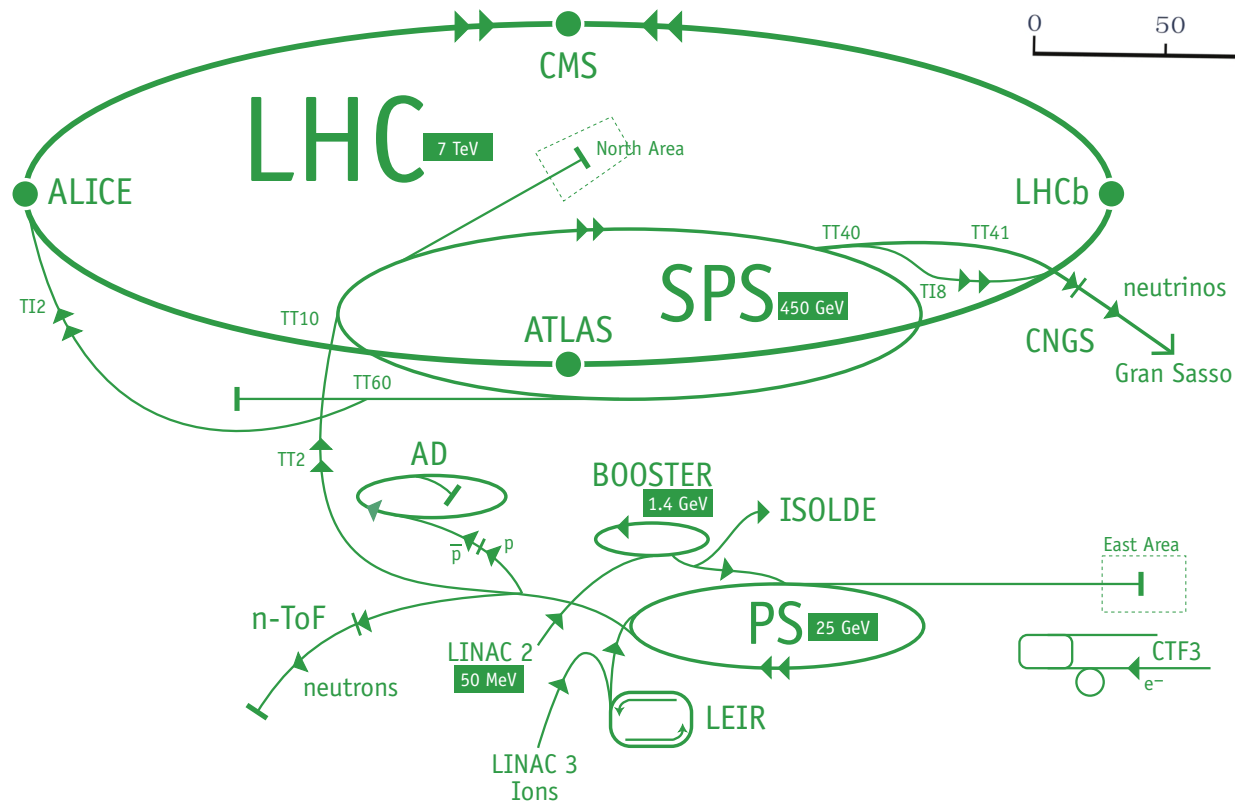
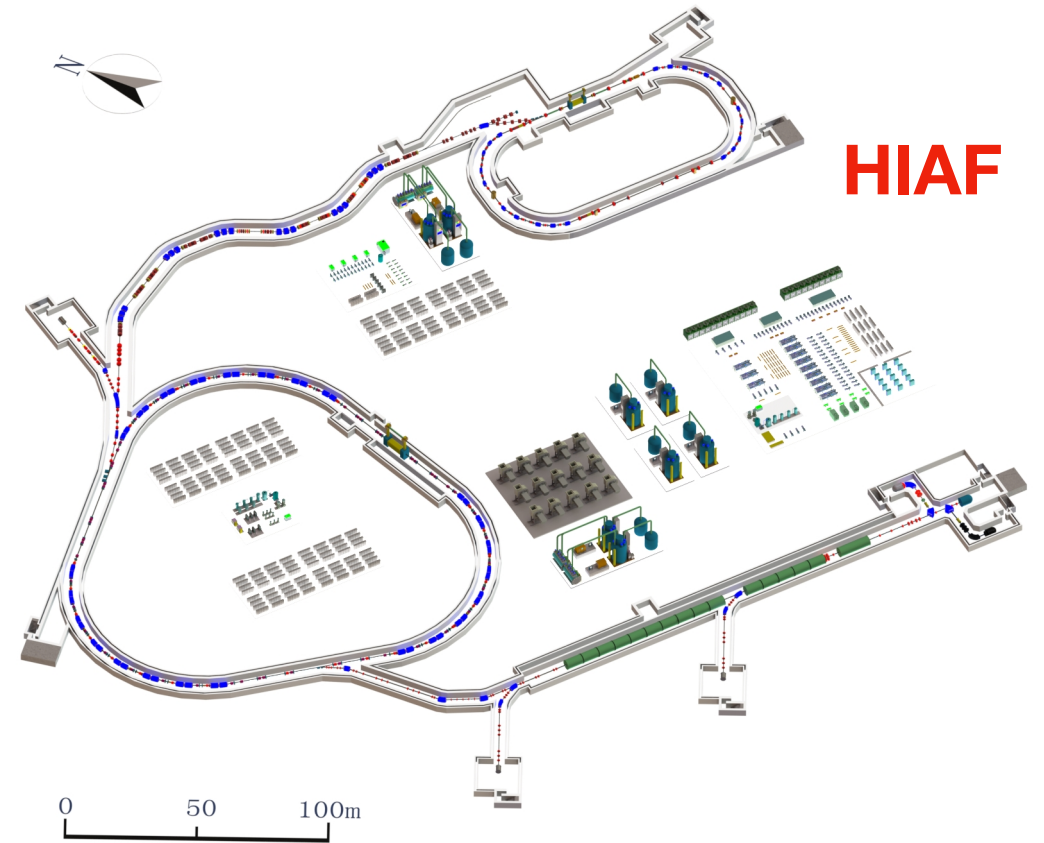
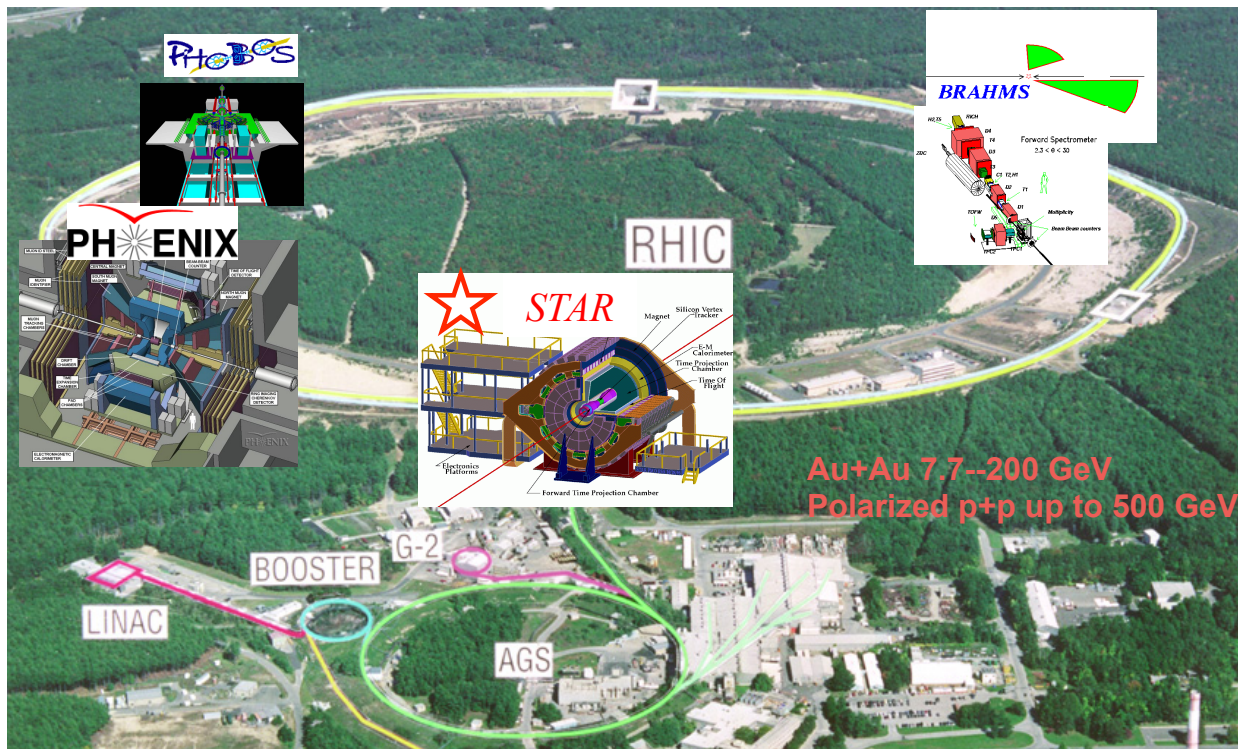
### Physics:

- 1) Parton distributions in nuclei
- 2) Initial conditions of the collision
- 3) a new state of matter – Quark-Gluon Plasma and its properties
- 4) hadronization





# Relativistic heavy-ion collider—RHIC





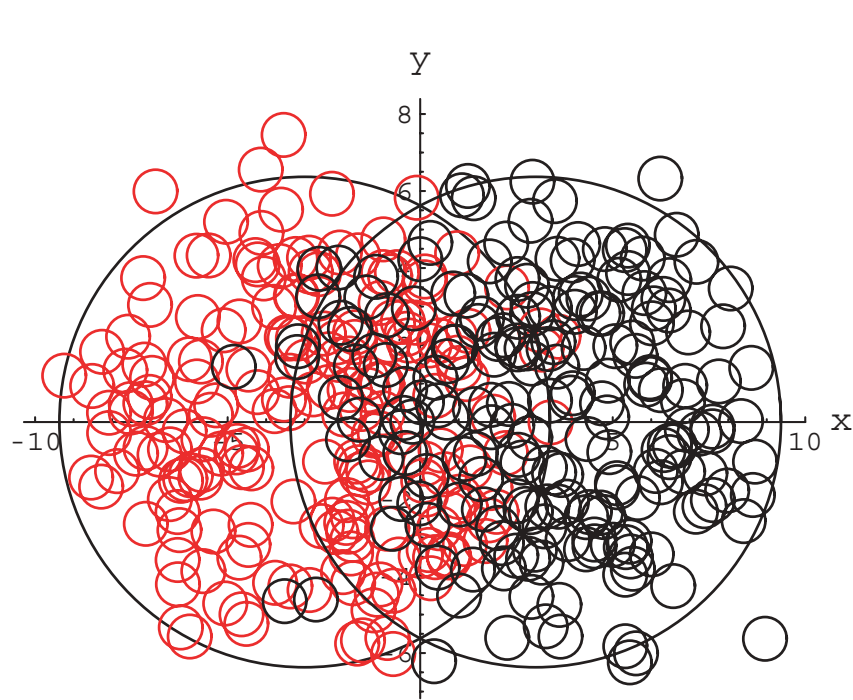
# Initial fluctuation and intrinsic geometry

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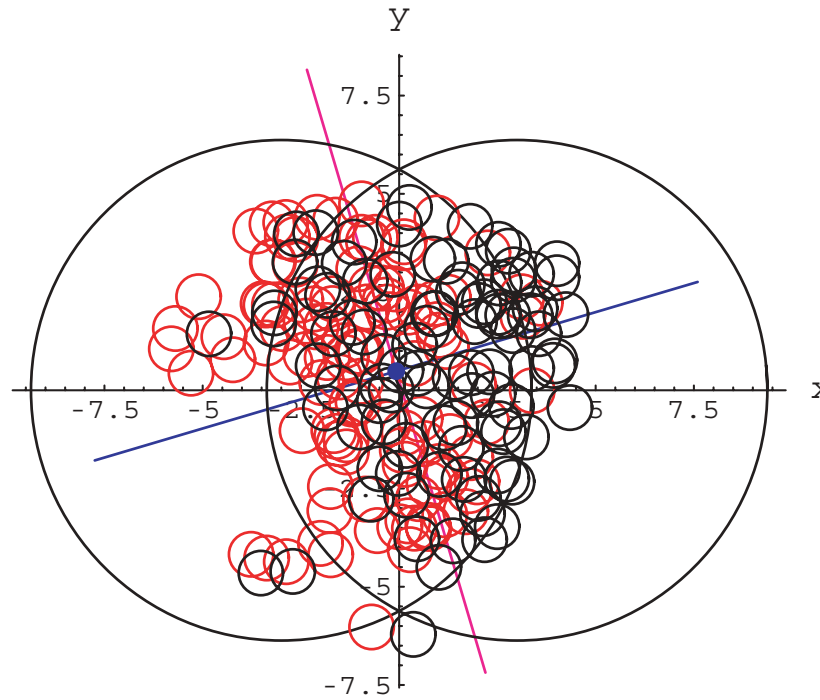
- Initial fluctuation
- Intrinsic geometry
- Flow in small system

# Initial geometry fluctuation

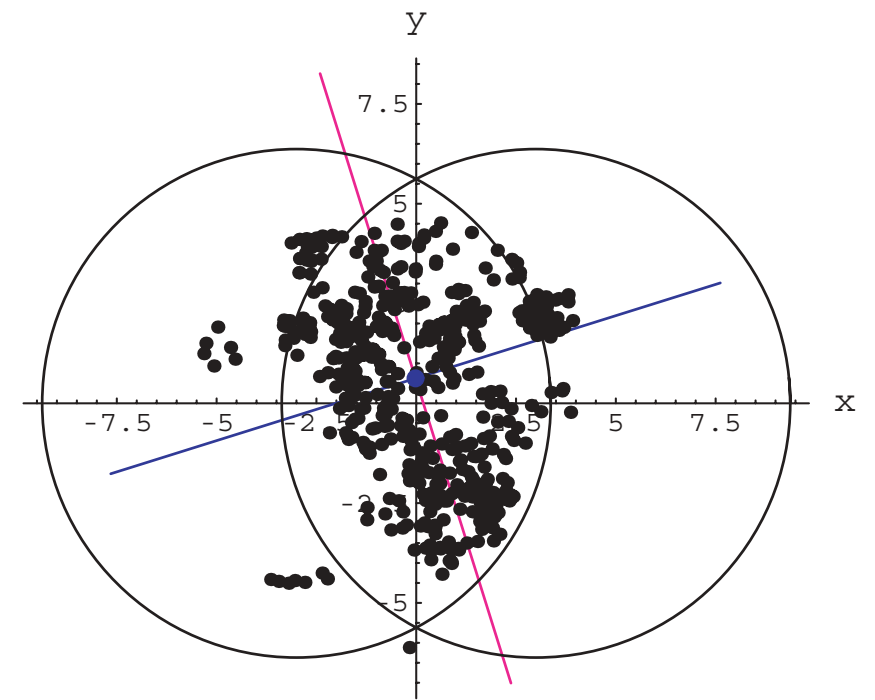
W. Broniowski et al., PRC-76-054905



Nucleon from  
nuclei A and B



Participant initial  
coordinates

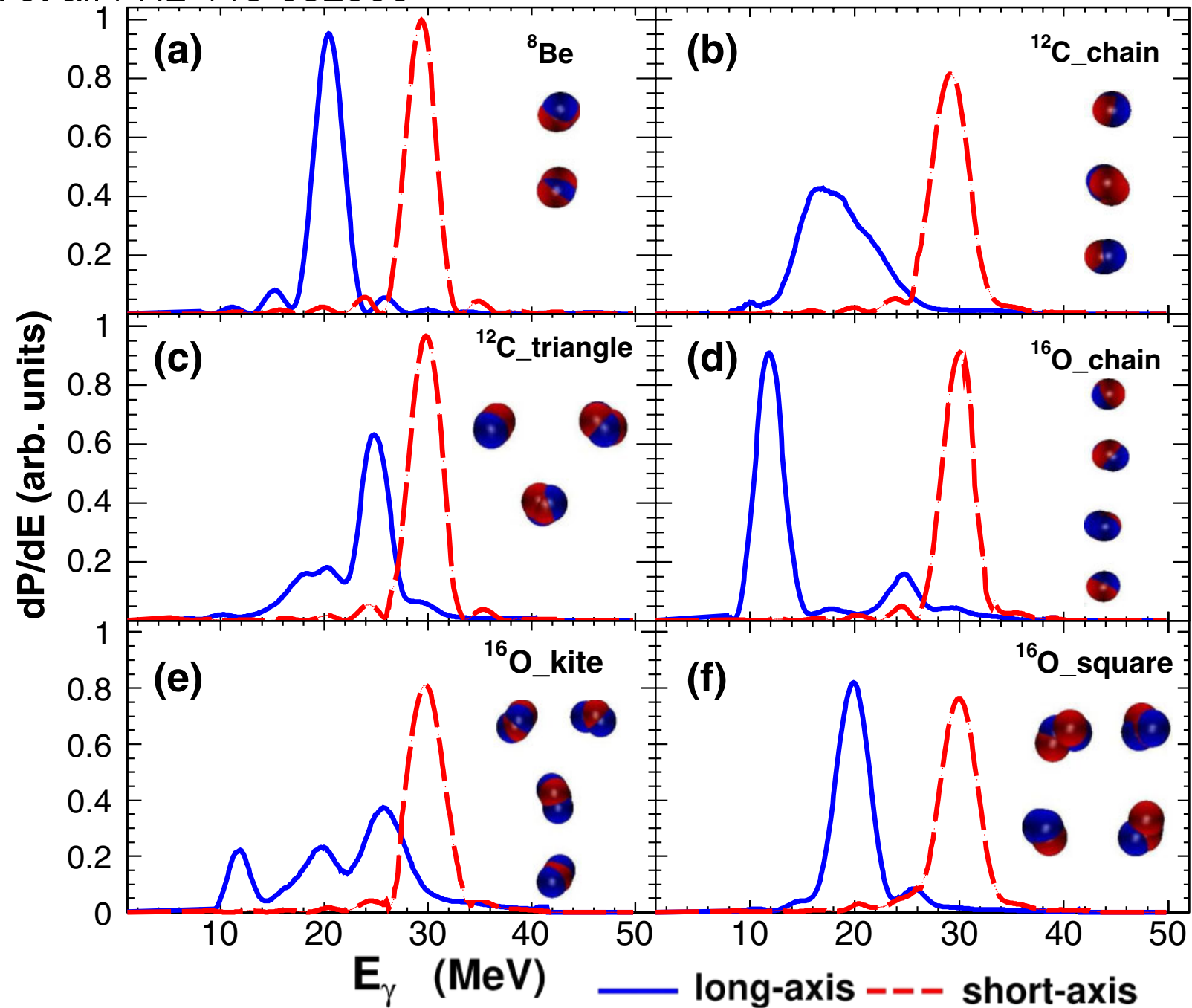


Participant in  
center of mass  
frame after  
binary collision

✓ **Fluctuation, significant in small system**

# $\alpha$ -cluster nuclear structure

W. B. He, Y. G. Ma et al. PRL-113-032506



✓ Intrinsic geometry distribution

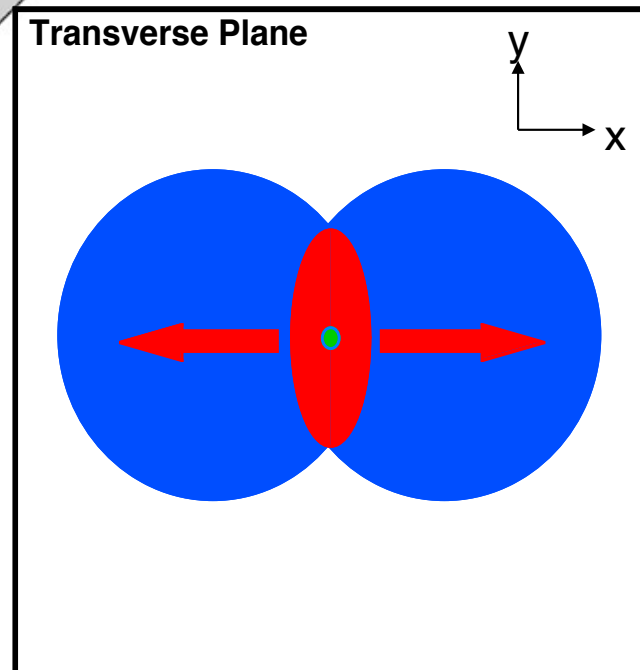
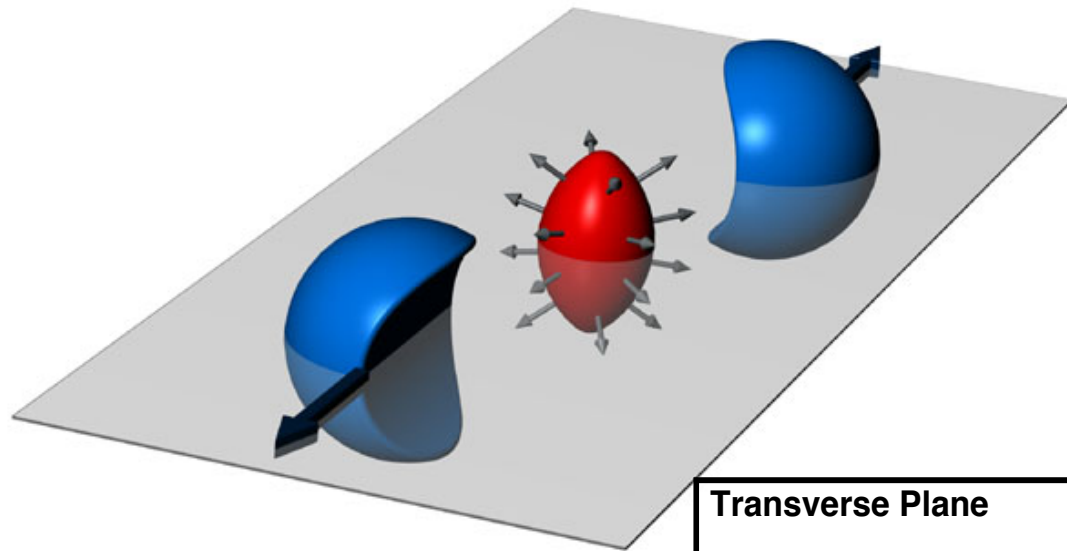


# Collective flow

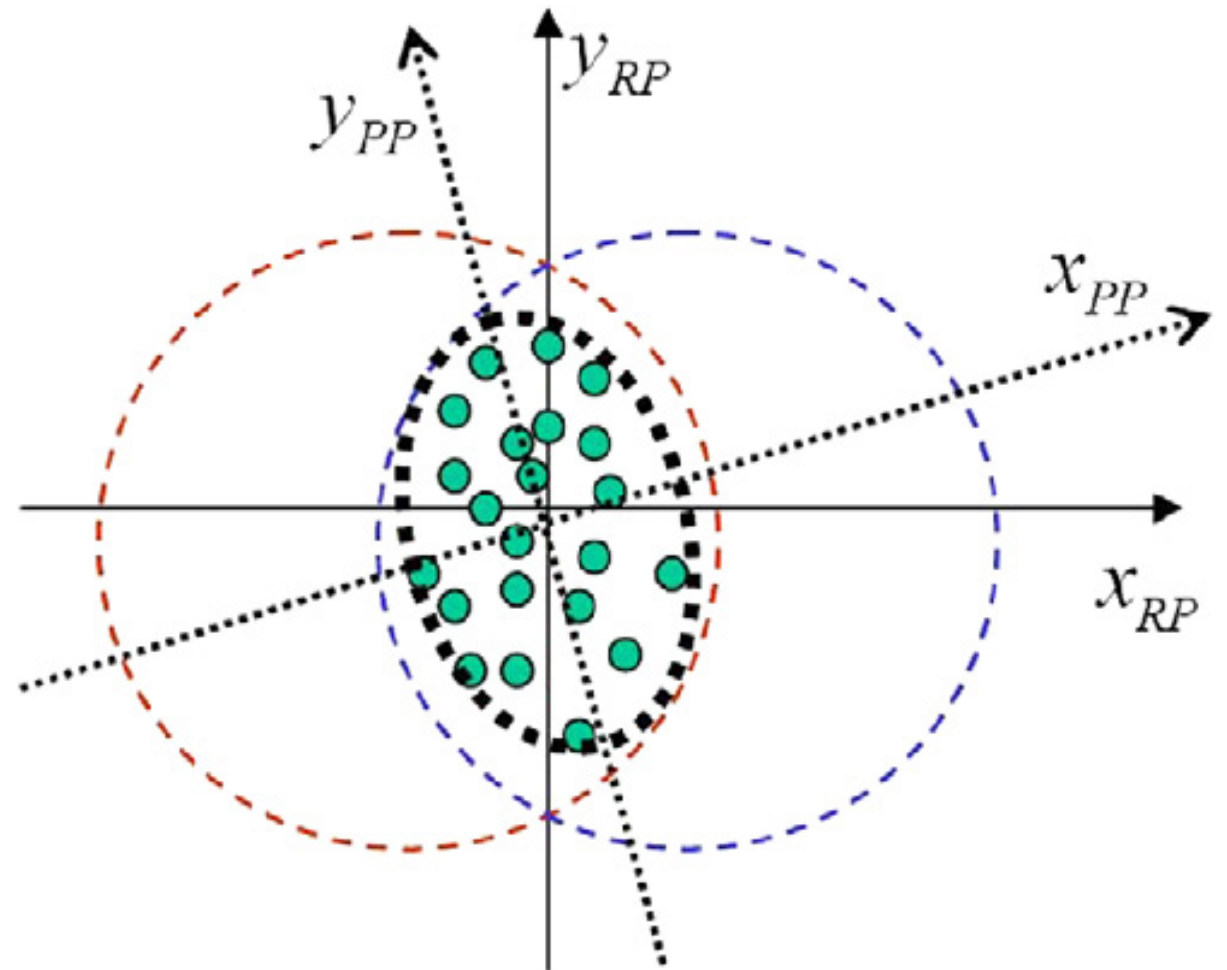
$$E \frac{d^3 N}{d^3 p} = \frac{1}{2\pi} \frac{d^2 N}{p_T dp_T dy} \left( 1 + \sum_{n=1}^{\infty} 2v_n \cos[n(\phi - \Psi_r)] \right)$$

A. M. Poskanzer, S. A. Voloshin, Phys. Rev. C 58 (1998) 1671

$$v_n = \langle \cos[n(\phi - \Psi_r)] \rangle$$



S.A. Voloshin et al. / Physics Letters B 659 (2008) 537–541



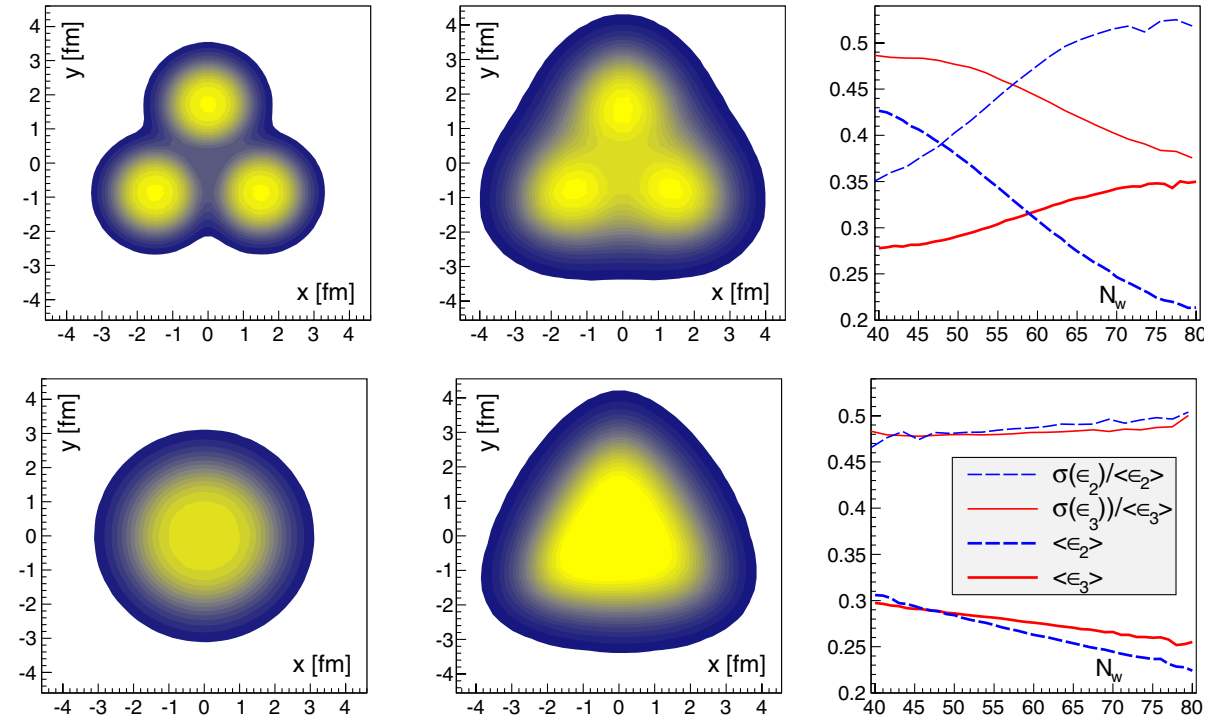


# $\alpha$ -cluster nuclei collide against heavy nuclei



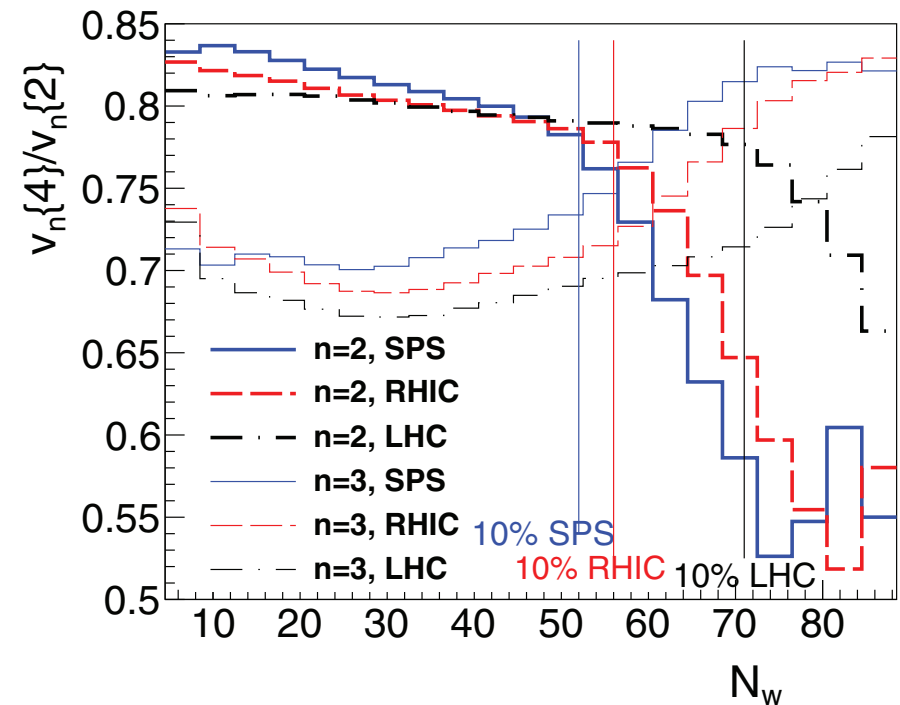
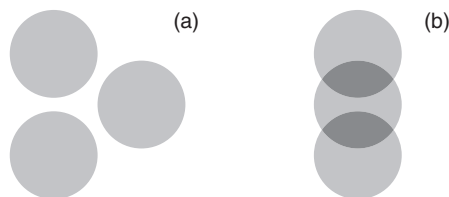
W. Broniowski, E. R. Arriola, PRL-112-112501

$^{12}\text{C}-^{208}\text{Pb}$



P. Bozek, W. Broniowski et al., PRC-90-064902

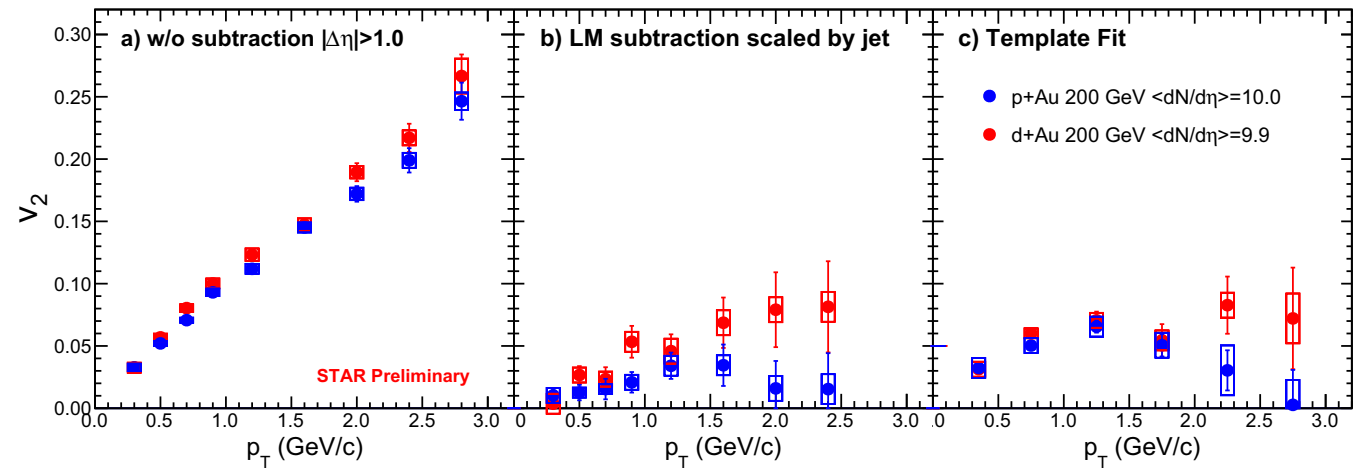
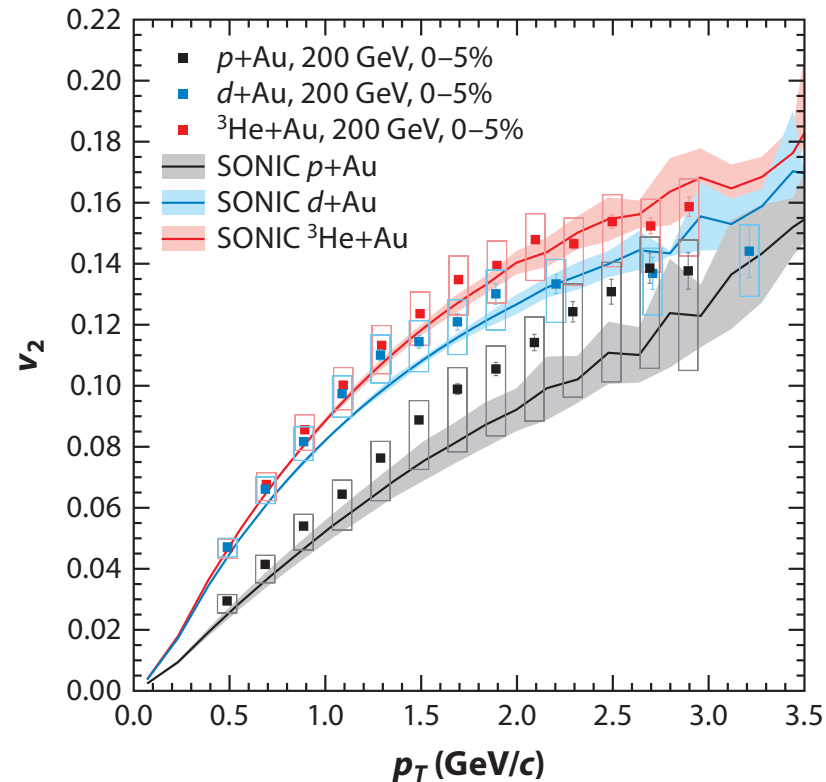
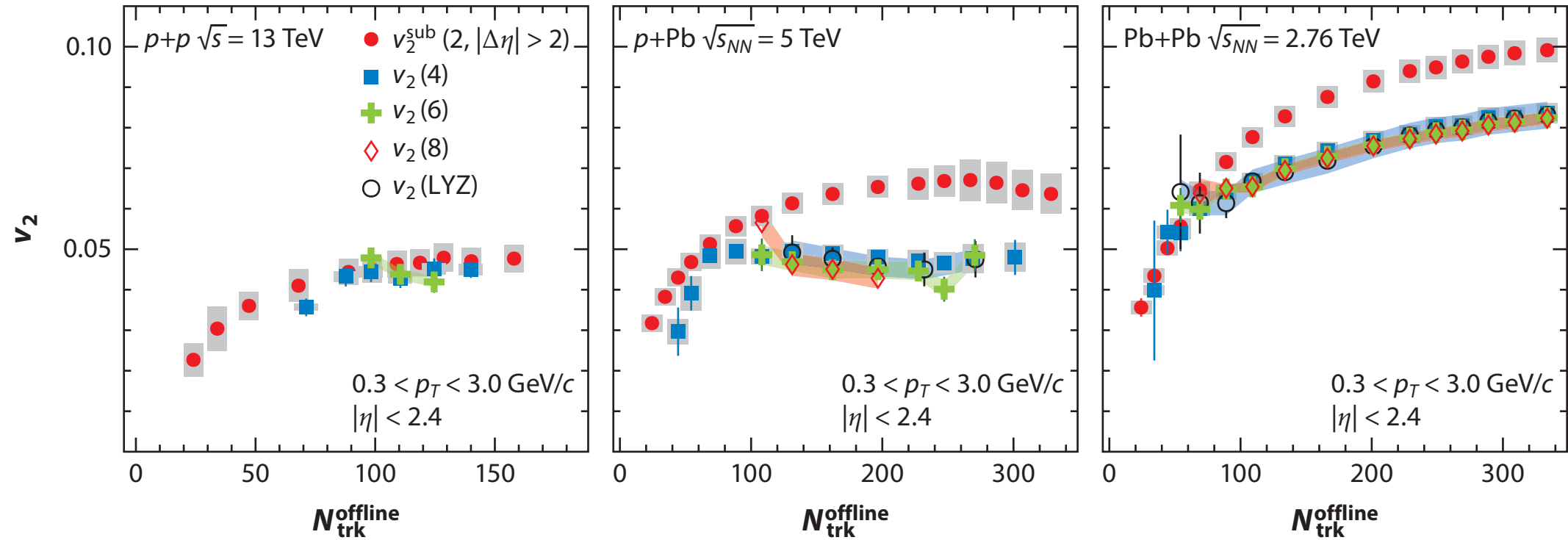
$$\frac{\epsilon_n\{4\}}{\epsilon_n\{2\}} \simeq \frac{v_n\{4\}}{v_n\{2\}}.$$





# Collective flow in small system from experiments

Khachatryan V, et al. (CMS), *Phys. Lett. B* 765:193 (2017)

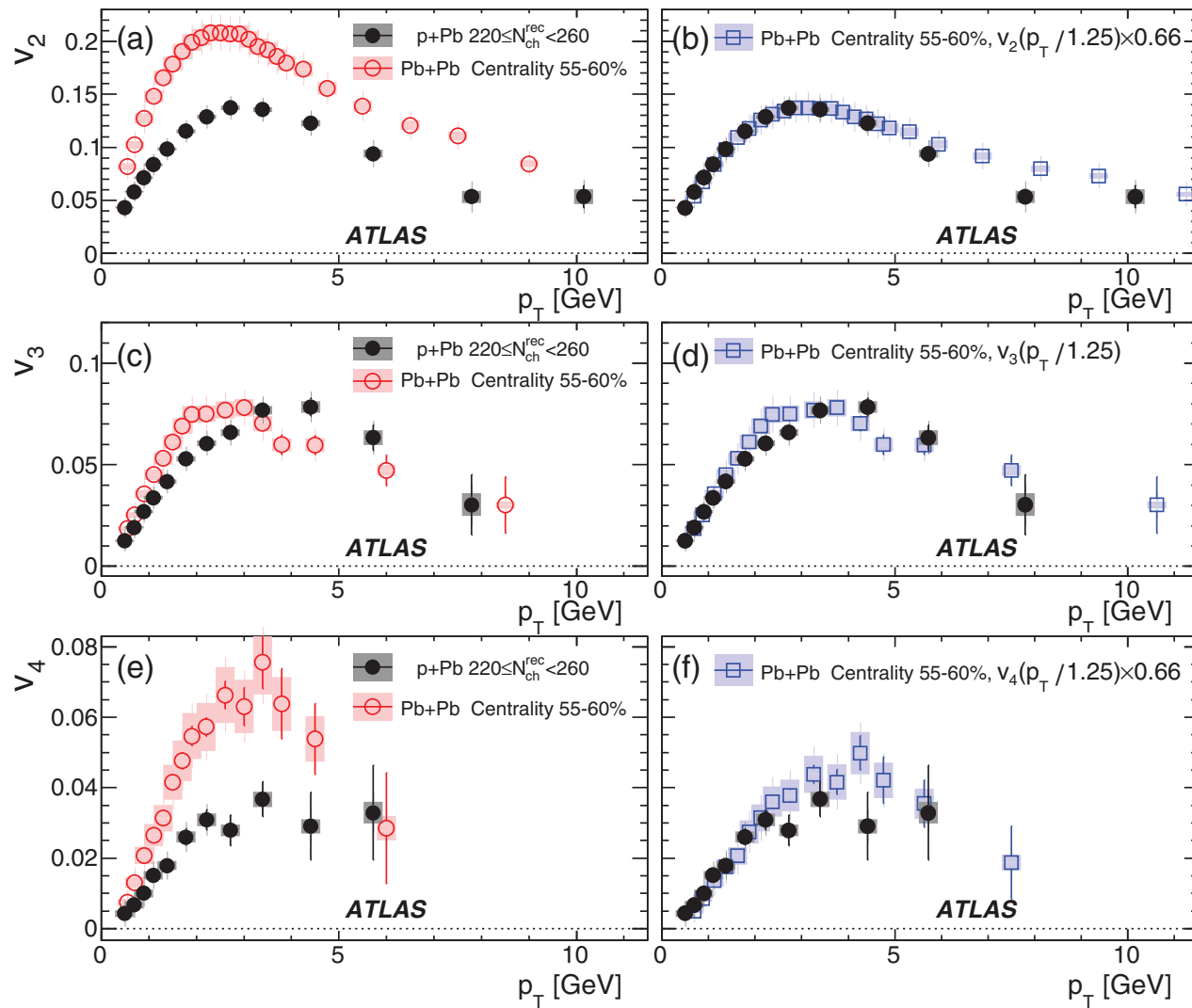


S. Huang, *Nuclear Physics A* 982 (2019) 475

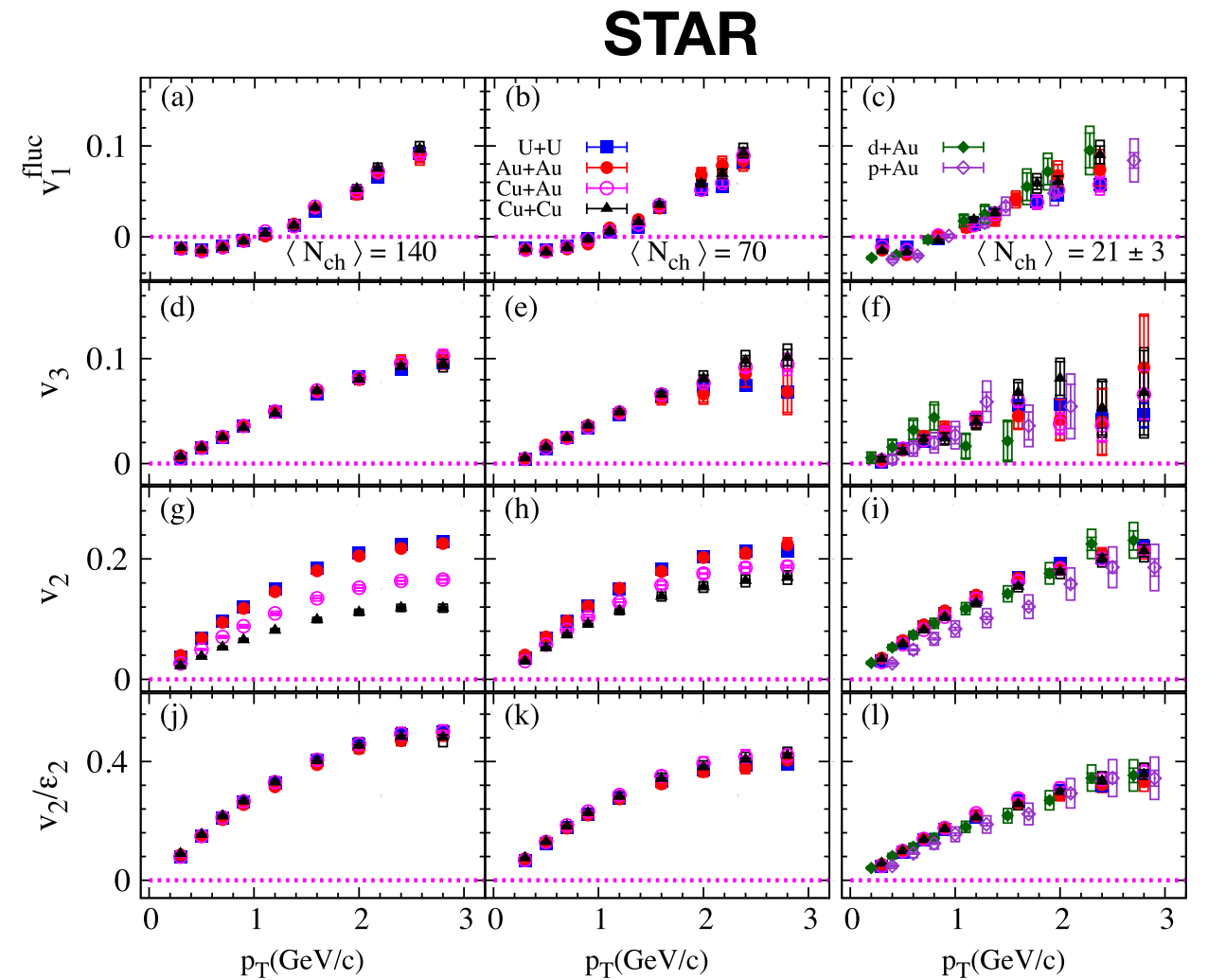
Aidala C, et al. *Phys. Rev. C* 95:034910 (2017)



# Collective flow in small/large system from experiments



Aad G, et al. *Phys. Rev. C* 90:044906 (2014)

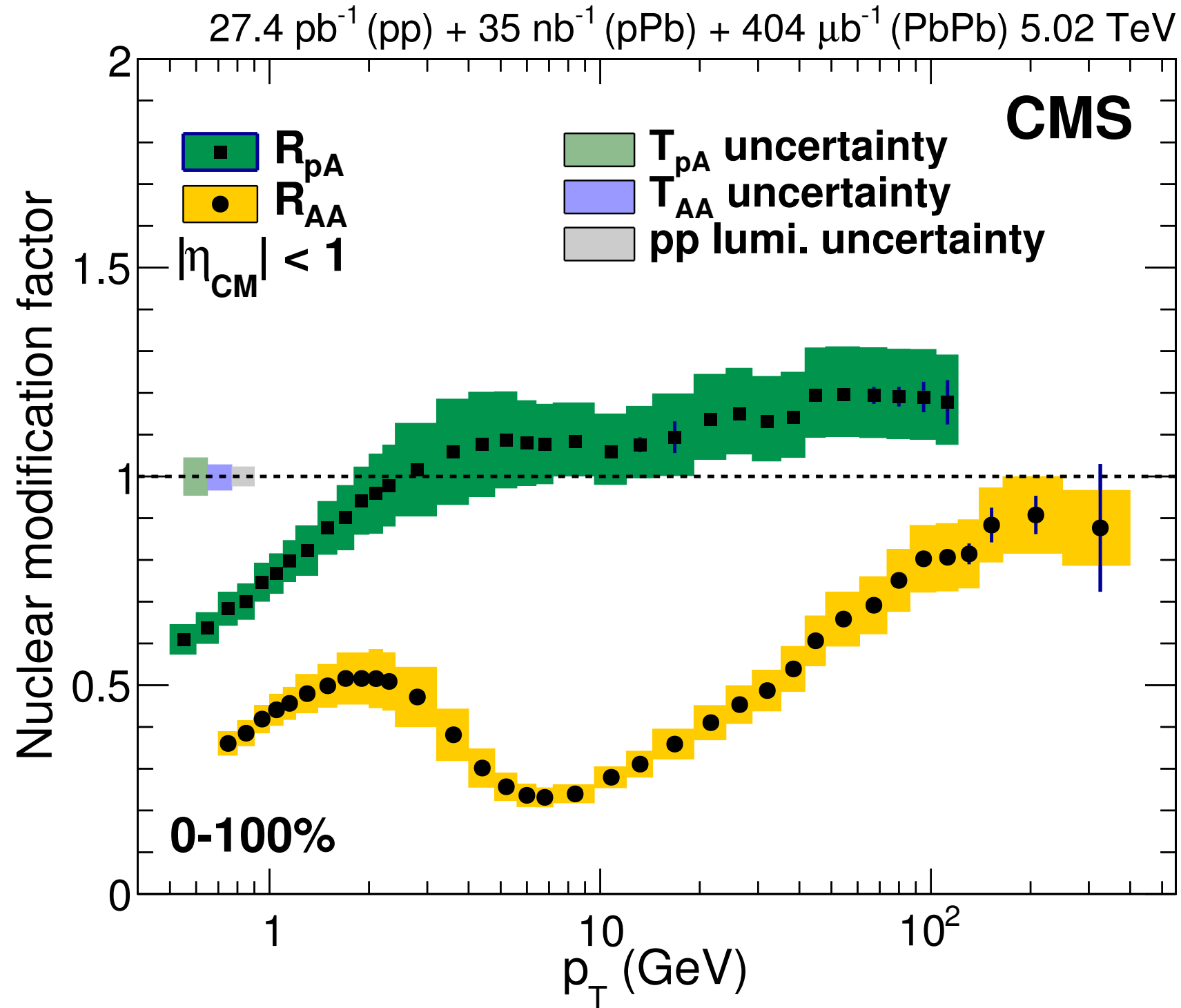


J. Adam, et al. STAR, *Phys. Rev. Lett.* 122, 172301 (2019)





# Jet “quenching” in small system

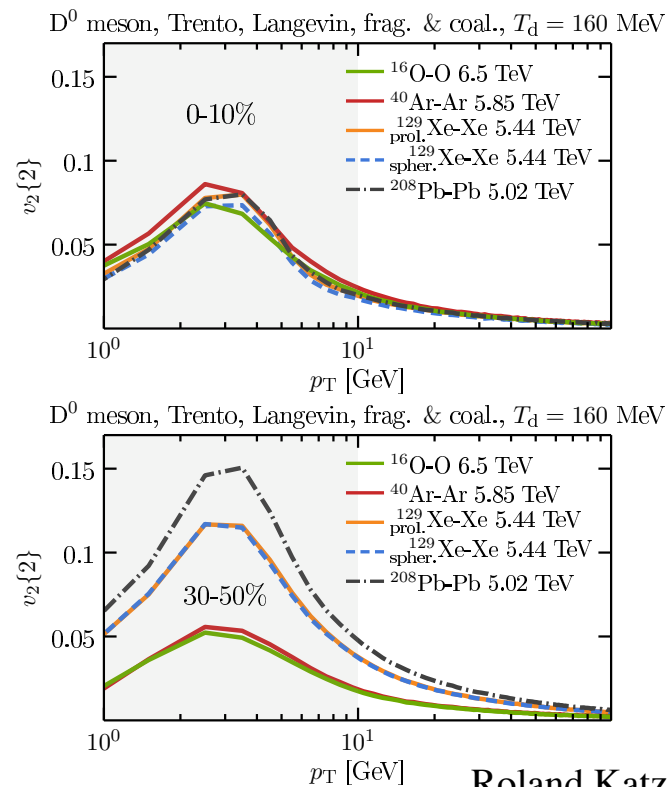
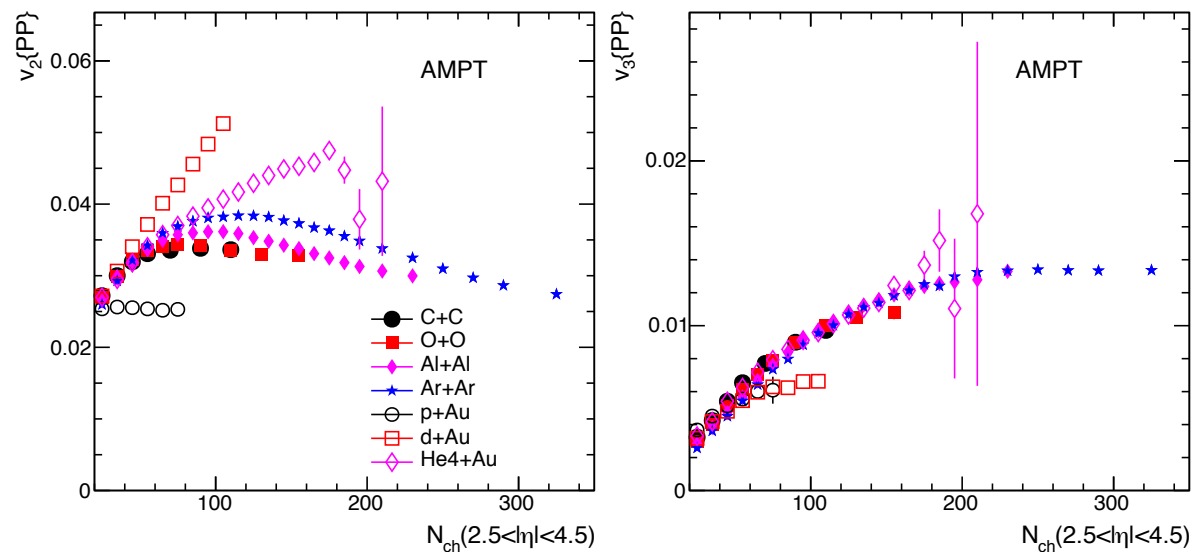


Khachatryan V, et al. *J. High Energy Phys.* 04:039 (2017)

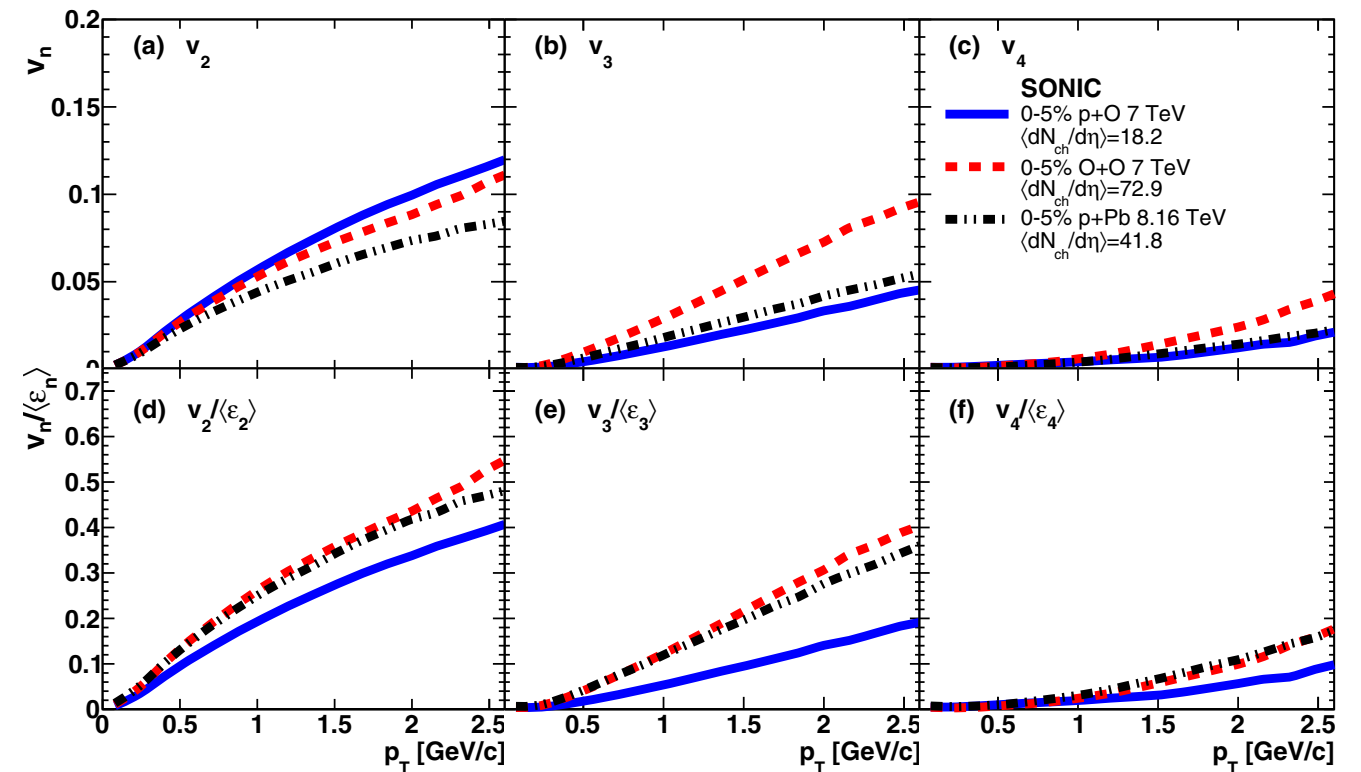
# Some recent theoretical works on collective flow in small system

Shengli Huang, et al., arXiv:1904.10415v1

S. H. Lim, et al., Phys. Rev. C **99**, 044904 (2019)



Roland Katz, et al., arXiv:1907.03308v1



Recently some theoretical works propose the system scan in experiments AMPT, SONIC, Hydro. RIHC & LHC

FIG. 3.  $D^0$  meson  $v_2\{2\}$  for PbPb, XeXe with spherical and prolate initial nuclei, ArAr, and OO collisions at the LHC top energies in 0–10% (top) and 30–50% (bottom) centrality classes.



# AMPT model and $\alpha$ -cluster nuclei effect

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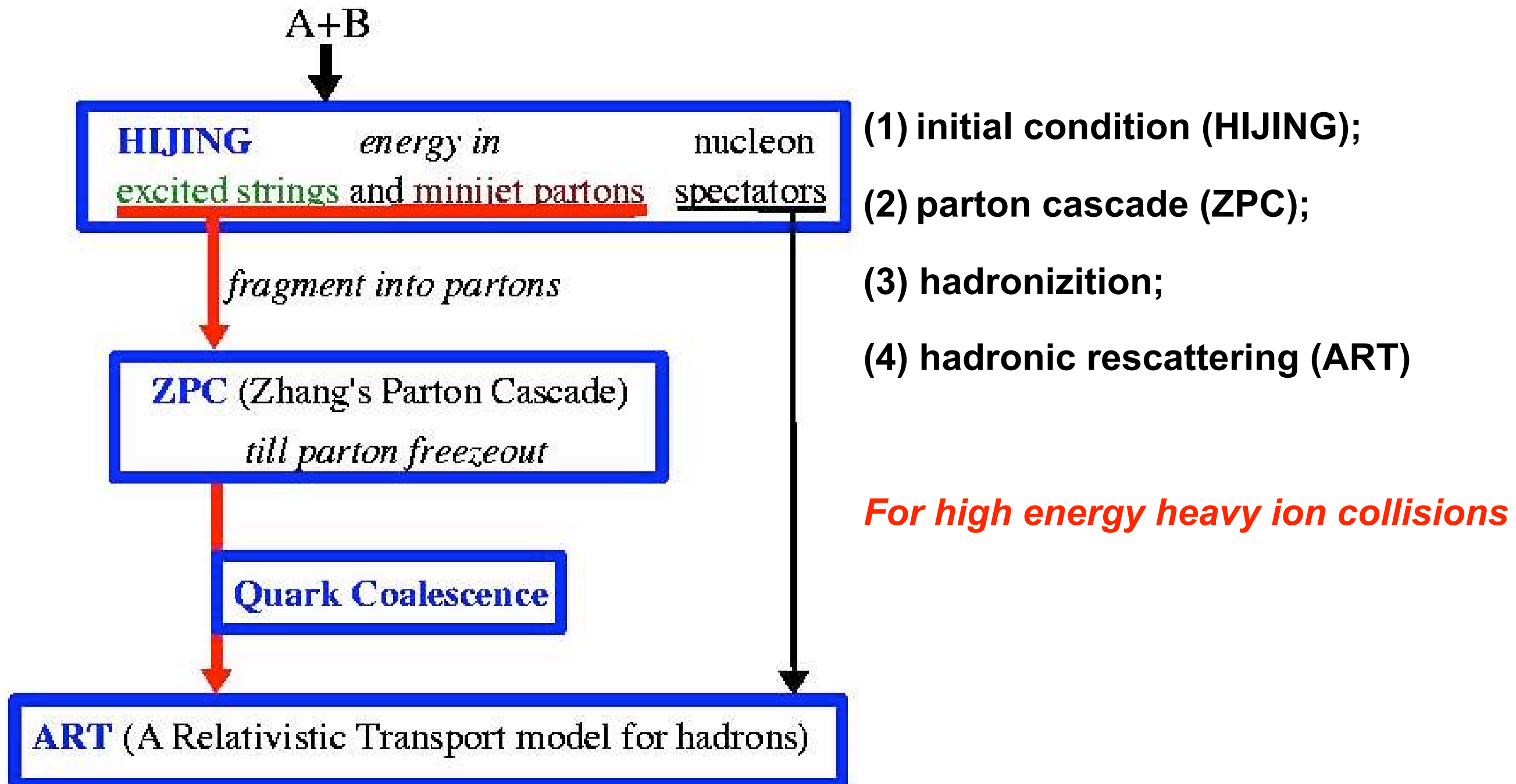
- AMPT
- $\alpha$ -cluster nuclei effect on collective flow
- $\alpha$ -cluster nuclei effect on electromagnetic field
- $\alpha$ -cluster nuclei effect on HBT correlations



# AMPT

AMPT (a multi-phase transport model), Z. W. Lin, C. M. Ko, B. A. Li, S. Pal, PRC-72-064901(2005)

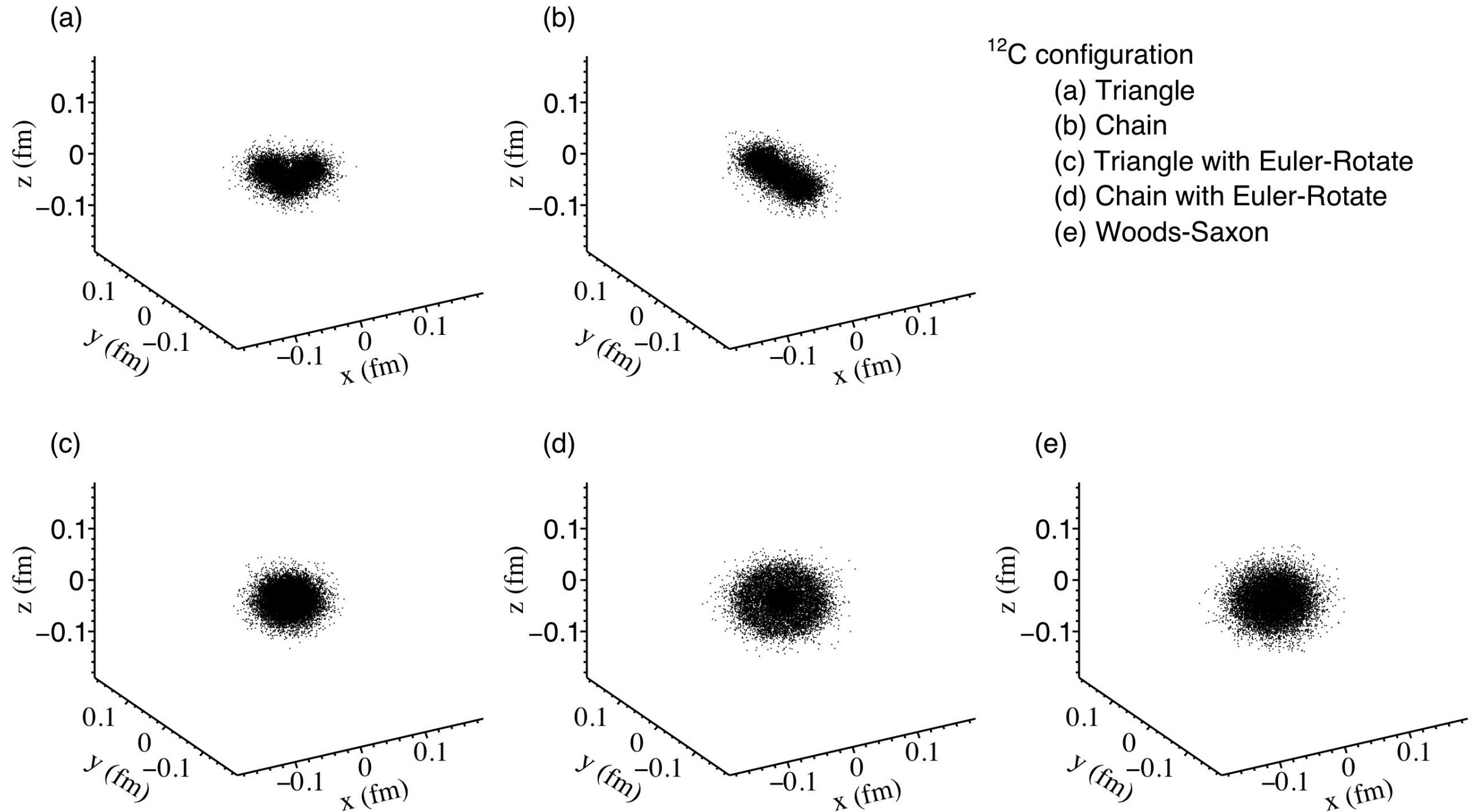
## *Structure of AMPT model with string melting*



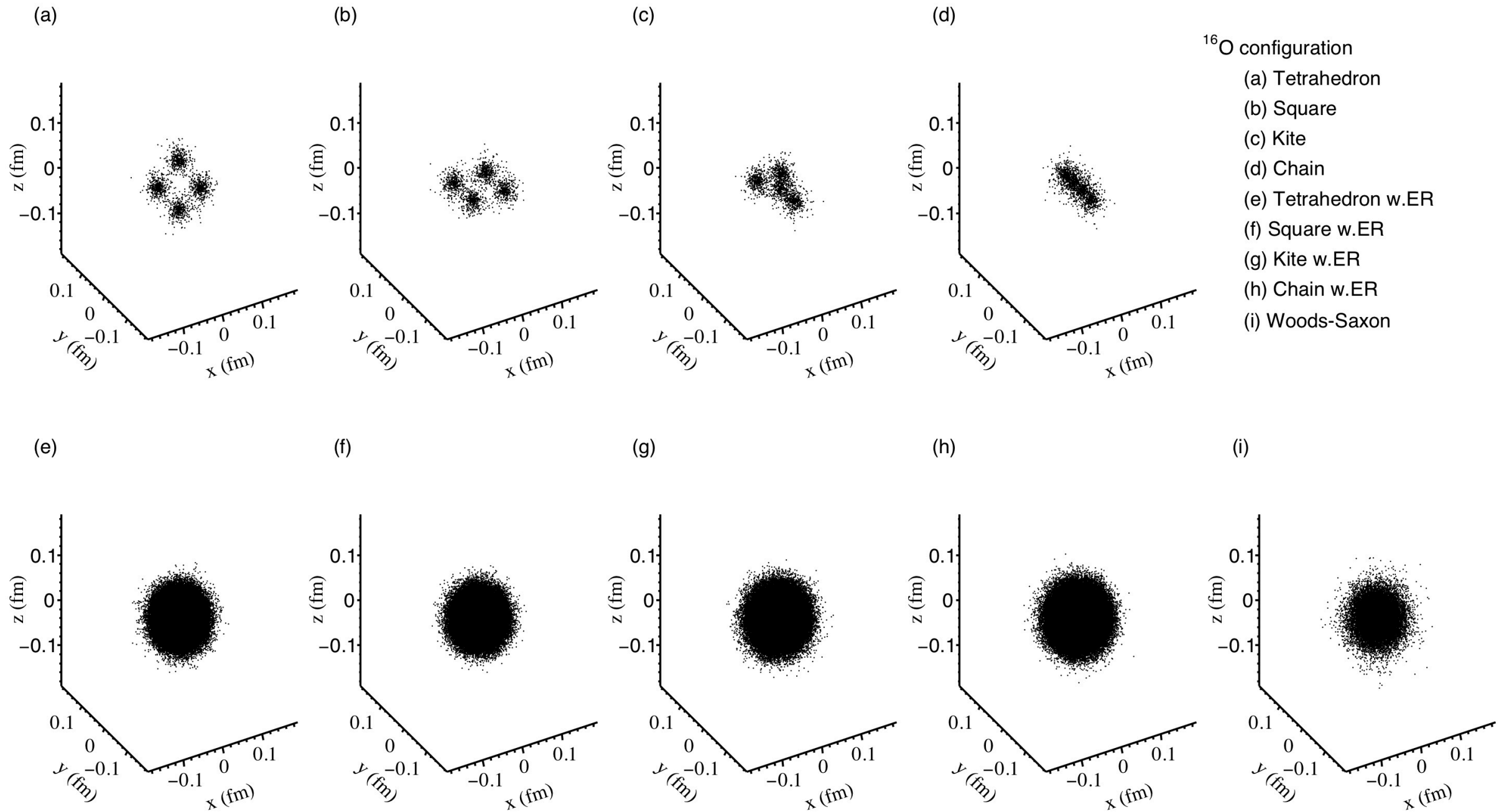




# Initial nucleon distribution ( $^{12}\text{C}$ )

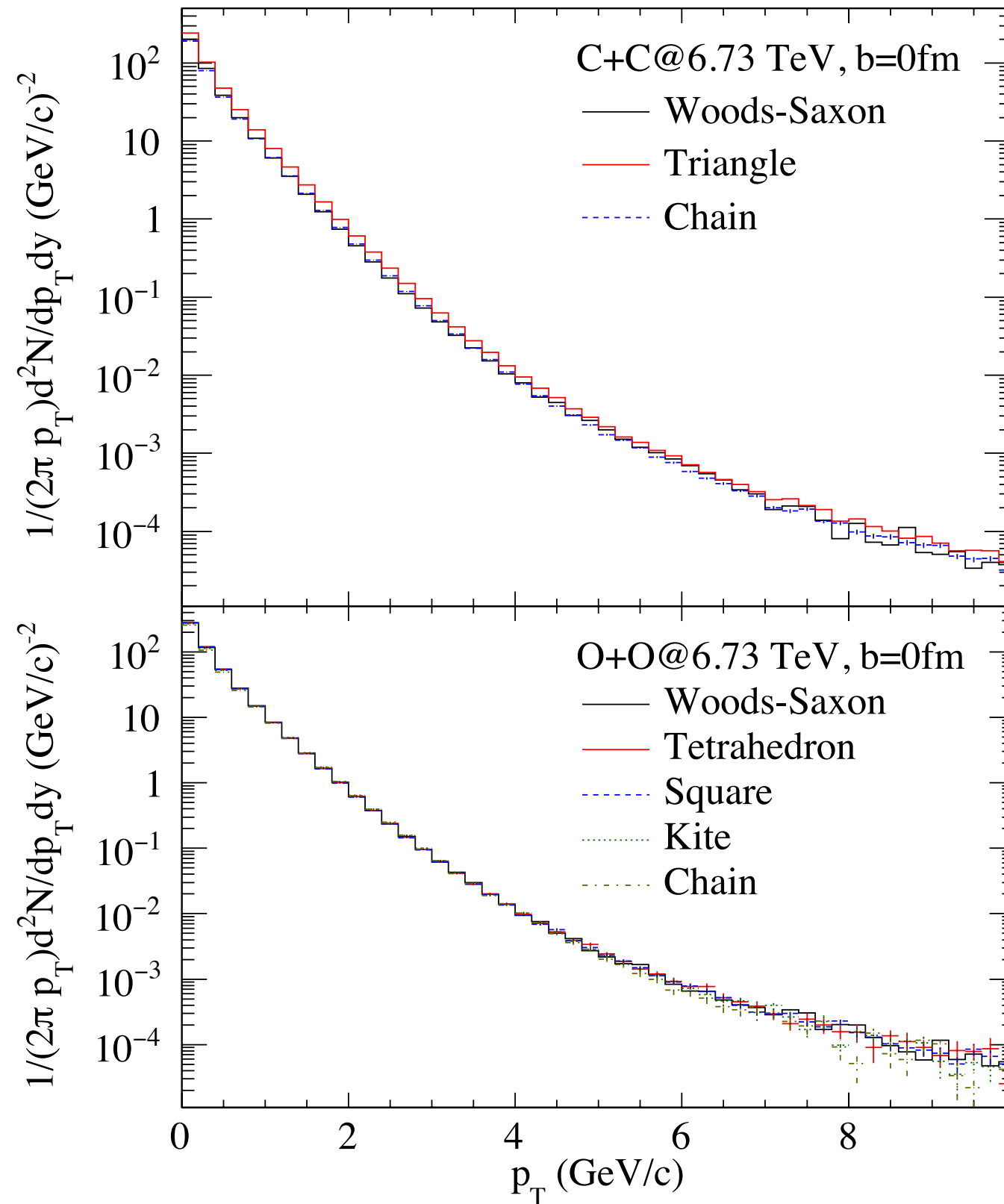


# Initial nucleon distribution ( $^{16}\text{O}$ )





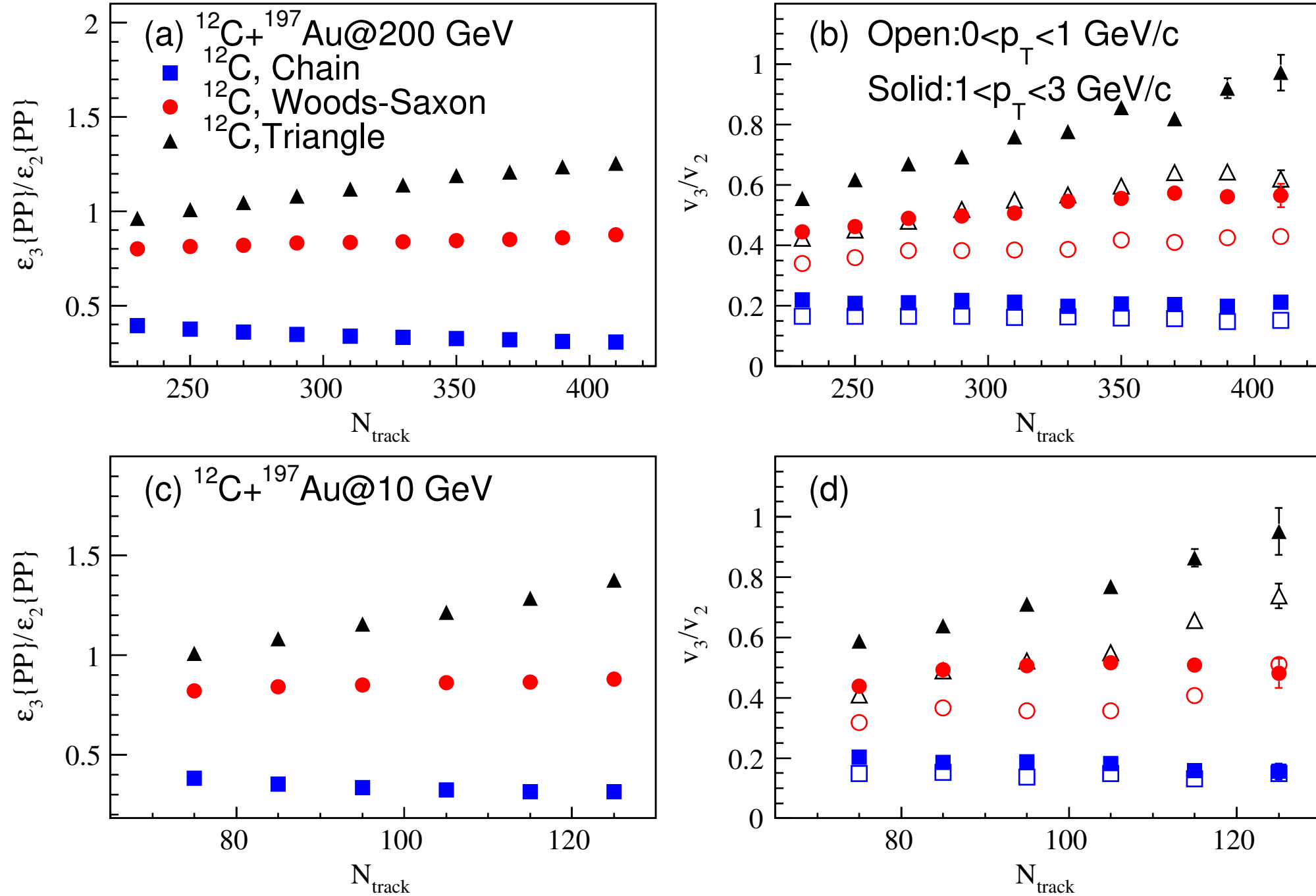
# Transvers momentum spectra





# $\alpha$ -cluster nuclei effect on collective flow

S. Zhang, Y. G. Ma, et al., Phys. Rev. C 95, 064904 (2017); S. Zhang, Y.G. Ma et al., Eur. Phys. J. A (2018) 54



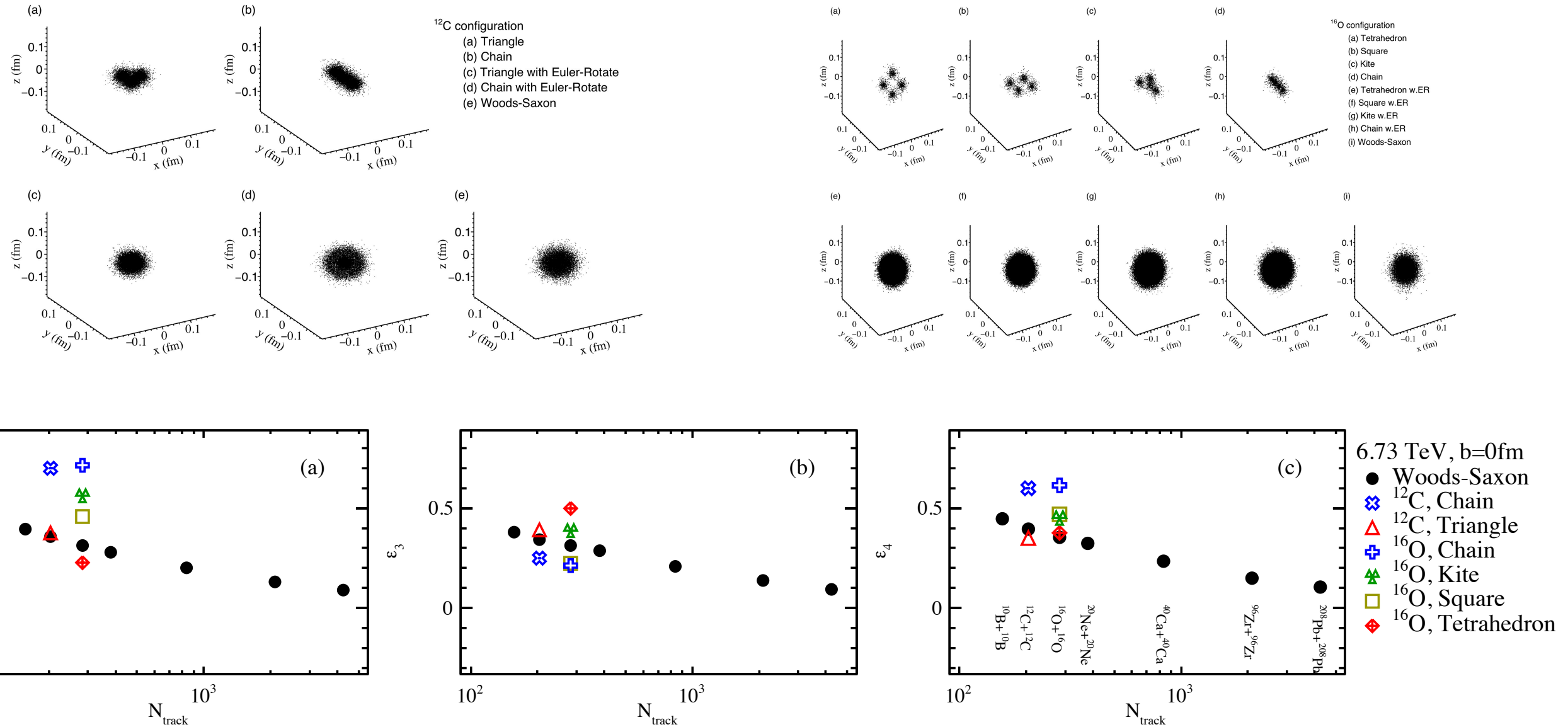
- ✓ The ratio keep flat tend with increasing of  $N_{\text{track}}$  for Woods-Saxon distribution and chain structure of  $^{12}\text{C}$
- ✓ The ratio increases with increasing of  $N_{\text{track}}$  for triangle structure.





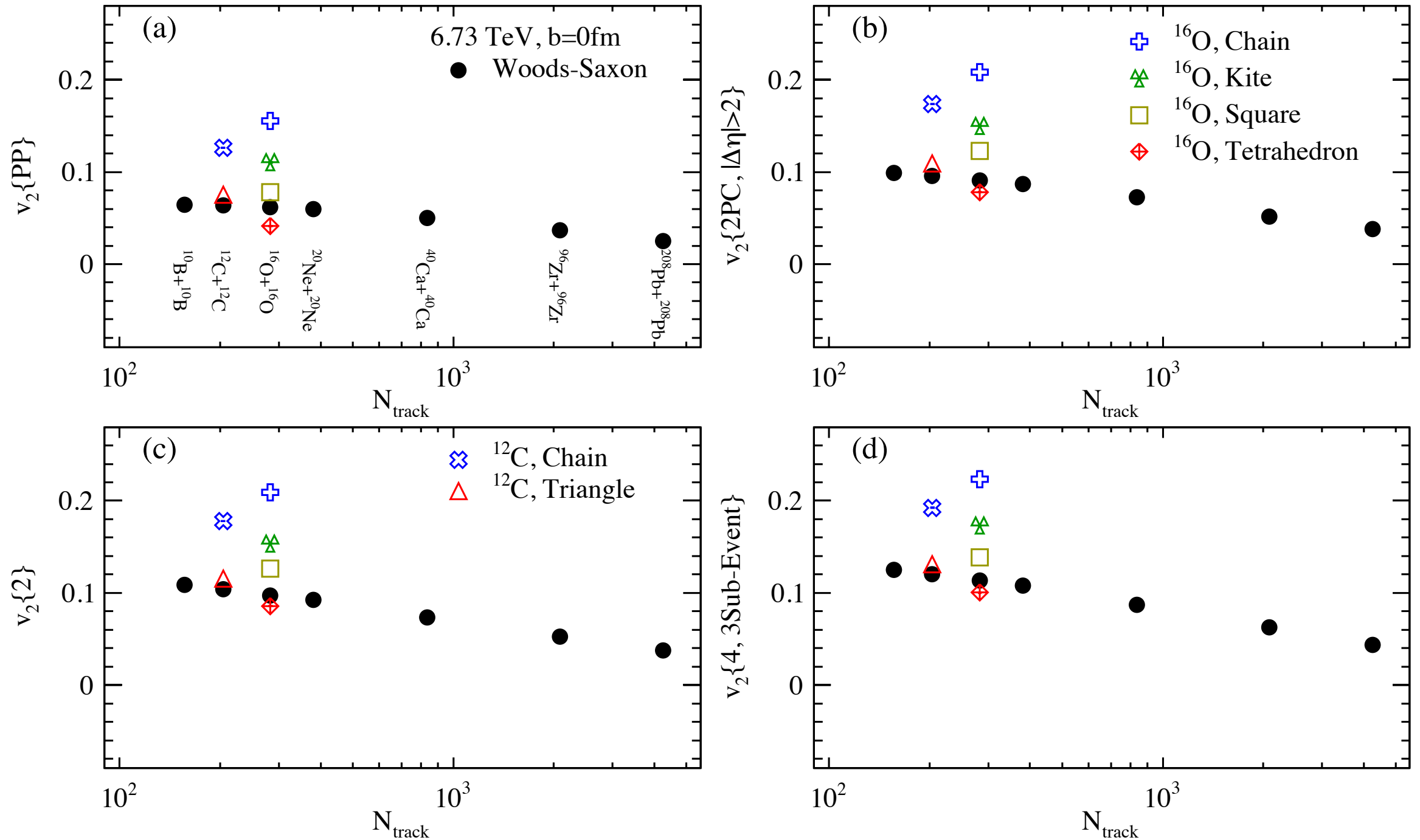
# System scan of collective flow and $\alpha$ -cluster nuclei effect

# Eccentricity coefficients



- ✓ Sensitive to fluctuation
- ✓ Also sensitive to intrinsic geometry (α-cluster structure)

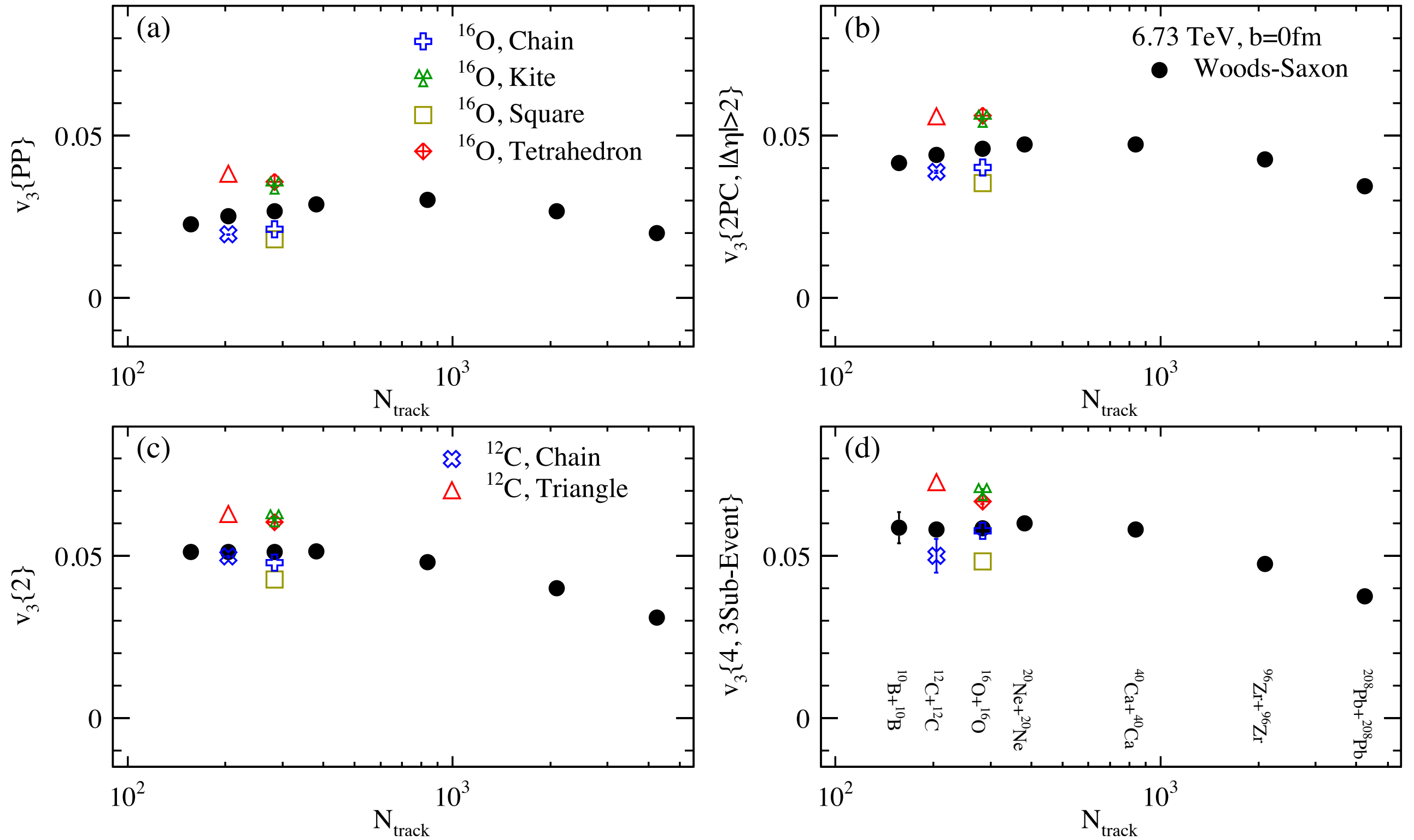
# Elliptic flow



- ✓ Smoothly decrease with increasing size of collision system (most central, Woods-Saxon distribution)
- ✓ Deviation from Woods-Saxon case for  $\alpha$ -clustered initial system

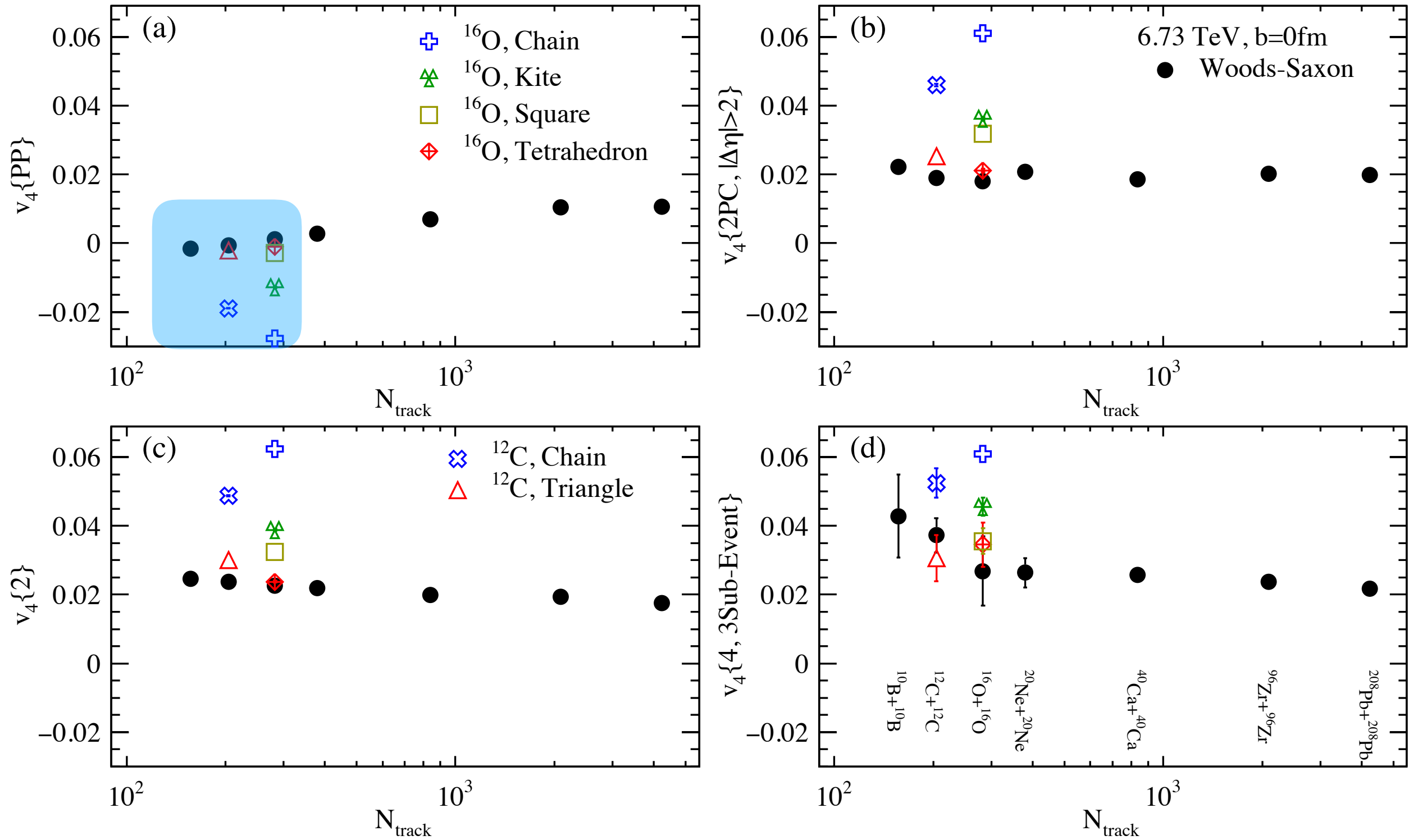


# Triangular flow





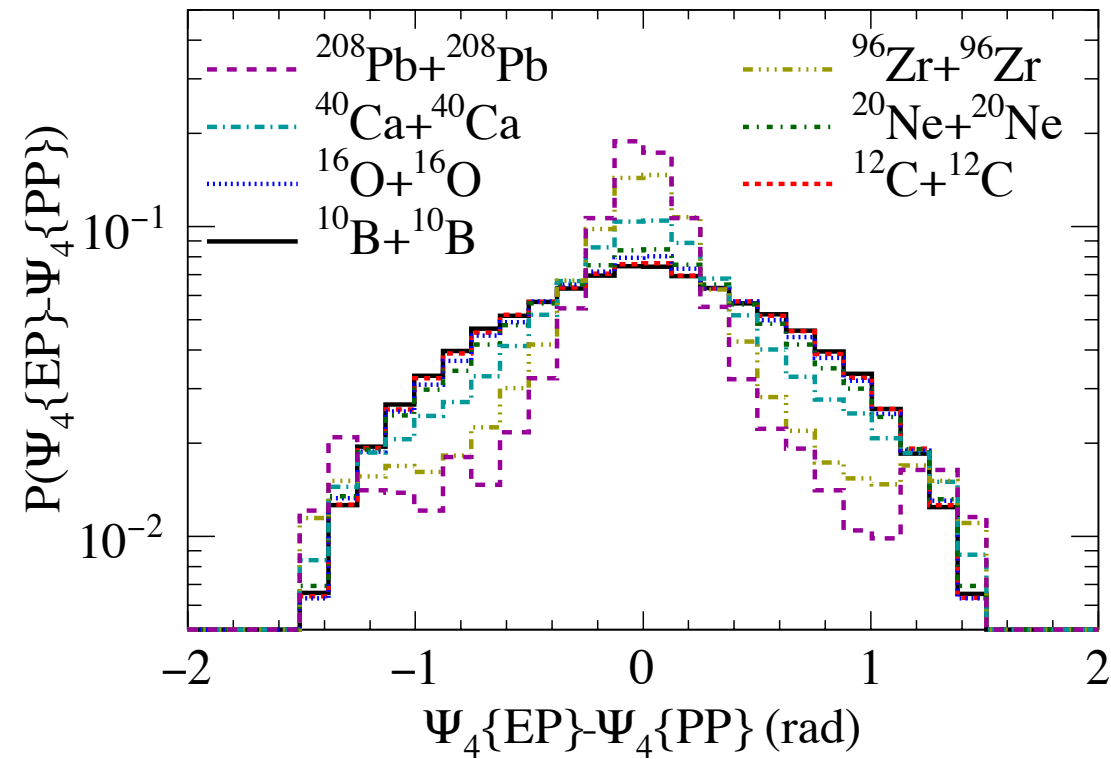
# Quadrangular flow







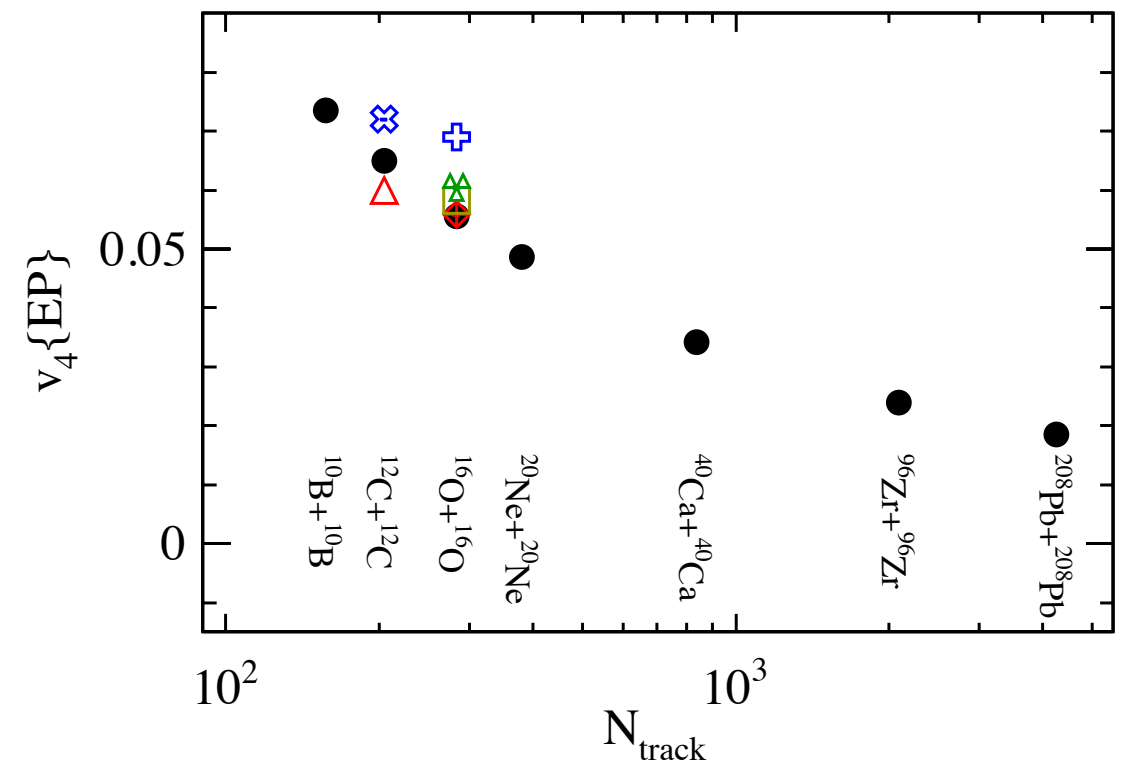
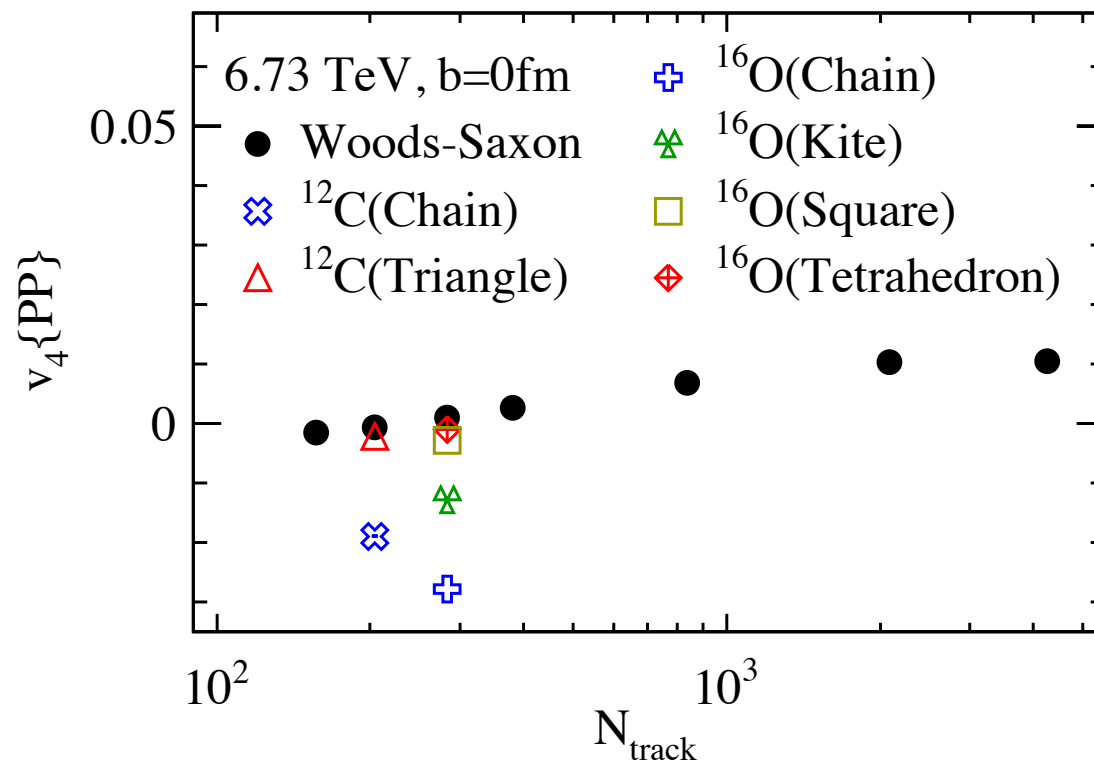
# Quadragonal flow via EP- and PP-plane



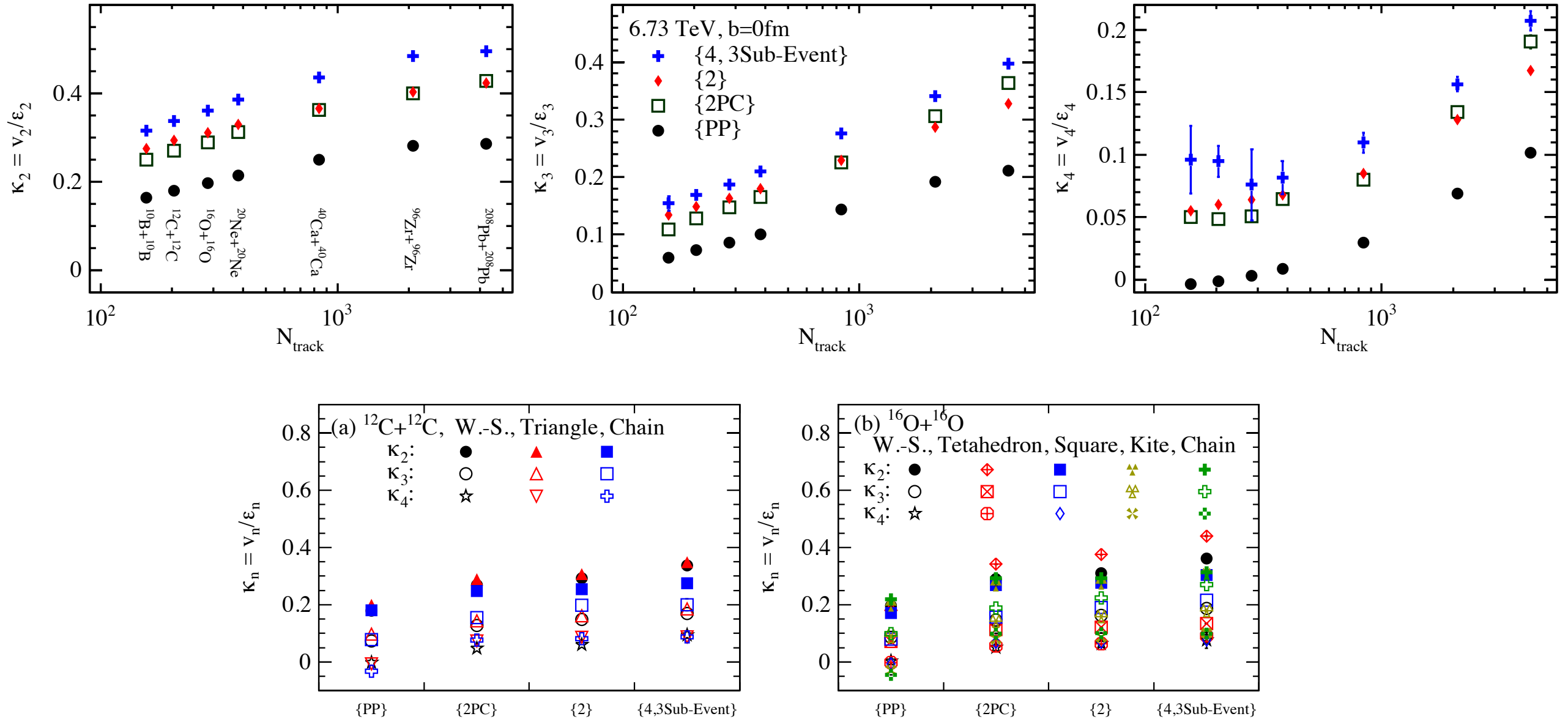
- ✓ EP-method and PP-method give different system dependence of  $v_4$
- ✓  $\Psi_4\{EP\}$  gradually approach  $\Psi_4\{PP\}$  from small system to large one

$$\Psi_n\{PP\} = \frac{\text{atan2} \left( \left\langle r^2 \sin(n\phi_{part}) \right\rangle, \left\langle r^2 \cos(n\phi_{part}) \right\rangle \right) + \pi}{n}$$

$$\Psi_n\{EP\} = \frac{1}{n} \tan^{-1} \left( \frac{Q_y}{Q_x} \right)$$



# Ratio of flow to eccentricity



- ✓  $\kappa_n$  increasing with the increasing of system size (most central collisions)
- ✓ Same A+A collisions with different initial structure configuration, the similar  $\kappa_n$

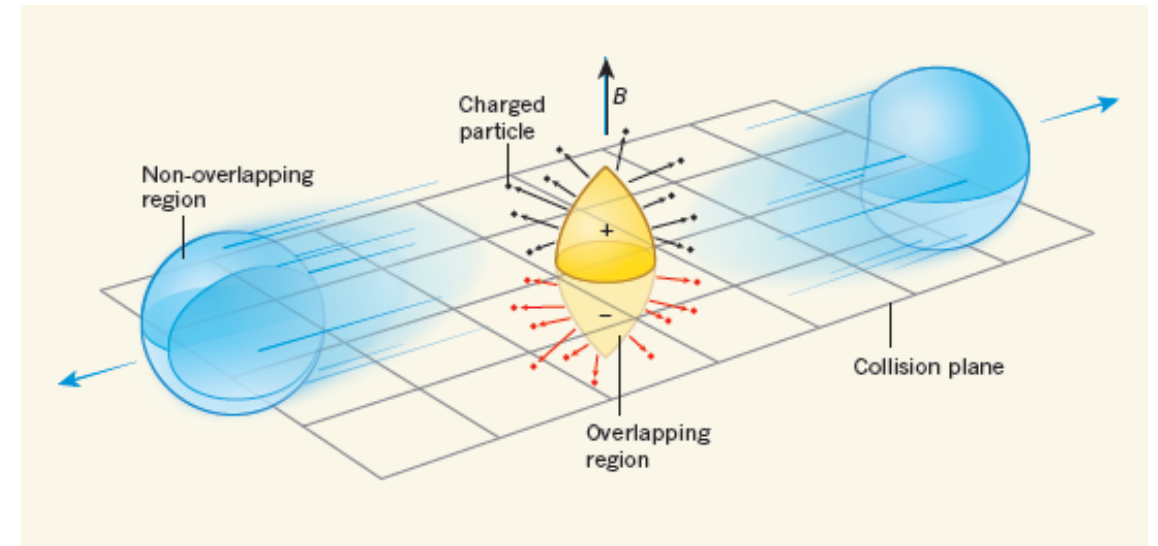
# System dependence and of electromagnetic fields and $\alpha$ -cluster nuclei effect (I)

## Li'enard-Wiechert potentials

Huang,(PRC) 85, 044907 (2012)

$$e\vec{E}(\vec{r}_i, t) = \frac{e^2}{4\pi} \sum_n Z_n \frac{1 - v_n^2}{(R_n - \vec{R}_n \cdot \vec{v}_n)^3} (\vec{R}_n - R_n \vec{v}_n)$$

$$e\vec{B}(\vec{r}_i, t) = \frac{e^2}{4\pi} \sum_n Z_n \frac{1 - v_n^2}{(R_n - \vec{R}_n \cdot \vec{v}_n)^3} \vec{v}_n \times \vec{R}_n$$



$Z_n$  : coordinate position

$R_n = r - r_n$  :  $r$  is the position of source point

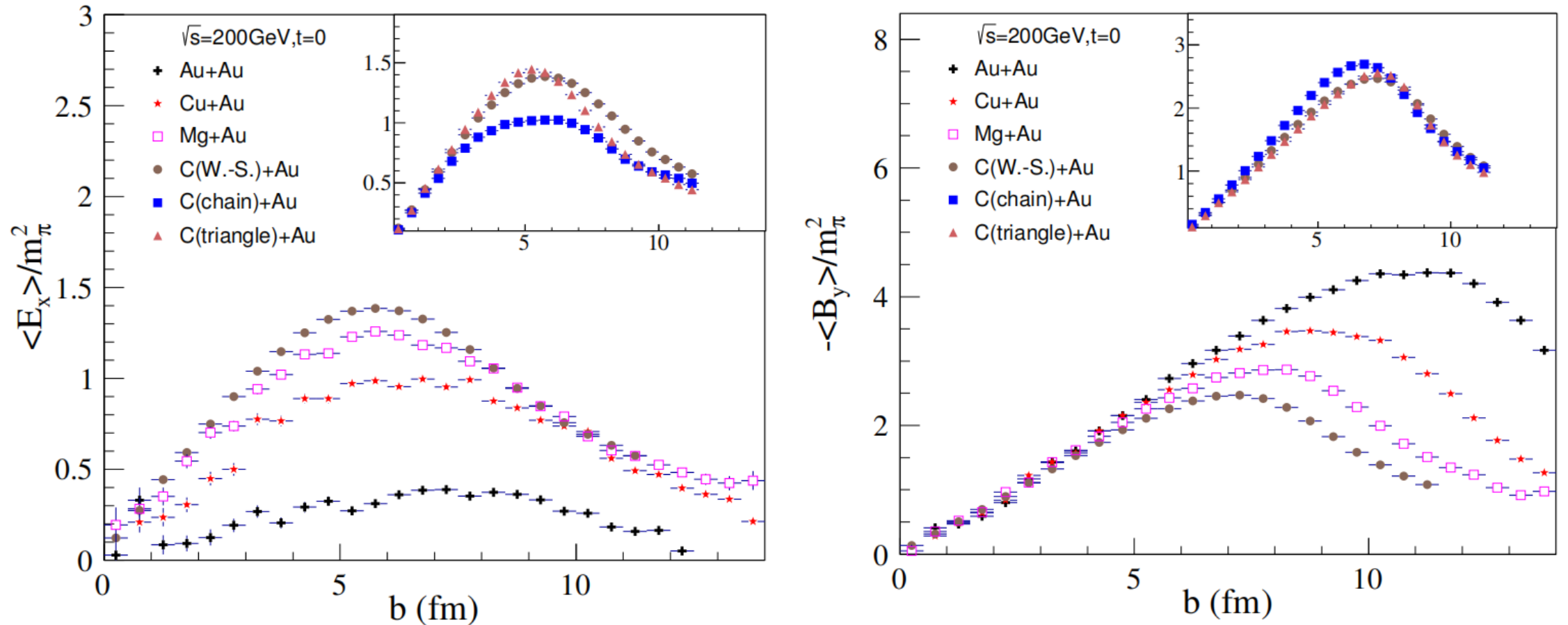
$r_n$  is the position of the  $n$ -th particle at the retarded time  $t_n = t - |\mathbf{r} - \mathbf{r}_n|$  and  $t_n < t$

$$v_x = v_y = 0, v_z^2 = 1 - (2m_N/\sqrt{s})^2 \quad (\text{the Lorentz contraction is considered})$$



# System dependence and of electromagnetic fields and $\alpha$ -cluster nuclei effect (II)

Y. L. Cheng (程艺林), S. Zhang, Y. G. Ma, et al., Phys. Rev. C 99, 054906 (2019)



- ✓  $\langle E_x \rangle$ : the asymmetric projectile and target nuclear collisions produce stronger electric field than symmetrical collision system
- ✓  $-\langle B_y \rangle$ : the magnetic field will be in the reverse trend
- ✓  $\alpha$ -cluster effect at semi-central collisions for chain structure



# HBT correlation and $\alpha$ -cluster nuclei effect (I)

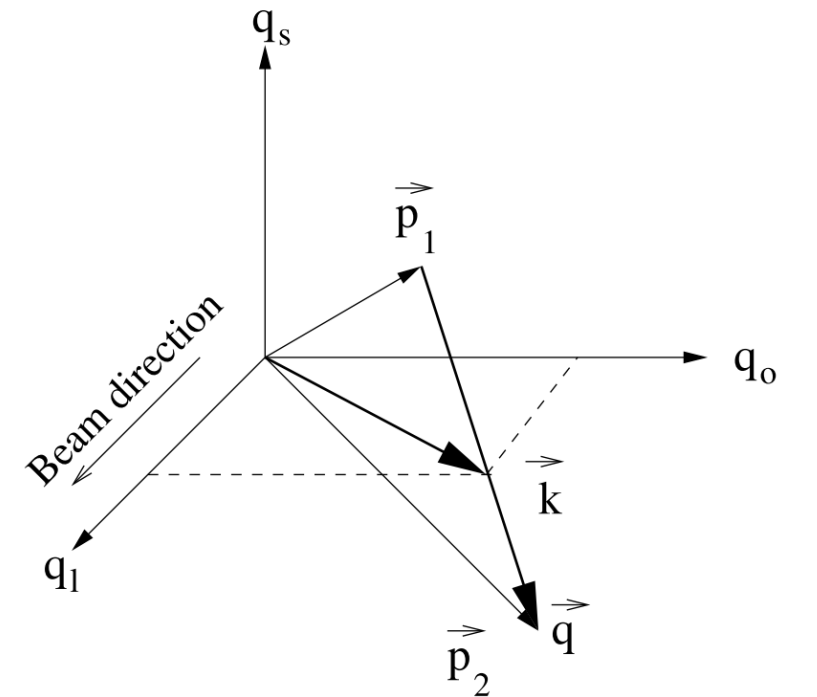
$$C(\vec{q}, \vec{K}) = \frac{\int d^4x_1 d^4x_2 S(x_1, p_1) S(x_2, p_2) |\phi(\vec{q}', \vec{r}')|^2}{\int d^4x_1 S(x_1, p_1) \int d^4x_2 S(x_2, p_2)} \quad (1)$$

$$C(\vec{q}, \vec{K}) = 1 \pm \left| \frac{\int d^4x e^{i\vec{q} \cdot (\vec{x} - \vec{\beta}t)} S(x, K)}{\int d^4x S(x, K)} \right|^2 \quad (2)$$

$$C(\vec{q}, \vec{K}) = 1 \pm e^{-\sum_{i,j=o,s,l} R_{ij}^2(\vec{K}) q_i q_j} \quad (3)$$

$$R_s^2(K_T, \Phi, Y) = \langle (y \cos \Phi - x \sin \Phi)^2 \rangle - \langle y \cos \Phi - x \sin \Phi \rangle^2 \quad (4)$$

$$R_o^2(K_T, \Phi, Y) = \langle (x \cos \Phi + y \sin \Phi - \beta_{\perp} t)^2 \rangle - \langle x \cos \Phi + y \sin \Phi - \beta_{\perp} t \rangle^2 \quad (5)$$



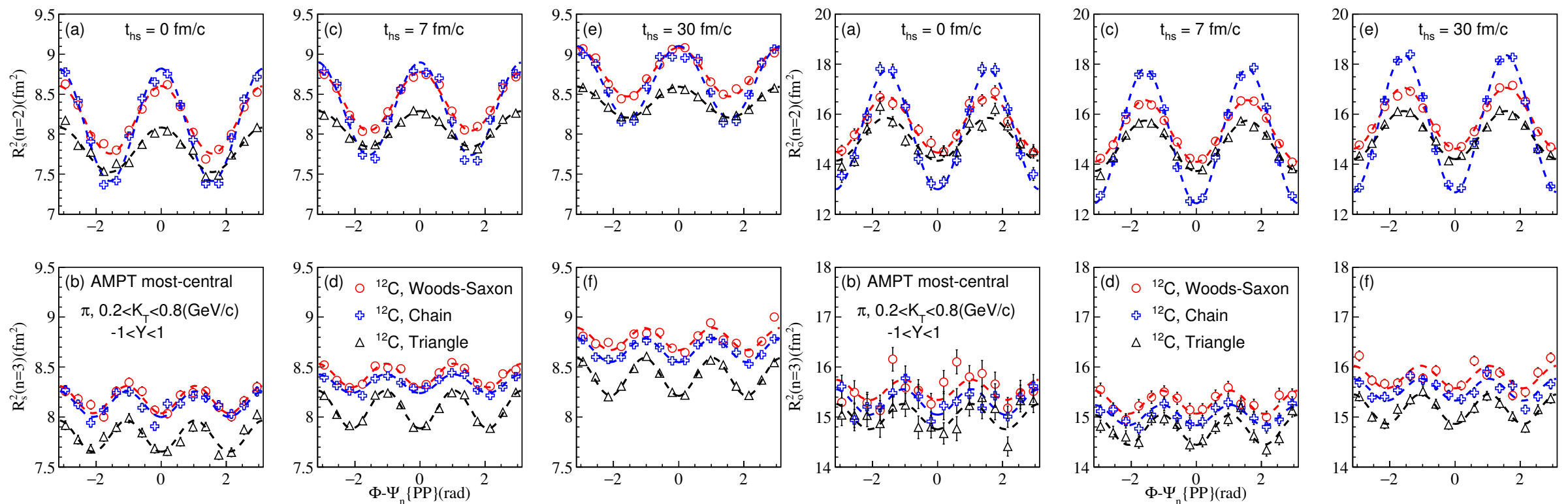




# HBT correlation and $\alpha$ -cluster nuclei effect (II)

✓Small HBT-radius in collisions with triangle nuclei structure

✓Significant participant plane dependence



Junjie He (何俊杰)

$$R_s^2(\Phi - \Psi_n) = a_{s,0} + a_{s,n} \cos[n(\Phi - \Psi_n)],$$

$$R_o^2(\Phi - \Psi_n) = a_{o,0} + a_{o,n} \cos[n(\Phi - \Psi_n)], n = 2, 3$$

(14)



# Summary

---

- Collective flow change smoothly with system size in most central collisions, Woods-Saxon distribution of nucleon
- $\alpha$ -cluster effect significant with the baseline from Woods-Saxon distribution
- Symmetry and asymmetry collision system result in different electromagnetic field effect
- HBT-radius sensitive to the  $\alpha$ -cluster effect
- Proposal of system scan experiments, experimentally illustrate how initial geometrical asymmetry transfer to momentum space

**Thank you for your attention!**





# Collective flow with respect to participant plane

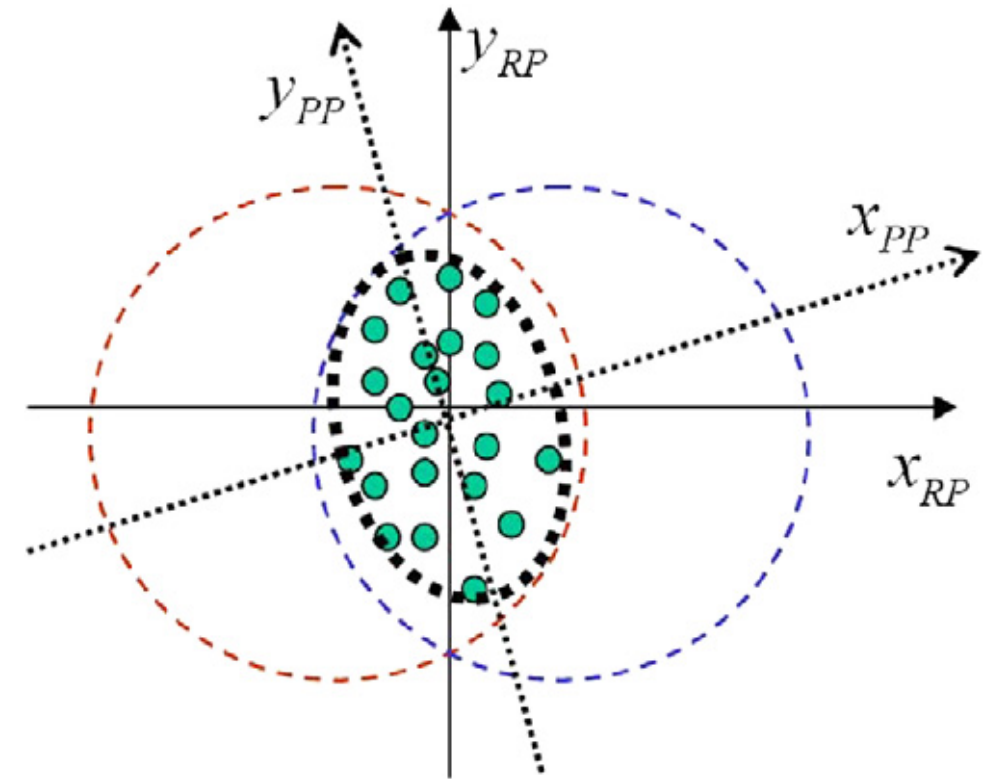
$$E \frac{d^3 N}{d^3 p} = \frac{1}{2\pi} \frac{d^2 N}{p_T dp_T dy} \left( 1 + \sum_{n=1}^{\infty} 2v_n \cos[n(\phi - \Psi_r)] \right)$$

$$v_n = \langle \cos[n(\phi - \Psi_r)] \rangle$$

$$\Psi_n\{PP\} = \frac{\text{atan2} \left( \langle r^2 \sin(n\phi_{Part}) \rangle, \langle r^2 \cos(n\phi_{Part}) \rangle \right) + \pi}{n}$$

$$v_n\{PP\} \equiv \langle \cos(n[\phi - \Psi_n\{PP\}]) \rangle$$

$$\epsilon_n\{PP\} \equiv \frac{\sqrt{\langle r^2 \cos(n\phi_{Part}) \rangle^2 + \langle r^2 \sin(n\phi_{Part}) \rangle^2}}{\langle r^2 \rangle}$$



*S.A. Voloshin et al. / Physics Letters B 659 (2008) 537–541*

*B. Alver, G. Roland, Phys. Rev. C 81 (2010) 054905*

*R. A. Lacey, R. Wei, J. Jia, et al., Phys. Rev. C 83 (2011) 044902*

*L. Ma, G. L. Ma, Y. G. Ma, Phys. Rev. C 94 (2016) 044915*

Hydrodynamical calculation suggested how the initial geometry distribution (fluctuation) transforms into final collective flow

$$v_n \approx \kappa_n \epsilon_n$$

*H. C. Song, Y. Zhou, and K. Gajdošová, Nucl. Sci. Tech. 28, 99 (2017)*

*F. G. Gardim, F. Grassi, M. Luzum, and J.-Y. Ollitrault, Phys. Rev. C 85, 024908 (2012).*

*H. Niemi, G. S. Denicol, H. Holopainen, and P. Huovinen, Phys. Rev. C 87, 054901 (2013)*



# Collective flow with respect to event plane

$$Q_x \equiv \sum_i^M \omega_i \cos(n\phi_i)$$

*A. M. Poskanzer, S. A. Voloshin, Phys. Rev. C 58 (1998) 1671*

*S. Afanasiev, , et al., Phys. Rev. C 80 (2009) 024909*

*L. Adamczyk, , et al., Phys. Rev. C 88 (2013) 014904*

$$Q_y \equiv \sum_i^M \omega_i \sin(n\phi_i)$$

$$\Psi_n\{EP\} = \frac{1}{n} \tan^{-1} \left( \frac{Q_y}{Q_x} \right)$$

$$v_n\{EP\} = \frac{v_n^{obs}}{\text{Res}\{\Psi_n\{EP\}\}},$$

$$v_n^{obs} = \langle \cos(km(\phi - \Psi_n\{EP\})) \rangle,$$

$$\text{Res}\{\Psi_n\{EP\}\} = \langle \cos(km(\Psi_n\{EP\} - \Psi_{RP})) \rangle$$





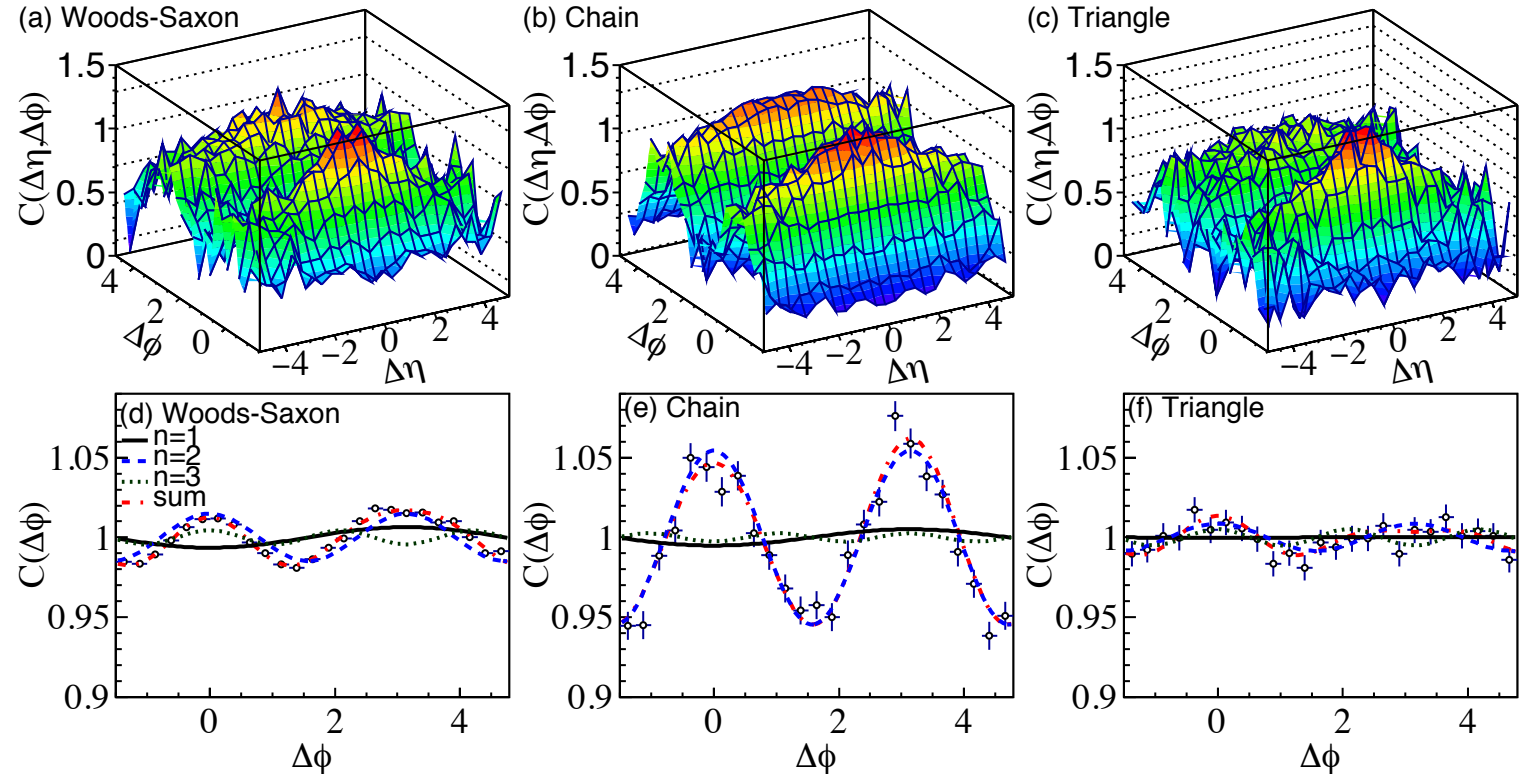
# Collective flow via 2-particle correlation

$$C(\Delta\phi, \Delta\eta) = \frac{S(\Delta\phi, \Delta\eta)}{B(\Delta\phi, \Delta\eta)}$$

$$S(\Delta\phi, \Delta\eta) = \frac{dN}{d\Delta\phi d\Delta\eta},$$

$$B(\Delta\phi, \Delta\eta) = \frac{dN}{d\Delta\phi d\Delta\eta}$$

$$C(\Delta\phi)_{2<|\Delta\eta|<5} = A \frac{\int S(\Delta\phi, \Delta\eta) d\Delta\eta}{\int B(\Delta\phi, \Delta\eta) d\Delta\eta}$$



$$\frac{dN_{pairs}}{d\Delta\phi} \propto 1 + 2 \sum_{n=1}^{\infty} v_{n,n} (p_T^a, p_T^b) \cos(n\Delta\phi)$$

$$v_{n,n} = \langle \cos(n\Delta\phi) \rangle = \frac{\sum_{m=1}^N \cos(n\Delta\phi_m) C(\Delta\phi_m)}{\sum_{m=1}^N C(\Delta\phi)}$$

$$v_n = v_{n,n} / \sqrt{|v_{n,n}|}$$

G. Aad, , et al., Phys. Rev. C 86 (2012) 014907

S. Chatrchyan, , et al., Eur. Phys. J C 72 (5) (2012)

S. Chatrchyan, , et al., Phys. Lett. B 724 (4) (2013) 213

A. Bzdak, G.-L. Ma, Phys. Rev. Lett. 113 (2014) 252301

V. Khachatryan, , et al., Phys. Lett. B 765 (2017) 193



# Collective flow via Q-cumulant (I)

$$Q_n = \sum_{i=1}^M e^{in\phi_i}$$

$$\langle 2 \rangle = \langle e^{in(\phi_1 - \phi_2)} \rangle = \frac{|Q_n|^2 - M}{M(M-1)},$$

$$\begin{aligned} \langle 4 \rangle &= \langle e^{in(\phi_1 + \phi_2 - \phi_3 - \phi_4)} \rangle \\ &= \{ |Q_n|^4 + |Q_{2n}|^2 - 2\text{Re}[Q_{2n}Q_n^*Q_n^*] \\ &\quad - 2[2(M-2)|Q_{2n}|^2 - M(M-3)] \} \\ &\quad / [M(M-1)(M-2)(M-3)]. \end{aligned}$$

$$\langle\langle 2 \rangle\rangle = \langle\langle e^{in(\phi_1 - \phi_2)} \rangle\rangle = \frac{\sum_{event} (W_{\langle 2 \rangle})_i \langle 2 \rangle_i}{\sum_{event} (W_{\langle 2 \rangle})_i},$$

$$\langle\langle 4 \rangle\rangle = \langle\langle e^{in(\phi_1 + \phi_2 - \phi_3 - \phi_4)} \rangle\rangle = \frac{\sum_{event} (W_{\langle 4 \rangle})_i \langle 4 \rangle_i}{\sum_{event} (W_{\langle 4 \rangle})_i}$$

$$c_n\{2\} = \langle\langle 2 \rangle\rangle,$$

$$c_n\{4\} = \langle\langle 4 \rangle\rangle - 2 \times \langle\langle 2 \rangle\rangle^2,$$

$$v_n\{2\} = \sqrt{c_n\{2\}},$$

$$v_n\{4\} = \sqrt[4]{-c_n\{4\}}$$

A. Bilandzic, R. Snellings, S. Voloshin, *Phys. Rev. C* 83 (2011) 044913

B. L. Adamczyk, et al., *Phys. Rev. C* 86 (2012) 054908



# Collective flow via Q-cumulant (II)

particles selected for flow calculation labeled as reference flow particle (RFP), particle of interest (POI)

$$p_n \equiv \sum_{i=1}^{m_p} e^{in\phi_i}$$

$$q_n \equiv \sum_{i=1}^{m_q} e^{in\phi_i}$$

$m_p$  total number of POIs and

$m_q$  total number for POIs labeled also as RFP

$$\langle 2' \rangle = \frac{p_n Q_n^* - m_q}{m_p M - m_q}$$

$$\begin{aligned} \langle 4' \rangle = & [p_n Q_n Q_n^* Q_n^* - q_{2n} Q_n^* Q_n^* - p_n Q_n Q_{2n}^* \\ & - 2M p_n Q_n^* - 2m_q |Q_n|^2 + 7q_n Q_n^* \\ & - Q_n q_n^* + q_{2n} Q_{2n}^* + 2p_n Q_n^* + 2m_q M \\ & - 6m_q] / [(m_p M - 2m_q)((M-1)(M-2))] . \end{aligned}$$

$$\langle \langle 2' \rangle \rangle = \frac{\sum_{i=1}^N (\omega_{\langle 2' \rangle})_i \langle 2' \rangle}{\sum_{i=1}^N (\omega_{\langle 2' \rangle})_i}$$

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$$\omega_{\langle 2' \rangle} \equiv m_p M - m_q$$

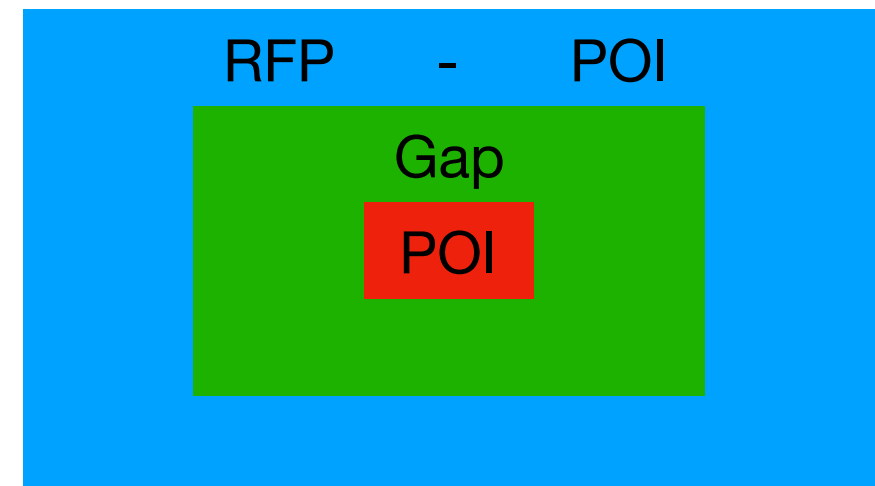
$$\omega_{\langle 4' \rangle} \equiv (m_p M - 3m_q)(M-1)(M-2) .$$

$$d_n\{2\} = \langle \langle 2' \rangle \rangle$$

$$d_n\{4\} = \langle \langle 4' \rangle \rangle - 2\langle \langle 2' \rangle \rangle \langle \langle 2' \rangle \rangle$$

$$v'_n\{2\} = \frac{d_n\{2\}}{\sqrt{c_n\{2\}}}$$

$$v'_n\{4\} = -\frac{d_n\{4\}}{(-c_n\{4\})^{3/4}}$$





# Collective flow via Q-cumulant (4-particle) with 3-subvent

$$-\eta_{max} < \eta_a < -\eta_{max}/3$$

$$|\eta_b| < \eta_{max}/3$$

$$\eta_{max}/3 < \eta_c < \eta_{max}$$

**a**

**b**

**c**

$M_a$

$M_b$

$M_c$

$$\langle \{2\}_n \rangle_{a|b} = \text{Re} \left[ \frac{Q_{n,a} Q_{n,b}^*}{M_a M_b} \right]$$

$$\langle \{4\}_n \rangle_{2a|b,c} = \frac{(Q_{n,a}^2 - Q_{2n,a}) Q_{n,b}^* Q_{n,c}^*}{M_a (M_a - 1) M_b M_c}$$

$$c^{2a|b,c} \{4\} \equiv \langle \{4\}_n \rangle_{2a|b,c} - 2 \langle \{2\}_n \rangle_{a|b} \langle \{2\}_n \rangle_{a|c},$$

*J. Jia, M. Zhou, A. Trzupek, Phys. Rev. C 96 (2017) 034906.*

*M. Aaboud, et al., Phys. Rev. C 97 (2018) 024904.*